# ABM update

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## PDF fit framework



## Higher twists: generalities

10 5 Operator product expansion:  $Q^2 (GeV^2)$ HERA • BCDMS  $F_{2,T} = F_{2,T}$  (leading twist) +  $H_{2,T}(x)/Q^2$  + ... – additive • NMC 10 SLAC  $F_{2,T} = F_{2,T}$  (leading twist)  $(1 + h_{2,T}(x)/Q^2 + ...)$  $W^2 = 12.5 \text{ GeV}^2$ 10<sup>3</sup>  $- Q^2 = 10 \text{ GeV}^2$ multiplicative The only one in accordance with QCD 10 For multiplicative form the LT anomalous dimensions strongly affect the HT terms at small x 10  $F_2(x,Q^2)$ 10 10 10 ١Ō Hydroger Deuterium 10 △ SLAC △ SLAC O BCDMS BCDMS  $Q^{2} (GeV/c)^{2}$ 1 10 10  $Q^{2} (GeV/c)^{2}$ 

Virchaux, Milsztajn PLB 274, 221 (1992)

Х



sa, Blümlein, Moch, Plačakytė PRD 96, 014011 (2017)

•  $H_{r}(x)$  continues a trend observed at larger x;  $H_{r}(x)$  is comparable to 0 at small x

• h\_=0.05 $\pm$ 0.07  $\rightarrow$  slow vanishing at x  $\rightarrow$  0

• No dramatic increase of F<sub>L</sub> at small x: different from the study with multiplicative form of HTs Abt et. al. hep-ph/1604.02229

 Alternative explanations are available in literature: resummation, saturation, etc.



# Higher twists: correlation with $\alpha_s$



- $\bullet$  The value of  $\boldsymbol{\alpha}_s$  and twist-4 terms are strongly correlated
- With HT=0 the errors are reduced → no uncertainty due to HTs
- With account of the HT terms the value of  $\alpha_s$  is stable with respect to the cuts

fit	$\alpha_s(M_Z)$		
higher twist modeling	cuts on DIS data	NLO	NNLO
higher twist fitted	$Q^2 > 2.5 \text{ GeV}^2, W > 1.8 \text{ GeV}$	0.1191(11)	0.1147(8)
higher twist fixed at 0	$Q^2 > 10 \text{ GeV}^2, W^2 > 12.5 \text{ GeV}^2$	0.1212(9)	0.1153(8)
	$Q^2 > 15 \text{ GeV}^2, W^2 > 12.5 \text{ GeV}^2$	0.1201(11)	0.1141(10)
	$Q^2 > 25 \text{ GeV}^2, W^2 > 12.5 \text{ GeV}^2$	0.1208(13)	0.1138(11)

sa, Blümlein, Moch EPJC 78, 477 (2018)

MRST:  $\alpha_{s}(M_{z})=0.1153(20)$  (NNLO) (W<sup>2</sup>>15 GeV<sup>2</sup>, Q<sup>2</sup>> 10 GeV<sup>2</sup>)

A stringent cut on Q is necessary for the fit with HT=0

Moch et al. hep-ph/1405.4781



## Higher twists: fit with stringent cut on Q,W

2 ...

	χ²/NL	JP
	HT fitted Q <sup>2</sup> >2.5 GeV <sup>2</sup> , W>1.8 GeV	HT=0, Q <sup>2</sup> >10 GeV <sup>2</sup> , W <sup>2</sup> >12.5 GeV <sup>2</sup>
HERA	1510/1168	1220/1007
Fixed target: SLAC, NMC,BCDMS	1145/1008	498/444

Value of  $\chi^2$  is stable w.r.t. to cuts



Stringent cut affects high-x data, however, the large-x PDF uncertainties remain stable

## HERA charm data and m

HERA I+II (ep --> e charm X) Theory: FFN scheme, running mass data/fit-1 definition (cf. talk afternoon) 0.4 0.2 -0.2 m\_(m\_)=1.245±0.019(exp.) GeV  $O^2 = 5 GeV^2$  $O^2 = 2.5 \text{ GeV}^2$  $O^2 = 7 \text{ GeV}^2$ -0.4present analysis 0.4 0.2 m\_(m\_)=1.252±0.018(exp.) GeV 0 -0.2ABMP16  $O^2 = 18 \text{ GeV}^2$  $O^2 = 12 \text{ GeV}^2$  $O^2 = 32 \text{ GeV}^2$ -0.4m (pole)~1.9 GeV (NNLO) 0.4 Marguard et al. PRL 114, 142002 (2015) 0.2 0 m\_(m\_)=1.246±0.023 (h.o.) GeV NNLO -0.2 $Q^2 = 60 \text{ GeV}^2$  $O^2 = 120 \text{ GeV}^2$  $O^2 = 200 \text{ GeV}^2$ -0.4Kiyo, Mishima, Sumino PLB 752, 122 (2016) 0.4 0.2 m<sub>(m)</sub>=1.279±0.008 GeV 0 Kühn, LoopsLegs2018 -0.2 $O^2 = 650 \text{ GeV}^2$  $=350 \text{ GeV}^2$  $O^2 = 2000 \text{ GeV}^2$ -0.4 10<sup>-4</sup> 10<sup>-3</sup>  $10^{-2}$  $10^{-2}$  $10^{-3}$  $10^{-2}$  $10^{-3}$  $10^{-4}$  $10^{-4}$ Good consistency with the earlier results Х X Х and other determinations  $\rightarrow$  further X<sup>2</sup>/NDP=86/52

confirmation of the FFN scheme relevance for the HERA kinematics

H1, ZEUS EPJC 78, 473 (2018)

## HERA beauty data and m



X<sup>2</sup>/NDP=36/27

Improved agreement with other determinations, evidently due to data purification

## Impact of stringent cut on PDFs at small x



Gluon goes higher, consistent with the constraint from charm/beauty

Strange sea goes lower at small x, consistent with 1 within errors  $\rightarrow$  SU(3) symmetry

## t-quark: pair production



Running t-quark mass can be determined simultaneously\*\*
m<sub>t</sub>(m<sub>t</sub>)= 160.8±1.1 GeV
m<sub>t</sub>(pole)=170.4±1.2 GeV
m<sub>t</sub>(MC)~172.5 GeV from LHC

(Hoang et al. try to quantify the difference)

\*\* Running-mass definition provides better perturbative stability (Extras)

## t-quark: single production (mass determination)



#### $m_t(m_t) = 161.1 \pm 3.8 \text{GeV}$ (single-top only)

sa, Moch, Thier PLB 763, 341 (2016)

Channel	ABM12 21	ABMP15 52	CT14 55	MMHT14 56	NNPDF3.0 57
tī	$158.6\pm0.6$	$158.4\pm0.6$	$164.7\pm0.6$	$164.6\pm0.6$	$164.3 \pm 0.6$
t-channel	$158.7\pm3.7$	$158.0\pm3.7$	$160.1\pm3.8$	$160.5 \pm 3.8$	$164.0 \pm 3.8$
s- & t-channel	$158.4\pm3.3$	$157.7 \pm 3.3$	$159.1 \pm 3.4$	$159.6 \pm 3.4$	$162.4 \pm 3.5$

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## t-quark: single production (flavour separation)



• The single-top data are sensitive to the u/d ratio, however in general they are not competitive with the DY constraints

 The only window opens when the hadronization MC is fixed and the modeling errors cancel in the ratio → model dependent result

• The comparison can be also inverted in order to discriminate hadronization models

Small errors due to cancellation of theor. unc. in case the MC version is fixed; they are much larger if different MCs are considered

## Data set used for study of impact PDF shape on $\alpha_{a}$

sa, Blümlein, Moch PLB 777, 134 (2018) sa, Blümlein, Kulagin, Moch, Petti hep-ph/1808.06871

Experiment	Process	NDP
DIS		
HERA I+II	$e^{\pm}p \rightarrow e^{\pm}X$	1168
	$e^{\pm}p \rightarrow \overset{(-)}{\nu}X$	
Fixed-target (BCDMS, NMC, SLAC)	$l^{\pm}p \to l^{\pm}X$	1935

#### **DIS heavy-quark production**

HERA I+II	$e^{\pm}p \rightarrow e^{\pm}cX$	52
H1, ZEUS	$e^{\pm}p \rightarrow e^{\pm}bX$	29
Fixed-target (CCFR, CHORUS, NOMAD, NuTeV)	${\overset{(-)}{\nu}}N \to \mu^{\pm}cX$	232

#### DY

Fixed-target (FNAL-605, FNAL-866)	$pN \rightarrow \mu^+ \mu^- X$	158
-	1	

#### The ABMP16 framework with:

 DY data replaced by the deuteron ones ⇒ comparable quark disentangling at moderate and large x

- t-quark data excluded (no relevance for the first round of estimates)



DY data have no essential impact on  $\alpha_s$ 

# Checking styles of PDF shape

	ABMP16	CJ15	CT10	CT14	epWZ16	MMHT14
N <sub>pdf</sub>	28	21	26	26	14	31
$\mu_0^{2}$ (GeV <sup>2</sup> )	9	1.69	1.69	1.69	1.9	1
χ <sup>2</sup>	4065	4108	4148	4153	4336	4048
PDF shape	$x^{\alpha}(1-x)^{\beta}$ exp[P(x,ln(x))]	x <sup>α</sup> (1-x) <sup>β</sup> P(x,√x)	$x^{\alpha}(1-x)^{\beta}$ exp[P(x, $\sqrt{x}$ )]	$x^{\alpha}(1-x)^{\beta}$ exp[P(x, $\sqrt{x}$ )]	x <sup>α</sup> (1-x) <sup>β</sup> P(x,√x)	x <sup>α</sup> (1-x) <sup>β</sup> P(x,√x)
Constraints		ū=đ (x→0)	$\alpha_{uv} = \alpha_{dv}$ $\alpha_{\bar{u}} = \alpha_{\bar{d}} = \alpha_{s}$ $\bar{u} = \bar{d}  (x \to 0)$	$\alpha_{uv} = \alpha_{dv}$ $\beta_{uv} = \beta_{dv}$ $\alpha_{u} = \alpha_{d} = \alpha_{s}$	$\alpha_{\bar{u}} = \alpha_{\bar{d}} = \alpha_{\bar{s}}$ $\bar{u} = \bar{d} (x \rightarrow 0)$	
$\alpha_{s}(M_{z})$	0.1153	0.1147	0.1150	0.1160	0.1162	0.1158

• Various PDF-shape modifications provide comparable description with  $N_{PDF} \sim 30$ 

 Some deterioration, which happens in cases is apparently due to constraints on large(small)-x exponents

Conservative estimate of uncertainty in  $\alpha_{s}(M_{r})$ : 0.0007, more optimistic: 0.0003

## DY: data used in the ABMP16 fit

Exp	periment	ATI	LAS	CN	MS	D	Ø	LHCb		
$\sqrt{s}$	s (TeV)	7	13	7	8	1.	96	7	7 8	
Fina	al states	$W^+ \rightarrow l^+ \nu$	$W^+ \rightarrow l^+ \nu$	$W^+ \rightarrow \mu^+ \nu$	$W^+ \rightarrow \mu^+ \nu$	$W^+ \rightarrow \mu^+ \nu$	$W^+ \rightarrow e^+ \nu$	$W^+ \rightarrow \mu^+ \nu$	$Z \rightarrow e^+ e^-$	$W^+ \rightarrow \mu^+ \nu$
		$W^- \rightarrow l^- \nu$	$W^- \rightarrow l^- \nu$	$W^- \rightarrow \mu^- \nu$	$W^- \rightarrow \mu^- \nu$	$W^- \rightarrow \mu^- \nu$	$W^- \rightarrow e^- v$	$W^- \rightarrow \mu^- \nu$		$W^- \rightarrow \mu^- \nu$
		$Z \rightarrow l^+ l^-$	$Z \rightarrow l^+ l^-$	(asym)		(asym)	(asym)	$Z \rightarrow \mu^+ \mu^-$		$Z \rightarrow \mu^+ \mu^-$
Cut on t	he lepton $P_T$	$P_T^l > 20 \text{ GeV}$	$P_T^e > 25 \text{ GeV}$	$P_T^{\mu} > 25 \text{ GeV}$	$P_T^{\mu} > 25 \text{ GeV}$	$P_T^{\mu} > 25 \text{ GeV}$	$P_T^e > 25 \text{ GeV}$	$P_T^{\mu} > 20 \text{ GeV}$	$P_T^e > 20 \text{ GeV}$	$P_T^{\mu} > 20 \text{ GeV}$
Lumin	osity (1/fb)	0.035	0.081	4.7	18.8	7.3	9.7	1	2	2.9
1	<i>NDP</i>	30	6	11	22	10	13	31(33) <sup>a</sup>	17	32(34)
	ABMP16	31.0	9.2	22.4	16.5	17.6	19.0	45.1(54.4)	21.7	40.0(59.2)
	CJ15	-	-	-	-	20	29	-	—	-
	CT14	42	_	_ <sup>b</sup>	-	-	34.7	_	_	_
	HERAFitter	-	—	-	-	13	19	—	-	—
	MMHT16	39 <sup>c</sup>	-	-	21	21 <sup>c</sup>	26	(43)	29	(59)
	NNPDF3.1	29	—	19	-	16	35	(59)	19	(47)

<sup>*a*</sup> The values of NDP and  $\chi^2$  correspond to the unfiltered samples. <sup>*b*</sup> For the statistically less significant data with the cut of  $P_T^{\mu} > 35$  GeV the value of  $\chi^2 = 12.1$  was obtained. <sup>*c*</sup> The value obtained in MMHT14 fit.

Experiment	NDP	$\chi^2$ after the data sets excuded					
		—	ATLAS	CMS	DØ	LHCb	
ATLAS	36	37.7	—	37.0	38.3	39.6	
CMS	33	26.6	25.6	_	26.0	23.5	
DØ	23	48.5	48.1	47.7	_	44.2	
LHCb	80	98.2	100.2	97.4	78.8	_	

Good overall agreement in NNLO with some tension between D0 and LHCb data

## New input: ATLAS at 7 TeV

ATLAS (7 TeV)



W±, Z(central),

Z(forward)

84/43

 Different trends for the central and forward Z-boson data

## DY: impact of the recent data (ATLAS, 5 TEV)



PRELIMINARY: Uncertainty correlations are not taken into account (still unpublished); smaller impact on fit is expected when they are included

## DY: towards double differential distributions



Reasonable agreement with the ABMP16 predictions

- Complimentary constraint on PDFs → improved quark disentangling
- Other CMS and ATLAS data in progress; the bottleneck is NNLO computations with the fiducial-volume cuts

## Summary

- The fit with stringent cuts, W<sup>2</sup>>12.5 GeV<sup>2</sup>, Q<sup>2</sup>> 10 GeV<sup>2</sup>, on the DIS data is considered
  - impact of the higher-twist terms is minimized
  - small-x gluon goes higher, consistent with the constraint from charm/beauty; small-x strange sea goes lower at small x, consistent with 1 within errors; valence quarks stable
  - reasonable description of the recent charm/beauty HERA data with  $m_c(m_c)=1.245\pm0.019(exp.)$  GeV  $m_b(m_b)=3.96\pm0.10(exp.)$  GeV
- Update of the pair- and single-top production with

 $m_t(m_t) = 160.8 \pm 1.1 \text{ GeV}$  $m_t(m_t) = 161.1 \pm 3.8 \text{GeV}$  (single-top only)

- potential impact on the d/u ratio form t/tbar, however validation of MC tools is still needed
- Steady progress with accommodating more DY data into the fit
  - recent ATLAS data at 5 and 7 Tev
  - double differential data on Z-boson production from CMS and ATLAS

# EXTRAS

## Impact of high twists on SLAC data



Power-like terms affect comparison even with a cut  $W^2 \ge 12.5 \text{ GeV}^2$ 

## Impact of the t-quark data on the ABMP16 fit



HATHOR (NNLO terms are checked with TOP++)

Langenfeld, Moch, Uwer PRD 80, 054009 (2009)

Running mass definition provides nice perturbative stability Czakon, Fiedler, Mitov PRL 110, 252004 (2013)



## NNLO tools benchmarking



DYNNLO-FEWZ difference not fully understood; further benchmarking is needed



## Closure test of the NNPDF3.1 fit



• Different trend for W and Z data  $\Rightarrow \chi^2/NDP=400/34$ ; problems with the flavor disentangling

 Suppressed (fitted) charm distribution requires corresponding enhancement of strangeness sur to constraint from W data Thorne QCD@LHC2018

### DY: ATLAS versus CMS



## NNLO DY corrections in the fit

The existing NNLO codes (DYNNLO, FEWZ) are quite time-consuming  $\rightarrow$  fast tools are employed (FASTNLO, Applgrid,....)

- the corrections for certain basis of PDFs are stored in the grid
- the fitted PDFs are expanded over the basis
- the NNLO c.s. in the PDF fit is calculated as a combination of expansion coefficients with the pre-prepared grids

The general PDF basis is not necessary since the PDFs are already constrained by the data, which do not require involved computations  $\rightarrow$  use as a PDF basis the eigenvalue PDF sets obtained in the earlier version of the fit

- $\mathbf{P}_{0} \pm \Delta \mathbf{P}_{0}$  vector of PDF parameters with errors obtained in the earlier fit
- **E** error matrix
- $\mathbf{P}$  current value of the PDF parameters in the fit
- store the DY NNLO c.s. for all PDF sets defined by the eigenvectors of E
- the variation of the fitted PDF parameters  $(\mathbf{P} \mathbf{P}_0)$  is transformed into this eigenvector basis
- the NNLO c.s. in the PDF fit is calculated as a combination of transformed ( $\mathbf{P} \mathbf{P}_0$ ) with the stored eigenvector values

## DY: tool benchamrking

![](_page_27_Figure_1.jpeg)

A variety of tools/methods employed in the PDF fits: DYNNO/FEWZ/ResBos, NLO combined with NNLO K-factors, etc.  $\rightarrow$  a consolidation is required for using potential of the existing data.

## Test fit with the neural network shape

![](_page_28_Figure_1.jpeg)

• Valence u-quark is modeled by  $x^{\alpha}(1-x)^{\beta}NN(x)$ , where NN is neural network with 37 parameters (NNPDF3.0 ansatz), other PDFs use MMHT14 shape

- Result is in quite agreement with the MMHT14 shape  $x^{\alpha}(1-x)^{\beta}P(x)$  with 4 paramters in  $P(x) \Rightarrow$  no particular flexibility is provided by neural network
- Study of sea and gluon distribution in progress, the same behaviour expected