





The dipole picture and the non-relativistic expansion

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tribution of the relativistic degrees of freedom to oction renormalization of the non-relativistic outed in [4].	 Exclusive quarkonium production in the G Our final goal is to compute this process in the For this we need the NLO photon wave function talks by Beuf in HP2018. At the moment, we check that all divergences polarization case. We get consistent results compatible with B
	Tree level
tributions that can be encoded as a redefinition tial between non-relativistic quarks.	
t will not appear explicitly in our equations. nodifies the value of the non-relativistic n at the origin.	One loop corrections to photon wave fund
	$\left. \Psi_{\gamma}({\it z},{\it r}_{\perp}) ight _{\it NL}$
	Recently computed in [6]. In our case we need the
computed in perturbation theory. \rightarrow	One loop corrections to quarkonium wave
to $\alpha_s(m)$. The interaction from the point of view of tivistic quarks. \rightarrow Proportional to the leading n-relativistic wave function at the origin.	
	Dependence on μ
	Comes only from the wave function renormalization
onal to $g(m)$. leck. One can recover the wave-function lization by computing the square of this tion.	Dependence on x_0 Can be divided into two pieces: • One which cancels the x_0 dependence of the • One whose derivative is proportional to $\frac{d\delta Z_{\gamma}}{dt}$
	Contribution of the $q\bar{q}g$ Fock state
$(\nabla)^{k} \int \frac{d\lambda}{dk} \phi^{m}(\lambda, 0) $ (3)	Dependence on <i>u</i>
$(m) \int 4\pi^{\prime}$ (b) $\lambda = \frac{1}{2}$	Note that in the ultraviolet $\sigma_{q\bar{q}g} \rightarrow \sigma_{q\bar{q}}$. It has a quarkonium.
of the Fock space. For example, $C_{q\bar{q}\leftarrow q\bar{q}}^{k}(z, \mathbf{x}_{\perp})$ he same component of the non-relativistic wave	Dependence on x_0 Can be divided in two terms: • One proportional to $(\sigma_{q\bar{q}g} - \sigma_{q\bar{q}})$ which can • One proportional to $\sigma_{q\bar{q}}$ which cancels the divided of $\sigma_{q\bar{q}}$ which cancels t
$\sim \alpha_{s}(mv).$	for the piece related with the Coulomb singul
(<i>m</i>) and $\alpha_s(mv)$.	 Conclusions We have computed the NLO corrections to the We have checked that the light-cone distribut We recovered known results for the decay of a light-cone gauge.
tion It has also have served at the	vve nave checked that when the wave function will cancel.
Therefore, we know	 Once the photon wave function with massive
$\int d\lambda \phi(\lambda 0) \tag{4}$	Bibliography
$\int d \mathcal{A} \varphi(\mathcal{A}, \mathbf{C}) $	[1] M. G. Ryskin, <i>Diffractive J/psi electroprodue</i>
$)) \int d d d d () 0 $ (5)	[2] S. J. Brodsky, L. Frankfurt, J. F. Gunion, A. mesons in QCD, Phys. Rev. D50 (1994) 313
$\int \int dx \psi(x, \mathbf{v}) \tag{3}$	[3] G. T. Bodwin, D. Kang and J. Lee, <i>Reconcilie</i> $e^+e^- \rightarrow J/\psi + \eta_c$, <i>Phys. Rev.</i> D74 (2006)
M) but they can appear in our case. $ _{z} = \frac{1}{z} _{z} \sim \frac{x_{0}}{z} \ll 1$ Coulomb singularity	[4] D. Mustaki, S. Pinsky, J. Shigemitsu and K.D43 (1991) 3411.
$\begin{vmatrix} 2 \\ -2 \end{vmatrix} = 2 $ 1. Coulding singularity.	[5] R. Barbieri, R. Gatto, R. Kogerler and Z. Ku (1975) 455.
$+ \frac{1}{dx_0} \int d\lambda \phi(\lambda, \mathbf{U}) = 0 $ (6)	[6] G. Beuf, <i>Dipole factorization for DIS at NLC</i>
t is indeed the case.	0/4033 [arXiv:1708.06557 [hep-ph]].

$Q \gg m$ limit at NLO he general case $Q \sim m$.
ion with massive quarks. This is being investigated at the moment, see
s cancel in the $Q \gg m$ limit. We focus on the simpler, longitudinal
JIMWLK evolution.
Dependence on x_0 hidden in two terms. $\sigma_{q\bar{q}}$, which fulfils B-JIMWLK evolution, and the non-relativistic wave function, which depends on x_0 (see eq. (6)).
ction
$\int_{O} = \Psi_{\gamma}(z, r_{\perp}) \big _{LO} \left(1 + \delta Z_{\gamma}(z, r_{\perp}) \right)$
e value at $2 - \frac{1}{2}$.
on and fulfils that $\frac{d\delta Z}{d\mu} = \frac{d\delta Z_{\gamma}\left(\frac{1}{2}, r_{\perp}\right)}{d\mu}$
non-relativistic wave function (eq.(6)). $\left(\frac{\frac{1}{2}, r_{\perp}}{x_{0}}\right)$.
divergence that cancels that of the wave functions of the photon and
cels the B-JIMWLK evolution of the target. vergences of the wave functions of the photon and quarkonium, except arity
ne quarkonium wave function in the non-relativistic limit. tion amplitude obtained in this framework fulfils ERBL equation. quarkonium into leptons. To our knowledge, first computation in
on is applied to compute exclusive quarkonium production all divergences
quarks is known we are ready for phenomenological applications.
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