

European Neutrino Town Meeting

# Hadron and Nuclear Physics for Oscillation Experiments

Luis Alvarez Ruso



# Introduction

- $\nu$  cross sections are **crucial** to achieve the **precision goals** of **oscillation experiments**

$$\frac{N_{events}^{far}(E_\nu)}{N_{events}(E_\nu)} = \frac{\int \sigma(E'_\nu) \Phi(E'_\nu) P(E_\nu | E'_\nu) P_{osc}(E'_\nu) dE'_\nu}{\int \sigma(E'_\nu) \Phi(E'_\nu) P(E_\nu | E'_\nu) dE'_\nu}$$

F. Sanchez @ NuPhys2015

- Need for theory?
  - Measurements are not (cannot be) comprehensive
    - the same (semi)-inclusive cross section can correspond to **different exclusive final states**, depending on the **reaction mechanism**
    - measurements (partially) rely on **simulations  $\approx$  theory** to determine efficiency, acceptance, ...
  - $E_\nu$  is not known: reconstructed using kinematics and/or calorimetry
  - $\sigma(\nu_\mu)$  to  $\sigma(\nu_e)$  extrapolations
- **Neutrino-nucleus** c.s. mismodeling could lead to unacceptably large systematic uncertainties or biased measurements  
Coloma, Huber, PRL 111 (2013)

# Nucleon axial form factor

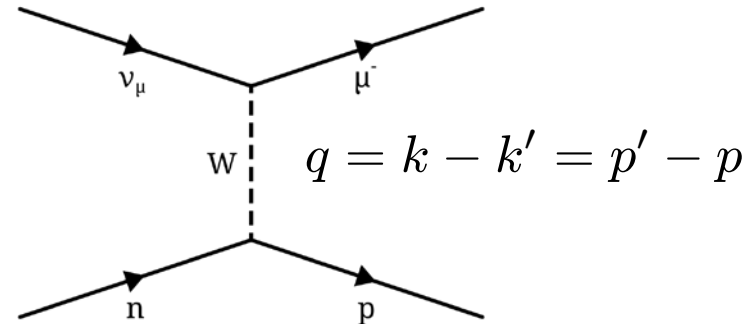
- Fundamental **nucleon** property
- Main source of uncertainty for **QE scattering** on **nucleons**:

$$\text{CCQE} : \nu(k) + n(p) \rightarrow l^-(k') + p(p')$$

$$\bar{\nu}(k) + p(p) \rightarrow l^+(k') + n(p')$$

$$\text{NCE} : \nu(k) + N(p) \rightarrow \nu(k') + N(p')$$

$$\bar{\nu}(k) + N(p) \rightarrow \bar{\nu}(k') + N(p')$$



- Largest contribution at **T2K, MicroBooNE**
- Used for kinematic  $E_\nu$  reconstruction:

$$E_\nu^{\text{QE}} = \frac{2m_n E_\mu - m_\mu^2 - m_n^2 + m_p^2}{2(m_n - E_\mu + p_\mu \cos \theta_\mu)}$$

- Input in models of non-resonant inelastic reactions (**meson production**) and **two-nucleon currents**

# Nucleon axial form factor

- What is known:

- $F_A(0) = g_A \leftarrow \beta \text{ decay}$

- $F_A(\infty) \sim Q^{-4} \leftarrow \text{QCD}$

- Main source of information: bubble chamber (ANL, BNL, FNAL) data

- **Dipole ansatz:** Bodek et al., EPJC 53 (2008)

$$F_A(Q^2) = g_A \left( 1 + \frac{Q^2}{M_A^2} \right)^{-2} \quad \langle r_A^2 \rangle = \frac{12}{M_A^2}$$

- **z-expansion:** Meyer et al., PRD 93 (2016)

- **Neural networks + Bayesian statistics:** LAR, Graczyk, Saúl-Sala, arXiv:1805.00905

- All methods obtain similar  $F(Q^2)$ ...

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- $\langle r_A^2 \rangle = 0.453(12) \text{ fm}^2$

- **z-expansion:** Meyer et al., PRD 93 (2016)

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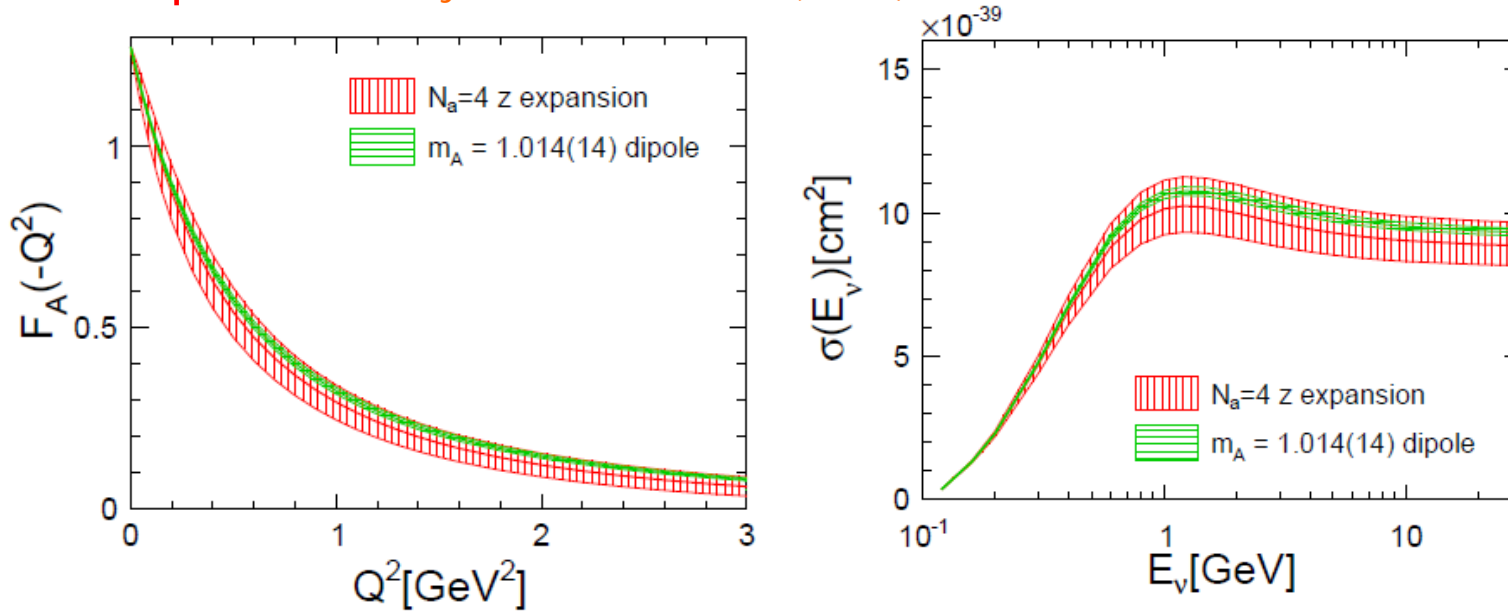
- $\langle r_A^2 \rangle = 0.471(15) \text{ fm}^2 \leftarrow \text{ANL only so far}$

- All methods obtain similar  $F(Q^2)$ ...

- ... but with **different errors**

# QE scattering on the nucleon

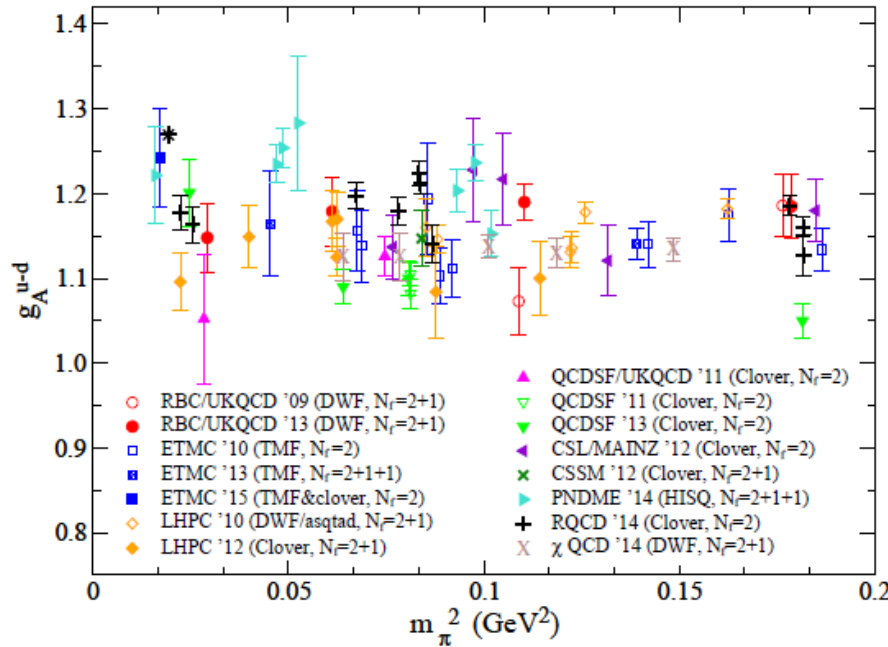
- **z-expansion** Meyer et al., PRD 93 (2016)



- At  $E_\nu \sim 1$  GeV  $\sigma(\text{CCQE})$  has  $\approx 10\%$  error
- **More precise information about  $F_A$  is needed**
  - Direct or indirect **CCQE** measurement on n/p
  - Lattice QCD

# $F_A$ & LQCD

- $g_A$  : lower than exp. values have been recurrently obtained



Constantinou, PoS CD15 (2015) 009

- Recent progress:
  - improved algorithms for a careful treatment of excited states
  - low pion masses
  - A per-cent-level determination of the nucleon axial coupling from QCD

Chang et al., Nature 558 (2018)

# $F_A$ & LQCD

## Recent progress:

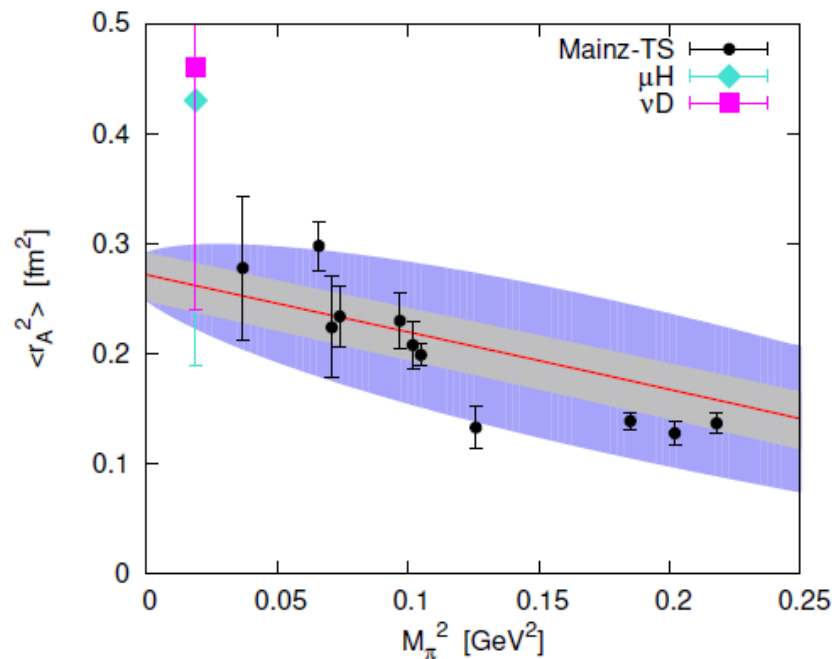
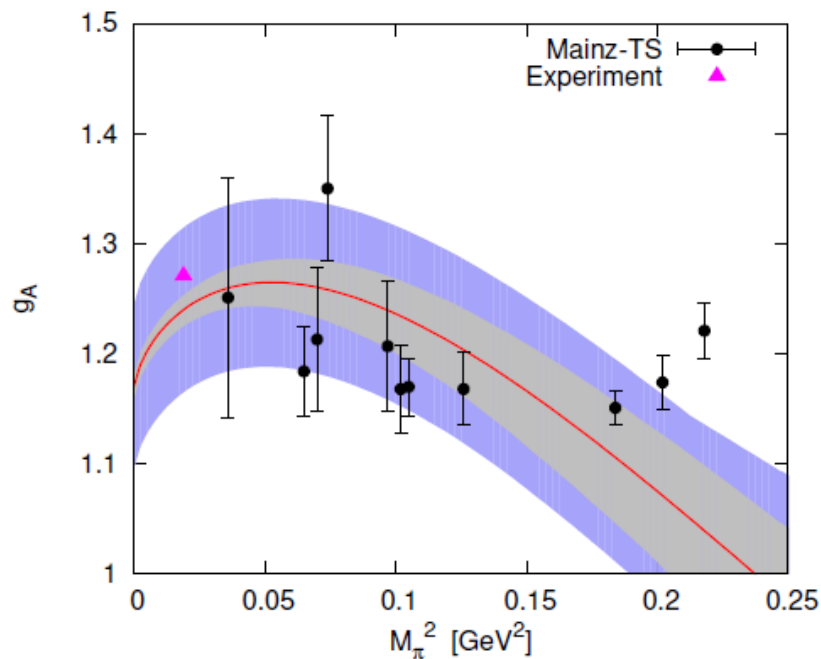
Alexandrou et al., PRD 96 (2017)

Capitani et al., arXiv:1705.06186

Gupta et al., PRD 96 (2017)

## Baryon ChPT analysis: Yao, LAR, Vicente Vacas, PRD 96 (2017)

- $O(p^3)$ ,  $Q^2 < 0.36 \text{ GeV}^2$ ,  $130 \text{ MeV} < M_\pi < 473 \text{ MeV}$ , explicit  $\Delta(1232)$



- $g_A = 1.237(74)$ ,  $\langle r_A^2 \rangle = 0.263(38) \text{ fm}^2$



# $1\pi$ production on the nucleon

$$\nu_l N \rightarrow l \pi N'$$

- CC:  $\nu_\mu p \rightarrow \mu^- p \pi^+$ ,  $\bar{\nu}_\mu p \rightarrow \mu^+ p \pi^-$   
 $\nu_\mu n \rightarrow \mu^- p \pi^0$ ,  $\bar{\nu}_\mu p \rightarrow \mu^+ n \pi^0$   
 $\nu_\mu n \rightarrow \mu^- n \pi^+$ ,  $\bar{\nu}_\mu n \rightarrow \mu^+ n \pi^-$

- source of CCQE-like events (in nuclei)

- needs to be subtracted for a good  $E_\nu$  reconstruction

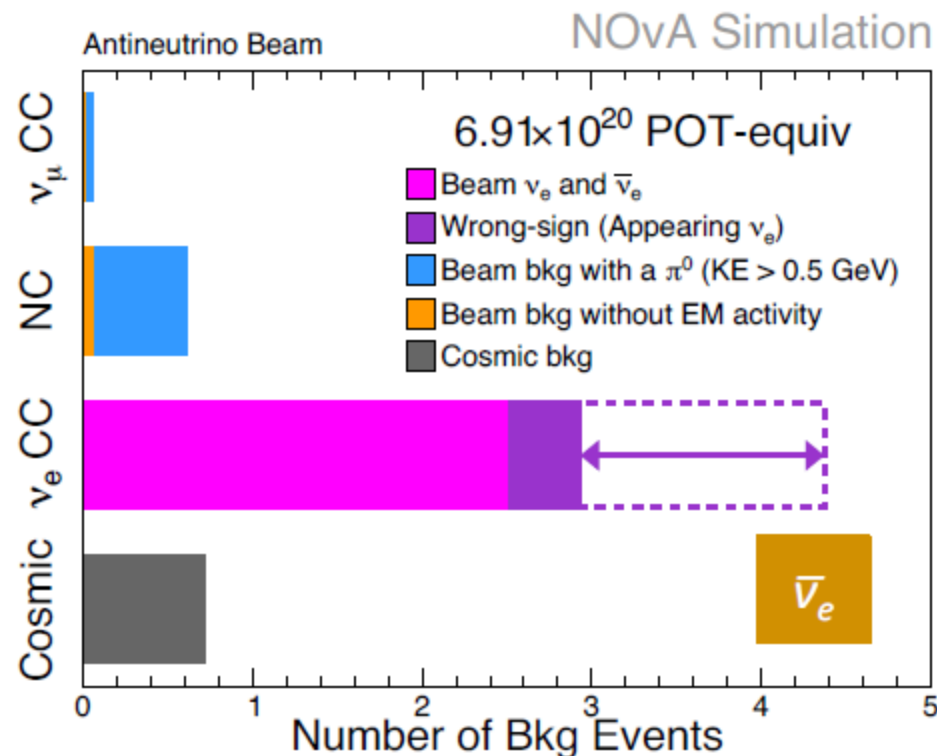
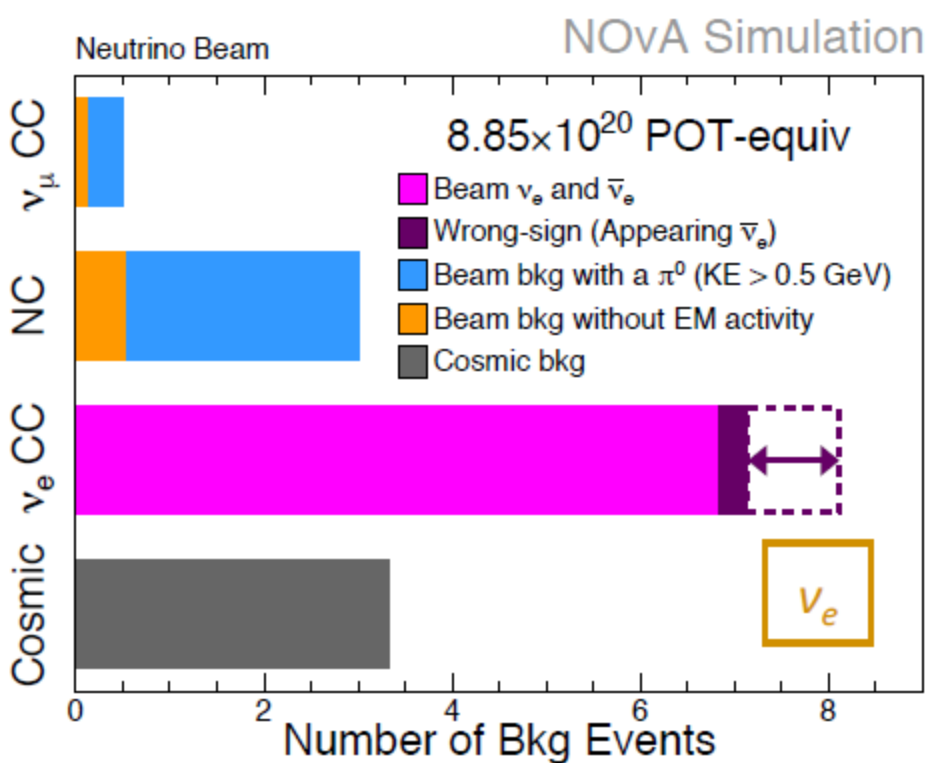
- NC:  $\nu_\mu p \rightarrow \nu_\mu p \pi^0$ ,  $\bar{\nu}_\mu p \rightarrow \bar{\nu}_\mu p \pi^0$   
 $\nu_\mu p \rightarrow \nu_\mu n \pi^+$ ,  $\bar{\nu}_\mu n \rightarrow \bar{\nu}_\mu n \pi^0$   
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 $\nu_\mu n \rightarrow \nu_\mu p \pi^-$ ,  $\bar{\nu}_\mu n \rightarrow \bar{\nu}_\mu p \pi^-$

- e-like background to  $\nu_\mu \rightarrow \nu_e$  (T2K, NOvA)

# 1 $\pi$ production on the nucleon

$$\nu_l N \rightarrow l \pi N'$$

## $\nu_e$ and $\bar{\nu}_e$ Background at the Far Detector



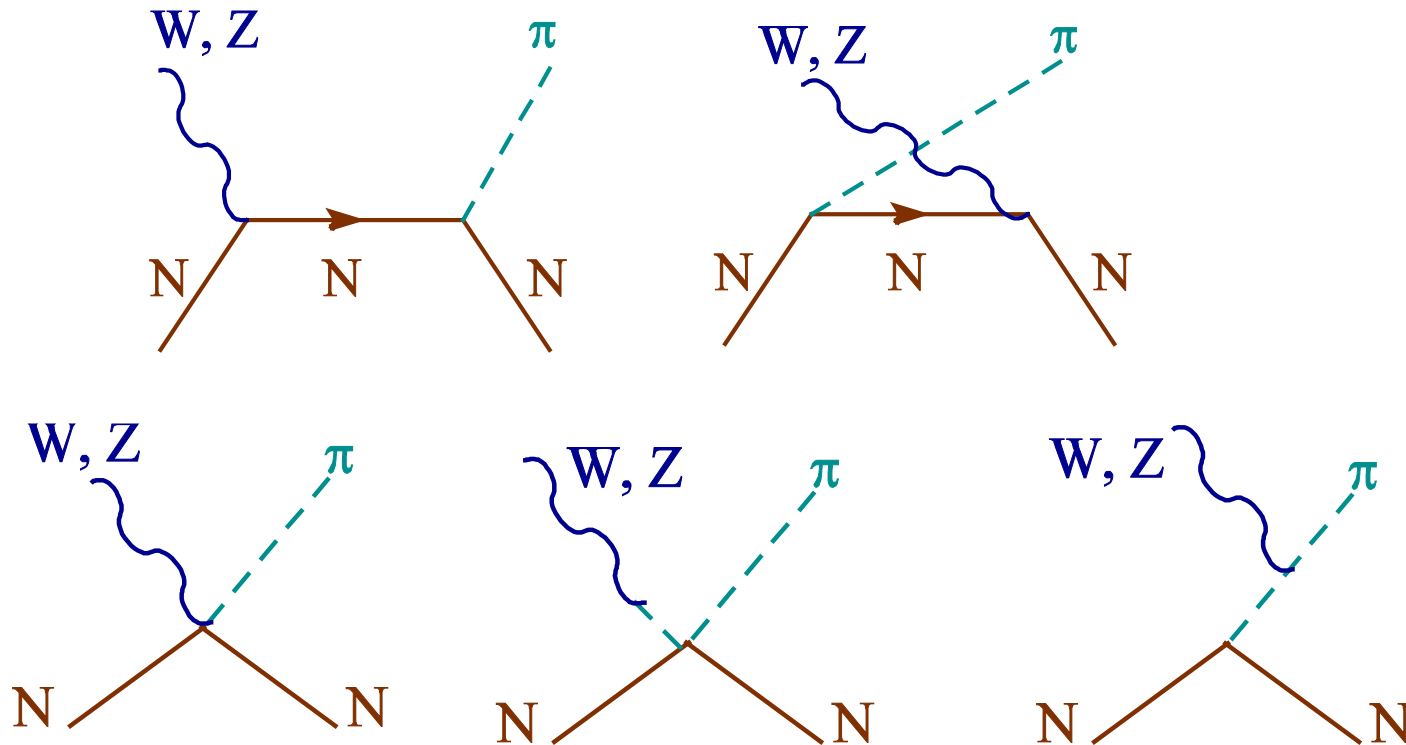
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M. Muether @ NUSTEC 2018

# $1\pi$ production on the nucleon

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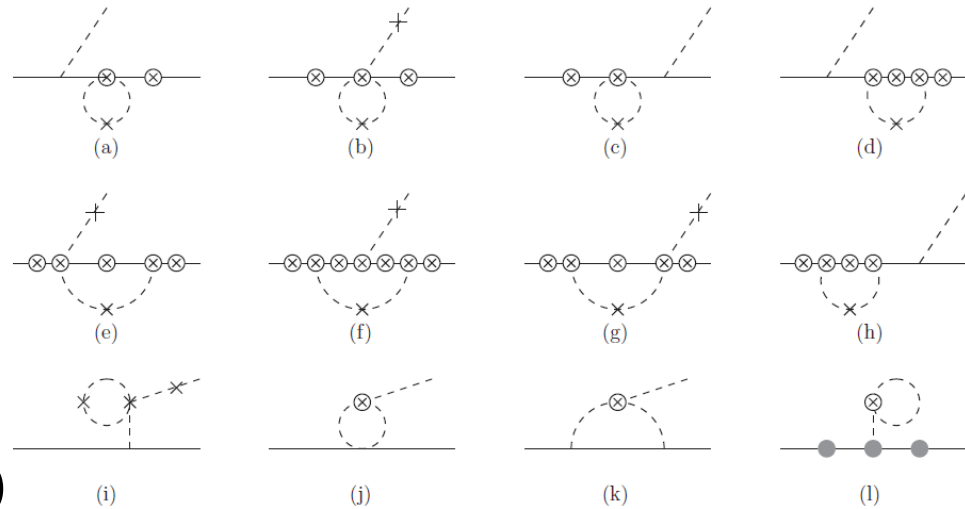
■ From **Chiral symmetry**:



Hernandez et al., Phys.Rev. D76 (2007) 033005

# Weak pion production in ChPT

- First study in ChPT: Yao et al., PRD 98 (2018)
- Part of a comprehensive study of  $\pi N \rightarrow N\pi$ ,  $\gamma^* N \rightarrow N\pi$ ,  $W^*$ ,  $Z^* N \rightarrow N\pi$ , ...
- EOMS, explicit  $\Delta(1232)$ ,  $O(p^3)$  in the  $\delta$ -counting:  $\delta = m_\Delta - m_N \sim O(p^{1/2})$

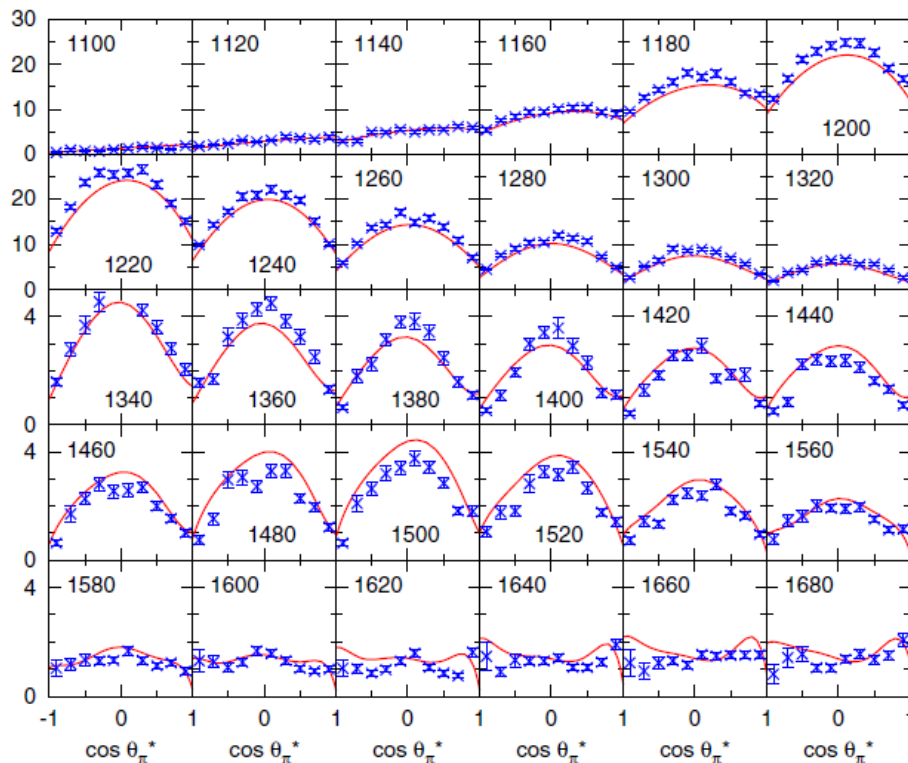


- LECs : 22 in total
  - 7 unknown (not very relevant)
    - 4 can be extracted from pion electroproduction
    - information about remaining 3 could be obtained from new close-to-threshold measurements of  $\nu$ -induced  $\pi$  production on protons
- Valid only close to threshold
- Benchmark for phenomenological models

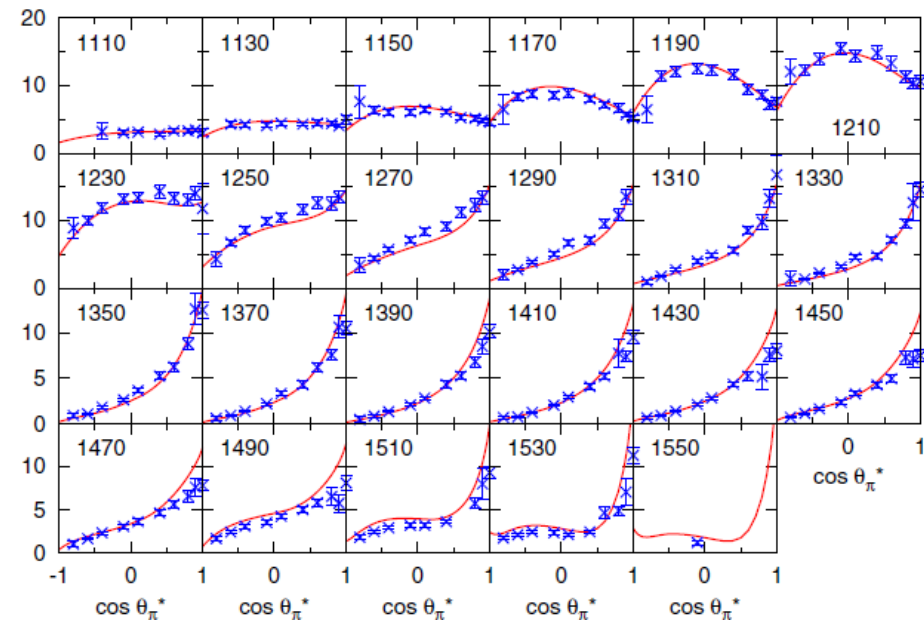
# $1\pi$ production on the nucleon

- Pheno models rely on (non- $\nu$ ) data as **input** and/or **validation**
  - **Vector current** can be constrained with  $\gamma N \rightarrow N \pi$ ,  $e N \rightarrow e' N \pi$

$p(e, e' \pi^0) p$



$p(e, e' \pi^+) n$

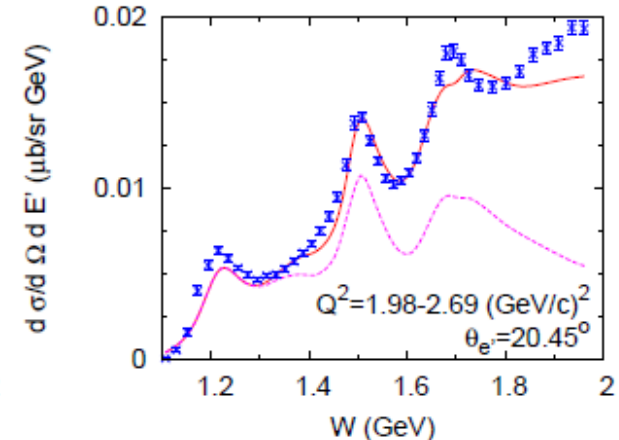
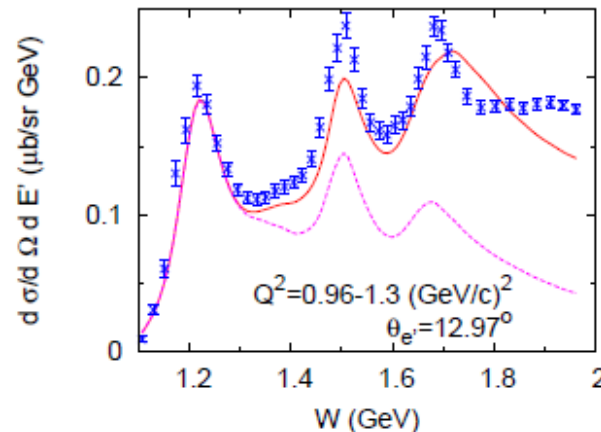
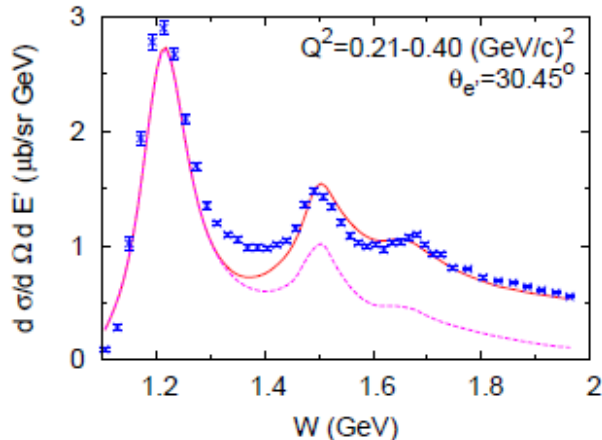


- e.g. **Dynamical Coupled Channel (DCC) Model** Nakamura et al., PRD92 (2015)

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  - Axial current at  $q^2 \rightarrow 0$  can be constrained with  $\pi N \rightarrow N\pi$  (**PCAC**)

$$\left. \frac{d\sigma_{CC\pi}}{dE_l d\Omega_l} \right|_{q^2=0} = \frac{G_F^2 V_{ud}^2}{2\pi^2} \frac{2f_\pi^2}{\pi} \frac{E_l^2}{E_\nu - E_l} \sigma_{\pi N}$$



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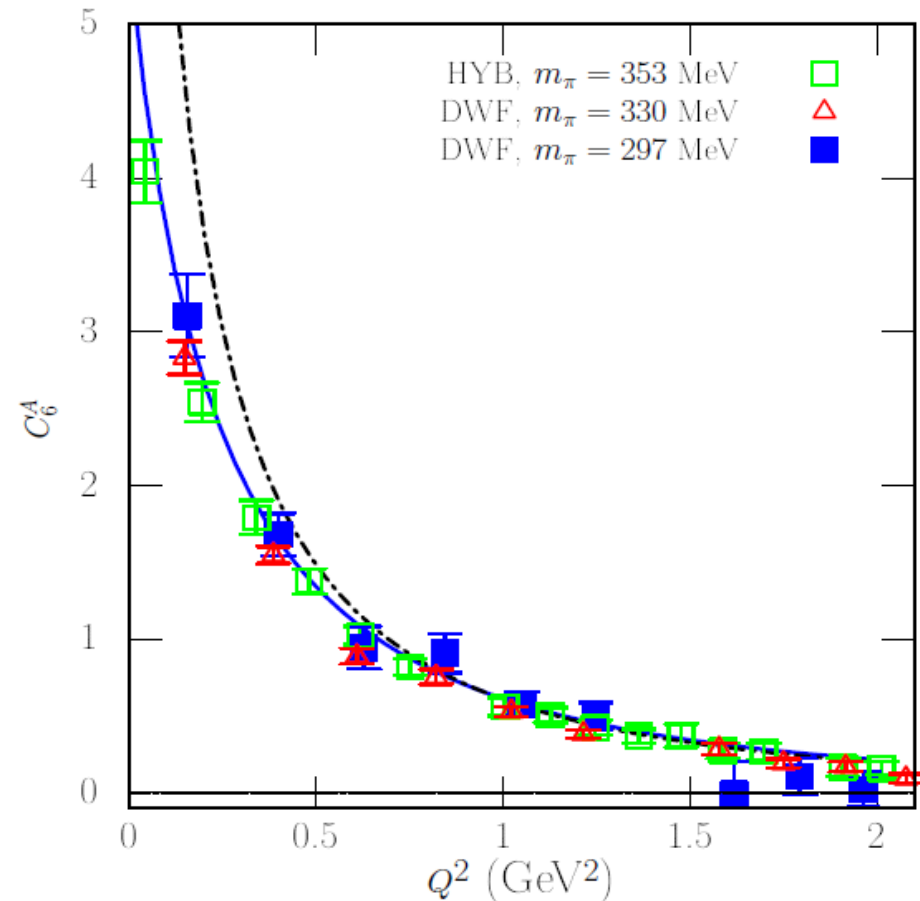
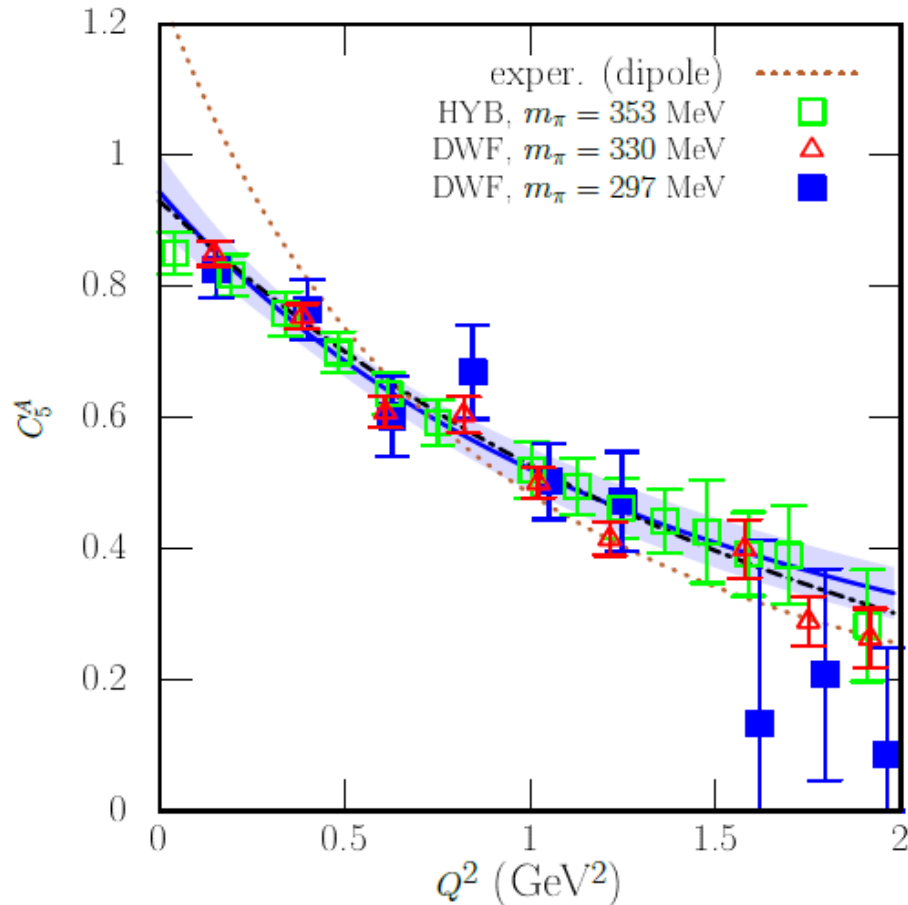
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- Very limited information about the axial current at  $q^2 \neq 0$ 
  - Some on **N- $\Delta(1232)$**  from **ANL** and **BNL** data on  $\nu_\mu d \rightarrow \mu^- \pi^+ p n$
  - Direct or indirect **CCQE** measurement on **n/p**
  - **Lattice QCD**

# Inelastic form factors & LQCD

## ■ N- $\Delta$ axial form factors in LQCD

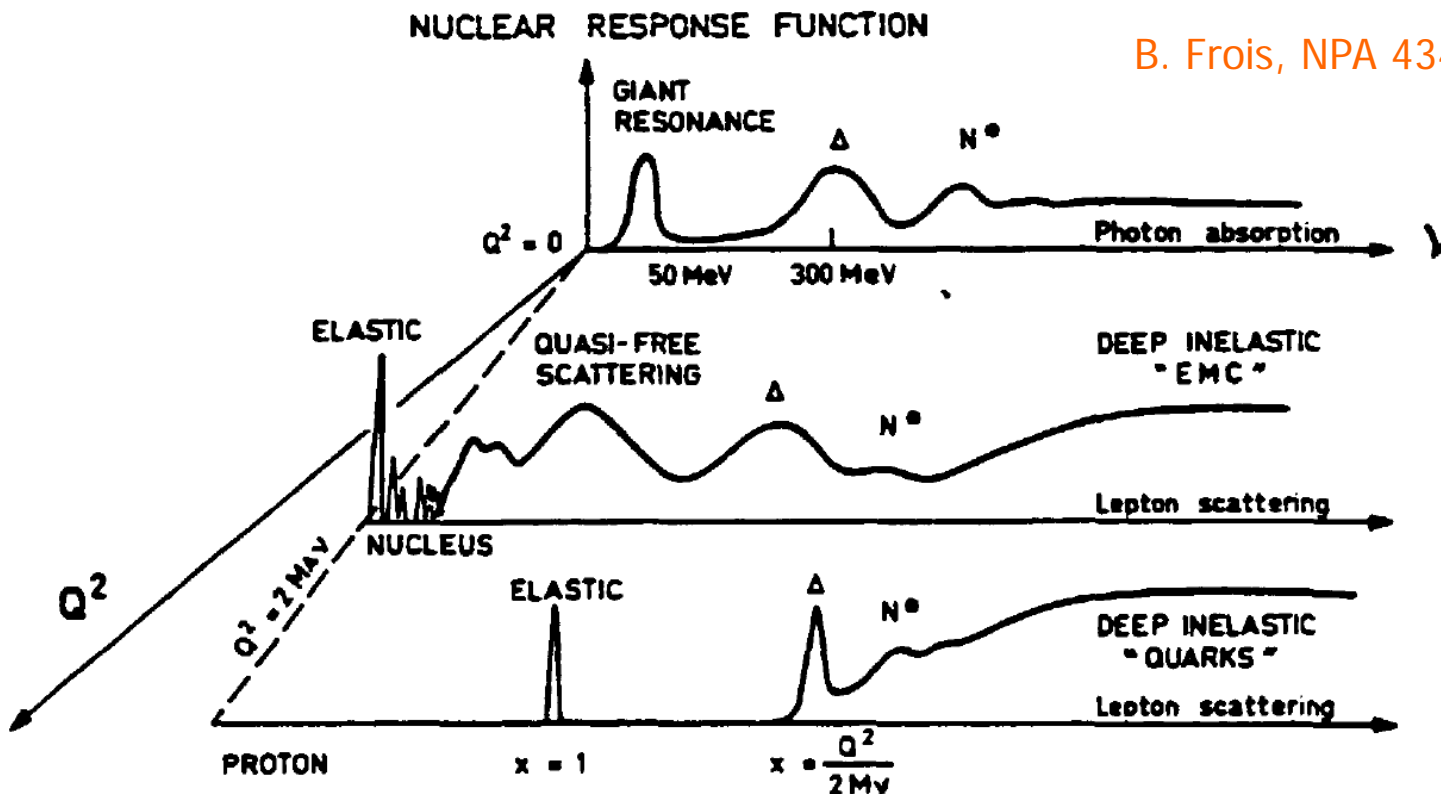
Alexandrou et al., PRD83 (2011)





# Neutrino interactions on nuclei

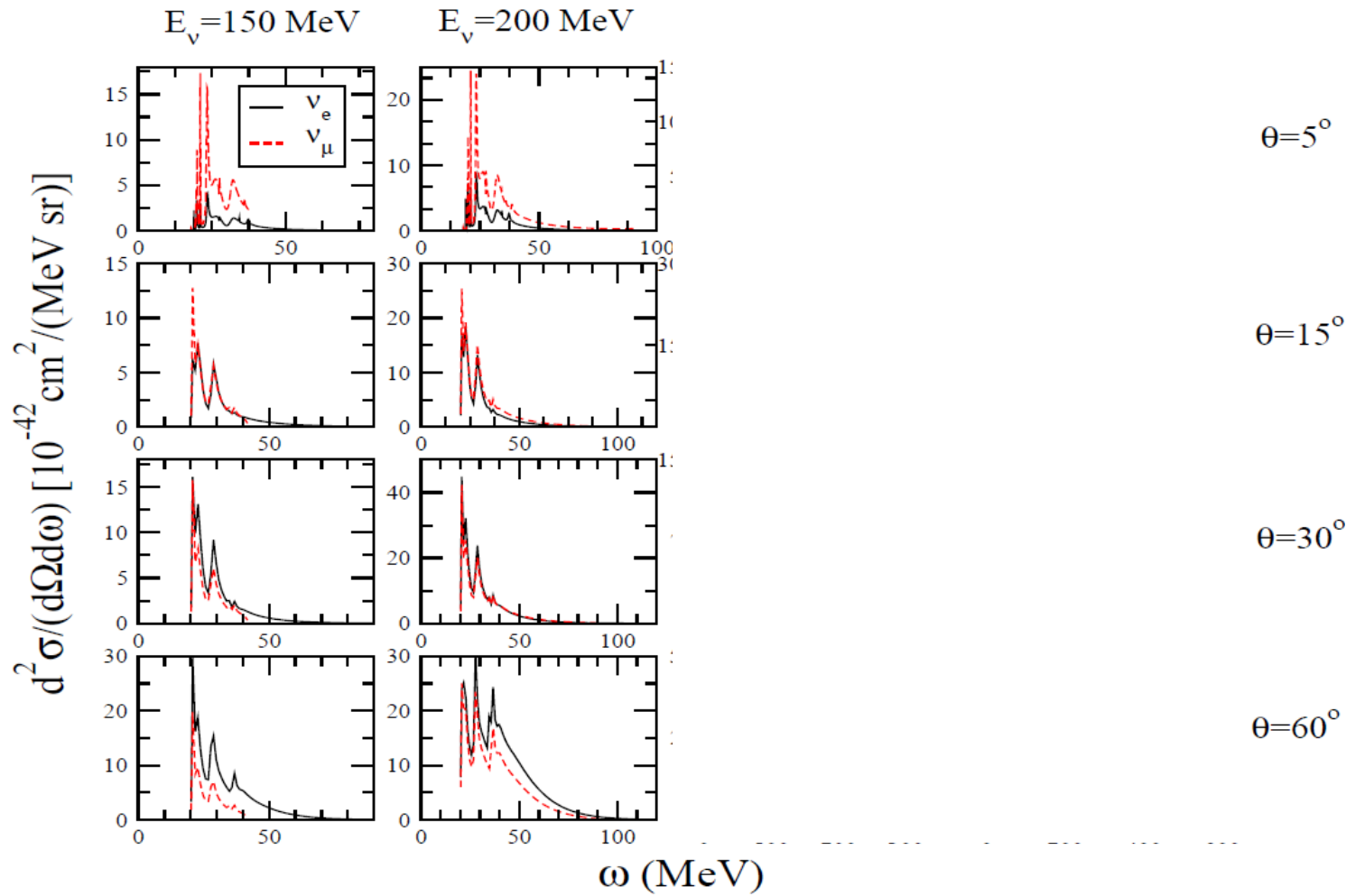
- Multiscale (even at a given  $E_\nu$ ), multi-nucleon problem



- Shell structure, collective excitations, QE peak, ...
- initial state description: non-relativistic
- final state interactions: (relativistic)  $NN$ ,  $\pi N$ , ...

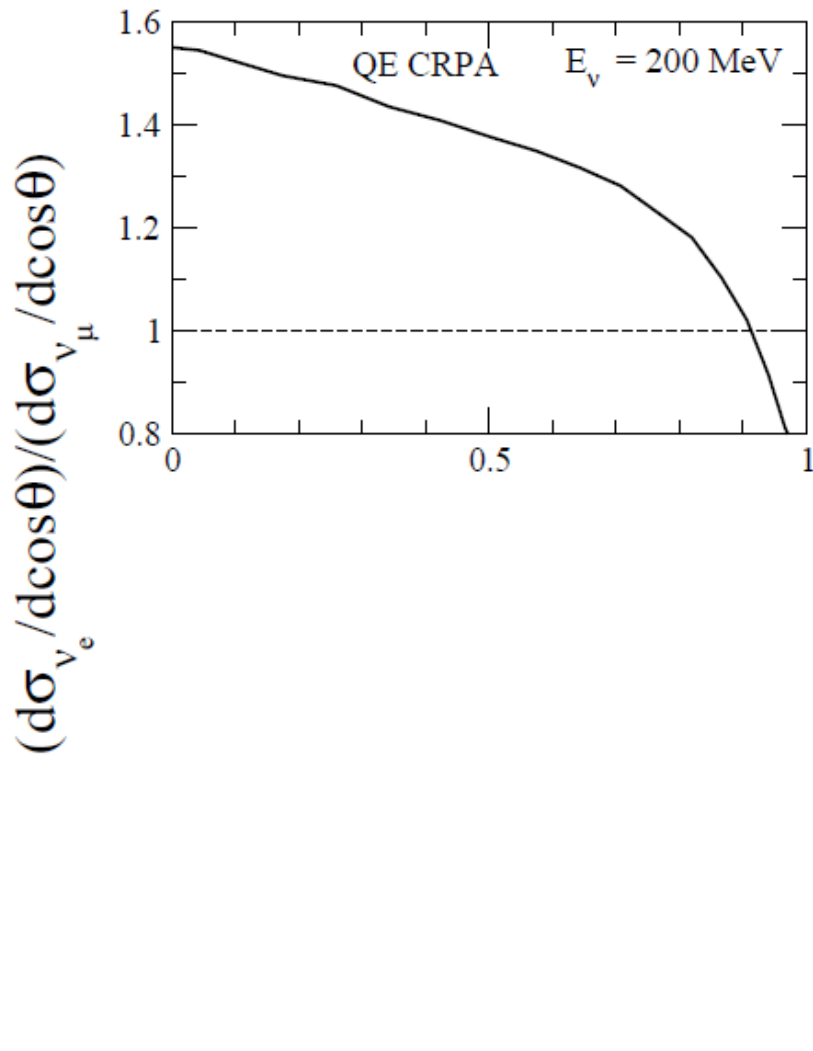
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CRPA Gent, Jachowicz et al.

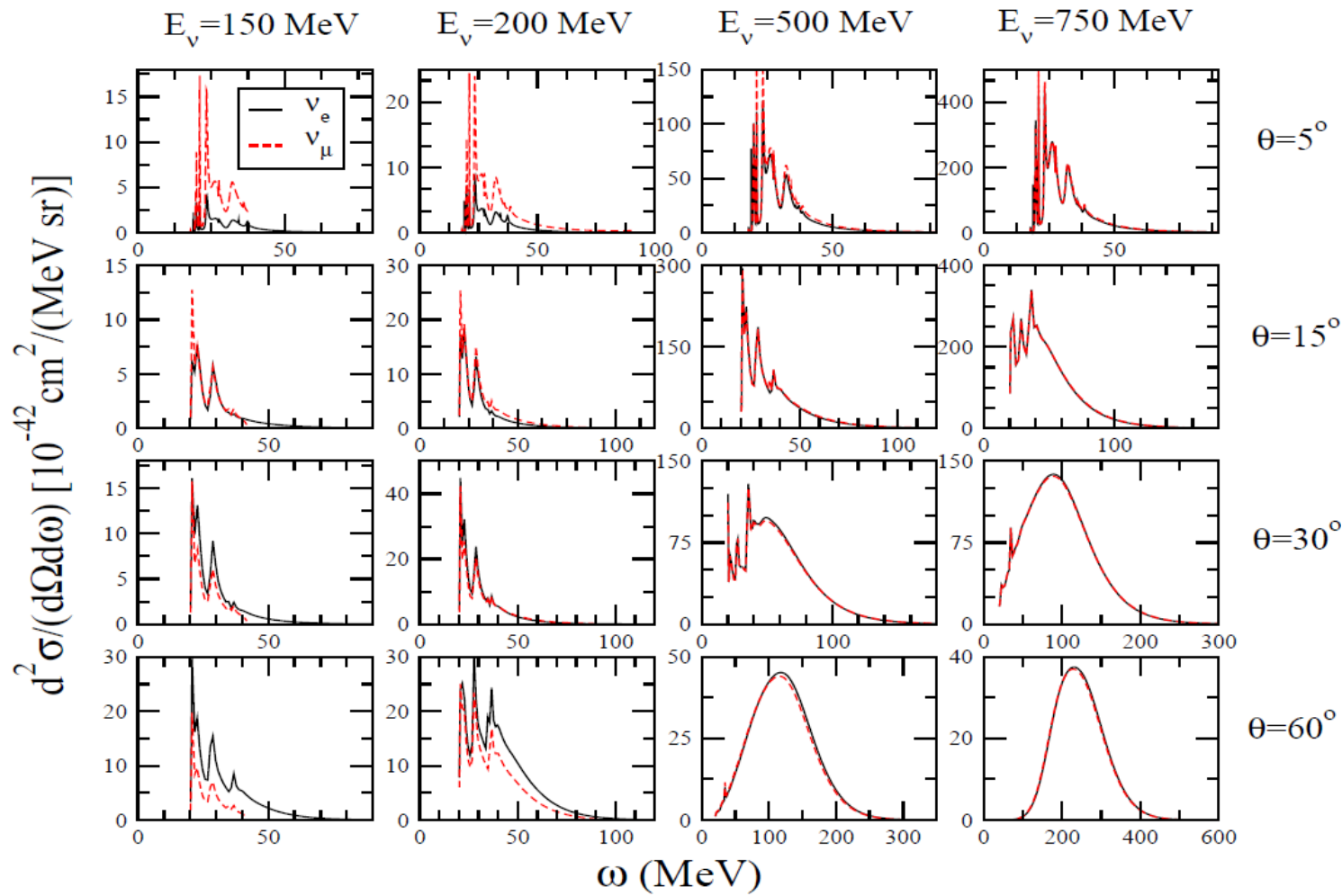
$$\sigma(\nu_e)/\sigma(\nu_\mu)$$



Martini, Jachowicz et al., PRC94 (2016)

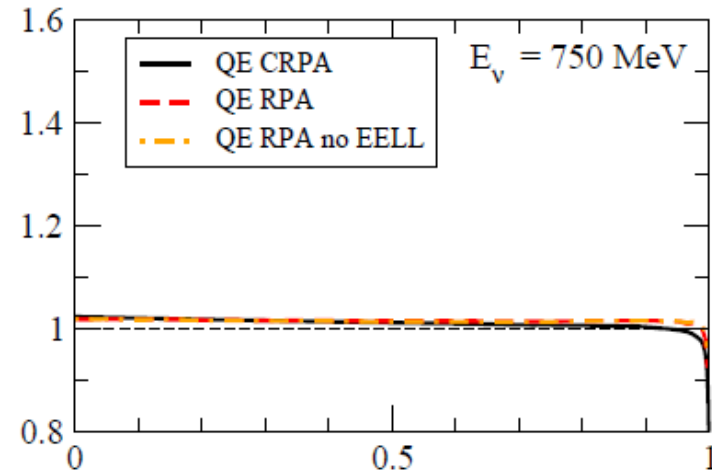
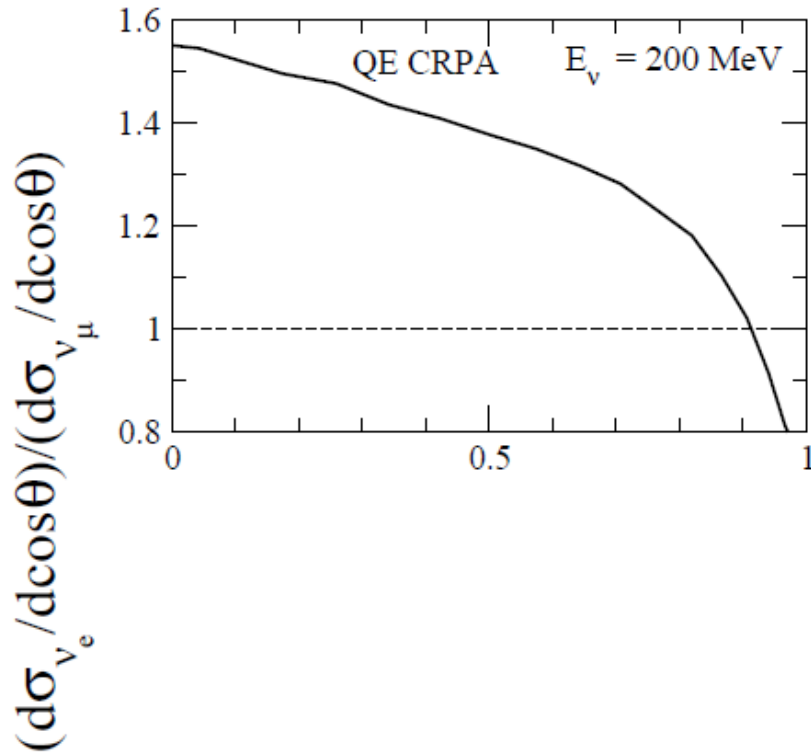
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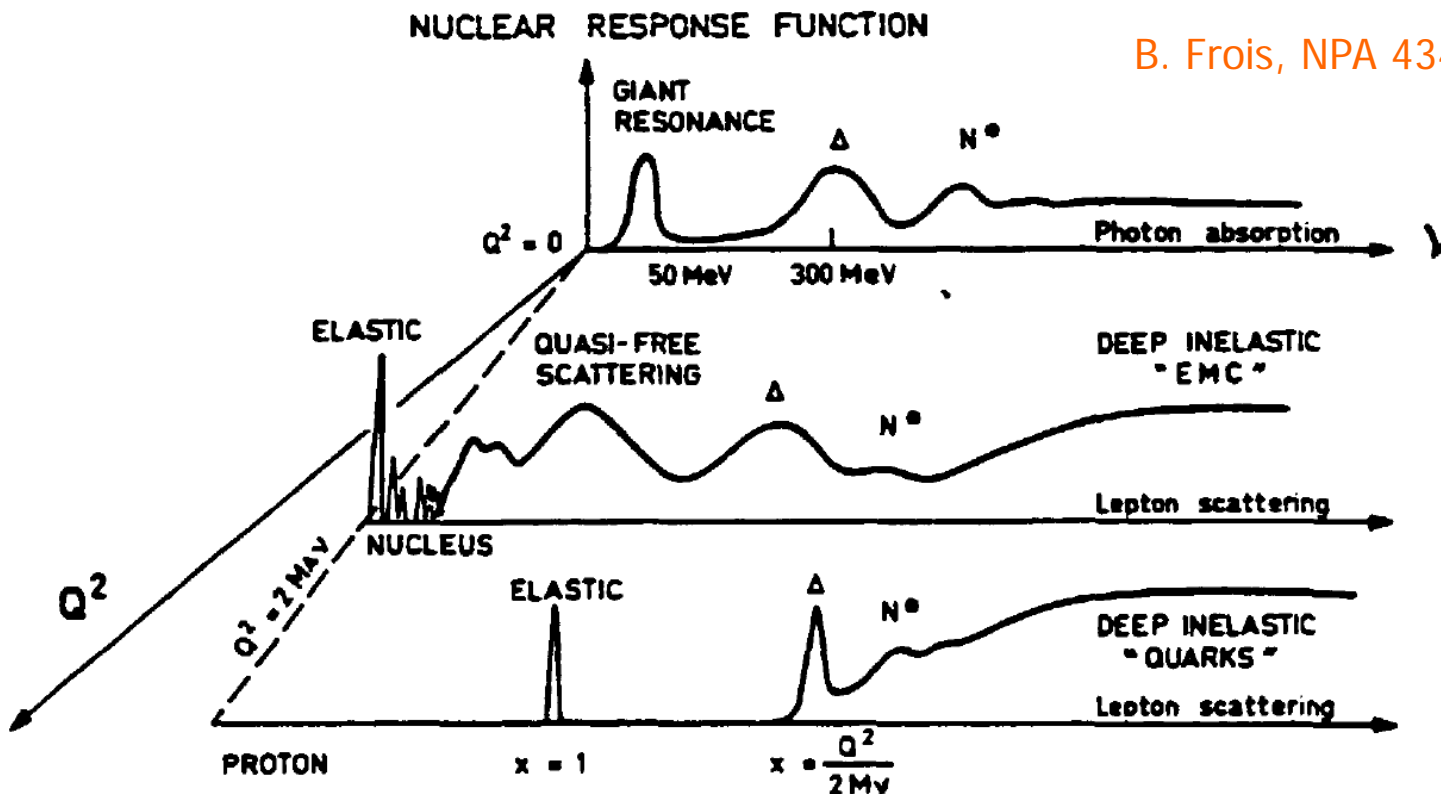


$\cos\theta$

Martini, Jachowicz et al., PRC94 (2016)

# Neutrino interactions on nuclei

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# Neutrino interactions on nuclei

- **Impulse approximation**: interactions on **single nucleons** in the presence of **mean fields** and **short-range correlations**

- **Spectral functions**:

$$D(p) = (\not{p} + M)G(p)$$

$$G(p) = \frac{1}{p^0 + E_p - i\epsilon} \left[ \int_{-\infty}^{\mu} \frac{\mathcal{A}_h(\omega, \vec{p})}{p^0 - \omega - i\epsilon} d\omega + \int_{\mu}^{\infty} \frac{\mathcal{A}_p(\omega, \vec{p})}{p^0 - \omega + i\epsilon} d\omega \right]$$

$$\mathcal{A}_{p,h}(p) = \mp \frac{1}{\pi} \frac{\text{Im}\Sigma(p)}{[p^2 - M^2 - \text{Re}\Sigma(p)]^2 + [\text{Im}\Sigma(p)]^2}$$

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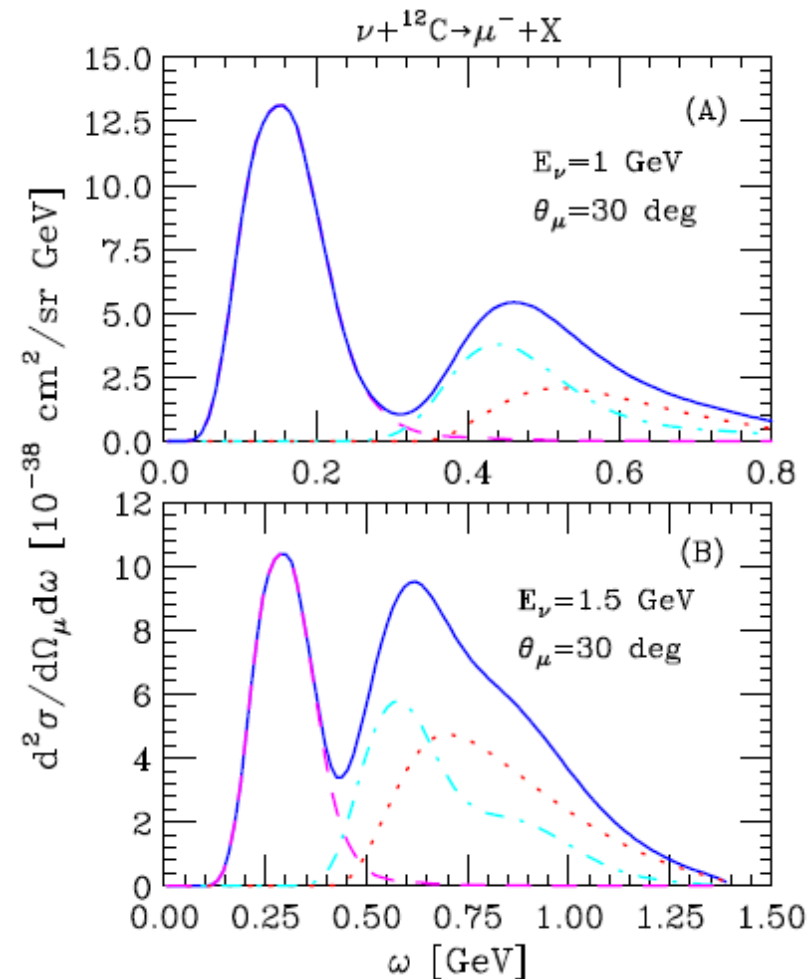
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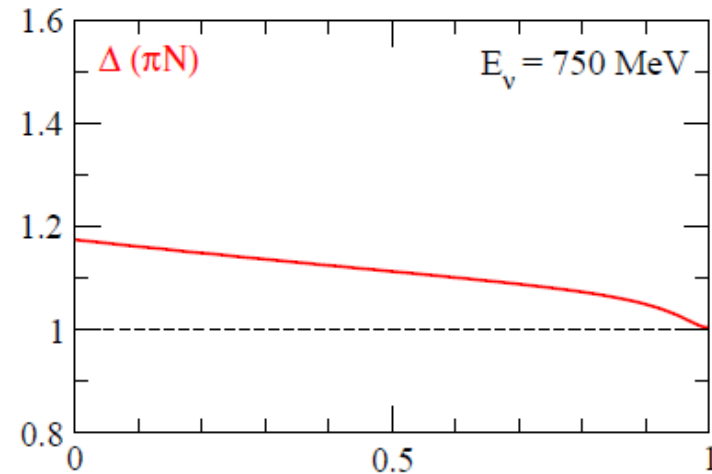
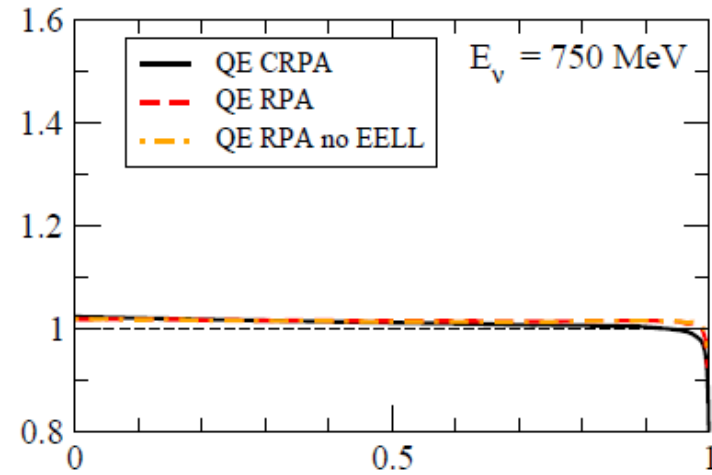
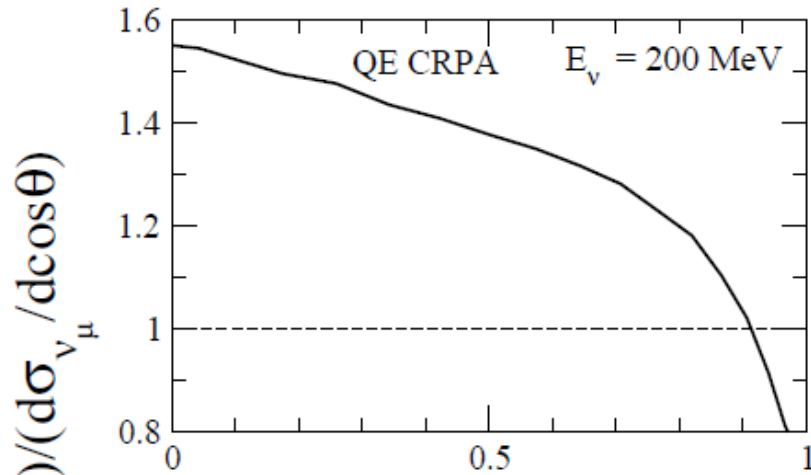
- **Inclusive** cross section in the **QE** and **inelastic** regions:



Vagnoni, Benhar, Meloni, PRL 118 (2017)



$$\sigma(\nu_e)/\sigma(\nu_\mu)$$

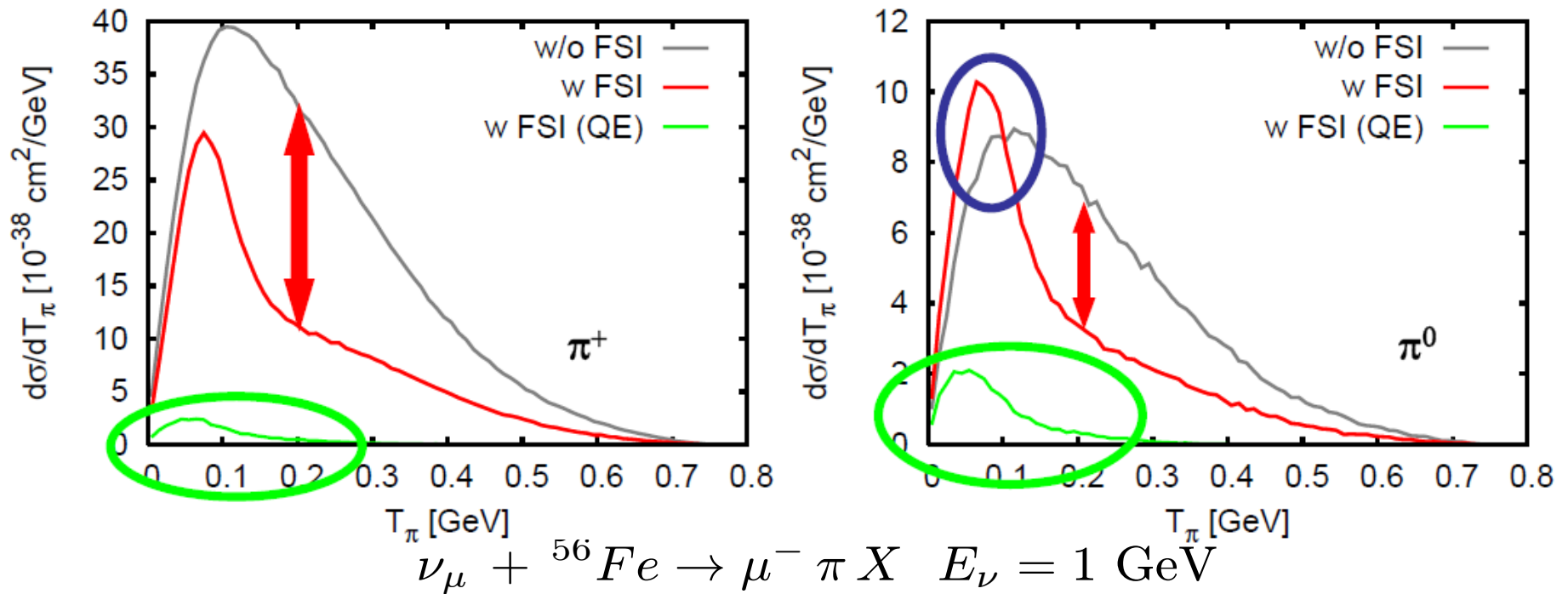


$\cos\theta$

Martini, Jachowicz et al., PRC94 (2016)

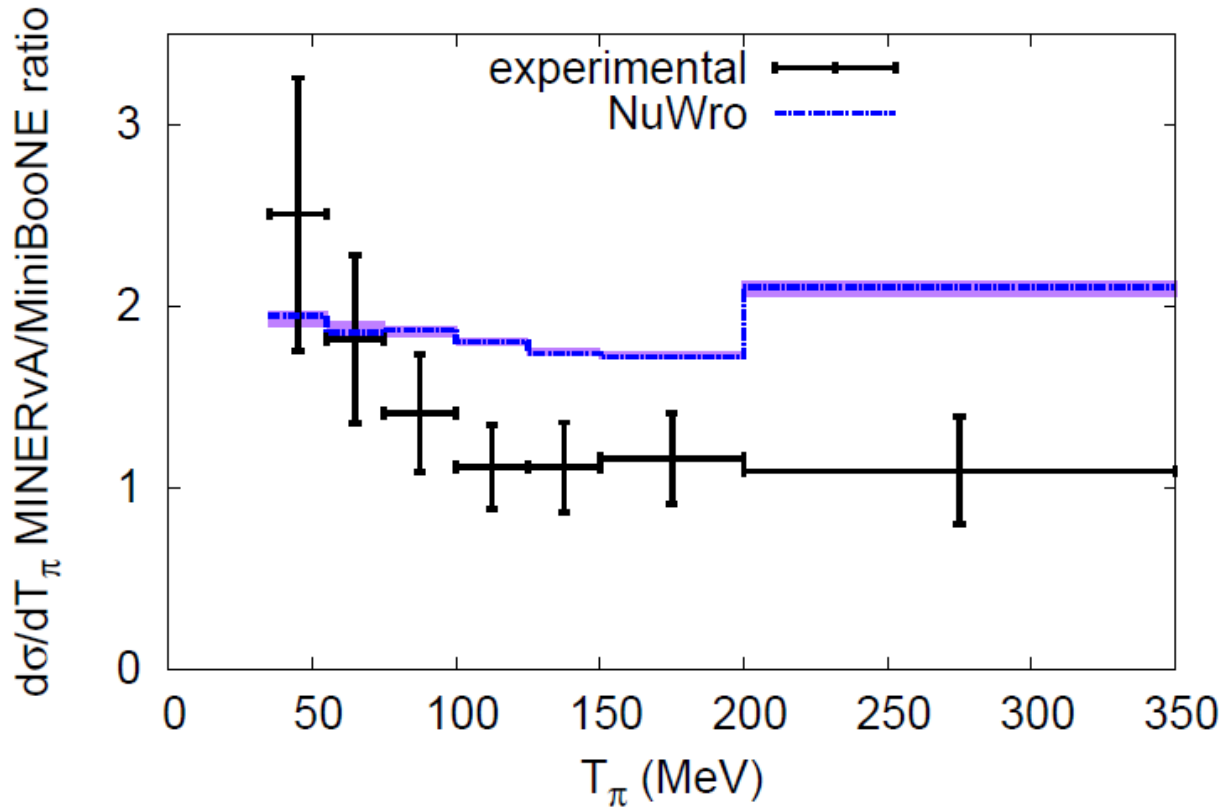
# $1\pi$ production on nuclei

- GiBUU Leitner, LAR, Mosel, PRC 73 (2006)
  - Effects of FSI on pion kinetic energy spectra
    - strong absorption in  $\Delta$  region
    - side-feeding from dominant  $\pi^+$  into  $\pi^0$  channel
    - secondary pions through FSI of initial QE protons



# $1\pi$ production on nuclei

- Experimentally studied by MiniBooNE, T2K (ND280) and MINERvA

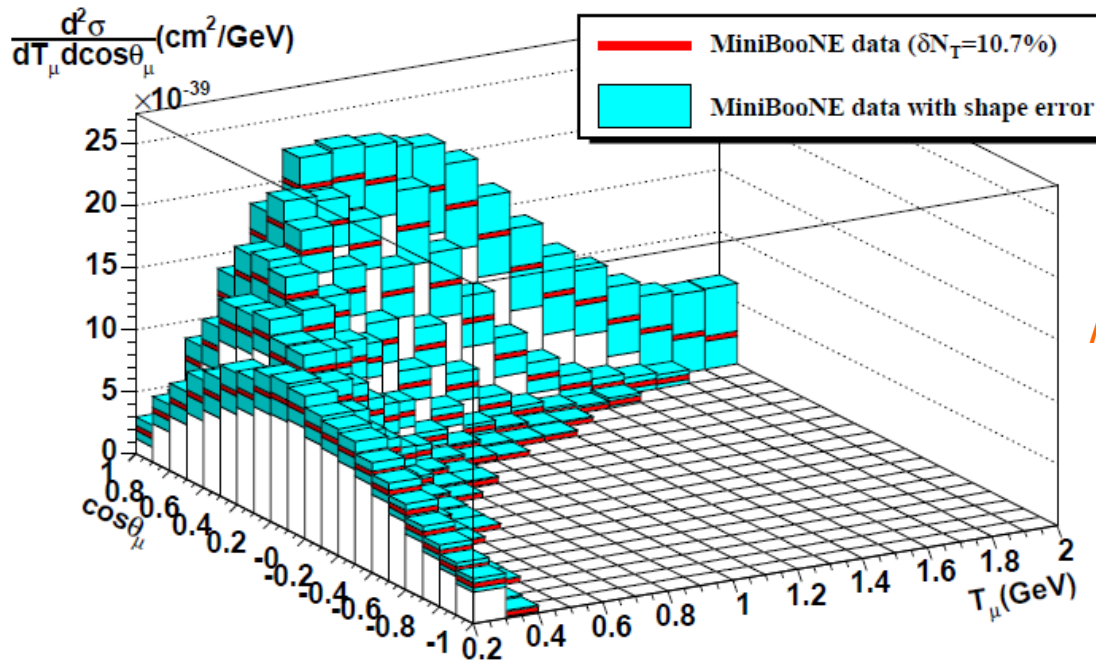


Sobczyk, Zmuda, PRC 91 (2015)

- In spite of flux difference, MiniBooNE and MINERvA data probe the **same dynamics** and should be strongly **correlated**

# Two-nucleon currents

- MiniBooNE data for “CCQE” 2D cross section:



Aguilar-Arevalo et al., PRD81 (2010)

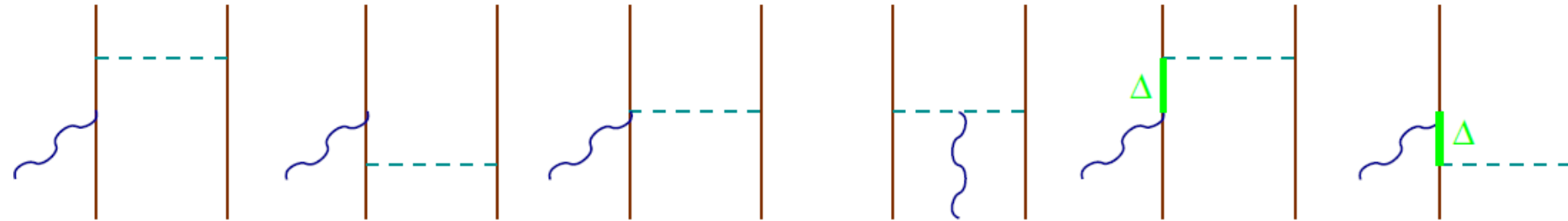
can be explained with a Relativistic Fermi Gas model and  $M_A \approx 1.35$  GeV

- in disagreement with  $M_A \approx 1$  GeV from bubble chamber data
- but consistent with  $F_A$  from the z-expansion

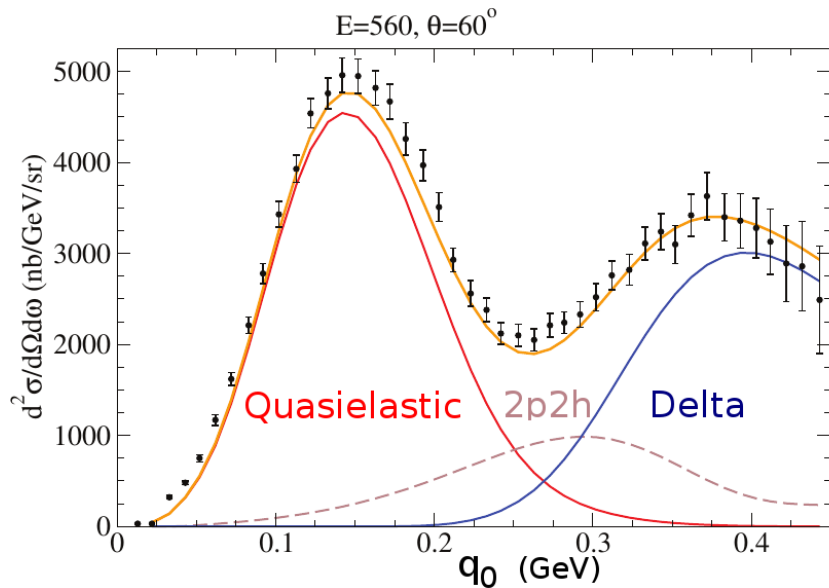
$$F_A(Q^2) = g_A \left( 1 + \frac{Q^2}{M_A^2} \right)^{-2}$$

# Two-nucleon currents

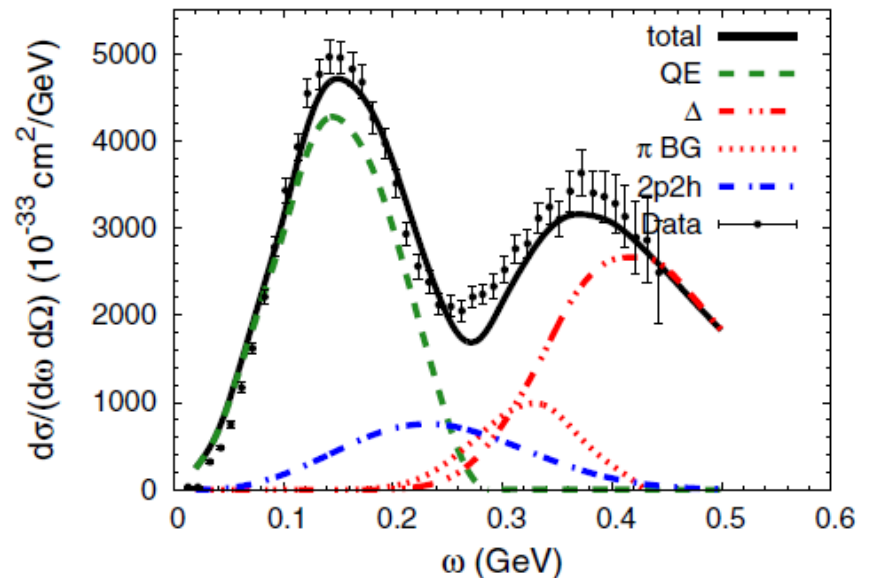
- 2-nucleon EW currents exist (are allowed by symmetries)



- Sizable contribution can be inferred from  $A(e, e')X$



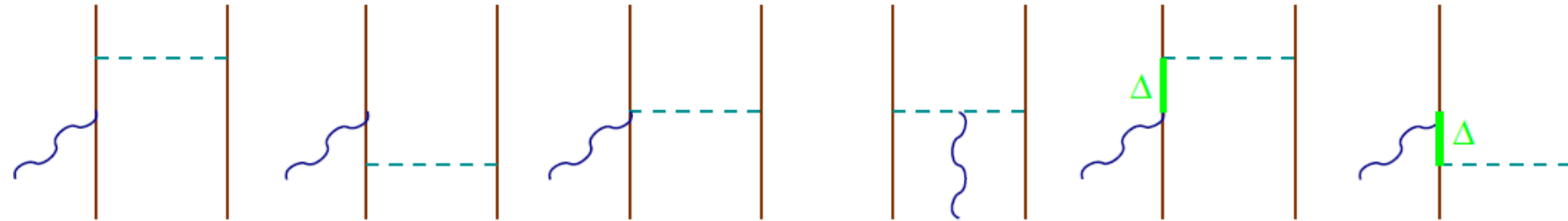
Megias et al., PRD 94 (2016)



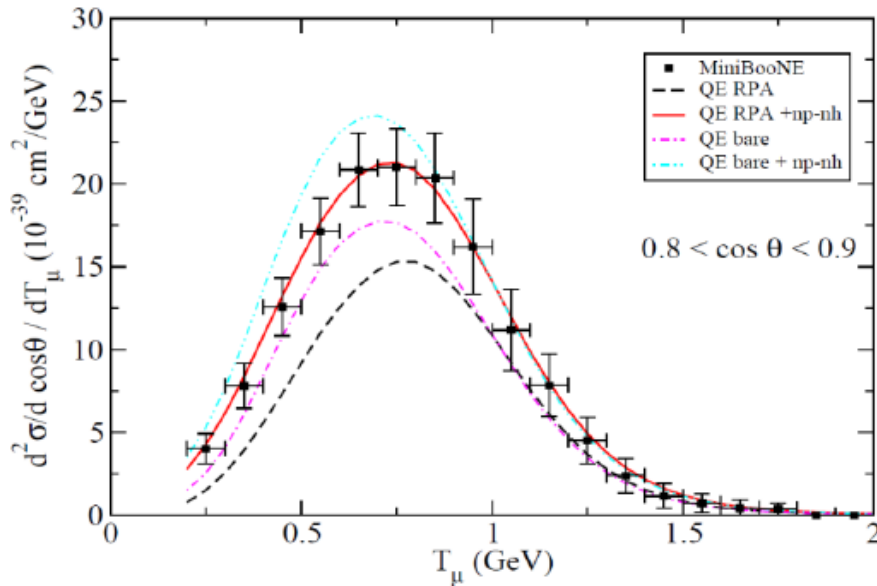
Gallsmeiter et al., PRD 94 (2016)

# Two-nucleon currents

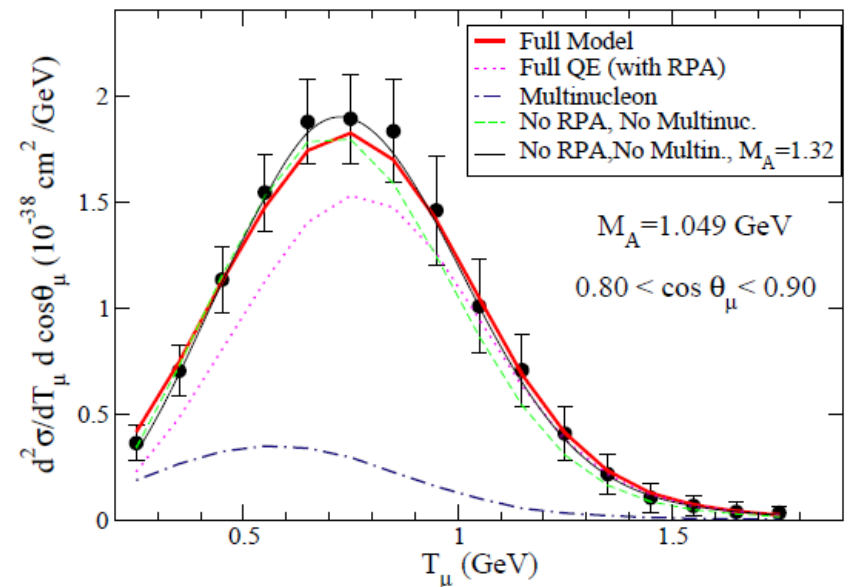
- 2-nucleon EW currents exist (are allowed by symmetries)



- together with better QE nuclear models can explain MiniBooNE data with  $M_A \approx 1$  GeV



Martini et al.

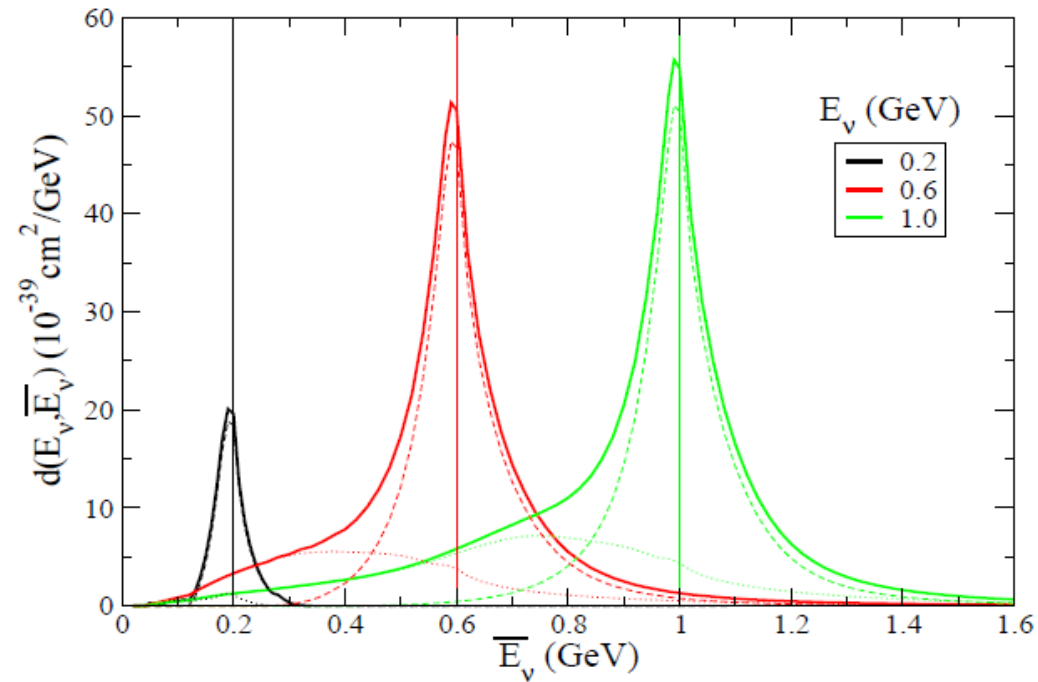


Nieves et al.

# Two-nucleon currents

- Large implications for oscillation measurements
  - bias in (kinematic)  $E_\nu$  reconstruction

$$E_\nu^{\text{QE}} = \frac{2m_n E_\mu - m_\mu^2 - m_n^2 + m_p^2}{2(m_n - E_\mu + p_\mu \cos \theta_\mu)}$$

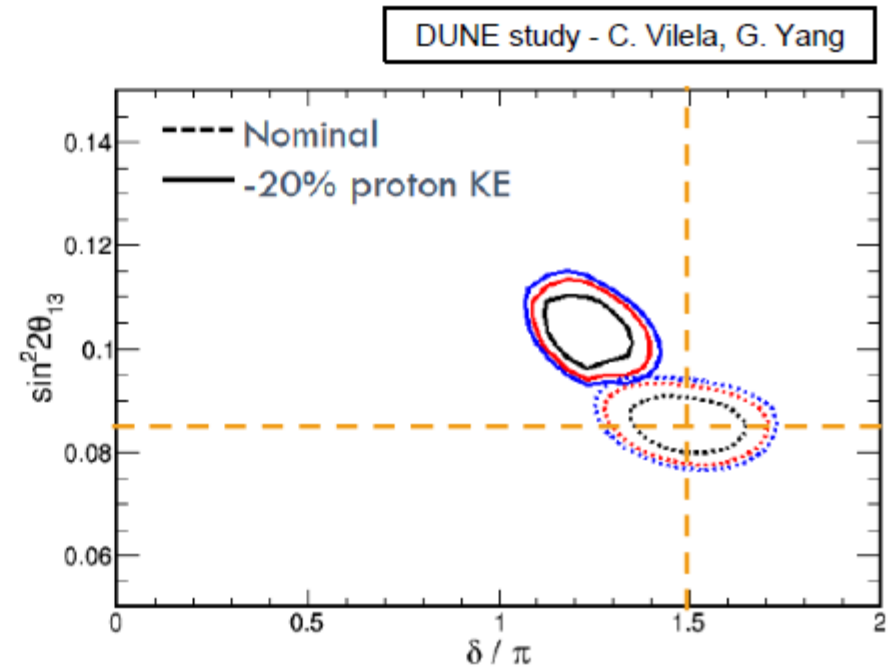
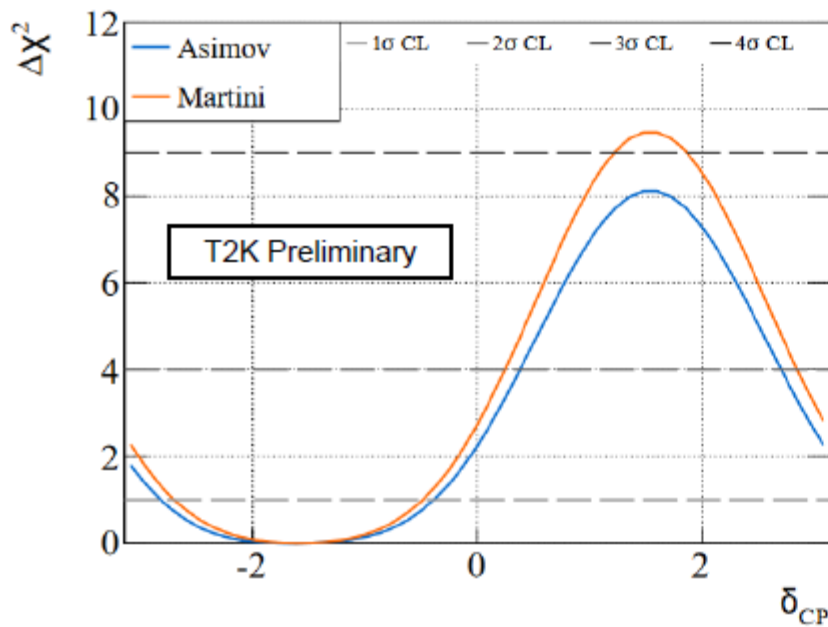


Martini et al., PRD 87 (2013)

# Two-nucleon currents

- Large implications for oscillation measurements

## Mock data studies



M. Scott



# Photon emission in NC interactions

■ on nucleons  $\nu(\bar{\nu}) N \rightarrow \nu(\bar{\nu}) \gamma N$

■ on nuclei  $\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma X \leftarrow$  incoherent

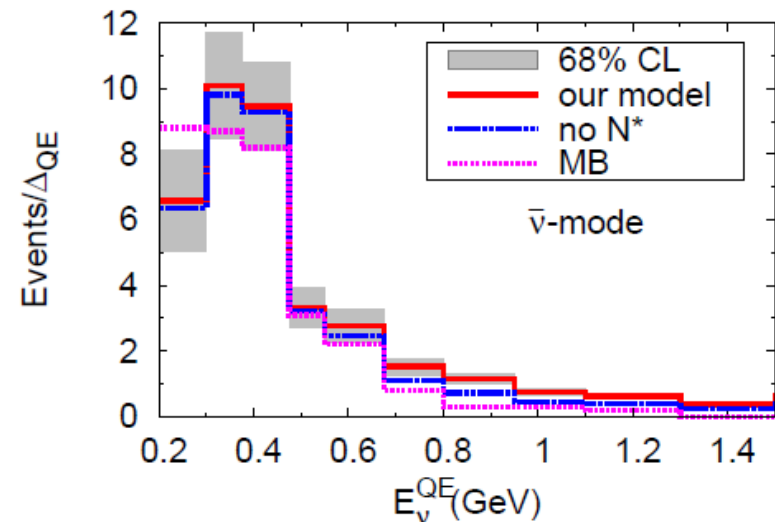
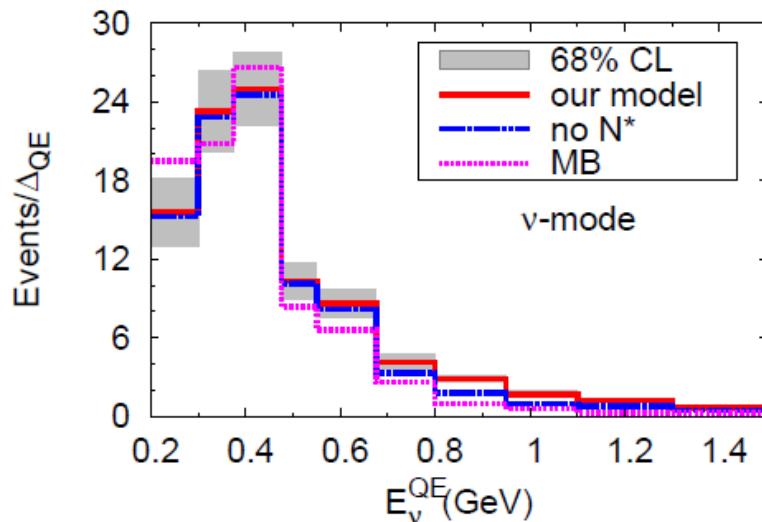
$\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma A \leftarrow$  coherent

R. Hill, PRD 81 (2010)

Zhang & Serot, PRC 86 (2012)

Wang, LAR, Nieves, PRC 89 (2014)

■ Comparison to the MiniBooNE estimate E. Wang, LAR, J. Nieves, PLB 740 (2015)



■  $NC_\gamma$ : insufficient to explain the excess of e-like events at MiniBooNE

■ Same conclusion as Zhang, Serot, PLB 719 (2013)

# Photon emission in NC interactions

- on nucleons  $\nu(\bar{\nu}) N \rightarrow \nu(\bar{\nu}) \gamma N$

R. Hill, PRD 81 (2010)

Zhang & Serot, PRC 86 (2012)

Wang, LAR, Nieves, PRC 89 (2014)

- on nuclei  $\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma X \leftarrow$  incoherent

$$\nu(\bar{\nu}) A \rightarrow \nu(\bar{\nu}) \gamma A \leftarrow \text{coherent}$$

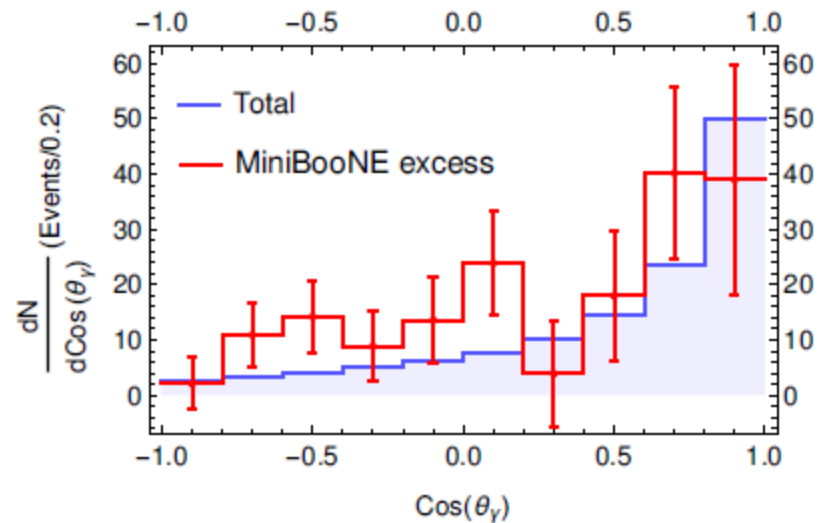
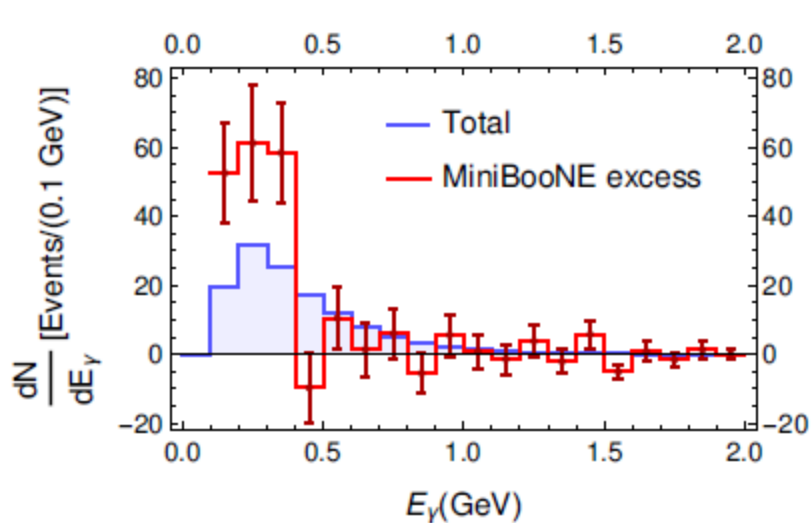
- **Heavy** ( $\sim 50$  MeV)  $\nu$  produced weakly or EM, followed by  $\nu_h \rightarrow \nu \gamma$

S. Gninenko, PRL 103 (2009), M. Masip et al, JHEP 1301 (2013)

- Difficult to describe **both**  $E_\gamma$  and  $\cos\theta_\gamma$  distributions

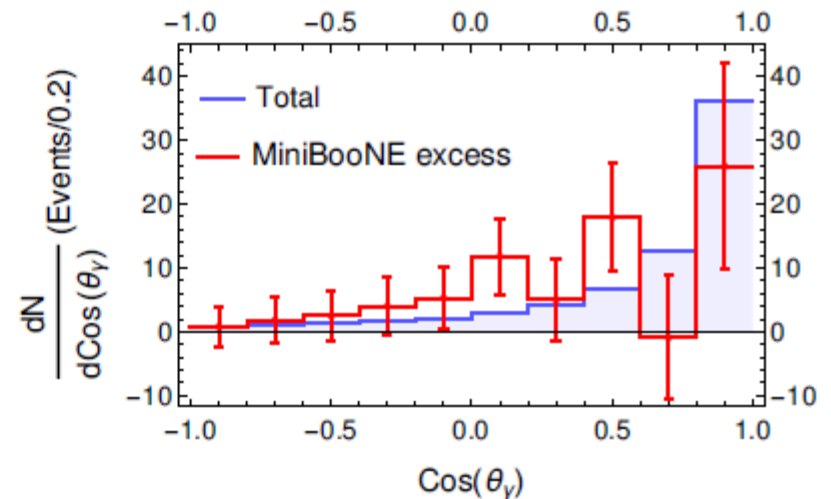
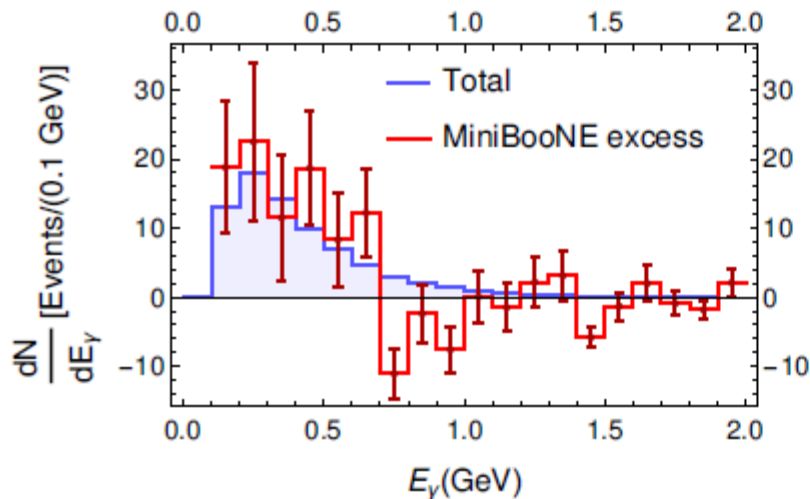
# Events @ MiniBooNE

## ■ $\nu$ mode



## ■ $\bar{\nu}$ mode

LAR, E. Saúl Sala, in preparation, POS EPS-HEP (2017)

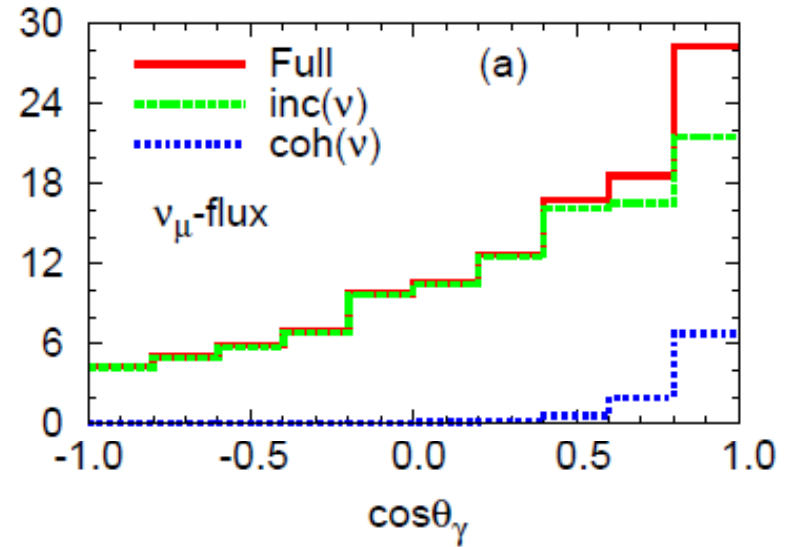
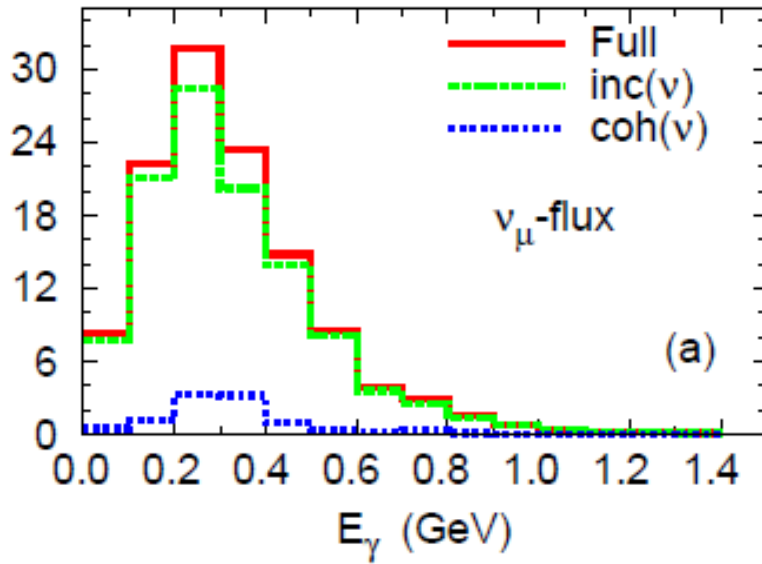


# Photon emission in NC interactions

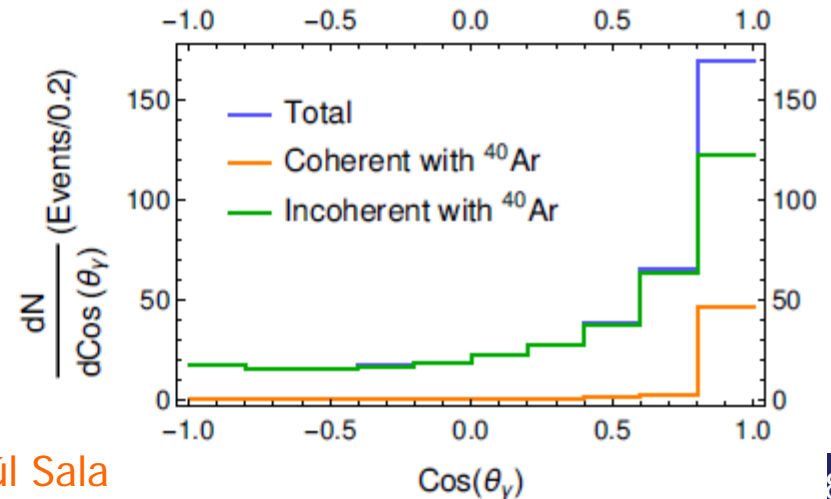
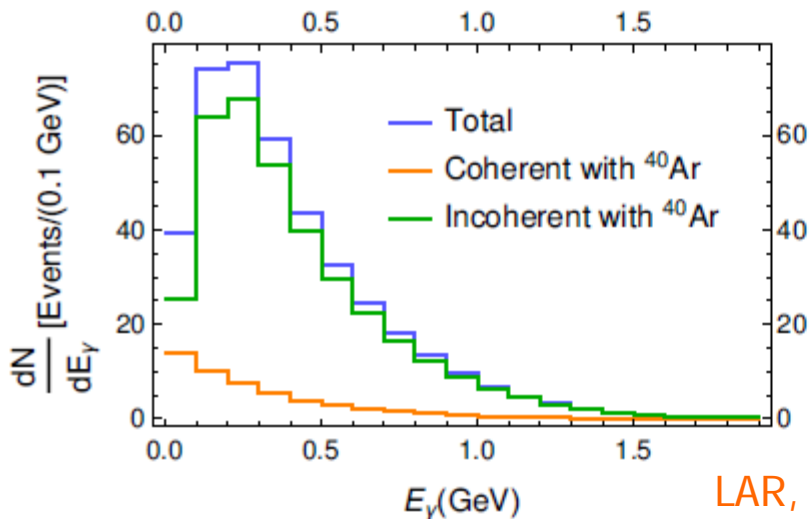
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  - Difficult to describe **both**  $E_\gamma$  and  $\cos\theta_\gamma$  distributions
- Ongoing NC $\gamma$  analysis: [MICROBOONE-NOTE-1041-PUB.pdf](#)

# MicroBooNE

## SM prediction LAR, Wang

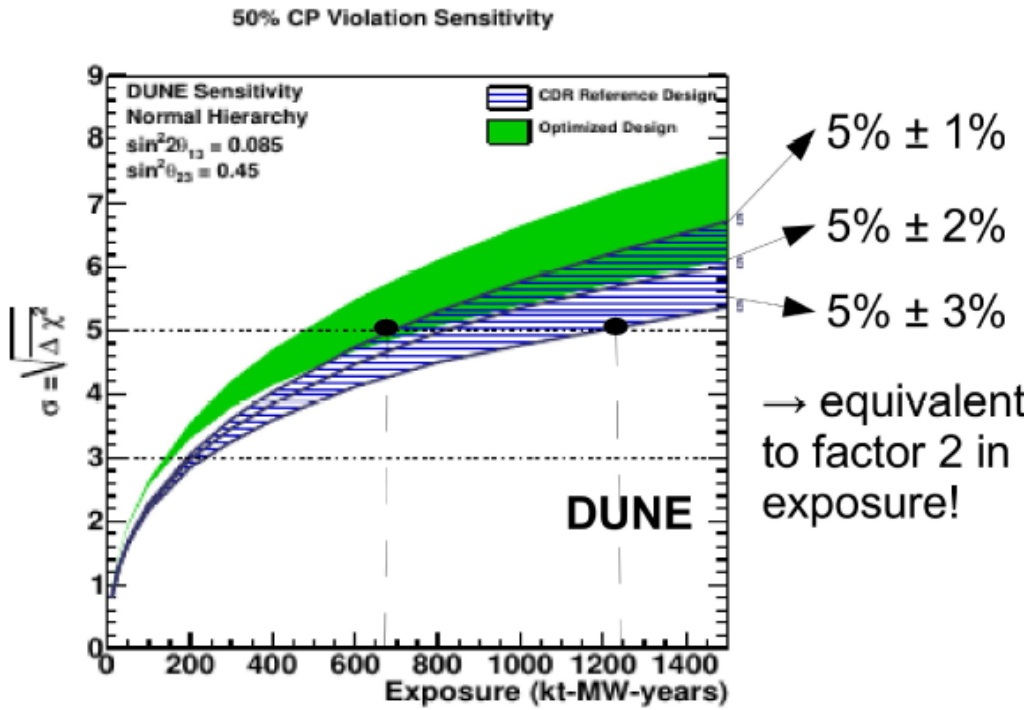


## $\nu_h \rightarrow \nu \gamma$



LAR, E. Saúl Sala

# Conclusion



- Systematic errors are expensive

*It is faster and cheaper to pay a theoretician to reduce 2 % your systematics than building new huge detectors!*

G. D. Megias @ NuInt 2018