

27th International Workshop  
on Deep-Inelastic Scattering & Related Subjects



Top Quark Properties

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# Introduction

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What do we mean by “*top quark properties*”?

*Person A:* Mass, Width

*Person B:* Gauge and Yukawa couplings

*Person C:* Cross section,  $A_C$ ,  $W$  helicity fractions

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At the level of the SM Lagrangian, it is a well-defined question:

$$\mathcal{L}_{\text{top}}^{\text{SM}} = \bar{t} i \left( \not{\partial} + \frac{ie}{c_w} Y \not{B} - \frac{ie}{s_w} I^a \not{W}^a - ig_s T^c \not{G}^c \right) t - m_t \bar{t} t$$

Everything is determined by:  $\alpha, s_w, \alpha_s, m_t$  (+SM symmetries).

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Everything is determined by:  $\alpha, s_w, \alpha_s, m_t$  (+SM symmetries).

These are not observables but free parameters of the theory, fixed by some measurement.

$$\mathcal{O}_{\text{measured}}^{\text{nature}} = \mathcal{O}_{\text{predicted}}^{\text{theory}}(\alpha) \xrightarrow[\text{theory} \approx \text{nature}]{\text{solve}} \alpha$$

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Everything is determined by:  $\alpha, s_w, \alpha_s, m_t$  (+SM symmetries).

Once the parameters are reliably fixed, we try to *test the theory*, i.e. try to *falsify* the model, i.e. *find New Physics*:

$$\mathcal{O}_{\text{measured}}^{\text{nature}} = \mathcal{O}_{\text{predicted}}^{\text{theory}}(\alpha) \quad \leftarrow \begin{array}{c} \text{test} \\ \text{theory} \approx \text{nature?} \end{array} \quad \alpha$$

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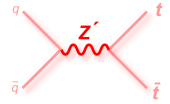
Everything is determined by:  $\alpha, s_w, \alpha_s, m_t$  (+SM symmetries).

→ We have to probe observables that are sensitive to physics beyond the SM

→ We need high precision to reliably identify small deviations

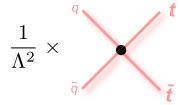
# How to search for New Physics?

**Strategy I:** Explicit model building and testing the predictions



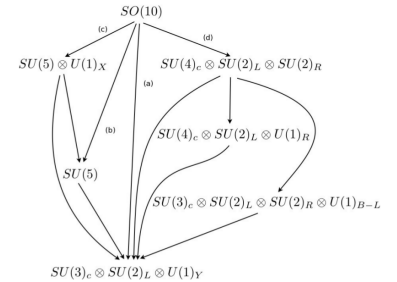
Introduce a new  $\mathcal{L}_{\text{BSM}}$  such that  $\mathcal{L}_{\text{BSM}} \rightarrow \mathcal{L}_{\text{SM}}$  in some limit

**Strategy II:** Model-independent Effective Field Theory (EFT)



Extend the SM such that  $\mathcal{L} = \mathcal{L}_{\text{SM}} + \frac{c_i}{\Lambda^2} \mathcal{O}_i^{\text{dim6}} + \dots$ , fit to data yields constraint on  $\frac{c_i}{\Lambda^2}$

$\mathcal{L}^{\text{dim6}}$  is the most general expression that respects all symmetries of the SM





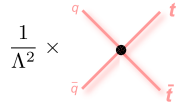
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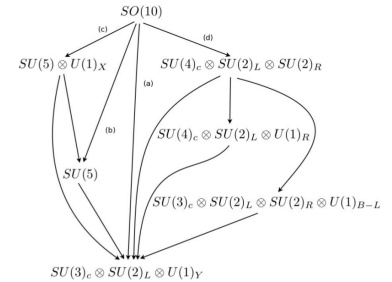
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**SM-EFT:** Assumptions:

- New Physics is heavy
- New Physics does not break  $SU(2)_L \times U(1)$  at  $E \leq \Lambda$

Consequences:

- Effects from dim6 dominate over dim8, ...
- Relations between anomalous couplings of SM fields

# How to search for New Physics?

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## Example:

Add new dim6 Lagrangian term

$$\mathcal{O}_{\phi q1}^{\text{dim6}} = i(\underbrace{\phi^\dagger D_\mu \phi}_{\text{SU(2) \times U(1) invariant}})(\bar{U}_L \gamma^\mu U_L)$$

# How to search for New Physics?

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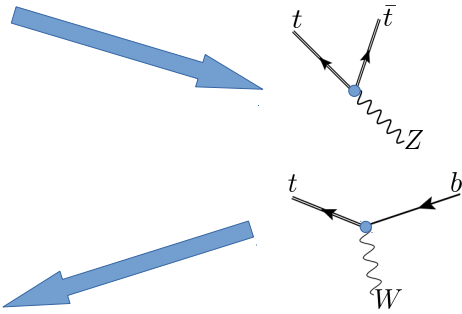
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Cross section contribution:

$$\sigma_{\text{BSM}} = \sigma_{\text{SM}} + \frac{v^2}{\Lambda^2} \sigma_{\text{EFT}} + \frac{v^4}{\Lambda^4} \sigma_{\text{EFT}^2}$$

Yields modified coupling for  $ttZ$  and  $tbW$



$$= \frac{ie}{2s_w c_w} \gamma^\mu \left\{ \left( 1 + \frac{c_{\phi q1}}{\Lambda^2} \right) P_L + P_R - 2s_w^2 Q_t \right\}$$

$$= \frac{ie}{\sqrt{2}s_w} \gamma^\mu P_L \left( 1 + \frac{c_{\phi q1}}{\Lambda^2} \right)$$

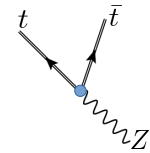
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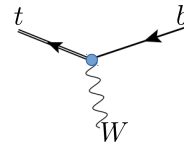
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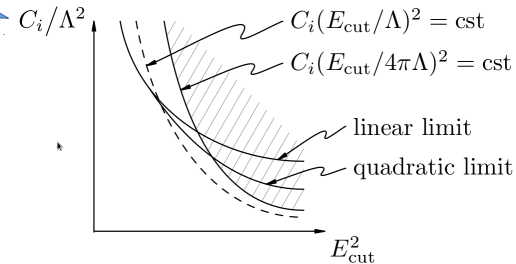
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Cross section contribution:

$$\sigma_{\text{BSM}} = \underbrace{\sigma_{\text{SM}} + \frac{v^2}{\Lambda^2} \sigma_{\text{EFT}}}_{\text{SM-EFT interference}} + \underbrace{\frac{v^4}{\Lambda^4} \sigma_{\text{EFT}^2}}_{\text{squared dim6 EFT term}}$$



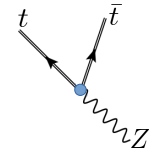
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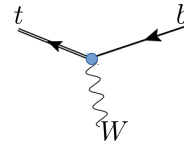
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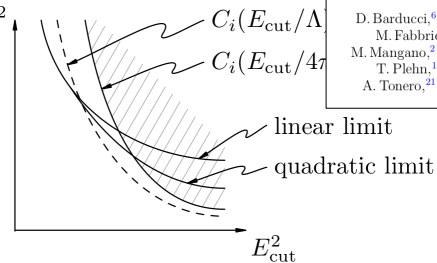
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SM-EFT interference

squared dim6 EFT term

$C_i/\Lambda^2$



Interpreting top-quark LHC measurements  
in the standard-model effective field theory

J.A. Aguilar Saavedra,<sup>1</sup> C. Degrande,<sup>2</sup> G. Durieux,<sup>3</sup>  
F. Maltoni,<sup>4</sup> E. Vryonidou,<sup>2</sup> C. Zhang<sup>5</sup> (editors),  
D. Barducci,<sup>6</sup> I. Brivio,<sup>7</sup> V. Cirigliano,<sup>8</sup> W. Dekens,<sup>8,9</sup> J. de Vries,<sup>10</sup> C. Englert,<sup>11</sup>  
M. Fabbrichesi,<sup>12</sup> C. Grojean,<sup>3,13</sup> U. Haisch,<sup>2,14</sup> Y. Jiang,<sup>7</sup> J. Kamenik,<sup>15,16</sup>  
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T. Plehn,<sup>18</sup> F. Riva,<sup>2</sup> M. Russell,<sup>18</sup> J. Santiago,<sup>19</sup> M. Schulze,<sup>13</sup> Y. Soreq,<sup>20</sup>  
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# How to search for New Physics?

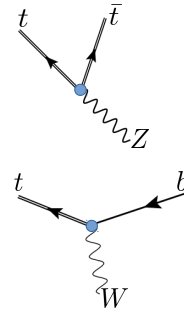
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$$\begin{aligned} &= \Gamma_{\text{SM}}^Z + i \frac{\sigma^{\mu\nu}}{m_t} (g_L^Z P_L + g_R^Z P_R) \mathbf{q}_\mu \varepsilon_\nu^Z \} \\ &= \Gamma_{\text{SM}}^W + i \frac{\sigma^{\mu\nu}}{m_t} (g_L^W P_L + g_R^W P_R) \mathbf{q}_\mu \varepsilon_\nu^W \end{aligned}$$

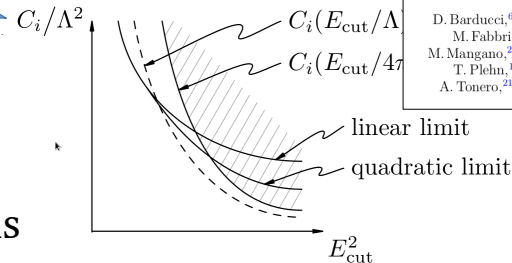
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energy dependence leads to violation of unitarity

Require:  $E \ll \Lambda$

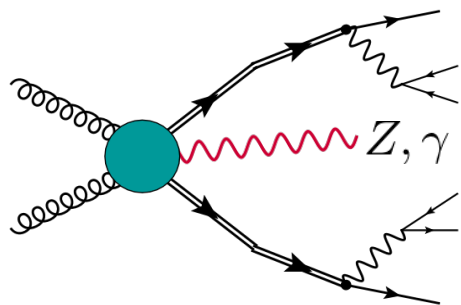
→ Limit energy range of the analysis



Interpreting top-quark LHC measurements in the standard-model effective field theory

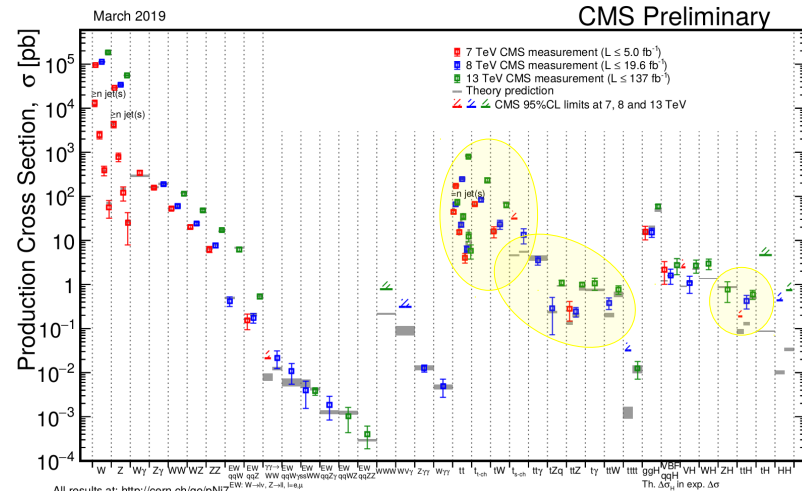
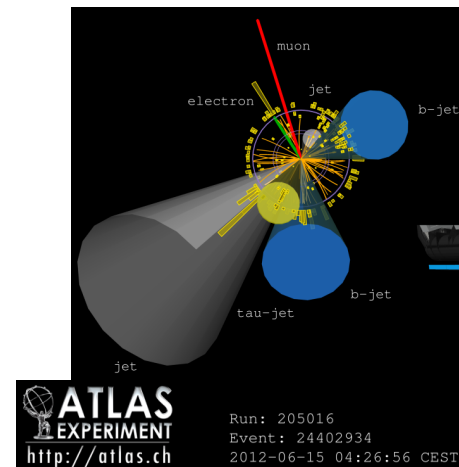
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# Anatomy of Top Quark Production at the LHC



## Features:

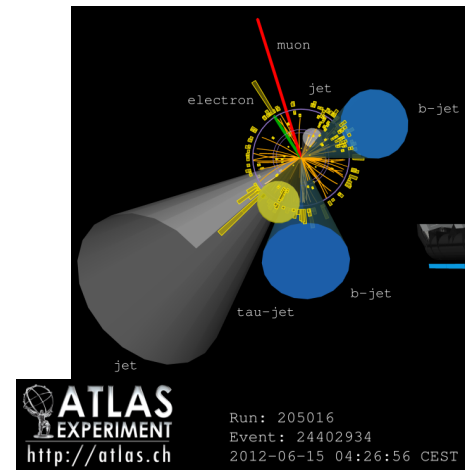
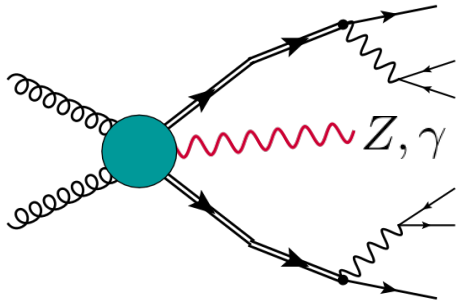
- Very complex final state (often up to 8 particles)
- Sufficiently large cross sections
- Small backgrounds & clean signature (if  $W \rightarrow$  leptons)
- Meaningful separation into production and decay dynamics
- Sensitivity to New Physics



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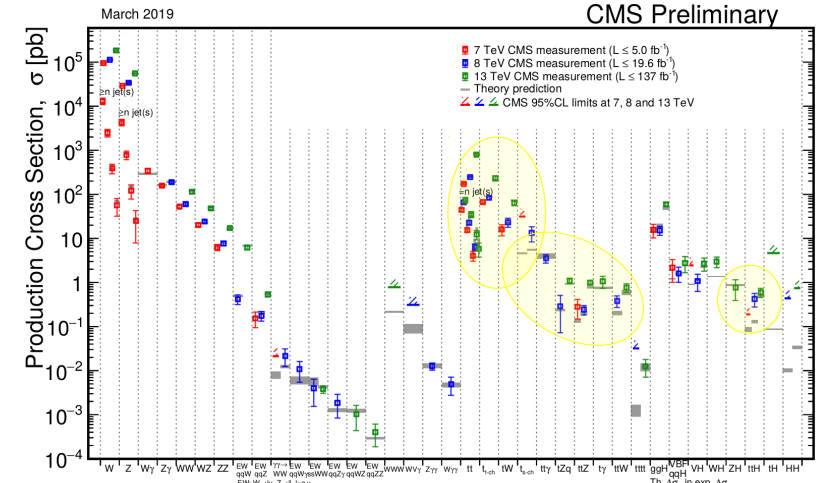
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## Special property:

$$\Lambda_{\text{QCD}} \ll \Gamma_t \ll m_t$$

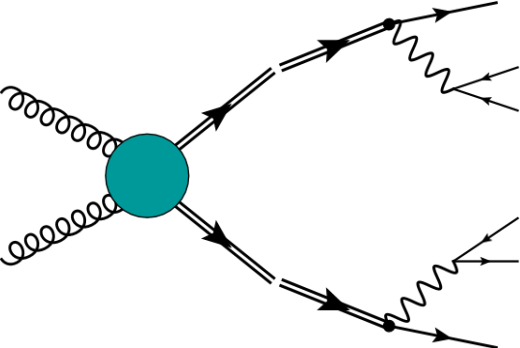
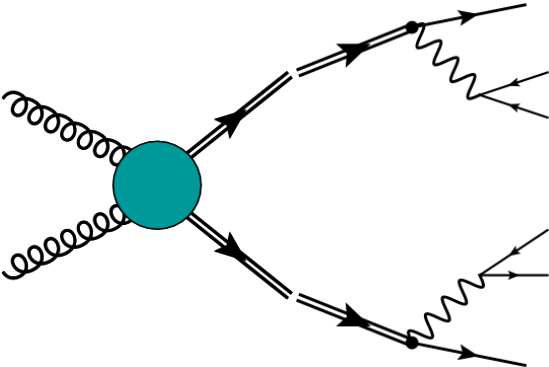
- No hadronic bound states
- Spin information is transferred to decay products
- Production and decay are separated by large time scale
- Top quarks like to go on-shell before they decay



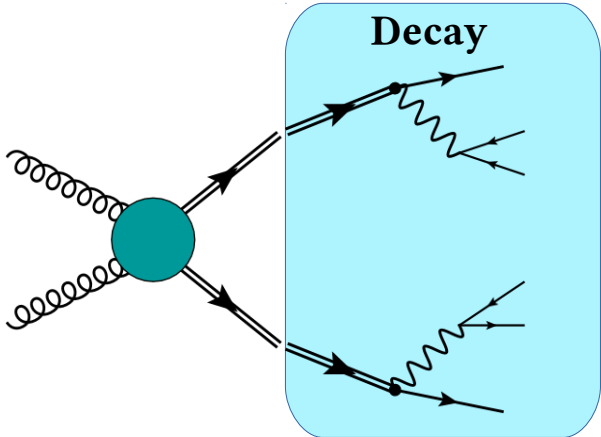
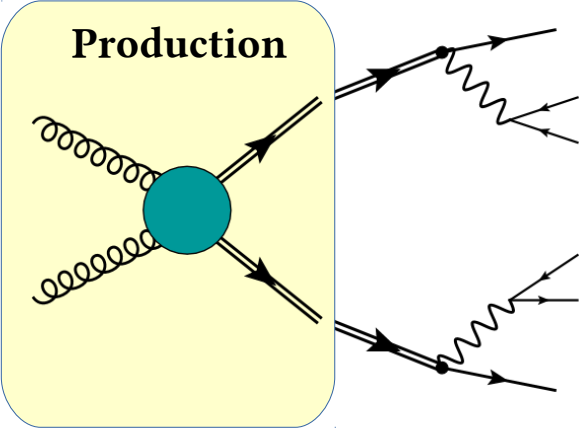


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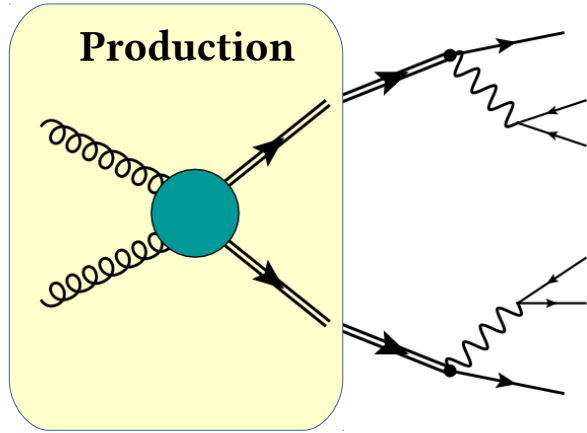
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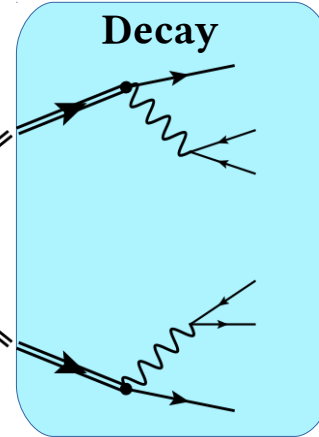
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# Anatomy of Top Quark Production at the LHC

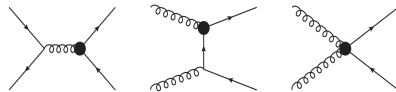


Production  
Sensitivity to QCD dynamics

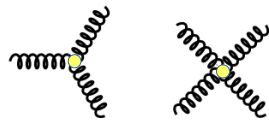


Decay  
Sensitivity to EW physics

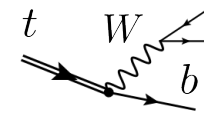
$$\begin{aligned} \mathcal{O}_{Qq}^{(8,3)} &= (\bar{Q}_L \gamma_\mu T^a \tau^i Q_L) (\bar{q}_L \gamma^\mu T^a \tau^i q_L) \\ \mathcal{O}_{Qq}^{(8,1)} &= (\bar{Q}_L \gamma_\mu T^a Q_L) (\bar{q}_L \gamma^\mu T^a q_L) \\ \mathcal{O}_{td}^{(8)} &= (\bar{t}_R \gamma_\mu T^a t_R) (\bar{d}_R \gamma^\mu T^a d_R) \\ \mathcal{O}_{tu}^{(8)} &= (\bar{t}_R \gamma_\mu T^a t_R) (\bar{u}_R \gamma^\mu T^a u_R) \\ \mathcal{O}_{tq}^{(8)} &= (\bar{t}_R \gamma_\mu T^a t_R) (\bar{q}_L \gamma^\mu T^a q_L) \\ \mathcal{O}_{qd}^{(8)} &= (\bar{Q}_L \gamma_\mu T^a Q_L) (\bar{d}_R \gamma^\mu T^a d_R) \\ \mathcal{O}_{qu}^{(8)} &= (\bar{Q}_L \gamma_\mu T^a Q_L) (\bar{u}_R \gamma^\mu T^a u_R) \\ \mathcal{O}_{Qq}^{(1,3)} &= (\bar{Q}_L \gamma_\mu \tau^i Q_L) (\bar{q}_L \gamma^\mu \tau^i q_L) \\ \mathcal{O}_{Qq}^{(1,1)} &= (\bar{Q}_L \gamma_\mu Q_L) (\bar{q}_L \gamma^\mu q_L) \\ \mathcal{O}_{td}^{(1)} &= (\bar{t}_R \gamma_\mu t_R) (\bar{d}_R \gamma^\mu d_R) \\ \mathcal{O}_{tu}^{(1)} &= (\bar{t}_R \gamma_\mu t_R) (\bar{u}_R \gamma^\mu u_R) \\ \mathcal{O}_{tq}^{(1)} &= (\bar{t}_R \gamma_\mu t_R) (\bar{q}_L \gamma^\mu q_L) \\ \mathcal{O}_{qd}^{(1)} &= (\bar{Q}_L \gamma_\mu Q_L) (\bar{d}_R \gamma^\mu d_R) \\ \mathcal{O}_{qu}^{(1)} &= (\bar{Q}_L \gamma_\mu Q_L) (\bar{u}_R \gamma^\mu u_R) \end{aligned}$$



$$O_{tG} = y_t g_s (\bar{Q} \sigma^{\mu\nu} T^A t) \tilde{\phi} G_{\mu\nu}^A$$



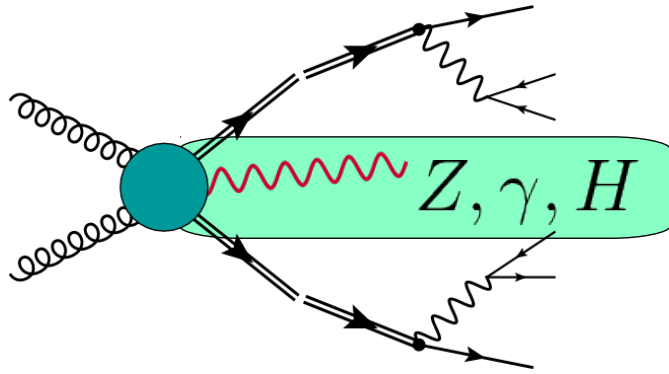
$$c_G \mathcal{O}_G = \frac{g_s c_G}{\Lambda^2} f_{abc} G_{ab}^c G_{b\lambda}^a G_{c\lambda}^b \rightarrow \text{see [Krauss, Kuttimalai, Plehn] (2016)}$$



$$\begin{aligned} C_{\phi q}^{(3,33)} &= i(\phi^\dagger \tau^a D_\mu \phi) (\bar{t}_L \gamma^\mu \tau_a t_L), \\ \mathcal{O}_{\phi\phi}^{33} &= i(\tilde{\phi}^\dagger D_\mu \phi) (\bar{u}_R \gamma^\mu d_R) \\ \mathcal{O}_{uW}^{33} &= (\bar{q}_L \sigma^{\mu\nu} \tau^I t_R) \tilde{H} W_{\mu\nu}^I, \\ \mathcal{O}_{dW}^{33} &= (\bar{q}_L \sigma^{\mu\nu} \tau^I b_R) H W_{\mu\nu}^I, \\ \mathcal{O}_{uB\phi}^{33} &= (\bar{q}_L \sigma^{\mu\nu} t_R) \tilde{H} B_{\mu\nu}, \end{aligned}$$

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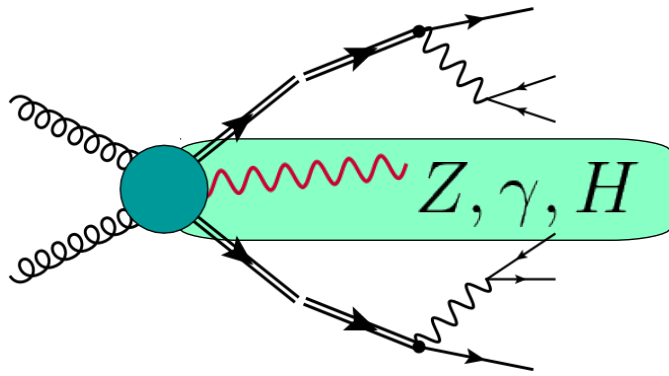
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## Associated production:

Sensitivity to couplings of neutral gauge bosons and the Higgs Boson

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$$C_{u\phi}^{33} = (\tilde{\phi}^\dagger \phi)(\bar{q}_L u_R)$$

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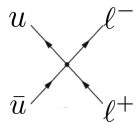
$$C_{\phi q}^{(1,33)} = i(\phi^\dagger D_\mu \phi)(\bar{t}_L \gamma^\mu t_L),$$

$$C_{\phi u}^{33} = i(\phi^\dagger D_\mu \phi)(\bar{t}_R \gamma^\mu t_R).$$

$$\mathcal{O}_{uW}^{33} = (\bar{q}_L \sigma^{\mu\nu} \tau^I t_R) \tilde{H} W_{\mu\nu}^I,$$

$$\mathcal{O}_{dW}^{33} = (\bar{q}_L \sigma^{\mu\nu} \tau^I b_R) H W_{\mu\nu}^I,$$

$$\mathcal{O}_{uB\phi}^{33} = (\bar{q}_L \sigma^{\mu\nu} t_R) \tilde{H} B_{\mu\nu},$$



$$O_{lq}^1 \equiv \bar{l} \gamma_\mu l \quad \bar{q} \gamma^\mu q,$$

$$O_{lu} \equiv \bar{l} \gamma_\mu l \quad \bar{u} \gamma^\mu u,$$

$$O_{eq} \equiv \bar{e} \gamma_\mu e \quad \bar{q} \gamma_\mu q,$$

$$O_{eu} \equiv \bar{e} \gamma_\mu e \quad \bar{u} \gamma^\mu u,$$

$$O_{lequ}^1 \equiv \bar{l} e \varepsilon \bar{q} u,$$

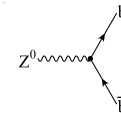
$$O_{lequ}^3 \equiv \bar{l} \sigma_{\mu\nu} e \varepsilon \bar{q} \sigma^{\mu\nu} u,$$

$$O_{lq}^3 \equiv \bar{l} \gamma_\mu \tau^I l \quad \bar{q} \gamma^\mu \tau^I q,$$

- Allows to probe a large range of new couplings
- Electroweak top quark couplings are not very well constrained
- Tevatron never produced  $t\bar{t}+X$  final states
- Relations from EW precision observables

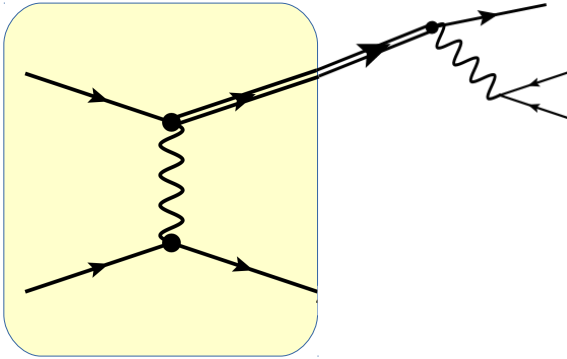
$$\delta\epsilon_1 = \frac{3m_t^2 C_F}{2\sqrt{2}\pi^2} \text{Re} \left[ C_{\phi q}^{(3,33)} - C_{\phi q}^{(1,33)} + C_{\phi u}^{33} + \mathcal{O}\left(\frac{v^2}{\Lambda^2}\right) \right] \left( \frac{v^2}{\Lambda^2} \right) \log\left(\frac{\Lambda^2}{m_t^2}\right)$$

$$\delta\epsilon_3 = -\frac{m_t^2 C_F}{2\sqrt{2}\pi^2} \text{Re} \left[ C_{\phi q}^{(3,33)} - C_{\phi q}^{(1,33)} + \frac{1}{4} C_{\phi u}^{33} \right] \left( \frac{v^2}{\Lambda^2} \right) \log\left(\frac{\Lambda^2}{m_t^2}\right).$$



$$C_{\phi q}^{(3,33)} \approx -C_{\phi q}^{(1,33)}$$

# Anatomy of Top Quark Production at the LHC



## Single top quark production:

Only mentioned briefly for brevity

Excellent sensitivity to  $tbW$  coupling and top quark mass



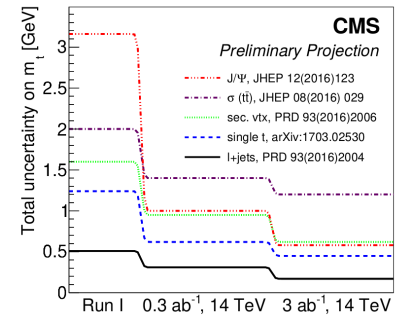
$$C_{\phi q}^{(3,33)} = i(\phi^\dagger \tau^a D_\mu \phi)(\bar{t}_L \gamma^\mu \tau_a t_L),$$

$$O_{\phi\phi}^{33} = i(\tilde{\phi}^\dagger D_\mu \phi)(\bar{u}_R \gamma^\mu d_R)$$

$$O_{uW}^{33} = (\bar{q}_L \sigma^{\mu\nu} \tau^I t_R) \tilde{H} W_{\mu\nu}^I,$$

$$O_{dW}^{33} = (\bar{q}_L \sigma^{\mu\nu} \tau^I b_R) H W_{\mu\nu}^I,$$

$$O_{uB\phi}^{33} = (\bar{q}_L \sigma^{\mu\nu} t_R) \tilde{H} B_{\mu\nu},$$



# The big picture

---

$$\mathcal{L}_{Wtb} = -\frac{g}{\sqrt{2}} \bar{b} \gamma^\mu (V_L P_L + V_R P_R) t W_\mu^- - \frac{g}{\sqrt{2}} \bar{b} \frac{i\sigma^{\mu\nu} q_\nu}{M_W} (g_L P_L + g_R P_R) t W_\mu^- + \text{H.c.}$$

$$\mathcal{L}_{\gamma tt} = -e Q_t \bar{t} \gamma^\mu t A_\mu - e \bar{t} \frac{i\sigma^{\mu\nu} q_\nu}{m_t} (d_V^\gamma + i d_A^\gamma \gamma_5) t A_\mu$$

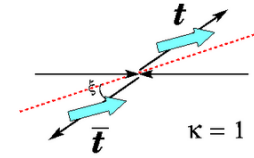
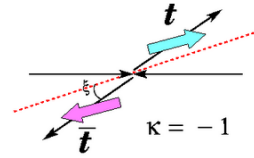
$$\mathcal{L}_{Ztt} = -\frac{g}{2c_W} \bar{t} \gamma^\mu (X_{tt}^L P_L + X_{tt}^R P_R - 2s_W^2 Q_t) t Z_\mu - \frac{g}{2c_W} \bar{t} \frac{i\sigma^{\mu\nu} q_\nu}{M_Z} (d_V^Z + i d_A^Z \gamma_5) t Z_\mu$$

# Spin Correlations



# Spin Correlations

Top quarks produced at the LHC are unpolarized.



However, the relative polarization of top and anti-top is correlated.

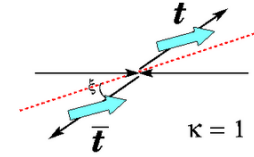
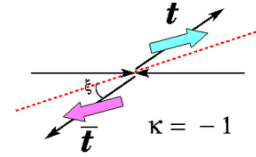
[Barger,Ohnemus,Philips] (1988)

$$C_{LO}^{SM} = \frac{\#(\uparrow\uparrow + \downarrow\downarrow) - \#(\uparrow\downarrow + \downarrow\uparrow)}{\#total} = \begin{cases} -46\% \text{ at Tevatron,} \\ +31\% \text{ at LHC.} \end{cases}$$

(quantization axis = direction of flight)

# Spin Correlations

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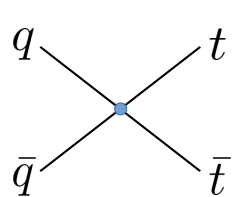
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$$C_{\text{LO}}^{\text{SM}} = \frac{\#(\uparrow\uparrow + \downarrow\downarrow) - \#(\uparrow\downarrow + \downarrow\uparrow)}{\#_{\text{total}}} = \begin{cases} -46\% \text{ at Tevatron,} \\ +31\% \text{ at LHC.} \end{cases}$$

(quantization axis = direction of flight)

Interesting quantity because very sensitive to New Physics:



$$\mathcal{L}_{\text{BSM}} = \frac{g_s^2}{2m_t^2} \hat{c}_{VV} (\bar{q}\gamma^\mu t^a q) (\bar{t}\gamma_\mu t^a t) + \frac{g_s^2}{4m_t^2} \hat{c}_1 \{ (\bar{q}\gamma^\mu \sigma_3 t^a q) (\bar{t}\gamma_\mu t^a t) + (\bar{q}\gamma^\mu \gamma^5 \sigma_3 t^a q) (\bar{t}\gamma_\mu t^a t) \}$$

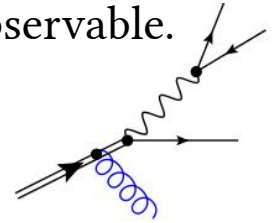
$$C_{\text{LO}}^{\text{BSM}} = \begin{cases} -89\% & c_{VV} \\ +18\% & c_1 \end{cases}$$

[Bernreuther,Heisler,Si] (2015)

# Spin Correlations

In the early days (Tevatron run-II) it was questionable whether spin correl. are observable.

Non-perturbative effects and radiative top quark decays wash out the correlation.



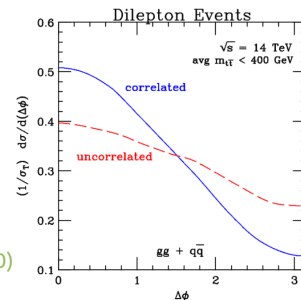
Thanks to  $\Lambda_{\text{QCD}} \ll \Gamma_t \ll m_t$  the non pert. dilution is small. No collinear enhancement.

→ Spin correlations first observed by DZero (2011) in  $\Delta\phi_{\ell\ell}$  distribution using MEM methods.

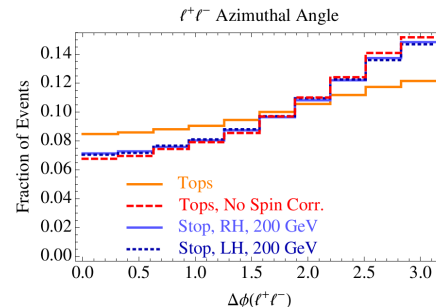
[Melnikov, M.S.] (2011)

Important: ( $V-A$ ) interaction in decay transfers spin information to decay products

Top quark spin correlation is imprinted in lepton angular distribution



[Mahlon] (2010)



[Han, Katz, Krohn, Reece] (2012)

# Spin Correlations

State-of-the-art:

NNLO QCD for top quark production + decay (NWA)

Higher order corrections to spin correlations in top quark pair production at the LHC

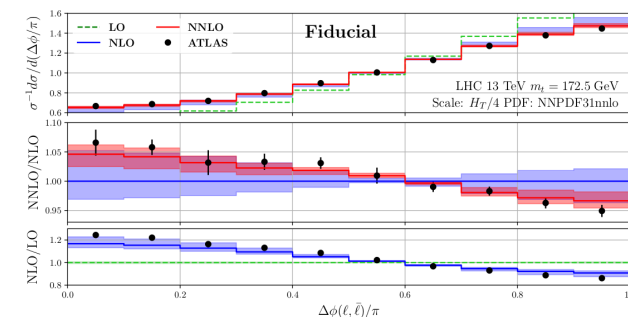
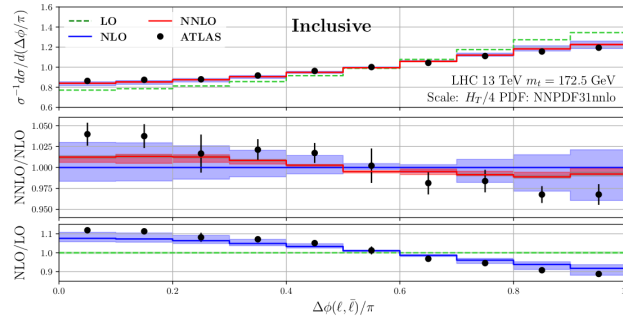
Arnd Behring  
 Institut für Theoretische Teilchenphysik und Kosmologie,  
 RWTH Aachen University, D-52056 Aachen, Germany and  
 Institute for Theoretical Particle Physics, KIT, Karlsruhe, Germany

Michał Czakon  
 Institut für Theoretische Teilchenphysik und Kosmologie,  
 RWTH Aachen University, D-52056 Aachen, Germany

Alexander Mitov, Andrew S. Papanastasiou, and Rene Poncelet  
 Cavendish Laboratory, University of Cambridge, Cambridge CB3 0HE, UK  
 (Dated: January 17, 2019)

→ see also talk by  
 Rene Poncelet

$$\begin{aligned}
 d\sigma^{\text{LO}} &= d\sigma^{\text{LO}\times\text{LO}}, \\
 d\sigma^{\text{NLO}} &= d\sigma^{\text{NLO}\times\text{LO}} + d\sigma^{\text{LO}\times\text{NLO}} - \frac{2\Gamma_t^{(1)}}{\Gamma_t^{(0)}} d\sigma^{\text{LO}}, \quad (1) \\
 d\sigma^{\text{NNLO}} &= d\sigma^{\text{NNLO}\times\text{LO}} + d\sigma^{\text{LO}\times\text{NNLO}} + d\sigma^{\text{NLO}\times\text{NLO}} \\
 &\quad - \frac{2\Gamma_t^{(1)}}{\Gamma_t^{(0)}} d\sigma^{\text{NLO}} - \frac{(\Gamma_t^{(1)})^2 + 2\Gamma_t^{(0)}\Gamma_t^{(2)}}{(\Gamma_t^{(0)})^2} d\sigma^{\text{LO}}.
 \end{aligned}$$



Quote: “In our view the most plausible explanation for this discrepancy lies in the extrapolation of the fiducial measurement to the full phase space.”

Exp. data from ATLAS-CONF-2018-027  
 13 TEV, 36 fb-1

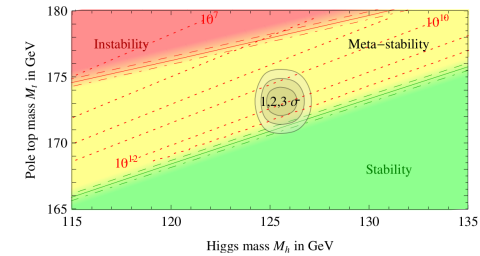
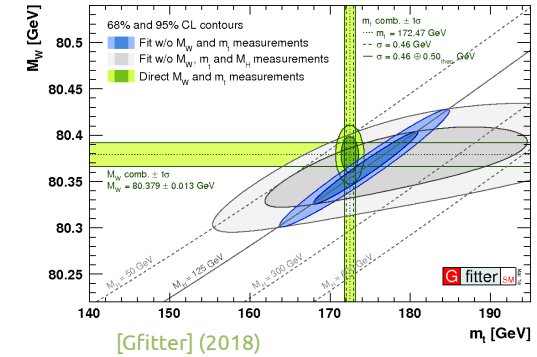
Sensible since extrapolation does not use NNLO QCD simulation.

# Top Quark Mass

# Top Quark Mass

This is a very broad field. Therefore *just the basics*:

- $m_t$  is an important parameter of the SM: consistency checks, vacuum stability
- $m_t$  is a parameter of the Lagrangian  $\rightarrow \mathcal{O}_{\text{measured}}^{\text{nature}} = \mathcal{O}_{\text{predicted}}^{\text{N}^{\times}\text{LOtheory}}(m_t, \text{ren. scheme})$
- Typical mass definitions: Pole mass, MSbar mass, MSR mass

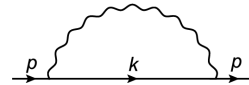


[Degrassi, Di Vita, Elias-Miro, Espinosa, Giudice, Isidori, Strumia] (2012)

# Top Quark Mass

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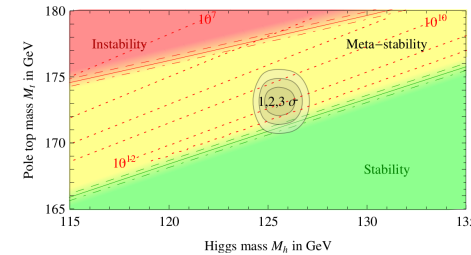
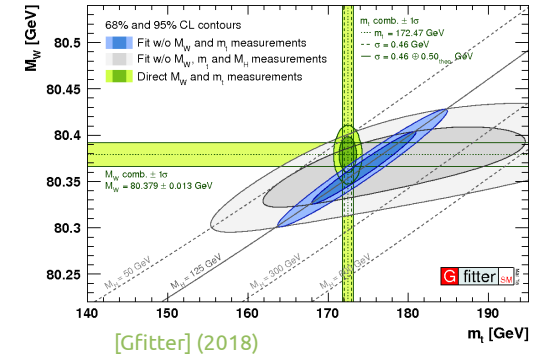
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- Typical mass definitions: Pole mass, MSbar mass, MSR mass



- Since MC generators are involved in the extraction of  $m_t$ , the term “MC mass” appeared  
 Strictly speaking: not a well-defined mass. No relation between  $\mathcal{O}_{\text{measured}}^{\text{nature}}$ ,  $\mathcal{O}_{\text{predicted}}^{\text{theory}}$ .  
 Arguments have been presented that MC mass should be numerically close to pole mass

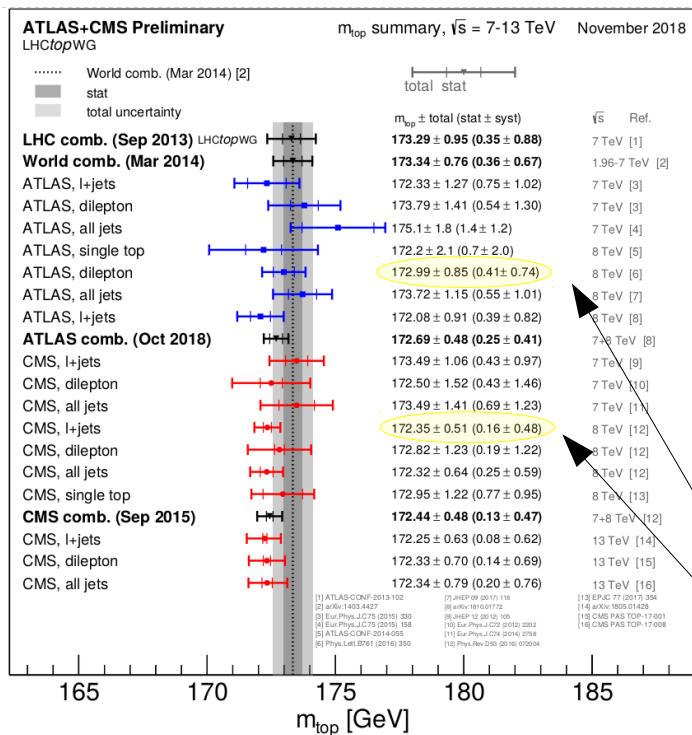
see e.g. [Beneke], [Hoang], [Mangano], [Nason]

- MC mass is a slippery notion. It would be better to discuss sources of uncertainties.
- Monte Carlo modeling cannot be avoided completely, but should be reduced to a minimum in favor of first principle calculations.



# Top Quark Mass

## State-of-the-art:



At this level of precision:  
 Spin correlated top quark production+decay needs to be accounted for. Unfolding/simulation of stable top quarks is no longer justified.

single measurements with smallest systematics



# Top Quark Mass

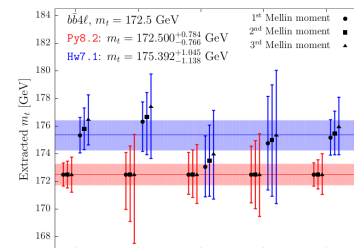
## State-of-the-art:

- NLO QCD
- Top quark decays
- Off-shell effects
- Advanced understanding of PS uncert.

### A Theoretical Study of Top-Mass Measurements at the LHC Using NLO+PS Generators of Increasing Accuracy

(Jan 2018)

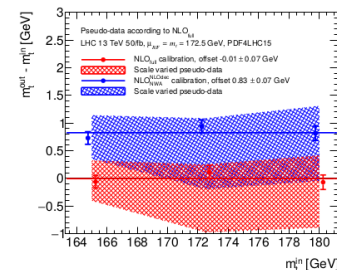
Silvia Ferrario Ravasio,<sup>a</sup> Tomáš Ježo,<sup>b</sup> Paolo Nason,<sup>c</sup> Carlo Oleari<sup>a</sup>



### NLO and off-shell effects in top quark mass determinations

(Sep 2017)

Gudrun Heinrich,<sup>a</sup> Andreas Maier,<sup>b</sup> Richard Nisius,<sup>a</sup> Johannes Schlenk,<sup>c</sup> Markus Schulze,<sup>d</sup> Ludovic Scyboz,<sup>a</sup> Jan Winter<sup>c</sup>



### Fragmentation uncertainties in hadronic observables for top-quark mass measurements

Gennaro Corcella<sup>a</sup>, Roberto Franceschini<sup>b</sup>, Doojin Kim<sup>c,\*</sup>

<sup>a</sup> INFN, Laboratori Nazionali di Frascati, Via E. Fermi 40, 00044 Frascati (RM), Italy

<sup>b</sup> Dipartimento di Matematica e Fisica, Università degli Studi Roma Tre and INFN, sezione di Roma Tre, I-00146 Rome, Italy

<sup>c</sup> Theoretical Physics Department, CERN, CH-1211 Geneva 23, Switzerland

Received 22 December 2017; received in revised form 19 February 2018; accepted 20 February 2018

Available online 27 February 2018

Editor: Tommy Ohlsson

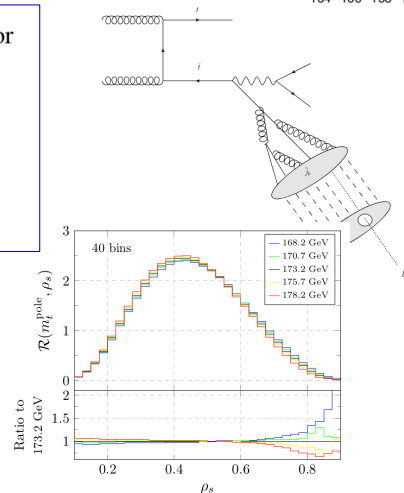
Journal of High Energy Physics

March 2018, 2018:169 | Cite as

### Top quark mass studies with $t\bar{t}j$ at the LHC

Authors Authors and affiliations

G. Bevilacqua, H. B. Hartanto, M. Kraus, M. Schulze, M. Worek ✉



# New Physics in Single Top

# New Physics in Single Top

Eur. Phys. J. C (2018) 78:919  
https://doi.org/10.1140/epjc/s10052-018-6399-3

THE EUROPEAN  
PHYSICAL JOURNAL C



Regular Article - Theoretical Physics

## Effective operators in $t$ -channel single top production and decay

M. de Beurs<sup>1</sup>, E. Laenen<sup>1,2,3</sup>, M. Vreeswijk<sup>1</sup>, E. Vryonidou<sup>1,4,a</sup>

<sup>1</sup> Nikhef, Science Park 105, Amsterdam, The Netherlands

<sup>2</sup> ITFA, University of Amsterdam, Science Park 904, Amsterdam, The Netherlands

<sup>3</sup> IIF, Utrecht University, Leuvenlaan 4, Utrecht, The Netherlands

<sup>4</sup> CERN Theory Division, 1211 Geneva 23, Switzerland

$$\mathcal{L}_{Wtb}^{\text{SM}} = - \sum_{f=d,s,b}^3 \frac{gV_{tf}}{\sqrt{2}} \bar{q}_f(x) \gamma^\mu P_L t(x) W_\mu(x) + \text{h. c.}$$

$$O_{\varphi Q}^{(3)} = i \frac{1}{2} y_t^2 \left( \varphi^\dagger \overleftrightarrow{D}_\mu^I \varphi \right) (\bar{Q} \gamma^\mu \tau^I Q)$$

$$O_{tW} = y_t g_w (\bar{Q} \sigma^{\mu\nu} \tau^I t) \tilde{\varphi} W_{\mu\nu}^I$$

$$O_{qQ,rs}^{(3)} = (\bar{q}_r \gamma^\mu \tau^I q_s) (\bar{Q} \gamma_\mu \tau^I Q)$$

} simultaneously affect  
production and decay

# New Physics in Single Top

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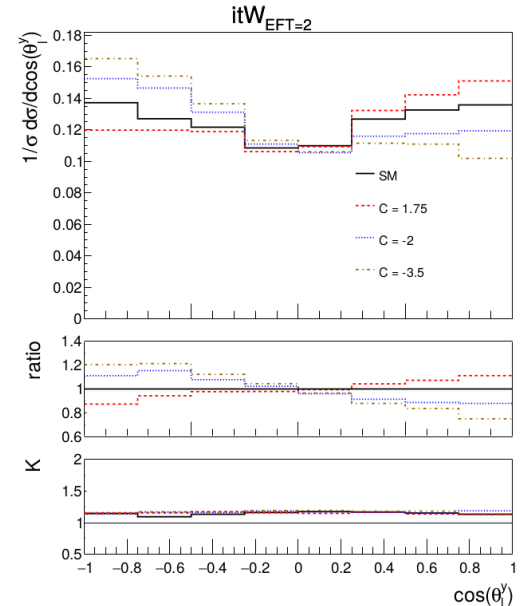
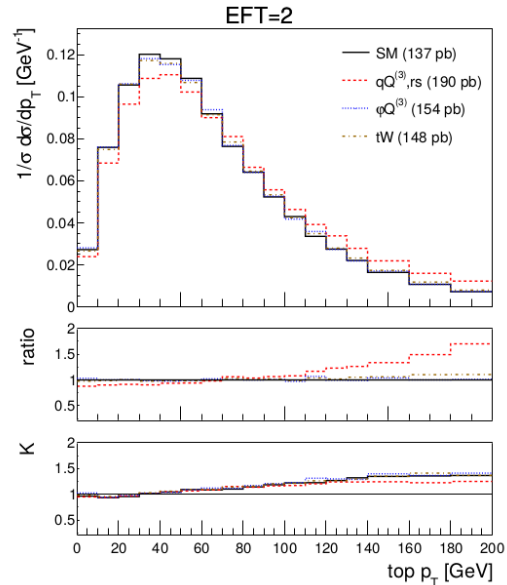
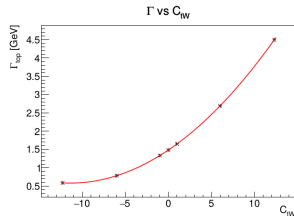
$$O_{qQ,rs}^{(3)} = (\bar{q}_r \gamma^\mu \tau^I q_s) (\bar{Q} \gamma_\mu \tau^I Q)$$

simultaneously affect  
 production and decay

→ First time consistent treatment at NLO QCD

e.g. top quark width changes:

$$\Gamma_{\text{top}}(C_{tW}) = \Gamma_{\text{SM}} + \frac{1\text{TeV}^2}{\Lambda^2} C_{tW} \Gamma_{tW} + \frac{1\text{TeV}^4}{\Lambda^4} C_{tW}^2 \Gamma_{tW,tW}$$



Note: SM NNLO QCD calculations for production x decay are available see e.g. [Berger, Gao, Yuan, Zhu] (2017)

# Towards Global Analyses

# Towards Global Analyses

---

## A Monte Carlo global analysis of the Standard Model Effective Field Theory: the top quark sector

Nathan P. Hartland,<sup>1,2</sup> Fabio Maltoni,<sup>3,4</sup> Emanuele R. Nocera,<sup>2,5</sup> Juan Rojo,<sup>1,2</sup>  
Emma Slade,<sup>6</sup> Eleni Vryonidou,<sup>7</sup> and Cen Zhang<sup>8</sup>

**Basic Idea:** Use all available top quark measurements and allow for most general NP parametrization. Then do a simultaneous fit to all degrees of freedom.

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**Basic Idea:** Use all available top quark measurements and allow for most general NP parametrization. Then do a simultaneous fit to all degrees of freedom.

Class	Notation	Degree of Freedom	Operator Definition	Diagram	
QQQQ	0Qq1	$c_{QQ}^1$	$2C_{qq}^{1(3333)} - \frac{3}{2}C_{qq}^{2(3333)}$	Top quark pair	
	0Qq8	$c_{QQ}^8$	$8C_{qq}^{3(3333)}$	ttW	
	0Qt1	$c_{Qt}^1$	$C_{uu}^{1(3333)}$	ttZ	
	0Qt8	$c_{Qt}^8$	$C_{uu}^{8(3333)}$	ttb	
	0Qb1	$c_{Qb}^1$	$C_{dd}^{1(3333)}$	ttW	
	0Qb8	$c_{Qb}^8$	$C_{dd}^{8(3333)}$	ttZ	
	0tt1	$c_{tt}^1$	$C_{uu}^{3(3333)}$	ttb	
	0tb1	$c_{tb}^1$	$C_{dd}^{3(3333)}$	ttW	
	0tb8	$c_{tb}^8$	$C_{dd}^{3(3333)}$	ttZ	
	0QtQb1	$c_{QtQb}^1$	$C_{quqd}^{1(3333)}$	ttW	
	0QtQb8	$c_{QtQb}^8$	$C_{quqd}^{8(3333)}$	ttZ	
	QQqq	081qq	$c_{Qq}^{1,8}$	$C_{qq}^{1(3331)} + 3C_{qq}^{2(3331)}$	ttW
		011qq	$c_{Qq}^{1,1}$	$C_{qq}^{1(3331)} + \frac{1}{6}C_{qq}^{8(3331)} + \frac{1}{2}C_{qq}^{3(3331)}$	ttZ
		083qq	$c_{Qq}^{3,8}$	$C_{qq}^{3(3331)} - C_{qq}^{8(3331)}$	ttb
013qq		$c_{Qq}^{3,1}$	$C_{qq}^{3(3331)} + \frac{1}{6}(C_{qq}^{1(3331)} - C_{qq}^{8(3331)})$	ttW	
08qt		$c_{qt}^8$	$C_{qu}^{8(3331)}$	ttZ	
01qt		$c_{qt}^1$	$C_{qu}^{1(3331)}$	ttb	
08ut		$c_{tu}^8$	$2C_{uu}^{(3331)}$	ttW	
01ut		$c_{tu}^1$	$C_{uu}^{(3331)} + \frac{1}{3}C_{uu}^{8(3331)}$	ttZ	
08qu		$c_{qu}^8$	$C_{qu}^{8(3331)}$	ttb	
01qu		$c_{qu}^1$	$C_{qu}^{1(3331)}$	ttW	
08dt		$c_{td}^8$	$8C_{qd}^{(3331)}$	ttZ	
01dt		$c_{td}^1$	$C_{qd}^{1(3331)}$	ttb	
08qd		$c_{qd}^8$	$8C_{qd}^{(3331)}$	ttW	
01qd		$c_{qd}^1$	$C_{qd}^{1(3331)}$	ttZ	

$QQ + V, G, \varphi$   
 DtG, CtG, Re{C<sub>uG</sub><sup>(33)</sup>}  
 OtW, CtW, Re{C<sub>uW</sub><sup>(33)</sup>}  
 ObW, CtW, Re{C<sub>uW</sub><sup>(33)</sup>}  
 OtZ, CtZ, Re{-8yC<sub>uB</sub><sup>(33)</sup> + c<sub>W</sub>C<sub>uW</sub><sup>(33)</sup>}  
 OfF, CtF, Re{C<sub>uφ</sub><sup>(33)</sup>}  
 Ofq3, CtF, C<sub>φq</sub><sup>(33)</sup>  
 OpQH, CtF, C<sub>φq</sub><sup>(33)</sup> - C<sub>φq</sub><sup>(33)</sup>  
 Opt, CtF, C<sub>φφ</sub><sup>(33)</sup>  
 Otφ, CtF, Re{C<sub>bφ</sub><sup>(33)</sup>}

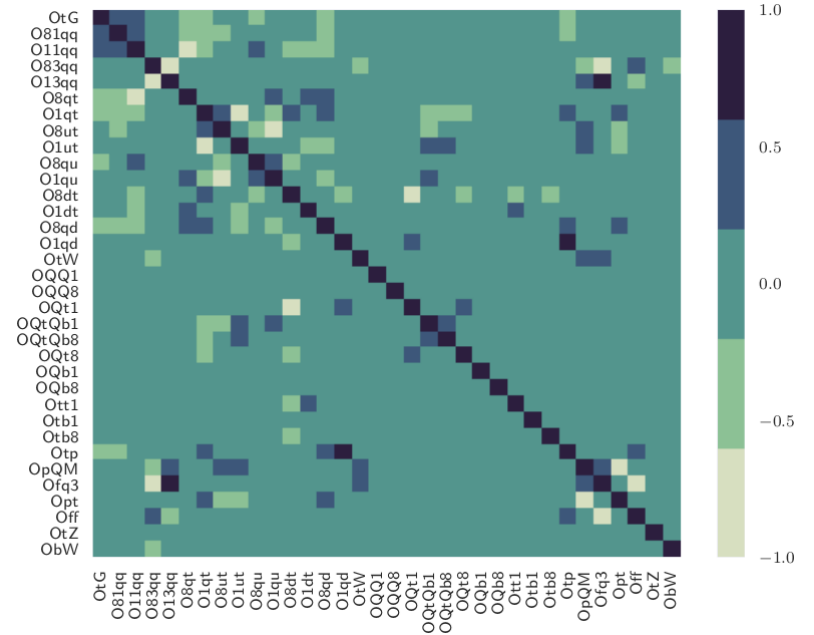
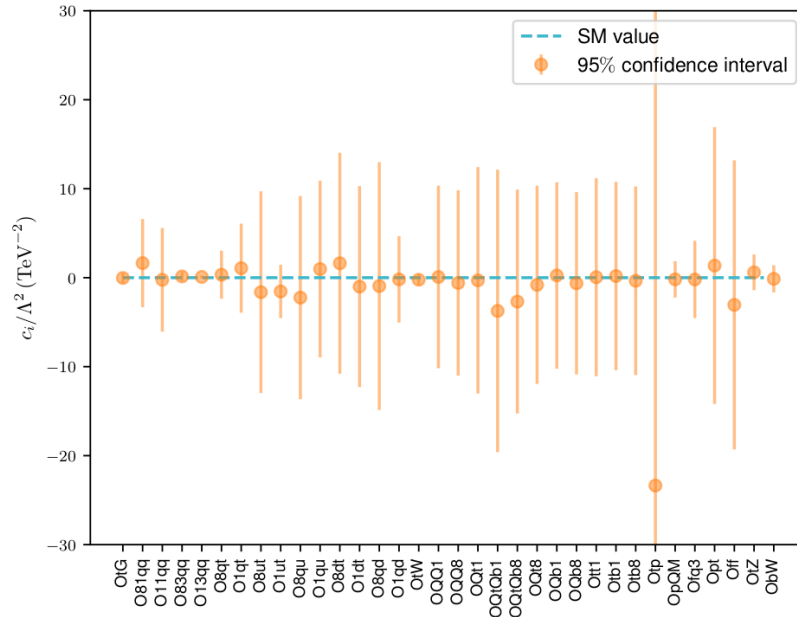
Notation	Sensitivity at O(Λ <sup>-2</sup> ) (O(Λ <sup>-4</sup> ))								
	t $\bar{t}$	single-top	tW	tZ	tW	tZ	tH	t $\bar{t}$ t	t $\bar{t}$ b
0Qq1								✓	✓
0Qq8								✓	✓
0Qt1								✓	✓
0Qt8								✓	✓
0Qb1								✓	✓
0Qb8								✓	✓
0tt1								✓	
0tb1								✓	
0tb8								✓	
0QtQb1								(✓)	
0QtQb8								(✓)	
081qq	✓				✓	✓	✓	✓	✓
011qq	[✓]				[✓]	[✓]	[✓]	✓	✓
083qq	✓	[✓]		[✓]	[✓]	[✓]	[✓]	✓	✓
013qq	✓	✓		✓	[✓]	[✓]	[✓]	✓	✓
08qt	✓				✓	✓	✓	✓	✓
01qt	[✓]				[✓]	[✓]	[✓]	✓	✓
08ut	✓					✓	✓	✓	✓
01ut	[✓]					[✓]	[✓]	✓	✓
08qu	✓					✓	✓	✓	✓
01qu	[✓]					[✓]	[✓]	✓	✓
08dt	✓					✓	✓	✓	✓
01dt	[✓]					[✓]	[✓]	✓	✓
08qd	✓					✓	✓	✓	✓
01qd	[✓]					[✓]	[✓]	✓	✓
0tG	✓		✓		✓	✓	✓	✓	✓
0tW		✓	✓	✓					
0bW		(✓)	(✓)	(✓)					
0tZ					✓				
0fF		(✓)	(✓)	(✓)					
0fQ3			✓	✓					
0pQH			✓	✓					
0pt					✓				
0tφ						✓			

34 operators, 30 different measurements form 10 processes

# Towards Global Analyses

Main ingredient: Generation of MC replicas (N=1000), similar to PDF fits

Results:

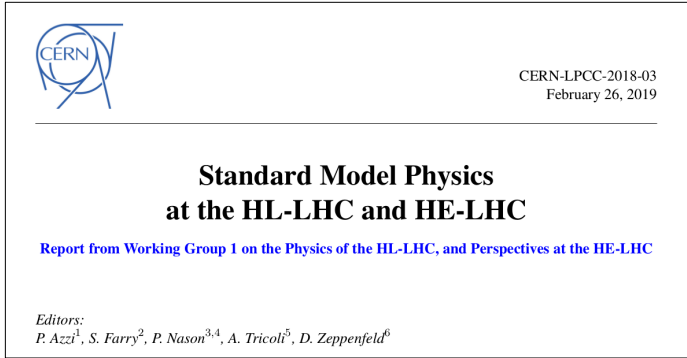


→ see talk by Emma Slade



Community Effort: HL-LHC and HE-LHC

# Community Effort: LHC-HL & LHC-HE Working Groups

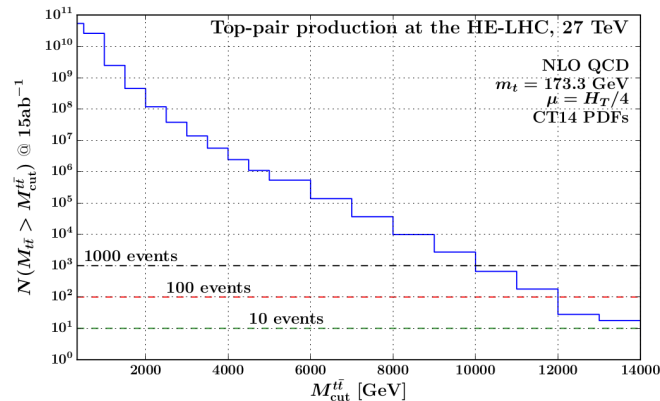
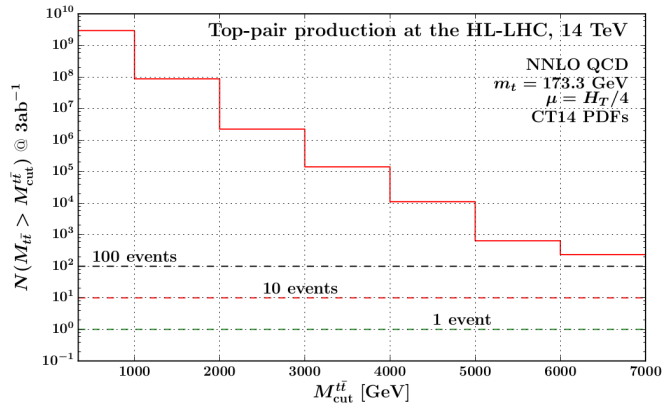


A large compendium of studies for

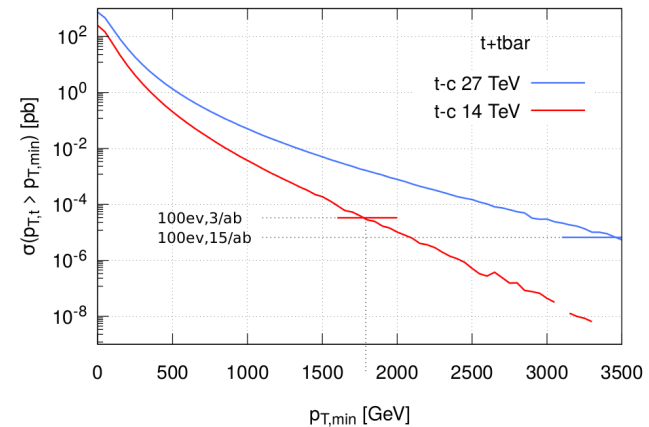
- HL-LHC: 14 TeV, 3000 fb<sup>-1</sup>
- HE-LHC: 27 TeV, 15 000 fb<sup>-1</sup>

A few selections: ...

## Top quark pair production

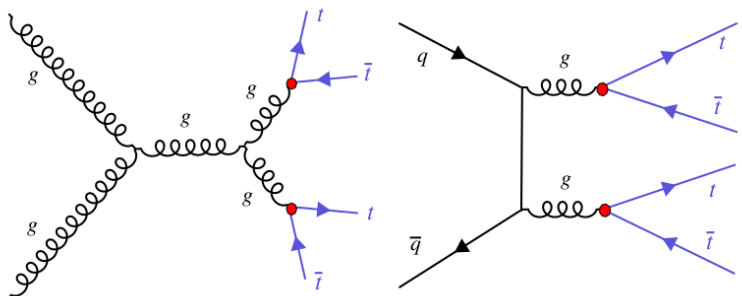


## Single top production



# Community Effort: LHC-HL & LHC-HE Working Groups

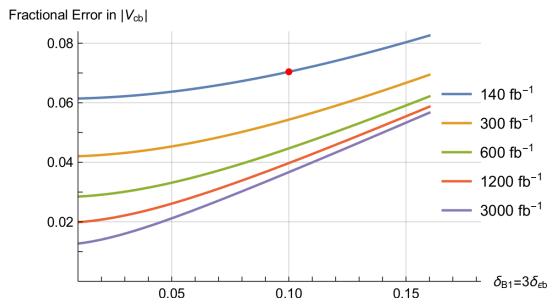
## Four top production



HL-LHC	Basic
$\bar{t}t\bar{t}t_H$	577.22
$\bar{t}t\bar{t}t_{g/Z/\gamma}$	5006.34
$\bar{t}t\bar{t}t_{\text{int}}$	-764.67
$\bar{t}t$	$2.5 \times 10^8$
$\bar{t}tW^+$	32670
$\bar{t}tW^-$	16758
$\bar{t}tZ$	24516
$W^\pm W^\pm jj$	4187.7

HE-LHC	Basic
$\bar{t}t\bar{t}t_H$	15174.4
$\bar{t}t\bar{t}t_{g/Z/\gamma}$	148898.
$\bar{t}t\bar{t}t_{\text{int}}$	-20141.9
$\bar{t}t$	$3.3 \times 10^7$
$\bar{t}tW^+$	$1.3 \times 10^6$
$\bar{t}tW^-$	$7.6 \times 10^5$
$\bar{t}tZ$	$3.9 \times 10^6$
$W^\pm W^\pm jj$	888700

## Vcb extraction



Quote: “To date,  $|V_{cb}|$  has always been measured in  $B$  decays, i.e. at an energy scale  $mb$ , far below the weak scale, and it is currently known to an uncertainty of about 2%.”

## Rare decays

$B$ limit at 95% C.L.	$3 \text{ ab}^{-1}, 14 \text{ TeV}$	$15 \text{ ab}^{-1}, 27 \text{ TeV}$	Ref.
$t \rightarrow gu$	$3.8 \times 10^{-6}$	$5.6 \times 10^{-7}$	[731]
$t \rightarrow gc$	$32.1 \times 10^{-6}$	$19.1 \times 10^{-7}$	[731]
$t \rightarrow Zq$	$2.4 - 5.8 \times 10^{-5}$		[743]
$t \rightarrow \gamma u$	$8.6 \times 10^{-6}$		[734]
$t \rightarrow \gamma c$	$7.4 \times 10^{-5}$		[734]
$t \rightarrow Hq$	$10^{-4}$		[743]

# SUMMARY

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- Studying top quark properties is a way of searching for physics beyond the SM
- The top quark system is an ideal place because it yields sensitivity to a large variety of possible New Physics interactions
- Assuming  $SU(2) \times U(1)$  symmetry holds, certain top quark interactions are related
- I presented a selection of state-of-the-art on:
  - Spin correlations
  - Top quark mass
  - Single top and Top pair associated production
- General trend in theory: Modeling is replaced by first principle calculations  
This is what is required for reliably interpreting the data

Thanks for your attention!