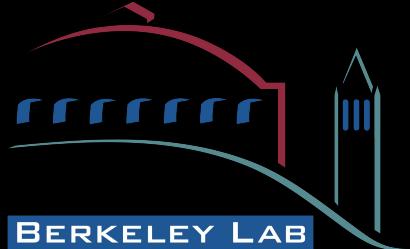


# Using a quantum annealer for particle tracking at the LHC

*on behalf of the HEP.QPR project at LBL*

Lucy Linder  
April 3, 2019

<http://bit.ly/hepqpr-cdots>



Office of Science

**iCoSys**

Institute of Complex Systems  
(HEIA-FR)



Q

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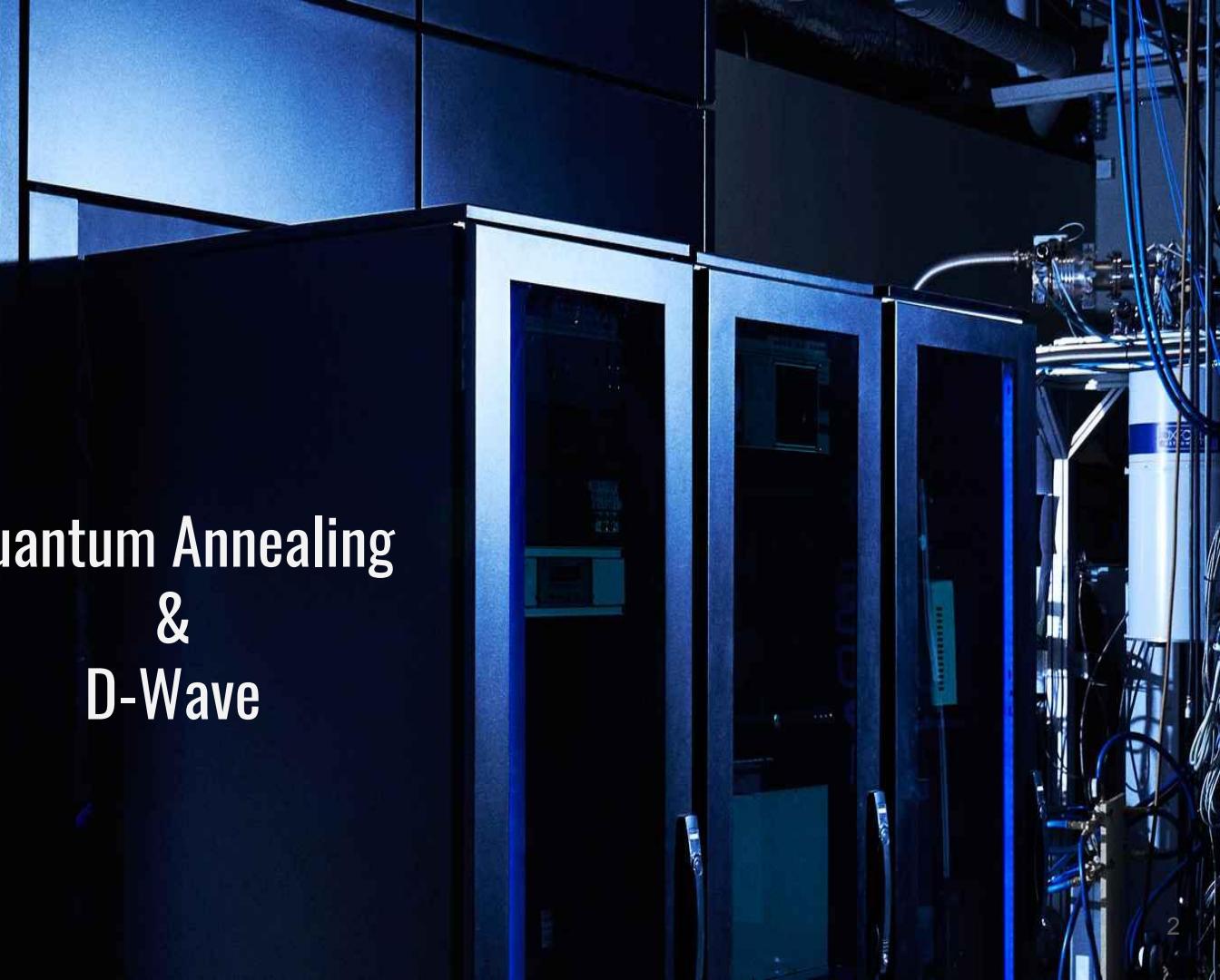
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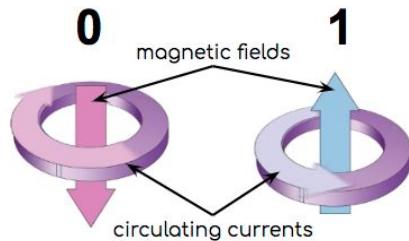
m

# Quantum Annealing & D-Wave

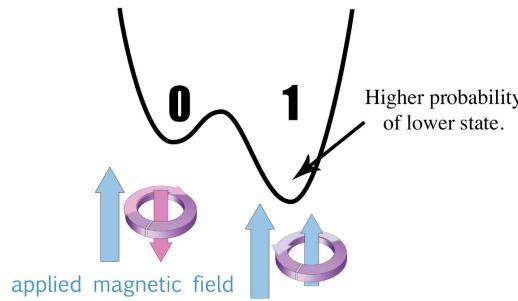


# QA in D-Wave computers

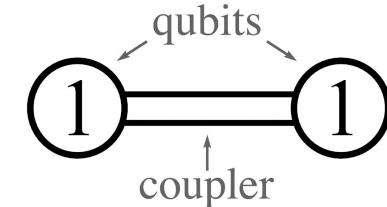
source: [dwavesys on YouTube](#)



$qubits \Rightarrow q_i$



$bias weights \Rightarrow a_i$



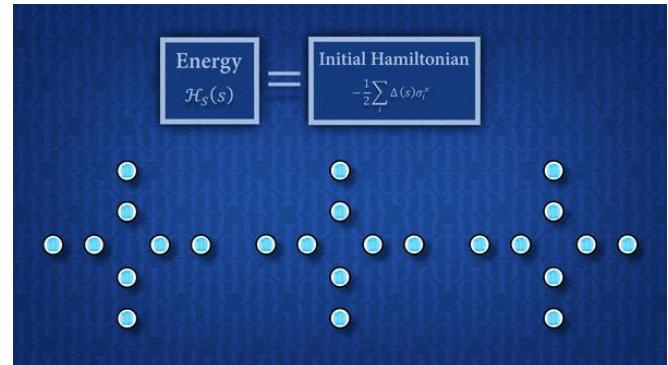
$coupling strength \Rightarrow b_{ij}$

quantum machine instruction (QMI)  
objective function:

$$O(a; b; q) = \sum_{i=1}^N a_i q_i + \sum_i \sum_j b_{ij} q_i q_j \quad q_i \in \{0, 1\}$$

QUBO

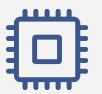
Quadratic Unconstrained  
Binary Optimisation



anneal time  $\sim 20\mu s$

# D-Wave hardware & usage

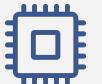
D-Wave 2X (2015)



1152 qubits

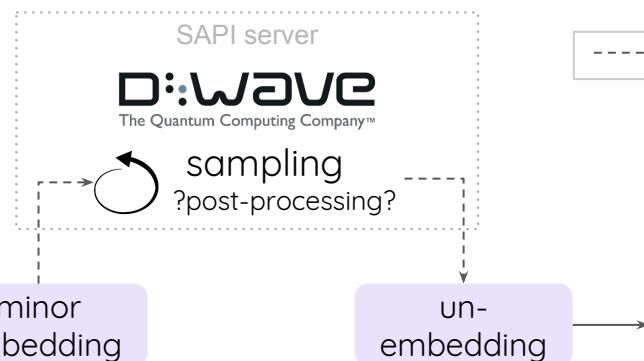
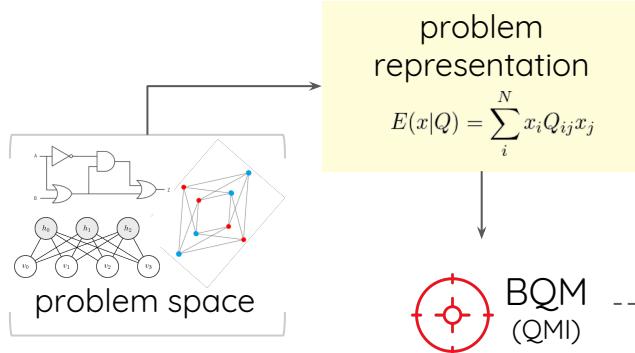
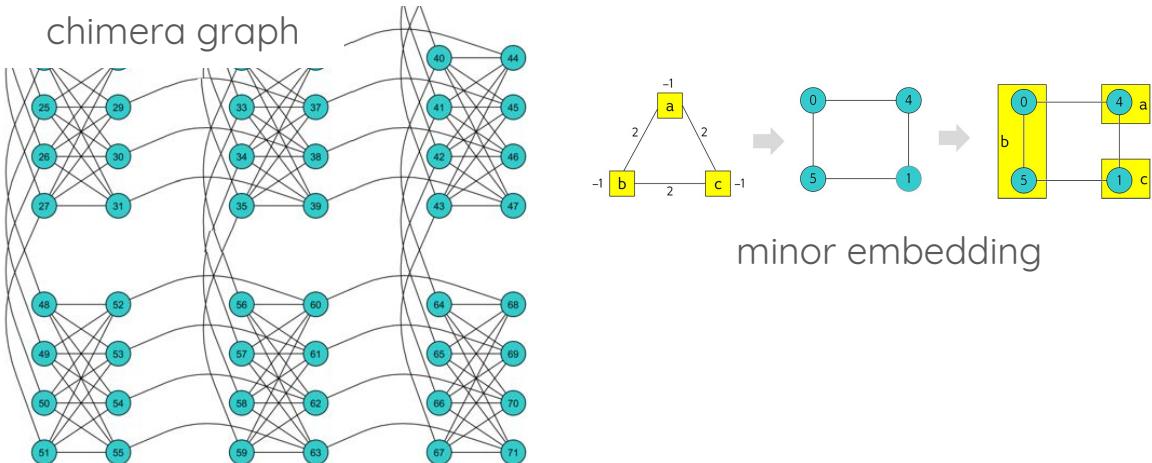
3360 couplers

D-Wave 2000Q (2017)



2048 qubits

6016 couplers



-----> API exists

The background features a complex network of black lines forming a geometric pattern of triangles and hexagons against a light blue gradient. A large, solid white circle is centered in the middle of the slide. Inside this circle, the text is displayed.

# QUBO for track reconstruction

# Stimpfle-Abele & Garrido (1990) *ref*

“We can regard a *track* with  $n$  hits as a set of  $n-1$  consecutive lines [doublets] with a smooth shape and without bifurcation”.

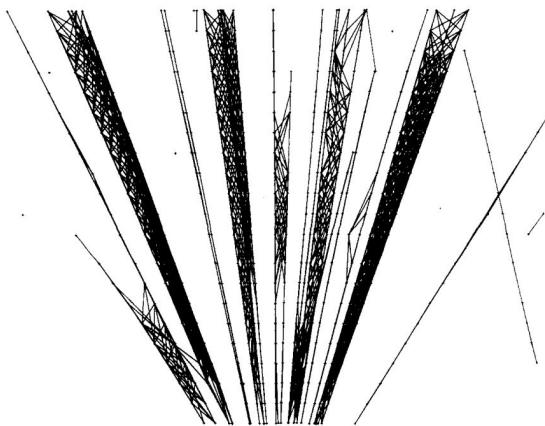


Fig. 2. Display of all generated lines for a real  $Z^0 \rightarrow$  hadrons ( $RZ$  projection).

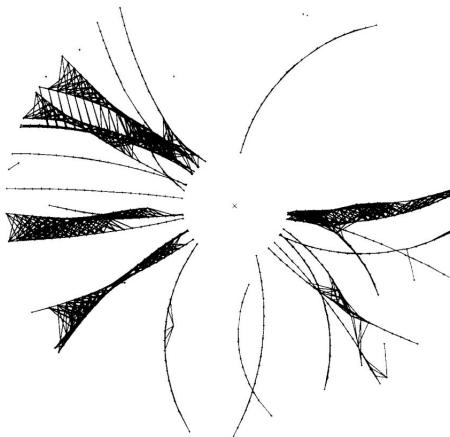


Fig. 1. Display of all generated lines for a real  $Z^0 \rightarrow$  hadrons ( $XY$  projection).

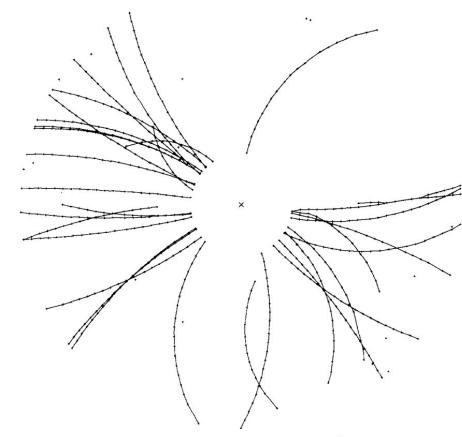


Fig. 3. Display of the activated lines after convergence for a real  $Z^0 \rightarrow$  hadrons ( $XY$  projection).

source: [fast track finding with neural nets](#)

1. generate the set of potential doublets (apply early cuts)
2. *binary classification task* to determine which doublets should be kept in the track candidates, using Hopfield Networks

# Stimpfl-Abele & Garrido (1990) *ref*

“We can regard a *track* with  $n$  hits as a set of  $n-1$  consecutive lines [doublets] with a smooth shape and without bifurcation”.

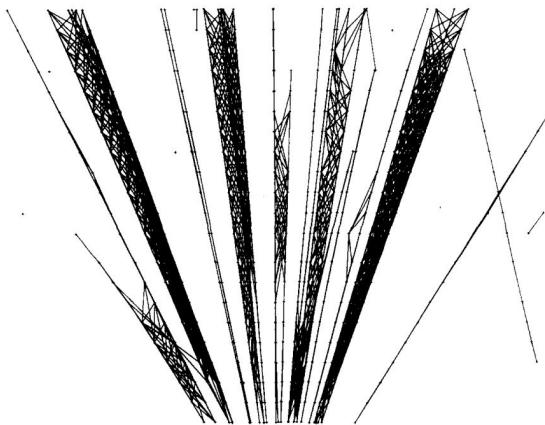


Fig. 2. Display of all generated lines for a real  $Z^0 \rightarrow$  hadrons ( $RZ$  projection).

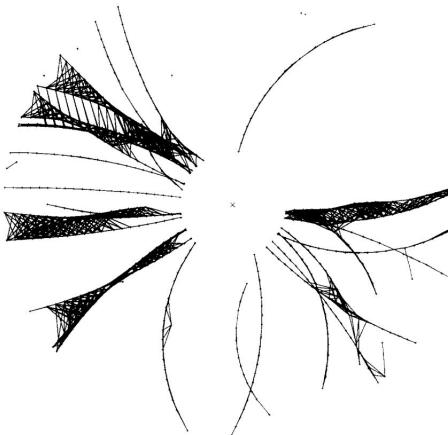


Fig. 1. Display of all generated lines for a real  $Z^0 \rightarrow$  hadrons ( $XY$  projection).

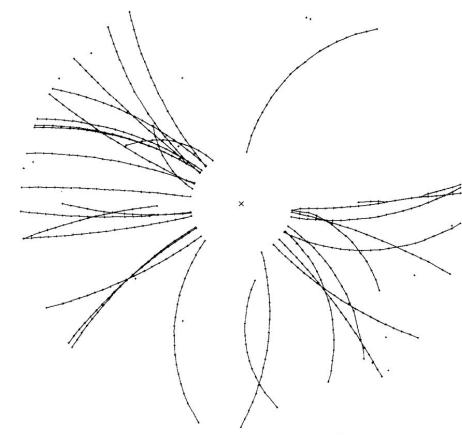


Fig. 3. Display of the activated lines after convergence for a real  $Z^0 \rightarrow$  hadrons ( $XY$  projection).

source: [fast track finding with neural nets](#)

1. (generate the set of potential doublets (apply early cuts))  
→ use a Python adaptation of the [ATLAS online seeding GPU code](#)
2. *binary classification task* to determine which doublets should be kept in the track candidates, using ~~Hopfield Networks~~ Quantum Annealing

# doublets triplets !

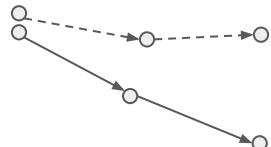
Internally, focus on triplets of hits:  $T_{a,b,c}$

Triplets can form interesting pairs or be in conflict.

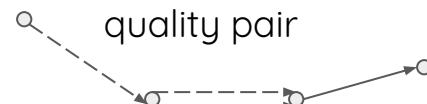
binary classification of **triplets**

- any  $P_t$
- any vertex location

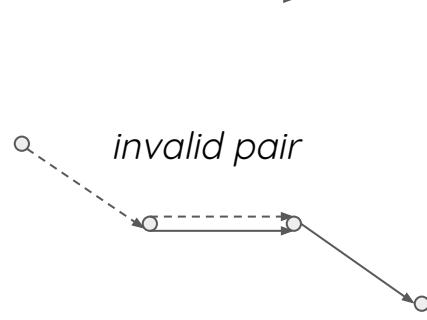
*unrelated triplets*



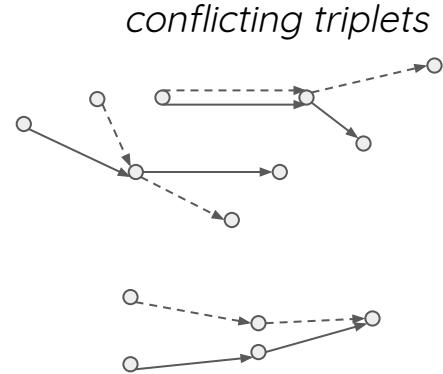
*quality pair*



*invalid pair*



*conflicting triplets*





# The energy function

Select the best triplets, in the form of pairs, that will constitute the track candidates:

$$E = -\frac{1}{2} \left[ \sum_{kln} T_{kln} V_{kl} V_{ln} \right. \\ \left. - \alpha \left( \sum_{klm(l \neq m)} V_{kl} V_{km} + \sum_{klm(k \neq m)} V_{kl} V_{ml} \right) \right. \\ \left. - \beta \left( \sum_{mn} V_{mn} - N_a \right) \right], \quad V \in \{0, 1\}$$

$$E = \alpha \left( \sum_i^N T_i \right) - \left( \sum_{i,j(\in pairs)} S_{ij} T_i T_j \right) + \zeta \left( \sum_{i,k(\in conflicts)} T_i T_k \right) \quad T \in \{0, 1\}$$

“**bias weight**” triplet prior  
can be set to 0

“**connection strength**”,  
interest of [keeping]  
a pair of triplets

avoid “**conflicts**”, a hit belongs  
to at most one track



# The energy function: QUBO

$$E = \alpha \left( \sum_i^N T_i \right) - \left( \sum_{i,j (\in qplets)} S_{ij} T_i T_j \right) + \zeta \left( \sum_{i,k (\in conflicts)} T_i T_k \right) \quad T \in \{0, 1\}$$



$$O(a; b; T) = \alpha \left( \sum_i^N T_i \right) + \sum_i \sum_{i < j} b_{ij} T_i T_j \quad T \in \{0, 1\}$$

$$b_{i,j} = \begin{cases} -S_{ij}, & \text{if } (Ti, Tj) \text{ form a pair that should form a track,} \\ \zeta & \text{if } (Ti, Tj) \text{ are in conflict,} \\ 0 & \text{otherwise.} \end{cases}$$



# Underlying math

a track of  $n$  hits is a set of  $n-2$  triplets that can be combined into  $n-3$  pairs

a set of track candidates is a set of triplets with no conflict

A triplet  $T_{a,b,c}$  has a higher quality when:

- it has little to no hole:  $\mathbf{H} = \mathbf{0}$
- the menger curvature  $\text{curv}(a,b,c)$  formed by the three hits in the X-Y plane is small;
- doublets ab and bc have similar  $\theta$  angles:  
 $\text{drz}(T_{a,b,c}) = |\varsigma(\theta_{ab}, \theta_{bc})|$  is small

A pair  $(T_i, T_j)$  has a higher quality when:

- it has few holes:  $\mathbf{H}_{ij} = \mathbf{0}$
- there are similar curvatures:  
 $\text{decurv}_{ij} = |\varsigma(\text{curv}(T_i), \text{curv}(T_j))|$  is small
- hits are aligned in R-Z:  
 $\text{drz}_{ij} = \max(\text{drz}(T_i), \text{drz}(T_j))$  is small

The interest of connecting two triplets into a pair can be expressed as:

$$S_{ij} = \frac{\alpha(\beta(1 - \text{decurv}_{ij})^\gamma + (1 - \beta)(1 - \text{drz}_{ij})^\delta)}{(1 + H_{ij})^\epsilon}$$

$\beta=0.5,$   
 $\epsilon=2,$   
others=1

$$S_{ij} = \frac{1 - \frac{1}{2}(\text{decurv}_{ij} + \text{drz}_{ij})}{(1 + H_{ij})^2}$$

# Experimental setup

## Dataset

TrackML dataset (== HL-LHC) with events split into lower multiplicity datasets:

- select P% of particles
- select P% of noise

Set weight=0 for hits belonging to particles with:

- $P_T < 1 \text{ GeV}$  or
- less than 5 hits

endcaps  
double hits

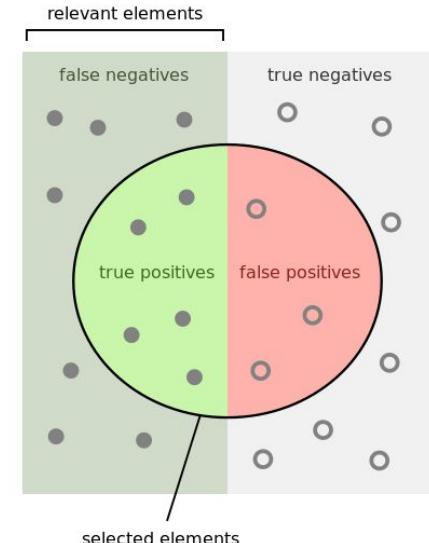
tune the model for that !

## Metrics

- TrackML score
- precision (~purity)
- recall (~efficiency)

## Machines

- CORI (1 Haswell node)
- D-Wave 2000Q ([leap](#))
- D-Wave 2X (LANL)



$$\text{Precision} = \frac{\text{How many selected items are relevant?}}{\text{How many relevant items are selected?}}$$
$$\text{Recall} = \frac{\text{How many relevant items are selected?}}{\text{How many relevant items are there?}}$$

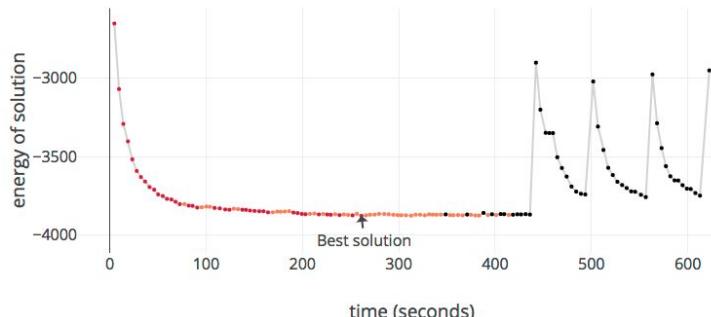
false negative = missings  
false positive = fakes

iterative hybrid classical/quantum algorithm

## QBSOLV

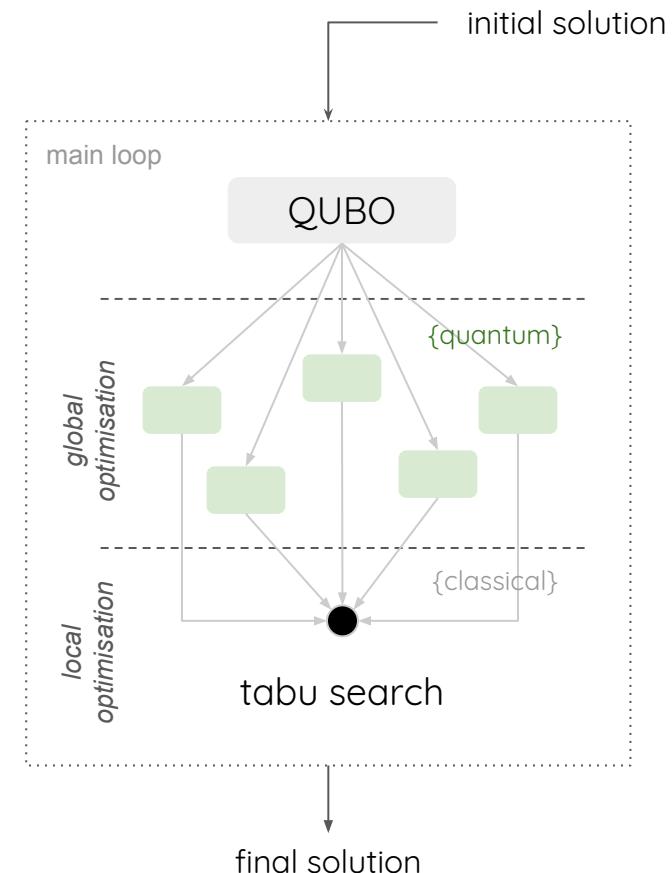
large and/or densely connected QUBOs split into sub-QUBOs fitting the D-Wave hardware.

*Tabu search* on the recomposed solutions.



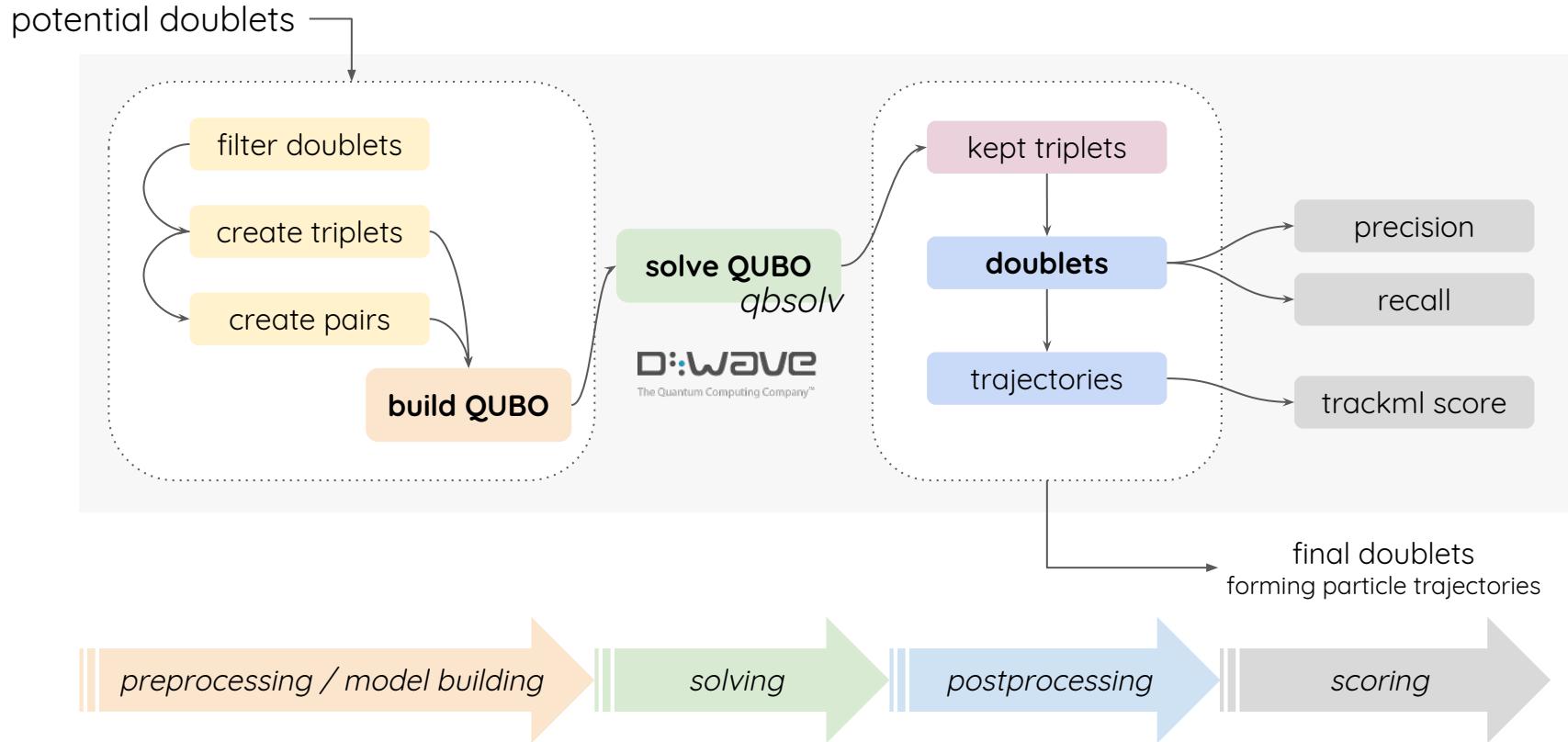
*evolution of the solution in each [absolv](#) loop.*

*The solution is sometimes randomised to escape local minima.*





# Algorithm overview





# Results

# Results

dataset size: ~20%  
1,637 particles, 11,030 hits

*plotting error: too many  
doublets 392529*

392,529 doublets  
 $p=0.26\%$ ,  $r=99.15\%$

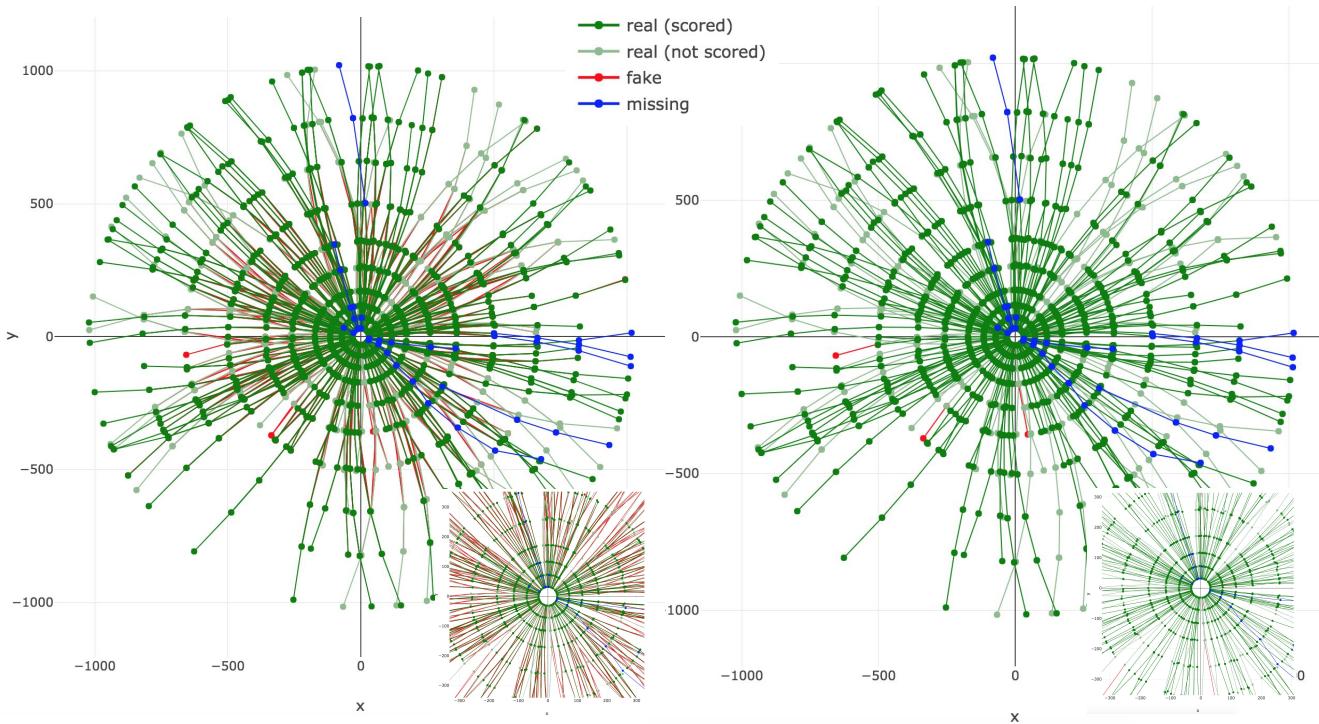
57.3s  
build QUBO

2,546 doublets  
(2,964 triplets)  
QUBO size: 14,345

17.1s  
sample QUBO  
running on CPU

1,512 doublets  
 $p=99.13\%$ ,  $r=97.06\%$

trackml score **97.55%**

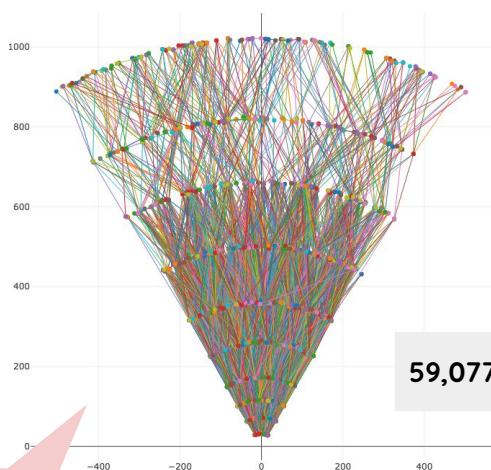




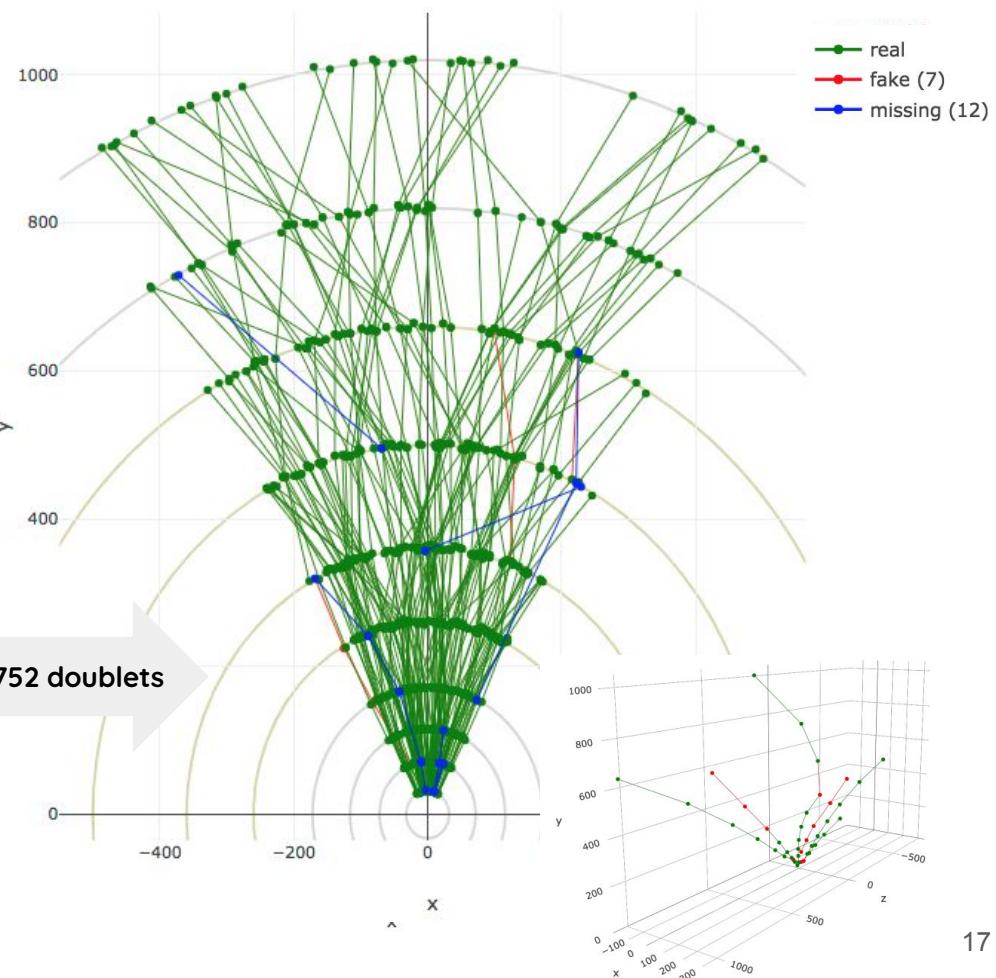
# Performances at low Pt

186 particles in a phi slice of  $\pi/3$

precision (%): 98.5, recall (%): 98.4,  
trackml score (%): **98.35**

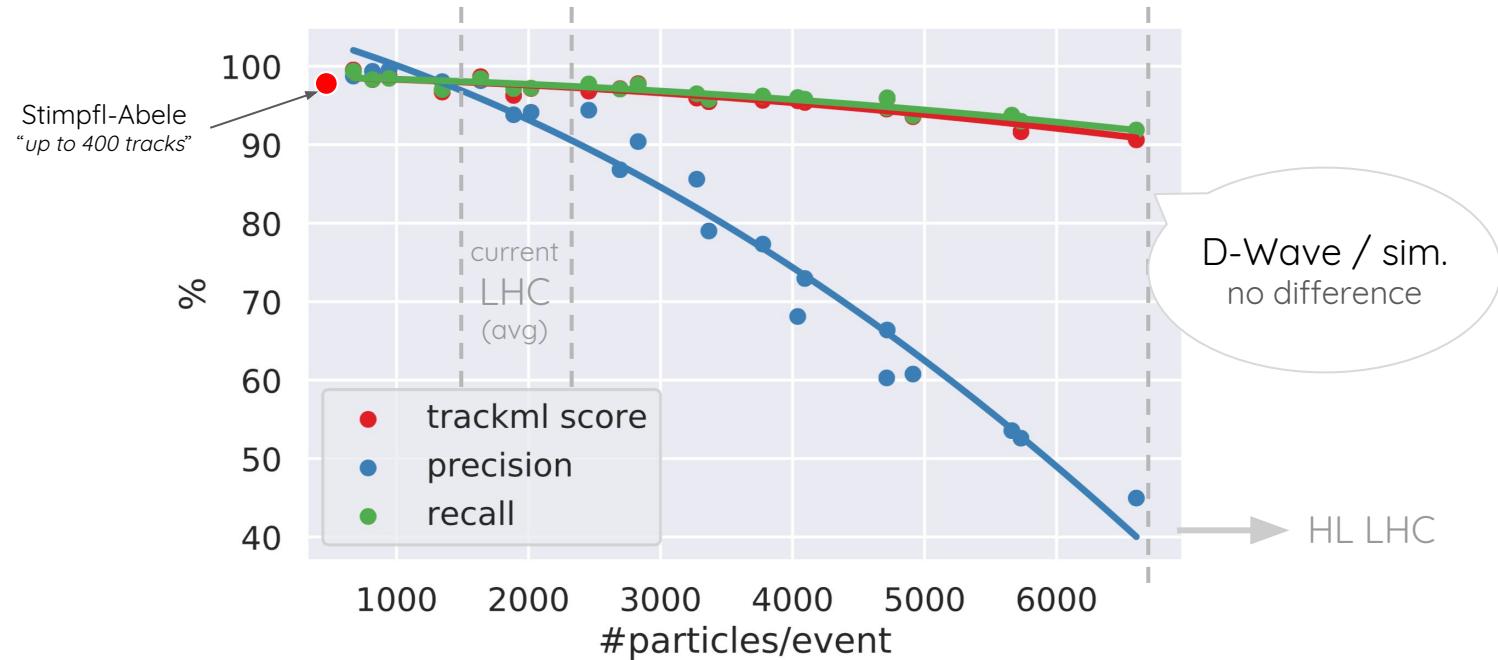


QUBO size  
68,043



# Physics performance

Full TrackML event 6,900 - 14,000 particles,  $Pt \geq 150$  MeV, ~15% noise/lower Pt hits  
recall: no endcaps & no double hits, focus on  $p_t \geq 1$  GeV BUT no hypothesis on vertex location



> 90% recall (efficiency) and trackml score on doublets classification

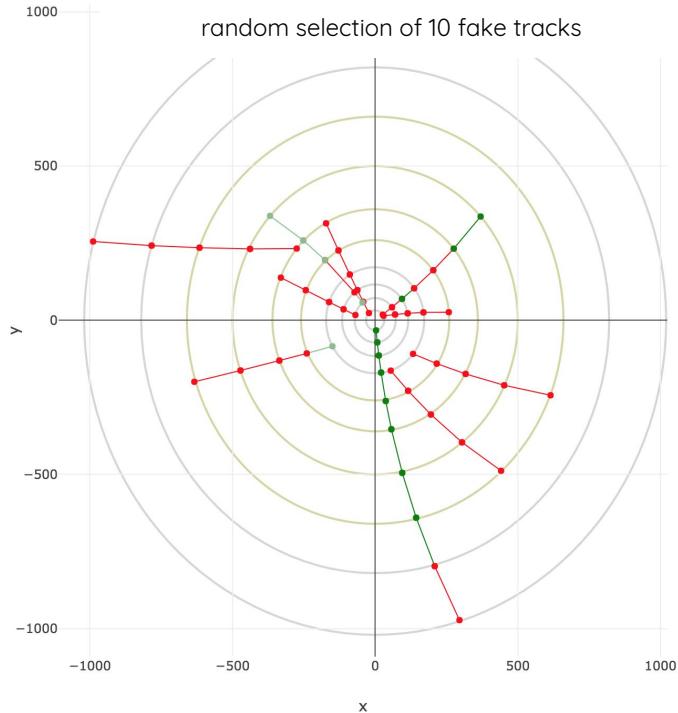
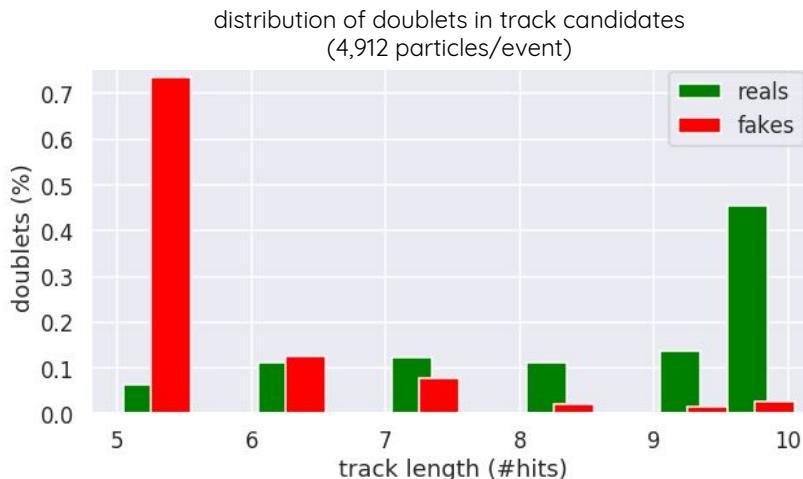


# What about the fakes ?

“The biggest difference [with conventional methods] is the number of wrongly associated coordinates [...]”

soft constraints and very simple geometrical constants is not as good as a sophisticated algorithm based on hard constraints (fits)”.

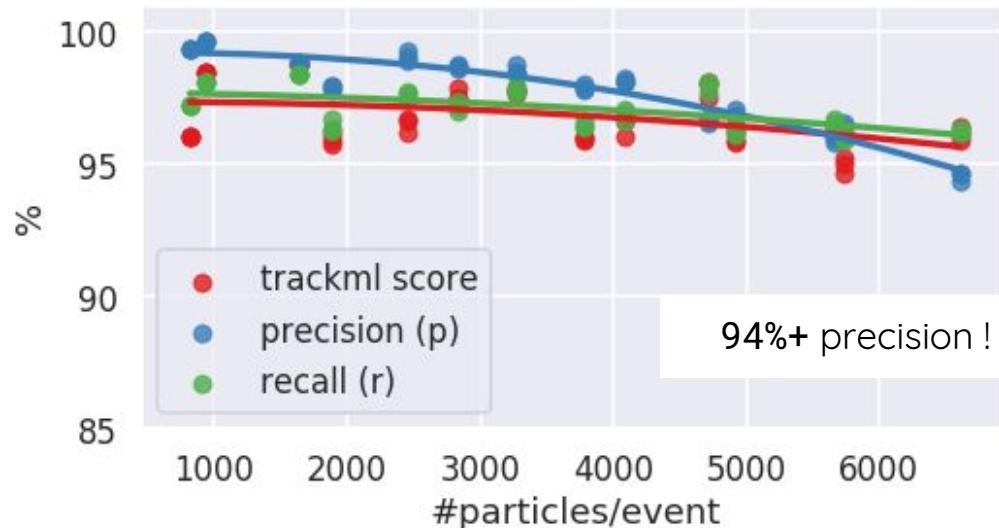
Stimpfl-Abele & Garrido, [fast track finding with neural networks](#)



→ post-processing *should* let us filter many fakes

# Improvement (TrackML-only)

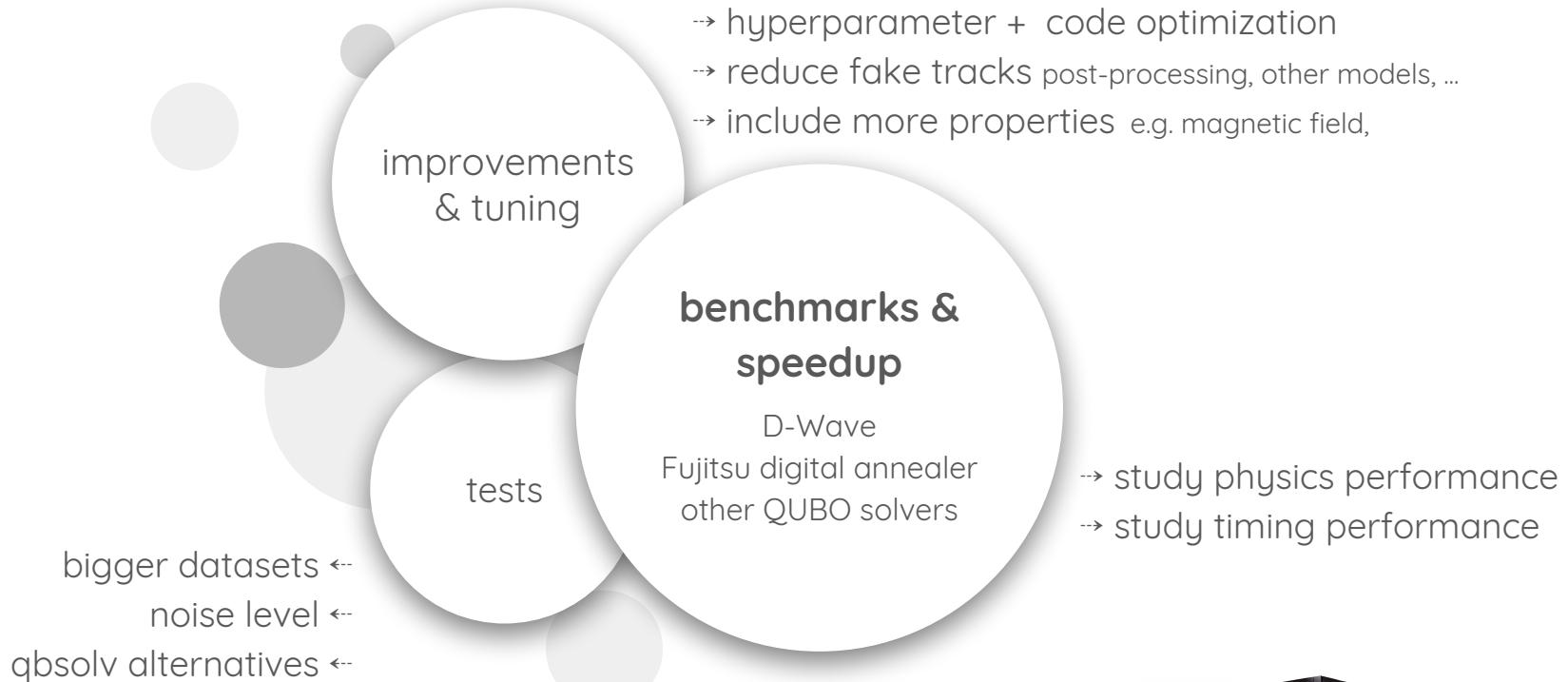
~~fixed~~ *variable* bias weights  
penalty based on the triplet's impact parameters ( $D_0, Z_0$ )



⚠ introduces biases and reintroduces a hypothesis on the vertex location



# Future work



HEP.QPR website

<https://hep-qpr.lbl.gov>

publication preprint

<https://arxiv.org/abs/1902.08324>

Github repository (and results)

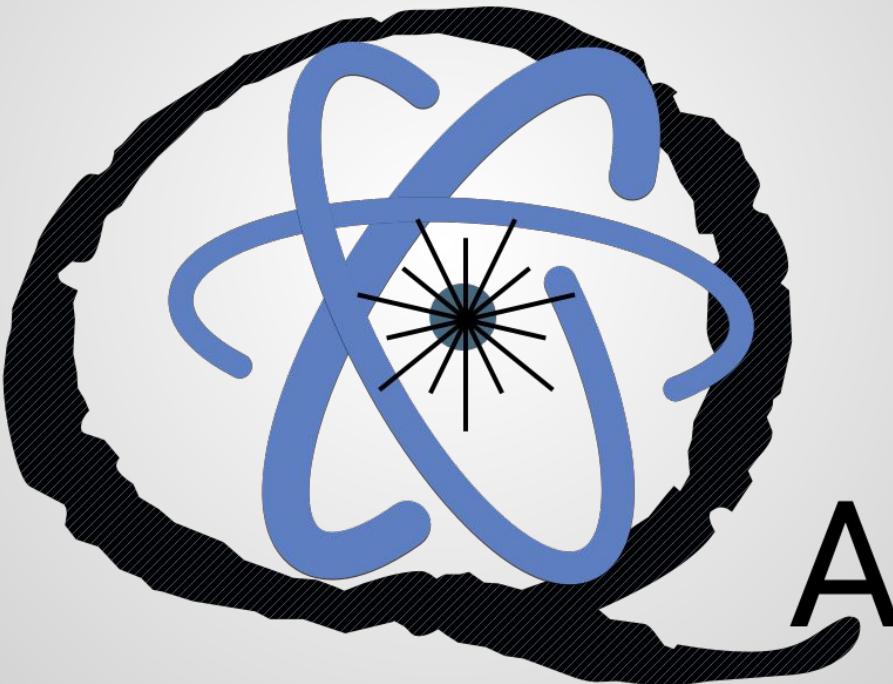
<https://github.com/derlin/hepqpr-qallse>

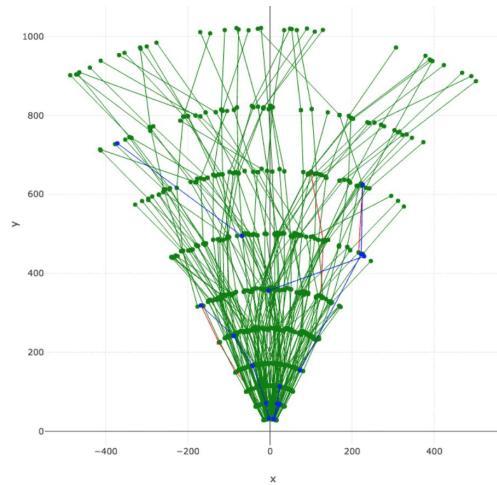
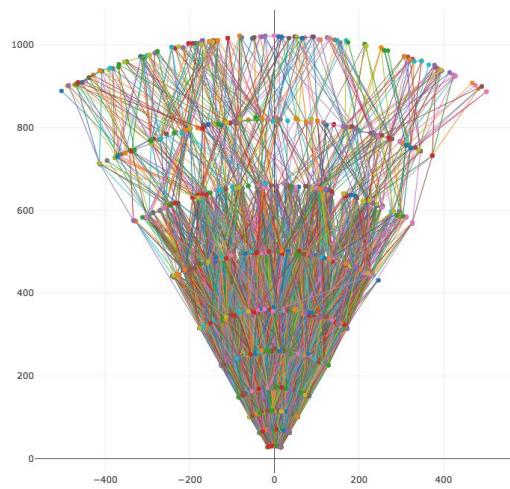
Master Thesis report

<https://github.com/derlin/hepqpr-qallse/tree/master/doc>

» arXiv:1902.08324 «

Thank you for your attention





I NOW HAVE  
ADDITIONAL QUESTIONS



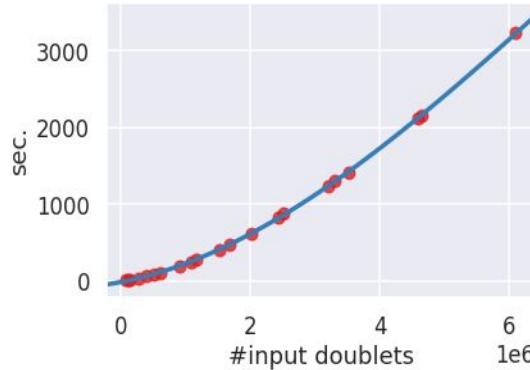


**BACKUP**



# Timing performance

Model building



currently no  
optimization or  
parallelization

---

QUBO solving

D-Wave internet latency, shared QPU, qbsolv ....  
too early to say !

neal (dwavesys)

6'600 particles/event = **12 s.**  
260,744 QUBO parameters

In the meantime, classical counterparts are surprisingly efficient.

# Basics of QA

*adiabatic theorem* of quantum mechanics,

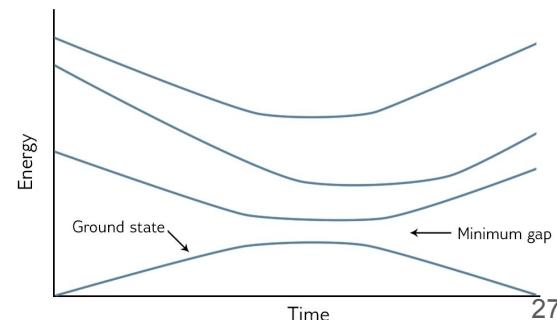
a physical system remains in the ground state if

$\left. \begin{array}{l} \text{perturbations are slow} \\ \text{there is a gap} \end{array} \right\}$

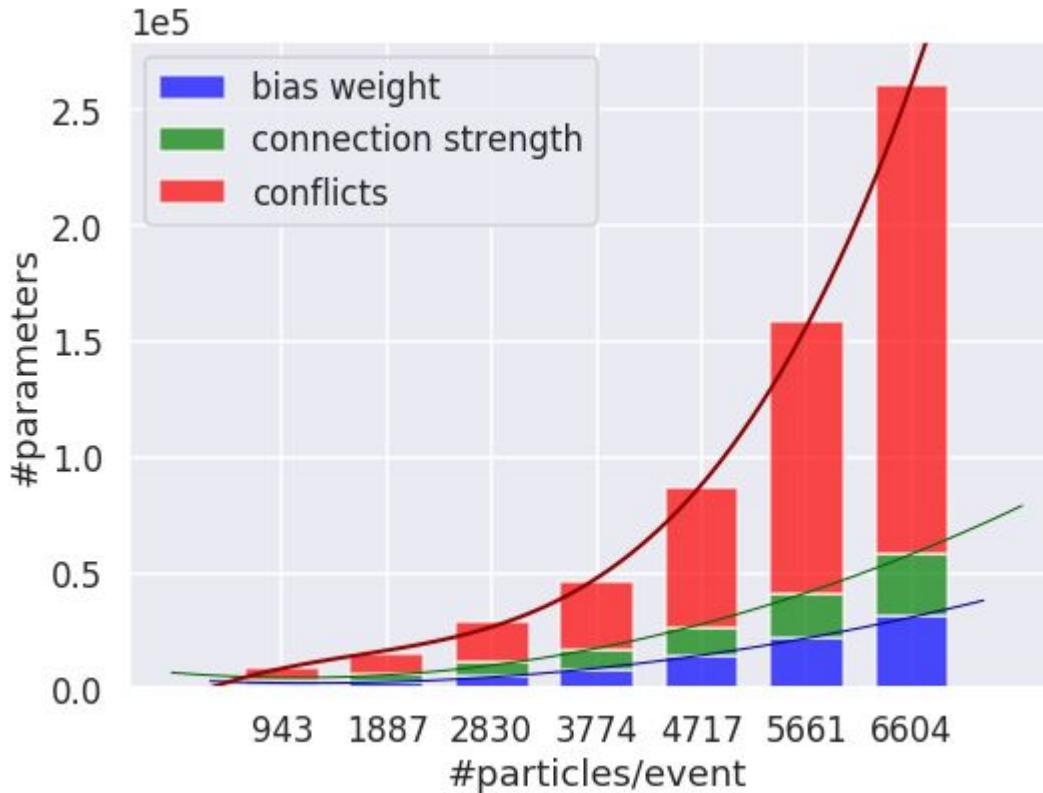
*QA recipe:*

initial Hamiltonian  $H_0$        $H(s) = A(s)H_0 + B(s)H_p$  with  
problem Hamiltonian  $H_p$        $A(s) \downarrow$  and  $B(s) \uparrow$  given  $s = t/t_f \ll 1$  ( $t_f = \text{anneal time}$ )

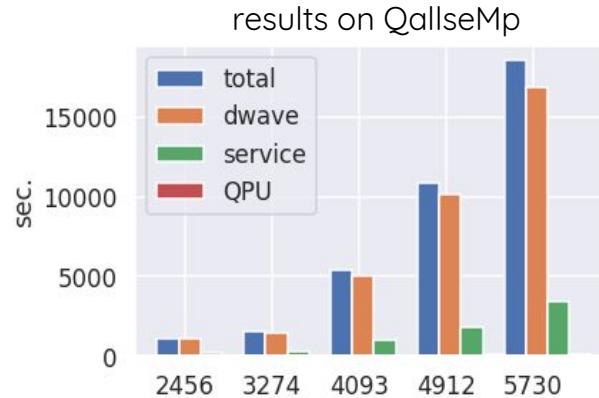
If the adiabatic conditions are respected,  
the system's ground state at  $t=t_f$  encodes the solution.



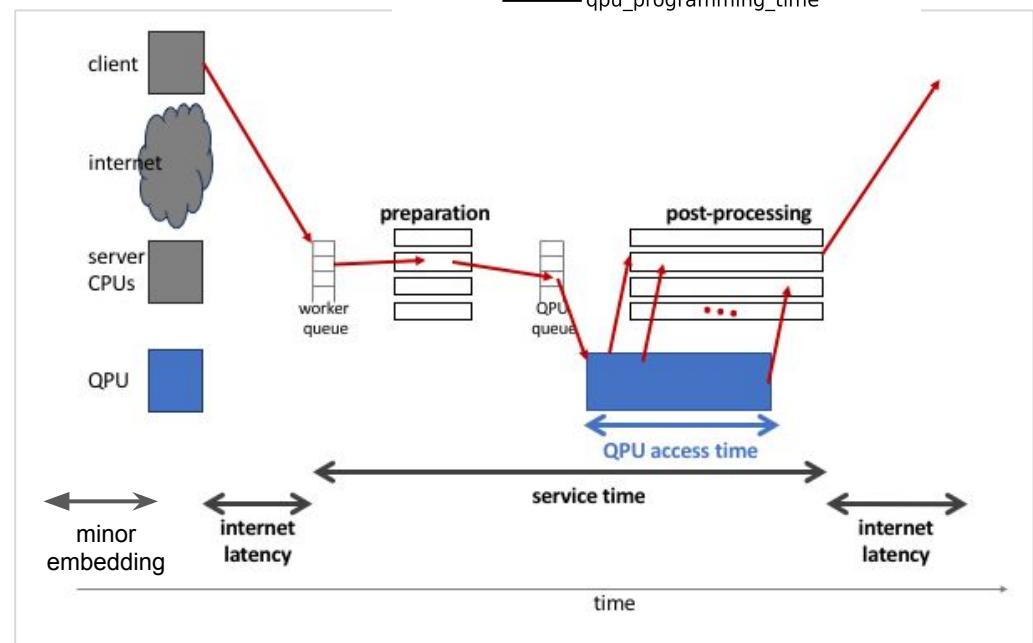
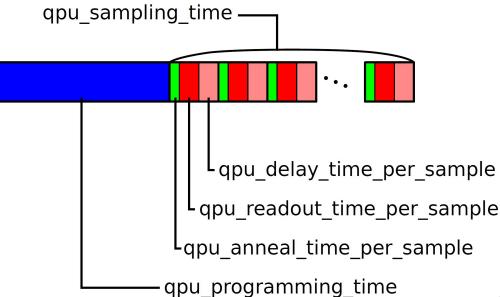
# QUBO composition



# D-Wave timing



QPU access time:





# A slightly different approach

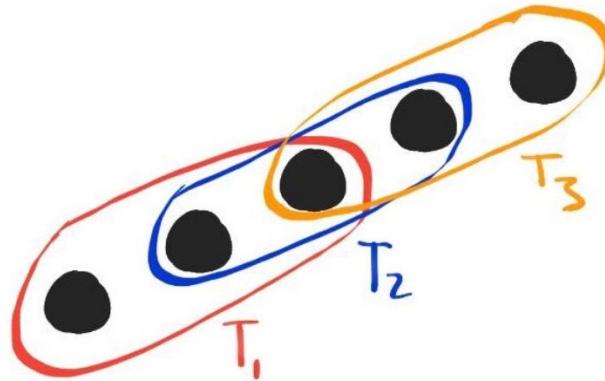
Triplets combined three-by-three.

## Model A

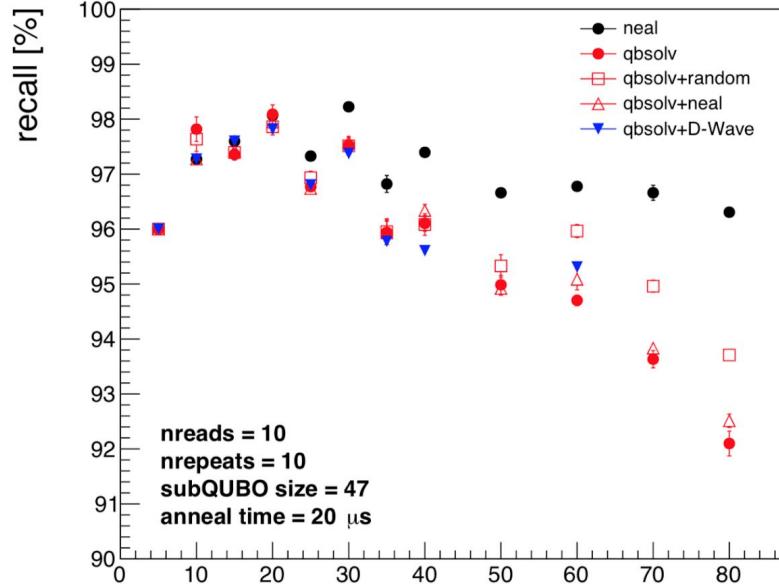
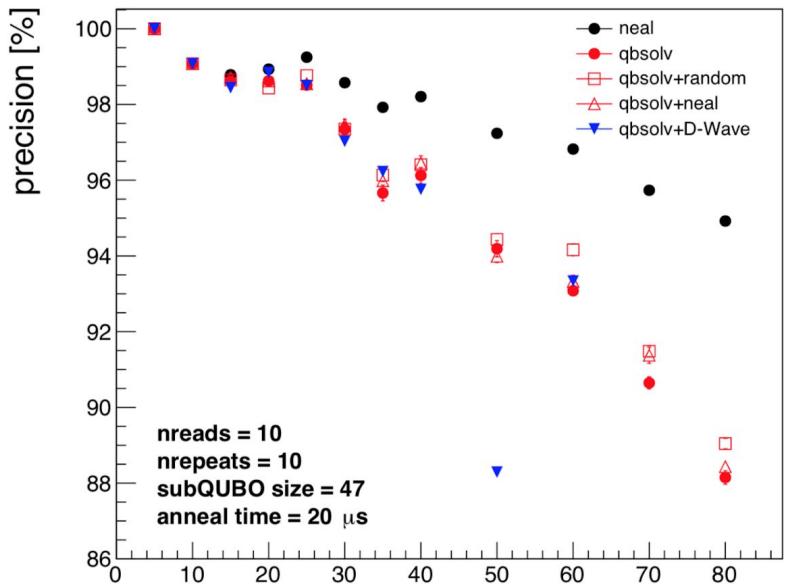
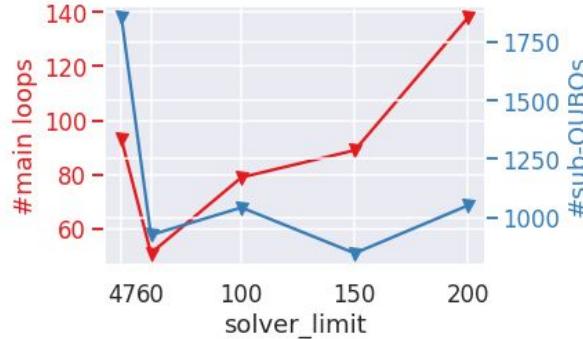
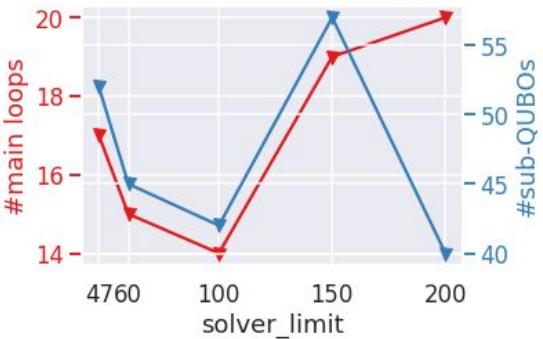
In the QUBO, use the same formula for the coupling T1-T2, but a new formula based on the stdev for T1-T3 (+ sum multiple scores): ~ +5% precision on a 60%-dataset.

## Model B

Use the stdev formula for all pairs: ~ +15% precision on a 60%-dataset.

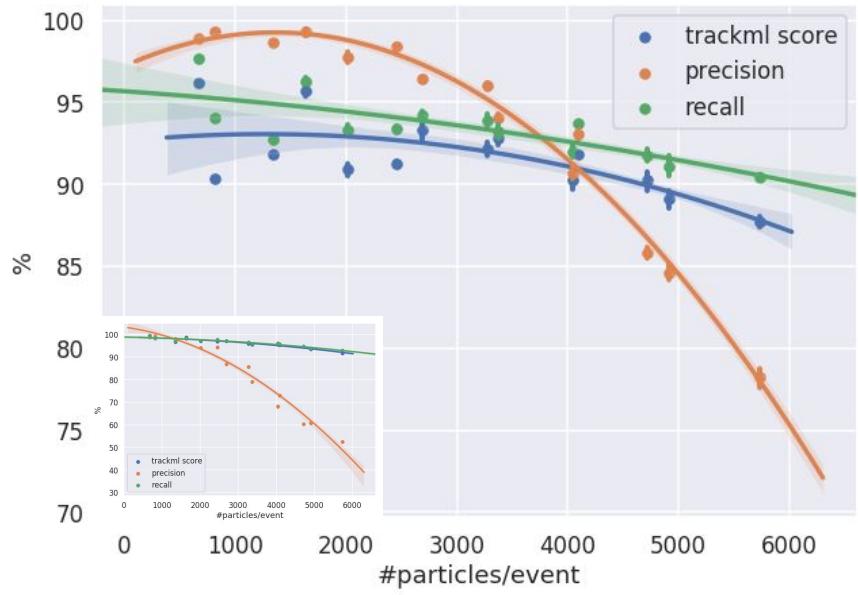
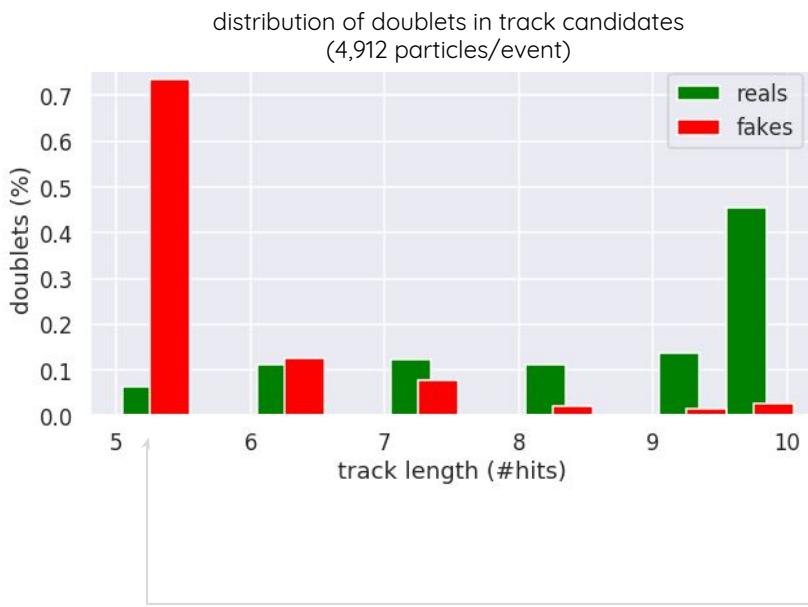


Credits: Alex Smith





# Should we discard small tracks ?

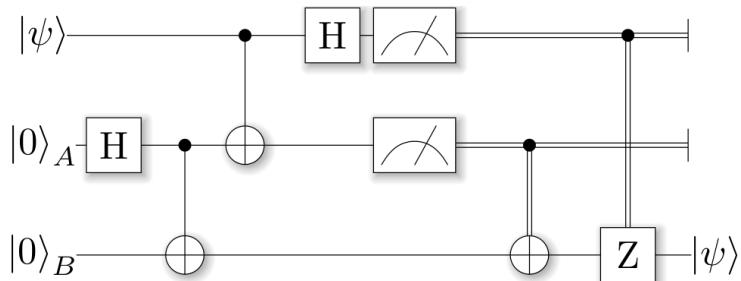


Scores after removing all tracks with 5 hits from the output.



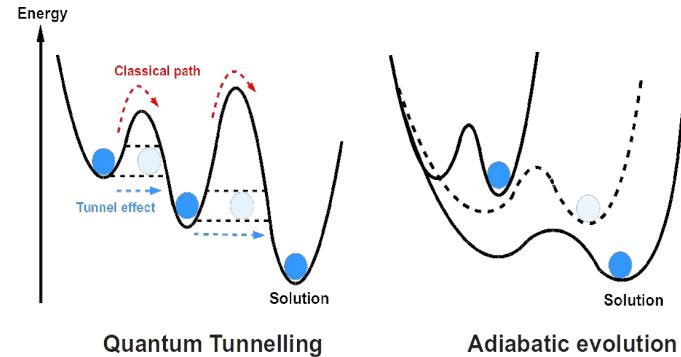
# State of Quantum Computing & HEP.QPR

## Universal quantum computers quantum circuits



IBM 50Q  
Rigetti 19Q  
Intel Tangle Lake (49Q)  
Google Bristlecone (72Q)  
...  
» [arXiv:1902.00498](https://arxiv.org/abs/1902.00498) «

## Quantum annealers



D-Wave (2000Q)

» [arXiv:1902.08324](https://arxiv.org/abs/1902.08324) «