

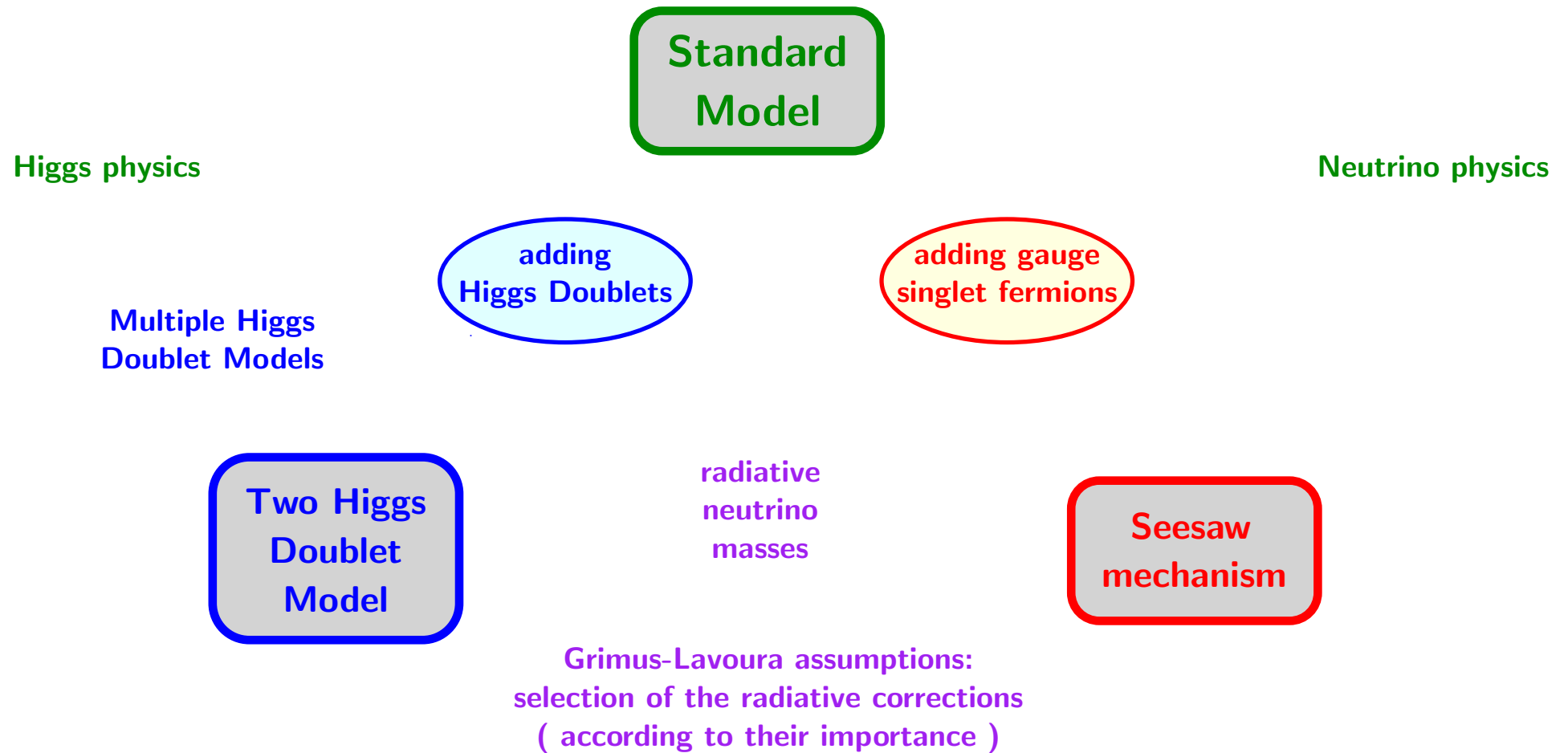
**The Grimus-Neufeld model:  
Restricting Yukawa couplings  
with the neutrino sector**

full time	<i>Vytautas Dūdėnas, <u>Thomas Gajdosik</u></i>
part time	<i>Andrius Juodagalvis, Darius Jurčiukonis</i>
former students	<i>Simonas Draukšas, Anton Kunčinas</i>
bachelor students	<i>Rokas Garbačauskas, Vytautas Mickus</i>
master students	<i>Paulius Juodsnukis, Gediminas Ringys</i>

Our model: the 312- $\nu$ SM (i.e. the Grimus-Neufeld model)

Standard Model (SM) + one fermionic singlet + two Higgs doublets

- is not a new idea: [G-N] W. Grimus and H. Neufeld, Nucl. Phys. B **325** (1989) 18.



The 312- $\nu$ SM has parameters additionally to the "original" SM

- the singlet Majorana mass term  $M_R$
- the neutrino Yukawa coupling of the first Higgs doublet

$$(Y_N^{(1)})_j := \tilde{Y}_{Lj}^1 = \frac{\sqrt{2}}{v} (M_D)_j \dots \text{the "Dirac mass" term}$$

- the Yukawa couplings of the second Higgs doublet

$$(Y_E^{(2)})_{jk} := Y_{Ljk}^2 \text{ to lepton doublets and charged lepton singlets } \ell_{Rj}$$

$$(Y_N^{(2)})_j := \tilde{Y}_{Lj}^2 \text{ to lepton doublets and neutral fermionic singlet } N_R$$

- additional parameters in the Higgs sector

[H-ON] H. E. Haber and D. O'Neil, Phys. Rev. D **83** (2011) 055017 [arXiv:1011.6188 [hep-ph]]

–  $m_{H_2}^2, m_{H_3}^2, m_{H^\pm}^2$  masses of the additional Higgs bosons

–  $\theta_{12}, \theta_{13}$  mixing angles between the neutral Higgs fields

assuming CP conservation forces the mixing to the pseudo-scalar  $A^0$  to zero:  $\theta_{13} = 0$

–  $Z_2, Z_3, Z_7 \dots$  parameters of the Higgs potential,

not fixed by tree level mass relations

## 312- $\nu$ SM generic model predictions

- additional Higgses:  $H^\pm, H_{(1,)}^0, H_{2,3}^0$  ( like the generic 2HDM )  
⇒ generic 2HDM phenomenology
  - one heavy fermionic singlet ("heavy neutrino")
    - most probably invisible @ colliders ( like a neutrino )
  - only one seesaw neutrino at tree level
  - one light neutrino gets a radiative mass at one-loop level
  - the third light neutrino can get a radiative mass at 2 or 3-loop level
    - ! we have only a single mass difference at tree level !
- ⇒ we need the one-loop level to determine parameters

## Using the Grimus-Lavoura procedure ( i.e. approximation )

[G-L] W. Grimus and L. Lavoura, JHEP **0011** (2000) 042 [arXiv:hep-ph/0008179].

allows to determine the "light" neutrino masses  $\tilde{m}_j$  analytically :

$$\tilde{m}_o = 0 \quad \text{and} \quad \tilde{m}_{r,s} = \tilde{m}_{r,s} \left[ m_h^2, m_H^2, m_A^2, \theta_{12}, v^2, \tilde{m}_4, m_D^2, d, d' = |d'|e^{i\phi'} \right]$$

- we can invert these relations and determine ( with  $d' = |d'|e^{i\phi'}$  )

$$d^2 = d^2 \left[ m_h^2, m_H^2, m_A^2, \theta_{12}, v^2, \tilde{m}_r, \tilde{m}_s, \tilde{m}_4, m_D^2 \right]$$

$$|d'| = |d'| \left[ m_h^2, m_H^2, m_A^2, \theta_{12}, v^2, \tilde{m}_r, \tilde{m}_s, \tilde{m}_4, m_D^2, \phi' \right]$$

- which fully determine the Yukawa couplings:

$$(Y_N^{(1)})_k = \frac{\sqrt{2}m_D}{v} u_{ks} \quad (Y_N^{(2)})_k = d u_{kt} + d' u_{ks}$$

- when we express the  $u_{k\alpha}$  by  $U_{\text{PMNS}}$  and the mixing of the states

⇒ possible predictions

## Comparison with SPheno and FlexibleSUSY

[Drau] (<http://talpykla.elaba.lt/elaba-fedora/objects/elaba:29420143/datastreams/MAIN/content>)

- S. Draukšas implemented the GN model in SPheno and FlexibleSUSY
  - the code generation worked
  - SPheno could not reproduce the small neutrino masses
  - FlexibleSUSY gave qualitatively an expected spectrum

## Plans

- We want a full renormalization of the GN model
  - giving us an estimate of the size of the GL approximation
- We want to extend the comparison with SPheno and FlexibleSUSY
- FlexibleSUSY allows predictions for leptonic rare processes
  - like:  $\mu \rightarrow e\gamma$ ,  $\mu \rightarrow eee$ , ...
  - when the parameters are constrained by other "normal" measurements