



The Dominion of Light Dark Matter

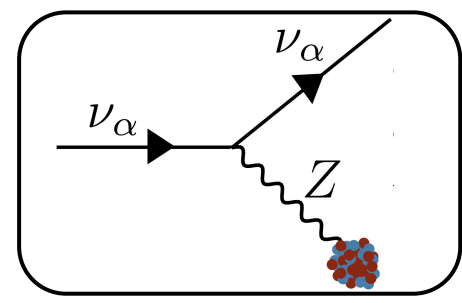
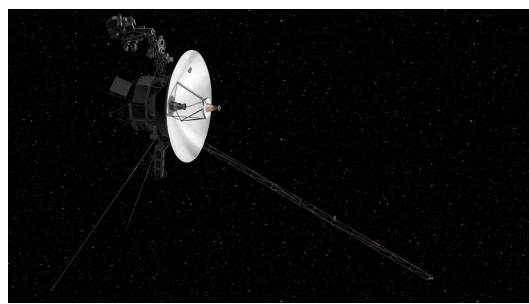
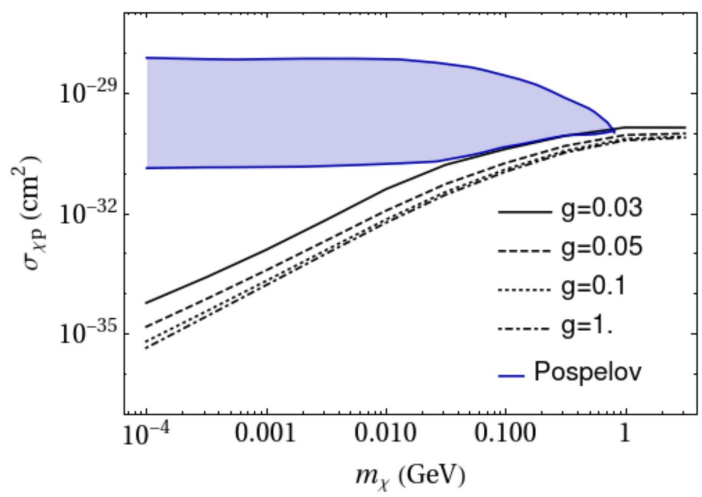
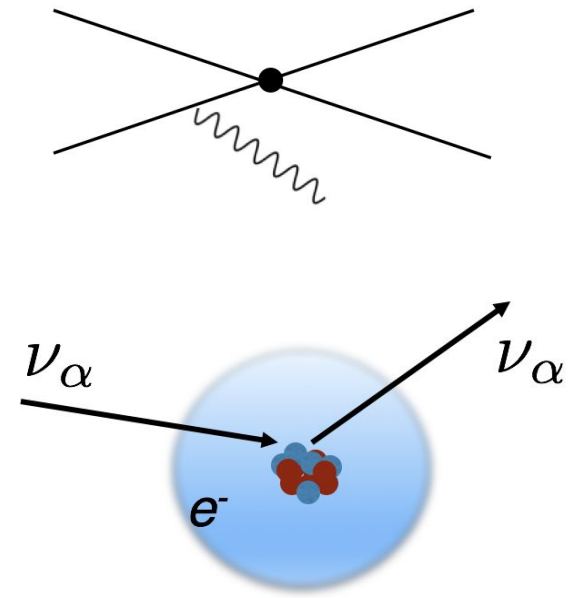
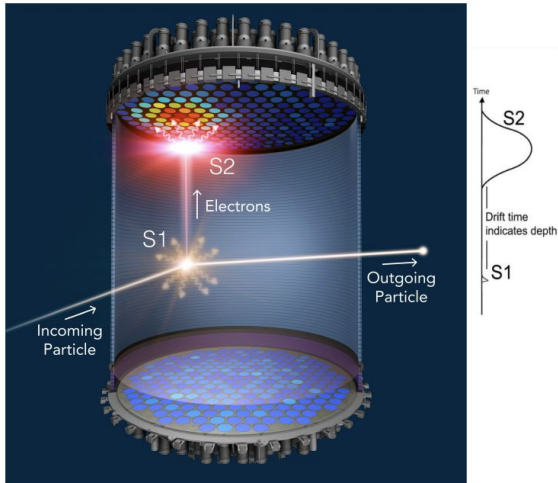
James Dent



Sam Houston State University

René Magritte, *L'empire des lumières*

Outline



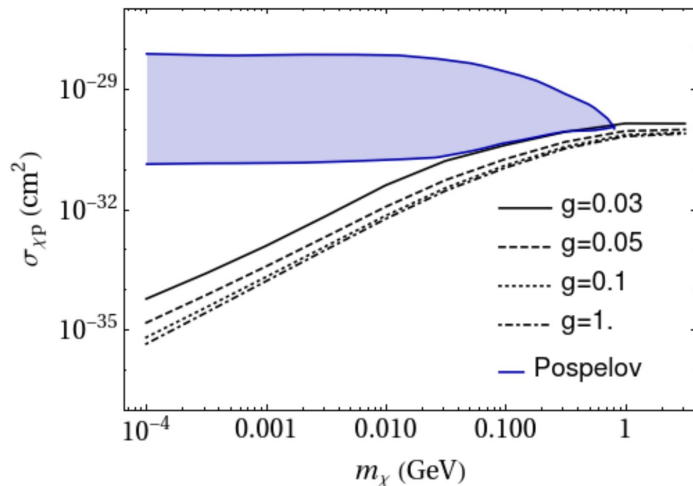
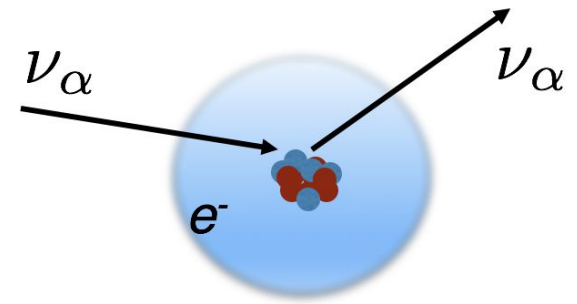
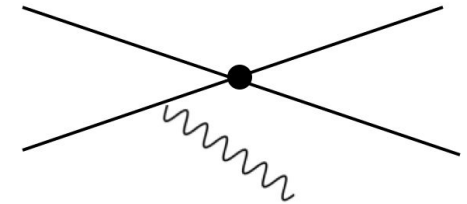
The Migdal Effect and Photon Bremsstrahlung in effective field theories of dark matter direct detection and coherent elastic neutrino-nucleus scattering

[arXiv:1905.00046](https://arxiv.org/abs/1905.00046)

Nicole Bell Jayden Newstead Subir Sabharwal Tom Weiler

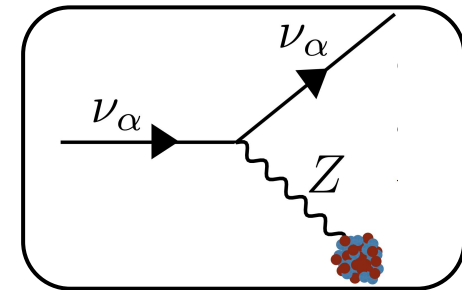


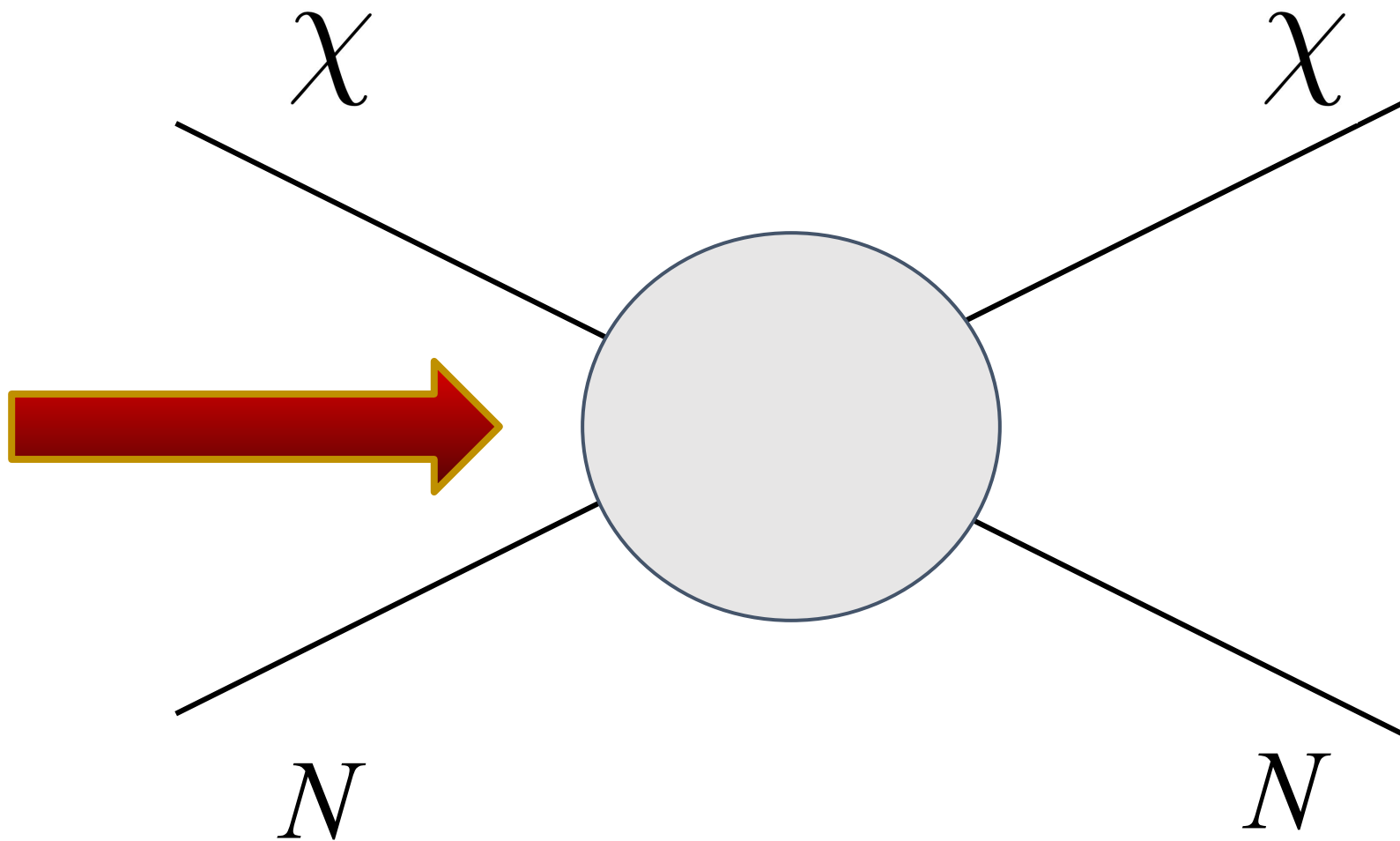
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Jayden Newstead

Bhaskar Dutta Ian Shoemaker





Direct Detection Review

Momentum Exchanged $O(<100\text{MeV})$

$$q = \sqrt{2m_T E_R}$$

Recoil energy $O(10\text{keV})$

$$E_R = \frac{\mu_{\chi T}^2 v^2}{m_T} (1 - \cos \theta)$$

Incident energy

$$E_i = \frac{m_\chi v^2}{2}$$

$$v \sim \mathcal{O}(10^{-3})$$

$$E_{R,\text{max}} = \frac{2\mu_{\chi T}^2 v^2}{m_T}$$

Direct Detection Review

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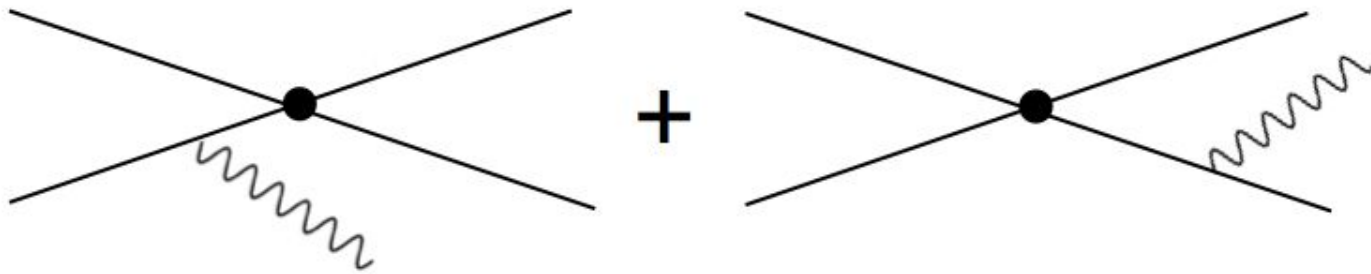
$$E_{R,\text{max}} = \frac{2\mu_{\chi T}^2 v^2}{m_T}$$

For: $m_\chi = 100 \text{ GeV}$ $m_T = 130 \text{ GeV}$, $E_{R,\text{max}} \simeq 50 \text{ keV}$.

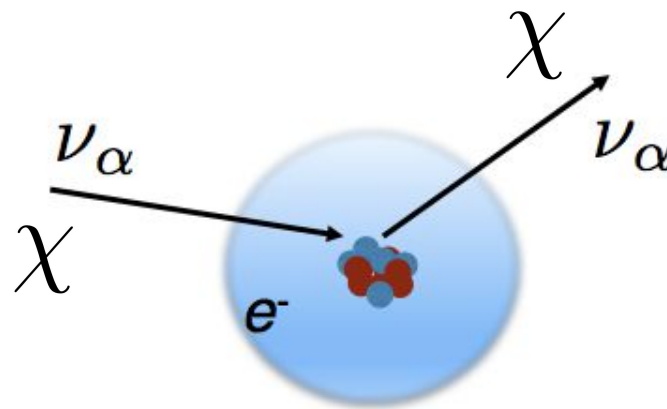
For: $m_\chi = 10 \text{ GeV}$ $m_T = 130 \text{ GeV}$, $E_{R,\text{max}} \simeq 1.3 \text{ keV}$.

Alternative Signals for sub-GeV Probes

Bremsstrahlung



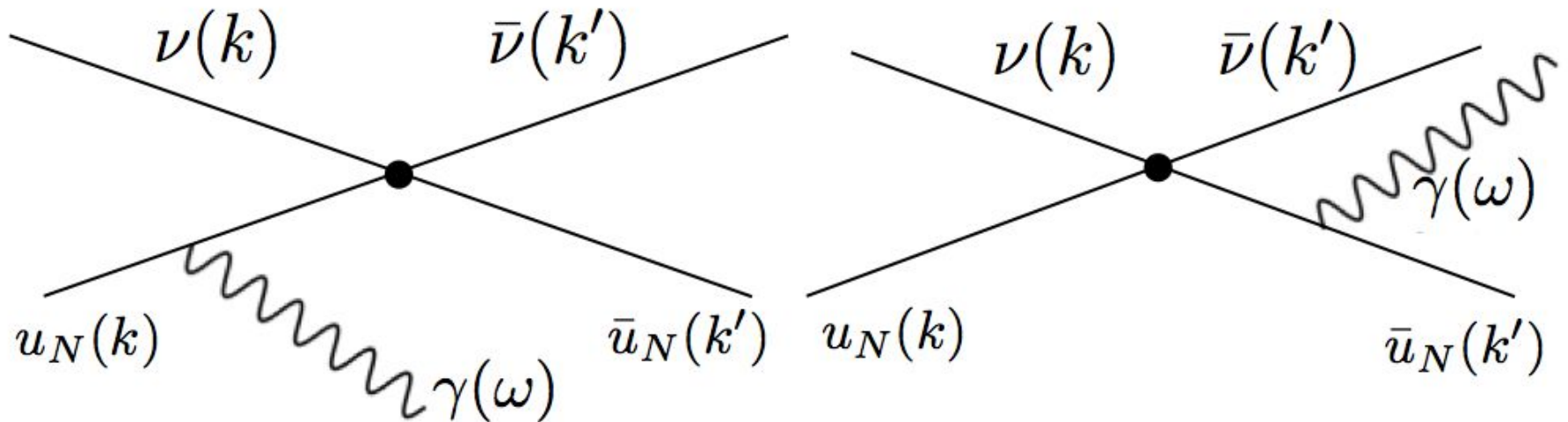
Migdal



Bremsstrahlung in $\chi + N \rightarrow \chi + N + \gamma$ DM scattering has been explored as a means of accessing sub-GeV mass DM

C. Kouvaris and J. Pradler, PRL 2017, 1607.01789

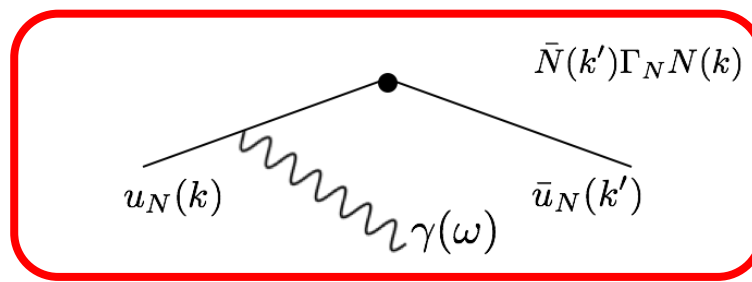
C.McCabe, PhysRevD (2017) 1702.04730



$$\nu + N \rightarrow \nu + N + \gamma$$

We want to examine the possibility of brem signals when nuclear recoil energies are below threshold.

Also see the recent paper: A.Millar, G.Raffelt, L.Stodolsky, and E.Vitagliano, 1810.06584 for very low E_ν with an examination of neutrino mass effects



Bremsstrahlung in the process $\chi + N \rightarrow \chi + N + \gamma$
 Can be used to detect scattering processes that produce nuclear recoils below detector thresholds.

The endpoints of the maximum nuclear recoil energy and emitted photon are key to the extended reach

$$v_{\min} = \frac{m_T E_R + \mu_T \delta}{\mu_T \sqrt{2m_T E_R}}$$

$$E_{R,\max} = \frac{2\mu_T^2 v_{\max}^2}{m_T},$$

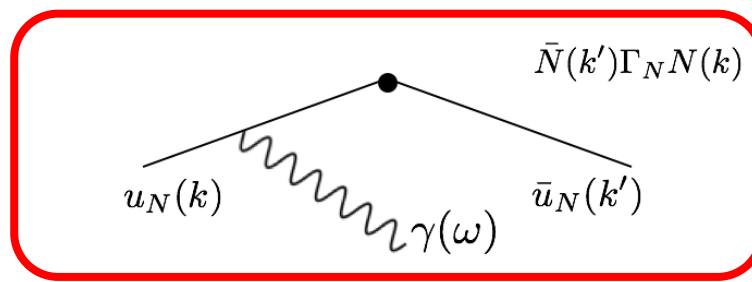
$$\delta_{\max} = \frac{\mu_T v_{\max}^2}{2}.$$

For the case of dark matter much lighter than the target nucleus

$$m_T \gg m_\chi$$

$$E_{R,\max} \approx 2 \left(\frac{m_\chi}{\text{GeV}} \right)^2 \left(\frac{\text{GeV}}{m_T} \right) \left(\frac{v_{\max}^2}{10^{-6}} \right) \text{keV}$$

$$\delta_{\max} \approx \frac{1}{2} \left(\frac{m_\chi}{\text{GeV}} \right) \left(\frac{v_{\max}^2}{10^{-6}} \right) \text{keV},$$



$$E_{R,\max} \approx 2 \left(\frac{m_\chi}{\text{GeV}} \right)^2 \left(\frac{\text{GeV}}{m_T} \right) \left(\frac{v_{\max}^2}{10^{-6}} \right) \text{keV}$$

$$\delta_{\max} \approx \frac{1}{2} \left(\frac{m_\chi}{\text{GeV}} \right) \left(\frac{v_{\max}^2}{10^{-6}} \right) \text{keV},$$

Typically one finds that sub-GeV dark matter creates

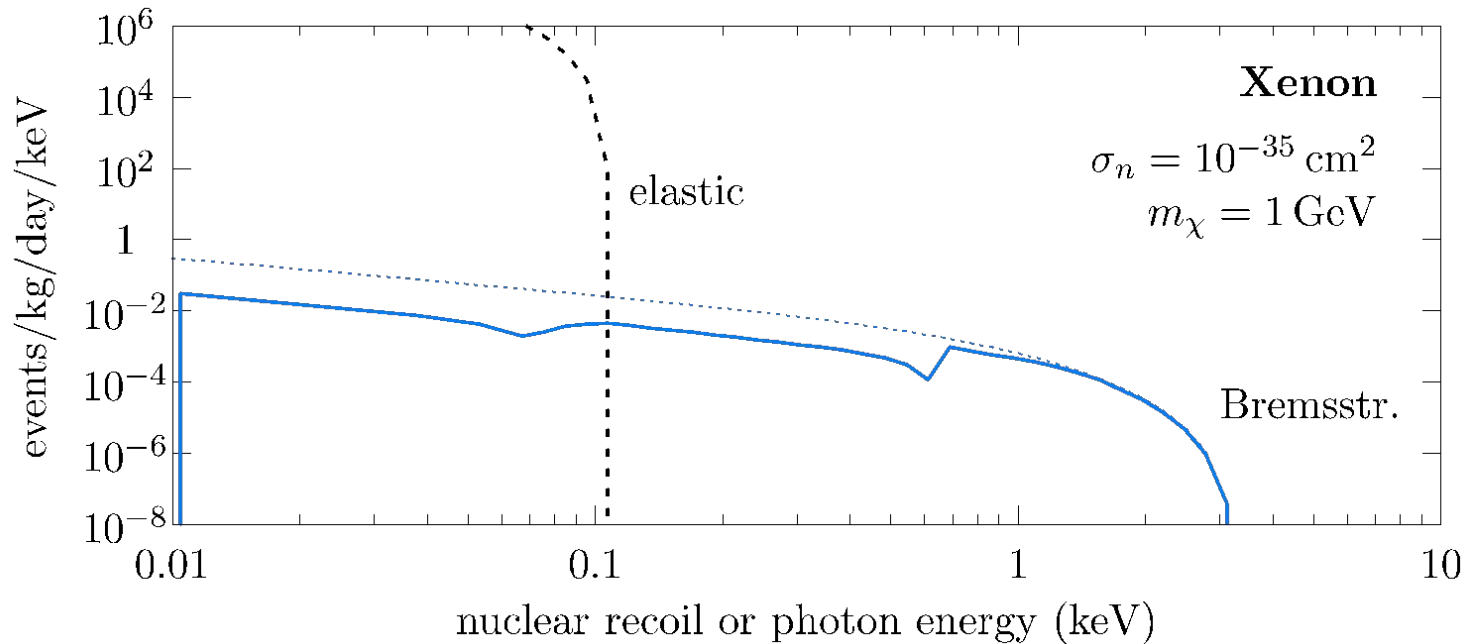
$$\delta_{\max} > E_{R,\max}$$

For example, a 1 GeV particle incident on xenon will produce

$$E_{R,\max} \lesssim 10^{-1} \text{keV} \text{ and } \delta_{\max} \sim 3 \text{keV}$$

The double differential cross-section factorizes into kinematic terms multiplied by the 2-2 elastic differential cross-section

$$\frac{d^2\sigma}{dE_R d\omega} = \frac{4\alpha Z^2}{3\pi} \frac{E_R}{m_T \omega} \left(\frac{d\sigma}{dE_R} \right)_{(2\rightarrow 2)} \quad \text{or} \quad \frac{d^3 R}{dE_R d\omega dv} = \frac{d^2 R_{\chi T}}{dE_R dv} \frac{4\alpha Z^2}{3\pi} \frac{E_R}{m_T \omega}$$

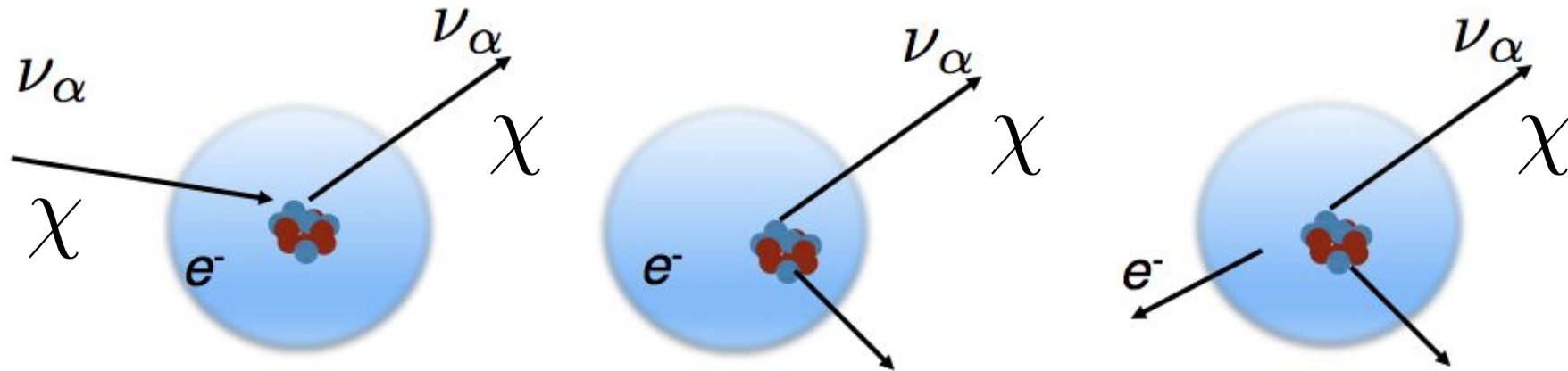


$$\frac{dR}{d\omega} = N_T \frac{\rho_\chi}{m_\chi} \int_{|\mathbf{v}| \geq v_{\min}} d^3\mathbf{v} v f_v(\mathbf{v} + \mathbf{v}_e) \frac{d\sigma}{d\omega}$$

The Migdal Effect

A.B.Migdal, J.Phys. USSR (1941), Landau & Lifschitz, QM Sec.41

Ionization and excitation of electron states from the relative momentum arising when the nucleus is given an impulse.



Proposed for dark matter detection years ago, and recently revisited in more detail.

M. Ibe, W. Nakano, Y. Shoji, and K. Suzuki, JHEP (2018) 1707.07258

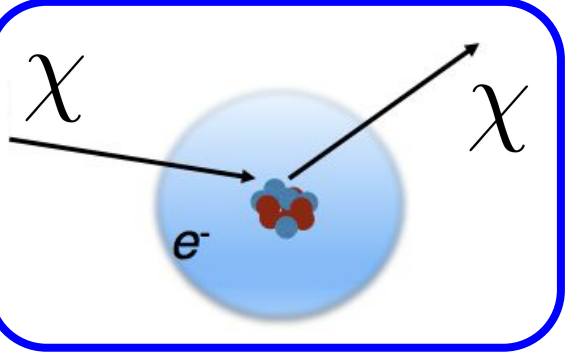
M. Dolan, F. Kahlhoefer, and C. McCabe, PRL(2018) 1711.09906

(above figure adapted from this paper)

Does *not* suffer from the same suppression as brem.

R. Bernabei et al., Int. J. Mod. Phys. A22, 3155 (2007), arXiv:0706.1421

B. M. Roberts, V. V. Flambaum, and G. F. Gribakin, Phys. Rev. Lett. 116, 023201 (2016), arXiv:1509.09044

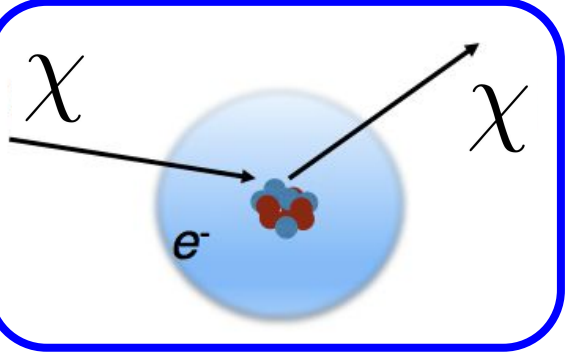


$$v_{\min} = \frac{m_T E_R + \mu_T E_{\text{EM}}}{\mu_T \sqrt{2m_T E_R}}$$

The endpoints of the maximum nuclear recoil energy and emitted electronic energy are key to the extended reach

$$E_{R,\max} = \frac{2\mu_T^2 v_{\max}^2}{m_T}$$

$$E_{\text{EM},\max} = \frac{\mu_T v_{\max}^2}{2}$$



The double differential cross-section factorizes into the ionization rate multiplied by the 2-2 elastic differential cross-section

$$\frac{d^2 R}{dE_R dv} = \frac{d^2 R_{\chi T}}{dE_R dv} \times |Z_{\text{ion}}|^2$$

The ionization rate is given in terms of the ionization probability

$$|Z_{\text{ion}}|^2 = \frac{1}{2\pi} \sum_{n,\ell} \int dE_e \frac{d}{dE_e} p_{q_e}^c(n\ell \rightarrow (E_e))$$

The differential rate is then

$$\frac{d^3 R}{dE_R dE_{\text{EM}} dv} = \frac{d^2 R_0}{dE_R dv} \times \frac{1}{2\pi} \sum_{n,\ell} \frac{d}{dE_e} p_{q_e}^c(n\ell \rightarrow (E_e))$$

The Migdal Effect and Photon Bremsstrahlung in effective field theories of dark matter direct detection and coherent elastic neutrino-nucleus scattering

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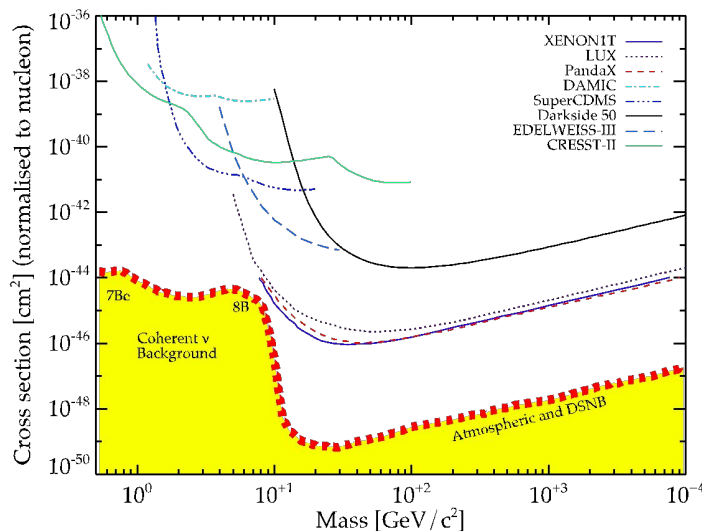


Tom Weiler



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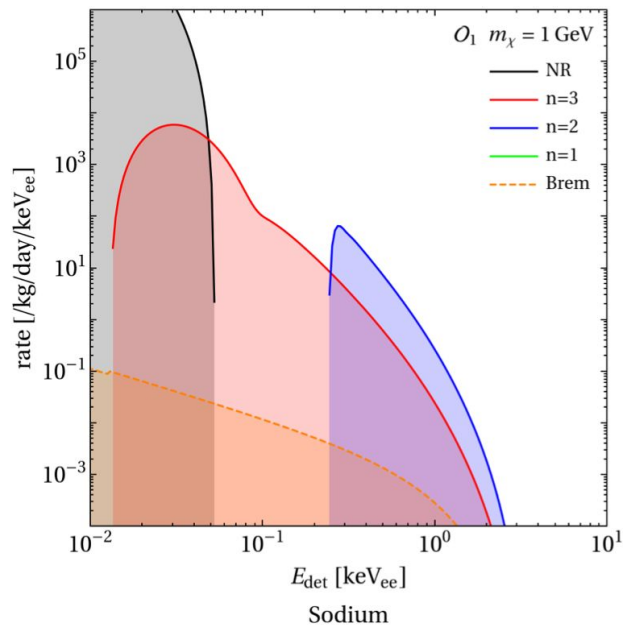
We have examined the Migdal effect and photon brem in the context of the EFT approach, placing new limits on Xe1T



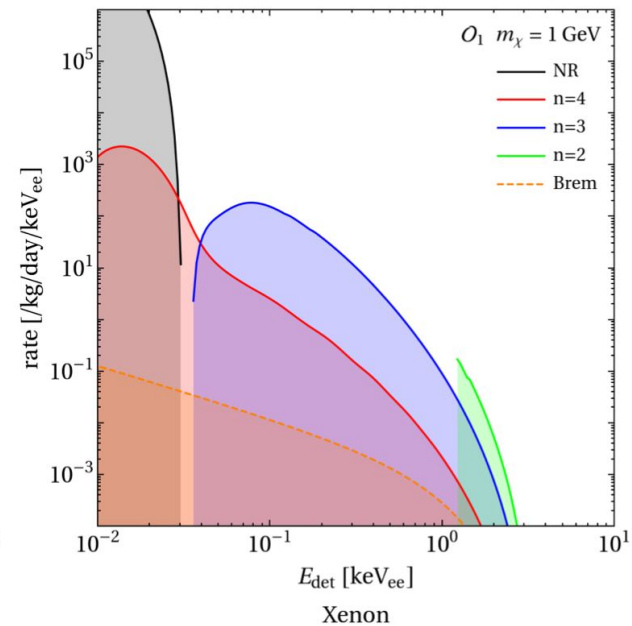
$$\begin{aligned}
 \mathcal{O}_1 & \quad \mathbb{1}_\chi \mathbb{1}_N \\
 \mathcal{O}_4 & \quad \vec{S}_\chi \cdot \vec{S}_N \\
 \mathcal{O}_6 & \quad \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi \right) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N \right) \\
 \mathcal{O}_{10} & \quad \mathbb{1}_\chi \left(i \frac{\vec{q}}{m_N} \cdot \vec{S}_N \right)
 \end{aligned}$$

We've also reassessed the neutrino background in the presence of these effects

Argon



Germanium

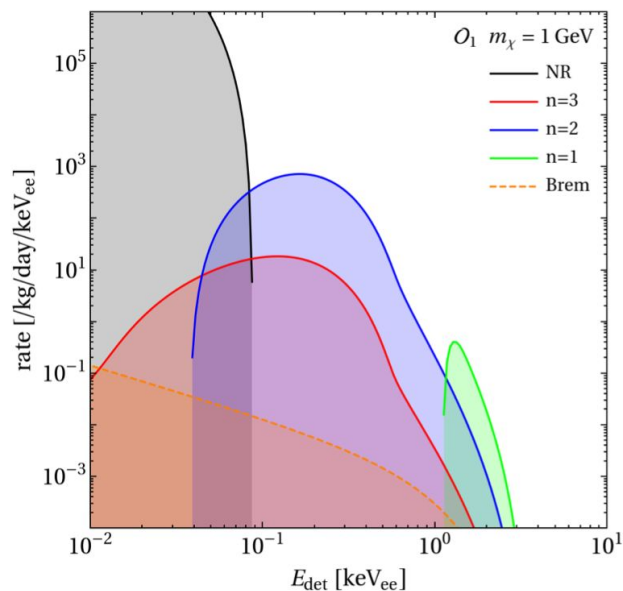


$$\rho_{\chi,\odot} = 0.3 \text{ GeV} \cdot \text{cm}^{-3}$$

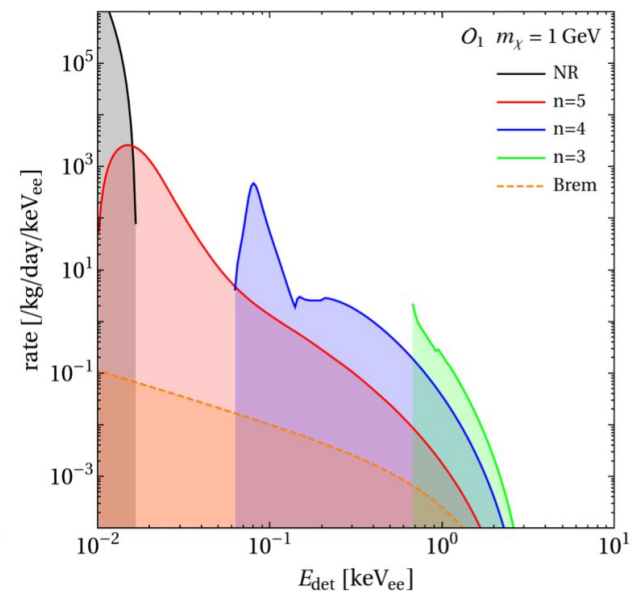
$$v_{\text{esc}} = 544 \text{ km} \cdot \text{s}^{-1}$$

$$v_0 = 220 \text{ km} \cdot \text{s}^{-1}$$

Sodium



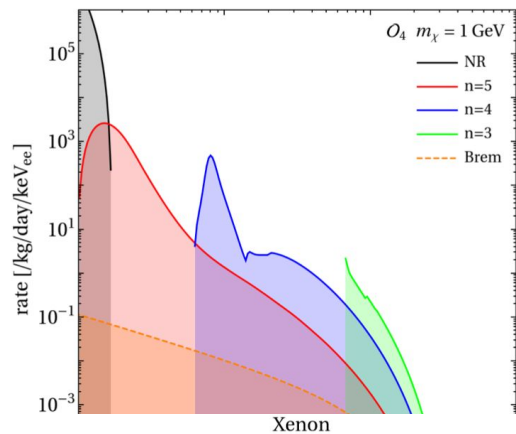
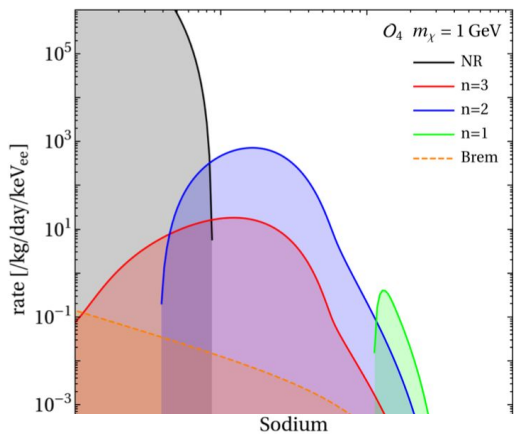
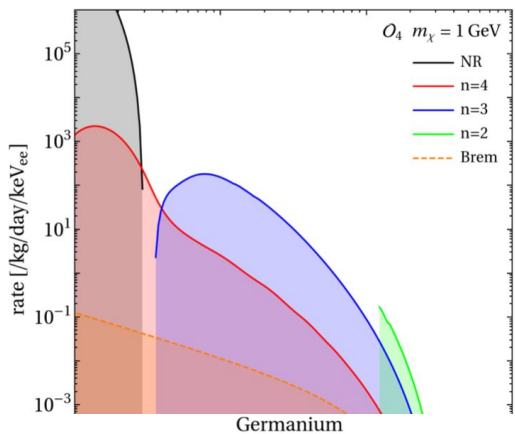
Xenon



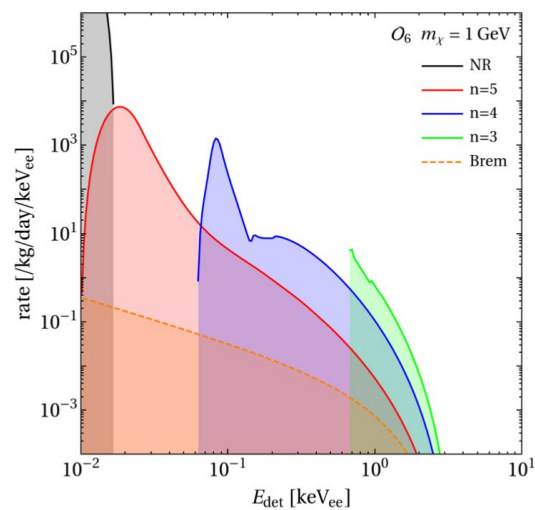
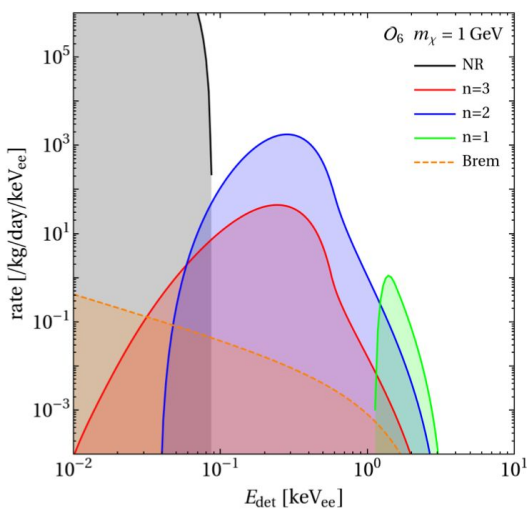
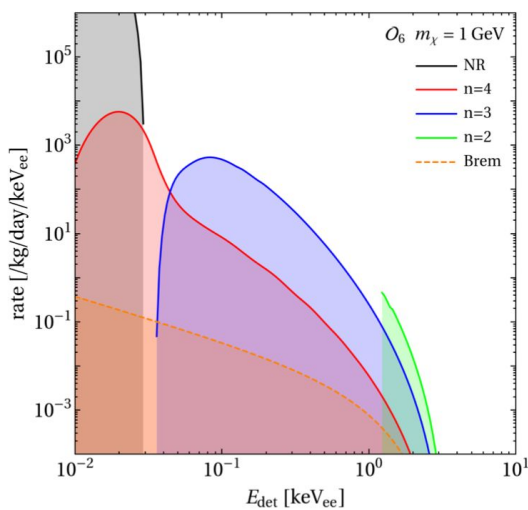
$$\frac{dR}{dE_R} = N_T \frac{\rho_{\chi,\odot}}{m_\chi m_T} \int_{v > v_{\text{min}}} \frac{d\sigma}{dE_R} v f(\vec{v}) d^3v.$$

 \mathcal{O}_1 $\mathbb{1}_\chi \mathbb{1}_N$

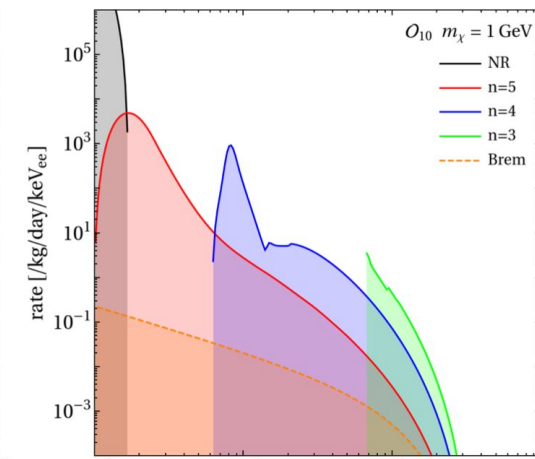
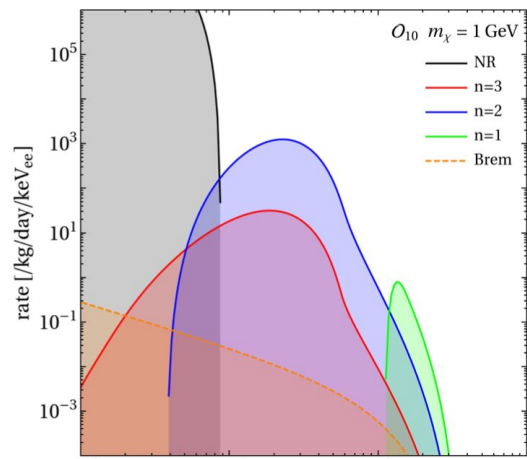
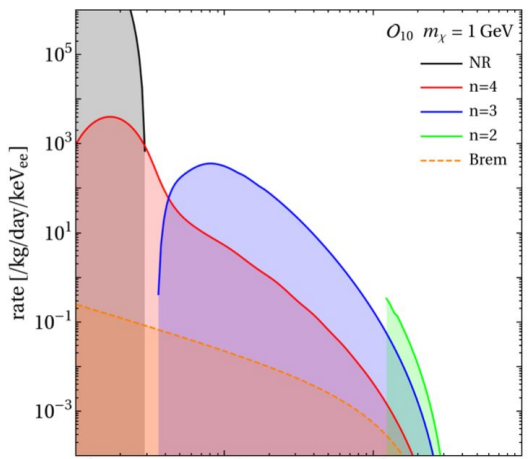
$$\vec{S}_\chi \cdot \vec{S}_N$$

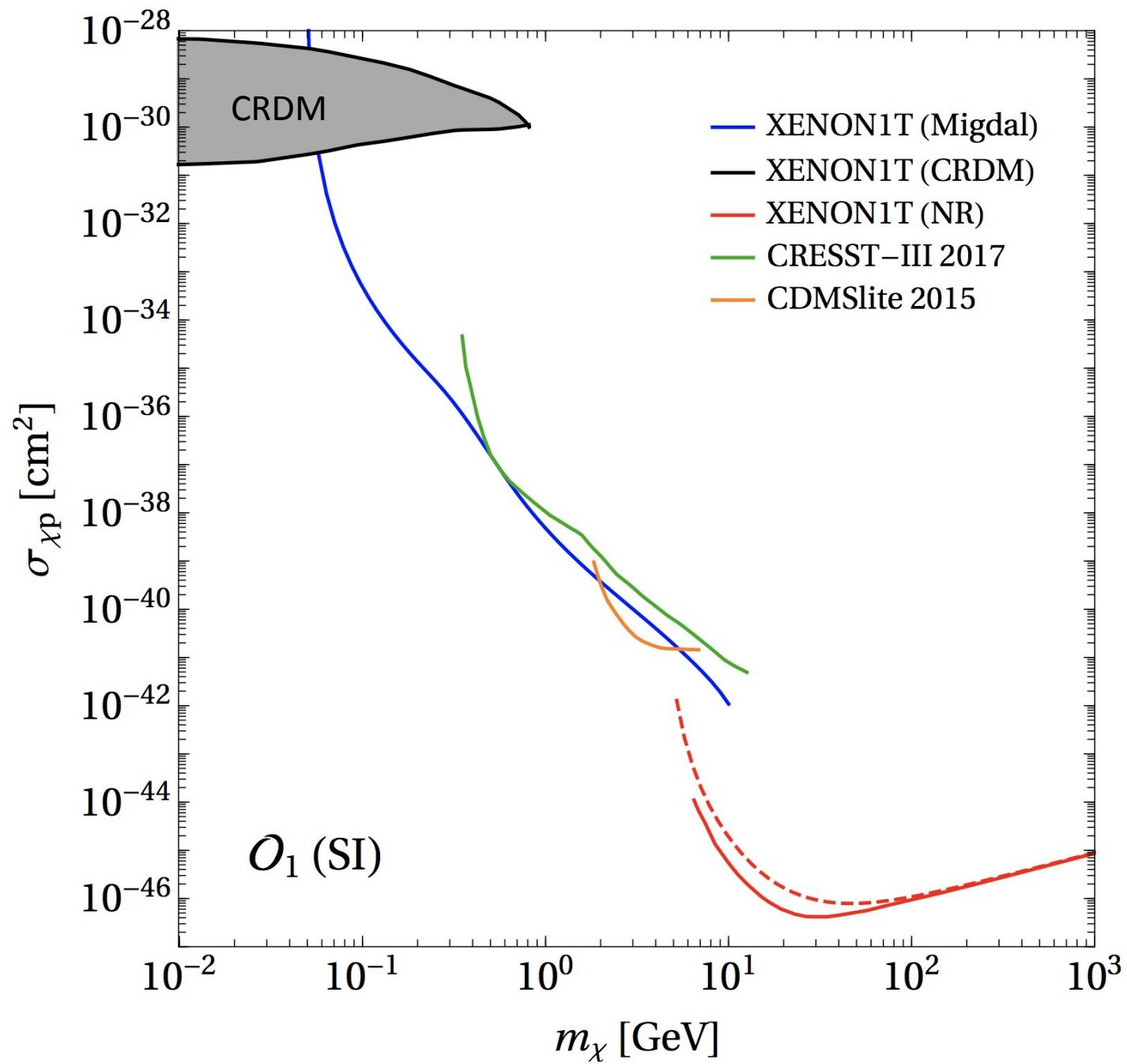


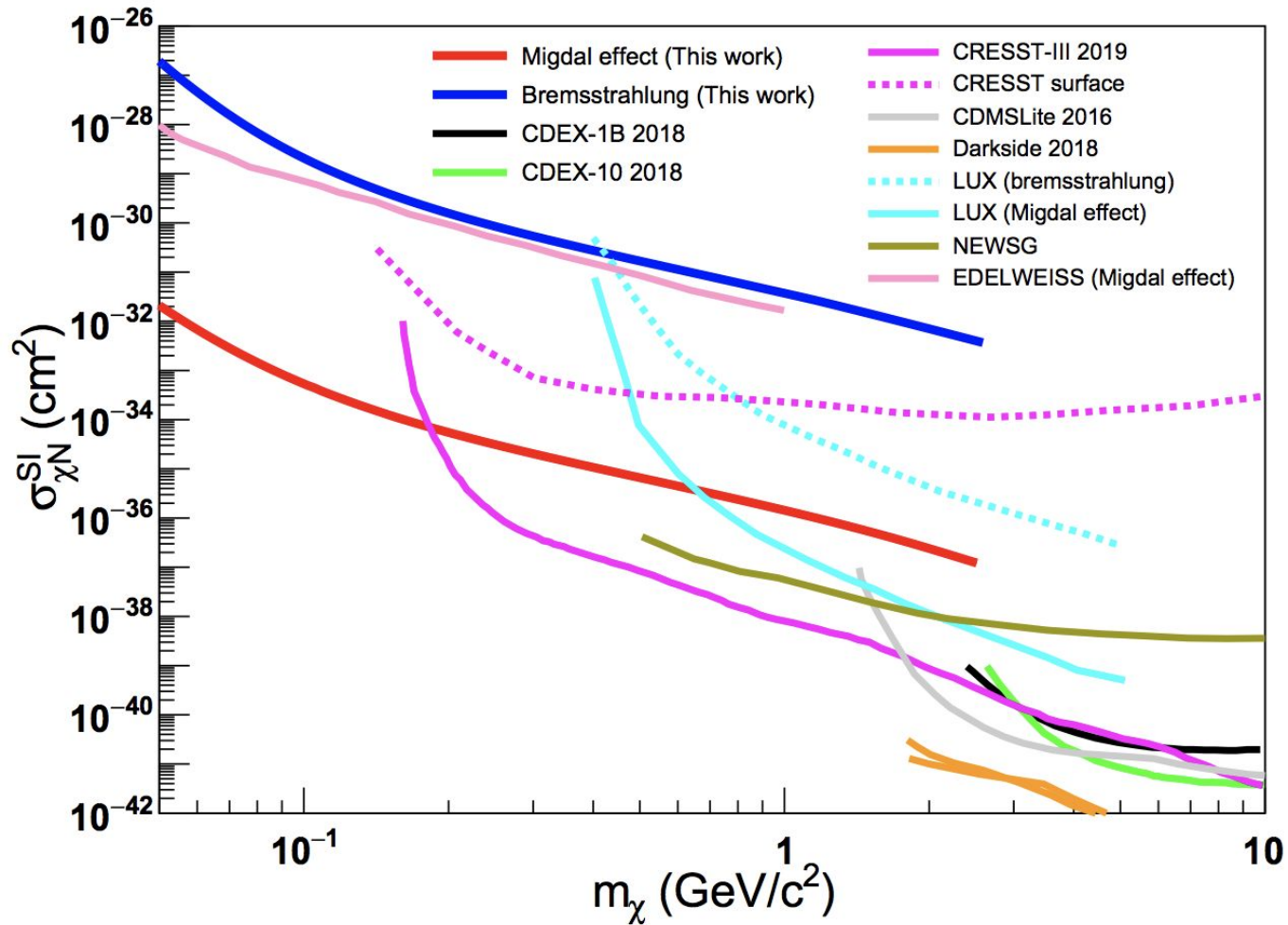
$$\left(\frac{\vec{q}}{m_N} \cdot \vec{S}_\chi \right) \left(\frac{\vec{q}}{m_N} \cdot \vec{S}_N \right)$$



$$\mathbb{1}_\chi \left(i \frac{\vec{q}}{m_N} \cdot \vec{S}_N \right)$$





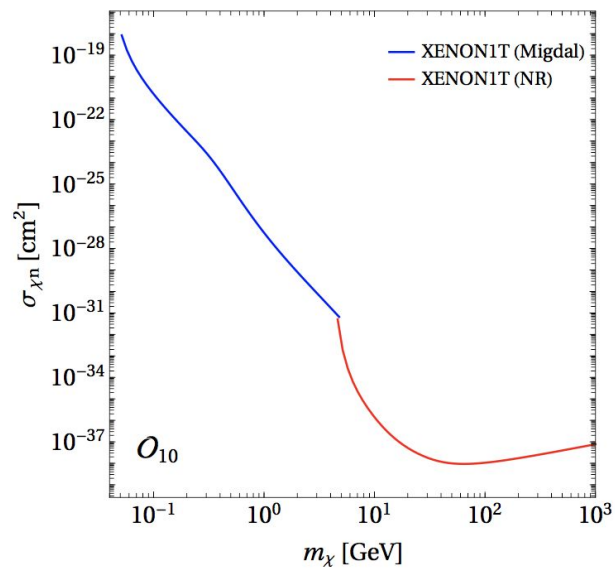
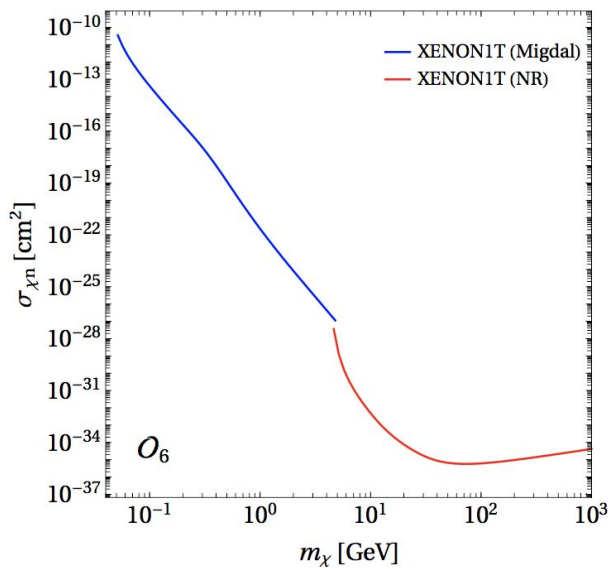
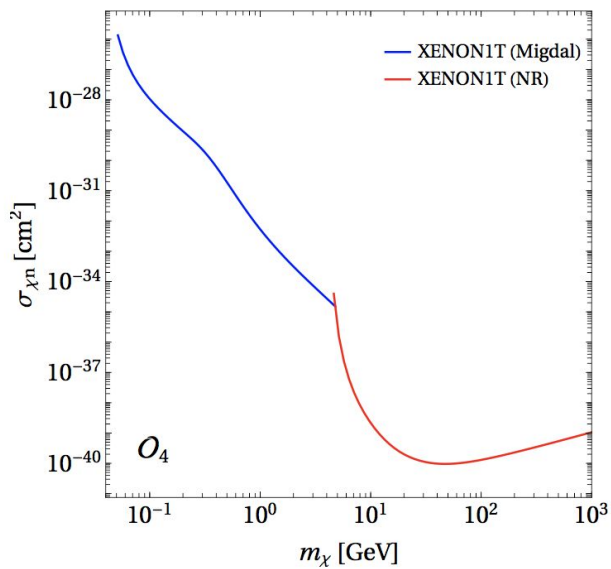
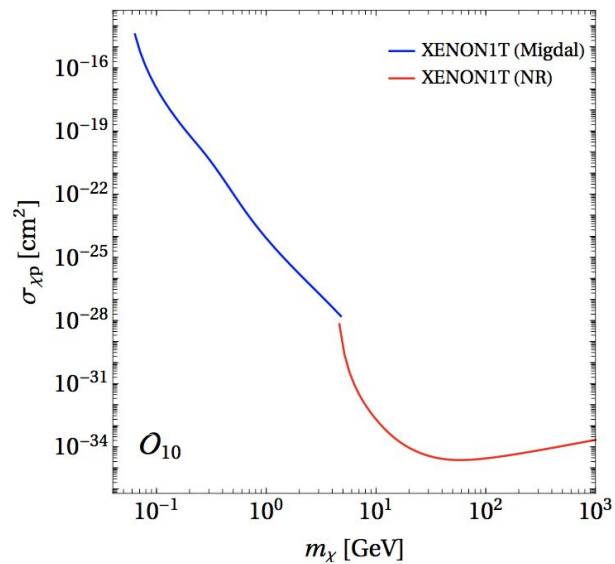
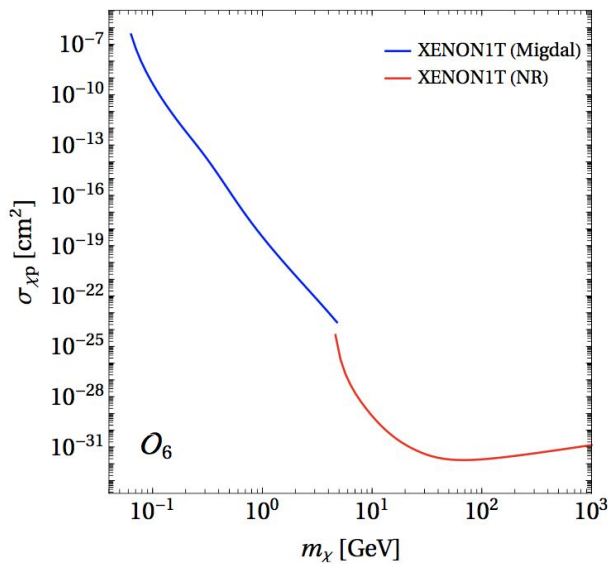
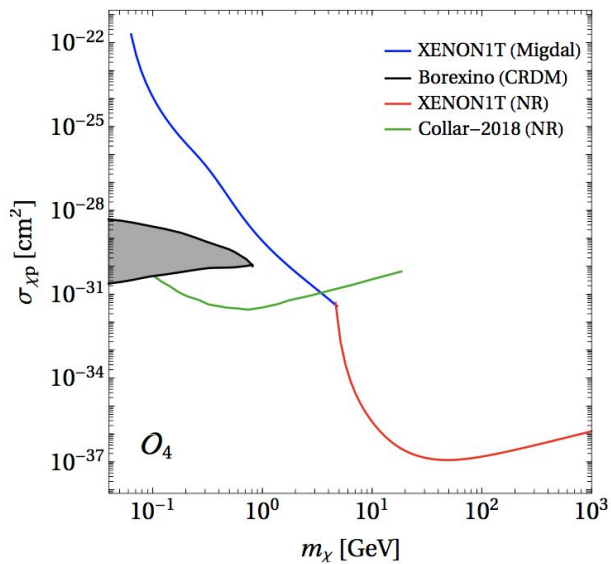


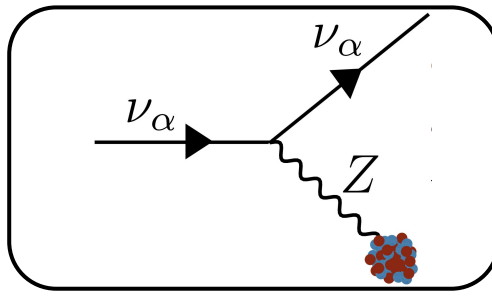
939 g Germanium detector at CJPL
 737.1 kg·day exposure and 160 eVee threshold

Constraints on spin-independent nucleus scattering with sub-GeV WIMP dark matter from the CDEX-1B Experiment at CJPL

CDEX Collaboration ([Z.Z. Liu](#) (Tsinghua U., Beijing) *et al.*). May 1, 2019. 5 pp.

e-Print: [arXiv:1905.00354](https://arxiv.org/abs/1905.00354) [hep-ex]





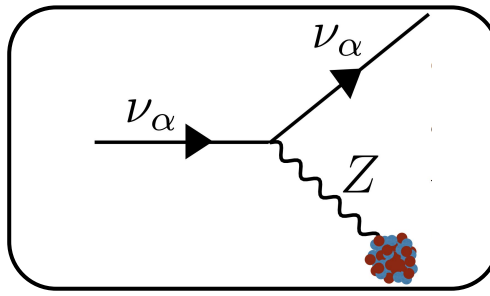
To include the Migdal effect for coherent neutrino-nucleus scattering, we include the ionization rate

$$\frac{d\sigma}{dE_R} = \frac{G_F^2}{4\pi} Q_V^2 m_T \left(1 - \frac{m_T E_R - E_{EM}^2}{2E_\nu^2} \right) F(q)^2 \times |Z_{FI}|^2$$

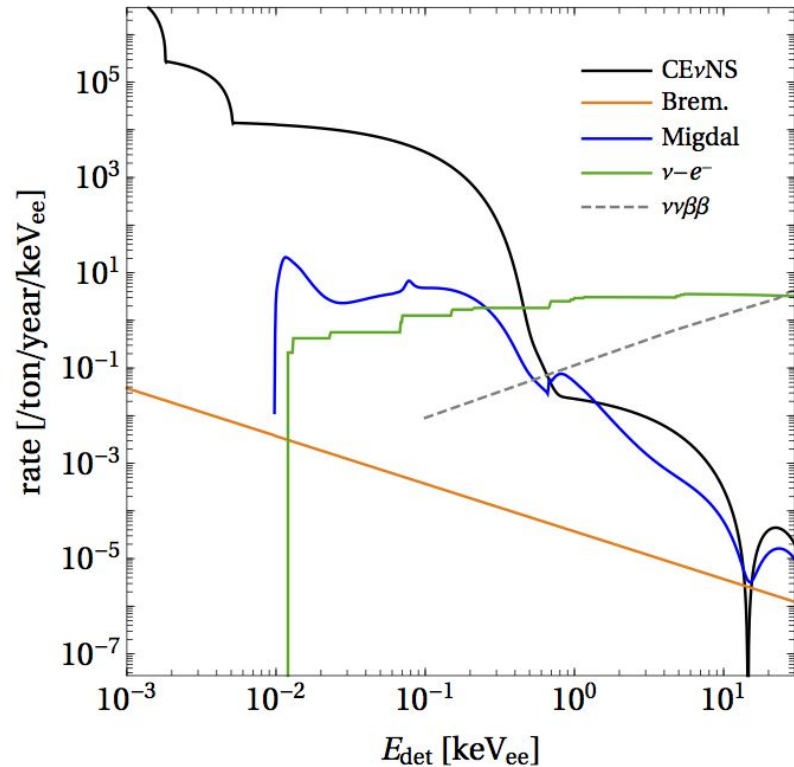
The kinematic endpoints are

$$\frac{(E_e + E_{nl})^2}{2m_T} < E_R < \frac{(2E_\nu - (E_e + E_{nl}))^2}{2(m_T + 2E_\nu)}$$

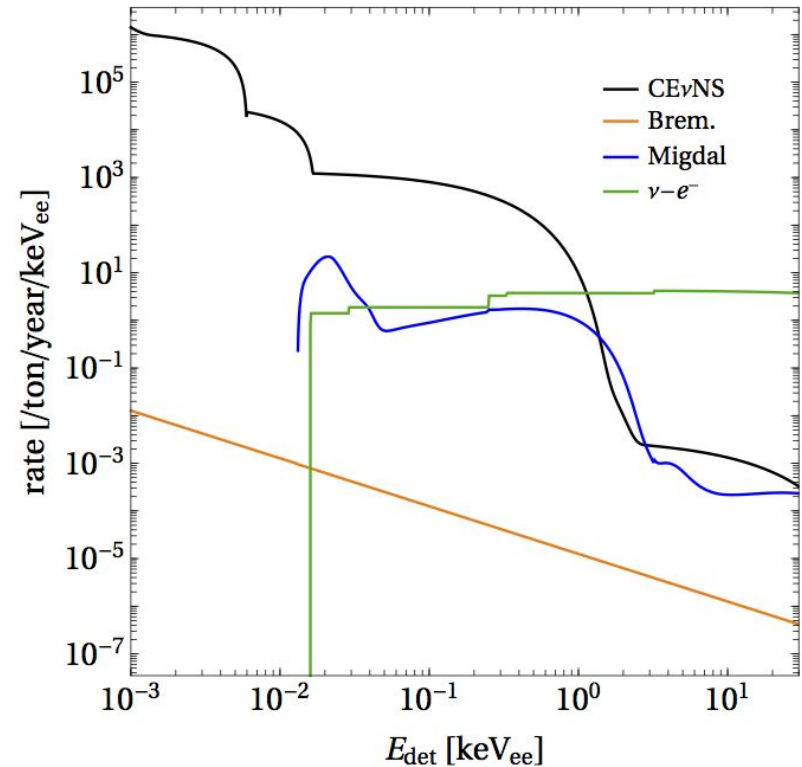
Including the incident fluxes from solar and atmospheric neutrinos, we have calculated the new rates as a function of detected energy



Xenon

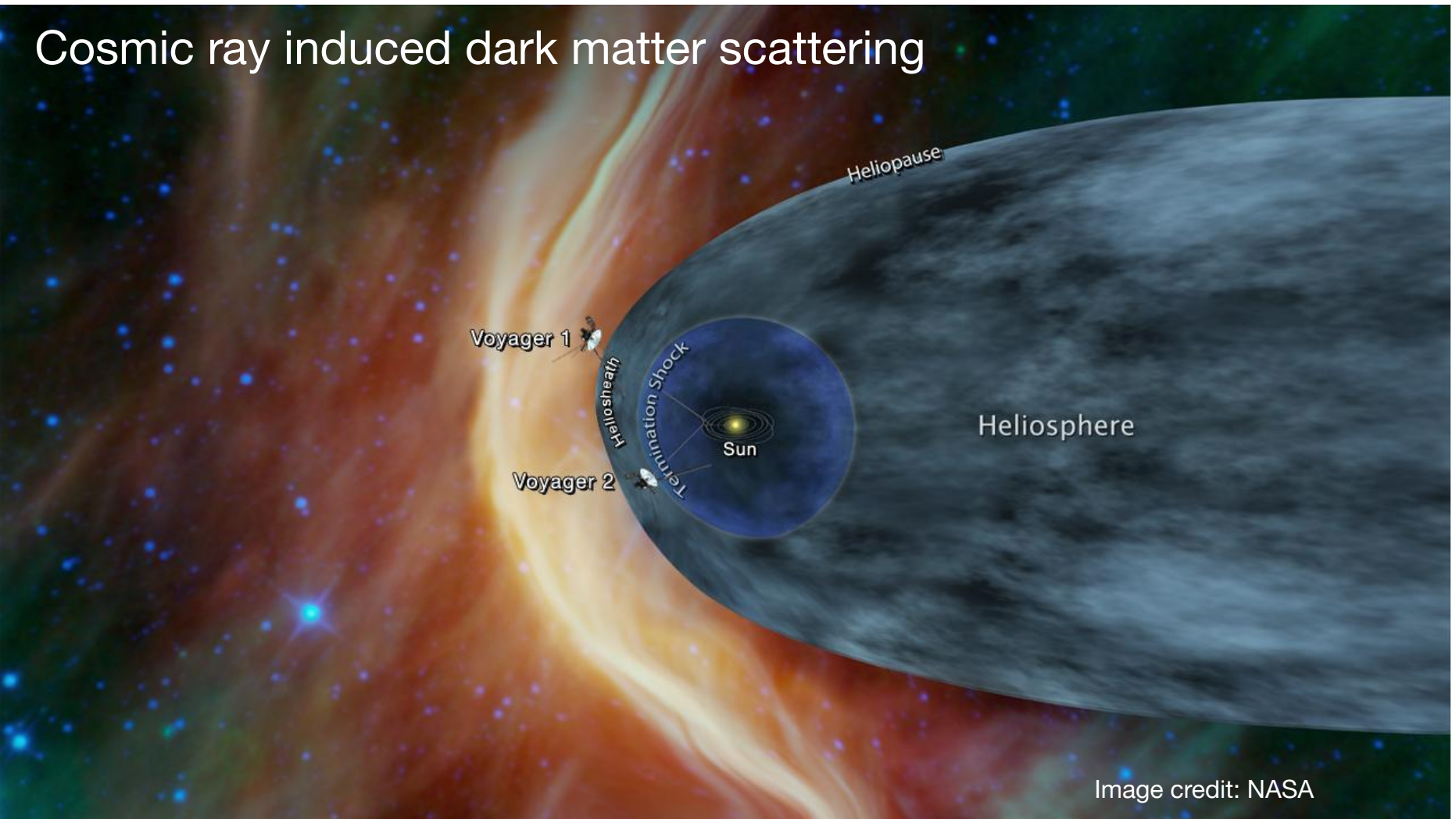


Argon



There is a small window where the Migdal effect induced signal is comparable in rate to the nuclear recoil signal.

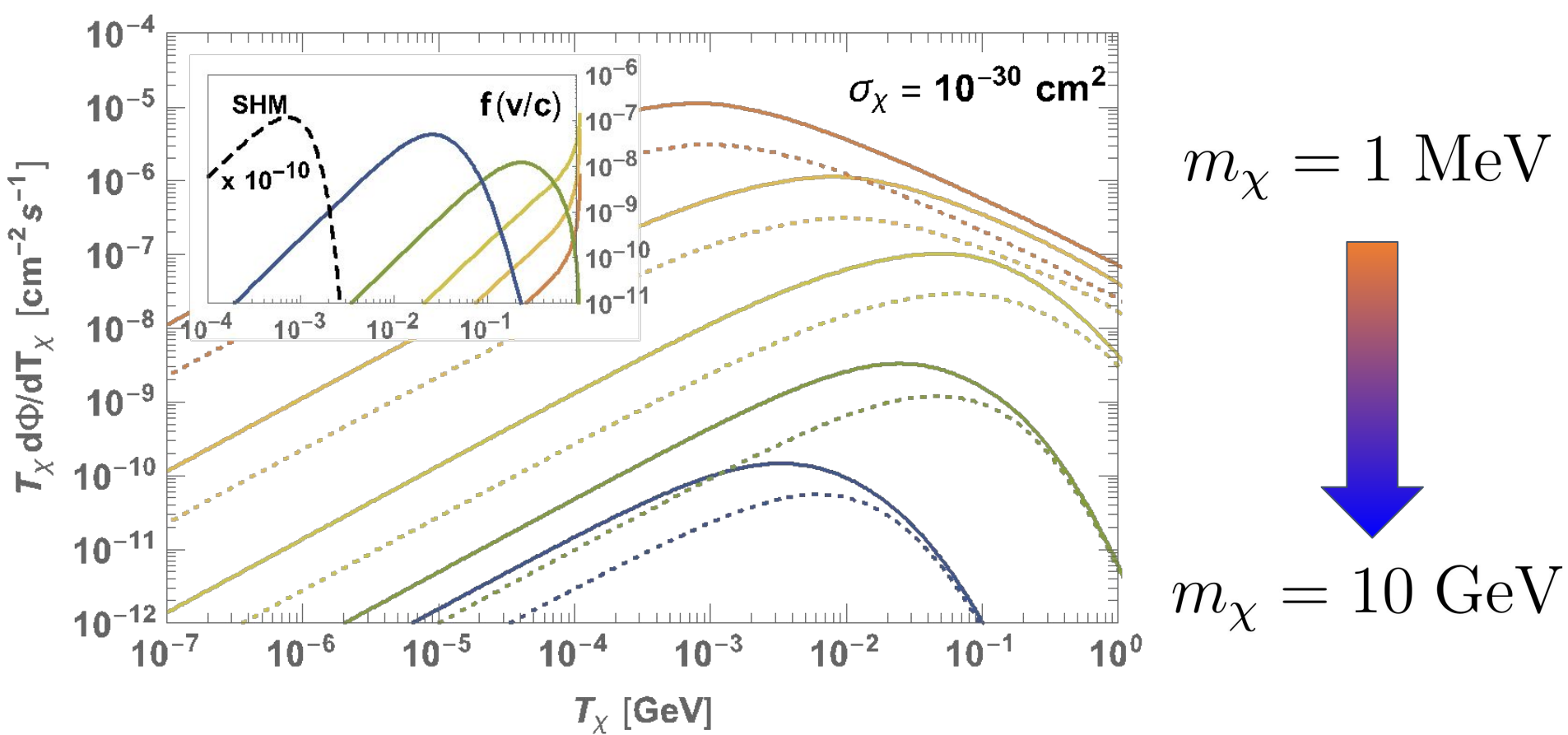
Cosmic ray induced dark matter scattering



C.V. Cappiello, K.C.Y. Ng, and J.F. Beacom PRD 2019, 1810.07705

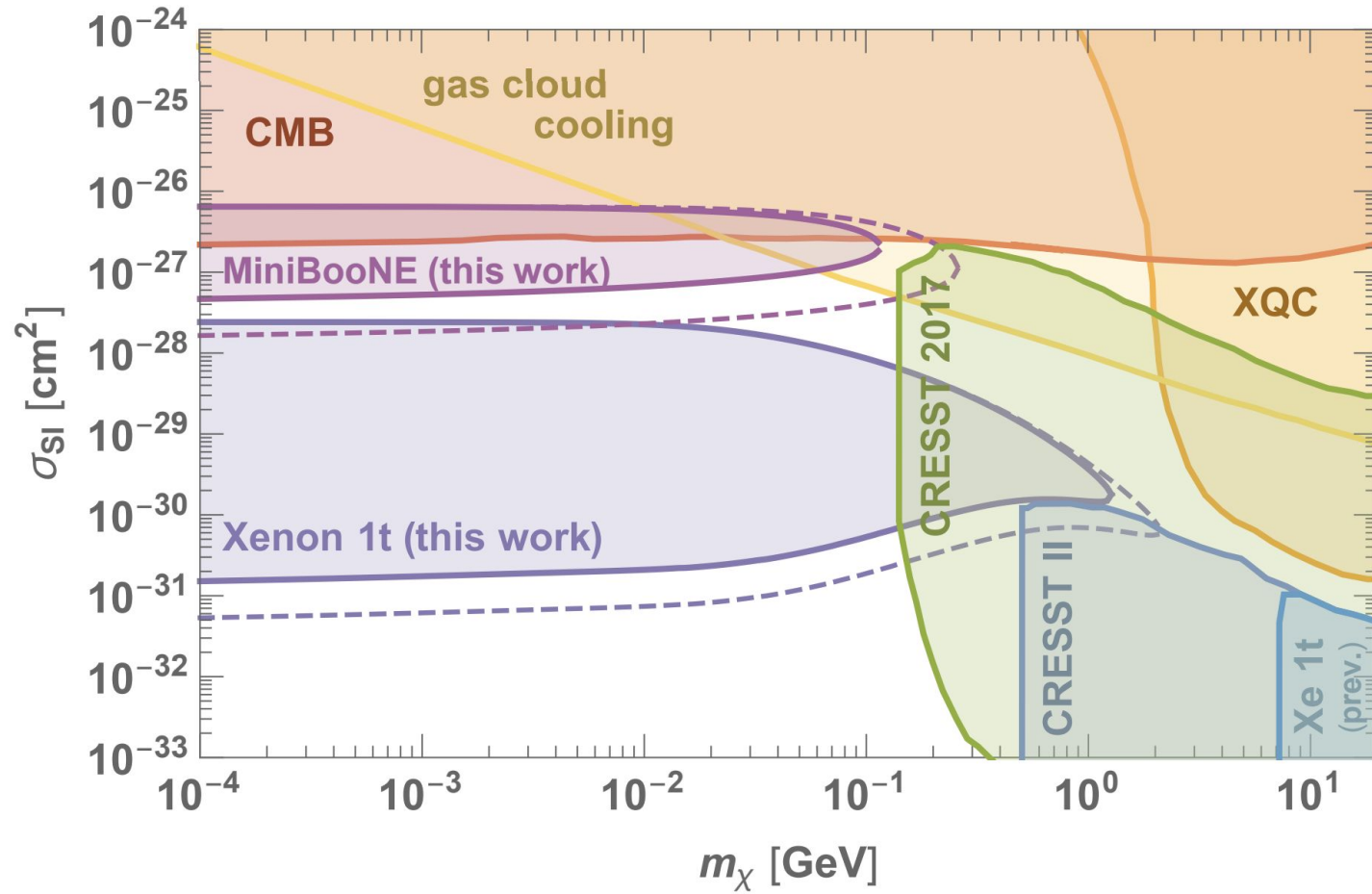
Bringmann and Pospelov PRL 2019, 1810.10543

JBD, B.Dutta, J.L.Newstead, I.Shoemaker, to appear soon



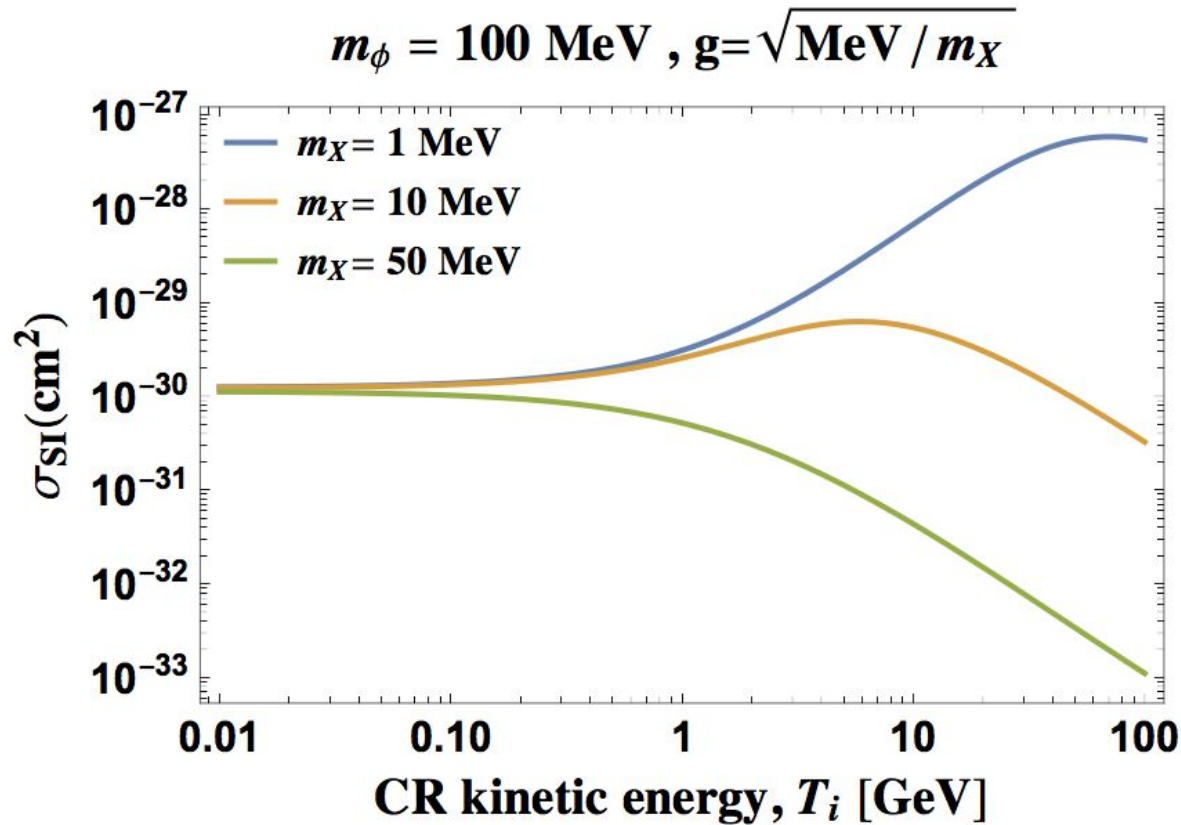
$$\frac{d\Phi_\chi}{dT_i} = \int \frac{d\Omega}{4\pi} \int_{l.o.s.} dl \sigma_{\chi i} \frac{\rho_\chi}{m_\chi} \frac{d\Phi_i}{dT_i} \equiv \sigma_{\chi i} \frac{\rho_\chi^{\text{local}}}{m_\chi} \frac{d\Phi_i^{\text{LIS}}}{dT_i} D_{\text{eff}}$$

$$\frac{d\Phi_\chi}{dT_\chi} = \int_0^\infty dT_i \frac{d\Phi_\chi}{dT_i} \frac{1}{T_\chi^{\text{max}}(T_i)} \Theta [T_\chi^{\text{max}}(T_i) - T_\chi]$$



$$\mathcal{L}_{\text{int}} \supset g_{\chi s} \phi \bar{\chi} \chi + g_{N s} \phi \bar{N} N$$

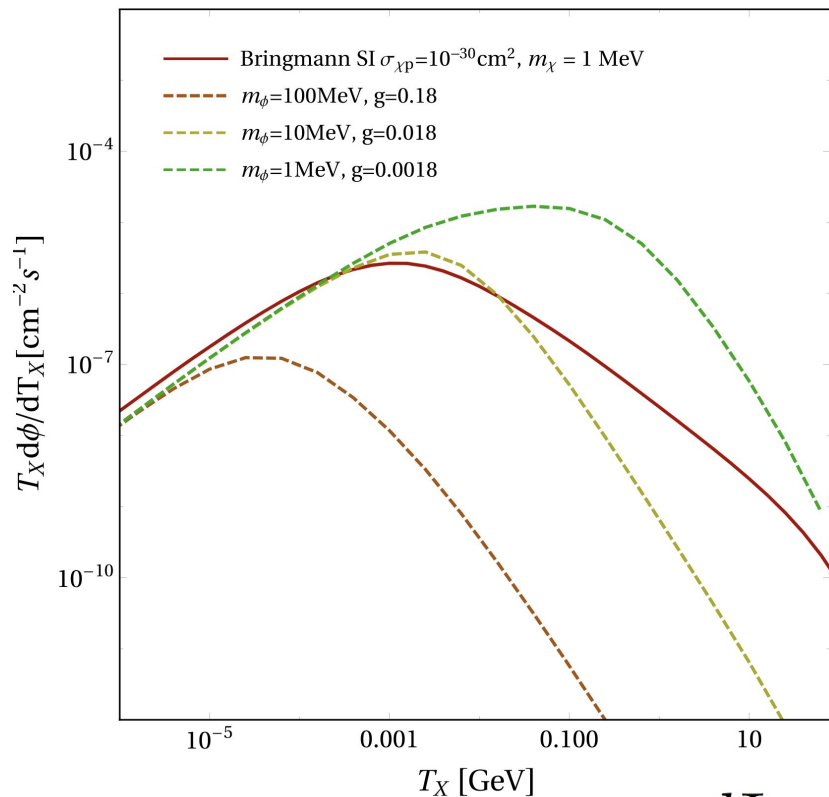
CRDM Preliminary Results



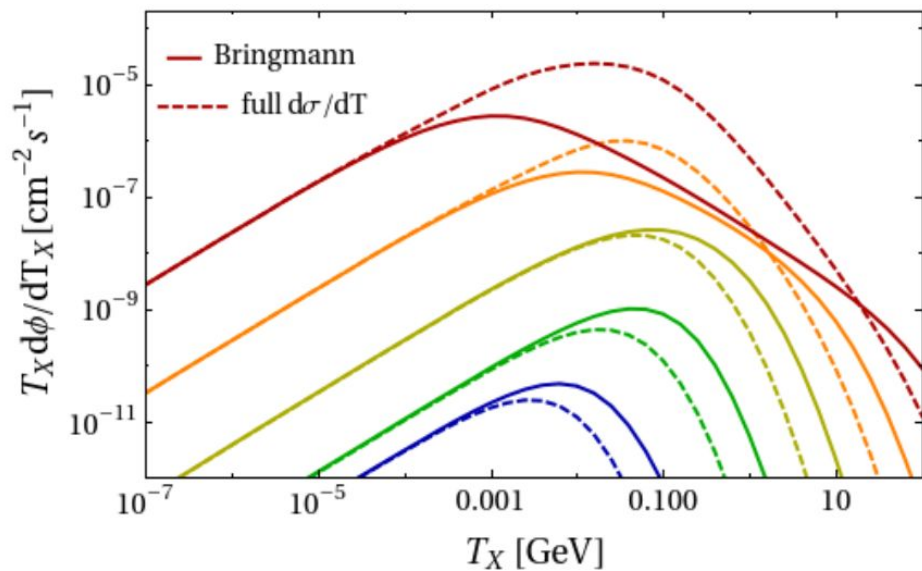
$$\left(\frac{d\sigma}{dT_\chi} \right)_{\text{scalar, CR}} = g_{\chi s}^2 g_{N s}^2 \frac{(4m_\chi m_N^2 + 2T_\chi (m_\chi^2 + m_N^2) + m_\chi T_\chi^2)}{8\pi (2m_\chi T_\chi + m_\phi^2)^2 (T_i^2 + 2m_T T_i)}$$

Fluxes and rates

CRDM Preliminary Results

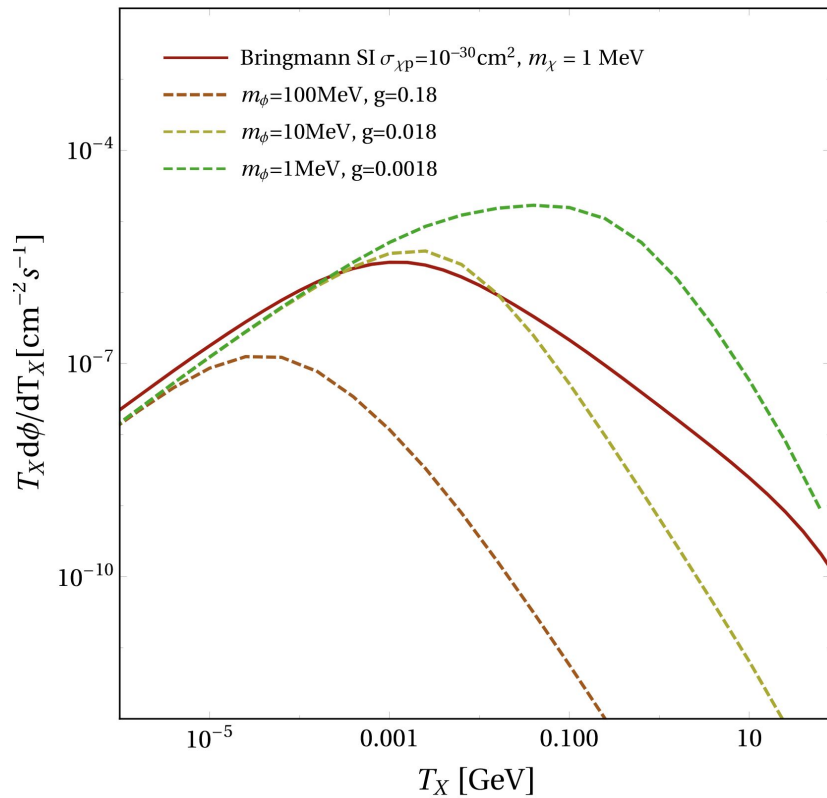


$$\sigma_{\chi p} = 10^{-30} \text{cm}^2$$



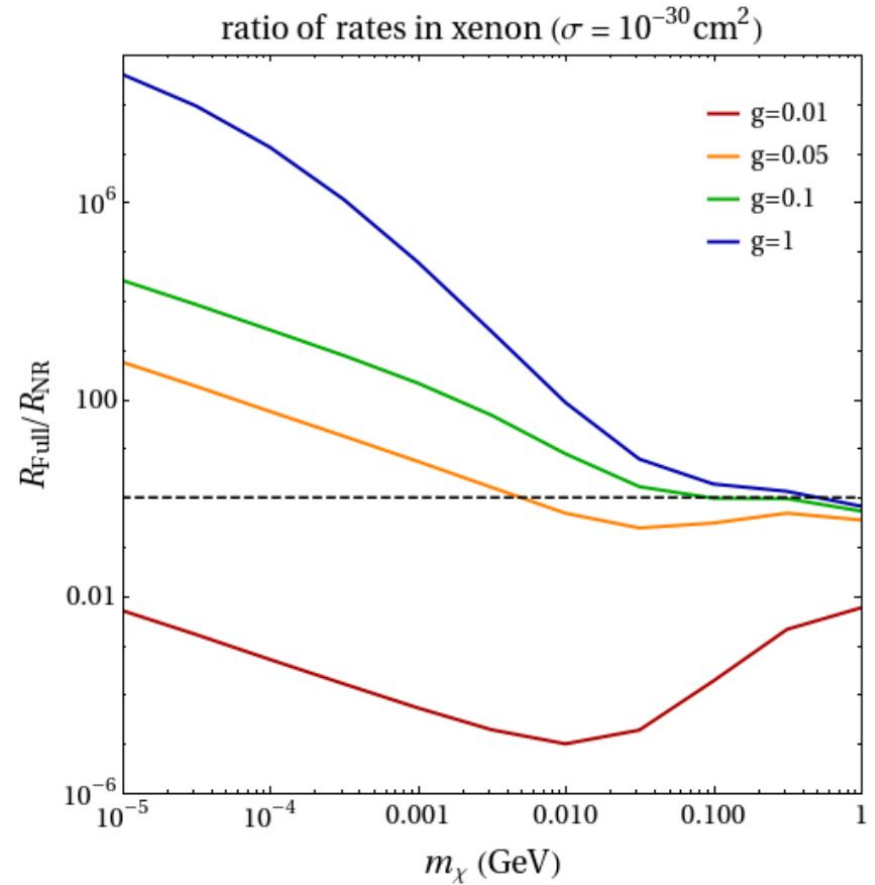
$$\begin{aligned} \frac{d\Phi_\chi}{dT_\chi} &= \int_V dV \int_{T_i^{\min}} dT_i \frac{d^2\Gamma_{\text{CR}_i \rightarrow \chi}}{dT_i dT_\chi} \\ &= D_{\text{eff}} \frac{\rho_\chi}{m_\chi} \sum_i \int_{T_i^{\min}} dT_i \frac{d\sigma_{\chi i}}{dT_\chi} \frac{d\Phi_i^{\text{LIS}}}{dT_i} \end{aligned}$$

Fluxes and rates



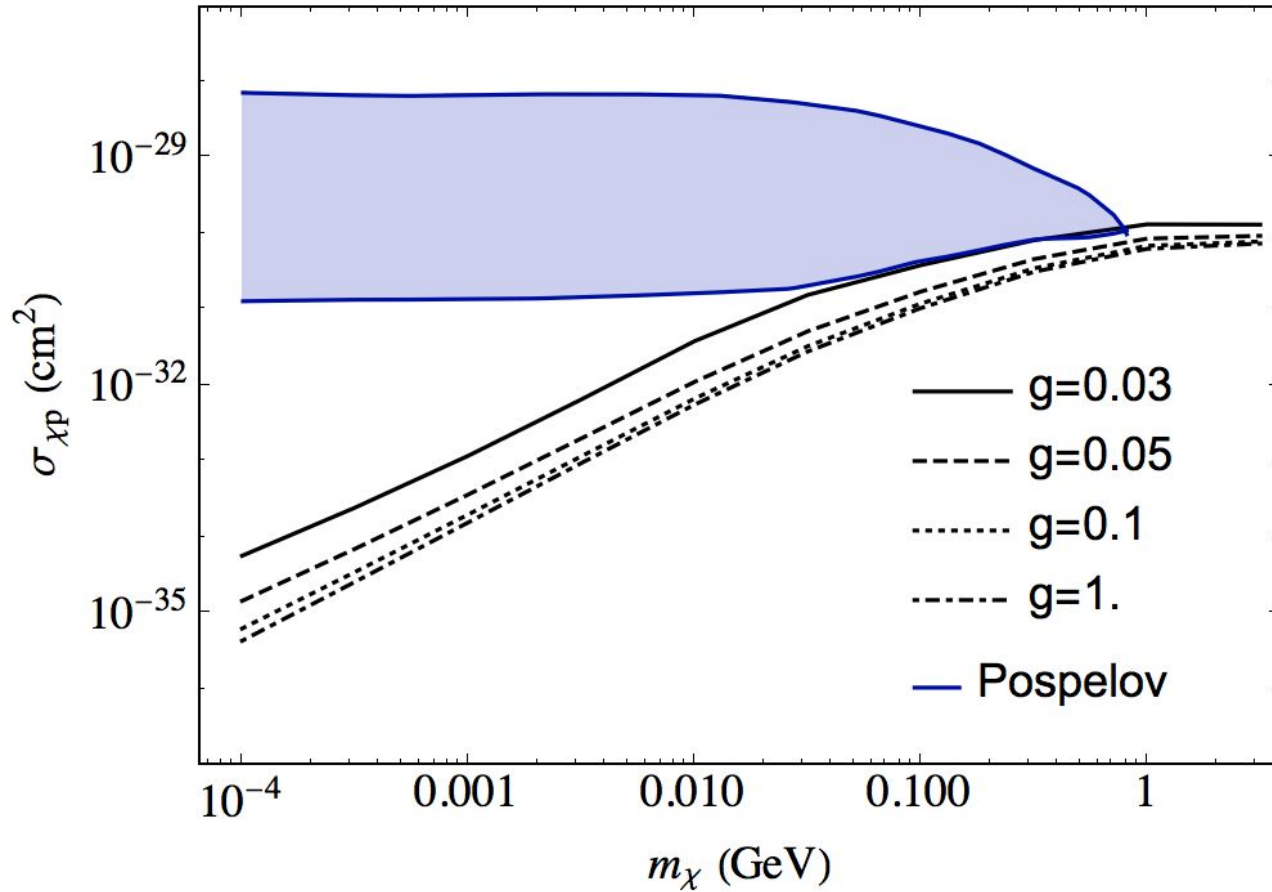
$$\frac{dR}{dE_T} = \frac{1}{m_N} \int_{T_\chi^{\min}}^{\infty} dT_\chi \frac{d\Phi_\chi}{dT_\chi} \frac{d\sigma_{\chi-n}}{dE_T}$$

CRDM Preliminary Results

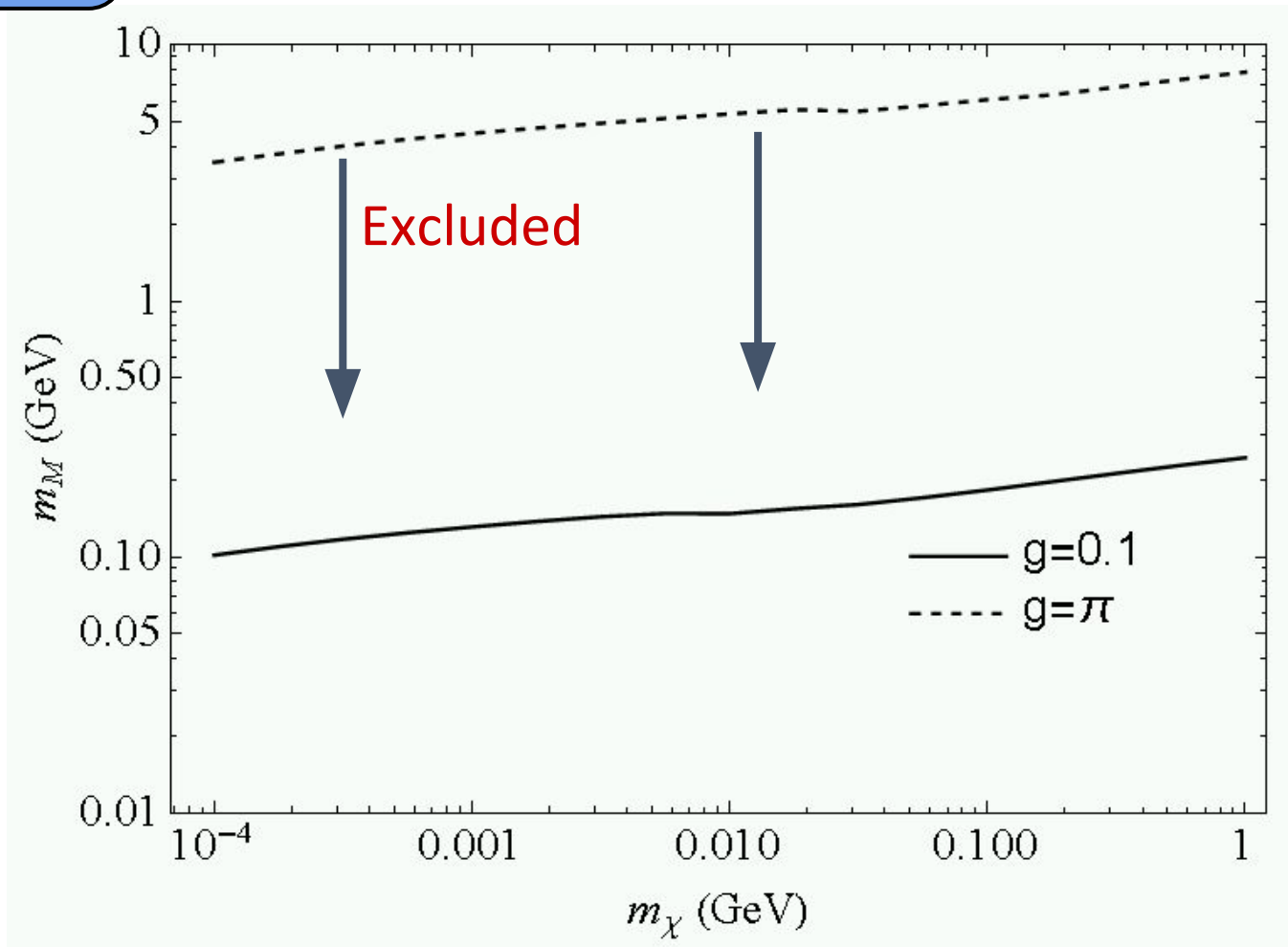


Energy dependence must be accounted for on the direct detection side as well

SI

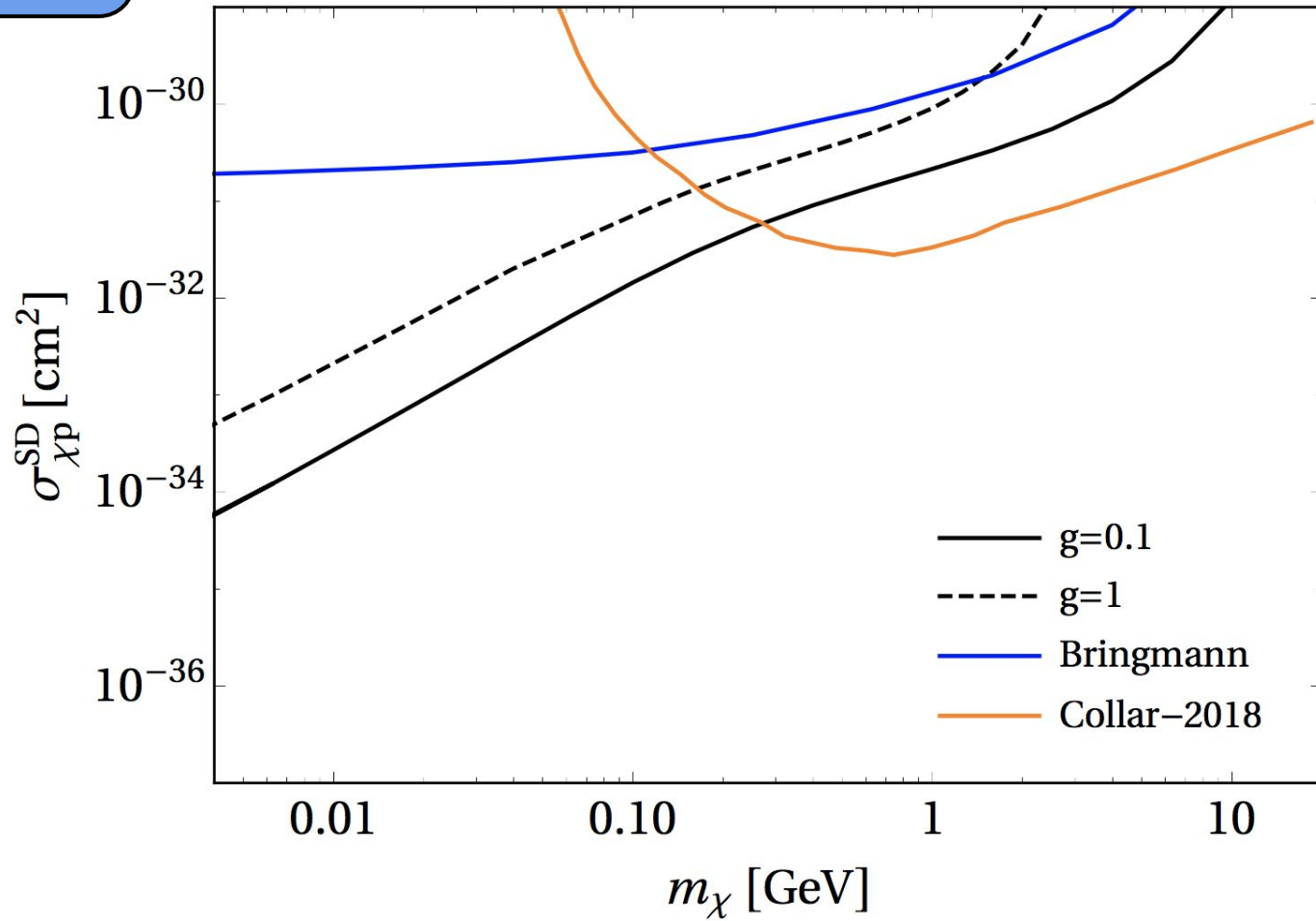


SI

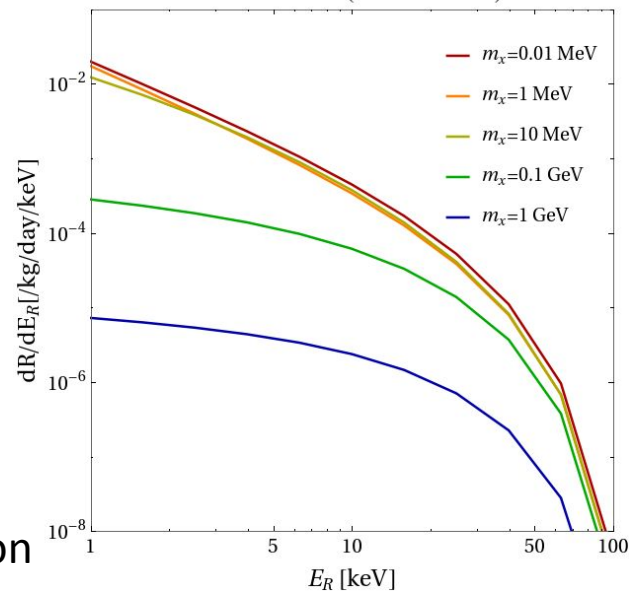
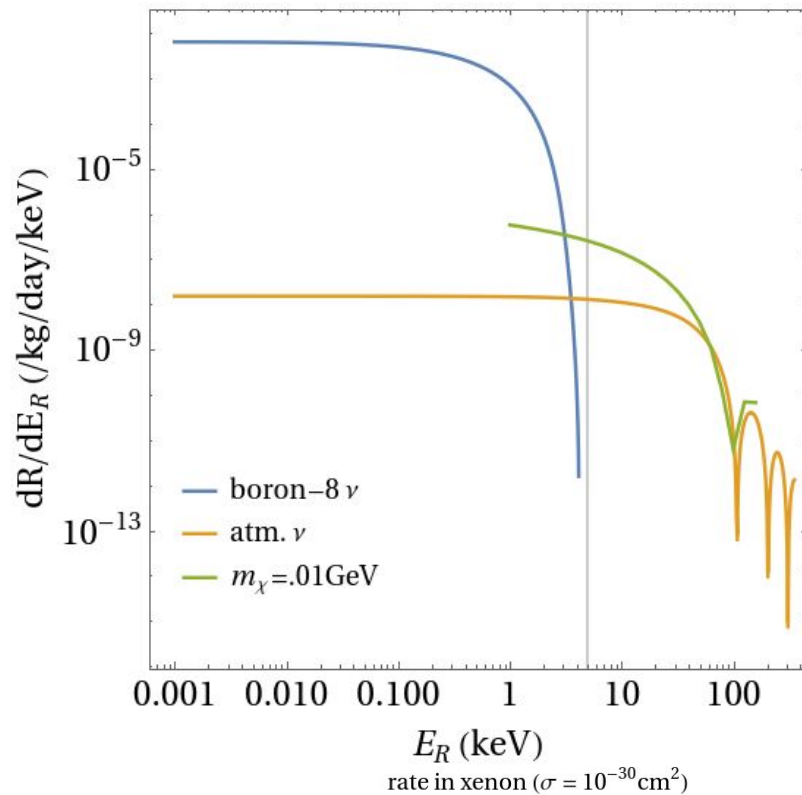
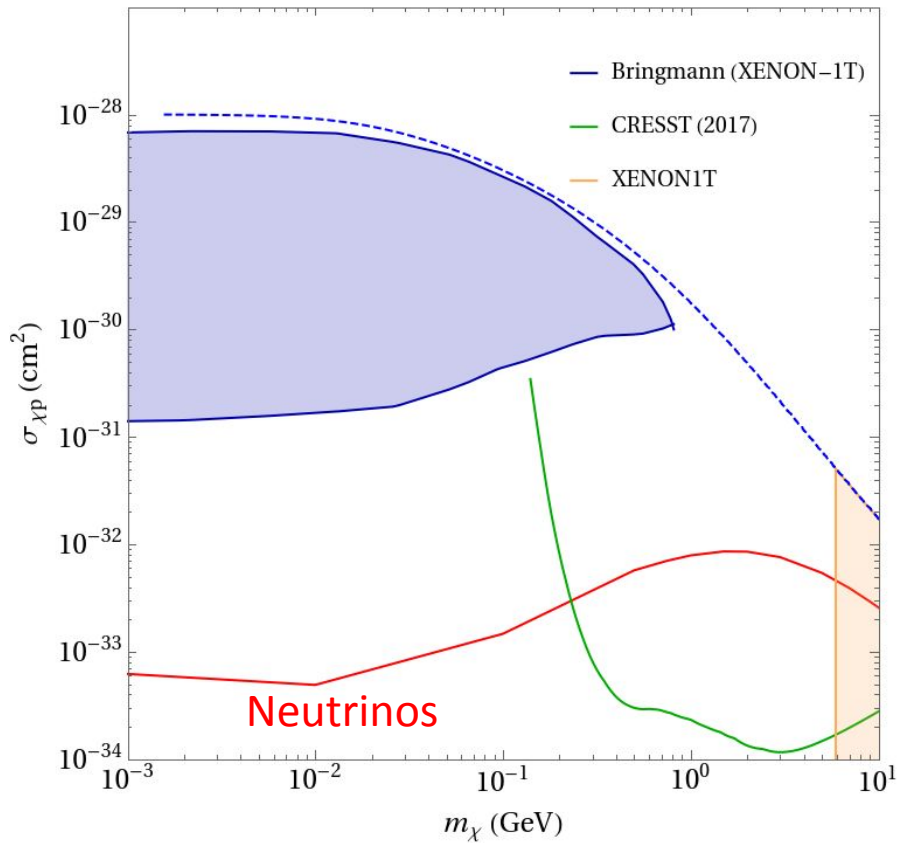


SD

CRDM Preliminary Results



CRDM Preliminary Results



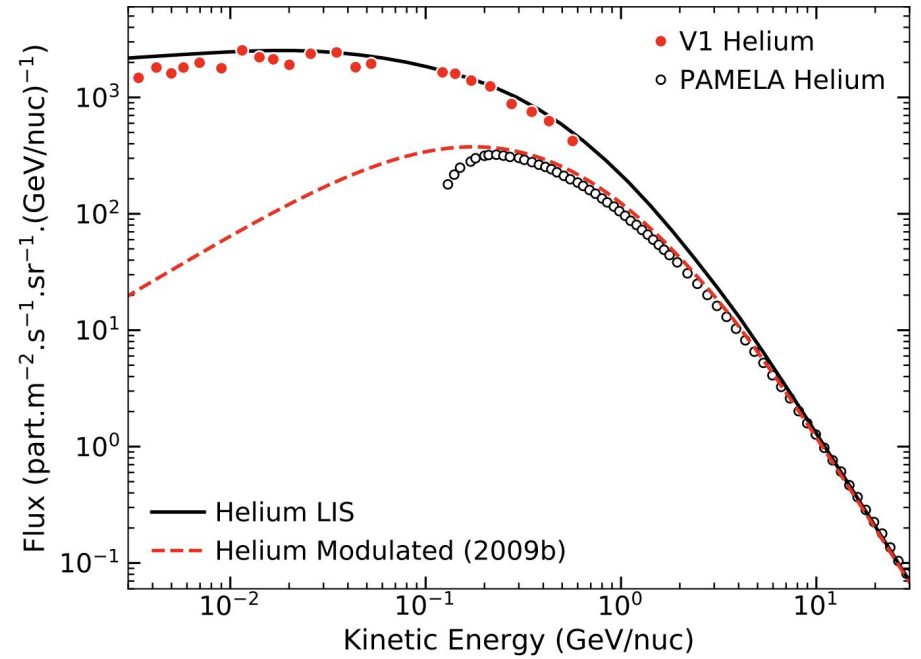
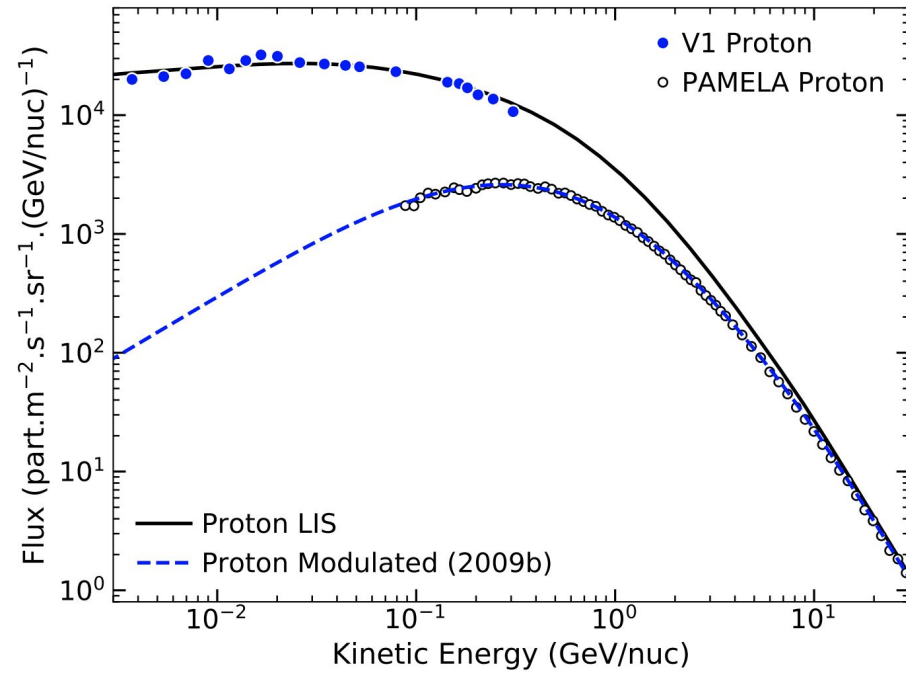
JBD, B.Dutta, J.L.Newstead, I.Shoemaker, to appear soon

Summary

A tremendous variety of searches are being carried out for sub-GeV mass dark matter.

Utilizing complementary approaches from experiment and theory in astrophysics, cosmology, and particle physics, we expect a continued coverage of unexplored regions of parameter space.

CR Spectra



New very local interstellar spectra for electrons, positrons, protons and light cosmic ray nuclei

D. Bisschoff, M.S. Potgieter, O.P.M. Aslam (Potchefstroom U.). Feb 27, 2019. 14 pp.

e-Print: [arXiv:1902.10438](https://arxiv.org/abs/1902.10438) [astro-ph.HE] | [PDF](#)

Attenuation due to the Earth's overburden

$$T_{\chi}^0 = 2m_{\chi} T_{\chi}^z e^{z/\ell} \left(2m_{\chi} + T_{\chi}^z - T_{\chi}^z e^{z/\ell} \right)^{-1}$$

Cross-sections above a critical value will decelerate the dark matter flux to unobservable energies.

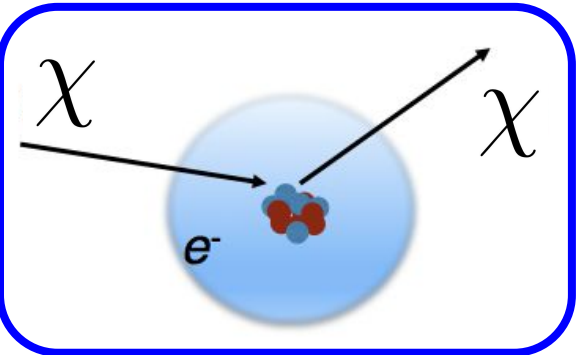
$$\ell^{-1} \equiv \sum_{T_i} \sigma_{\chi T_i} \frac{2m_{T_i} m_{\chi}}{(m_{T_i} + m_{\chi})^2}$$

$$\sigma_{\chi T_i} = \sigma_{\chi}^{\text{SI}} A^2 \left(\frac{m_{T_i} (m_{\chi} + m_p)}{m_p (m_{\chi} + m_{T_i})} \right)^2$$

This provides an upper bound on the cross-section sensitivity for underground experiments.

$$\sigma_{\text{thick}} \simeq \frac{1}{n_{\text{SI}} z} \log \left(1 + \sqrt{\frac{8m_{\chi}^2}{E_{\text{th}} m_{T_i}}} \right)$$

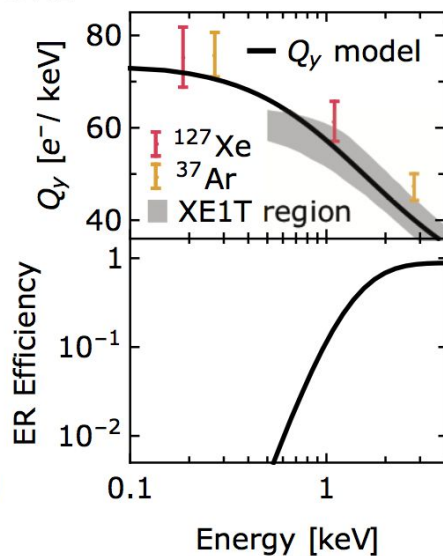
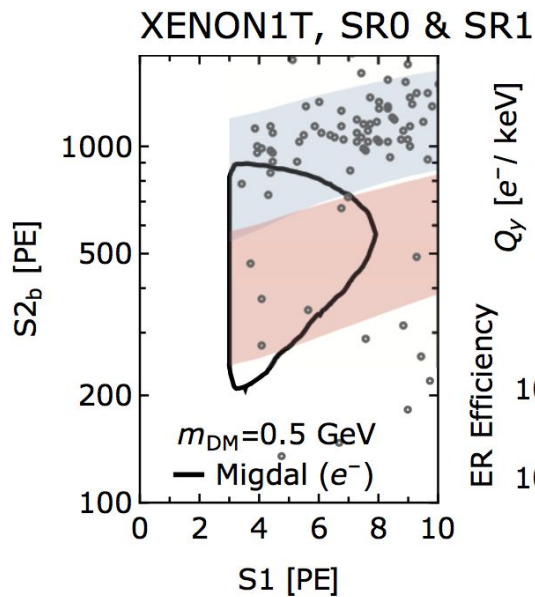
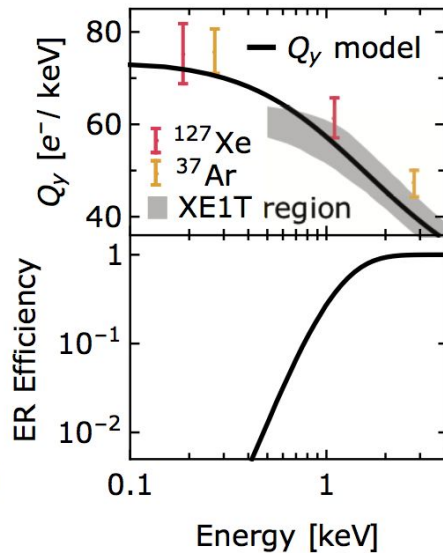
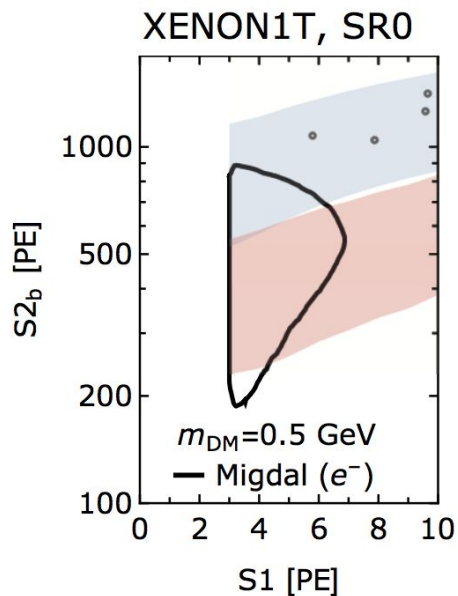
$$n_{\text{SI}}(T_{\chi}) \equiv (\ell(T_{\chi}) \sigma_{\text{SI}})^{-1}$$



$$S1 = g_1 L_y E_{EM}$$

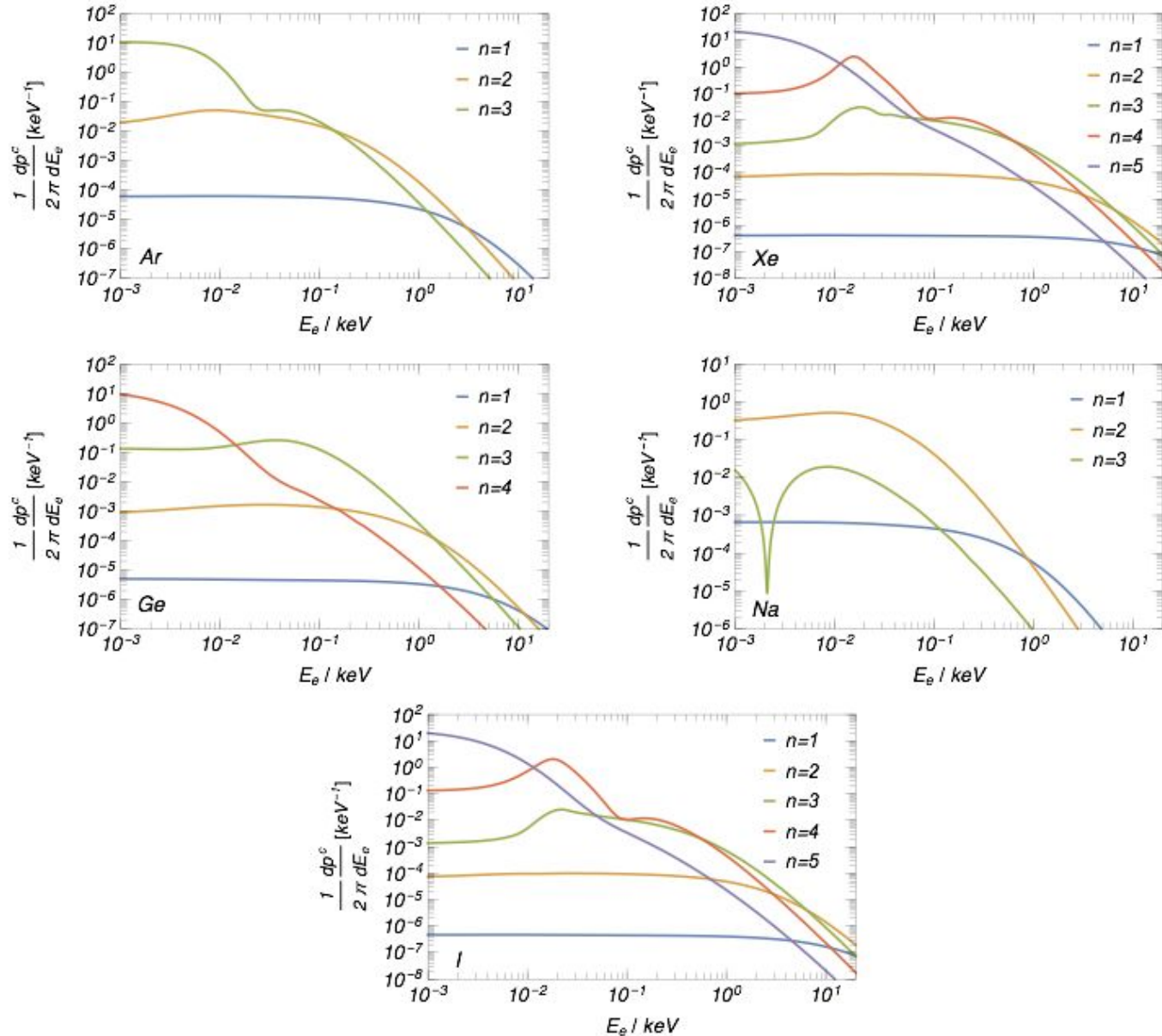
$$S2 = g_2 Q_y E_{EM}$$

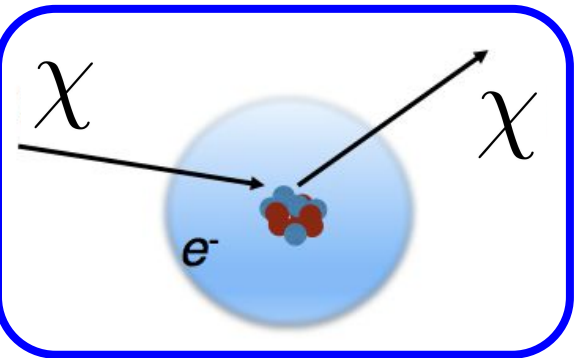
$$\frac{1}{W} = L_y + Q_y$$



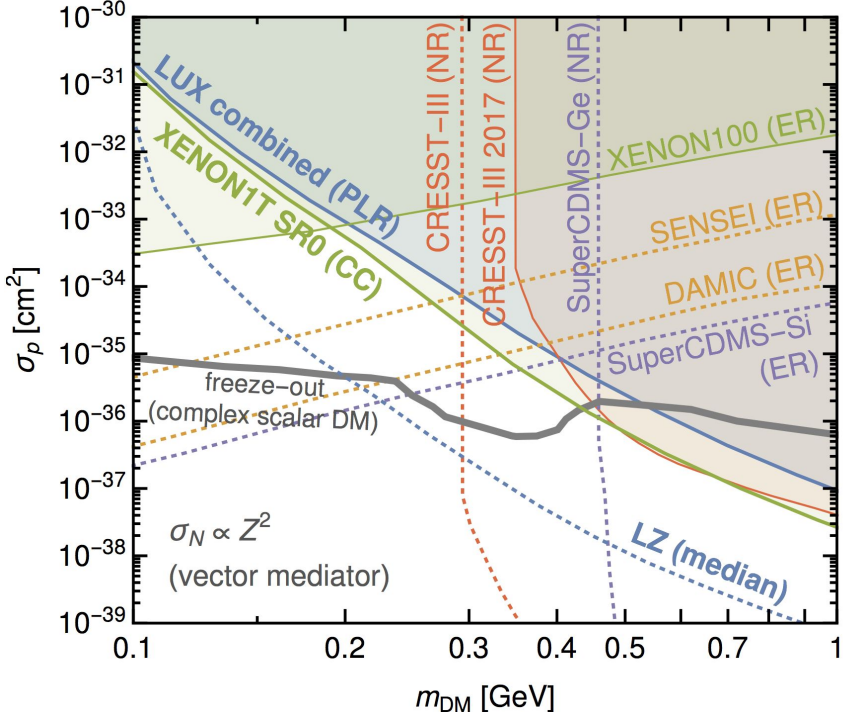
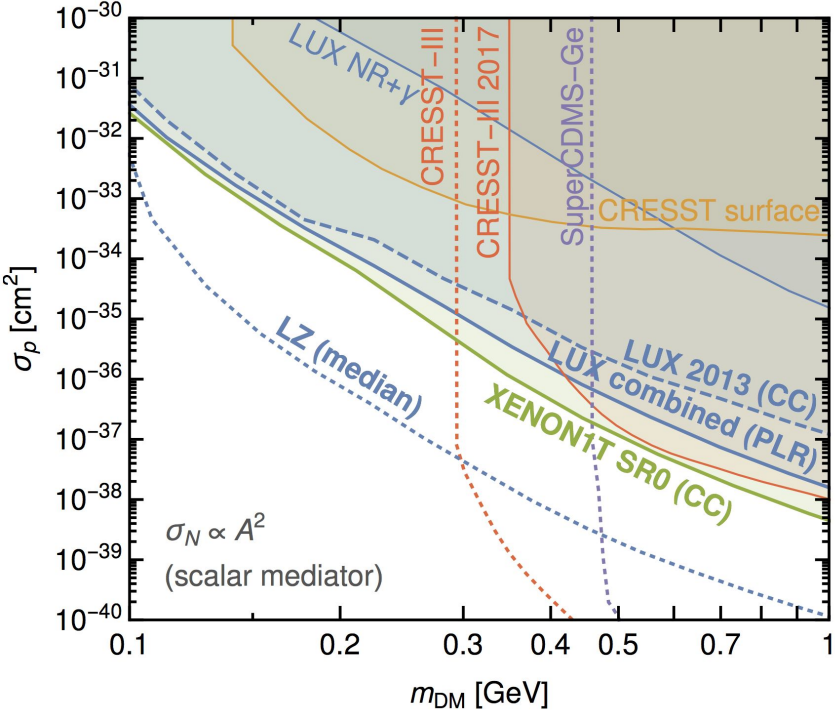
Migdal and Brem limits and experimental results

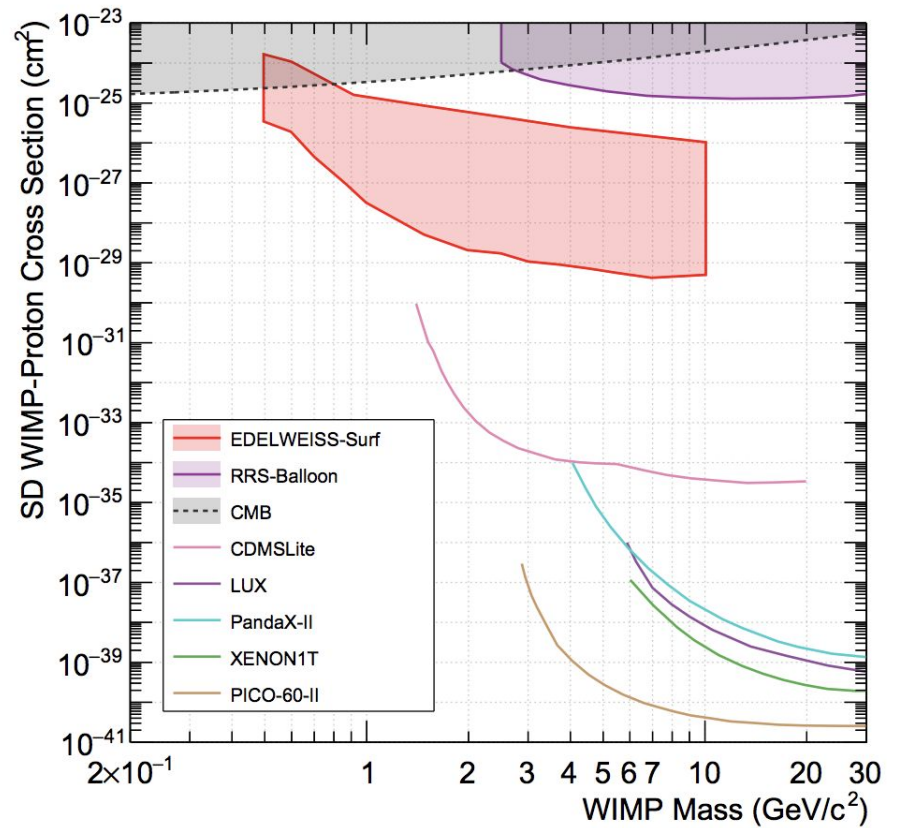
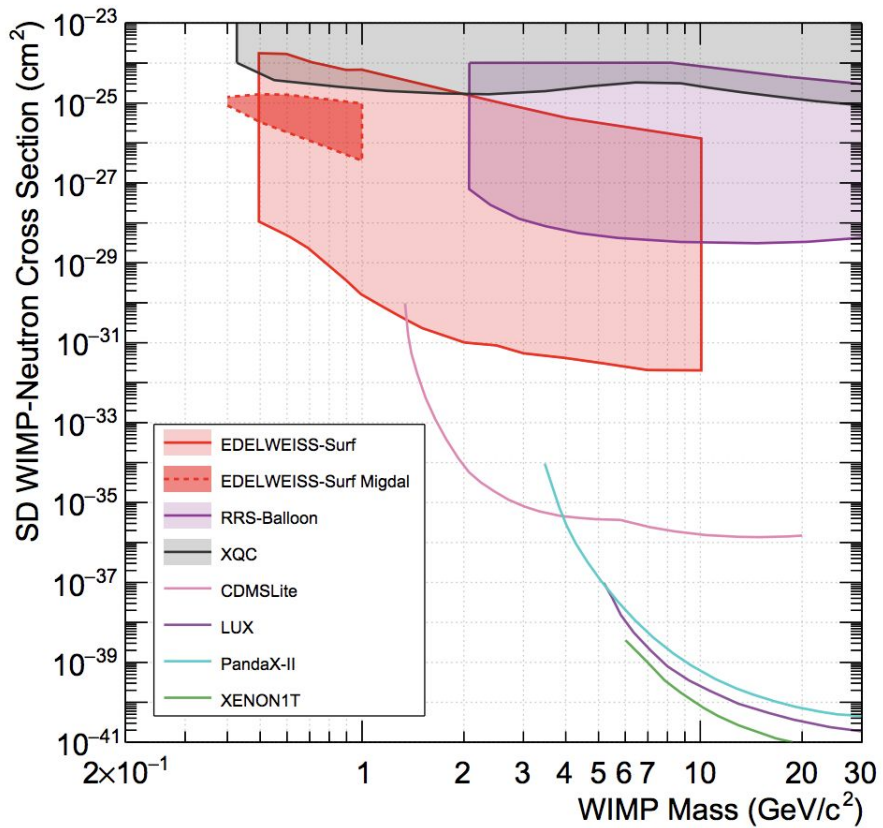
Ionization Probabilities have been calculated: Flexible Atomic Code



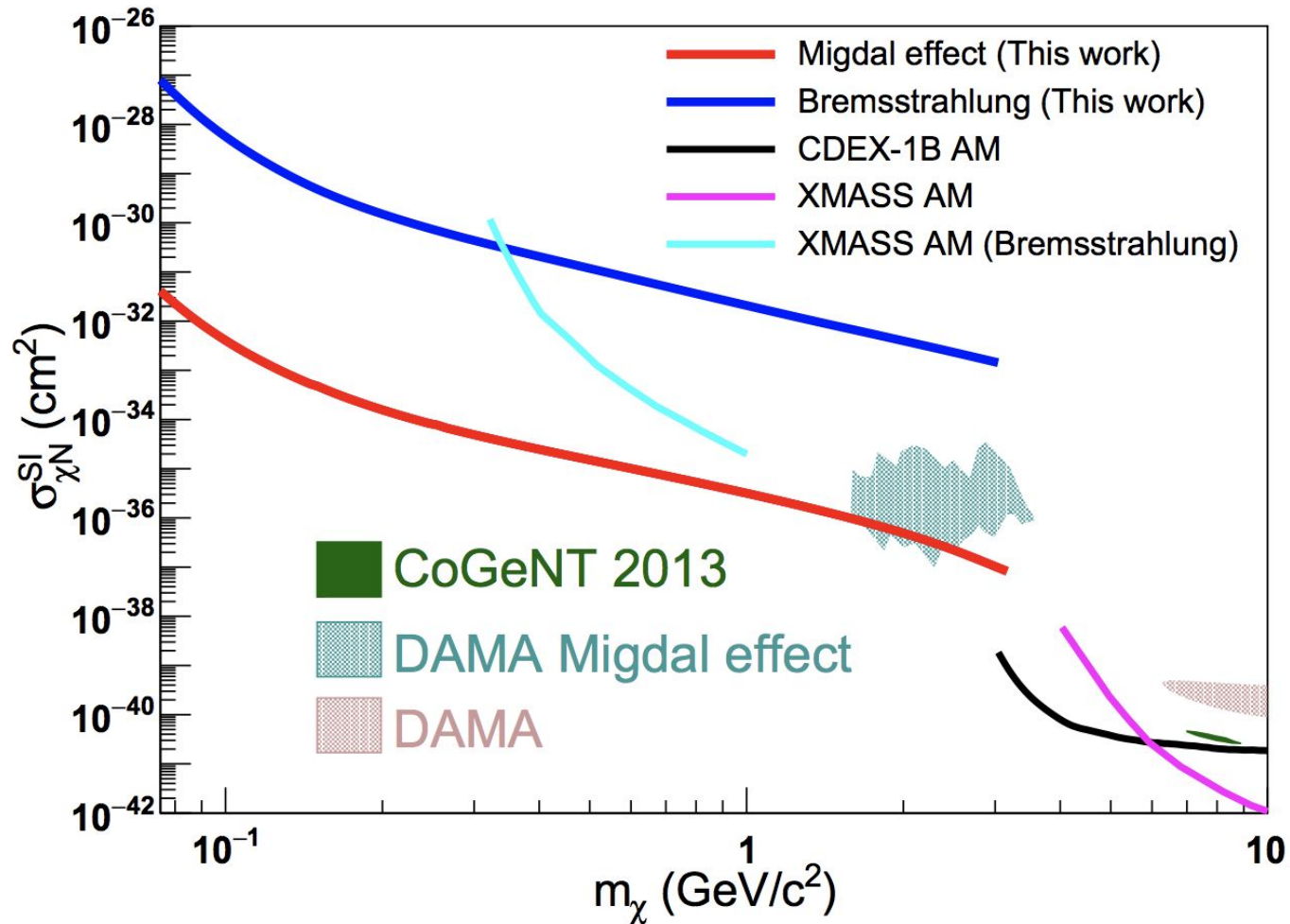


The Migdal effect has been used to place new bounds on sub-GeV dark matter





33.4 g Ge, 60 eV threshold



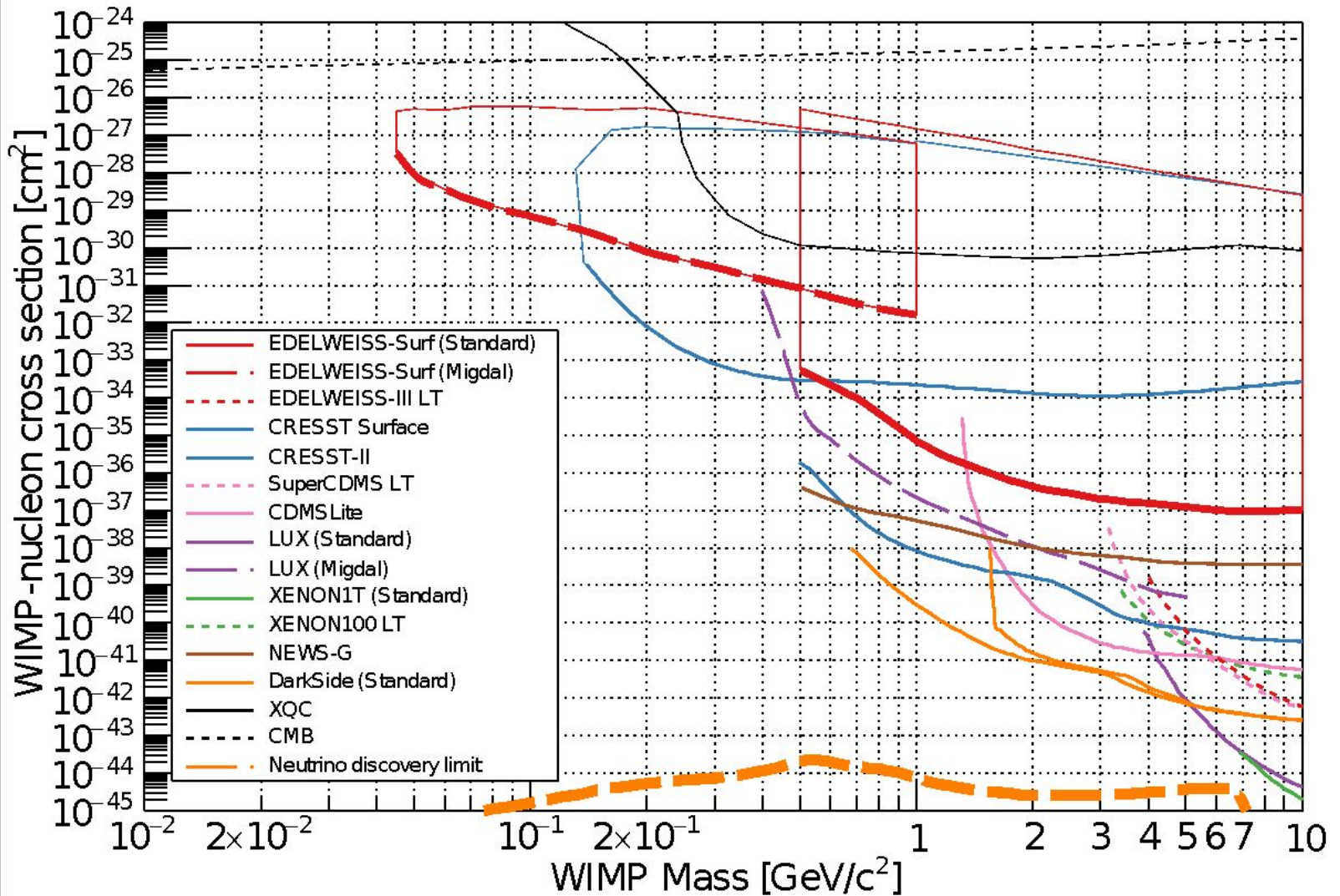
939 g Germanium detector at CJPL
 1107.5 kg·day exposure and 250 eVee
 threshold for annual modulation search

**Constraints on spin-independent nucleus scattering with
 sub-GeV WIMP dark matter from the CDEX-1B Experiment
 at CJPL**

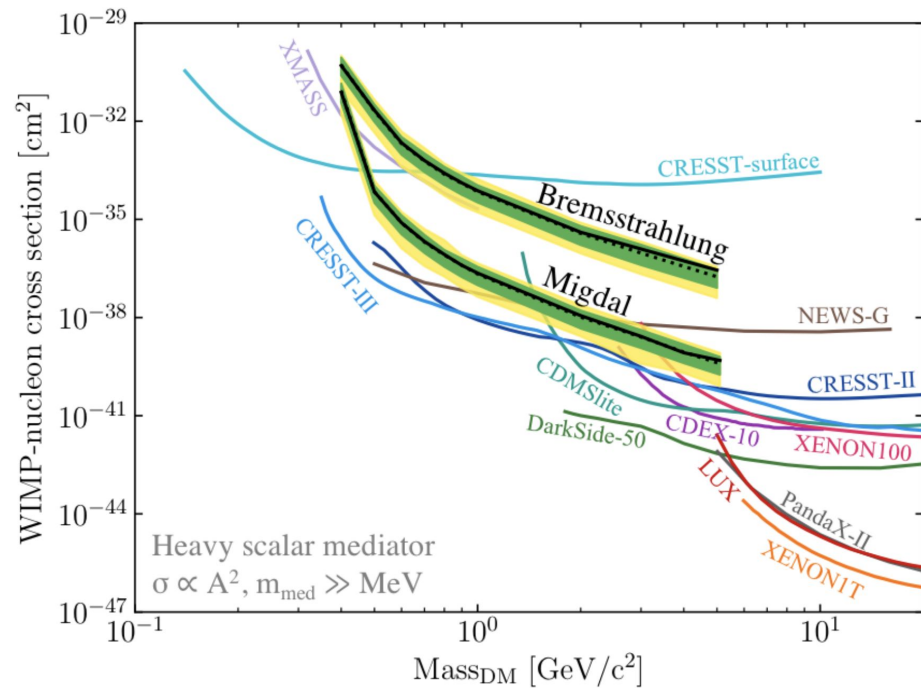
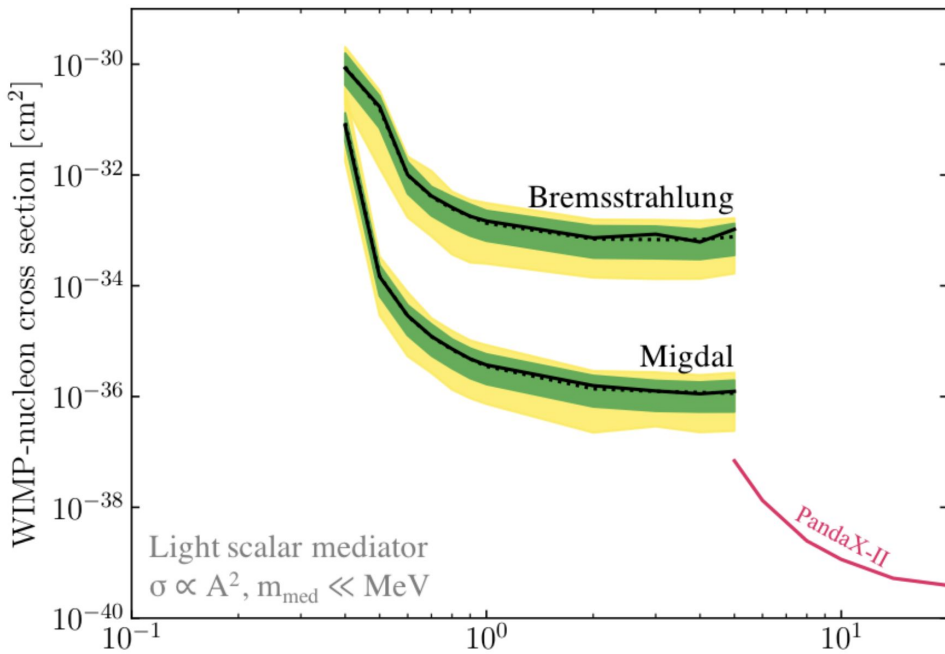
CDEX Collaboration ([Z.Z. Liu](#) (Tsinghua U., Beijing) *et al.*). May

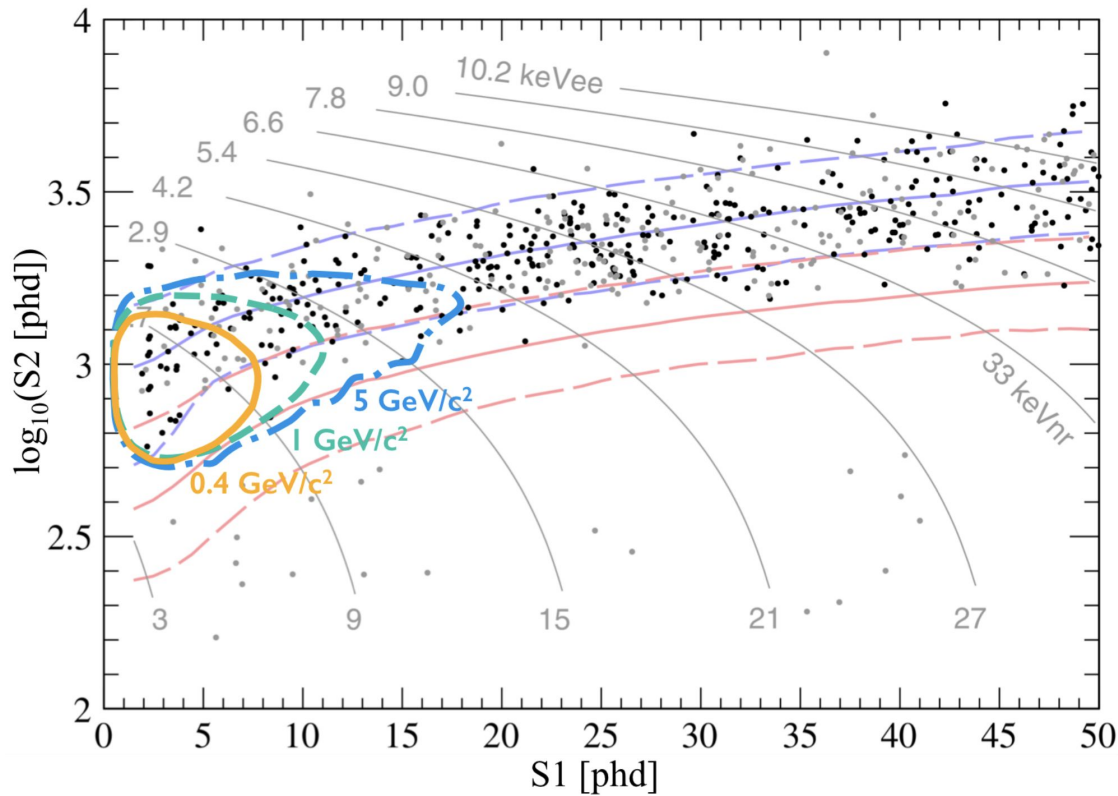
1, 2019. 5 pp.

e-Print: [arXiv:1905.00354](https://arxiv.org/abs/1905.00354) [hep-ex]

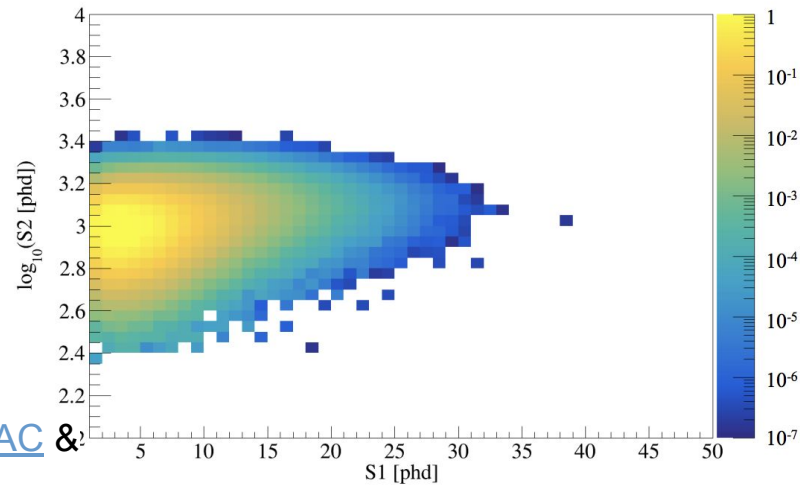


33.4 g Ge, 60 eV threshold





$$E = W (n_\gamma + n_e) = W \left(\frac{S1}{g_1} + \frac{S2}{g_2} \right)$$



LUX Collaboration ([D.S. Akerib](#) (Case Western Reserve U. & [SLAC](#) & [KIPAC, Menlo Park](#)) *et al.*). Nov 27, 2018. 7 pp.

Published in **Phys.Rev.Lett.** **122** (2019) no.13, 131301

Direct Detection Review

Momentum Exchanged $O(<100\text{MeV})$

$$q = \sqrt{2m_T E_R}$$

Recoil energy $O(10\text{keV})$

$$E_R = \frac{\mu_{\chi T}^2 v^2}{m_T} (1 - \cos \theta)$$

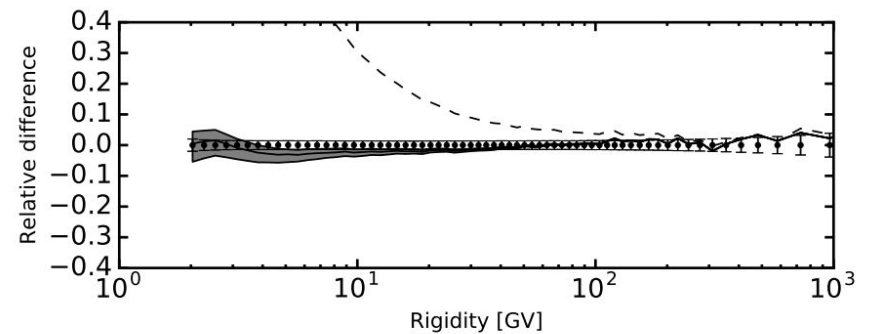
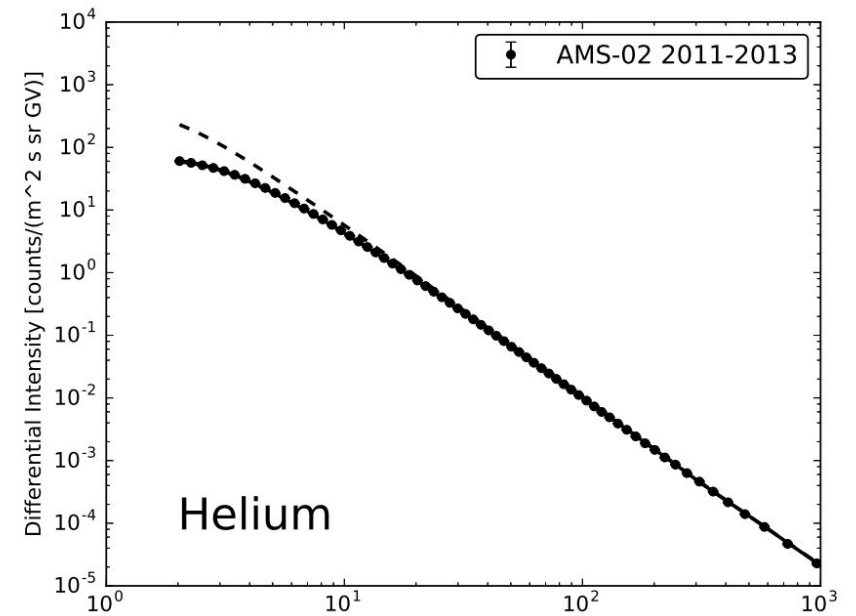
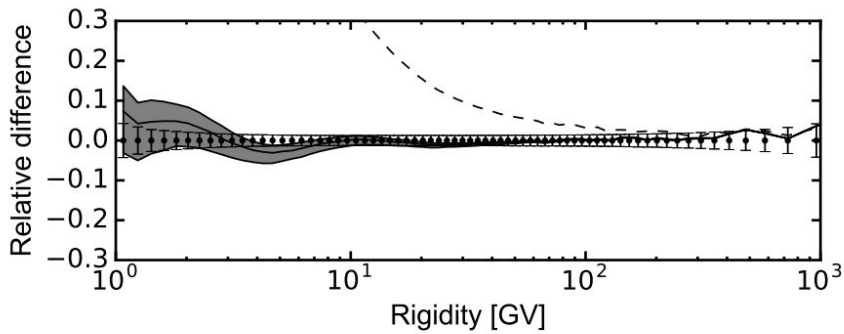
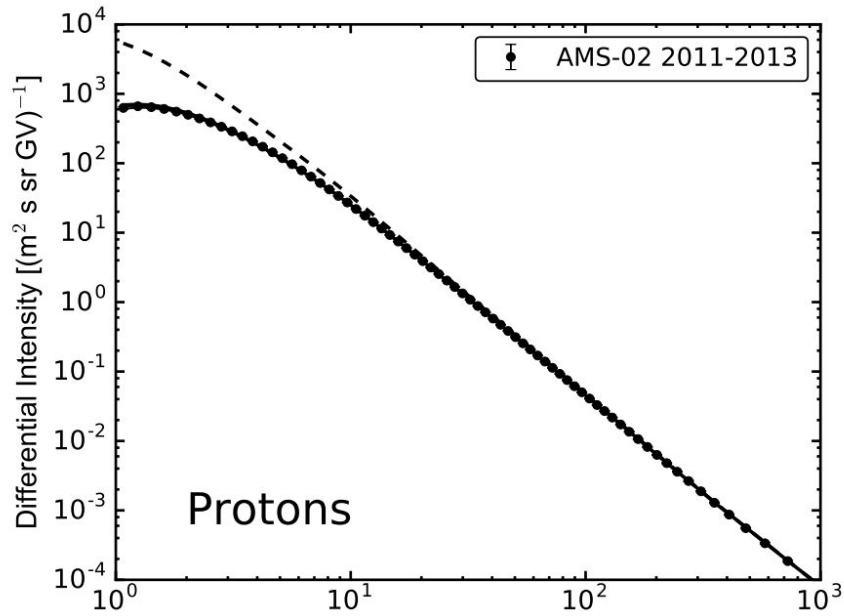
Incident energy

$$E_i = \frac{m_\chi v^2}{2}$$

$$v \sim \mathcal{O}(10^{-3})$$

$$E_{R,\text{max}} = \frac{2\mu_{\chi T}^2 v^2}{m_T}$$

$$\frac{dR}{dE_R} = N_T \frac{\rho_{\chi, \odot}}{m_\chi m_T} \int_{v > v_{\text{min}}} \frac{d\sigma}{dE_R} v f(\vec{v}) d^3 v$$



From Observations near the Earth to the Local Interstellar Spectra

[S. Della Torre](#) ([INFN, Milan Bicocca](#)) *et al.*. Dec 29, 2016.

Conference: [C16-09-04.3](#)