

# Conformal Extensions of the Standard Model

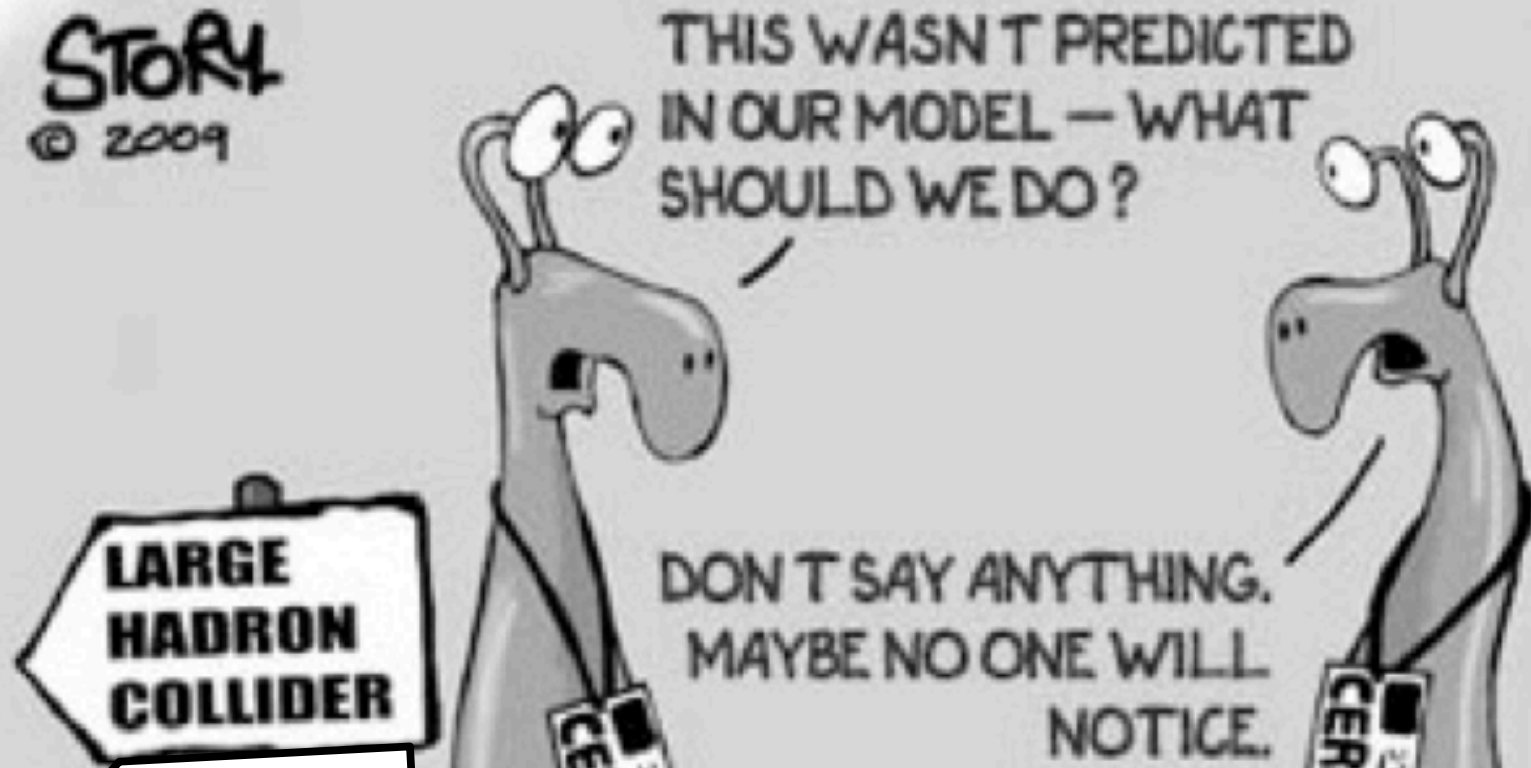
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Scale invariance in particle physics and cosmology

28 January 2019 to 1 February 2019  
CERN

STORY  
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### Very interesting lessons:

- SM works perfectly
- triumph (precision) of concepts (QFT, symmetries)
- ☺ Higgs discovered  $\leftrightarrow$  SM particle masses
- ☺ quantum structure of SM
- ☺ neutrino masses, - DM, - DE ... → very exciting, but...
- ☹ nothing BSM connected to EWSB (so far...)
  - things may be different than expected
  - exp. facts **require new ideas** → **bottom-up guided**

# Look again carefully at the SM as a QFT

- **The SM itself (without embedding) is a 4d QFT like QED**
  - infinities, renormalization  $\leftrightarrow \delta^* \delta \rightarrow$  only differences are calculable
  - SM itself is perfectly OK  $\rightarrow$  many things unexplained...
- **Has (like QED) a triviality problem (Landau poles  $\leftrightarrow$  infinite  $\lambda$ )**
  - triviality = inconsistency  $\rightarrow$  requires some scale  $\Lambda$  where the SM is embedded
  - running  $U(1)_Y$  coupling: pole well beyond Planck scale... - like in QED
  - running Higgs / top coupling  $\rightarrow$  upper bounds on  $m_H$  and  $m_t$
  - $\rightarrow$  the physics at  $\Lambda$  is unknown  $\rightarrow$  explicit scale or effective?
- **Another potential problem is vacuum instability ( $\leftrightarrow$  negative  $\lambda$ )**
  - does occur in SM for large top mass  $> 79$  GeV  $\rightarrow$  lower bounds on  $m_H$

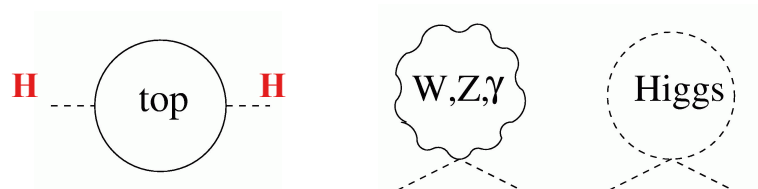
The SM as QFT (without an embedding) works perfectly:

- a hard cutoff  $\Lambda$  and the sensitivity towards  $\Lambda$  has no meaning
- renormalizable, calculable ... - just like QED
- **BUT: an embedding is required  $\leftrightarrow$  triviality...**

# SM Hierarchy Problems

- 1) why are scales vastly different
- 2) why do scales remain vastly different under quantum corrections

- **Loops** → Higgs mass depends on ‘cutoff  $\Lambda$ ’



$$\delta M_H^2 = \frac{\Lambda^2}{32\pi^2 V^2} (6M_W^2 + 3M_Z^2 + 3M_H^2 - 12M_t^2)$$

$$\simeq \mathbf{O}(\Lambda^2/4\pi^2)$$

$m_H \leq 200$  GeV requires  $\Lambda \sim$  TeV → new physics → embedding at  $\Lambda \sim$  TeV

\*OR\* explain how  $m_H$  be  $O(100$  GeV) if  $\Lambda$  is huge ?

- **SM + Dirac neutrinos:** no problem – just like SM
- **SM + Majorana  $\nu$ 's:** → **two scales: VEV and the Majorana mass(es)  $M$**

→  $\delta m_H^2 \simeq \frac{y_\nu^2}{16\pi^2} M^2$  with  $y_\nu^2 = M m_\nu / v^2$  →  $M \lesssim 10^7 - 10^8$  GeV

→ generates a HP problem for large  $M$  even if  $y_\nu$  is tiny ↔ leptogenesis?

# The Problem: Separation of EXPLICIT Scales

- Renormalizable QFT with two scalars  $\varphi$ ,  $\Phi$  with masses  $m$ ,  $M$  and a hierarchy  $m \ll M$
- These scalars must interact since  $\varphi^+\varphi$  and  $\Phi^+\Phi$  are singlets  
→  $\lambda_{\text{mix}}(\varphi^+\varphi)(\Phi^+\Phi)$  must exist (= portal) in addition to  $\varphi^4$  and  $\Phi^4$
- Quantum corrections  $\sim M^2$  drives both masses to the (heavy) scale  
→ vastly different explicit scalar scales are generically unstable

- Since SM Higgs exists → problem: embedding with a 2<sup>nd</sup> scalar
  - gauge extensions → must be broken...
  - GUTs → must be broken
  - even for SUSY GUTS → doublet-triplet splitting...
  - also for fashionable Higgs-portal scenarios...

## Options:

- no 2<sup>nd</sup> Higgs → just the SM → triviality → requires a new scale...
- symmetry: SUSY, ... → conformal symmetry = no explicit scales!

# The main Idea

- **Do not introduce any fundamental (explicit) scales**  
→ **theories with conformal or shift symmetry**
- **Dynamical breaking of CS → Coleman Weinberg  $V_{\text{eff}}$**   
→ **scale(s) by dimensional transmutation**  
→ **Non-linear realization of CS:**
  - naïve power counting ( $\sim \Lambda^2$ ) misleading
  - similar to gauge symmetry and vector boson masses
- **An UV complete theory should have UV fixedpoints to avoid conformal anomalies**

**Anything pointing in that direction?**

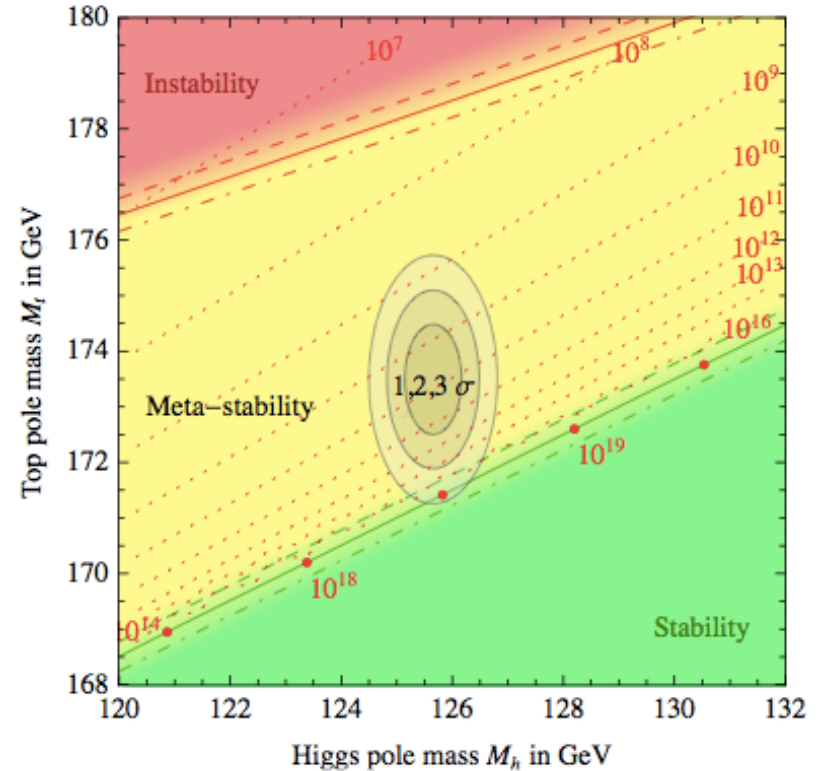
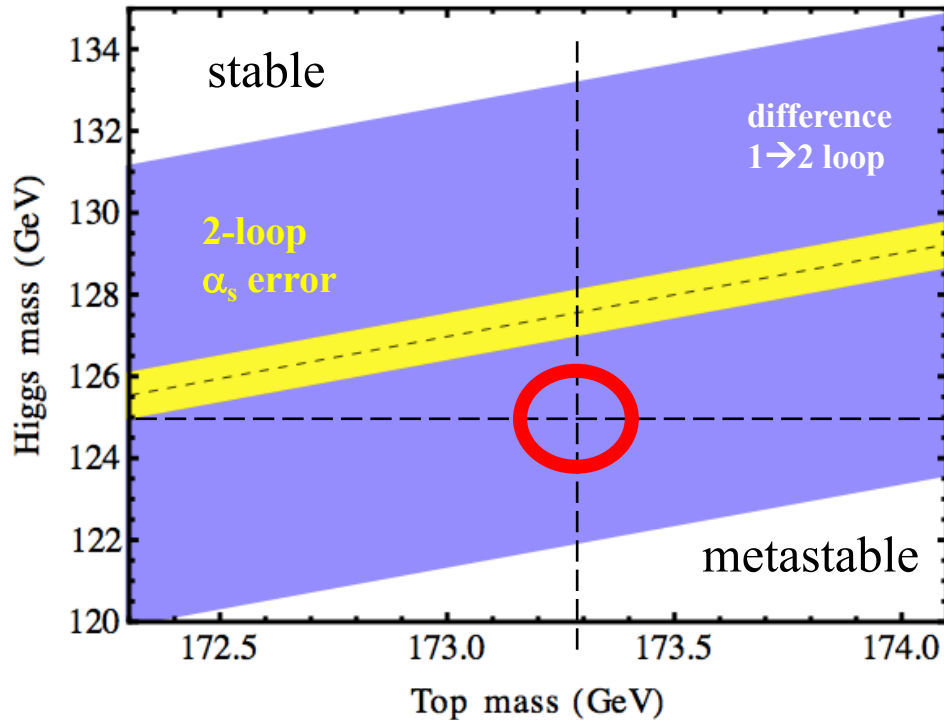
# Is the Higgs Potential at $M_{\text{Planck}}$ flat?

Holthausen, ML, Lim

12 Dec 2011

Elias-Miro, Espinosa, Giudice, Isidori, Riotto, Strumia

13 Dec 2011



**Experimental values point to metastability. Is it fully established?**

→ we need to include DM, neutrino masses, ...? are all errors (EX+TH) fully included?

→ be cautious about claiming that metastability is established

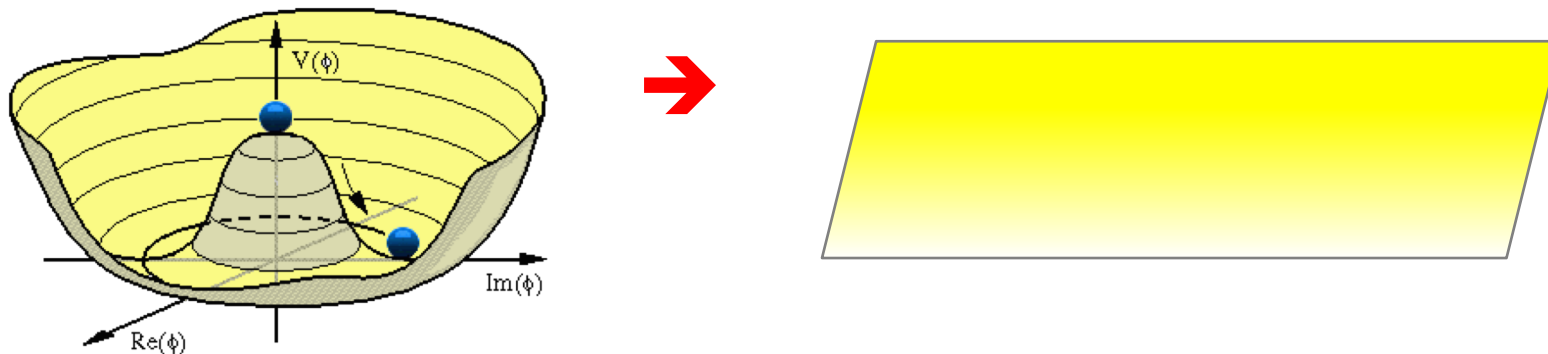
→ **May be a very important observation:**

- remarkable relation between weak scale,  $m_t$ , couplings and  $M_{\text{Planck}}$   $\leftrightarrow$  precision

- remarkable interplay between gauge, Higgs and top loops (log divergences – not  $\Lambda^2$ )

# Is there a Message?

- $\lambda(M_{\text{Planck}}) \simeq 0$ ?  $\rightarrow$  remarkable log cancellations  $\leftrightarrow$  CA  $\sim$   $\beta$ -fcts.  
 $M_{\text{planck}}$ ,  $M_{\text{weak}}$ , gauge, Higgs & Yukawa couplings are unrelated
- remember:  $\mu$  is the only single scale of the SM  $\rightarrow$  special role
  - $\rightarrow$  if in addition  $\mu^2 = 0 \rightarrow V(M_{\text{Planck}}) \simeq 0$
  - $\rightarrow$  flat Mexican hat (<1%) at the Planck scale!



$\rightarrow$  conformal (or shift) symmetry as solution to the HP

$\rightarrow$  combined conformal & EW symmetry breaking

- conceptual issues

- minimal realizations  $\leftrightarrow$  SM seems to know about high scales  $\rightarrow$  bottom-up

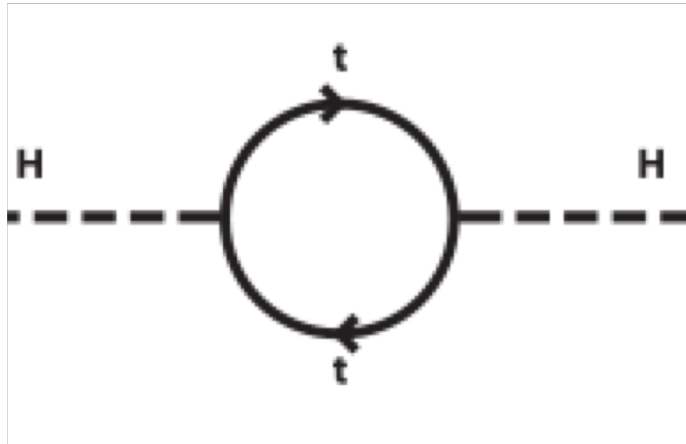
$\leftrightarrow$  many new d.o.f. (fields, big reps.)  $\sim$  UV-instabilities



# Generic Questions

- **Isn't the Planck-scale spoiling things (explicit scale, cut-off, ...)?**
  - non-linear realization of conformal symmetry...
  - **~conformal gravity...**
  - protected by conformal symmetry up to conformal anomaly
  - **generate  $M_{\text{Planck}}$  by dimensional transmutation**
  - for now assumption:  $M_{\text{Planck}}$  somehow generated in a conformal setting
- **Are  $M_{\text{planck}}$  and  $M_{\text{weak}}$  connected?**
  - 1<sup>st</sup> part: assumed to be independently generated scales
  - later more...
- **UV: ultimate solution should be asymptotically safe → UV-FPs...**
- **Conceptual change for scale setting:**
  - So far a rollover of scale generation: SM → BSM → GUT → gravity ( $M_{\text{Planck}}$ )
  - Now → only relative scales – **absolute scale is meaningless**
  - Could solve both HPs ↔ scale is a quantum effect**
  - Fully consistent realization → now new concept for scale setting required**

# Non-linear Realization of Conformal Symmetry



## SB of conformal symmetry

→ naïve power counting invalid

→ similar to Higgs mech. vs. explicit  $M_V$

→ only log sensitivity

↔ conformal anomaly ↔ UV-FP

↔  $\beta$ -functions

- Avoids hierarchy problem, even though there is the conformal anomaly - only logs ↔  $\beta$ -functions
- Dimensional transmutation of conformal theories by log running like in QCD
  - scalar QCD: scalars can condense and set scales like fermions
  - also for massless scalar QCD: scale generation; no hierarchy

# Why the minimalistic SM does not work

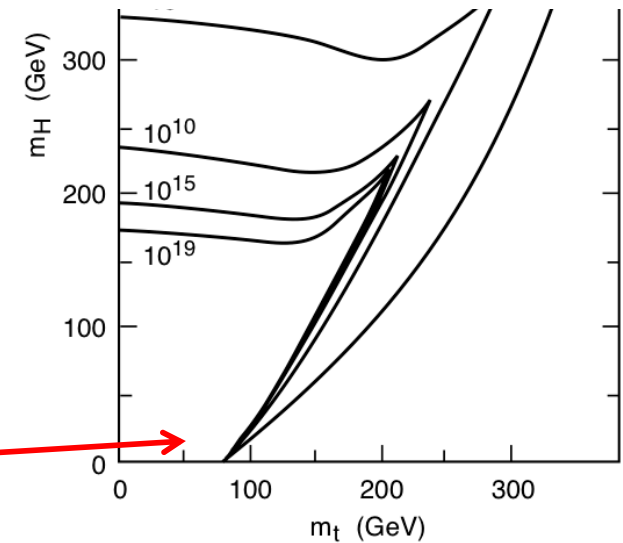
Minimalistic version:  $\rightarrow$  “SM-”

SM + with  $\mu=0 \leftrightarrow$  CS

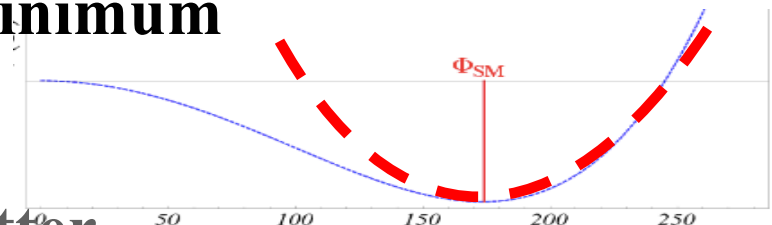
Coleman Weinberg: effective potential

$\rightarrow$  CS breaking (**dimensional transmutation**)

$\rightarrow$  induces for  $m_t < 79$  GeV  
a Higgs mass  $m_H = 8.9$  GeV



- This would conceptually realize the idea, but:  
**Higgs too light and the idea does not work for  $m_t > 79$  GeV**
- DSB for weak coupling  $\leftrightarrow$  CS = phase boundary  
 $\rightarrow$  **scale set by running couplings**
- Reason for  $m_H \ll v$ :  $V_{\text{eff}}$  flat around minimum  
 $\leftrightarrow m_H \sim$  loop factor  $\sim 1/16\pi^2$



**AND:** We need neutrino masses, dark matter, ...

# Realizing the Idea via Higgs Portals

- SM scalar  $\Phi$  plus some new scalar  $\varphi$  (or more scalars)
- CS  $\rightarrow$  no scalar mass terms
- the scalar portal  $\lambda_{\text{mix}}(\varphi^+\varphi)(\Phi^+\Phi)$  must exist

$\rightarrow$  a condensate of  $\langle\varphi^+\varphi\rangle$  produces  $\lambda_{\text{mix}}\langle\varphi^+\varphi\rangle(\Phi^+\Phi) = \mu^2(\Phi^+\Phi)$   
 $\rightarrow$  effective mass term for  $\Phi$

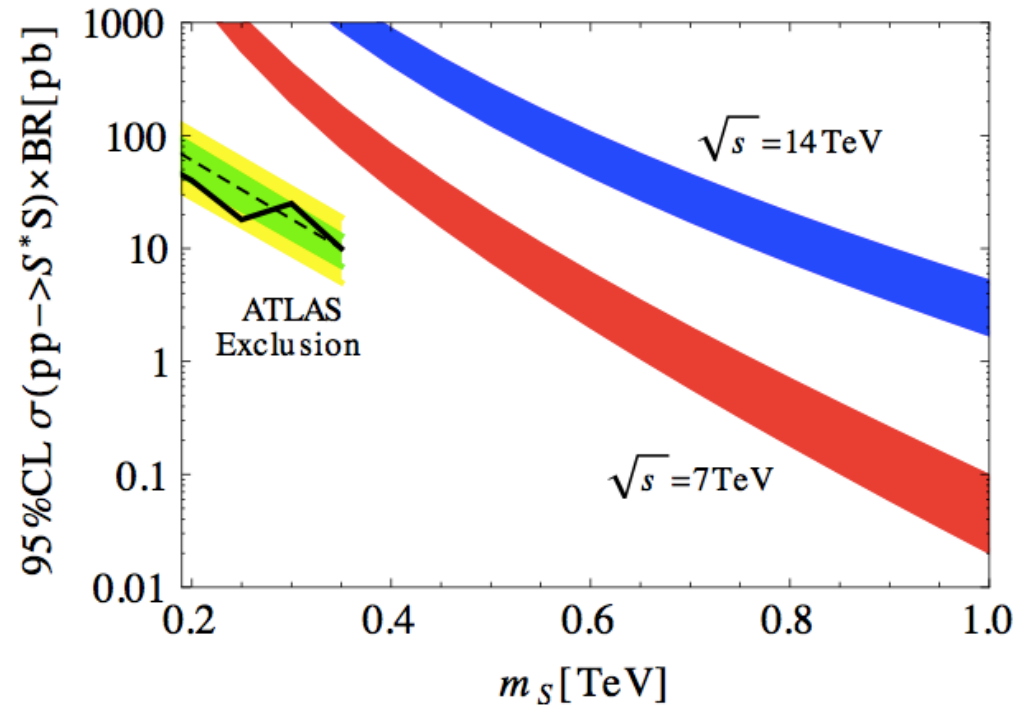
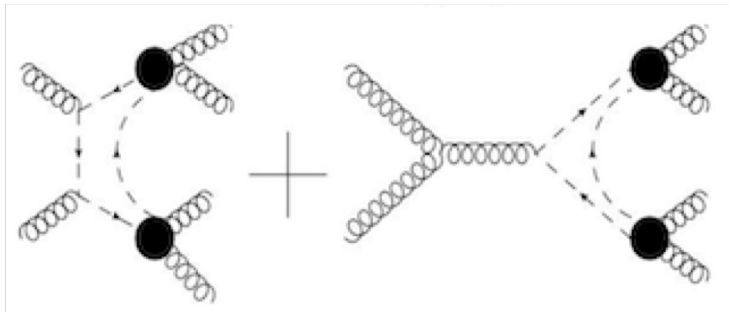
- CS anomalous ...  $\rightarrow$  breaking  $\rightarrow$  only  $\ln(\Lambda)$   
 $\rightarrow$  implies a TeV-ish condensate for  $\varphi$  to obtain  $\langle\Phi\rangle = 246$  GeV
- **Model building possibilities / phenomenological aspects:**
  - $\varphi$  could be an effective field of some hidden sector DSB
  - further particles could exist in hidden sector; e.g. confining...
  - extra hidden U(1) potentially problematic  $\leftrightarrow$  U(1) mixing
  - avoid Yukawas which couple visible and hidden sector $\rightarrow$  phenomenology safe due to Higgs portal, but there is TeV-ish new physics!



# Phenomenology

TeV-ish hidden sector  $\leftrightarrow$  may show up at LHC

S pair production cross section from gluon fusion (assumption: 100% BR into two jets)



## Drawback of this scenario:

- large representations appear less attractive
- Tend to lead to instabilities at high energy  
→ cannot run all the way...

# Realizing this Idea: Left-Right Extension

M. Holthausen, ML, M. Schmidt

## Radiative SB in conformal LR-extension of SM

(use isomorphism  $SU(2) \times SU(2) \simeq Spin(4) \rightarrow$  representations)

particle	parity $\mathcal{P}$	$Z_4$	$Spin(1, 3) \times (SU(2)_L \times SU(2)_R) \times (SU(3)_C \times U(1)_{B-L})$
$\mathbb{L}_{1,2,3} = \begin{pmatrix} L_L \\ -iL_R \end{pmatrix}$	$P\mathbb{P}L(t, -x)$	$L_R \rightarrow iL_R$	$\left[ \left( \frac{1}{2}, \underline{0} \right) (\underline{2}, \underline{1}) + \left( \underline{0}, \frac{1}{2} \right) (\underline{1}, \underline{2}) \right] (\underline{1}, -1)$
$\mathbb{Q}_{1,2,3} = \begin{pmatrix} Q_L \\ -iQ_R \end{pmatrix}$	$P\mathbb{P}Q(t, -x)$	$Q_R \rightarrow -iQ_R$	$\left[ \left( \frac{1}{2}, \underline{0} \right) (\underline{2}, \underline{1}) + \left( \underline{0}, \frac{1}{2} \right) (\underline{1}, \underline{2}) \right] (\underline{3}, \frac{1}{3})$
$\Phi = \begin{pmatrix} 0 & \tilde{\Phi} \\ -\tilde{\Phi}^\dagger & 0 \end{pmatrix}$	$\mathbb{P}\Phi^\dagger\mathbb{P}(t, -x)$	$\Phi \rightarrow i\Phi$	$(\underline{0}, \underline{0}) (\underline{2}, \underline{2}) (\underline{1}, 0)$
$\Psi = \begin{pmatrix} \chi_L \\ -i\chi_R \end{pmatrix}$	$\mathbb{P}\Psi(t, -x)$	$\chi_R \rightarrow -i\chi_R$	$(\underline{0}, \underline{0}) [(\underline{2}, \underline{1}) + (\underline{1}, \underline{2})] (\underline{1}, -1)$

→ the usual fermions, one bi-doublet, two doublets

→ a  $Z_4$  symmetry

→ no scalar mass terms  $\leftrightarrow$  CS

→ **Most general gauge and scale invariant potential respecting  $Z_4$**

$$\mathcal{V}(\Phi, \Psi) = \frac{\kappa_1}{2} (\bar{\Psi}\Psi)^2 + \frac{\kappa_2}{2} (\bar{\Psi}\Gamma\Psi)^2 + \lambda_1 (\text{tr}\Phi^\dagger\Phi)^2 + \lambda_2 (\text{tr}\Phi\Phi + \text{tr}\Phi^\dagger\Phi^\dagger)^2 + \lambda_3 (\text{tr}\Phi\Phi - \text{tr}\Phi^\dagger\Phi^\dagger)^2 + \beta_1 \bar{\Psi}\Psi\text{tr}\Phi^\dagger\Phi + f_1 \bar{\Psi}\Gamma[\Phi^\dagger, \Phi]\Psi,$$

→ calculate  $V_{\text{eff}}$

→ Gildner-Weinberg formalism (RG improvement of flat directions)

- anomaly breaks CS

- spontaneous breaking of parity,  $Z_4$ , LR and EW symmetry

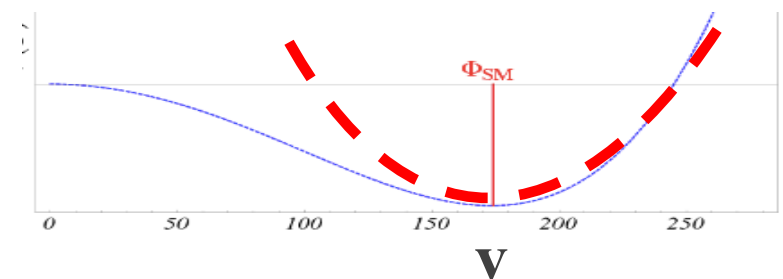
-  $m_H \ll v$  ; typically suppressed by 1-2 orders of magnitude

Reason:  $V_{\text{eff}}$  flat around minimum

$\leftrightarrow m_H \sim \text{loop factor} \sim 1/16\pi^2$

→ generic feature → predictions

- everything works nicely...



→ requires moderate parameter adjustment for the separation of the LR and EW scale... PGB...?



# SM $\otimes$ hidden $SU(3)_H$ Gauge Sector

Holthausen, Kubo, Lim, ML

- hidden  $SU(3)_H$ :

$$\mathcal{L}_H = -\frac{1}{2}\text{Tr } F^2 + \text{Tr } \bar{\psi}(i\gamma^\mu D_\mu - yS)\psi$$

gauge fields ;  $\psi = 3_H$  with  $SU(3)_F$  ; **S = real singlet scalar**

- SM coupled by S via a Higgs portal:

$$V_{SM+S} = \lambda_H(H^\dagger H)^2 + \frac{1}{4}\lambda_S S^4 - \frac{1}{2}\lambda_{HS}S^2(H^\dagger H)$$

- no scalar mass terms
- use similarity to QCD, use NJL approximation, ...
- $\chi$ -ral symmetry breaking in hidden sector:  
 $SU(3)_L \times SU(3)_R \rightarrow SU(3)_V \rightarrow$  **generation of TeV scale**  
 **$\rightarrow$  transferred into the SM sector through the singlet S**  
 **$\rightarrow$  dark pions are PGBs: naturally stable  $\rightarrow$  DM**

# Realizing the Idea: Specific Realizations

**SM + extra singlet:  $\Phi, \varphi$**

Nicolai, Meissner, Farzinnia, He, Ren, Foot, Kobakhidze, Volkas, ...

**SM  $\otimes$  SU(N)<sub>H</sub> with new N-plet in a hidden sector**

Ko, Carone, Ramos, Holthausen, Kubo, Lim, ML, Hambye, Strumia, ...

**SM embedded into larger symmetry (CW-type LR)**

Holthausen, ML, M. Schmidt

**SM + QCD colored scalar which condenses at TeV scale**

Kubo, Lim, ML

**SM  $\otimes$  [SU(2)<sub>X</sub>  $\otimes$  U(1)<sub>X</sub>]**

Altmannshofer, Bardeen, Bauer, Carena, Lykken

**Since the SM-only version does not work  $\rightarrow$  observable effects:**

- Higgs coupling to other scalars (singlet, hidden sector, ...)
- dark matter candidates  $\leftrightarrow$  hidden sectors & Higgs portals
- consequences for neutrino masses

# Conformal Symmetry & Neutrino Masses

ML, S. Schmidt and J. Smirnov

- **No explicit scale  $\rightarrow$  no explicit (Dirac or Majorana) mass term  $\rightarrow$  only Yukawa couplings  $\otimes$  generic scales**
- **Enlarge the Standard Model field spectrum like in 0706.1829 - R. Foot, A. Kobakhidze, K.L. McDonald, R. Volkas**
- **Consider direct product groups: SM  $\otimes$  HS**
- **Two scales: CS breaking scale at O(TeV) + induced EW scale**

**Important consequence for fermion mass terms:**

$\rightarrow$  spectrum of Yukawa couplings  $\otimes$  TeV or EW scale

$\rightarrow$  interesting consequences  $\leftrightarrow$  Majorana mass terms are no longer expected at the generic L-breaking scale  $\rightarrow$  anywhere

# Examples

$$\mathcal{M} = \begin{pmatrix} 0 & y_D \langle H \rangle \\ y_D^T \langle H \rangle & y_M \langle \phi \rangle \end{pmatrix}$$

## Yukawa seesaw:

SM +  $\nu_R$  + singlet

$$\langle \phi \rangle \approx \text{TeV}$$

$$\langle H \rangle \approx 1/4 \text{ TeV}$$

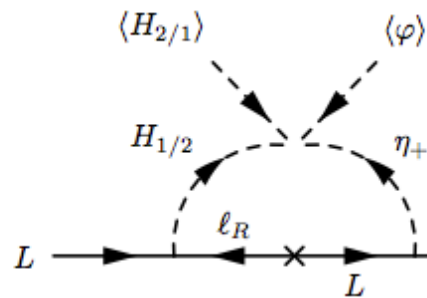
→ generically expect a TeV seesaw

BUT:  $y_M$  can be tiny

→ wide range of sterile masses → including pseudo-Dirac case

→ suppressed  $0\nu\beta\beta$

## Radiative masses



$$\mathcal{M} = m_L \quad \text{or}$$

$$\mathcal{M} = \begin{pmatrix} \mu_1 & y_D \langle H \rangle \\ y_D^T \langle H \rangle & \mu_2 \end{pmatrix}$$

→ pseudo-Dirac case

## The punch line:

all usual neutrino mass terms can be generated

→ suitable scalars required

→ no explicit masses:

**all via Yukawa couplings**

→ different numerical expectations  $\leftrightarrow$  could easily explain keV masses

# Another Example: Inverse Seesaw

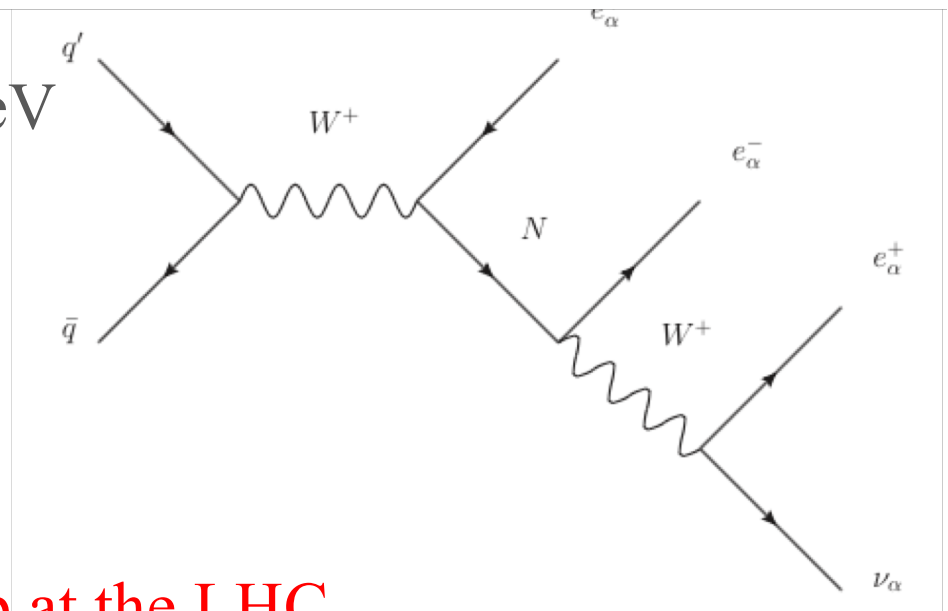
$SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)_X$

Humbert, ML, J. Smirnov

	$H$	$\phi_1$	$\phi_2$	$L$	$\nu_R$	$N_R$	$N_L$
$U(1)_X$	0	1	2	0	0	1	1
Lepton Number	0	0	0	1	1	0	0
$U(1)_Y$	1	0	0	-1	0	0	0
$SU(2)_L$	2	1	1	2	1	1	1

$$\mathcal{M} = \begin{pmatrix} 0 & y_D \langle H \rangle & 0 & 0 \\ y_D \langle H \rangle & 0 & y_1 \langle \phi_1 \rangle & \tilde{y}_1 \langle \phi_1 \rangle \\ 0 & y_1 \langle \phi_1 \rangle & y_2 \langle \phi_2 \rangle & 0 \\ 0 & \tilde{y}_1 \langle \phi_1 \rangle & 0 & \tilde{y}_2 \langle \phi_2 \rangle \end{pmatrix}$$

- light eV “active” neutrino(s)
- two pseudo-Dirac neutrinos;  $m \simeq \text{TeV}$
- sterile state with  $\mu \approx \text{keV}$
- tiny non-unitarity of PMNS matrix
- tiny lepton universality violation
- suppressed  $0\nu\beta\beta$  decay ←!
- lepton flavour violation
- tri-lepton production could show up at the LHC
- keV neutrinos as warm dark matter →



# Conformal Symmetry & Dark Matter

## Different natural and viable options:

- 1) eV, **keV = DM**, TeV, ... sterile  $\nu$  mass easily possible  
 $\leftarrow \rightarrow$  not so easy in standard see-saw's
- 2) New particles which are fundamental or composite DM candidates:
  - hidden sector pseudo-Goldstone-bosons
  - stable color neutral bound states from new QCD representations
  - $\rightarrow$  some look like WIMPs
  - $\rightarrow$  others are extremely weakly coupled (via Higgs portal)
  - $\rightarrow$  or even coupled to QCD (threshold suppressed...)

# The Planck Scale from CS Breaking

- dynamically generated from conformal gravity  $\otimes$  SU(N)
  - condensate via SU(N) helper field – similar to → Donoghue, Menezes, ...
- more symmetry + no scale → power counting renormalizable

J. Kubo, ML, K. Schmitz, M. Yamada → see talk with more details by M. Yamada

$$S_C = \int d^4x \sqrt{-g} \left[ -\hat{\beta} S^\dagger S R + \hat{\gamma} R^2 - \frac{1}{2} \text{Tr} F^2 + \right. \\ \left. + g^{\mu\nu} (D_\mu S)^\dagger D_\nu S - \hat{\lambda} (S^\dagger S)^2 + a R_{\mu\nu} R^{\mu\nu} + b R_{\mu\nu\alpha\beta} R^{\mu\nu\alpha\beta} \right]$$

R = Ricci curvature scalar,  $R_{\mu\nu}$  = Ricci tensor,  $R_{\mu\nu\alpha\beta}$  = Riemann tensor

F = field-strength tensor of the SU( $N_c$ ) gauge theory ; S = complex scalar in fund. rep. →  $N_c$

→ most general diffeomorphism invariance, gauge invariance, and global scale invariance

**Condensation in SU( $N_c$ ) gauge sector:  $\langle S^\dagger S \rangle$  → Planck mass → normal GR**

$$\rightarrow M_{\text{planck}} = 2\beta f_0 = \frac{N_c \beta}{16\pi^2} (2\lambda f_0) \left( 1 + 2 \ln \frac{2\lambda f_0}{\Lambda^2} \right) \quad \text{with } f_0 = \langle S^\dagger S \rangle$$

ghost? → don't quantize GR, but after condensation normal gravity → best of both worlds?

→ Dilaton-scalaron inflation → fits data very well!

# Scale dependence: EW vs. Planck Scale

- **Assume:**

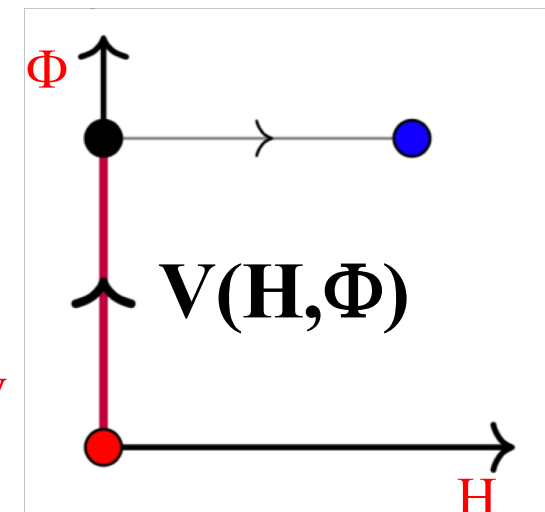
- SM scale generated by some TeV-ish conformal extension
- Planck scale generation by conformal gravity  $\otimes$  scalar QCD

**→ Do we understand the hierarchy between EW and Planck scale?**

$$V = \lambda_1(\mathbf{H}^\dagger\mathbf{H})^2 + \underbrace{\lambda_2(\mathbf{H}^\dagger\mathbf{H})(\Phi^\dagger\Phi)}_{\text{portal coupling}} + \lambda_3(\Phi^\dagger\Phi)^2$$

**→ Does  $\lambda_2$  portal lead to the usual hierarchy problem? → Ideas:**

- a tiny  $\lambda_2 \leftrightarrow$  additive RGE evolution...
- composite Higgs & loop generation of portal term
- sequential breaking by RG running → ‘CW tumbling’  
 $m^2 = 0$  is boundary broken/unbroken
- SSB for tiny attractive force
- if  $\langle\Phi^\dagger\Phi\rangle$  condenses first (stronger coupling)
- portal can induce  $m^2 > 0$  for H → shifts SSB boundary
- 2<sup>nd</sup> SSB by log running of couplings





# Summary

- **SM works (so far) perfectly**
  - be a bit more patient: new physics around the corner...
  - maybe it is time to re-consider some things...
- **The old hierarchy problem...? No new physics observed**
  - $\lambda(M_{\text{Planck}}) = 0$  ?  $\leftrightarrow$  precise value for  $m_t$  **→ is there a message?**
  - SM embeddings into QFTs with conformal symmetry**
    - combined conformal & electro-weak symmetry breaking
    - implications for BSM phenomenology
    - implications for Higgs couplings, dark matter, ...
    - implications for neutrino masses
  - testable consequences: @LHC, dark matter, neutrinos**
- **Planck scale generation by gauge induced breaking of conformal GR**
  - very nice phenomenology: inflation...
  - consistent quantum gravity: renormalizability?, ghost?
    - $\leftrightarrow$  normal GR from a theory with more symmetry
  - stabilizing large scale hierarchies...