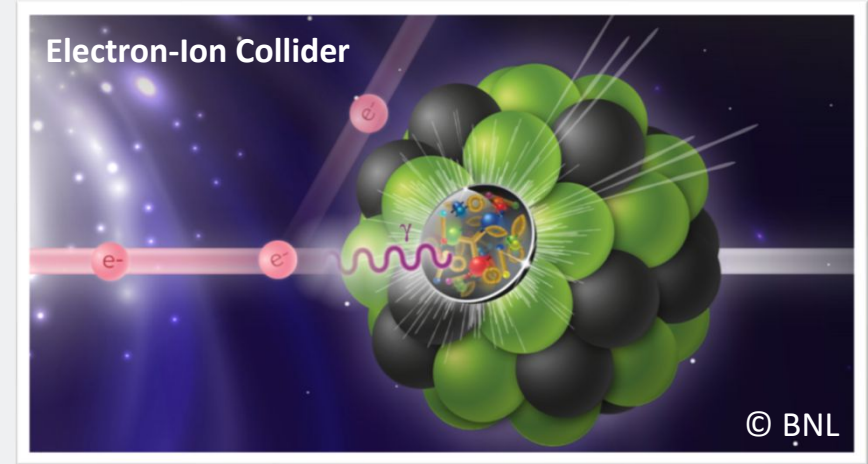
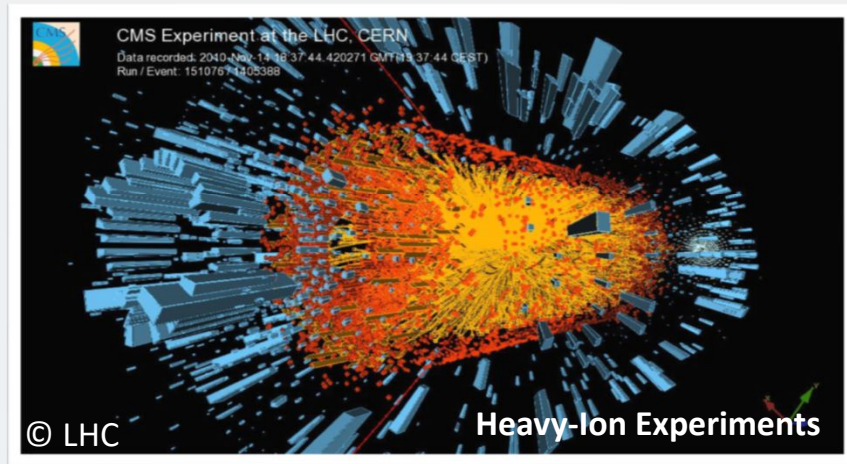


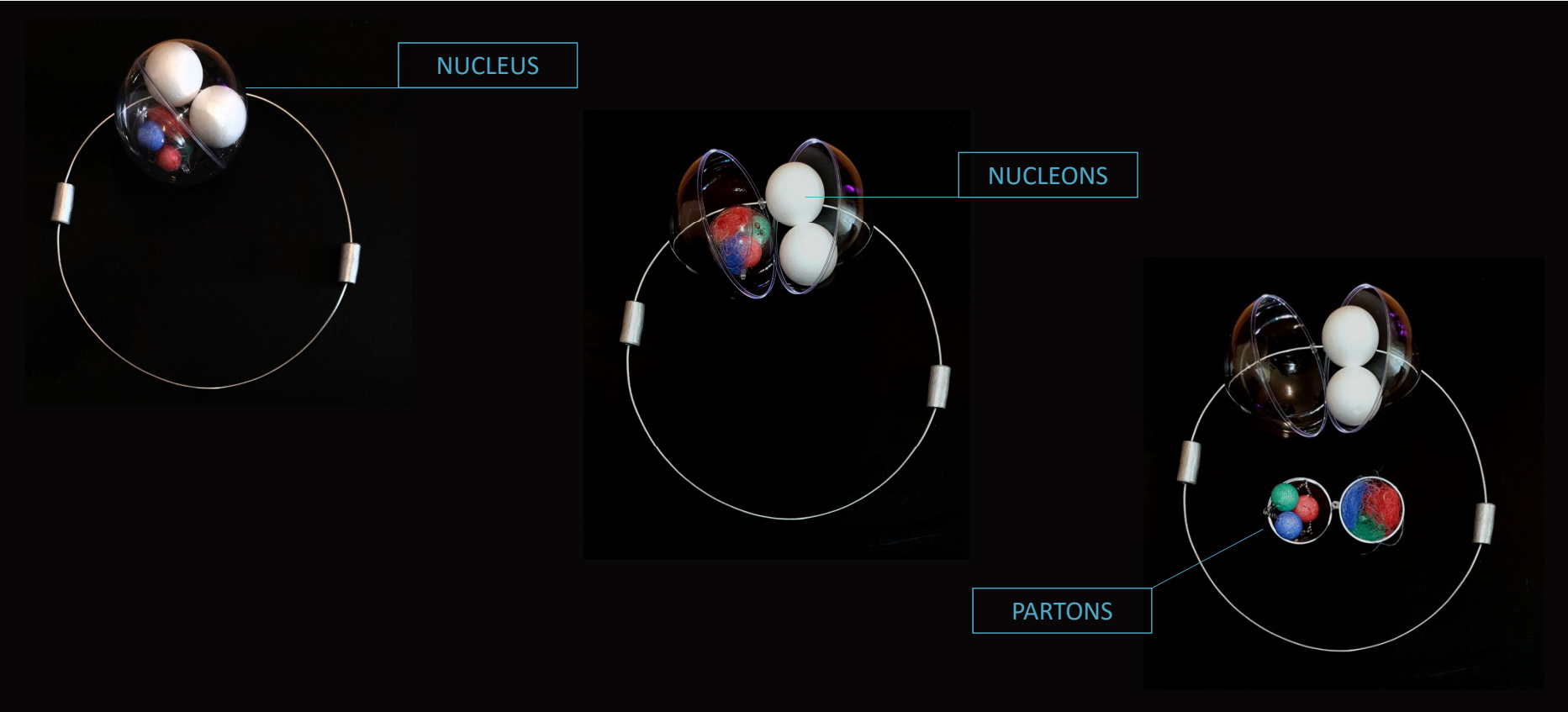


# A QCD analysis for nuclear PDFs at NNLO

MARINA WALT,

In collaboration with Ilkka Helenius, Werner Vogelsang

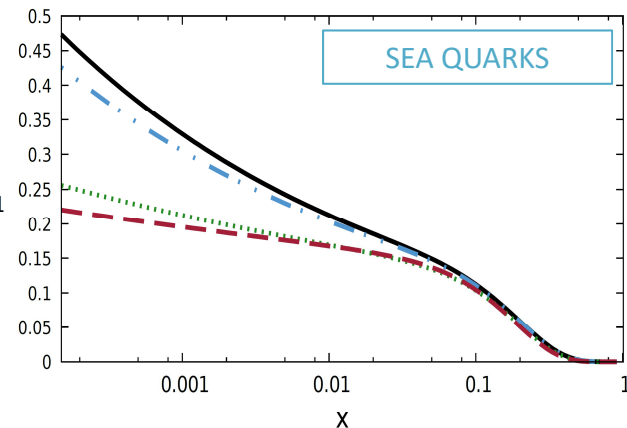
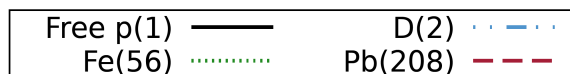
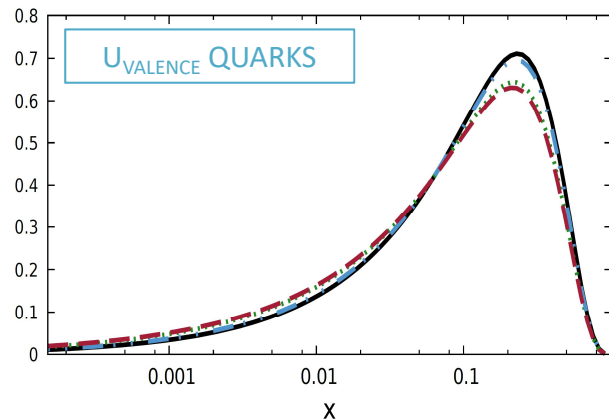
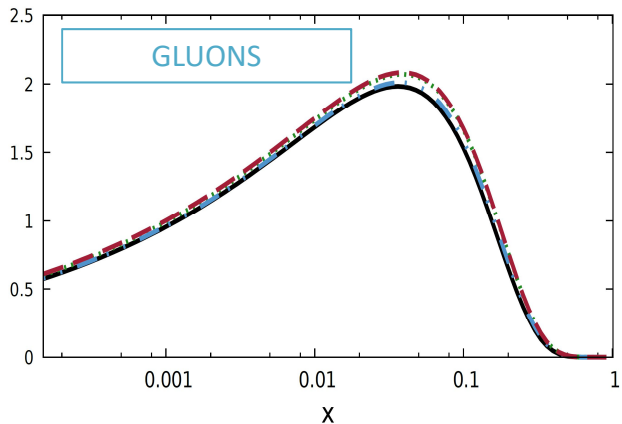




# NNLO RESULTS – NUCLEAR PDFs

nPDFs at initial scale  $Q_0^2=1.69 \text{ GeV}^2$ :

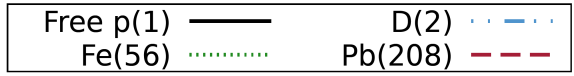
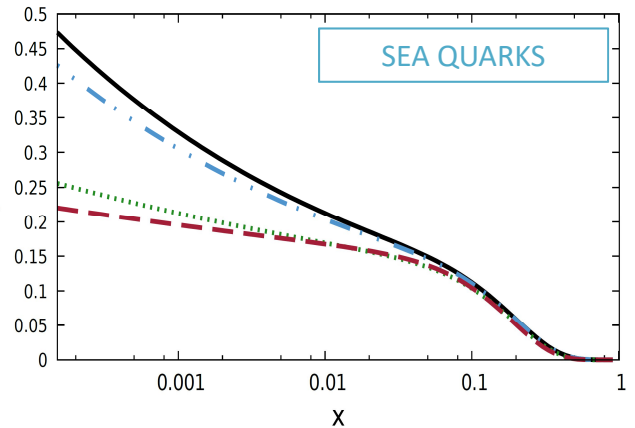
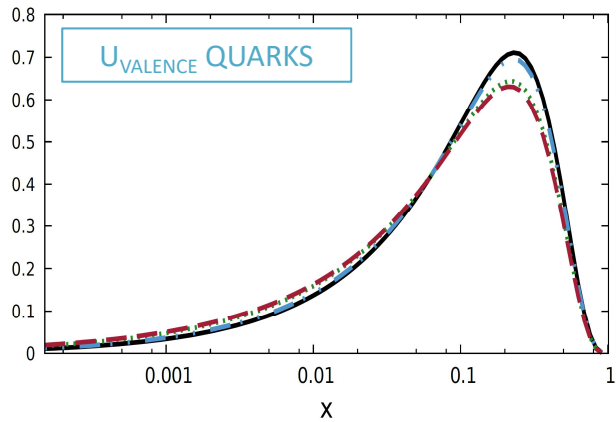
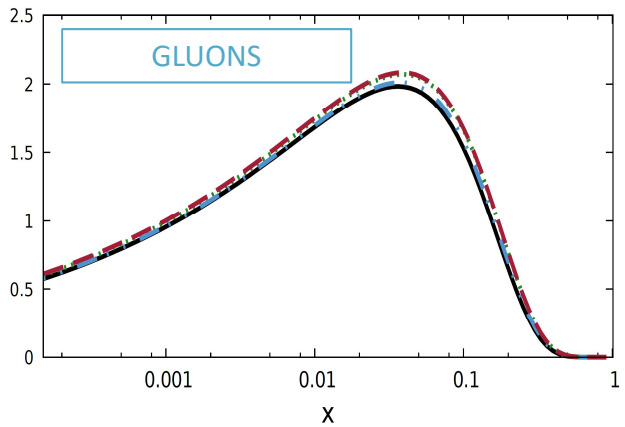
$$d\sigma^{\ell A} = \sum_i f(x, Q^2)_i \otimes d\sigma_i^{\text{part}}$$



# NNLO RESULTS – NUCLEAR PDFs

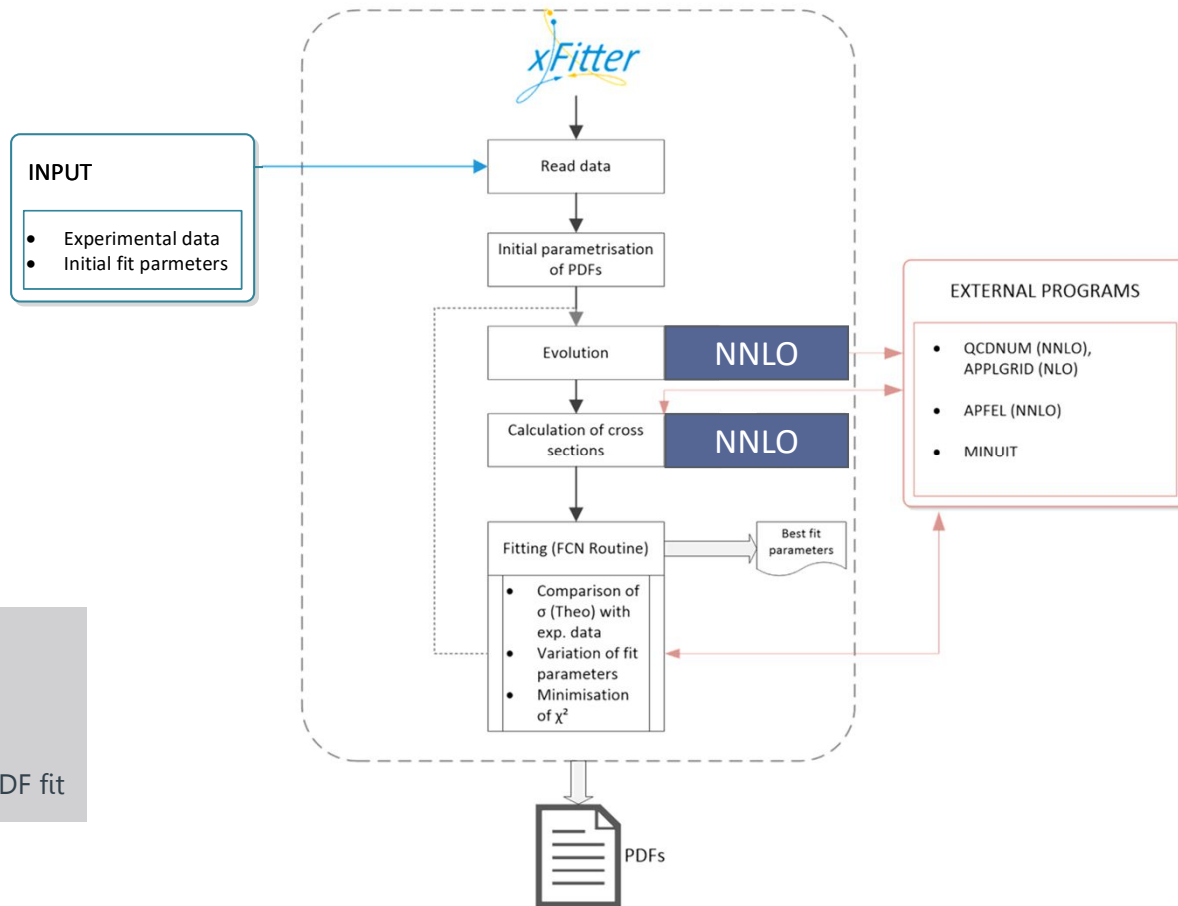
Preliminary NNLO nPDFs

nPDFs at initial scale  $Q_0^2=1.69 \text{ GeV}^2$ :





# ANALYSIS PROCEDURE AT NNLO



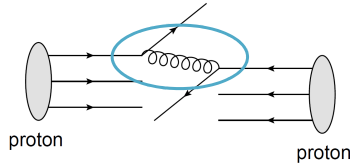
xFitter

xFitter modifications  
required for nuclear PDF fit

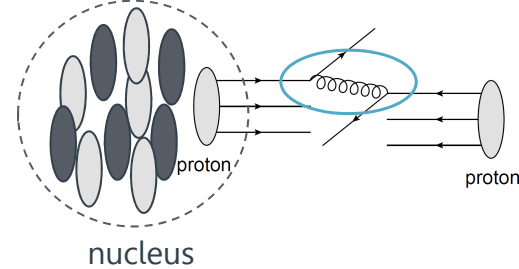


# FREE PROTON PDFs VS. NUCLEAR PDFs

Free proton:



Nucleus:



$$x f_i^{p/A}(x, Q_0^2) = c_0 x^{c_1} (1-x)^{c_2} (1 + c_3 x + c_4 x^2)$$

$$c_k \rightarrow c_k(A) := c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}})$$



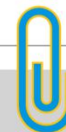
PDFType=,nucleus'  
(A=1, Z=1 for proton)



[HERAPDF2.0:  
Eur.Phys.J. C75 (2015) no.12, 580]

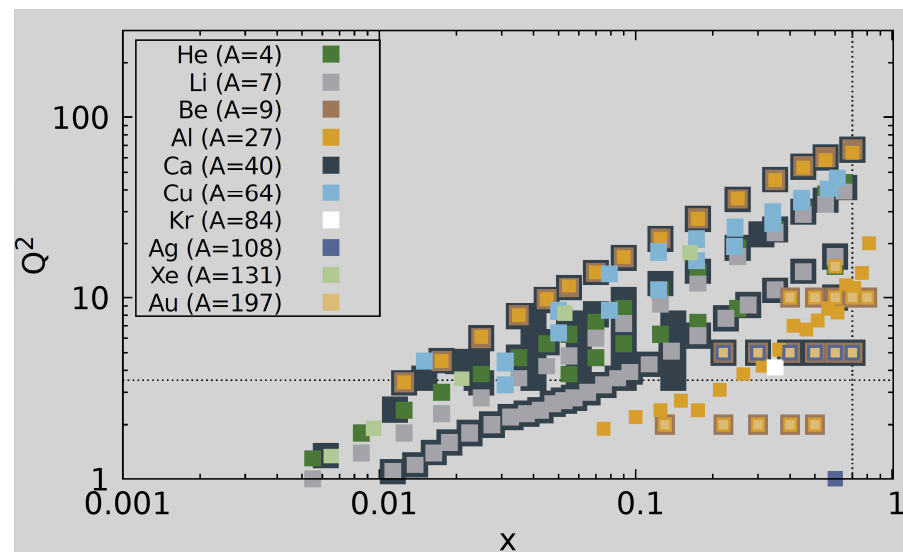
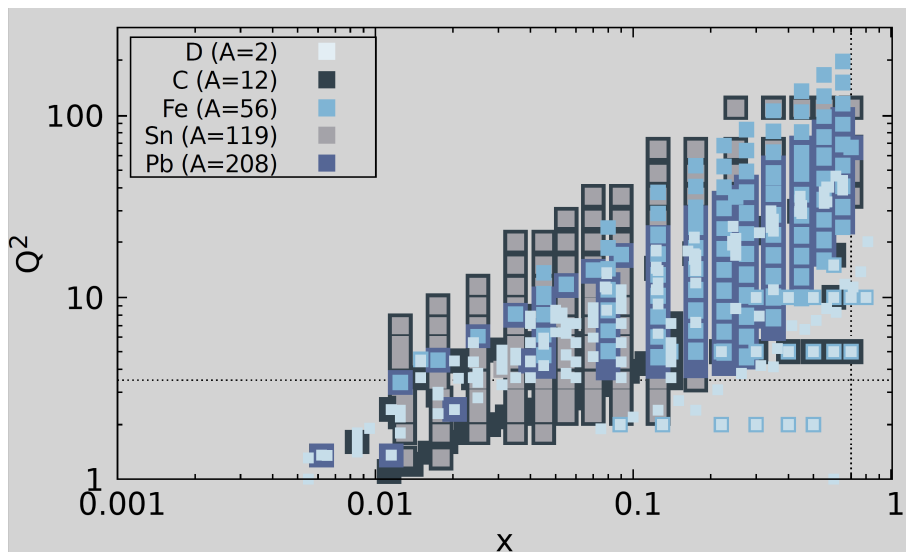


[nCTEQ: PRD 93, 085037 (2016)]



A dependent coefficients

$$c_k \rightarrow c_k(A) := c_{k,0} + c_{k,1} (1 - A^{-c_{k,2}})$$

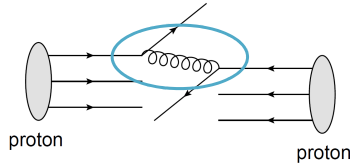


Used nuclear DIS data: neutral current DIS and charged current neutrino DIS data.



# FREE PROTON PDFs VS. NUCLEAR PDFs

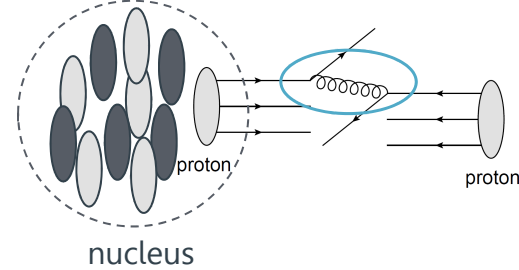
Free proton:



→ PDF of a **free** proton

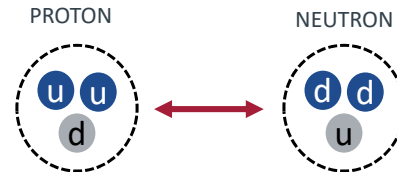
$$f^p(Q^2, x)$$

Nucleus:



→ PDF of a **bound** nucleon

$$f^A = \frac{Z}{A} f^{p/A} + \frac{(A-Z)}{A} f^{n/A}$$

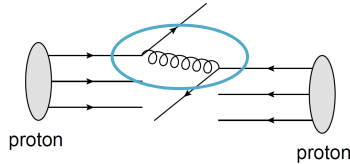


PDF decomposition of a bound nucleon.



# FREE PROTON PDFs VS. NUCLEAR PDFs

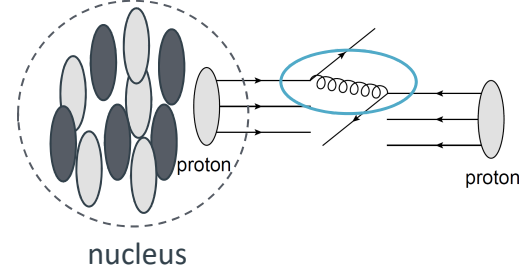
Free proton:



→ PDF of a **free** proton

$$f^p(Q^2, x)$$

Nucleus:



→ PDF of a **bound** nucleon

$$f^A = \frac{Z}{A} f^{p/A} + \frac{(A-Z)}{A} f^{n/A}$$

If  $Z \neq \frac{A}{2}$  → **isoscalar corrections** applied by experiments become relevant.

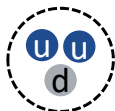


Flags for isoscalar corrections:

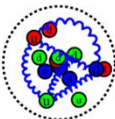
CInfo = ‚NMC‘, ‚EMC‘, ‚SLAC‘.

well constrained by data

Number sum rule:



Momentum sum rule:



$$u_v \neq d_v$$

known

unknown

Isospin symmetry:

$$s = \frac{1}{2} (\bar{u} + \bar{d})$$

$$s = \bar{s}$$

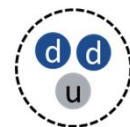
$$\bar{u} = \bar{d}$$

→ 16 free nuclear parameters

PROTON



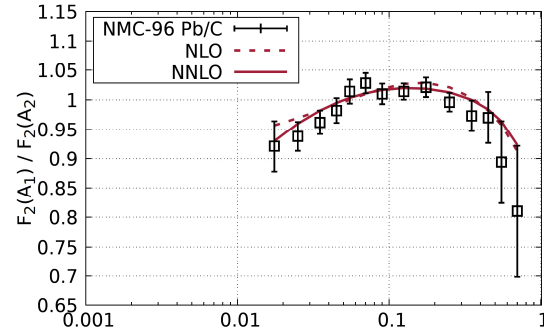
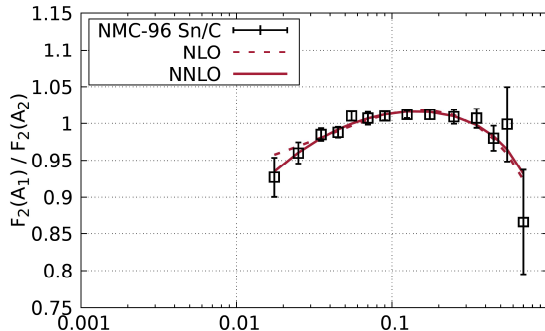
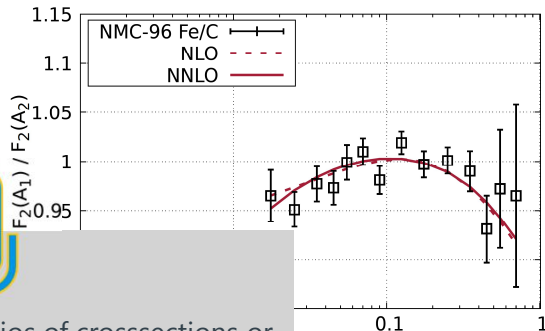
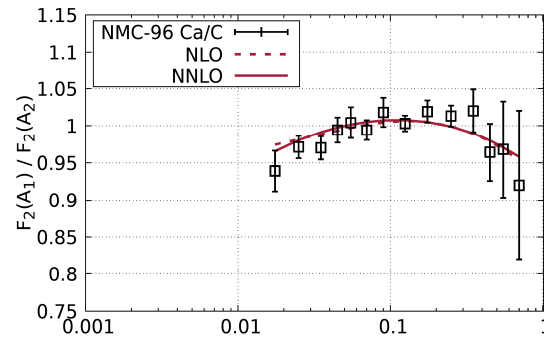
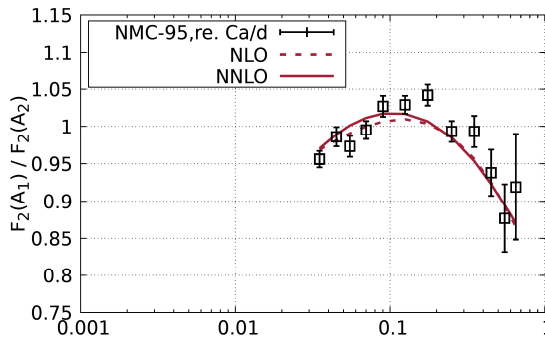
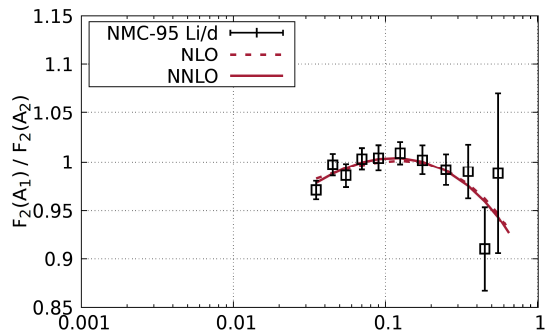
NEUTRON



not constrained by data



# COMPARISON TO DIS DATA

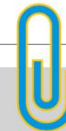


Ratios of crosssections or  
structure functions:

$R_{A_1/A_2} = F_2(A_1)/F_2(A_2)$

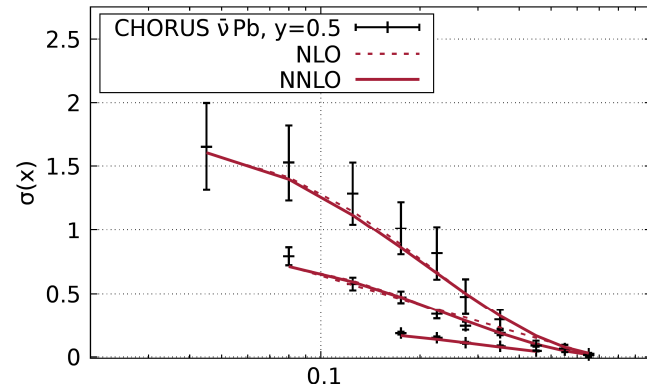
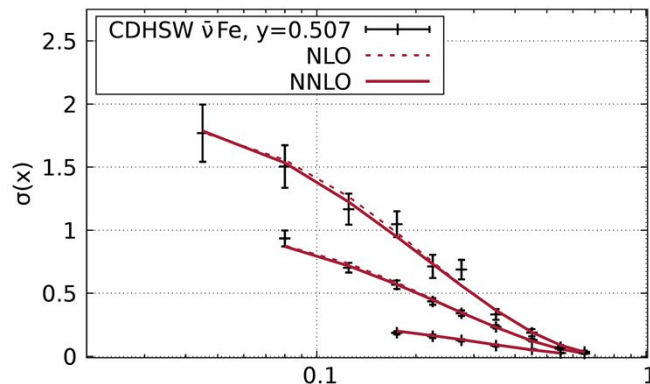
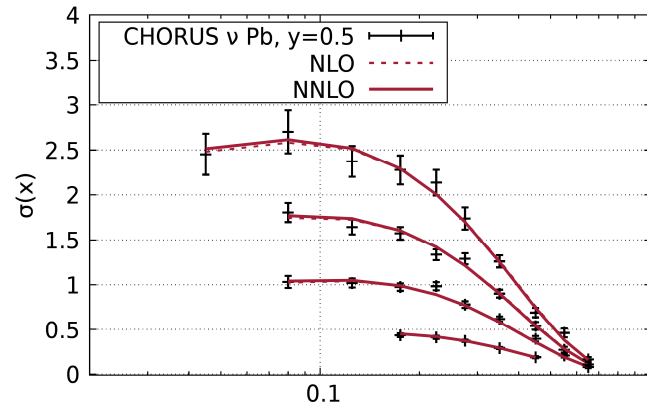
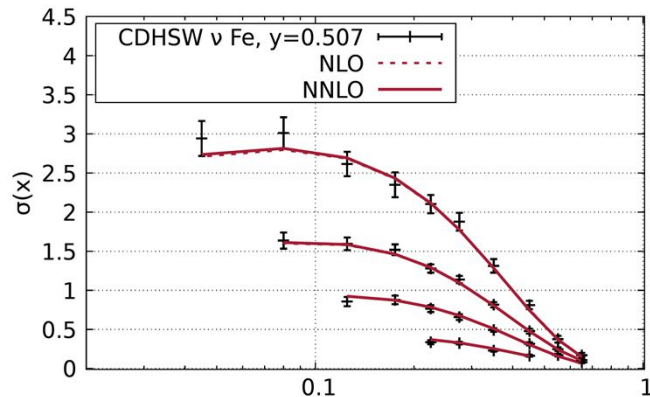


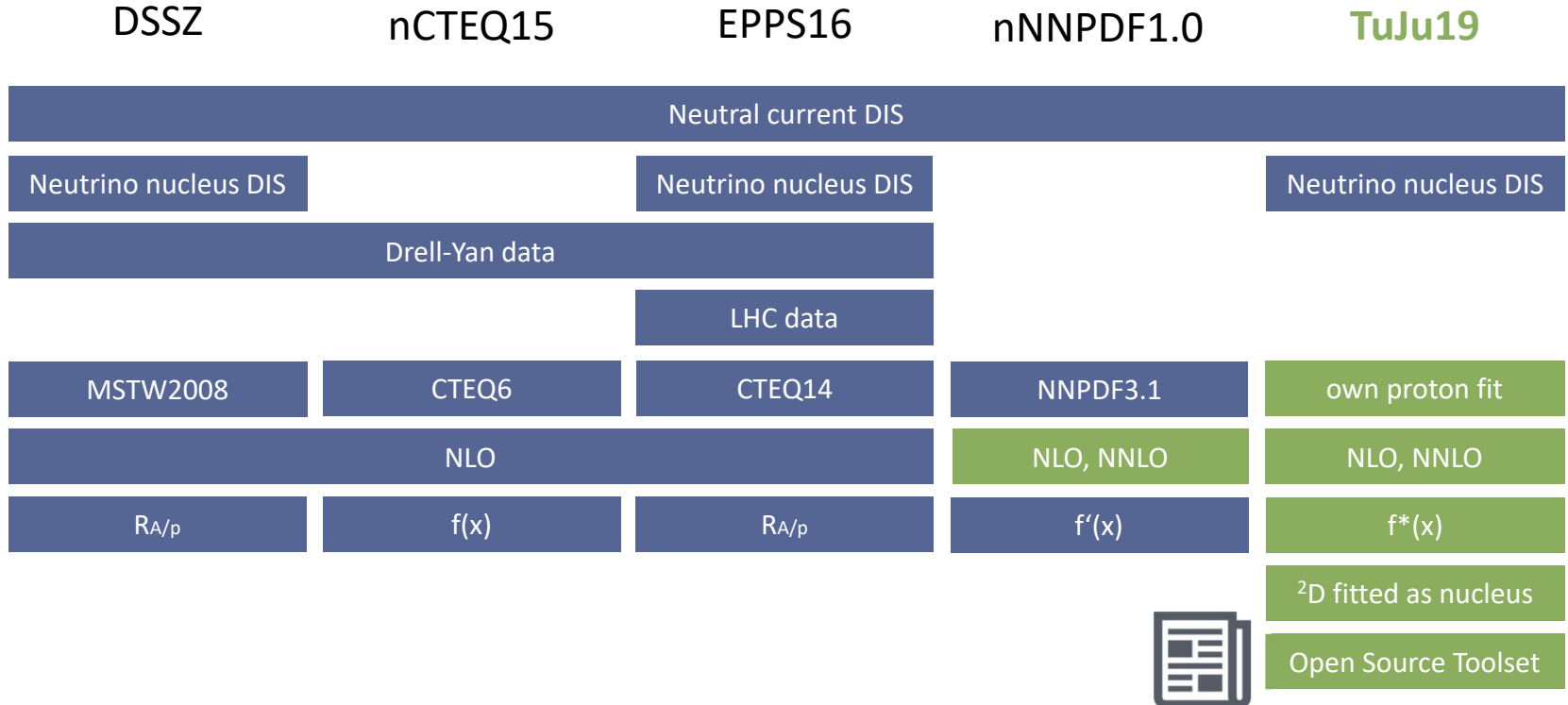
# COMPARISON TO NEUTRINO DIS DATA

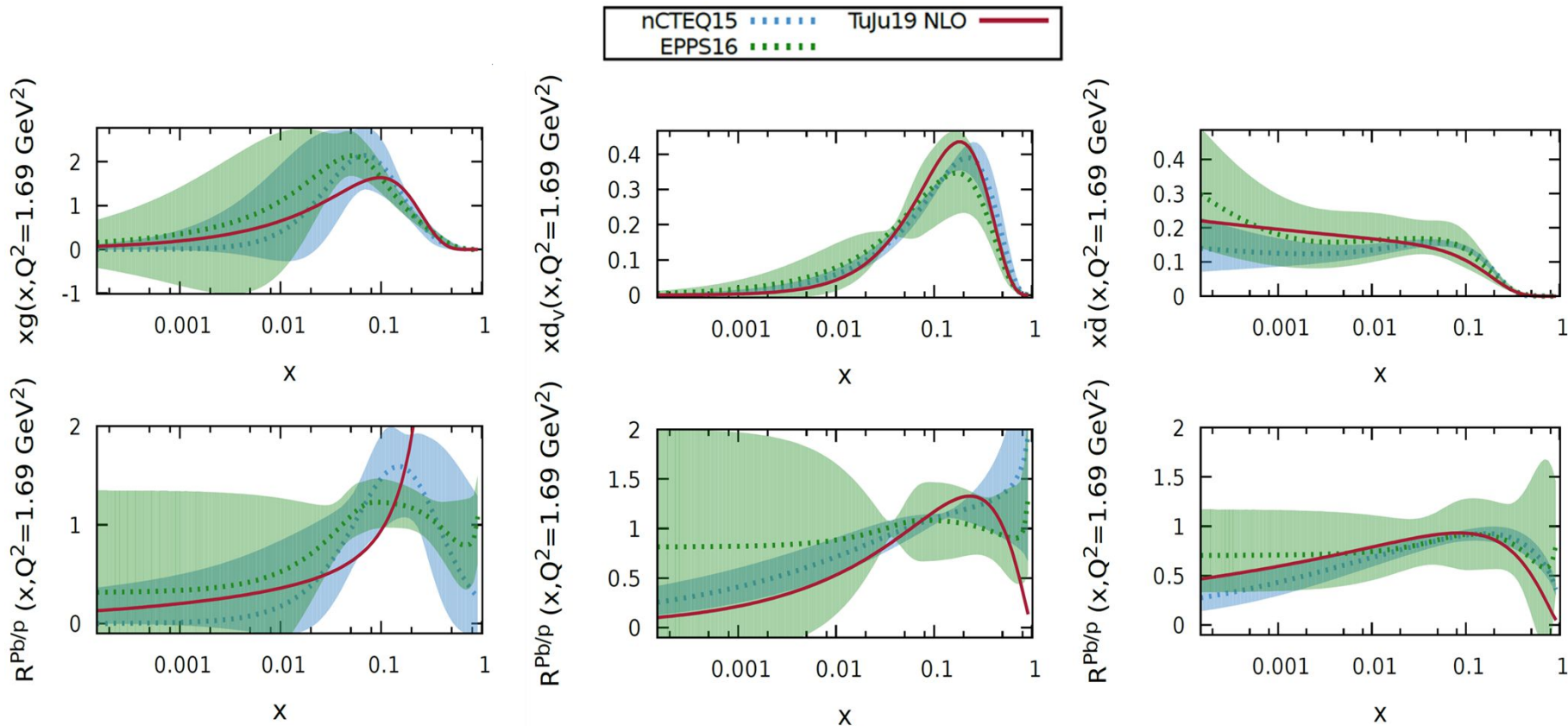


Charged Current DIS  
processes included:

Reaction = ,neutrino+p CC'

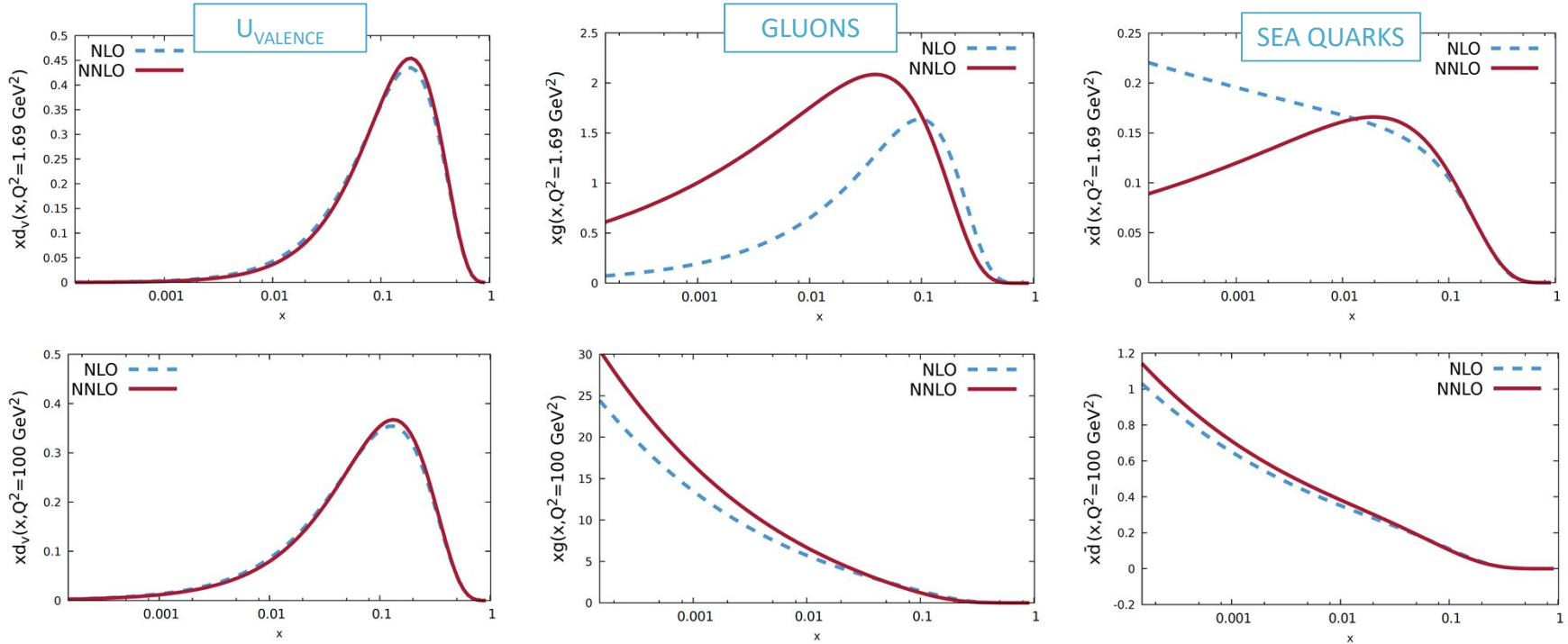








nPDFs for proton bound in lead Pb(208):

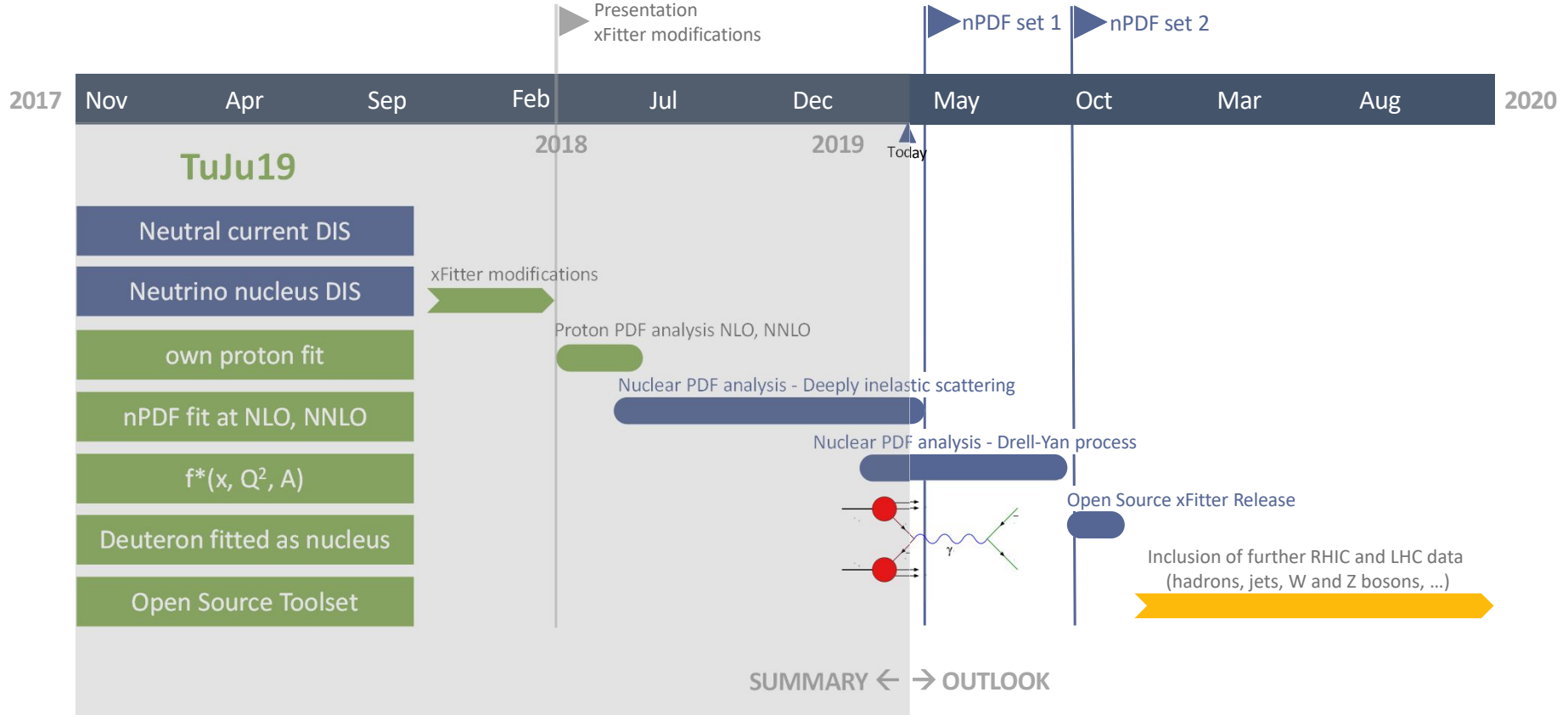




## TuJu19

- Neutral current DIS
- Neutrino nucleus DIS
- own proton fit
- nPDF fit at NLO, NNLO
- $f^*(x, Q^2, A)$
- Deuteron fitted as nucleus
- Open Source Toolset

# SUMMARY & OUTLOOK

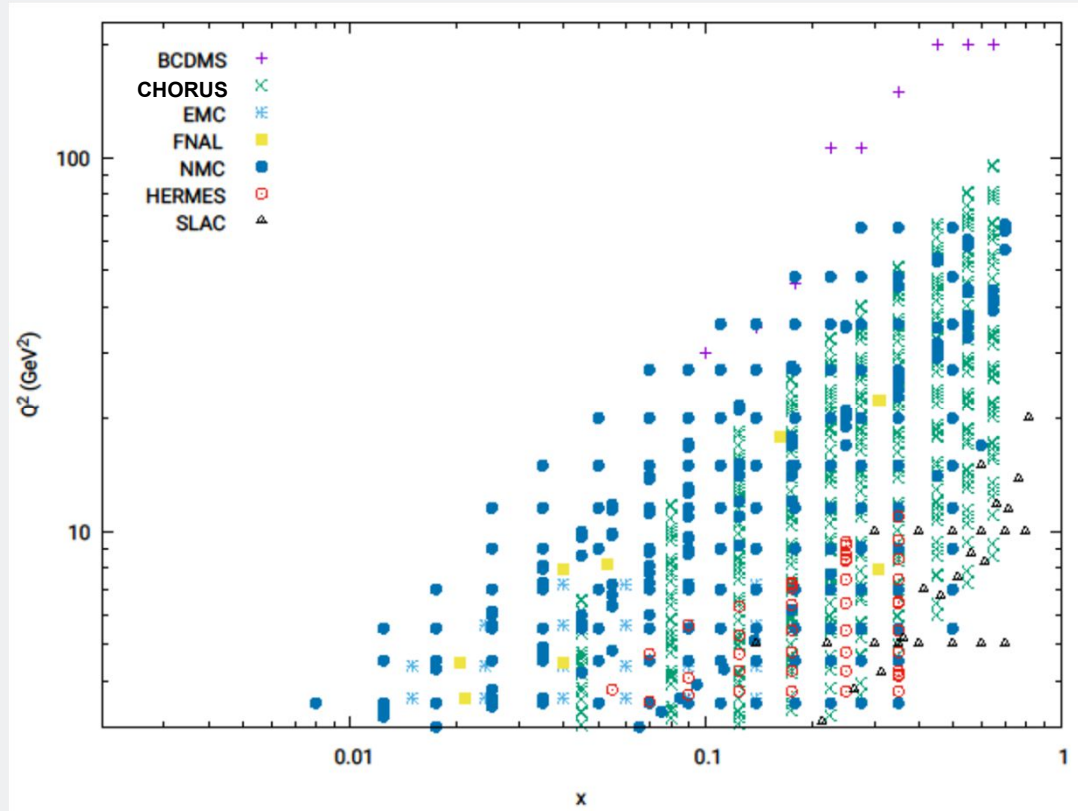




THANK YOU!

MARINA WALT  
[marina.walt@uni-tuebingen.de](mailto:marina.walt@uni-tuebingen.de)

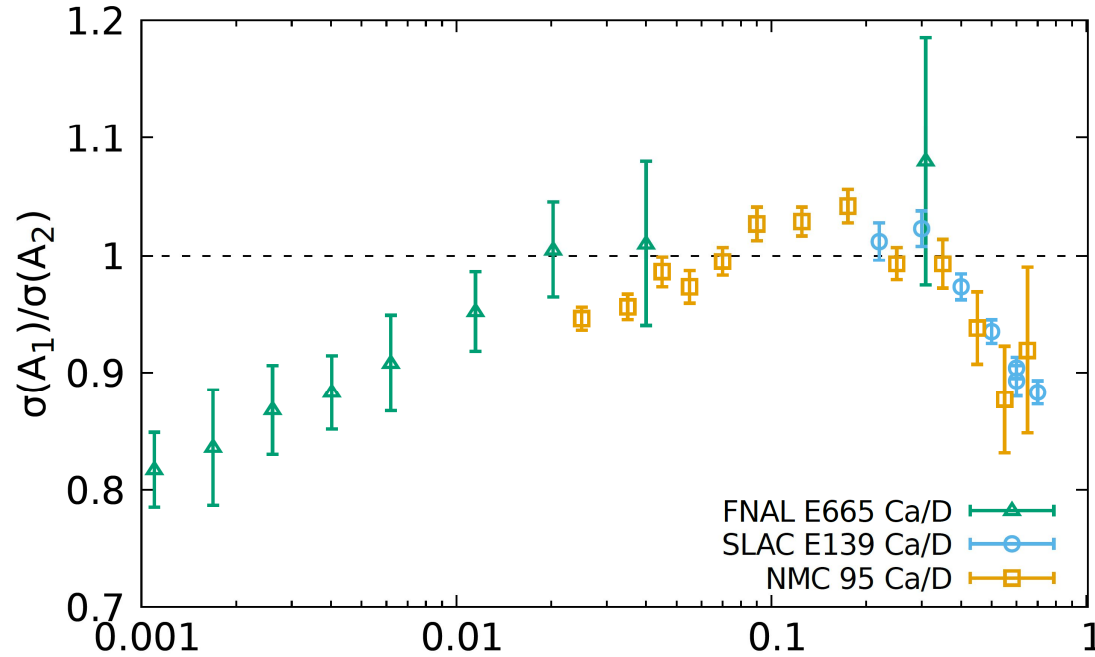
**In collaboration with:**  
Dr. Ilkka Helenius  
Prof. Dr. Werner Vogelsang

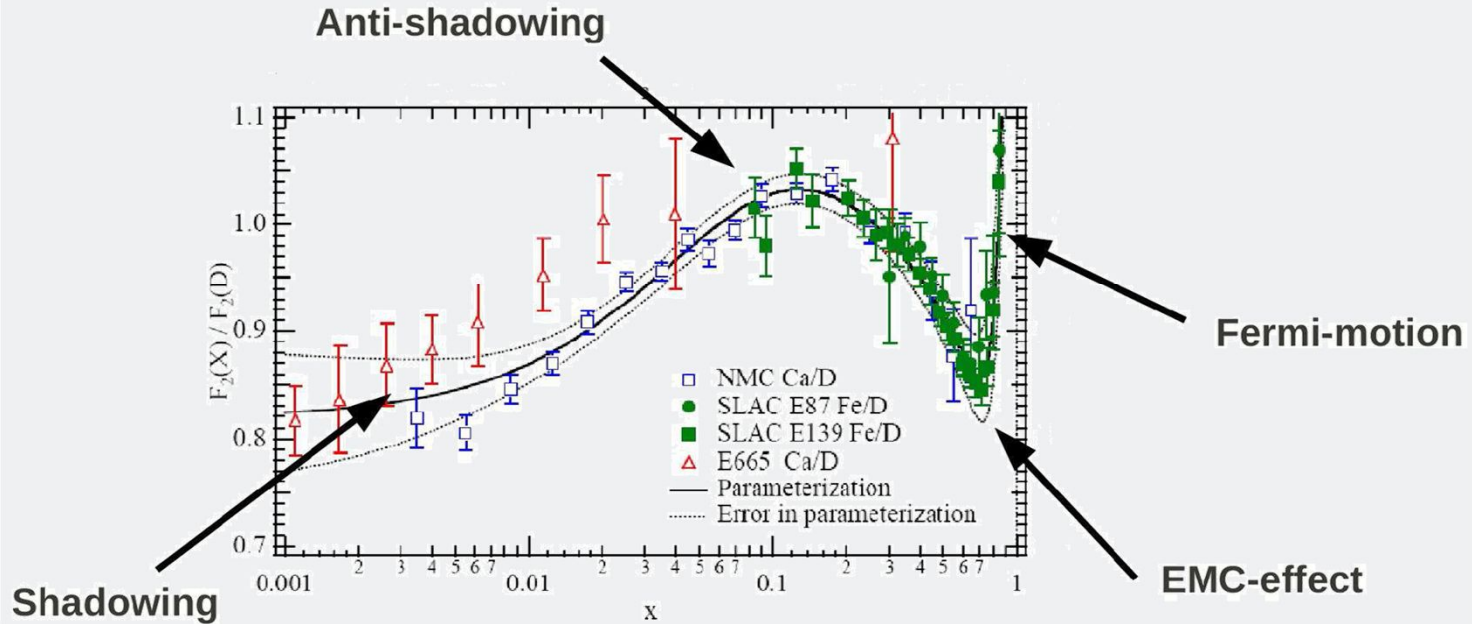




Ratios of crosssections or  
structure functions:

CInfo = ,ratio'





[Picture: Ilkka Helenius, Hannu Paukkunen]



$$\hat{F}_2^A = \beta F_2^A,$$

[ arXiv:1612.05741v1]

where

$$\beta = \frac{A}{2} \left( 1 + \frac{F_2^{n,A}}{F_2^{p,A}} \right) / \left( Z + N \frac{F_2^{n,A}}{F_2^{p,A}} \right)$$

– EMC parametrization :

$$\frac{F_2^n}{F_2^p} = 0.92 - 0.86x,$$

– SLAC parametrization :

$$\frac{F_2^n}{F_2^p} = 1 - 0.8x,$$

– NMC parametrization :

$$\frac{F_2^n}{F_2^p} = A(x) \left( \frac{Q^2}{20} \right)^{B(x)} \left( 1 + \frac{x^2}{Q^2} \right)$$

$$A(x) = 0.979 - 1.692x + 2.797x^2 - 4.313x^3 + 3.075x^4$$

$$B(x) = -0.171x^2 + 0.244x^3.$$

# THE ANALYSIS PROCEDURE



*xFitter*

A dependent coefficients

- Steering file
- Exp. data files
- Initial parameters

PDFType=,nucleus'  
(A=1, Z=1 for proton)

Flags for isoscalar corrections:  
CInfo = ,NMC', ,EMC', ,SLAC'.

Read input

Initialization of theory modules

Initial PDF parametrization

Evolution (e.g. DGLAP)

Minimization routine (FCN)

Store output

PDF decomposition of a bound nucleon.

Ratios of crosssections or structure functions:

CInfo = ,ratio'

Charged Current DIS processes included:

Reaction = ,neutrino+p CC'



PDFs



# ANALYSIS PROCEDURE AT NNLO

## DGLAP equations

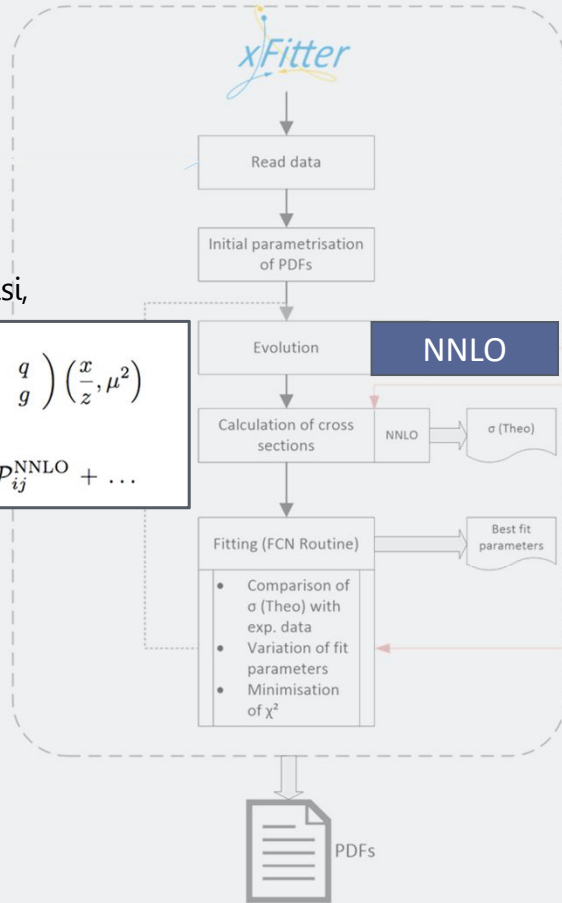
by Dokshitzer, Gribov, Lipatov, Altarelli, Parisi,

$$\mu^2 \frac{d}{d\mu^2} \begin{pmatrix} q(x, \mu^2) \\ g(x, \mu^2) \end{pmatrix} = \int_x^1 \frac{dz}{z} \begin{pmatrix} \mathcal{P}_{qq} & \mathcal{P}_{qg} \\ \mathcal{P}_{gq} & \mathcal{P}_{gg} \end{pmatrix} \begin{pmatrix} q \\ g \end{pmatrix} \left( \frac{x}{z}, \mu^2 \right)$$

$$\mathcal{P}_{ij} = \frac{\alpha_s}{2\pi} \mathcal{P}_{ij}^{\text{LO}} + \left( \frac{\alpha_s}{2\pi} \right)^2 \mathcal{P}_{ij}^{\text{NLO}} + \left( \frac{\alpha_s}{2\pi} \right)^3 \mathcal{P}_{ij}^{\text{NNLO}} + \dots$$

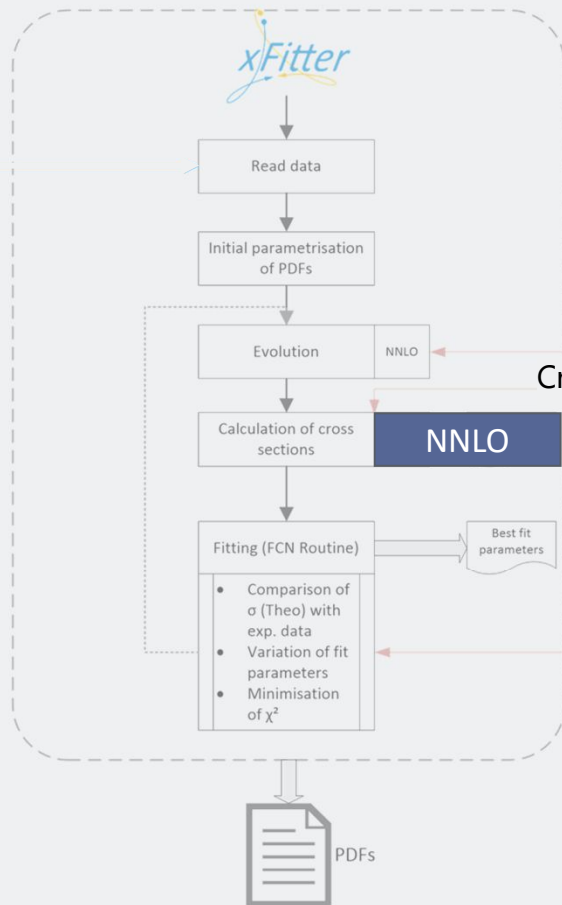


[NNLO:  
Nucl. Phys. B 688.1-2 (2004), 101-134,  
Nucl. Phys. B 691.1-2 (2004), 129-181]





# ANALYSIS PROCEDURE AT NNLO



Cross sections for neutral- & charged-current DIS

$$\frac{d^2\sigma^i}{dx dy} = \frac{4\pi\alpha^2}{xyQ^2} \eta^i \left\{ \left( 1 - y - \frac{x^2 y^2 M^2}{Q^2} \right) F_2^i + y^2 x F_1^i \mp \left( y - \frac{y^2}{2} \right) x F_3^i \right\},$$



[NNLO  $F_2$ :  
Nucl. Phys. B 890 (2015), 48-151]

