

Jet substructure and a possible determination of the QCD coupling

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Trento, 02/13/18



Jets at the LHC

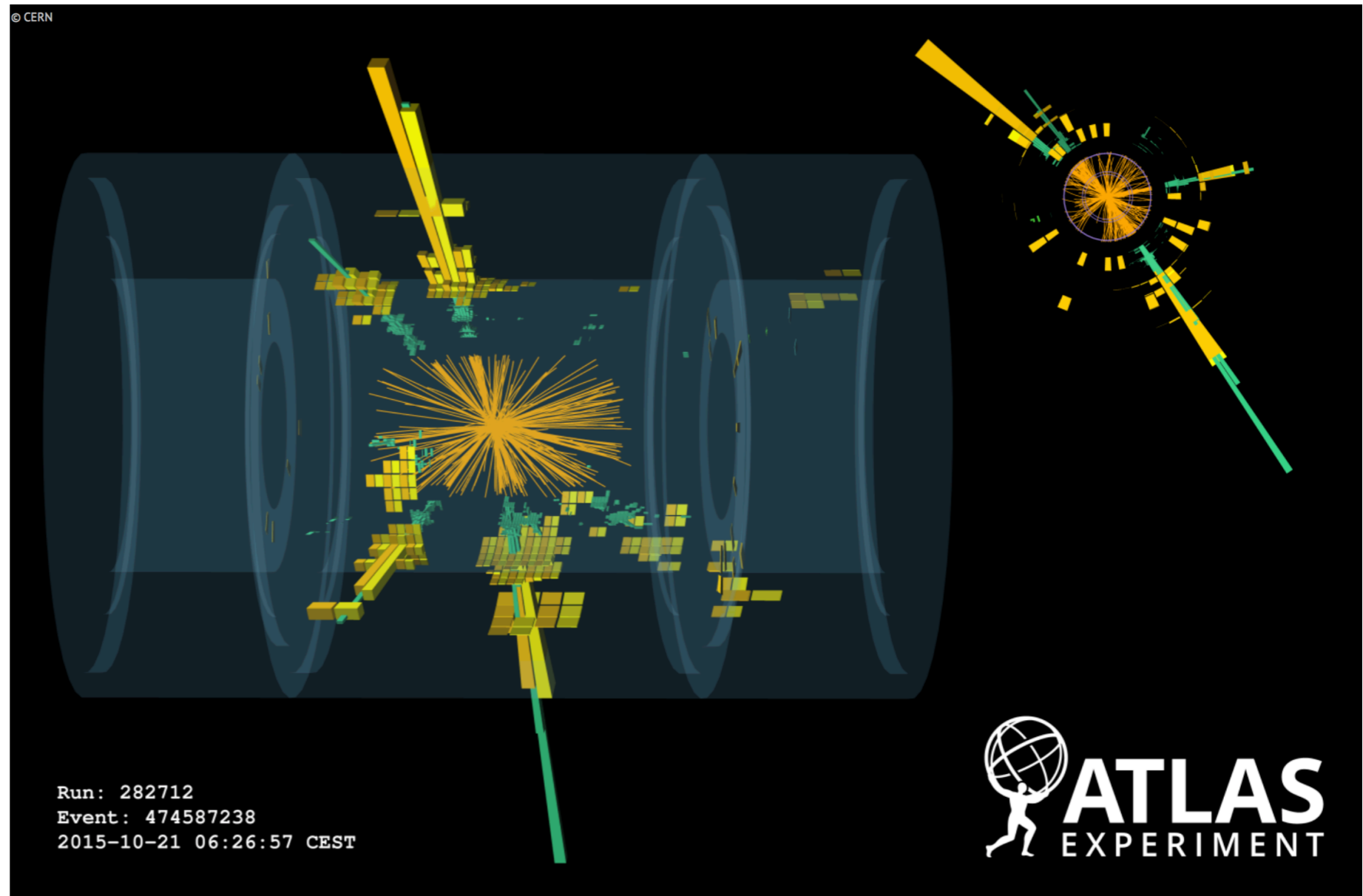
- Inclusive jet production

$$\longrightarrow \frac{d\sigma^{pp \rightarrow \text{jet} + X}}{dp_T d\eta}$$

see talk by Joao Pires

- Measure additional jet substructure

$$\longrightarrow \frac{d\sigma^{pp \rightarrow (\text{jet } \tau) X}}{dp_T d\eta d\tau}$$



Jet substructure

- Design observables to tag boosted objects

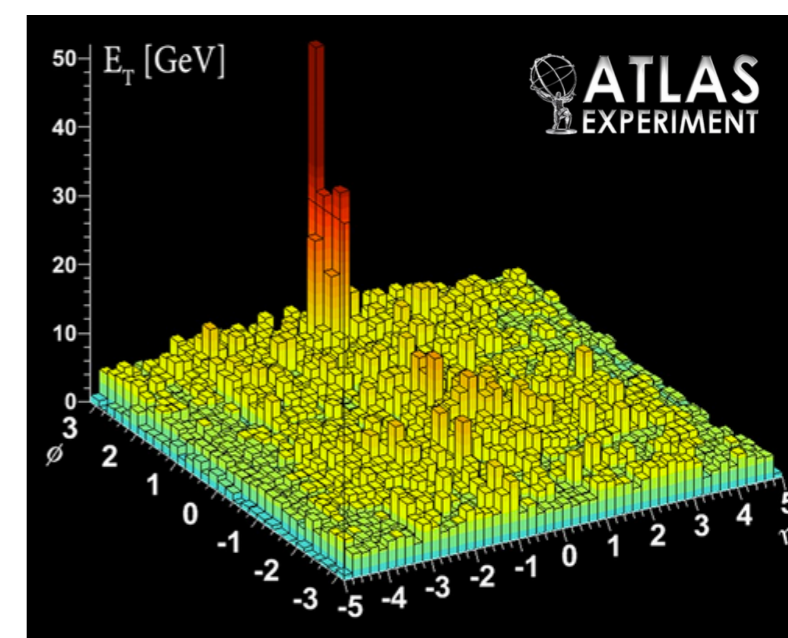
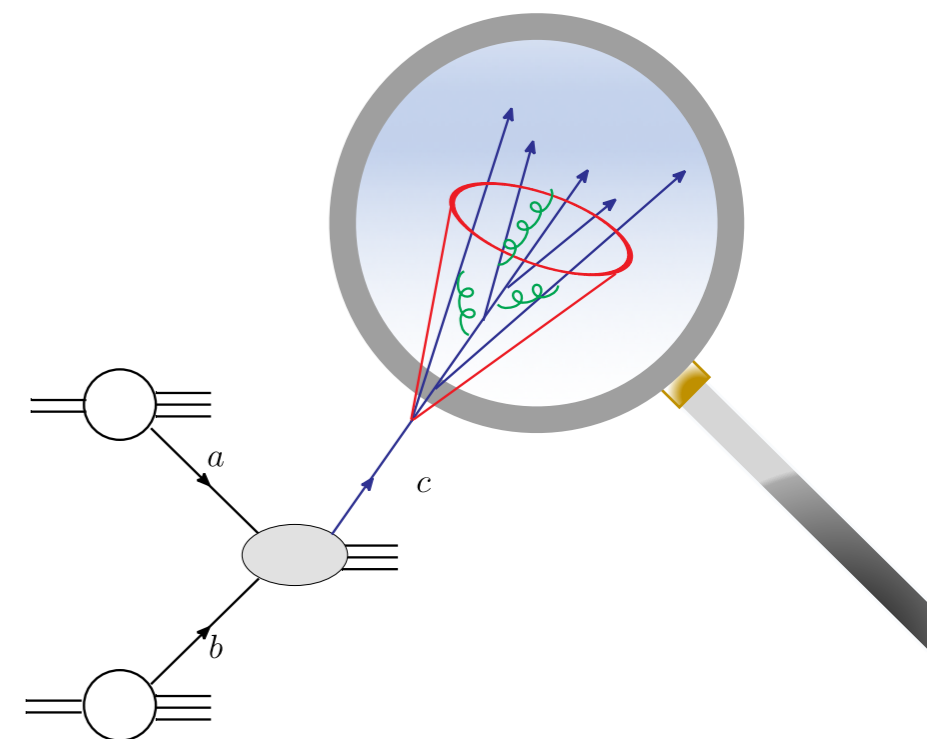
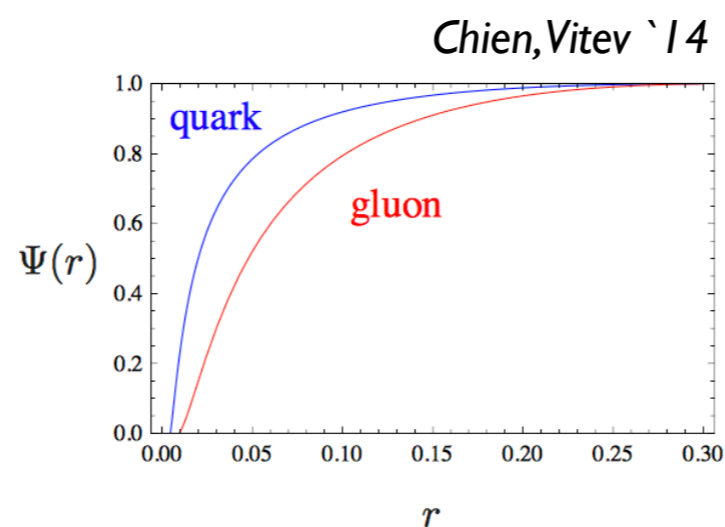
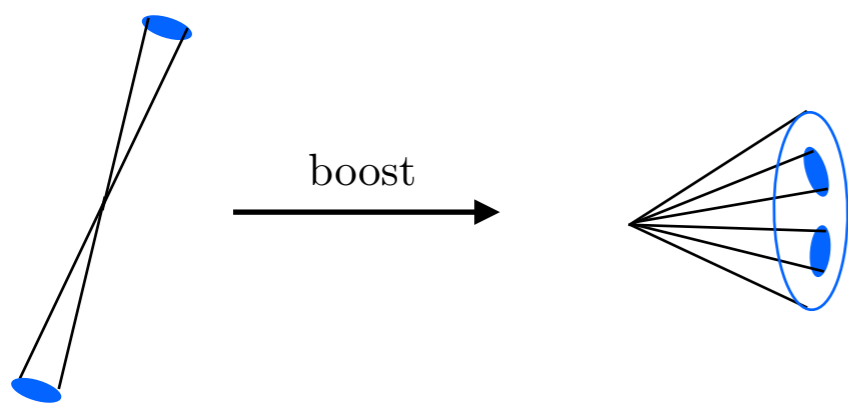
Butterworth, Davison, Rubin, Salam '08

- Quark/gluon discrimination

- Search for BSM physics

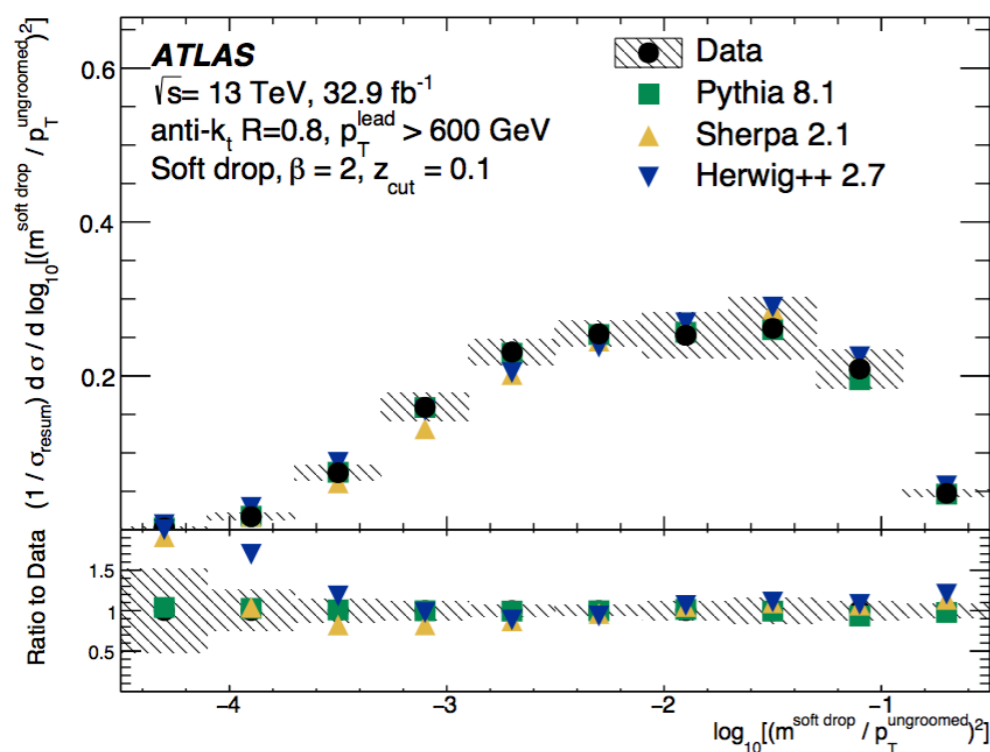
- Probe in heavy-ion collisions

- Precision QCD studies ...

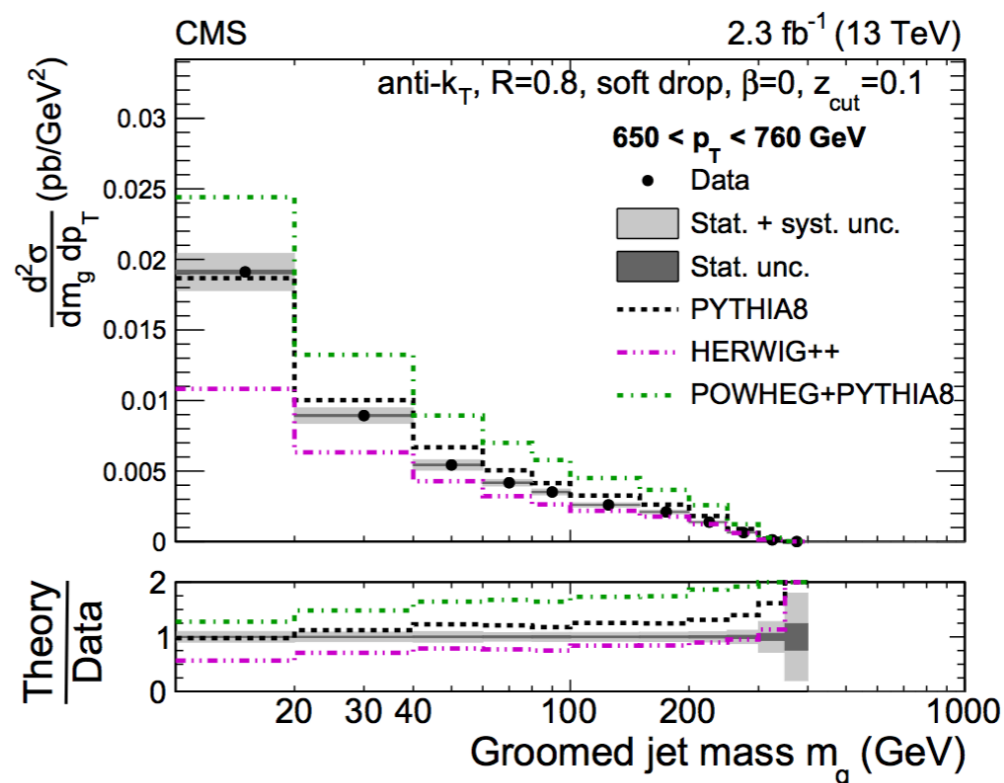


Jet substructure as a tool for precision QCD studies

- The soft drop groomed jet mass



ATLAS, PRL 121 (2018) 092001



CMS, JHEP 1811 (2018) 113

- Extraction of the QCD strong coupling constant

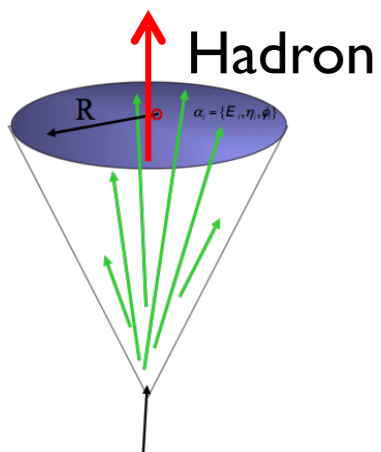
Les Houches '17

- Three theory calculations for the LHC *Frye, Larkoski, Schwartz, Yan '16, Marzani, Schunk, Soyez '17*
Kang, Lee, Liu, FR '18

- e^+e^- *Baron, Marzani, Theeuwes '18, Kardos, Somogyi, Trocsanyi '18* → See talk by Gabor Somogyi's talk

Jet substructure as a tool for precision QCD studies

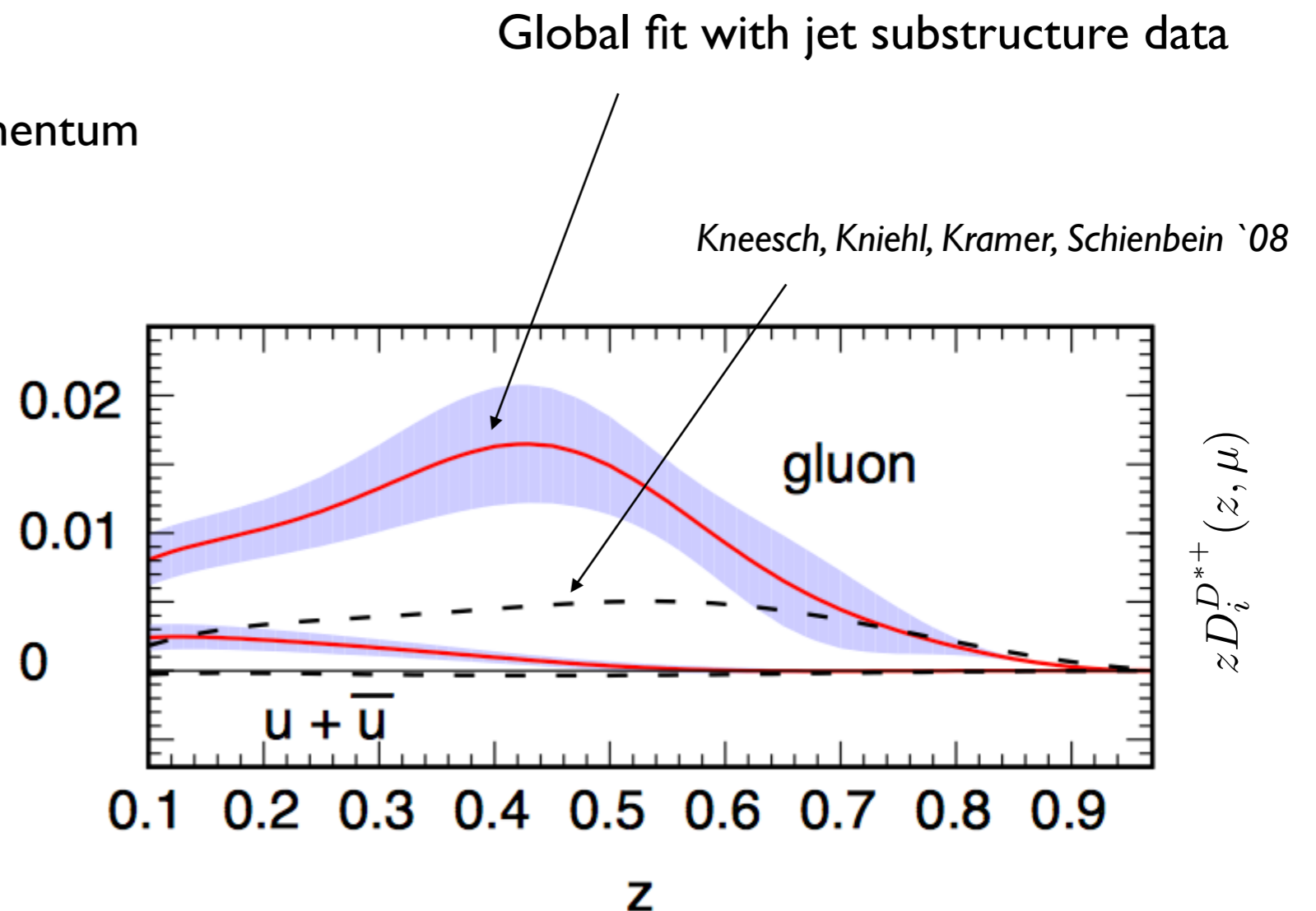
- Extraction of the QCD strong coupling constant
Les Houches '17
- Fragmentation functions *Anderle, Kaufmann, FR, Stratmann, Vitev '16*



$$z = p_T^h / p_T$$

longitudinal momentum structure

- Transverse structure TMDFFs



Jet substructure as a tool for precision QCD studies

- Extraction of the QCD strong coupling constant

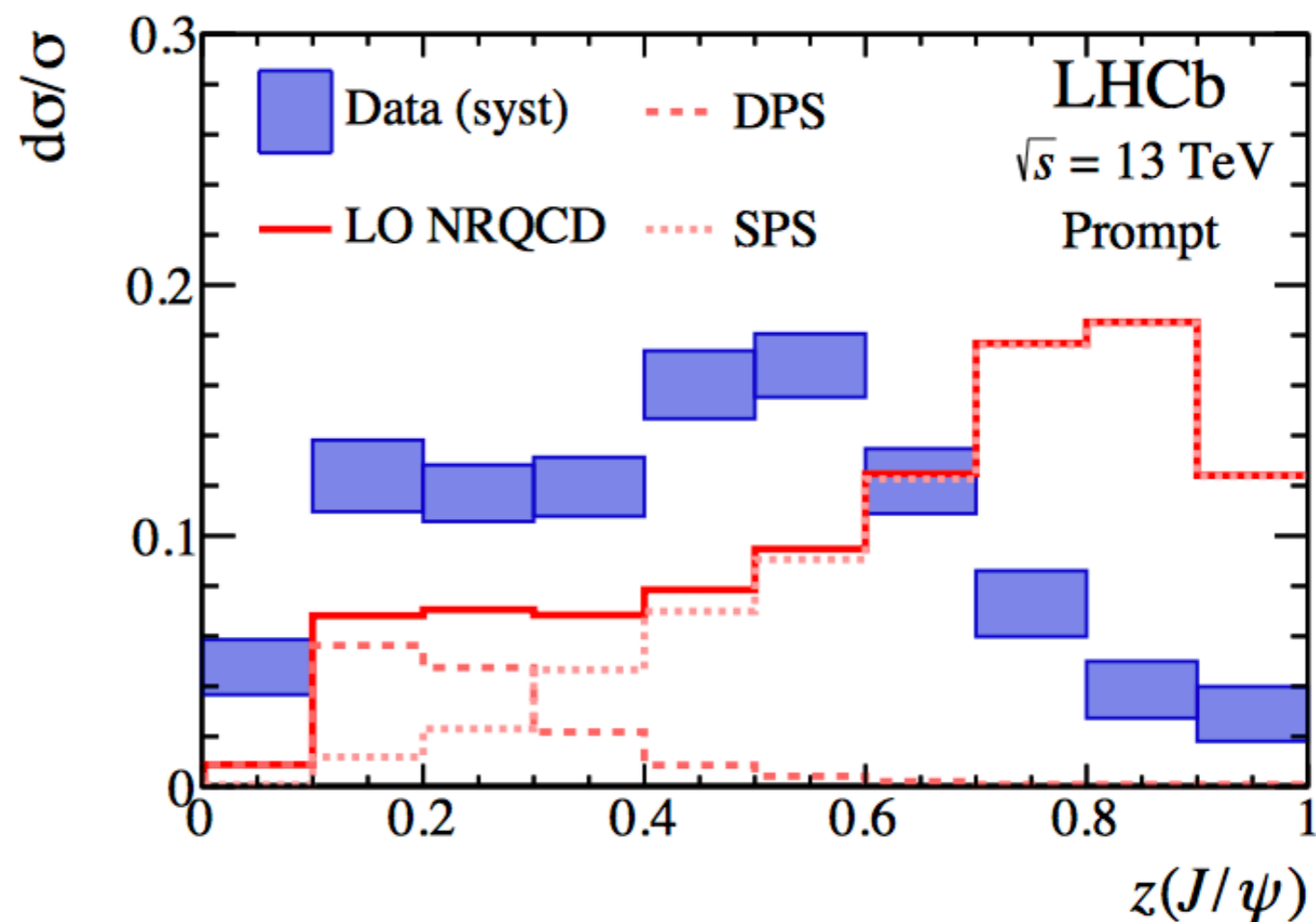
Les Houches '17

- Fragmentation functions

- Quarkonium

LHCb, PRL 118 (2017) 192001

CMS-PAS-HIN-18-012



Jet substructure as a tool for precision QCD studies

- Extraction of the QCD strong coupling constant

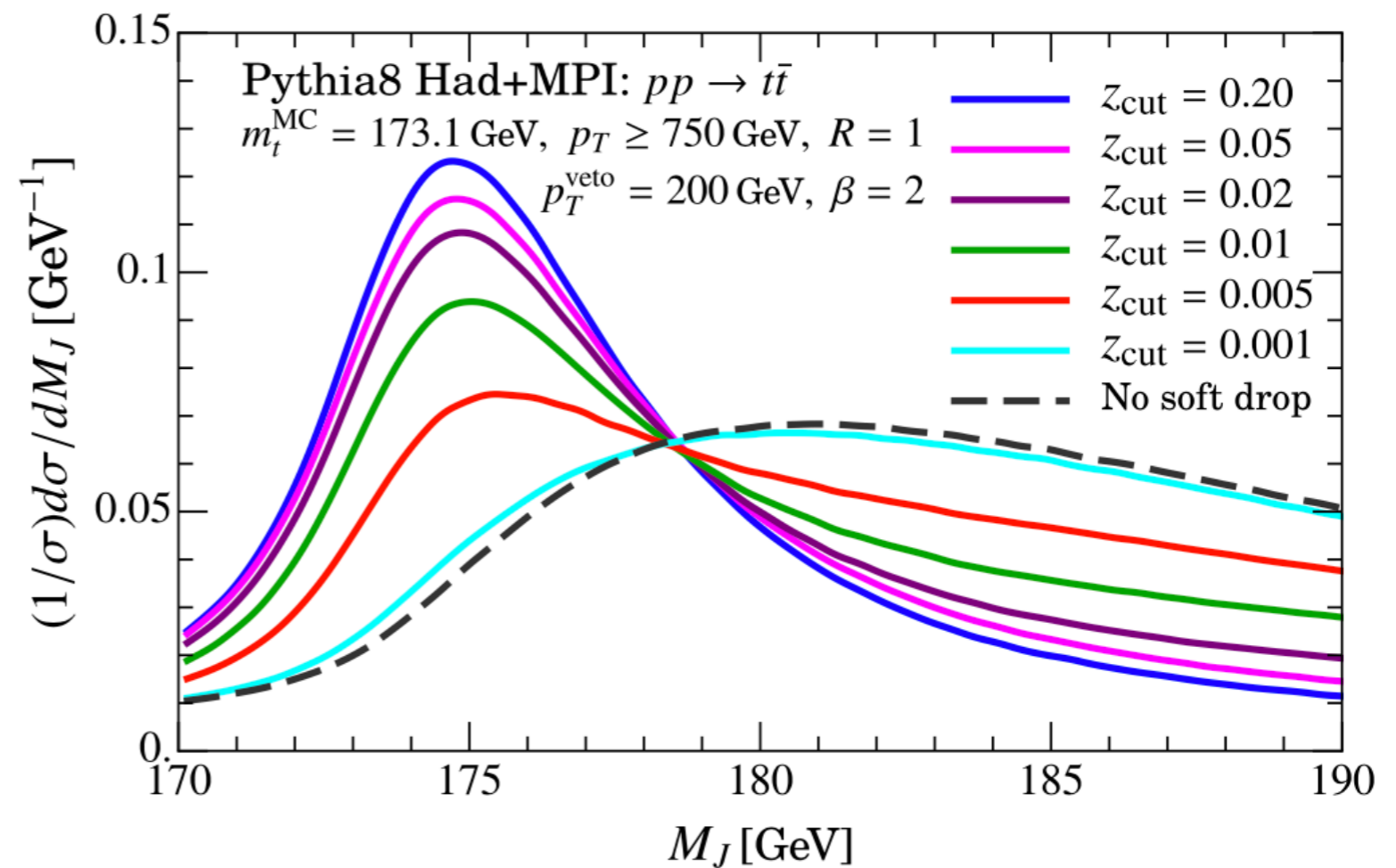
Les Houches '17

- Fragmentation functions

- Quarkonium

- Top quark mass

Hoang, Mantry, Pathak, Stewart '17



Jet substructure as a tool for precision QCD studies

- Extraction of the QCD strong coupling constant

Les Houches '17

- Fragmentation functions

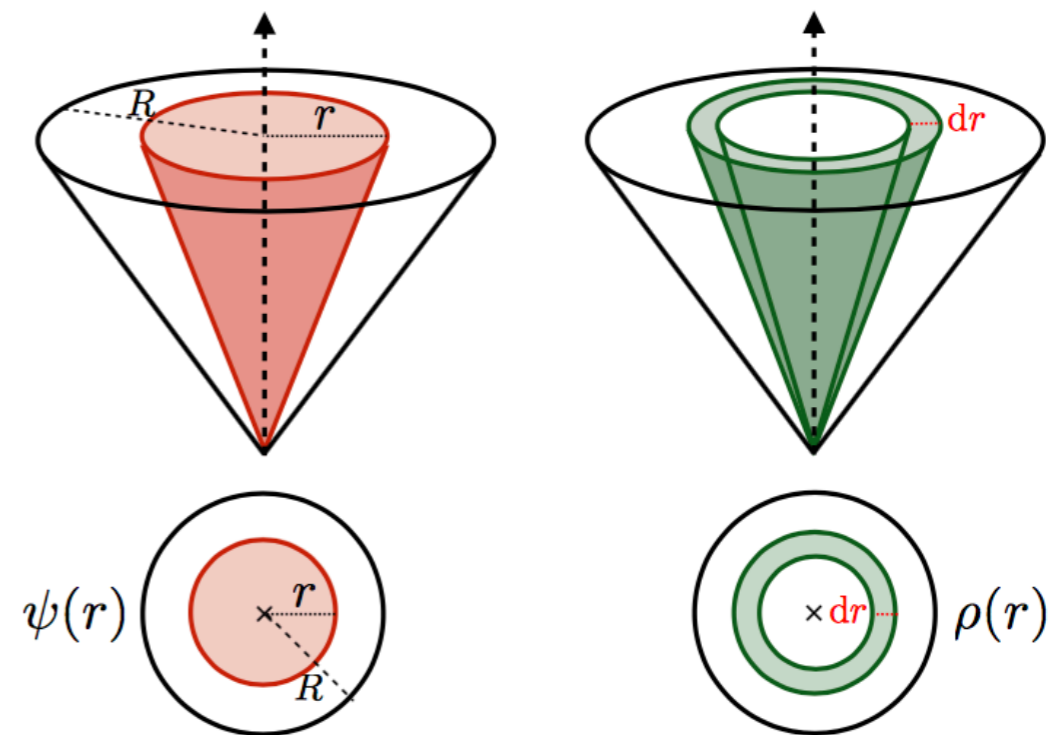
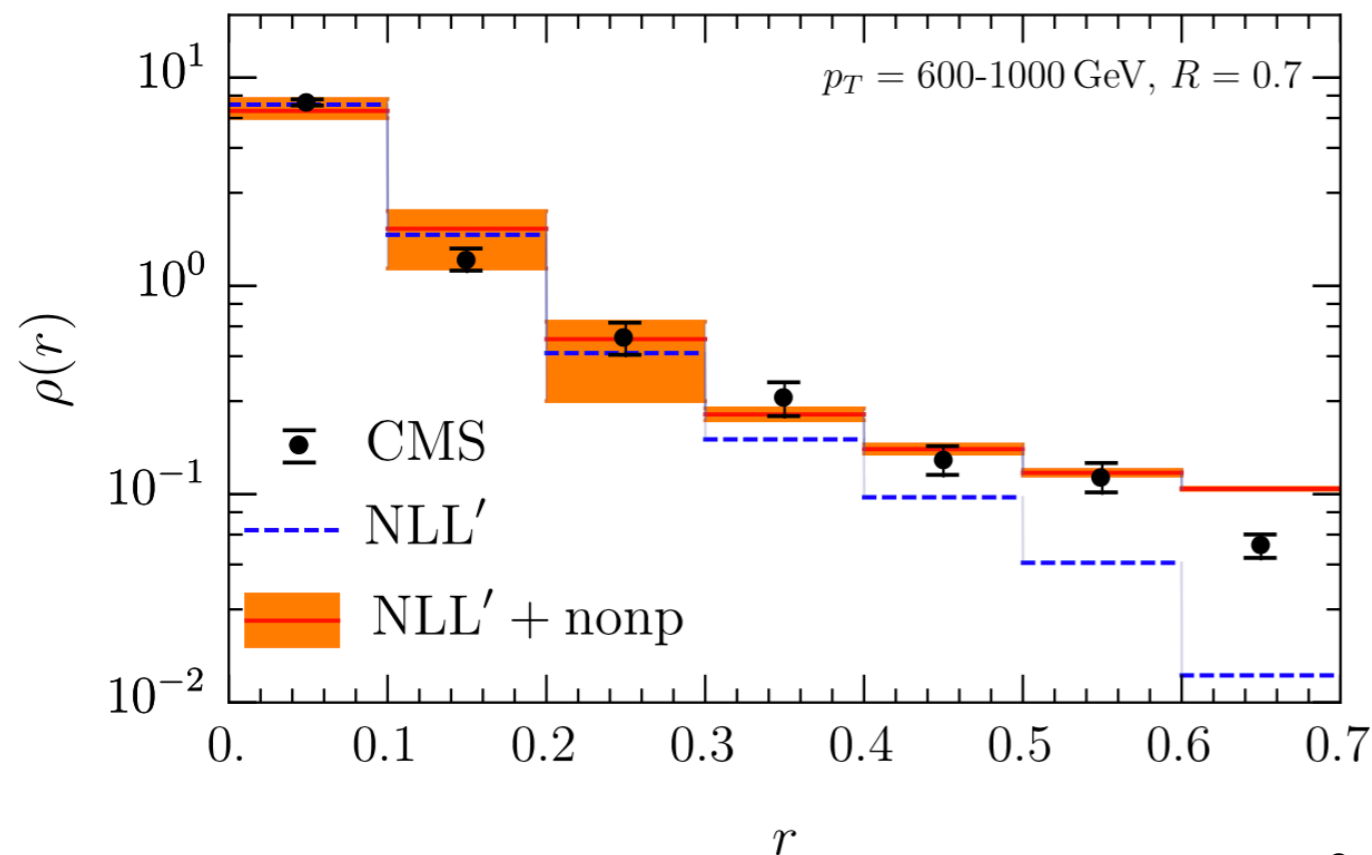
- Quarkonium

- Top quark mass

Hoang, Mantry, Pathak, Stewart '17

- Tuning of MCs, e.g. jet shape at NLL

Cal, FR, Waalewijn '19



ATLAS, PRD 83 (2011) 052003,
CMS, JHEP 06 (2012) 160

Jet substructure as a tool for precision QCD studies

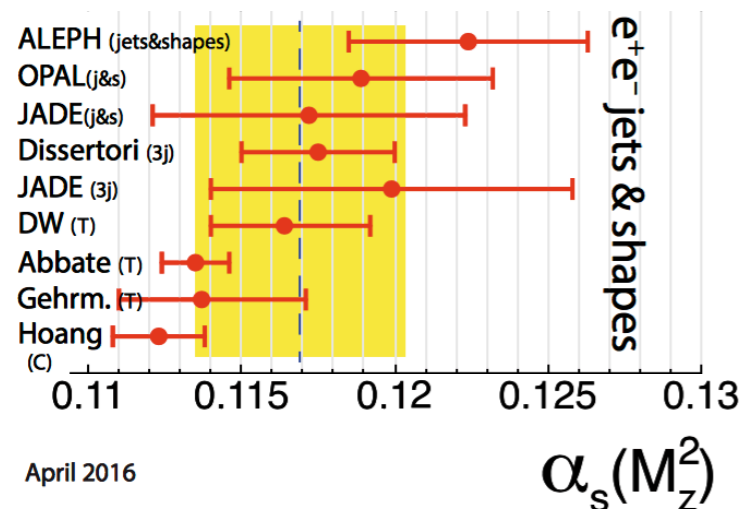
- Extraction of the QCD strong coupling constant

Les Houches '17

- Hadron collider extraction
- Similarity to e^+e^- event shapes

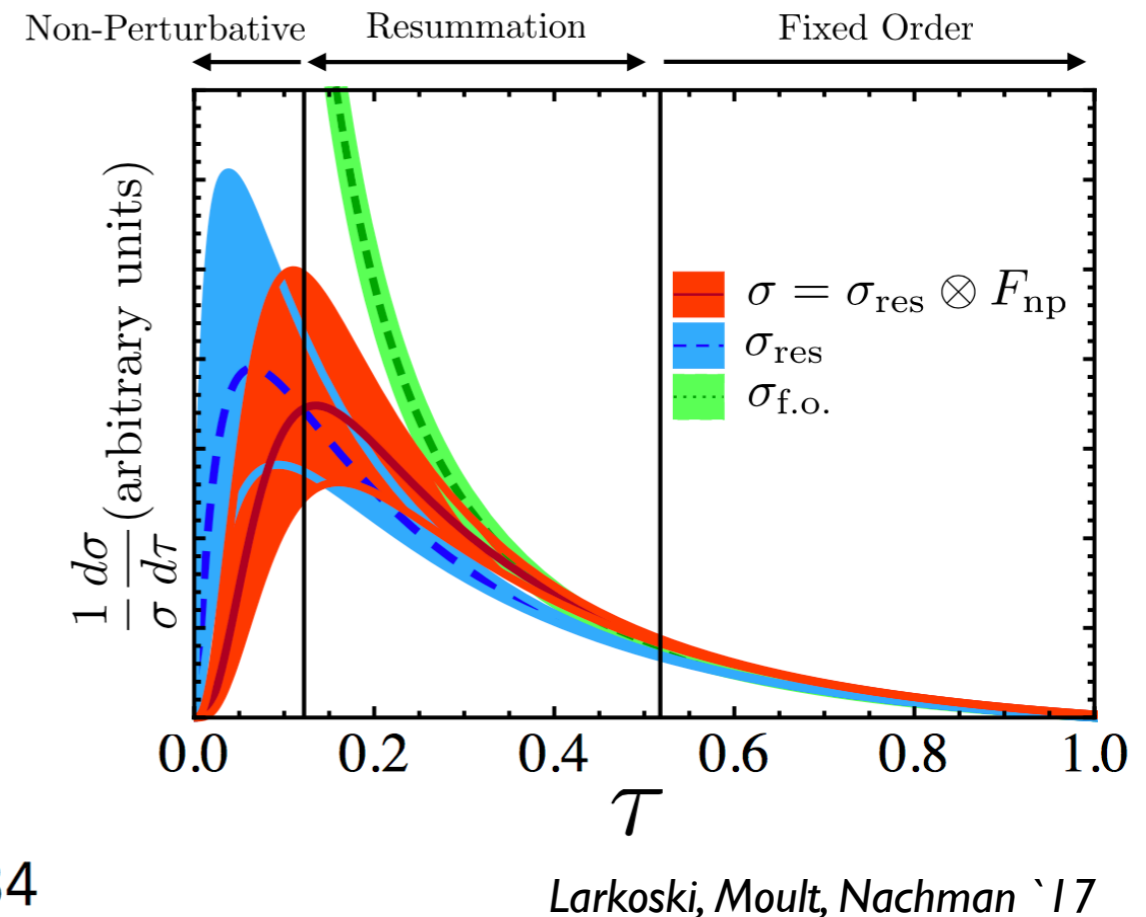
e.g. thrust, C-parameter

Non-perturbative: Shape function vs. MC



- Very challenging for both theory and experiment

Current estimate $\sim 10\%$ *Les Houches '17*




Outline

- Introduction
- Groomed jet substructure observables at the LHC
- Determination of the QCD coupling
- Conclusions

QCD factorization

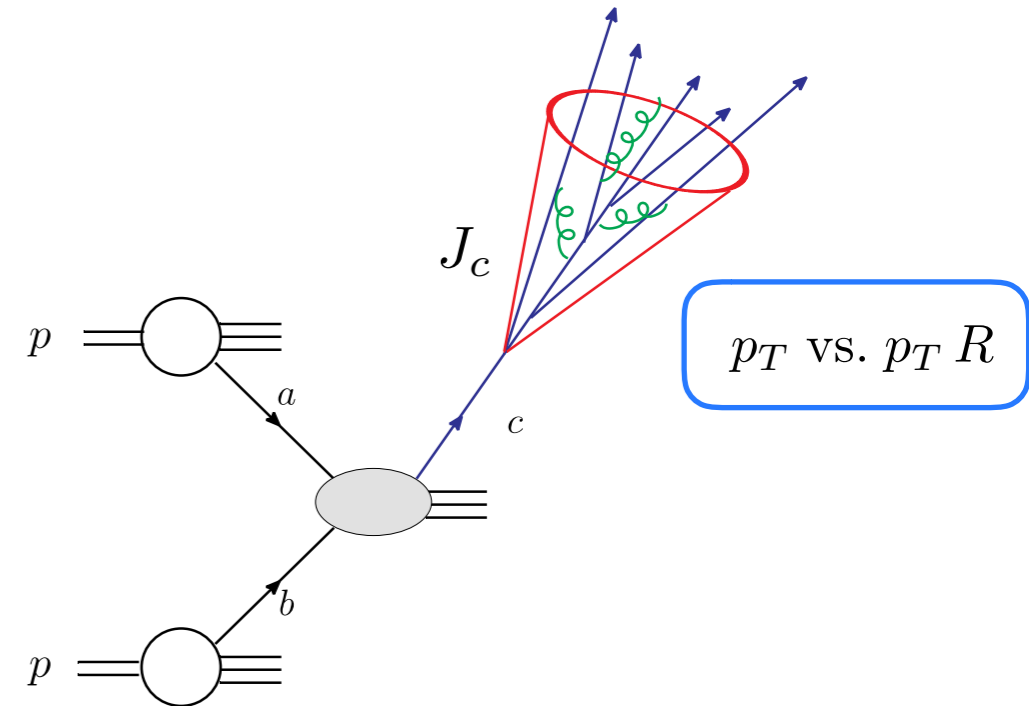
- Inclusive jet production $pp \rightarrow \text{jet} + X$

$$\frac{d\sigma^{pp \rightarrow \text{jet} X}}{dp_T d\eta} = \sum_{a,b,c} f_a \otimes f_b \otimes H_{ab}^c \otimes J_c + \mathcal{O}(R^2)$$

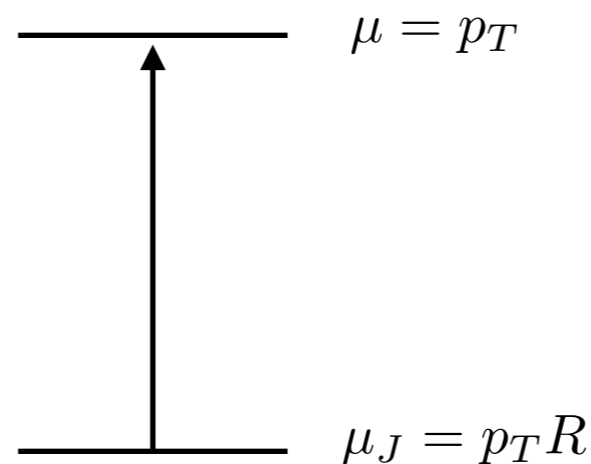


 perturbatively calculable

$$\mu \frac{d}{d\mu} J_i = \sum_j P_{ji} \otimes J_j$$



- Resummation of $\alpha_s^n \ln^n R$
- Scale dependence for small R



Dasgupta, Dreyer, Salam, Soyez `15
 Kaufmann, Mukherjee, Vogelsang `15
 Kang, FR, Vitev `16
 Dai, Kim, Leibovich `16
 Liu, Moch, FR `18

QCD factorization

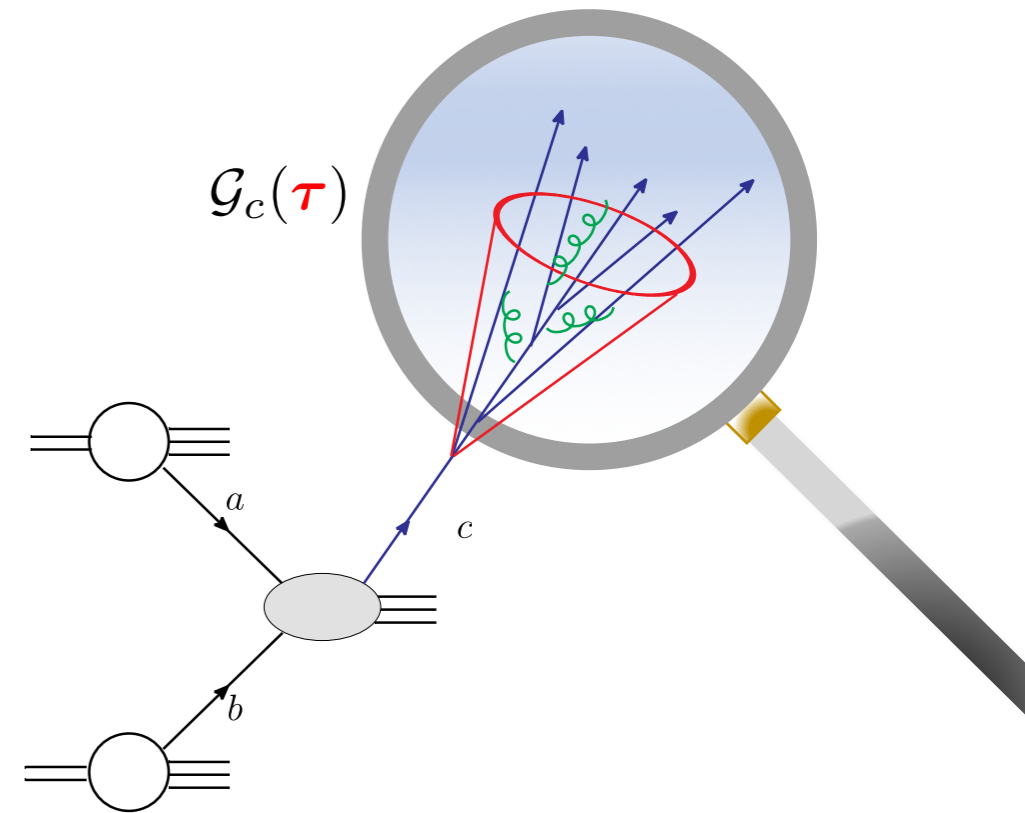
- Inclusive jet production $pp \rightarrow \text{jet} + X$

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- Jet substructure τ

$$\frac{d\sigma^{pp \rightarrow (\text{jet } \tau) X}}{dp_T d\eta d\tau} = \sum_{abc} f_a \otimes f_b \otimes H_{ab}^c \otimes \mathcal{G}_c(\tau) + \mathcal{O}(R^2)$$

- In R resummation
- Definition of quark-gluon fractions beyond LO
- Mostly analytical calculations

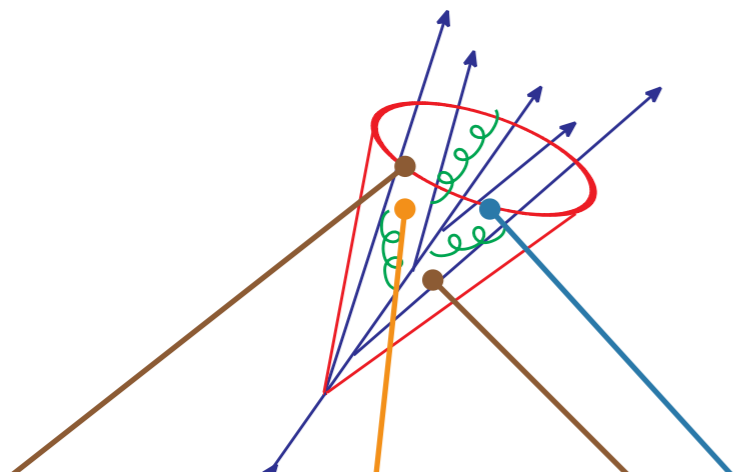
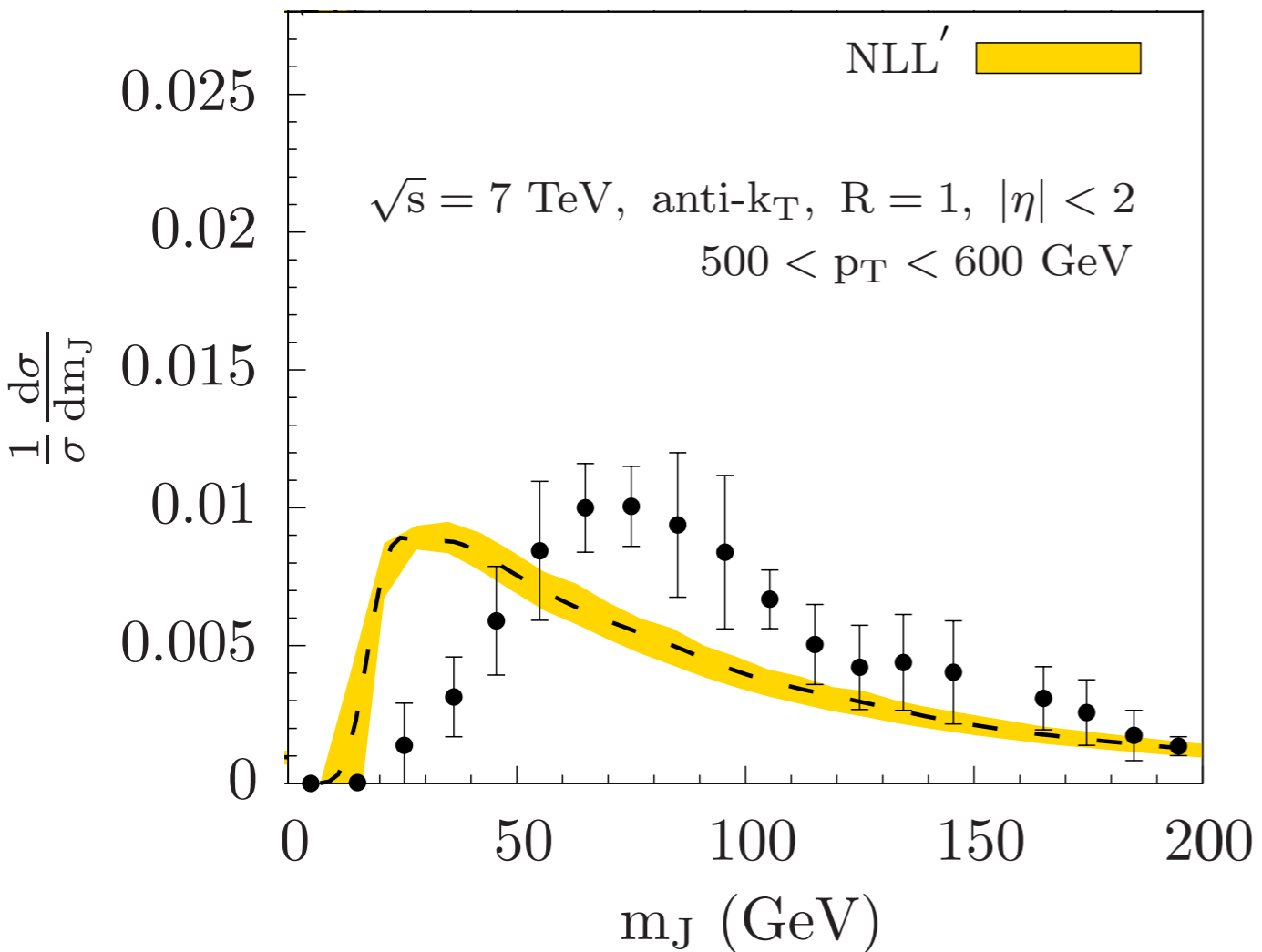


Dasgupta, Dreyer, Salam, Soyez `15
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Jet mass distributions

Kang, Lee, Liu, FR '18

ATLAS, JHEP 05 (2012) 128



$pp \rightarrow \text{jet} + X$
Soft sensitivity

● Hadronization

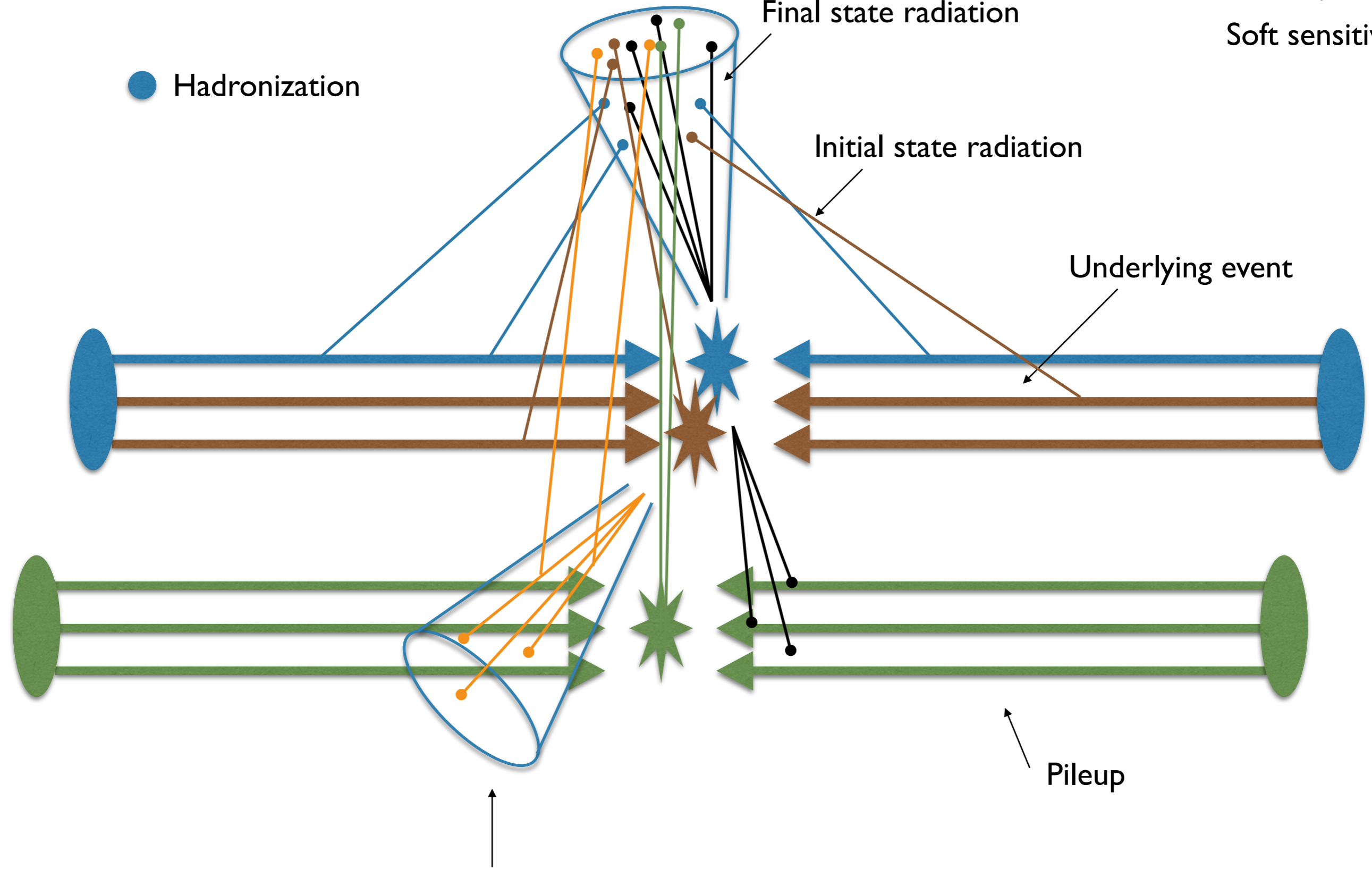
Final state radiation

Initial state radiation

Underlying event

Pileup

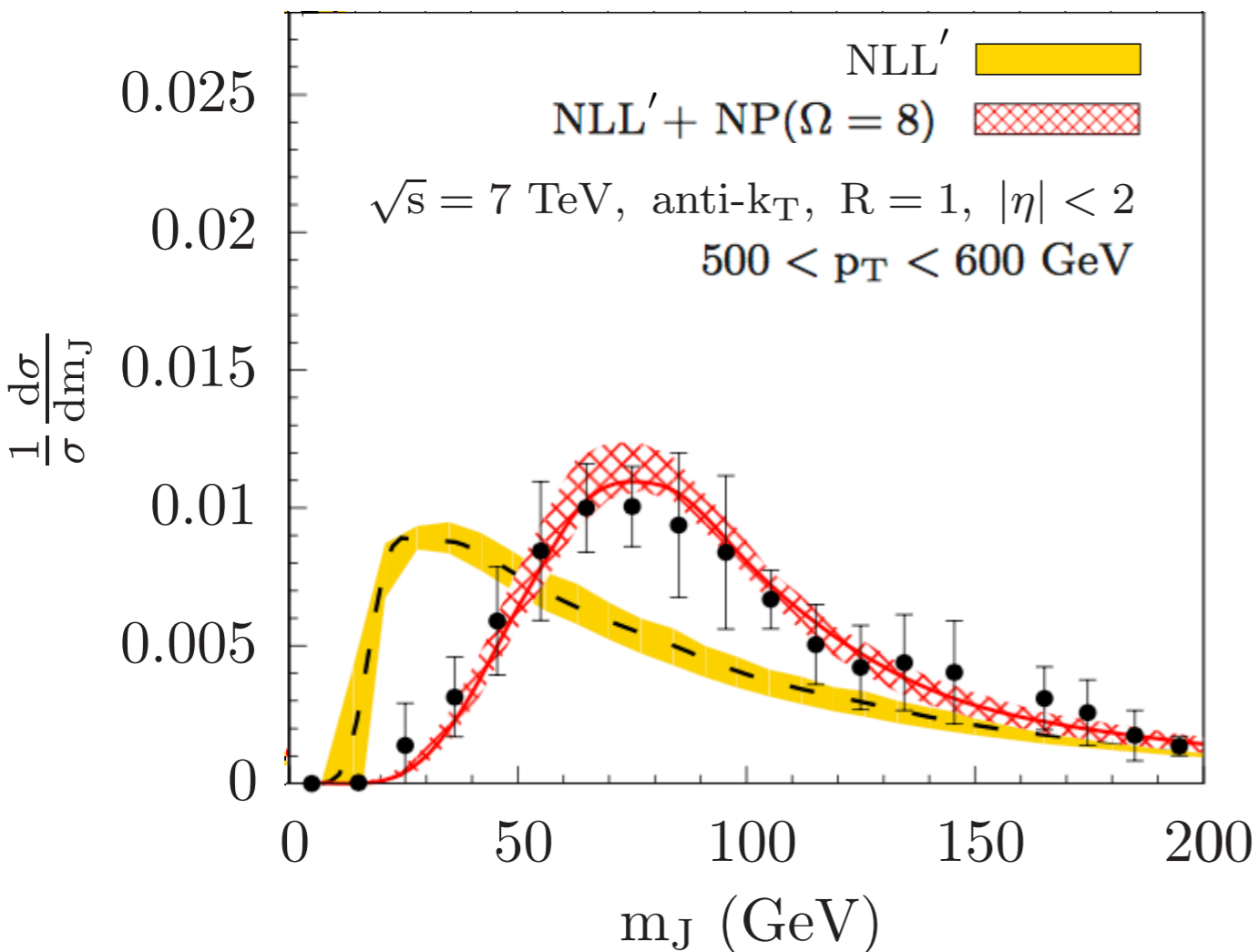
Additional jets, non-global structure



Jet mass distributions

Kang, Lee, Liu, FR '18

ATLAS, JHEP 05 (2012) 128



Capture hadronization and MPI using a shape function

$$F_i(k) = \frac{4k}{\Omega^2} \exp(-2k/\Omega)$$

$$\int_0^\infty dk k F_i(k) = \Omega \quad \text{and normalized}$$

$$d\sigma = d\sigma^{\text{pert}} \otimes F$$

For quarks there is a relation to thrust for $R \rightarrow 0$ in terms of the energy flow operator

Lee, Sterman '07

Dasgupta, Magnea, Salam '08

Stewart, Tackmann, Waalewijn '15

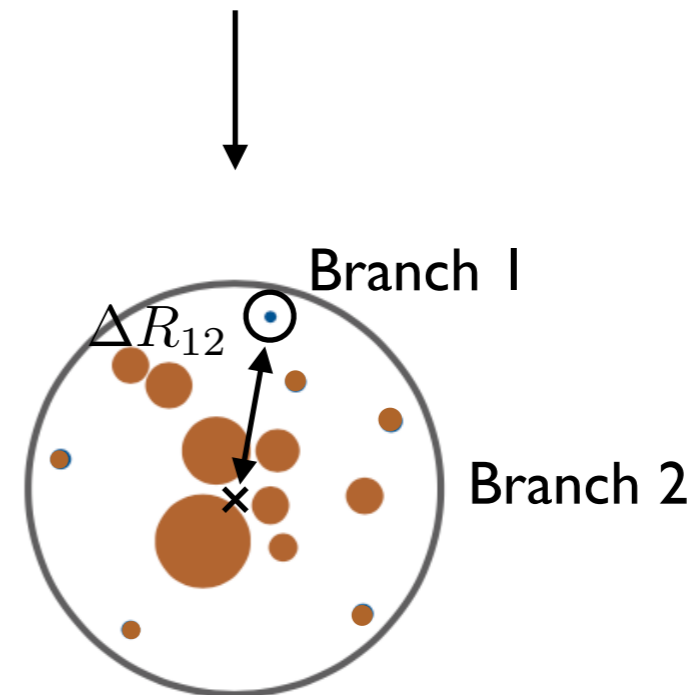
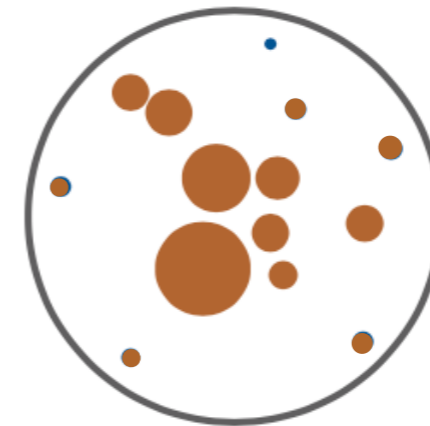
Kang, Lee, Stewart '15

Soft drop grooming

Dasgupta, Fregoso, Marzani, Salam '13
Larkoski, Marzani, Soyez, Thaler '14

- Recluster jet constituents with the C/A algorithm
- Recursively decluster the jet and remove soft branches that fail the soft drop criterion

$$\frac{\min[p_{T1}, p_{T2}]}{p_{T1} + p_{T2}} > z_{\text{cut}} \left(\frac{\Delta R_{12}}{R} \right)^\beta$$



Geometric distance $\Delta R_{12}^2 = \Delta\eta^2 + \Delta\phi^2$

Soft threshold z_{cut}

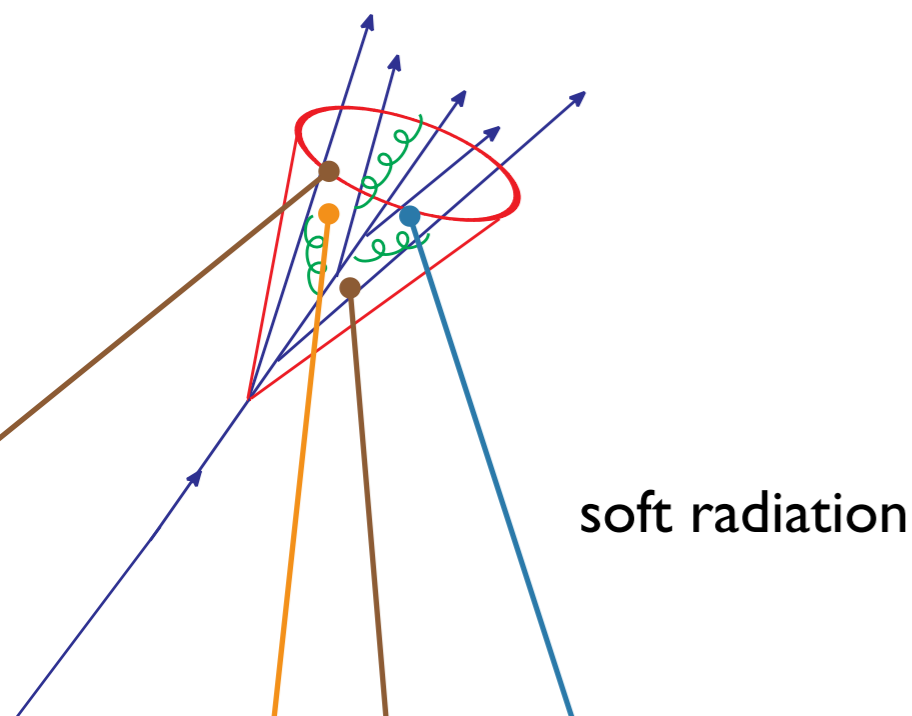
Angular exponent β

- Non-global logarithms largely removed $\beta = 0$
or power suppressed $\beta > 0$
- See also e.g. trimming, pruning
Krohn, Thaler, Wang '10, Ellis, Vermilion, Walsh '10

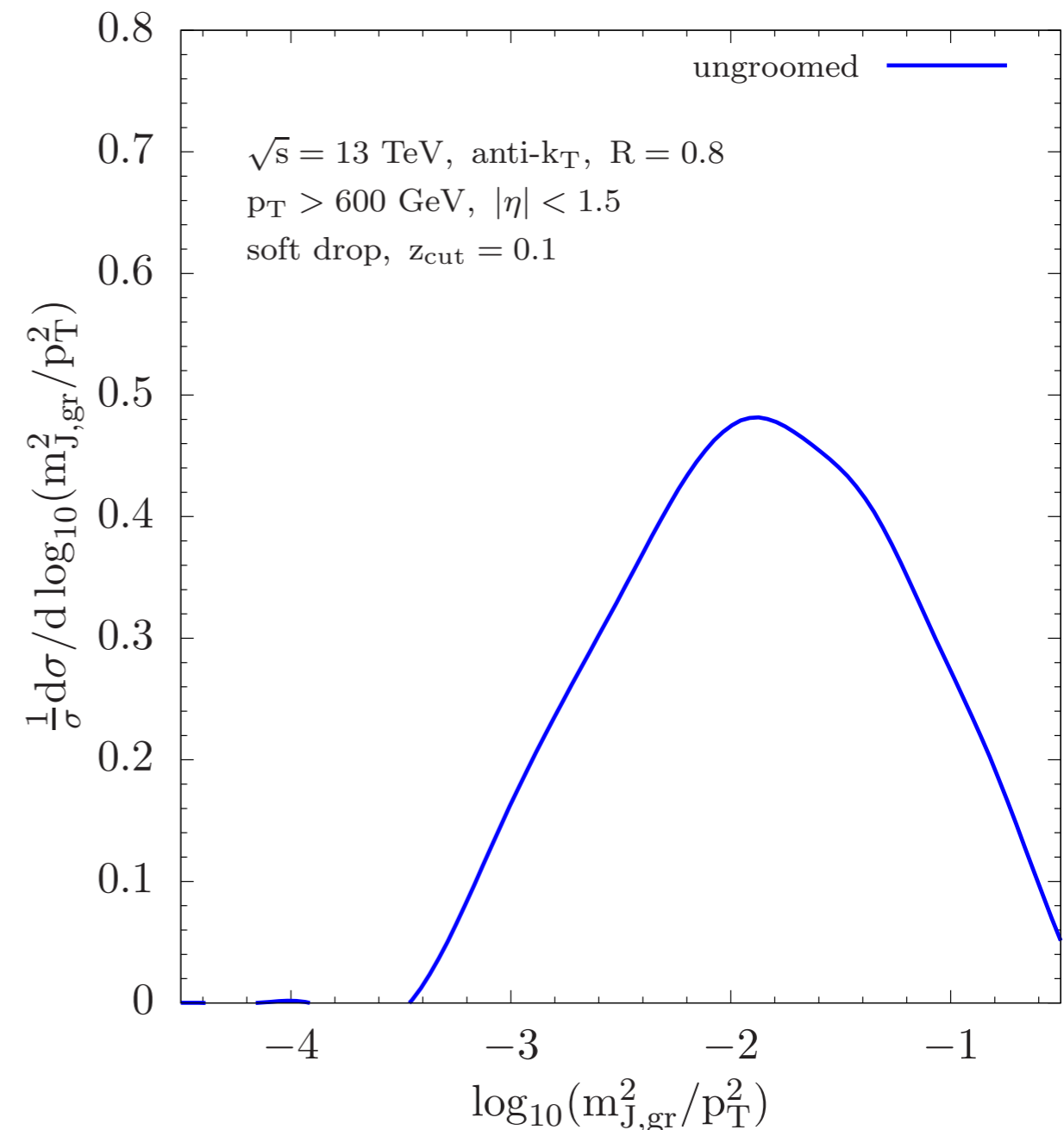
The soft drop groomed jet mass

- Jet mass $m_J^2 = \left(\sum_{i \in J} p_i \right)^2$
- Reduced sensitivity to UE, NP, ISR ...
Larkoski, Marzani, Soyez, Thaler '14
- Resummation of logarithms in $m_J/p_T, R, z_{\text{cut}}$

$$\frac{\min[p_{T1}, p_{T2}]}{p_{T1} + p_{T2}} > z_{\text{cut}} \left(\frac{\Delta R_{12}}{R} \right)^\beta$$



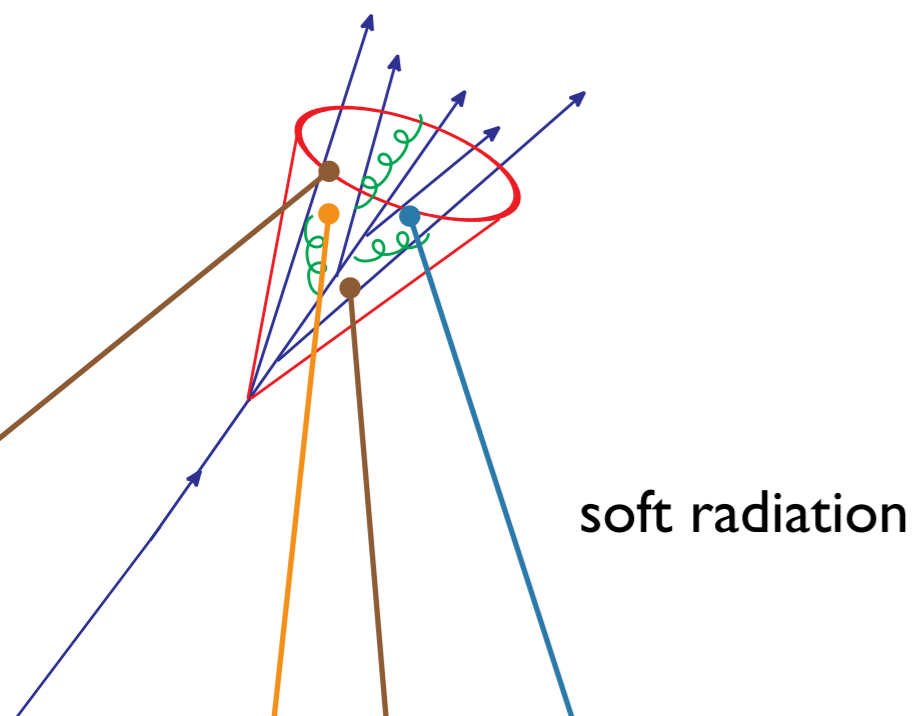
Frye, Larkoski, Schwartz, Yan '16
Marzani, Schunk, Soyez '17
Kang, Lee, Liu, FR '18



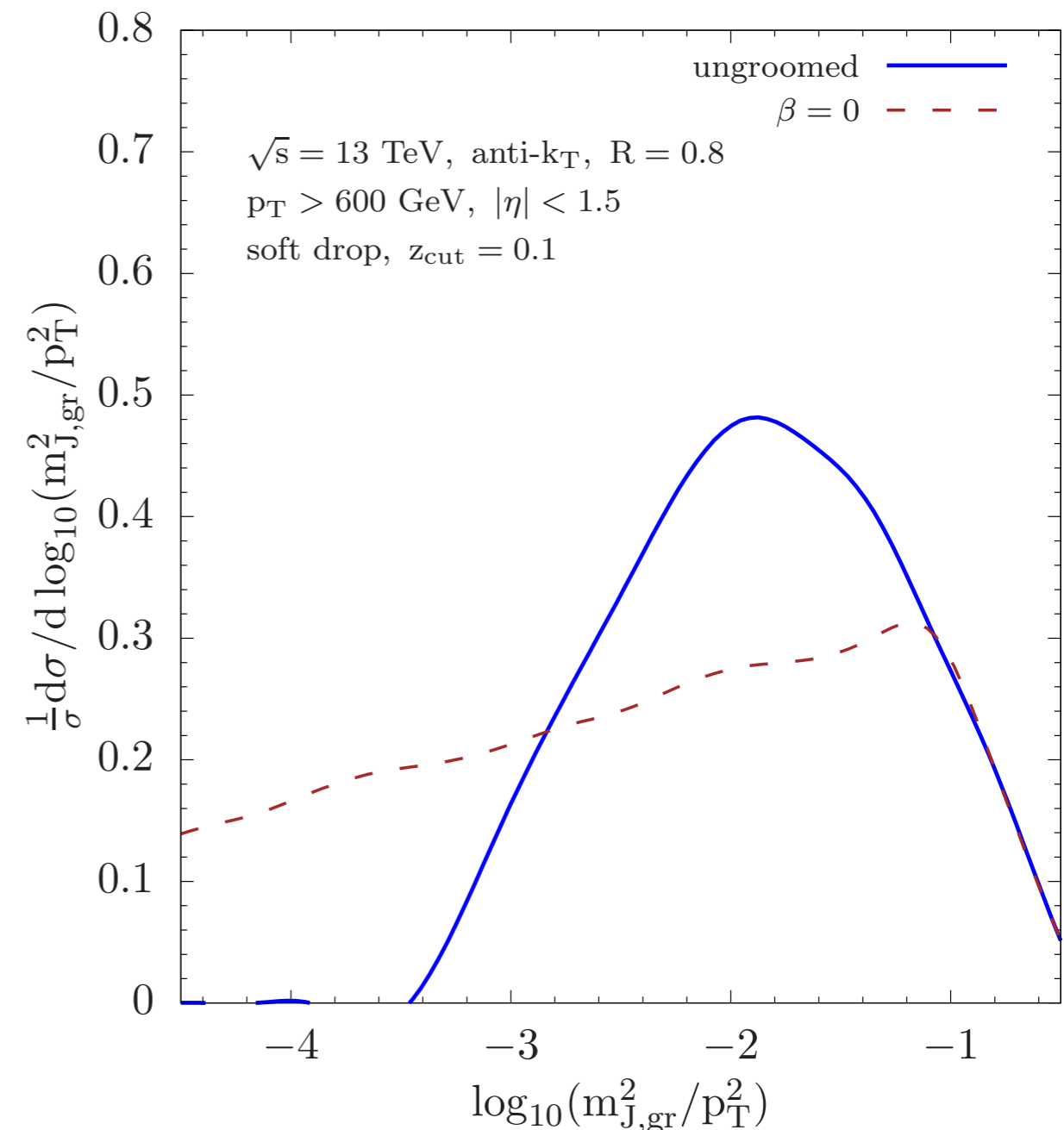
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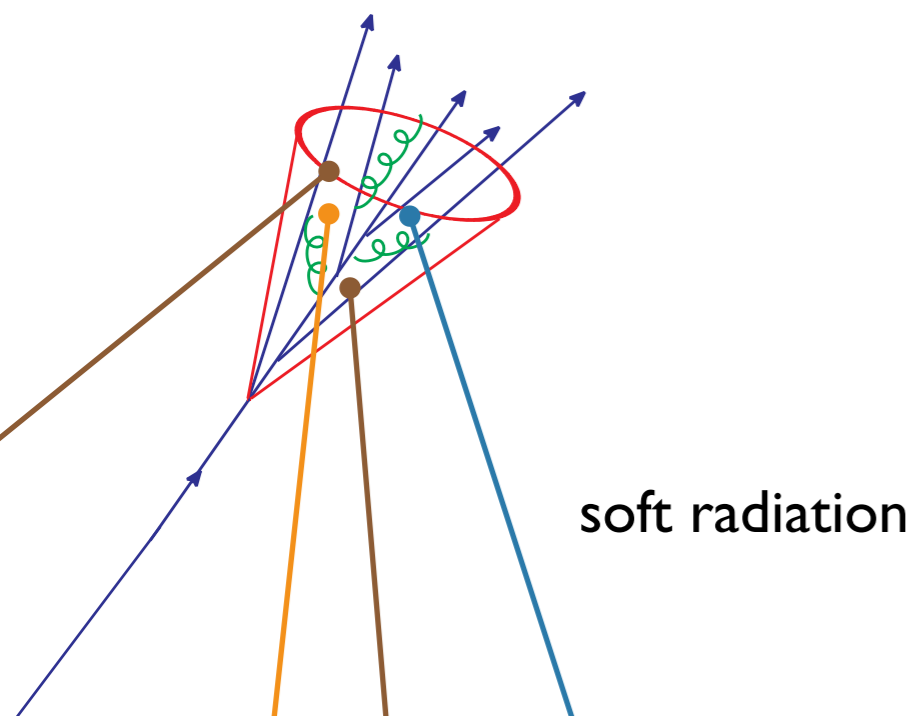
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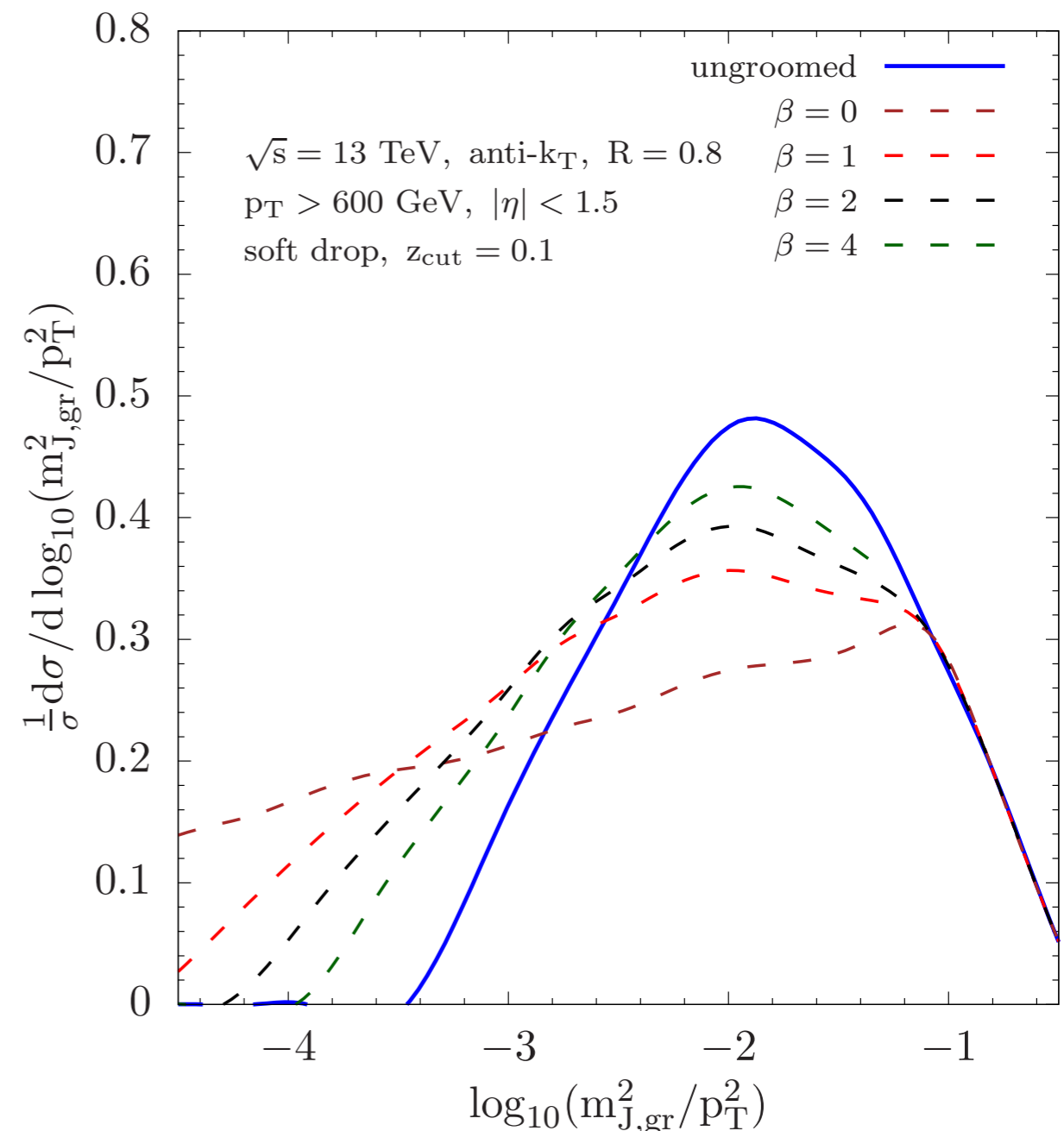
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Marzani, Schunk, Soyez '17
Kang, Lee, Liu, FR '18



Jet mass distributions

Kang, Lee, Liu, FR '18

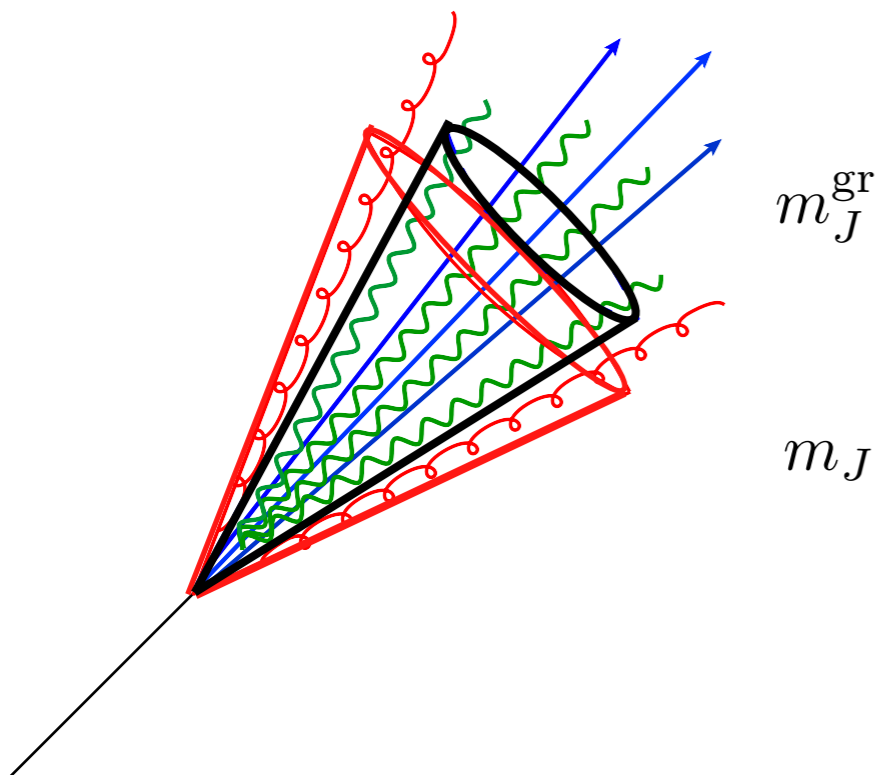
- The ungroomed case $R \ll 1$, $\tau/R^2 \ll 1$

$$\mathcal{G}_i(z, p_T R, \tau, \mu) = \sum_i \mathcal{H}_{i \rightarrow j}(z, p_T R, \mu) C_j(\tau, p_T, \mu) \otimes S_j(\tau, p_T, R, \mu)$$

$$\tau = \frac{m_J^2}{p_T^2}$$

- The groomed case $R \ll 1$, $\tau_{\text{gr}}/R^2 \ll z_{\text{cut}} \ll 1$

$$\mathcal{G}_i^{\text{gr}}(z, p_T R, \tau_{\text{gr}}, z_{\text{cut}}, \mu) = \sum_j \mathcal{H}_{i \rightarrow j}(z, p_T R, \mu) S_i^{\not{\text{gr}}}(z_{\text{cut}} p_T R, \beta, \mu) C_i(\tau_{\text{gr}}, p_T, \mu) \otimes S_i^{\text{gr}}(\tau_{\text{gr}}, p_T, R, z_{\text{cut}}, \mu)$$



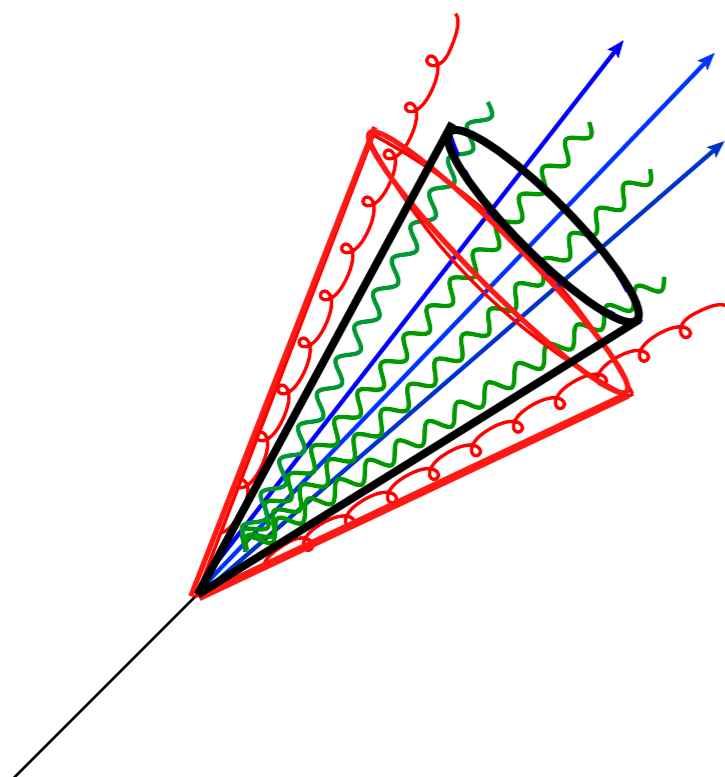
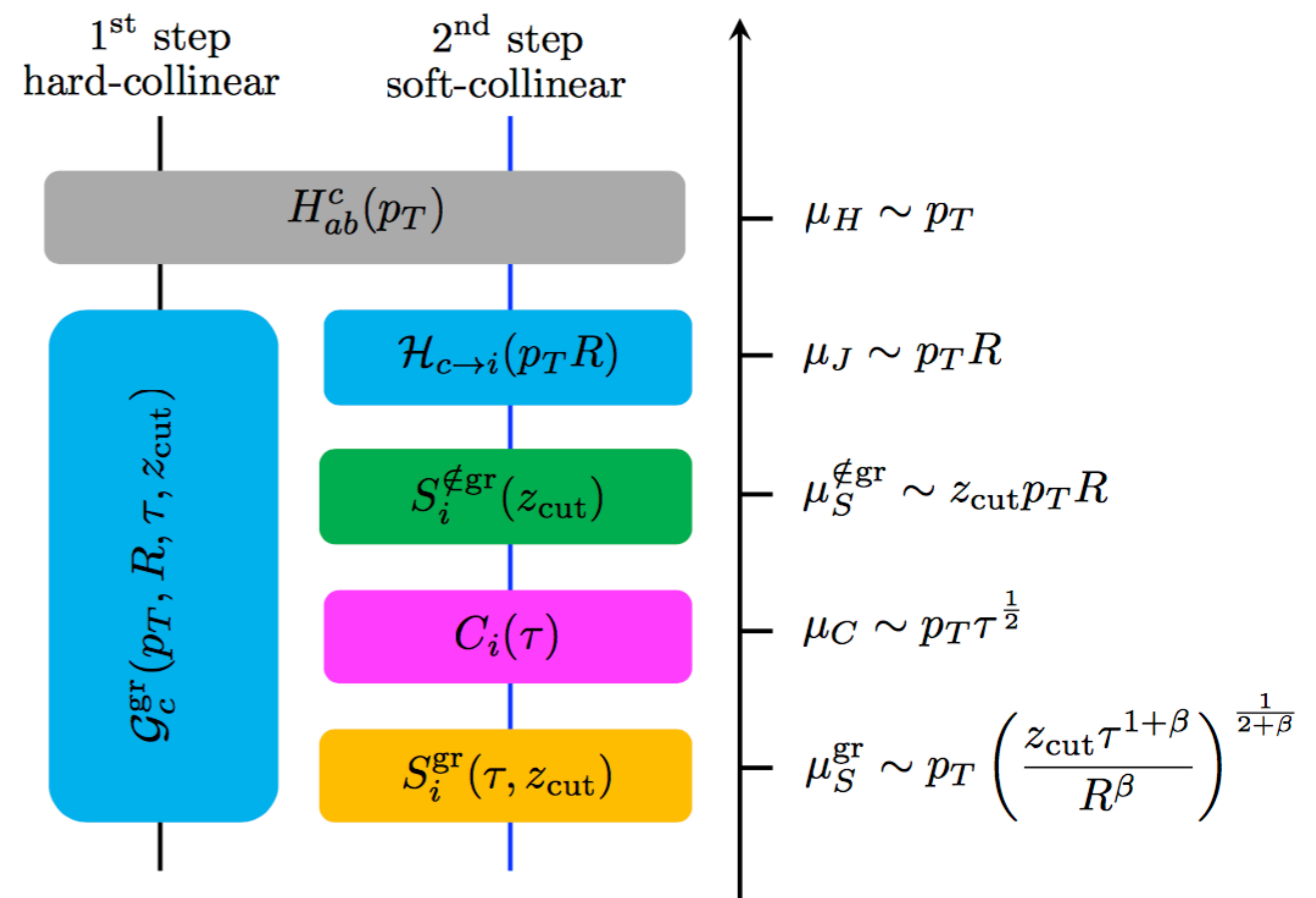
Jet mass distributions

Kang, Lee, Liu, FR '18

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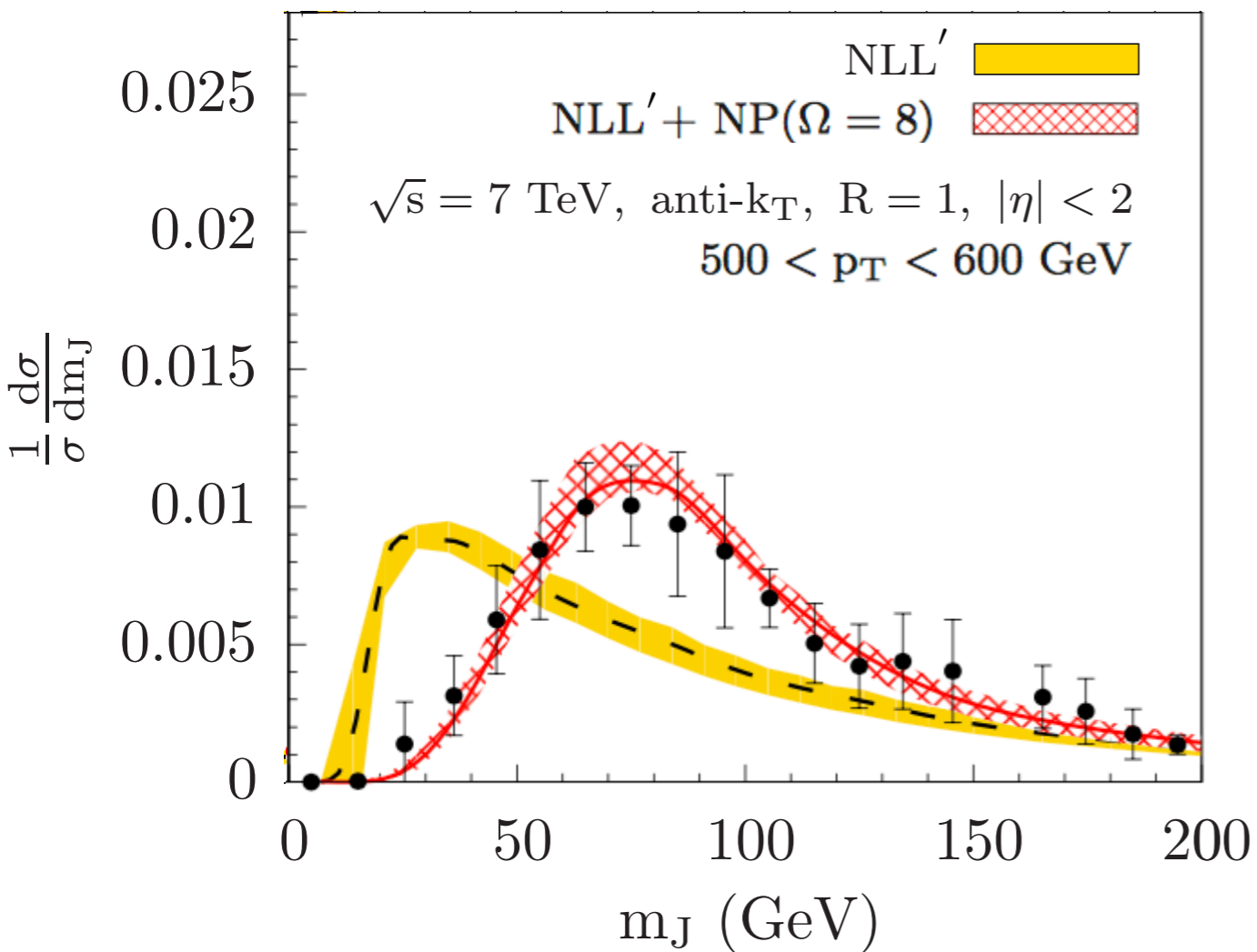
- Resummation of 3 classes of logarithms $\alpha_s^n \ln^n R$, $\alpha_s^n \ln^{2n}(m_J/p_T)$, $\alpha_s^n \ln^{2n} z_{\text{cut}}$

 m_J^{gr} m_J 

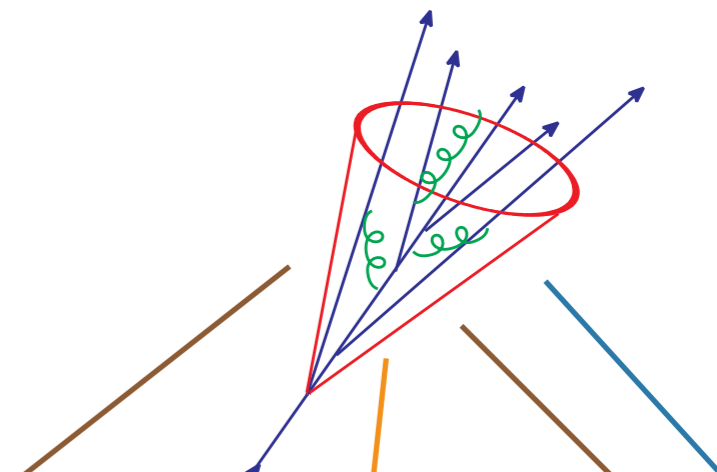
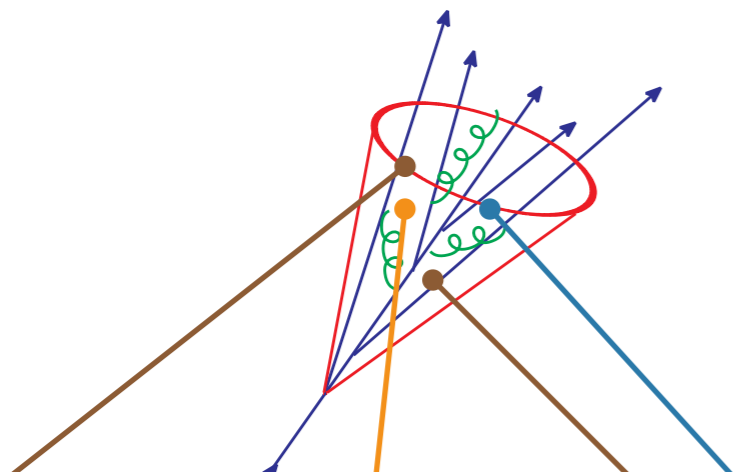
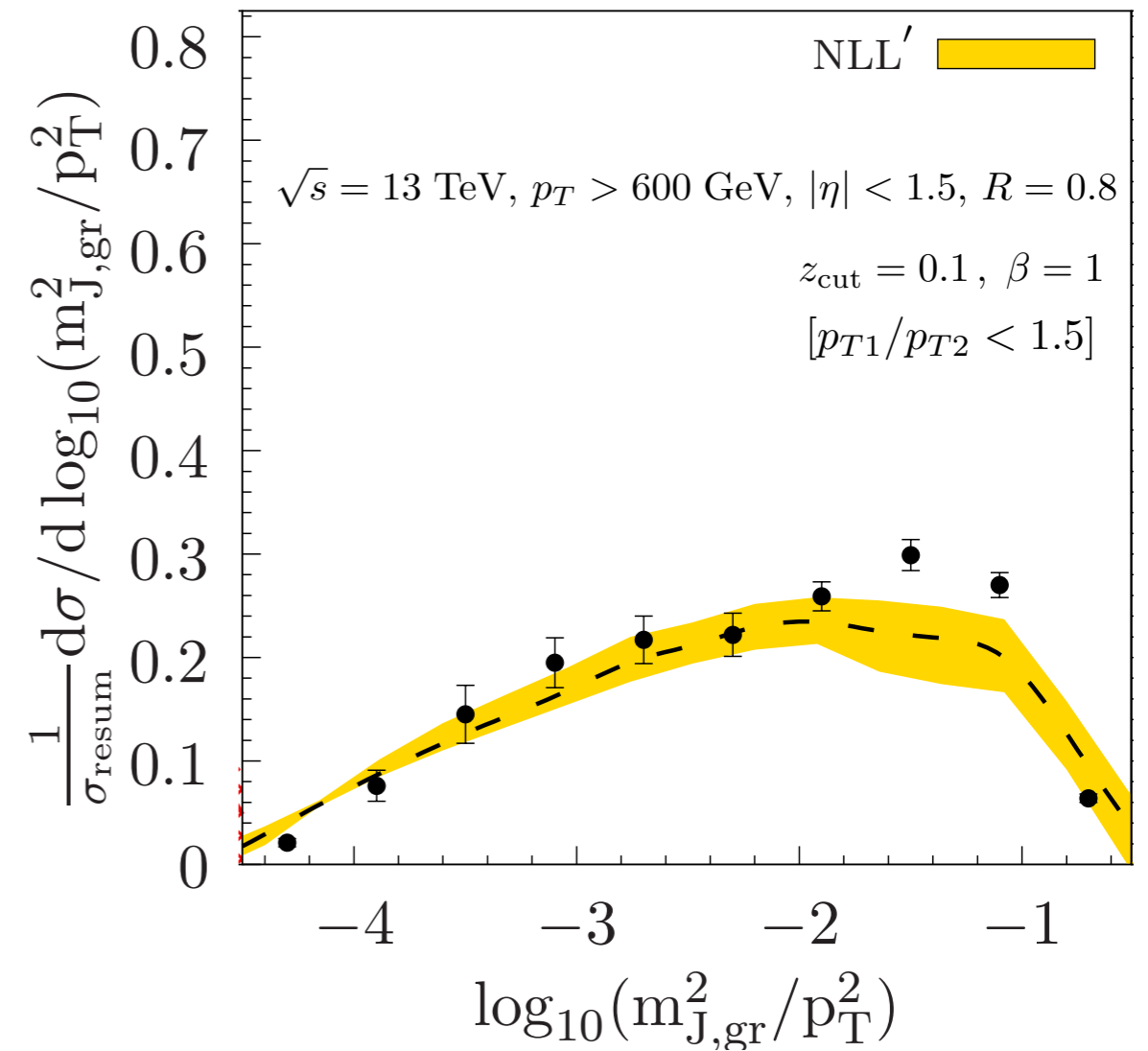
Jet mass distributions

Kang, Lee, Liu, FR '18

ATLAS, JHEP 05 (2012) 128



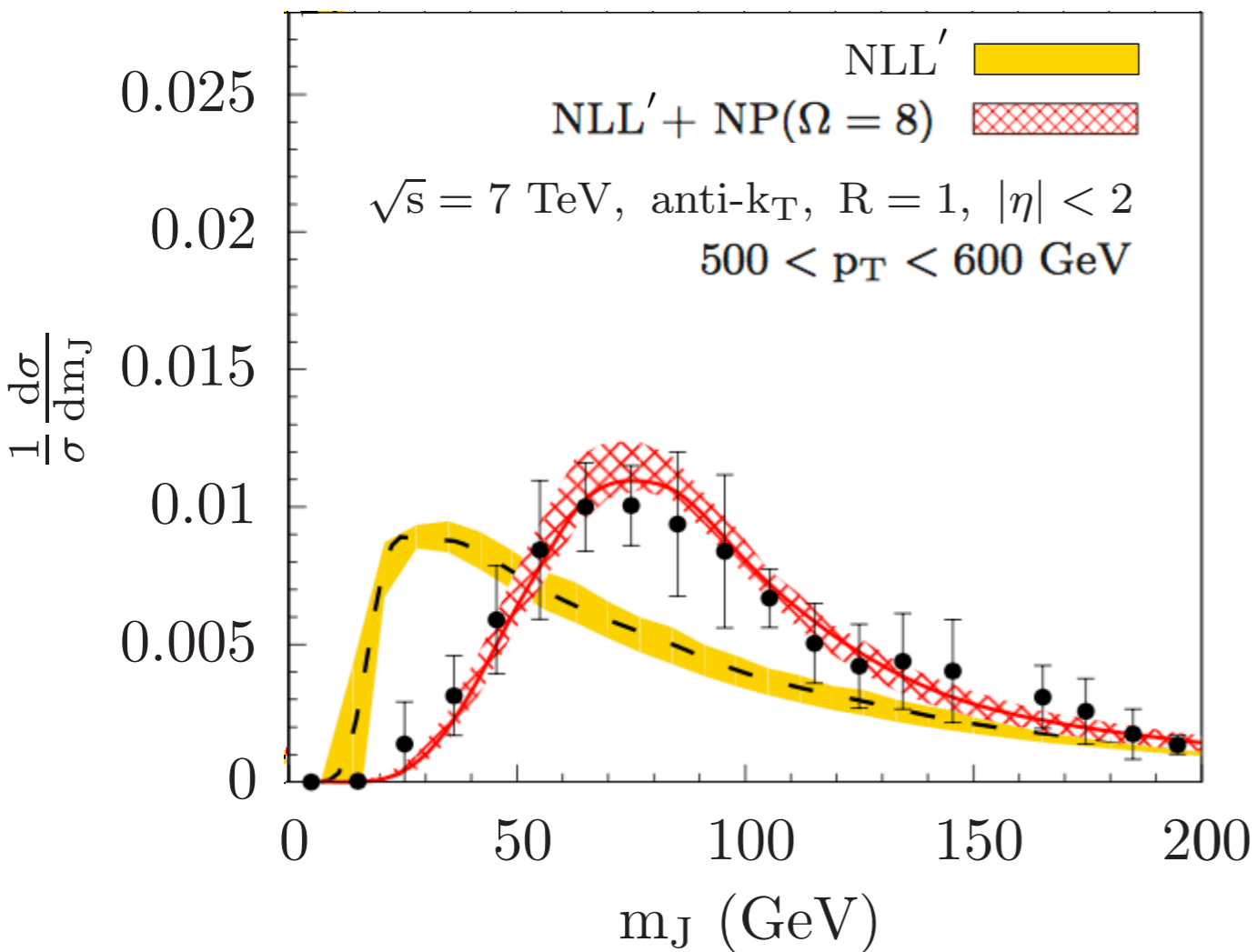
ATLAS, PRL 121 (2018) 092001



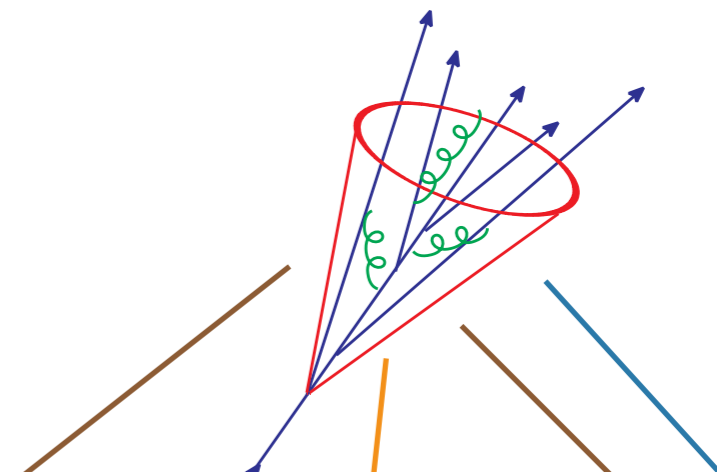
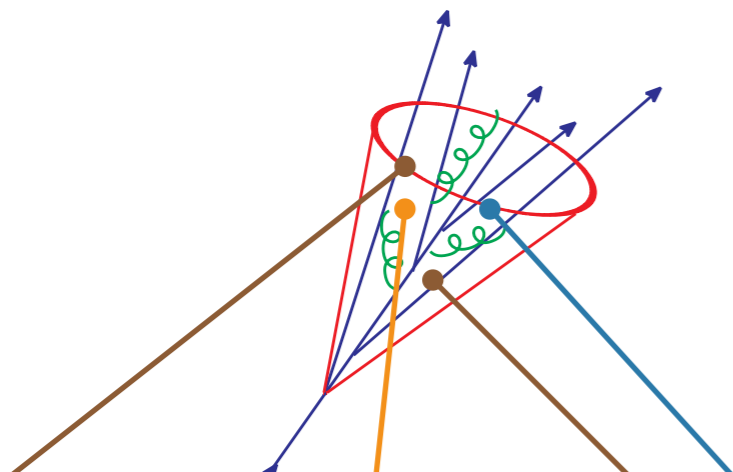
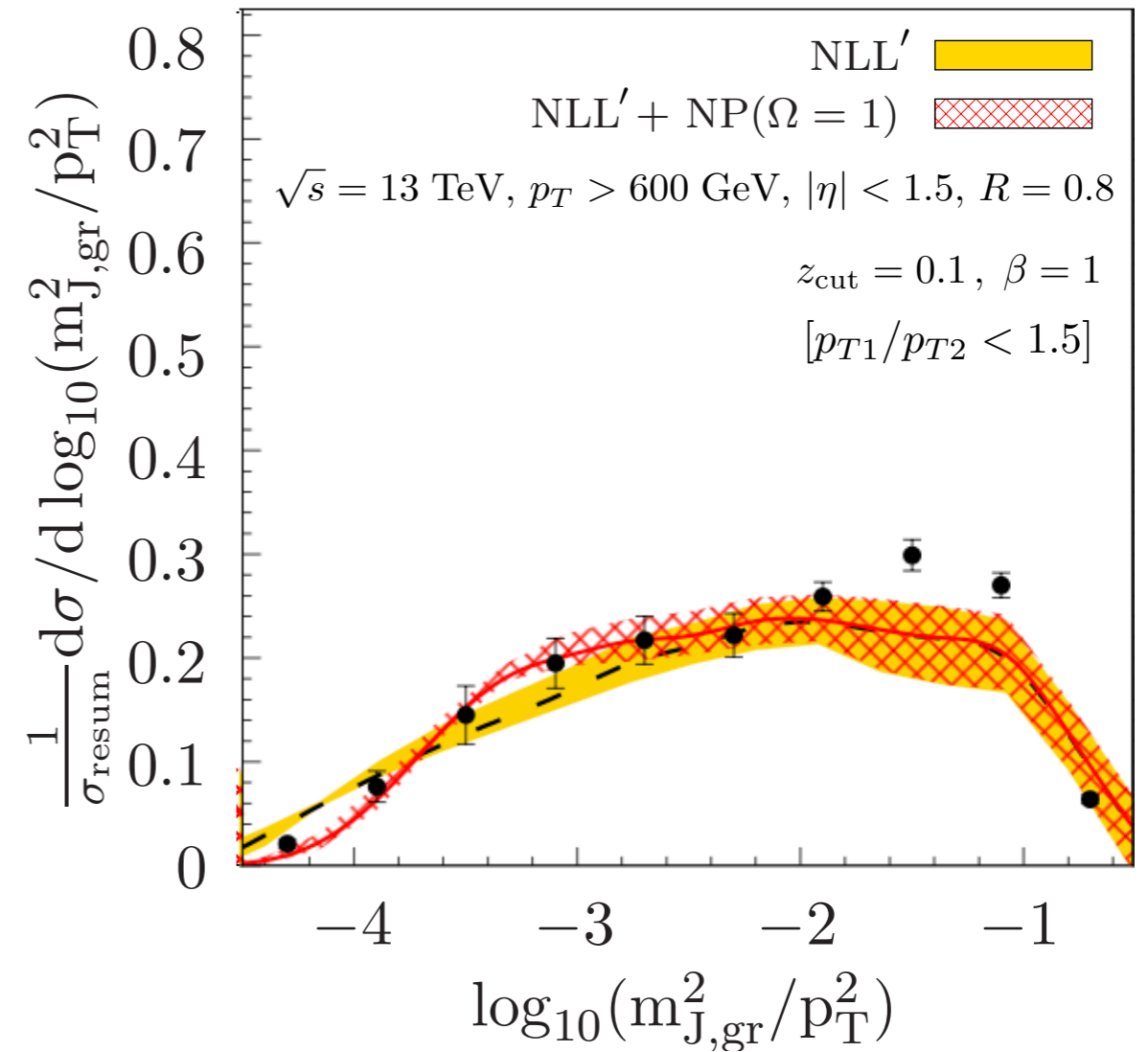
Jet mass distributions

Kang, Lee, Liu, FR '18

ATLAS, JHEP 05 (2012) 128

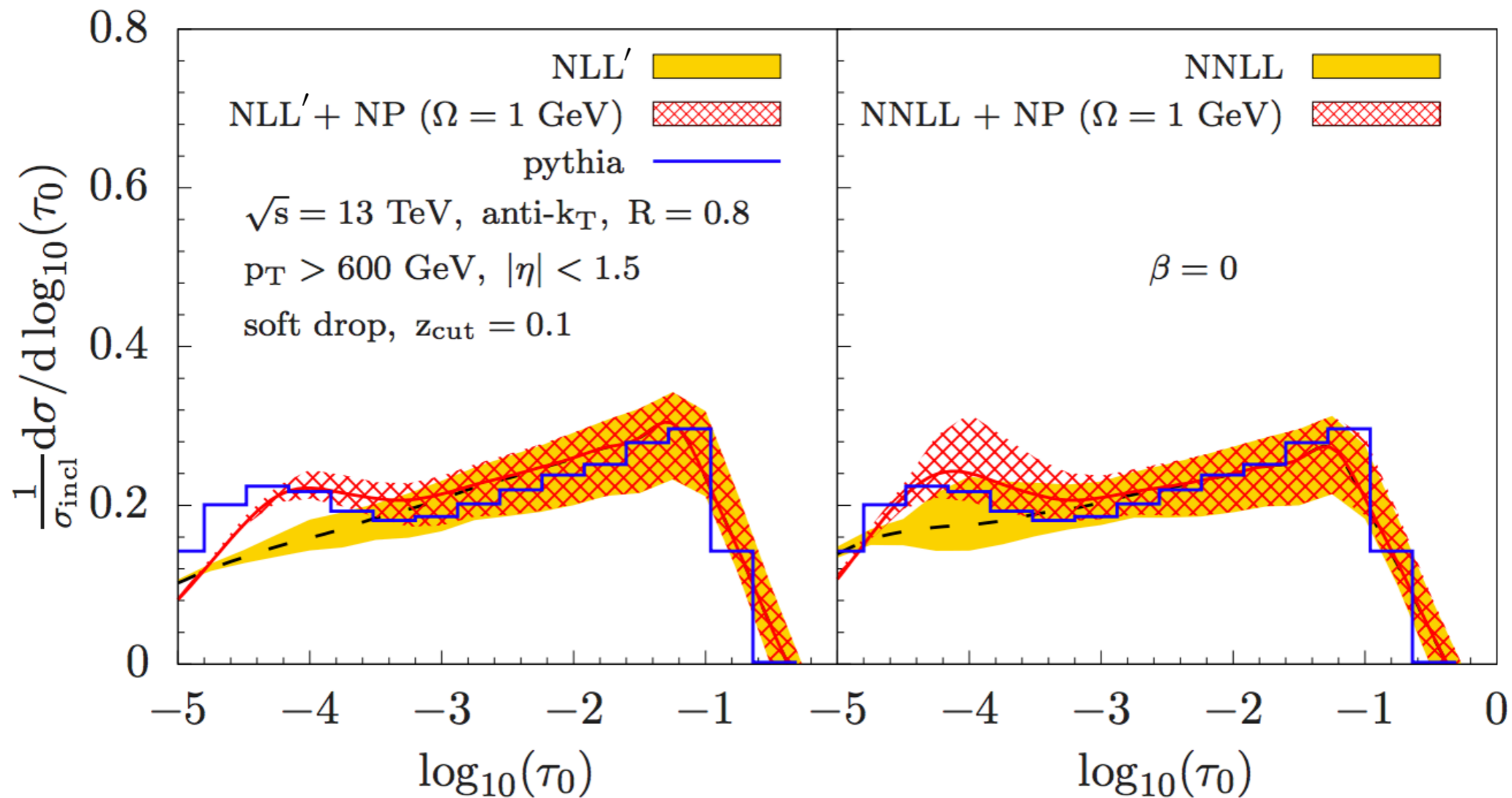


ATLAS, PRL 121 (2018) 092001



Jet mass distributions

Kang, Lee, Liu, FR '18



- Non-perturbative shape functions with grooming

see: Hoang, Mantry, Pathak, Stewart - BOOST18

$$\tau_0 = m_J^2 / p_T^2$$

Non-global logarithms

- The ungroomed case

$$\mathcal{G}_i(z, p_T R, \tau, \mu) = \sum_j \mathcal{H}_{i \rightarrow j}(z, p_T R, \mu) C_i(\tau, p_T, \mu) \otimes S_i(\tau, p_T, R, \mu)$$

Dasgupta, Salam '01,
Banfi, Marchesini, Smye '02
Larkoski, Moult, Neill '15
Becher, Rahn, Shao '17 ...

NGLs directly in the jet mass variable $\alpha_s^n \ln^n(\tau/R^2)$ $n \geq 2$

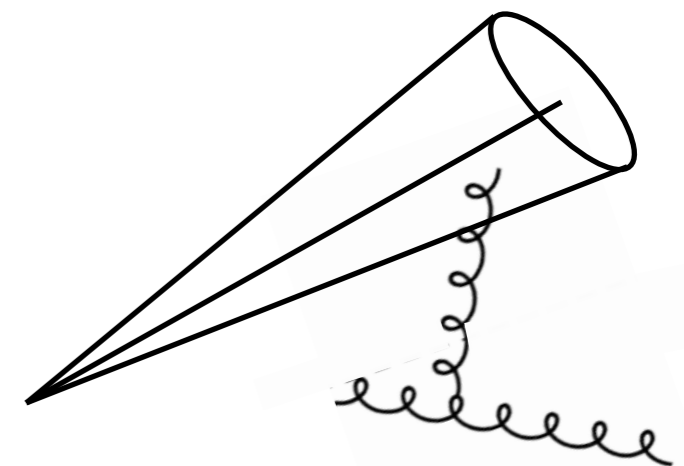
- The groomed case

$$\mathcal{G}_i^{\text{gr}}(z, p_T R, \tau_{\text{gr}}, z_{\text{cut}}, \mu) = \sum_j \mathcal{H}_{i \rightarrow j}(z, p_T R, \mu) S_i^{\not\text{gr}}(z_{\text{cut}} p_T R, \beta, \mu) C_i(\tau_{\text{gr}}, p_T, \mu) \otimes S_i^{\text{gr}}(\tau_{\text{gr}}, p_T, R, z_{\text{cut}}, \mu)$$

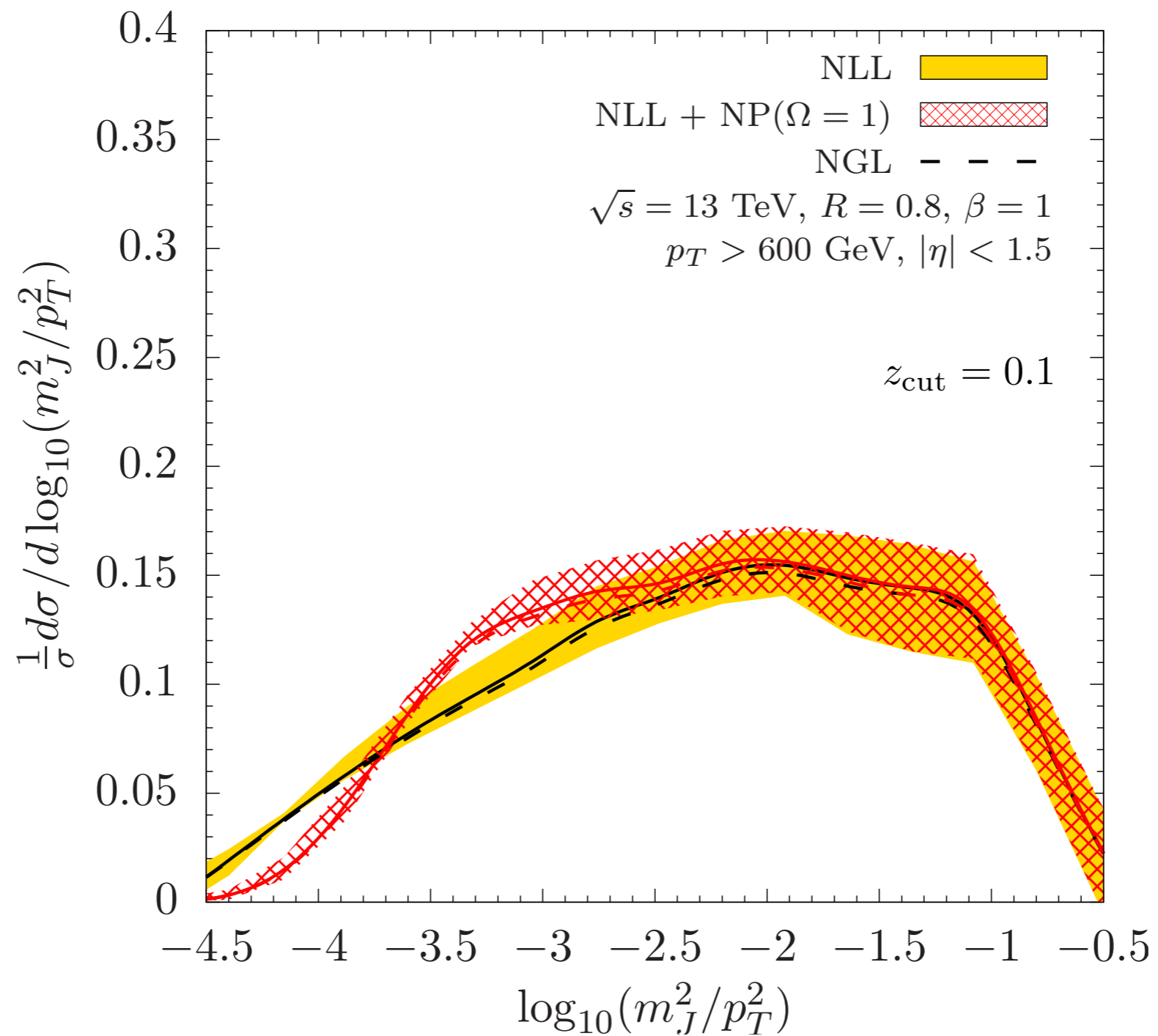
NGLs affect the normalization and only indirectly affect the spectrum

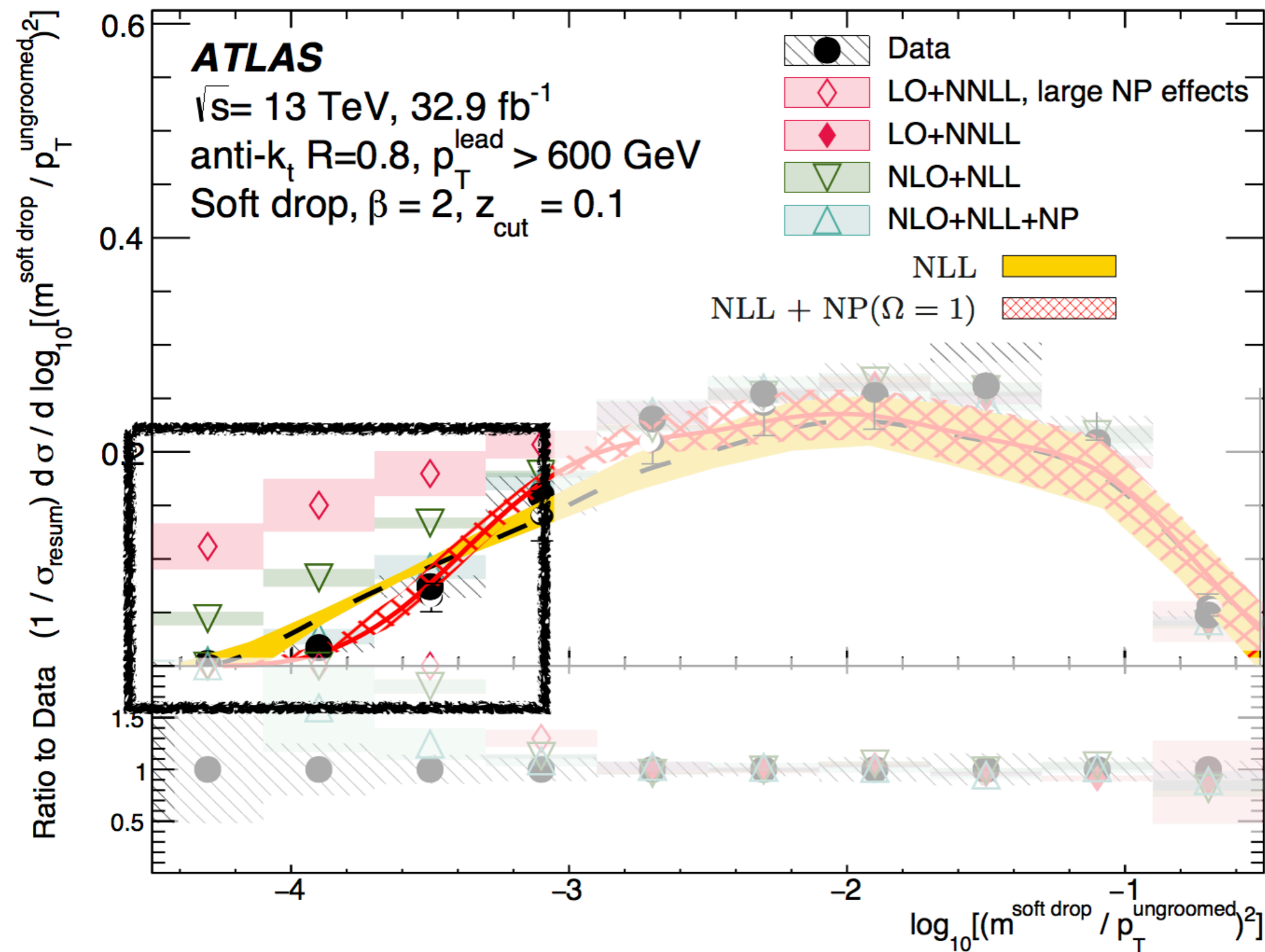
$$\alpha_s^n \ln^n z_{\text{cut}} \quad n \geq 2$$

→ NGLs can be included in both cases



Non-global logarithms





Frye, Larkoski, Schwartz, Yan '16
 Marzani, Schunk, Soyez '17
 Kang, Lee, Liu, FR '18

ATLAS, PRL 121 (2018) 092001

A lot of important progress but still work to do!

Ben Nachman, BOOST18

Comparison of the theory calculations

Frye, Larkoski, Schwartz, Yan `16

- NNLL
- Energy-energy correlation functions
- large R
- SCET

Marzani, Schunk, Soyez `17

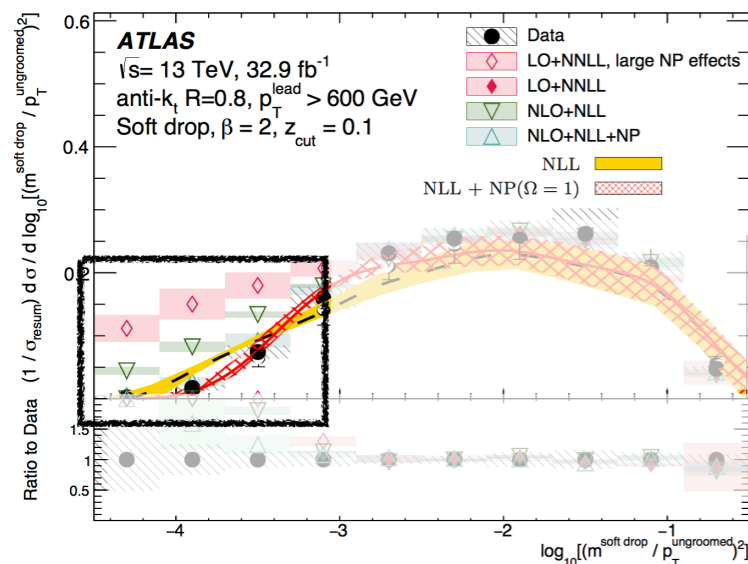
- NLL, jet mass
- NLO fixed order matching
- Finite z_{cut} corrections
- large R
- pQCD

Kang, Lee, Liu, FR `18, `18

- (N)NLL, jet angularities
- small R , $\ln R$ resummation
- $\ln z_{\text{cut}}$ resummation
- Q/g fractions beyond LO
- Possible to use universality of NP corrections
- NGLs can be included
- SCET



Ideally combine advantages of the different calculations



Ben Nachman, BOOST18

Outline

- Introduction
- Groomed jet substructure observables at the LHC
- Determination of the QCD coupling
- Conclusions

Jet substructure at the LHC

- Groomed jet mass: Sensitivity to NP physics

Ungroomed: $\mu_S \sim \frac{p_T \tau}{R}$

SD groomed: $\mu_S \sim \frac{p_T \tau}{R} \left(\frac{z_{\text{cut}} R^2}{\tau^2} \right)^{\frac{1}{2+\beta}}$

with $\mu_S = \Lambda_{\text{QCD}} \sim 1 \text{ GeV}$

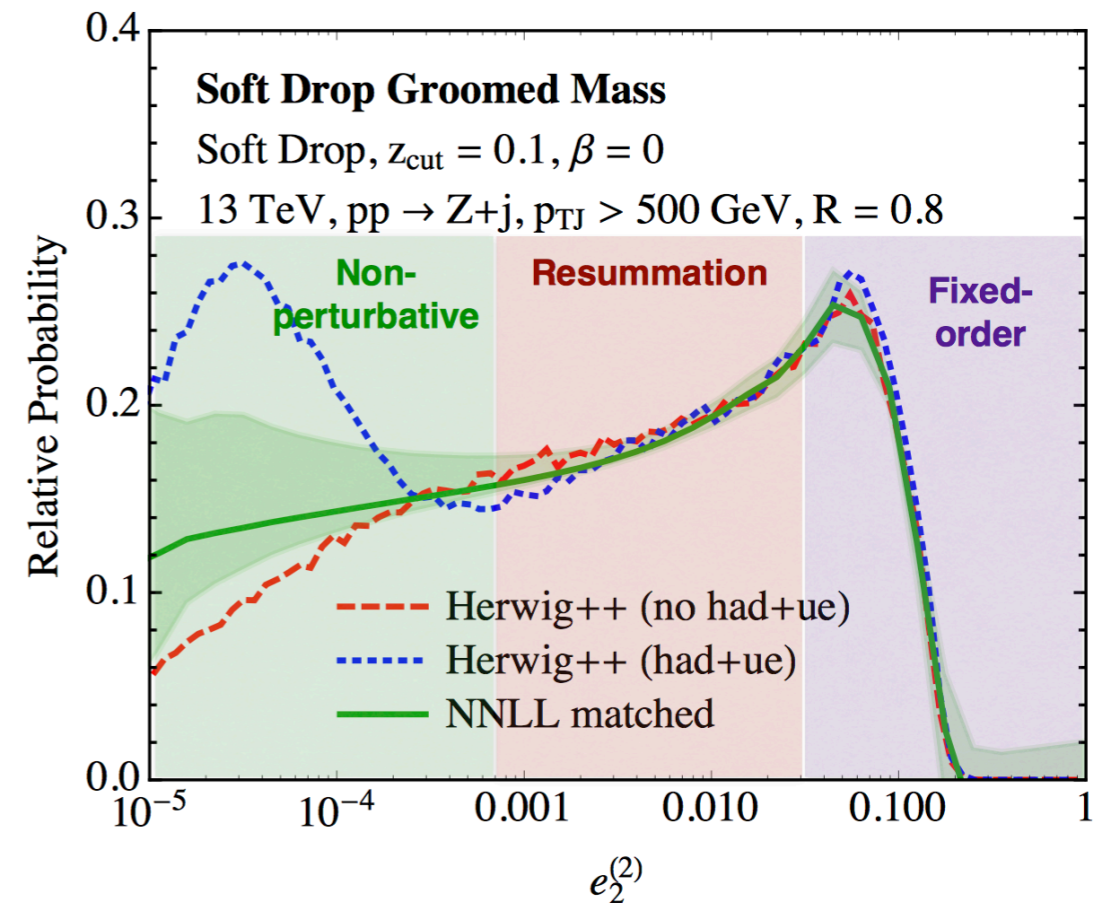
→ Onset of NP physics

$$\tau_{\text{gr}} = \tau_{\text{ungr}} \left(\frac{\Lambda_{\text{QCD}}}{p_T R z_{\text{cut}}} \right)^{\frac{1}{1+\beta}}$$

Potentially 2 orders of magnitude difference for a 1 TeV jet!

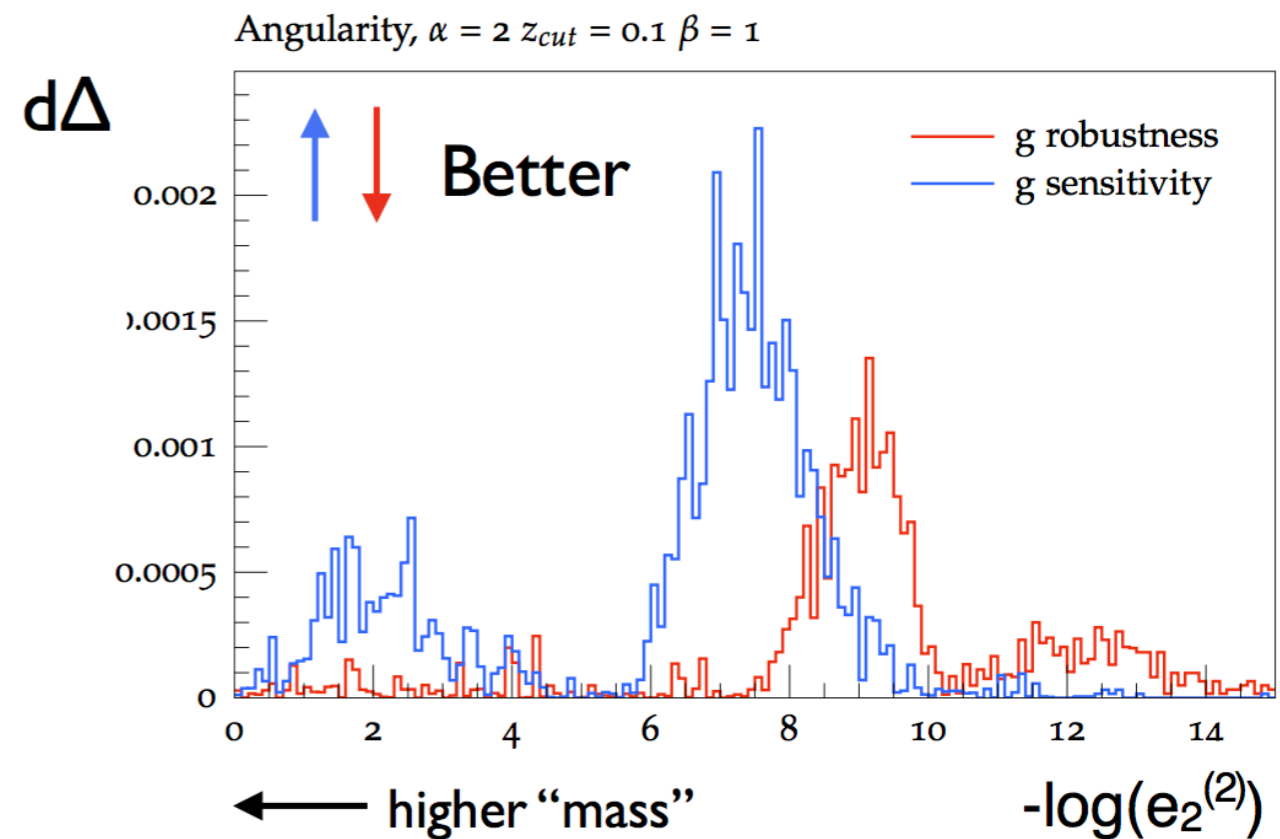
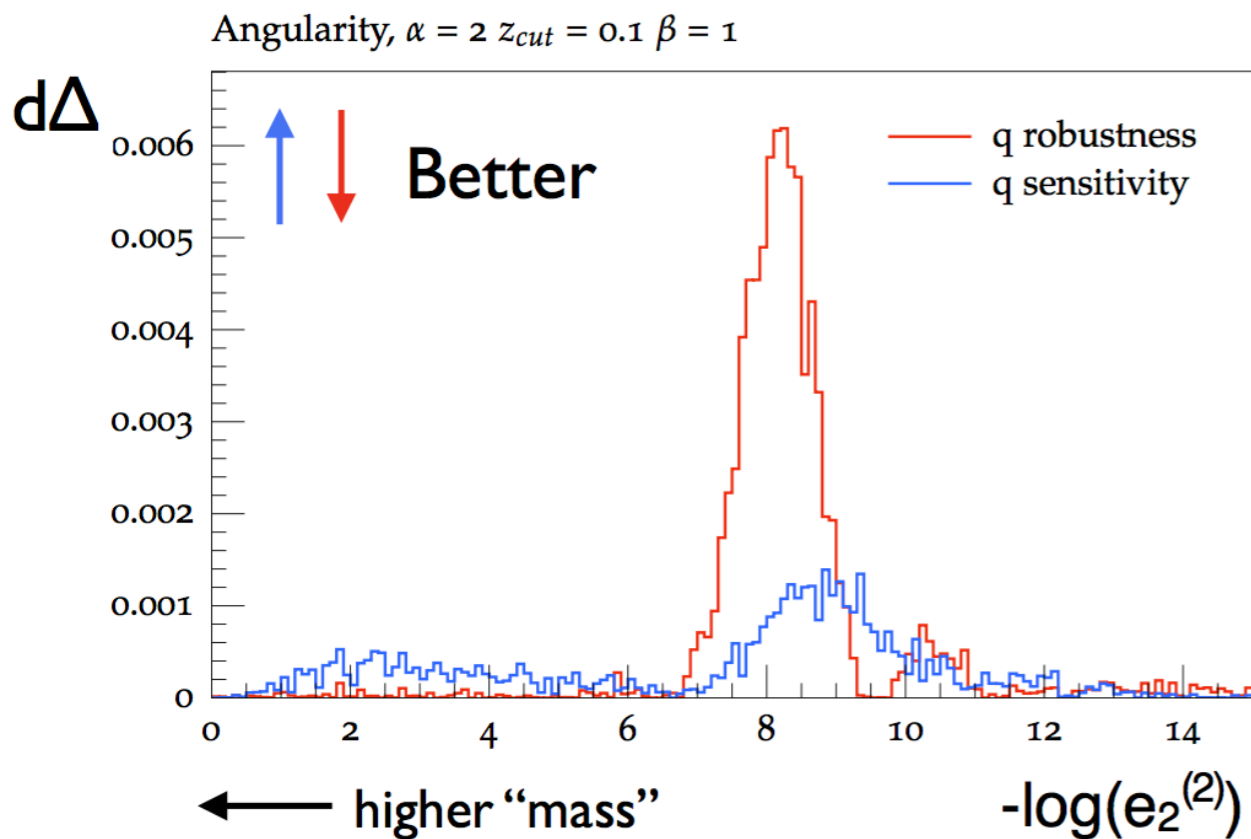
Les Houches '17

Frye, Larkoski, Schwartz, Yan '16



Sensitivity to α_s and NP effects

- Sensitivity α_s (+10%)
- NP robustness (had. on/off)



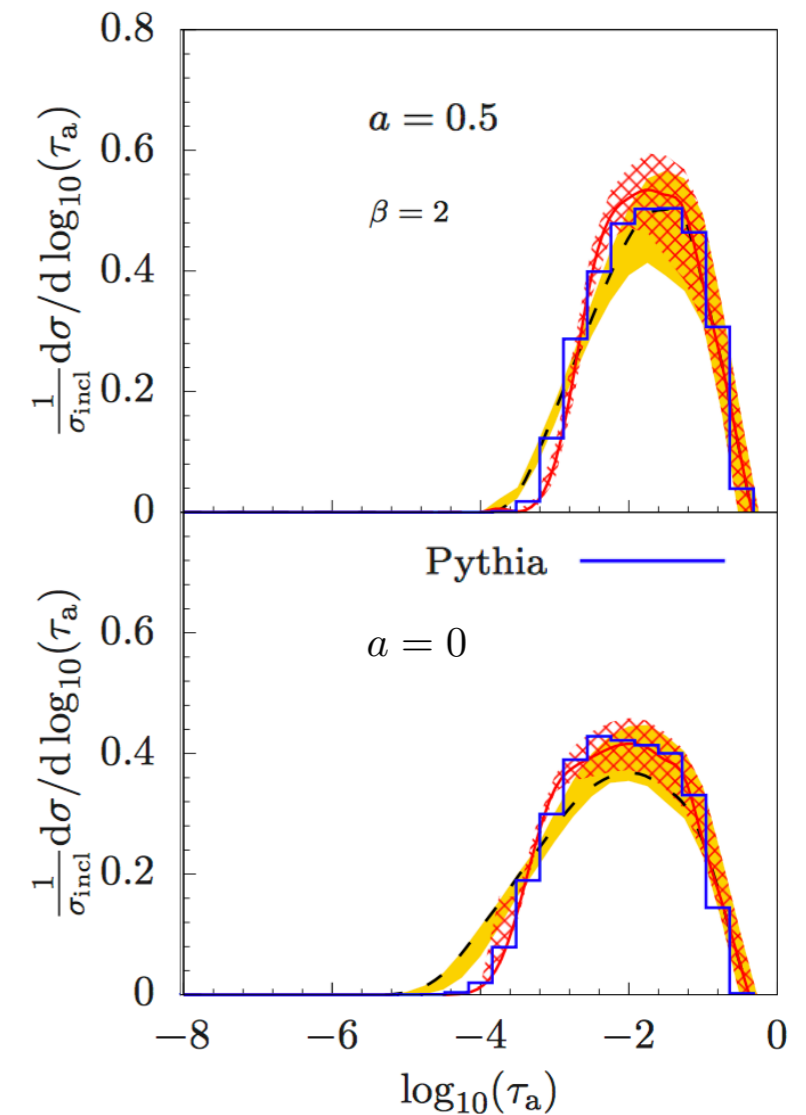
Choice of observables

- Jet angularities
- Family of observables with a continuous parameter a
- Jet mass ($a = 0$), jet broadening ($a = 1$)

$$\tau_a = \frac{1}{p_T} \sum_{i \in J} p_{Ti} \Delta R_{iJ}^{2-a}$$

NLL
 NLL + NP($\Omega_a = \frac{1 \text{ GeV}}{1-a}$)
 $\sqrt{s} = 13 \text{ TeV}$, anti- k_T , $R = 0.8$
 $p_T > 600 \text{ GeV}$, $|\eta| < 1.5$
 soft drop, $z_{\text{cut}} = 0.1$, $\beta = 0$

Berger, Kucs, Sterman '03
 Kang, Lee, Liu, FR '18



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*Berger, Kucs, Sterman '03
Kang, Lee, Liu, FR '18*

$$\tau_a = \frac{1}{p_T} \sum_{i \in J} p_{Ti} \Delta R_{iJ}^{2-a}$$

- Energy-energy correlation functions e.g. 2-point

*Banfi, Salam, Zanderighi '05
Larkoski, Salam, Thaler '13
Frye, Larkoski, Schwartz, Yan '16*

$$e_2^{(\alpha)} = \frac{1}{p_T^2} \sum_{i < j \in J} p_{Ti} p_{Tj} \Delta R_{ij}^\alpha$$

Further considerations

- Normalized vs. unnormalized distribution: LO $\mathcal{O}(\alpha_s^2)$ and involves PDFs
- Combined fit with PDFs?

- Jet angularities could break degeneracy of α_s and NP effects $\frac{\Omega}{1-a}$ Lee, Sterman '07

But need double differential distributions

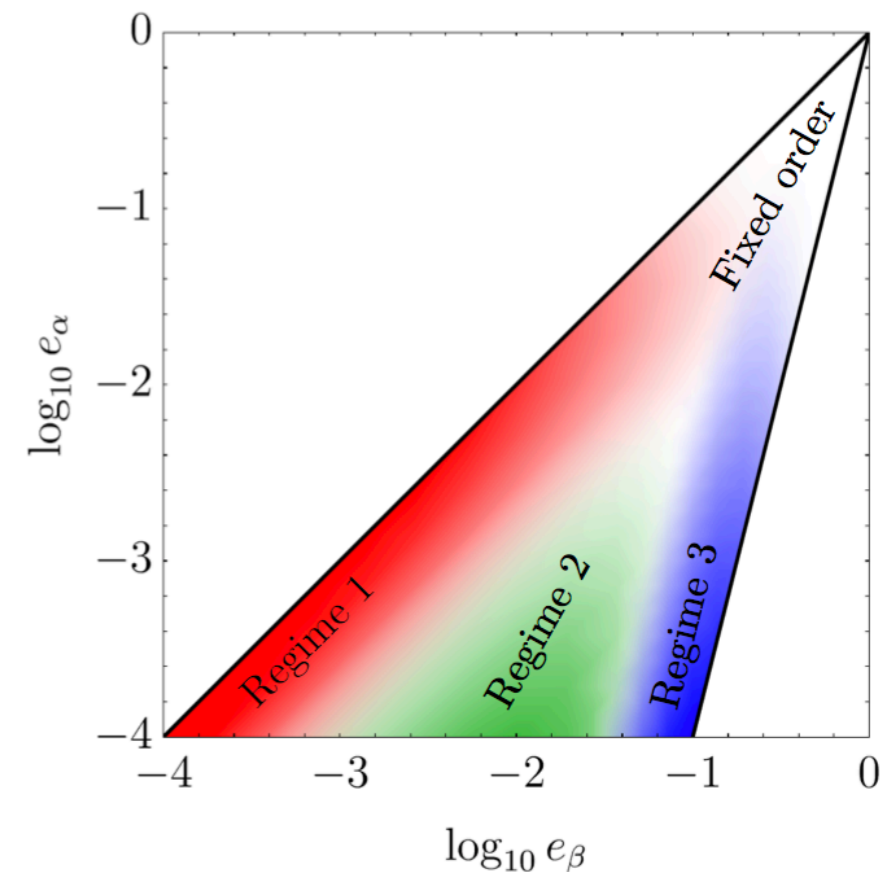
→ Correlations within multi observable fit

Procura, Waalewijn, Zeune '18

$$\frac{d^2\sigma}{de_\alpha de_\beta}$$

- Relate NP shape functions between different experiments
- Non-perturbative effects using shape functions?

see: Hoang, Mantry, Pathak, Stewart - BOOST18



Future directions

- Theory

- Precision goal NNLL' or $N^3LL + 2 \rightarrow 3$ at NNLO
- Observables: Different choices of the jet axis?
- Double differential distributions?
- Non-perturbative shape functions with grooming?

Badger, Biedermann, Uwer, Yundin `14

Gehrmann, Henn, Presti `15

Dunbar, Perkins `16

Abreu, Cordero, Ita, Page, Zeng `17

Badger, Hansen, Hartanto, Peraro `17

Moult, Zhu `18

...

- Experiment

- Mass scale and resolution uncertainties
- Pileup modeling and mitigation especially for high p_T jets for Run3+
- Track based observables possible? *Chang, Procura, Thaler, Waalewijn `13*

Outline

- Introduction
- Groomed jet substructure observables at the LHC
- Determination of the QCD coupling
- Conclusions

Conclusions

- Precision era of jet substructure at the LHC is just starting
- Possibility to extract α_s from jet substructure data
- Hadron collider observables, soft drop grooming
- Currently $\sim 10\%$ expected and interesting NP aspects
- Competitive extractions require advances from both theory and experiment

