

# Experiments in $(e^-/e^+)$ beam driven PWA

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THANK YOU  
to my colleagues  
of the *E-167* Collaboration:

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*Stanford Linear Accelerator Center*

D. Auerbach, C. E. Clayton, C. Huang, C. Joshi, K. A. Marsh, W. B. Mori, W. Lu, M. Zhou

*University of California, Los Angeles*

T. Katsouleas, E. Oz, P. Muggli

*University of Southern California*

and of the *E-157/162/164/164X* Collaborations

and

M. Babzien, K. Kusche, J. Park, D. Stolyarov, V. Yakimenko

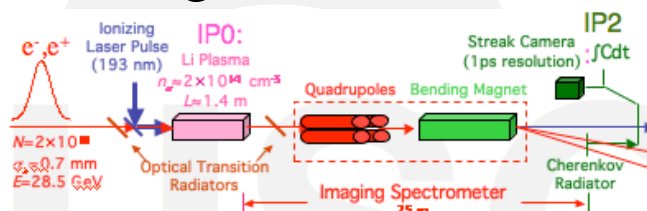
*Brookhaven National Laboratory, Upton, Long Island, NY*

# OUTLINE

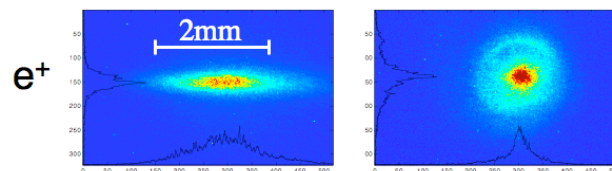
- ◆ Plasma Wakefield Accelerator (PWFA) for  $e^+$



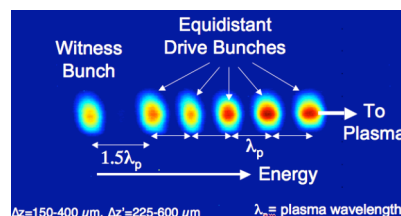
- ◆ Experimental Setup & Diagnostics



- ◆ Experimental results for  $e^-$  &  $e^+$  bunches (SLAC)



- ◆ Multi-bunch PWFA (ATF)



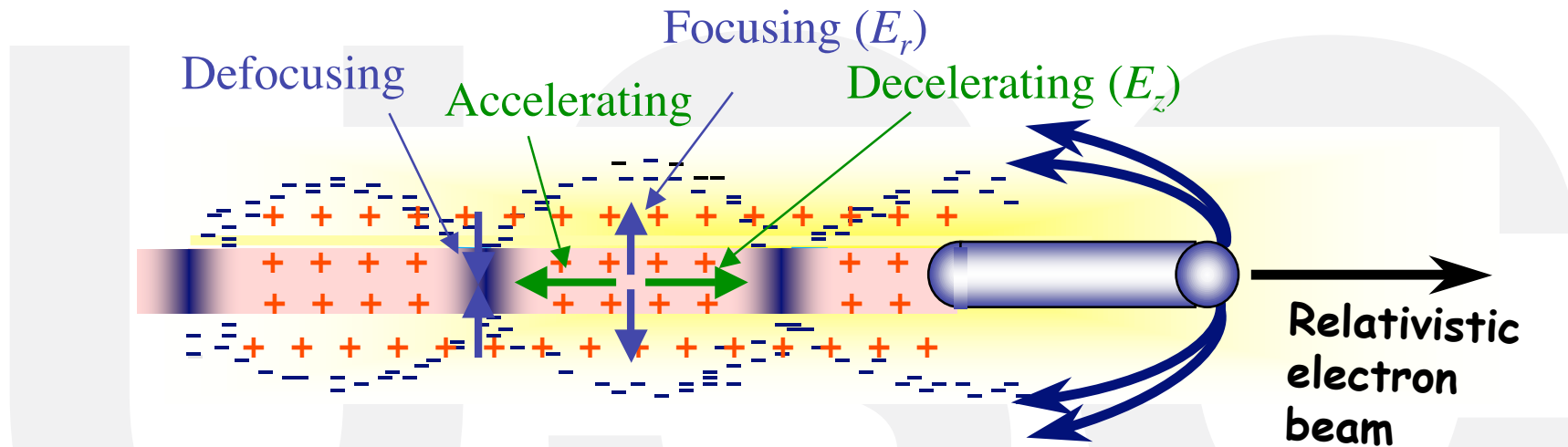
- ◆ Conclusions

Review of High-energy Plasma Wakefield Experiments

P. Muggli and M.J. Hogan, Comptes Rendus Physique, 10(2-3), 116 (2009).

# PLASMA WAKEFIELD ACCELERATOR\* 101

- ◆ Two-beam, co-linear, plasma-based accelerator

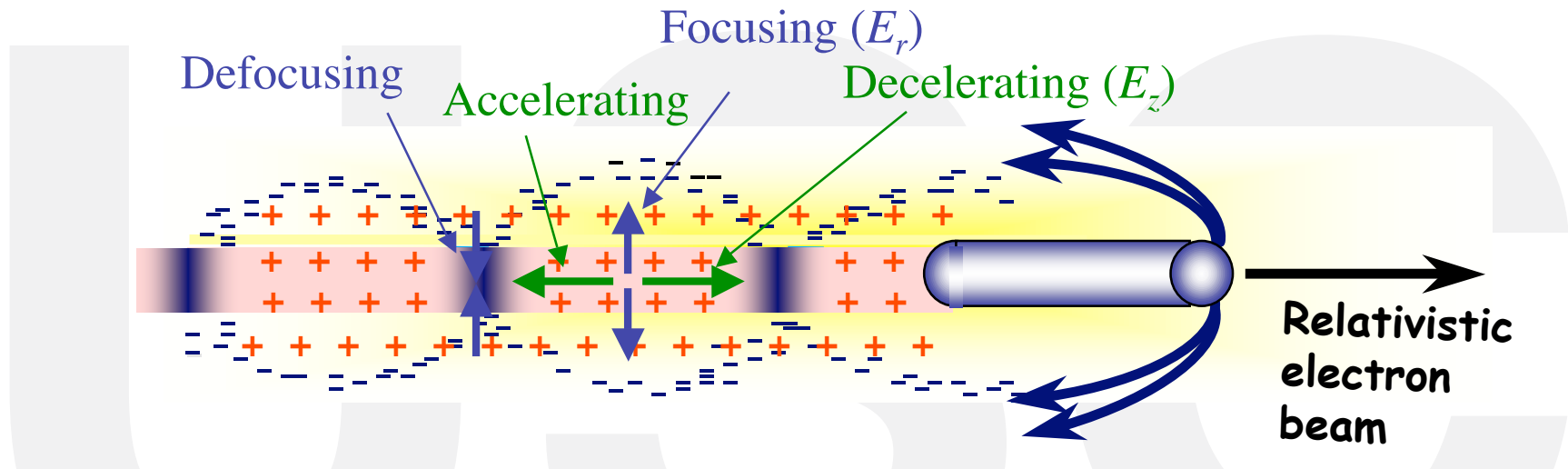


- ◆ Deceleration, acceleration, focusing by plasma
- ◆ Accelerating field/gradient scales as  $n_e^{1/2}$
- ◆ Typical:  $n_e \approx 10^{16}-10^{17} \text{ cm}^{-3}$ ,  $\lambda_p \approx 150 \text{ } \mu\text{m}$ ,  $f_p \approx 2 \text{ THz}$ ,  $E > 10 \text{ GV/m}$
- ◆ High-gradient, high-efficiency energy transformer



# PLASMA WAKEFIELD ACCELERATOR\* 101

- ◆ Two-beam, co-linear, plasma-based accelerator

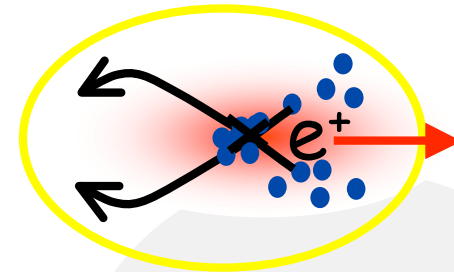
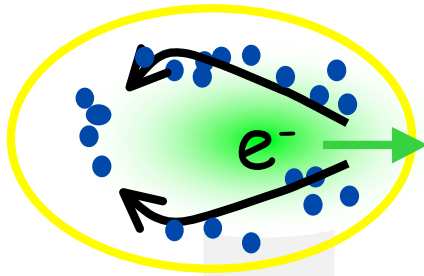


Single bunch experiments:  
Bunch ( $e^-/e^+$ ) covers all phases of the “rf” wave  
or wake

Ultra-relativistic  $e^-$  ( $\gamma=50,000$ ) “don’t” dephase ...

# $e^-$ & $e^+$ BEAM PWFA

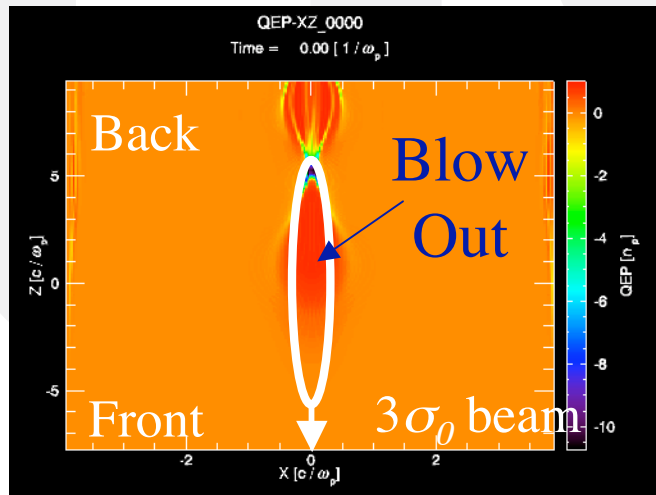
- ◆ Transverse dynamics, emittance preservation?



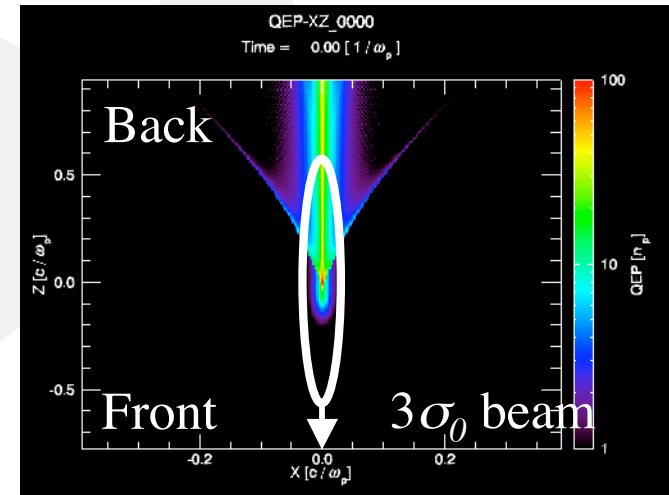
3-D QuickPIC simulations, plasma  $e^-$  density:

$e^-$ :  $n_{e0} = 2 \times 10^{14} \text{ cm}^{-3}$ ,  $c/\omega_p = 375 \text{ } \mu\text{m}$

$e^+$ :  $n_{e0} = 2 \times 10^{12} \text{ cm}^{-3}$ ,  $c/\omega_p = 3750 \text{ } \mu\text{m}$



$\sigma_r = 35 \text{ } \mu\text{m}$   
 $\sigma_z = 700 \text{ } \mu\text{m}$   
 $N = 1.8 \times 10^{10}$   
 $L = 2 \text{ mm}$

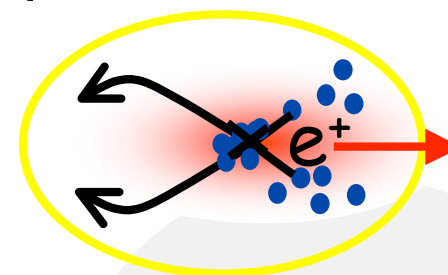
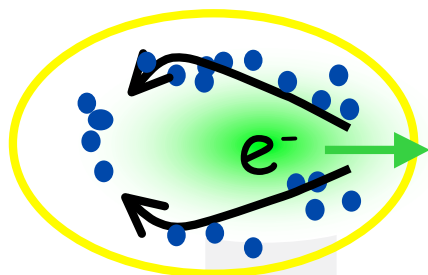


- Uniform focusing force ( $r, z$ )
- Free of geometric aberrations
- Emittance preserved

- Non-uniform focusing force ( $r, z$ )
- Emittance growth?

# $e^-$ & $e^+$ BEAM PWFA

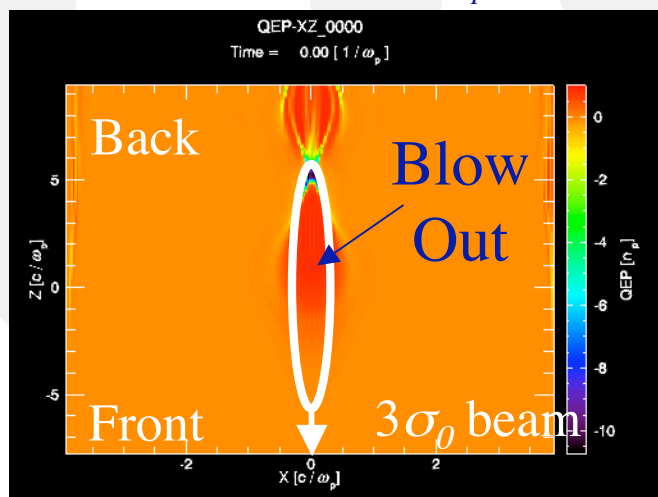
- ◆ Transverse dynamics, emittance preservation?



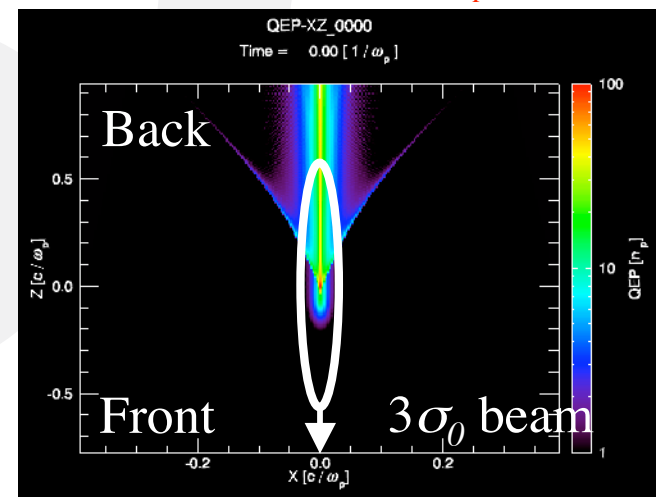
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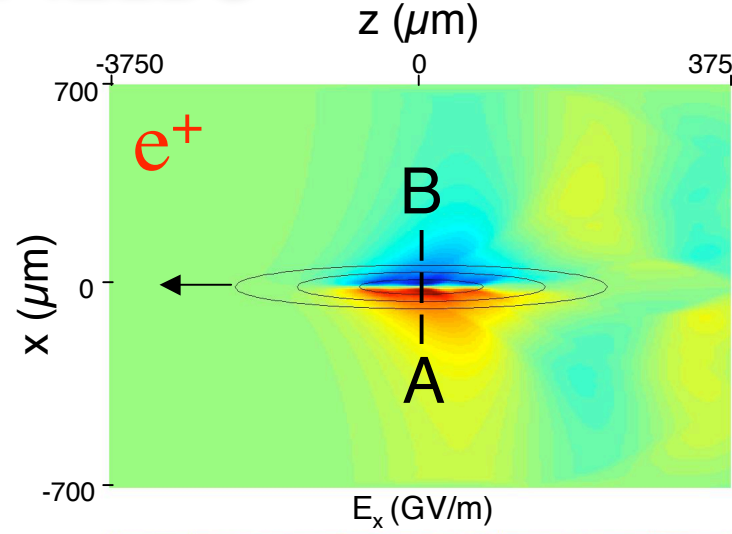
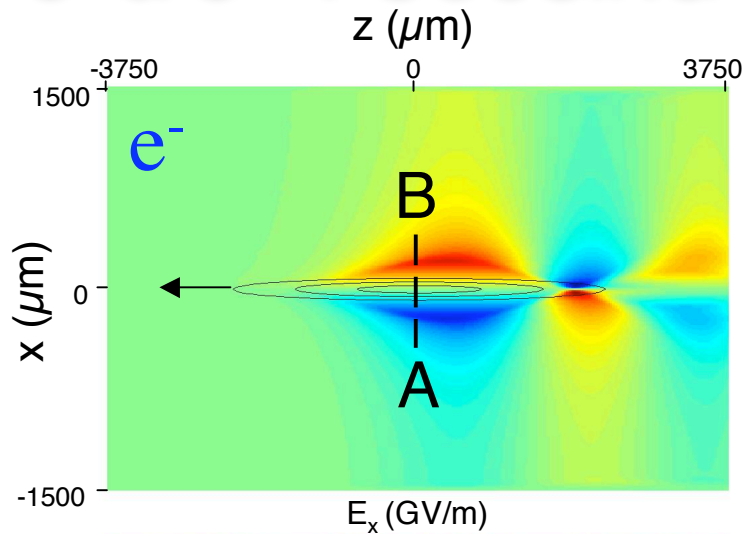


Proton beams in plasmas  $\Leftrightarrow$  Positron beams in plasmas

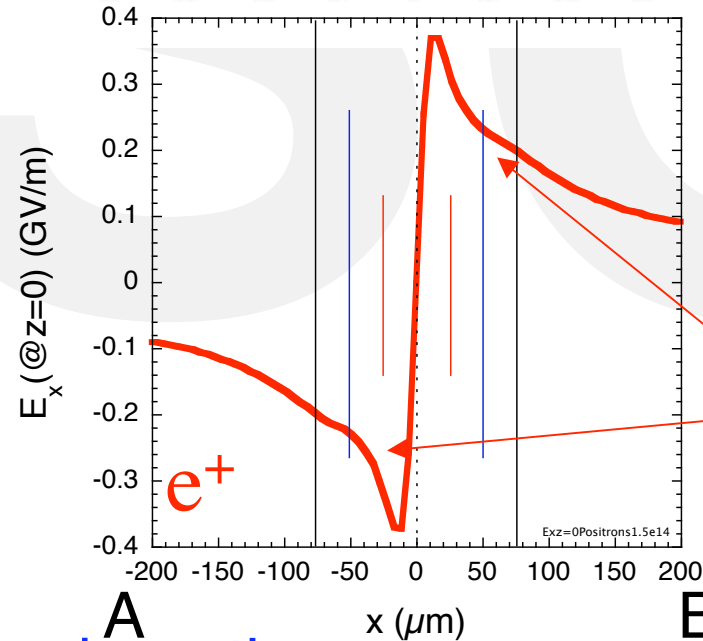
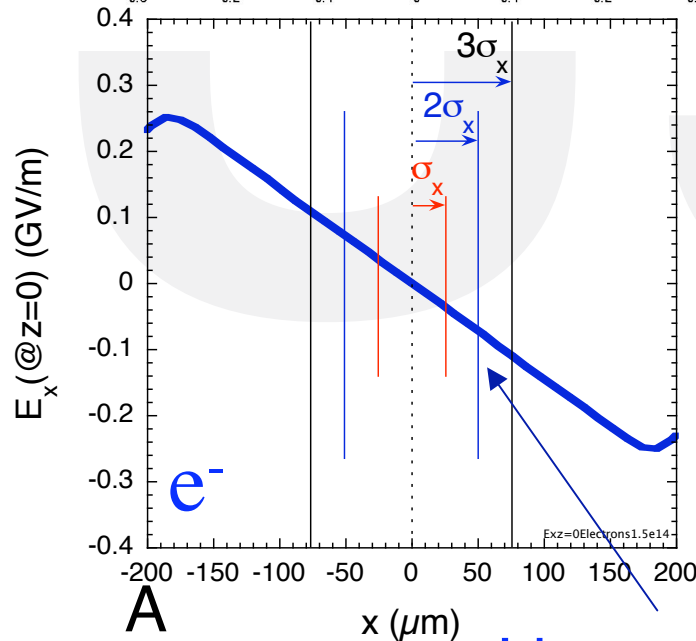
Witness bunch

Drive bunch

# $e^-$ & $e^+$ FOCUSING FIELDS



QuickPIC  
 $\sigma_{x0} = \sigma_{y0} = 25 \mu\text{m}$   
 $\sigma_z = 730 \mu\text{m}$   
 $N = 1.9 \times 10^{10} e^+/e^-$   
 $n_e = 1.5 \times 10^{14} \text{ cm}^{-3}$

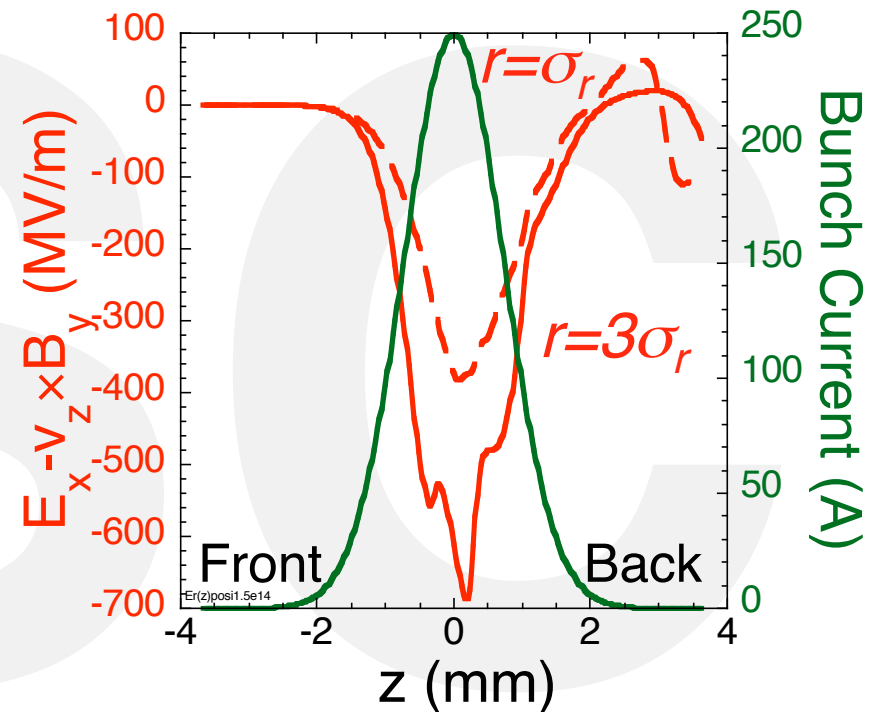
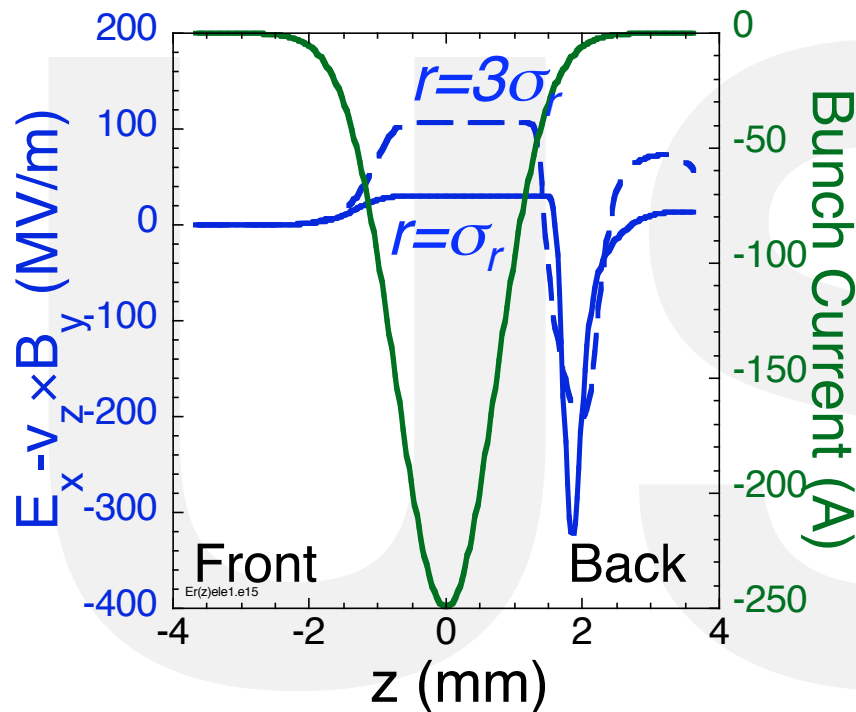


Non-linear,  
aberrations

Linear, no aberrations

# $e^-$ & $e^+$ FOCUSING FIELDS

QuickPIC:  $\sigma_{x0} \approx \sigma_{y0} \approx 25 \mu\text{m}$ ,  $\varepsilon_{Nx} \approx 390 \times 10^{-6}$ ,  $\varepsilon_{Ny} \approx 80 \times 10^{-6}$  m-rad,  $N = 1.9 \times 10^{10}$   $e^+$ ,  
 $\sigma_z \approx 730 \mu\text{m}$ ,  $n_e = 1.5 \times 10^{-6}$ ,  $L \approx 1.1$  cm

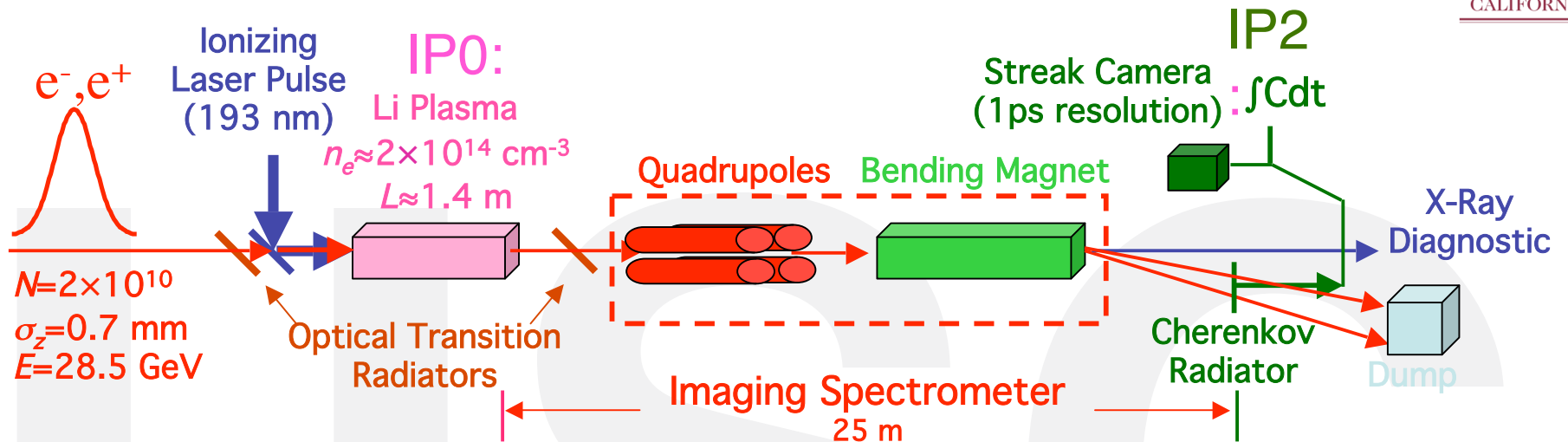


- Uniform focusing force ( $r, z$ )
- Weaker focusing force

- Non-uniform focusing force ( $r, z$ )
- Stronger focusing force

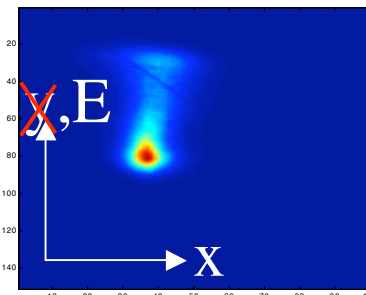
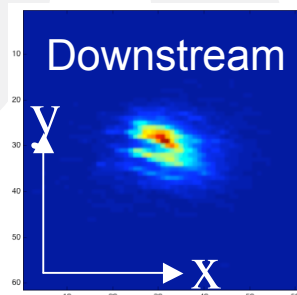
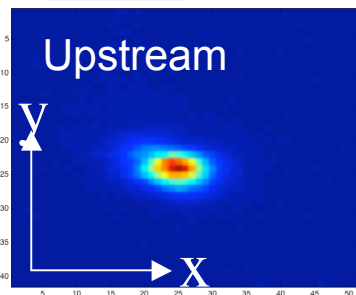
- ◆  $e^+$ : focusing fields vary along  $r$  and  $z$ !
- ◆ Emittance growth expected

# EXPERIMENTAL SET UP



• Optical Transition Radiation (OTR)

• CHERENKOV (aerogel)



- 1:1 imaging, spatial resolution  $< 9 \mu\text{m}$

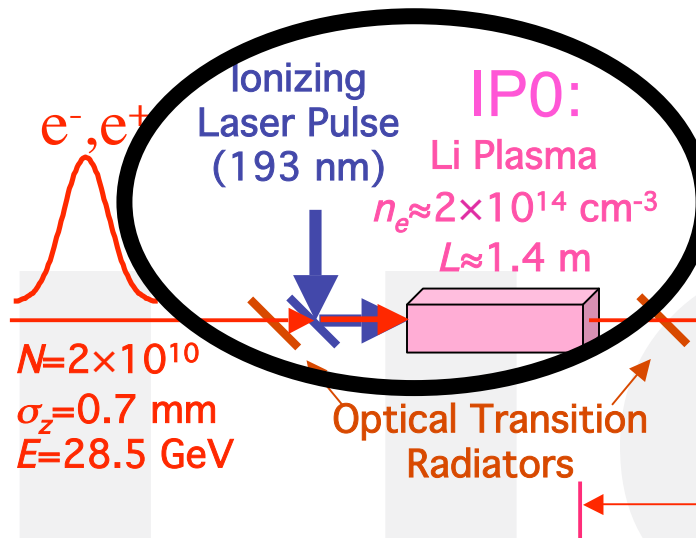
- Spatial resolution  $\approx 100 \mu\text{m}$

- Energy resolution  $\approx 30 \text{ MeV}$

- Time resolution:  $\approx 1 \text{ ps}$



# EXPERIMENTAL SET UP



Plasma:

Lithium vapor in heat-pipe oven

$\phi_1 = 5.4 \text{ eV}$ ,  $\phi_2 = 75.6 \text{ eV}$

Laser-ionized,  $\lambda = 157 \text{ nm}$  (excimer)

-variable density

Field ionized,  $E > 6 \text{ GV/m}$ ,  $\sim 100 \text{ fs}$

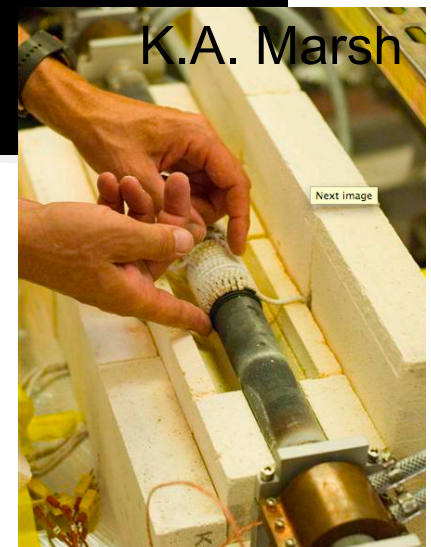
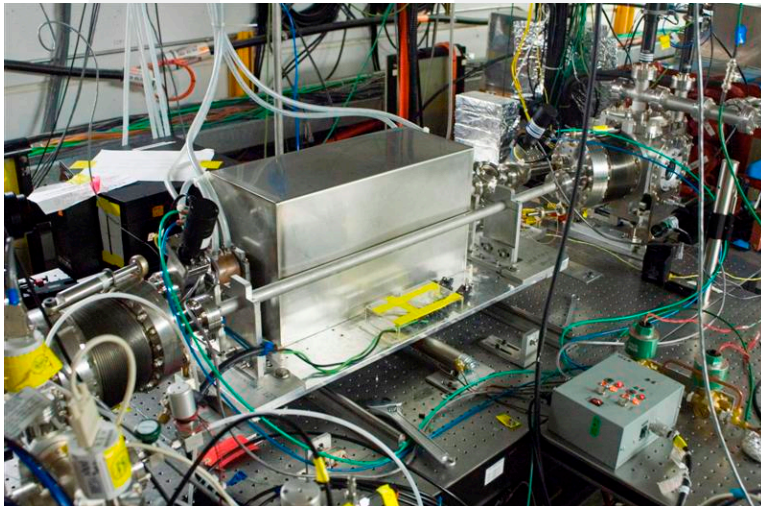
-need ON/OFF

-long time constant

Variable length

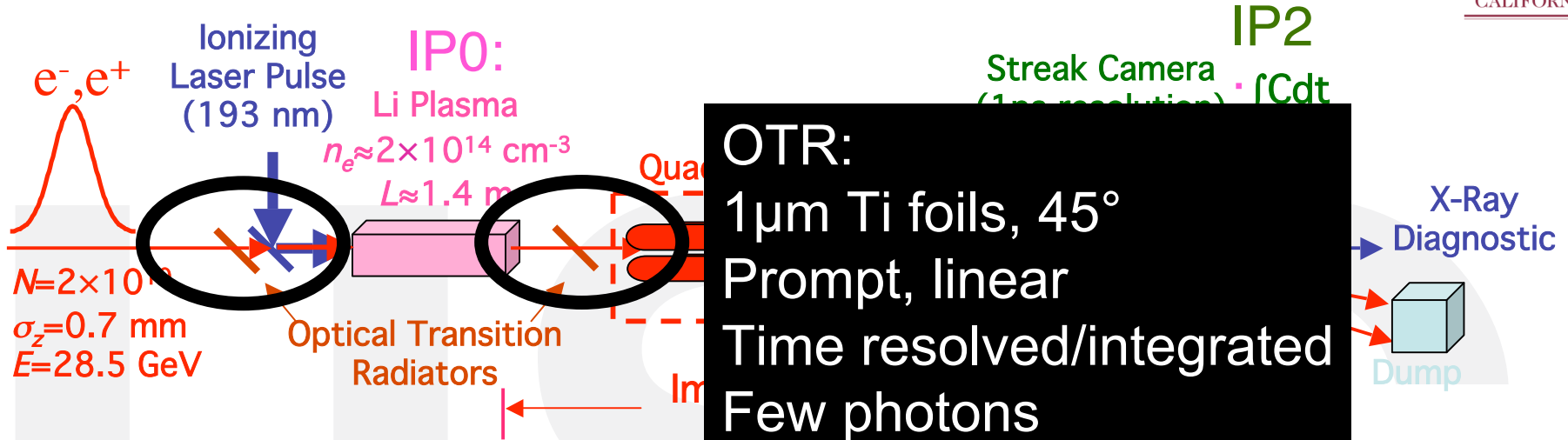
Field-free

Very reproducible



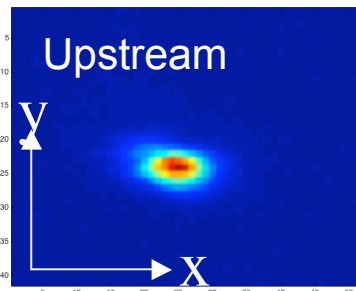
P. Muggli et al., IEEE Trans. on Plasma Science 27(3), pp. 791-799 (1999).

# EXPERIMENTAL SET UP

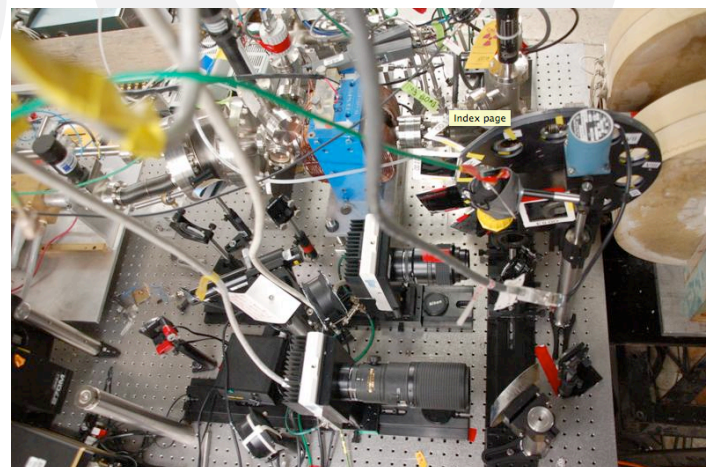
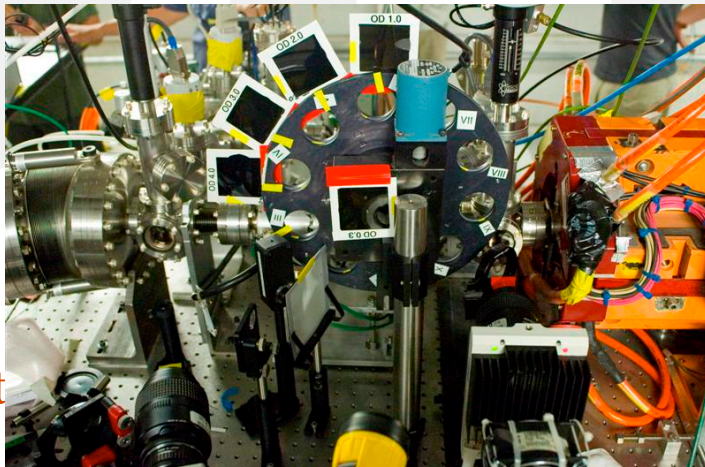


**OTR:**  
 1  $\mu\text{m}$  Ti foils, 45°  
 Prompt, linear  
 Time resolved/integrated  
 Few photons  
 ~  $\mu\text{m}$  resolution  
 Before and after plasma

- Optical Transition Radiation (OTR)

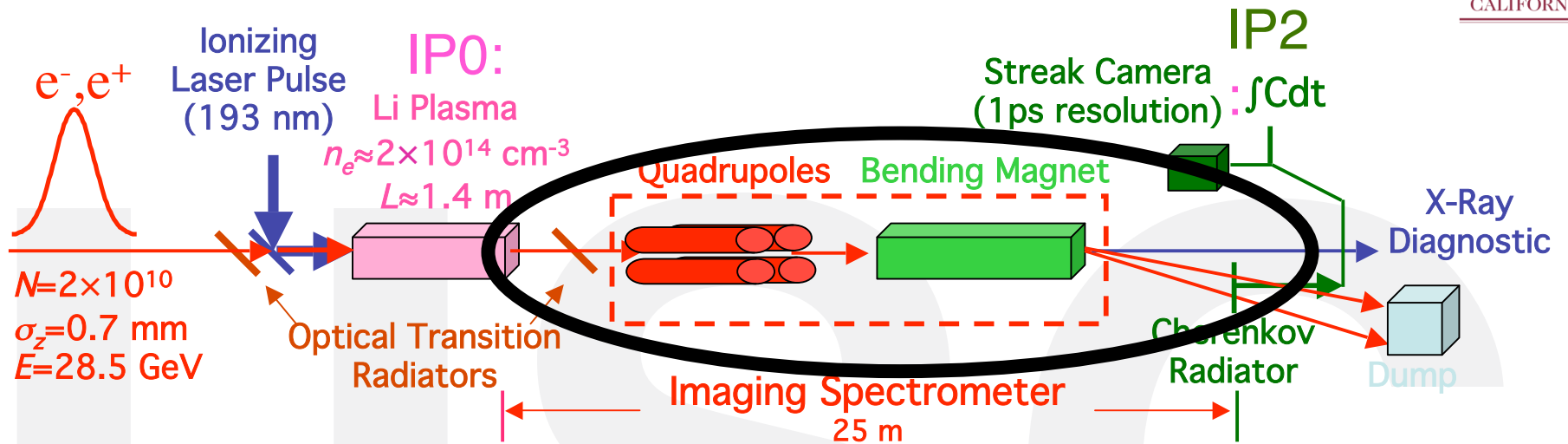


- 1:1 imaging, spat



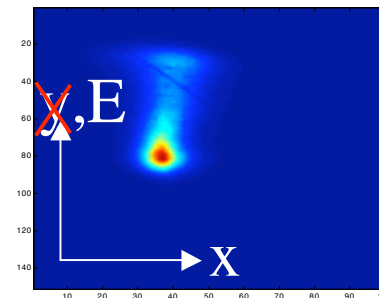


# EXPERIMENTAL SET UP



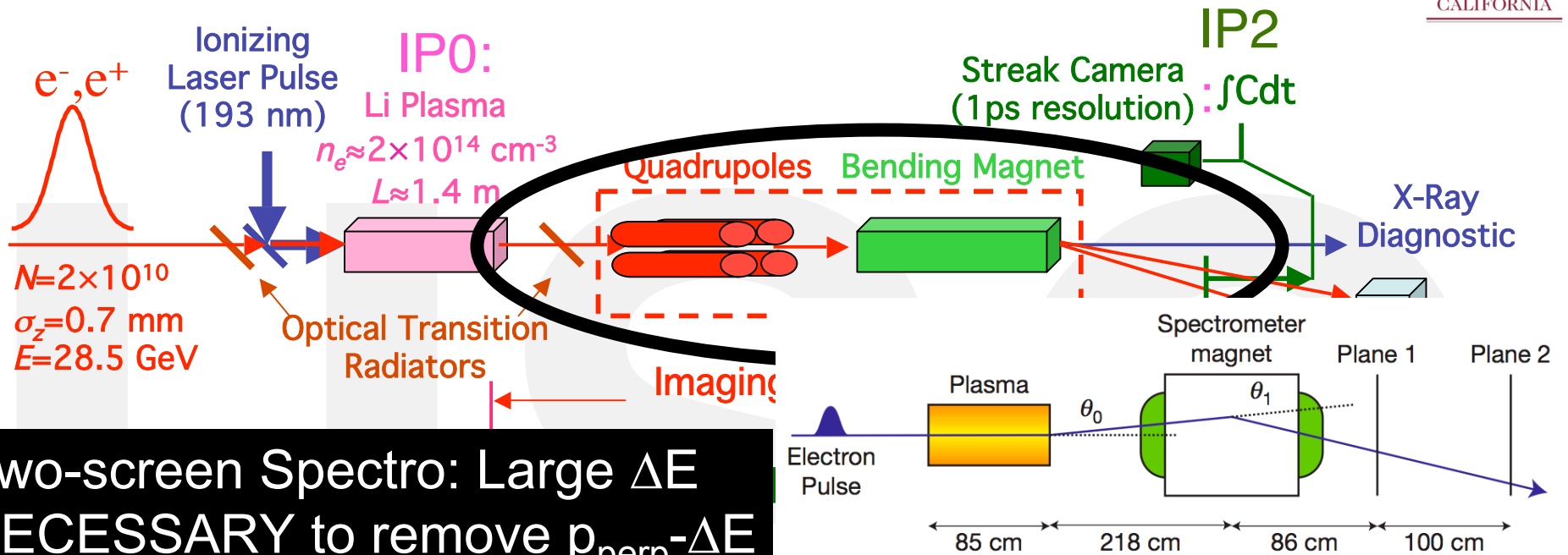
Imaging Spectrometer: Small  $\Delta E$   
Transverse field  $\sim$  Longitudinal fields  
**NECESSARY** to remove  $p_{\text{perp}} - \Delta E$   
ambiguity  
 $\beta_y \varepsilon_y \ll (\eta_y \Delta E / E_0)^2$

- **CHERENKOV** (aerogel)

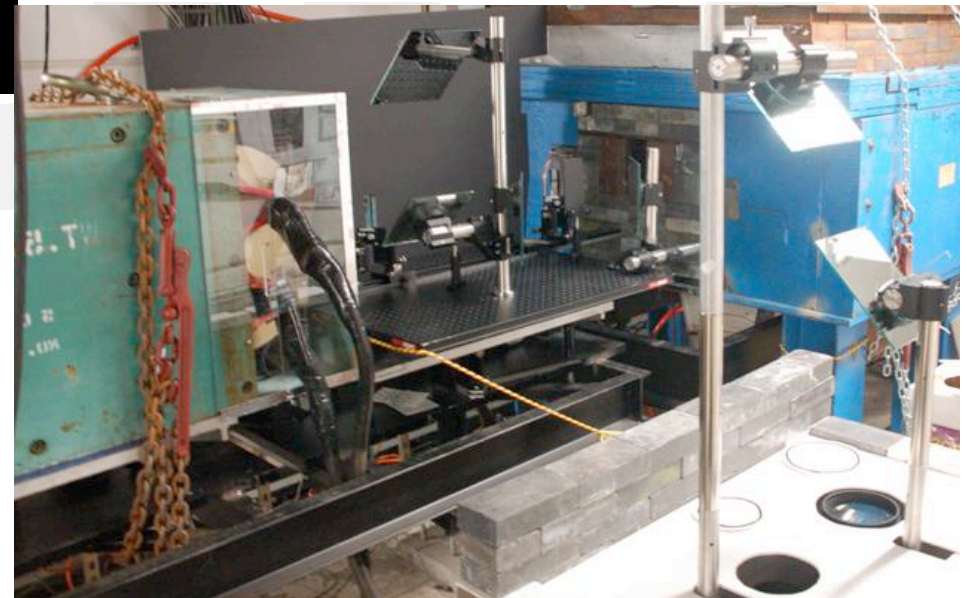
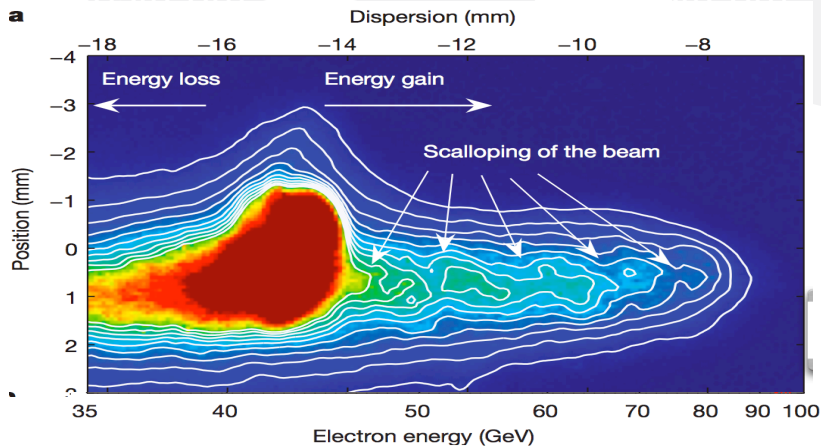


- Spatial resolution  $\approx 100 \mu\text{m}$
- Energy resolution  $\approx 30 \text{ MeV}$
- Time resolution:  $\approx 1 \text{ ps}$

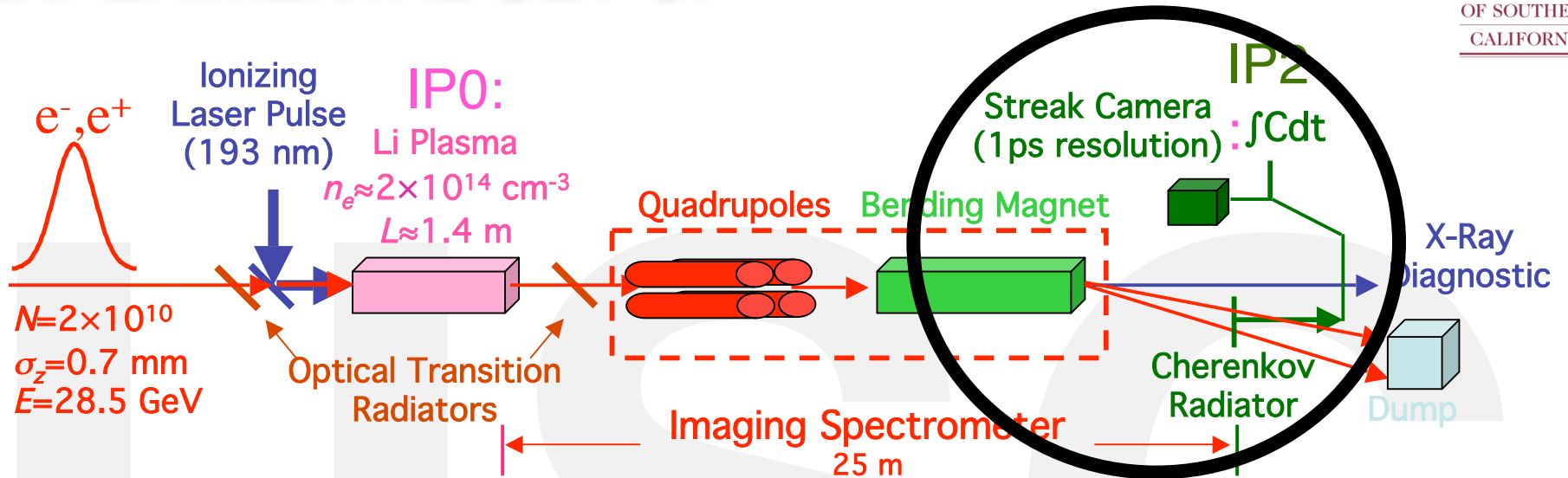
# EXPERIMENTAL SET UP



Two-screen Spectro: Large  $\Delta E$  NECESSARY to remove  $p_{\text{perp}} - \Delta E$  ambiguity



# EXPERIMENTAL SET UP



Cherenkov Radiator:  
Aerogel,  $n=1.009$ ,  $\theta_c \approx 8^\circ$

Many photons

-beam large-x, dispersed-y

Prompt, linear

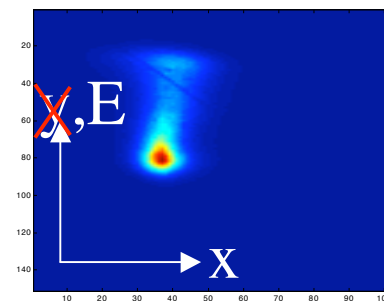
Time resolved/integrated

Emit in a cone:  $\cos\theta_c \approx 1/n$

Limited spatial/energy resolution

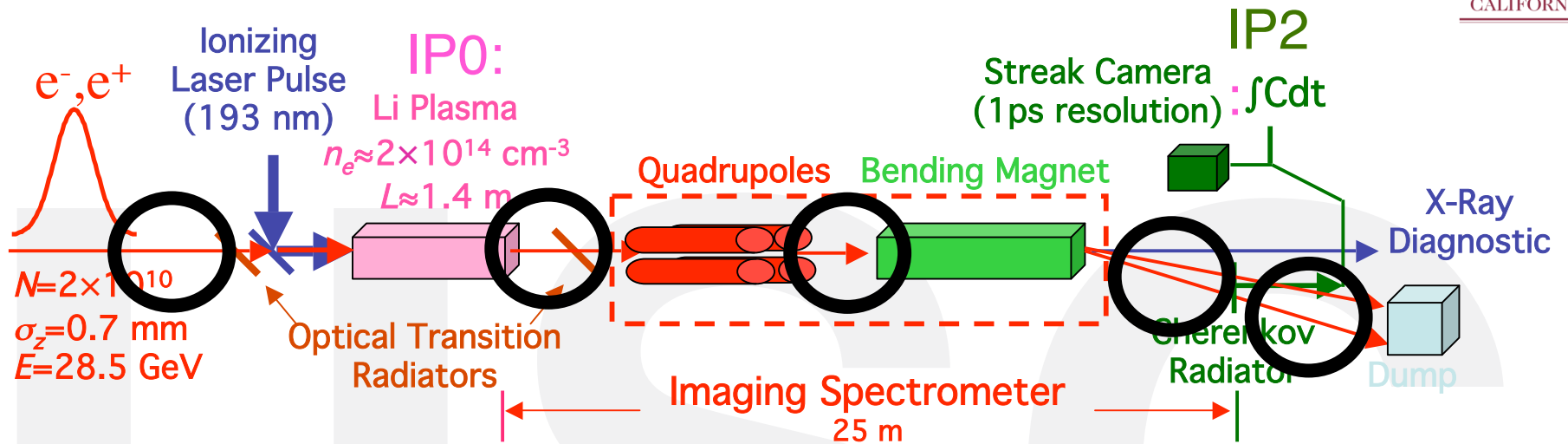
$$\Delta r = L * \cos\theta_c$$

- **CHERENKOV** (aerogel)



- Spatial resolution  $\approx 100 \mu\text{m}$
- Energy resolution  $\approx 30 \text{ MeV}$
- Time resolution:  $\approx 1 \text{ ps}$

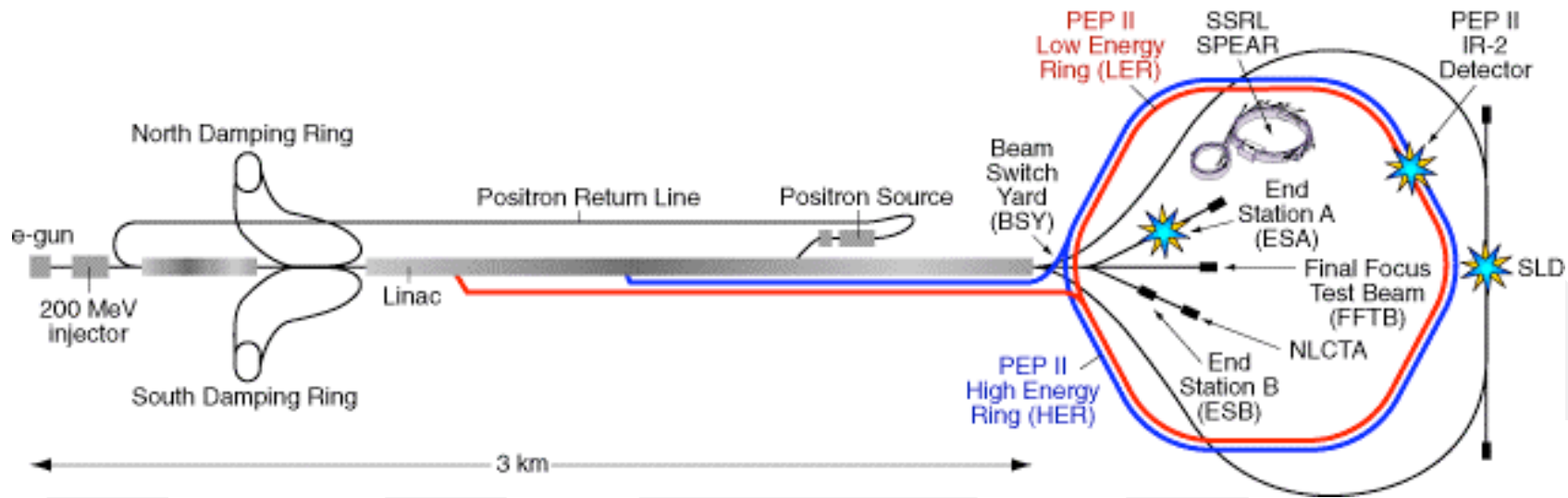
# EXPERIMENTAL SET UP



Beamline diagnostics:  
As many as possible  
BPM, wires, OTRs, etc.

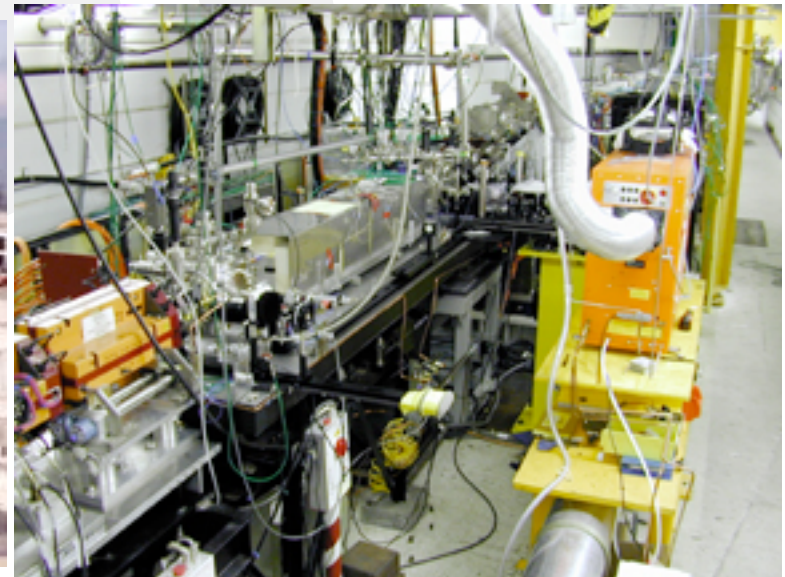


# PLASMA WAKEFIELD EXPERIMENT @ SLAC

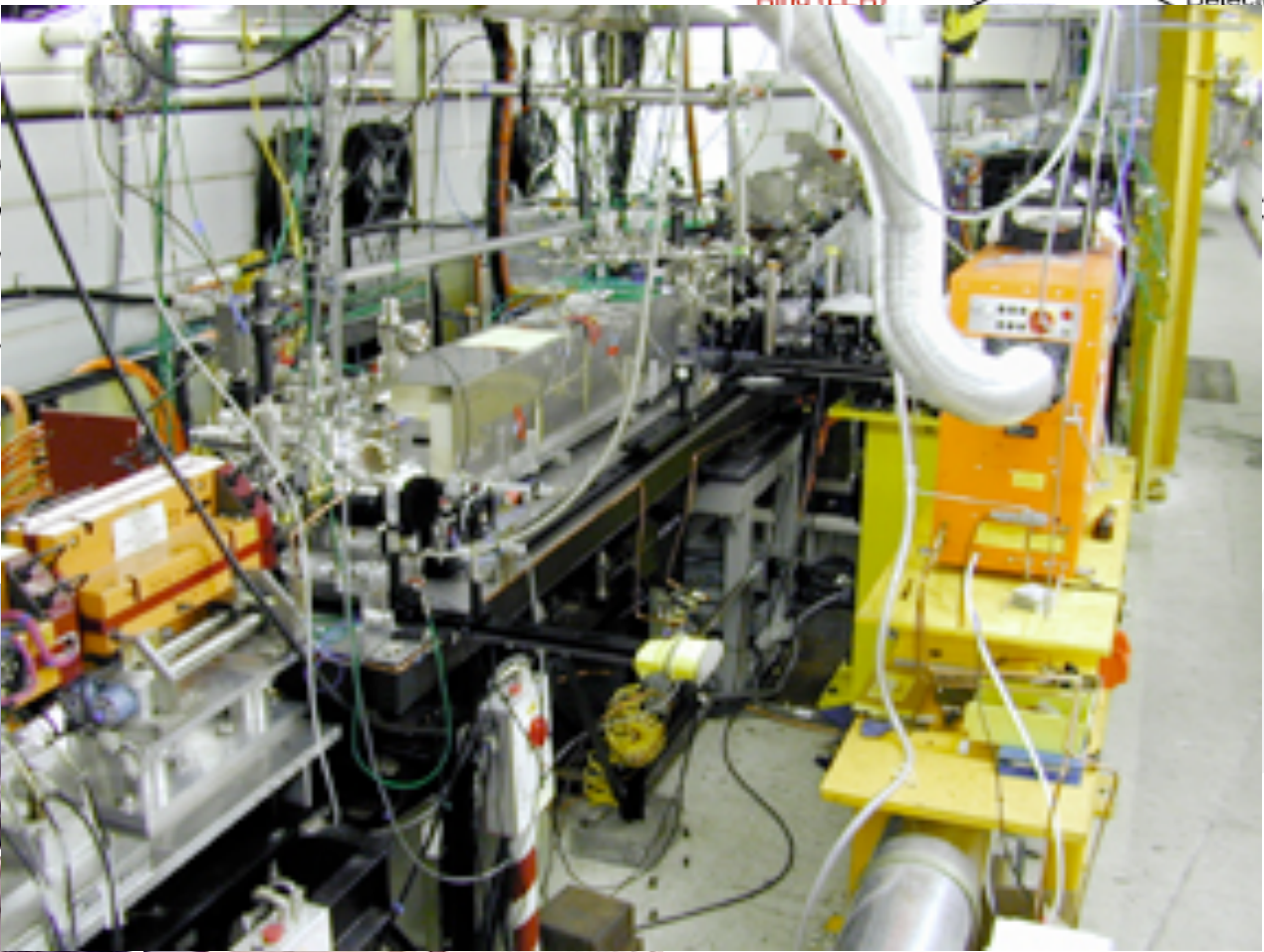
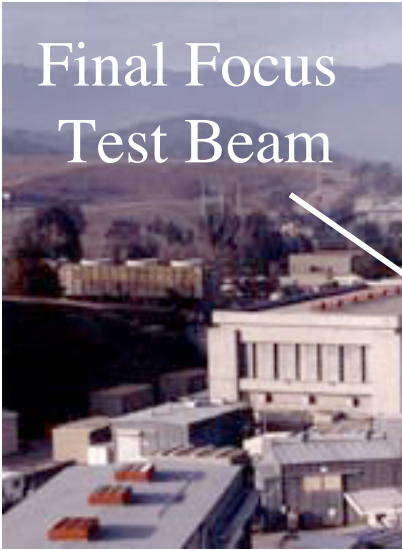


3 km for 50 GeV

1 m for 1 GeV?



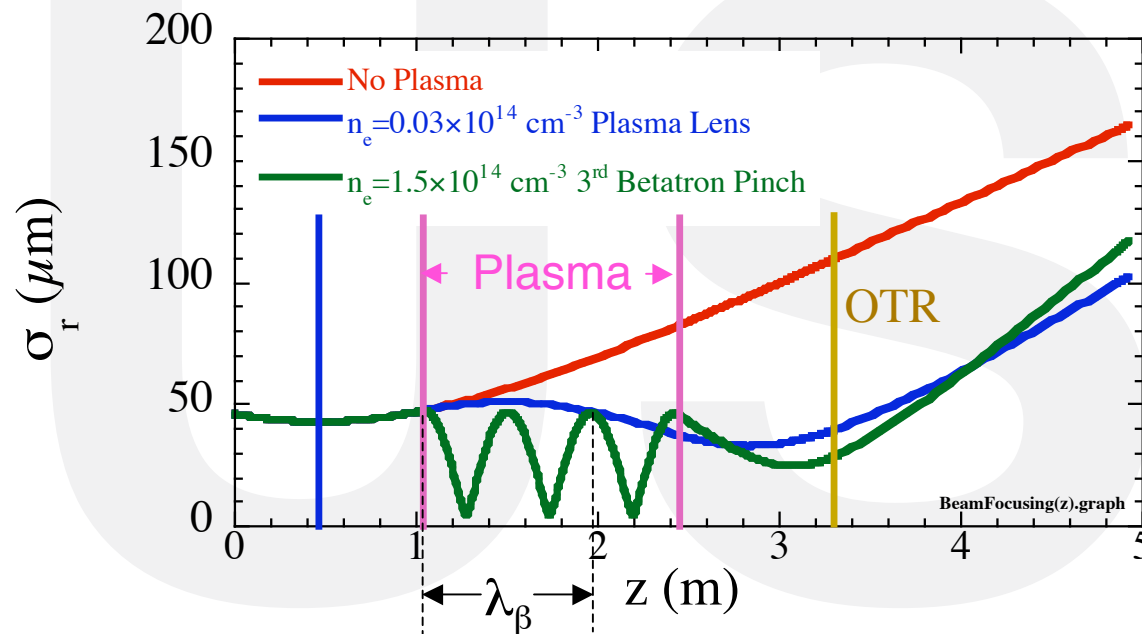
# PLASMA WAKEFIELD EXPERIMENT @ SLAC



# PLASMA FOCUSING OF $e^-$

## Beam Envelope Model for Plasma Focusing

Plasma Focusing Force > Beam "Emittance Force"  
 $(\beta_{beam} = 1/K > \beta_{plasma})$



Envelope equation:

$$\frac{\partial^2 \sigma}{\partial z^2} + K^2 \sigma = \frac{\epsilon^2}{\sigma^3}$$

In an ion channel:

$$K = \frac{\omega_{pe}}{\sqrt{2}\gamma c} \propto (n_e)^{1/2}$$

with a focusing strength

$$W = \frac{E_r}{rc} = \frac{B_\theta}{r} = \frac{1}{2} \frac{n_e e}{\epsilon_0 c}$$

$$= 6 \text{ kT/m}$$

$$@ n_e = 2 \times 10^{14} \text{ cm}^{-3}$$

- ➡ Multiple foci (betatron oscillation) within the plasma
- ➡  $\sigma_{x,y}(z)$  at fixed  $n_e \Rightarrow \sigma_{x,y}(n_e)$  at fixed  $z$

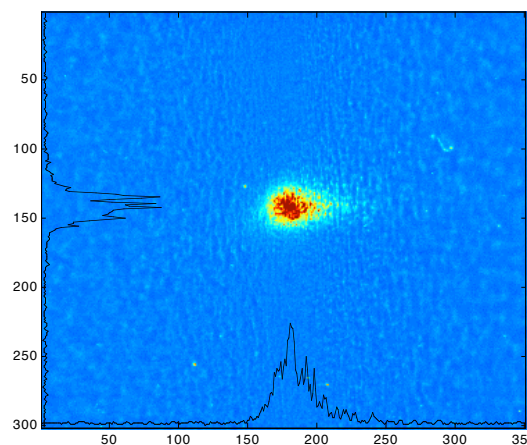
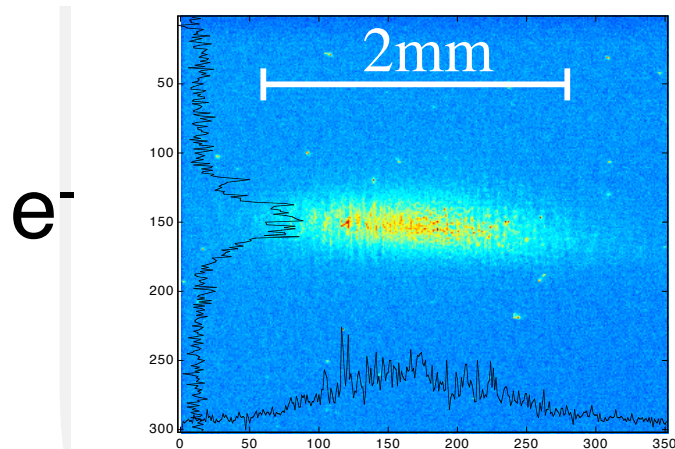


# FOCUSING OF $e^-/e^+$

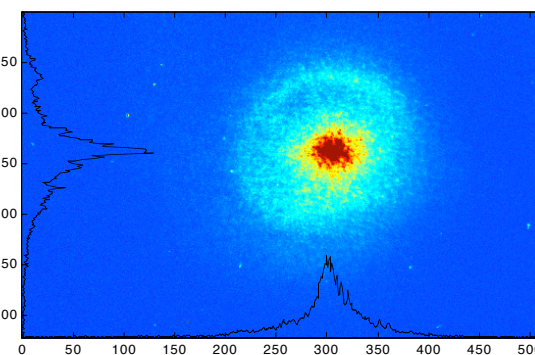
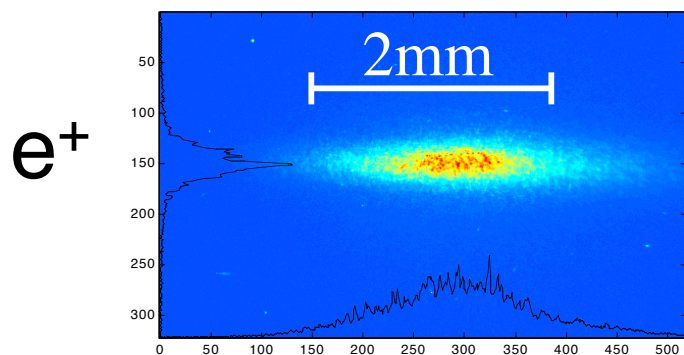
- ◆ OTR images  $\approx 1$  m from plasma exit ( $\varepsilon_x \neq \varepsilon_y$ )
- ◆ Single bunch experiments

$n_e = 0$

$n_e \approx 10^{14} \text{ cm}^{-3}$



- Ideal Plasma Lens in Blow-Out Regime



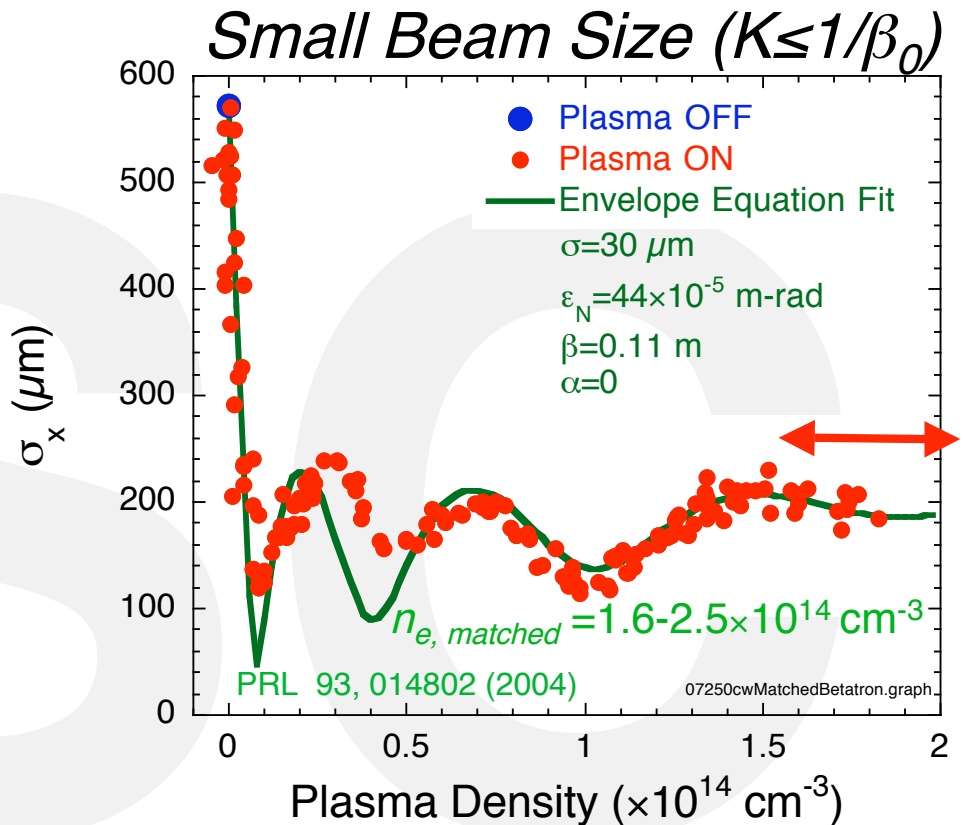
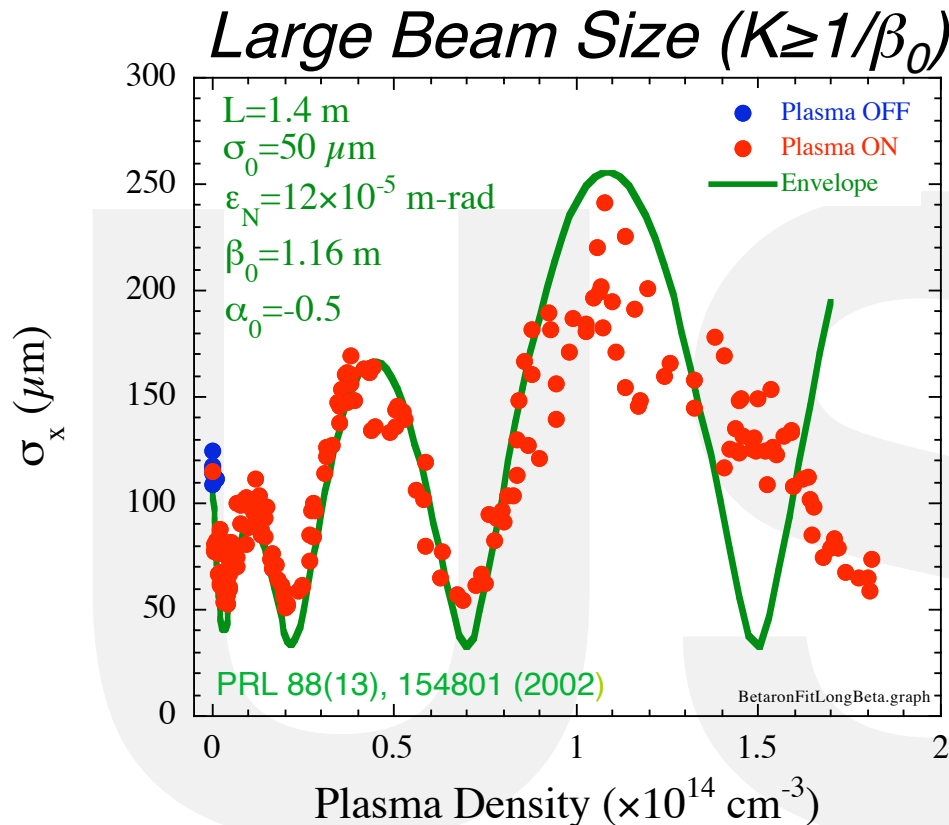
- Plasma Lens with Aberrations, Halo

- ◆ Qualitative differences



# FOCUSING OF $e^-$

OTR Images  $\approx 1\text{m}$  downstream from plasma



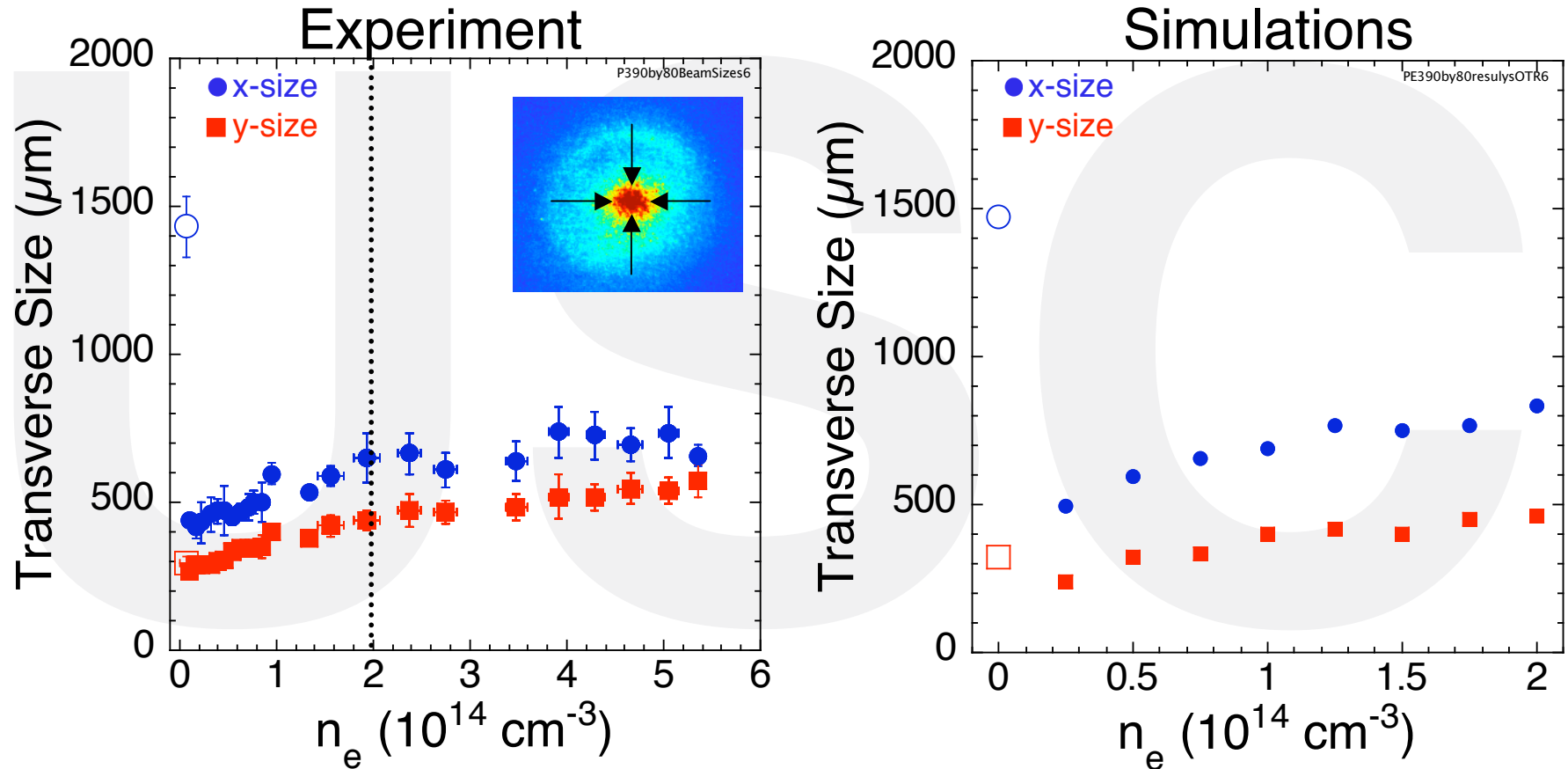
- ➡ Focusing of the beam well described by a simple model ( $n_b > n_e$ ): **Plasma = Ideal Thick Lens**
- ➡ No emittance growth observed as  $n_e$  is increased
- ➡ Stable propagation over  $L=1.4\text{ m}$  up to as  $n_e=1.8 \times 10^{14}\text{ cm}^{-3}$
- ➡ Channeling of the beam over  $1.4\text{ m}$  or  $>12\beta_0$

**=> Matched Propagation over long distance!**

# EXPERIMENT/SIMULATIONS: BEAM SIZE

$$\sigma_{x0}=\sigma_{y0}=25\mu\text{m}, \varepsilon_{Nx}=390\times 10^{-6}, \varepsilon_{Ny}=80\times 10^{-6} \text{ m-rad}, N=1.9\times 10^{10} \text{ e}^+, L=1.4 \text{ m}$$

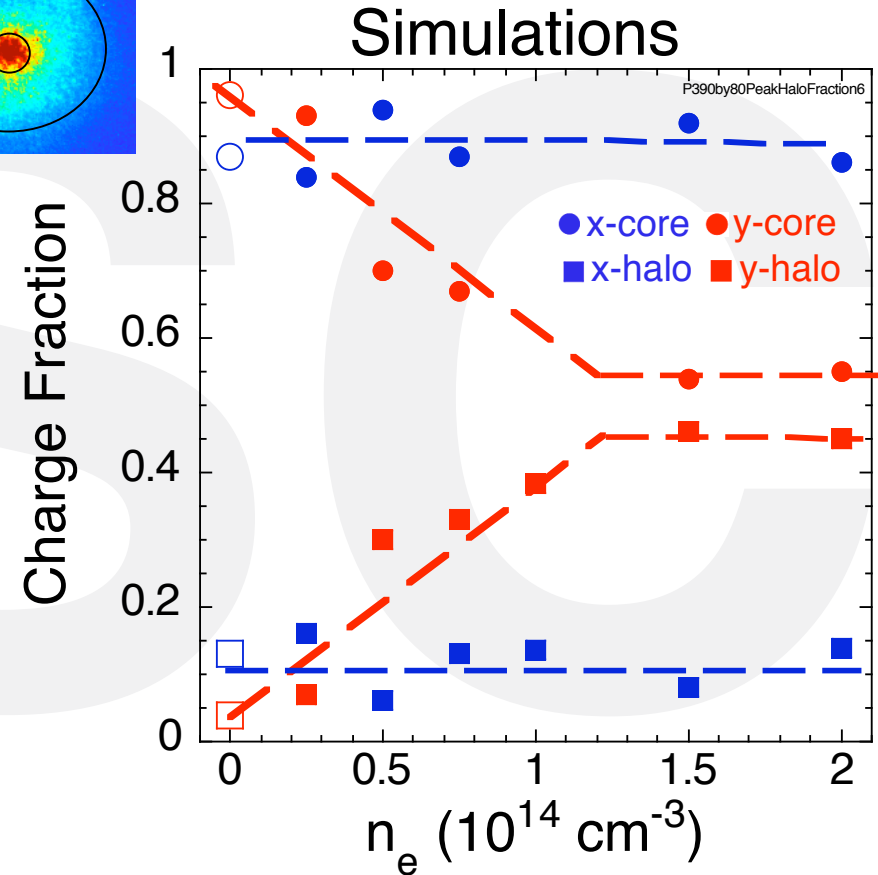
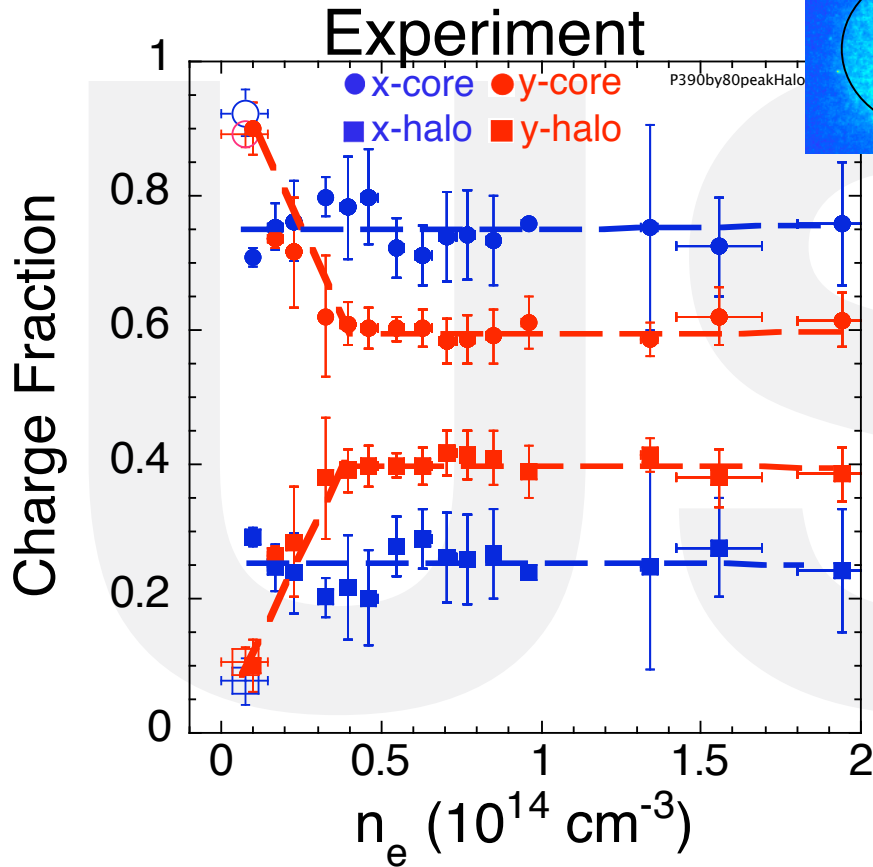
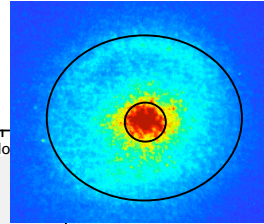
## Downstream OTR



- ◆ Excellent experimental/simulation results agreement!
- ◆ The beam is  $\approx$ round with  $n_e \neq 0$

# EXPERIMENT/SIMULATIONS: HALO FORMATION

$$\sigma_{x0} \approx \sigma_{y0} \approx 25 \mu\text{m}, \quad \varepsilon_{Nx} \approx 390 \times 10^{-6}, \quad \varepsilon_{Ny} \approx 80 \times 10^{-6} \text{ m-rad}, \quad N = 1.9 \times 10^{10} e^+, \quad L \approx 1.4 \text{ m}$$

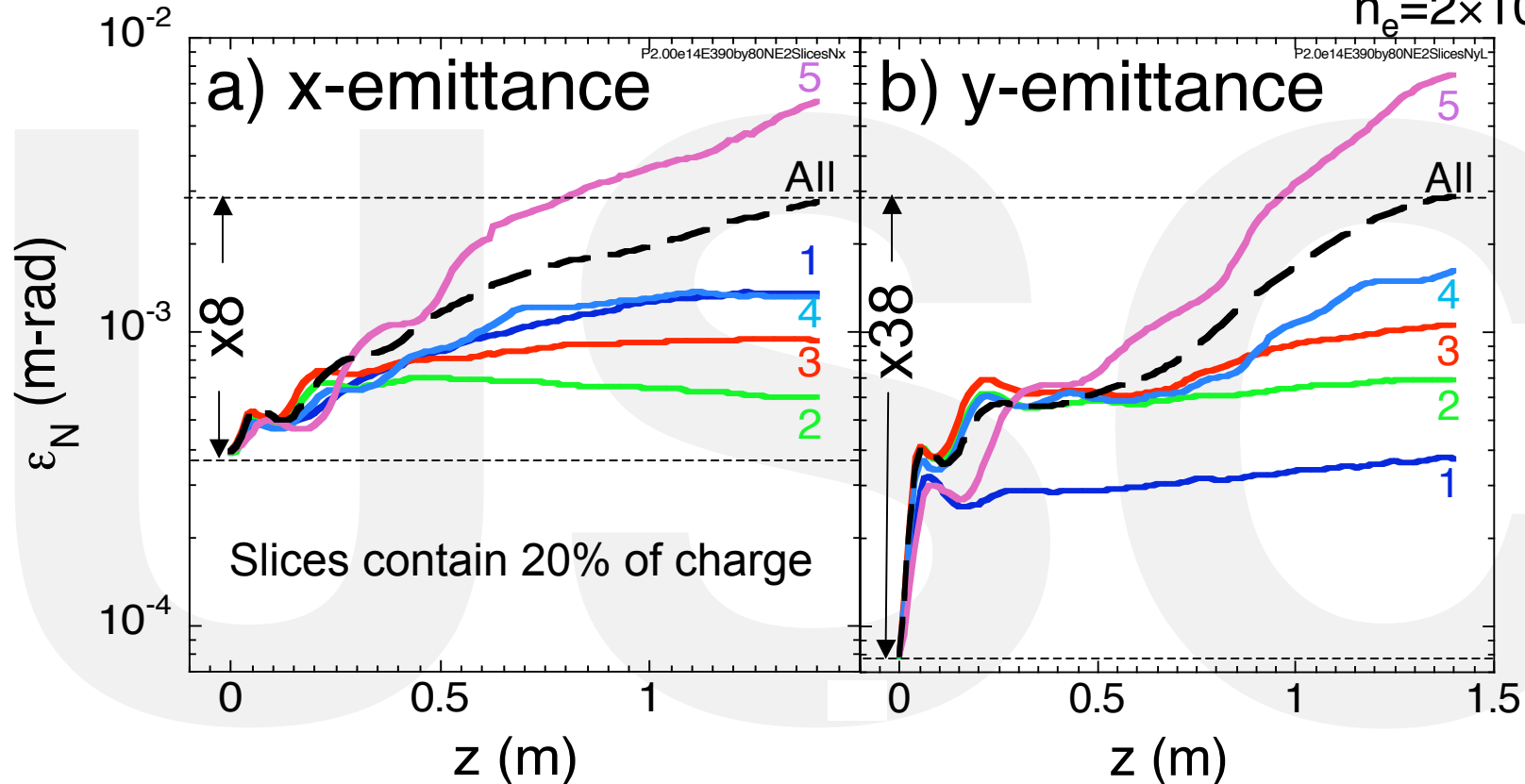


- ◆ Very nice qualitative agreement
- ◆ Simulations to calculate emittance

# $e^+$ : SLICE EMITTANCE (SIMULATIONS)

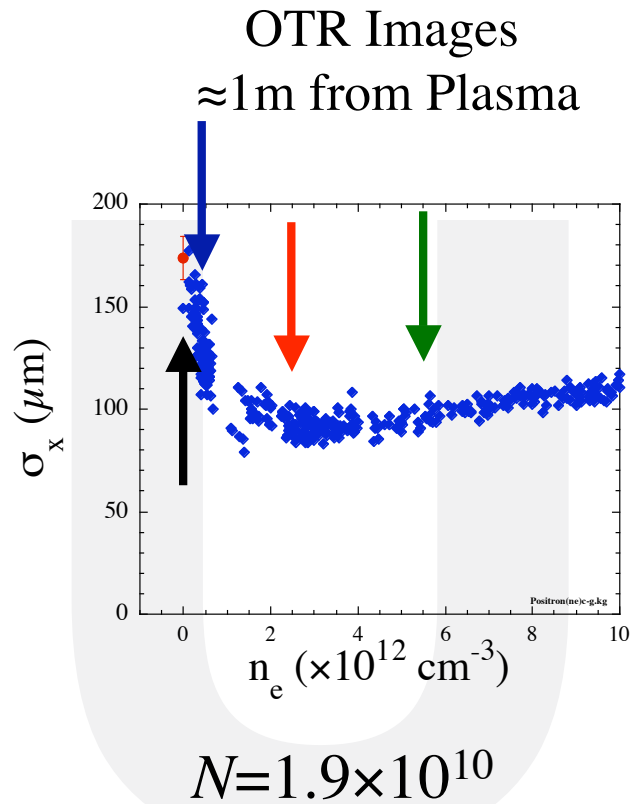
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$$n_e = 2 \times 10^{14} \text{ cm}^{-3}$$

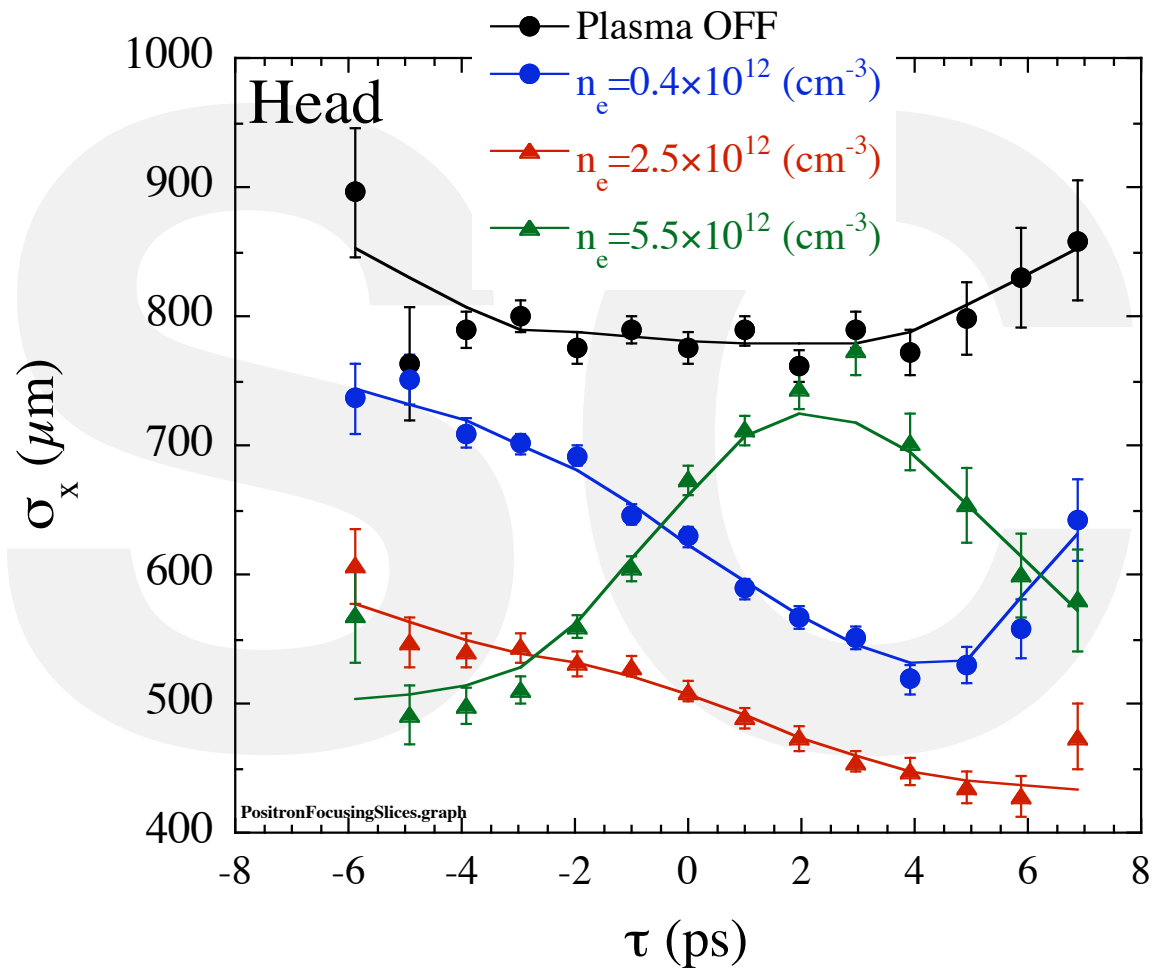


- ◆ The  $e^+$  beam exits the plasma with  $\approx$ equal emittances and  $\approx$ equal transverse sizes

# FOCUSING OF $e^+$ : LOW $n_e$



Cherenkov Images  $\approx 12\text{m}$  from Plasma  
Time Resolved Using a Streak Camera



○ Focusing dynamics

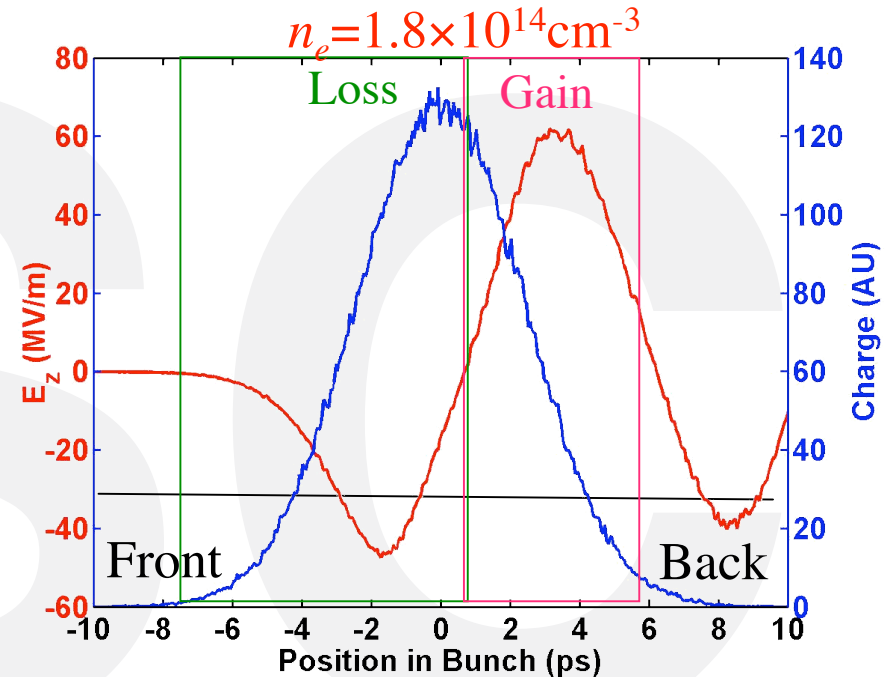
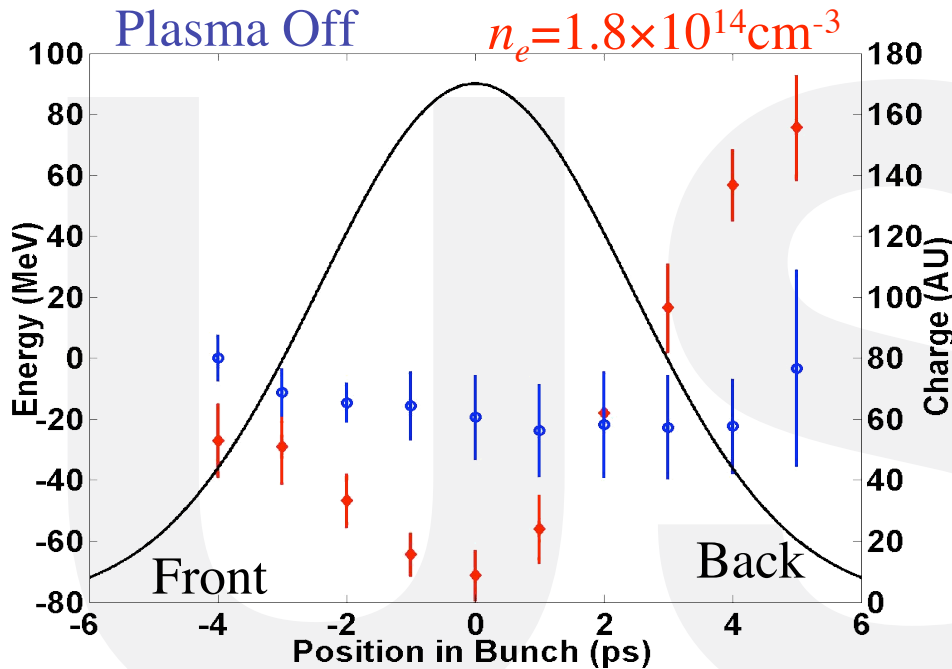
M. J. Hogan, PRL 90, 205002 (2003)

# ENERGY LOSS/GAIN $e^+$

## Experiment

$\sigma_z \approx 730 \mu\text{m}$   
 $N = 1.2 \times 10^{10} e^+$

## 2-D Simulation



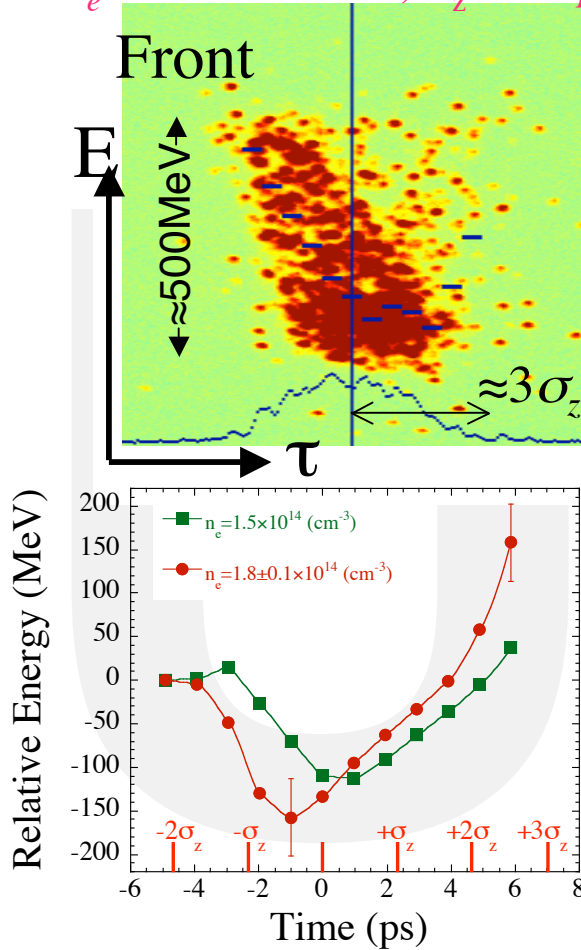
- Loss  $\approx 70 \text{ MeV}$   
(over 1.4 m)
- Gain  $\approx 75 \text{ MeV}$

- Loss  $\approx 45 \text{ MeV/m} \times 1.4 \text{ m} = 63 \text{ MeV}$
- Gain  $\approx 60 \text{ MeV/m} \times 1.4 \text{ m} = 84 \text{ MeV}$

➔ Excellent agreement!

# e<sup>-</sup> ACCELERATION

$n_e = 1.8 \times 10^{14} \text{ cm}^{-3}$ ,  $\sigma_z \approx 700 \mu\text{m}$



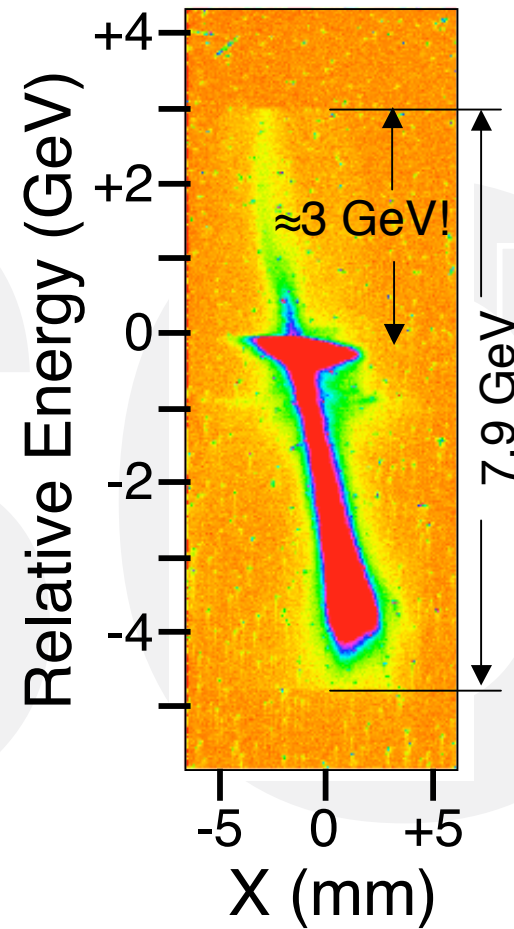
- Gain  $\approx 280 \text{ MeV}$ ,  $L_p = 1.4 \text{ m}$   
Gradient  $\approx 200 \text{ MV/m}$

Muggli et al., PRL 93, 014802 (2004)

- No time resolution needed anymore!!!!

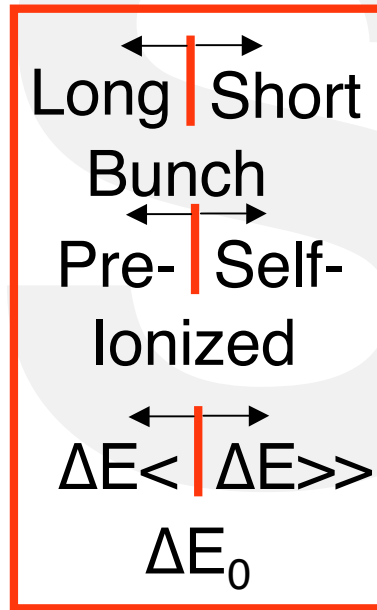
P. Muggli, PPA 09. 09/12/17

$n_e = 2.6 \times 10^{17} \text{ cm}^{-3}$ ,  $\sigma_z \approx 20\text{-}30 \mu\text{m}$



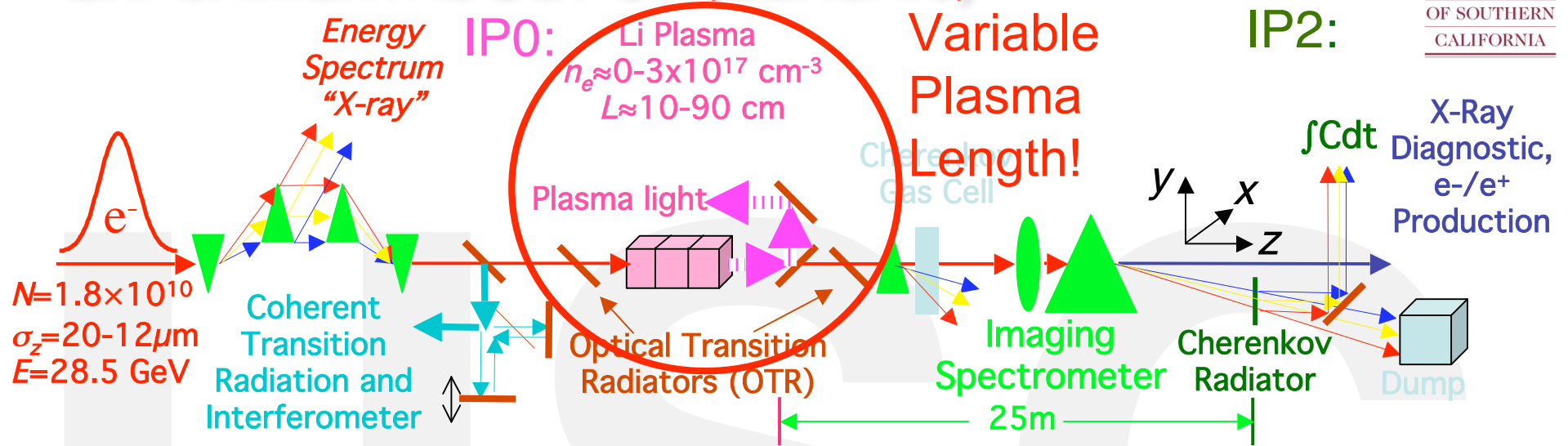
- Gain  $\approx 4 \text{ GeV}$ ,  $L_p = 10 \text{ cm}$
- Gradient  $\approx 40 \text{ GV/m}$

Hogan et al., PRL 95, 054802 (2005)

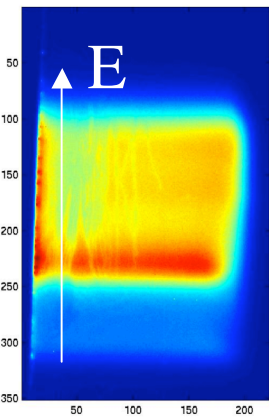




# EXPERIMENTAL SET UP (GENERIC)

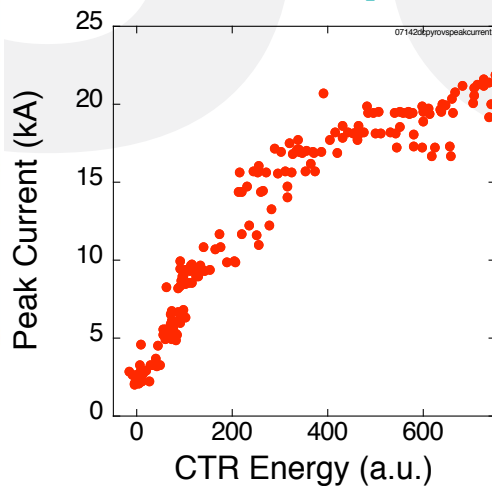


- X-ray Chicane

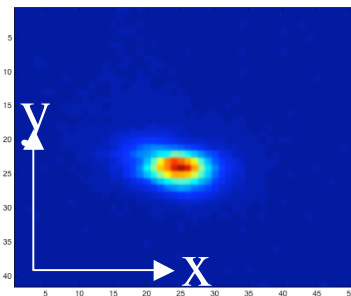


- Coherent Transition Radiation (CTR)

- CTR Energy  $\approx I_{\text{peak}} \approx 1/\sigma_z$



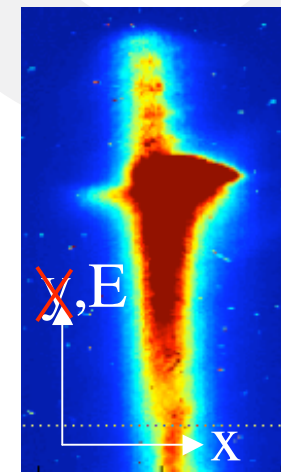
- OTR



- Spatial resolution  $\approx 9 \mu\text{m}$

- Cherenkov (aerogel)

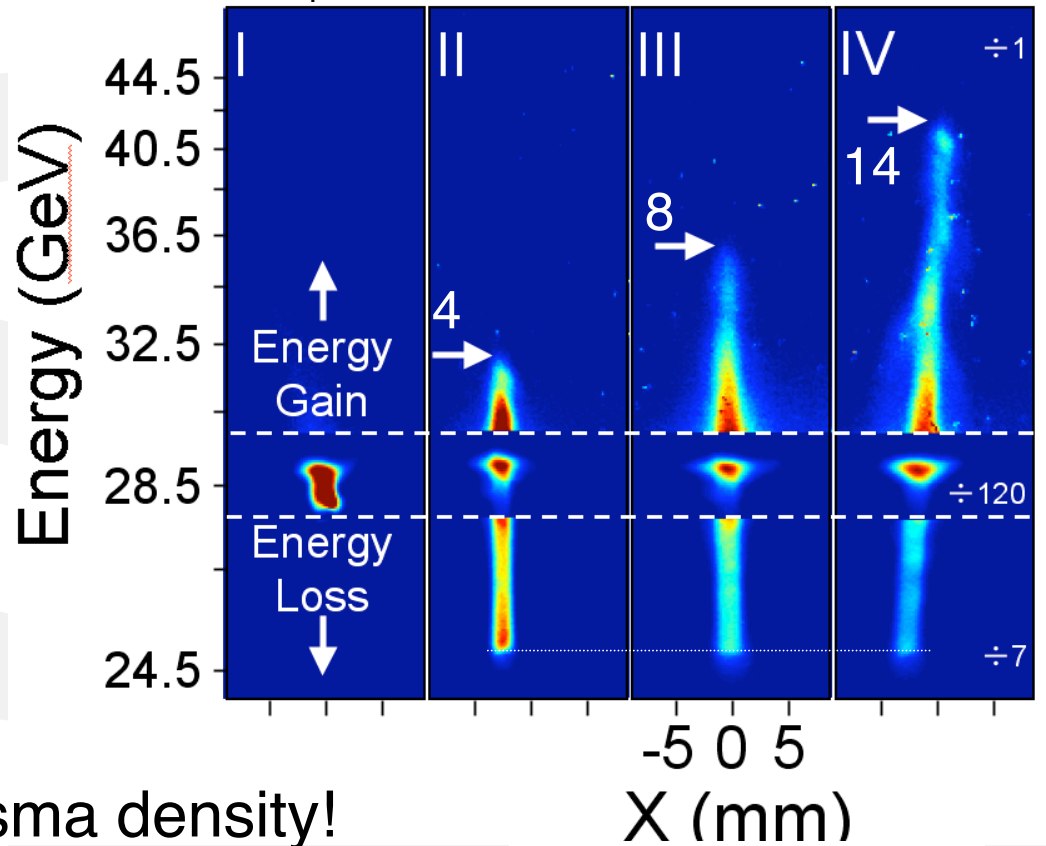
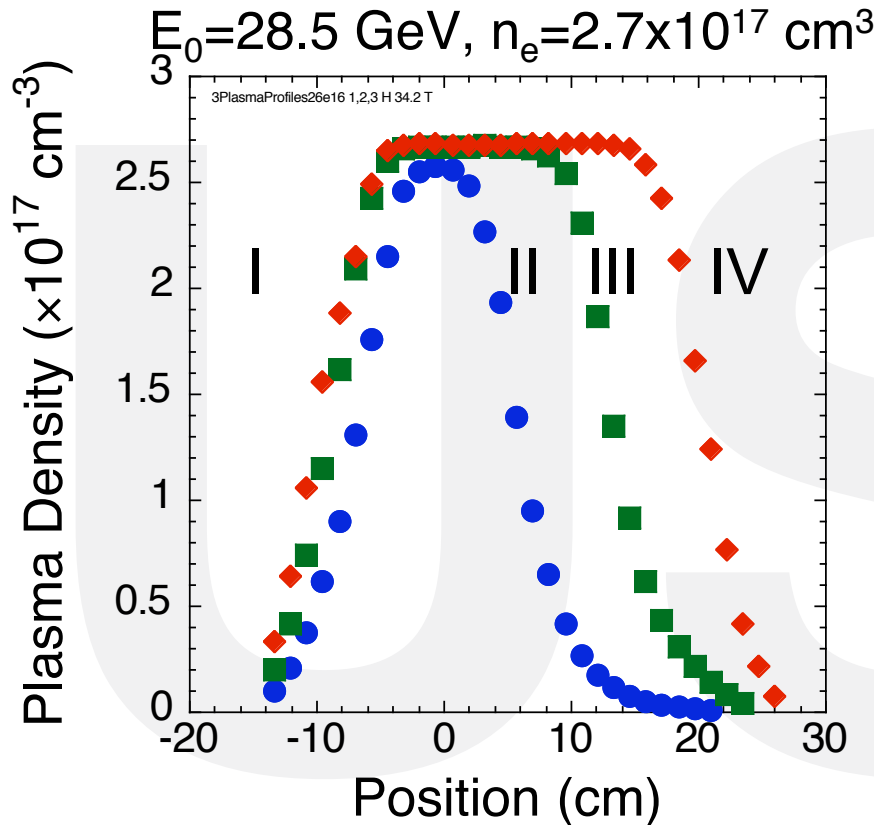
- Spatial resolution  $\approx 100 \mu\text{m}$   
- Energy resolution  $\approx 30 \text{ MeV}$





# $\sigma_z \approx 25 \mu\text{m}$ : SCALING WITH PLASMA LENGTH

Same incoming beam!  $\sigma_z \approx 25 \mu\text{m}$   
 $L_p = 0, 13, 22, 31 \text{ cm}$



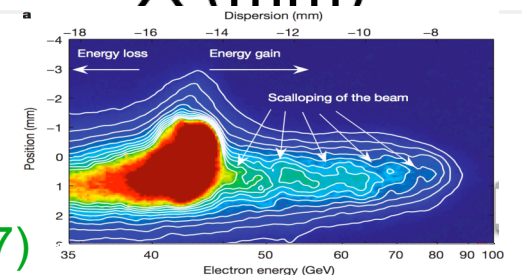
➡ Energy gain scales with plasma density!

➡ Gain >14 GeV over (only!)  $L_p = 31 \text{ cm}$ !

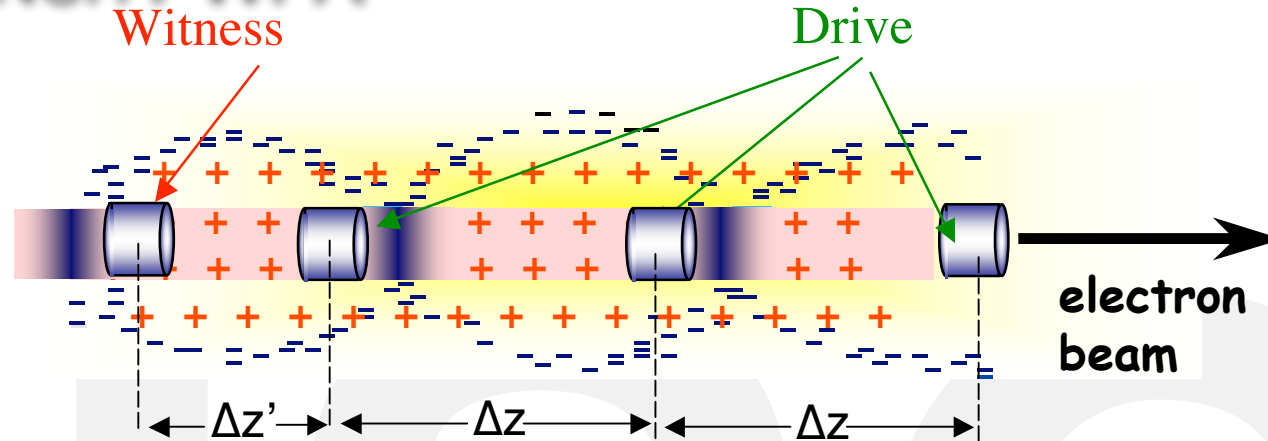
➡  $E_{\text{acc}} \approx 45 \text{ GV/m}$



Nature 445, 741(2007)



# MULTIBUNCH PWFA



➔ Bunch spacing/plasma density condition:

$$\Delta z = \lambda_p \text{ (resonance)} \quad \sigma_z \leq \lambda_p / 2$$

$$\Delta z' \approx (m + 1/2) \lambda_p$$

Plasma wavelength:  $\lambda_p = \frac{2\pi c}{\omega_{pe}}$

Plasma angular frequency, density  $n_e$ :  $\omega_{pe} = \left( \frac{n_e e^2}{\epsilon_0 m_e} \right)^{1/2}$

➔ Wake fields add up (linear theory):

$$E_z \text{ N bunches} = N \times E_z \text{ 1 bunch} \quad \text{(Maximize wakefield!)}$$

➔ Maximize transformer ratio with “shaping” (beyond energy doubling!)

➔ Finite energy spread, beam acceleration

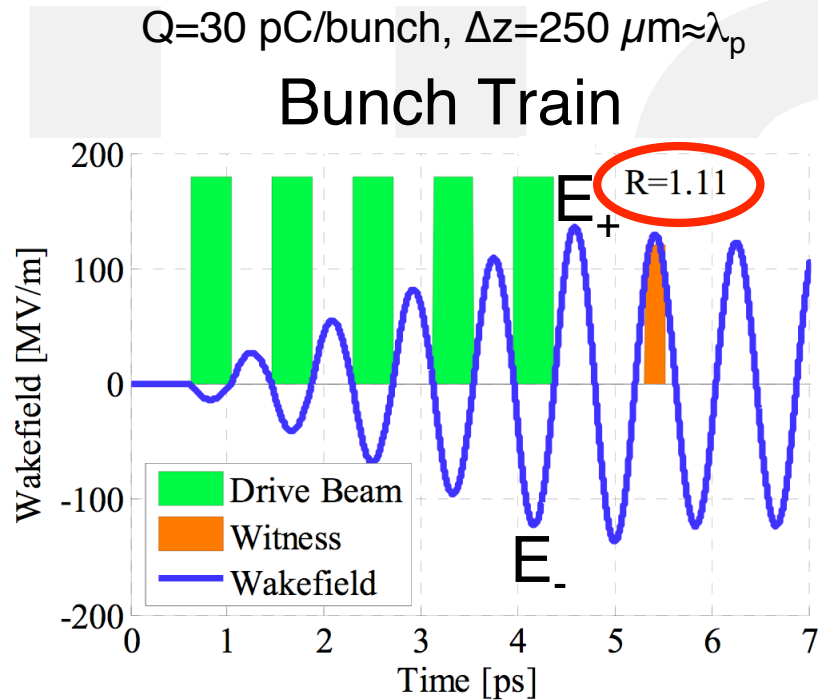
# MULTIBUNCH PWFA

Transformer Ratio:  $R = E_+ / E_-$

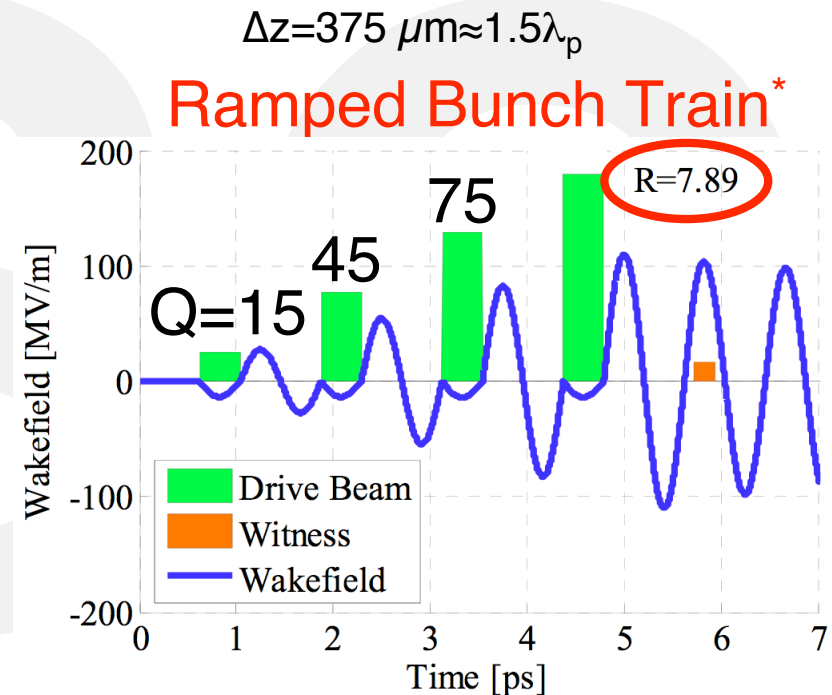
Energy Gain:  $\leq RE_0$

$\sigma_r = 125 \mu\text{m}$ ,  $n_e = 1.8 \times 10^{16} \text{ cm}^{-3}$ ,  $\lambda_p = 250 \mu\text{m}$

$E_0$ : incoming energy



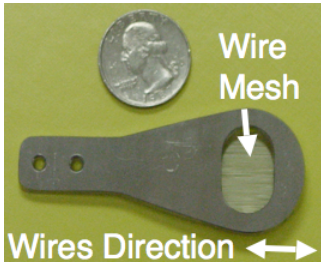
Kallos, PAC'07 Proceedings



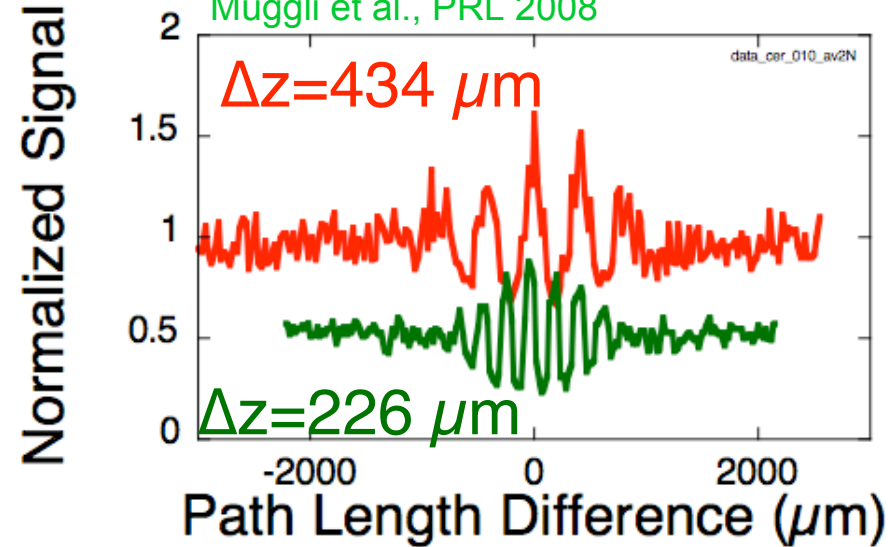
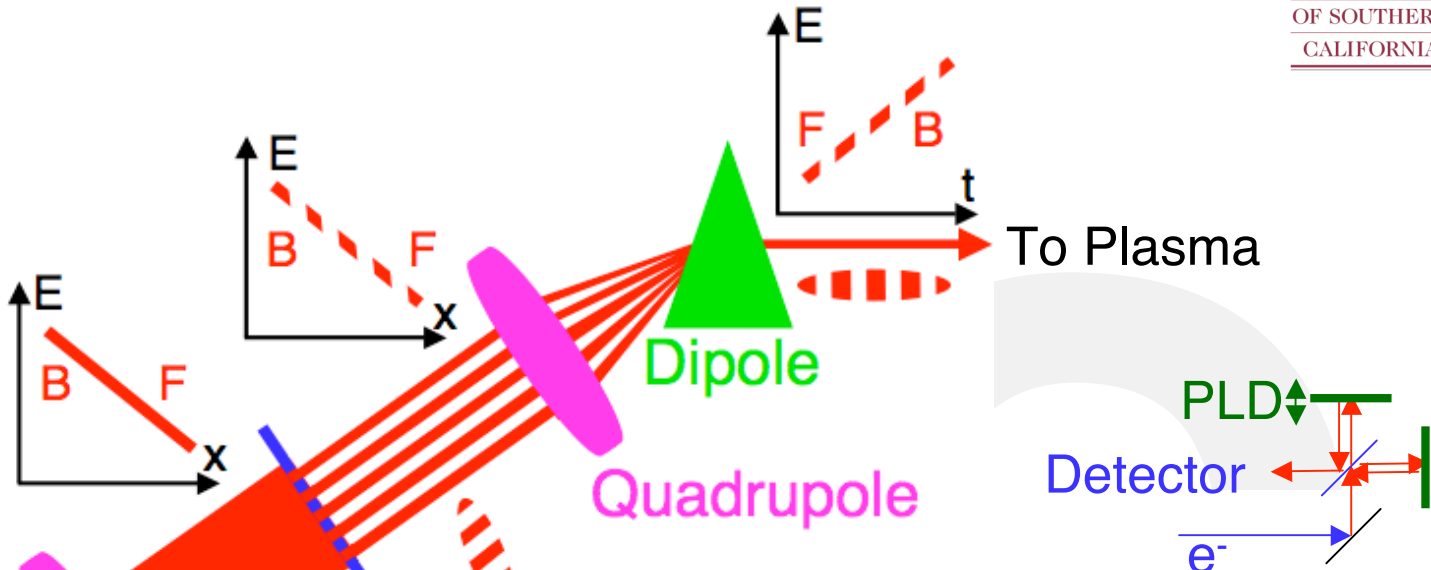
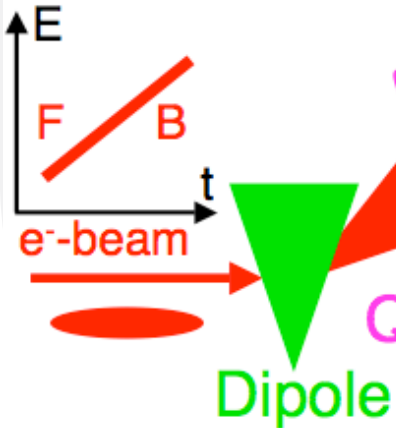
\*Tsakanov, NIMA, 1999

➔  $R = 7.9 \Rightarrow$  multiply energy by  $\approx 8$  in a single PWFA stage!

# MULTI-BUNCH SOURCE



Correlated energy chirp from linac



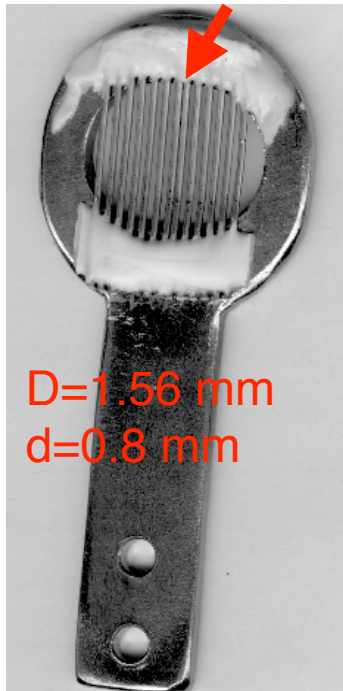
➔ Emittance selection

➔ Mask+Slit

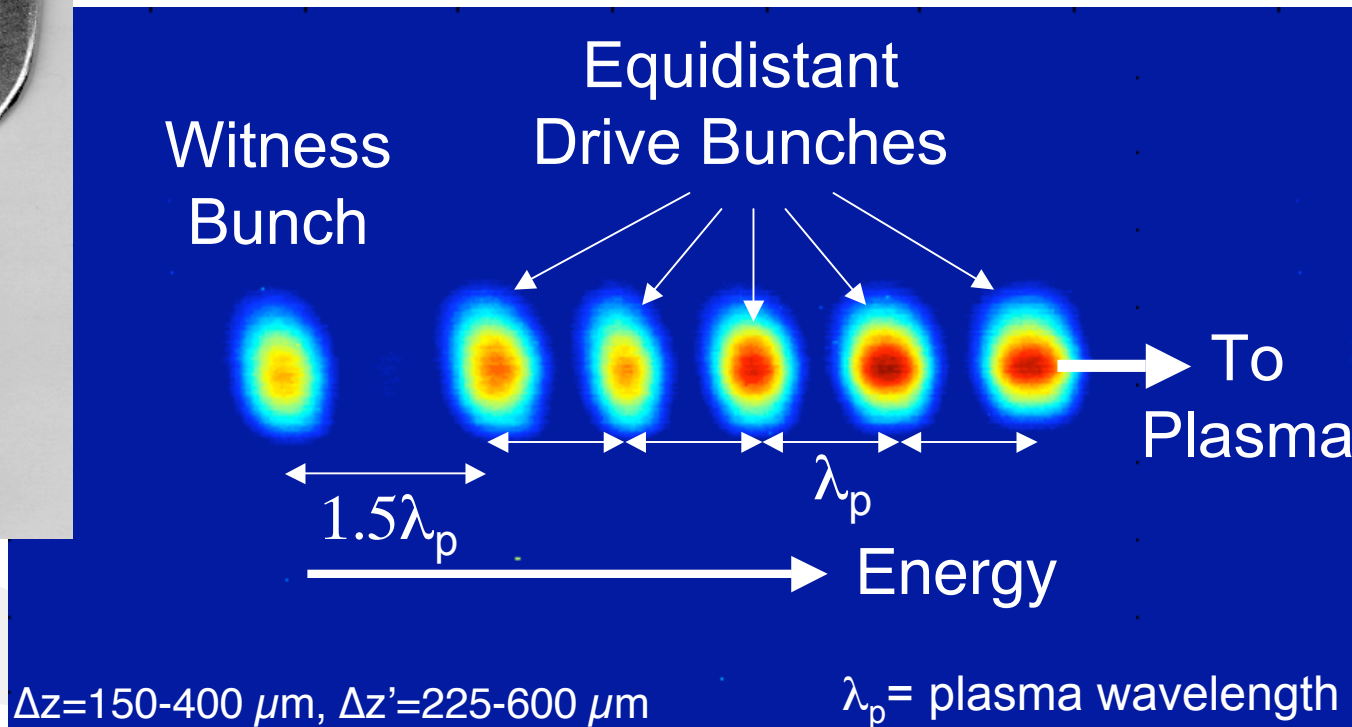
➔ Choose microbunches spacing and widths with mask and beam parameters:

$N, \Delta z, \sigma_z, Q$   
P. Muggli, PPA 09. 09/12/17

# TRAIN FOR PWFA



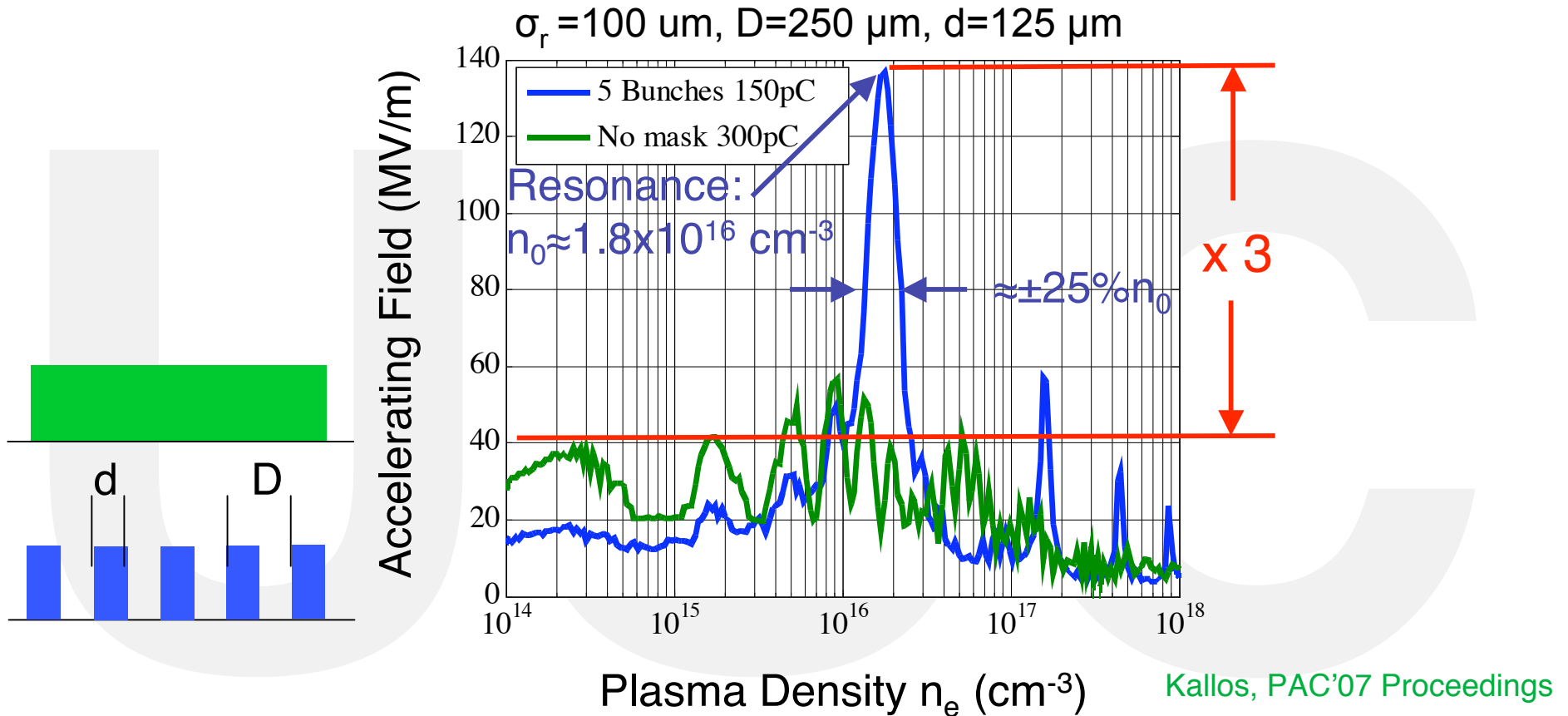
Mask with non-equidistant “wires”  
Measurement in energy plane



- ➡ Generate “ideal” spacing for resonant PWFA
- ➡ Charge modulation optimization possible
- ➡ Plasma density must be adjusted for resonant excitation

# ACCELERATING FIELD

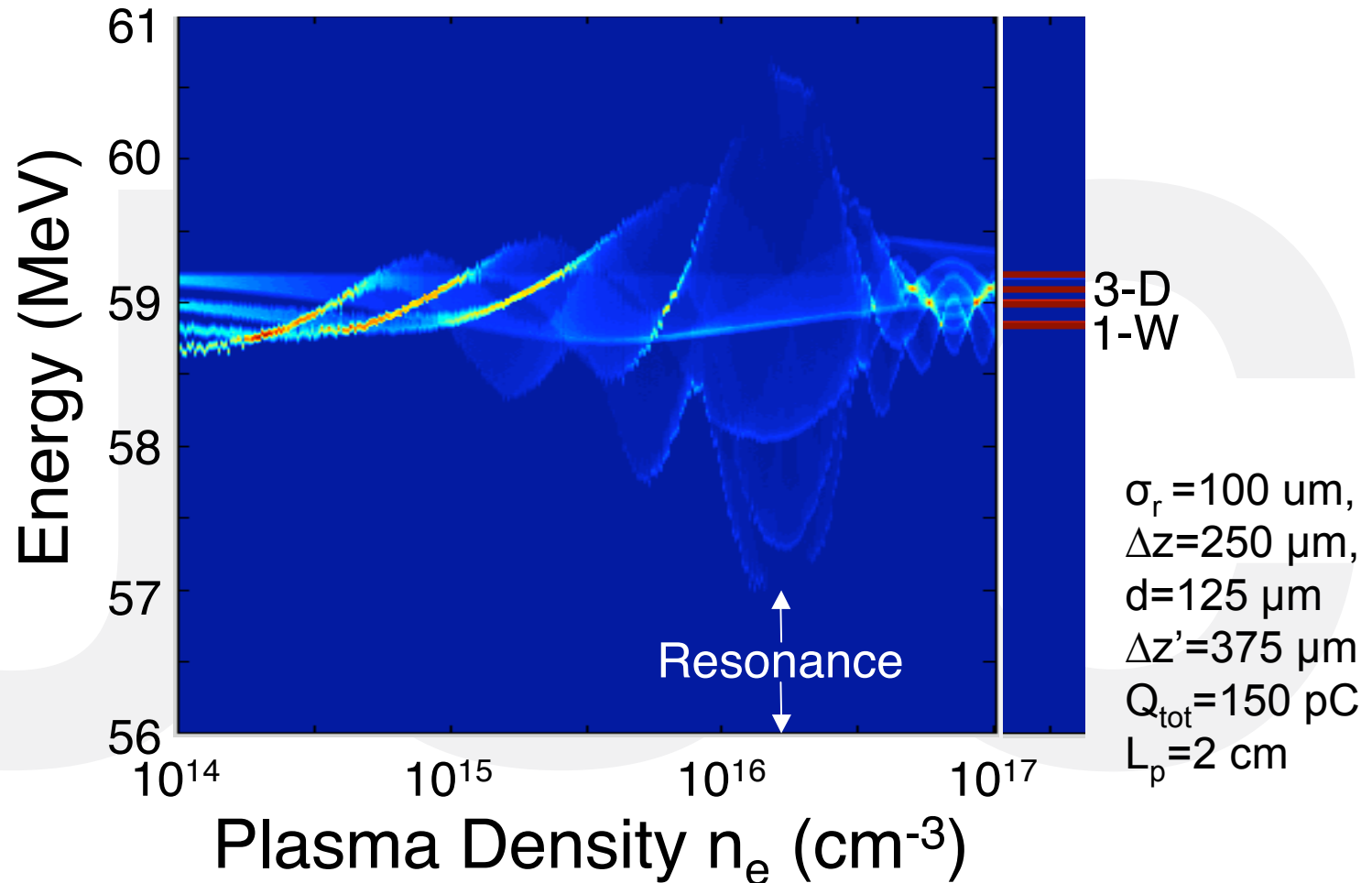
Linear calculation microbunches with equal charge



- ➡ Expect  $\approx$ MeV energy gain/loss over 1 cm
- ➡ Microbunch resonance clear, and narrow
- ➡ Drive larger wakefields with the train ( $< Q_0/2$ ) than with the long bunch!

# ENERGY CHANGE

Linear calculation: microbunches with equal charge



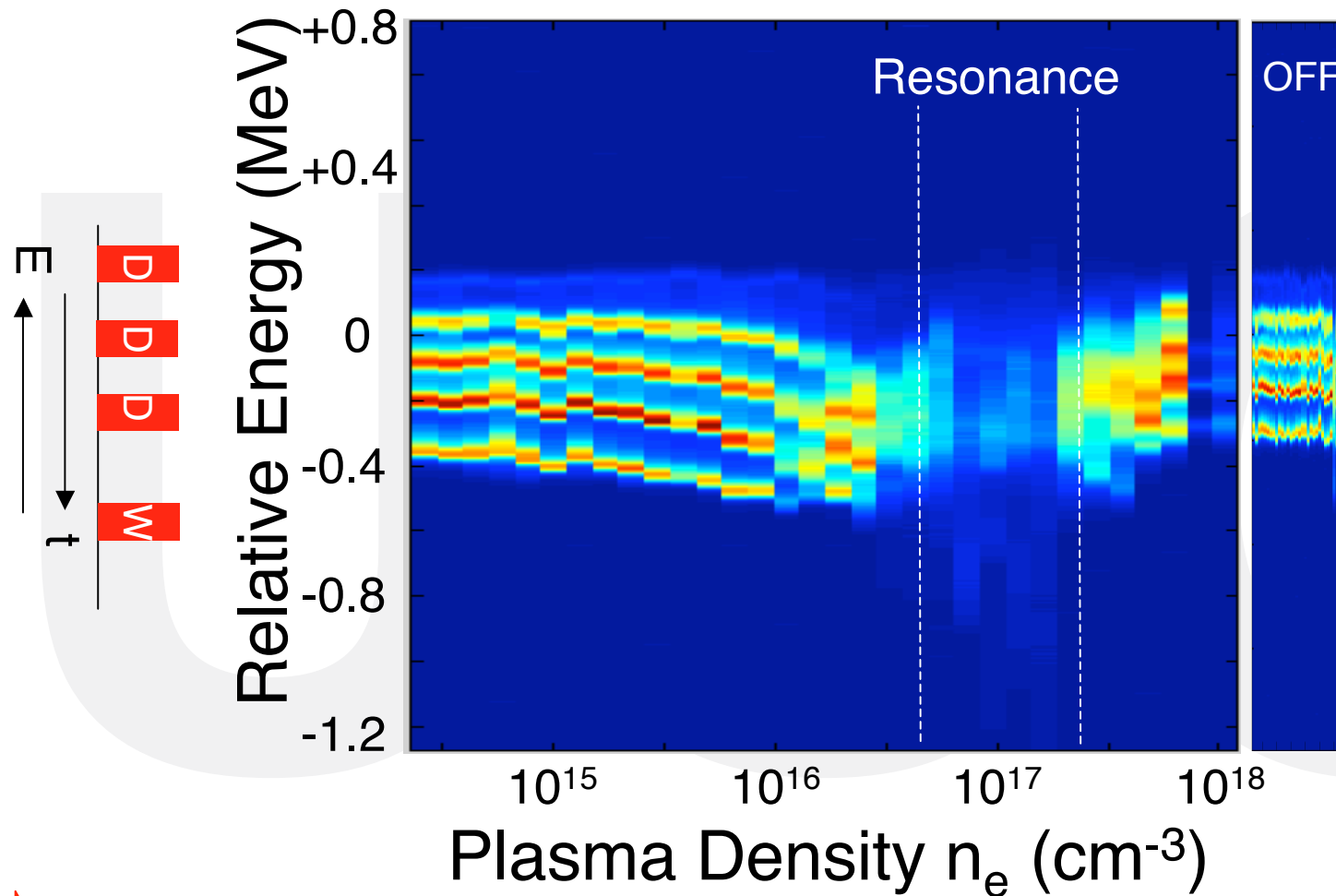
➔ Resonant excitation of wakefield is the main feature

➔ Note: case of witness bunch at lowest energy,

**WRONG CHIRP!**

# ENERGY CHANGE

Experiment

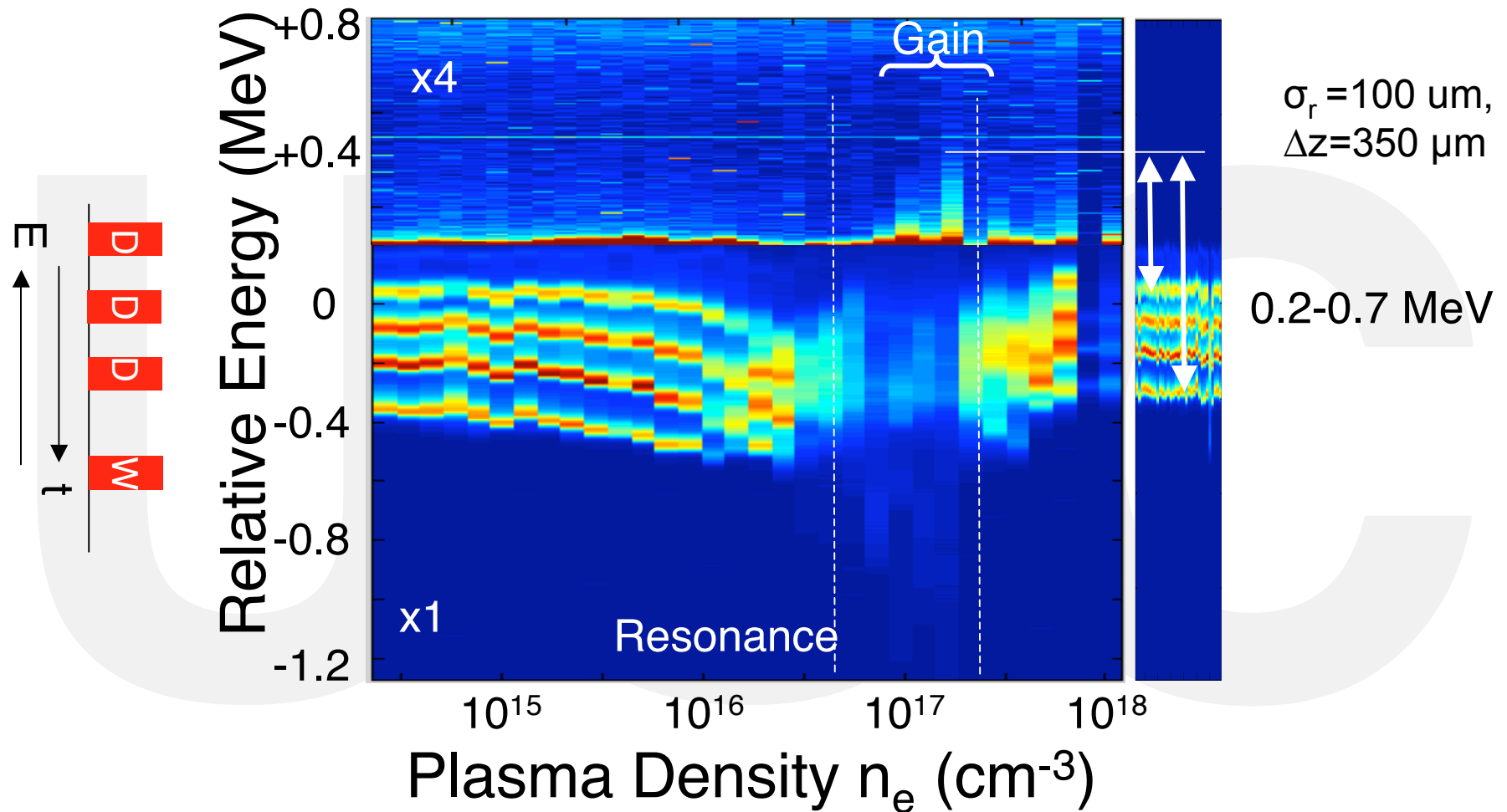


- ➔ Resonance clearly observed
- ➔ Large energy loss,  $>0.8$  MeV or  $>40$  MeV/m
- ➔ Energy gain?



# ENERGY CHANGE

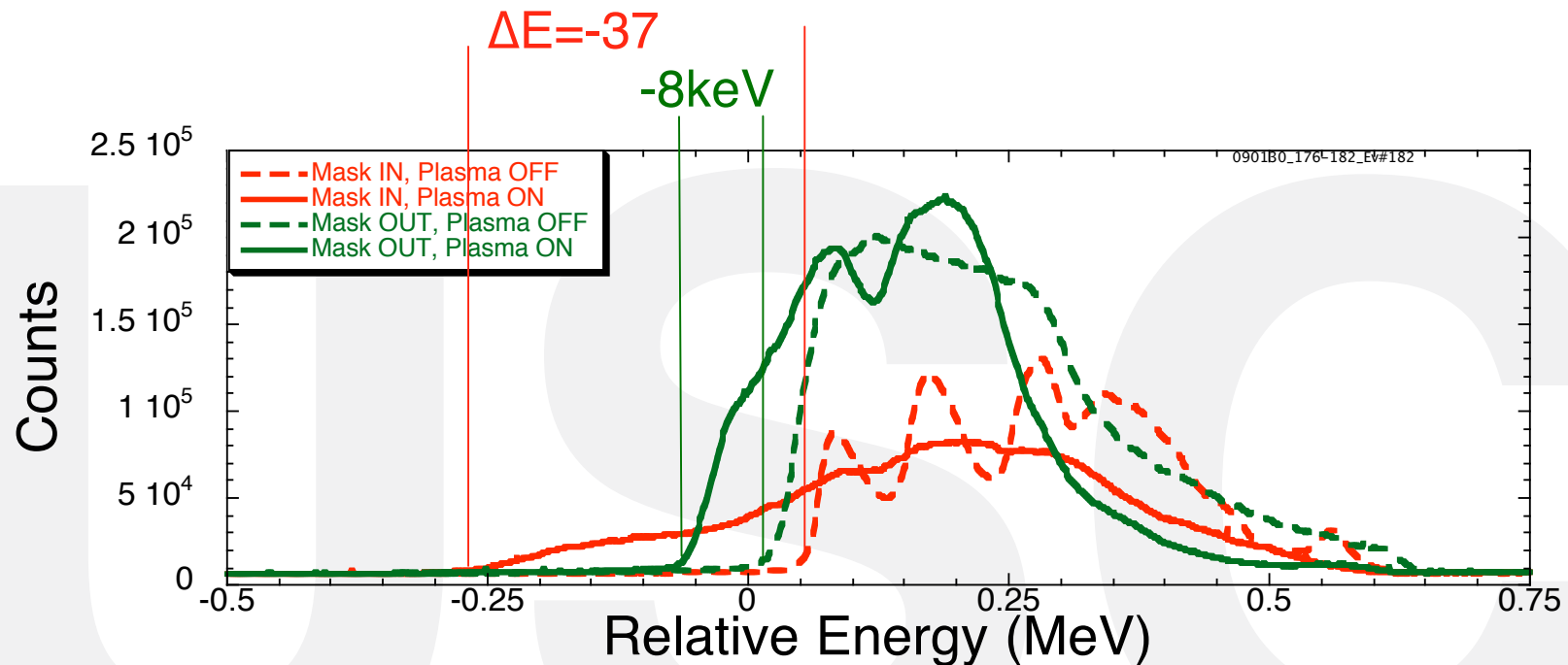
Experimental



- ➔ Energy gain, up to 0.7 MeV?
- ➔ Stability of  $\Delta E/E_0 \Rightarrow$  stability of  $\Delta z$ !

➔ More experiments needed!

# RESONANT DENSITY INTERACTION



- ➡ Much larger loss with microbunches at/near resonance
- ➡ Drive large wakefield with half the charge and large  $n_e$
- ➡ Decelerating gradient with  $\mu$ bunches  $\approx 18$  MV/m

# CONCLUSIONS

- ◆ Wealth of experience in  $e^-/e^+$  PWFA experiments at SLAC and BNL-ATF
- ◆ Very well diagnosed experiments built over time
- ◆ “Perfect” plasma source: field free, stable, ...
- ◆ Many optical diagnostics for info within the bunch (OTR, Cher., CTR)
- ◆ Magnetic spectrometer is key
- ◆ Understanding “all” aspects of the PWFA is important
- ◆ Masking technique for long  $p^+$  bunches?
- ◆ Many more results not presented
- ◆ Experience acquired with  $e^-/e^+$  transfers to PPA

Thank You!



Mozambique: suggested location for the next PWFA experiments