

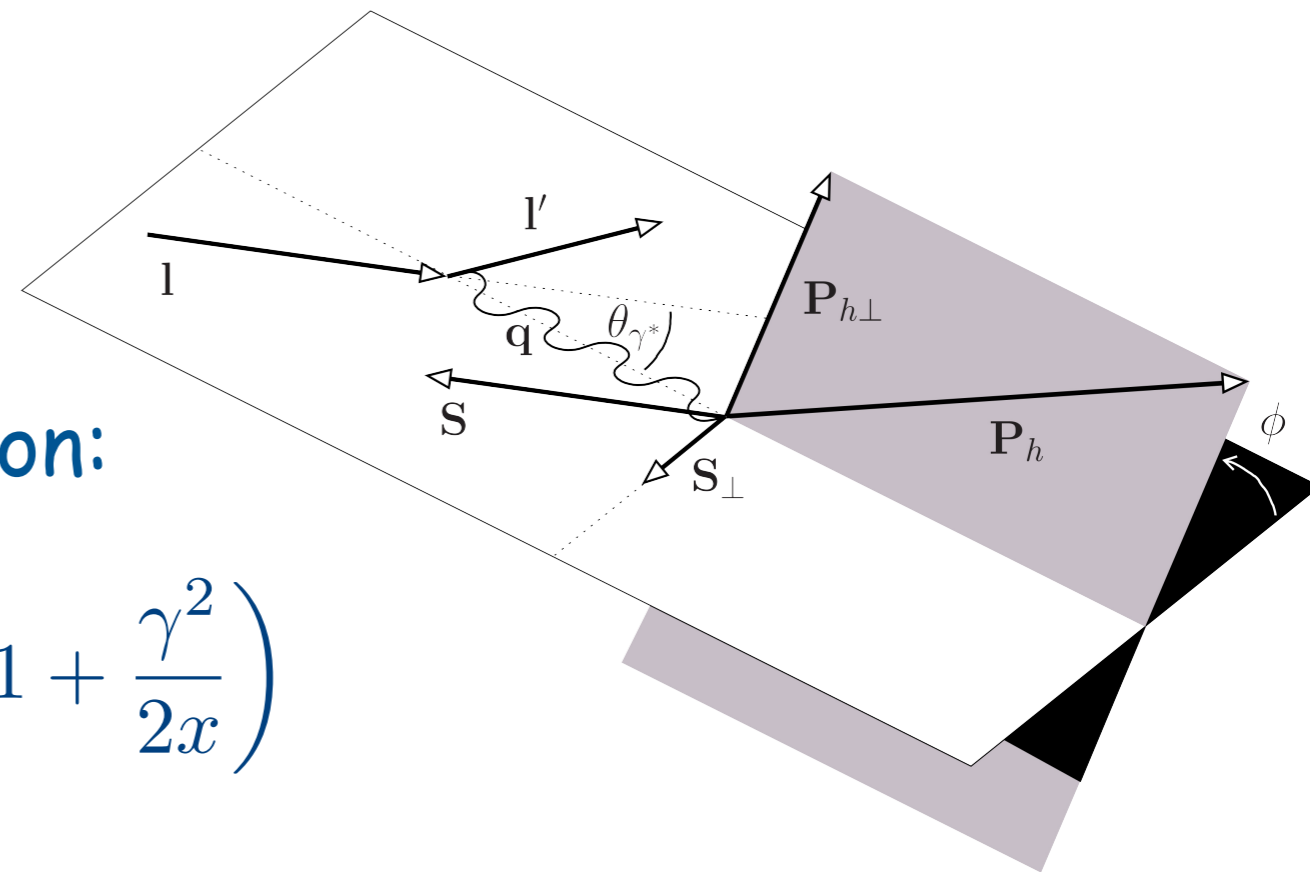
27th International Workshop on Deep-Inelastic Scattering and Related Subjects



Beam-helicity asymmetries in semi-inclusive
deep-inelastic single-hadron production
from unpolarized hydrogen and deuterium
targets

semi-inclusive DIS

- excluding transverse polarization:



$$\frac{d\sigma^h}{dx dy dz dP_{h\perp}^2 d\phi} = \frac{2\pi\alpha^2}{xyQ^2} \frac{y^2}{2(1-\epsilon)} \left(1 + \frac{\gamma^2}{2x} \right)$$

$$\left\{ F_{UU,T}^h + \epsilon F_{UU,L}^h + \lambda\Lambda\sqrt{1-\epsilon^2} F_{LL}^h \right.$$

$$+ \sqrt{2\epsilon} \left[\lambda\sqrt{1-\epsilon} F_{LU}^{h,\sin\phi} + \Lambda\sqrt{1+\epsilon} F_{UL}^{h,\sin\phi} \right] \sin\phi$$

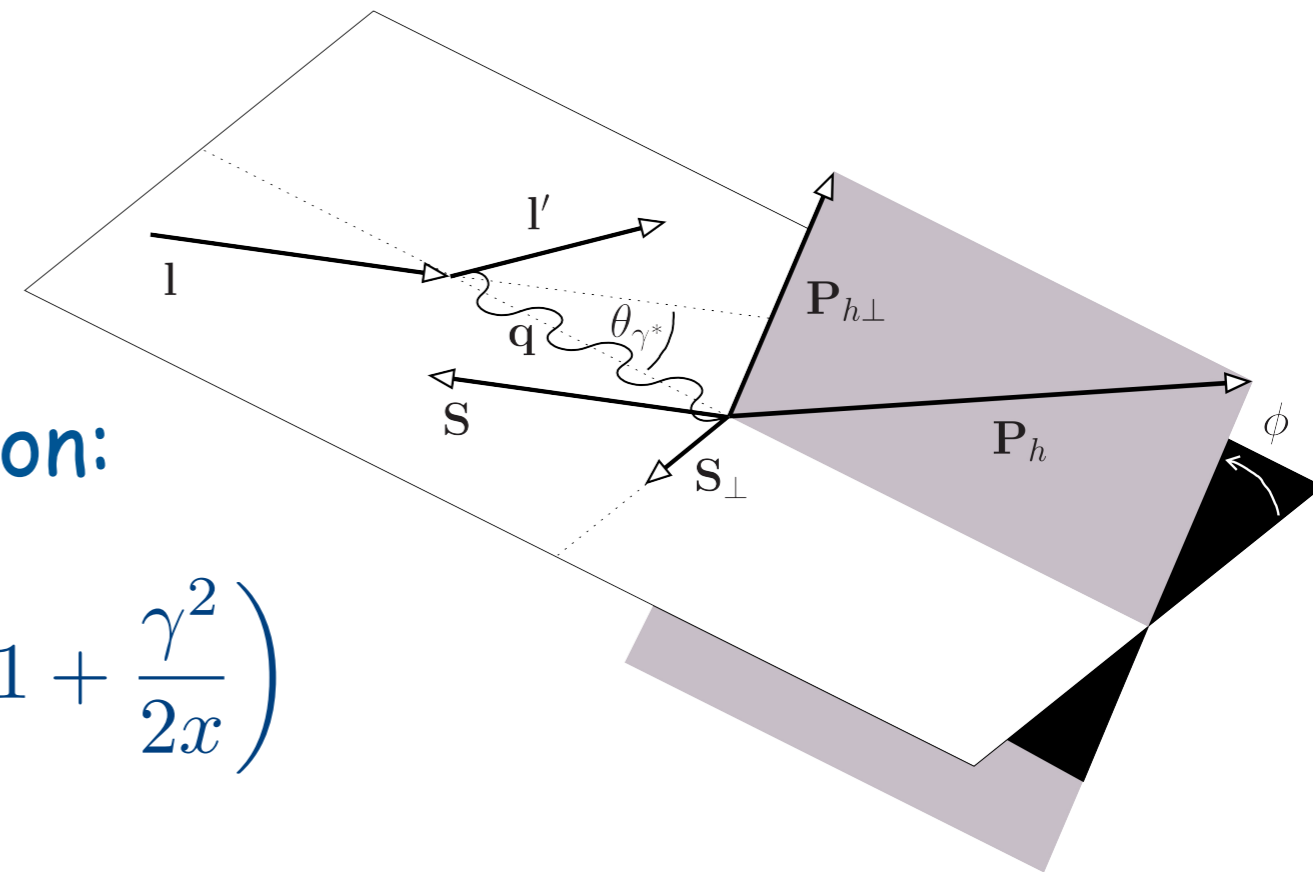
$$+ \sqrt{2\epsilon} \left[\lambda\Lambda\sqrt{1-\epsilon} F_{LL}^{h,\cos\phi} + \sqrt{1+\epsilon} F_{UU}^{h,\cos\phi} \right] \cos\phi$$

$$\left. + \Lambda\epsilon F_{UL}^{h,\sin 2\phi} \sin 2\phi + \epsilon F_{UU}^{h,\cos 2\phi} \cos 2\phi \right\}$$

- single-spin asymmetry

$$A_{LU}^h \equiv \frac{\sigma_{+-}^h + \sigma_{++}^h - \sigma_{-+}^h - \sigma_{--}^h}{\sigma_{+-}^h + \sigma_{++}^h + \sigma_{-+}^h + \sigma_{--}^h}$$

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- single-spin asymmetry $A_{LU}^h \simeq \sqrt{2\epsilon(1-\epsilon)} \frac{F_{LU}^{h,\sin\phi}}{F_{UU}^h} \sin\phi$

beam-helicity asymmetry

$$\frac{M_h}{M_z} h_1^\perp \tilde{E} \oplus x g^\perp D_1 \oplus \frac{M_h}{M_z} f_1 \tilde{G}^\perp \oplus x e H_1^\perp$$

- naive-T-odd Boer-Mulders (BM) function coupled to a twist-3 FF
 - signs of BM from unpolarized SIDIS
 - little known about interaction-dependent FF

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 - interpreted as color force (from remnant) on transversely polarized quarks at the moment of being struck by virtual photon

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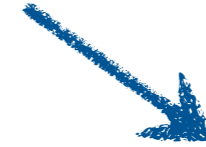
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 - e linked to the pion-nucleon σ -term
 - interpreted as color force (from remnant) on transversely polarized quarks at the moment of being struck by virtual photon
- all terms vanish in WW-type approximation

→ K. Tezgin (We, WG-6)

choice of fitting function

$$A_{LU}^h \simeq \sqrt{2\epsilon(1-\epsilon)} \frac{F_{LU}^{h,\sin\phi}}{F_{UU}^h} \sin\phi$$

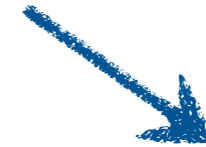


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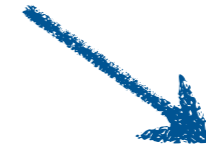
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- what about twist suppression and other kinematically suppressed contributions?

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- asymmetry amplitudes extracted by minimizing

$$-\ln \mathbb{L} = - \sum_i w_i \ln \left[1 + P_{B,i} \sqrt{2\epsilon_i(1-\epsilon_i)} A_{LU}^{h,\sin(\phi)} \sin(\phi_i) \right]$$

where w_i is event weight from hadron-ID, charge-symmetric BG etc.

interlude: dealing with
multi-d dependences

multi-d dependences

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 - some easily parametrized (e.g., azimuthal dependences)
 - others mostly unknown

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- one-dimensional binning provide only glimpse of true physics
 - even different kinematic bins can't disentangle underlying physics dependences
 - e.g., binning in x involves [incomplete] integration(s) over $P_{h\perp}$
- further complication: physics (cross sections) folded with acceptance
 - NO experiment has flat acceptance in full multi-d kinematic space

multi-d dependences

$$\frac{N^+(x) - N^-(x)}{N^+(x) + N^-(x)} = \frac{\int d\omega \epsilon(x, \omega) \Delta\sigma(x, \omega)}{\int d\omega \epsilon(x, \omega) \sigma(x, \omega)}$$

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- measured cross sections / asymmetries often contain "remnants" of experimental acceptance ϵ
- difficult to evaluate precisely in absence of good physics model
 - general challenge to statistically precise data sets
 - avoid 1d binning/presentation of data
 - theorist: watch out for precise definition (if given!) of experimental results reported ... and try not to treat data points of different projections as independent

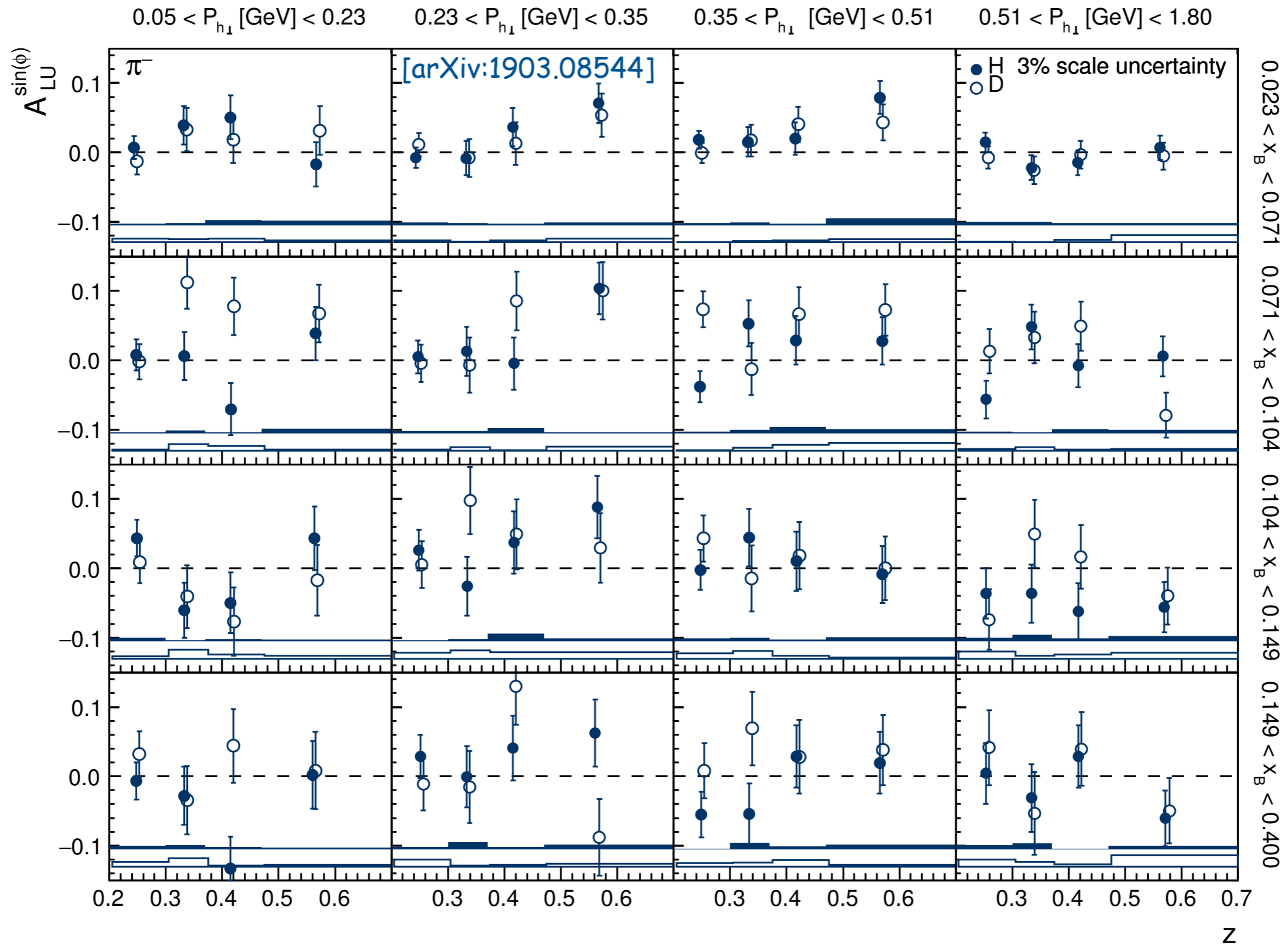
multi-d dependences

- in analysis, implement data-driven model^{*)} into Monte Carlo
- analyzed like real data
- difference between input model evaluated at average kinematics and extracted MC asymmetry in each bin assigned as systematic uncertainty

^{*)} first terms in Taylor expansion in kinematic variables
fit to data in unbinned max. likelihood fit

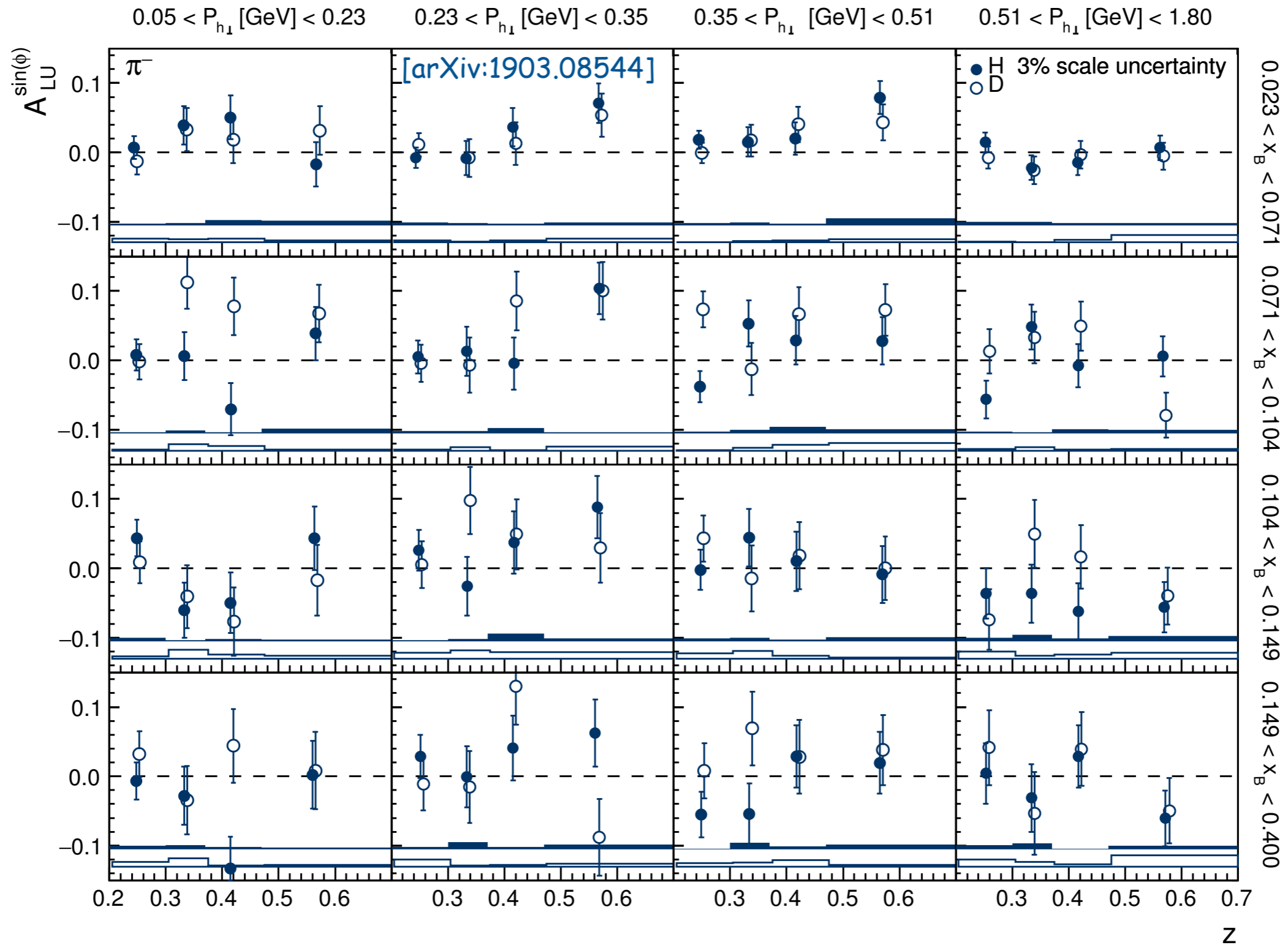
results

3d beam-helicity asymmetry for π^-



● full 1996-2007 data set; precision driven by statistical uncertainty

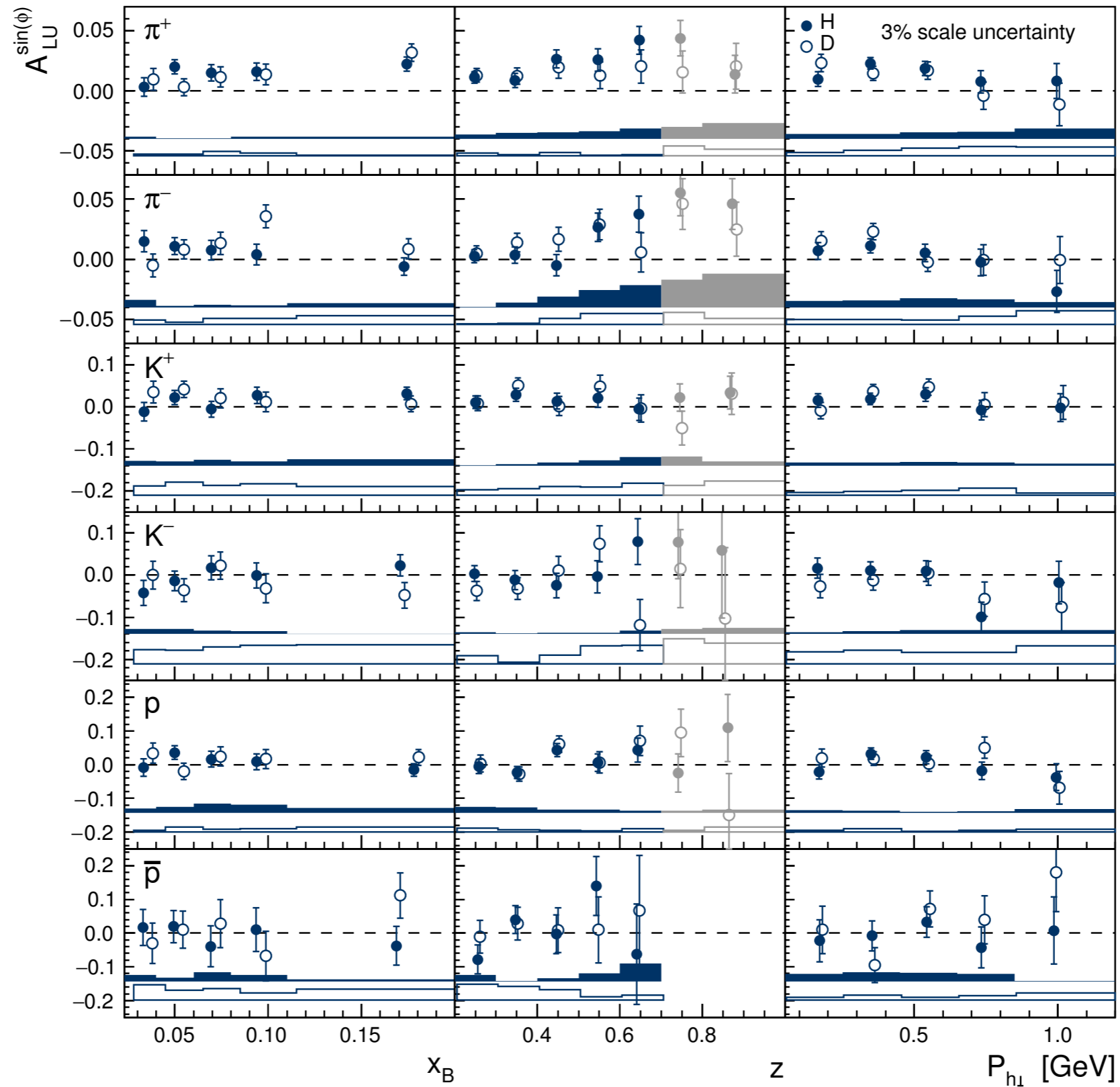
3d beam-helicity asymmetry for π^-



● most comprehensive presentation, for discussion use 1d binning

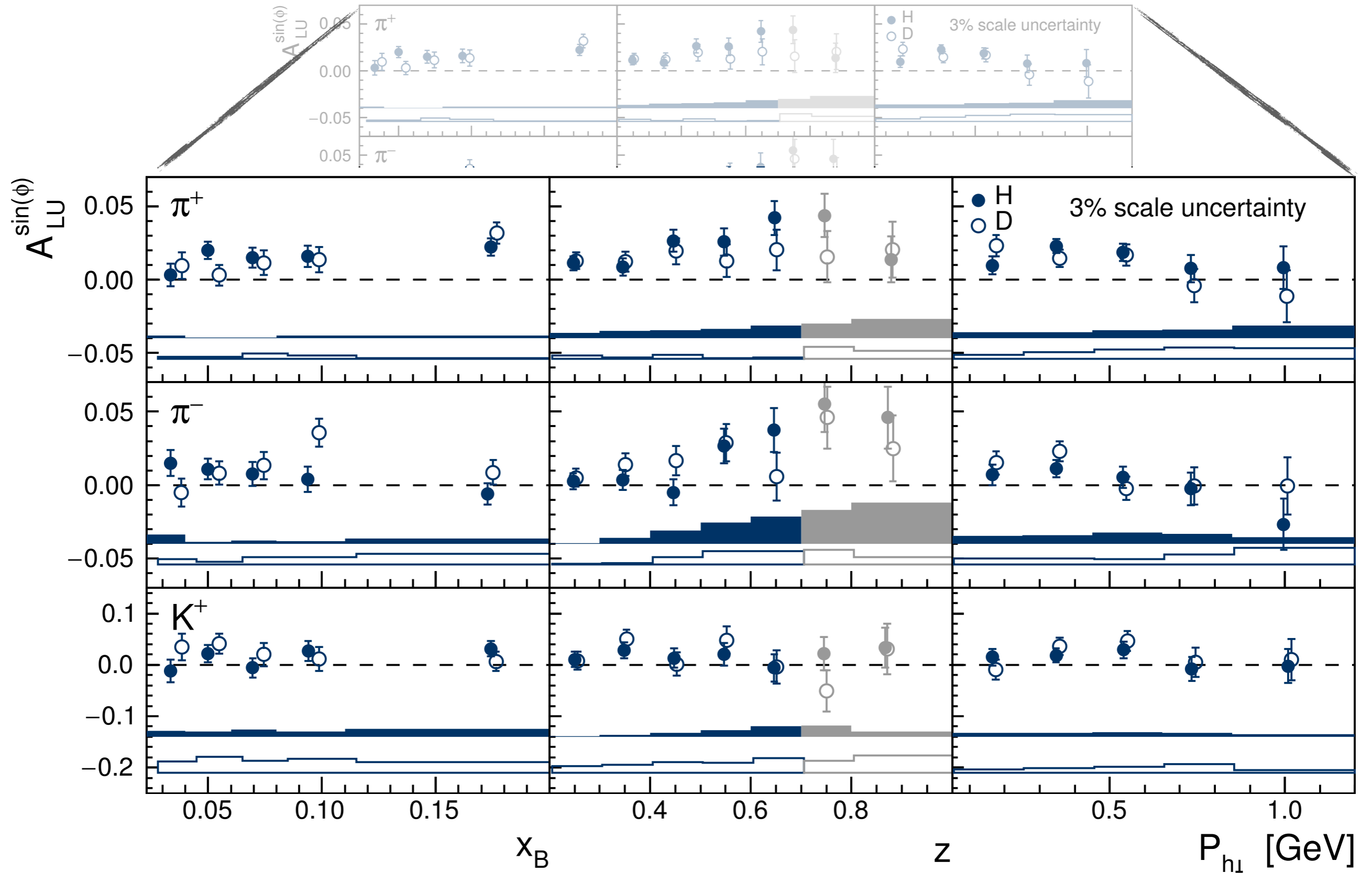
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[arXiv:1903.08544]



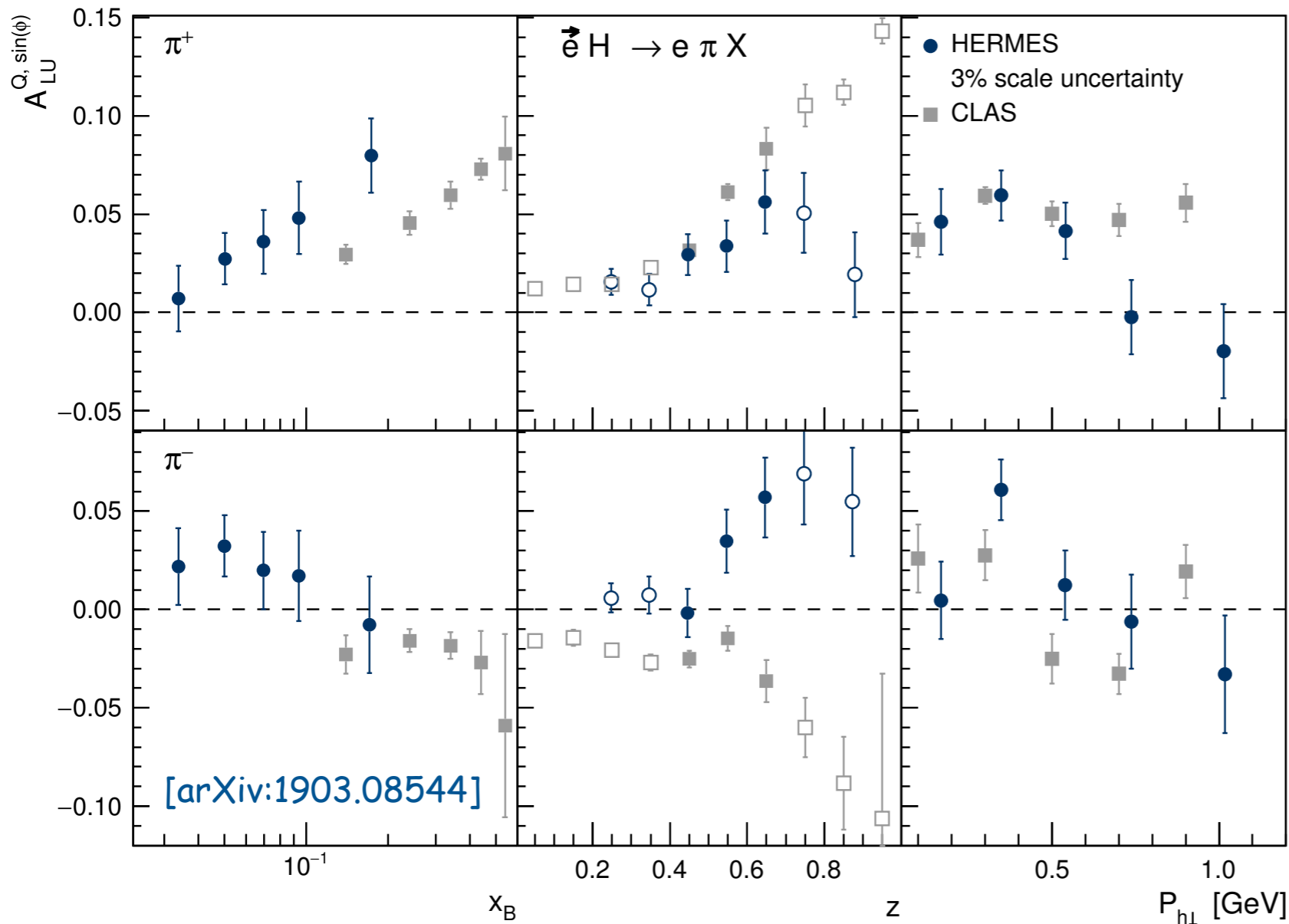
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HERMES - CLAS comparison

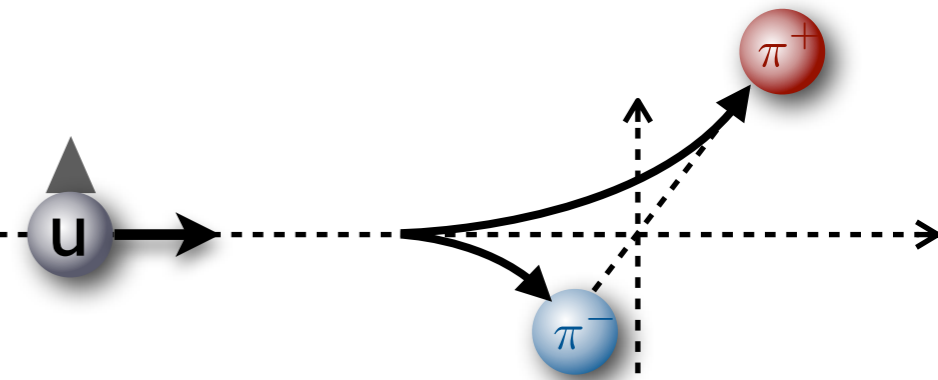
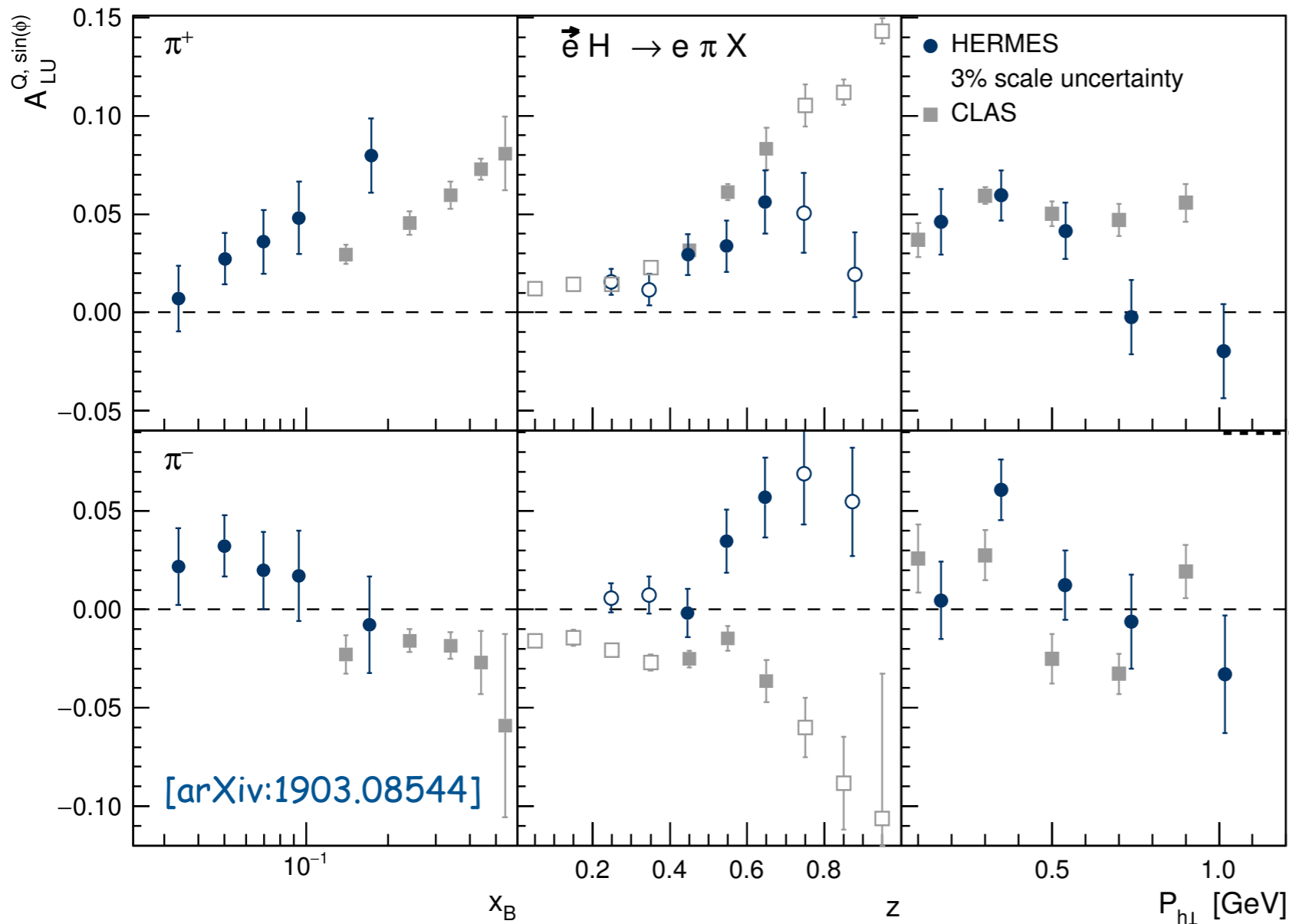
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- opposite behavior at HERMES/CLAS of negative pions in z projection due to different x -range probed

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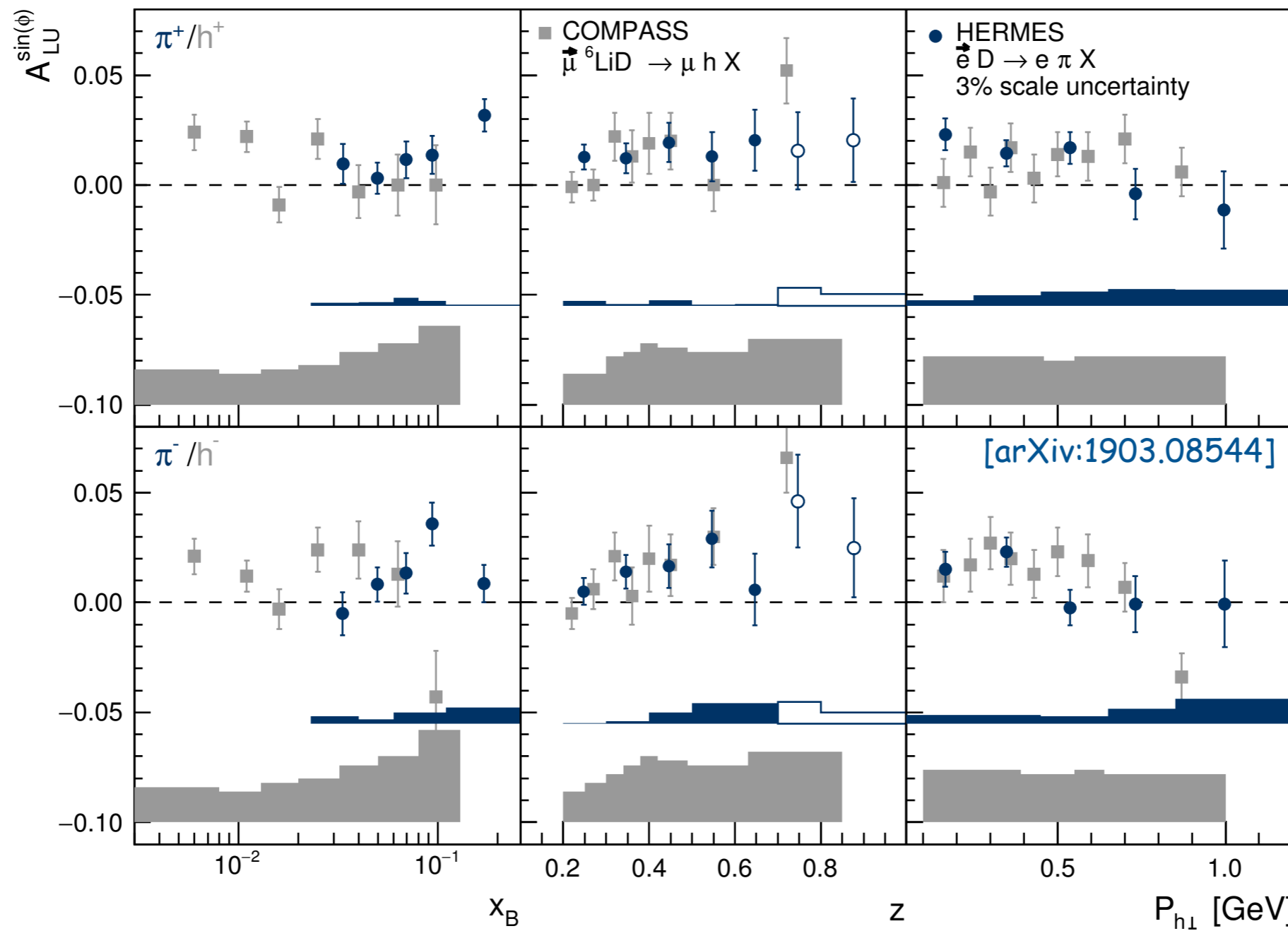
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- opposite behavior at HERMES/CLAS of negative pions in z projection due to different x -range probed
- CLAS more sensitive to $e(x)$ Collins term due to higher x probed?

HERMES - COMPASS comparison

$$\frac{M_h}{M_z} h_1^\perp \tilde{E} \oplus x g^\perp D_1 \oplus \frac{M_h}{M_z} f_1 \tilde{G}^\perp \oplus x e H_1^\perp$$



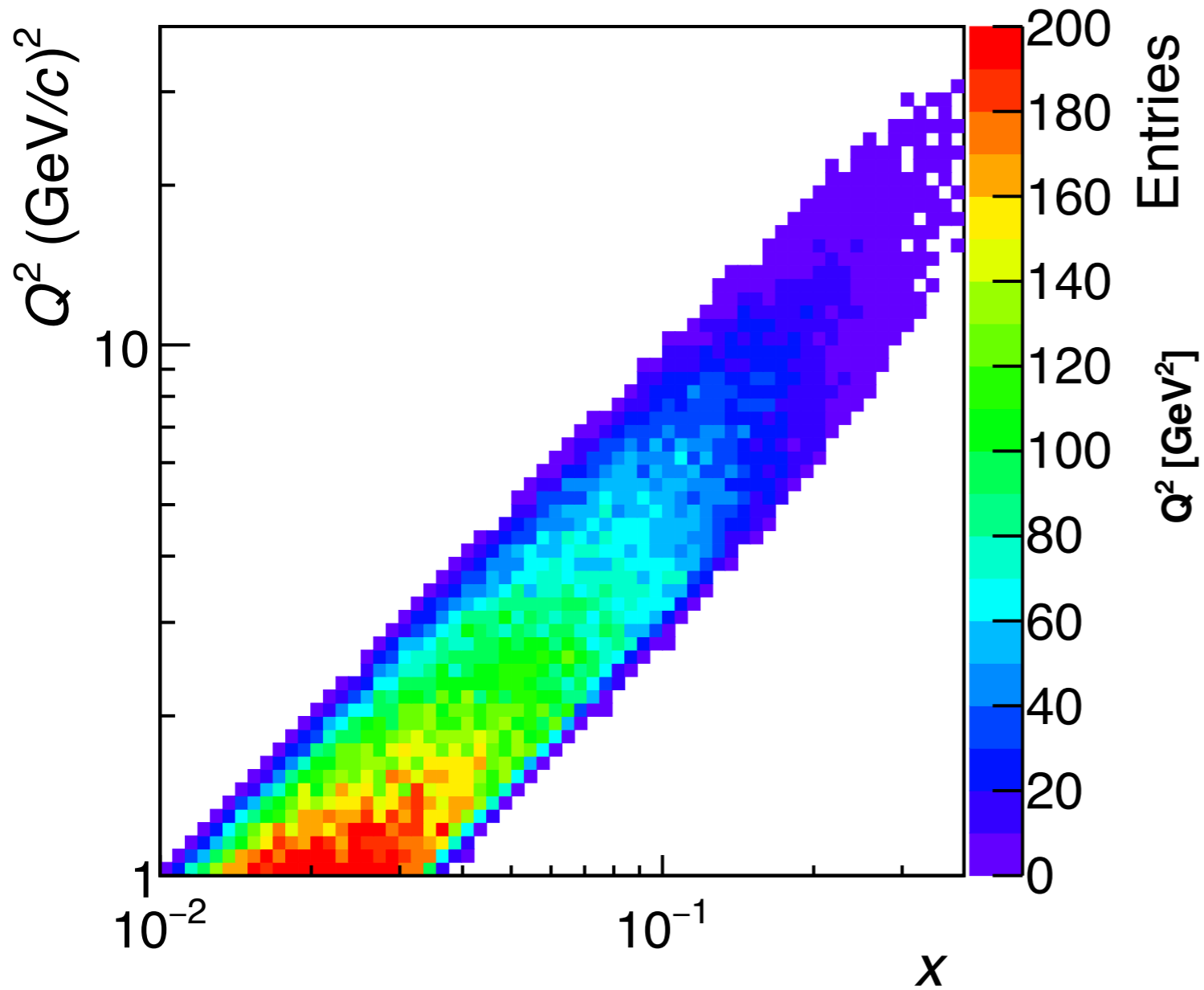
- consistent behavior for charged pions / hadrons at HERMES / COMPASS for isoscalar targets

conclusions

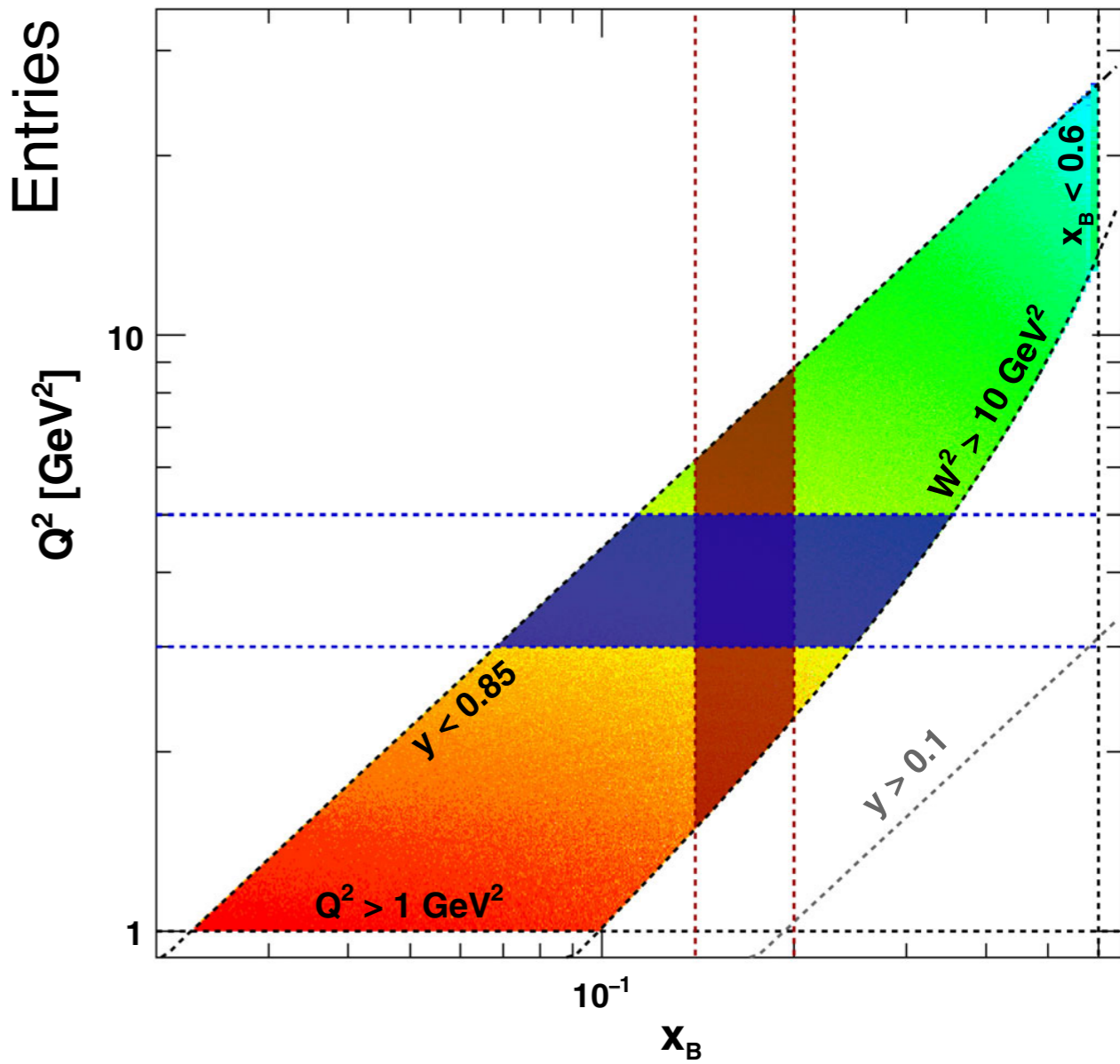
- clearly non-zero beam-helicity asymmetries observed for charged pions and K^+
- sizable twist-3 effects, in contrast to WW-type approx.
- intriguing kinematic dependences might shed light at different roles of the various terms contributing
- high- x behavior might be driven by TMD e & Collins FF
- COMPASS and HERMES in agreement despite different Q^2 ranges probed
- (not shown:) $\sin 2\phi$ asymmetry, which could arise from 2-photon exchange, found to be consistent with zero

backup

kinematic coverage



● COMPASS



● HERMES