

LHCb γ measurements with $B \rightarrow D^{(*)} K^{(*)}$

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on behalf of

the LHCb collaboration

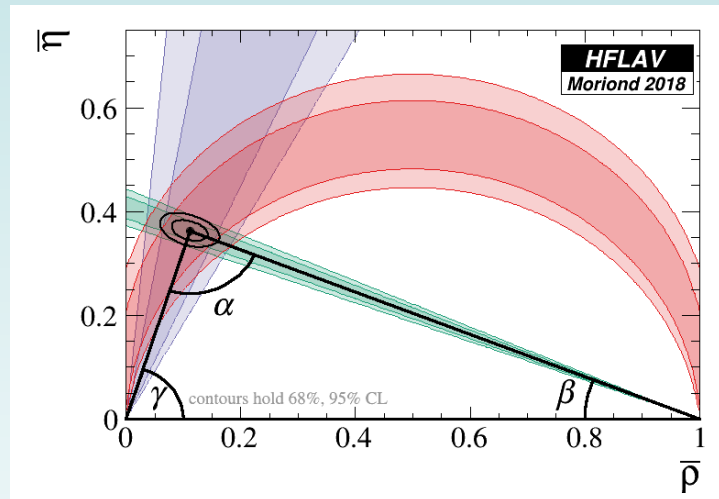
***Implications of LHCb measurements and future
prospects – October 2018***



The Leverhulme Trust

CKM angle γ

- For many years, least well measured Unitarity Triangle angle; now entering precision measurement era
- Can measure at tree level with $B \rightarrow DX$ decays



- Exploit weak phase difference γ between $b \rightarrow u$ and $b \rightarrow c$ transitions
- Theoretically clean but room for NP

[JHEP 01 \(2014\) 051](#)

[PRD 92 033002 \(2015\)](#)

- At LHCb, perform

- time-integrated measurements

$$B^- \rightarrow D^{(*)}K^{(*)-}, B^0 \rightarrow DK^{*0}, B^0 \rightarrow DK^+\pi^-, B^- \rightarrow DK^-\pi^+\pi^-$$

[PLB 557 198 \(2003\)](#)

- GLW analysis ($D \rightarrow CP$ eigenstate)

[PLB 253 483 \(1991\)](#) [PLB 265 172 \(1991\)](#)

- ADS analysis ($D \rightarrow$ flavour specific)

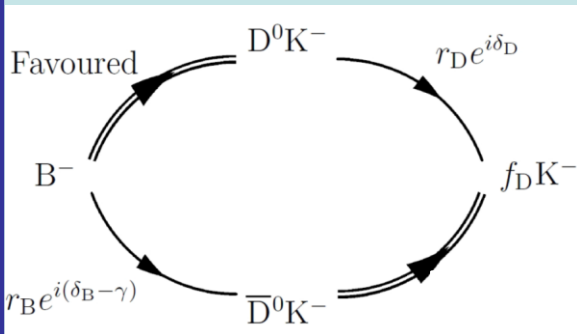
[PRL 78 3257 \(1997\)](#) [PRD 63 036005 \(2001\)](#)

- GGSZ analysis ($D \rightarrow$ multibody)

[PRD 68 054018 \(2003\)](#) [PRD 70 072003 \(2004\)](#)

- Dalitz analysis ($B \rightarrow$ multibody)

[PRD 79 051301\(R\) \(2009\)](#) [PRD 80 092002 \(2009\)](#)



- time-dependent measurements – see [Simon Stemmler's talk](#)

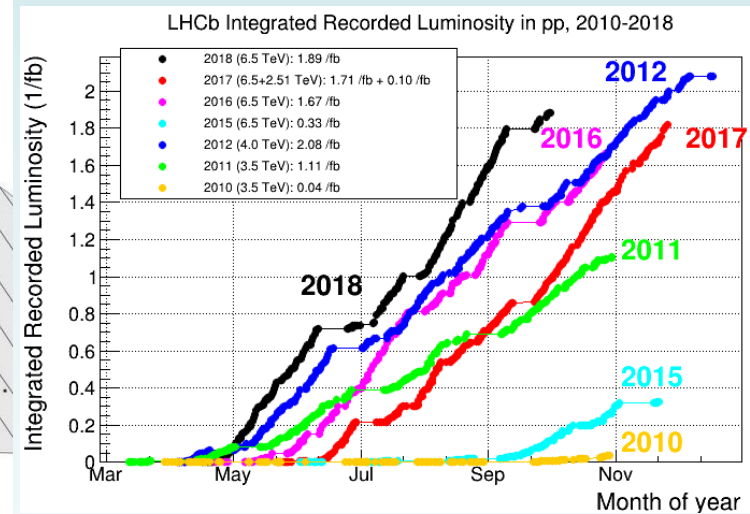
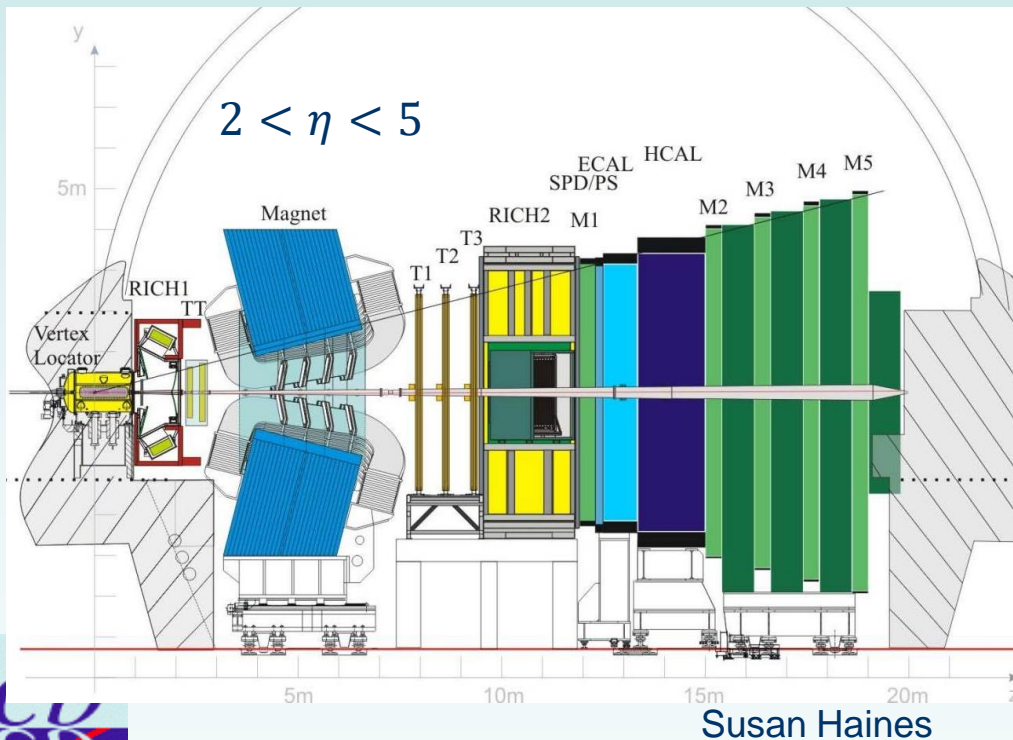
$$B_S^0 \rightarrow D_S^\mp K^\pm, B^0 \rightarrow D^\mp \pi^\pm$$

[PRD 37 3186 \(1988\)](#) [ZPC 54 653 \(1992\)](#) [NPB 671 459 \(2003\)](#)

- combination of LHCb γ measurements

The LHCb experiment

- Designed for study of particles containing b or c
 - High precision tracking and vertexing
 - Momentum resolution (0.5 – 1.0)%
 - Impact parameter resolution $(15 + 29 / p_T) \mu\text{m}$
 - RICH detectors for hadron PID ($K - \pi$ separation)

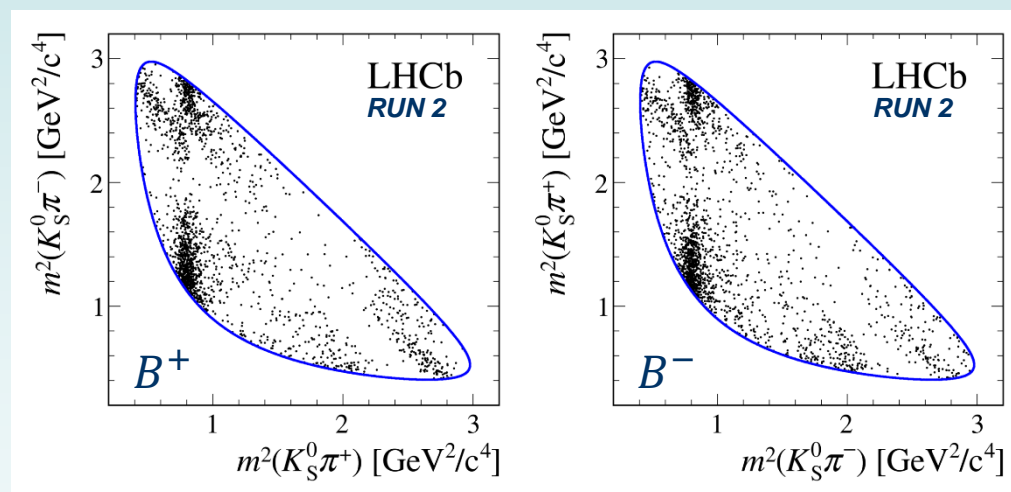


GGSZ analysis of $B^- \rightarrow DK^-, D \rightarrow K_S^0 h^+ h^-$

- Determine γ using D decay to three-body self-conjugate $K_S^0 \pi^+ \pi^-$ or $K_S^0 K^+ K^-$ final state
- One solution for γ in $[0, \pi]$
- Requires knowledge of resonant structure of $D \rightarrow K_S^0 h^+ h^-$ decay across phase space

$$A_{B^+} \propto \bar{A}_f + r_B e^{i(\delta_B + \gamma)} A_f$$

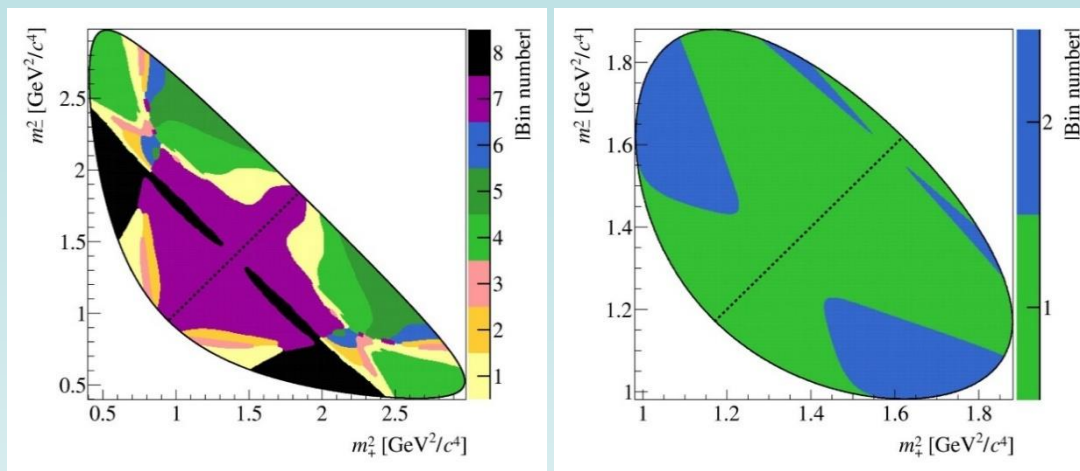
$$A_{B^-} \propto A_f + r_B e^{i(\delta_B - \gamma)} \bar{A}_f$$



- Observables: $x_{\pm} = r_B \cos(\delta_B \pm \gamma)$, $y_{\pm} = r_B \sin(\delta_B \pm \gamma)$

- Model-independent method: bin D decay phase space according to $D^0 - \bar{D}^0$ strong phase difference

$2N$ bins ($i \in [-N, N], i \neq 0$)
 $i > 0$ for $m_-^2 > m_+^2$



- Yield in bin i

$$N_{\pm i}^+ = h_{B^+} \left[F_{\mp i} + (x_+^2 + y_+^2) F_{\pm i} + 2\sqrt{F_i F_{-i}} (x_+ c_{\pm i} - y_+ s_{\pm i}) \right]$$

$$N_{\pm i}^- = h_{B^-} \left[F_{\pm i} + (x_-^2 + y_-^2) F_{\mp i} + 2\sqrt{F_i F_{-i}} (x_- c_{\pm i} + y_- s_{\pm i}) \right]$$

- (c_i, s_i) strong phase difference measurements from CLEO-c

[PRD 82 112006 \(2010\)](#)

- Results with Run 2 data (2 fb^{-1} at $\sqrt{s} = 13 \text{ TeV}$):

$$x_- = (9.0 \pm 1.7 \pm 0.7 \pm 0.4) \times 10^{-2}$$

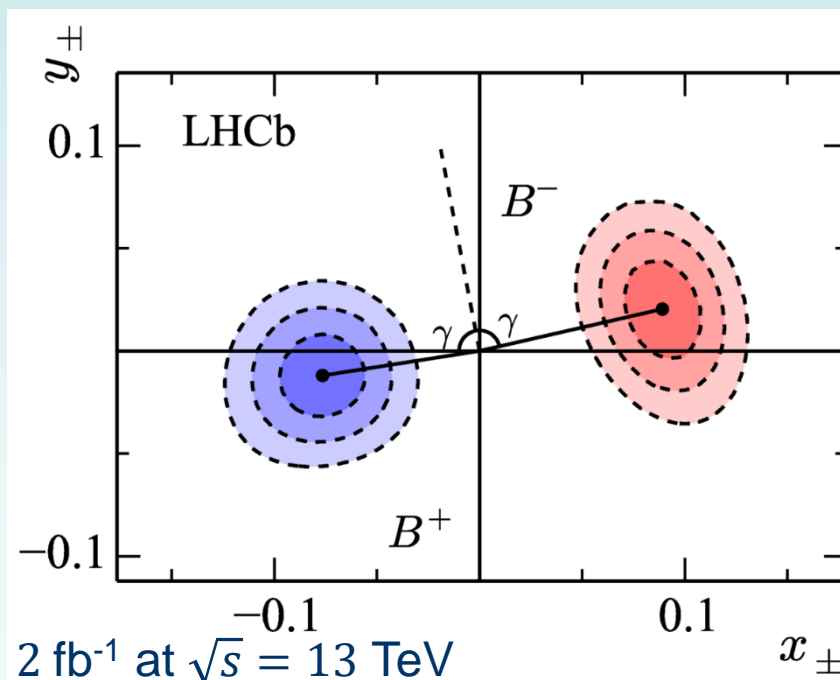
$$y_- = (2.1 \pm 2.2 \pm 0.5 \pm 1.1) \times 10^{-2}$$

$$x_+ = (-7.7 \pm 1.9 \pm 0.7 \pm 0.4) \times 10^{-2}$$

$$y_+ = (-1.0 \pm 1.9 \pm 0.4 \pm 0.9) \times 10^{-2}$$

First observation
of CP violation in

$$B^- \rightarrow DK^-, \\ D \rightarrow K_S^0 h^+ h^-$$

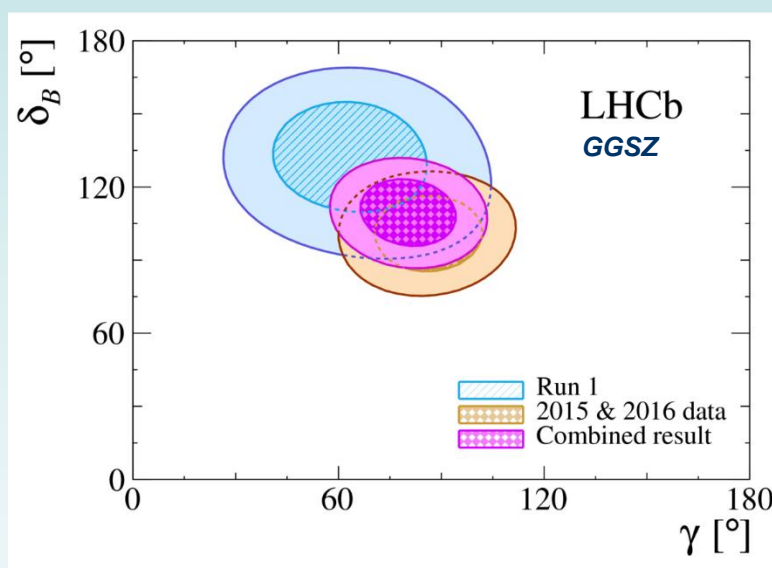
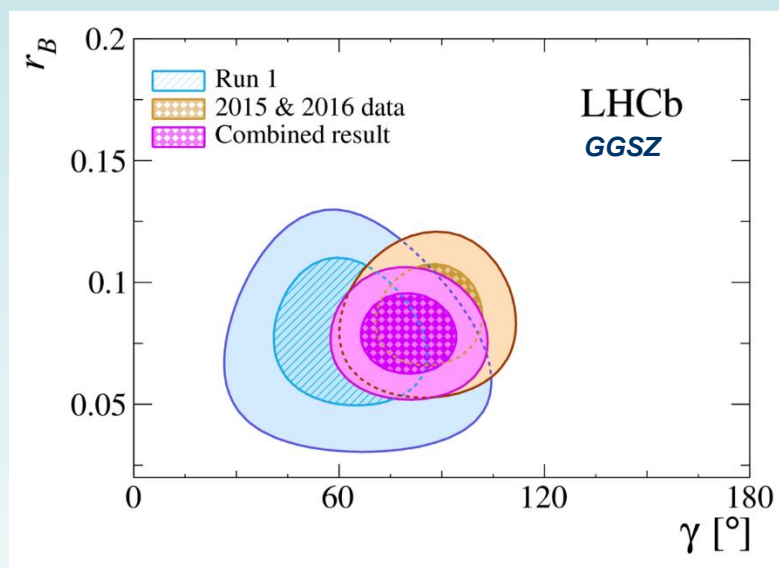


Statistical
uncertainties
only

- Combine with Run 1 results (3 fb⁻¹ at $\sqrt{s} = 7,8$ TeV) to give constraint on γ :

$$\gamma = \left(80_{-9}^{+10}\right)^{\circ}$$

GGSZ



$$\text{Run 1: } \gamma = \left(62_{-14}^{+15}\right)^{\circ}$$

$$\text{2015 \& 2016: } \gamma = \left(87_{-12}^{+11}\right)^{\circ}$$

Combination of LHCb measurements

- Combine tree-level LHCb γ measurements:

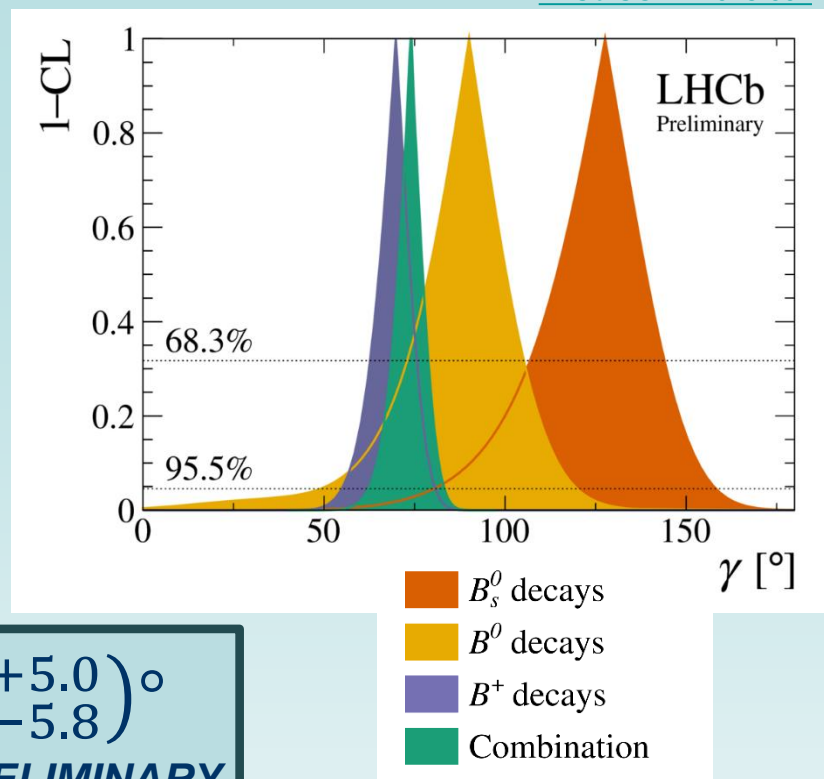
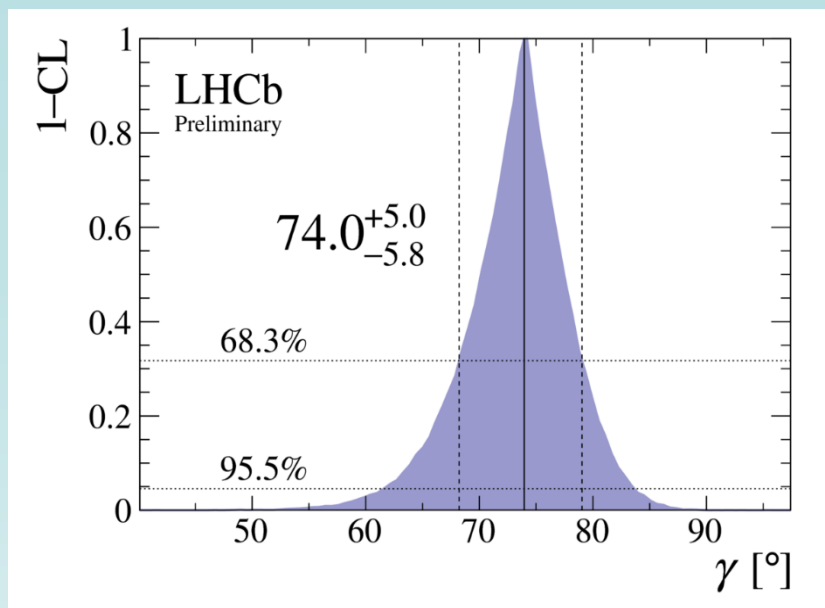
B decay	D decay	Method	Ref.	Dataset [†]	Status since last combination [3]
$B^+ \rightarrow DK^+$	$D \rightarrow h^+h^-$	GLW	[14]	Run 1 & 2	Minor update
$B^+ \rightarrow DK^+$	$D \rightarrow h^+h^-$	ADS	[15]	Run 1	As before
$B^+ \rightarrow DK^+$	$D \rightarrow h^+\pi^-\pi^+\pi^-$	GLW/ADS	[15]	Run 1	As before
$B^+ \rightarrow DK^+$	$D \rightarrow h^+h^-\pi^0$	GLW/ADS	[16]	Run 1	As before
$B^+ \rightarrow DK^+$	$D \rightarrow K_s^0 h^+ h^-$	GGSZ	[17]	Run 1	As before
$B^+ \rightarrow DK^+$	$D \rightarrow K_s^0 h^+ h^-$	GGSZ	[18]	Run 2	New
$B^+ \rightarrow DK^+$	$D \rightarrow K_s^0 K^+ \pi^-$	GLS	[19]	Run 1	As before
$B^+ \rightarrow D^* K^+$	$D \rightarrow h^+ h^-$	GLW	[14]	Run 1 & 2	Minor update
$B^+ \rightarrow DK^{*+}$	$D \rightarrow h^+ h^-$	GLW/ADS	[20]	Run 1 & 2	Updated results
$B^+ \rightarrow DK^{*+}$	$D \rightarrow h^+\pi^-\pi^+\pi^-$	GLW/ADS	[20]	Run 1 & 2	New
$B^+ \rightarrow DK^+\pi^+\pi^-$	$D \rightarrow h^+ h^-$	GLW/ADS	[21]	Run 1	As before
$B^0 \rightarrow DK^{*0}$	$D \rightarrow K^+ \pi^-$	ADS	[22]	Run 1	As before
$B^0 \rightarrow DK^+\pi^-$	$D \rightarrow h^+ h^-$	GLW-Dalitz	[23]	Run 1	As before
$B^0 \rightarrow DK^{*0}$	$D \rightarrow K_s^0 \pi^+ \pi^-$	GGSZ	[24]	Run 1	As before
$B_s^0 \rightarrow D_s^\mp K^\pm$	$D_s^+ \rightarrow h^+ h^- \pi^+$	TD	[25]	Run 1	Updated results
$B^0 \rightarrow D^\mp \pi^\pm$	$D^+ \rightarrow K^+ \pi^- \pi^+$	TD	[26]	Run 1	New

– see [Simon Stemmler's talk](#)

[†] Run 1 corresponds to an integrated luminosity of 3 fb^{-1} taken at centre-of-mass energies of 7 and 8 TeV. Run 2 corresponds to an integrated luminosity of 2 fb^{-1} taken at a centre-of-mass energy of 13 TeV.

- Frequentist approach
- Auxiliary inputs from HFLAV, CLEO and LHCb

Susan Haines



$$\gamma = (74.0^{+5.0}_{-5.8})^\circ$$

PRELIMINARY

- Most precise determination of γ from a single experiment
- World average: $\gamma = (73.5^{+4.2}_{-5.1})^\circ$ [HFLAV](#)
- Indirect constraints: $\gamma = (65.6^{+1.0}_{-3.4})^\circ$ [CKMfitter](#)

Outlook: exploiting existing data

- Run 2 updates

- $B^- \rightarrow DK^-$

- $D \rightarrow h^+h^-$ (ADS), $D \rightarrow h^+\pi^-\pi^+\pi^-$, $D \rightarrow h^+h^-\pi^0$, $D \rightarrow K_S^0K^+\pi^-$

- $B^0 \rightarrow DK^{*0} / B^0 \rightarrow DK^+\pi^-$

- $D \rightarrow h^+h^-$, $D \rightarrow K_S^0h^+h^-$

- $B^- \rightarrow DK^-\pi^+\pi^-$

- $D \rightarrow h^+h^-$

- New possible decay modes

- $B^- \rightarrow DK^-\pi^+\pi^-$, $B^- \rightarrow DK^{*-}$

- $D \rightarrow K_S^0h^+h^-$

- $B^- \rightarrow D^*h^-$

- $D \rightarrow K_S^0h^+h^-$, $D \rightarrow h^+h^-$

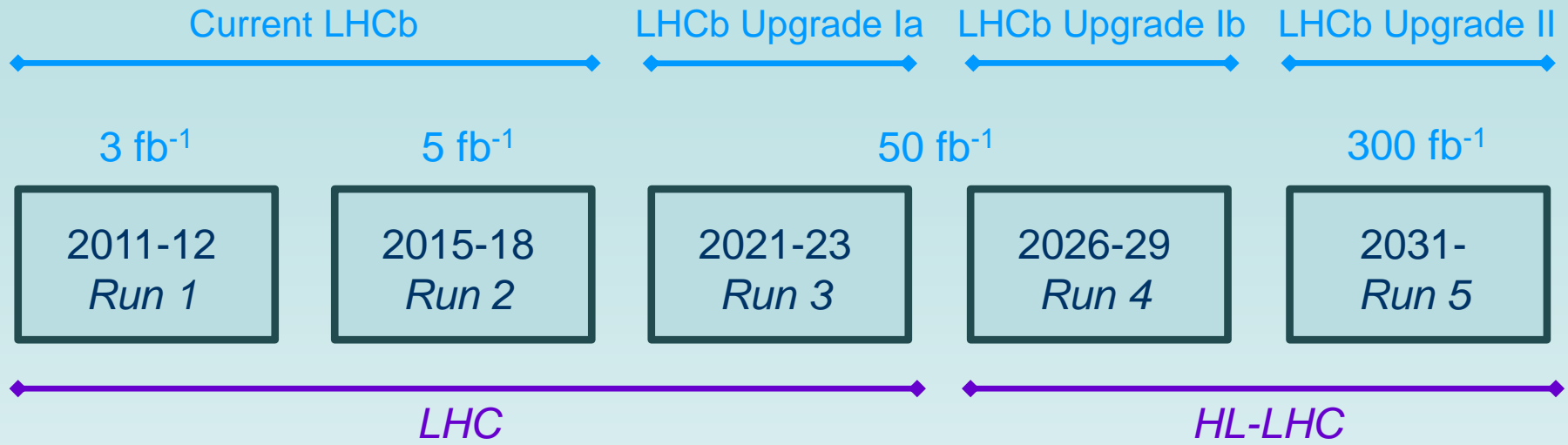
- $D \rightarrow K^+K^-\pi^+\pi^-$, $D \rightarrow K_S^0\pi^+\pi^-\pi^0$...

Expect $\sigma(\gamma) = 4^\circ$

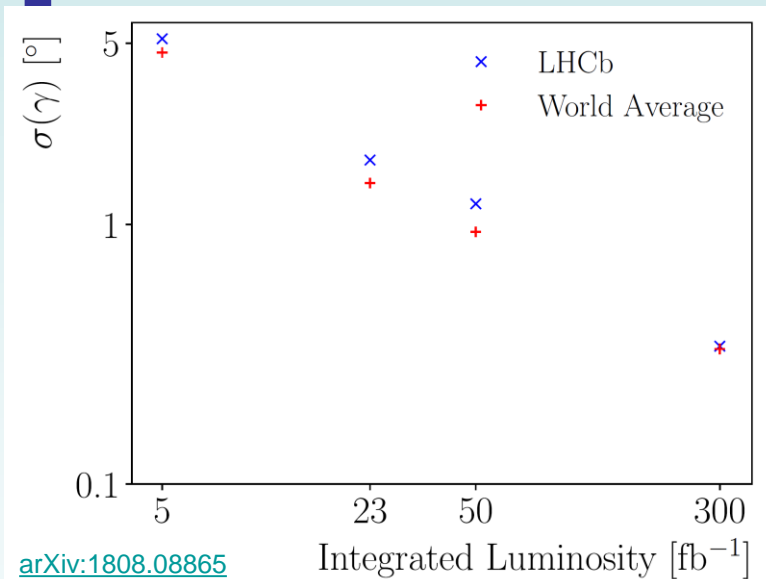
[EPJ C 73 \(2013\) 2373](#)

(+ time-dependent analyses)

Outlook: future data



Outlook: future data



$$\sigma(\gamma) = 4^\circ$$

[EPJ C 73 \(2013\) 2373](https://arxiv.org/abs/1808.08865)

$$\sigma(\gamma) = 0.9^\circ$$

[EPJ C 73 \(2013\) 2373](https://arxiv.org/abs/1808.08865)

$$\sigma(\gamma) = 1.5^\circ$$

(Belle II similar)

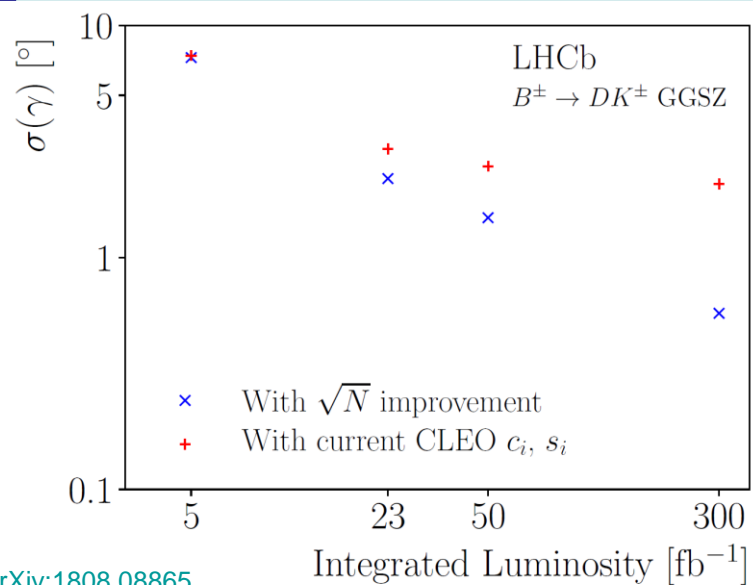
[arXiv:1808.08865](https://arxiv.org/abs/1808.08865)

[arXiv:1808.10567](https://arxiv.org/abs/1808.10567)

$$\sigma(\gamma) = 0.35^\circ$$

[arXiv:1808.08865](https://arxiv.org/abs/1808.08865)

- Expect main experimental systematic uncertainties to scale with data/simulation sample sizes
 - Production/instrumentation asymmetries
 - Understanding of backgrounds/control modes and simulation
- For GGSZ, uncertainties from CLEO-c (c_i, s_i) inputs will become limiting in upgrade era ($\sigma(\gamma) \sim 2^\circ$)



- Ongoing cooperation between BESIII and LHCb to measure (c_i, s_i) and other charm inputs

[BESIII-LHCb workshop 2018](#)

- Constrain with other decay modes e.g. $B^0 \rightarrow DK^+ \pi^-$, $D \rightarrow K_S^0 \pi^+ \pi^-$

[PRD 97 056002 \(2018\)](#)

[arXiv:1808.08865](#)

Outlook: further sensitivity gains

- New possible decay modes?
 - High multiplicity B and D decay modes
 - Modes with neutrals, e.g. $D \rightarrow K_S^0 \pi^0$ (Upgrade Ib onwards)
 - γ from B_c or b-baryons
- New strategies?
 - Model-independent unbinned (Fourier analysis) GGSZ approach [EPJC \(2018\) 78:121](#)
 - Unified approach – simultaneous GLW/ADS/GGSZ [arXiv:1804.05597](#)

Conclusions

- Combination of LHCb results, including new GGSZ measurement, gives most precise determination of γ from a single experiment

$$\gamma = (74.0^{+5.0}_{-5.8})^\circ$$

PRELIMINARY

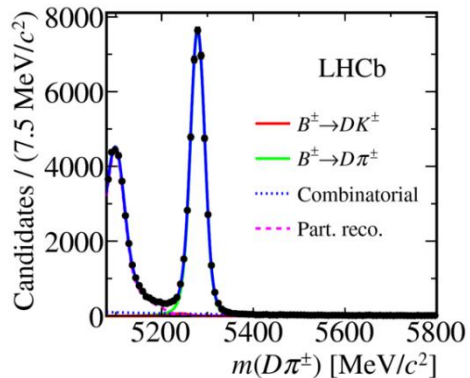
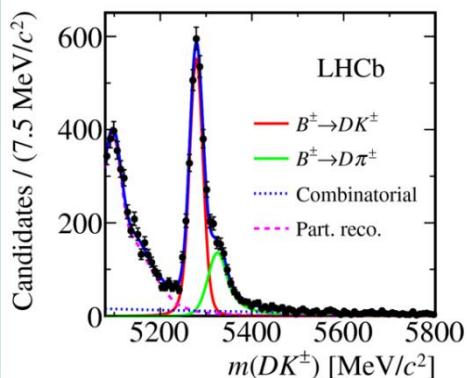
- Coming soon:
 - Further updates including Run 2 data set
 - Studies of new decay modes

Now entering era of precision γ measurement

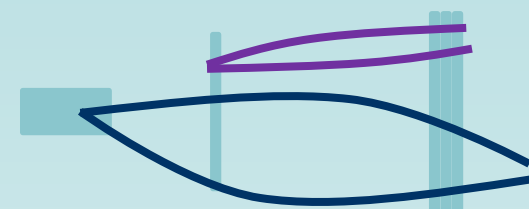
- Expect $\sigma(\gamma) = 1.5^\circ$ in 2025; $\sigma(\gamma) = 0.35^\circ$ with LHCb Upgrade II

Backup:

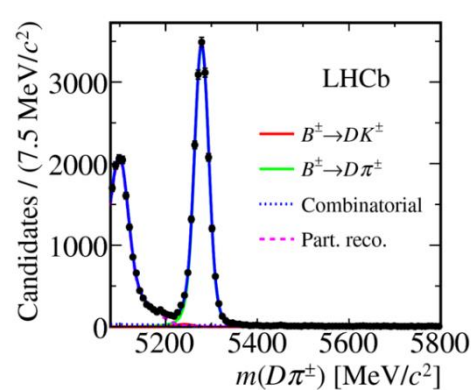
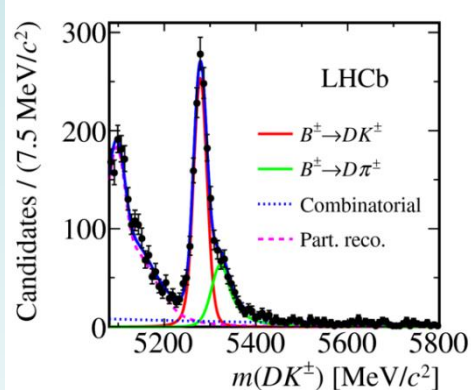
GGSZ analysis of $B^- \rightarrow DK^-, D \rightarrow K_S^0 h^+ h^-$



K_S^0 without VELO (Si vertex tracker) daughter hits

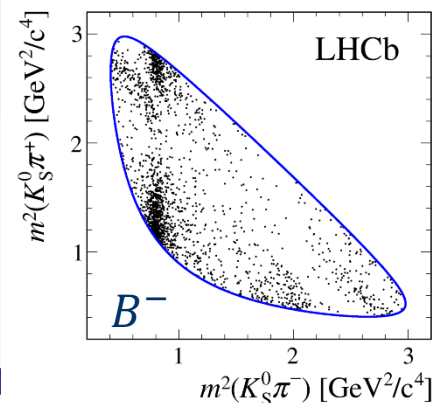
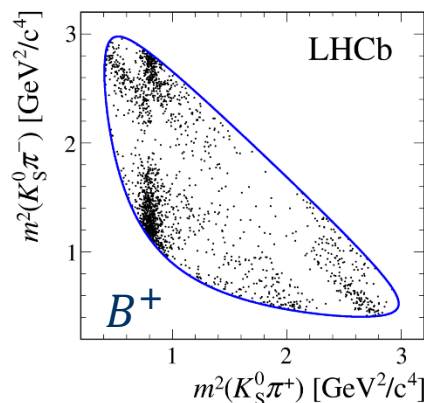


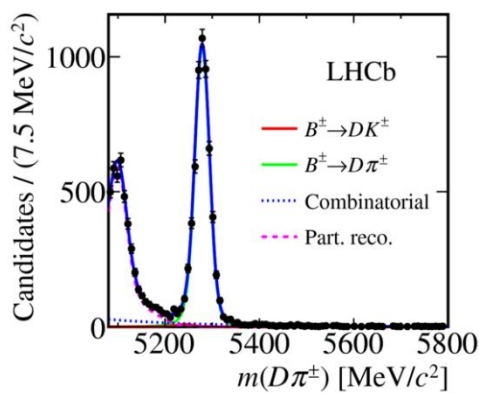
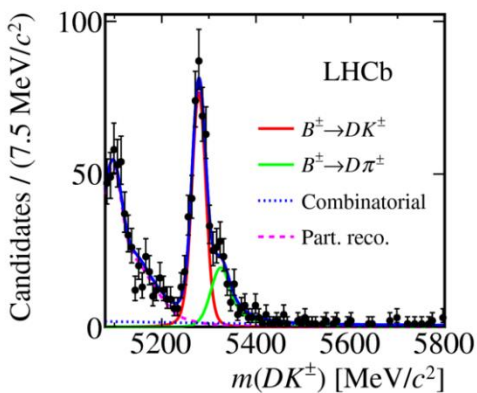
K_S^0 with VELO (Si vertex tracker) daughter hits



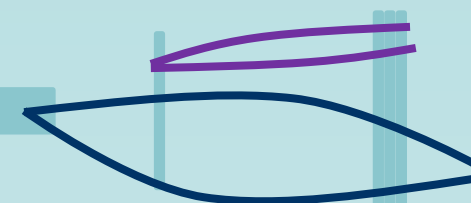
$$B^- \rightarrow Dh^-,$$

$$D \rightarrow K_S^0 \pi^+ \pi^-$$

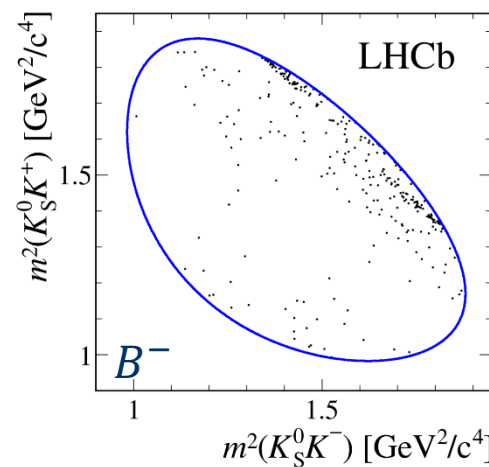
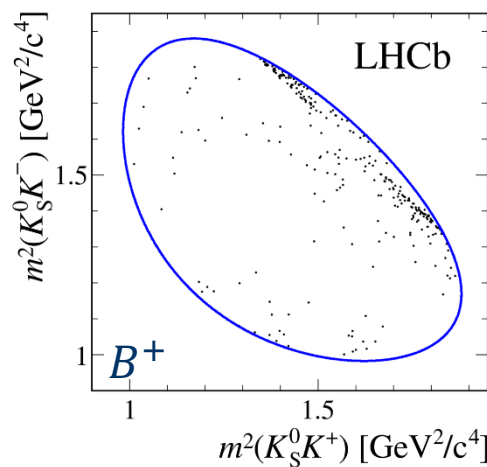
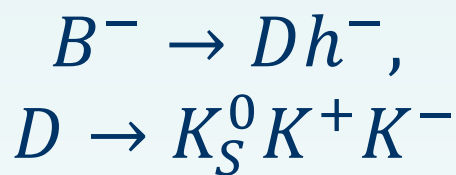
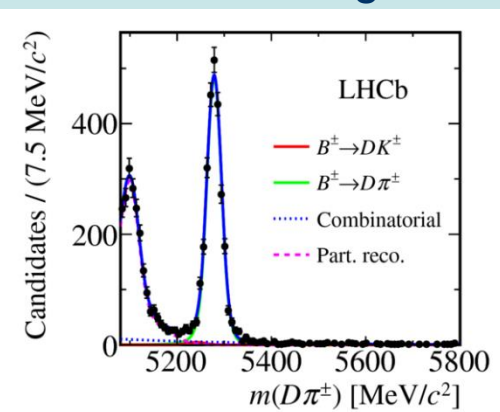
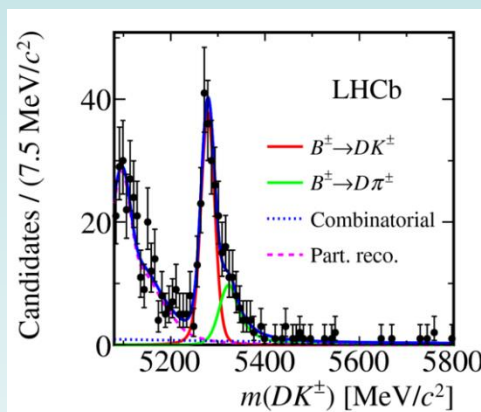




K_S^0 without
VELO (Si
vertex tracker)
daughter hits



K_S^0 with VELO
(Si vertex tracker)
daughter hits



Backup: Combination of LHCb measurements

