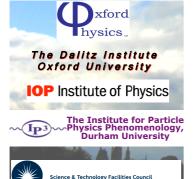
Boosted Massive Jets @ CDF and Template Overlap Method for Massive Jets

Gilad Perez

Weizmann Institute

R, Alon, E. Duchovni, GP & P. Sinervo, for the CDF collaboration; blessed preliminary data;

L. Almeida, S.J. Lee, GP, G. Sterman, & I. Sung, arXiv:1006.2035







Outline

- Semi-analytical dist' for inner-jet energy flow:
 - (i) jet mass => perturbative @ high mass =>
 - (ii) angularity <-> 2-body (iii) planar flow <-> 3 body.
- → First measurements: CDF preliminary.
- ◆ Can improve systematically? Template method.
- Summary

Jet Mass-Overview

♦ Jet mass-sum of "massless" momenta in h-cal inside the cone: $m_J^2 = (\sum_{i \in R} P_i)^2, \;_{Pi^2 = 0}$

→Jet mass is non-trivial both for S & B for concreteness mostly focus on top-jets.

- lack Naively the signal is $J \propto \delta(m_J m_t)$
- lacktriangle In practice $m_J^t \sim m_t + \delta m_{QCD} + \delta m_{EW}$

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Pure kinematical bW(qq)
dist'
in/out cone
~0.2 GeV

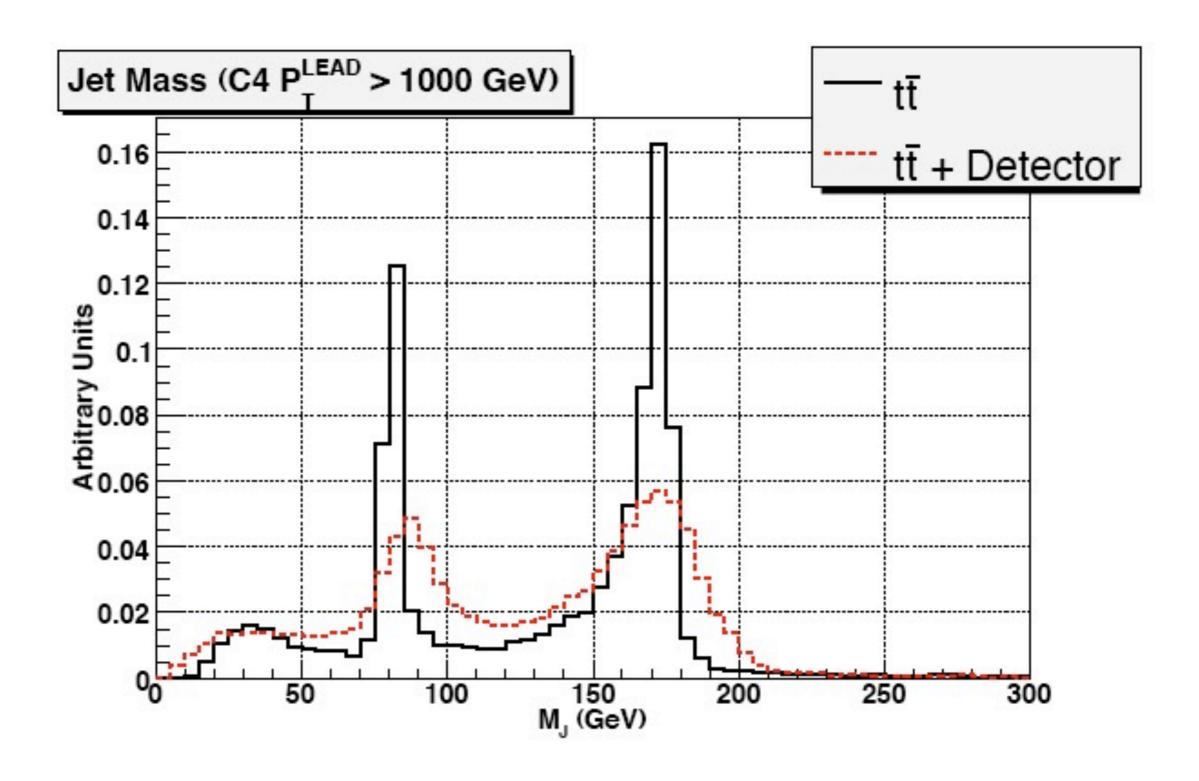
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Can understood perturbatively fast & small~10GeV

+ detector smearing.

Pure kinematical bW(qq)
dist'
in/out cone
~0.2 GeV

Sherpa => Transfer functions,.



QCD jet mass distribution

→ Boosted QCD Jet via factorization:

$$\frac{d\sigma^{i}}{dm_{J}} = J^{i}(m_{J}, p_{T}^{min}, R^{2}) \sigma^{i} \left(p_{T}^{min}\right)$$

$$\int_{dm_{J}J^{i}=1} i = Q, G$$

- can interpret the jet function as a probability density functions for a jet with a given pT to acquire a mass between mJ and mJ + δ mJ

Full expression:

$$\frac{d\sigma_{H_A H_B \to J_1 J_2}}{dm_{J_1}^2 dm_{J_2}^2 d\eta} = \sum_{abcd} \int dx_a \, dx_b \, \phi_a(x_a, p_T) \, \phi_b(x_b, p_T) \frac{d\hat{\sigma}_{ab \to cd}}{dp_T d\eta} \left(x_a, x_b, \eta, p_T\right)$$

$$S\left(m_{J_1}^2, m_{J_2}^2, \eta, p_T, R^2\right) \, J_1^{(c)}(m_{J_1}^2, \eta, p_T, R^2) J_2^{(d)}(m_{J_2}^2, \eta, p_T, R^2)$$

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For large jet mass & small R, no big corrections => leading log can be captured via perturbative QCD!

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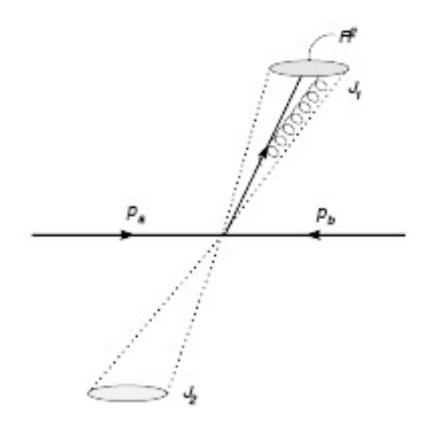
$$S\left(m_{J_1}^2, m_{J_2}^2, \eta, p_T, R^2\right) \, J_1^{(c)}(m_{J_1}^2, \eta, p_T, R^2) J_2^{(d)}(m_{J_2}^2, \eta, p_T, R^2)$$

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en pt to

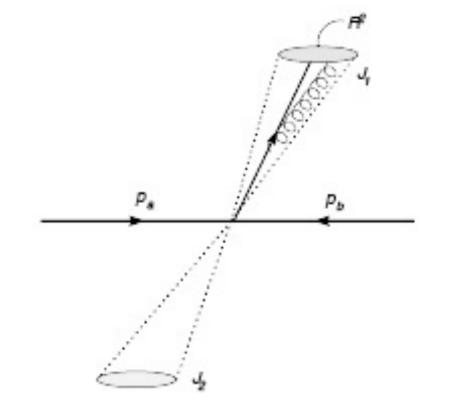
QCD jet mass distribution, Q+G

Main idea: calculating mass due to two-body QCD bremsstrahlung:



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$$J^{(eik),c}(m_J, p_T, R) \simeq \alpha_{\rm S}(p_T) \frac{4C_c}{\pi m_J} \log \left(\frac{R p_T}{m_J}\right)$$

 $C_F = 4/3$ for quarks, $C_A = 3$ for gluons.

7

QCD jet mass distribution, Q+G

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 $C_F = 4/3 \text{ for quarks, } C_A = 3 \text{ for gluons.}$

Data is admixture of the two, should be bounded by them:

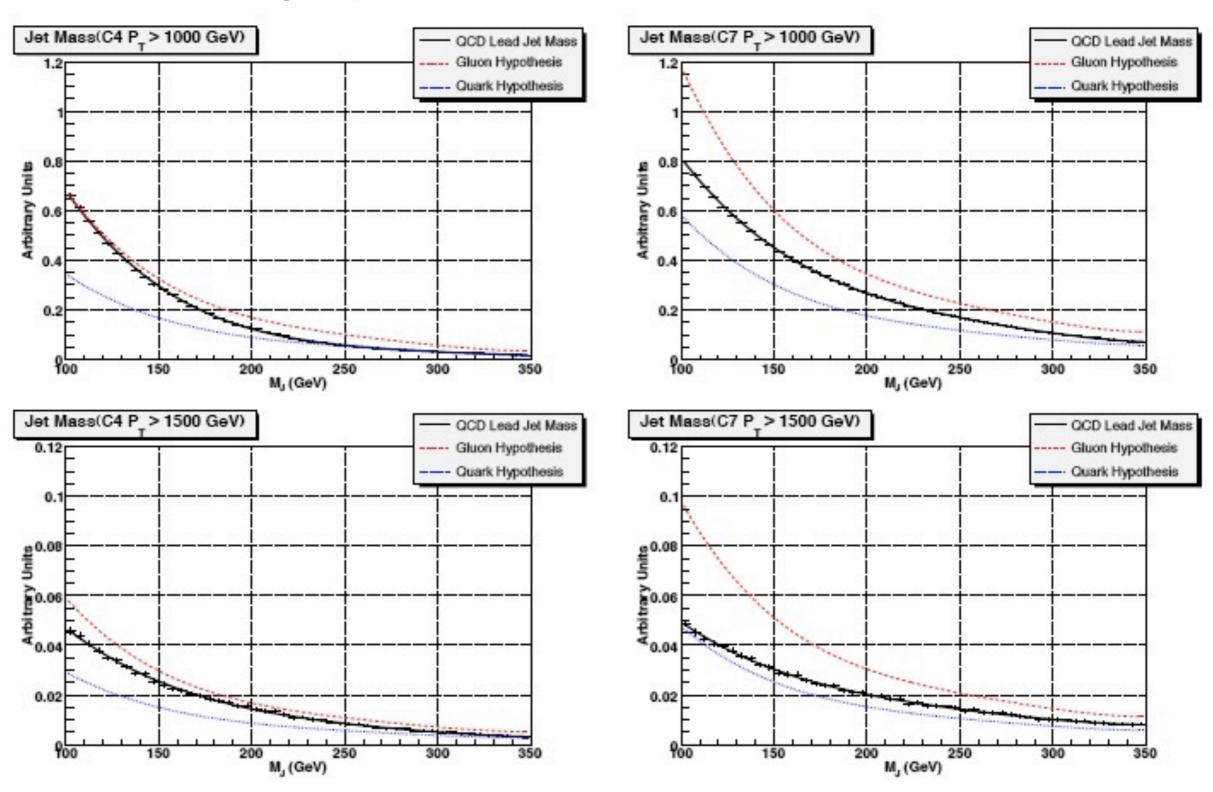
$$\frac{d\sigma_{pred}(R)}{dp_T dm_J}_{upper\ bound} = J^g(m_J, p_T, R) \sum_c \left(\frac{d\sigma^c(R)}{dp_T}\right) ,$$

$$\frac{d\sigma_{pred}(R)}{dp_T dm_J}_{lower\ bound} = J^q(m_J, p_T, R) \sum_c \left(\frac{d\sigma^c(R)}{dp_T}\right) ,$$
,

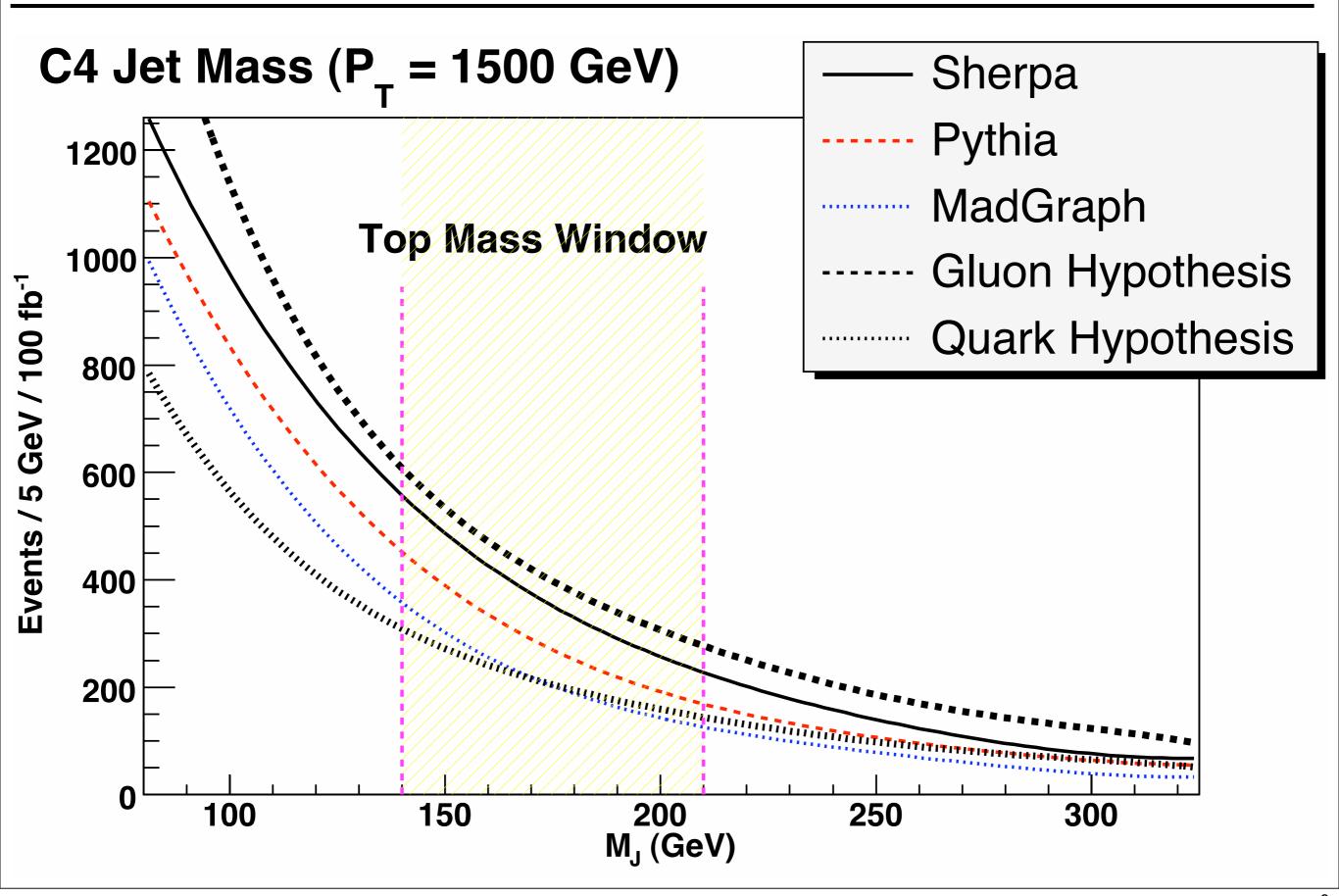
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Jet mass distribution theory vs. MC

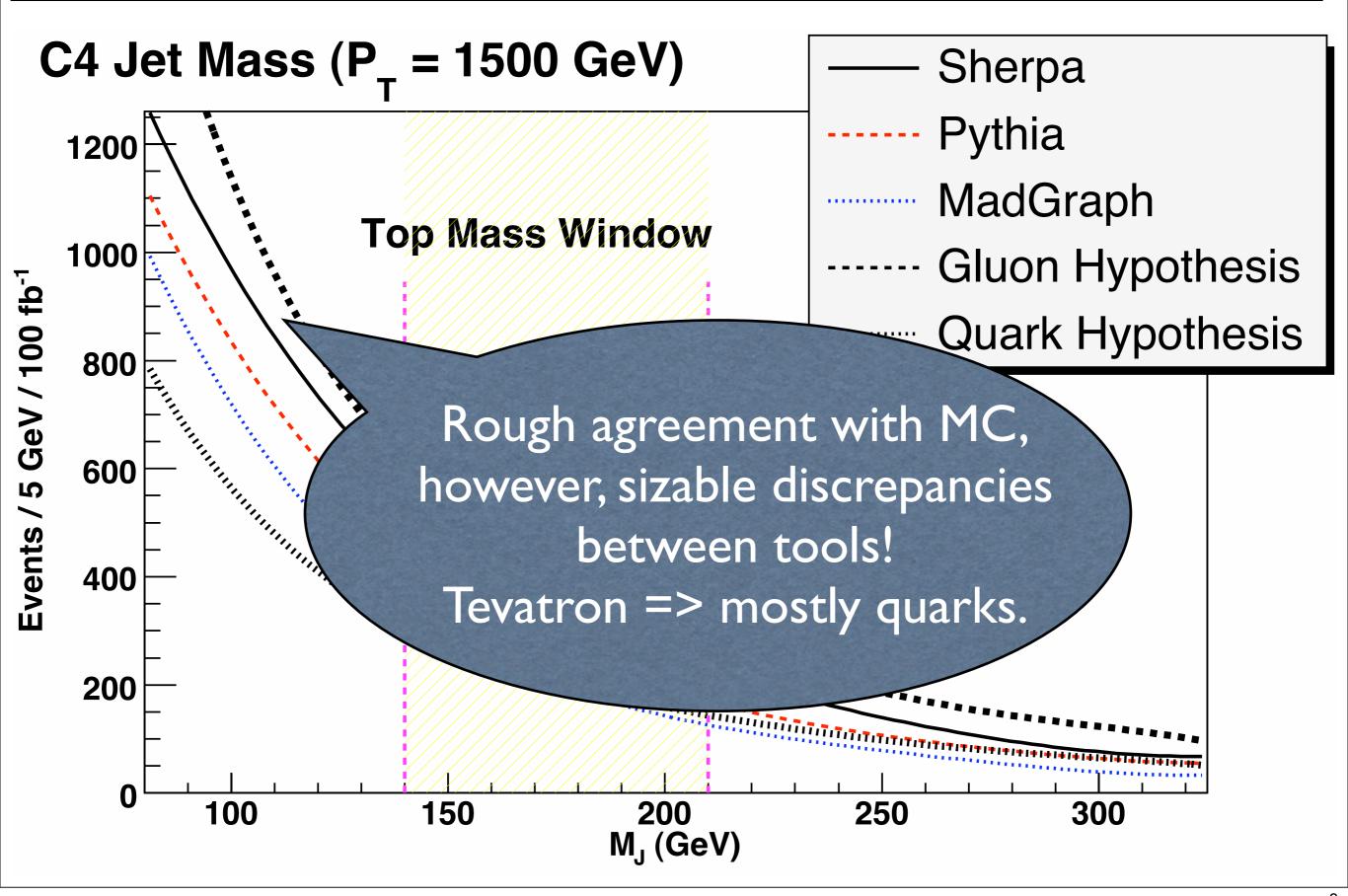
Sherpa, jet function convolved above $\,p_T^{ m min}$



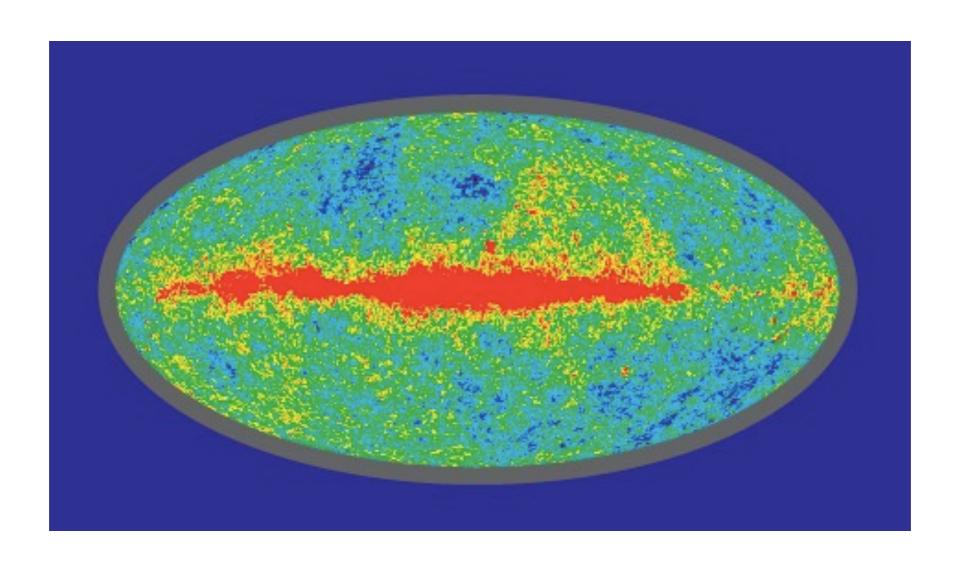
Jet mass distribution theory vs. MC



Jet mass distribution theory vs. MC



Jet sub-structure



angularity; planar flow <=> no manipulation of jet energy deposition

IR-safe jet-shapes which distinguish between massive & QCD jets?

◆ Successes in high jet mass => jet function well described by single gluon radiation.

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 - → Large class of jet-shapes become perturbatively calculable

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- ◆ Successes in high jet mass => jet function well described by single gluon radiation.
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 - → Large class of jet-shapes become perturbatively calculable

Angularity (2-body final state): Berger, K'ucs and Sterman (03)

$$\tau_a(R, p_T) = \frac{1}{m_J} \sum_{i \in jet} \omega_i \sin^a \theta_i \left[1 - \cos \theta_i \right]^{1-a} \sim \frac{2^{a-1}}{m_J} \sum_{i \in jet} \omega_i \theta_i^{2-a} \propto_{a=-2} \sum_i \omega_i \theta_i^4$$

emphasize cone-edge radiation

Almeida, Lee, GP, Sterman, Sung, & Virzi (08)

◆Angularities distinguish between Higgs and QCD jets (2-body only one variable<=>ysplitter):

$$\frac{dJ^h}{d\tilde{\tau}_a} \propto \frac{1}{|a| (\tilde{\tau}_a)^{1-\frac{2}{a}}} \qquad \text{VS.} \qquad \frac{dJ^{\text{QCD}}}{d\tilde{\tau}_a} \propto \frac{1}{|a| \tilde{\tau}_a}$$

$$P^x(\theta_s) = (dJ^x/d\theta_s)/J^x \Longrightarrow P^x(\tilde{\tau}_a); \qquad R(\tilde{\tau}_a) = \frac{P^{\text{sig}}(\tilde{\tau}_a)}{P^{\text{QCD}}(\tilde{\tau}_a)}$$

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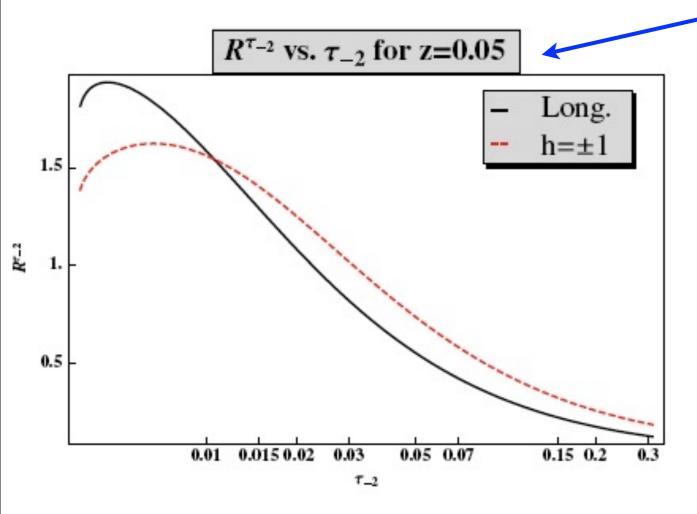


FIG. 3 (color online). The ratio between the signal and background probabilities to have jet angularity $\tilde{\tau}_{-2}$, $R^{\tilde{\tau}_{-2}}$.

$$(z = m_J/p_T)$$

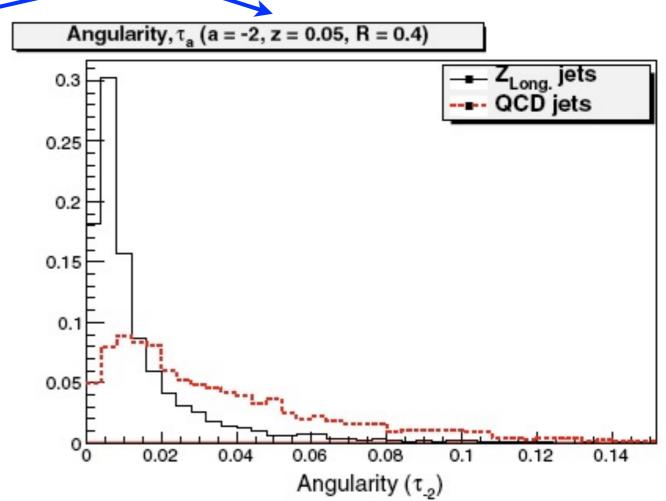
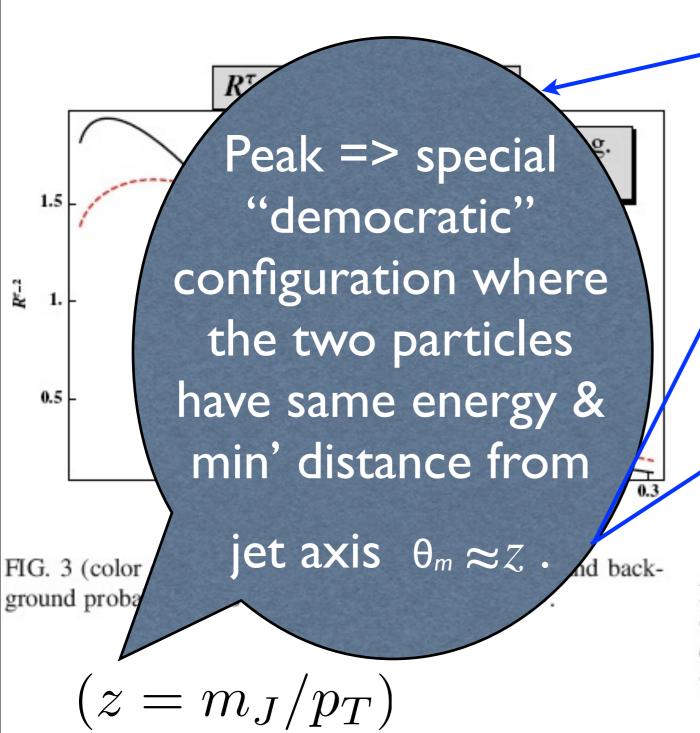


FIG. 4 (color online). The angularity distribution for QCD (red-dashed curve) and longitudinal Z (black-solid curve) jets obtained from MADGRAPH. Both distributions are normalized to the same area.

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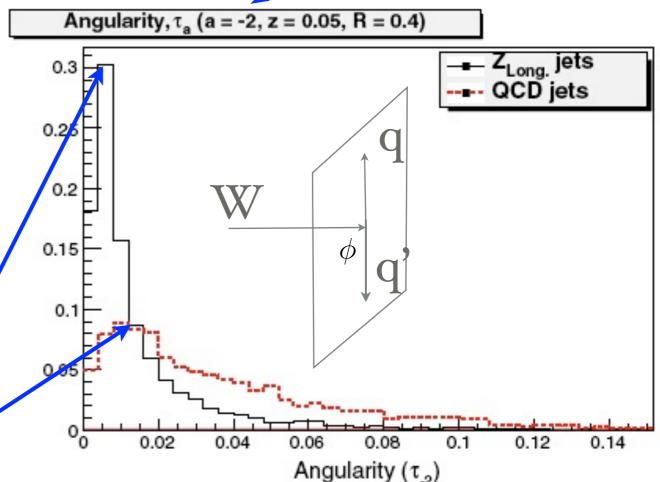
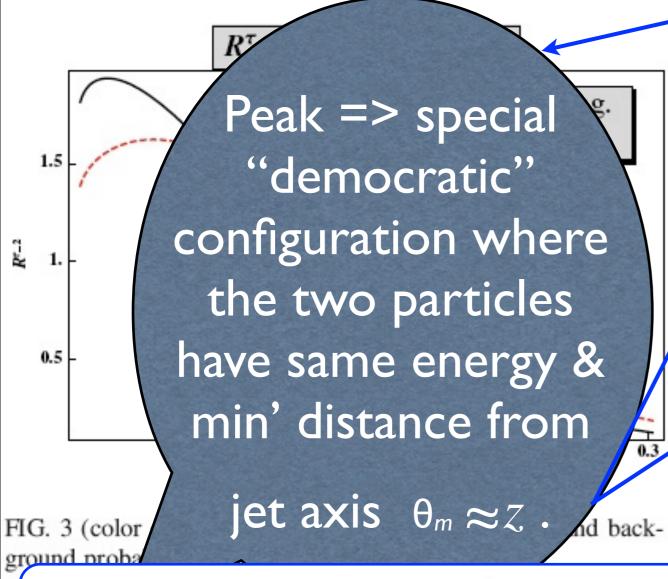


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2-body jet's kinematics, $\mathbb{Z}/\mathbb{W}/h$

$$P^x(\theta_s) = (dJ^x/d\theta_s)/J^x \Longrightarrow P^x(\tilde{\tau}_a); \qquad R(\tilde{\tau}_a) = \frac{P^{\text{sig}}(\tilde{\tau}_a)}{P^{\text{QCD}}(\tilde{\tau}_a)}$$



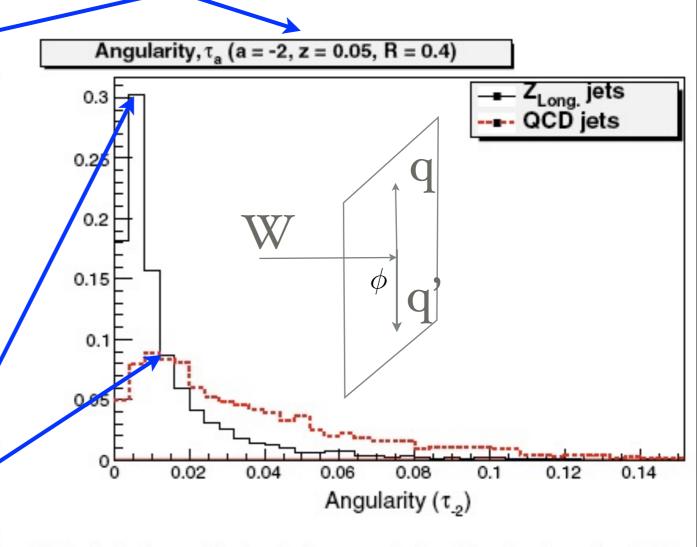
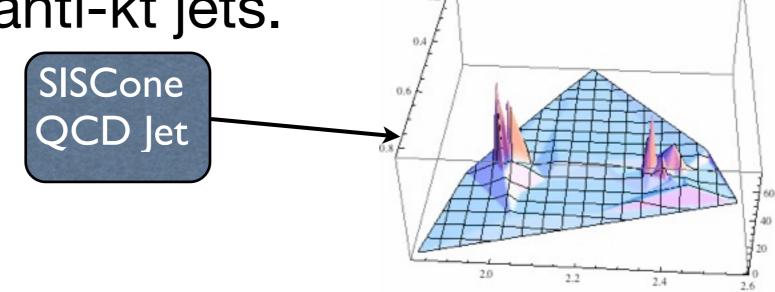


FIG. 4 (color online). The angularity distribution for OCD

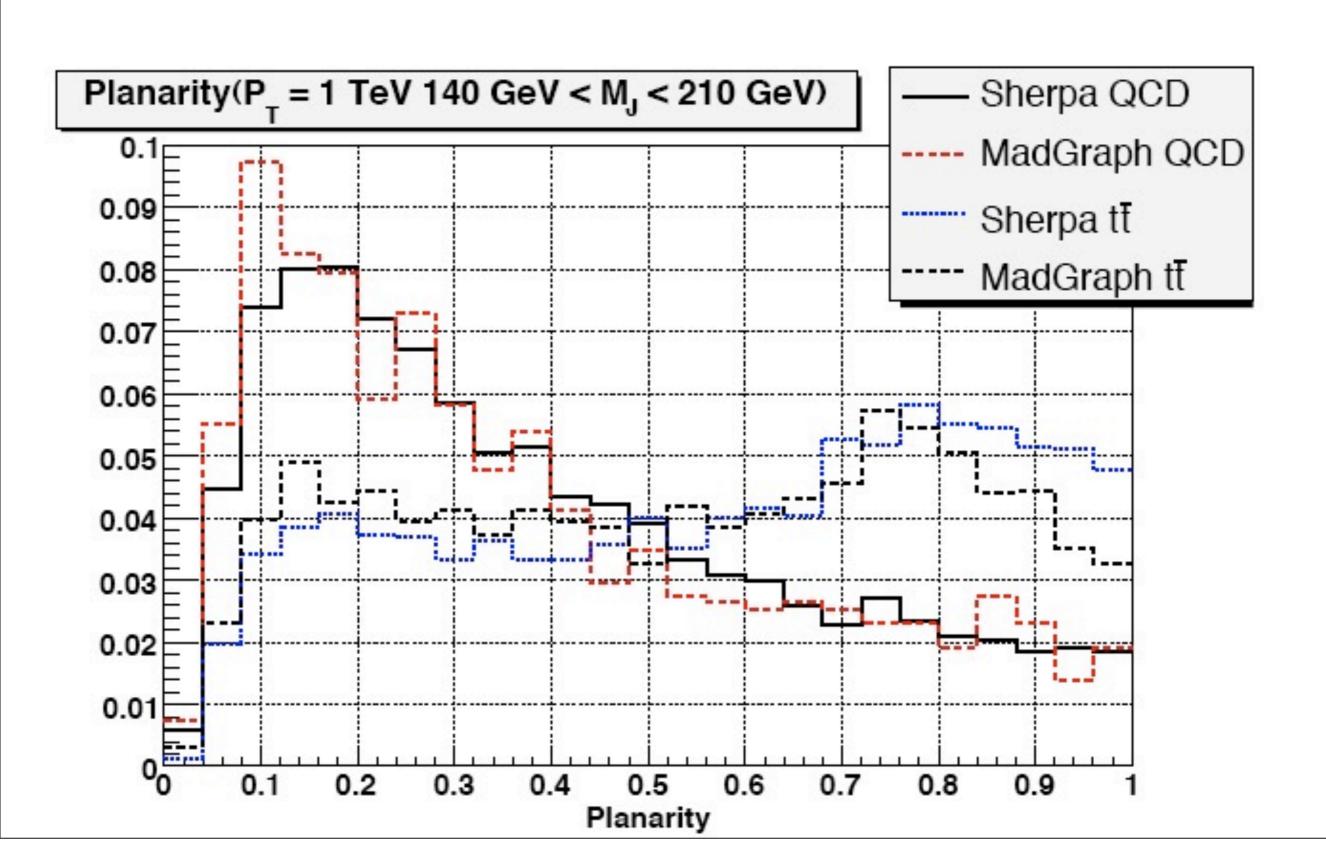
$$\tau_a^{\min}(z) \sim \left(\frac{z}{2}\right)^{1-a}; \quad \tau_a^{\max}(R, p_T) \sim 2^{a-1} R^{-a} z$$

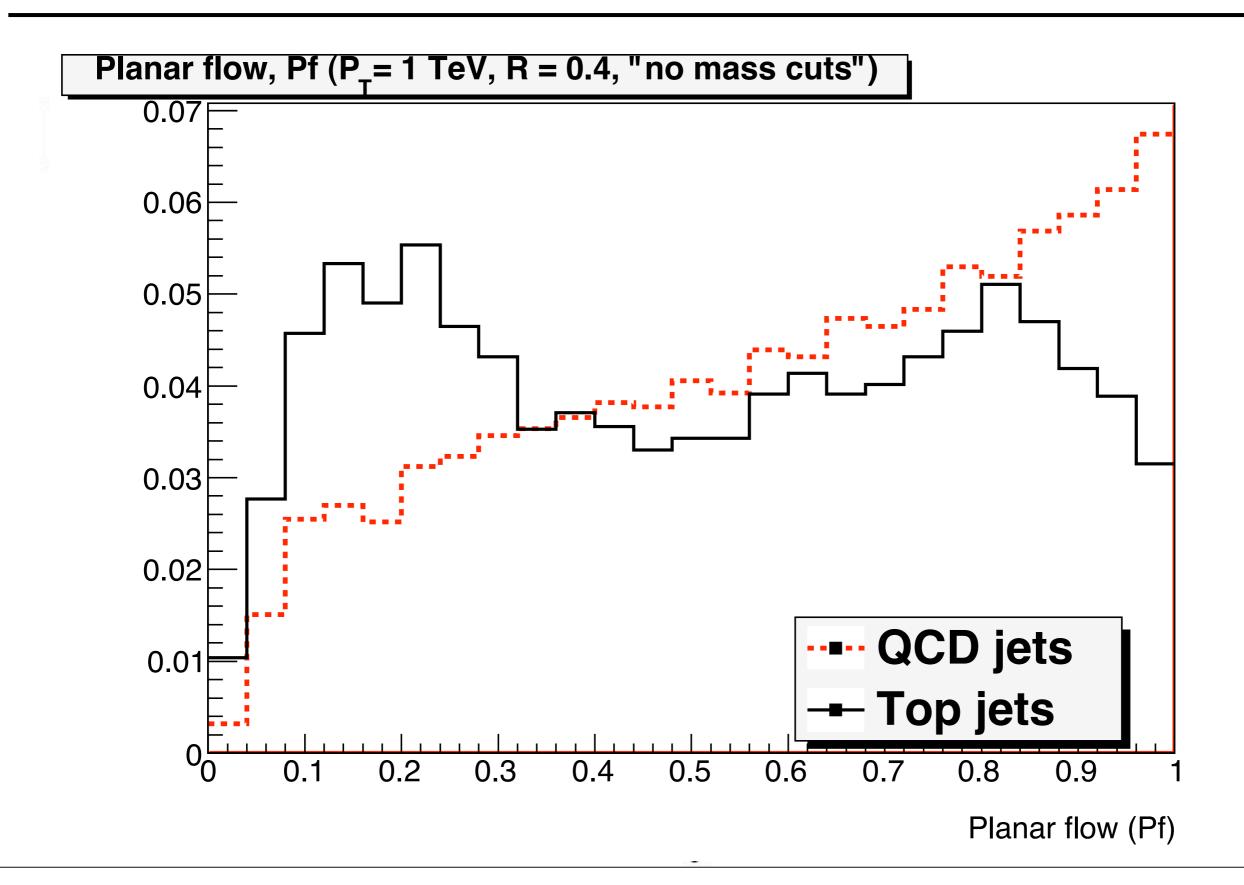
QCD jets vs top jets via planar flow

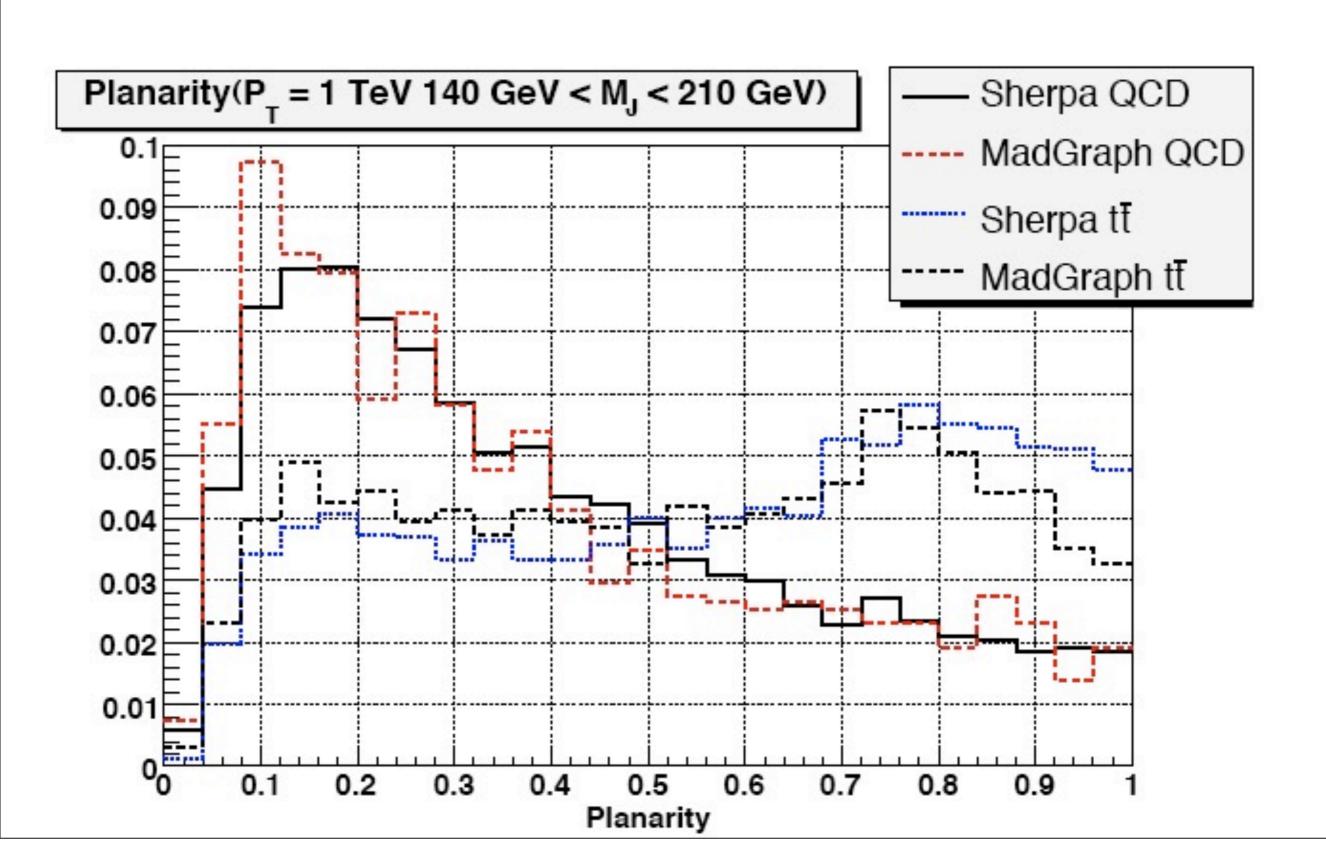
QCD jets are democratic & broad, shown both for cone & anti-kt jets.

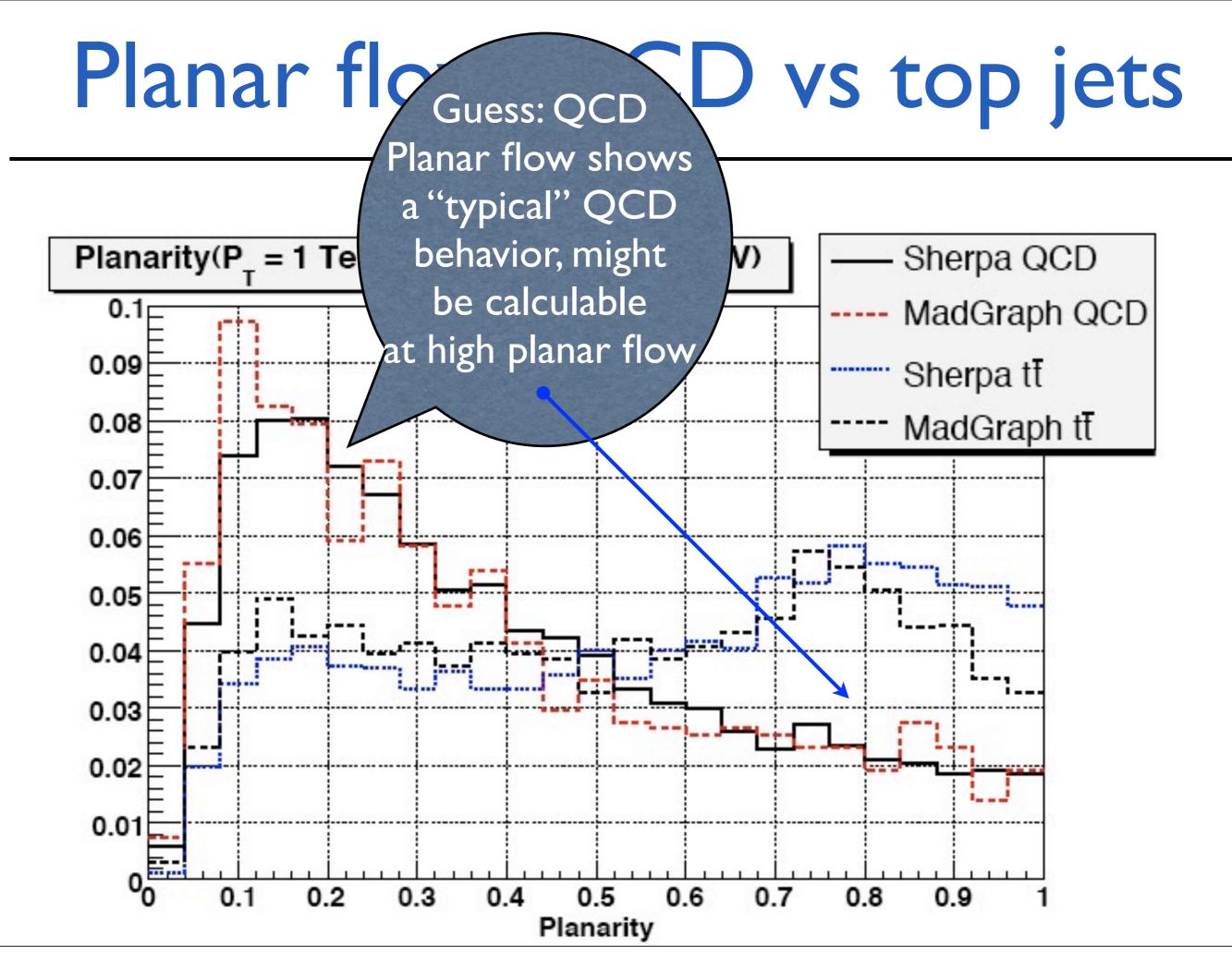


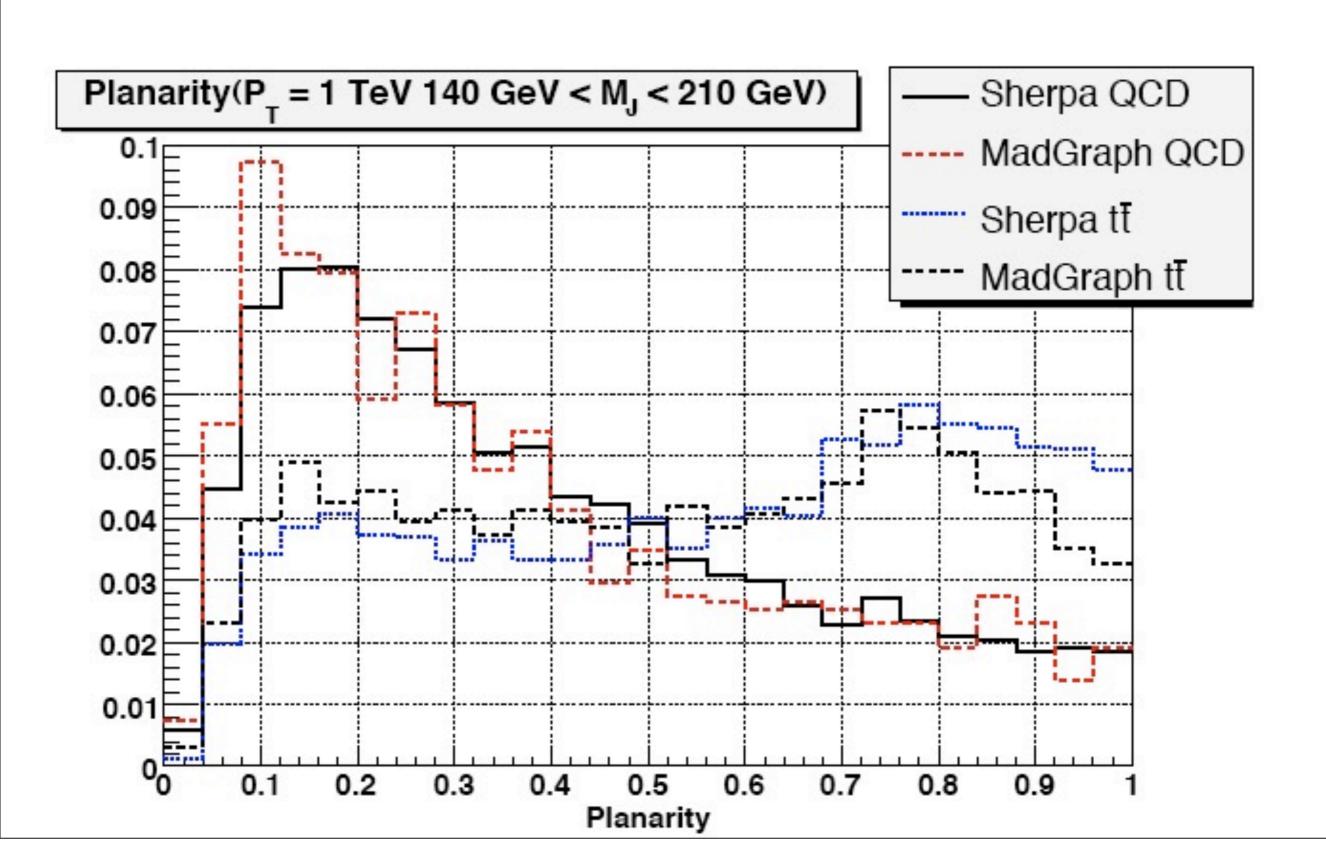
- ◆QCD-linear, top-planar E-deposition in the cone
- ♦ IR-safe E-flow tensor: $I_w^{kl} = \frac{1}{m_J} \sum_i w_i \frac{p_{i,k}}{w_i} \frac{p_{i,l}}{w_i}$
- ightharpoonup Planar flow: $Pf = \frac{4 \det(I_w)}{\operatorname{tr}(I_w)^2} = \frac{4 \lambda_1 \lambda_2}{(\lambda_1 + \lambda_2)^2}$

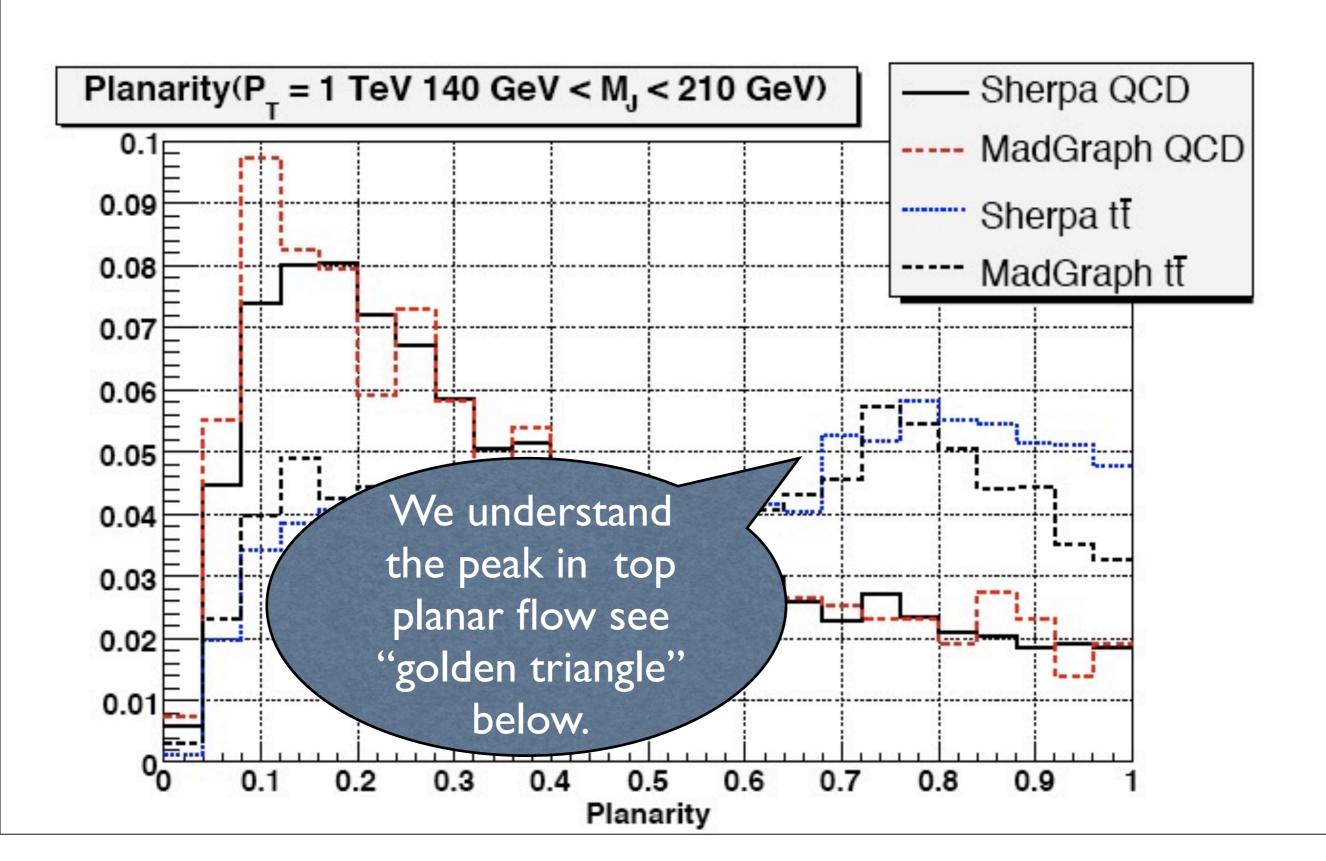












Boosted massive jets @ CDF



R, Alon, E. Duchovni, GP & P. Sinervo, for the CDF; blessed preliminary data;

The data to be looked at

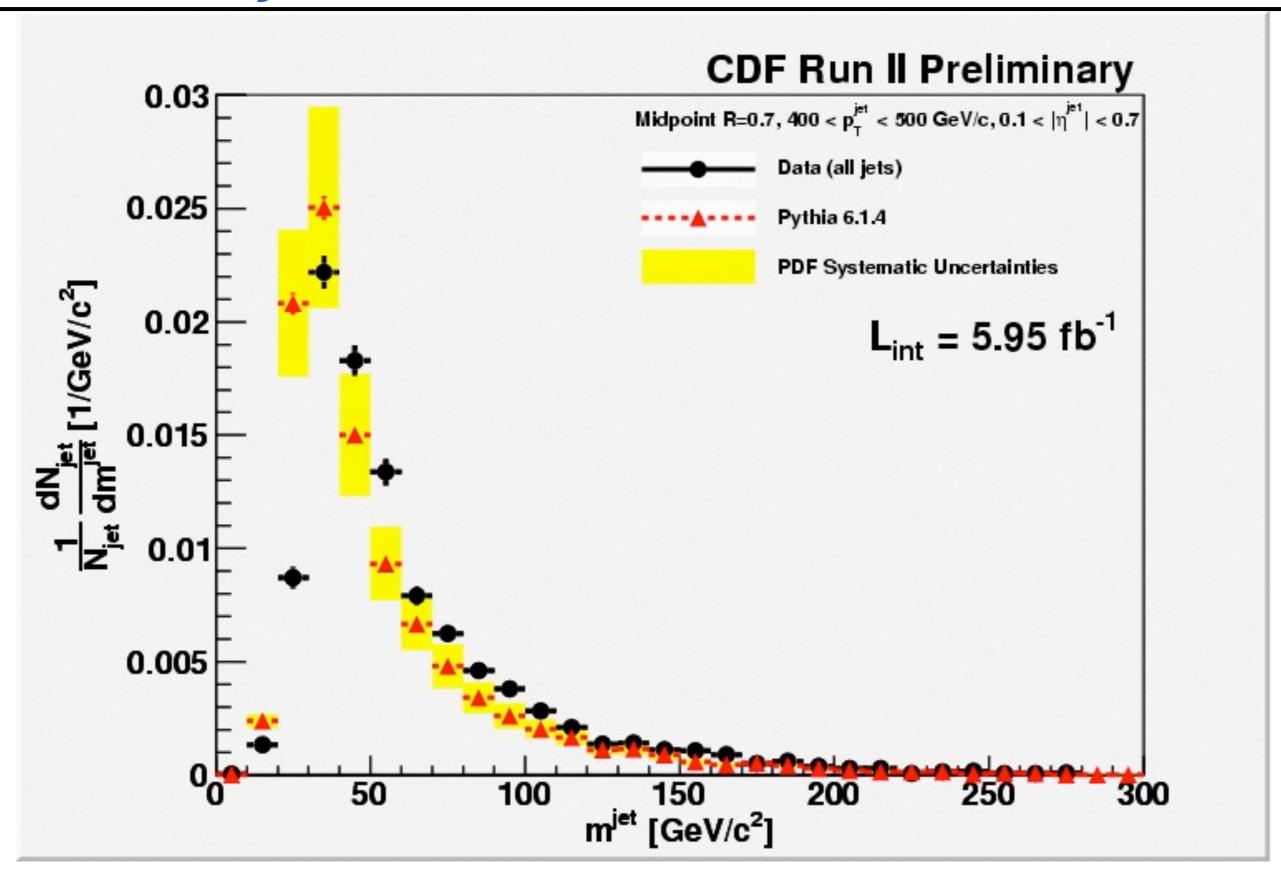
CDF Preliminary

Cut Flow		
All Data, 5.95 fb ⁻¹	75,764,270 events	
	R = 0.4	R = 0.7
At least one jet with $p_T > 400$ GeV/c, $0.1 < \eta < 0.7$, and event quality cuts	3136 events	3621 events
$ m m^{jet2}$ < 100 GeV/c ² and S_{MET} < 4 (with p_T^{jet2} > 100 GeV/c and MI corrections)	2579 events	2576 events

CDF Preliminary

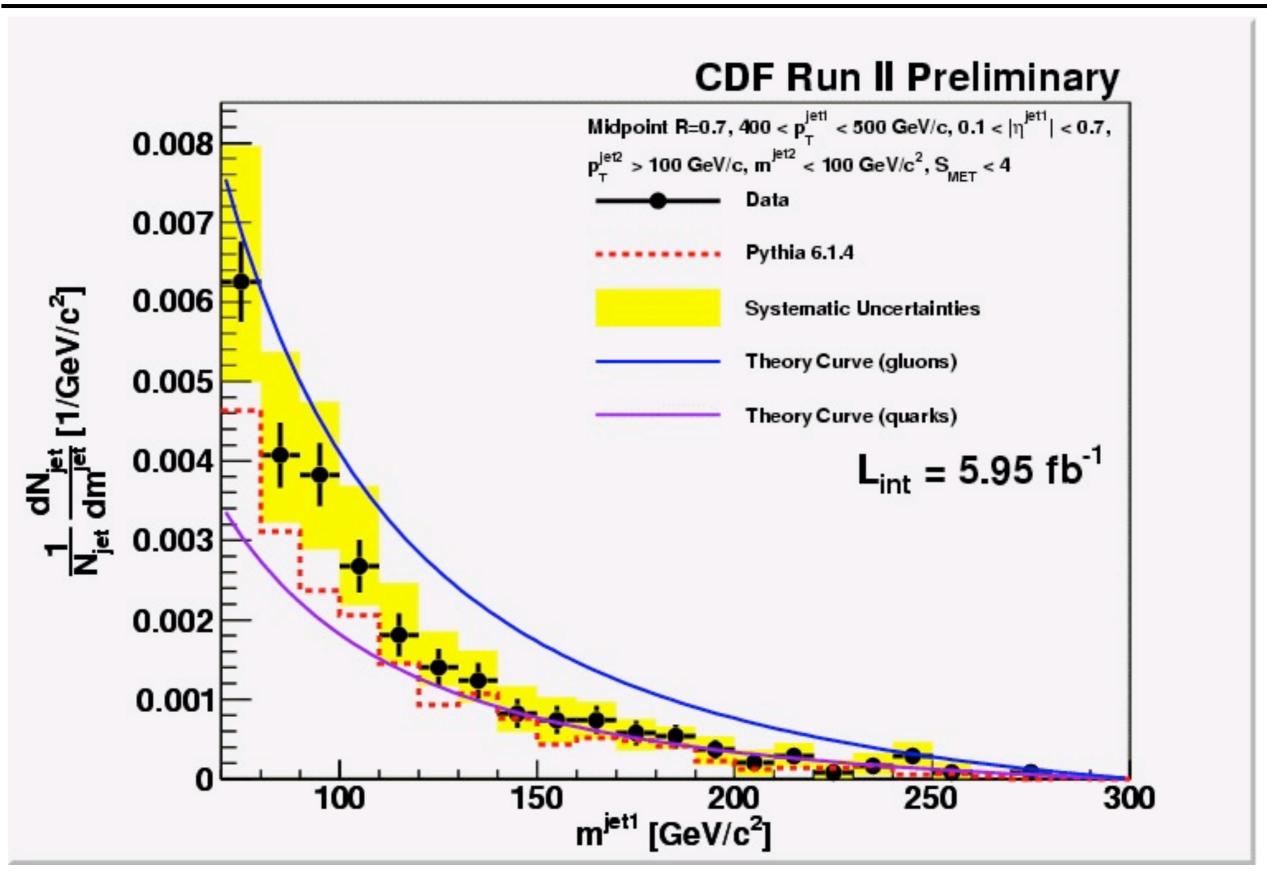
Events with at least one jet within \boldsymbol{p}_T interval and 0.1 $<\!\! \eta \!<$ 0.7 and passing top rejection cuts		
p _T interval (GeV/c)	R = 0.4	R = 0.7
$400 < p_T < 500$	2428 events	2431 events
$p_{T} > 500$	151 events	145 events

Jet mass distribution

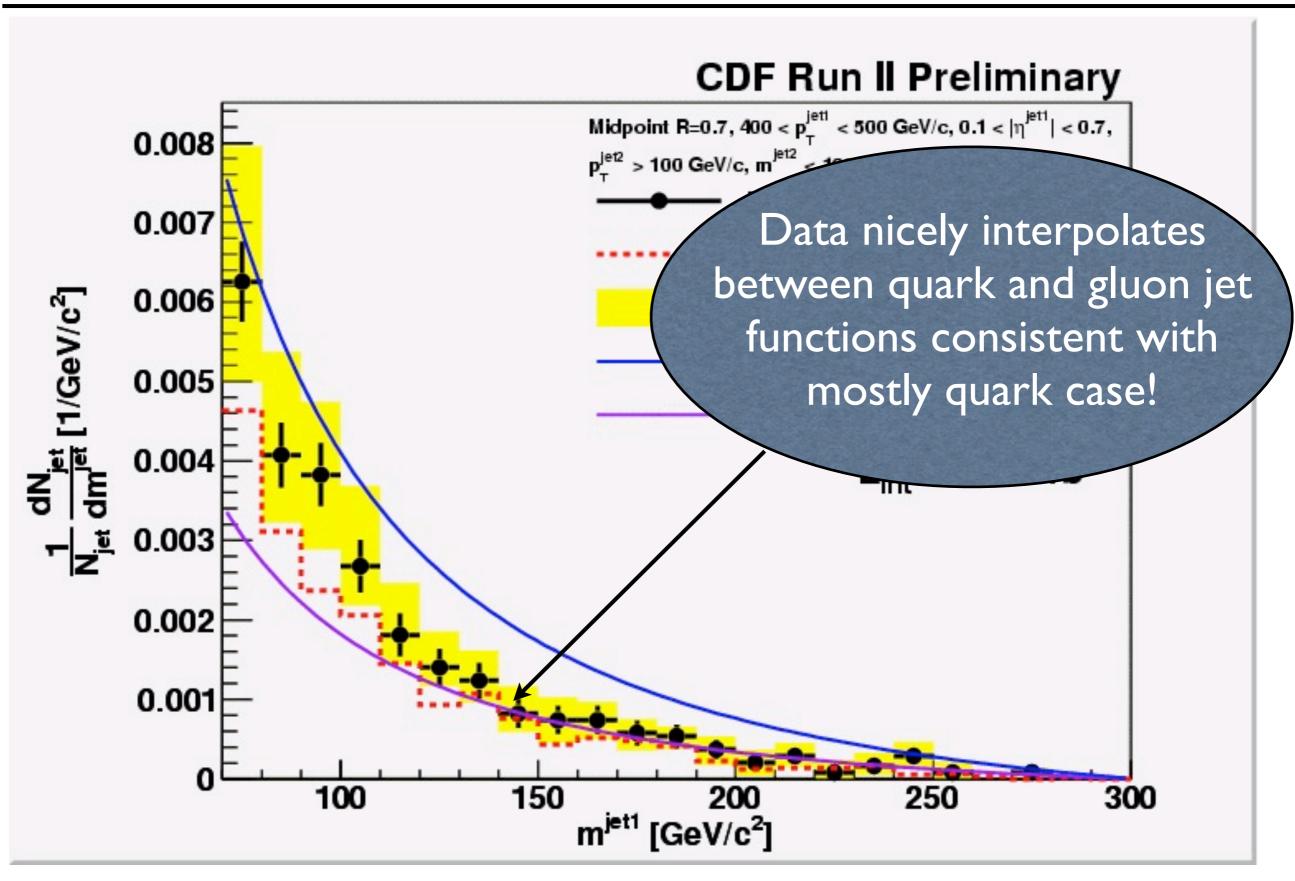


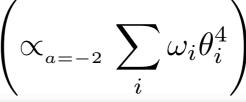
Distribution of jet mass after MI correction for jets with $400 < p_T < 500$ GeV/c, cone R=0.7, data and QCD MC

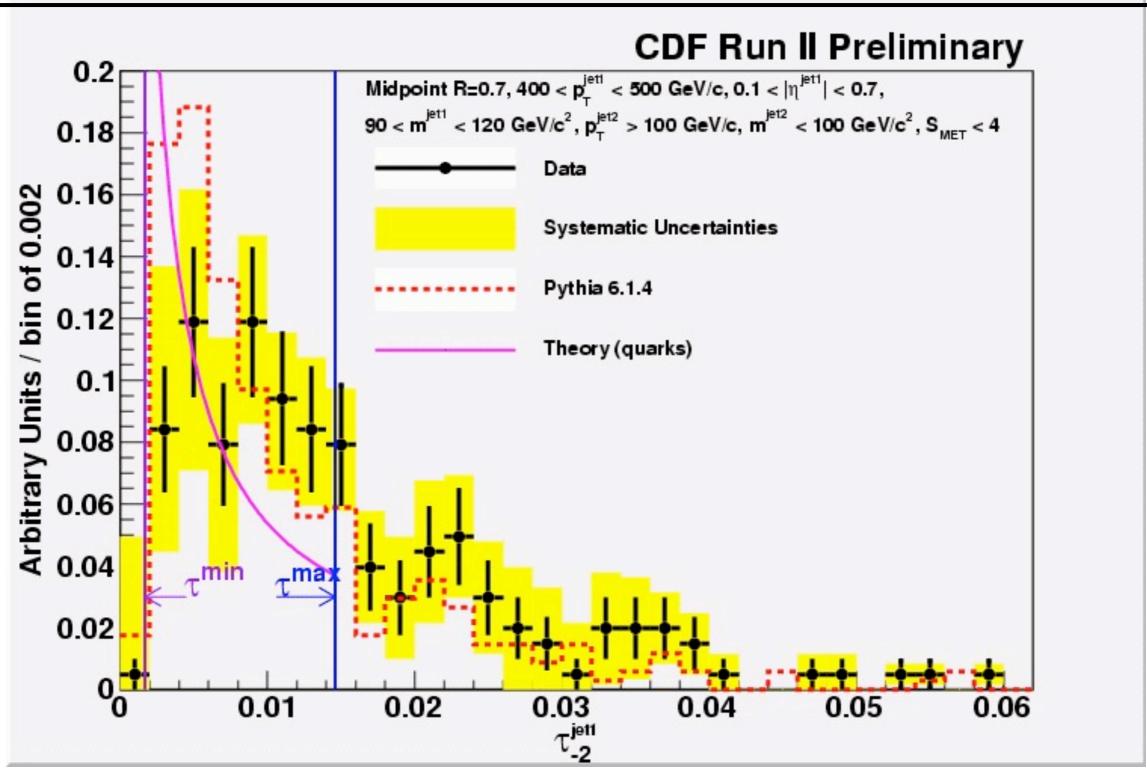
Jet mass distribution, high mass region



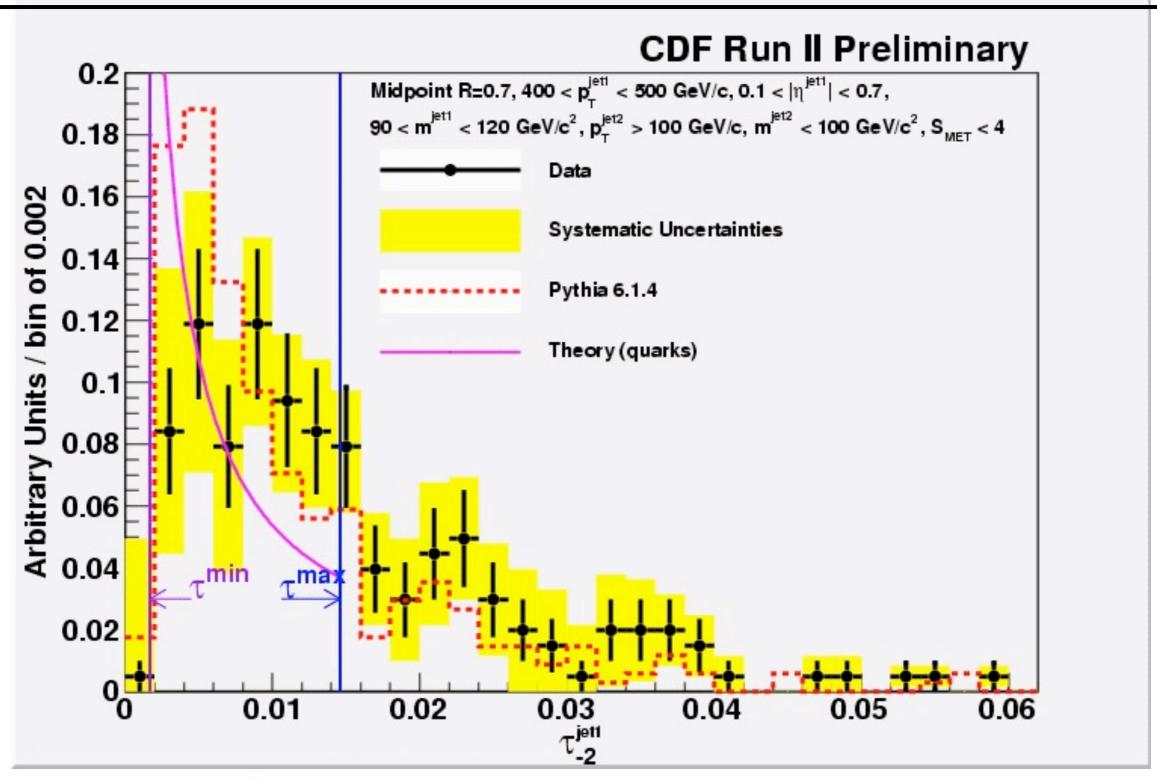
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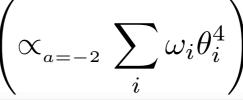


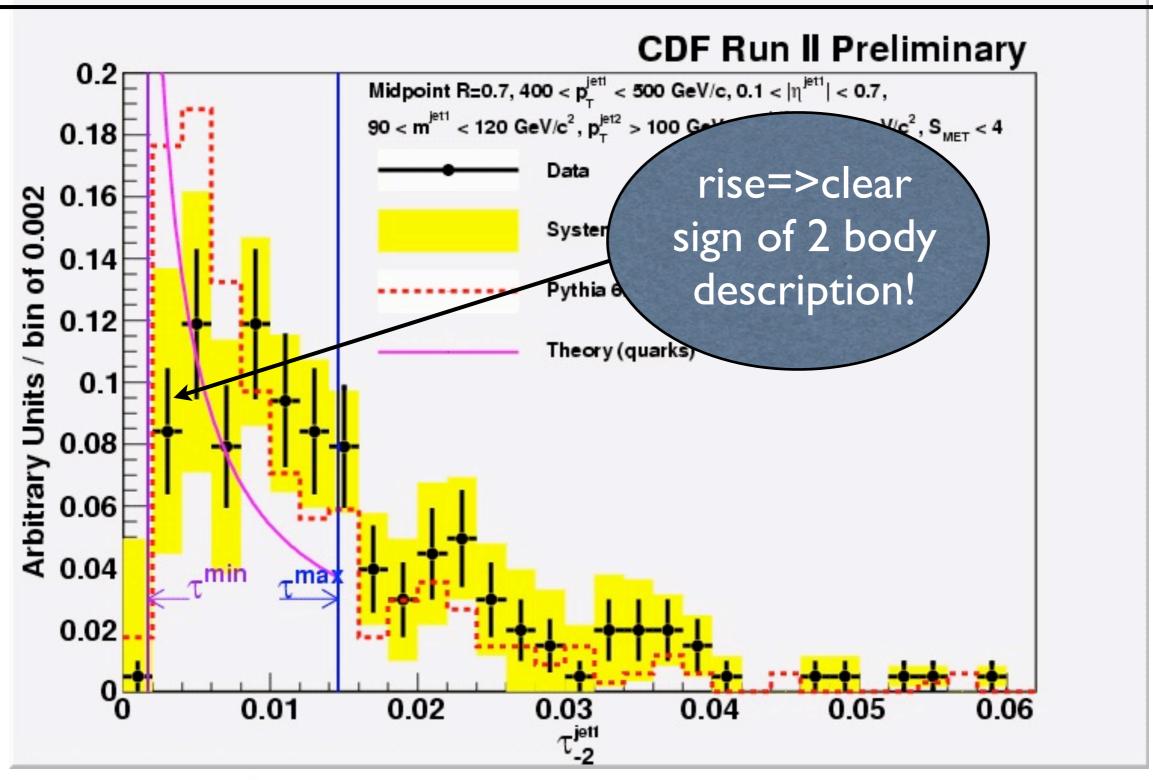


$$\left(\propto_{a=-2} \sum_{i} \omega_{i} \theta_{i}^{4} \right)$$

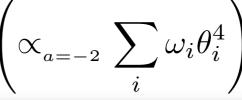


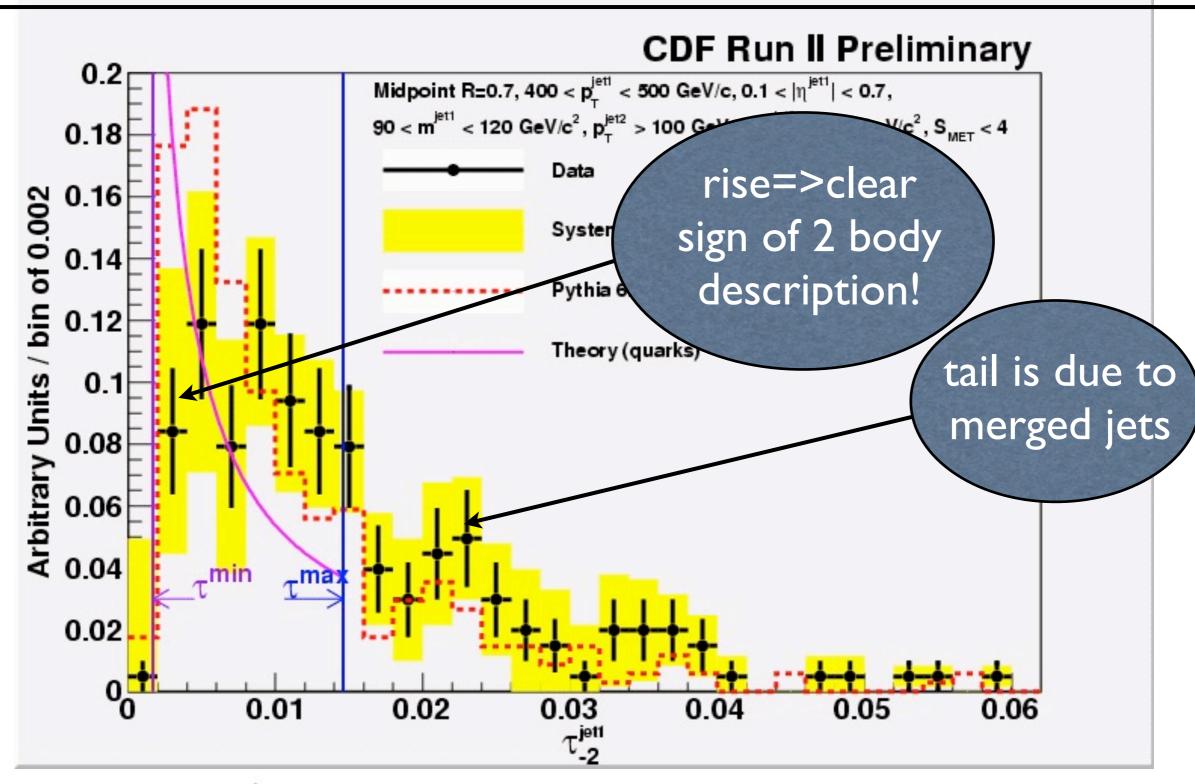
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, $\tau_a^{\max}(R, p_T) \sim 2^{a-1}R^{-a}z$





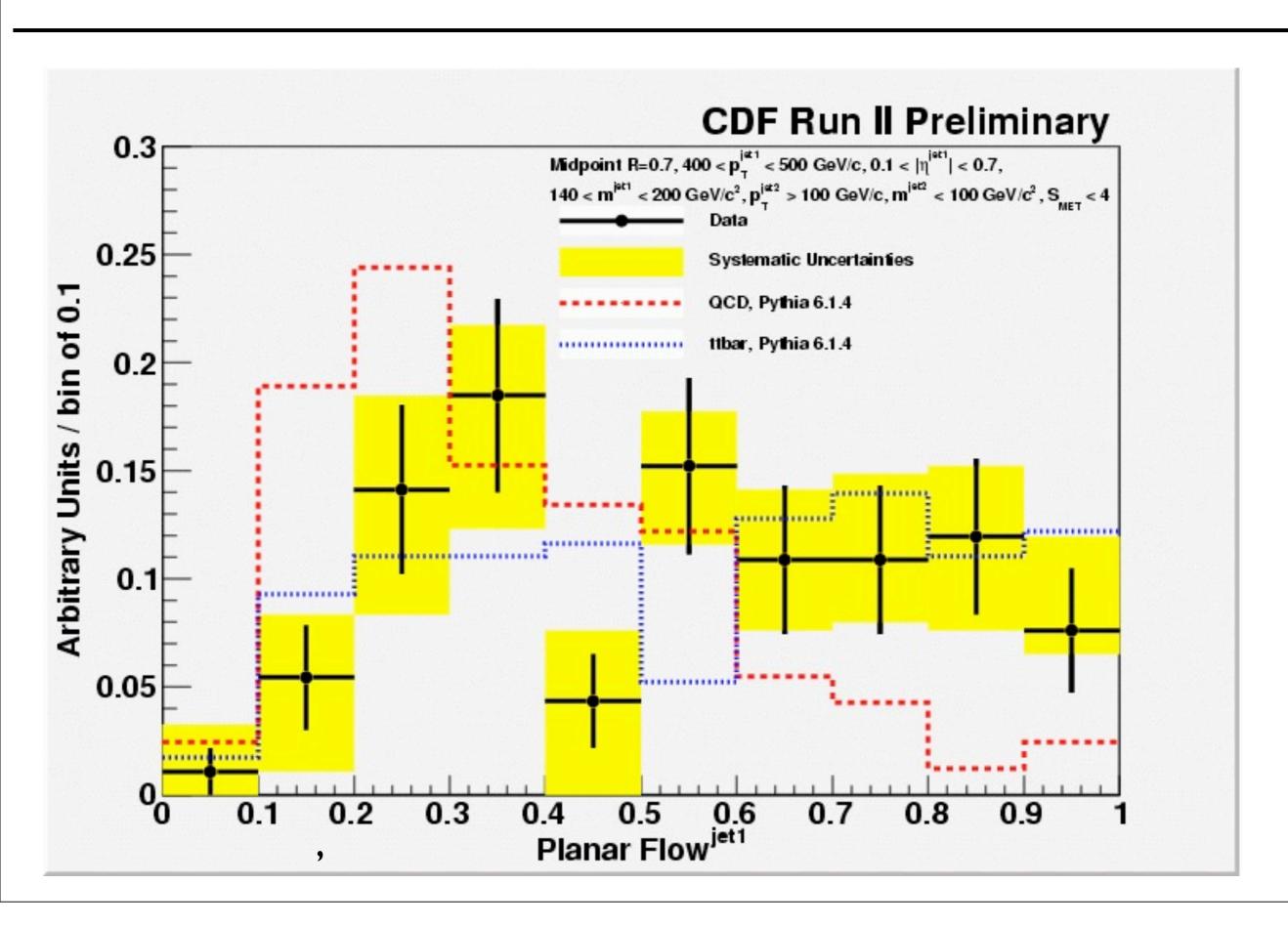
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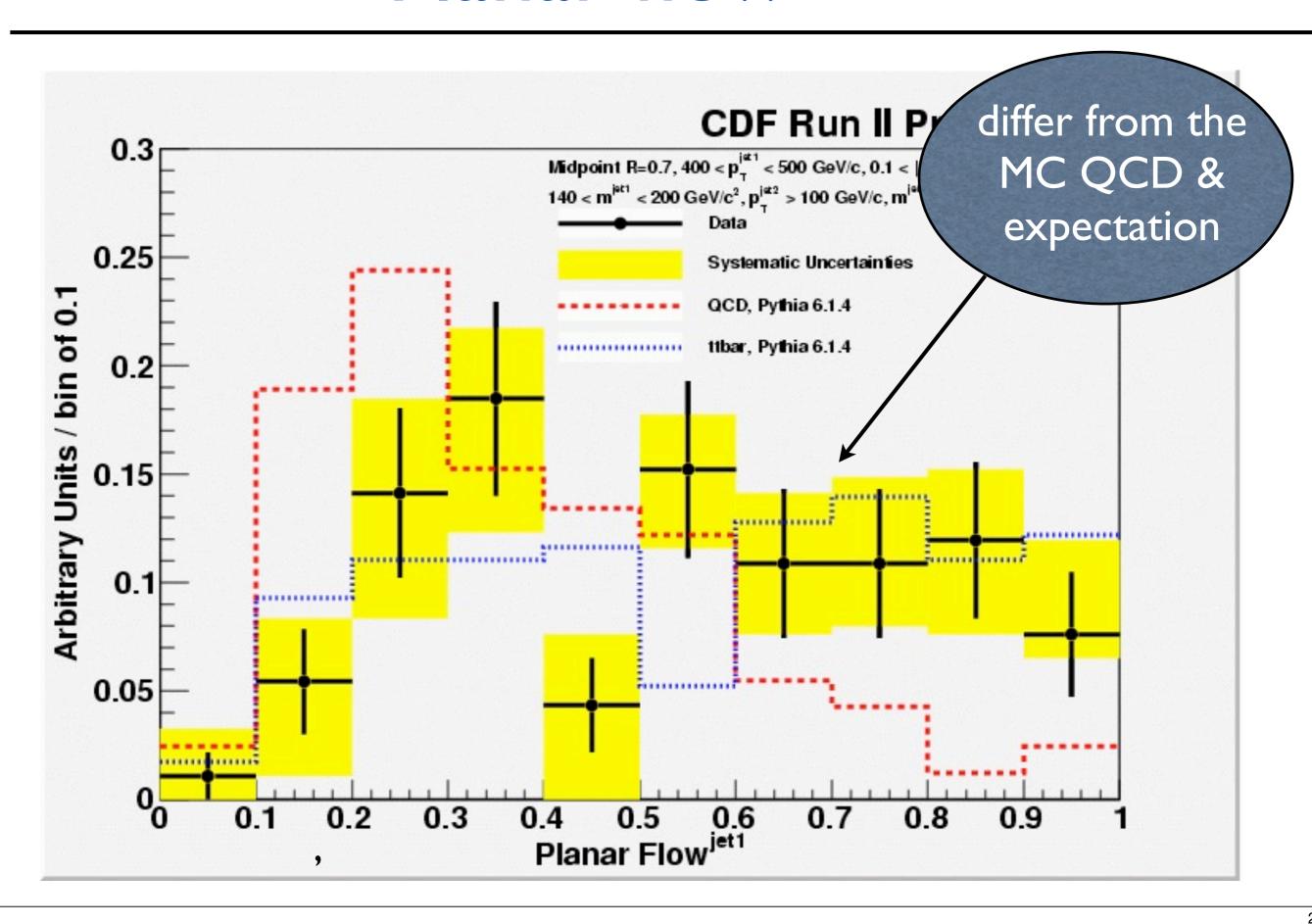


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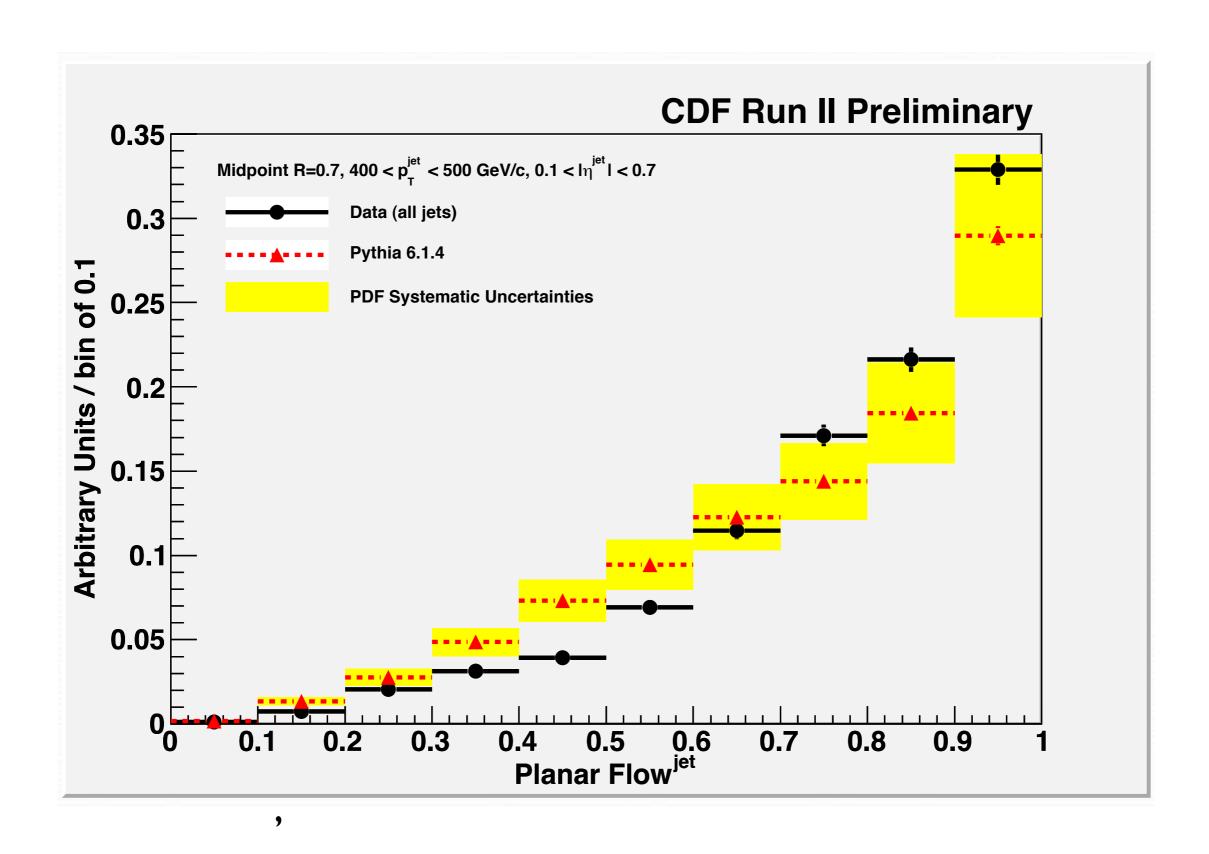
Planar flow



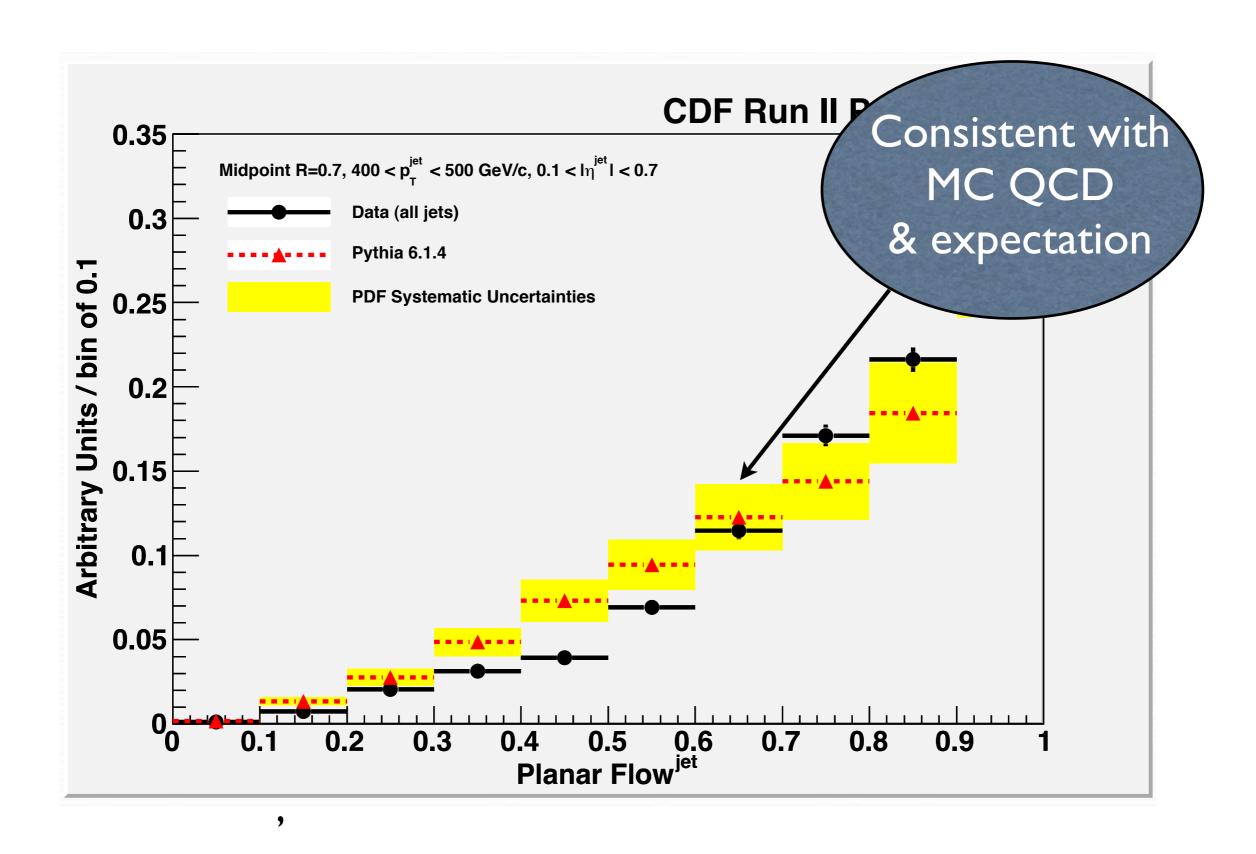
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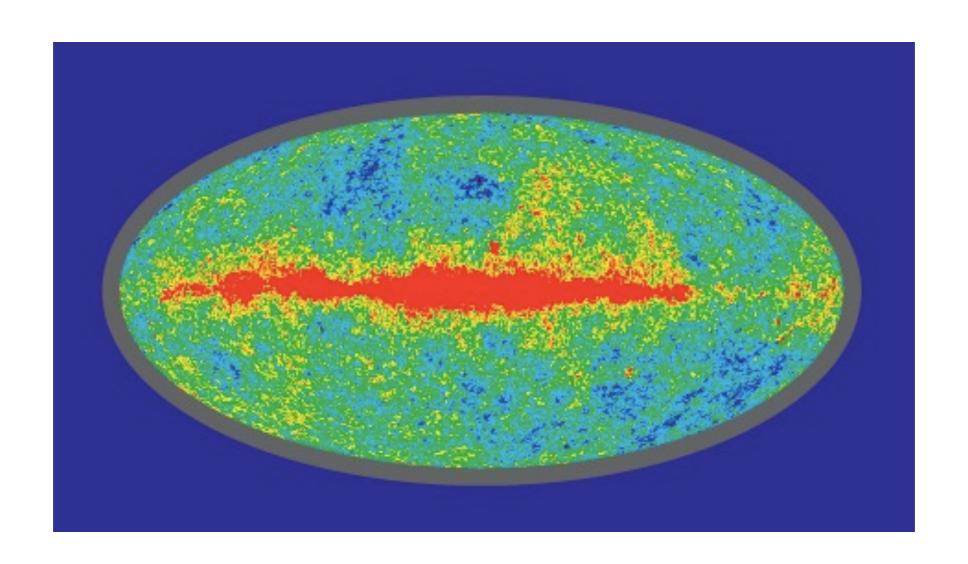
Planar flow, no mass cut



Planar flow, no mass cut



Template Method



Template Overlap Method

ightharpoonup Pf/ angularity are 2 variables in a multi-body kinematical-variable phase-space => info' is lost.

Can we be more systematic in our approach? Fixing jet mass & pT @ LO in PQCD: single parameter for 2-pronged decay; four (5 without W mass) parameters for 3 pronged decay.

Template Overlap Method

Template overlap: functional measure of how well jet-energy-flow matches flow of a certain template calculated from 1st principle (LO, partonic)

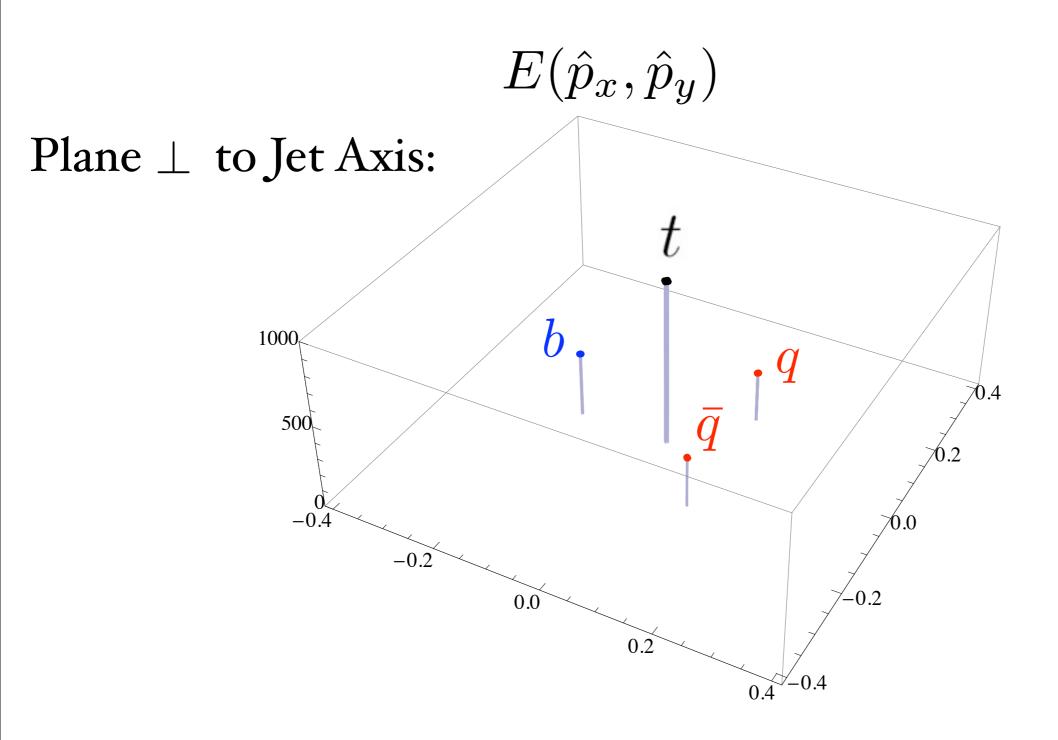
$$|t>$$
 = top distribution
 $|g>$ = massless QCD distribution

We need a probe distribution, |f>, such that

$$R = \left(\frac{\langle f|t\rangle}{\langle f|g\rangle}\right)$$
 is maximized.

general overalp functional: $Ov(j, f) = \langle j | f \rangle = \mathcal{F}\left[\frac{dE(j)}{d\Omega}, \frac{dE(f)}{d\Omega}\right]$

Example, top jet: "Golden Triangle"



Template Overlap Method

- Any region of partonic phase space for the boosted decays, {f}, defines a template
- Ansatz: good (if not best) rejection power using signal distribution for templates
- Define "template overlap" as the maximum functional overlap of j to a state f[j]:

$$Ov(j, f) = \max_{\{f\}} \mathcal{F}(j, f)$$

 \diamond Can match arbitrary final states j to partonic partners f[j] at any given order in PQCD.

Constructing a functional

♦ A natural measure of the matching between

state j and the template: weighted difference of their energy flows (employ a Gaussian)

$$Ov^{(F)}(j,f) = \max_{\tau_n^{(R)}} \ \exp \left[-\frac{1}{2\sigma_E^2} \left(\int d\Omega \ \left[\frac{dE(j)}{d\Omega} - \frac{dE(f)}{d\Omega} \right] F(\Omega,f) \right)^2 \right]$$

Alternatively, we may choose F to be a normalized step function around the directions of the template momenta p_i

for a given template, with direction of particle a, \hat{n}_a & its energy $\mathsf{E}^{\scriptscriptstyle (f)}$ a:

$$Ov(j, p_1 \dots p_n) = \max_{\tau_n^{(R)}} \exp \left[-\sum_{a=1}^n \frac{1}{2\sigma_a^2} \left(\int d^2 \hat{n} \, \frac{dE(j)}{d^2 \hat{n}} \theta(\hat{n}, \hat{n}_a^{(f)}) - E_a^{(f)} \right)^2 \right]$$

for an n-particle final state

Construct template: three particle phase space

for top decay
$$t \rightarrow b + W \rightarrow b + q + \bar{q}$$
. with $(p_q + p_{\bar{q}})^2 = M_W^2$

- 4 d.o.f.: most straightforward method by 4 angles:
- I)polar and azimuthal angles that define b and W directions in the top rest frame
- 2)polar and azimuthal angles that define q and qbar directions relative to the boost axis from the W rest frame

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Lorentz transformations => 4 angles identified determine the energies and directions of the three decay products of the top at LO

• jet mass window 160 GeV < m_J <190 GeV, cone size R = 0.5 (D = 0.5 for anti-kT jet), jet energy 950 GeV < E_J < 1050 GeV.

Template Overlap with data discretization

$$Ov(j, f) = \max_{\tau_n^{(R)}} \exp \left[-\sum_{a=1}^{3} \frac{1}{2\sigma_a^2} \left(\sum_{k=i_a-1}^{i_a+1} \sum_{l=j_a-1}^{j_a+1} E(k, l) - E(i_a, j_a)^{(f)} \right)^2 \right]$$

$$\sigma_a = E(i_a, j_a)^{(f)}/2.$$

Ov with top-jet @ partonic level

Proof of principle, nearly a perfect match

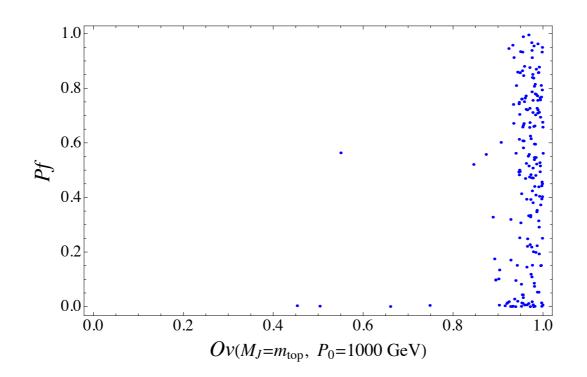
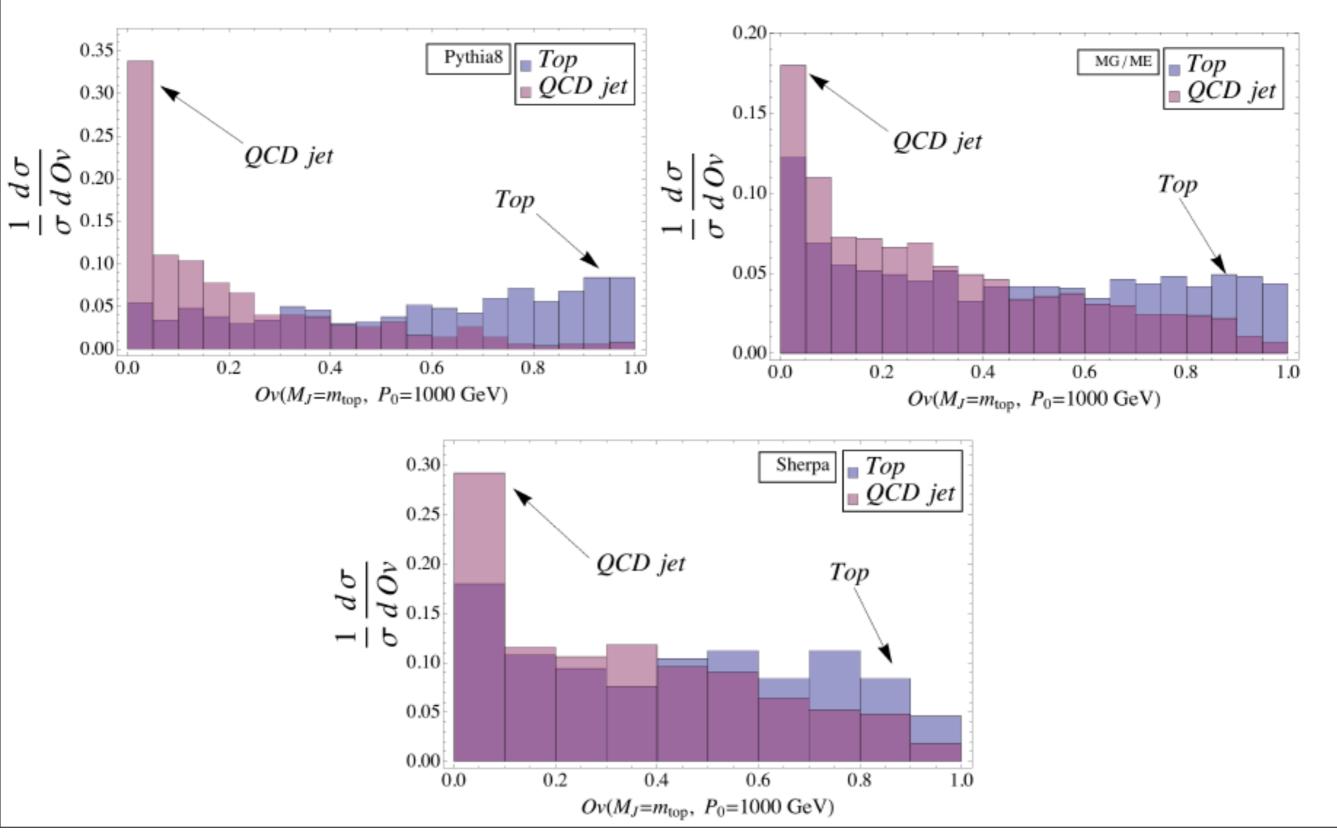


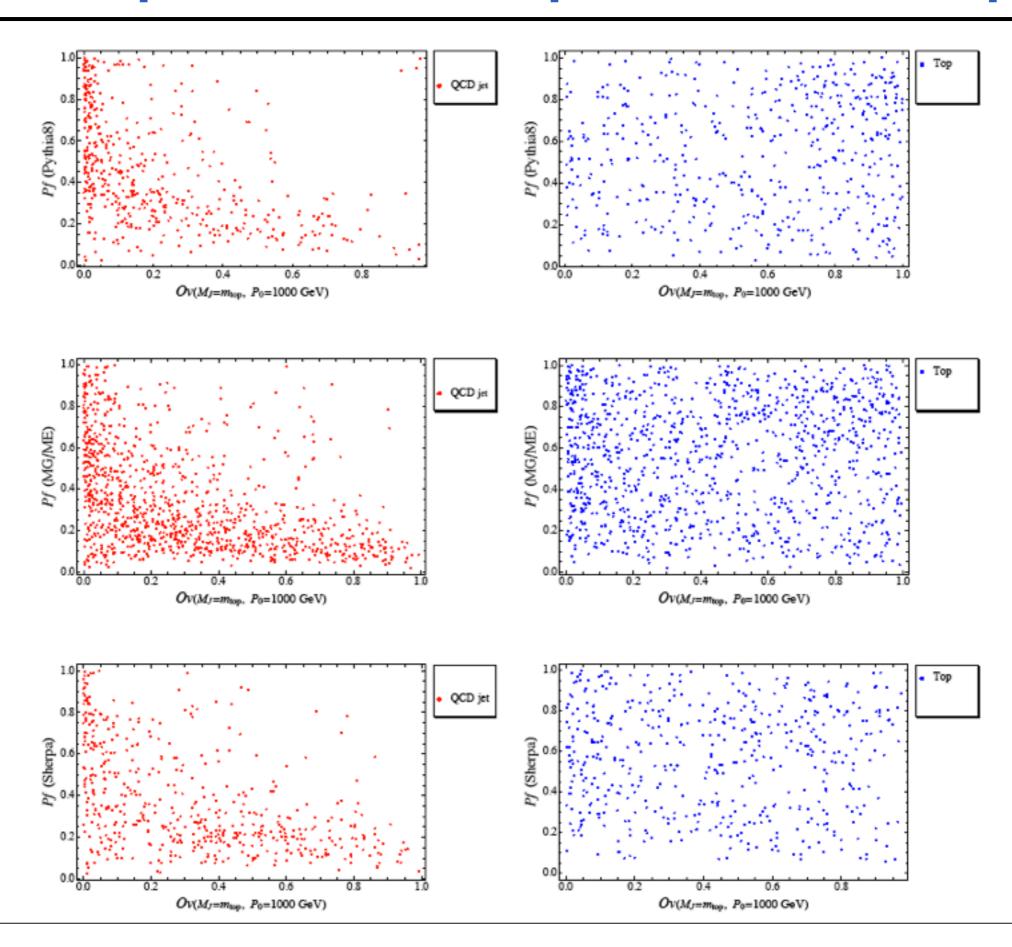
Figure 2: A scatter plot of template overlap, Eq. (6) and Pf for LO parton-level MC output for top quark decay, with $P_0 = 1$ TeV, $m_{top} = 174$ GeV.

Three-particle Templates @ Jet Level (after showering, hadronization etc.)



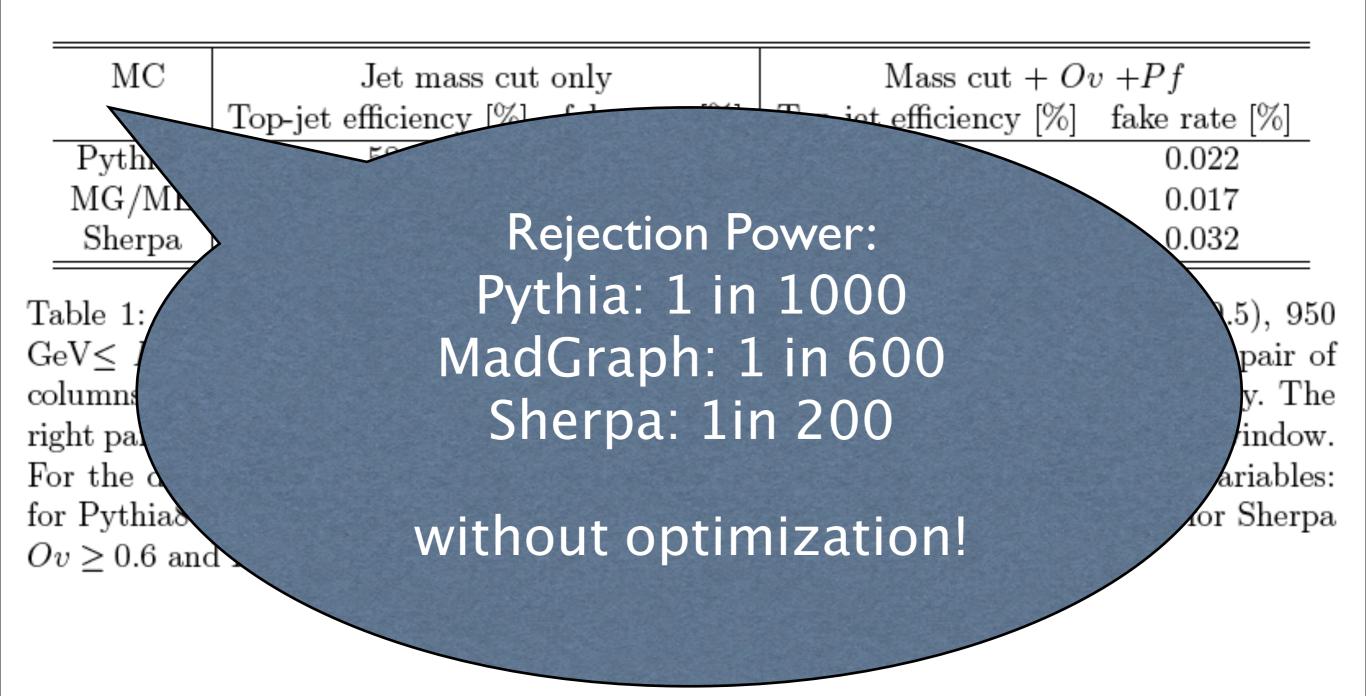
Combine with Planar flow- distinguish between "3-prong" events with large template overlaps.

QCD jets with large Ov tend to have smaller planar flow than top decay events.



MC	Jet mass cut only		Mass cut $+ Ov + Pf$	
	Top-jet efficiency [%]	fake rate $[\%]$	Top-jet efficiency [%]	${\rm fake}\ {\rm rate}\ [\%]$
Pythia8	58	3.6	21	0.022
MG/ME	52	3.7	11	0.017
Sherpa	34	3.2	7	0.032

Table 1: Efficiencies and fake rates for jets with R=0.5 (using anti- k_T : D=0.5), 950 GeV $\leq P_0 \leq 1050$ GeV, 160 GeV $\leq m_J \leq 190$ GeV and $m_{top}=174$ GeV. The left pair of columns shows efficiencies and fake rates found by imposing the jet mass window only. The right pair takes into account the effects of cuts in Ov and Pf in addition to the mass window. For the different MC simulations, we have imposed various cuts on Ov and Pf variables: for Pythia8 $Ov \geq 0.6$ and $Pf \geq 0.4$, for MG/ME $Ov \geq 0.7$ and $Pf \geq 0.39$ and for Sherpa $Ov \geq 0.6$ and $Pf \geq 0.48$.

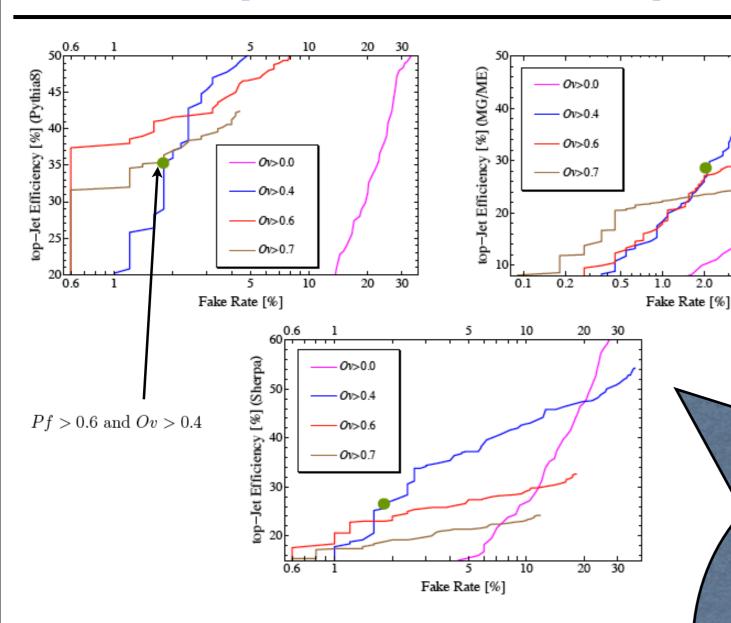


Template method among highest rejection powers.

Template method among highest rejection powers.

Method theoretically defined, while no strong dependence on jet-reconstruction & no manipulation of soft radiation is made!

10.0



different generators yield different energy flow patterns.

caution regarding interpretation of tests for all methods; especially those that rely heavily on the anticipated structure of soft radiation in final states

♦ Template method allows for systematic

improvement:

e.g. by incorporating the effect of gluon emission in the template, or by weighting phase space by squared matrix elements.

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Can also optimize the cut for getting higher rejection power

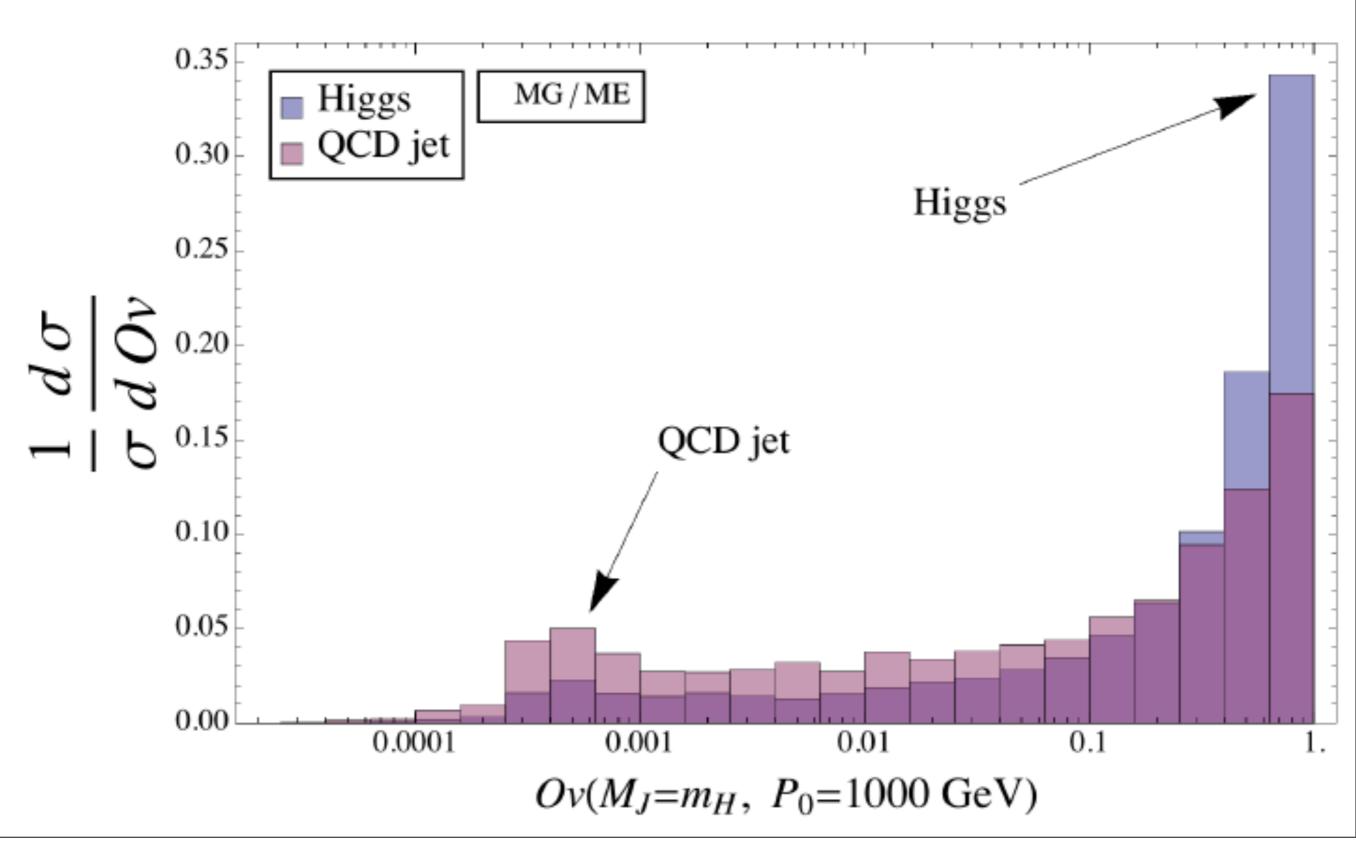
Construct template: two particle phase space

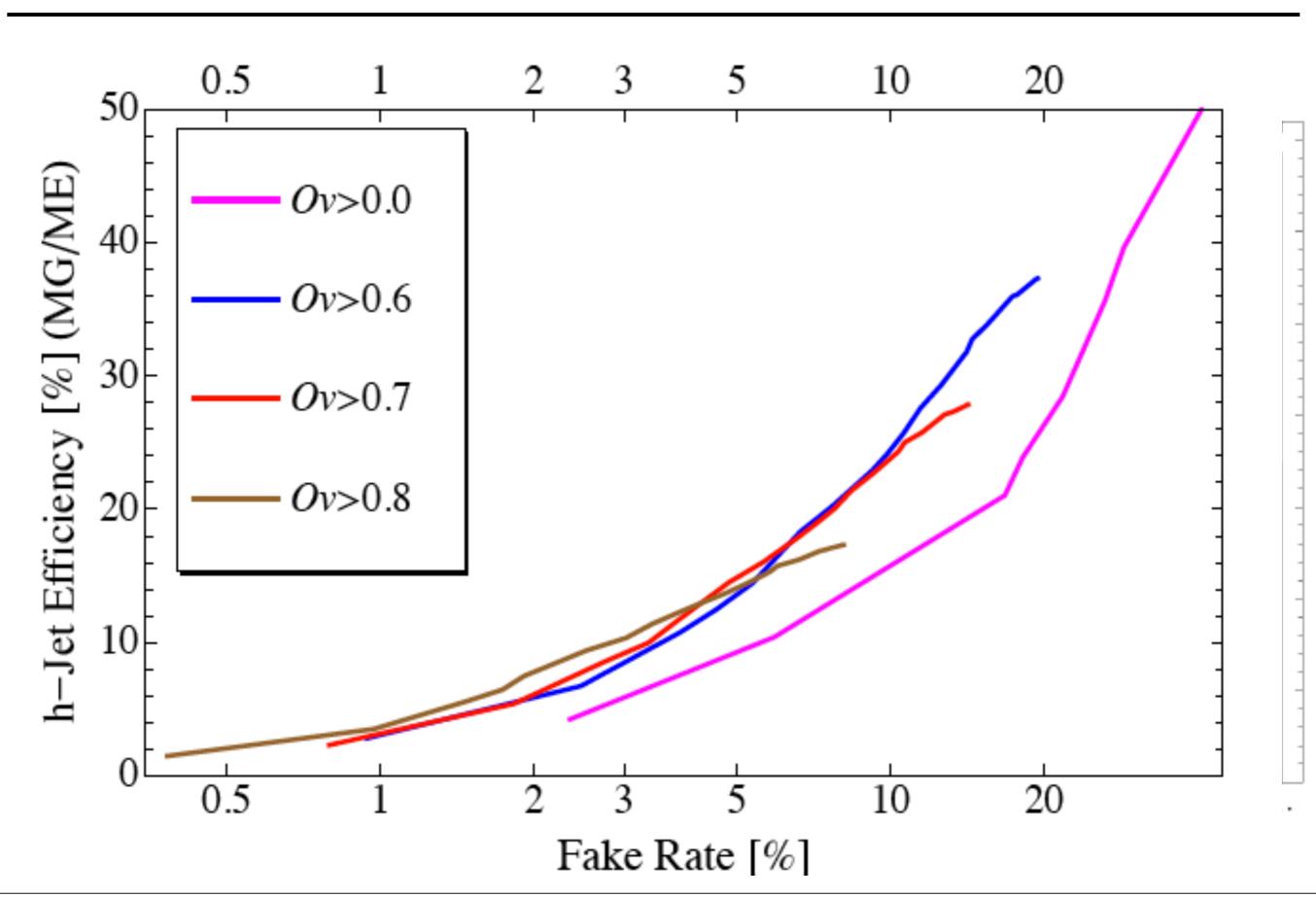
for top decay
$$|f\rangle = |h\rangle^{\text{(LO)}} = |p_1, p_2\rangle$$

- ♦ Higgs: at fixed $z = m_J/P_0 <<1$, Θ_s distribution is peaked around Θ_s in its minimum value
- => decays "democratic" (sharing energy evenly) $\frac{dJ^h}{d\theta_s} \propto \frac{1}{\theta_s^3}$
- lack lowest-order QCD events is also peaked, but much less so $dJ^{
 m QCD}$ 1

- jet mass window II0 GeV < m_J < I30 GeV, cone size R = 0.4 (D = 0.4 for anti-kT jet), jet energy 950 GeV < E_J < I050 GeV.
- ♦ Template Overlap with data discretization

$$Ov(j,f) = \max_{\tau_n^{(R)}} \exp \left[-\sum_{a=1}^2 \frac{1}{2\sigma_a^2} \left(\sum_{k=i_a-1}^{i_a+1} \sum_{l=j_a-1}^{j_a+1} E(k,l) - E(i_a,j_a)^{(f)} \right)^2 \right]$$

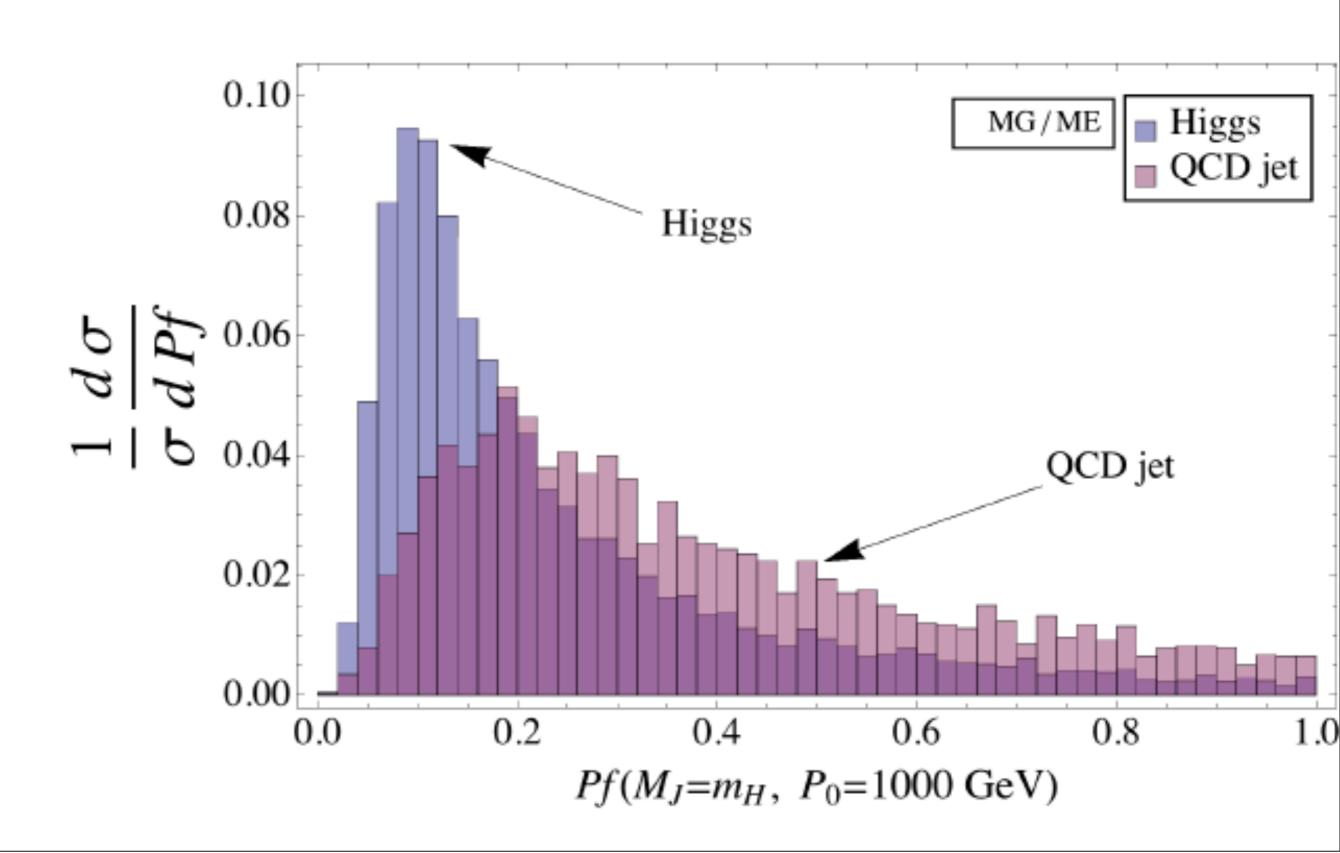


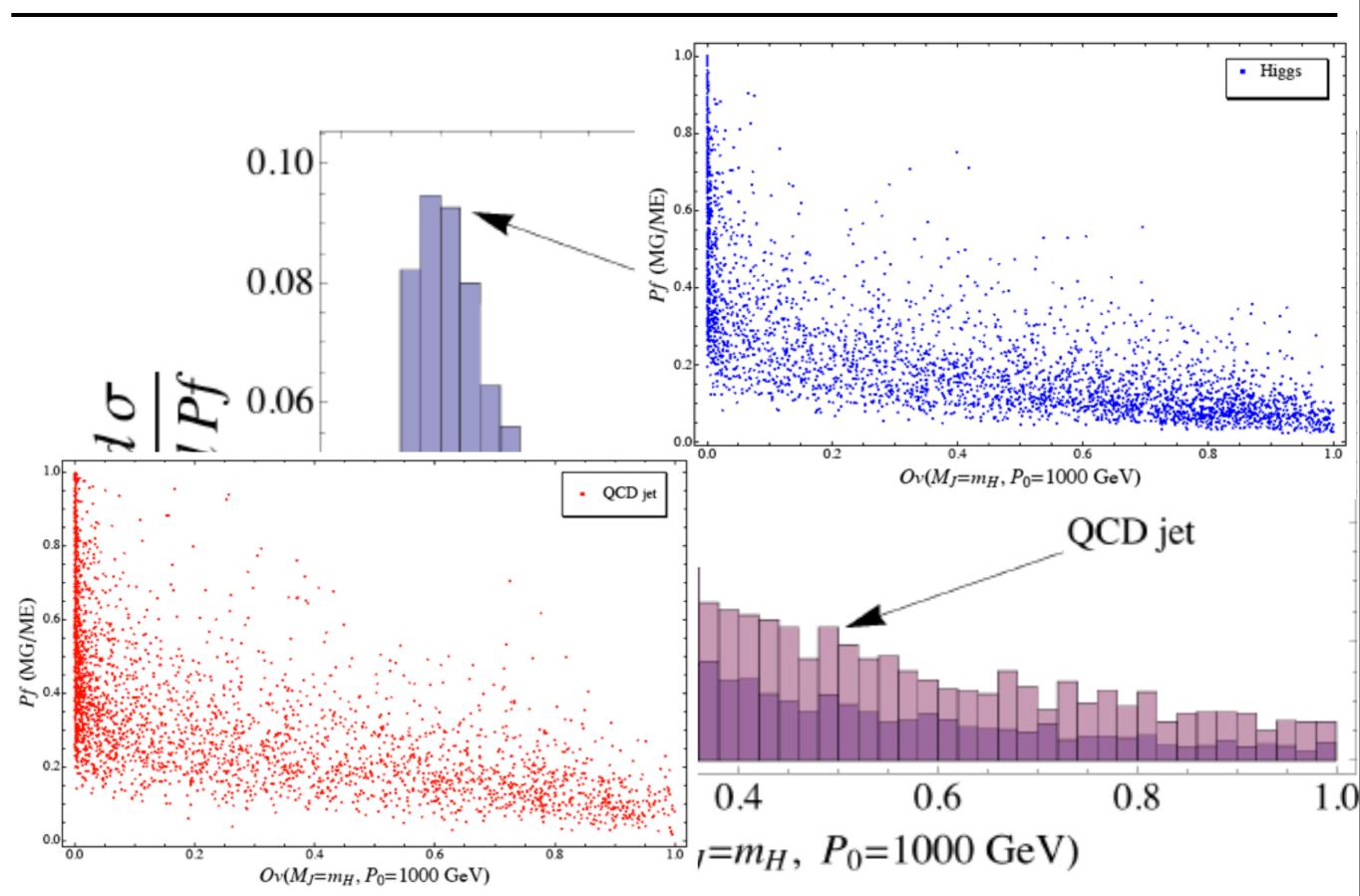


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- The templates can be systematically improved by including the effects of gluon emissions, which contain color flow information
- The effects of higher-order effects can be partly captured by using Planar flow

(expect soft radiation from the boosted color singlet Higgs to be concentrated between the b and bbar decay products, in contrast to QCD light jet)

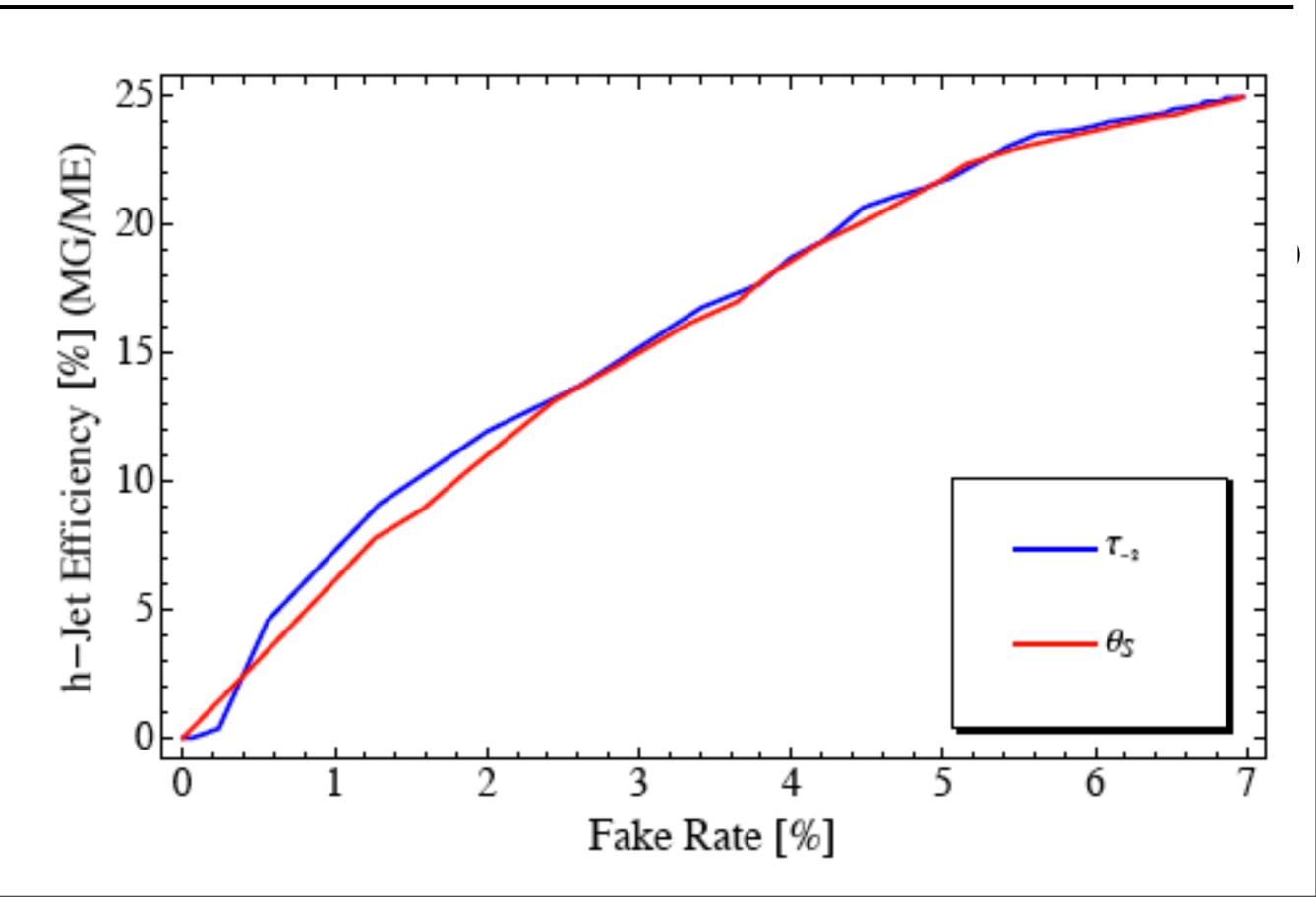


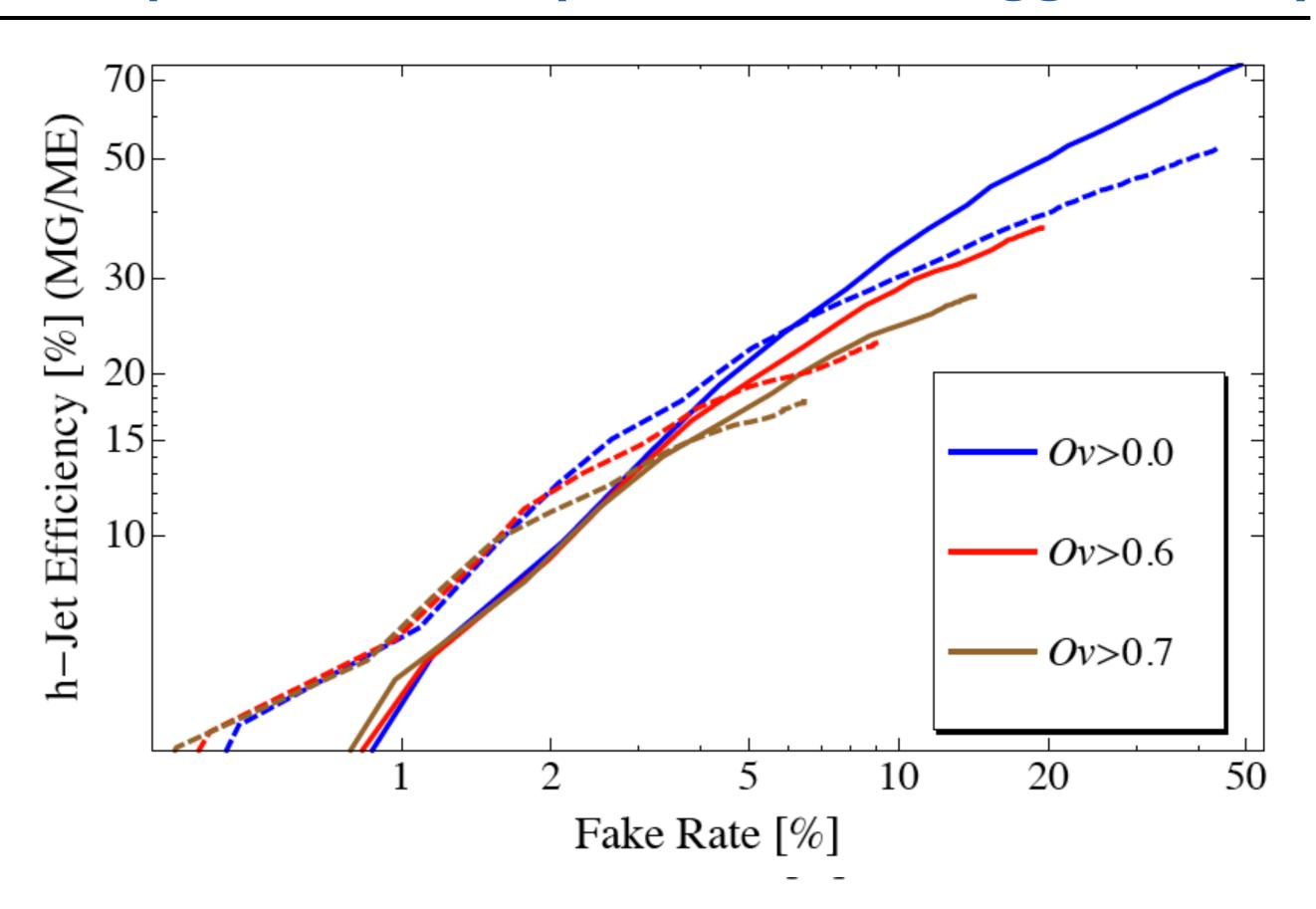


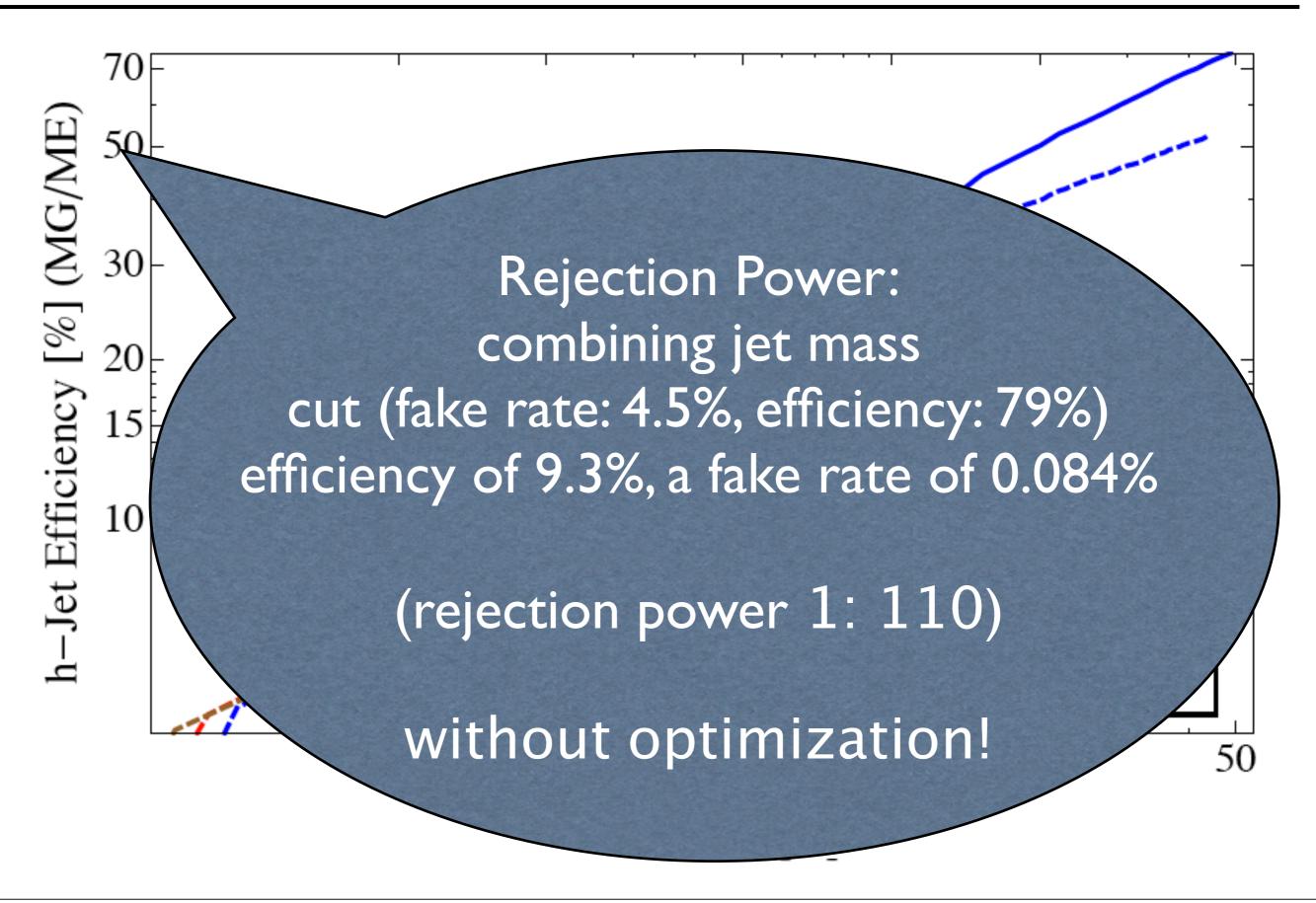
♦ Combined with angularity or Θ_s : can improved rejection power (Θ_s and angularities are related)

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♦ Compared to angularities, Θ_s is a parameter for two-body template states, which already provides useful information on physical states, as well as a clear picture of their energy flow.

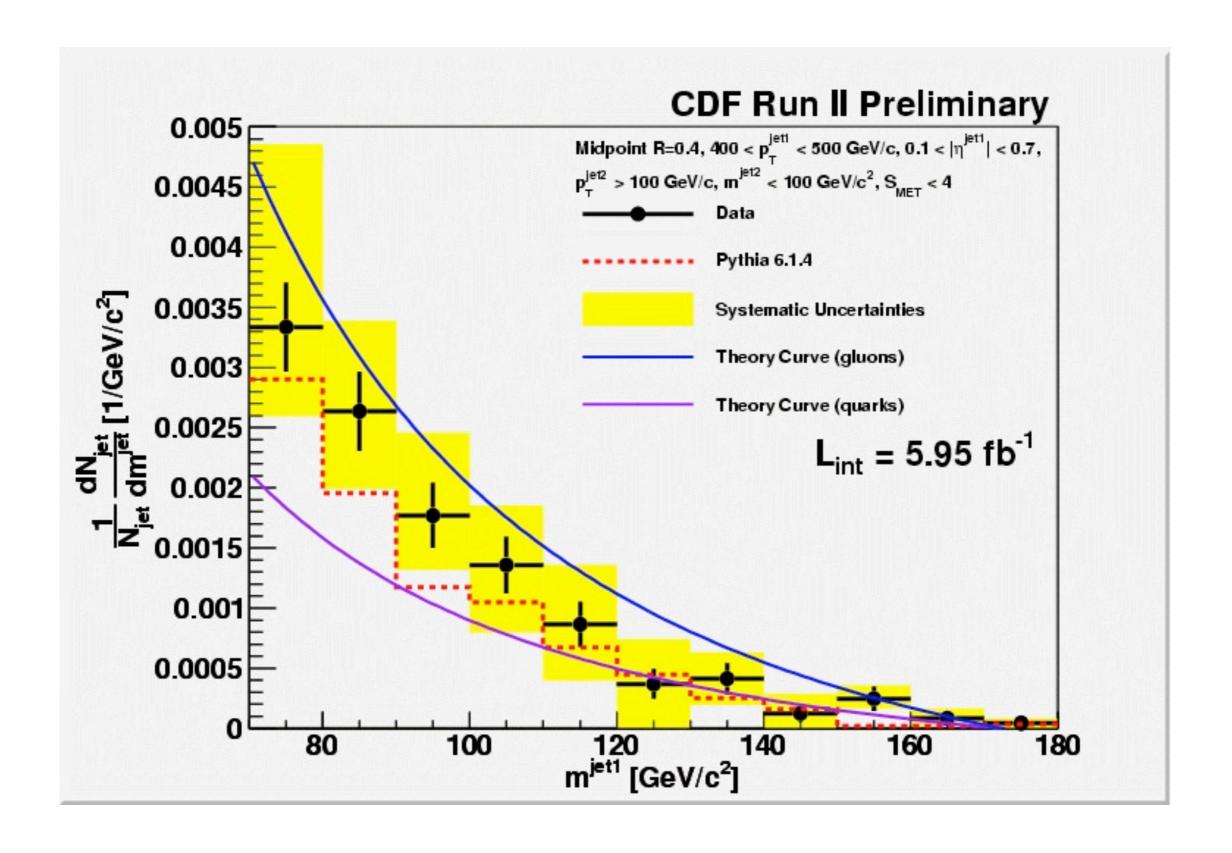


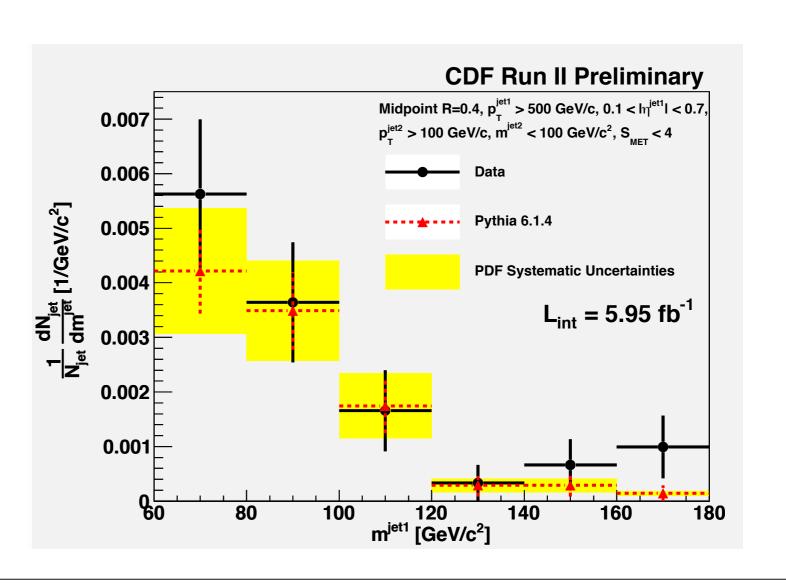




Summary

- ◆ LHC => new era, boosted massive jets important for studying QCD & NP discoveries.
- → Jet function (gluon emission) gives correct qualitative description of data => 2 body physics; quark jets.
- Angularity distribution further confirmed this description, affected by jet algorithm, data differ from Pythia.
- →Planar flow (3 body) shows larger deviation at large masses.
- Template Overlap method provides a theoretical handle with good rejection power (systematically improvable).





Three-particle Templates and Top Decay

