

# Time dependent CP asymmetry in beauty @ LHCb

---

Simon Stemmler

Heidelberg University

LHCb Implications Workshop, 17.10.2018



UNIVERSITÄT  
HEIDELBERG  
ZUKUNFT  
SEIT 1386

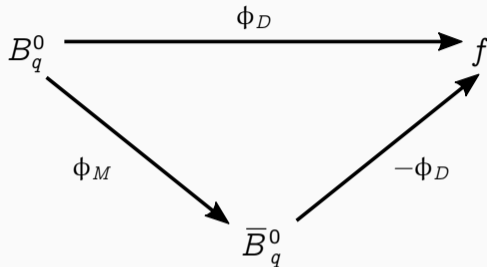
# Why time dependent CP violation?

Interference between mixing and decay is sensitive to:

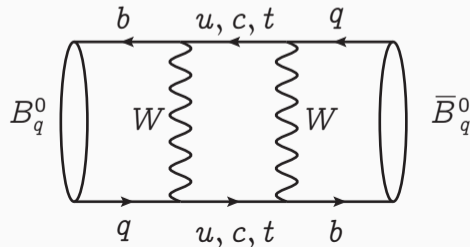
- The weak mixing phases themselves
- Several CKM angles ( $\beta$ ,  $\beta_s$ ,  $\gamma$ ,  $\alpha$ )

Probing beyond the standard model:

- FCNC in the mixing  
→ Possible non SM contributions
- Some final states are not allowed at tree level  
→ Further non SM contributions



Accessible weak phase:  $\phi_q^f = \phi_M - 2\phi_D$



Time dependent decay rates:

$$\frac{d\Gamma_{B_q^0 \rightarrow f}(t)}{dt} = |A_f| \frac{1}{1 + C_f} e^{-\Gamma_q t} \left[ \cosh\left(\frac{\Delta\Gamma_q t}{2}\right) + A_f^{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_q t}{2}\right) + C_f \cos(\Delta m_q t) - S_f \sin(\Delta m_q t) \right]$$

$$\frac{d\Gamma_{\bar{B}_q^0 \rightarrow f}(t)}{dt} = |A_f| \frac{p}{q} \frac{1}{1 + C_f} e^{-\Gamma_q t} \left[ \cosh\left(\frac{\Delta\Gamma_q t}{2}\right) + A_f^{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_q t}{2}\right) - C_f \cos(\Delta m_q t) + S_f \sin(\Delta m_q t) \right]$$

$$C_f = \frac{1 - |\lambda_f|^2}{1 + |\lambda_f|^2}$$

$$S_f = \frac{2\mathfrak{I}(\lambda_f)}{1 + |\lambda_f|^2}$$

$$A_f^{\Delta\Gamma} = -\frac{2\Re(\lambda_f)}{1 + |\lambda_f|^2}$$

$$\lambda_f = \frac{q}{p} \frac{\bar{A}_f}{A_f};$$

$\arg(\lambda_f)$  is a combination of the strong and weak mixing and decay phases  
 $\rightarrow$  allows a determination of CKM angles (depending on the final state)

In case of a CP eigenstate f:

$C_f \hat{=}$  CP violation in decay/mixing

$S_f \hat{=}$  CP violation in interference

# Experimental ingredients

Time dependent decay rates:

$$\frac{d\Gamma_{B_q^0 \rightarrow f}(t)}{dt} = |A_f| \frac{1}{1 + C_f} e^{-\Gamma_q t} \left[ \cosh\left(\frac{\Delta\Gamma_q t}{2}\right) + A_f^{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_q t}{2}\right) + C_f \cos(\Delta m_q t) - S_f \sin(\Delta m_q t) \right]$$

$$\frac{d\Gamma_{\bar{B}_q^0 \rightarrow f}(t)}{dt} = |A_f| \frac{p}{q} \frac{1}{1 + C_f} e^{-\Gamma_q t} \left[ \cosh\left(\frac{\Delta\Gamma_q t}{2}\right) + A_f^{\Delta\Gamma} \sinh\left(\frac{\Delta\Gamma_q t}{2}\right) - C_f \cos(\Delta m_q t) + S_f \sin(\Delta m_q t) \right]$$

**Oscillation:**

- Large mass splitting in the  $B_s^0$  system requires excellent decay time resolution
- Depending on the final state LHCb reaches **O(45 fs)**

**Decay width (difference):**

- A precise knowledge of the decay time acceptance shape is crucial

**Initial flavour:**

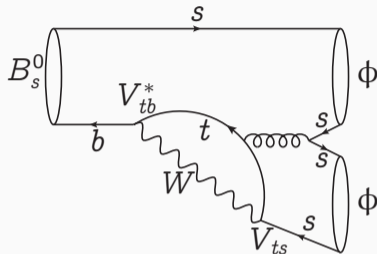
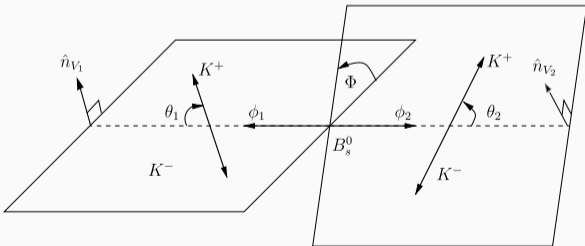
- The effective power of the flavor tagging is directly linked to the CPV sensitivity (**O(4 – 6%)** of effective tagged sample size)

What do we measure there?

$$\phi_s^{s\bar{s}s} := \arg(\lambda_f) = \arg\left(\frac{q}{p} \frac{\bar{A}_f}{A_f}\right)$$

$$\stackrel{\text{1.order}}{\approx} \arg\left(\frac{V_{tb}^* V_{ts}}{V_{tb} V_{ts}^*} \frac{V_{tb} V_{ts}^*}{V_{tb}^* V_{ts}}\right) = 0$$

SM upper limit:  $\phi_s^{s\bar{s}s} \leq 0.02 \text{ rad}$



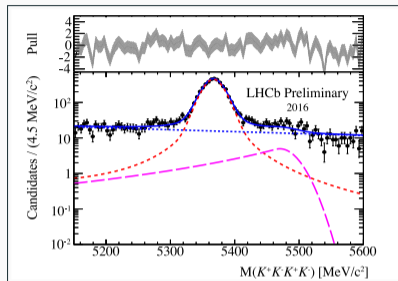
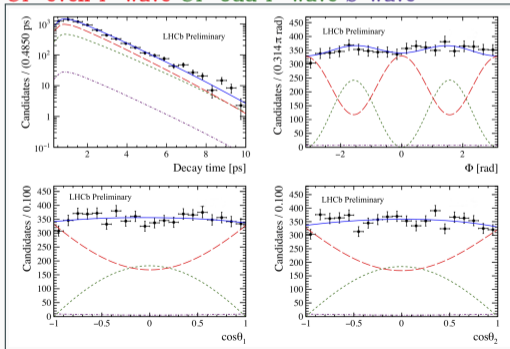
Experimental complications

- $B_s^0 \rightarrow \phi\phi$  is a  $P \rightarrow VV$  decay  
 $\Rightarrow$  No CP eigenstate:  
 $CP |\phi\phi\rangle = (-1)^l |\phi\phi\rangle$
- $S$ -wave contributions (VS and SS) from non-resonant and  $f_0(980)$

$\Rightarrow$  Angular analysis is necessary

- Background subtraction by fit to  $B_s^0$  mass
- $\Gamma_s$ ,  $\Delta\Gamma_s$  and  $\Delta m_s$  constrained to values from HFLAV and LHCb

*CP-even P-wave CP-odd P-wave S-wave*



Signal  
 $\Lambda_b \rightarrow \phi p K^-$   
 Combinatorial  
 bkg.

**Results:**

$$\phi_s^{\bar{s}s} = -0.07 \pm 0.13(\text{stat.}) \pm 0.03(\text{syst.}) \text{ rad}$$

$$|\lambda| = 1.02 \pm 0.05(\text{stat.}) \pm 0.03(\text{syst.})$$

$$|A_0|^2 = 0.382 \pm 0.008(\text{stat.}) \pm 0.011(\text{syst.})$$

$$|A_{\perp}|^2 = 0.287 \pm 0.008(\text{stat.}) \pm 0.005(\text{syst.})$$

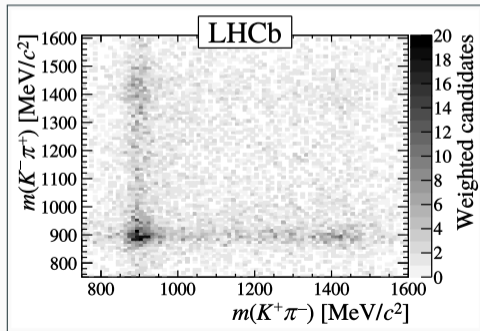
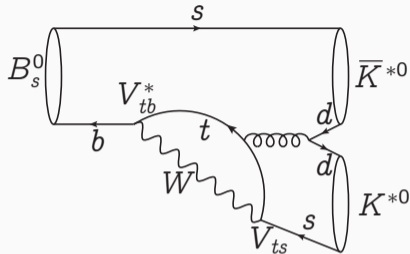
$$\delta_{\perp} = 2.81 \pm 0.21(\text{stat.}) \pm 0.10(\text{syst.}) \text{ rad}$$

$$\delta_{\parallel} = 2.52 \pm 0.05(\text{stat.}) \pm 0.07(\text{syst.}) \text{ rad}$$

What do we measure there?

In analogy to  $B_s^0 \rightarrow \phi\phi$ :

$$\phi_s^{d\bar{d}s} := \arg(\lambda_f) = \arg\left(\frac{q}{p} \frac{\bar{A}_f}{A_f}\right) \stackrel{1.\text{order}}{\approx} \arg\left(\frac{V_{tb}^* V_{ts}}{V_{tb} V_{ts}^*} \frac{V_{tb} V_{ts}^*}{V_{tb}^* V_{ts}}\right) = 0$$



## Experimental complications

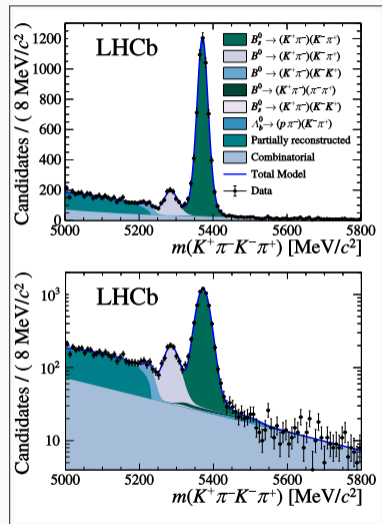
- Rich  $(K^-\pi^+)$  spectrum:  
 $K_0^*(800)^0$ ,  $K_0^*(1430)^0$ ,  $K^*(892)^0$ ,  $K_2^*(1430)^0$
- Many amplitudes with different CP eigenvalues

⇒ Full time dependent amplitude analysis

Scalar (S), Vector (V) and Tensor (T) contributions:

Decay	Polarization amplitudes
$B_s^0 \rightarrow (K^+\pi^-)_0^*(K^+\pi^-)_0^*$	SS
$B_s^0 \rightarrow (K^+\pi^-)_0^*\bar{K}^*(892)^0$	SV
$B_s^0 \rightarrow K^*(892)^0(K^+\pi^-)_0^*$	VS
$B_s^0 \rightarrow (K^+\pi^-)_0^*\bar{K}_2^*(1430)^0$	ST
$B_s^0 \rightarrow K_2^*(1430)^0(K^-\pi^+)_0^*$	TS
$B_s^0 \rightarrow K^*(892)^0\bar{K}^*(892)^0$	VV0, VV $\parallel$ , VV $\perp$
$B_s^0 \rightarrow K^*(892)^0\bar{K}_2^*(1430)^0$	VT0, VT $\parallel$ , VT $\perp$
$B_s^0 \rightarrow K_2^*(1430)^0\bar{K}^*(892)^0$	TV0, TV $\parallel$ , TV $\perp$
$B_s^0 \rightarrow K_2^*(1430)^0\bar{K}_2^*(1430)^0$	TT0, TT $\parallel_1$ , TT $\perp_1$ , TT $\parallel_2$ , TT $\perp_2$

In total 19 different polarization amplitudes!



$$N_{\text{signal}} = 6080 \pm 83$$



## Results:

- Most precise measurement of the 19 polarization amplitudes

E.g.:

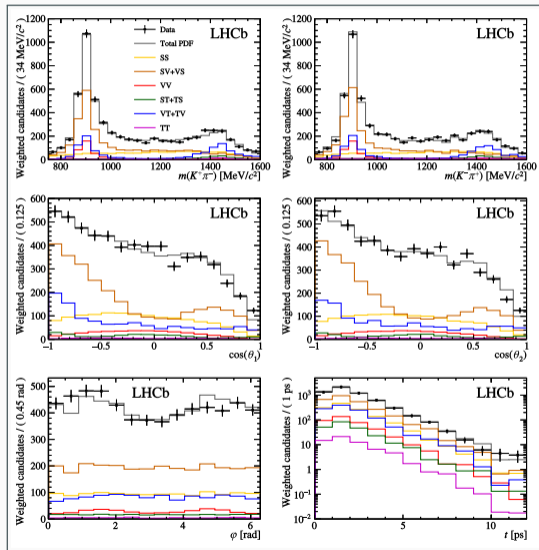
$$f_L^{VV} = 0.208 \pm 0.032(\text{stat.}) \pm 0.046(\text{syst.})$$

- $CP$  observables (Common for all polarizations):

$$\phi_s^{d\bar{d}s} = -0.10 \pm 0.13(\text{stat.}) \pm 0.14(\text{syst.}) \text{ rad}$$

$$|\lambda| = 1.035 \pm 0.034(\text{stat.}) \pm 0.089(\text{syst.})$$

Systematic dominated by size of simulation samples



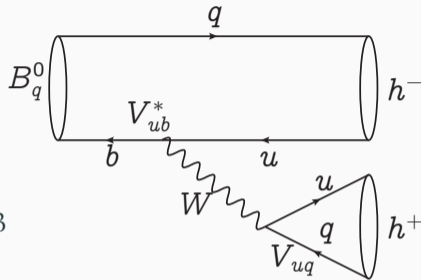
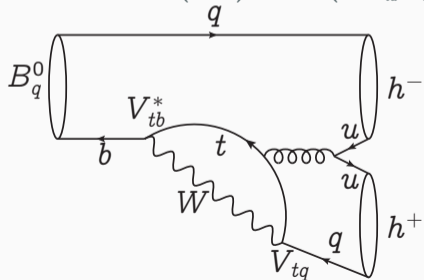
What do we measure there?

$B_s^0 \rightarrow K^- K^+$ :

$$\arg(\lambda_f) = \arg\left(\frac{q}{p} \frac{\bar{A}_f}{A_f}\right) \neq \arg\left(\frac{V_{tb}^* V_{ts}}{V_{tb} V_{ts}^*} \frac{V_{ub} V_{us}^*}{V_{ub}^* V_{us}}\right) \approx -2\gamma + 2\beta_s$$

$B^0 \rightarrow \pi^- \pi^+$ :

$$\arg(\lambda_f) = \arg\left(\frac{q}{p} \frac{\bar{A}_f}{A_f}\right) \neq \arg\left(\frac{V_{tb}^* V_{td}}{V_{tb} V_{td}^*} \frac{V_{ub} V_{ud}^*}{V_{ub}^* V_{ud}}\right) = \alpha \parallel -2\gamma - 2\beta$$



**But:** The situation is not that easy!

- Tree level heavily CKM suppressed
- Penguin diagrams not negligible

$\Rightarrow$  Will only measure  $CP$  observables  $C$ ,  $S$  and  $A^{\Delta\Gamma}$

But:  $\gamma/\alpha$  and  $\beta_s$  can be inferred by relating

$B_s^0 \rightarrow K^- K^+$  and  $B^0 \rightarrow \pi^- \pi^+$  via U-spin symmetry

[JHEP 10 \(2013\)183](#)

## Analysis strategy:

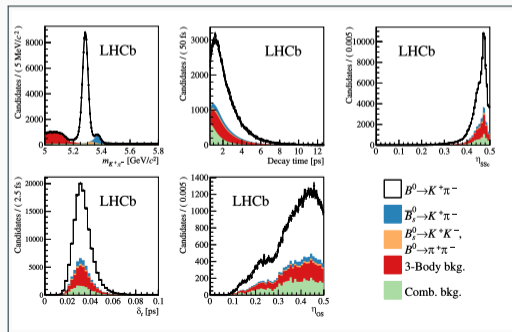
- Simultaneous fit to three samples:

$K^-K^+$  (for  $B_s^0 \rightarrow K^-K^+$ ),  $\pi^+\pi^-$  (for  $B^0 \rightarrow \pi^+\pi^-$ ) and  $K^\pm\pi^\mp$  (for  $B^0 \rightarrow K^+\pi^-$ ,  $B_s^0 \rightarrow K^-\pi^+$ )

- Fitting  $m(h^+h^-)$ , decay time, per event decay time uncertainty, and tagging parameter ( $\eta$ ) distributions of all three samples

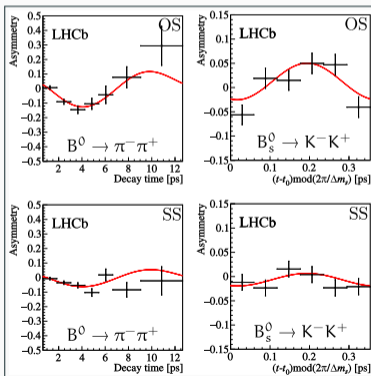
## Including flavour specific decays:

- On the fly calibration of many of the tagging parameters
- Determination of time integrated CP asymmetries
- Disentangling of B production asymmetries and direct CP asymmetries



Nice visualization of the results: Projections of the time dependent asymmetry

$$A_{CP}(t) = \frac{\Gamma_{\bar{B}_q^0 \rightarrow f}(t) - \Gamma_{B_q^0 \rightarrow f}(t)}{\Gamma_{\bar{B}_q^0 \rightarrow f}(t) + \Gamma_{B_q^0 \rightarrow f}(t)} = \frac{-C_f \cos(\Delta m_q t) + S_f \sin(\Delta m_q t)}{\cosh(\frac{\Delta\Gamma_q}{2} t) + A_f^{\Delta\Gamma} \sinh(\frac{\Delta\Gamma_q}{2} t)}$$



$$C_{\pi^+\pi^-} = -0.34 \pm 0.06 \pm 0.01$$

$$S_{\pi^+\pi^-} = -0.63 \pm 0.05 \pm 0.01$$

$$C_{K^+K^-} = 0.20 \pm 0.06 \pm 0.02$$

$$S_{K^+K^-} = 0.18 \pm 0.06 \pm 0.02$$

$$A_{K^+K^-}^{\Delta\Gamma} = -0.79 \pm 0.07 \pm 0.10$$

$$A_{CP}^{B^0 \rightarrow K^+\pi^-} = -0.084 \pm 0.004 \pm 0.003$$

$$A_{CP}^{B_s^0 \rightarrow K^-\pi^+} = 0.213 \pm 0.015 \pm 0.007$$

**4 $\sigma$  significance for TD CPV in  $B_s^0$  system!**

What do we measure there?

$$\begin{aligned} \arg(\lambda_f) &= \arg\left(\frac{q}{p} \frac{\bar{A}_f}{A_f}\right) \\ &\approx \delta + \arg\left(\frac{V_{tb}^* V_{ts}}{V_{tb} V_{ts}^*} \frac{V_{ub} V_{cs}^*}{V_{cb}^* V_{us}}\right) \approx \delta - (\gamma - 2\beta_s) \end{aligned}$$

$\delta$ : strong phase difference between  $\bar{A}_{D_s^- K^+}$  and  $A_{D_s^- K^+}$

Five observables for three unknowns:

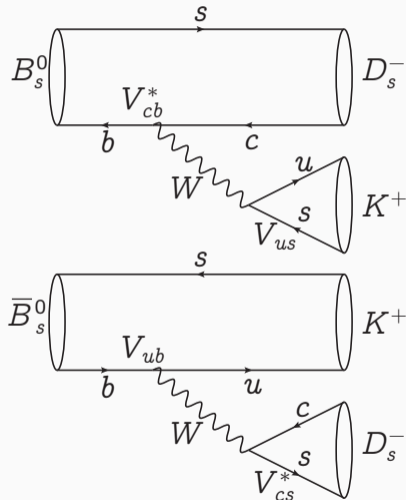
(No CPV in decay and mixing)

$$C_f = \frac{1 - r_{D_s K}^2}{1 + r_{D_s K}^2} = -C_{\bar{f}}$$

$$A_f^{\Delta\Gamma} = \frac{-2r_{D_s K} \cos(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2} \quad A_{\bar{f}}^{\Delta\Gamma} = \frac{-2r_{D_s K} \cos(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

$$S_f = \frac{2r_{D_s K} \sin(\delta - (\gamma - 2\beta_s))}{1 + r_{D_s K}^2} \quad S_{\bar{f}} = \frac{-2r_{D_s K} \sin(\delta + (\gamma - 2\beta_s))}{1 + r_{D_s K}^2}$$

Determine  $\gamma - 2\beta_s$ ,  $\delta$  and  $r_{D_s K} = |\lambda_{D_s K}|$



What do we measure there?

$$\begin{aligned} \arg(\lambda_f) &= \arg\left(\frac{q}{p} \frac{\bar{A}_f}{A_f}\right) \\ &\approx \delta + \arg\left(\frac{V_{tb}^* V_{td}}{V_{tb} V_{td}^*} \frac{V_{ub} V_{cd}^*}{V_{cb}^* V_{ud}}\right) \approx \delta - (\gamma + 2\beta) \end{aligned}$$

$\delta$ : strong phase difference between  $\bar{A}_{D^-\pi^+}$  and  $A_{D^-\pi^+}$

Difference to  $B_s^0 \rightarrow D_s^- K^+$ :

CKM:  $r_{D\pi} \approx 0.02 \Rightarrow C$  indistinguishable from unity

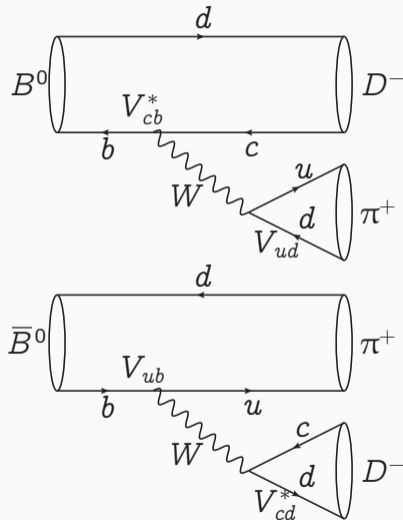
$B^0$  system:  $\Delta\Gamma = 0 \Rightarrow$  No access to  $A_f^{\Delta\Gamma}$

Two observables for three unknowns:

(No CPV in decay and mixing)

$$S_f = \frac{2r_{D\pi} \sin(\delta - (\gamma + 2\beta))}{1 + r_{D\pi}^2} \quad S_{\bar{f}} = \frac{-2r_{D\pi} \sin(\delta + (\gamma + 2\beta))}{1 + r_{D\pi}^2}$$

External input needed to determine  $\gamma + 2\beta$



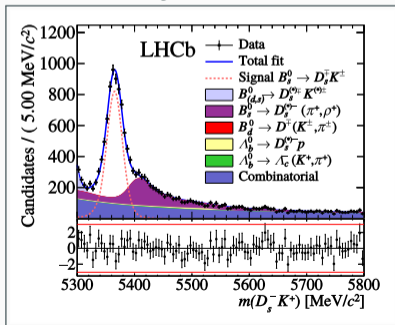
# Analysis of $B_s^0 \rightarrow D_s^\mp K^\pm$

## Advantages:

- Large interference effects
- Additional observables due to  $\Delta\Gamma_s \neq 0$
- Nice control channel:  $B_s^0 \rightarrow D_s^- \pi^+$

## Disadvantages:

- Small yield ( $N_{sig} = 5955 \pm 90$ )



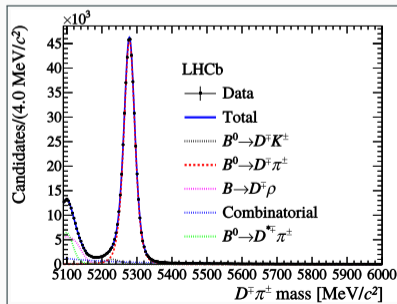
# Analysis of $B^0 \rightarrow D^\mp \pi^\pm$

## Advantages:

- Huge yield ( $N_{sig} = 479.000 \pm 700$ )
- Direct tagging calibration (exploit  $C_f = 1$ )

## Disadvantages:

- Small interference effects
- Less observables

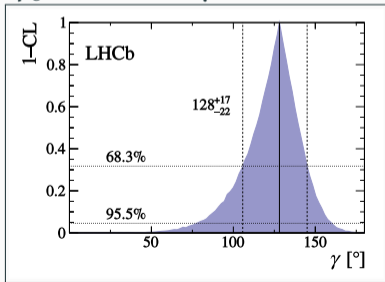


# Analysis of $B_s^0 \rightarrow D_s^\mp K^\pm$

Results: JHEP 03 (2018) 059

$$\begin{aligned}
 C_f &= 0.730 \pm 0.142 \pm 0.045 \\
 A_f^{\Delta\Gamma} &= 0.387 \pm 0.277 \pm 0.153 \\
 A_{\bar{f}}^{\Delta\Gamma} &= 0.308 \pm 0.275 \pm 0.152 \\
 S_f &= -0.519 \pm 0.202 \pm 0.070 \\
 S_{\bar{f}} &= -0.489 \pm 0.196 \pm 0.068
 \end{aligned}$$

Using  $\phi_s$  to extract  $\gamma$ :



# Analysis of $B^0 \rightarrow D^\mp \pi^\pm$

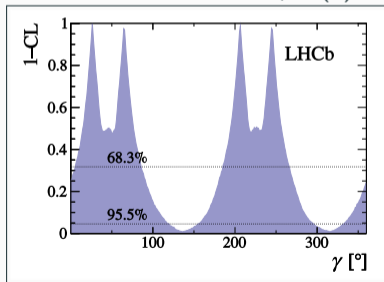
Results: JHEP 06 (2018) 084

$$\begin{aligned}
 S_f &= -0.058 \pm 0.020 \pm 0.011 \\
 S_{\bar{f}} &= -0.038 \pm 0.020 \pm 0.007
 \end{aligned}$$

Extracting  $\gamma$  (using  $2\beta$ ):

Use SU(3) symmetry to estimate  $r_{D\pi}$ :

$$r_{D\pi} = 0.0182 \pm 0.0012 \pm 0.0036 (\text{SU(3) breaking})$$





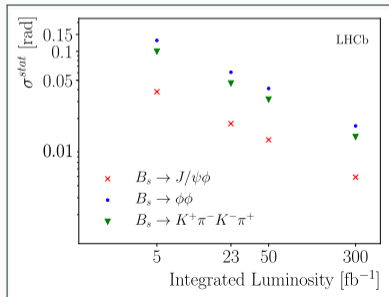
# Summary and outlook

What was presented: Only the most recent time dependent CPV measurements

- SM null-tests:  $B_s^0 \rightarrow \phi\phi$  and  $B_s^0 \rightarrow (K^+\pi^-)(K^-\pi^+) \Rightarrow$  Consistent with SM at  $O(0.1\text{rad})$
- Measurements of CP observables related to combinations of  $\beta$ ,  $\beta_s$  with  $\gamma$ :
  - In  $B_q^0 \rightarrow h^+h^-$  (puts constraints on  $\gamma$  and  $\beta_s$ )
  - In  $B_s^0 \rightarrow D_s^- K^+ \rightarrow 2\sigma$  tension to other  $\gamma$  measurements ( $\gamma \approx (130 \pm 20)^\circ$ )
  - In  $B^0 \rightarrow D^-\pi^+ \rightarrow$  Although not ideal, will add interesting sensitivity

What is to come?

- Updating old measurements:  
( $B_s^0 \rightarrow J/\psi\phi$ ,  $B^0 \rightarrow J/\psi K_s^0$ , ...) with Run II data
- Other interesting new measurements.  
E.g.:  $\gamma$  from  $B_s^0 \rightarrow D_s^\mp K^\pm \pi^+ \pi^-$
- Statistically dominated measurements  $\Rightarrow$  will scale



LHCb-PUB-2018-009

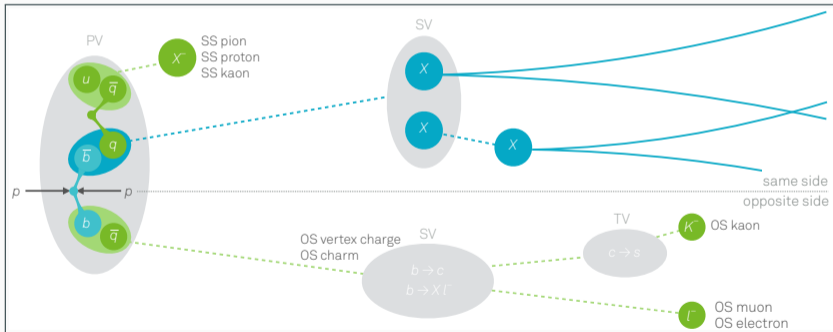
Thanks for your attention!

Backup

# Flavour tagging

Relies on the reconstruction of the rest of the event  $\rightarrow$  Charge of other particles

Classification in **same side** (hadronisation of the signal  $B$ ) and **opposite side** (decay products of the other  $B$ )



Tagging efficiency:  $\epsilon_{tag}$

Mistag probability:  $\omega$

Effective tagging power:

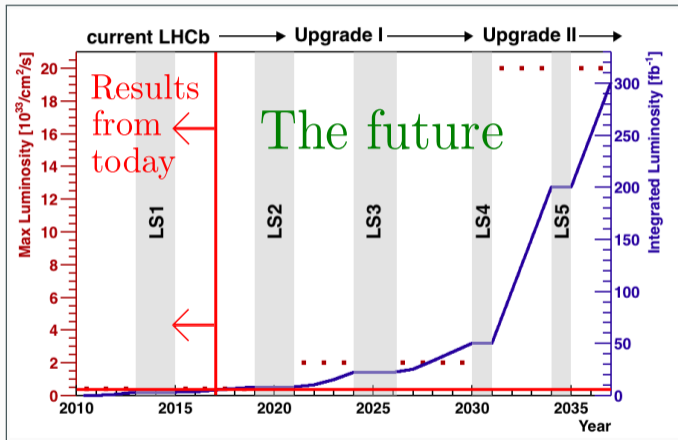
$$\epsilon_{eff} = \epsilon_{tag}(1 - 2\omega)^2$$

$$\sigma^{stat} \propto \frac{1}{\sqrt{\epsilon_{eff} N}}$$

Combining opposite and same sign taggers yields  $\epsilon_{eff}$  of  $O(4 - 6\%)$

# Outlook

What is to come?



For details see:

[LHCb-PUB-2018-009](#)

A teaser:

	Now	$\sigma_{stat}$ @50 $\text{fb}^{-1}$
$\phi_s^{c\bar{c}s}$	0.049 rad	0.0065 rad
$\sin(\phi_d^{c\bar{c}s})$	0.035	0.006
$\Gamma$ from $B_s^0 \rightarrow D_s^\mp K^\pm$	20°	2.5°

Just getting started!