

# A critical look at the *B*-decay anomalies at the end of 2019

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IISER Mohali



WHEPP XVI, IIT Guwahati  
December 1-10, 2019

*An experimental*  
~~A~~ critical look at the  
*B*-decay anomalies  
at the end of 2019

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# Disclaimer

- Not a real expert, will try to summarize and introduce needed information for the anomalies.
- Hopeful that the material cover is sufficient for most of the people to follow the “discussions to follow” in the coming days.
- Apologies if some statement(s) is(are) wrong.
- Will introduce “*B-anomalies*” and their implications to be explained in detail by *Prof. R. Mohanta* “Combined explanation  $R_D/R_{D^*}$  and  $R_K/R_{K^*}$ ” on Wednesday.

# B decay anomalies

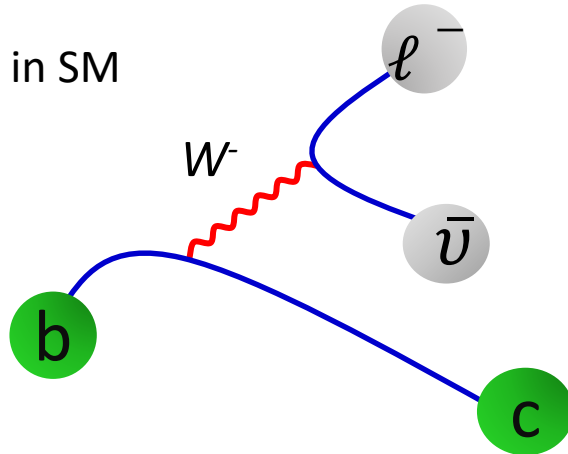
Two words are enough to wind up my presentation:

$$R_{D,D^*}$$

$b \rightarrow c$  Charged current

$b \rightarrow c\tau\nu$

Tree-level in SM



$$R_{D^{(*)}} = \frac{\mathcal{B}(B \rightarrow D^{(*)}\tau\nu)}{\mathcal{B}(B \rightarrow D^{(*)}\ell\nu)}$$

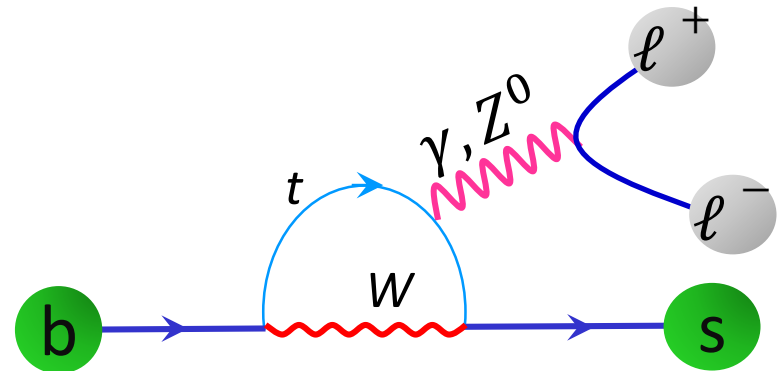
$$R_{D^{(*)}}^{exp} > R_{D^{(*)}}^{SM}$$

$$R_{K,K^*}$$

$b \rightarrow s$  Neutral current

$b \rightarrow s\ell\ell$

Loop-level in SM



$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)}\mu^+\mu^-)}{\mathcal{B}(B \rightarrow K^{(*)}e^+e^-)}$$

$$R_{K^{(*)}}^{exp} < R_{K^{(*)}}^{SM}$$

Scale of NP  
must be "low"  
 $\Lambda \sim \text{TeV}$

Scale of NP  
can be "high"  
 $\Lambda \sim 30\text{-}50 \text{ TeV}$

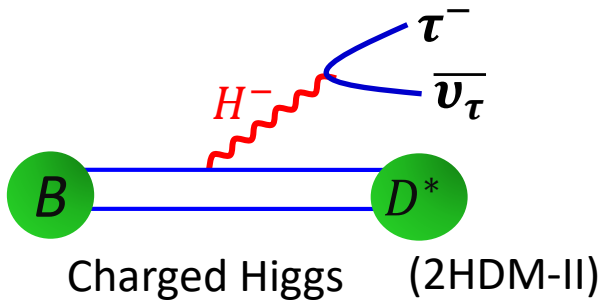
Lepton Flavor Universality Violation (LFUV) in  $B$  decays

$$B \rightarrow D^{(*)} \tau \nu$$

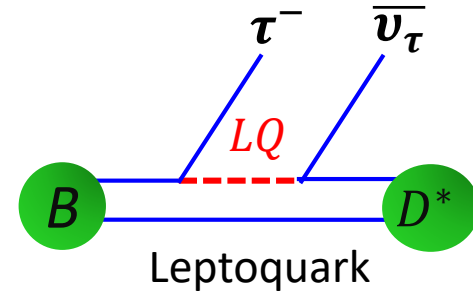
Not a rare decay, Branching fraction : 1-2 %

- Allow one to test theory of low-energy QCD, which contribute to  $\bar{B} \rightarrow D^*$  transition.
- Weak interaction can be tested precisely.

$\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau$  decays are sensitive to new scalar fields (New Physics at tree level)



Grossman, Ligeti, PLB332, 3 (1994)  
Tanaka, Z. Phys. C 67, 321 (1995)



Davidson et al, Z. Phys. C 61, 613 (1994)

What one looks for

$$R_{D^*} = \frac{\mathcal{B}(\bar{B} \rightarrow D^* \tau^- \bar{\nu}_\tau)}{\mathcal{B}(\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell)}$$

← Signal  
←  $\ell = e, \mu$  Normalization (background)

Theory: cancels common factors :  $|V_{cb}|$  and hadronic FFs

Experiment: reduce experimental uncertainties (detector efficiencies)

$$\mathcal{R}(D)_{SM} = 0.300 \pm 0.011 \text{ Lattice, PRD92,034506 (2015)}$$

$$\mathcal{R}(D^*)_{SM} = 0.252 \pm 0.003 \text{ Fajfer et al/PRD85.094025(2012)}$$

Other variables :

$\tau$  and  $D^*$  polarization,  $q^2$  distributions, lepton momentum

2007

Observation of  $B \rightarrow D^{*+} \tau^+ \nu_\tau$   
Belle, PRL99, 191807(2007)

2008

First  $R_{D^{(*)}}$  measured  
BaBar, PRL100, 021801(2008)

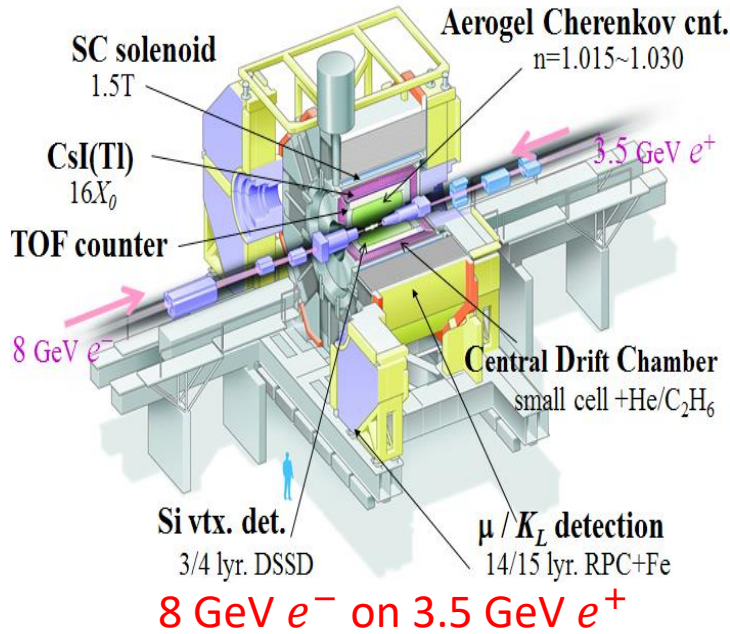
2010

Evidence of  $B \rightarrow D^0 \tau^+ \nu_\tau$   
Belle, PRD82, 072005(2010)

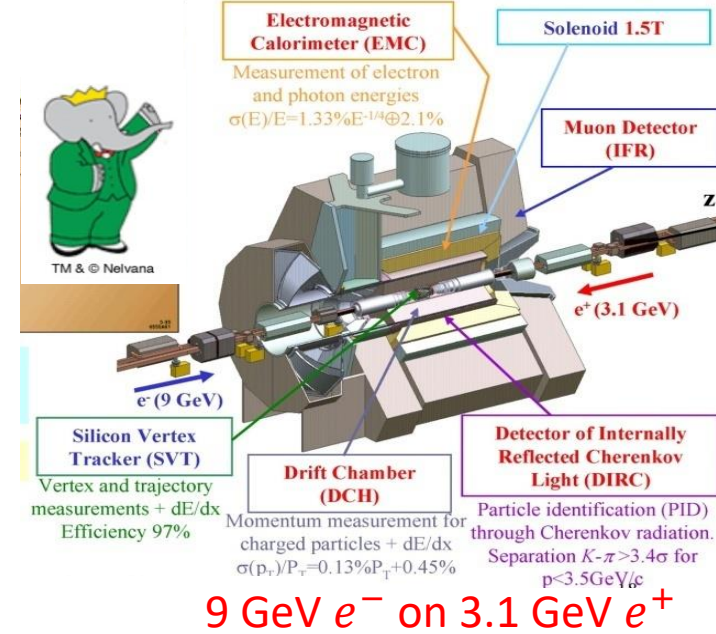
2012

Evidence of the excess  
BaBar, PRL109, 101802 (2012)

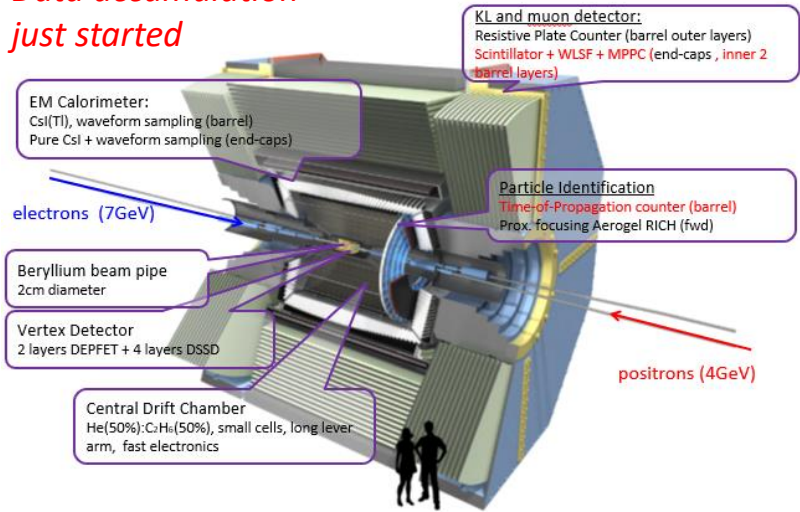
# $e^+e^-$ colliders for B physics



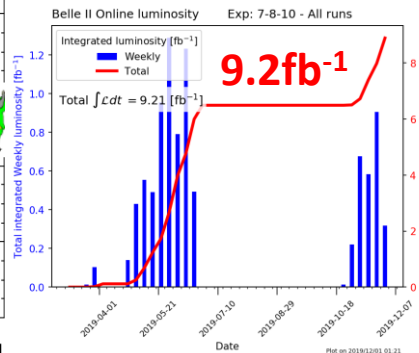
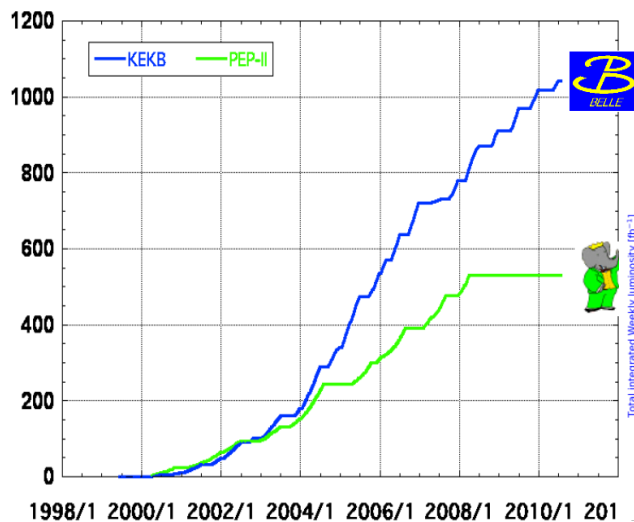
Already data accumulated



Data accumulation just started

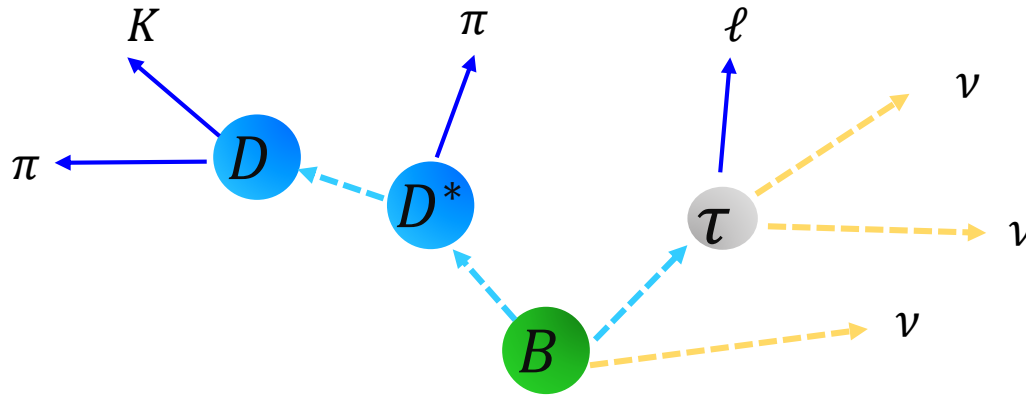


7 GeV e<sup>-</sup> on 4 GeV e<sup>+</sup>



# How one measures $R_{D^{(*)}}$ at $e^+e^-$ colliders

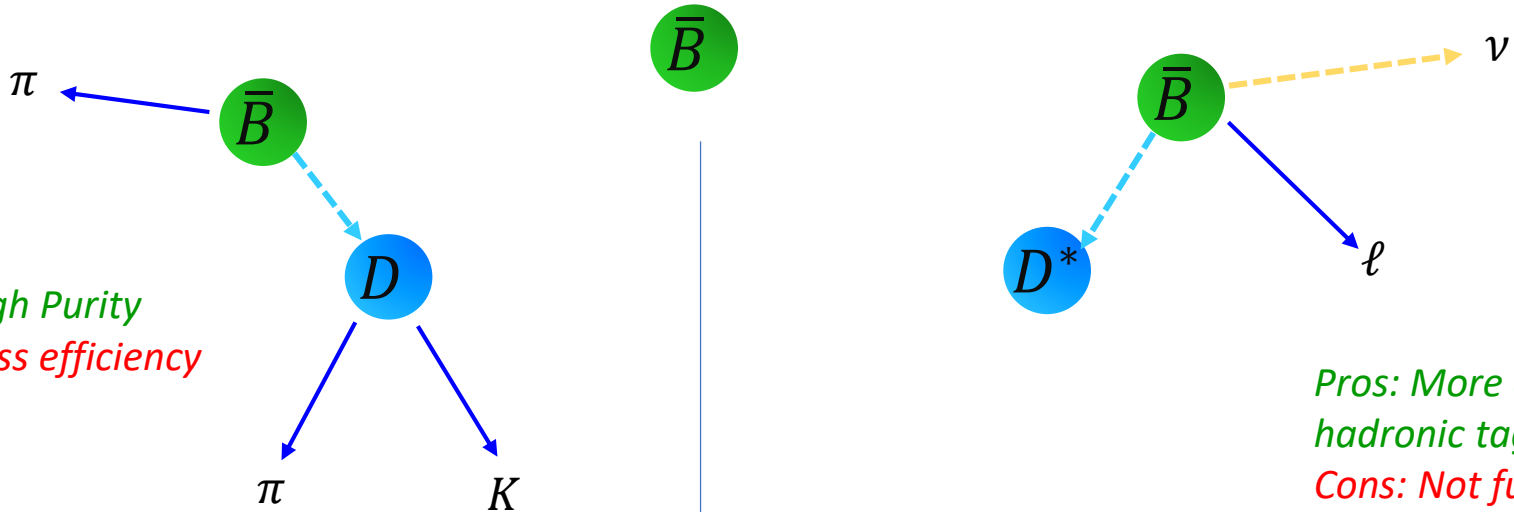
Signal side



$e^-$

$e^+$

Tag side



*Pros: High Purity*  
*Cons: Less efficiency*

*Pros: More efficient than hadronic tag*  
*Cons: Not full kinematics*

Hadronic tag ( $\epsilon_{sig} \sim 0.2\%$ )

Semileptonic tag ( $\epsilon_{sig} \sim 0.5\%$ )

Simultaneous UML fit to  
4 signal samples  $D^0\ell$ ,  $D^{*0}\ell$ ,  $D^+\ell$  and  $D^{*+}\ell$

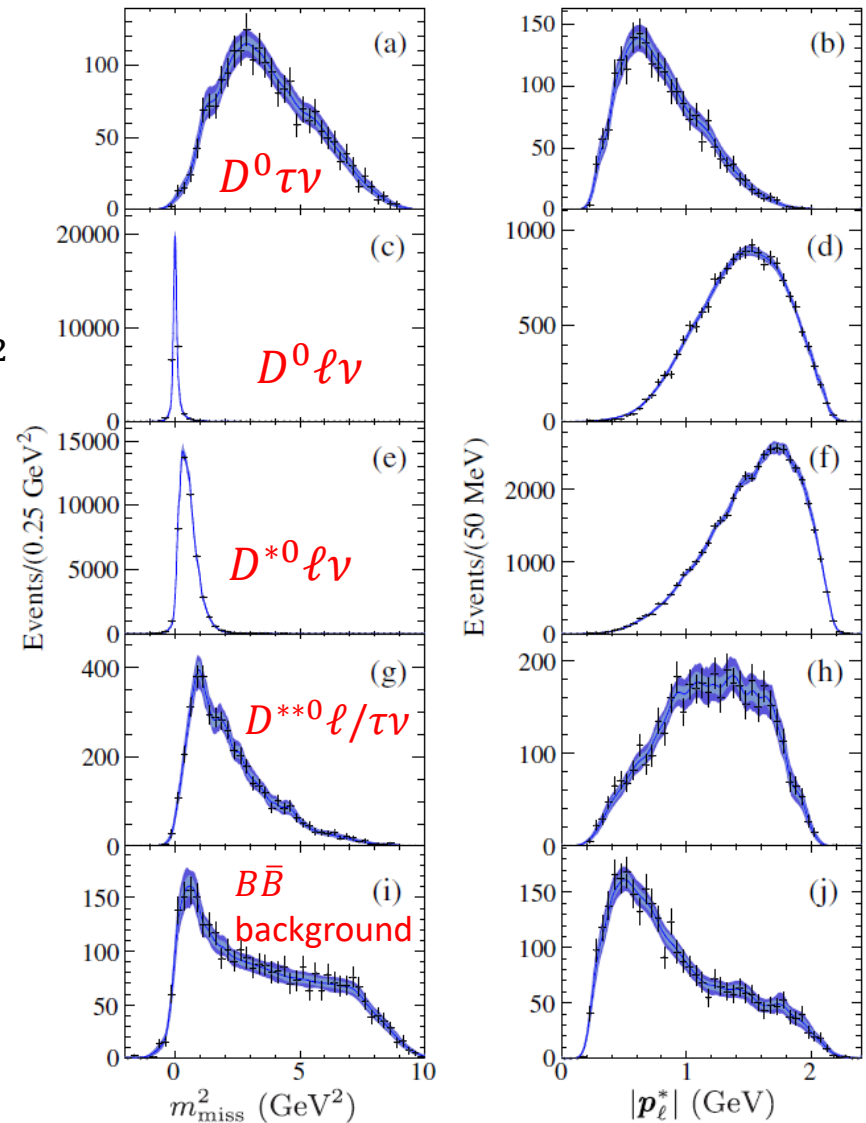
$\tau \rightarrow \mu\nu\nu$  and  $\tau \rightarrow e\nu\nu$

Signal is identified by:

- $m_{miss}^2 = (p_{e^+e^-} - p_{tag} - p_{D^{(*)}} - p_{\ell})^2$
- $|p_{\ell}^*|$  in the  $B_{sig}$  rest-frame

Signal extracted together with control  
sample of  $B \rightarrow D^{**}\ell\nu$  (addition of an  
extra  $\pi^0$ )

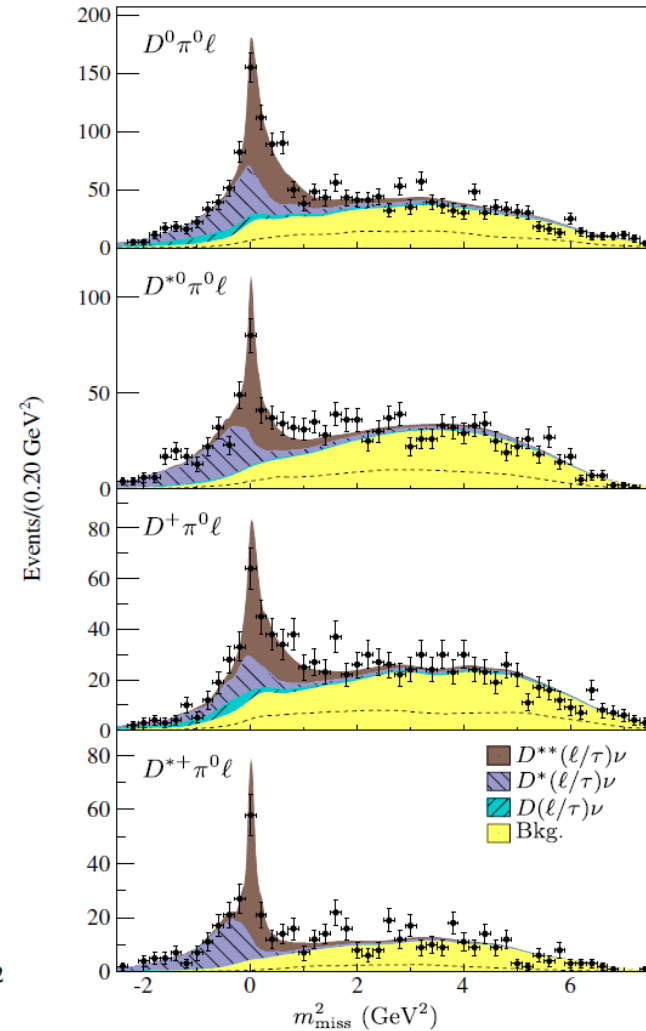
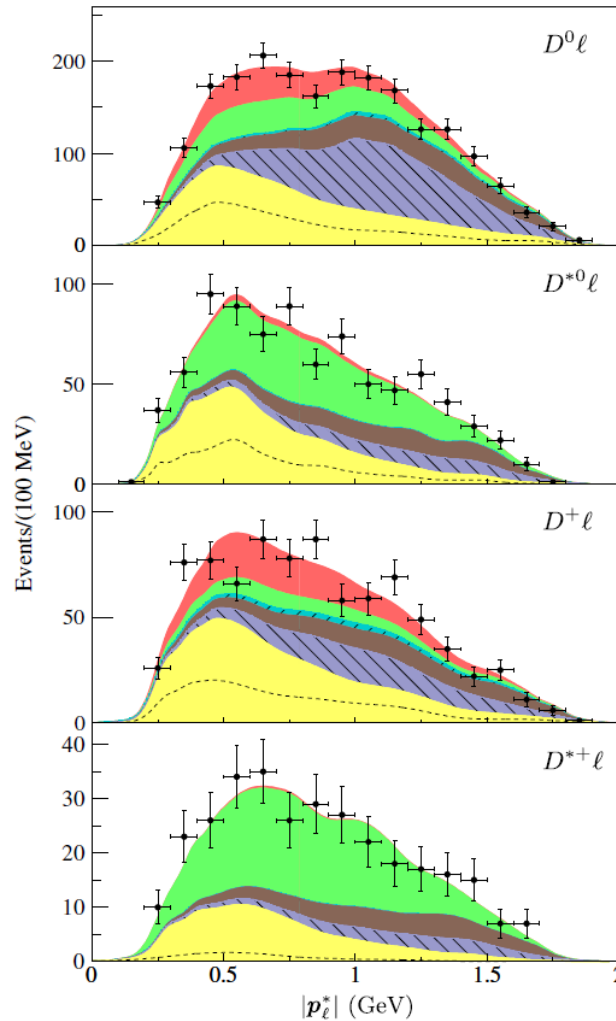
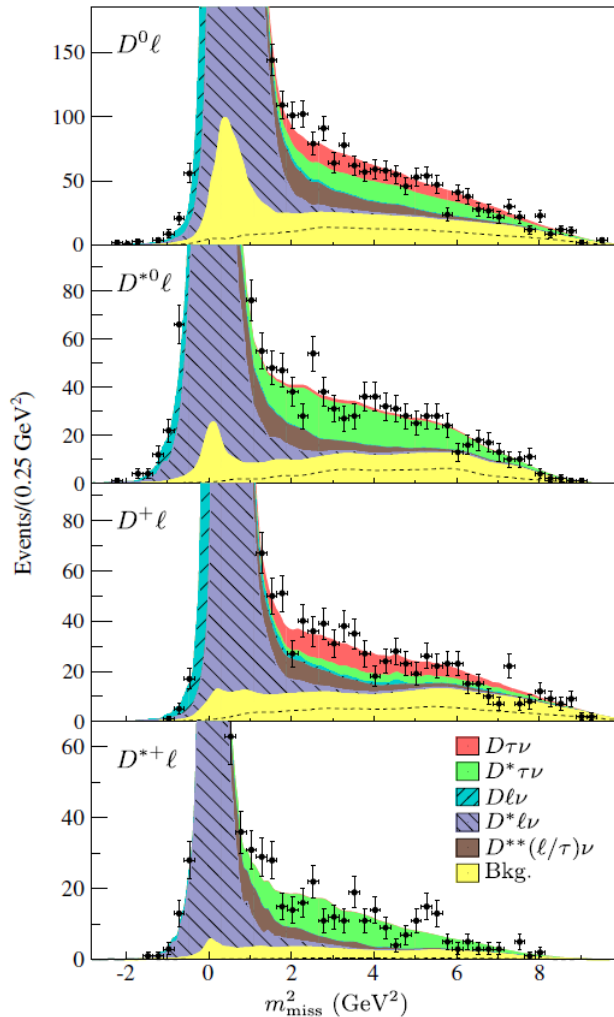
$D^0 \rightarrow K^- \pi^+, K^- K^+, K^- \pi^+ \pi^0, K^- \pi^+ \pi^- \pi^+,$   
 $K_S^0 \pi^+ \pi^-,$  and  $D^+ \rightarrow K^- \pi^+ \pi^+, K^- \pi^+ \pi^+ \pi^0, K_S^0 \pi^+,$   
 $K_S^0 \pi^+ \pi^+ \pi^-, K_S^0 \pi^+ \pi^0, K_S^0 K^+,$  with  $K_S^0 \rightarrow \pi^+ \pi^-.$





# Results

BaBar  
PRL 109, 101802(2012)  
PRD 88, 072012 (2013)



$$\mathcal{R}(D) = 0.440 \pm 0.058 \pm 0.042 \quad (2.0\sigma \text{ from SM})$$

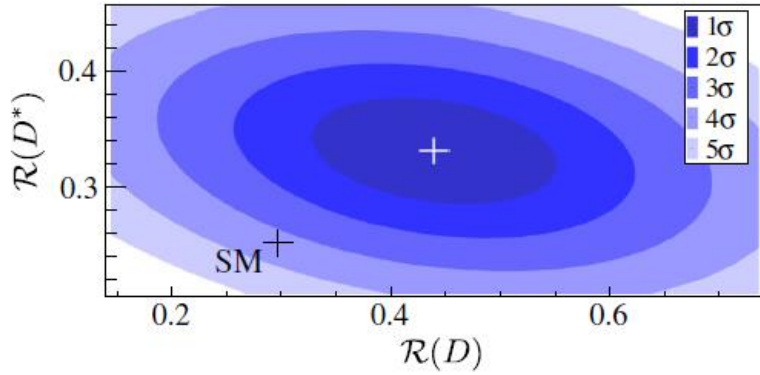
$$\mathcal{R}(D^*) = 0.332 \pm 0.024 \pm 0.018 \quad (2.7\sigma \text{ from SM})$$

$$\mathcal{R}(D)_{\text{SM}} = 0.300 \pm 0.011$$

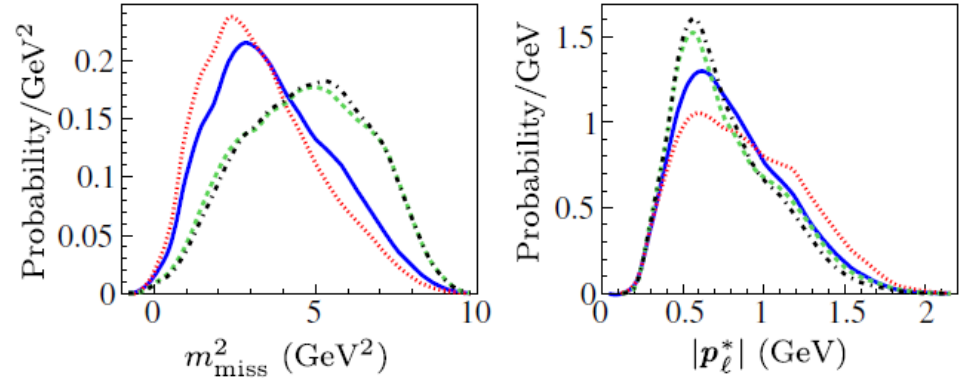
$$\mathcal{R}(D^*)_{\text{SM}} = 0.252 \pm 0.003$$

# How one should interpret the result

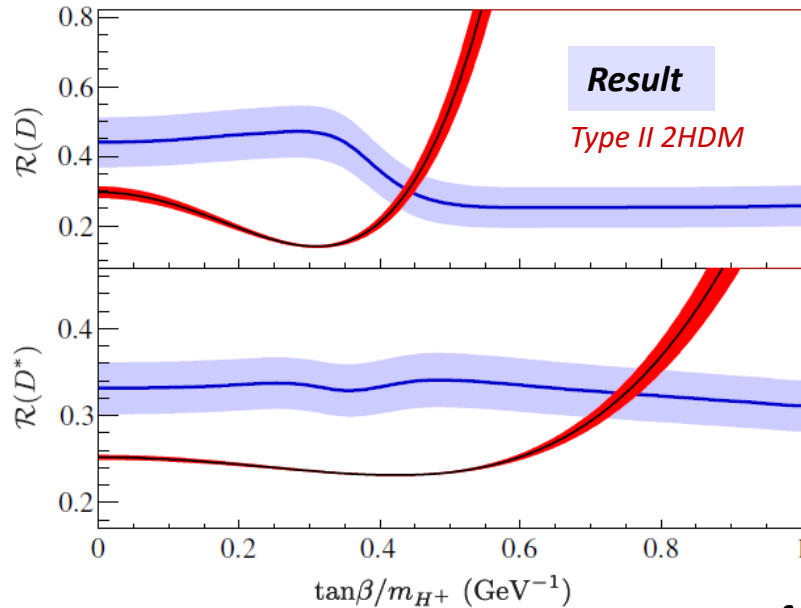
BaBar  
PRD 88, 072012 (2013)



Based on the mass and vacuum expectation (Signal PDF modifies)



— SM  
 .....  $\tan\beta/m_{H^\pm} = 0.3 \text{ GeV}^{-1}$   
 .....  $\tan\beta/m_{H^\pm} = 1 \text{ GeV}^{-1}$

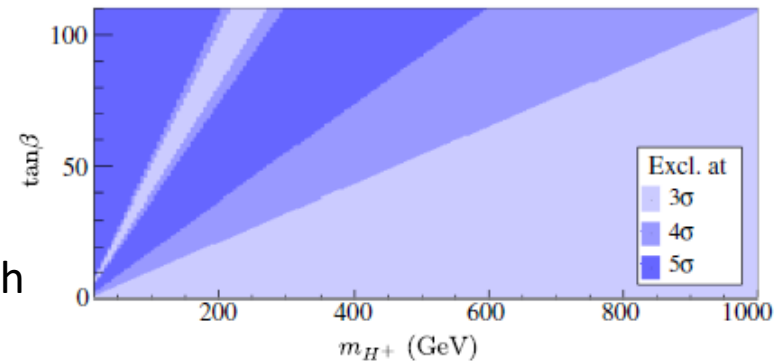


Matches value :

$$\mathcal{R}(D) \rightarrow \frac{\tan\beta}{m_{H^\pm}} = 0.44 \pm 0.02 \text{ GeV}^{-1}$$

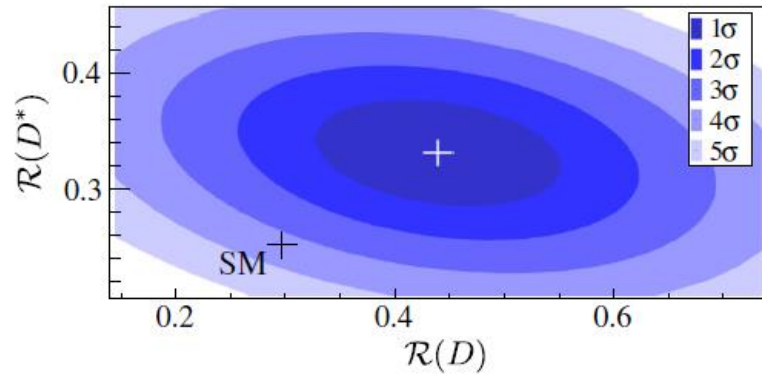
$$\mathcal{R}(D^*) \rightarrow \frac{\tan\beta}{m_{H^\pm}} = 0.75 \pm 0.04 \text{ GeV}^{-1}$$

If one takes both

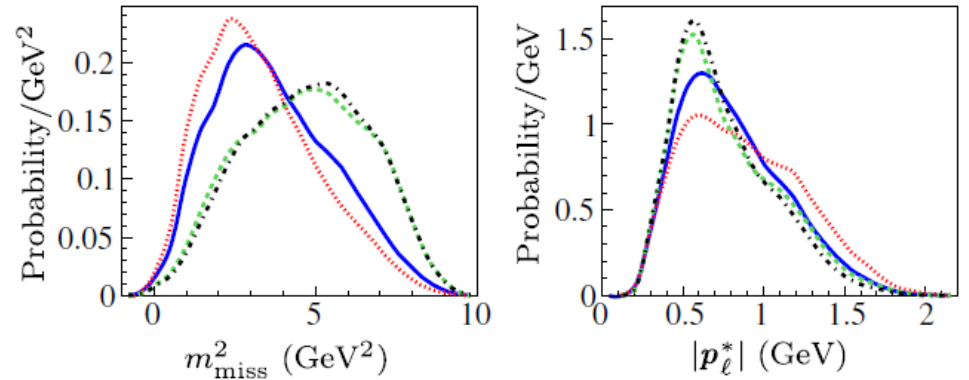


# How one ~~should~~ can interpret the result

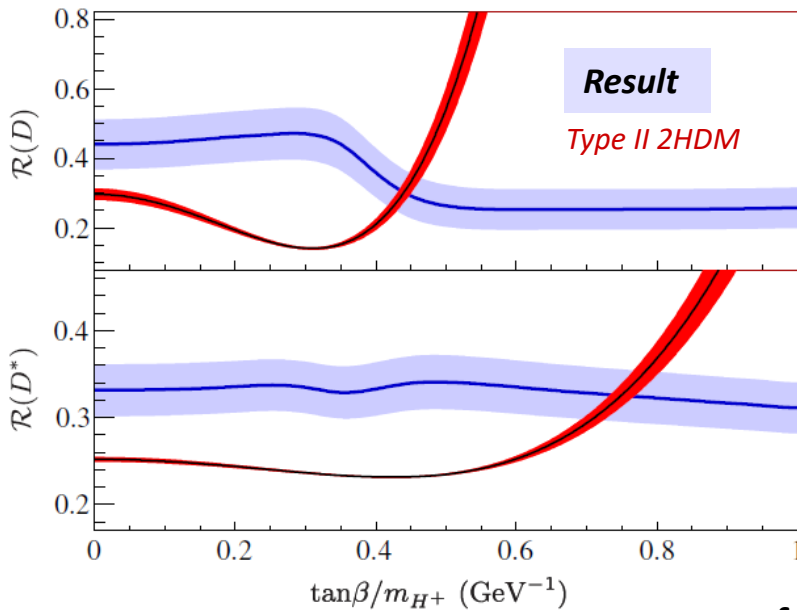
BaBar  
PRD 88, 072012 (2013)



Based on the mass and vacuum expectation (Signal PDF modifies)



— SM  
 .....  $\tan\beta/m_{H^\pm} = 0.3 \text{ GeV}^{-1}$   
 .....  $\tan\beta/m_{H^\pm} = 1 \text{ GeV}^{-1}$

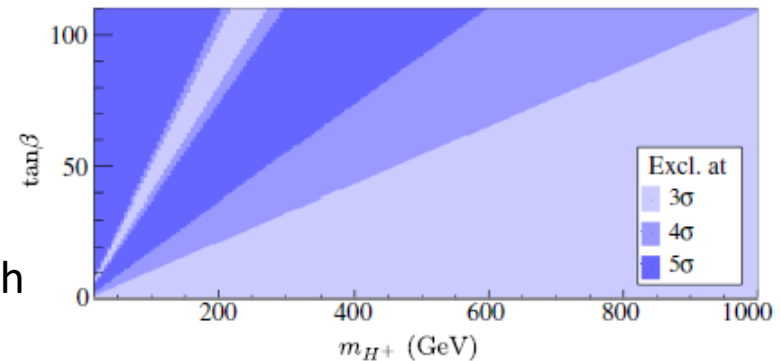


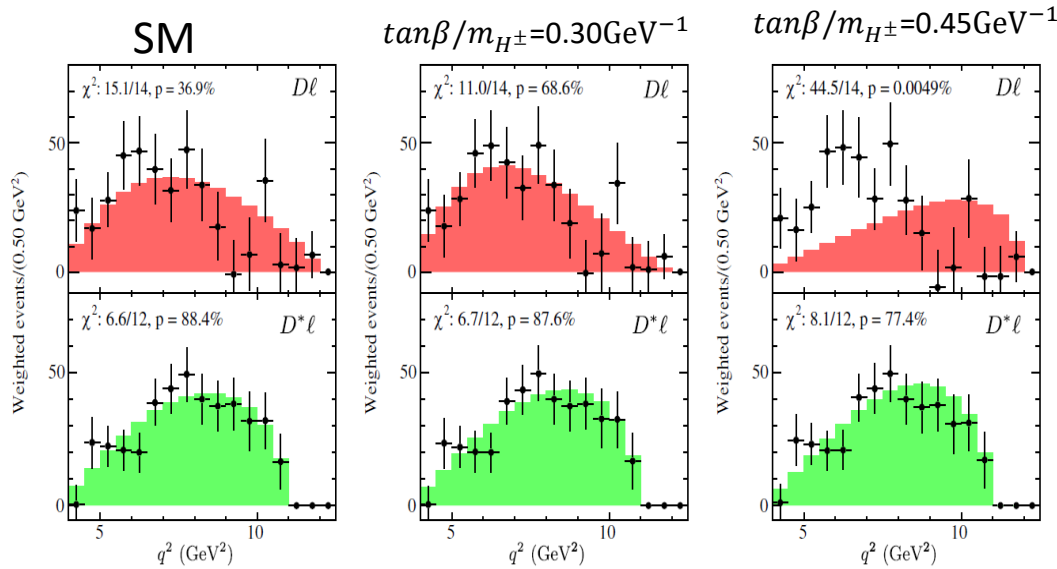
Matches value :

$$\mathcal{R}(D) \rightarrow \frac{\tan\beta}{m_{H^\pm}} = 0.44 \pm 0.02 \text{ GeV}^{-1}$$

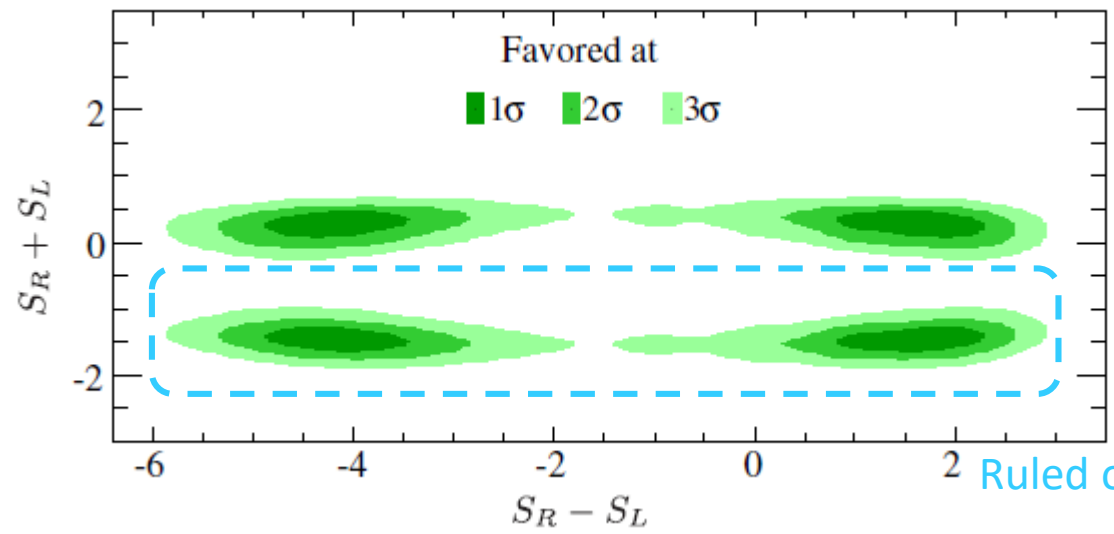
$$\mathcal{R}(D^*) \rightarrow \frac{\tan\beta}{m_{H^\pm}} = 0.75 \pm 0.04 \text{ GeV}^{-1}$$

If one takes both





Type III 2HDM survives  
 $|S_R + S_L| < 1.4$



Favored regions  
of real values of  
the type III 2HDM  
parameters  
 $S_R$  and  $S_L$

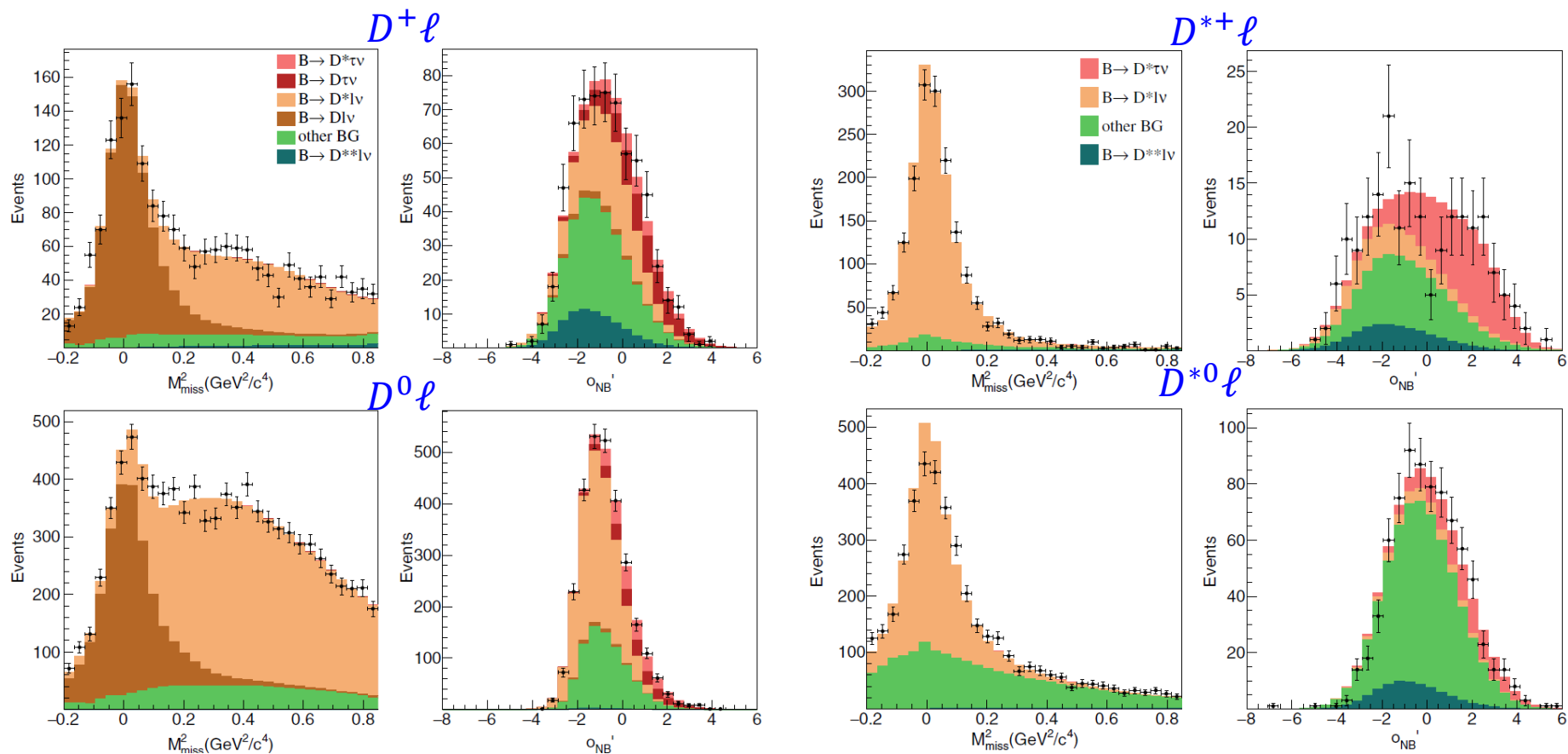
Ruled out by  $q^2$  distribution

PS: Uncertainties in the extrapolation of type II 2HDM are not included

Four signal sample  $D^0\ell$ ,  $D^{*0}\ell$ ,  $D^+\ell$  and  $D^{*+}\ell$

$\tau \rightarrow \mu\nu\nu$  and  $\tau \rightarrow e\nu\nu$

We reconstruct  $D^+$  mesons in the decays to  $K^-\pi^+\pi^+$ ,  $K_S^0\pi^+$ ,  $K_S^0\pi^+\pi^0$ , and  $K_S^0\pi^+\pi^+\pi^-$ ;  $D^0$  mesons to  $K^-\pi^+$ ,  $K^-\pi^+\pi^+\pi^-$ ,  $K^-\pi^+\pi^0$ ,  $K_S^0\pi^0$ , and  $K_S^0\pi^+\pi^-$ ;  $D^{*+}$  mesons to  $D^0\pi^+$  and  $D^+\pi^0$ ; and  $D^{*0}$  mesons to  $D^0\pi^0$  and  $D^0\gamma$ .



$$\mathcal{R}(D) = 0.375 \pm 0.064 \pm 0.026 \quad (1.4\sigma \text{ from SM})$$

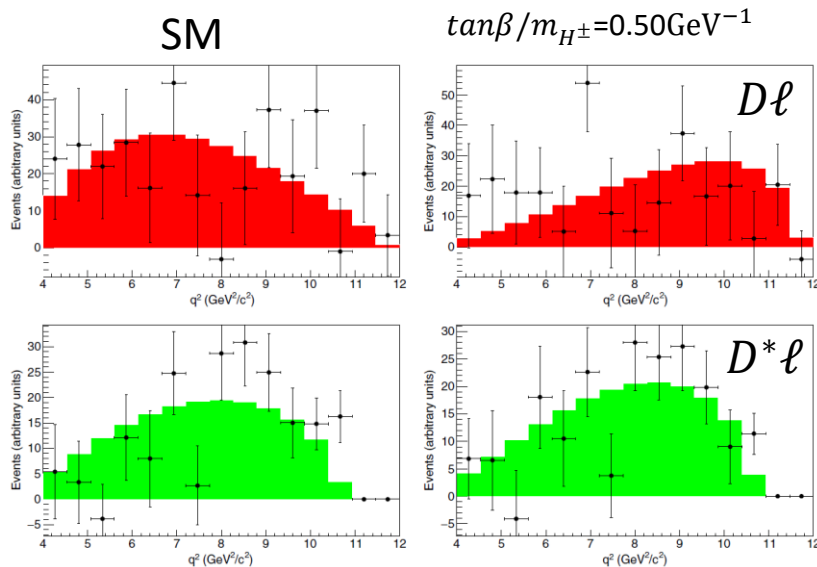
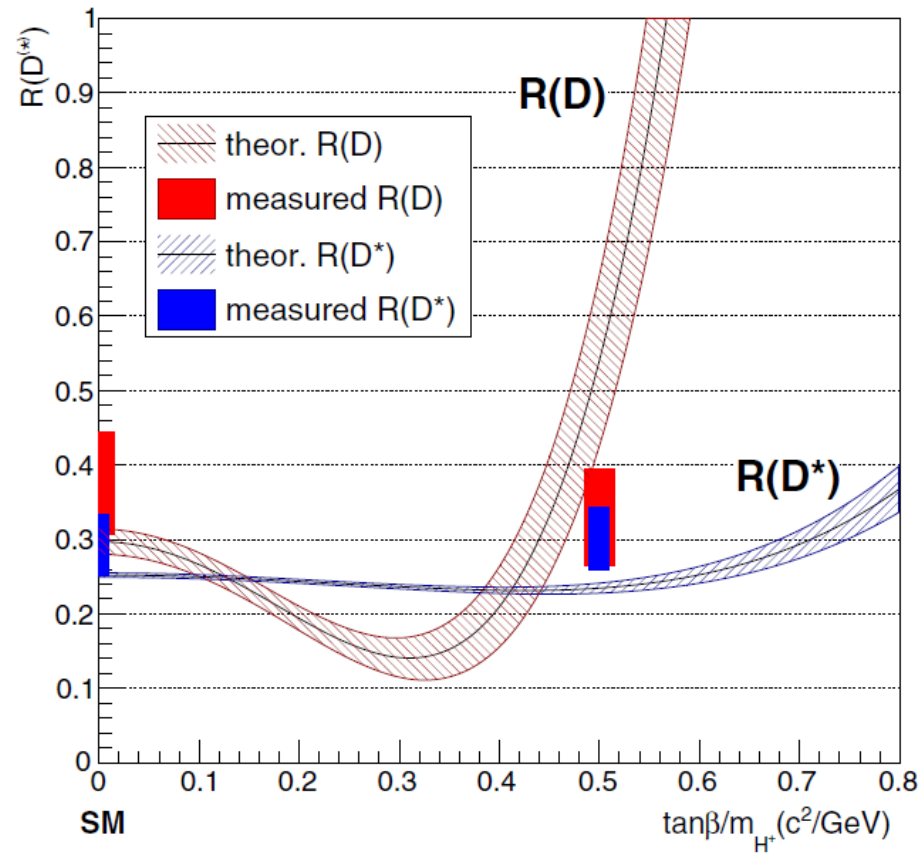
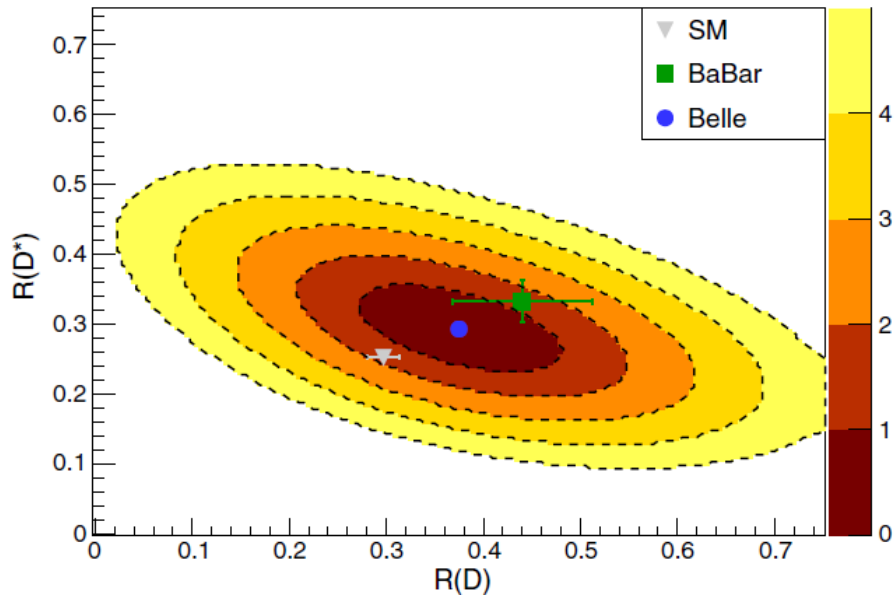
$$\mathcal{R}(D^*) = 0.295 \pm 0.038 \pm 0.015 \quad (1.8\sigma \text{ from SM})$$

$$\mathcal{R}(D)_{SM} = 0.300 \pm 0.011$$

$$\mathcal{R}(D^*)_{SM} = 0.252 \pm 0.003$$

# Interpretation

Belle PRD92, 072014 (2015)



Belle result lies between SM expectation and the BaBar result (compatible with both).

Also compatible with 2HDM of type II around  $\tan\beta/m_{H^\pm} = 0.50\text{GeV}^{-1}$

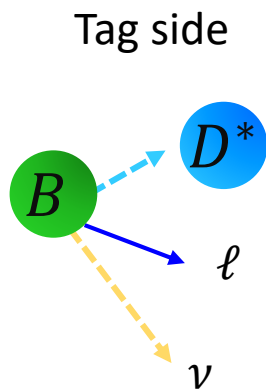
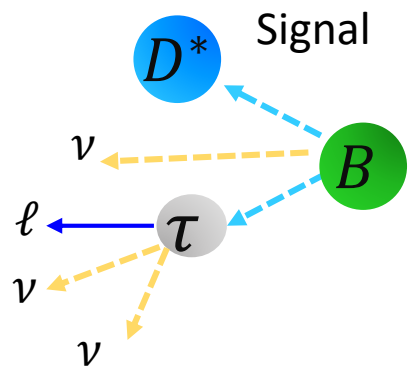
Independent analysis of previous Belle measurement.

Better efficiency in tagging (*somewhat double*)

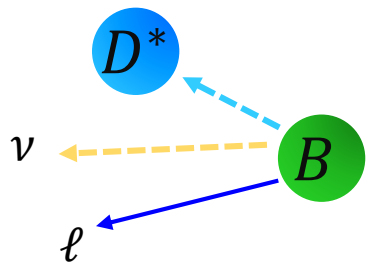
✎ More background due to missing particle in tag side

Analysis focus on  $D^{*+}\tau\bar{\nu}_\tau$   $\tau \rightarrow \mu\nu\nu$  and  $\tau \rightarrow e\nu\nu$

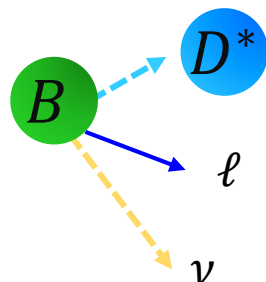
$$\cos\theta_{B-D^*\ell} = \frac{E_{beam}^* E_{D^*\ell}^* - m_B^2 - m_{D^*\ell}^2}{2|p_{beam}^*||p_{D^*\ell}^*|}$$



Normalization



Tag side



2D fit to neural network output ( $O_{NB}$ ) and  $E_{ECL}$

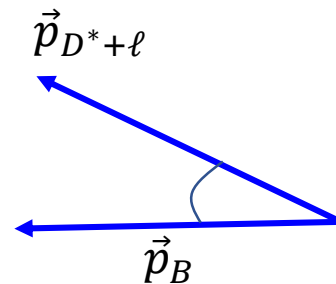
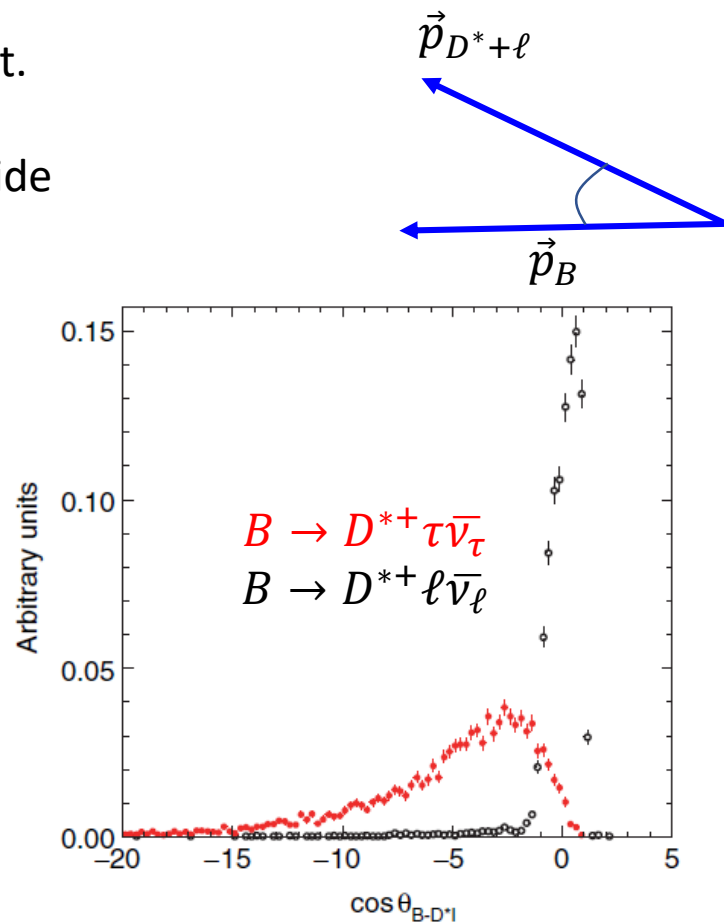
$O_{NB}$ :

➤  $\cos\theta_{B-D^*\ell}$

➤  $M_{miss}^2$

➤ Total energy of  $B_{tag} + B_{sig}$

$E_{ECL}$ : Sum of energy in ECL not associated with reconstruction

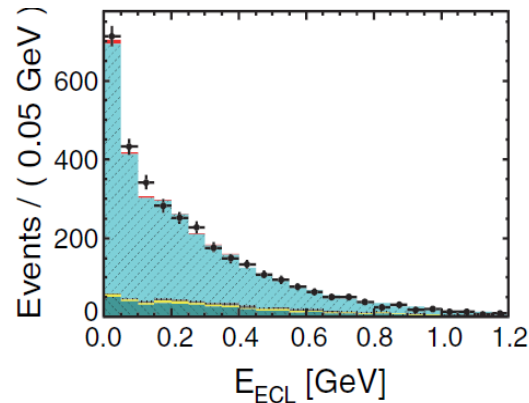
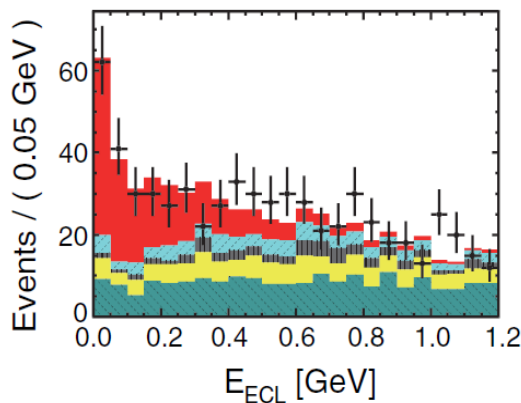
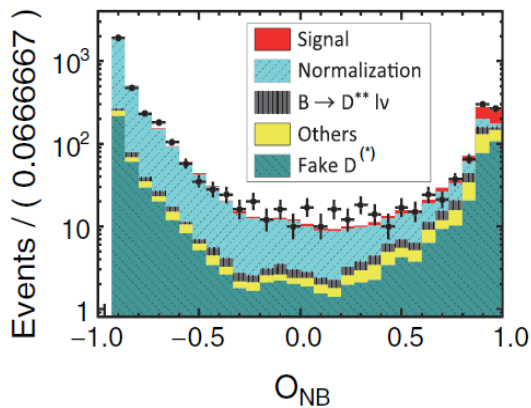




# Result from semileptonic

Belle PRD94, 072007 (2016)

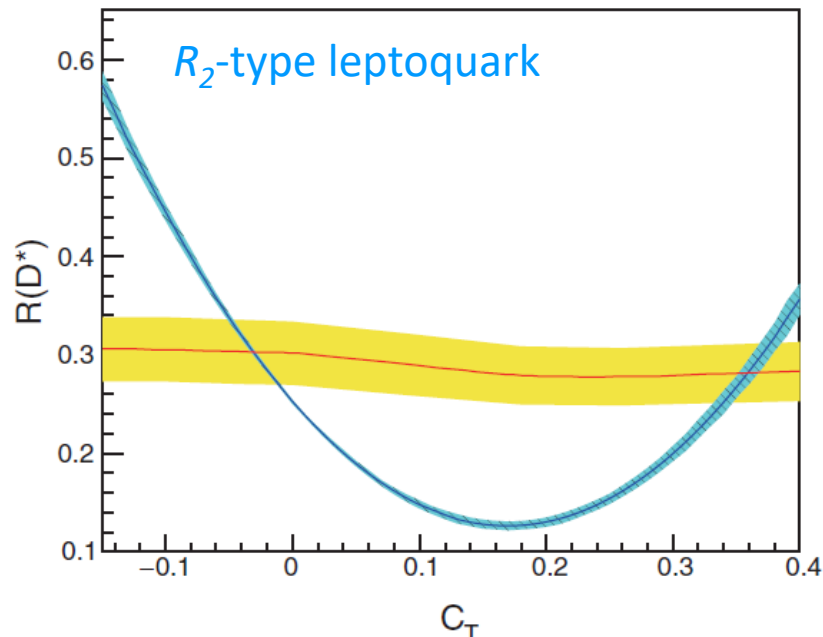
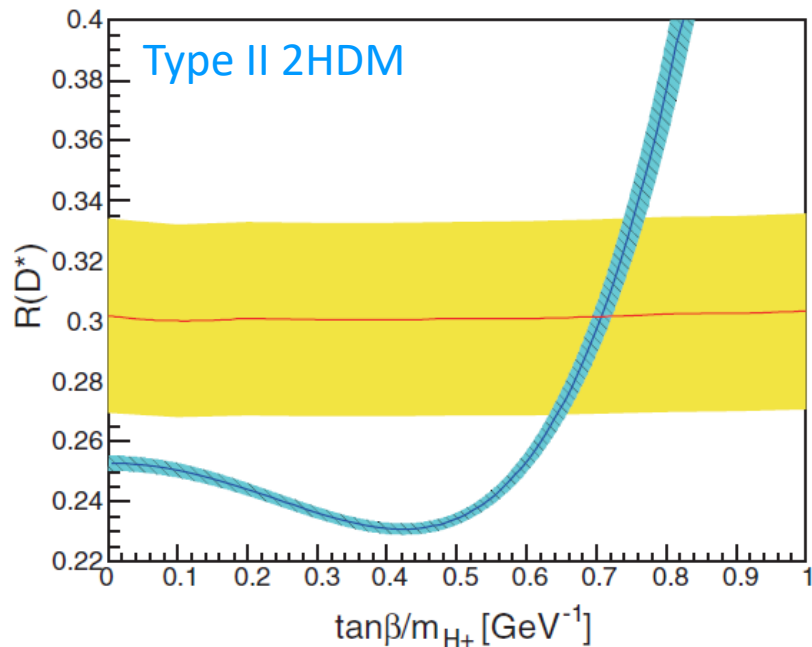
$D^0 \rightarrow K^- \pi^+, K_S^0 \pi^0, K^+ K^-, \pi^+ \pi^-, K_S^0 \pi^+ \pi^-,$   
 $K^- \pi^+ \pi^0, \pi^+ \pi^- \pi^0, K_S^0 K^+ K^-, K^- \pi^+ \pi^+ \pi^-,$  and  $K_S^0 \pi^+ \pi^- \pi^0$ .  
 Charged  $D$  mesons are reconstructed in the following modes:  $D^+ \rightarrow K_S^0 \pi^+, K^- \pi^+ \pi^+, K_S^0 \pi^+ \pi^0, K^+ K^- \pi^+,$  and  $K_S^0 \pi^+ \pi^+ \pi^-$ .



$$\mathcal{R}(D^*) = 0.302 \pm 0.030 \pm 0.011 \quad (1.6\sigma \text{ from SM})$$

$$\mathcal{R}(D^*) = 0.295 \pm 0.038 \pm 0.015$$

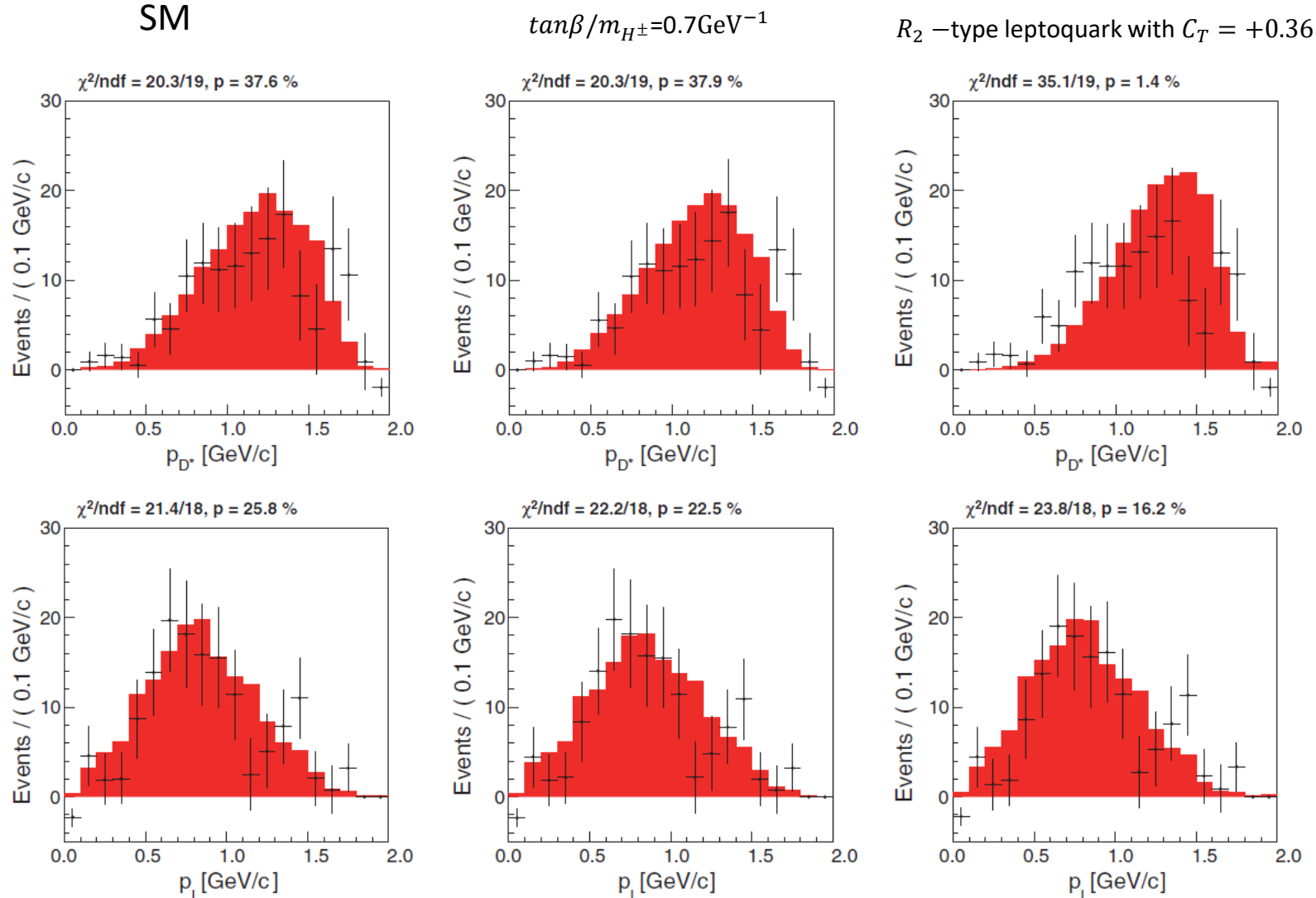
*Previous from Hadron Tag*



$$\mathcal{R}(D^*)_{SM} = 0.252 \pm 0.003$$



## More distribution



Allow additional contribution from scalar and vector operators while disfavouring large additional contributions from a tensor operator with  $+0.34 < C_T < +0.39$ , and  $R_2$ -type leptoquark model with  $+0.34 < C_T < +0.38$ , or an  $S_1$ -type leptoquark model with  $+0.22 < C_T < +0.28$

# Other variable : $P_\tau(D^*)$

Hadronic Tag

$\tau$  polarization :

$$P_\tau(D^*) = \frac{\Gamma^+ - \Gamma^-}{\Gamma^+ + \Gamma^-}$$

$\Gamma^+$  for right handed  $\tau$

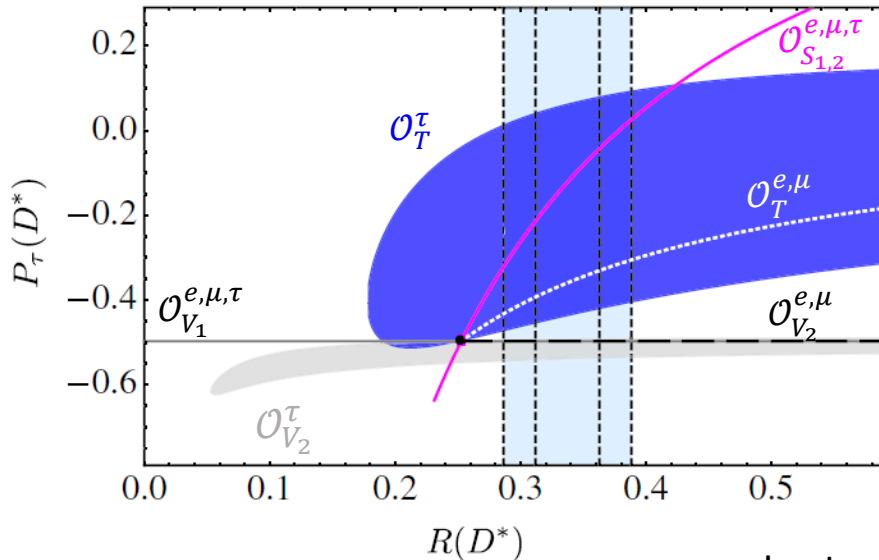
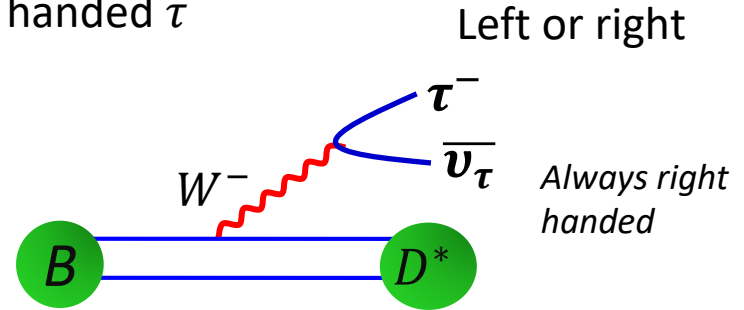
$\Gamma^-$  for left handed  $\tau$

$$P_\tau(D^*)_{SM} = -0.497 \pm 0.013$$

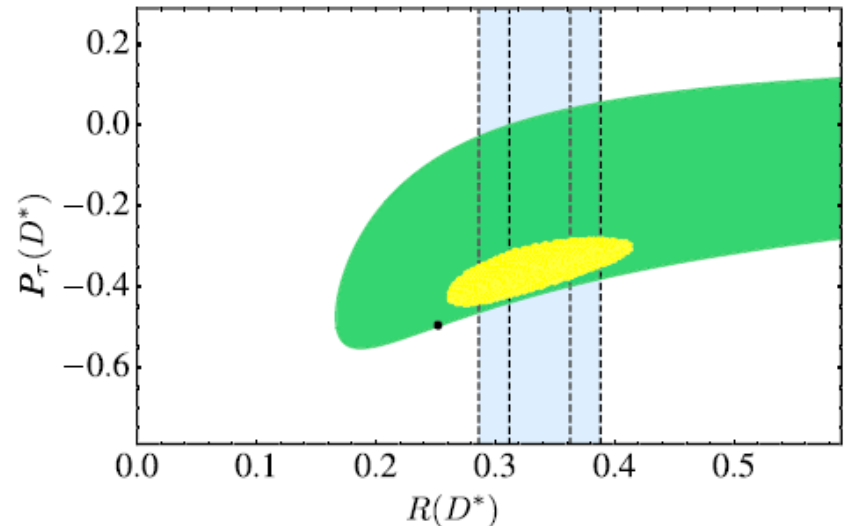
M. Tanaka and R. Watanabe PRD87, 034028 (2013)

$\tau$  polarization is sensitive to the NP contribution.

One can measure the  $\tau$  polarization using its two-body decay



Relevant mass scale of leptoquark could be  $\sim 500\text{GeV}$



Leptoquark having mass of 1 TeV will lead to  $P_\tau(D^*) \in [-0.5, 0]$

Sakaki et al PRD88, 094012 (2013).

New variable to search for NP

Provide independent study/confirmation of previous measurements

Angular distribution of  $\tau$  decay

$$\frac{1}{\Gamma} \frac{d\Gamma}{d\cos\theta_{\text{hel}}} = \frac{1}{2} [1 + \alpha P_\tau(D^*) \cos\theta_{\text{hel}}] \quad \alpha = \begin{cases} 1 & \text{for } \tau \rightarrow \pi\nu \\ 0.45 & \text{for } \tau \rightarrow \rho\nu \end{cases}$$

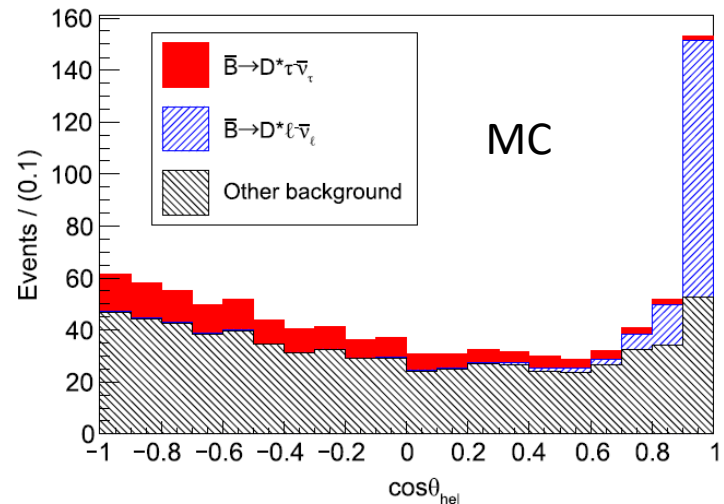
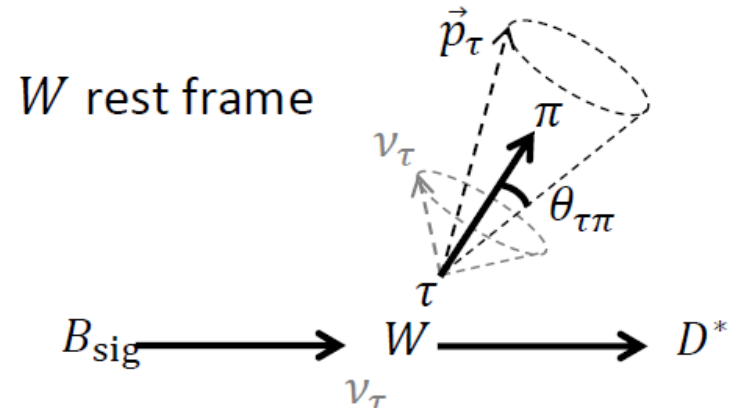
$\tau$  rest frame estimated

$$q = p_{e^+e^-} - p_{\text{tag}} - p_{D^*}$$

$$E_\tau = \frac{q^2 + m_\tau^2}{2\sqrt{q^2}} \quad |\vec{p}_\tau| = \frac{q^2 - m_\tau^2}{2\sqrt{q^2}}$$

$$\cos\theta_{\tau d} = \frac{2E_\tau E_d - m_\tau^2 - m_d^2}{2|\vec{p}_\tau||\vec{p}_d|}$$

$$|\vec{p}_d^\tau| \cos\theta_{\text{hel}} = -\gamma|\vec{\beta}|E_d + \gamma|\vec{p}_d| \cos\theta_{\tau d}$$

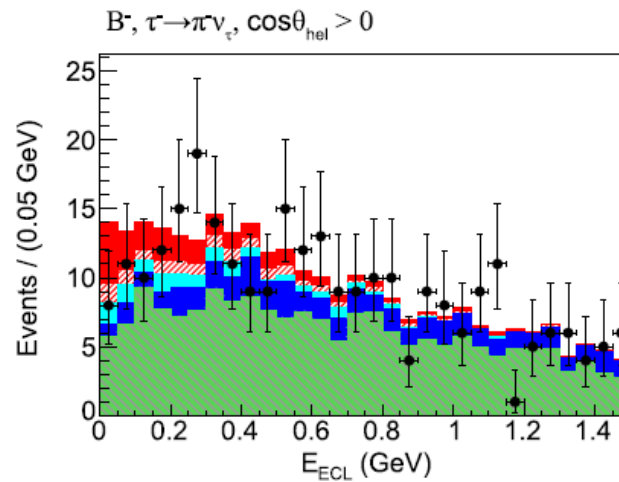
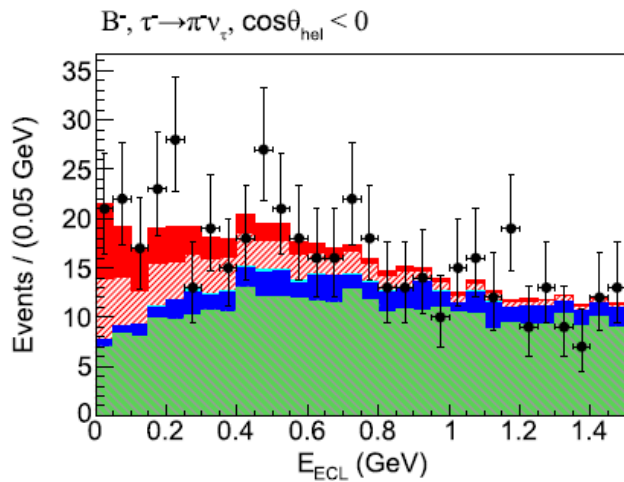
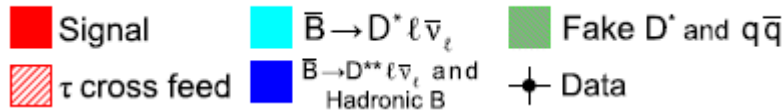
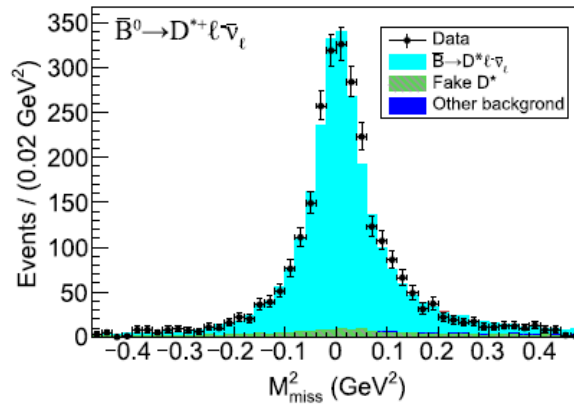
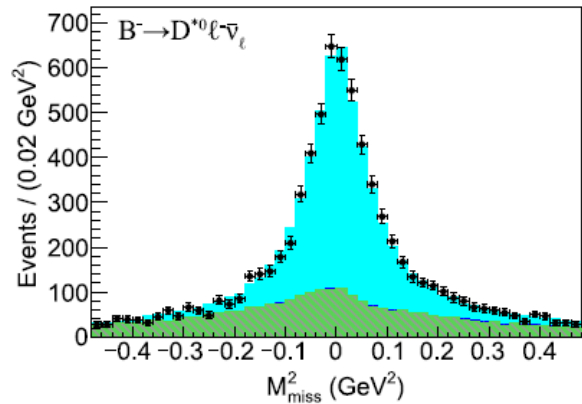


# How the signal look

$$M_{\text{miss}}^2 = (p_{e^+e^-} - p_{\text{tag}} - p_{D^*} - p_{\ell})^2,$$

$$D^{*0} \rightarrow D^0\gamma, D^0\pi^0, D^{*+} \rightarrow D^+\pi^0, D^0\pi^+$$

$$\tau \rightarrow \pi^+\nu, \rho^+\nu$$



Simultaneous fit to 8 samples

$$[B^0, B^+] \otimes [\pi^+, \rho^+] \otimes [\cos\theta_{\text{hel}} > 0, \cos\theta_{\text{hel}} < 0]$$

$$D^0 \rightarrow K_S^0\pi^0, \pi^+\pi^-, K^-\pi^+, K^+K^-,$$

$$K^-\pi^+\pi^0, K_S^0\pi^+\pi^-, K_S^0\pi^+\pi^-\pi^0, K^-\pi^+\pi^+\pi^-, D^+ \rightarrow K_S^0\pi^+,$$

$$K_S^0K^+, K_S^0\pi^+\pi^0, K^-\pi^+\pi^+, K^+K^-\pi^+, K^-\pi^+\pi^+\pi^0, \text{ and}$$

$$K_S^0\pi^+\pi^+\pi^-$$

# Result

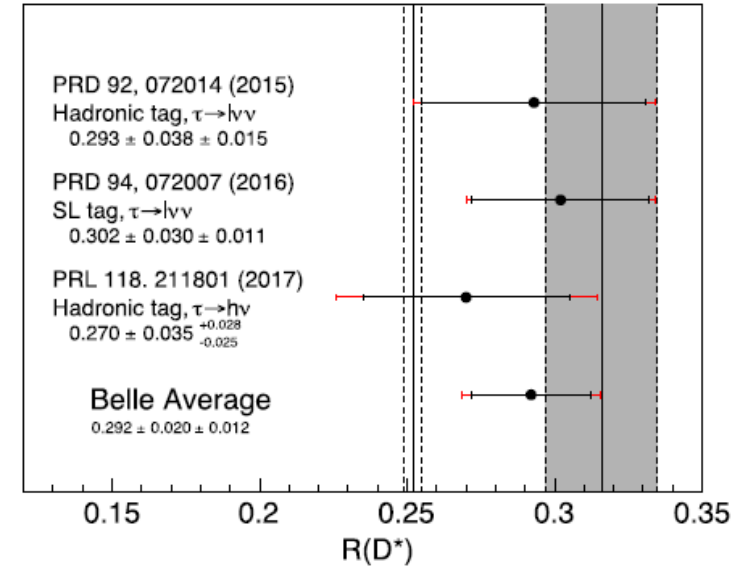
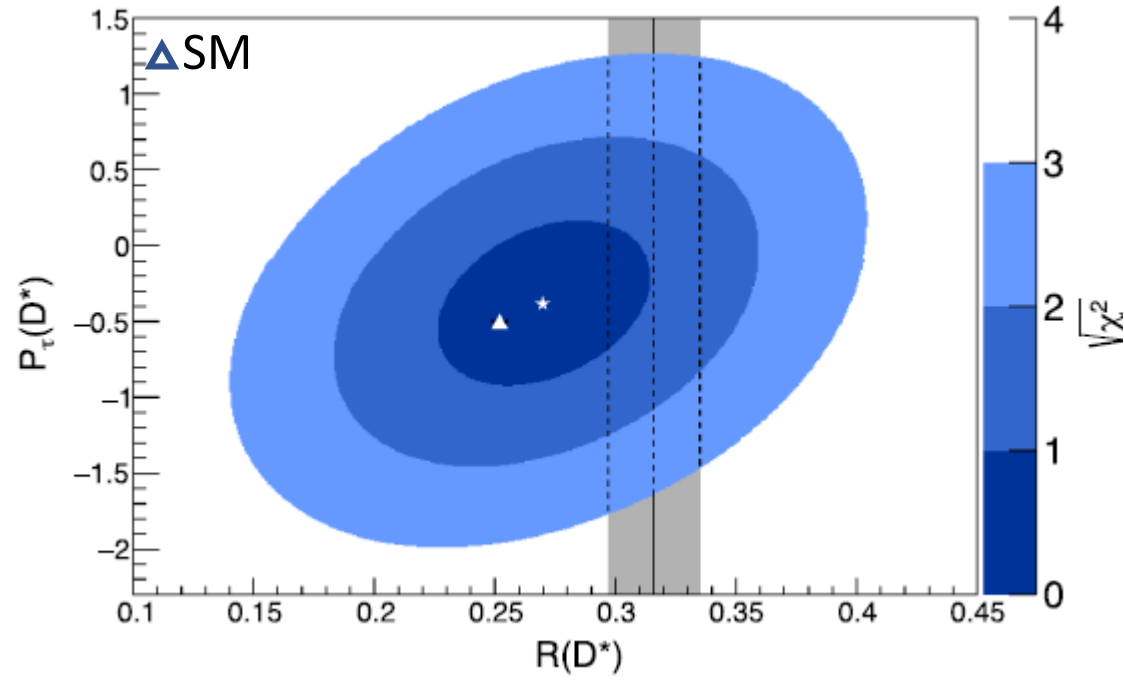
Belle  
 PRL118,211801 (2017)  
 PRD97, 012004 (2018)

Signal significance of  $7.1\sigma$

$$R(D^*) = 0.270 \pm 0.035(\text{stat})_{-0.025}^{+0.028}(\text{syst}),$$

$$P_\tau(D^*) = -0.38 \pm 0.51(\text{stat})_{-0.16}^{+0.21}(\text{syst}),$$

$$\text{SM} = -0.497 \pm 0.013$$



Measurement is consistent with the SM prediction

Excludes  $P_\tau(D^*)$  larger than 0.5 at 90% CL.

$$\mathcal{R}(D^*) = 0.295 \pm 0.038 \pm 0.015$$

*Previous from Hadron Tag*

$$\mathcal{R}(D^*)_{SM} = 0.252 \pm 0.003$$

# $D^*$ polarization

$D^*$  polarization can give clue about the NP signature

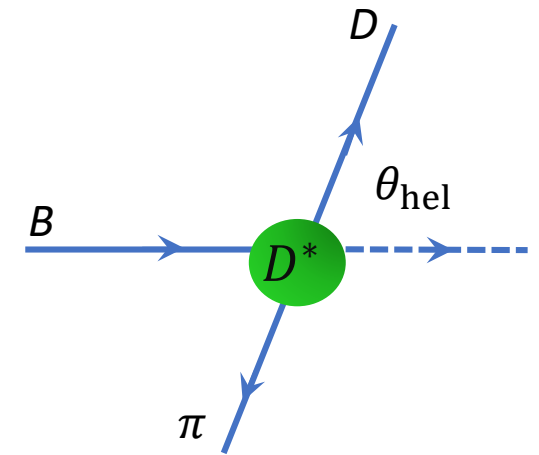
$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_{\text{hel}}} = \frac{3}{4} (2F_L^{D^*} \cos^2 \theta_{\text{hel}} + (1 - F_L^{D^*}) \sin^2 \theta_{\text{hel}})$$

$\theta_{\text{hel}}$  = angle in  $D^*$ - rest frame between  $D^0$  and  $B^0$  flight  
 $F_L^{D^*}$  fraction of longitudinal polarization of  $D^*$

Evis and Xmiss

$$X_{\text{miss}} = \frac{E_{\text{miss}} - |p_{D^*} - p_{d_\tau}|}{\sqrt{E_{\text{beam}}^2 - m_{B^0}^2}}$$

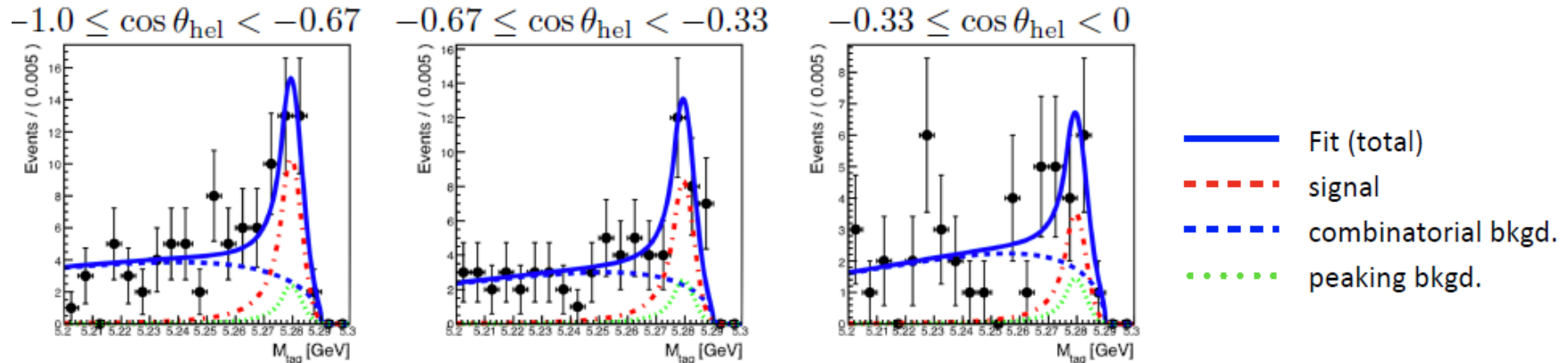
Peaking background from  $B \rightarrow D^*(X)\ell\nu$



- All  $\tau$  decays are useful (cross-feed no effect)
- Strong dependence on  $\cos \theta_{\text{hel}}$  and  $q^2$  due to slow  $\pi$  from  $D^*$  [softer at  $(\cos \theta_{\text{hel}}) > 0$ ].

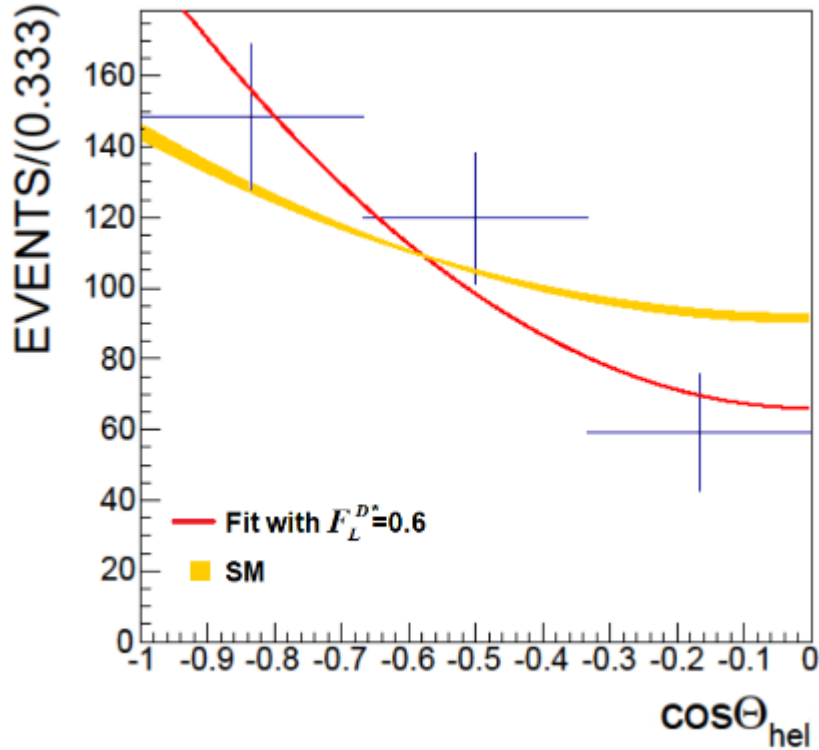
Measured  $F_L$  for  $F_L^{D^*}(B \rightarrow D^{*-} e^+ \nu) = 0.56 \pm 0.02$

SM : 0.54



# First measurement of $D^*$ polarization

Belle, arXiv:1903.03102



$$F_L^{D^*} = 0.60 \pm 0.08 \pm 0.04$$

$$(F_L^{D^*})_{SM} = 0.457 \pm 0.010$$

Li et al PRD98, 095018(2018)

Agrees with SM within  $1.6\sigma$

TABLE I. Summary of systematic uncertainties

Source		$\Delta F_L^{D^*}$
Monte Carlo statistics	AR shape and peaking background	$\pm 0.032$
	CB shape	$\pm 0.010$
	Background scale factors	$\pm 0.001$
Background modeling	$B \rightarrow D^{**}\ell\nu$	$\pm 0.003$
	$B \rightarrow D^{**}\tau\nu$	$\pm 0.011$
	$B \rightarrow \text{hadrons}$	$\pm 0.005$
	$B \rightarrow \bar{D}^*M$	$\pm 0.004$
Signal modeling	Form factors	$\pm 0.002$
	$\cos\theta_{\text{hel}}$ resolution	$\pm 0.003$
	Acceptance non-uniformity	+0.015 -0.005
Total		+0.039 -0.037

# Update on semileptonic tagging by Belle

Previous

$\mathcal{R}(D^*)$  only

$B^0$  only

Semileptonic

Updated

$\mathcal{R}(D^*)$  and  $\mathcal{R}(D^0)$  simultaneously

$B^0$  and  $B^+$

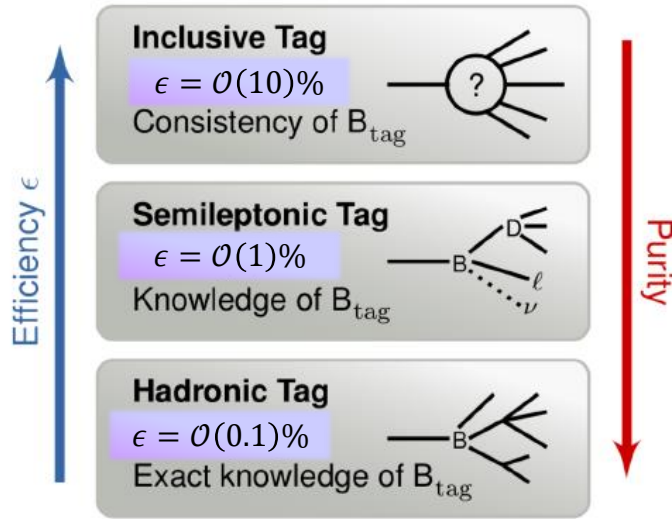
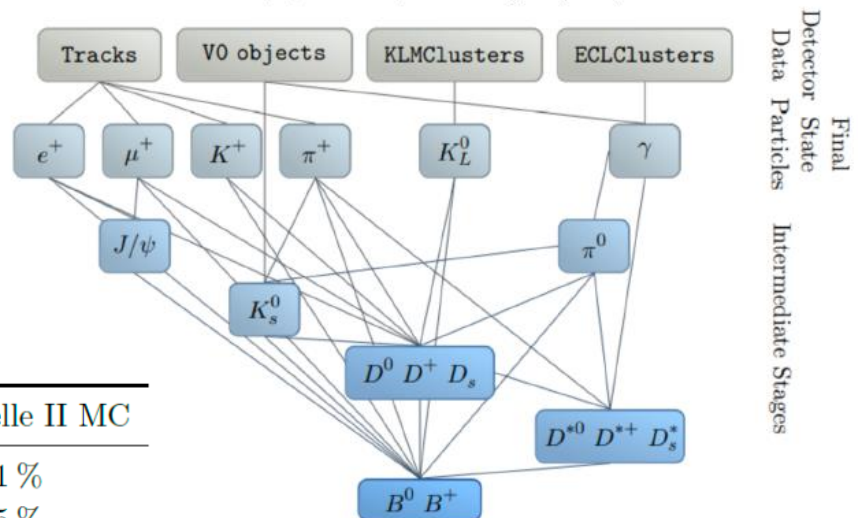
Improved tagging, FEI

FEI developed for Belle II; used in several Belle studies.

## Exclusive Tagging:

### The Full Event Interpretation (FEI)

Keck, T., et al. Comput Softw Big Sci (2019)

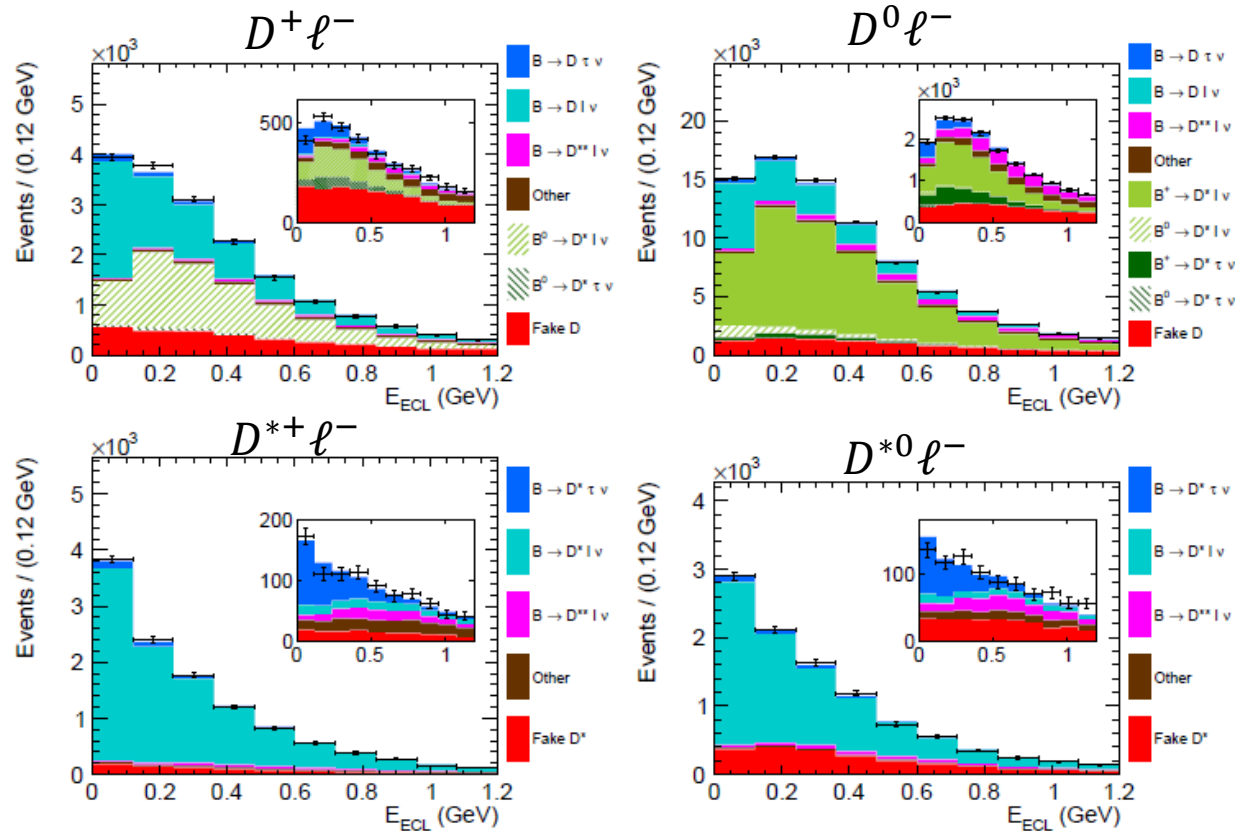


Tag	FR <sup>4</sup> @ Belle	FEI @ Belle MC	FEI @ Belle II MC
Hadronic $B^+$	0.28 %	0.49 %	0.61 %
Semileptonic $B^+$	0.67 %	1.42 %	1.45 %
Hadronic $B^0$	0.18 %	0.33%	0.34 %
Semileptonic $B^0$	0.63 %	1.33%	1.25 %



# Updated result

Belle arXiv:1910.05864  
submitted to PRL



Signal enhanced  
 $\mathcal{O}_{cls} > 0.9$  (inset)

$$\mathcal{R}(D) = 0.307 \pm 0.037 \pm 0.016$$

$$\mathcal{R}(D^*) = 0.282 \pm 0.018 \pm 0.014$$

Most precise measurement to date !

$\mathcal{R}(D^*) = 0.302 \pm 0.030 \pm 0.011$   
Previous semileptonic measurement

$$\mathcal{R}(D)_{SM} = 0.300 \pm 0.011$$

$$\mathcal{R}(D^*)_{SM} = 0.252 \pm 0.003$$

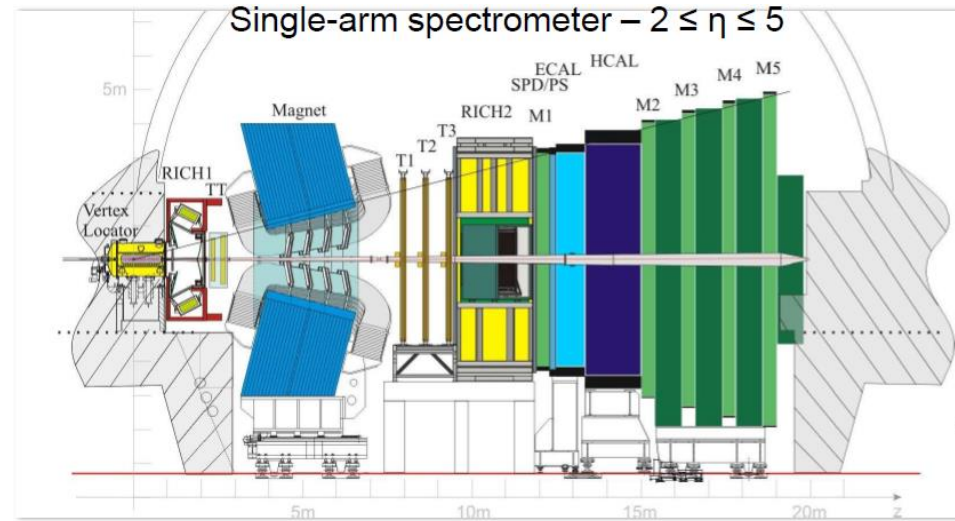
# LHCb : beauty at the beast

LHCb is a single arm spectrometer optimized for beauty and charm physics at large  $\eta$

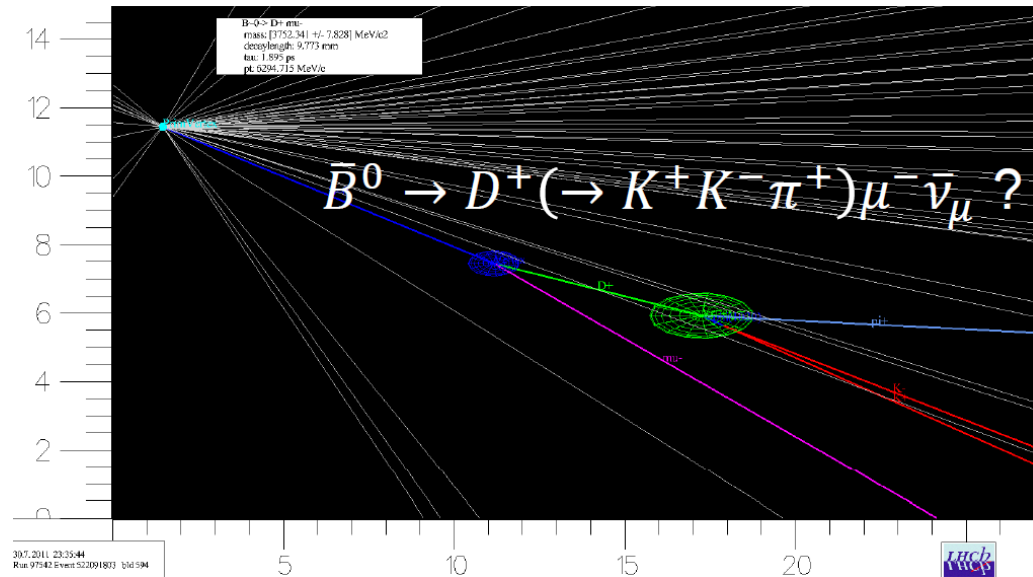
Excellent vertex resolution:  $20\mu\text{m}$   
resolution on impact parameter.

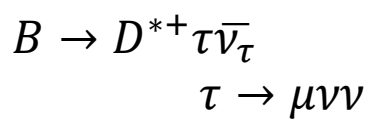
Excellent particle identification

Dipole magnet polarity periodically flipped to change the sign of many reconstruction asymmetries



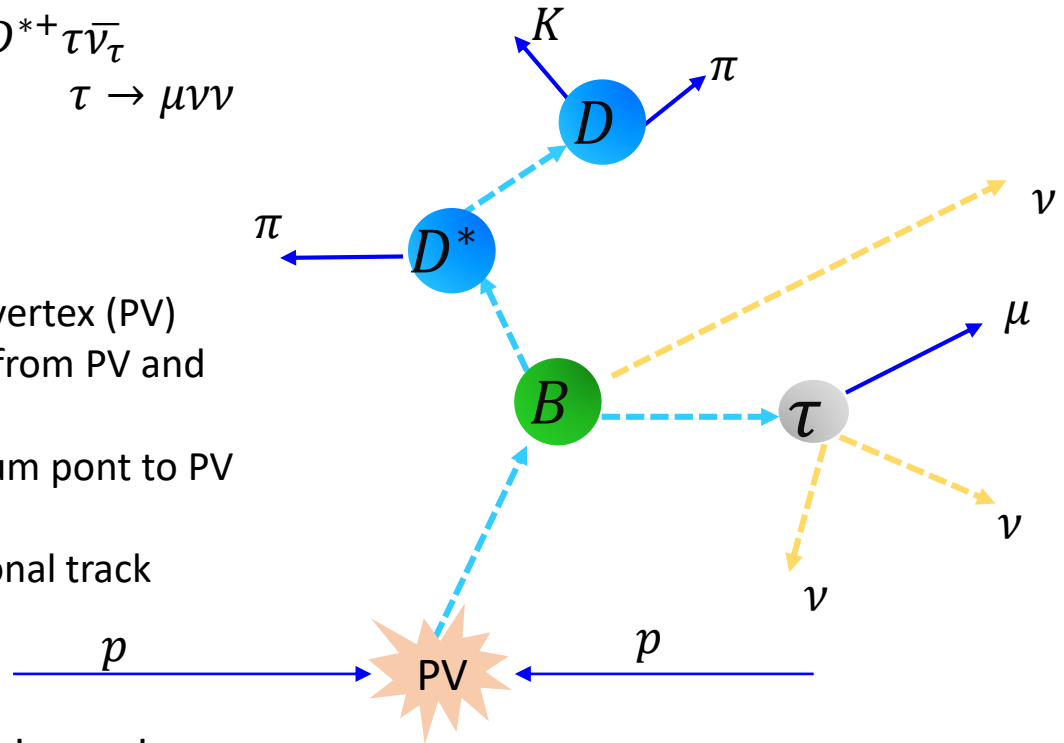
Semileptonic decays : High trigger efficiency





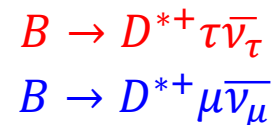
### Signal identify

- Identify  $D^*$  with  $\Delta M$
- D0 decay vertex separate from primary vertex (PV)
- $\mu$  candidate  $3 < p < 100$  GeV/c, separate from PV and form good vertex with  $D^0$
- $M(D^* \mu) < 5.280$  GeV/c<sup>2</sup> and momentum point to PV location.
- $D^* \mu$  required to be isolated from additional track

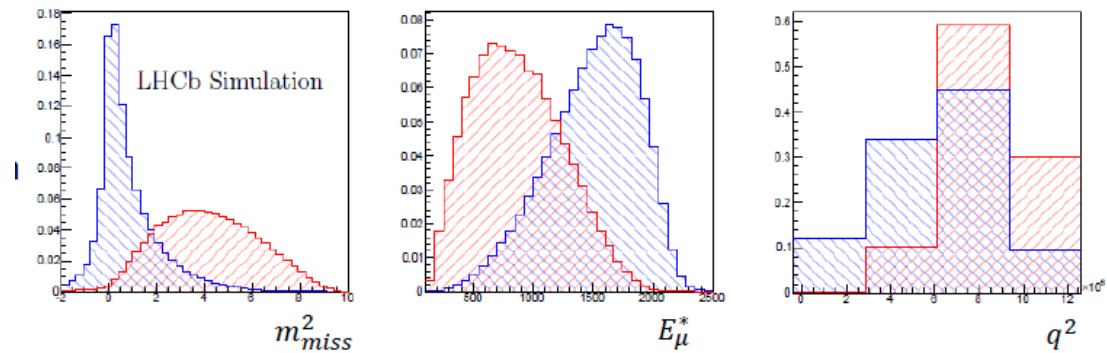


### Separate signal from the normalization channel

- $E^*$ , muon energy in the  $B$  rest frame
- $m_{miss}^2 = (p_B^\mu - p_{D^*}^\mu - p_\mu^\mu)^2$  where  $p^\mu$  is four momentum.
- $q^2 = (p_B^\mu - p_{D^*}^\mu)^2$



*3 missing vs, analysis seems to look impossible for LHCb. Thanks to the boost and vertex capability of LHCb, they made it possible*



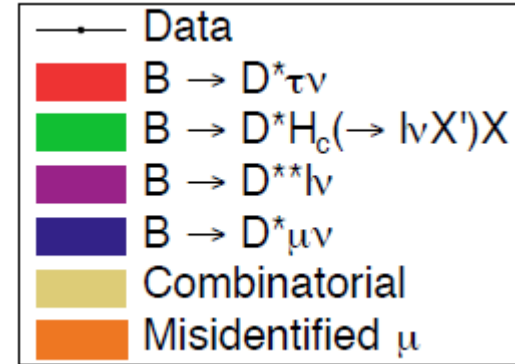
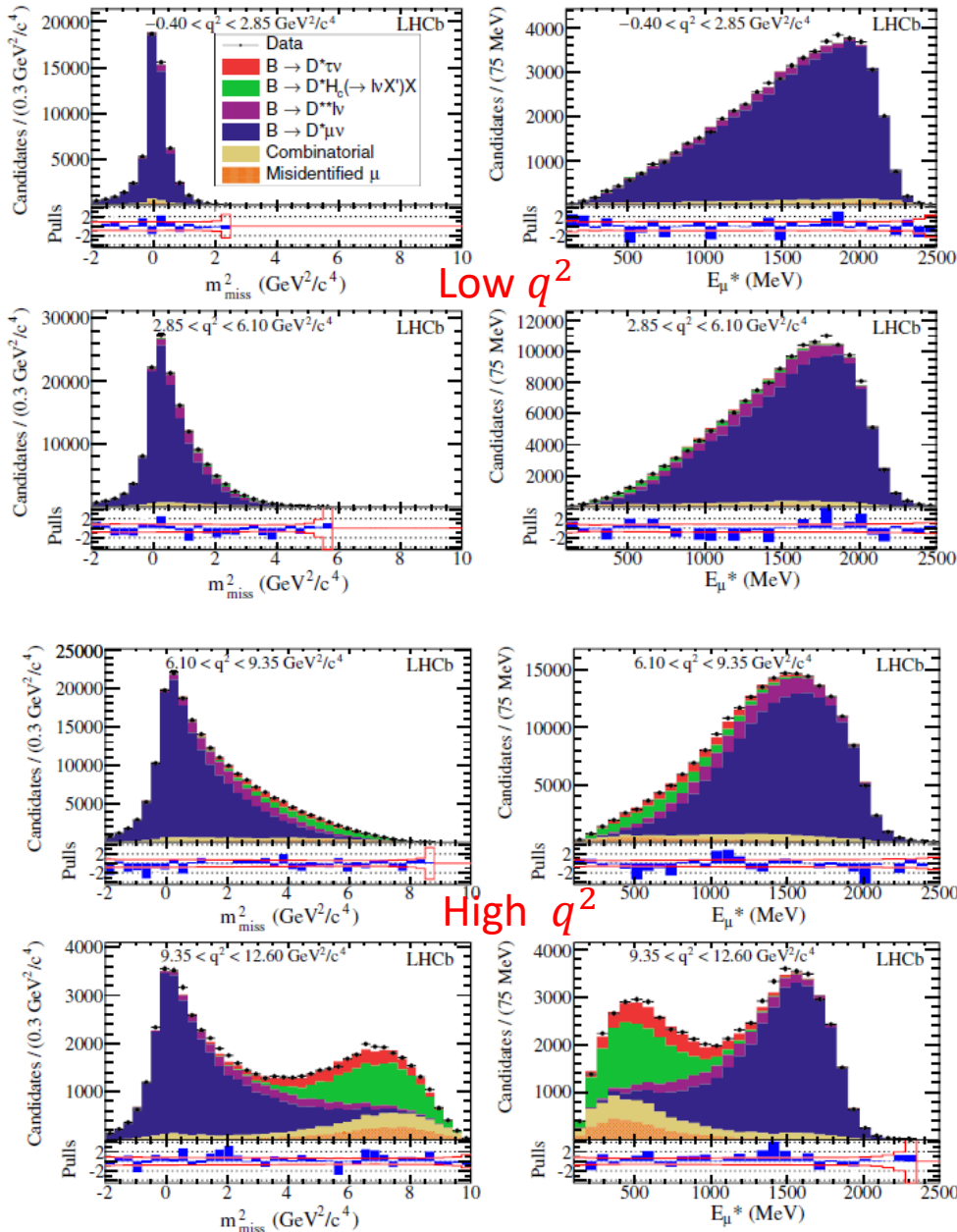
$B$  momentum direction is determined from unit vector to  $B$  decay vertex from the associated PV.

Component of  $B$  momentum along the  $B$  momentum along the beam axis is approximated using  $(p_B)_z = (m_B/m_{reco})(p_{reco})_z$

# Deviate from SM

LHCb, PRL 115, 111803 (2015)

$3fb^{-1}$  2011-2012 data



$\sim 16400$  events for  $\overline{B}^0 \rightarrow D^{*+} \tau^- \overline{\nu}_\tau$

$$\mathcal{R}(D^*) = 0.336 \pm 0.027 \pm 0.030$$

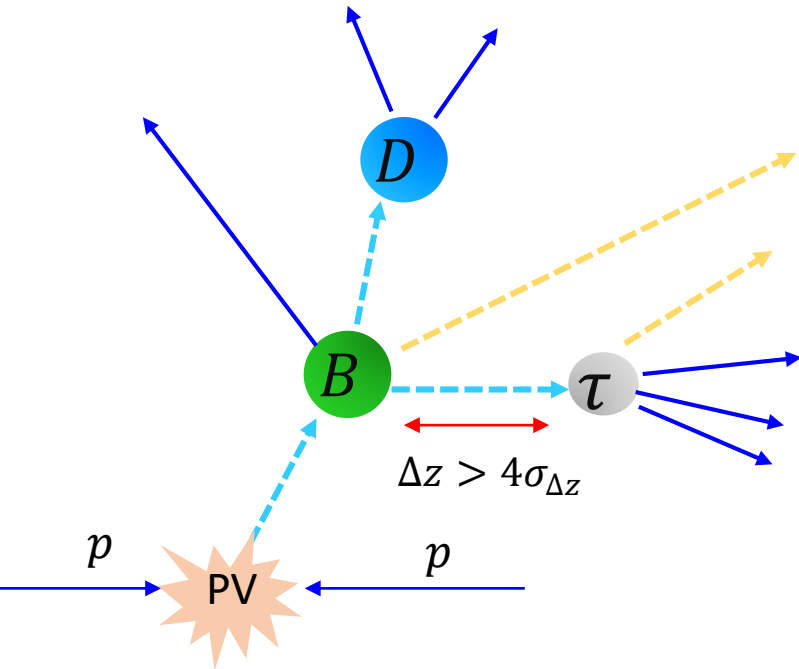
(2.1 $\sigma$  from SM)

$$\mathcal{R}(D^*)_{SM} = 0.252 \pm 0.003$$

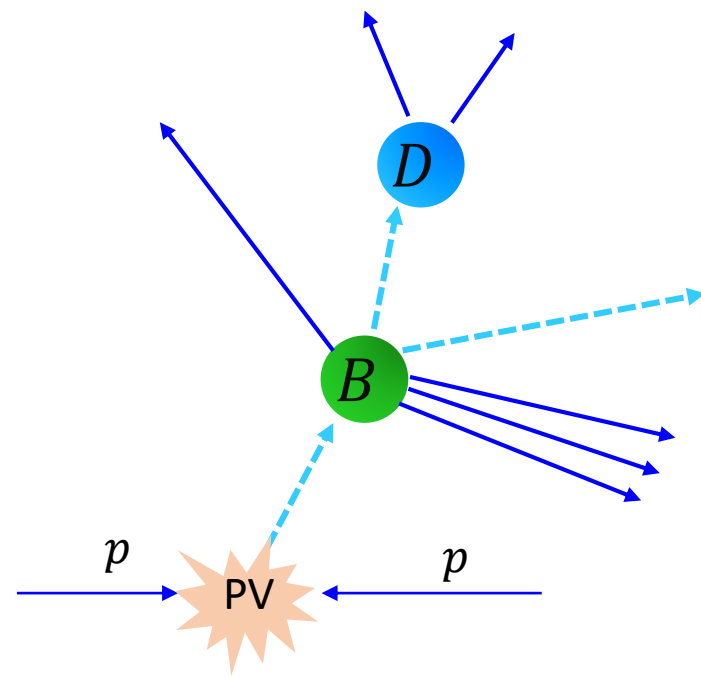
# $R_{D^*}$ using 3-prong $\tau^- \rightarrow \pi^- \pi^+ \pi^- (\pi^0) \nu$ decays

$$B \rightarrow D^{*+} \tau \bar{\nu}_\tau$$

$$\tau \rightarrow \pi^- \pi^+ \pi^- \nu$$



$$B \rightarrow D^{*+} \pi^- \pi^+ \pi^- (+N)$$

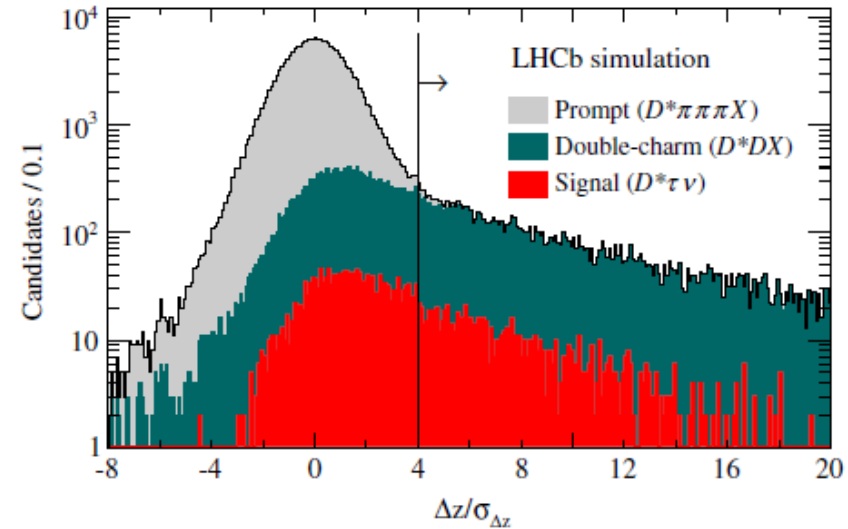


- Absence of charged lepton avoids background from semileptonic  $b \rightarrow c$  decays
- Three prong helps in getting precise  $\tau$  decay vertex.
- Only one  $\nu$  emitted at the  $\tau$  vertex.
- Background  $B \rightarrow D^{*-} DX$  leads to nice mass peaks and not the signal. Provide handle to control various background.

# $R_{D^*}$ using 3-prong $\tau^- \rightarrow \pi^- \pi^+ \pi^- (\pi^0) \nu$ decays

Signal candidates are required to be well isolated.

Events with extra charged particles pointing to B and/or  $\tau$  vertices are vetoed.



$$\mathcal{K}(D^{*-}) \equiv \frac{\mathcal{B}(B^0 \rightarrow D^{*-} \tau^+ \nu_\tau)}{\mathcal{B}(B^0 \rightarrow D^{*-} 3\pi)} = \frac{N_{\text{sig}} \epsilon_{\text{norm}}}{N_{\text{norm}} \epsilon_{\text{sig}}} \frac{1}{\mathcal{B}(\tau^+ \rightarrow 3\pi \bar{\nu}_\tau) + \mathcal{B}(\tau^+ \rightarrow 3\pi \pi^0 \bar{\nu}_\tau)}$$

Most of the systematic cancel in this ratio.

$$\mathcal{R}(D^*) = \mathcal{K}(D^{*-}) \times \frac{\mathcal{B}(B^0 \rightarrow D^{*-} \pi^+ \pi^- \pi^+)}{\mathcal{B}(B^0 \rightarrow D^{*-} \mu^+ \nu_\mu)}$$

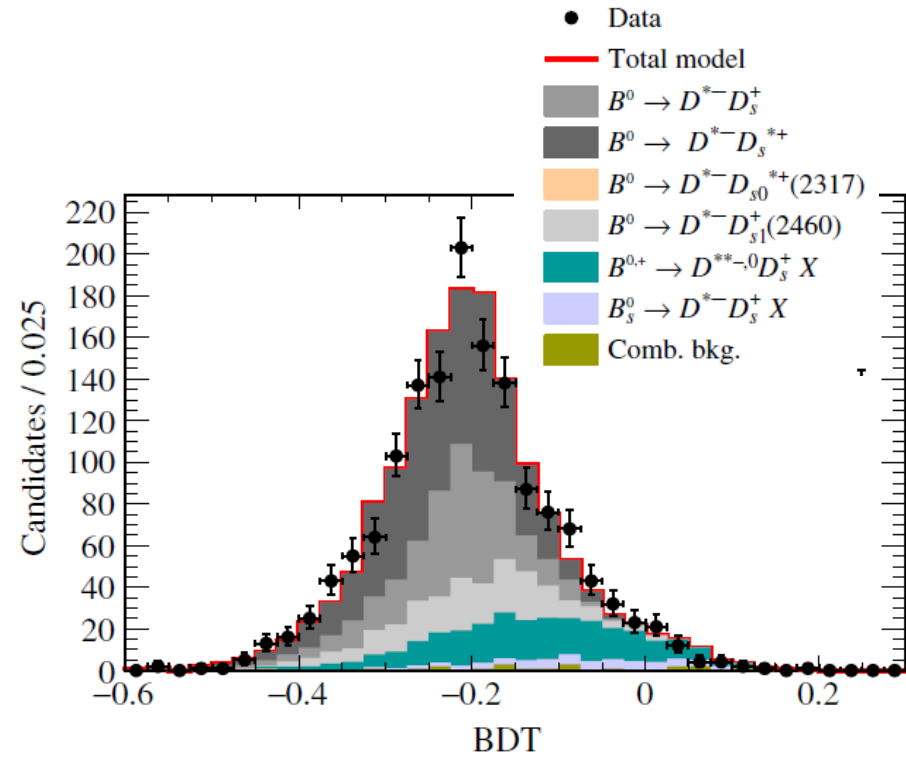
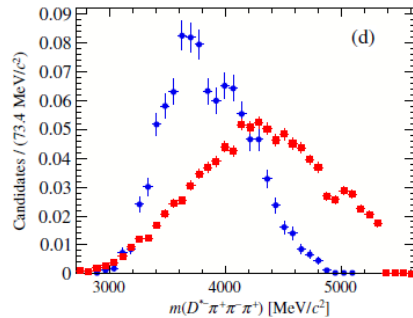
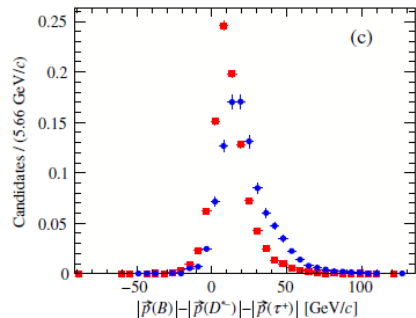
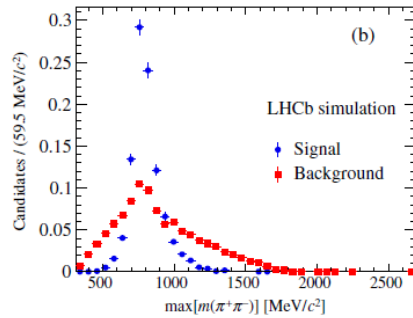
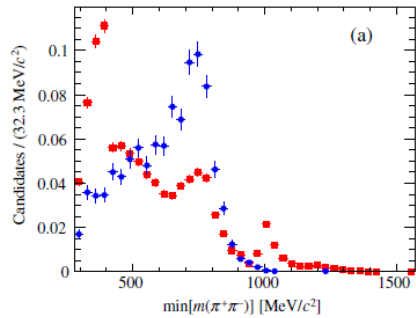
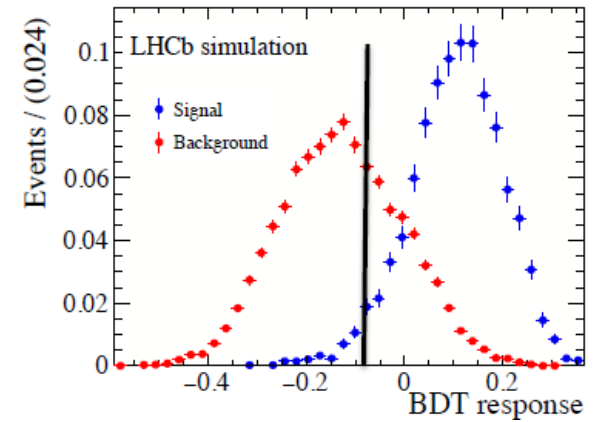
$N_{\text{sig}}$  from a 3D fit to  $q^2$  (8 bins),  $3\pi$  decay time (8 bins) and BDT (4 bins)

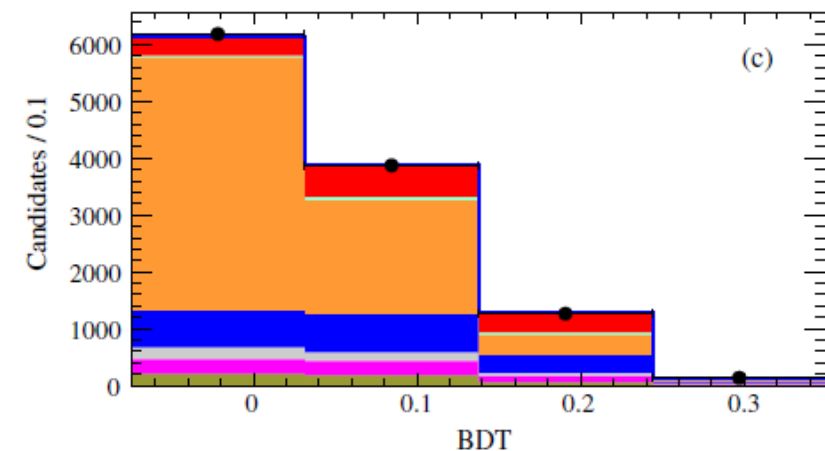
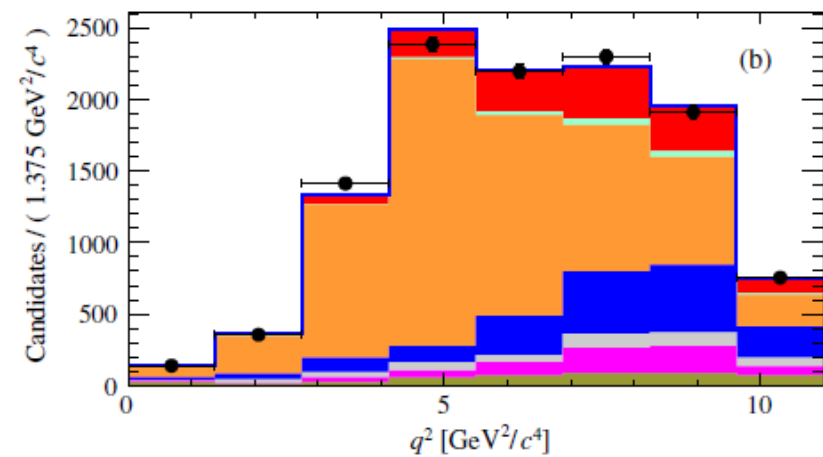
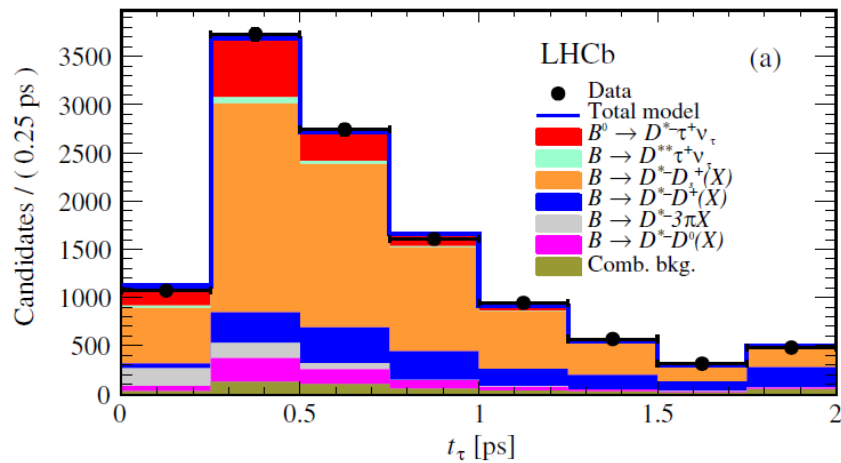
$N_{\text{sig}}$  from a fit to  $M(D^{*-} \pi^+ \pi^- \pi^+)$

# $R_{D^*}$ using 3-prong $\tau^- \rightarrow \pi^- \pi^+ \pi^- (\pi^0) \nu$ decays

BDT trained to suppress main background from  $D^{*-} D_s^+ X$  events

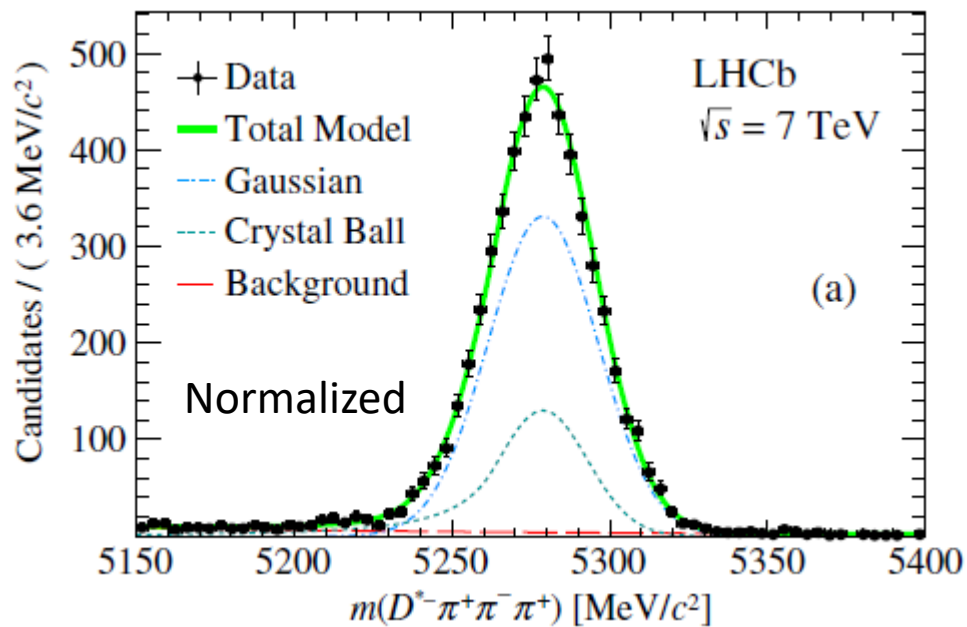
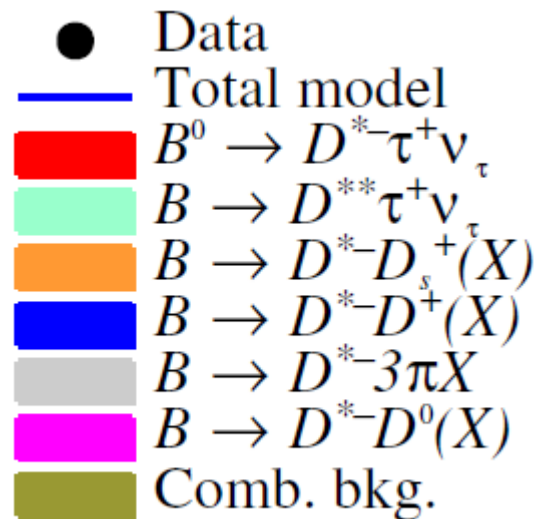
Input variables:  
 $3\pi$  dynamics,  $D^* 3\pi$  dynamics, neutrals isolation





## $R_{D^*}$ using 3-prong

LHCb, PRD 97, 072013 (2018)





## Result by 3 prong

 $3fb^{-1}$  data

$$\mathcal{R}(D^*) = 0.291 \pm 0.019 \pm 0.026 \pm 0.013$$

(1.1 $\sigma$  from SM)

Previous one prong result

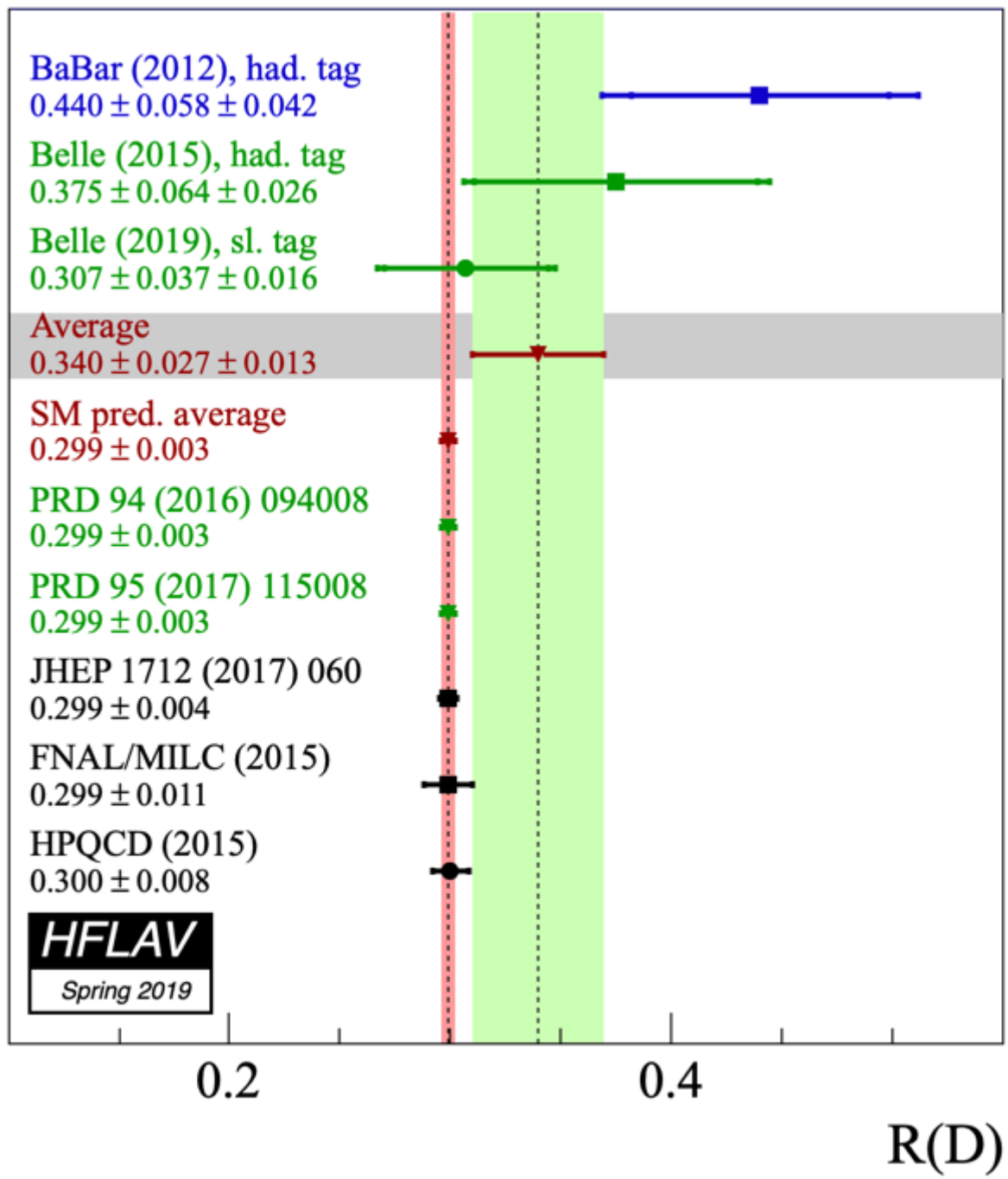
$$\mathcal{R}(D^*) = 0.336 \pm 0.027 \pm 0.030$$

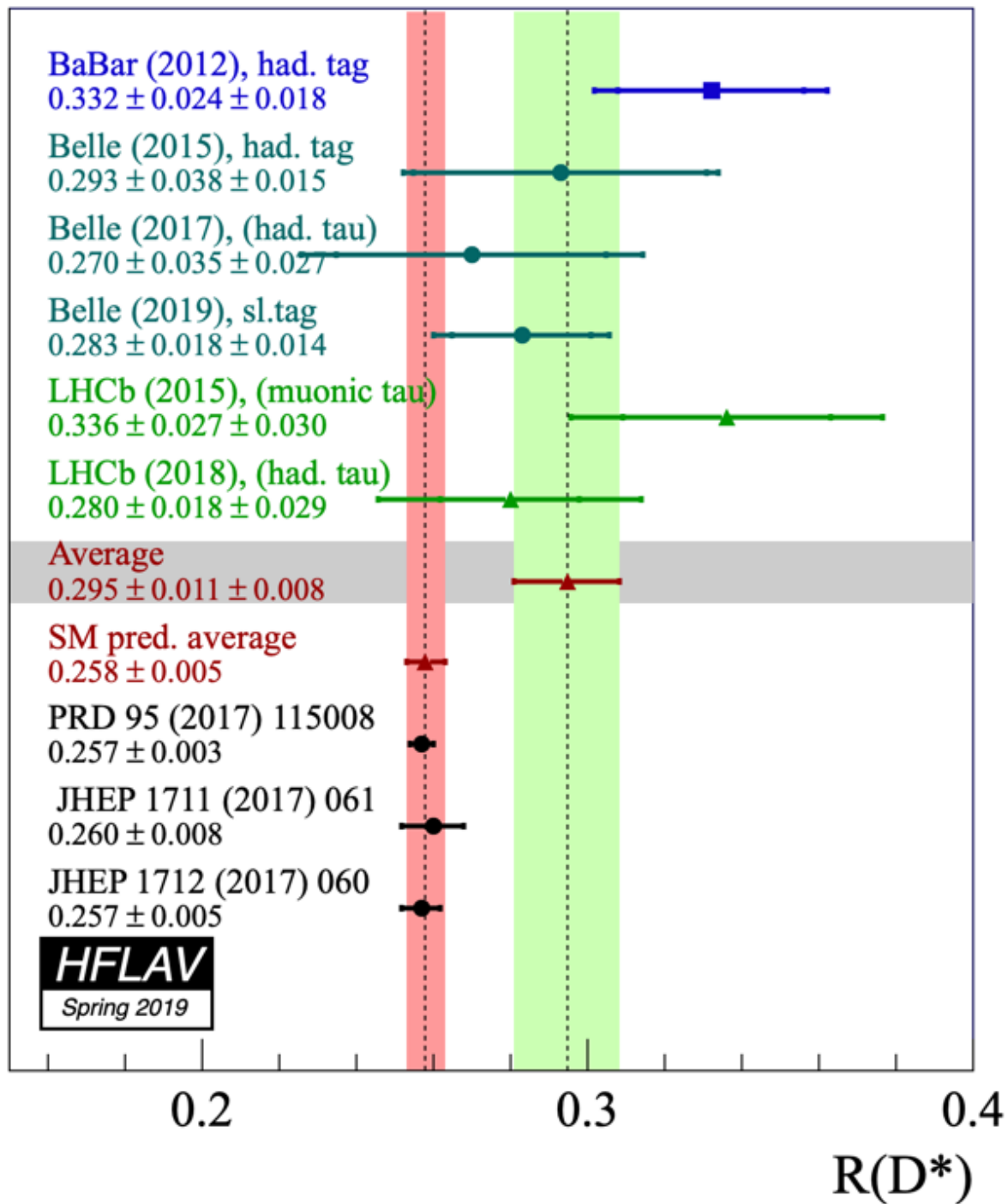
(2.1 $\sigma$  from SM)

LHCb, PRL 115, 111803 (2015)

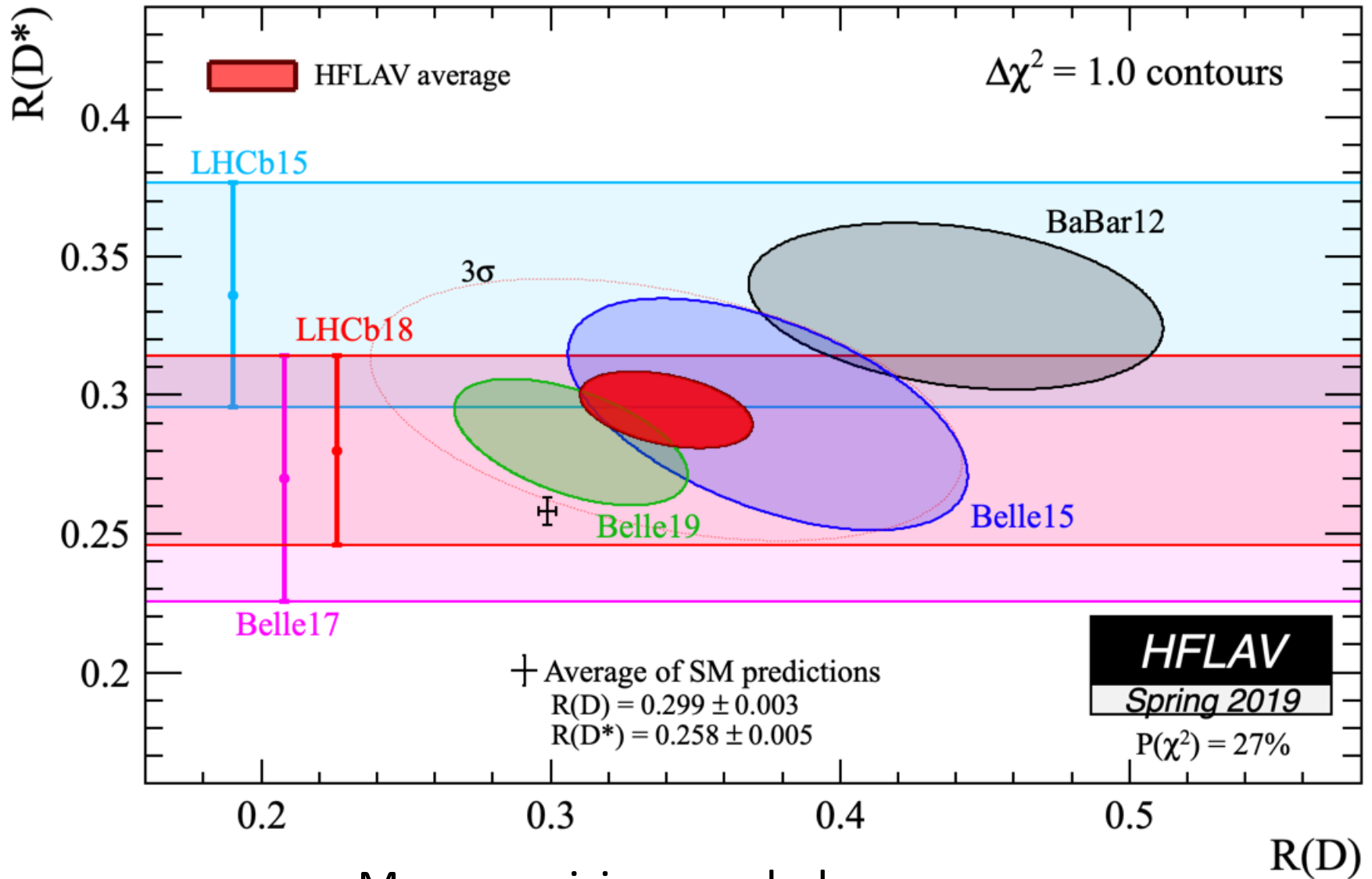
Contribution	Value in %
$B(\tau^+ \rightarrow 3\pi\bar{\nu}_\tau)/B(\tau^+ \rightarrow 3\pi(\pi^0)\bar{\nu}_\tau)$	0.7
Form factors (template shapes)	0.7
Form factors (efficiency)	1.0
$\tau$ polarization effects	0.4
Other $\tau$ decays	1.0
$B \rightarrow D^{*+}\tau^+\nu_\tau$	2.3
$B_s^0 \rightarrow D_s^{*+}\tau^+\nu_\tau$ feed-down	1.5
$D_s^+ \rightarrow 3\pi X$ decay model	2.5
$D_s^+$ , $D^0$ and $D^+$ template shape	2.9
$B \rightarrow D^{*-}D_s^+(X)$ and $B \rightarrow D^{*-}D^0(X)$ decay model	2.6
$D^{*-}3\pi X$ from $B$ decays	2.8
Combinatorial background (shape + normalization)	0.7
Bias due to empty bins in templates	1.3
Size of simulation samples	4.1
Trigger acceptance	1.2
Trigger efficiency	1.0
Online selection	2.0
Offline selection	2.0
Charged-isolation algorithm	1.0
Particle identification	1.3
Normalization channel	1.0
Signal efficiencies (size of simulation samples)	1.7
Normalization channel efficiency (size of simulation samples)	1.6
Normalization channel efficiency (modeling of $B^0 \rightarrow D^{*-}3\pi$ )	2.0
Total uncertainty	9.1

$$\mathcal{R}(D^*)_{SM} = 0.252 \pm 0.003$$





# Current scenario



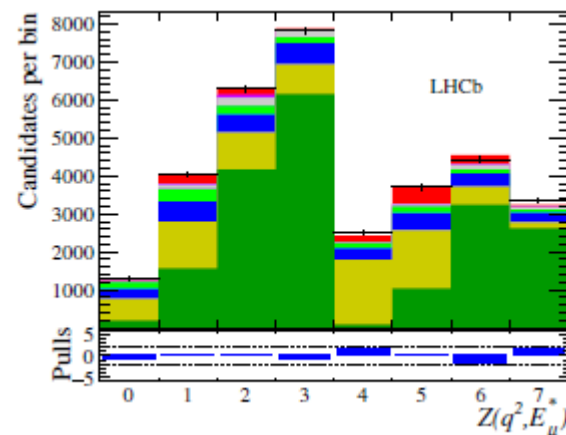
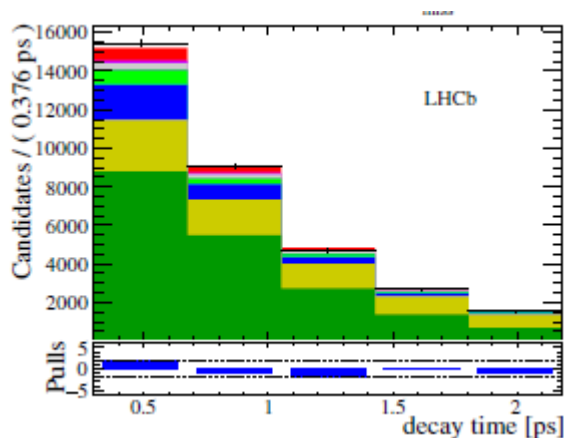
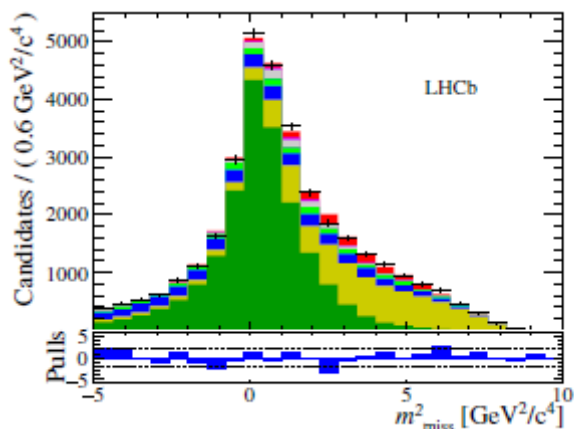
More precision needed.

Picture more clear by 202X

Skip

# Anomaly $\mathcal{R}_{J/\psi}$

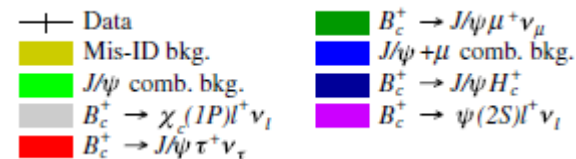
LHCb, PRL120, 121801 (2018)



$$\mathcal{R}(J/\psi) = \frac{\mathcal{B}(B_c^+ \rightarrow J/\psi \tau^+ \nu_\tau)}{\mathcal{B}(B_c^+ \rightarrow J/\psi \mu^+ \nu_\mu)}$$

$$= 0.71 \pm 0.17(\text{stat}) \pm 0.18(\text{syst}).$$

SM predicts within range: 0.25-0.28



Source of uncertainty	Size ( $\times 10^{-2}$ )
Finite simulation size	8.0
$B_c^+ \rightarrow J/\psi$ form factors	12.1
$B_c^+ \rightarrow \psi(2S)$ form factors	3.2
Fit bias correction	5.4
Z binning strategy	5.6
Mis-ID background strategy	5.6
combinatorial background cocktail	4.5
combinatorial $J/\psi$ background scaling	0.9
$B_c^+ \rightarrow J/\psi H_c^+ X$ contribution	3.6
$\psi(2S)$ and $\chi_c$ feed-down	0.9
Weighting of simulation samples	1.6
Efficiency ratio	0.6
$\mathcal{B}(\tau^+ \rightarrow \mu^+ \nu_\mu \bar{\nu}_\tau)$	0.2
Systematic uncertainty	17.7
Statistical uncertainty	17.3

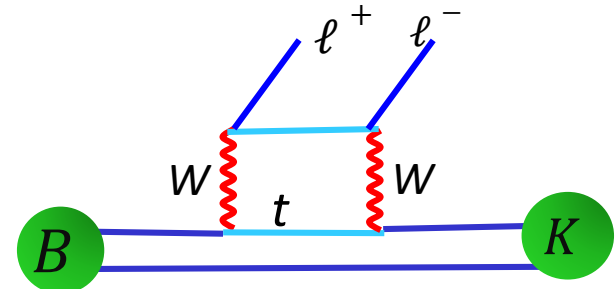
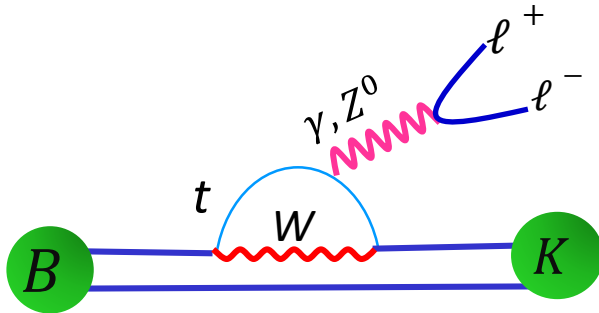
# $b \rightarrow s\ell\ell$

Rare decays, FCNC

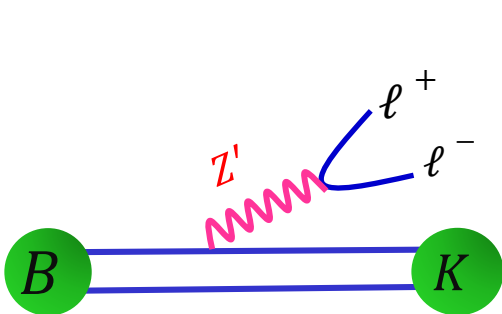
Small branching fraction :  $\mathcal{O}(10^{-6})$

- Decays are sensitive to NP
- Modify the decay rate and the angular distribution of final state

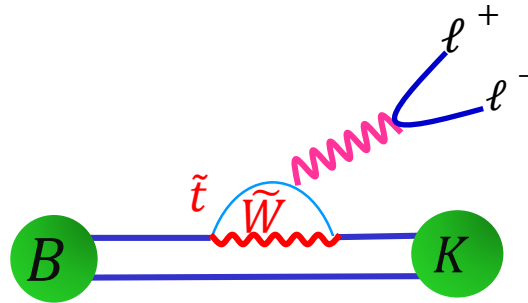
- Give strong constraints on many BSM by probing energy scales higher than direct searches
- Experimentally: full reconstruction but background dominated



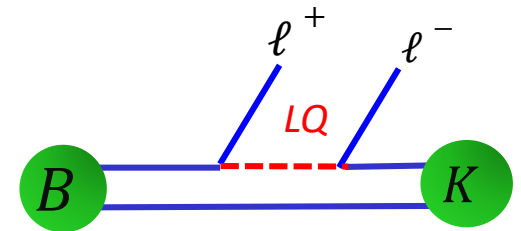
Processes which are suppressed or even forbidden in the SM, one expect the NP effect to be relatively large.



New Heavy Gauge Bosons



Supersymmetry



Leptoquarks

Amplitude of a hadron decay process is described as

$$\mathcal{A}(I \rightarrow F) = \langle F | \mathcal{H}_{eff} | I \rangle = \frac{G_F}{\sqrt{2}} \sum_i V_{CKM}^i C_i(\mu) \langle F | O_i(\mu) | M \rangle$$

CKM      Wilson      Hadronic Matrix  
couplings   coefficients   Elements

At  $\mu$  scale

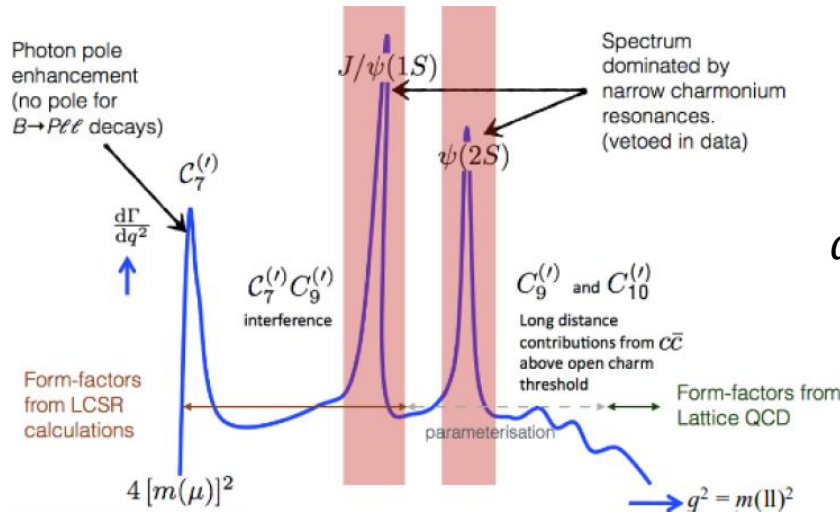
Wilson Coefficients  $C_i$  = Perturbative short distance effects

Operators  $O_i$  = non-perturbative long distance effects

$i = 7$  : Photon penguin

$i = 9, 10$  : Electroweak penguin

NP modify the SM operator contribution ( $C_i$ ) and /or enter through new operators



Contribution of  $C_7$ ,  $C_9$  and  $C_{10}$  depends on  $q^2$  (invariant mass of two leptons)

In the SM, couplings of the gauge bosons to leptons are independent of lepton flavour  
 Any sign of lepton non-universal interaction would be a direct sign of new physics

# What we observe is effect of the particle involved affecting the $\mathcal{B}$

To give an idea from an old plot

Hou, Willey, and Soni PRL 58, 1608 (1987)

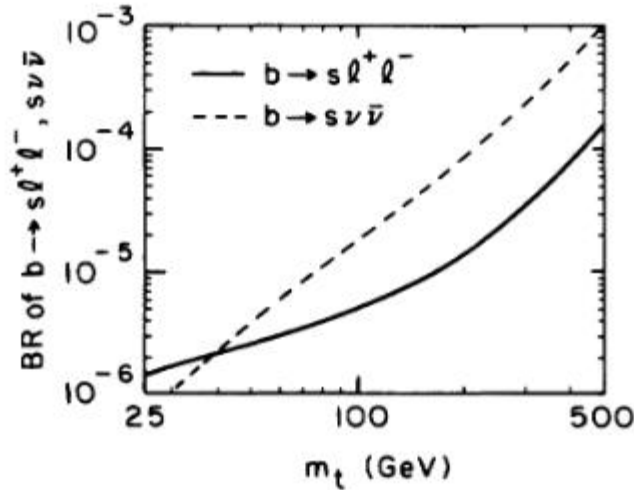
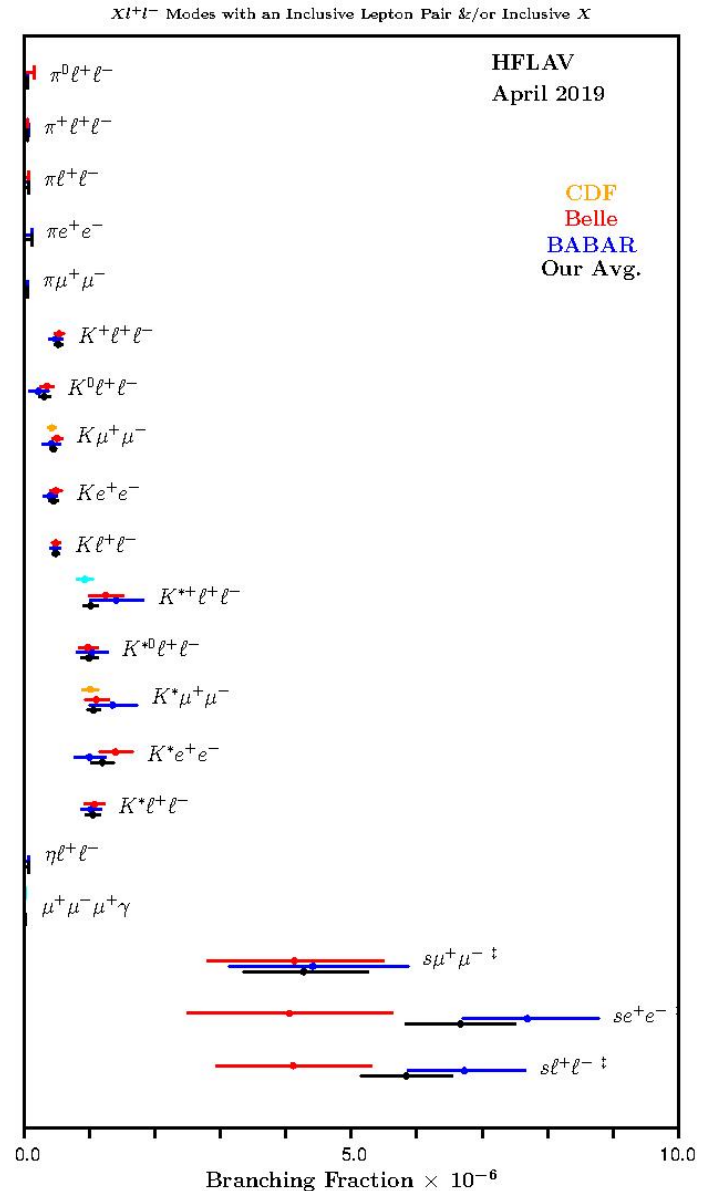


FIG. 2. Branching ratios for the processes  $b \rightarrow se^+e^-$ ,  $sv\bar{\nu}$  in the three-generation case. For  $b \rightarrow sv\bar{\nu}$  the three neutrino species have been summed over. For  $b \rightarrow s\mu^+\mu^-$  the rate is slightly smaller (see Refs. 15 and 16).

$$m_t = 173.0 \pm 0.4 \text{ GeV}/c^2$$



Provide unique way to look for the (new) physics



# Forward-backward Asymmetry in $B \rightarrow K^* \ell \ell$

A.Ali et al PLB 273, 505 (1991)

Interference between  $\gamma$  and weak coupling in  $b \rightarrow s \ell^+ \ell^-$  production give rise to a forward-backward asymmetry

$$\frac{N_F - N_B}{N_F + N_B} = A_{FB}(B \rightarrow K^* \ell^+ \ell^-) = -C_{10} \xi(q^2) \left[ \text{Re}(C_9) F_1 + \frac{1}{q^2} C_7 F_2 \right]$$

$F_1, F_2$  are form factors

$q^2 = m_{\ell^+ \ell^-}^2$

↓

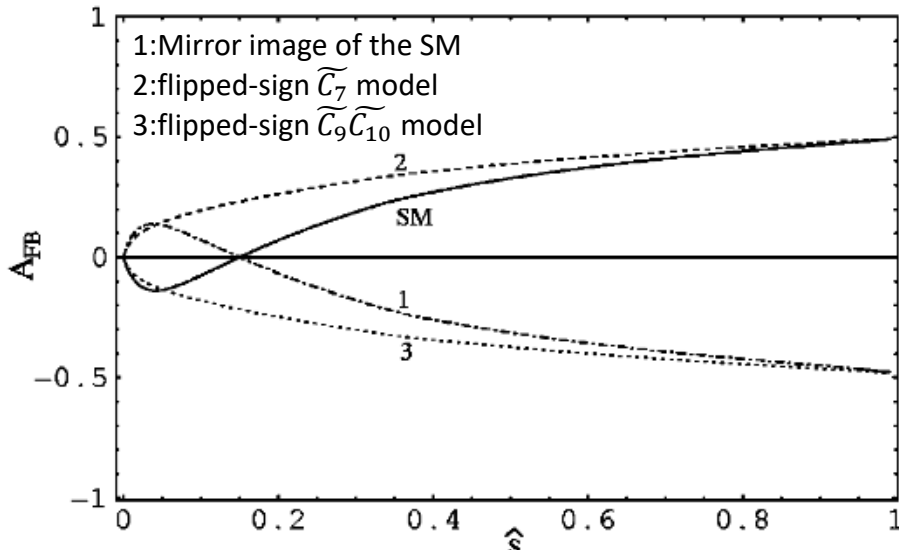
Z contribution

↙

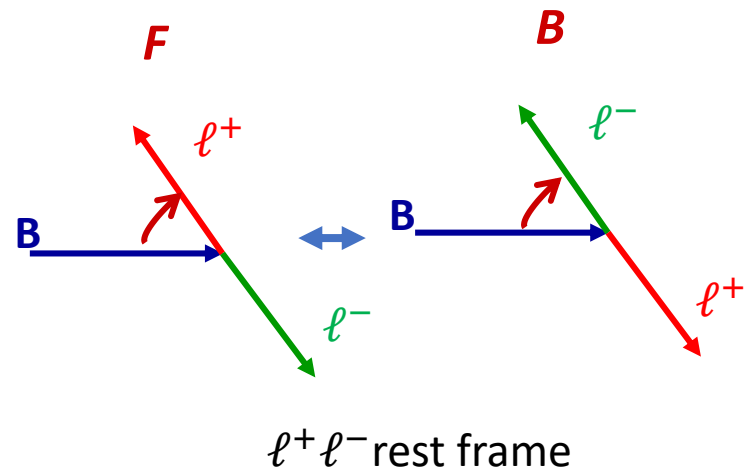
↘

Effective photon contribution

A.Ali et al PRD66,034002 (2002)



SM predictions are not sensitive to QCD corrections



# Measurement of $\mathcal{A}_{FB}$

Belle, PRL96, 251801(2006)

$$B \rightarrow K^{*0} \ell^+ \ell^-, K^{*+} \ell^+ \ell^-, K^+ \ell^+ \ell^-$$

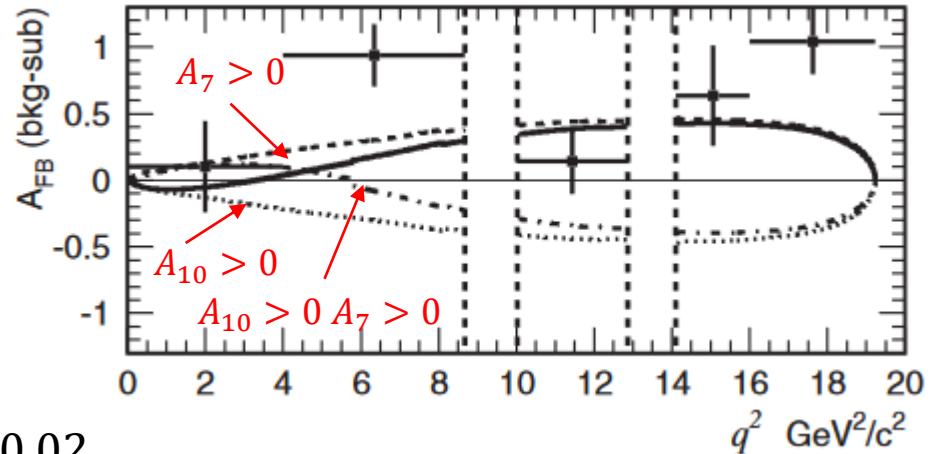
$$K^{*0} \rightarrow K^+ \pi^-,$$

$$K^{*+} \rightarrow K_S^0 \pi^+, K^+ \pi^0$$

357fb<sup>-1</sup>

SM (solid line)

$$A_7 = -0.330; A_9 = 4.069; A_{10} = -4.213;$$



$$\mathcal{A}_{FB}(B \rightarrow K^* \ell^+ \ell^-) = 0.50 \pm 0.15 \pm 0.02$$

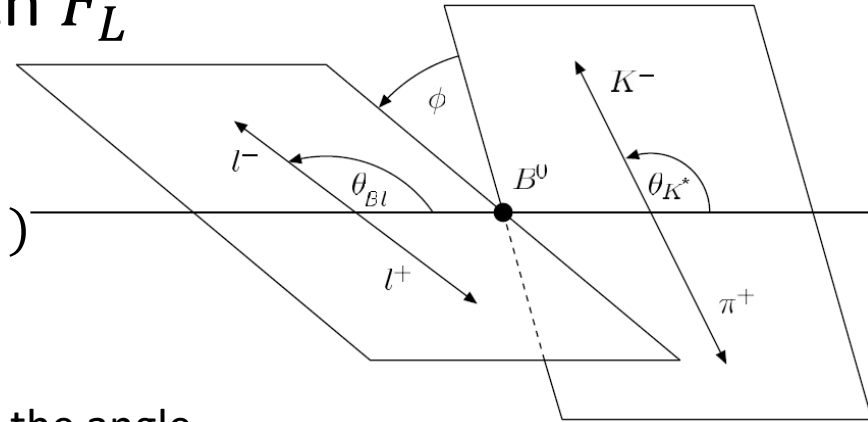
$$\mathcal{A}_{FB}(B \rightarrow K^+ \ell^+ \ell^-) = 0.10 \pm 0.14 \pm 0.01$$

It seems  $C_7 = -C_7^{SM}$  preferred the  $\mathcal{A}_{FB}$  data

Flipping the sign of photonic penguin, would turn on the large rate of  $B \rightarrow X_s \ell \ell$  (then what seen in experiments) Cite19

Addition to measuring  $\mathcal{A}_{FB}$  one can also measure  $K^*$  longitudinal polarization  $F_L$

# $\mathcal{A}_{FB}$ along with $F_L$



$$\frac{d\Gamma}{d\cos\theta_{K^*}} = \frac{3}{4}F_L\cos^2\theta_{K^*} + \frac{3}{4}(1-F_L)(1-\cos^2\theta_{K^*})$$

$\mathcal{A}_{FB}$  is extracted from the fit to  $\cos\theta_{Bl}$ , where  $\theta_{Bl}$  is the angle between  $l^+$  and  $B^0(B^+)$  in dilepton rest frame.

$$\frac{d\Gamma}{d\cos\theta_{Bl}} = \frac{3}{4}F_L(1-\cos^2\theta_{Bl}) + \frac{3}{8}(1-F_L)\left(1+\cos^2\theta_{K^*}\right) + \mathcal{A}_{FB}\cos\theta_{Bl}$$

TABLE III. Results for the fits to the  $K\ell^+\ell^-$  and  $K^*\ell^+\ell^-$  samples.  $N_S$  is the number of signal events in the  $m_{ES}$  fit. The quoted errors are statistical only.

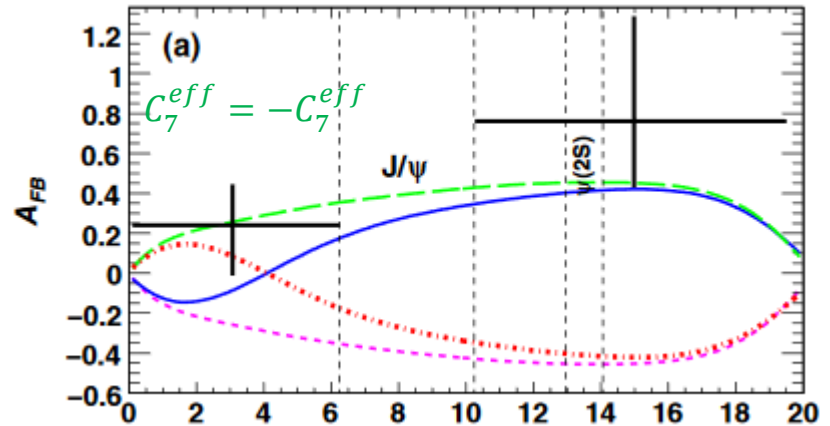
Decay	$q^2$	$N_S$	$F_L$	$\mathcal{A}_{FB}$
$K\ell^+\ell^-$	low	$26.0 \pm 5.7$		$+0.04^{+0.16}_{-0.24}$
	high	$26.5 \pm 6.7$		$+0.20^{+0.14}_{-0.22}$
$K^*\ell^+\ell^-$	low	$27.2 \pm 6.3$	$0.35 \pm 0.16$	$+0.24^{+0.18}_{-0.23}$
	high	$36.6 \pm 9.6$	$0.71^{+0.20}_{-0.22}$	$+0.76^{+0.52}_{-0.32}$

$A_i \approx C_i$   $A_i$  are  $q^2$  independent real term of  $C_i$   
 $C_7 C_9 C_{10}$  are real up to higher order corrections.

One need to use Wilson coefficient complex (not only for NP, but also for SM)

Wou, Hovhannisyanyan, Mahajan PRD 77, 014016 (2008)

SM (solid line)  $C_9^{eff} C_{10}^{eff} = -C_9^{eff} C_{10}^{eff}$



$C_7^{eff} = -C_7^{eff}$  and  $C_9^{eff} C_{10}^{eff} = -C_9^{eff} C_{10}^{eff}$

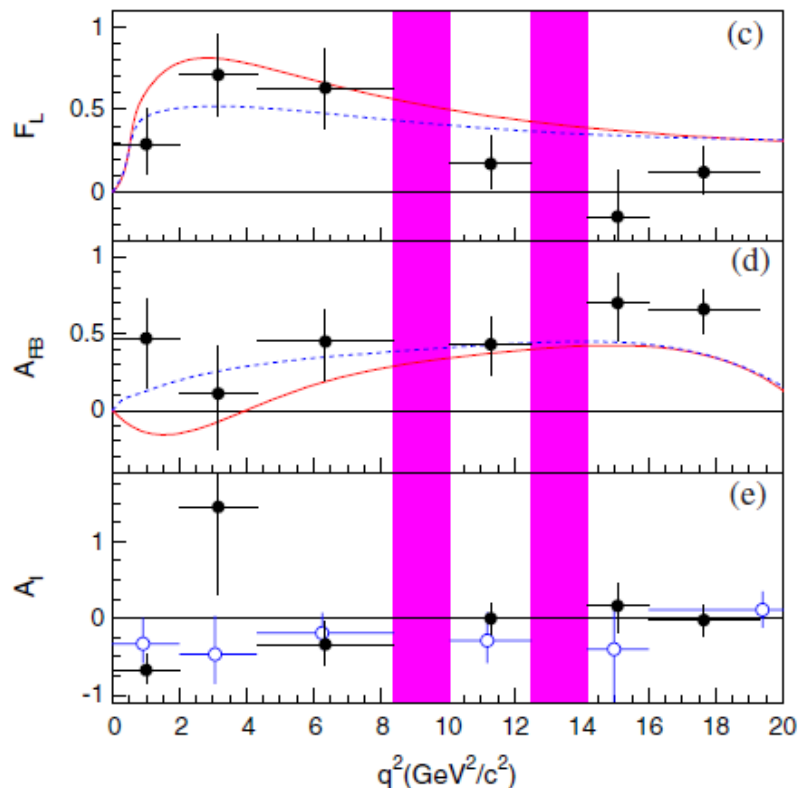
BaBar, PRD79, 031102 (R) (2009).

# $\mathcal{A}_{FB}$ in $B \rightarrow K^* \ell^+ \ell^-$

Belle updated the study and found the opposite sign again

Belle PRL103,171801 (2009)

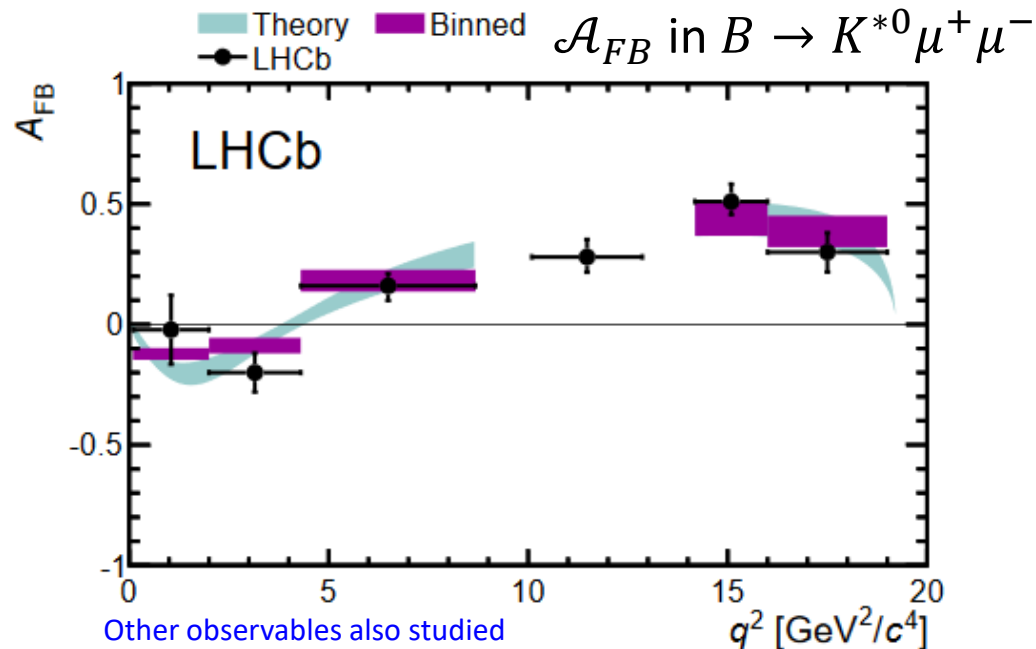
LHCb, JHEP08, 131 (2013)



Both  $e$  and  $\mu$  modes are included

$C_7 = -C_7^{SM}$  seems to be favourable. If then data favoured 4<sup>th</sup> generation case.

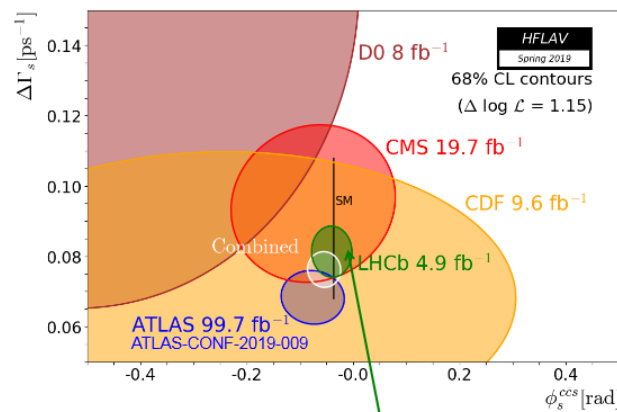
Should be visible else where  
( $\sin 2\phi_{B_s}$  negative)



Other observables also studied

First measurement of zero-crossing point of  $\mathcal{A}_{FB} : q_0^2 = 4.9 \pm 0.9 \text{ GeV}^2/c^4$

Consistent with SM

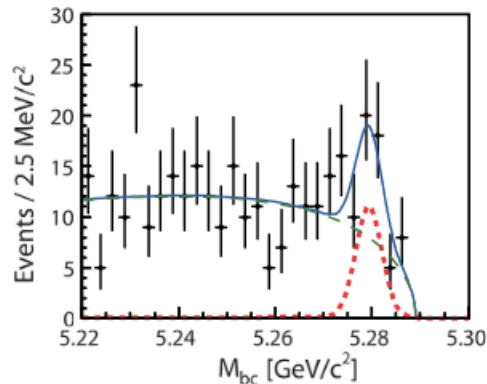


# $\mathcal{A}_{FB}$ in Sum of Exclusive

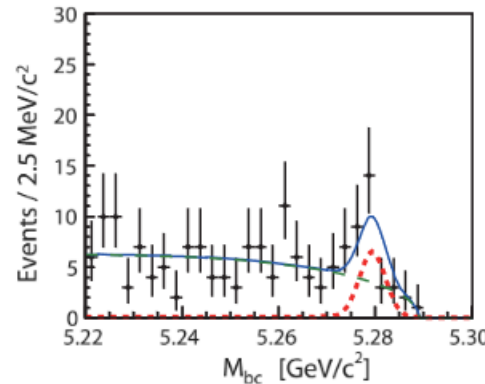
Inclusive measurement is theoretically cleaner than exclusive, but experimentally challenging

$\bar{B}^0$ decays		$B^-$ decays	
$K^- \pi^+$	$(K_S^0)$	$K^-$	$K_S^0 \pi^-$
$K^- \pi^+ \pi^0$	$(K_S^0 \pi^0)$	$K^- \pi^0$	$K_S^0 \pi^- \pi^0$
$K^- \pi^+ \pi^- \pi^+$	$(K_S^0 \pi^- \pi^+)$	$K^- \pi^+ \pi^-$	$K_S^0 \pi^- \pi^+ \pi^-$
$(K^- \pi^+ \pi^- \pi^+ \pi^0)$	$(K_S^0 \pi^- \pi^+ \pi^0)$	$K^- \pi^+ \pi^- \pi^0$	$(K_S^0 \pi^- \pi^+ \pi^- \pi^0)$
	$(K_S^0 \pi^- \pi^+ \pi^- \pi^+)$	$(K^- \pi^+ \pi^- \pi^+ \pi^-)$	

$M(X_S) < 2.0 \text{ GeV}/c^2$



(a)  $B \rightarrow X_s e^+ e^-$  candidates with  $\cos \theta > 0$



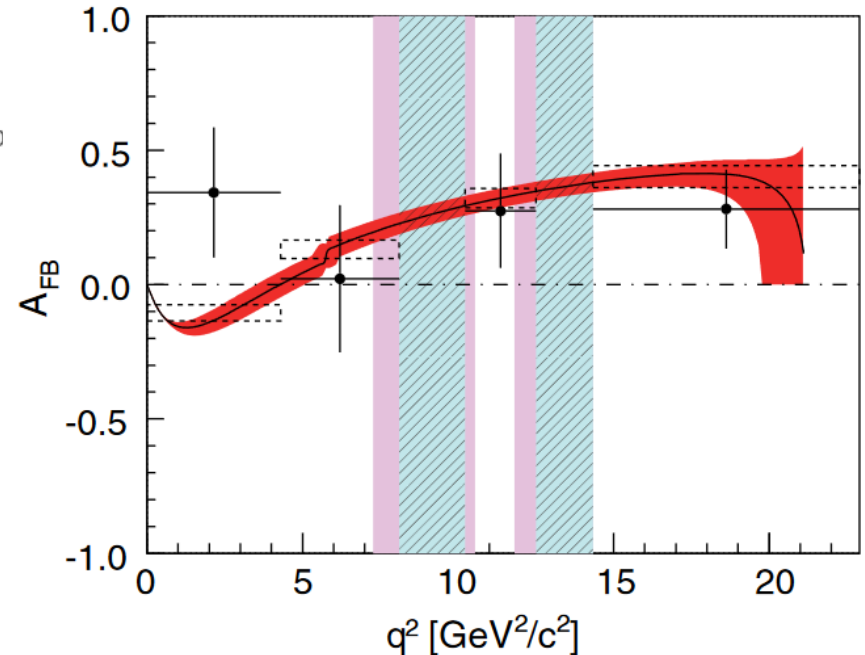
(b)  $B \rightarrow X_s e^+ e^-$  candidates with  $\cos \theta < 0$

Result is consistent with SM prediction within error

1.8 $\sigma$  tension in low  $q^2$

Need more data points for this study

Belle, PRD 93, 032008 (2016)



# $P'_5$ anomaly Continuing with $B \rightarrow K^* \ell^+ \ell^-$

Angular analysis of  $B \rightarrow \ell^+ \ell^- K^* (892) (\rightarrow K^- \pi^+)$ .

One can simply measure the angles between the direction of flight of all the different particles as function of  $q^2$

Differential Angular distribution can be written as

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{d\cos\theta_\ell d\cos\theta_K d\phi dq^2} = \frac{9}{32\pi} \left[ \frac{3}{4} (1 - F_L) \sin^2\theta_K + F_L \cos^2\theta_K + \frac{1}{4} (1 - F_L) \sin^2\theta_K \cos 2\theta_\ell \right. \\ \left. - F_L \cos^2\theta_K \cos 2\theta_\ell + S_3 \sin^2\theta_K \sin^2\theta_\ell \cos 2\phi + S_4 \sin 2\theta_K \sin 2\theta_\ell \cos\phi \right. \\ \left. + S_5 \sin 2\theta_K \sin\theta_\ell \cos\phi + S_6 \sin^2\theta_K \cos\theta_\ell + S_7 \sin 2\theta_K \sin\theta_\ell \sin\phi \right. \\ \left. + S_8 \sin 2\theta_K \sin 2\theta_\ell \sin\phi + S_9 \sin^2\theta_K \sin^2\theta_\ell \sin 2\phi \right].$$

$F_L$  is the longitudinal polarization fraction

One has additional angular observables  $S_n$  ( $n = 3, 4, 5, 7, 8, 9$ ) from the decay amplitude, which are functions of the Wilson coefficients and form factors

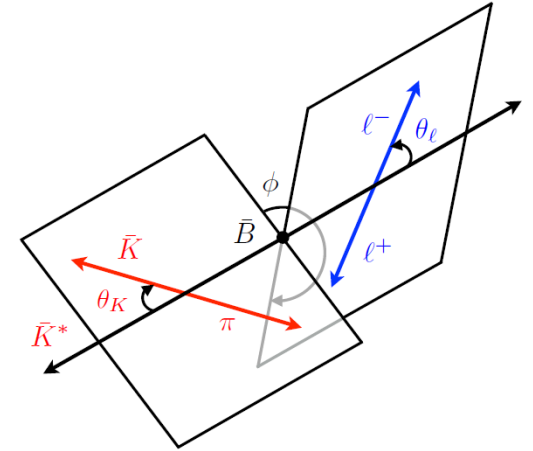
Suggested by [Decoste-Genon etal JHEP 2013, 137 \(2013\)](#)

$$P'_{4,5,6,8} = \frac{S_{4,5,6,8}}{\sqrt{F_L(1 - F_L)}}$$

These observables are largely free from form factor uncertainties (especially at low  $q^2$ )

Each transformation preserves the first five terms and corresponding  $S_i$  term.

Resulting angular distribution depend only on  $F_L, S_3$  and one of the observables  $S_{4,5,7,8}$



$$P'_{4, S_4}: \begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \phi \rightarrow \pi - \phi & \text{for } \theta_\ell > \pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases}$$

$$P'_{5, S_5}: \begin{cases} \phi \rightarrow -\phi & \text{for } \phi < 0 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases}$$

$$P'_{6, S_7}: \begin{cases} \phi \rightarrow \pi - \phi & \text{for } \phi > \pi/2 \\ \phi \rightarrow -\pi - \phi & \text{for } \phi < -\pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2, \end{cases}$$

$$P'_{8, S_8}: \begin{cases} \phi \rightarrow \pi - \phi & \text{for } \phi > \pi/2 \\ \phi \rightarrow -\pi - \phi & \text{for } \phi < -\pi/2 \\ \theta_K \rightarrow \pi - \theta_K & \text{for } \theta_\ell > \pi/2 \\ \theta_\ell \rightarrow \pi - \theta_\ell & \text{for } \theta_\ell > \pi/2. \end{cases}$$

# First anomaly observed in $P_5'$

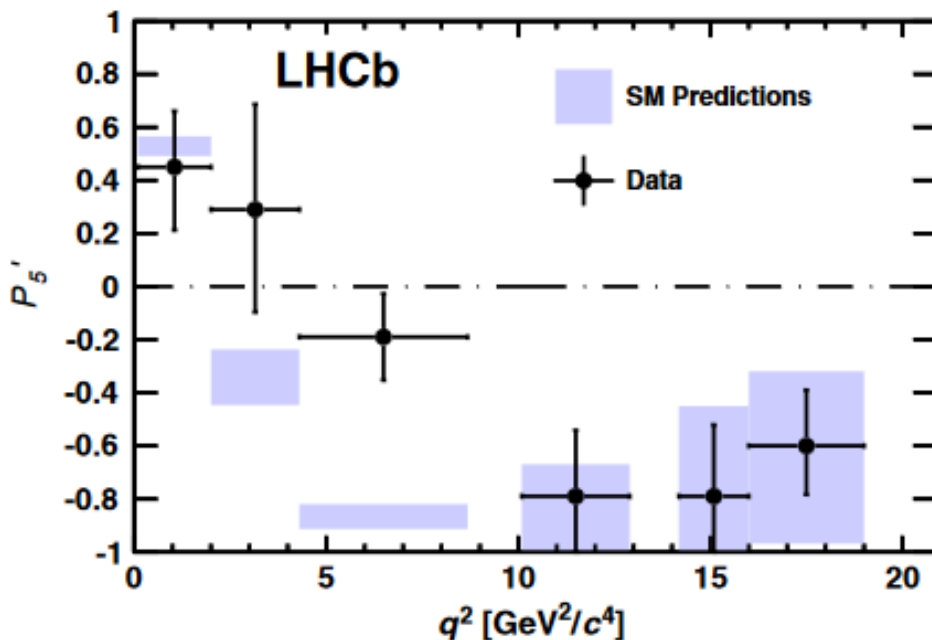
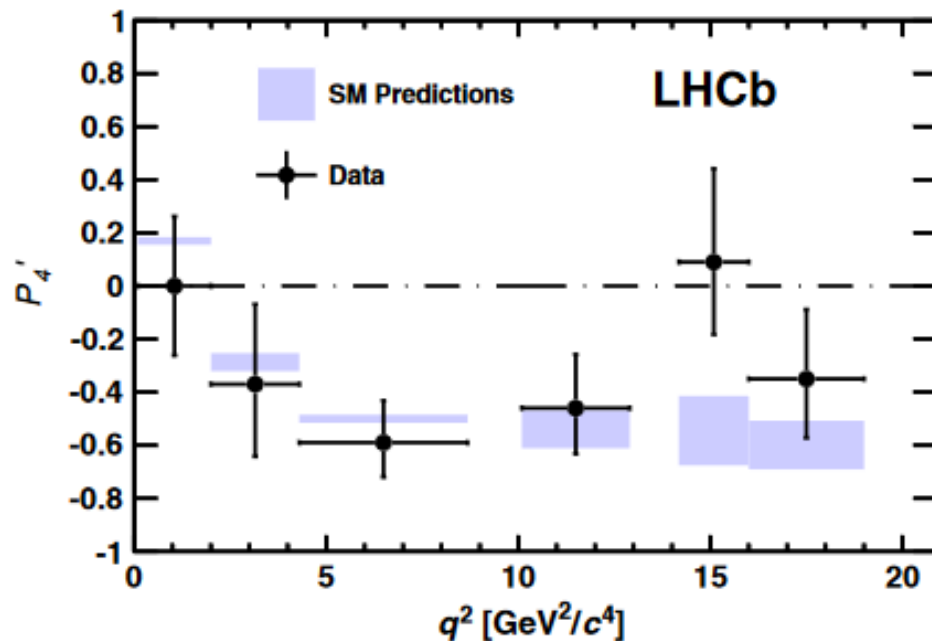
LHCb, PRL 111, 191801 (2013)

$$B \rightarrow K^*(892)\mu^+\mu^-$$

$$K^*(892) \rightarrow K^-\pi^+$$

Local discrepancy of  $3.7\sigma$  is observed in the interval  $4.30 < q^2 < 8.68 \text{ GeV}^2$  for  $P_5'$

Integrating over 1-6, is  $2.5\sigma$

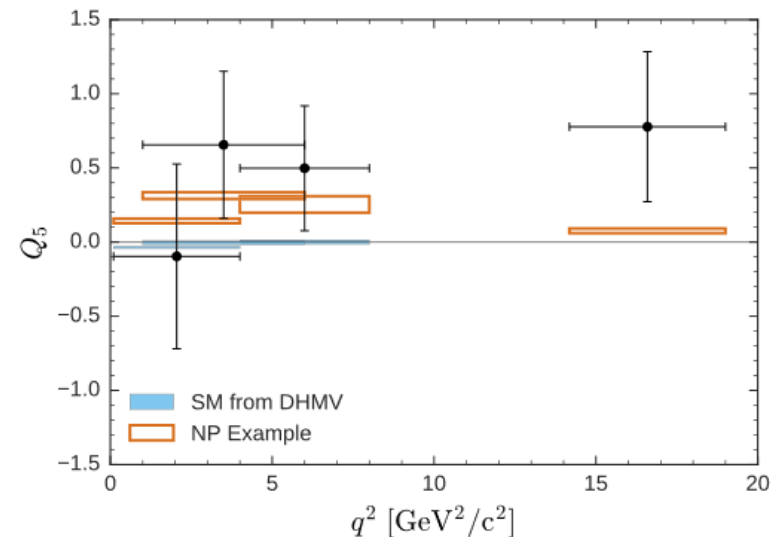
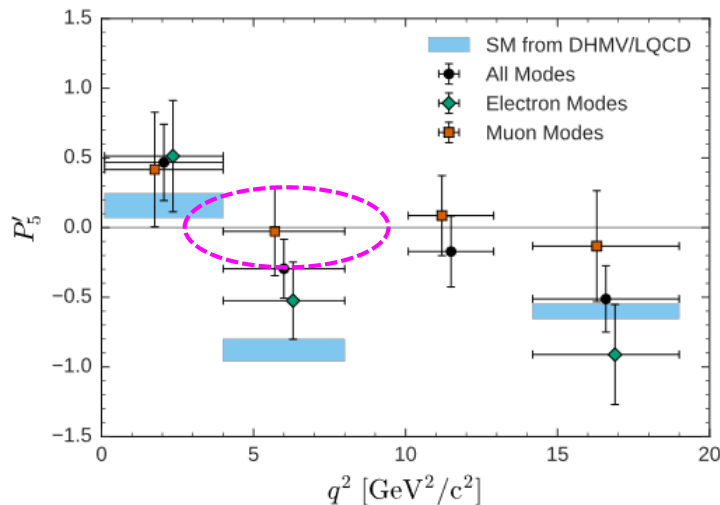
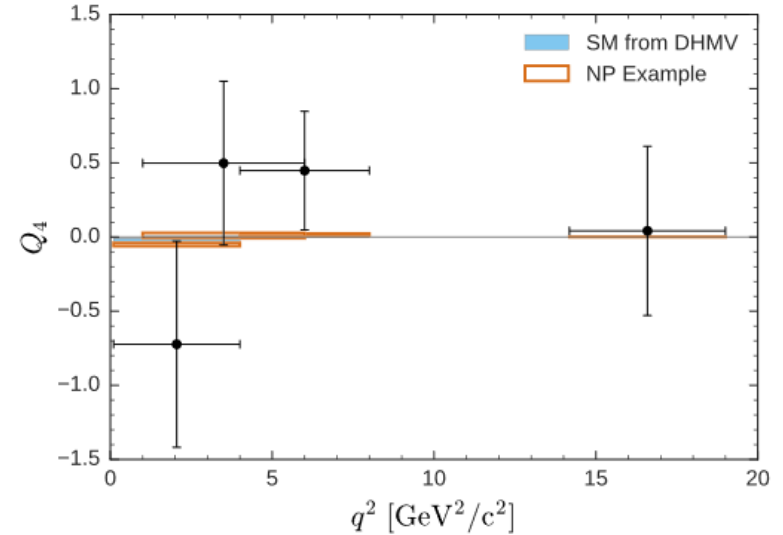
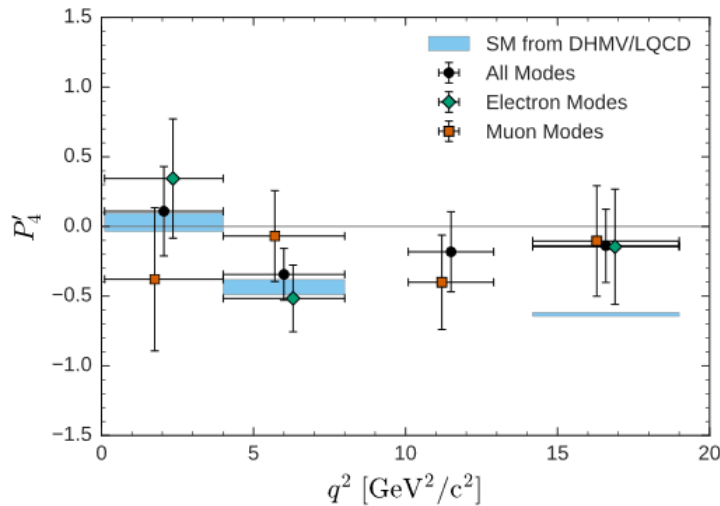


# Belle data support similar trend

Bernat *et al* JHEP 10,075 (2016)

$B \rightarrow K^*(892)\ell^+\ell^-$   $\ell$  for  $e$  and  $\mu$   
 $K^*(892) \rightarrow K^-\pi^+, K_S\pi^+, K^+\pi^0$

Observable to test LFU,  $Q_i = P_i'^{\mu} - P_i'^e$   
 Deviation from zero test of SM.



$Q_i$  provide unambiguous signal of NP, as in  $P_i$  hadronic uncertainties were argued.

Belle, PRL 118, 111801 (2017)



# First lepton-flavour-dependent measurement for $P'_5$ is reported

TABLE I. Fit results for  $P'_4$  and  $P'_5$  for all decay channels and separately, for the electron and muon modes. The first uncertainties are statistical and the second systematic.

$q^2$ in $\text{GeV}^2/c^2$	$P'_4$	$P_4^{e'}$	$P_4^{\mu'}$	$P'_5$	$P_5^{e'}$	$P_5^{\mu'}$
[1.00, 6.00]	$-0.45^{+0.23}_{-0.22} \pm 0.09$	$-0.72^{+0.40}_{-0.39} \pm 0.06$	$-0.22^{+0.35}_{-0.34} \pm 0.15$	$0.23^{+0.21}_{-0.22} \pm 0.07$	$-0.22^{+0.39}_{-0.41} \pm 0.03$	$0.43^{+0.26}_{-0.28} \pm 0.10$
[0.10, 4.00]	$0.11^{+0.32}_{-0.31} \pm 0.05$	$0.34^{+0.41}_{-0.45} \pm 0.11$	$-0.38^{+0.50}_{-0.48} \pm 0.12$	$0.47^{+0.27}_{-0.28} \pm 0.05$	$0.51^{+0.39}_{-0.46} \pm 0.09$	$0.42^{+0.39}_{-0.39} \pm 0.14$
[4.00, 8.00]	$-0.34^{+0.18}_{-0.17} \pm 0.05$	$-0.52^{+0.24}_{-0.22} \pm 0.03$	$-0.07^{+0.32}_{-0.31} \pm 0.07$	$-0.30^{+0.19}_{-0.19} \pm 0.09$	$-0.52^{+0.28}_{-0.26} \pm 0.03$	$-0.03^{+0.31}_{-0.30} \pm 0.09$
[10.09, 12.90]	$-0.18^{+0.28}_{-0.27} \pm 0.06$	...	$-0.40^{+0.33}_{-0.29} \pm 0.09$	$-0.17^{+0.25}_{-0.25} \pm 0.01$	...	$0.09^{+0.29}_{-0.29} \pm 0.02$
[14.18, 19.00]	$-0.14^{+0.26}_{-0.26} \pm 0.05$	$-0.15^{+0.41}_{-0.40} \pm 0.04$	$-0.10^{+0.39}_{-0.39} \pm 0.07$	$-0.51^{+0.24}_{-0.22} \pm 0.01$	$-0.91^{+0.36}_{-0.30} \pm 0.03$	$-0.13^{+0.39}_{-0.35} \pm 0.06$

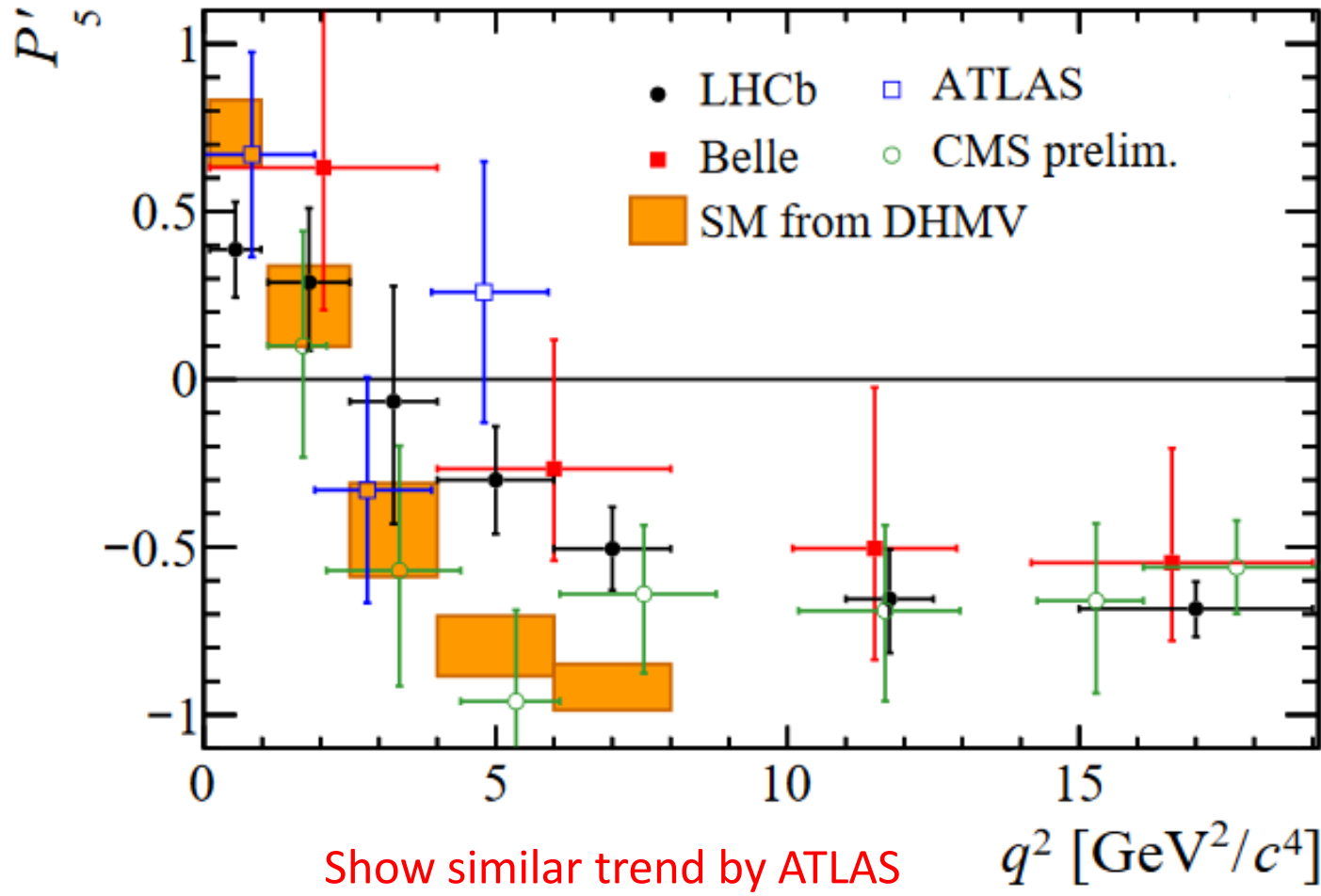
TABLE II. Results for the lepton-flavor-universality-violating observables  $Q_4$  and  $Q_5$ . The first uncertainty is statistical and the second systematic.

First time	$q^2$ in $\text{GeV}^2/c^2$	$Q_4$	$Q_5$
	[1.00, 6.00]	$0.498 \pm 0.527 \pm 0.166$	$0.656 \pm 0.485 \pm 0.103$
	[0.10, 4.00]	$-0.723 \pm 0.676 \pm 0.163$	$-0.097 \pm 0.601 \pm 0.164$
	[4.00, 8.00]	$0.448 \pm 0.392 \pm 0.076$	$0.498 \pm 0.410 \pm 0.095$
	[14.18, 19.00]	$0.041 \pm 0.565 \pm 0.082$	$0.778 \pm 0.502 \pm 0.065$

Results are compatible with SM within statistical uncertainty.

Largest discrepancy is  $2.6\sigma$  in  $P'_5$  for the muon channel

# Results from ATLAS and CMS on $P'_5$



Differential branching fraction in  $B \rightarrow K\mu\mu, B_s \rightarrow \phi\mu\mu, B \rightarrow K^*\mu\mu, \Lambda_b \rightarrow \Lambda\mu\mu$  consistently lower than SM prediction

# $R_{K^*} R_K$ anomaly

Lepton flavour universality (LFU): electroweak couplings treat all flavours of leptons same (*observed difference are due to their mass differences*)

LFU can be tested very precisely

$$R_K = \frac{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\Gamma[B^+ \rightarrow K^+ \mu^+ \mu^-]}{dq^2} dq^2}{\int_{q_{\min}^2}^{q_{\max}^2} \frac{d\Gamma[B^+ \rightarrow K^+ e^+ e^-]}{dq^2} dq^2}$$

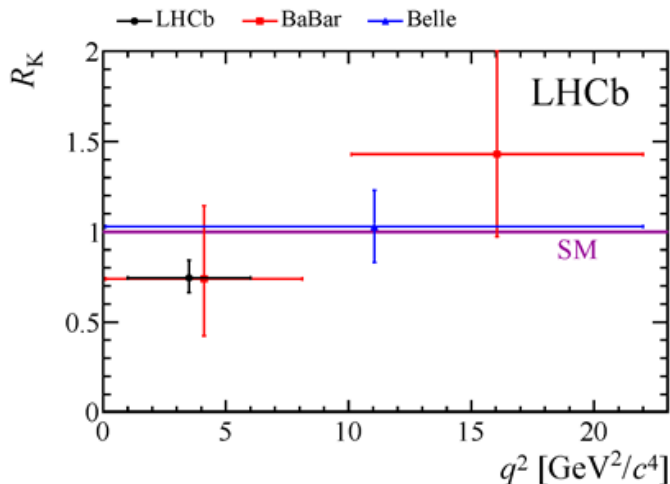
In ratio, hadronic uncertainties cancel and SM prediction is near unity.

$$R_K^{SM} = \frac{\mathcal{B}(B^+ \rightarrow K^+ \mu^+ \mu^-)}{\mathcal{B}(B^+ \rightarrow K^+ e^+ e^-)} = 1 \pm \mathcal{O}(10^{-4})$$

C. Bobeth et al, JHEP 07, 040 (2004)  
HPQCD, PRL111, 162002 (2013)

$R_H, H = K, K^*, X_S$  provides constraint to the New Physics G. Hiller, F. Kruger PRD69. 074020 (2004)  
0.001 typical error

In 2014, LHCb measured  $R_K$  and saw  $2.6\sigma$  hint of deviation from the SM.



Both BaBar and LHCb seems to favour a value below one.

Belle result didn't contradict  $q^2$  dependent.

$$R_K[1.0 < q^2 < 6.0 \text{ GeV}^2] = 0.745_{-0.074}^{+0.090} \pm 0.036$$

LHCb, PRL113, 151601(2014) BaBar, PRD86, 032012(2012) Belle, PRL103, 171801(2009)

# $B \rightarrow K^{*0} \ell \ell$

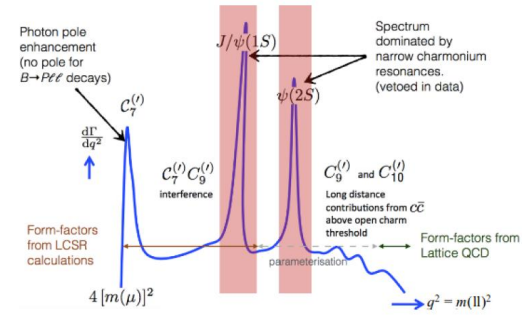
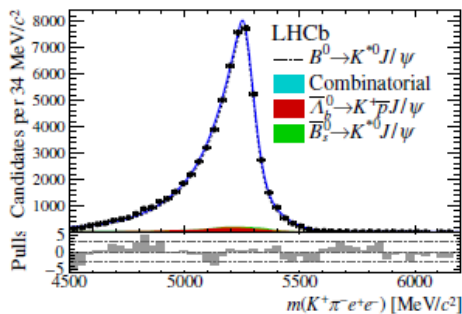
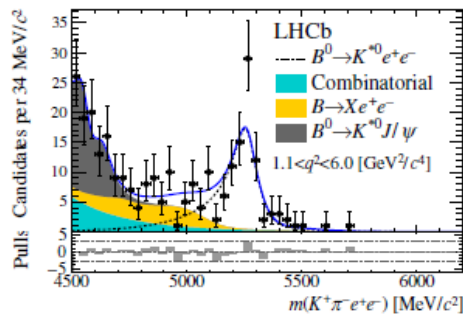
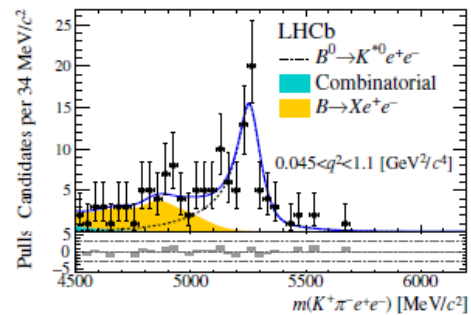
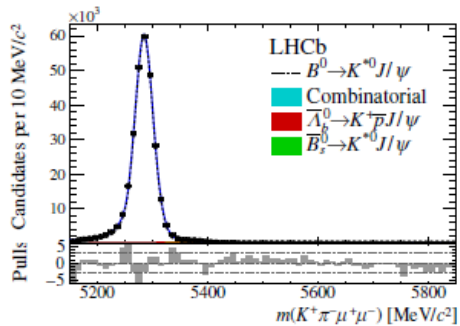
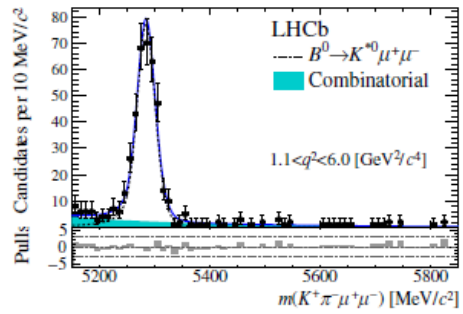
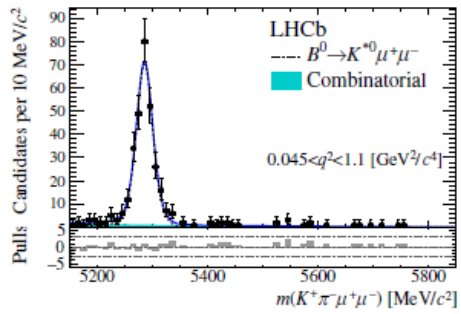
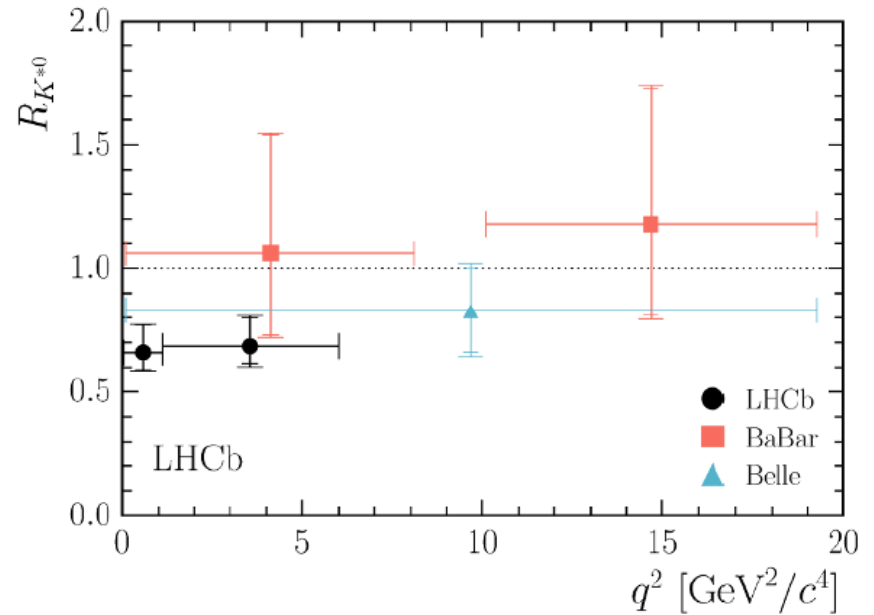
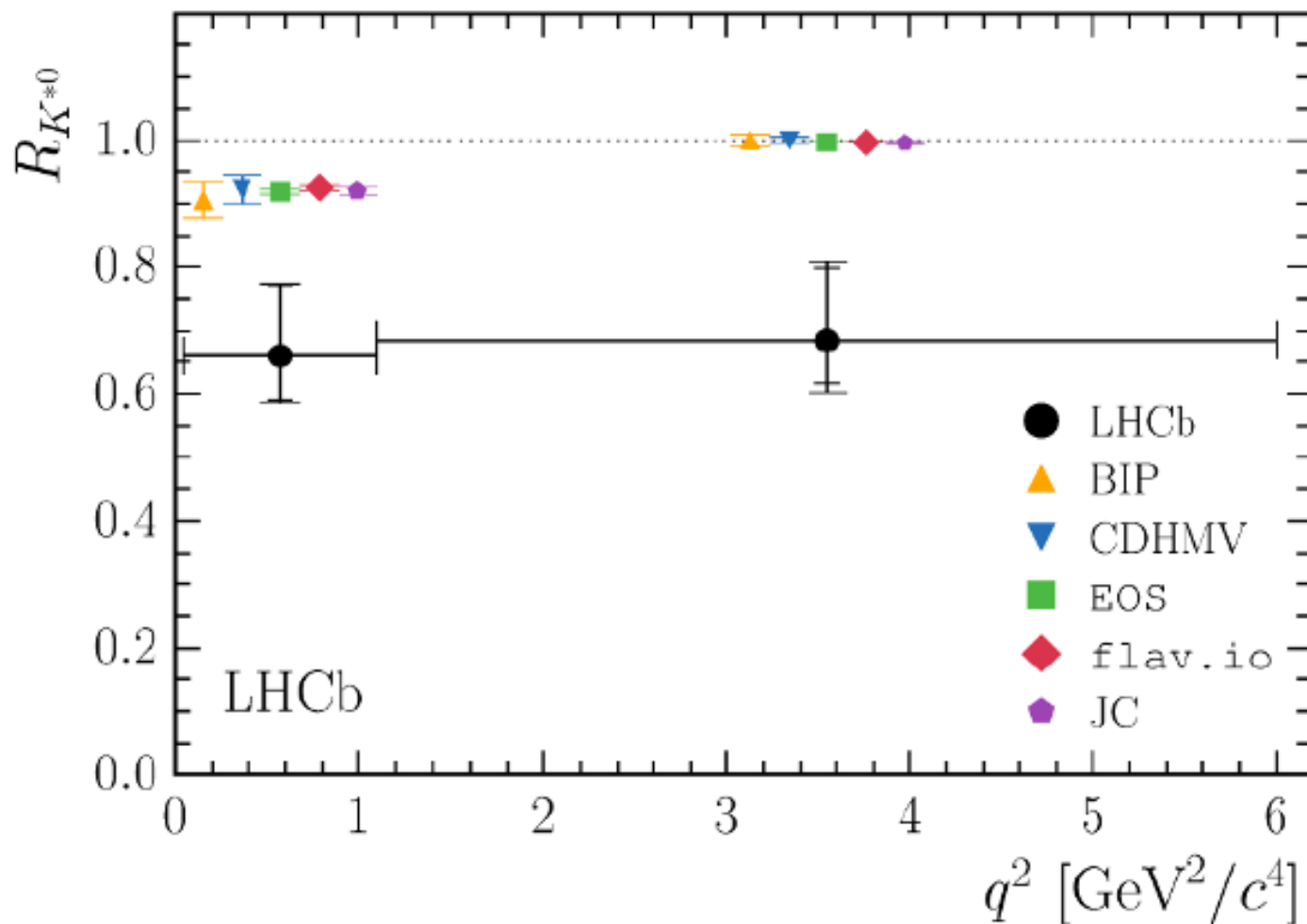


Photo peak, *missing in  $R_K$* , allow for enough statistics in low  $q^2$



# $R_{K^*}$ anomaly

LHCb, JHEP08, 055 (2017)

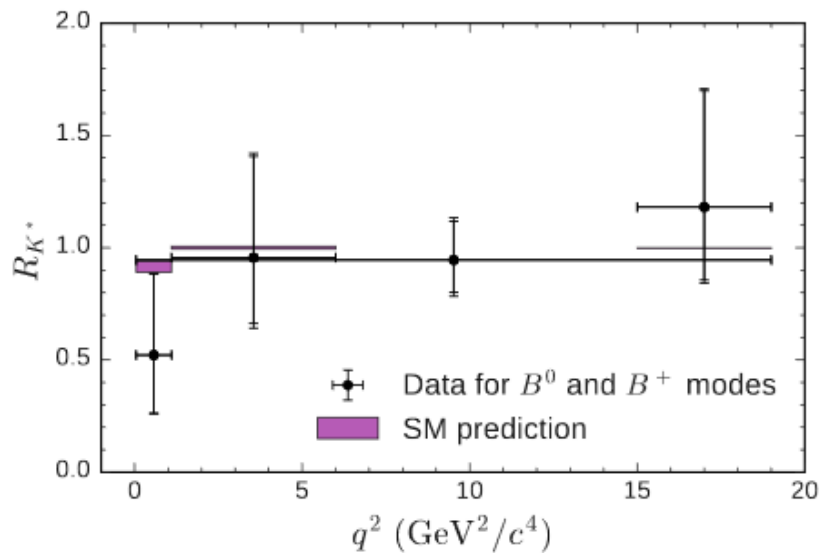
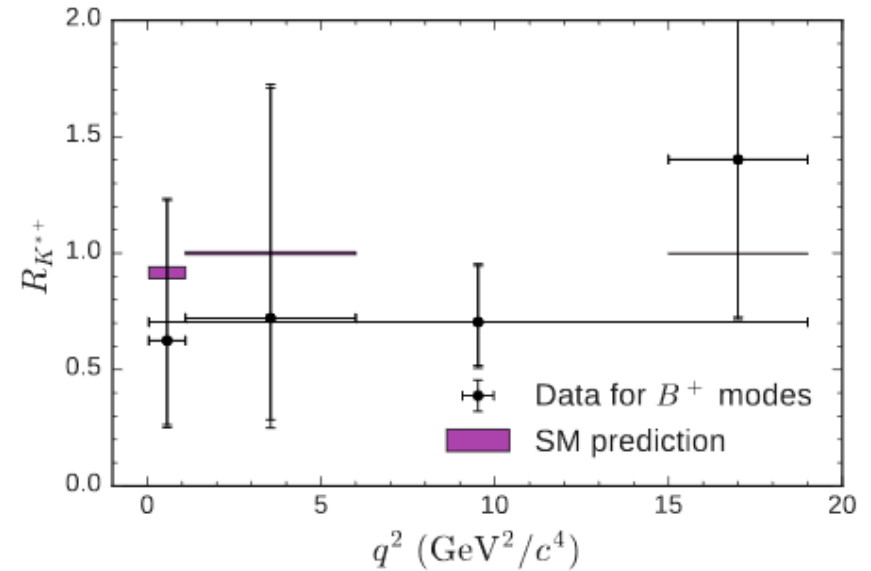
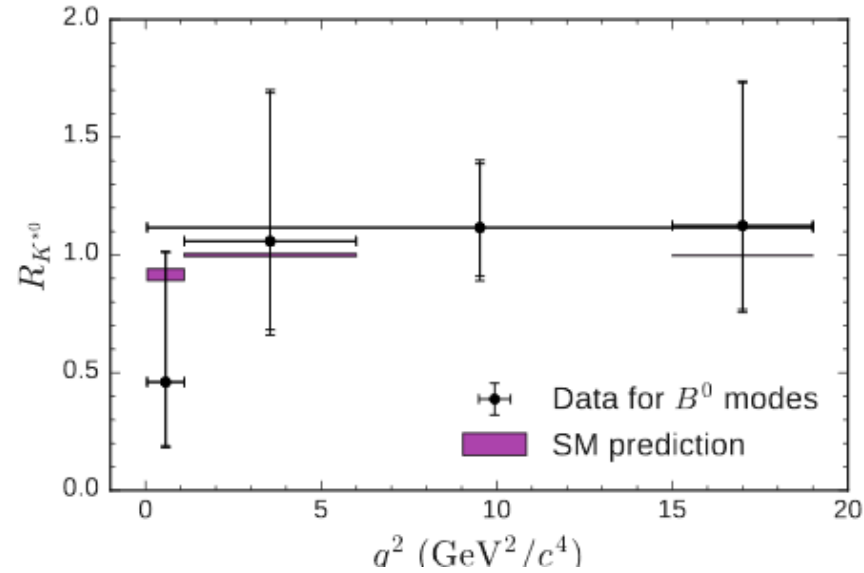


Deviation  
From SM

$2.1\sigma$

$2.4\sigma$

Trend similar to  $R_K$

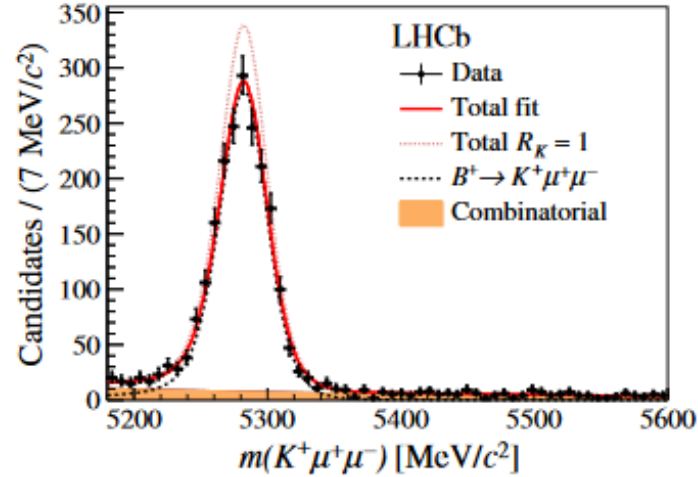
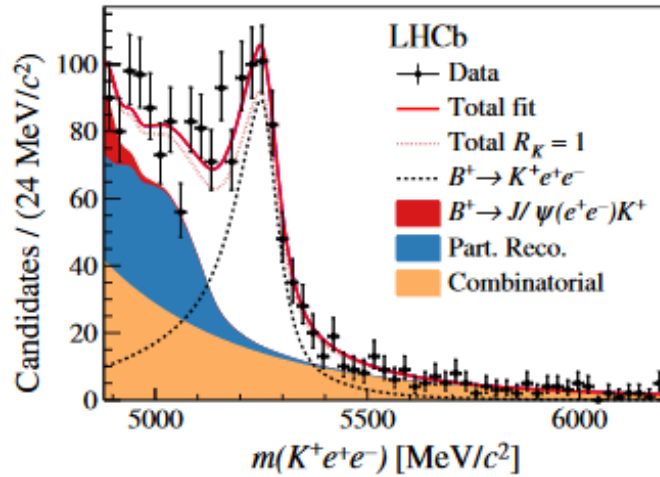
Belle result on  $R_{K^*}$  $K^*$  from  $K^+\pi^-$ ,  $K^+\pi^0$ , and  $K_S^0\pi^+$  $B^0 \rightarrow K^{*0}\mu^+\mu^-$ ,  $B^+ \rightarrow K^{*+}\mu^+\mu^-$ ,  $B^0 \rightarrow K^{*0}e^+e^-$  and  $B^+ \rightarrow K^{*+}e^+e^-$ First measurement of  $R_{K^{*+}}$ 

Consistent with SM, large uncertainty.

Need more statistics !

Trend similar to LHCb

# $B \rightarrow K^+ \ell \ell$ 2019 LHCb $R_K$ update



$$R_{K,\text{Run 1}}^{\text{new}} = 0.717_{-0.071}^{+0.083} (\text{stat})_{-0.016}^{+0.017} (\text{syst}),$$

$$R_{K,\text{Run 2}} = 0.928_{-0.076}^{+0.089} (\text{stat}) \pm_{-0.017}^{+0.020} (\text{syst}).$$

$$R_K[1.1 < q^2 < 6.0 \text{ GeV}^2] = 0.846_{-0.054-0.014}^{+0.060+0.016}$$

Most precise measurement to data

Consistent with SM at the level of  $2.5 \sigma$  deviation

$$R_K[1.0 < q^2 < 6.0 \text{ GeV}^2] = 0.745_{-0.074}^{+0.090} \pm 0.036 \quad \text{LHCb, PRL113, 151601(2014)}$$

# $B \rightarrow K \ell \ell$

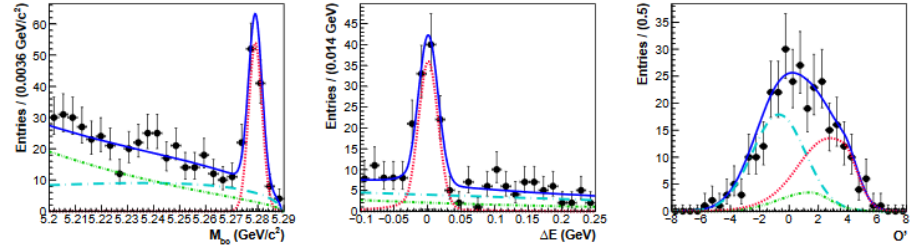
Here  $K$  can be  $K^+$  and  $K_S^0$

# $R_K$ result from Belle

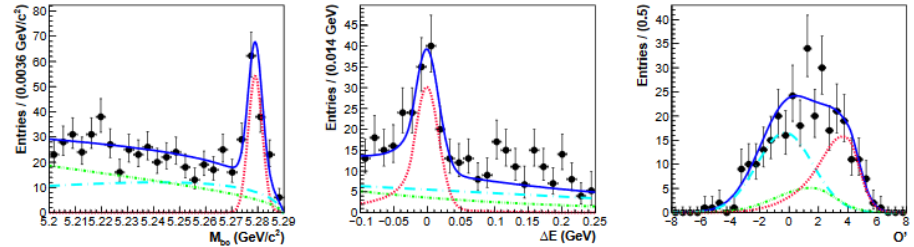
Belle, arXiv:190801848

Background and signal strength similar.

$$B \rightarrow K^+ \mu^+ \mu^-$$

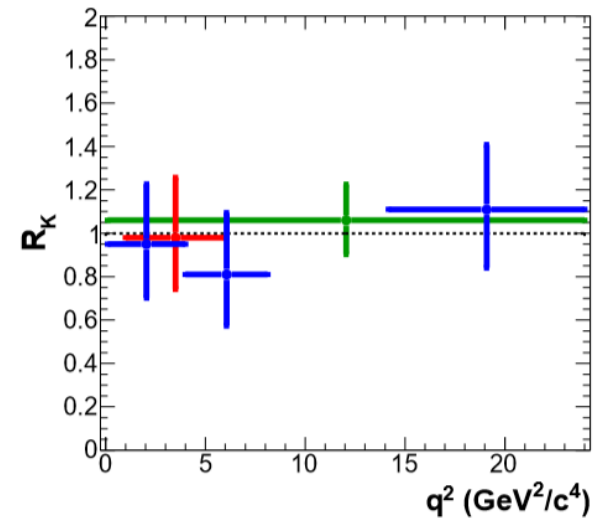
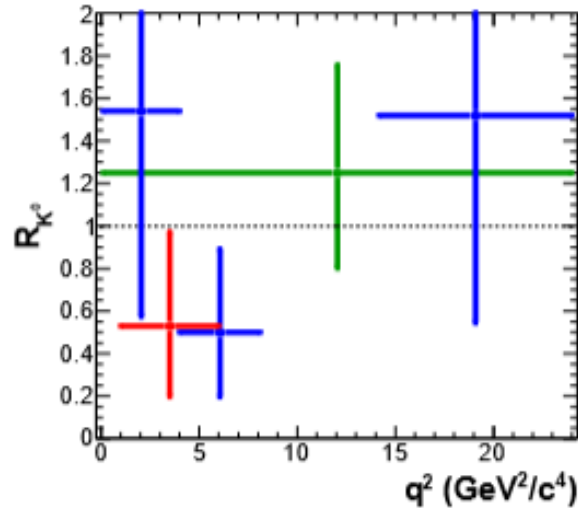
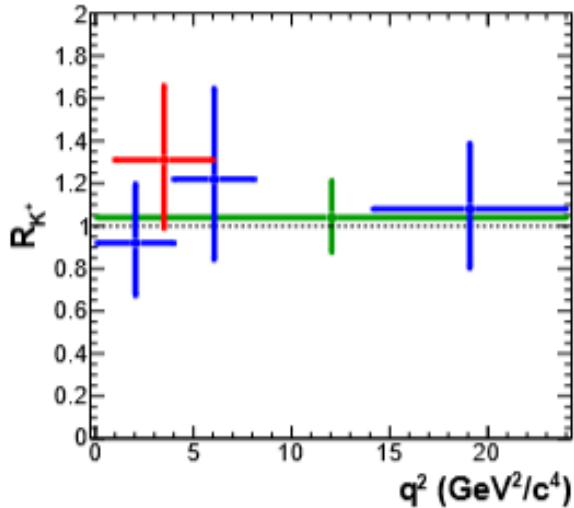


$$B \rightarrow K^+ e^+ e^-$$



$$1 < q^2 < 6 \text{ GeV}^2/c^4$$

$$0.1 < q^2 < 4 \text{ GeV}^2/c^4$$



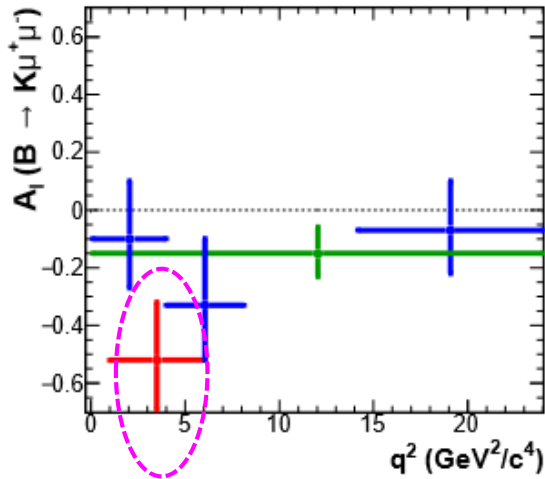
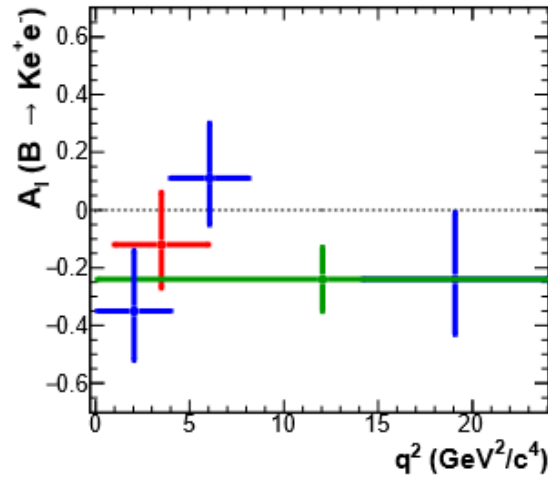
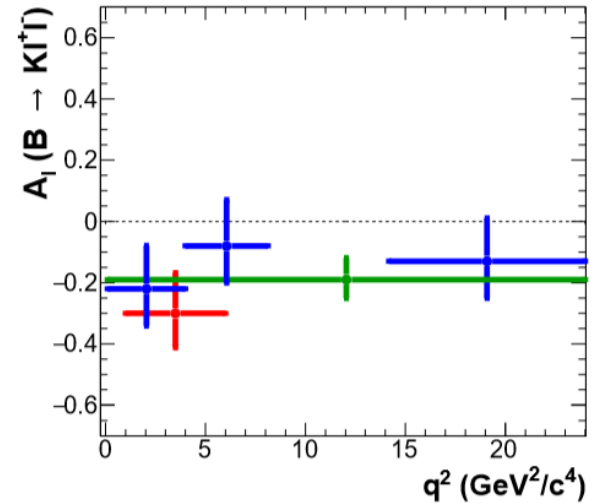
Result is consistent with LHCb as well as SM

More precision at Belle II



Isospin asymmetry

$$A_I = \frac{(\tau_{B^+}/\tau_{B^0})\mathcal{B}(B^0 \rightarrow K^0 \ell^+ \ell^-) - \mathcal{B}(B^+ \rightarrow K^+ \ell^+ \ell^-)}{(\tau_{B^+}/\tau_{B^0})\mathcal{B}(B^0 \rightarrow K^0 \ell^+ \ell^-) + \mathcal{B}(B^+ \rightarrow K^+ \ell^+ \ell^-)}$$


 $0.1 < q^2 < 4 \text{ GeV}^2/c^4$ 

 $1 < q^2 < 6 \text{ GeV}^2/c^4$ 


$A_I$  for all bins have negative asymmetry.

For bin  $1 < q^2 < 6 \text{ GeV}^2/c^4$  deviates from zero by  $2.7\sigma$  for muon final state.

First time provided by Belle

# Anomalies leading SM



or

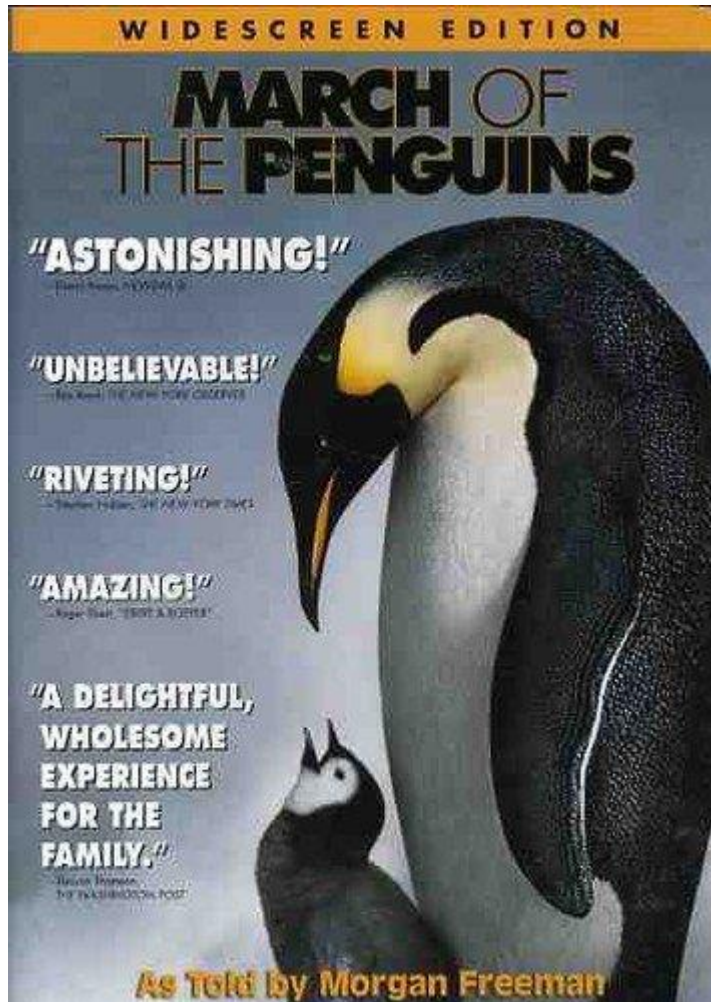
<https://www.mycustomer.com/experience/engagement/how-can-leaders-create-conditions-for-all-employees-to-deliver-outstanding-cx>



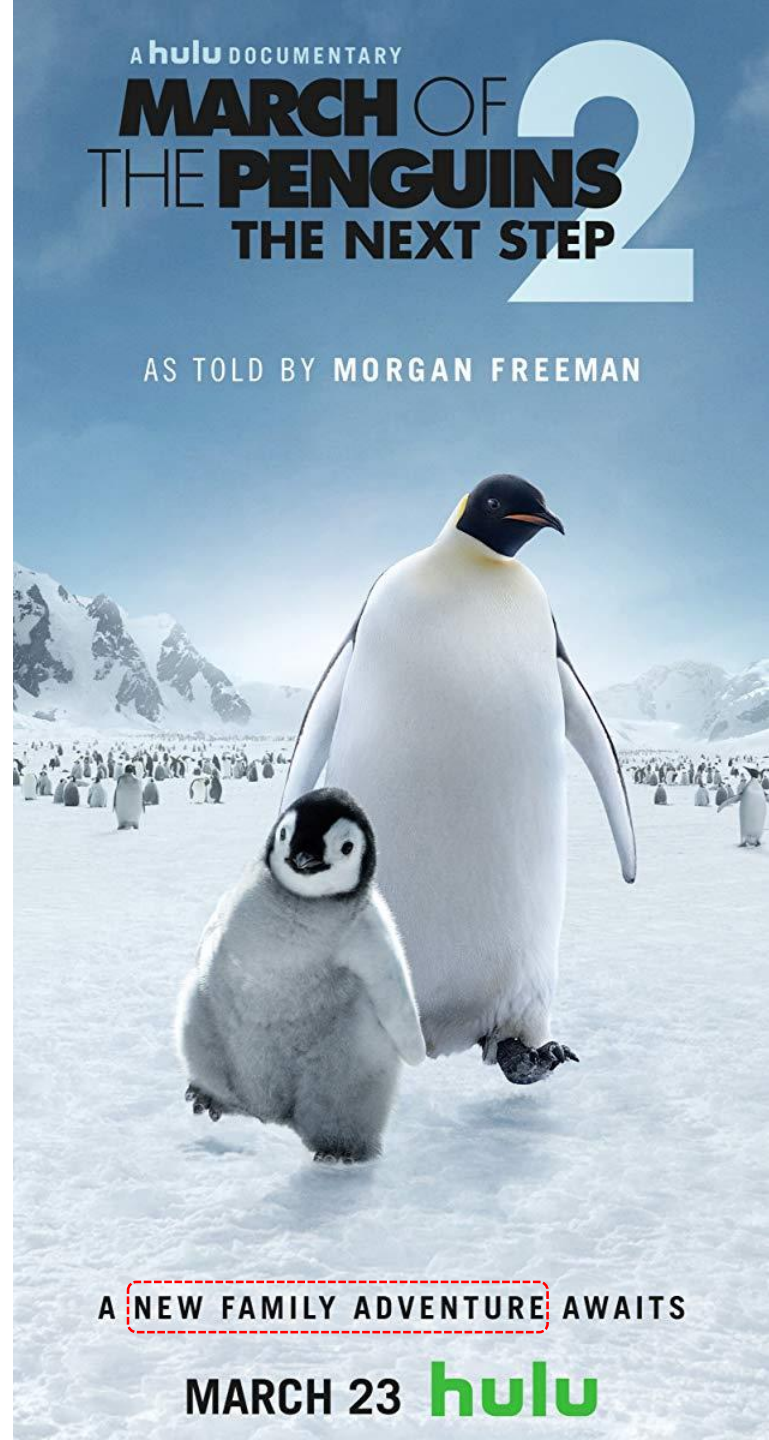
SM leading anomalies

# SM itself an anomaly (?)





<https://images-na.ssl-images-amazon.com/images/I/51fvLhfOxVL.jpg>





**Thank you**

Observables	Belle 0.71 ab <sup>-1</sup>	Belle II 5 ab <sup>-1</sup>	Belle II 50 ab <sup>-1</sup>
$R_K$ ([1.0, 6.0] GeV <sup>2</sup> )	28%	11%	3.6%
$R_K$ (> 14.4 GeV <sup>2</sup> )	30%	12%	3.6%
$R_{K^*}$ ([1.0, 6.0] GeV <sup>2</sup> )	26%	10%	3.2%
$R_{K^*}$ (> 14.4 GeV <sup>2</sup> )	24%	9.2%	2.8%
$R_{X_s}$ ([1.0, 6.0] GeV <sup>2</sup> )	32%	12%	4.0%
$R_{X_s}$ (> 14.4 GeV <sup>2</sup> )	28%	11%	3.4%
$P'_5$ ([1.0, 2.5] GeV <sup>2</sup> )	0.47	0.17	0.054
$P'_5$ ([2.5, 4.0] GeV <sup>2</sup> )	0.42	0.15	0.049
$P'_5$ ([4.0, 6.0] GeV <sup>2</sup> )	0.34	0.12	0.040
$P'_5$ (> 14.2 GeV <sup>2</sup> )	0.23	0.088	0.027

Given the above formula and input for  $b_n^{0,+}$ , the SM predicts  $R_\pi^{\text{SM}} = 0.641 \pm 0.016$ , whereas the experimental data suggests  $R_\pi^{\text{exp.}} \simeq 1.05 \pm 0.51$  by using  $\mathcal{B}(B \rightarrow \pi \ell \bar{\nu}_\ell) = (1.45 \pm 0.05) \times 10^{-4}$  [77]. Thus, at present the experimental result is consistent with the SM prediction

$$R_\pi^{5\text{ab}^{-1}} = 0.64 \pm 0.23,$$

$$R_\pi^{50\text{ab}^{-1}} = 0.64 \pm 0.09.$$

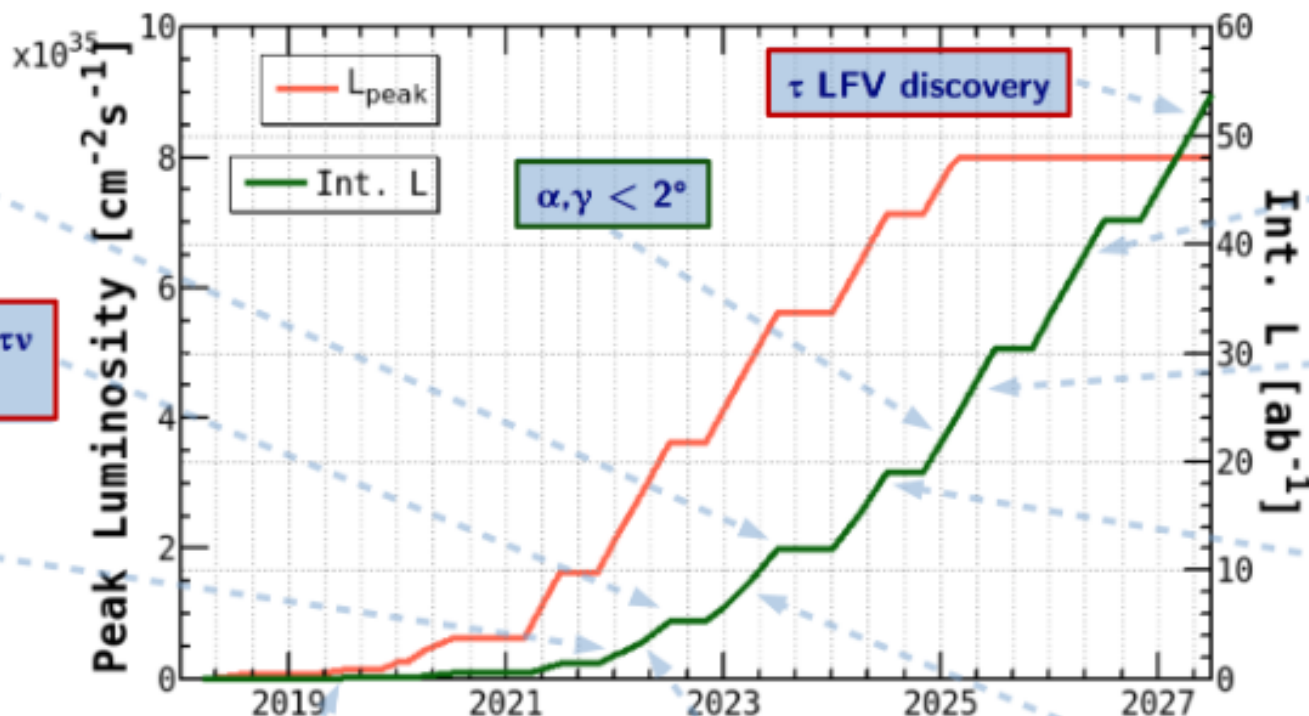
	5 ab <sup>-1</sup>	50 ab <sup>-1</sup>
$R_D$	(±6.0 ± 3.9)%	(±2.0 ± 2.5)%
$R_{D^*}$	(±3.0 ± 2.5)%	(±1.0 ± 2.0)%
$P_\tau(D^*)$	±0.18 ± 0.08	±0.06 ± 0.04

$$R(D^*) = 0.270 \pm 0.035(\text{stat})_{-0.025}^{+0.028}(\text{syst}),$$

$$P_\tau(D^*) = -0.38 \pm 0.51(\text{stat})_{-0.16}^{+0.21}(\text{syst}),$$



# Prospects for data & physics harvesting



$B \rightarrow \eta' K_s$   
new CP

Confirm  $B \rightarrow D^* \tau \nu$   
new physics

Resolve  
 $|V_{ub}|$  puzzle

$\tau$  LFV discovery

$\alpha, \gamma < 2^\circ$

$W_R$  in  
 $B \rightarrow \rho \gamma$

$B \rightarrow K \nu \nu$  SM  
discovery

$B \rightarrow K e e$  LFUV  
new physics

$ee \rightarrow A'(\chi\chi)\gamma$

$ee \rightarrow \pi\pi(\gamma)$   
precision for  $(g-2)_\mu$

$B \rightarrow \mu\nu$   
discovery

All the details are in  
"The Belle II Physics Book"  
arXiv:1808.10567

- $1 \text{ ab}^{-1}$  (= Belle) in 2021
- $5 \text{ ab}^{-1}$  in 2022
- $10 \text{ ab}^{-1}$  by mid 2023

Green box: Sure shot  
Red box: Wish list

# LHCb Upgrade II Physics Case

Taken from Eugeni Graugés

[LHCB-PUB-2018-009] arXiv:1808.08865

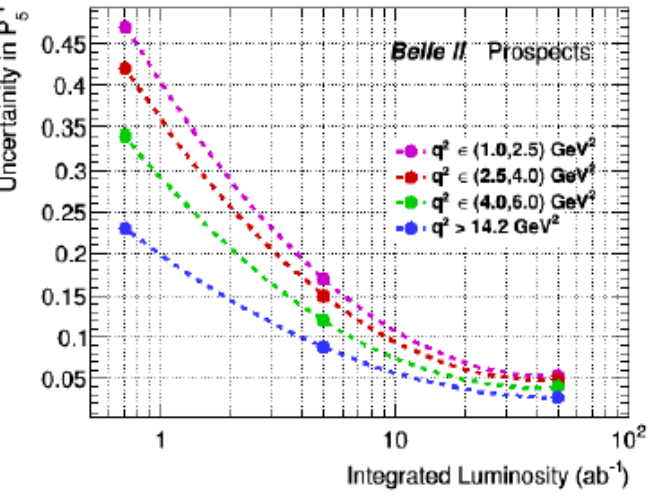
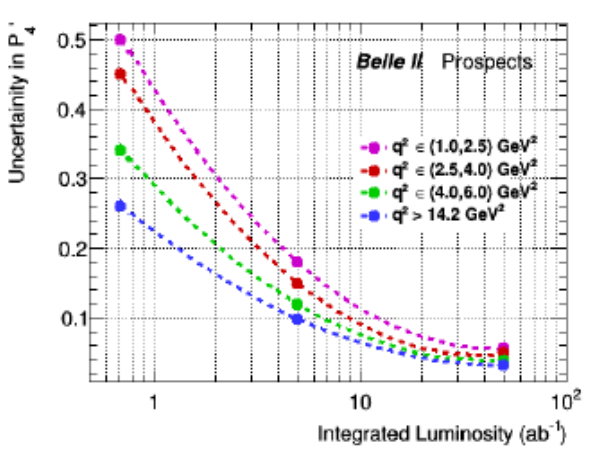
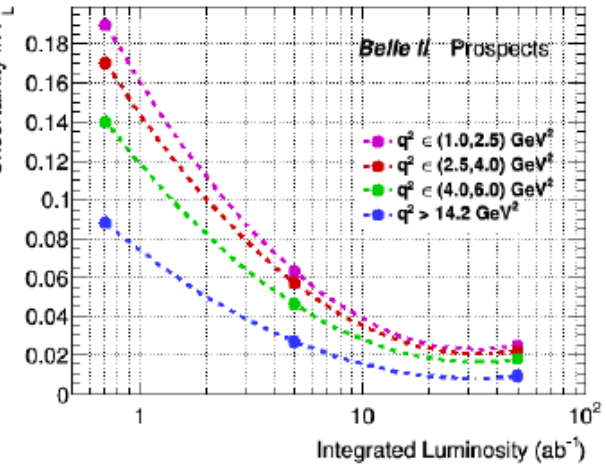
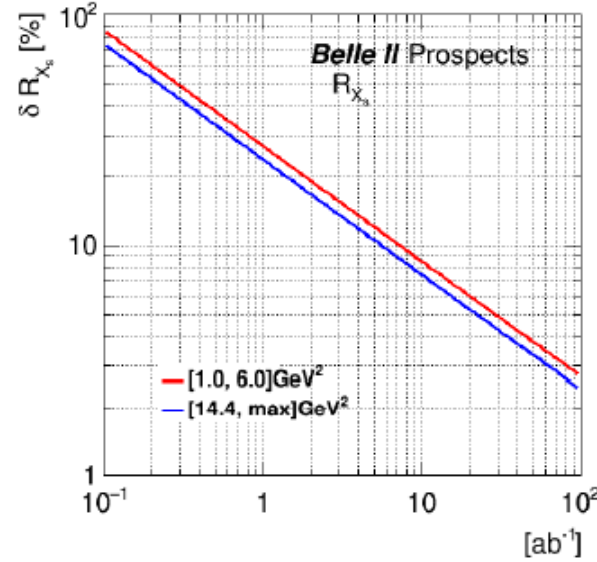
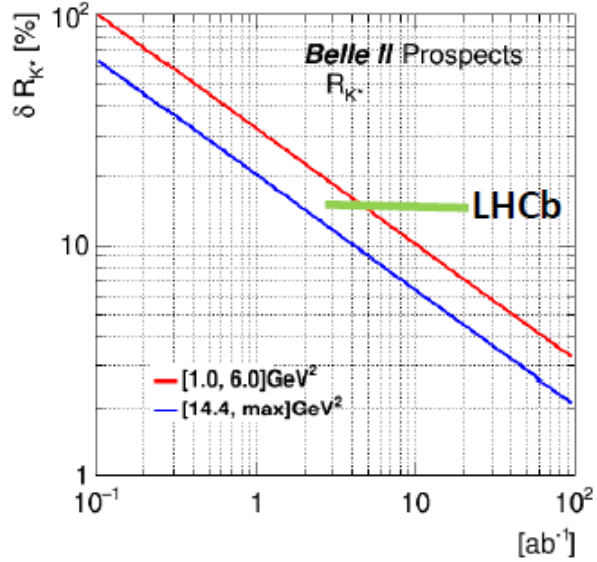
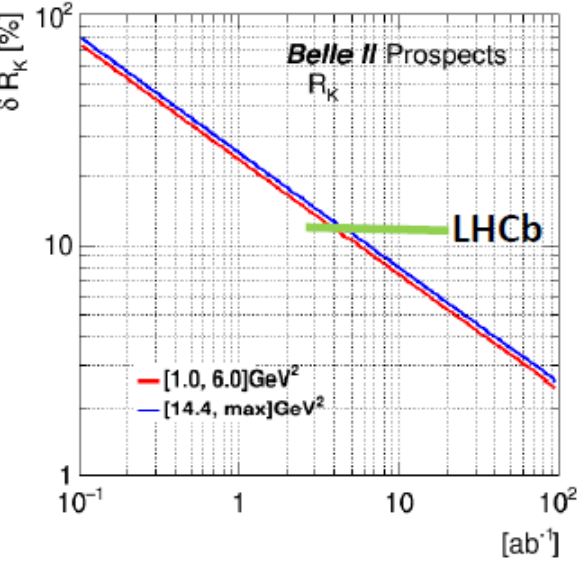
## Summary of Results.

Table 10.1: Summary of prospects for future measurements of selected flavour observables for LHCb, Belle II and Phase-II ATLAS and CMS. The projected LHCb sensitivities take no account of potential detector improvements, apart from in the trigger. The Belle-II sensitivities are taken from Ref. [608].

Observable	Current LHCb	LHCb 2025	Belle II	Upgrade II	ATLAS & CMS
<b>EW Penguins</b>					
$R_K (1 < q^2 < 6 \text{ GeV}^2 c^4)$	0.1 [274]	0.025	0.036	0.007	–
$R_{K^*} (1 < q^2 < 6 \text{ GeV}^2 c^4)$	0.1 [275]	0.031	0.032	0.008	–
$R_\phi, R_{\rho K}, R_\pi$	–	0.08, 0.06, 0.18	–	0.02, 0.02, 0.05	–
<b>CKM tests</b>					
$\gamma$ , with $B_s^0 \rightarrow D_s^+ K^-$	$(\begin{smallmatrix} +17 \\ -22 \end{smallmatrix})^\circ$ [136]	$4^\circ$	–	$1^\circ$	–
$\gamma$ , all modes	$(\begin{smallmatrix} +5.0 \\ -5.8 \end{smallmatrix})^\circ$ [167]	$1.5^\circ$	$1.5^\circ$	$0.35^\circ$	–
$\sin 2\beta$ , with $B^0 \rightarrow J/\psi K_S^0$	0.04 [609]	0.011	0.005	0.003	–
$\phi_s$ , with $B_s^0 \rightarrow J/\psi \phi$	49 mrad [44]	14 mrad	–	4 mrad	22 mrad [610]
$\phi_s$ , with $B_s^0 \rightarrow D_s^+ D_s^-$	170 mrad [49]	35 mrad	–	9 mrad	–
$\phi_s^{\bar{s}s}$ , with $B_s^0 \rightarrow \phi \phi$	154 mrad [94]	39 mrad	–	11 mrad	Under study [611]
$\alpha_{\text{nl}}^s$	$33 \times 10^{-4}$ [211]	$10 \times 10^{-4}$	–	$3 \times 10^{-4}$	–
$ V_{ub} / V_{cb} $	6% [201]	3%	1%	1%	–
<b><math>B_s^0, B^0 \rightarrow \mu^+ \mu^-</math></b>					
$\mathcal{B}(B^0 \rightarrow \mu^+ \mu^-)/\mathcal{B}(B_s^0 \rightarrow \mu^+ \mu^-)$	90% [264]	34%	–	10%	21% [612]
$\tau_{B_s^0 \rightarrow \mu^+ \mu^-}$	22% [264]	8%	–	2%	–
$S_{\mu\mu}$	–	–	–	0.2	–
<b><math>b \rightarrow c \ell^- \bar{\nu}_\ell</math> LUV studies</b>					
$R(D^*)$	0.026 [215, 217]	0.0072	0.005	0.002	–
$R(J/\psi)$	0.24 [220]	0.071	–	0.02	–
<b>Charm</b>					
$\Delta A_{CP}(KK - \pi\pi)$	$8.5 \times 10^{-4}$ [613]	$1.7 \times 10^{-4}$	$5.4 \times 10^{-4}$	$3.0 \times 10^{-5}$	–
$A_\Gamma (\approx x \sin \phi)$	$2.8 \times 10^{-4}$ [240]	$4.3 \times 10^{-5}$	$3.5 \times 10^{-4}$	$1.0 \times 10^{-5}$	–
$x \sin \phi$ from $D^0 \rightarrow K^+ \pi^-$	$13 \times 10^{-4}$ [228]	$3.2 \times 10^{-4}$	$4.6 \times 10^{-4}$	$8.0 \times 10^{-5}$	–
$x \sin \phi$ from multibody decays	–	$(K3\pi) 4.0 \times 10^{-5}$	$(K_S^0 \pi\pi) 1.2 \times 10^{-4}$	$(K3\pi) 8.0 \times 10^{-6}$	–



B2TIP report | arXiv:1808.10567



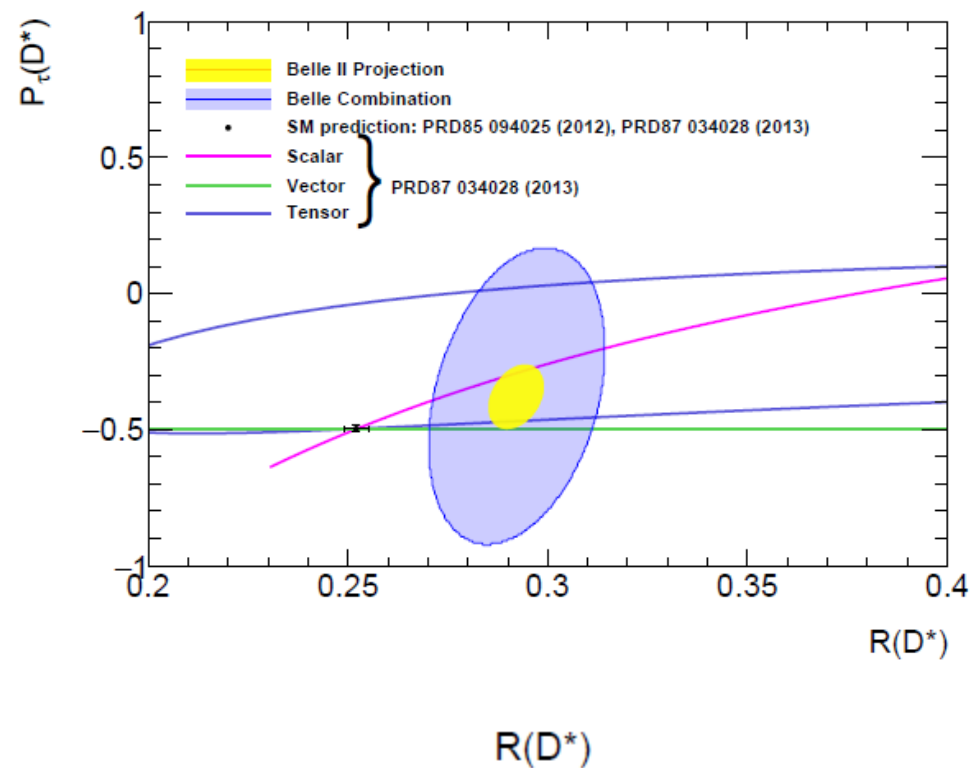
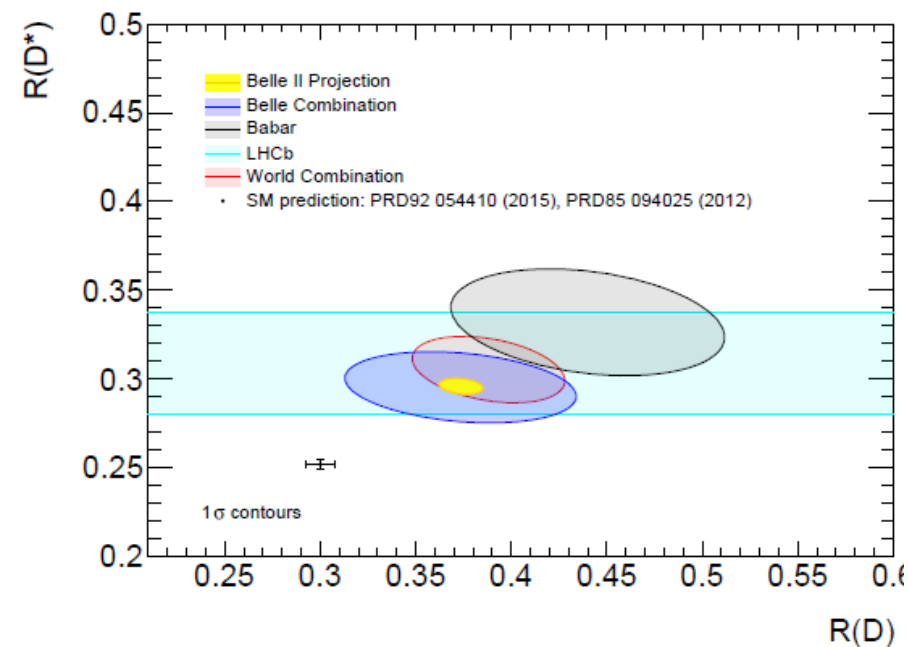


Fig. 72: Expected Belle II constraints on the  $R_D$  vs  $R_{D^*}$  plane (left) and the  $R_{D^*}$  vs  $P_\tau(D^*)$  plane (right) compared to existing experimental constraints from Belle. The SM predictions are indicated by the black points with theoretical error bars. In the right panel, the NP scenarios “Scalar”, “Vector” and “Tensor” assume contributions from the operators  $\mathcal{O}_{S_1}$ ,  $\mathcal{O}_{V_1}$  and  $\mathcal{O}_T$ , respectively.

Observables	Experimental Sensitivity	Multi-Higgs Models (§17.2)	generic SUSY	MFV (§17.3)	$Z'$ models (§17.6.1)	gauged flavour (§17.6.2)	3-3-1 (§17.6.3)	left-right (§17.6.4)	leptoquarks (§18.3.1)	compositeness (§17.7)	dark sector (§16.1)
-------------	--------------------------	----------------------------	--------------	-------------	-----------------------	--------------------------	-----------------	----------------------	-----------------------	-----------------------	---------------------

$B \rightarrow D^{(*)}\tau\bar{\nu}$ :

Branching ratio	**	**	×	×	×	×	×	*	***	*	*
$q^2$	**	***	×	×	×	×	×	**	***	*	*
$\tau$ properties	***	***	×	×	×	×	×	**	***	*	*

$B \rightarrow \pi\tau\bar{\nu}$ :

Branching ratio	**	**	×	×	×	×	×	*	***	□	*
$q^2$	**	***	×	×	×	×	×	**	***	□	*
$\tau$ properties	***	***	×	×	×	×	×	**	***	□	*

Leptonic B Decays:

$\mathcal{B}(B^+ \rightarrow \tau^+\nu)$	***	***	×	*	×	×	×	*	**	□	**
$\mathcal{B}(B^+ \rightarrow \mu^+\nu)$	***	**	×	*	×	×	×	*	***	×	***
$\mathcal{B}(B_{d,s}^0 \rightarrow \tau\tau)$	***	**	**	*	*	×	*	×	***	□	×
$\mathcal{B}(B_{d,s}^0 \rightarrow \tau^\pm\ell\bar{\nu})$	□	*	*	×	*	×	*	×	***	□	×

Observables	Experimental Sensitivity	Multi-Higgs Models (§17.2)	generic SUSY	MFV (§17.3)	$Z'$ models (§17.6.1)	gauged flavour (§17.6.2)	3-3-1 (§17.6.3)	left-right (§17.6.4)	leptoquarks (§18.3.1)	compositeness (§17.7)	dark sector (§16.1)
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Semileptonic  $b \rightarrow s$  Penguin Decays:

$B \rightarrow K^{(*)} \ell \ell$ angular	**	×	×	**	**	×	**	×	***	**	×
$R(K^*), R(K)$	**	×	×	×	**	×	**	×	***	**	×
$\mathcal{B}(B \rightarrow X_s \ell \ell)$	***	×	×	***	**	×	**	×	***	**	×
$R(X_s)$	***	×	×	×	**	×	**	×	***	**	×
$\mathcal{B}(B \rightarrow K^{(*)} \tau \tau)$	***	***	×	*	*	×	*	×	***	*	×
$\mathcal{B}(B \rightarrow X_s \tau \tau)$	□	***	×	*	*	×	*	×	***	*	×
$\mathcal{B}(B \rightarrow K^{(*)} \nu \nu)$	***	×	×	*	*	×	*	×	***	*	×
$\mathcal{B}(B \rightarrow X_s \nu \nu)$	□	×	×	*	*	×	*	×	***	*	×

Semileptonic  $b \rightarrow d$  Penguin Decays:

$B \rightarrow \pi \ell \ell$ angular	**	×	×	**	**	×	**	×	***	*	×
$R(\rho), R(\pi)$	**	×	×	×	**	×	**	×	***	*	×
$\mathcal{B}(B \rightarrow X_d \ell \ell)$	***	×	×	***	**	×	**	×	***	*	×
$R(X_d)$	***	×	×	×	**	×	**	×	***	*	×
$\mathcal{B}(B \rightarrow \pi \tau \tau)$	□	***	×	*	*	×	*	*	***	*	×
$\mathcal{B}(B \rightarrow \pi \nu \nu)$	***	×	×	*	*	×	*	×	***	*	×

TABLE II. The systematic uncertainties in  $R(D^*)$  and  $P_\tau(D^*)$ , where the values for  $R(D^*)$  are relative errors. The group “common sources” identifies the common systematic uncertainty sources in the signal and the normalization modes, which cancel to a good extent in the ratio of these samples. The reason for the incomplete cancellation is described in the text.

Source	$R(D^*)$	$P_\tau(D^*)$
Hadronic $B$ composition	+7.7%	+0.134
	-6.9%	-0.103
MC statistics for PDF shape	+4.0%	+0.146
	-2.8%	-0.108
Fake $D^*$	3.4%	0.018
$\bar{B} \rightarrow D^{**} \ell^- \bar{\nu}_\ell$	2.4%	0.048
$\bar{B} \rightarrow D^{**} \tau^- \bar{\nu}_\tau$	1.1%	0.001
$\bar{B} \rightarrow D^* \ell^- \bar{\nu}_\ell$	2.3%	0.007
$\tau$ daughter and $\ell^-$ efficiency	1.9%	0.019
MC statistics for efficiency estimation	1.0%	0.019
$\mathcal{B}(\tau^- \rightarrow \pi^- \nu_\tau, \rho^- \nu_\tau)$	0.3%	0.002
$P_\tau(D^*)$ correction function	0.0%	0.010
Common sources		
Tagging efficiency correction	1.6%	0.018
$D^*$ reconstruction	1.4%	0.006
Branching fractions of the $D$ meson	0.8%	0.007
Number of $B\bar{B}$ and $\mathcal{B}(\Upsilon(4S) \rightarrow B^+ B^- \text{ or } B^0 \bar{B}^0)$	0.5%	0.006
Total systematic uncertainty	+10.4%	+0.21
	-9.4%	-0.16

# $R(D^*)$ systematics

LHCb three prong 2017

LHCb one prong 2015

TABLE I. Systematic uncertainties in the extraction of  $\mathcal{R}(D^*)$ .

Model uncertainties	Absolute size ( $\times 10^{-2}$ )
Simulated sample size	2.0
Misidentified $\mu$ template shape	1.6
$\bar{B}^0 \rightarrow D^{*+}(\tau^-/\mu^-)\bar{\nu}$ form factors	0.6
$\bar{B} \rightarrow D^{*+}H_c(\rightarrow \mu\nu X')X$ shape corrections	0.5
$\mathcal{B}(\bar{B} \rightarrow D^{**}\tau^-\bar{\nu}_\tau)/\mathcal{B}(\bar{B} \rightarrow D^{**}\mu^-\bar{\nu}_\mu)$	0.5
$\bar{B} \rightarrow D^{**}(\rightarrow D^*\pi\pi)\mu\nu$ shape corrections	0.4
Corrections to simulation	0.4
Combinatorial background shape	0.3
$\bar{B} \rightarrow D^{**}(\rightarrow D^{*+}\pi)\mu^-\bar{\nu}_\mu$ form factors	0.3
$\bar{B} \rightarrow D^{*+}(D_s \rightarrow \tau\nu)X$ fraction	0.1
<b>Total model uncertainty</b>	<b>2.8</b>
Normalization uncertainties	Absolute size ( $\times 10^{-2}$ )
Simulated sample size	0.6
Hardware trigger efficiency	0.6
Particle identification efficiencies	0.3
Form factors	0.2
$\mathcal{B}(\tau^- \rightarrow \mu^-\bar{\nu}_\mu\nu_\tau)$	< 0.1
<b>Total normalization uncertainty</b>	<b>0.9</b>
<b>Total systematic uncertainty</b>	<b>3.0</b>

TABLE VII. List of the individual systematic uncertainties for the measurement of the ratio  $\mathcal{B}(B^0 \rightarrow D^{*-}\tau^+\nu_\tau)/\mathcal{B}(B^0 \rightarrow D^{*-}3\pi)$ .

Contribution	Value in %
$\mathcal{B}(\tau^+ \rightarrow 3\pi\bar{\nu}_\tau)/\mathcal{B}(\tau^+ \rightarrow 3\pi(\pi^0)\bar{\nu}_\tau)$	0.7
Form factors (template shapes)	0.7
Form factors (efficiency)	1.0
$\tau$ polarization effects	0.4
Other $\tau$ decays	1.0
$B \rightarrow D^{**}\tau^+\nu_\tau$	2.3
$B_s^0 \rightarrow D_s^{**}\tau^+\nu_\tau$ feed-down	1.5
$D_s^+ \rightarrow 3\pi X$ decay model	2.5
$D_s^+, D^0$ and $D^+$ template shape	2.9
$B \rightarrow D^{*-}D_s^+(X)$ and $B \rightarrow D^{*-}D^0(X)$ decay model	2.6
$D^{*-}3\pi X$ from $B$ decays	2.8
Combinatorial background (shape + normalization)	0.7
Bias due to empty bins in templates	1.3
Size of simulation samples	4.1
Trigger acceptance	1.2
Trigger efficiency	1.0
Online selection	2.0
Offline selection	2.0
Charged-isolation algorithm	1.0
Particle identification	1.3
Normalization channel	1.0
Signal efficiencies (size of simulation samples)	1.7
Normalization channel efficiency (size of simulation samples)	1.6
Normalization channel efficiency (modeling of $B^0 \rightarrow D^{*-}3\pi$ )	2.0
<b>Total uncertainty</b>	<b>9.1</b>

## Belle 2019 semileptonic

TABLE I. Systematic uncertainties contributing to the  $\mathcal{R}(D^{(*)})$  results, together with their correlation.

Source	$\Delta\mathcal{R}(D)$ (%)	$\Delta\mathcal{R}(D^*)$ (%)	Correlation
$D^{**}$ composition	0.76	1.41	-0.41
PDF shapes	4.39	2.25	-0.55
Feed-down factors	1.69	0.44	0.53
Efficiency factors	1.93	4.12	-0.57
Fake $D^{(*)}$ calibration	0.19	0.11	-0.76
$B_{\text{tag}}$ calibration	0.07	0.05	-0.76
Lepton efficiency and fake rate	0.36	0.33	-0.83
Slow pion efficiency	0.08	0.08	-0.98
$B$ decay form factors	0.55	0.28	-0.60
Luminosity, $f^{+-}$ , $f^{00}$ and $\mathcal{B}(\Upsilon(4S))$	0.10	0.04	-0.58
$\mathcal{B}(B \rightarrow D^{(*)} \ell \nu)$	0.05	0.02	-0.69
$\mathcal{B}(D)$	0.35	0.13	-0.65
$\mathcal{B}(D^*)$	0.04	0.02	-0.51
$\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$	0.15	0.14	-0.11
Total	5.21	4.94	-0.52

## Belle 2016 semileptonic

TABLE I. Summary of the systematic uncertainties on  $\mathcal{R}(D^*)$  for electron and muon modes combined and separated. The uncertainties are relative and are given in percent.

Sources	$\mathcal{R}(D^*)$ (%)		
	$\ell^{\text{sig}} = e, \mu$	$\ell^{\text{sig}} = e$	$\ell^{\text{sig}} = \mu$
MC size for each PDF shape	2.2	2.5	3.9
PDF shape of the normalization in $\cos\theta_{B-D^* \ell}$	+1.1 -0.0	+2.1 -0.0	+2.8 -0.0
PDF shape of $B \rightarrow D^{**} \ell \nu_\ell$	+1.0 -1.7	+0.7 -1.3	+2.2 -3.3
PDF shape and yields of fake $D^{(*)}$	1.4	1.6	1.6
PDF shape and yields of $B \rightarrow X_c D^*$	1.1	1.2	1.1
Reconstruction efficiency ratio $\epsilon_{\text{norm}}/\epsilon_{\text{sig}}$	1.2	1.5	1.9
Modeling of semileptonic decay $\mathcal{B}(\tau^- \rightarrow \ell^- \bar{\nu}_\ell \nu_\tau)$	0.2	0.2	0.3
Total systematic uncertainty	+3.4 -3.5	+4.1 -3.7	+5.9 -5.8