

# Higgs trilinear coupling from single Higgs observables

Marc Riembau  
11th Dec 2018

Based on:

Degrassi, Giardino, Maltoni, Pagani; 1607.04251

DiVita, Grojean, Panico, MR, Vantalon; 1704.01953

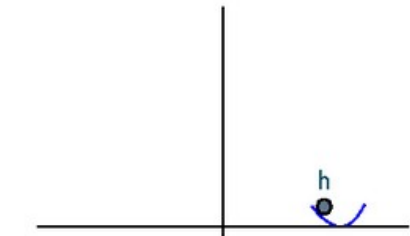
DiVita, Durieux, Gorjean, Gu, Liu, Panico, MR, Vantalon; 1704.01953



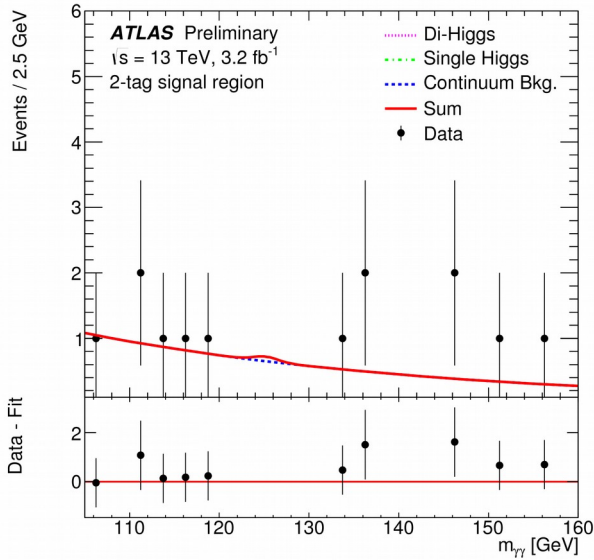
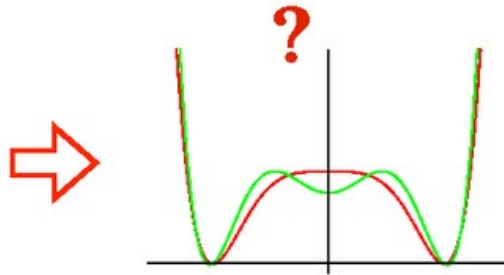
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DE GENÈVE**

# The multifaceted relevance of the Higgs self-coupling

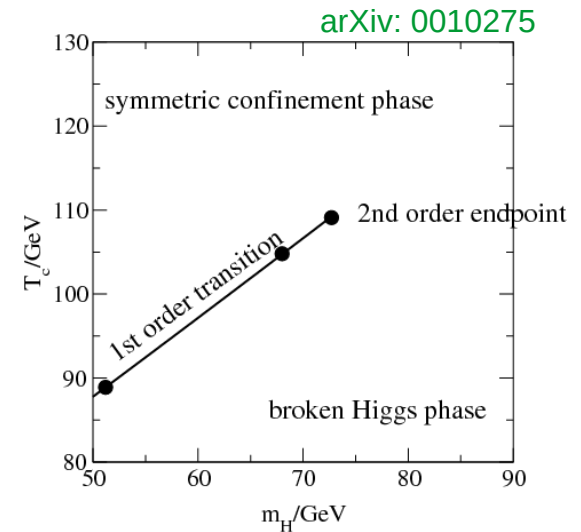
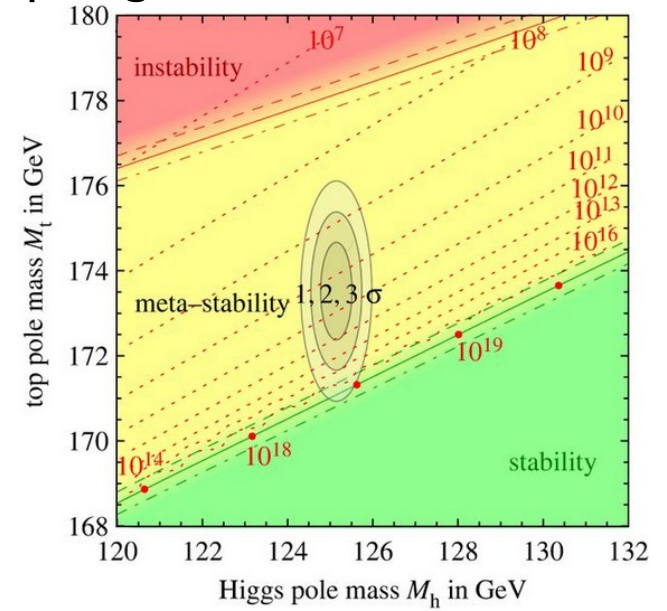
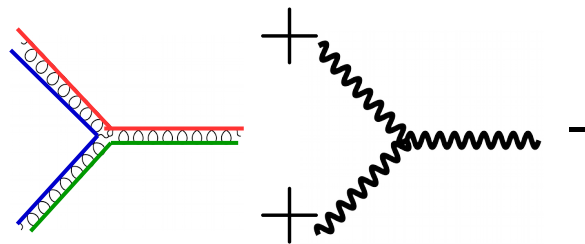
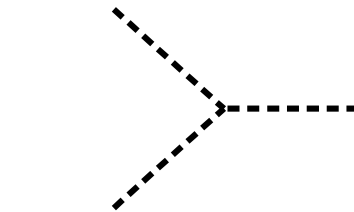
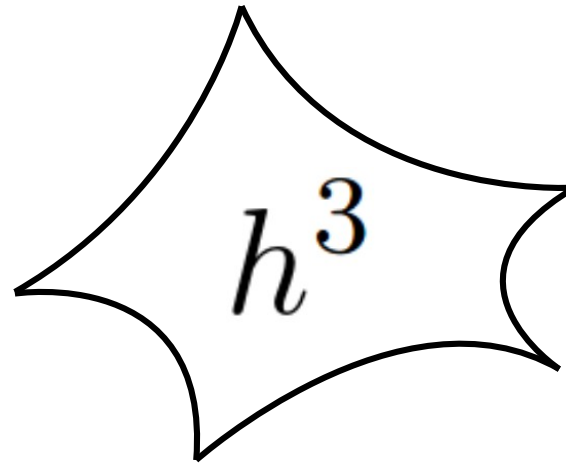
arXiv: 1205.6497



arXiv: 1511.06495



arXiv: 1511.06495

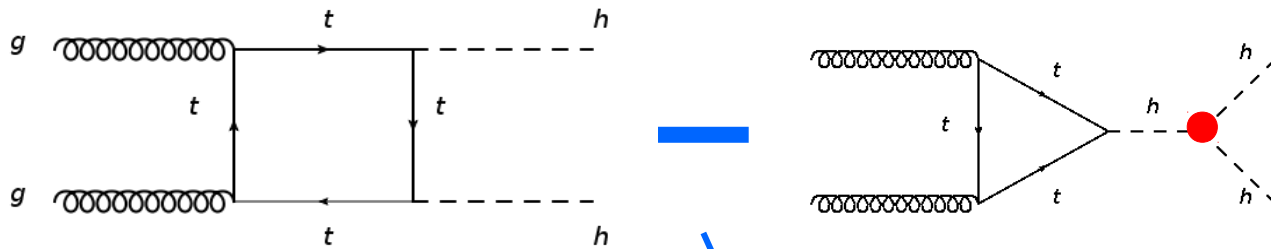


arXiv: 0010275

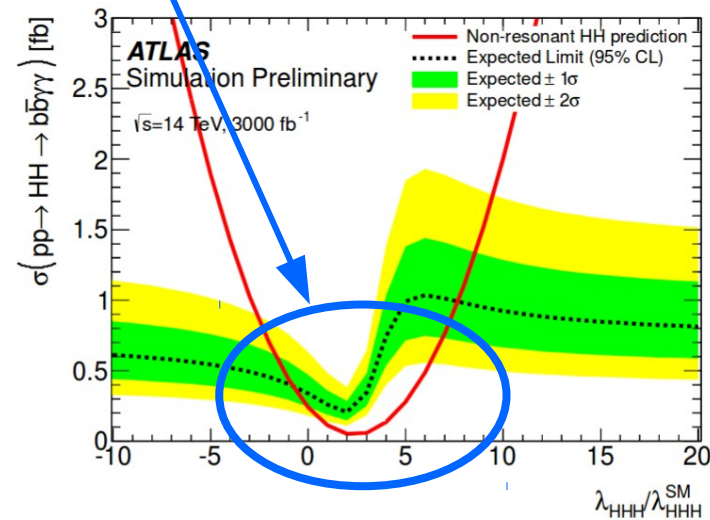
# Double Higgs production at LHC

Small production rate times a small visible branching ratio:

$$\frac{\sigma(pp \rightarrow hh)}{\sigma(pp \rightarrow h)} \sim 10^{-3} \quad \text{Br}(h \rightarrow b\bar{b}) \times \text{Br}(h \rightarrow \gamma\gamma) \sim 60\% \times 0.1\%$$



destructive interference

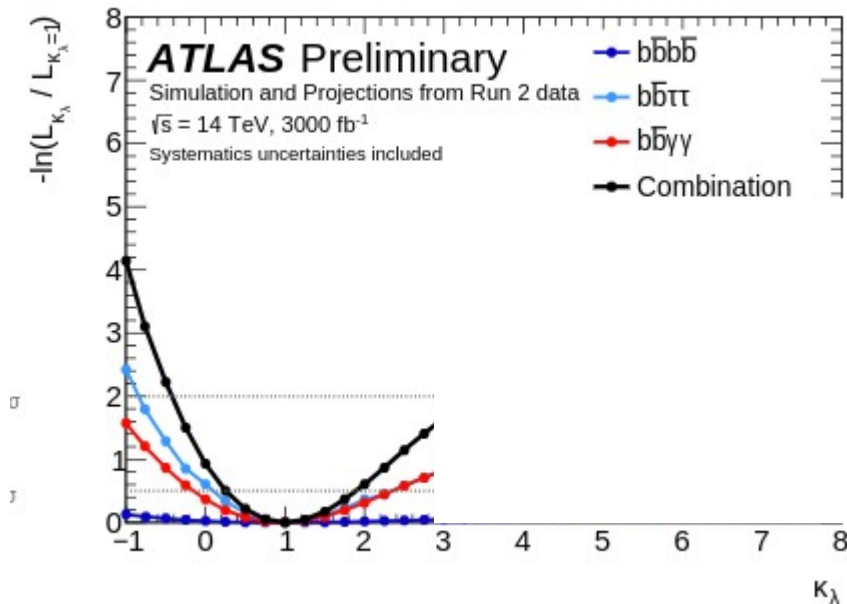
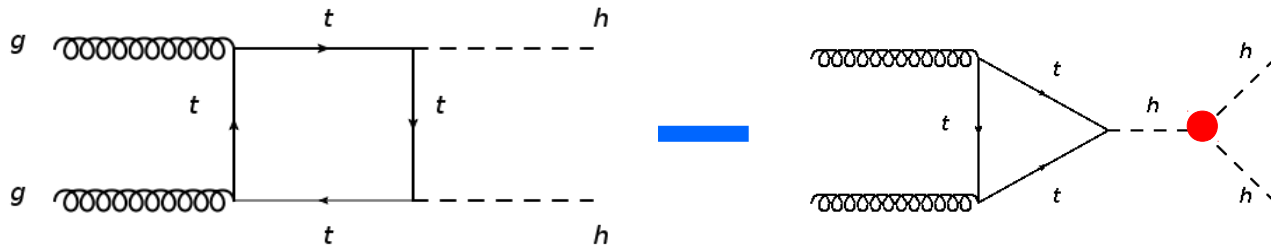


ATL-PHYS\_PUB\_2017-001

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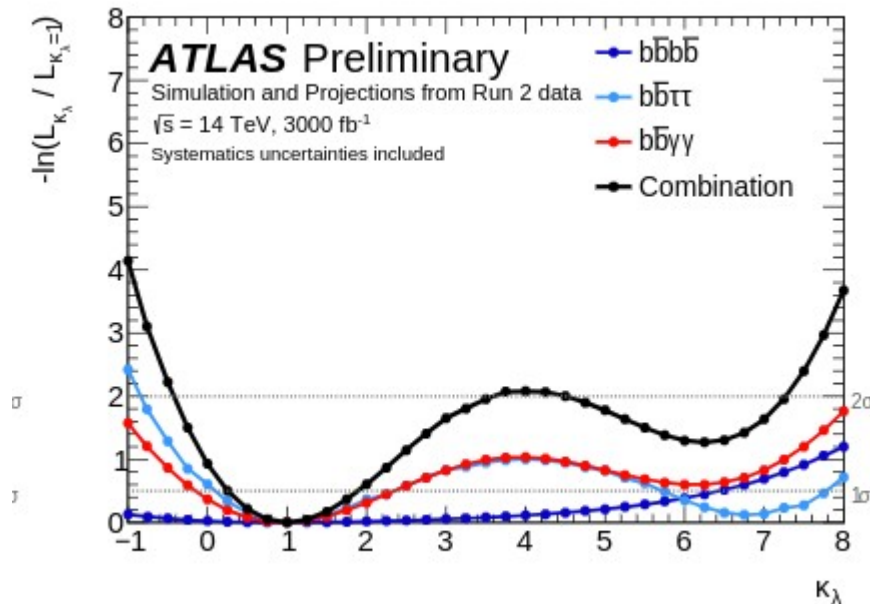
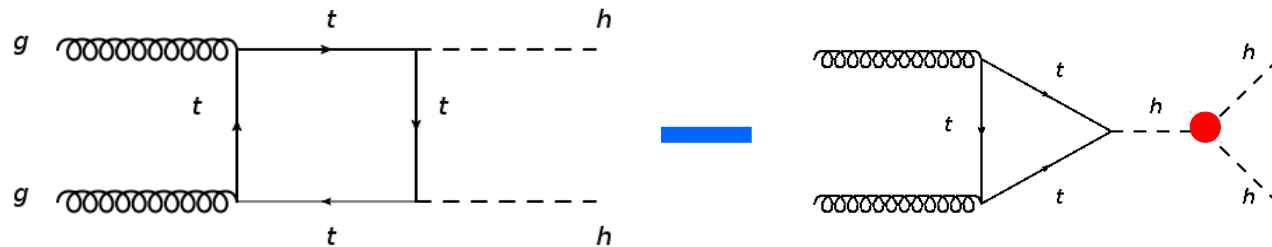
HL-LHC @  $3 \text{ ab}^{-1}$ , 95% CL

$$\kappa_\lambda \in \sim [-0.5, 3] ?$$

# Double Higgs production at LHC

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HL-LHC @ 3 ab<sup>-1</sup>, 95% CL

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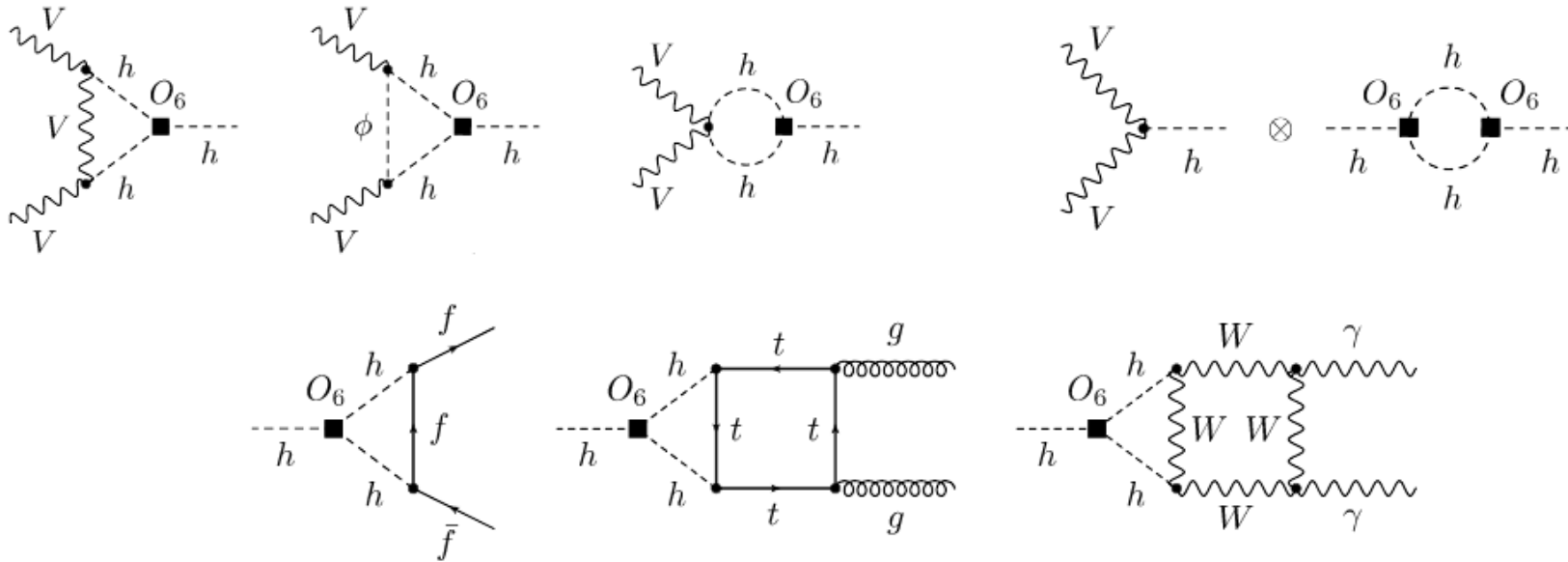
7!

Large and negative interference spoils sensitivity

# Higgs self-coupling from single Higgs processes

Given the loose constraints from double Higgs production, perhaps single Higgs processes can help

McCullough, 1312.3322  
 Gorbahn, Haisch 1607.03773  
 Degraasi, et al. 1607.04251  
 Bizon, et al. 1610.05771



# Higgs self-coupling from single Higgs processes

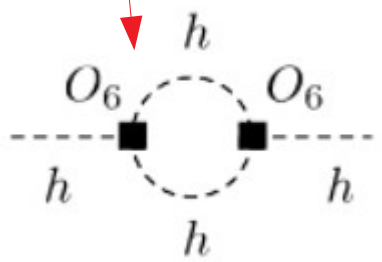
$$\mu_i^f \equiv \mu_i \times \mu^f = \frac{\sigma(i)}{\sigma^{\text{SM}}(i)} \times \frac{\text{BR}(f)}{\text{BR}^{\text{SM}}(f)}$$

$$\mu_i = 1 + (\kappa_3 - 1) C_1^\sigma + (\kappa_3^2 - 1) \delta Z_H \quad \mu^f = 1 + (\kappa_3 - 1) (C_1^f - C_1^{\Gamma_{\text{tot}}})$$

Process specific

Universal factor

Process specific



$C_1^\sigma$ [%]	$ggF$	$VBF$	$WH$	$ZH$	$ttH$	$tHj$
13 TeV	0.66	0.64	1.03	1.19	3.51	0.91
14 TeV	0.66	0.64	1.03	1.18	3.47	0.89
27 TeV	0.66	0.62	1.01	1.16	3.20	0.79

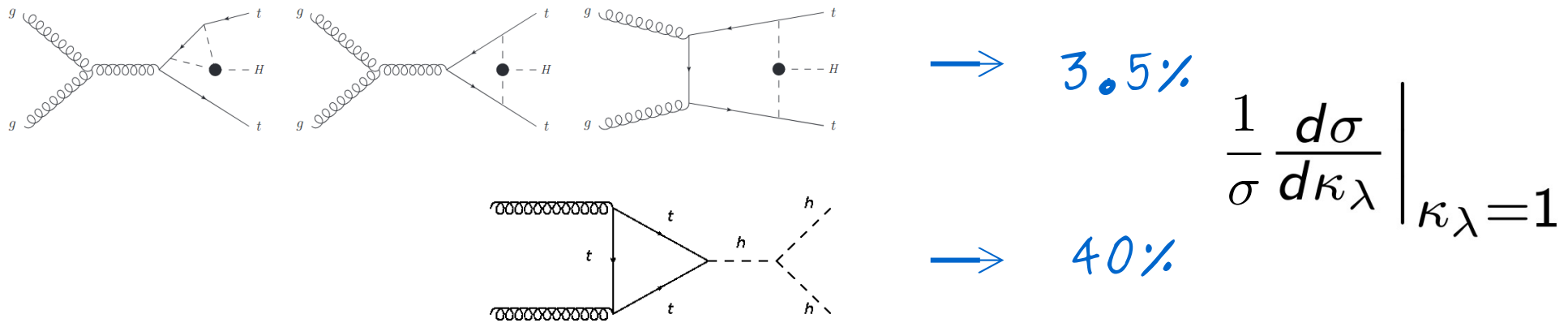
$C_1^\Gamma$ [%]	$\gamma\gamma$	$ZZ$	$WW$	$gg$
on-shell $H$	0.49	0.83	0.73	0.66

## 13 TeV

$p_T(H)$ [GeV]	[0, 25]	[25, 50]	[50, 100]	[100, 200]	[200, 500]	> 500
$VBF$	0.97	0.88	0.73	0.58	0.45	0.29
$ZH$	2.00	1.75	1.21	0.51	0.01	-0.10
$WH$	1.70	1.49	1.04	0.44	0.01	-0.09
$t\bar{t}H$	5.31	5.07	4.38	3.00	1.27	0.17
$tHj$	1.23	1.18	1.02	0.74	0.33	-0.06

# Higgs self-coupling in tth vs double Higgs

«Looking for loop effects in tth» sounds bad,  
but there is a better perspective:



Rule of thumb:

precision of tth x 10  
precision of di-Higgs

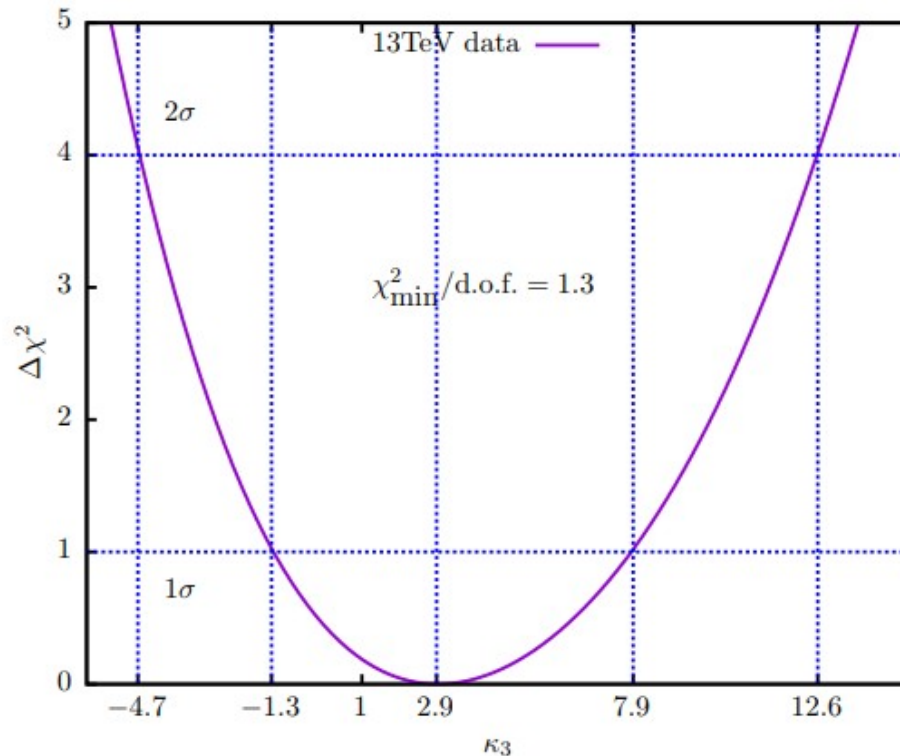
=

constraint on trilinear from tth  
constraint on trilinear from di-Higgs



Minimization of

$$\chi^2(\kappa_\lambda) \equiv \sum_{\bar{\mu}_i^f \in \{\bar{\mu}_i^f\}} \frac{(\mu_i^f(\kappa_\lambda) - \bar{\mu}_i^f)^2}{(\Delta_i^f(\kappa_\lambda))^2}$$



*plot done by  
Xiaoran Zhao*

*based on  
CMS-HIG-17-031*

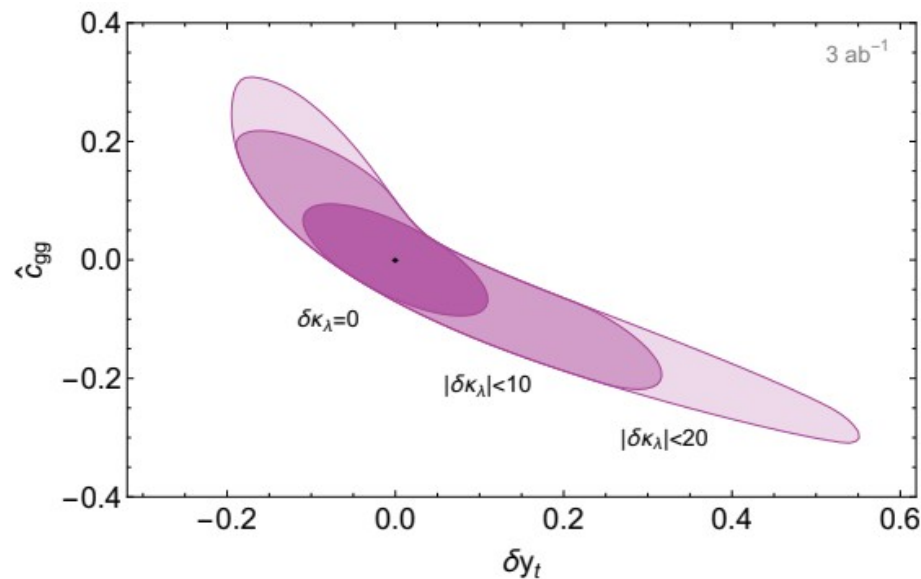
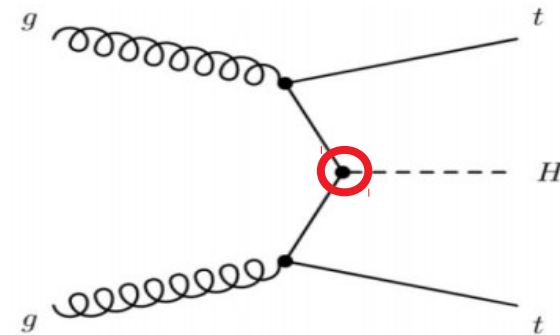
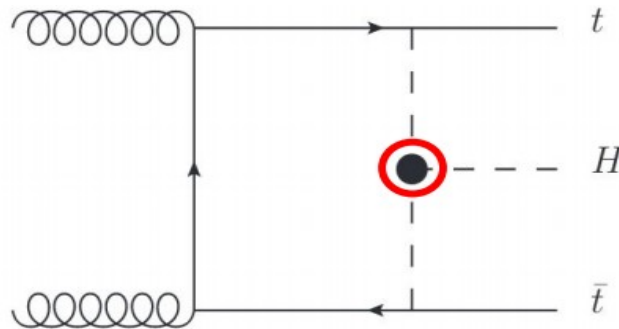
$$\kappa_\lambda^{\text{best}} = 2.9, \quad \kappa_\lambda^{1\sigma} = [-1.3, 7.9], \quad \kappa_\lambda^{2\sigma} = [-4.7, 12.6]$$

**EXP double Higgs:**

- ATLAS:  $-5.0 < \kappa_\lambda < 12.1$
- CMS:  $-11.8 < \kappa_\lambda < 18.8$

# Correlations of inclusive observables...

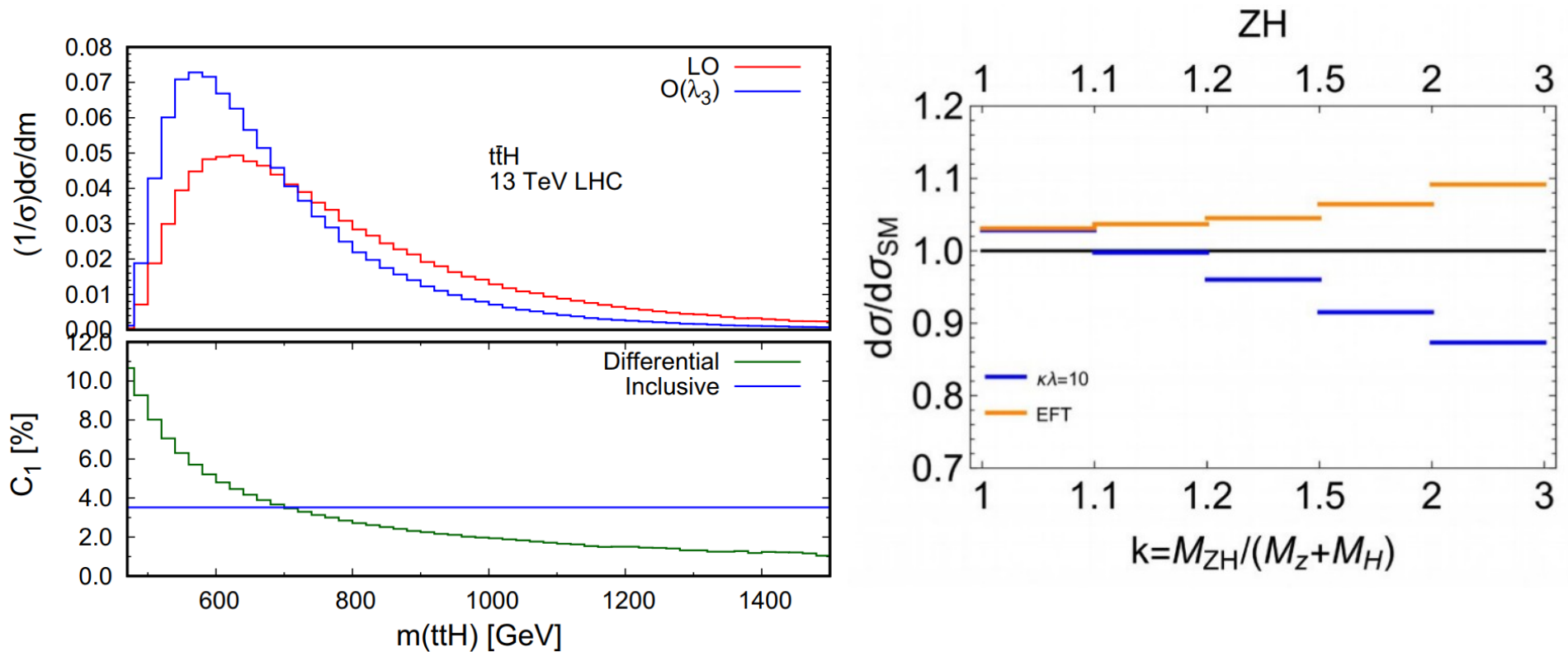
Imagine  $t\bar{t}h$  is measured to be different from SM...  
 who is the responsible?



Large trilinear affects precision  
 on single Higgs parameters,  
 and vice versa

## ... and the need for differential information

- EFT operators tend to show
  - larger effects at large invariant masses
  - global rescalings of the distribution
- Higgs self-coupling deforms the distribution nontrivially.



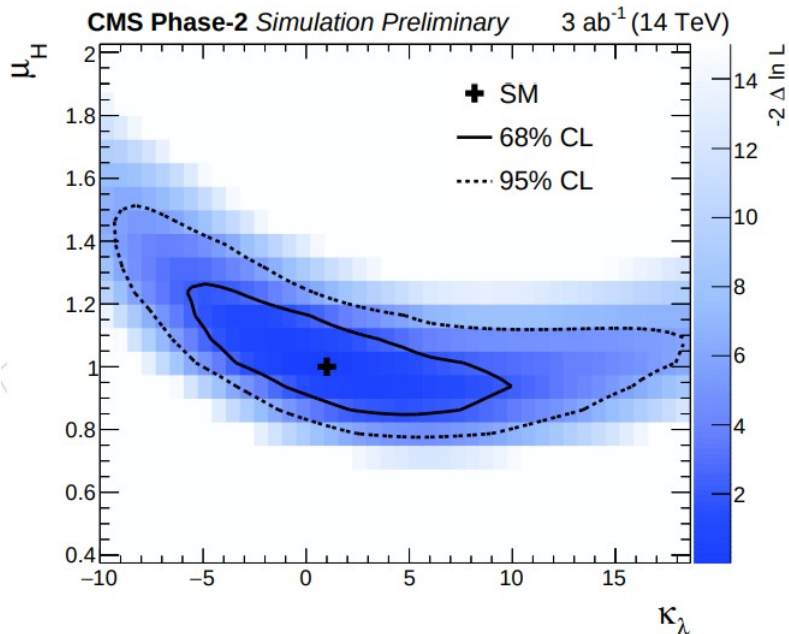
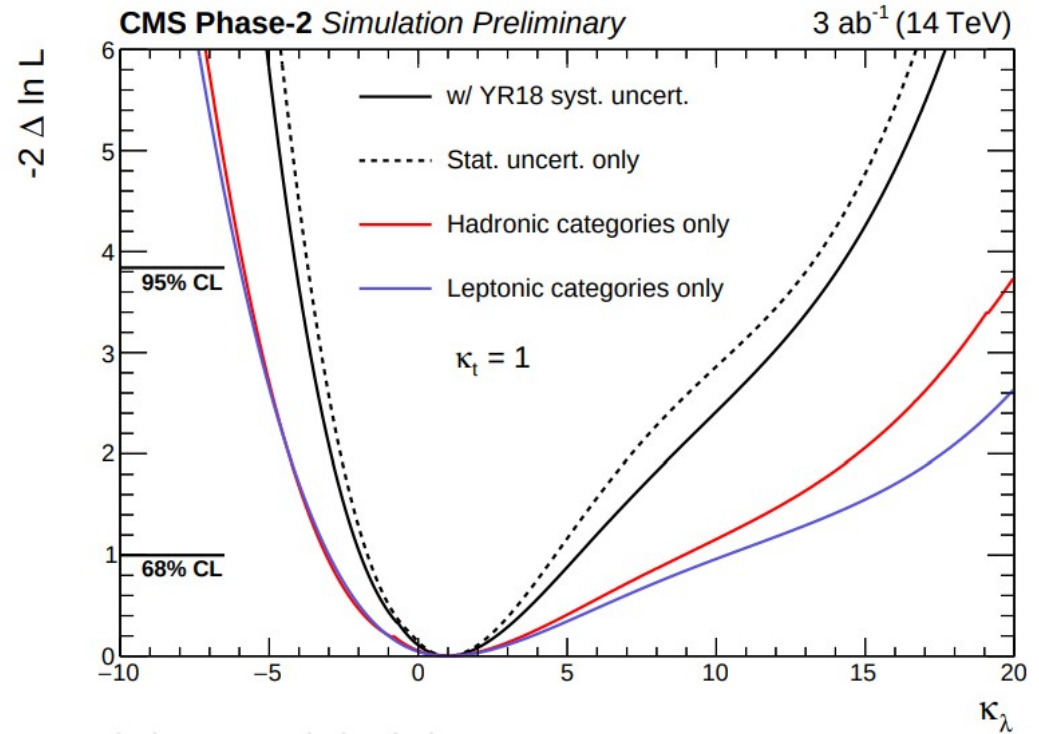
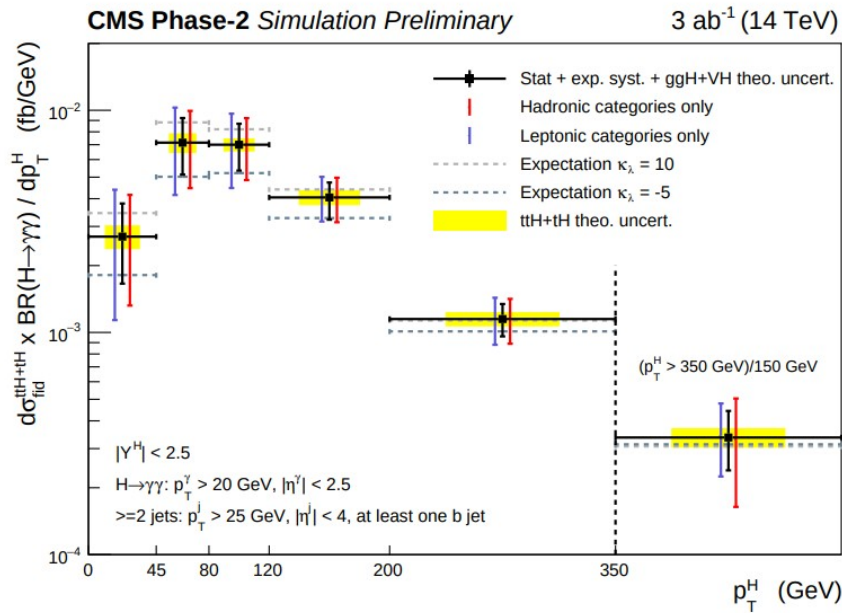


Figure 42: Results of the likelihood scan in  $\kappa_\lambda$ . The individual contributions of the statistical and systematic uncertainties are disentangled by performing a likelihood scan with all systematics removed. The observed deviation from the statistical uncertainty only curve is driven by the theoretical systematic uncertainties in the Higgs boson production yields. Additionally, the contributions from the hadronic and leptonic channels have been separated, shown in red and purple respectively.

First CMS study on tth:

CMS PAS FTR-18-020

## Global fit

$$\begin{aligned}
\mathcal{L} \supset & \frac{h}{v} \left[ \delta c_w \frac{g^2 v^2}{2} W_\mu^+ W^{-\mu} + \delta c_z \frac{(g^2 + g'^2) v^2}{4} Z_\mu Z^\mu \right. \\
& + c_{ww} \frac{g^2}{2} W_{\mu\nu}^+ W^{-\mu\nu} + c_{w\Box} g^2 (W_\mu^- \partial_\nu W^{+\mu\nu} + \text{h.c.}) + \hat{c}_{\gamma\gamma} \frac{e^2}{4\pi^2} A_{\mu\nu} A^{\mu\nu} \\
& \left. + c_{zz} \frac{g^2 + g'^2}{4} Z_{\mu\nu} Z^{\mu\nu} + \hat{c}_{z\gamma} \frac{e \sqrt{g^2 + g'^2}}{2\pi^2} Z_{\mu\nu} A^{\mu\nu} + c_{z\Box} g^2 Z_\mu \partial_\nu Z^{\mu\nu} + c_{\gamma\Box} g g' Z_\mu \partial_\nu A^{\mu\nu} \right] \\
& + \frac{g_s^2}{48\pi^2} \left( \hat{c}_{gg} \frac{h}{v} + \hat{c}_{gg}^{(2)} \frac{h^2}{2v^2} \right) G_{\mu\nu} G^{\mu\nu} - \sum_f \left[ m_f \left( \delta y_f \frac{h}{v} + \delta y_f^{(2)} \frac{h^2}{2v^2} \right) \bar{f}_R f_L + \text{h.c.} \right] \\
& - (\kappa_\lambda - 1) \lambda_3^{SM} v h^3,
\end{aligned}$$

7+2+1 independent parameters:  $\delta c_z, c_{zz}, c_{z\Box}, \hat{c}_{z\gamma}, \hat{c}_{\gamma\gamma}, \hat{c}_{gg}, \delta y_t, \delta y_b, \delta y_\tau, \kappa_\lambda$ .

$$\delta c_w = \delta c_z,$$

$$c_{ww} = c_{zz} + 2 \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{z\gamma} + \frac{g'^4}{\pi^2 (g^2 + g'^2)^2} \hat{c}_{\gamma\gamma},$$

$$c_{w\Box} = \frac{1}{g^2 - g'^2} \left[ g^2 c_{z\Box} + g'^2 c_{zz} - e^2 \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{\gamma\gamma} - (g^2 - g'^2) \frac{g'^2}{\pi^2 (g^2 + g'^2)} \hat{c}_{z\gamma} \right],$$

$$c_{\gamma\Box} = \frac{1}{g^2 - g'^2} \left[ 2g^2 c_{z\Box} + (g^2 + g'^2) c_{zz} - \frac{e^2}{\pi^2} \hat{c}_{\gamma\gamma} - \frac{g^2 - g'^2}{\pi^2} \hat{c}_{z\gamma} \right],$$

$$\hat{c}_{gg}^{(2)} = \hat{c}_{gg},$$

$$\delta y_f^{(2)} = 3\delta y_f - \delta c_z.$$

$$\delta g_{1,z} = \frac{g'^2}{2(g^2 - g'^2)} \left[ \hat{c}_{\gamma\gamma} \frac{e^2}{\pi^2} + \hat{c}_{z\gamma} \frac{g^2 - g'^2}{\pi^2} - c_{zz} (g^2 + g'^2) - c_{z\Box} \frac{g^2}{g'^2} (g^2 + g'^2) \right],$$

$$\delta \kappa_\gamma = - \frac{g^2}{2(g^2 + g'^2)} \left[ \hat{c}_{\gamma\gamma} \frac{e^2}{\pi^2} + \hat{c}_{z\gamma} \frac{g^2 - g'^2}{\pi^2} - c_{zz} (g^2 + g'^2) \right],$$

measured in diboson

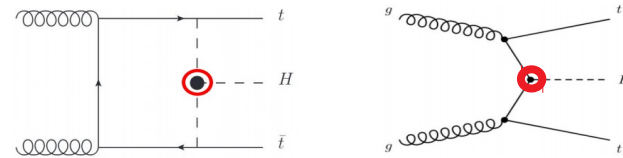
relations at dimension 6

# Global fit

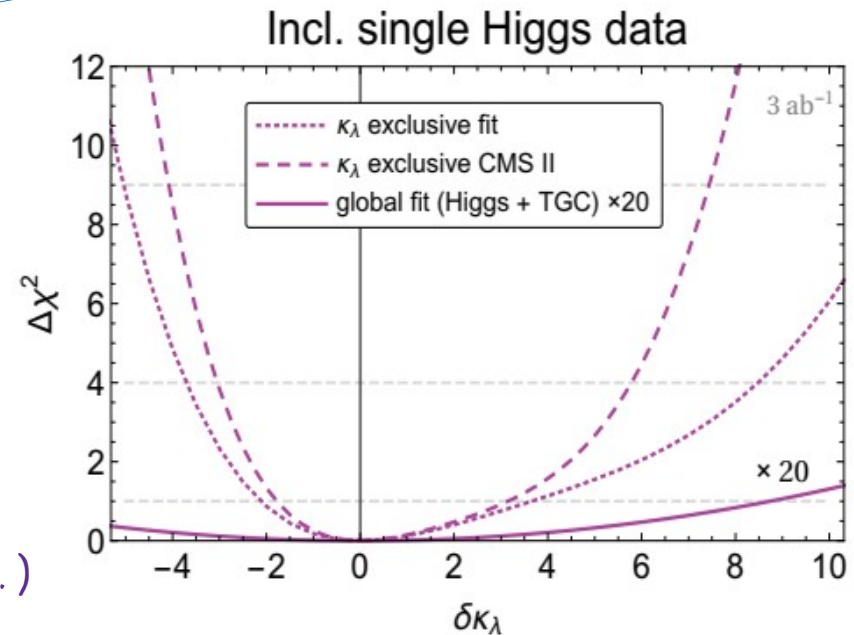
<https://twiki.cern.ch/twiki/bin/view/LHCPhysics/GuidelinesCouplingProjections2018>

## Signal strength per production x decay mode

L = 3000 fb <sup>-1</sup>		Expected uncertainty [%]				
POI	Scenario	Total	Stat	SigTh	BkgTh	Expt
$\mu_{ggH}^{\gamma\gamma}$	S1	7.1	1.9	5.8	1.0	3.3
	S2	4.2	1.9	3.1	0.9	2.1
$\mu_{ggH}^{ZZ}$	S1	6.6	2.1	5.4	1.7	2.7
	S2	4.0	2.1	2.8	0.7	1.8
$\mu_{ggH}^{WW}$	S1	6.6	1.2	6.2	1.0	1.5
	S2	3.7	1.2	3.1	0.9	1.2
$\mu_{ggH}^{\tau\tau}$	S1	8.1	2.6	6.6	1.7	3.5
	S2	5.5	2.6	3.9	0.7	2.9
$\mu_{ggH}^{bb}$	S1	34.0	20.6	23.5	3.2	10.0
	S2	24.7	20.6	12.2	1.5	2.6
$\mu_{ggH}^{\mu\mu}$	S1	16.6	13.4	5.5	1.9	8.0
	S2	13.8	13.4	3.2	0.6	2.0



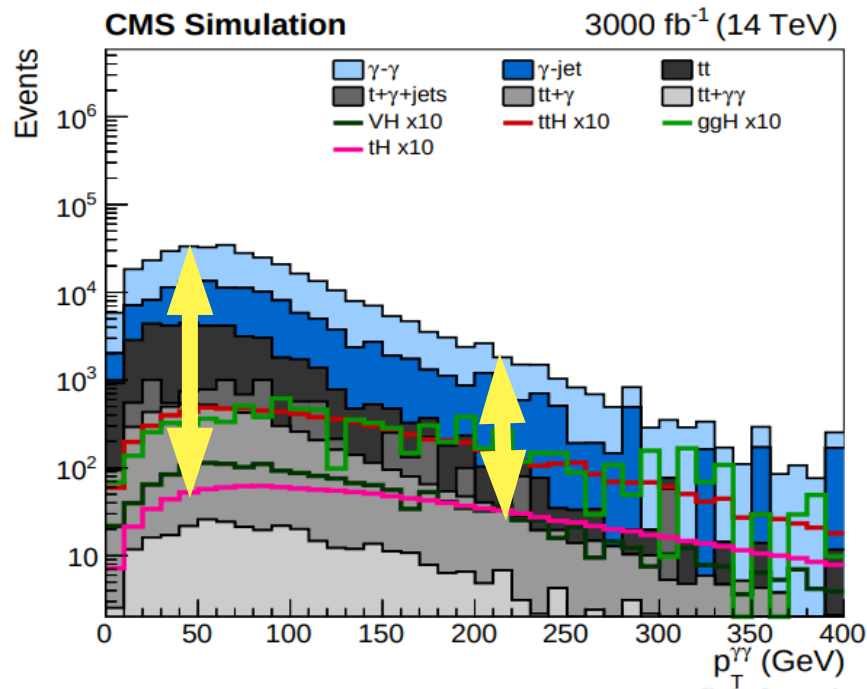
$$\chi^2 = \sum \frac{(1 - \mu(\kappa_\lambda))^2}{\sigma^2}$$



(plot done with old projections...)

## Global fit

- Differential uncertainties:
  - > Just rescaling uncertainties for cross section in each bin overestimates the reach:

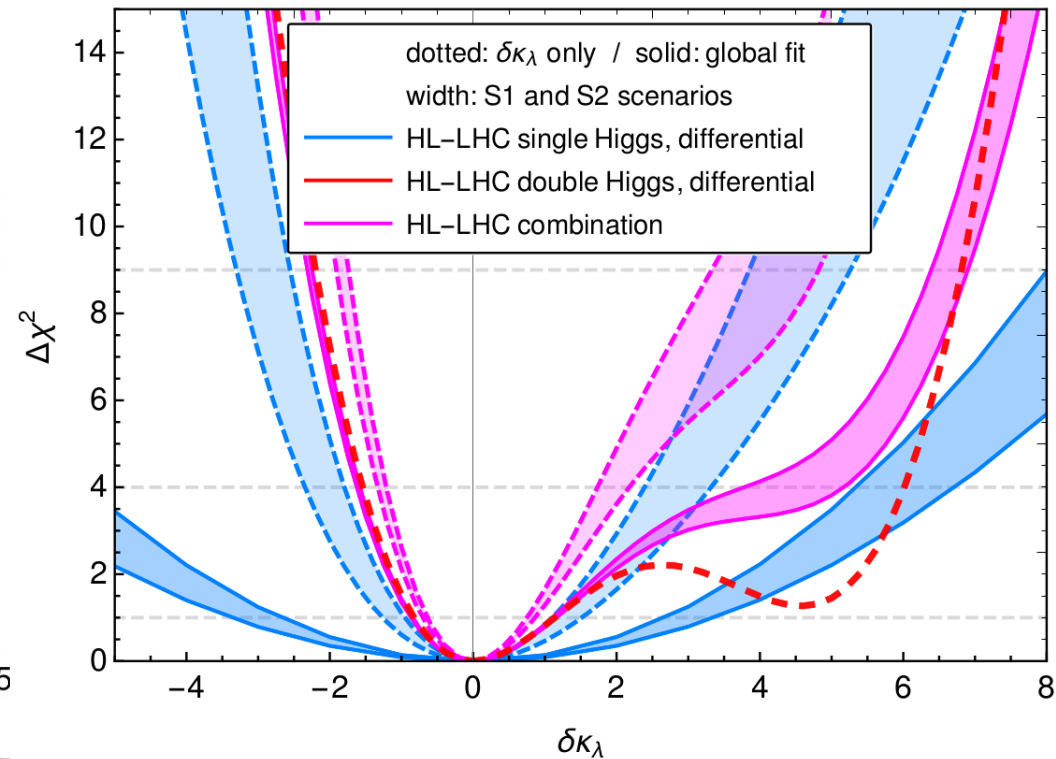
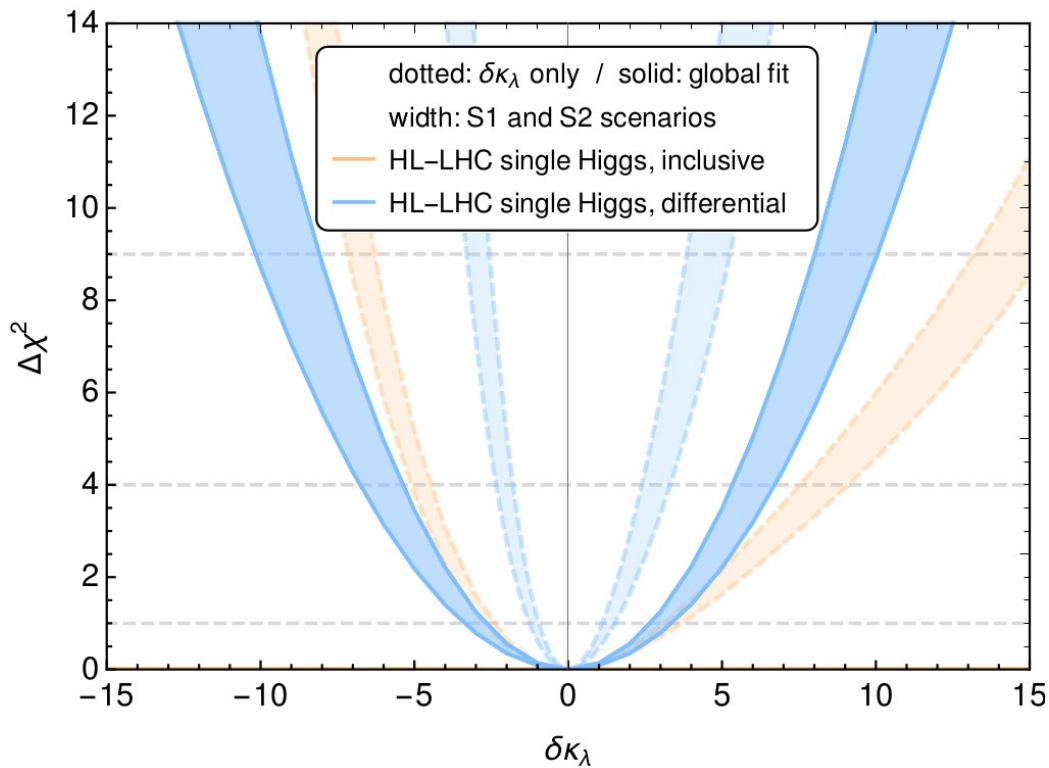


$p_T^H$ bin [GeV]	$\mu \pm \sigma_\mu = \mu \pm \sigma_\mu^{\text{stat}} \pm \sigma_\mu^{\text{syst.}}$
[0,45]	$1.00^{+0.410}_{-0.385} = 1.00^{+0.408+0.043}_{-0.385 -0.018}$
[45,80]	$1.00^{+0.290}_{-0.281} = 1.00^{+0.289+0.032}_{-0.281 -0.018}$
[80,120]	$1.00^{+0.243}_{-0.236} = 1.00^{+0.241+0.030}_{-0.235 -0.021}$
[120,200]	$1.00^{+0.168}_{-0.206} = 1.00^{+0.164+0.033}_{-0.204 -0.030}$
[200,350]	$1.00^{+0.172}_{-0.168} = 1.00^{+0.163+0.053}_{-0.159 -0.052}$
[350,∞]	$1.00^{+0.334}_{-0.304} = 1.00^{+0.303+0.141}_{-0.275 -0.130}$

- Background is larger at threshold, just where sensitivity to trilinear is larger.

Global fits using extrapolations of inclusive uncertainties to differential level must take this into account!

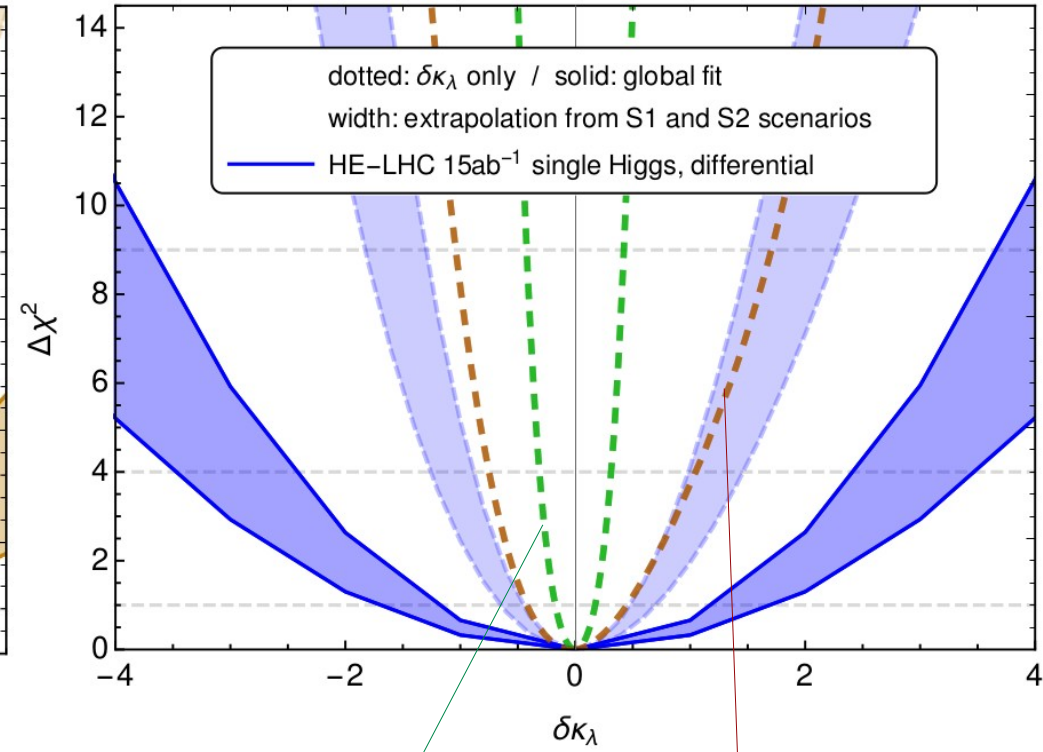
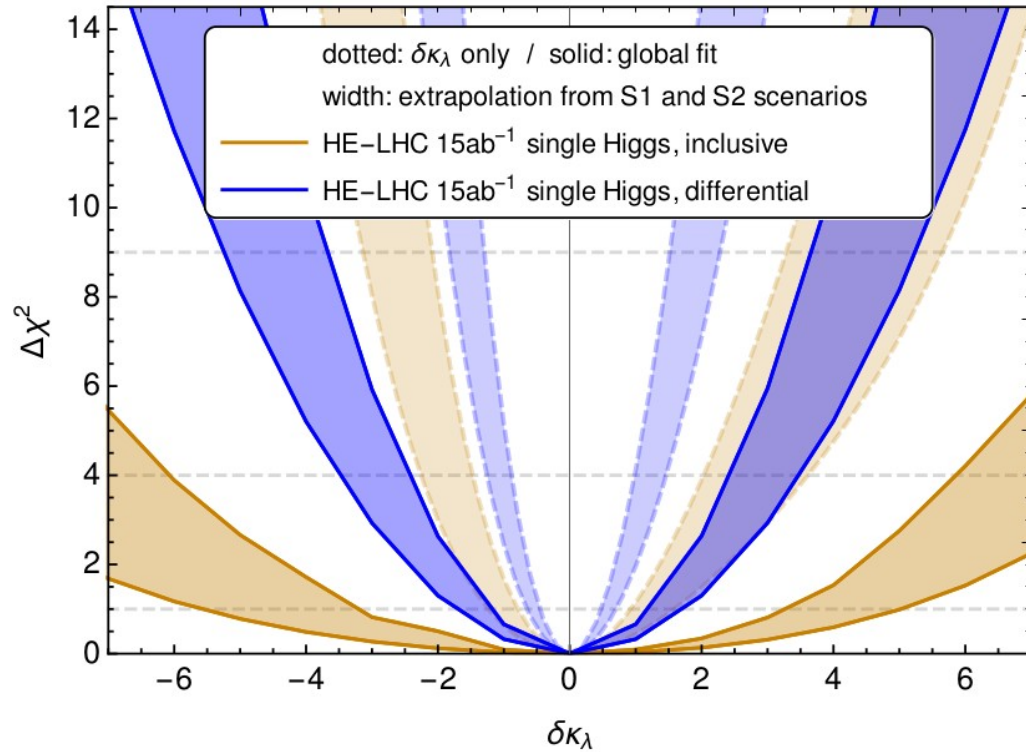
## Results at HL-LHC



- Differential information is crucial
- Differences between S1 and S2 scenarios: not limited by statistics
- Complementary with double Higgs production



## Results at HL-LHC



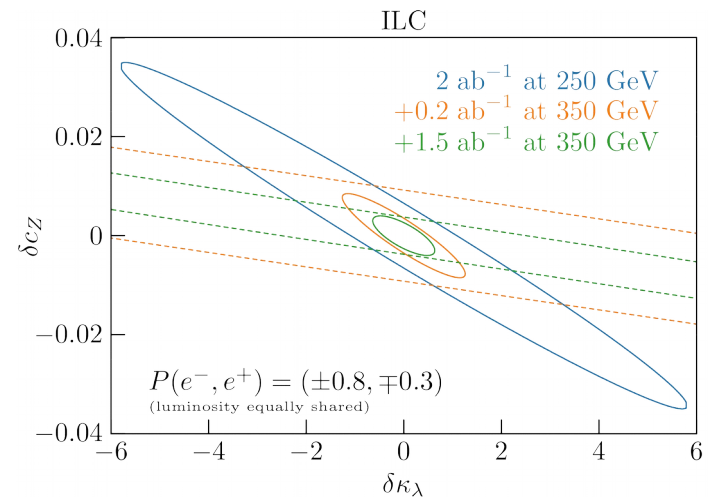
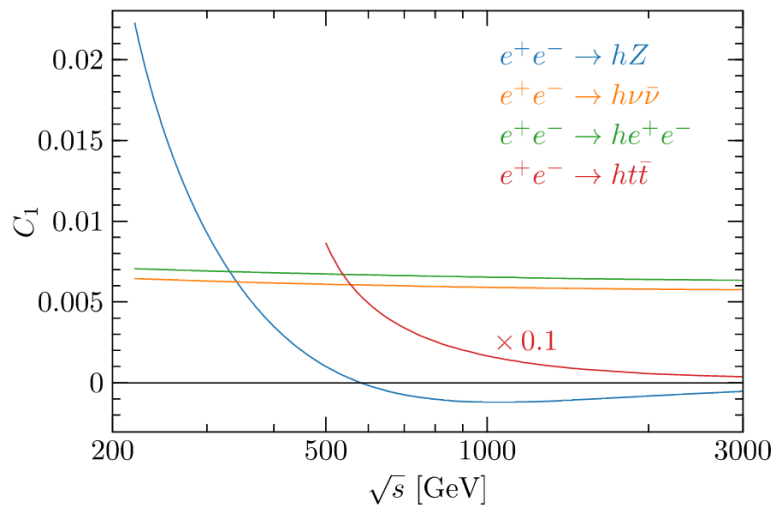
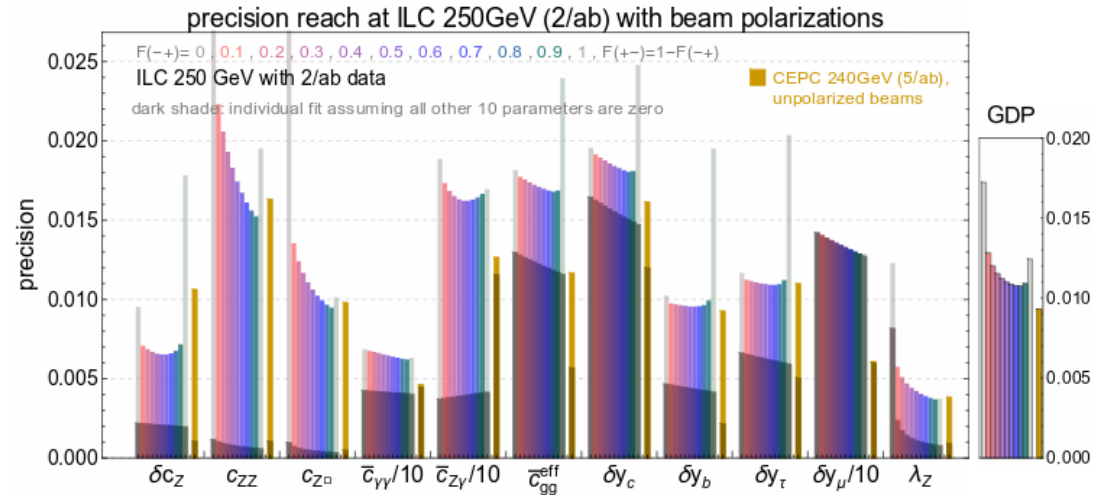
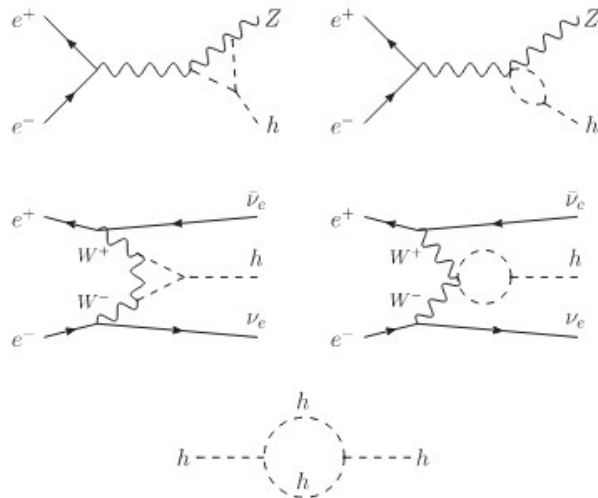
Homiller, Meade; 1811.02572  
 Goncalves, Han, Kling, Plehn, Takeuchi; 1802.04319

- Single Higgs production constrains trilinear between  $-3$  and  $3$  even in a global fit!
- Double Higgs production gives much stronger constraints.

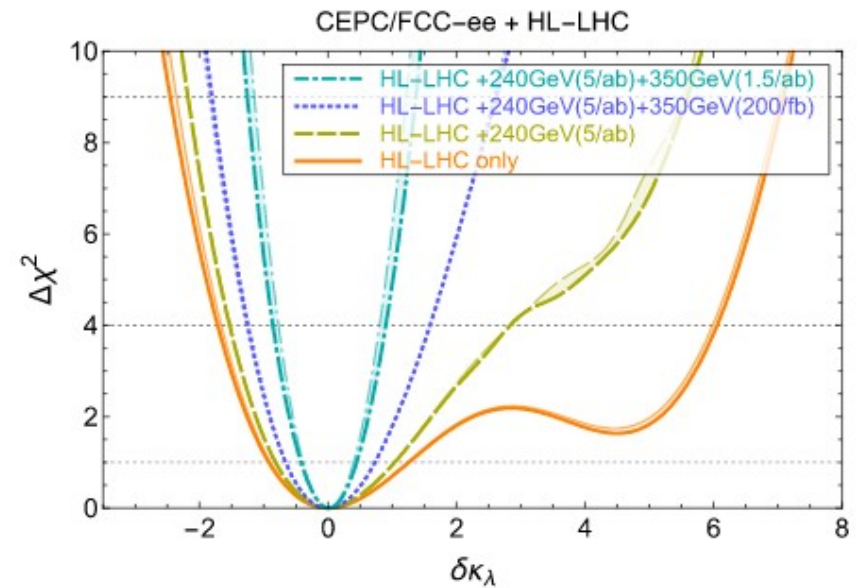
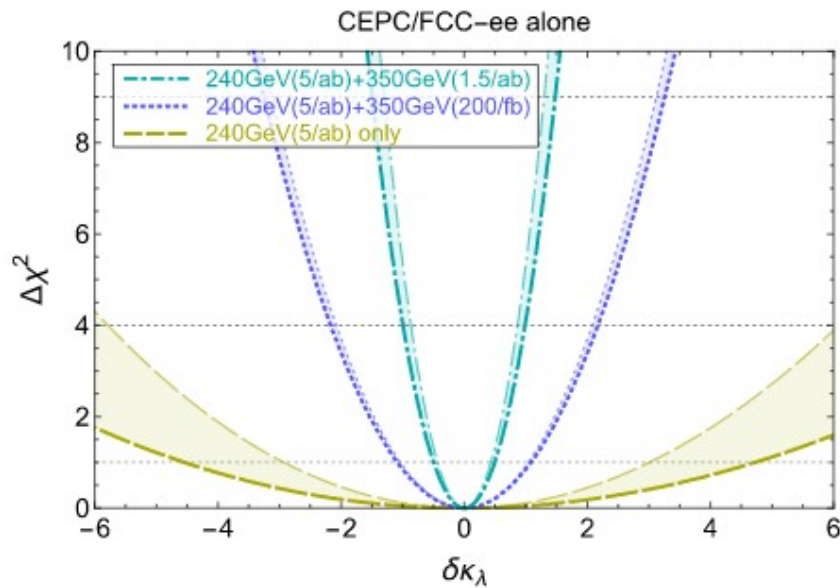
# Higgs self-coupling at lepton colliders

This program benefits from the high precision machines

arXiv:1704.02333

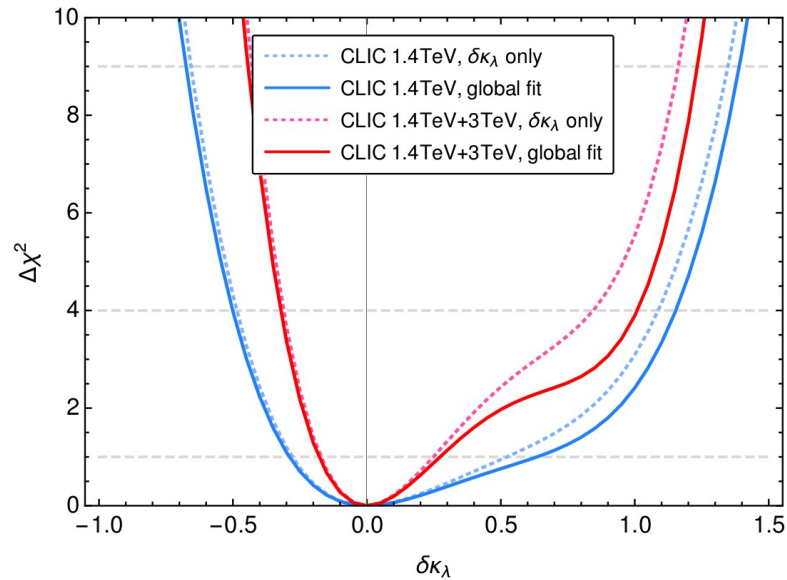
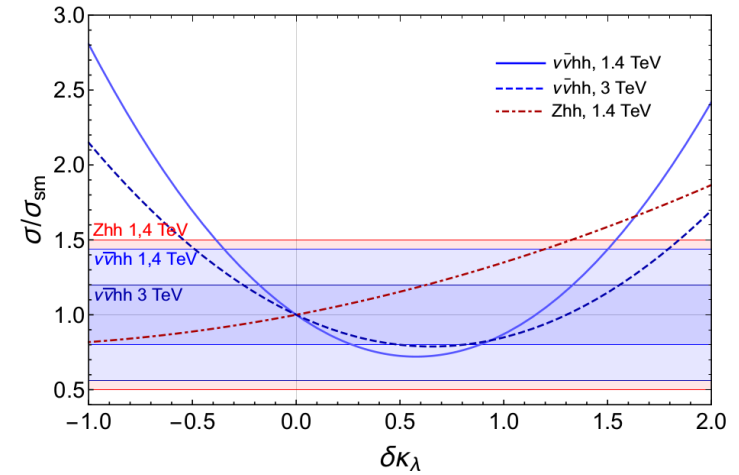
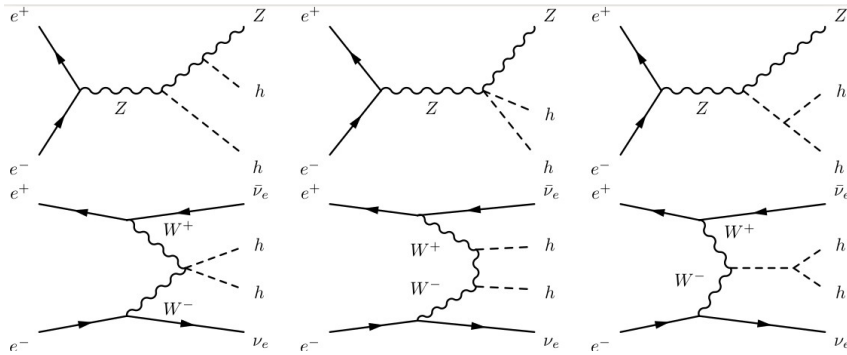


## Higgs self-coupling at lepton colliders



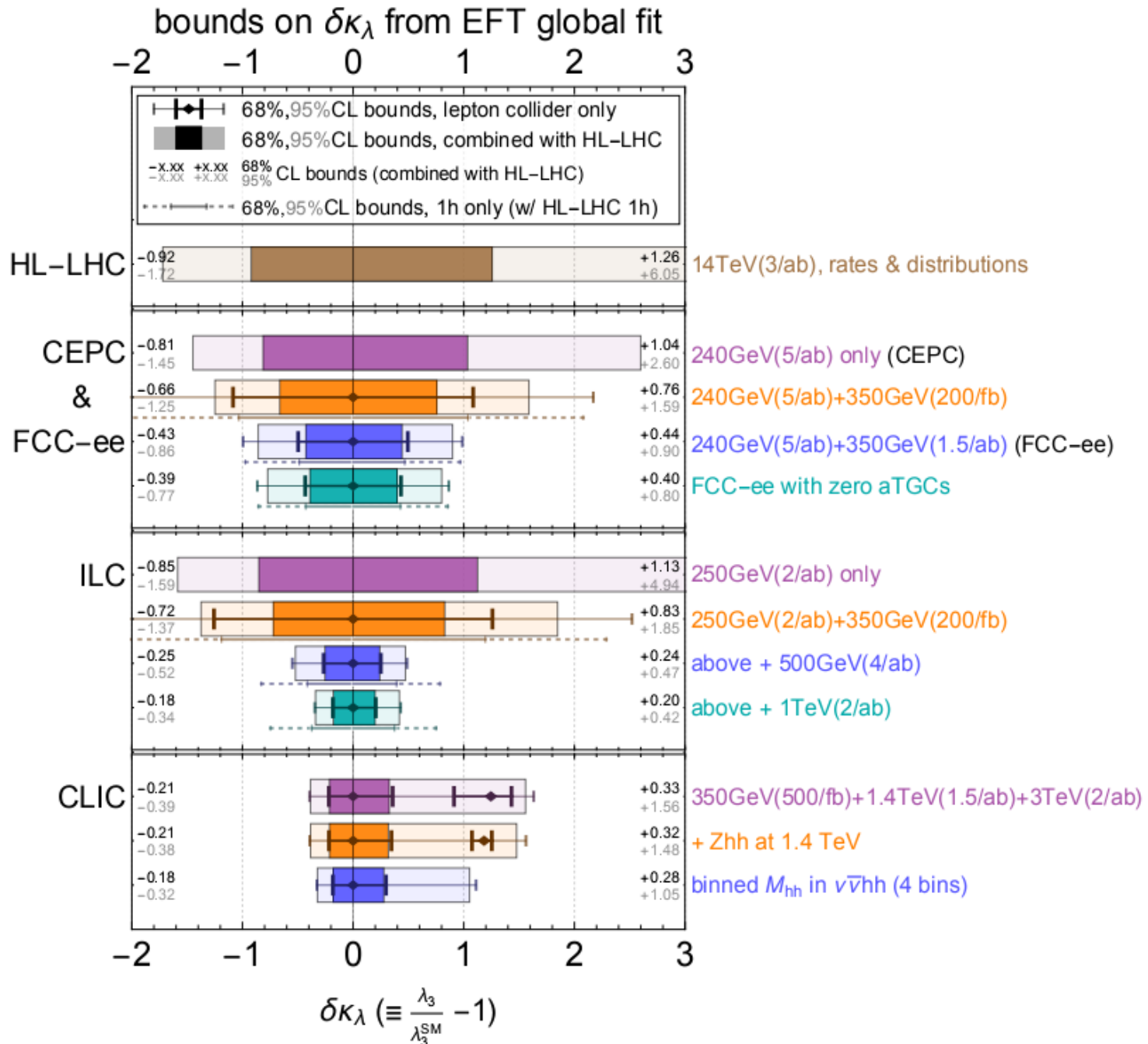
- Low energy lepton colliders set strong constraints on the self-coupling, even running below di-Higgs threshold.
- No self-coupling can be excluded at 95%CL!

# Higgs self-coupling at high energy lepton colliders



- At high energy lepton colliders, if kinematically allowed di-Higgs dominates the constraints.

## Summary



A few items for discussion...

- Some diff. distributions will get an amazing precision,

ATLAS											
$p_T^H$ [GeV]	0-10	10-15	15-20	20-30	30-45	45-60	60-80	80-120	120-200	200-350	350-1000
H $\rightarrow \gamma\gamma$	5.3%	4.6%		4.9%	4.7%	5.4%	5.7%	4.9%	4.2%	5.1%	8.7%
H $\rightarrow ZZ$	8.3%	7.6%	8.3%	6.3%	5.7%	6.2%	6.3%	5.7%	6.4%	13.1%	23.2%
Combination	4.5%	3.8%		3.9%	3.6%	4.1%	4.2%	3.7%	3.5%	4.5%	8.2%
CMS											
$p_T^H$ [GeV]	0-15	15-30	30-45	45-80	80-120	120-200	200-350	350-600	600- $\infty$		
H $\rightarrow \gamma\gamma$	5.1%	4.6%	5.1%	4.8%	4.9%	4.5%	5.1%	8.6%	32.2%		
H $\rightarrow ZZ$	5.4%	4.8%		4.1%	4.7%			9.1%			
H $\rightarrow bb$				none				31.4%	36.8%		
Combination	3.7%	3.3%	4.2%	3.7%	4.0%	3.8%	4.4%	8.0%	24.5%		

Table 26: Relative uncertainties on the projected  $p_T^H$  spectrum measurements by ATLAS and CMS under S2 at  $3000 \text{ fb}^{-1}$ .

there seems to be room for improvement.

- Different from *traditional* EFT dimension 6 effects, since they show up at large invariant masses, while here the crucial aspect is high precision near threshold.
- Current theory fit for tth is validated with CMS projections for tth, but the rest are not... need for more experimental studies!