

# Flavour SUSY GUTs + ED

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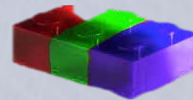
# Standard Model

Gauge symmetry  $SU(3)_C \times SU(2)_L \times U(1)_Y$   
 Global symmetry  $SO(3,1)$

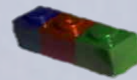


$g_\mu, W_\mu, B_\mu$

H



$Q_L^1$



$u_R$



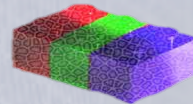
$d_R$



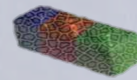
$L_L^1$



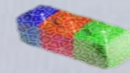
$e_R$



$Q_L^2$



$c_R$



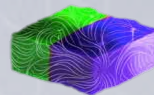
$s_R$



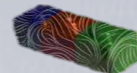
$L_L^2$



$\mu_R$



$Q_L^3$



$t_R$



$b_R$



$L_L^3$



$\tau_R$



# Standard Model

Gauge symmetry  $SU(3)_C \times SU(2)_L \times U(1)_Y$   
 Global symmetry  $SO(3,1)$



SUSY  
IE/D

GUT

FS



$g_\mu, W_\mu, B_\mu$

H

$Q_L^1$	$u_R$	$d_R$	$L_L^1$	$e_R$
$Q_L^2$	$c_R$	$s_R$	$L_L^2$	$\mu_R$
$Q_L^3$	$t_R$	$b_R$	$L_L^3$	$\tau_R$







Flavor

GUT

SUSY

ED



# Neutrino parameters

NuFIT 4.0 (2018)

	Normal Ordering (best fit)		Inverted Ordering ( $\Delta\chi^2 = 4.7$ )	
	bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range
$\sin^2 \theta_{12}$	$0.310^{+0.013}_{-0.012}$	0.275 $\rightarrow$ 0.350	$0.310^{+0.013}_{-0.012}$	0.275 $\rightarrow$ 0.350
$\theta_{12}/^\circ$	$33.82^{+0.78}_{-0.76}$	31.61 $\rightarrow$ 36.27	$33.82^{+0.78}_{-0.76}$	31.61 $\rightarrow$ 36.27
$\sin^2 \theta_{23}$	$0.580^{+0.017}_{-0.021}$	0.418 $\rightarrow$ 0.627	$0.584^{+0.016}_{-0.020}$	0.423 $\rightarrow$ 0.629
$\theta_{23}/^\circ$	$49.6^{+1.0}_{-1.2}$	40.3 $\rightarrow$ 52.4	$49.8^{+1.0}_{-1.1}$	40.6 $\rightarrow$ 52.5
$\sin^2 \theta_{13}$	$0.02241^{+0.00065}_{-0.00065}$	0.02045 $\rightarrow$ 0.02439	$0.02264^{+0.00066}_{-0.00066}$	0.02068 $\rightarrow$ 0.02463
$\theta_{13}/^\circ$	$8.61^{+0.13}_{-0.13}$	8.22 $\rightarrow$ 8.99	$8.65^{+0.13}_{-0.13}$	8.27 $\rightarrow$ 9.03
$\delta_{CP}/^\circ$	$215^{+40}_{-29}$	125 $\rightarrow$ 392	$284^{+27}_{-29}$	196 $\rightarrow$ 360
$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.39^{+0.21}_{-0.20}$	6.79 $\rightarrow$ 8.01	$7.39^{+0.21}_{-0.20}$	6.79 $\rightarrow$ 8.01
$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.525^{+0.033}_{-0.032}$	+2.427 $\rightarrow$ +2.625	$-2.512^{+0.034}_{-0.032}$	-2.611 $\rightarrow$ -2.412

without SK atmospheric data

# TBM

$$U = \begin{pmatrix} 2/3 & 1/3 & 0 \\ 1/6 & 1/3 & 1/2 \\ 1/6 & 1/3 & 1/2 \end{pmatrix}$$

Flavor symmetry  $G$ ,  
broken by flavons  
 $\phi$



# TBM Flavons

$$\langle \phi_1 \rangle \sim \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}, \quad \langle \phi_2 \rangle \sim \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix} \quad \langle \phi_3 \rangle \sim \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix}$$

**Doesn't change  
mixing angles.**

# TBM Flavons

$$m_\nu = \sum_i y_\nu^i \frac{v^2}{M_N^i \Lambda^2} \langle \phi_i \rangle \langle \phi_i \rangle^T$$

**Two RHN and seesaw**

$$m^\nu = a \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} + b \begin{pmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix},$$

**Highly predictive but not correct.**



# TBM Flavons

$$m_\nu = \sum_i y_\nu^i \frac{v^2}{M_N^i \Lambda^2} \langle \phi_i \rangle \langle \phi_i \rangle^T$$

**Two RHN and seesaw**

$$m^\nu = a \begin{pmatrix} 0 & 0 & 0 \\ \phi_2 & 1 & \phi_2 \\ 0 & 1 & 1 \end{pmatrix} + b \begin{pmatrix} 1 & 1 & 1 \\ \phi_1 & 1 & \phi_1 \\ 1 & 1 & 1 \end{pmatrix},$$

**Highly predictive but not correct.**





# CSD<sub>n</sub>

Phenomenological search for flavons  
with real integer entries.  
→ **Constrained Sequential  
Dominance**

$$\langle \phi_1 \rangle \sim \begin{pmatrix} 1 \\ n \\ n-2 \end{pmatrix}, \quad \langle \phi_2 \rangle \sim \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}$$

$$n=1,2,3,4$$



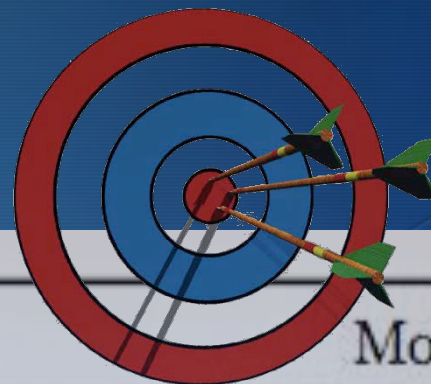
# Littlest Seesaw

- Neutrinos in CSD3.
- 2 RHNs.
- Diagonal Charged Leptons
- One physical fixed phase.
- Two free real parameters.

$$m_\nu = a \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} + be^{-2i\pi/3} \begin{pmatrix} 1 & 3 & 1 \\ 3 & 9 & 3 \\ 1 & 3 & 1 \end{pmatrix}$$



# Littlest Seesaw



Observable	Data		Model
	Central value	$1\sigma$ range	CSD3
$\theta_{12}^\ell / ^\circ$	33.62	32.86 $\rightarrow$ 34.38	34.33
$\theta_{13}^\ell / ^\circ$	8.54	8.57 $\rightarrow$ 8.69	8.58
$\theta_{23}^\ell / ^\circ$	47.20	45.30 $\rightarrow$ 49.10	44.3
$\delta^\ell / ^\circ$	234	178 $\rightarrow$ 290	266
$\Delta m_{21}^2 / (10^{-5} \text{ eV}^2)$	7.51	7.33 $\rightarrow$ 7.69	7.43
$\Delta m_{31}^2 / (10^{-3} \text{ eV}^2)$	2.52	2.48 $\rightarrow$ 2.56	2.49
$m_1 / \text{meV}$			0
$\alpha_{23} / ^\circ$			34
$\chi^2$			3.82

**$a=26.7 \text{ meV}$ ,  $b=2.67 \text{ meV}$**



# GUT

$$m_N, m_\nu^D, m_\nu^{LL}, m_u \sim ae^{i\eta} \begin{pmatrix} 1 & 3 & 1 \\ 3 & 9 & 3 \\ 1 & 3 & 1 \end{pmatrix} + b \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} + ce^{i\eta'} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
$$m_e, m_d \sim de^{i\eta} \begin{pmatrix} 0 & 1 & 1 \\ 1 & 6 & 4 \\ 1 & 4 & 2 \end{pmatrix} + f \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} + fe^{i\eta'} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- **Universal up-type**
- **Universal down-type**
- **At LE, 13 real parameters, 4 phases.**
- **22 observables.**



# GUT

$$m_N, m_\nu^D, m_\nu^{LL}, m_u \sim ae^{i\eta} \begin{pmatrix} 1 & 3 & 1 \\ \phi_3 & 1 & \phi_3 \\ 1 & 3 & 1 \end{pmatrix} + b \begin{pmatrix} 0 & 0 & 0 \\ \phi_2 & 1 & \phi_2 \\ 0 & 1 & 1 \end{pmatrix} + ce^{i\eta'} \begin{pmatrix} 0 & 0 & 0 \\ \phi_3 & 0 & \phi_3 \\ 0 & 0 & 1 \end{pmatrix}$$

$$m_e, m_d \sim de^{i\eta} \begin{pmatrix} 0 & 1 & 1 \\ \phi_3 & 6 & \phi_3 \\ 1 & 1 & 2 \end{pmatrix} + f \begin{pmatrix} 0 & 0 & 0 \\ \phi_2 & 1 & \phi_2 \\ 0 & 1 & 1 \end{pmatrix} + fe^{i\eta'} \begin{pmatrix} 0 & 0 & 0 \\ \phi_3 & 0 & \phi_3 \\ 0 & 0 & 1 \end{pmatrix}$$



# GUT

$$m_N, m_\nu^D, m_\nu^{LL}, m_u \sim ae^{i\eta} \begin{pmatrix} 1 & 3 & 1 \\ 3 & 9 & 3 \\ 1 & 3 & 1 \end{pmatrix} + b \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} + ce^{i\eta'} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$
$$m_e, m_d \sim de^{i\eta} \begin{pmatrix} 0 & 1 & 1 \\ 1 & 6 & 4 \\ 1 & 4 & 2 \end{pmatrix} + f \begin{pmatrix} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 0 & 1 & 1 \end{pmatrix} + fe^{i\eta'} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- **CSD3**
- **Perfect fit.**
- **Predictive.**
- **Highly symmetrical.**

# GUTs

CSD1

- TBM

CSD2

- $SO(10) \times S_4$  arXiv:1710.03229
- $SO(10) \times SU(3)$  arXiv:1807.07078

CSD3

- $SU(5) \times A_4$  arXiv:1503.03306
- $SO(10) \times \Delta(27)$  arXiv:1512.00850
- $SO(10) \times S_4$  arXiv:1705.01555
- $SU(5) \times S_4$  arXiv:1803.04978
- $SO(10) \times SU(3)$  arXiv:1807.07078



Where does CSDn  
come from?



# Flavons

$$\langle \phi_1 \rangle^{CSD3} \sim \begin{pmatrix} 1 \\ 3 \\ -1 \end{pmatrix}, \quad \langle \phi_1 \rangle^{CSD2} \sim \begin{pmatrix} 1 \\ 0 \\ 2 \end{pmatrix},$$
$$\langle \phi_2 \rangle \sim \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}, \quad \langle \phi_3 \rangle \sim \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix},$$

Up to overall rotation and reflection



# $S_4$

$S_4$	$S$	$T$	$U$
$1, 1'$	1	1	$\pm 1$
2	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \omega & 0 \\ 0 & \omega^2 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
$3, 3'$	$\frac{1}{3} \begin{pmatrix} -1 & 2 & 2 \\ 2 & -1 & 2 \\ 2 & 2 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & \omega^2 & 0 \\ 0 & 0 & \omega \end{pmatrix}$	$\mp \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$

# $S_4$

$$SU = \frac{1}{3} \begin{pmatrix} -1 & 2 & 2 \\ 2 & 2 & -1 \\ 2 & -1 & 2 \end{pmatrix}. \quad SU \langle \phi \rangle = \langle \phi \rangle = \begin{pmatrix} a \\ b \\ 2a - b \end{pmatrix}$$

$$\langle \phi_1 \rangle^{CSD3} \rightarrow b = 3a, \quad \langle \phi_1 \rangle^{CSD2} \rightarrow b = 0, \quad \langle \phi_2 \rangle \rightarrow a = 0$$

$$\omega^2 T \langle \phi_3 \rangle = \langle \phi_3 \rangle$$



# Alignment Potentials

F-term equations of X, Y, Z

CSD3

$$W_0^{\text{flavon}} \sim X_{3'}(\phi'_{S,U})^2 + X_2(\phi_T)^2 + X_1(\phi'_t)^2 + X_{1'}\phi_T\phi'_t \\ + Y_3\phi'_{S,U}\rho_{S,U} + Y_{3'}(\xi_T\phi'_t - \phi_T\rho_t) \\ + Z_{3'}(\phi'_{S,U}\phi_T - \xi_{S,U}\phi'_{\text{atm}}) + \tilde{Z}_{3'}(\phi'_{\text{atm}}\phi'_t - \rho_{S,U}\phi'_{\text{sol}}) .$$

# Alignment Potentials

F-term equations of X, Y, Z

CSD3



$$W_0^{\text{flavor}} \sim X_3(\phi'_{S,U})^2 + X_2(\phi'_T)^2 + X_1(\phi'_t)^2 + X_{1'}\phi'_T\phi'_t \\ + Y_3\phi'_{S,U}\rho_{S,U} + Y_3(\xi'_T\phi'_t - \phi'_T\rho_t) \\ + Z_3(\phi'_{S,U}\phi'_T - \xi_{S,U}\phi'_{\text{atm}}) + \tilde{Z}_3(\phi'_{\text{atm}}\phi'_t - \rho_{S,U}\phi'_{\text{sol}}) .$$





ED

ED

ED

Break nicely

GUT

SUSY

Flavor

Orb. Cond.

S. S.

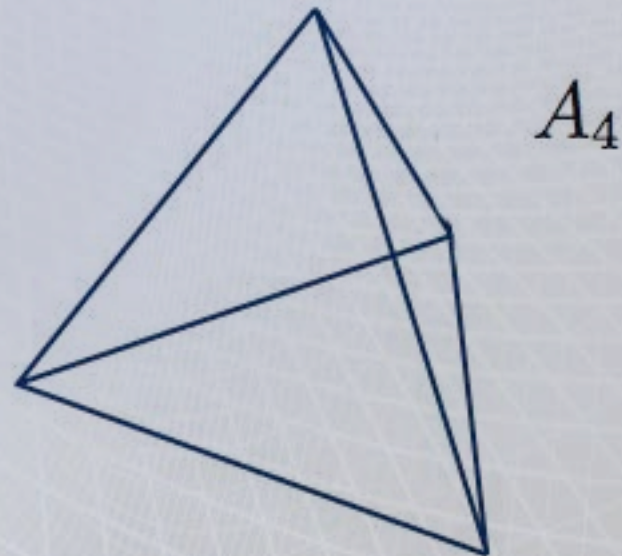
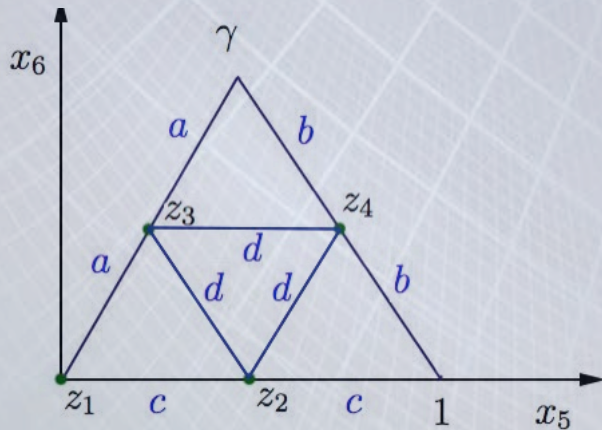
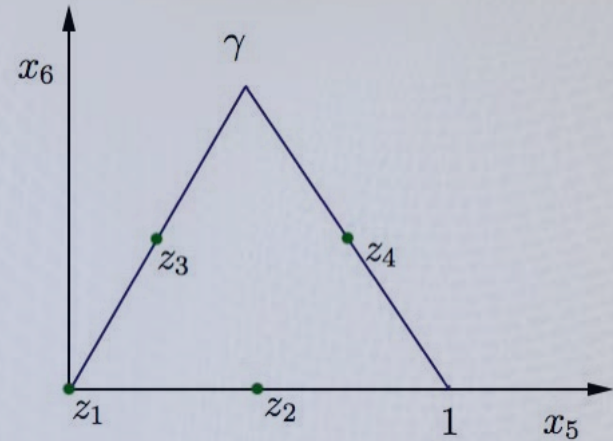
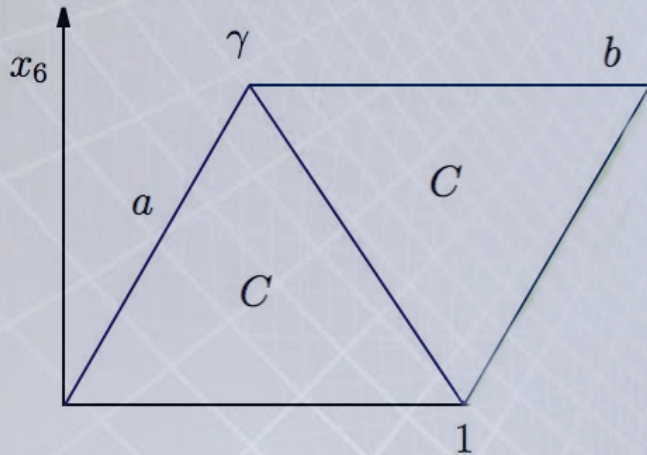
Up next...



Dear ED:  
Why  $S_4$ ?

# $A_4$ from $T^2/Z_2$

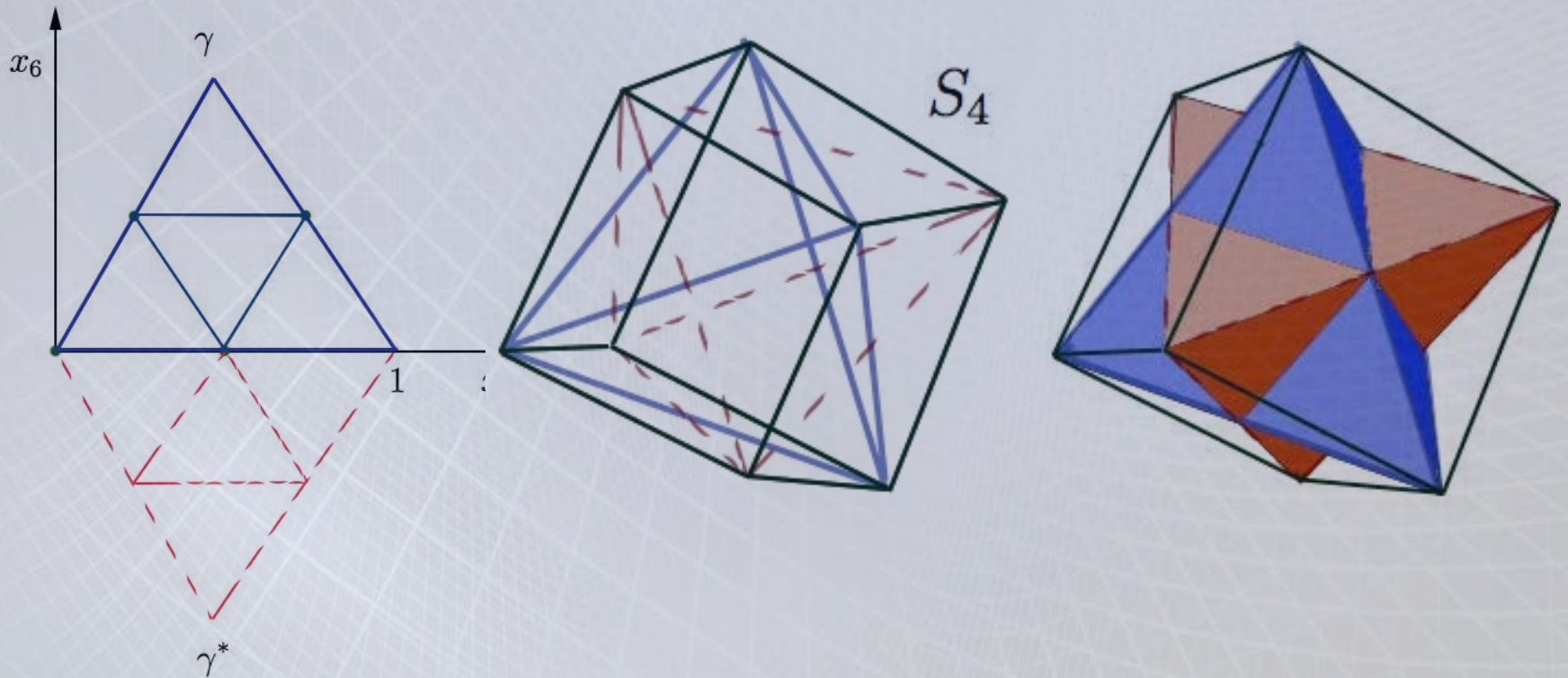
$$\gamma = \omega = e^{2\pi i/3}$$



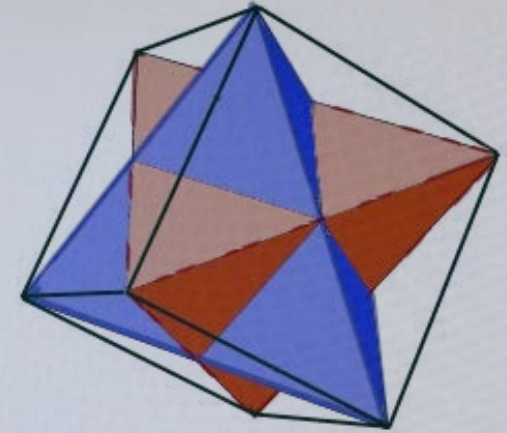
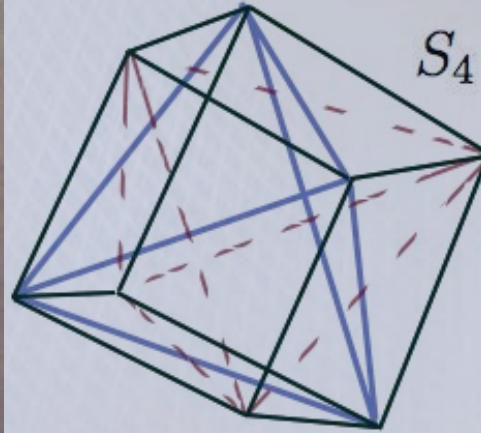


# $S_4$ from $T^2/Z_2$

Independent reflection of  $x_5$  and  $x_6$



# $S_4$ from ED



Remnant symmetry  
after  
compactification

Through the ancient art of extra dimensional origami.



Dear ED:  
Why CSDn?

$T^2/Z_2$  and  $S_4$





# $T^2/Z_2$ and $S_4$

$S_4$	$S$	$T$	$U$
$1, 1'$	1	1	$\pm 1$
2	$\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$	$\begin{pmatrix} \omega & 0 \\ 0 & \omega^2 \end{pmatrix}$	$\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$
$3, 3'$	$\frac{1}{3} \begin{pmatrix} -1 & 2 & 2 \\ 2 & -1 & 2 \\ 2 & 2 & -1 \end{pmatrix}$	$\begin{pmatrix} 1 & 0 & 0 \\ 0 & \omega^2 & 0 \\ 0 & 0 & \omega \end{pmatrix}$	$\mp \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix}$

# $T^2/Z_2$ and $S_4$

Boundary Condition  $U$  :

$$\langle \phi_2 \rangle = -U \langle \phi_2 \rangle = - \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 1 \\ 0 & 1 & 0 \end{pmatrix} \langle \phi_2 \rangle \rightarrow \langle \phi_2 \rangle \sim \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}.$$

$$\langle \rho \rangle = U \langle \rho \rangle = \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix} \langle \rho \rangle \rightarrow \langle \rho \rangle \sim \begin{pmatrix} 1 \\ 1 \end{pmatrix}.$$



# $T^2/Z_2$ and $S_4$

Alignment superpotential:

$$\mathcal{W}_A \sim A_1(\phi_3)^2 + A_3(\phi_2\phi_3 - \rho\phi_1),$$

# $T^2/Z_2$ and $S_4$

6D:  $W_A \sim A_1(\phi_3)^2 + A_3(\phi_2\phi_3 - \rho\phi_1),$

4D:

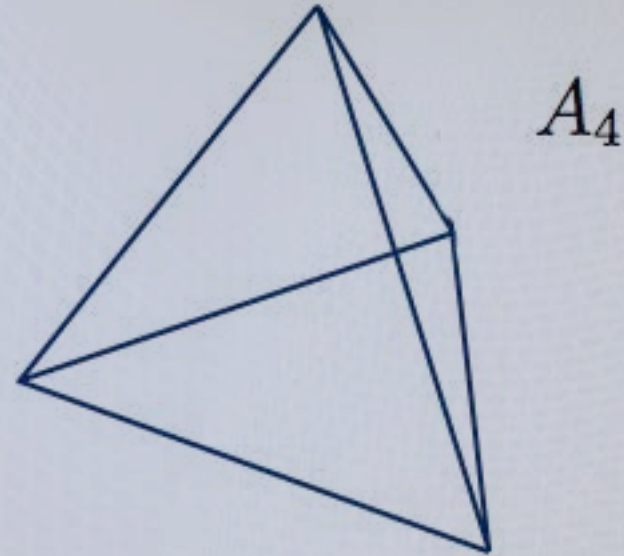
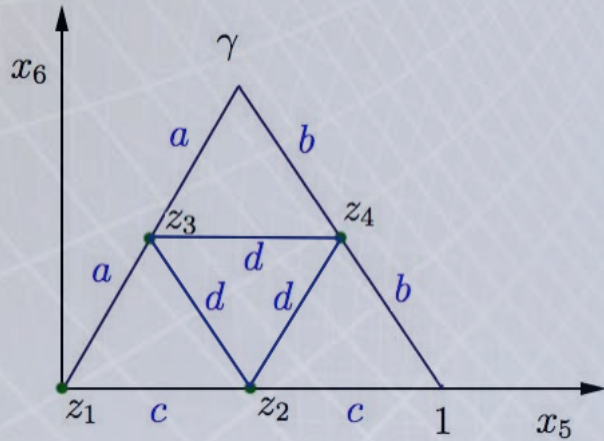
$$W_0^{\text{flavon}} \sim X_{3'}(\phi'_{S,U})^2 + X_2(\phi_T)^2 + X_1(\phi'_t)^2 + X_{1'}\phi_T\phi'_t \\ + Y_3\phi'_{S,U}\rho_{S,U} + Y_{3'}(\xi_T\phi'_t - \phi_T\rho_t) \\ + Z_{3'}(\phi'_{S,U}\phi_T - \xi_{S,U}\phi'_{\text{atm}}) + \tilde{Z}_{3'}(\phi'_{\text{atm}}\phi'_t - \rho_{S,U}\phi'_{\text{sol}}).$$



Could we have no  
superpotential?



# $A_4$ from $T^2/Z_2$



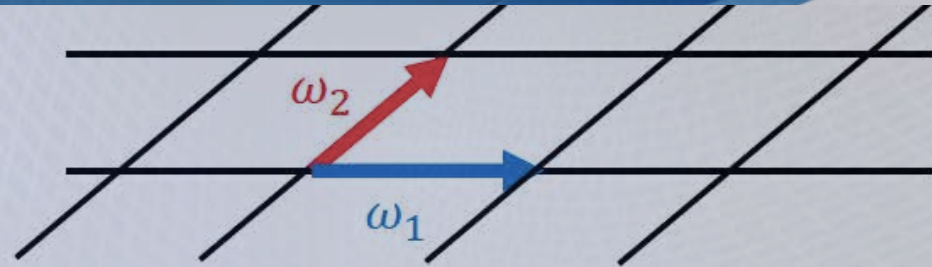
Active transformation  $\rightarrow A_4$  spacetime symmetry

Passive transformation  $\rightarrow A_4$  modular symmetry



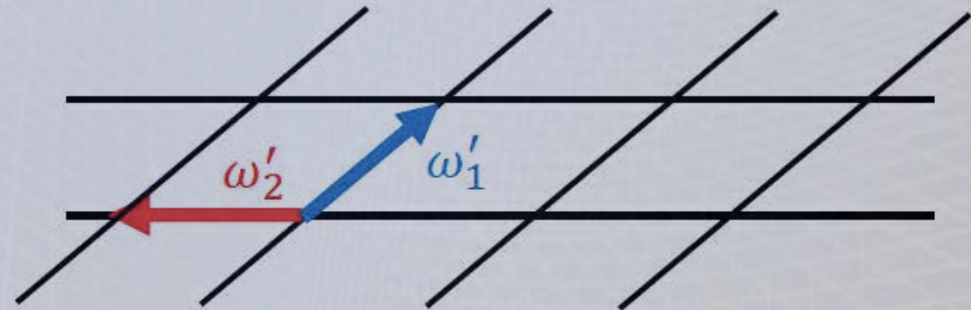
# Modular Transformations

There are two independent lattice invariant transformations.



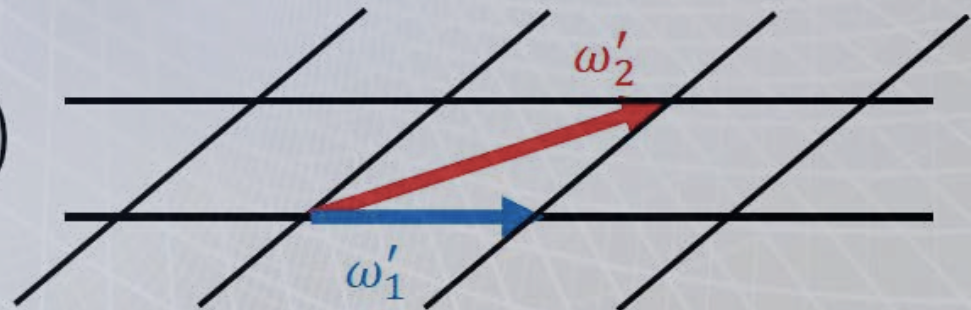
S-transformation

$$\begin{pmatrix} \omega'_1 \\ \omega'_2 \end{pmatrix} = \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix} \begin{pmatrix} \omega_1 \\ \omega_2 \end{pmatrix} = \begin{pmatrix} \omega_2 \\ -\omega_1 \end{pmatrix}$$



T-transformation

$$\begin{pmatrix} \omega'_1 \\ \omega'_2 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix} \begin{pmatrix} \omega_1 \\ \omega_2 \end{pmatrix} = \begin{pmatrix} \omega_1 \\ \omega_2 + \omega_1 \end{pmatrix}$$



# Modular Transformations

Yukawa couplings  $y$   $\rightarrow$   $Y(w_1, w_2)$  Modular forms

$$\begin{pmatrix} -1 \\ 2\omega \\ 2\omega^2 \end{pmatrix}$$

**Fixed by this specific orbifold (No extra freedom)**



# Modular Transformations

$$\text{Modular Form } Y \begin{pmatrix} -1 \\ 2\omega \\ 2\omega^2 \end{pmatrix} \quad \text{Flavon } \phi_2 \begin{pmatrix} 0 \\ 1 \\ 1 \end{pmatrix}$$

$$\mu - \tau \text{ symmetry: } \theta_{23}^1 = 45^\circ \quad \delta^1 = \pm 90^\circ$$

Leptonic Fit  $\chi^2=5$  with 4 neutrino parameters.

$T^2/Z_2$  and  $SU(3)$   
No superpotential





$$T^2/Z_2^2$$

**Independent reflection of  $x_5$  and  $x_6 \rightarrow$  effective  $Z_2^2$**

**4 4d branes in total**

**4 5d branes for each reflection  
(Lines that connect 4d branes)**

$$T^2/Z_2^2$$

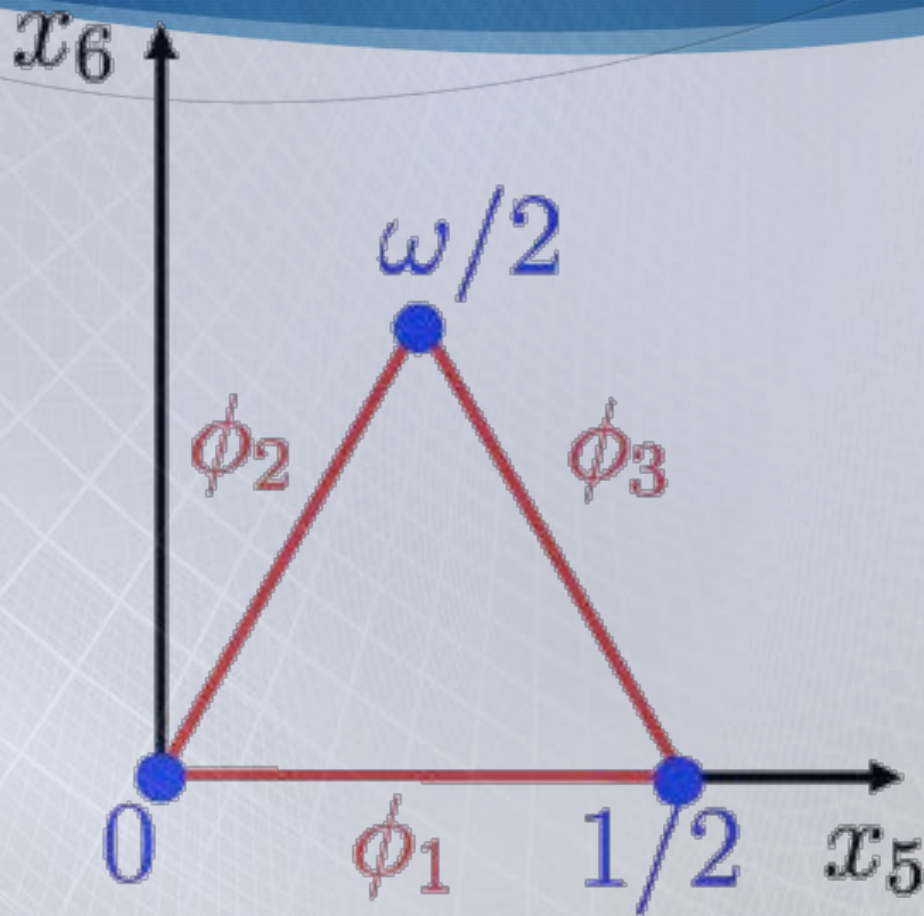
**Fermions in 4d branes (No boundary conditions)**

**Flavons in 5d branes (Some boundary conditions)**

**Higgs and Gauge F. in bulk (All boundary conditions)**



# Flavons in 5d branes



# Boundary conditions

$$CSD3: P_0 = SU, P_{\omega/2} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}, P_{1/2} = \begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{pmatrix}$$

$$CSD2: P_0 = SU, P_{\omega/2} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}, P_{1/2} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$



# Boundary conditions

$$CSD3: \quad P_0 = SU, \quad P_{\omega/2} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad P_{1/2} = \begin{pmatrix} 0 & 0 & -1 \\ 0 & 1 & 0 \\ -1 & 0 & 0 \end{pmatrix}$$

$$CSD2: \quad P_0 = SU, \quad P_{\omega/2} = \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{pmatrix}, \quad P_{1/2} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & -1 & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

$$P_0 \langle \phi_1 \rangle = P_{1/2} \langle \phi_1 \rangle = \langle \phi_1 \rangle$$

$$P_0 \langle \phi_2 \rangle = P_{\omega/2} \langle \phi_2 \rangle = \langle \phi_2 \rangle$$

$$P_{1/2} \langle \phi_3 \rangle = P_{\omega/2} \langle \phi_3 \rangle = \langle \phi_3 \rangle$$

# Flavons

$$\langle \phi_1 \rangle^{CSD3} \sim \begin{pmatrix} 1 \\ 3 \\ -1 \end{pmatrix}, \quad \langle \phi_1 \rangle^{CSD2} \sim \begin{pmatrix} 1 \\ 0 \\ 2 \end{pmatrix},$$
$$\langle \phi_2 \rangle \sim \begin{pmatrix} 0 \\ 1 \\ -1 \end{pmatrix}, \quad \langle \phi_3 \rangle \sim \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix},$$

Up to overall rotation and reflection



# The Whole Enchilada



# The Whole Enchilada

Field	Representation				Localization		
	$SU(3)$	$SO(10)$	$Z_6$	$Z_3$	$P_0$	$P_{1/2}$	$P_{i/2}$
$\psi$	$\bar{3}$	16	0	0			
$H_{10}^u$	1	10	0	0	+1	+1	+1
$H_{10}^d$	1	10	2	0	+1	+1	-1
$H_{\bar{16}}$	1	$\bar{16}$	0	0	+1	+1	-1
$H_{16}$	1	16	0	0	+1	+1	-1
$H_{45}^{X,Y}$	1	45	0	1	+1	+1	+1
$H_{45}^{W,Z}$	1	45	2	1	+1	+1	+1
$\phi_1$	3	1	2	1	+1	+1	
$\phi_2$	3	1	0	1	+1		+1
$\phi_3$	3	1	3	1		+1	+1



# The Whole Enchilada

Field	Representation				Localization		
	$SU(3)$	$SO(10)$	$Z_6$	$Z_3$	$P_0$	$P_{1/2}$	$P_{i/2}$
$\psi$	$\bar{3}$	16	0	0			
$H_{10}^u$	1	10	0	0	+1	+1	+1
$H_{10}^d$	1	10	2	0	+1	+1	-1
$H_{\bar{16}}$	1	$\bar{16}$	0	0	+1	+1	-1
$H_{16}$	1	16	0	0	+1	+1	-1
$H_{45}^{X,Y}$	1	45	0	1	+1	+1	+1
$H_{45}^{W,Z}$	1	45	2	1	+1	+1	+1
$\phi_1$	3	1	2	1	+1	+1	
$\phi_2$	3	1	0	1	+1		+1
$\phi_3$	3	1	3	1		+1	+1

- MSSM at LE.
- DT, DD split, GUT and Flavour breaking by ED.
- Fermion Unification.
- Highly predictive  $\nu$  s.
- Perfect fit Qs and CLs.
- Small reps.
- Few multiplets.

# 6d SUSY

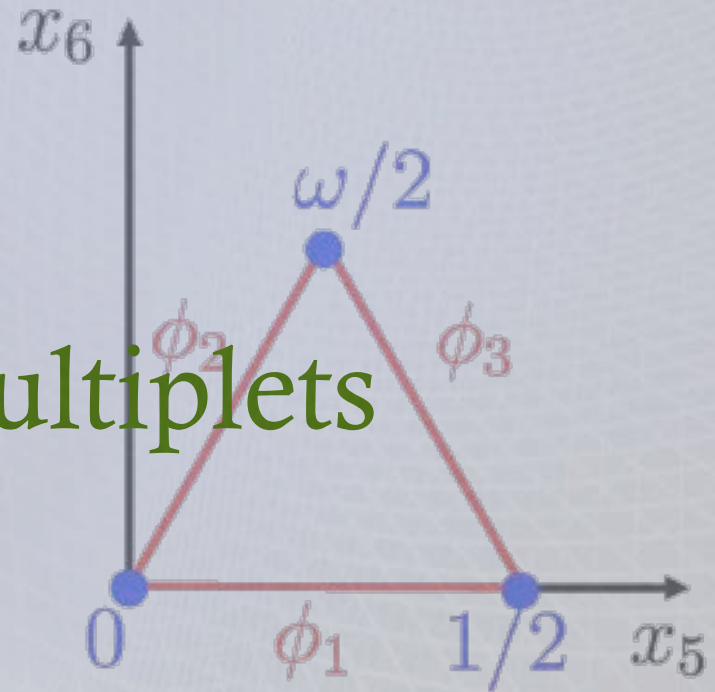
## SO(10) GUT SU(3) Flavor

- Rather complete.

- Predictive.

- Less superfield multiplets than the MSSM.

Field	Representation		Localization				
	$SU(3)$	$SO(10)$	$Z_6$	$Z_3$	$P_1$	$P_2$	$P_3$
$H_{10}^u$	$\bar{3}$	16	0	0	+1	+1	+1
$H_{10}^d$	1	10	2	0	+1	+1	-1
$H_{16}^{\bar{5}}$	1	$\bar{16}$	0	0	+1	+1	-1
$H_{16}^{\bar{10}}$	1	16	0	0	+1	+1	-1
$H_{45}^{X,Y}$	1	45	0	1	+1	+1	+1
$H_{45}^{W,Z}$	1	45	0	1	+1	+1	+1
$\phi_1$	3	1	2	1	+1	+1	
$\phi_2$	3	1	0	1	+1		+1
$\phi_3$	3	1	3	1		+1	+1





# Conclusion

We can easily obtain non trivial and predictive flavon alignments through Extra Dimensional mechanisms.