

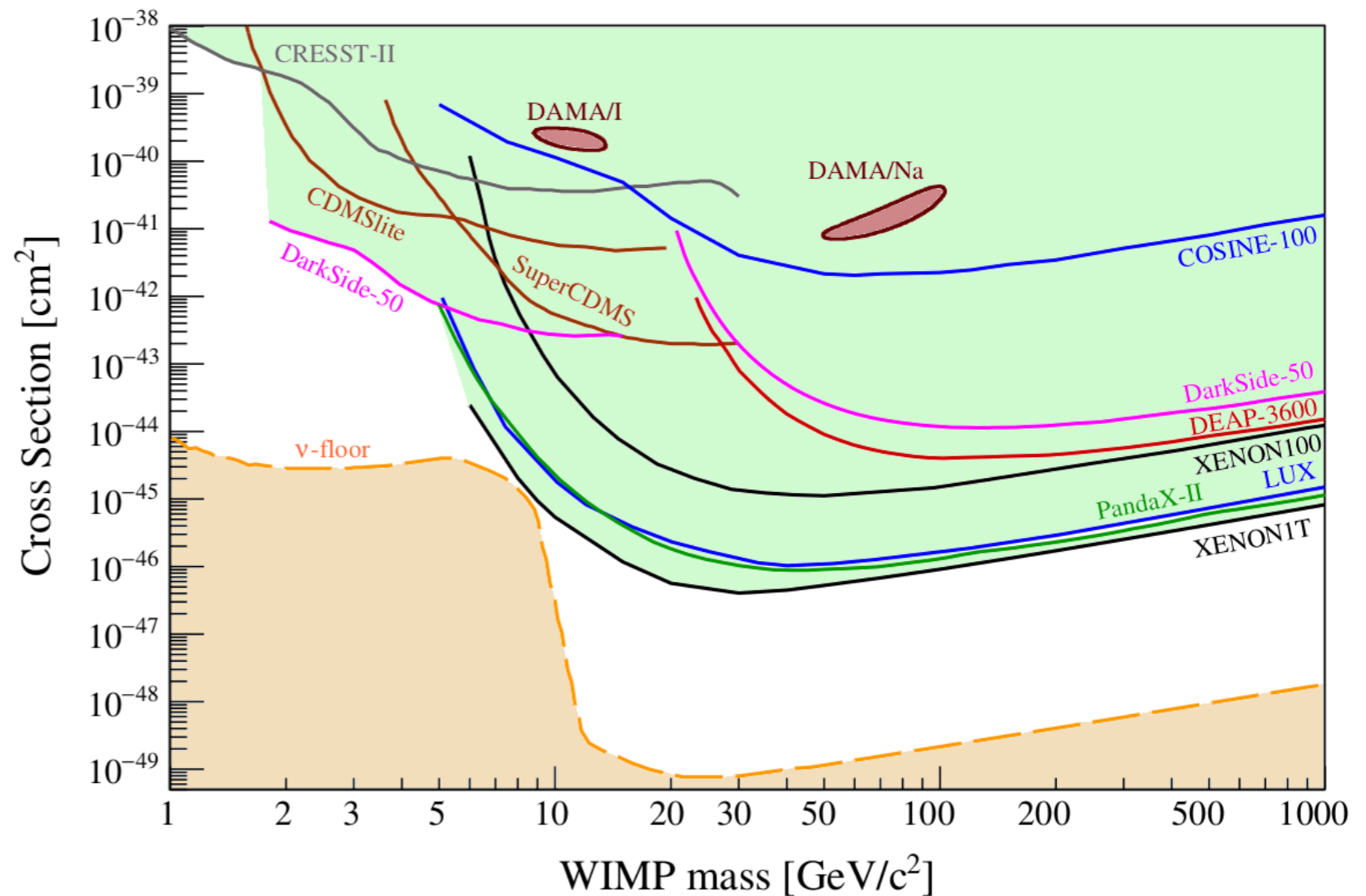
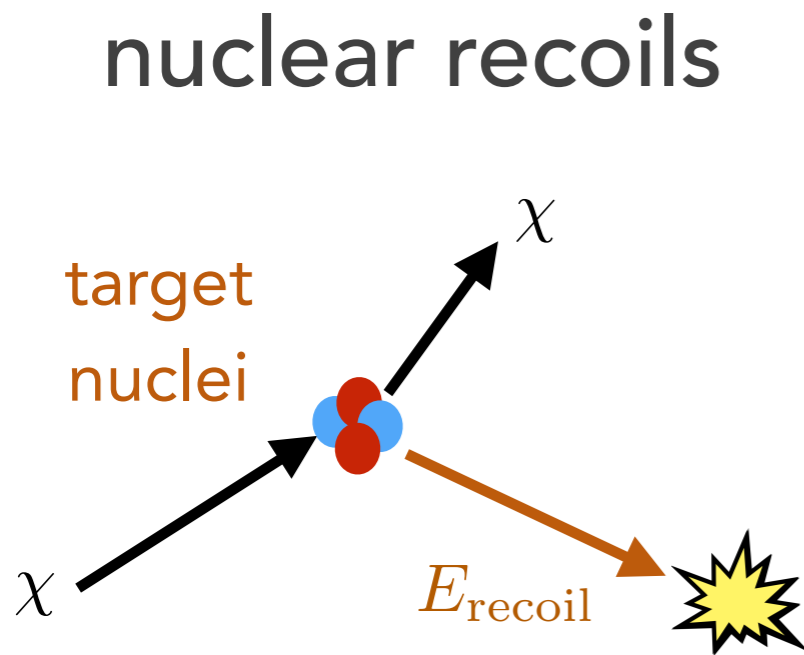
II. Models and mediators for dark sectors

Tongyan Lin (UCSD)

Summer Institute 2019, Korea

Dark sectors

Today: consider minimal sub-GeV dark sectors and implications mainly for **direct detection**.



Outline

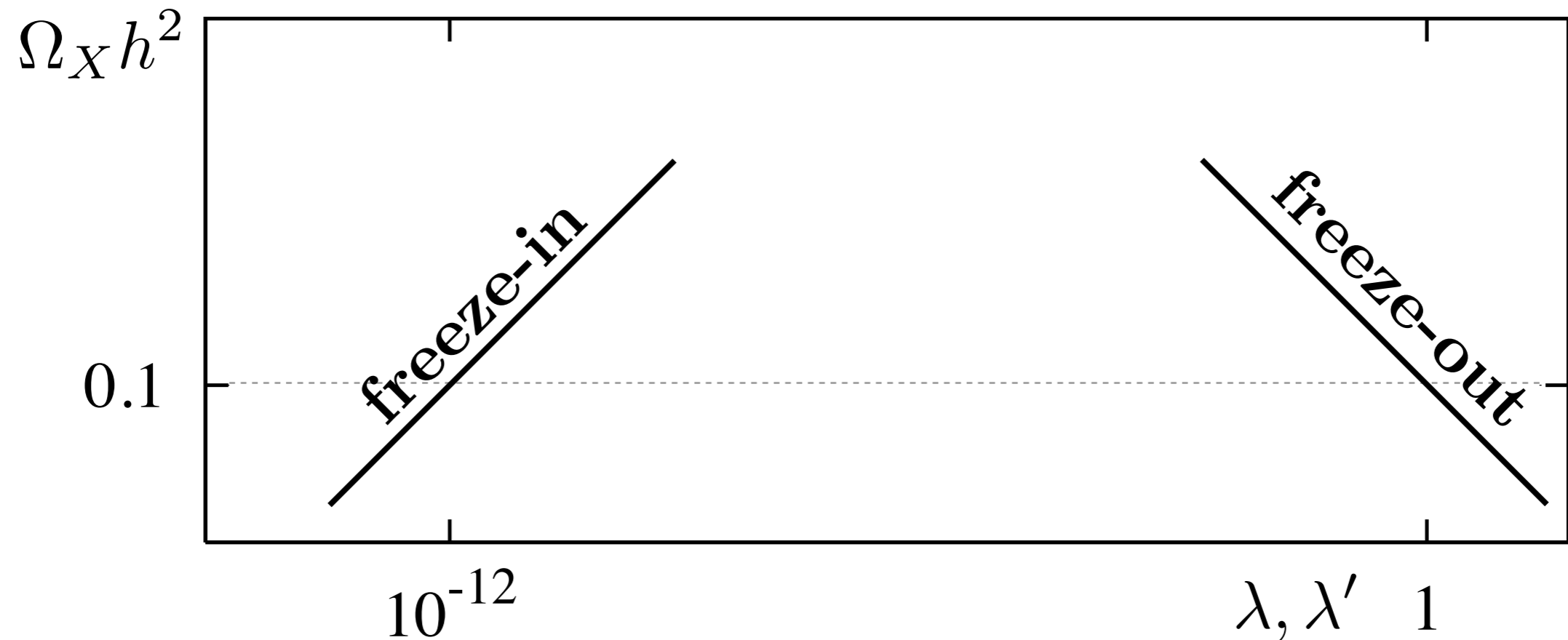
Scalar mediators & implications for
direct detection

Dark-photon mediated models

Cosmology of sub-MeV freeze-in DM

Based on Knapen, TL, Zurek 2017;
Dvorkin, TL, Schutz 2019; TL 2019;
additional refs throughout

Freeze-in and freeze-out

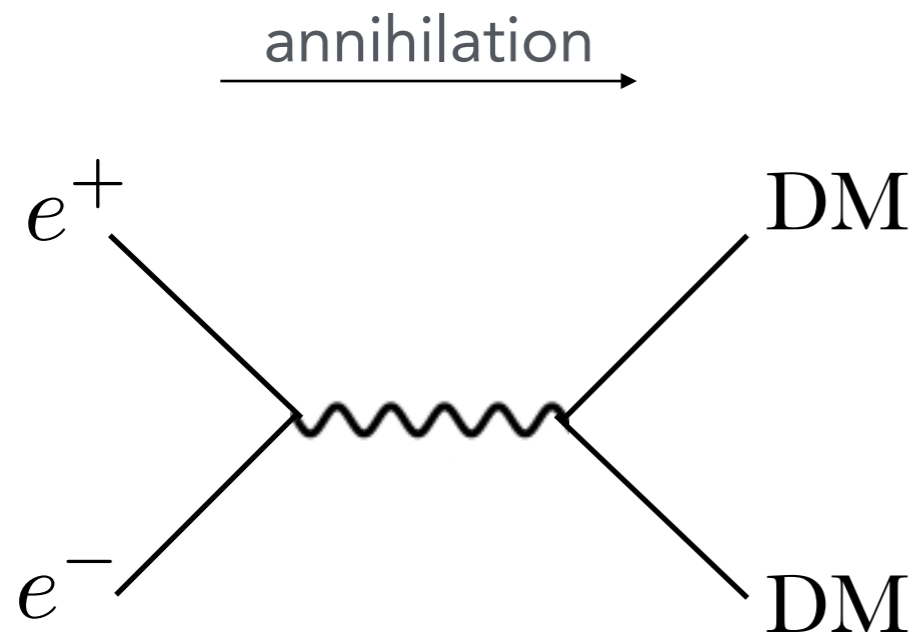


From Hall, Jedamzik, March-Russell, West 2009

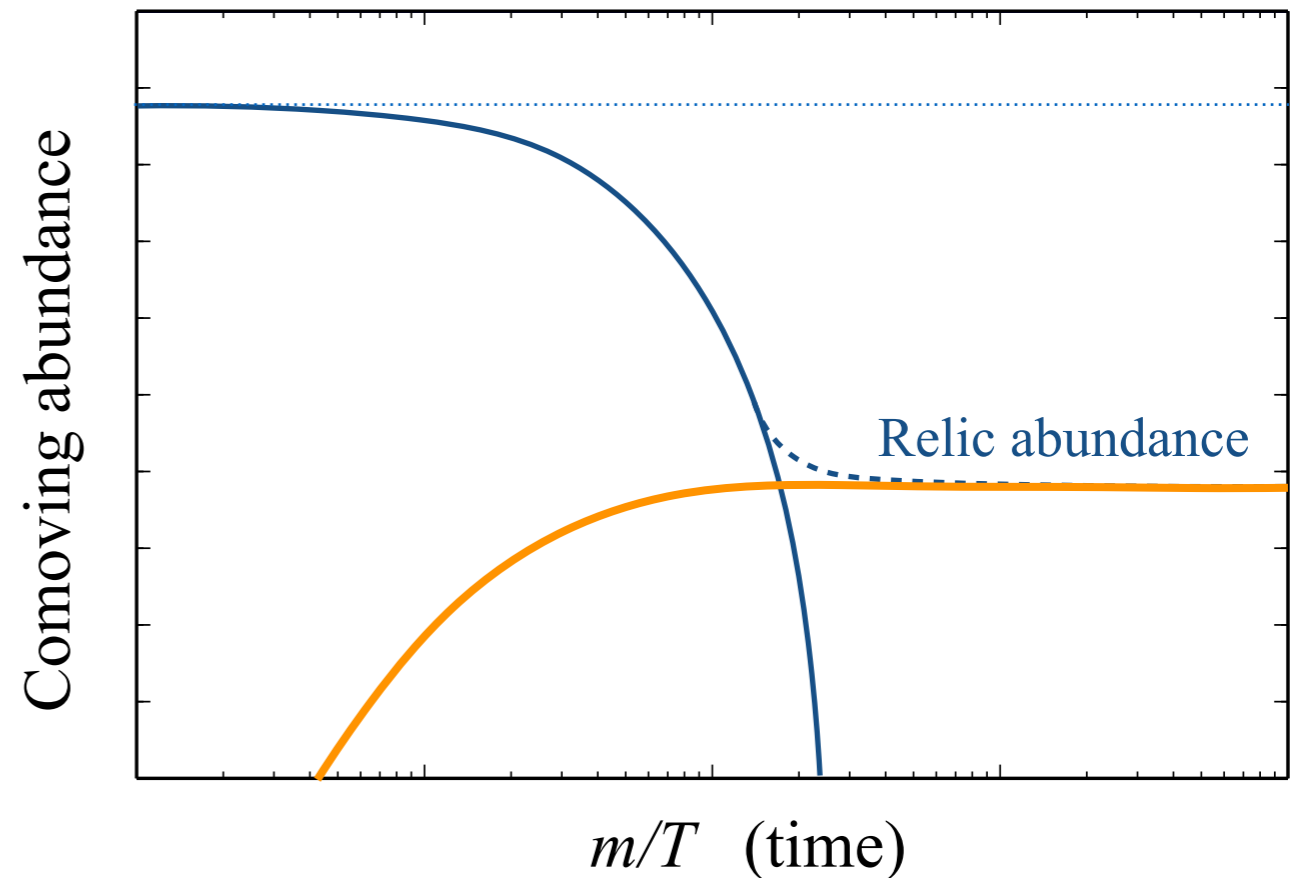
In general, couplings depend on mediator and DM masses, but this gives a rough idea of effective coupling range needed.

Freeze-in

Not just thermal freeze-out for light DM!



See also: sterile neutrino



Dark matter *only* populated by out-of-equilibrium annihilations of SM into dark sector

Freeze-in

UV freeze-in: $Y_{\text{DM}} \sim \frac{\Gamma}{H} \simeq \frac{\alpha_f \alpha_X T^3 M_{\text{pl}}}{\Lambda^4}$

Dominated by highest temperatures, reheating

Freeze-in

UV freeze-in: $Y_{\text{DM}} \sim \frac{\Gamma}{H} \simeq \frac{\alpha_f \alpha_X T^3 M_{\text{pl}}}{\Lambda^4}$

Dominated by highest temperatures, reheating

IR freeze-in: $Y_{\text{DM}} \sim \frac{\Gamma}{H} \simeq \frac{\alpha_f \alpha_X M_{\text{pl}}}{T}$

Dominated by lowest temperatures (m_f or m_{DM})

Freeze-in

UV freeze-in: $Y_{\text{DM}} \sim \frac{\Gamma}{H} \simeq \frac{\alpha_f \alpha_X T^3 M_{\text{pl}}}{\Lambda^4}$

Dominated by highest temperatures, reheating

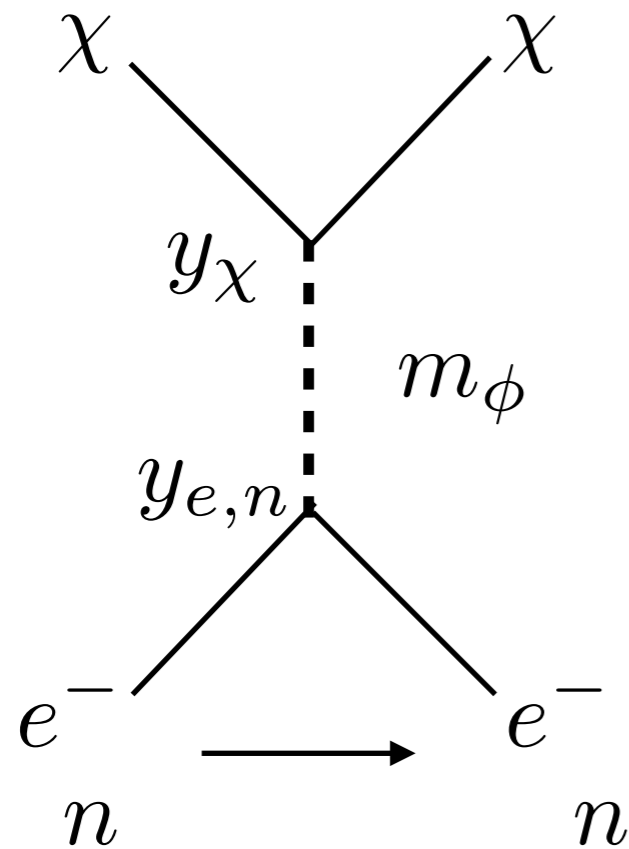
IR freeze-in: $Y_{\text{DM}} \sim \frac{\Gamma}{H} \simeq \frac{\alpha_f \alpha_X M_{\text{pl}}}{T}$

Dominated by lowest temperatures (m_f or m_{DM})

For correct relic abundance: $g_X g_f \sim 10^{-12} \times \min(1, \sqrt{m_f / m_{\text{DM}}})$

Freeze-in through a light mediator reproduces some appealing features of thermal freeze-out. Many freeze-in variations.

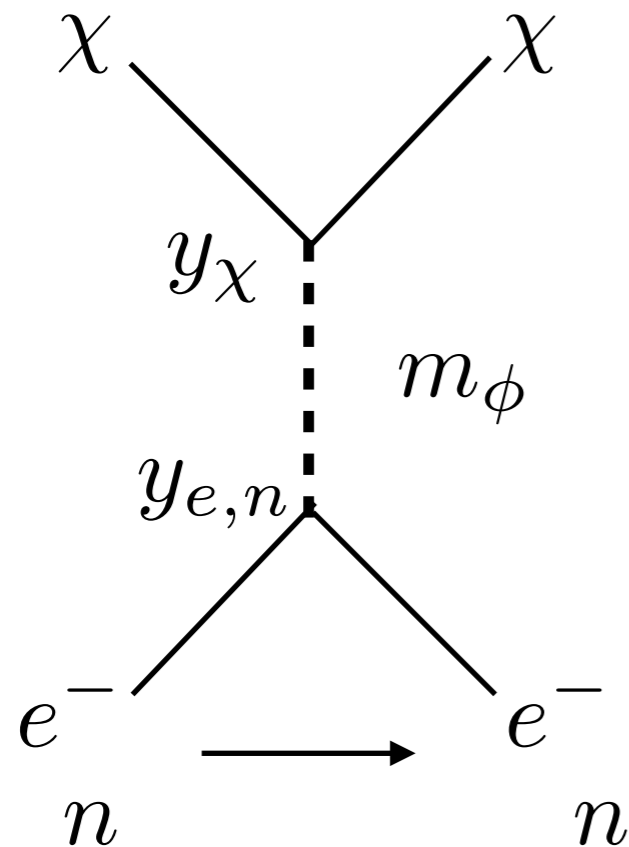
Simplified portal setup



For the moment, consider all scalars

$$\mathcal{L} \supset -\frac{1}{2}m_\chi^2\chi^2 - \frac{1}{2}m_\phi^2\phi^2 - \frac{1}{2}y_\chi m_\chi \phi \chi^2$$

Simplified portal setup



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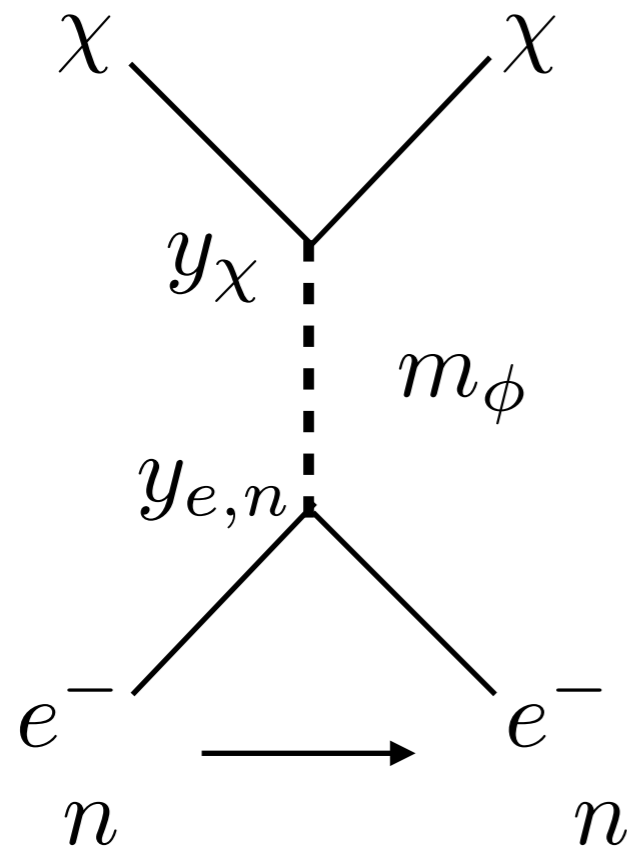
$$\mathcal{L} \supset -\frac{1}{2}m_\chi^2\chi^2 - \frac{1}{2}m_\phi^2\phi^2 - \frac{1}{2}y_\chi m_\chi\phi\chi^2$$

Scattering in direct detection:

$$\bar{\sigma}_e \equiv \frac{y_\chi^2 y_e^2}{4\pi} \frac{\mu_{\chi e}^2}{(m_\phi^2 + \alpha^2 m_e^2)^2} \quad q_{\text{typical}} \simeq \alpha m_e$$

$$\sigma_n \equiv \frac{y_n^2 y_\chi^2}{4\pi} \frac{\mu_{\chi n}^2}{(m_\phi^2 + v_{DM}^2 m_\chi^2)^2} \quad q_{\text{typical}} \simeq m_\chi v_{DM}$$

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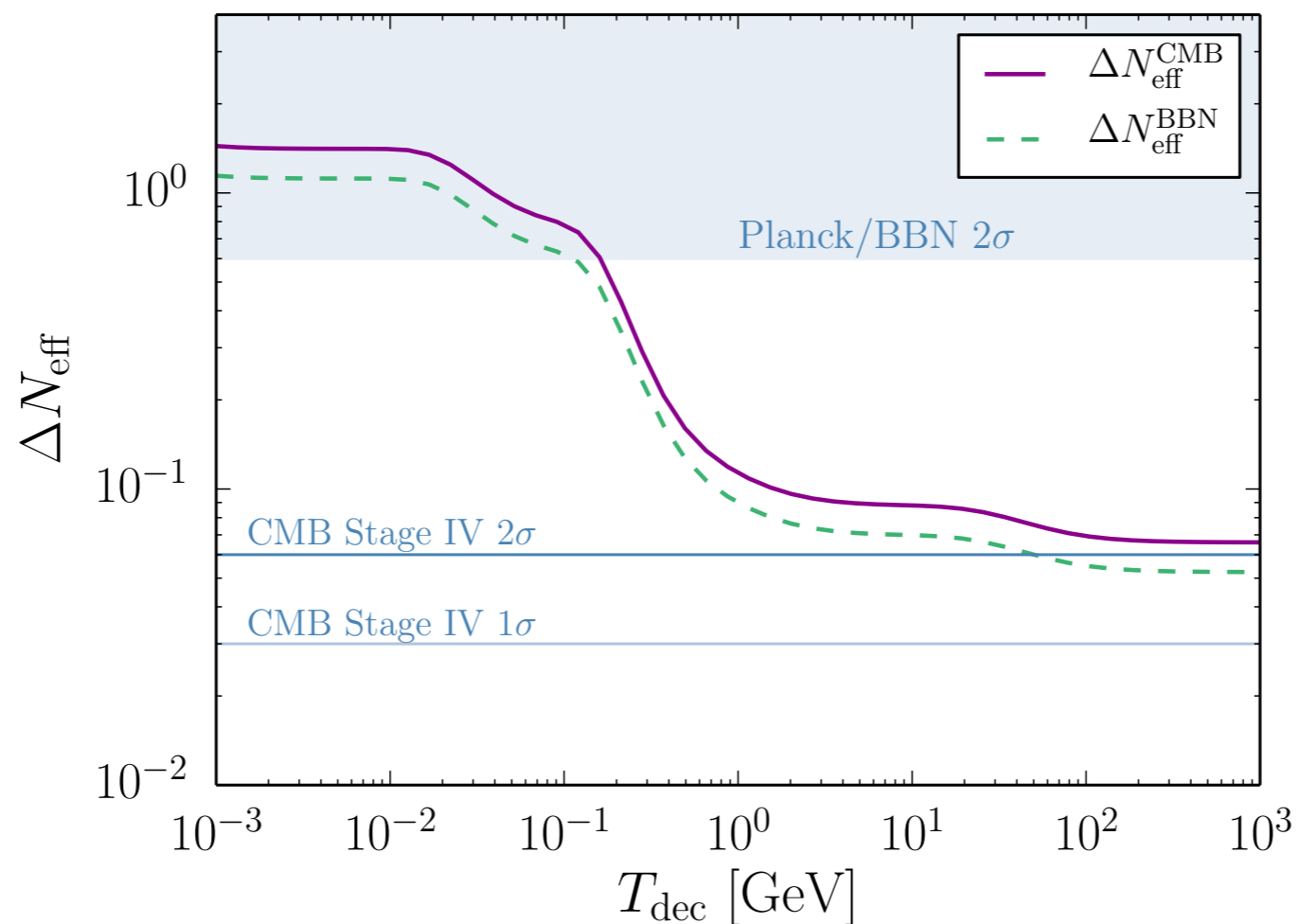
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Depending on the mass scales, DM annihilation to SM or mediator not allowed. Introduce dark radiation states for relic abundance:

$$\mathcal{L} \supset -\frac{1}{2}m_a a^2 - \frac{1}{2}y_a m_a \phi a^2 - \frac{1}{4}\lambda\chi^2 a^2$$

Sub-GeV model considerations

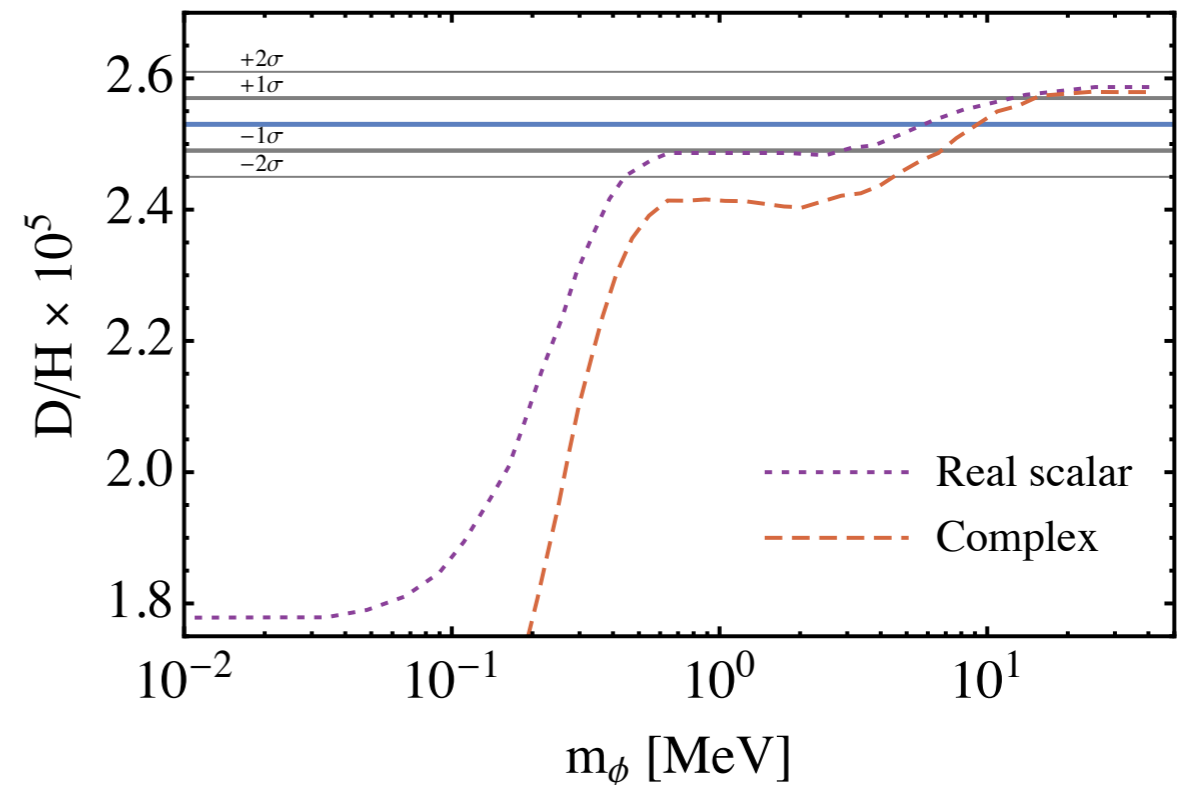
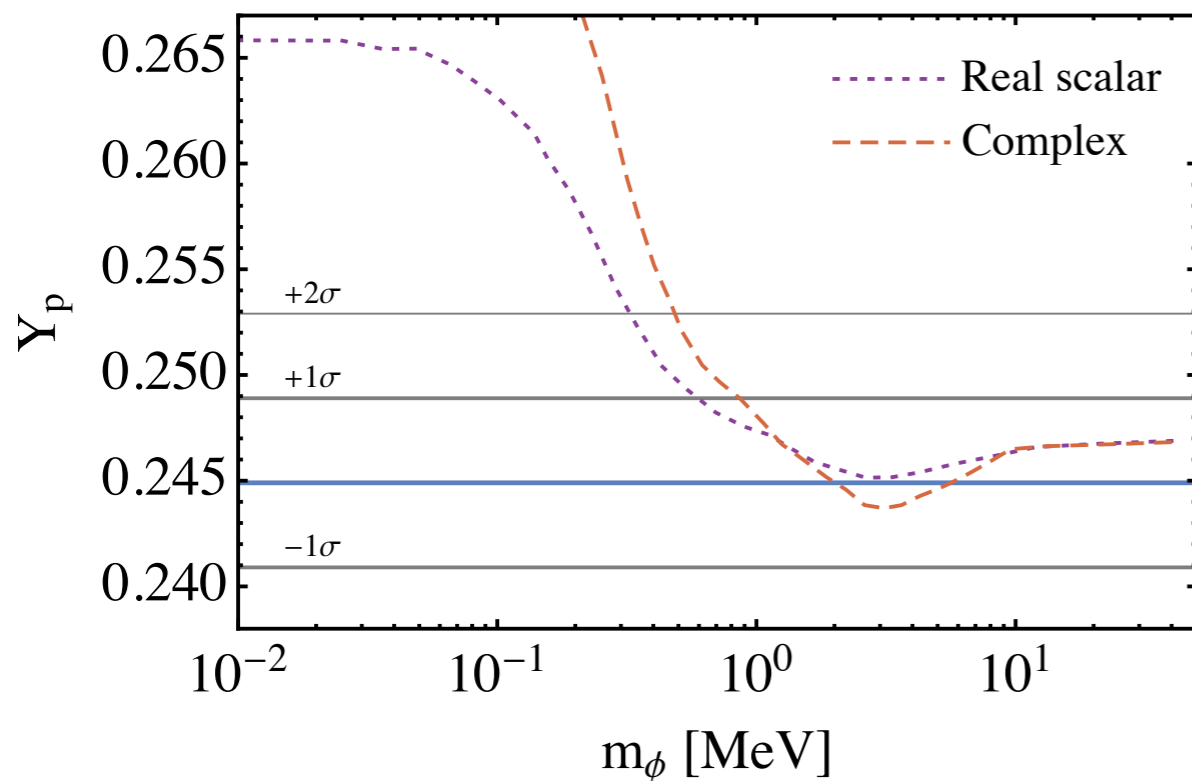
- Direct constraints on mediators (stellar production, lab bounds)
- Constraints on secluded mediator & DM sector from CMB, BBN (consider real fields to minimize effect)



BBN-epoch effect
is to increase
helium fraction (Y_p)
and deuterium (D/H)

Sub-GeV model considerations

- If DM or mediator is in equilibrium with the SM photons/electrons, this can effectively change the baryon-to-photon ratio and modify BBN abundances



For detailed discussion:

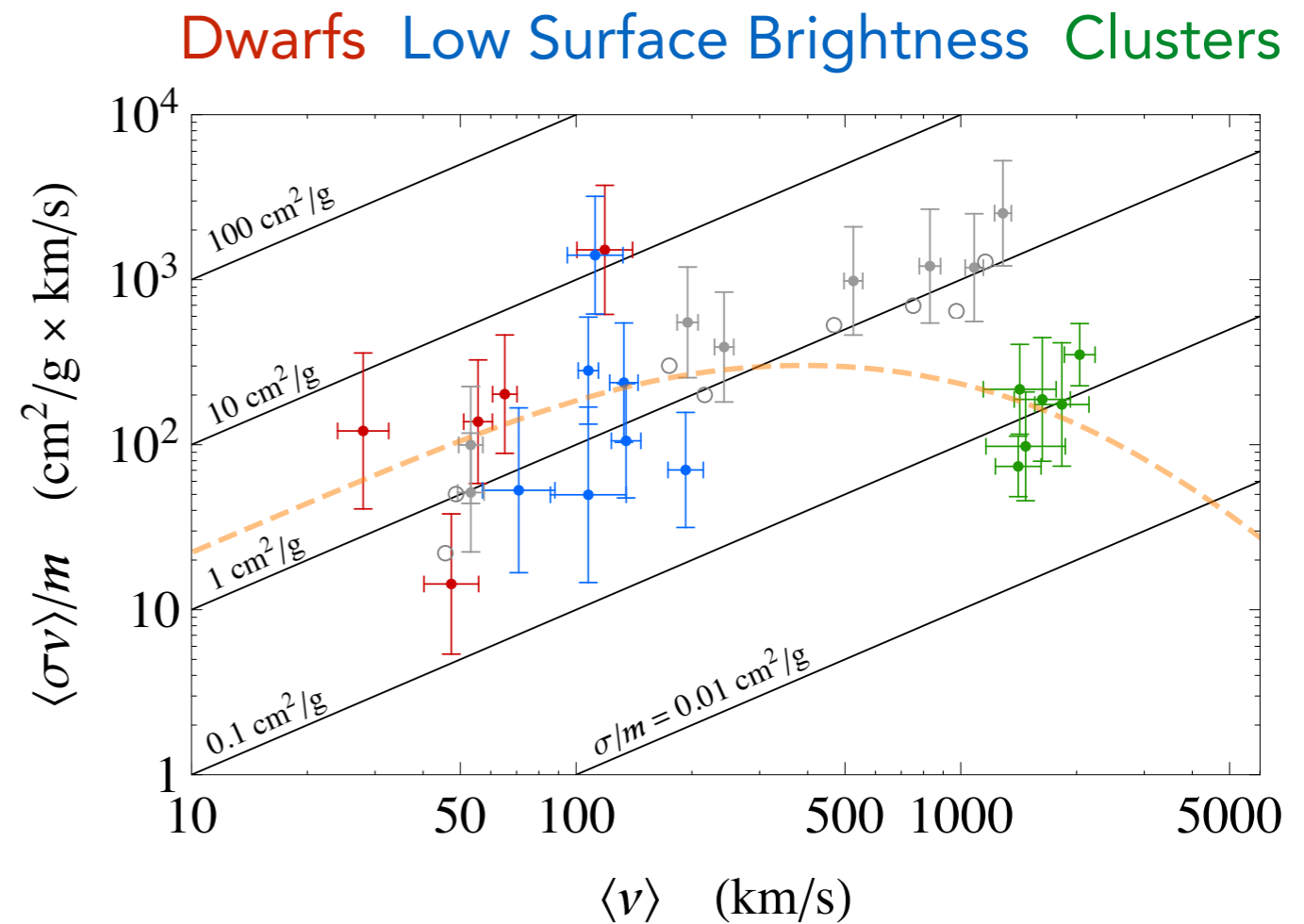
Nollett & Steigman 2014; Boehm et al. 1303.6270

See also Berlin, Blinov, Li 1904.04256

Sub-GeV model considerations

Low-mass dark sectors also affect late-time gravitational clustering on small scales.

$$\Gamma \approx \frac{\rho_{\text{DM}}}{m_\chi} \sigma v \approx \frac{1}{10^9 \text{ year}}$$



From Kaplinghat, Tulin, Yu 2015

Sub-GeV model considerations

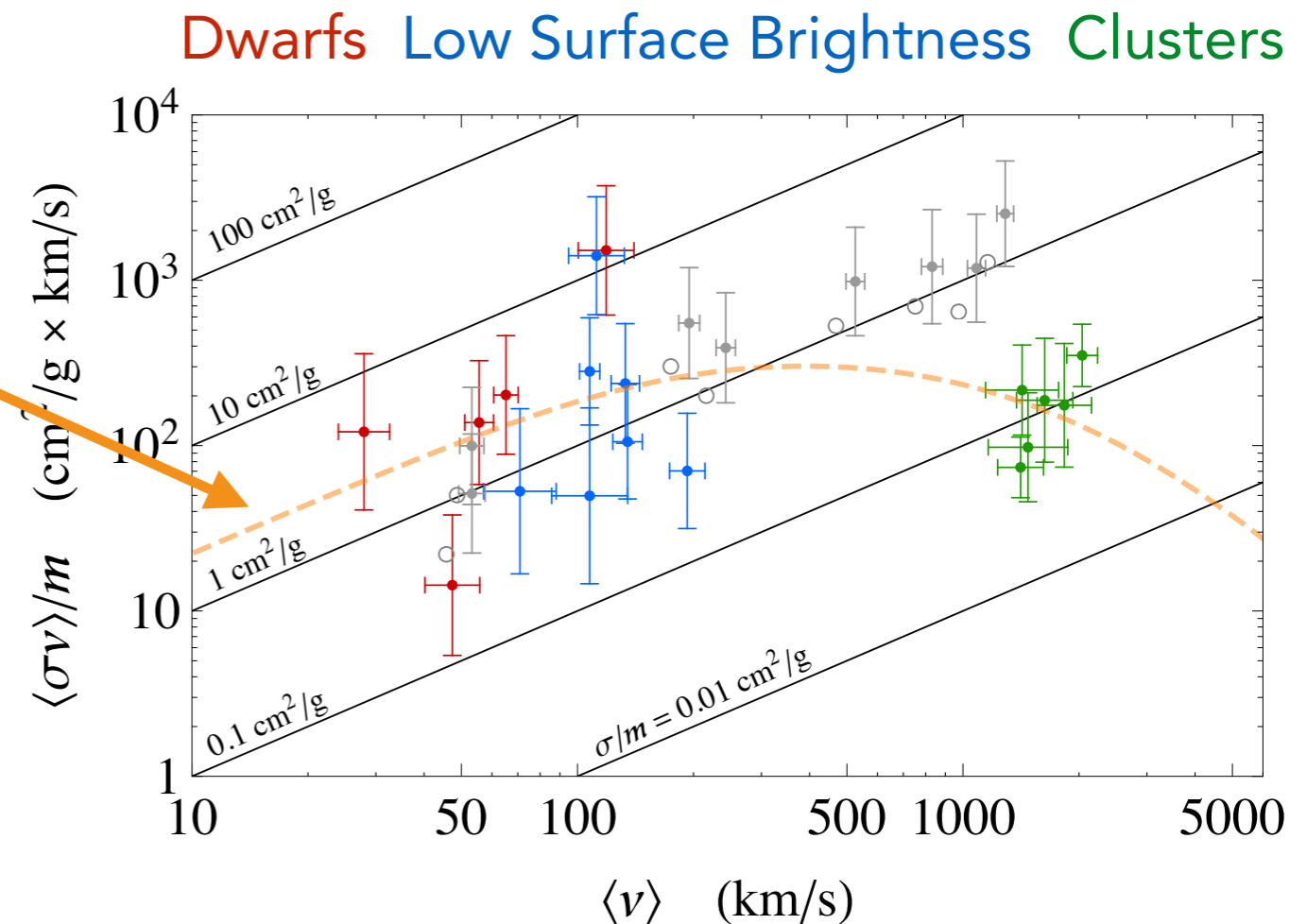
Fit to data with

$$m_\chi = 15 \text{ GeV}$$

$$m_V = 17 \text{ MeV}$$

Low-mass dark sectors also affect late-time gravitational clustering on small scales.

$$\Gamma \approx \frac{\rho_{\text{DM}}}{m_\chi} \sigma v \approx \frac{1}{10^9 \text{ year}}$$



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Sub-GeV model considerations

- Self-interaction bounds

Heavy mediator limit

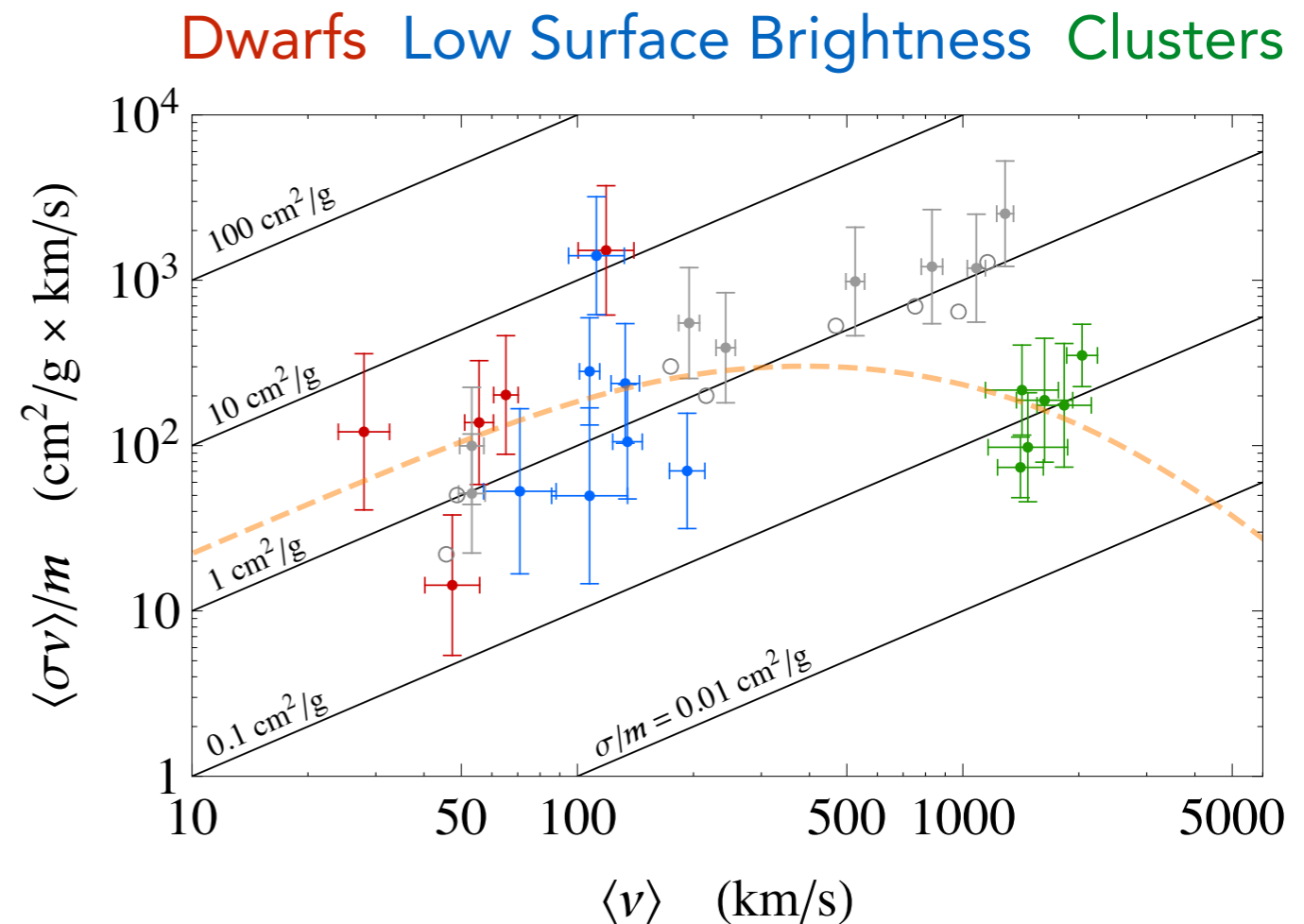
$$m_\phi \gg 10^{-3} m_\chi$$

$$\alpha_\chi \lesssim 0.025 \left(\frac{1 \text{ keV}}{m_\chi} \right)^{1/2} \left(\frac{m_\phi}{1 \text{ MeV}} \right)^2$$

Light mediator limit

$$m_\phi \lesssim 10^{-3} m_\chi$$

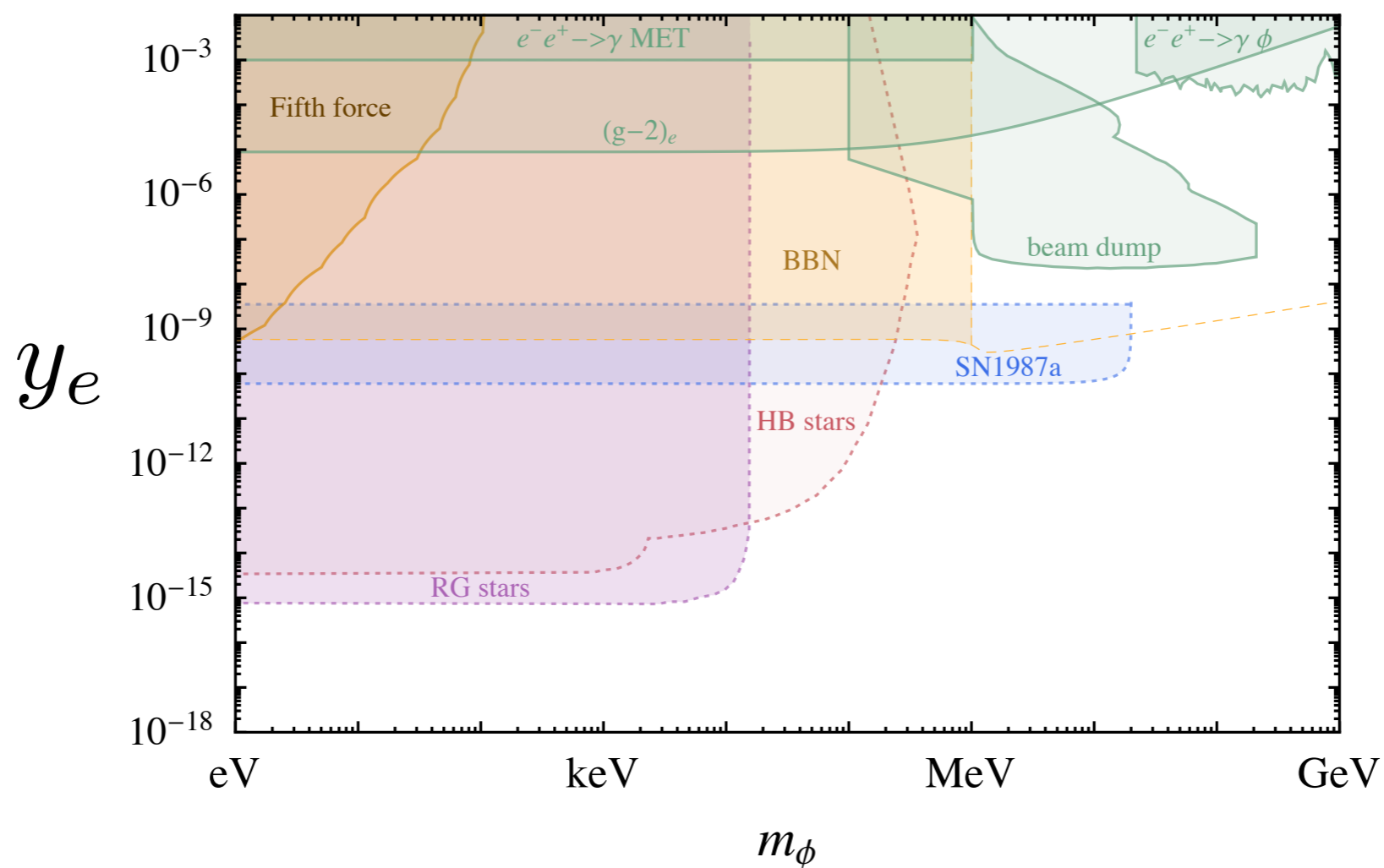
$$\alpha_\chi \lesssim 6 \times 10^{-10} \times \left(\frac{m_\chi}{1 \text{ MeV}} \right)^{3/2}$$



From Kaplinghat, Tulin, Yu 2015

Leptophilic scalar

Couplings to a light mediator are strongly constrained by stellar emission and fifth force searches on the low mass end

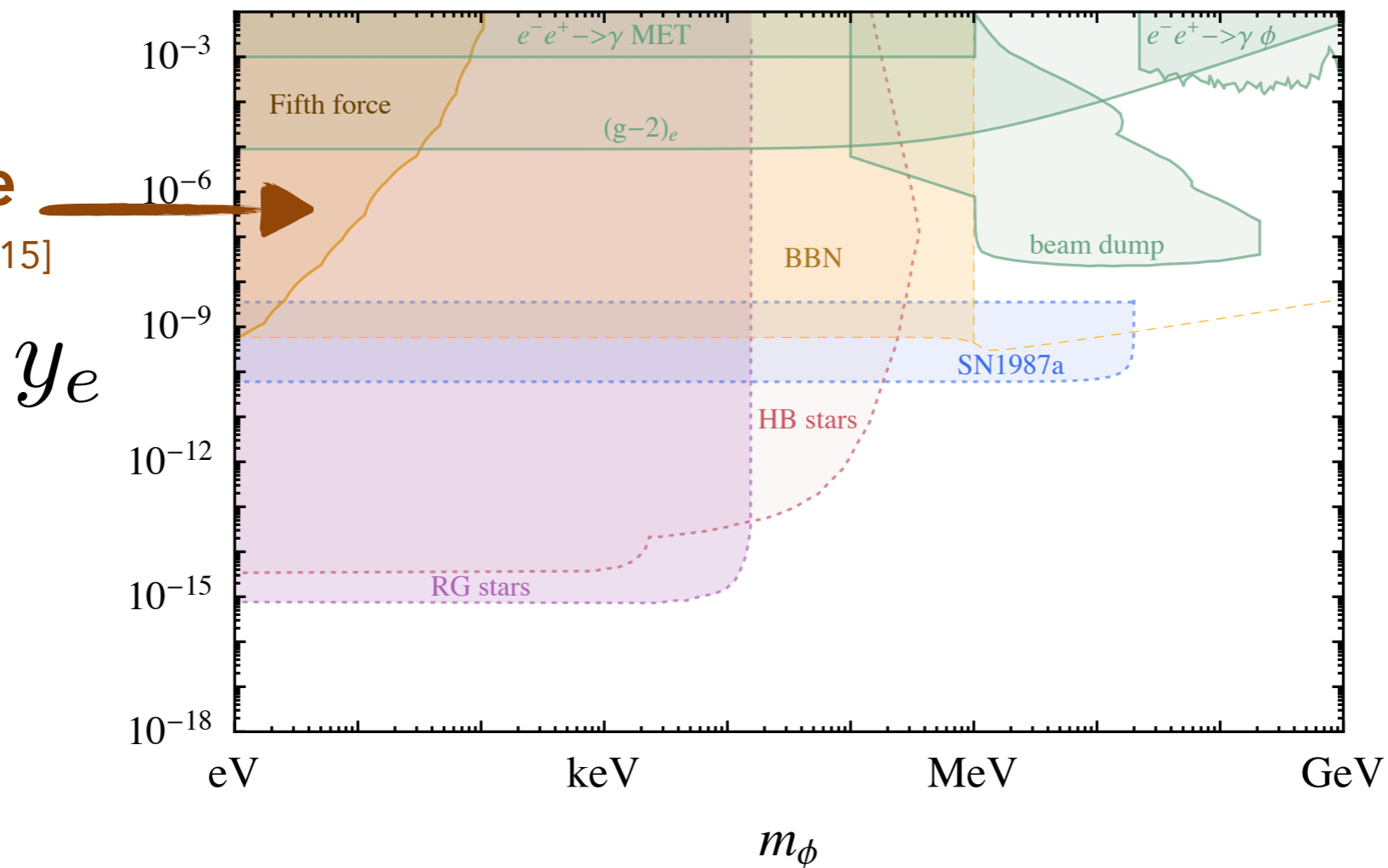


Scalar coupled to electron

Leptophilic scalar

Couplings to a light mediator are strongly constrained by stellar emission and fifth force searches on the low mass end

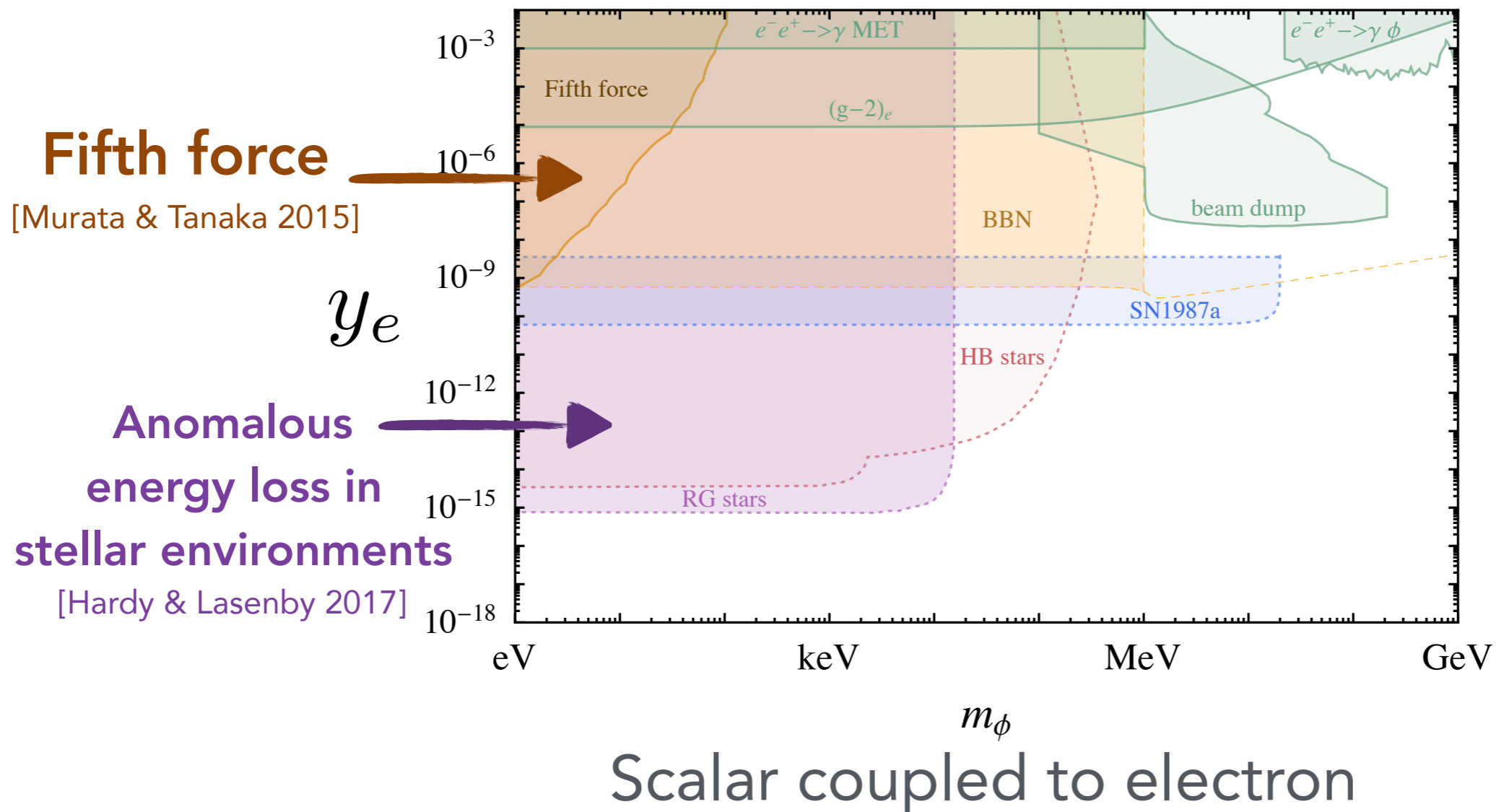
Fifth force
[Murata & Tanaka 2015]



Scalar coupled to electron

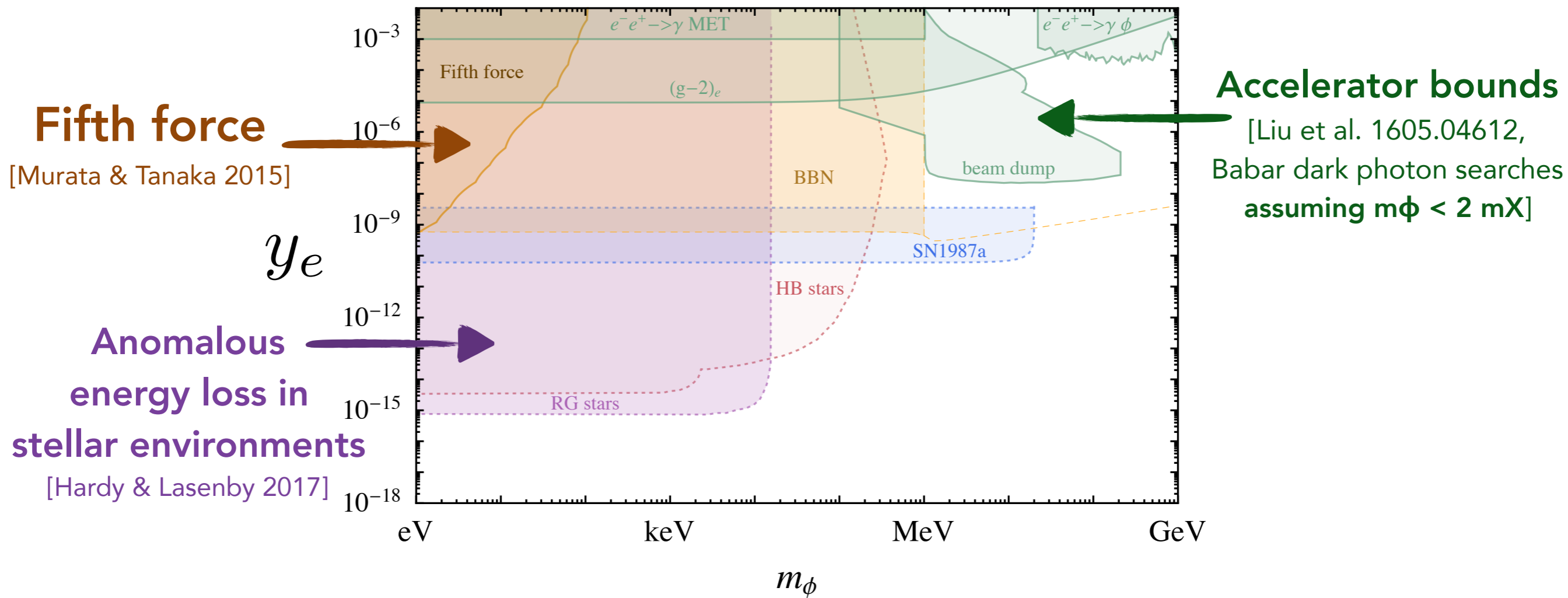
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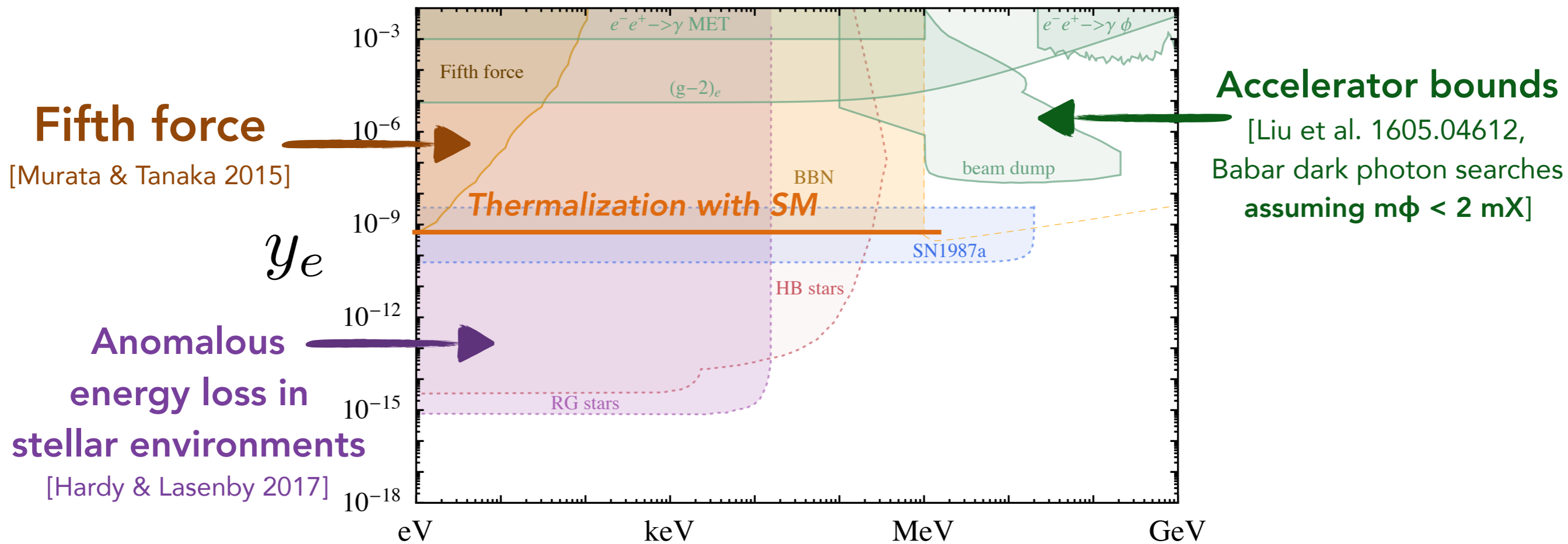
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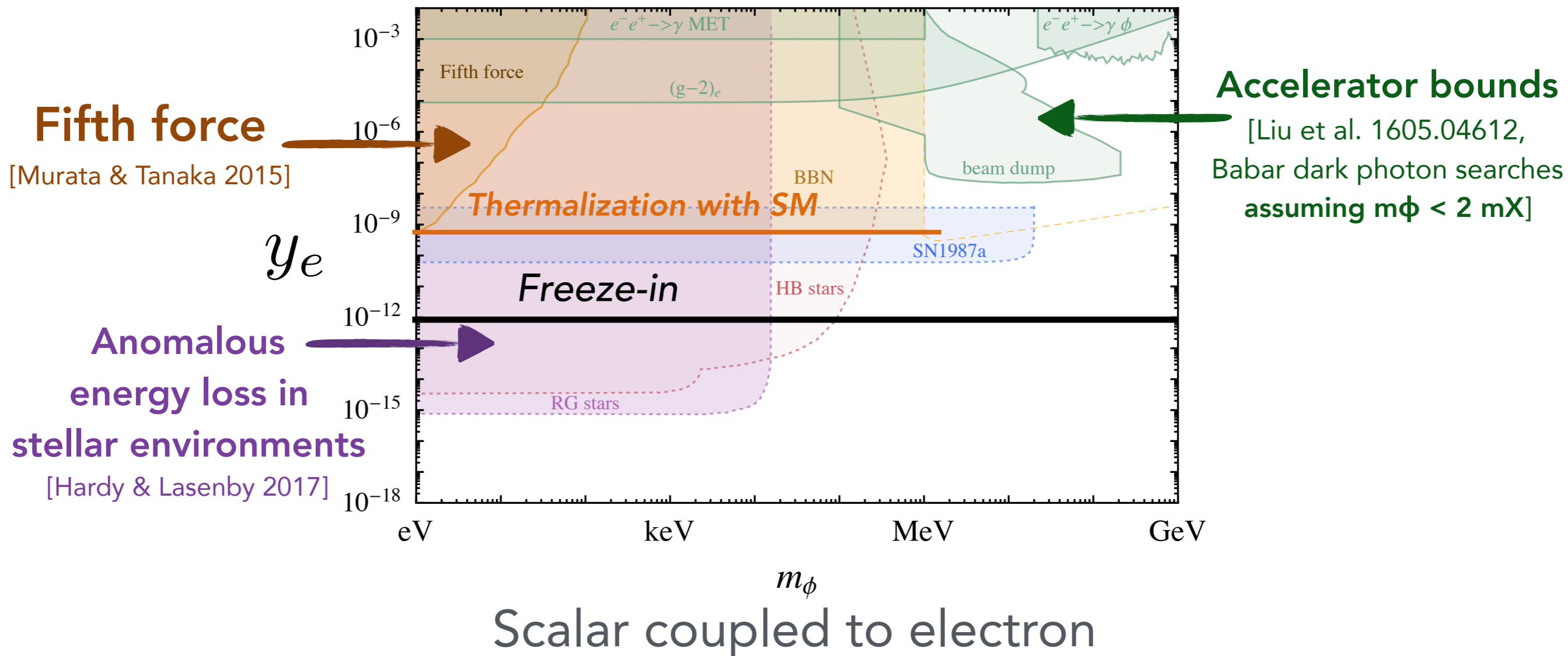
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Couplings to a light mediator are strongly constrained by stellar emission and fifth force searches on the low mass end



Electron scattering

$$\bar{\sigma}_e \equiv \frac{y_\chi^2 y_e^2}{4\pi} \frac{\mu_{\chi e}^2}{(m_\phi^2 + \alpha^2 m_e^2)^2}$$

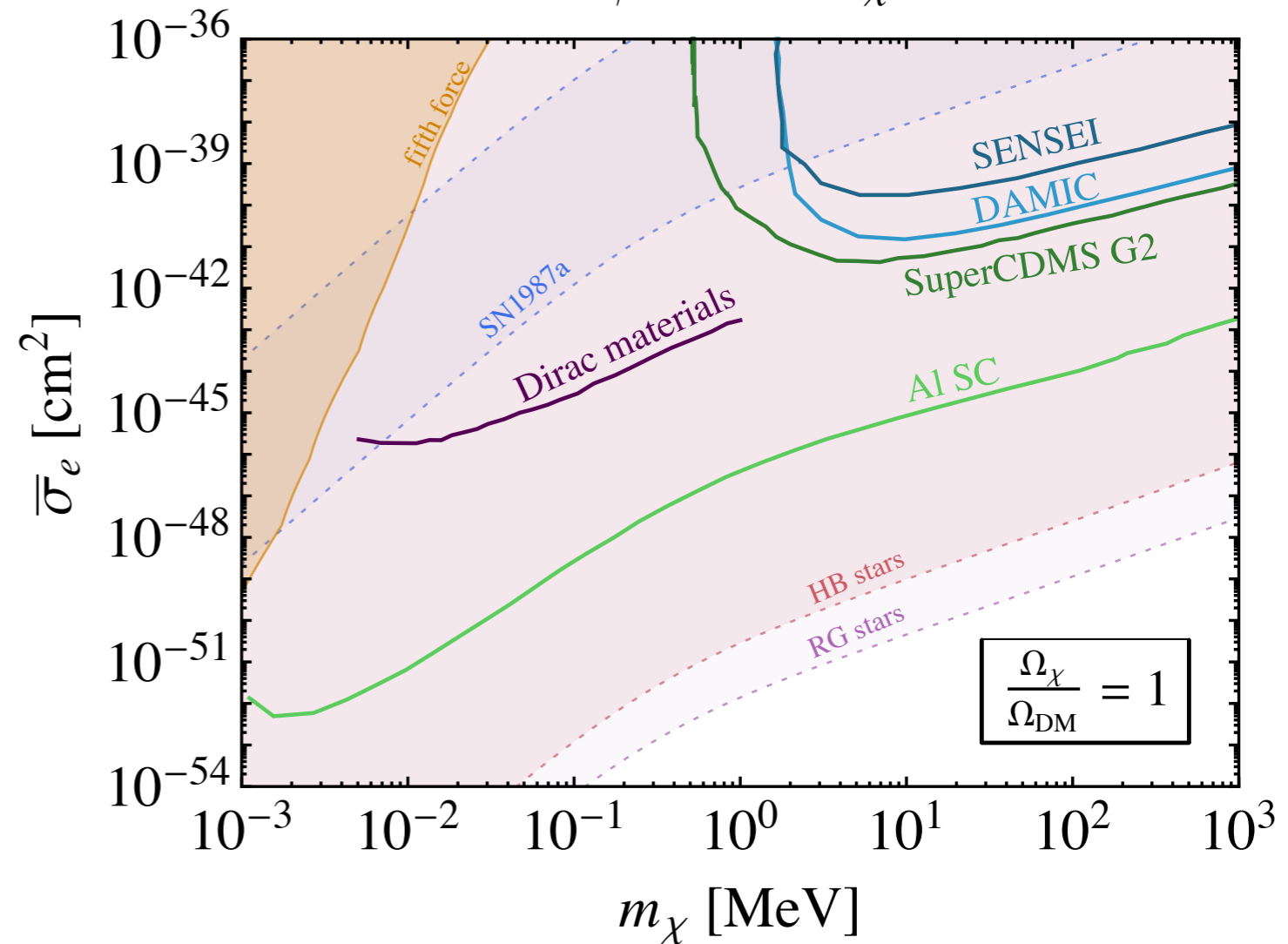
Typical momentum transfer²
for electron scattering in target

Combination of stellar+SIDM
constraints severely limits
open parameter space.

Considering sub-component
DM can open things up a little.

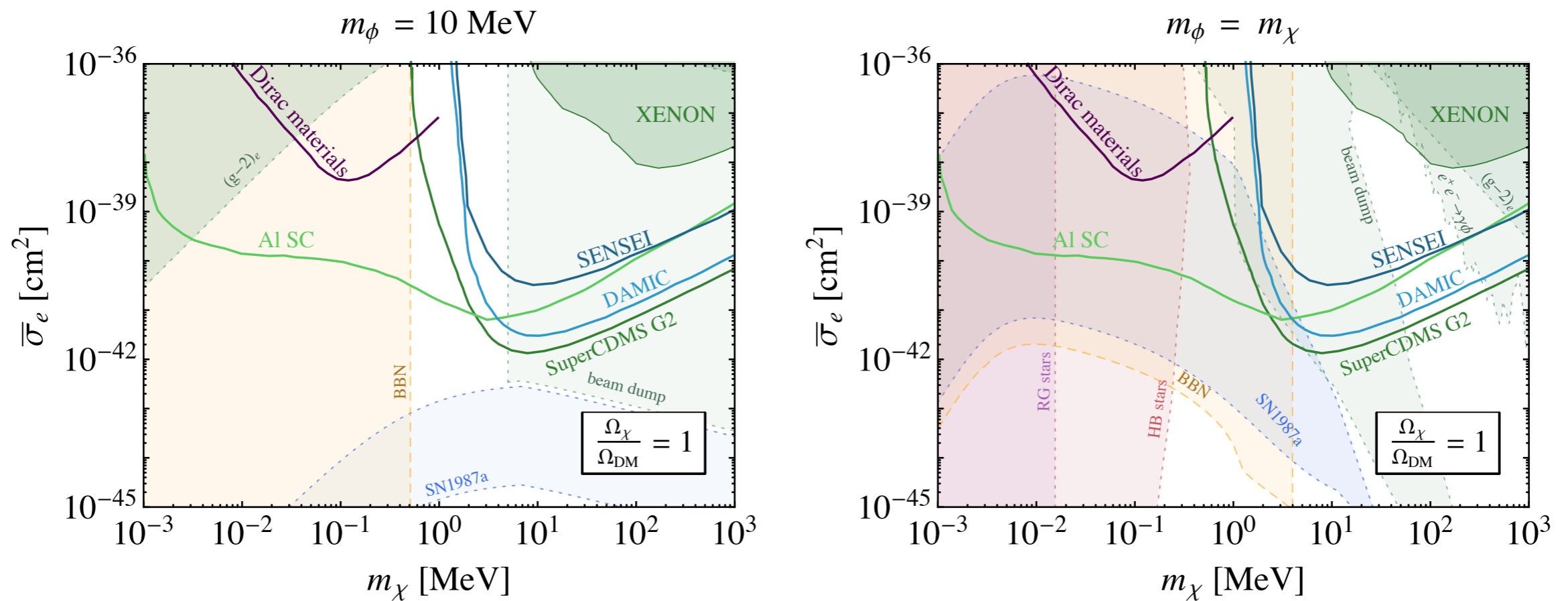
“Light” mediator case

$$m_\phi = 10^{-3} \mu_{\chi e}$$



Electron scattering

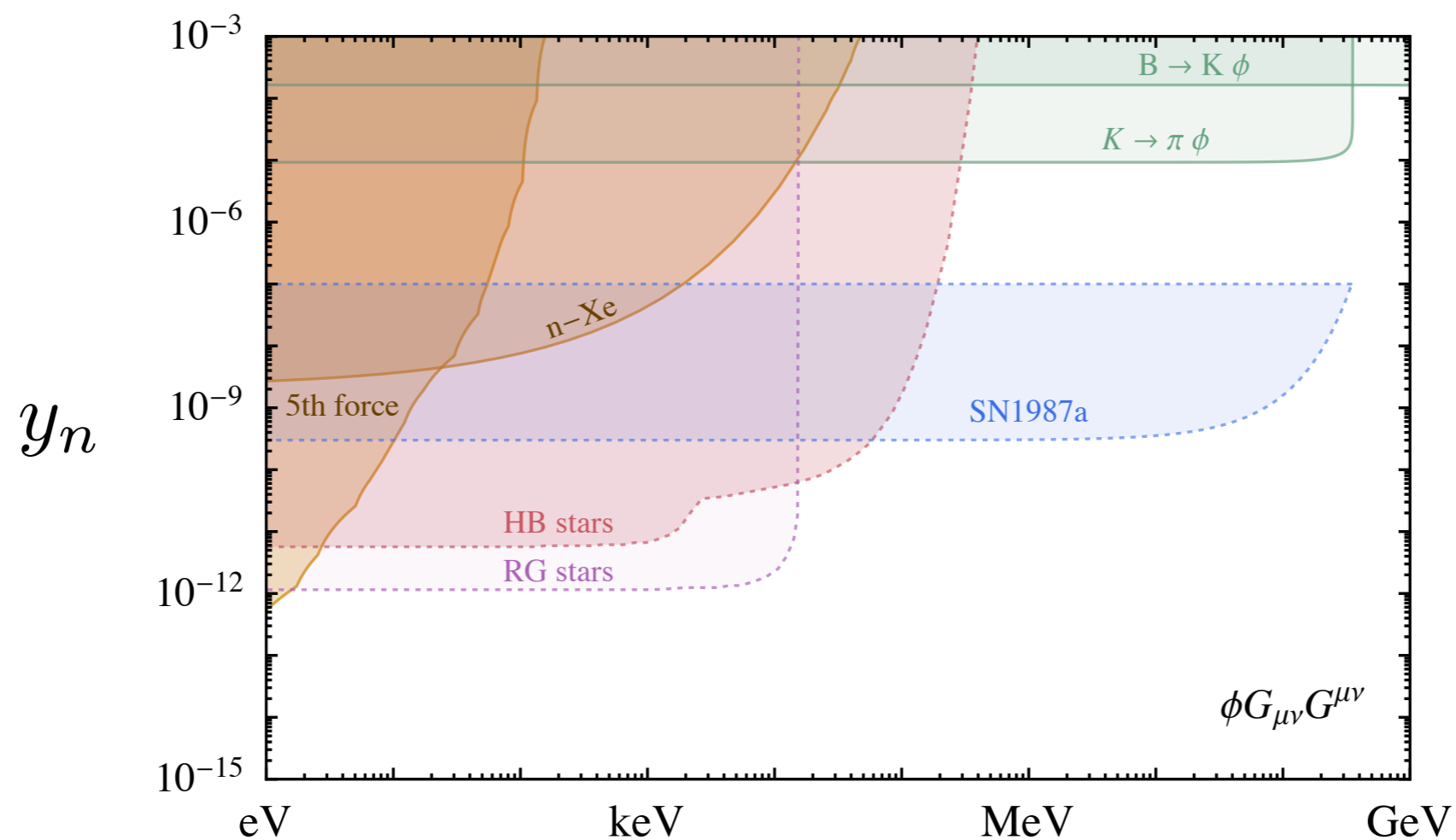
“Heavy” mediator case



DM masses below MeV are strongly constrained by BBN measurements of ΔN_{eff} .

Nucleo-philic scalar

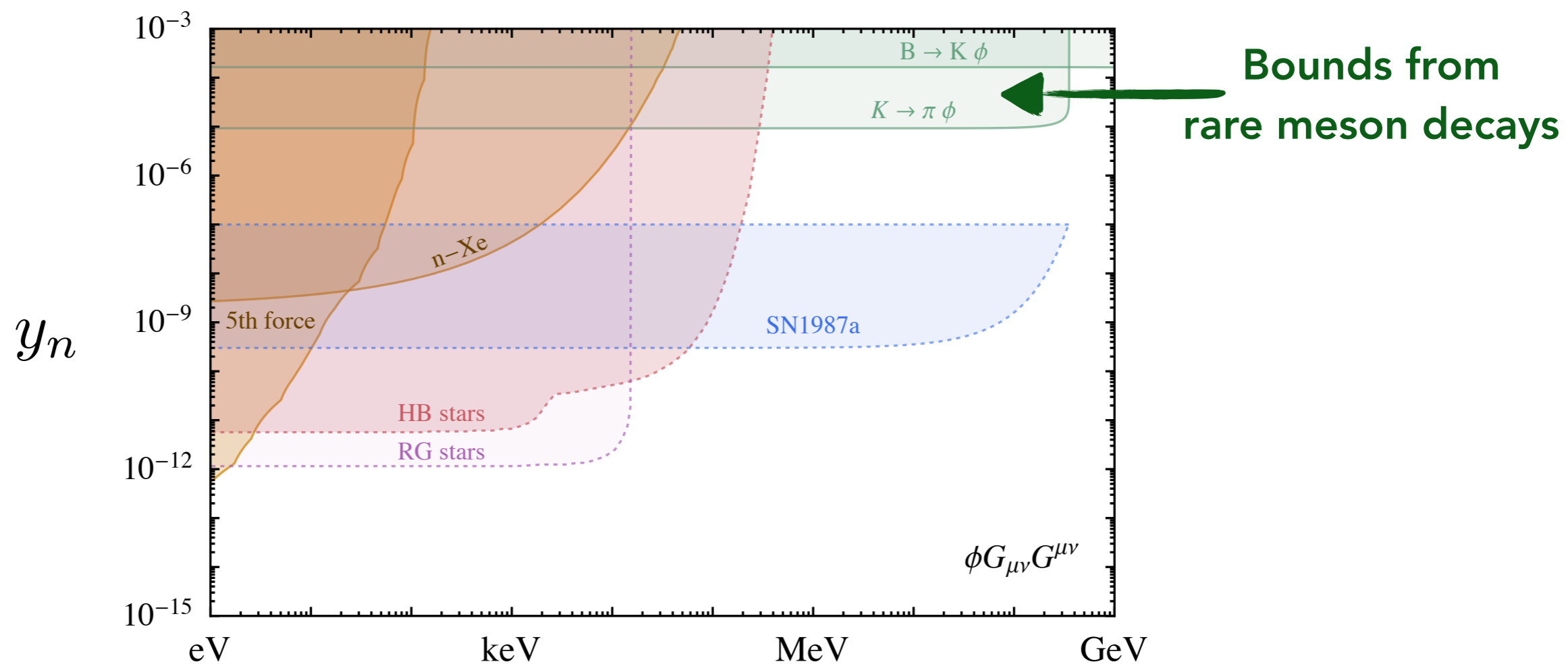
Thermalization of mediator is more dangerous here because fewer SM states to go back to...



Scalar coupled to gluons

Nucleo-philic scalar

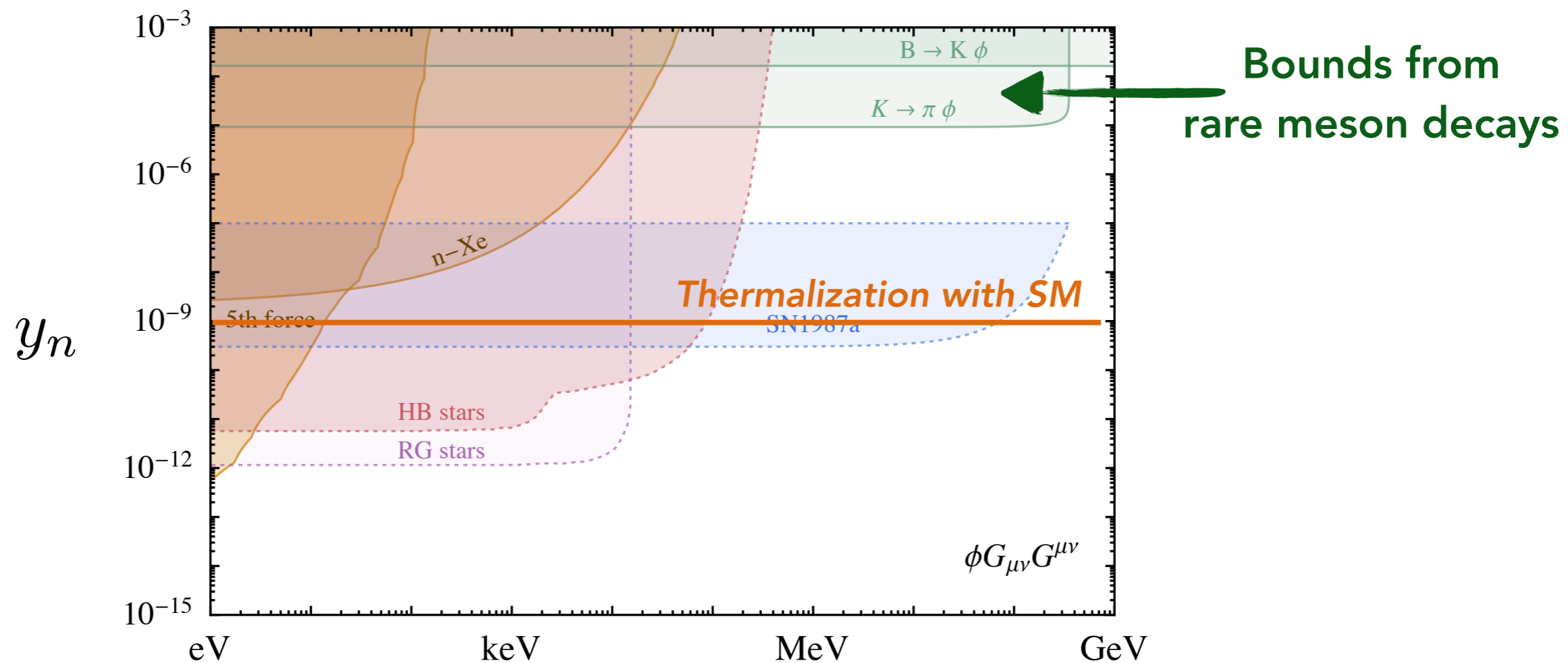
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Scalar coupled to gluons

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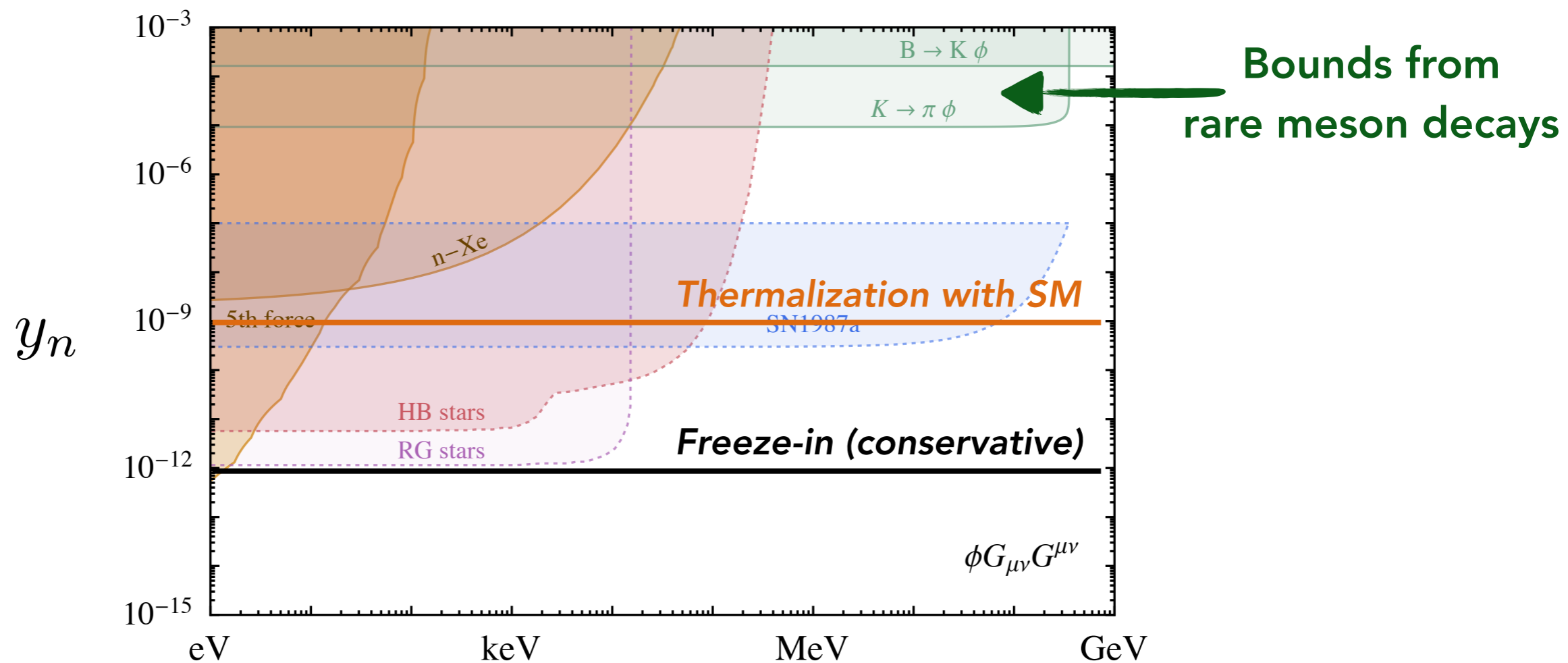
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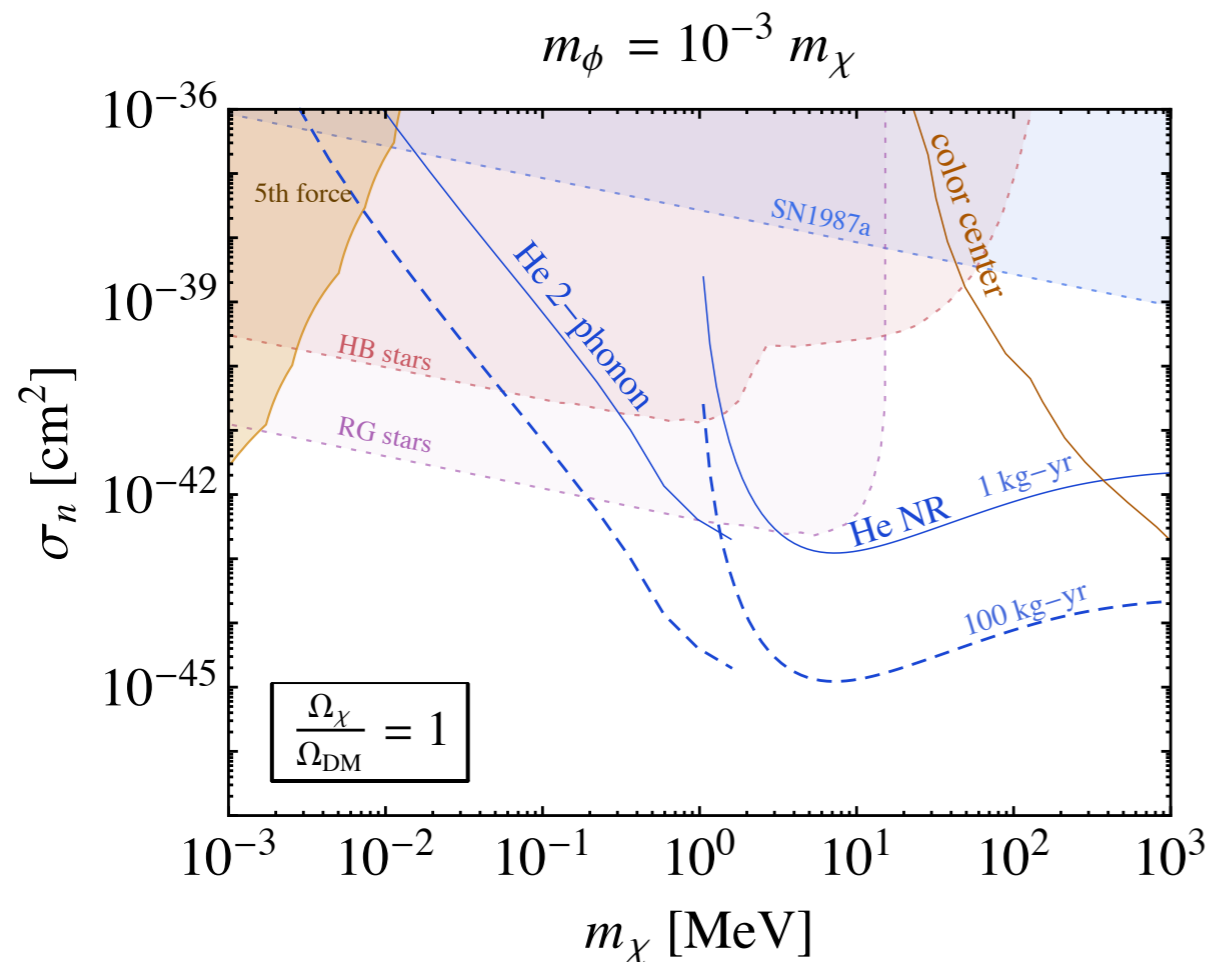
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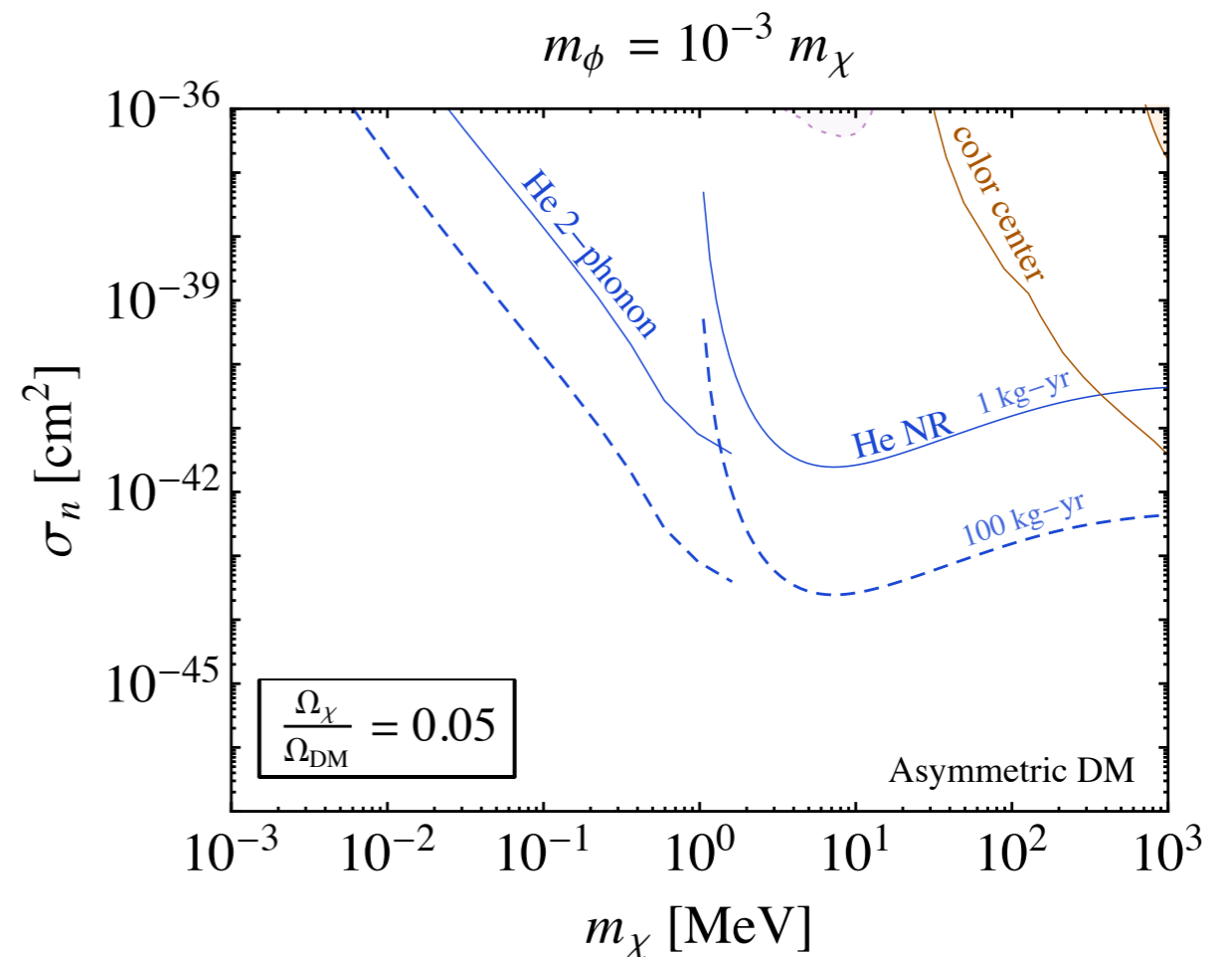
Scalar coupled to gluons

Nuclear recoils

“Light” mediator case $m_\phi \lesssim 10^{-3} m_\chi$



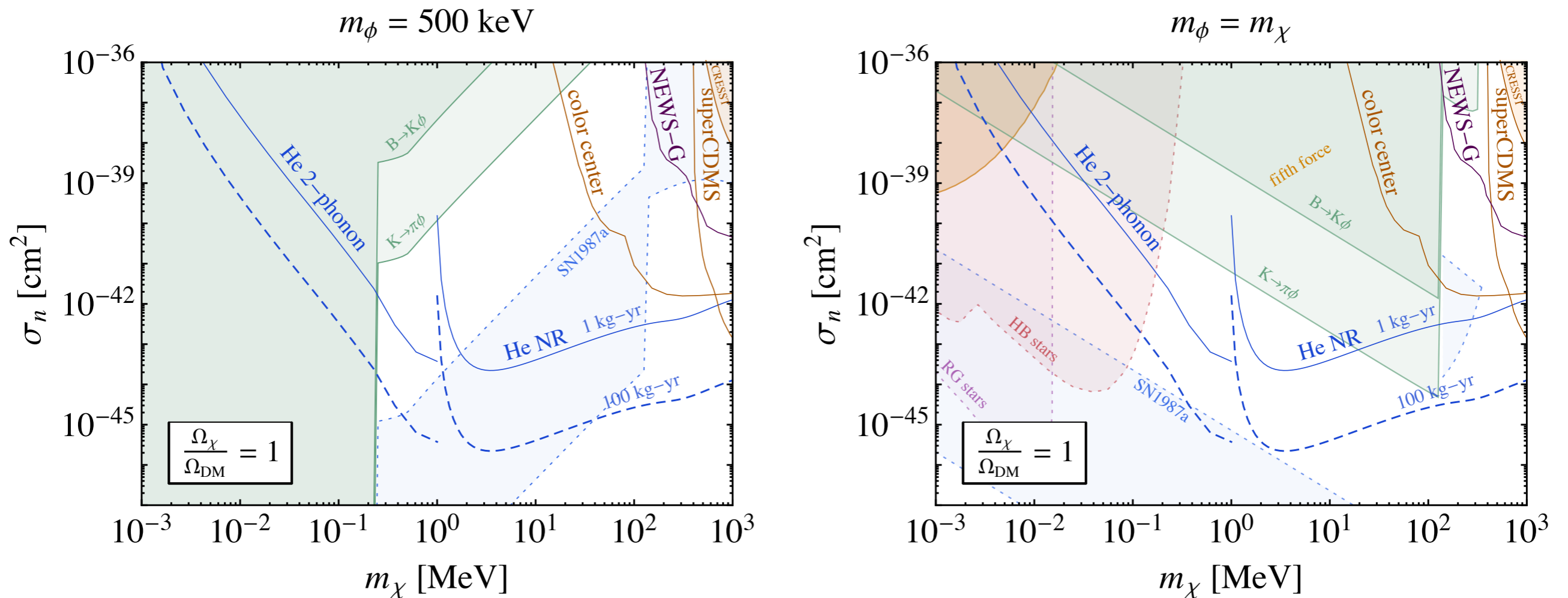
with SIDM bounds



without SIDM bounds

Nuclear recoils

“Heavy” mediator case

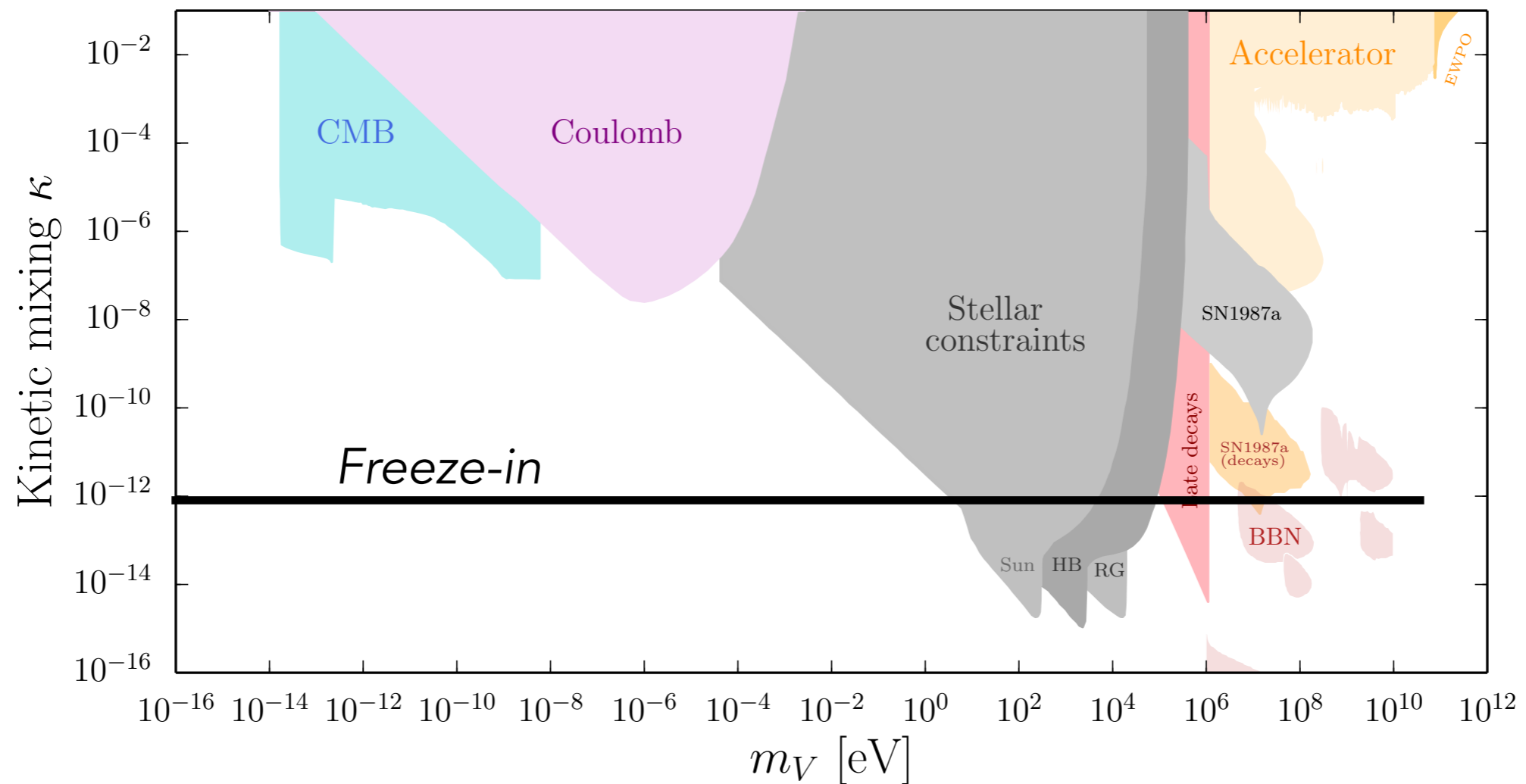


For $m_\chi < 100 \text{ MeV}$, mediator thermalizes with the SM bath after QCD phase transition and $\Delta N_{\text{eff}} = 0.57$!

Dark photon mediated models

Dark photon

Stellar and fifth force constraints are much weaker for dark photon mediators



Kinetically-mixed dark photon

In-medium dark photon couplings

$$\mathcal{L} \supset -\frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \frac{1}{4}V_{\mu\nu}V^{\mu\nu} + \frac{\kappa}{2}F_{\mu\nu}V^{\mu\nu} + \frac{1}{2}m_V^2 V_\mu V^\mu + eA_\mu J_{\text{EM}}^\mu + g_\chi V_\mu J_D^\mu$$

Usual (vacuum)
interaction basis \downarrow $A_\mu \rightarrow A_\mu + \kappa V_\mu$

$$e(A_\mu + \kappa V_\mu)J_{\text{EM}}^\mu + g_\chi V_\mu J_D^\mu$$

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↓

$A_\mu \rightarrow A_\mu + \kappa V_\mu$

$$e(A_\mu + \kappa V_\mu)J_{\text{EM}}^\mu + g_\chi V_\mu J_D^\mu$$

In-medium
interactions

↓

$$\mathcal{L} \supset -\frac{1}{2}A_\mu \Pi^{\mu\nu} A_\nu - \kappa A_\mu \Pi^{\mu\nu} V_\nu$$

$$\Pi^{\mu\nu}(q) = \Pi_L(q)\eta_L^\mu\eta_L^\nu + \Pi_T(q)(\eta_+^\mu)^*\eta_+^\nu + \Pi_T(q)(\eta_-^\mu)^*\eta_-^\nu$$

In-medium dark photon couplings

Diagonalizing quadratic terms gives effective in-medium couplings



$$\mathcal{L} \supset -\frac{1}{4}\bar{F}_{\mu\nu}^+ \bar{F}_+^{\mu\nu} - \frac{1}{4}\bar{V}_{\mu\nu}^+ \bar{V}_+^{\mu\nu} + \frac{1}{2}\Pi_T(q)\bar{A}_\mu^+ \bar{A}_+^\mu + \frac{1}{2}m_V^2 \bar{V}_\mu^+ \bar{V}_+^\mu$$
$$+ e \left(\bar{A}_\mu^+ + \frac{\kappa m_V^2}{m_V^2 - \Pi_T(q)} \bar{V}_\mu^+ \right) J_{\text{EM}}^\mu + g_\chi \left(\bar{V}_\mu^+ - \frac{\kappa \Pi_T(q)}{m_V^2 - \Pi_T(q)} \bar{A}_\mu^+ \right) J_D^\mu$$

(similar result for longitudinal modes)

For $|\mathbf{q}| \sim \omega$ and non-relativistic plasma, $\Pi_T(q) \approx \omega_p^2$

In-medium dark photon couplings

$$e \left(\bar{A}_\mu^+ + \frac{\kappa m_V^2}{m_V^2 - \Pi_T(q)} \bar{V}_\mu^+ \right) J_{\text{EM}}^\mu + g_\chi \left(\bar{V}_\mu^+ - \frac{\kappa \Pi_T(q)}{m_V^2 - \Pi_T(q)} \bar{A}_\mu^+ \right) J_D^\mu$$

Implications

In-medium dark photon couplings

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Implications

Production of dark photon in stars is suppressed by $(mV/\omega_p)^2 \sim (mV/\text{keV})^2$ for small mV . Resonant production is possible for

$$mV = \omega_p$$

In-medium dark photon couplings

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In the ultralight mediator limit, dark matter coupled to V can be treated as effectively millicharged.

In-medium dark photon couplings

$$e \left(\bar{A}_\mu^+ + \frac{\kappa m_V^2}{m_V^2 - \Pi_T(q)} \bar{V}_\mu^+ \right) J_{\text{EM}}^\mu + g_\chi \left(\bar{V}_\mu^+ - \frac{\kappa \Pi_T(q)}{m_V^2 - \Pi_T(q)} \bar{A}_\mu^+ \right) J_D^\mu$$

Implications

Production of dark photon in stars is suppressed by $(mV/\omega_p)^2 \sim (mV/\text{keV})^2$ for small mV . Resonant production is possible for

$$mV = \omega_p$$

In the ultralight mediator limit, dark matter coupled to V can be treated as effectively millicharged.

Benchmarks with dark matter coupling to massive mediators are mostly unaffected

Heavy mediator limit

Thermal freeze out with scalar DM or asymmetric fermion DM is viable above ~ 10 MeV

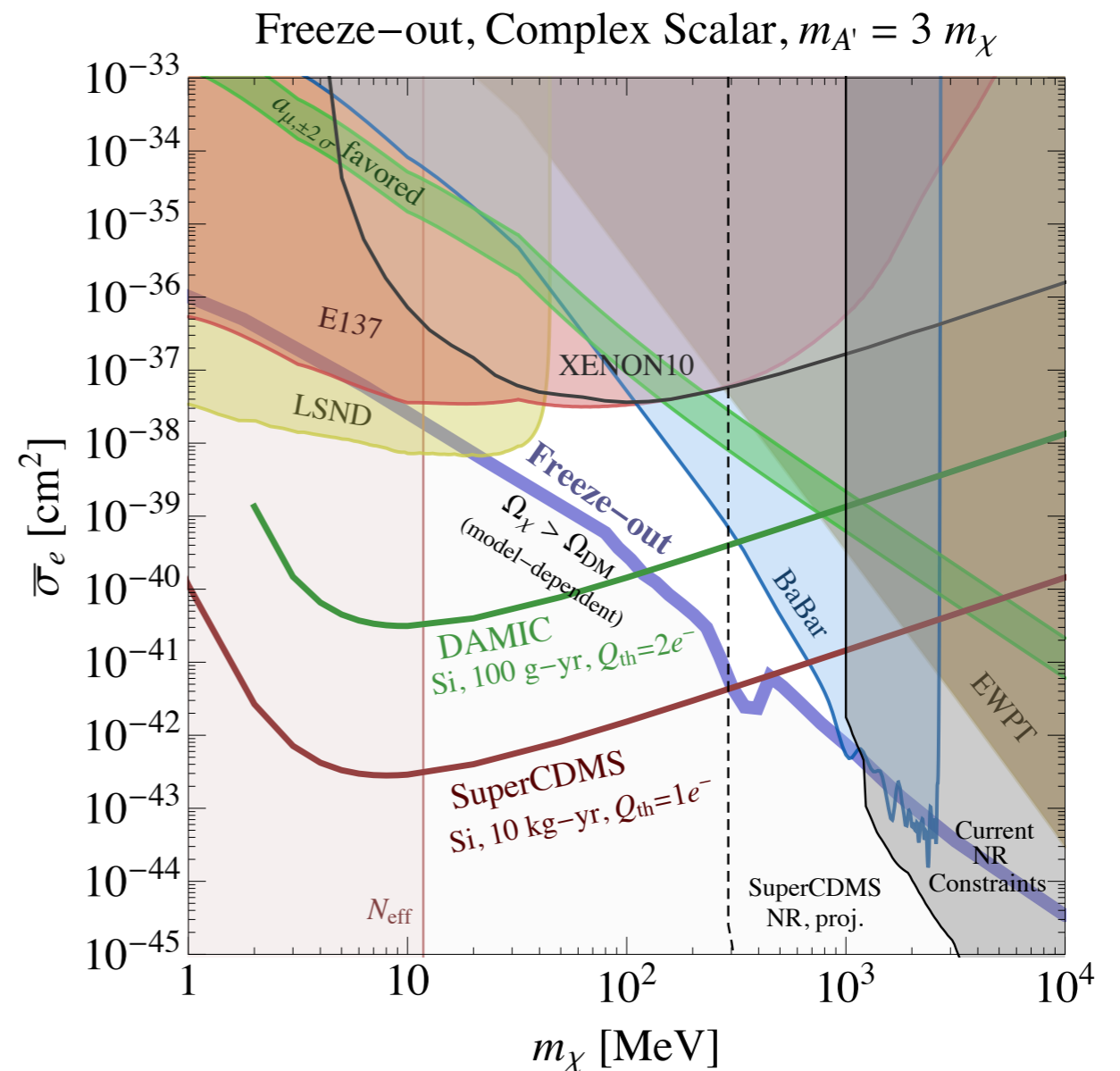
$$\bar{\sigma}_e \equiv \frac{16\pi\alpha_\chi\alpha_{em}\kappa^2\mu_{\chi e}^2}{(m_V^2 + \alpha_{em}^2 m_e^2)^2}$$

Example parameters:

$$m_\chi \simeq 20 \text{ MeV} \quad g_\chi \simeq 0.3$$

$$m_V \simeq 60 \text{ MeV} \quad \kappa \simeq 3 \times 10^{-4}$$

Accessible also with
accelerator searches



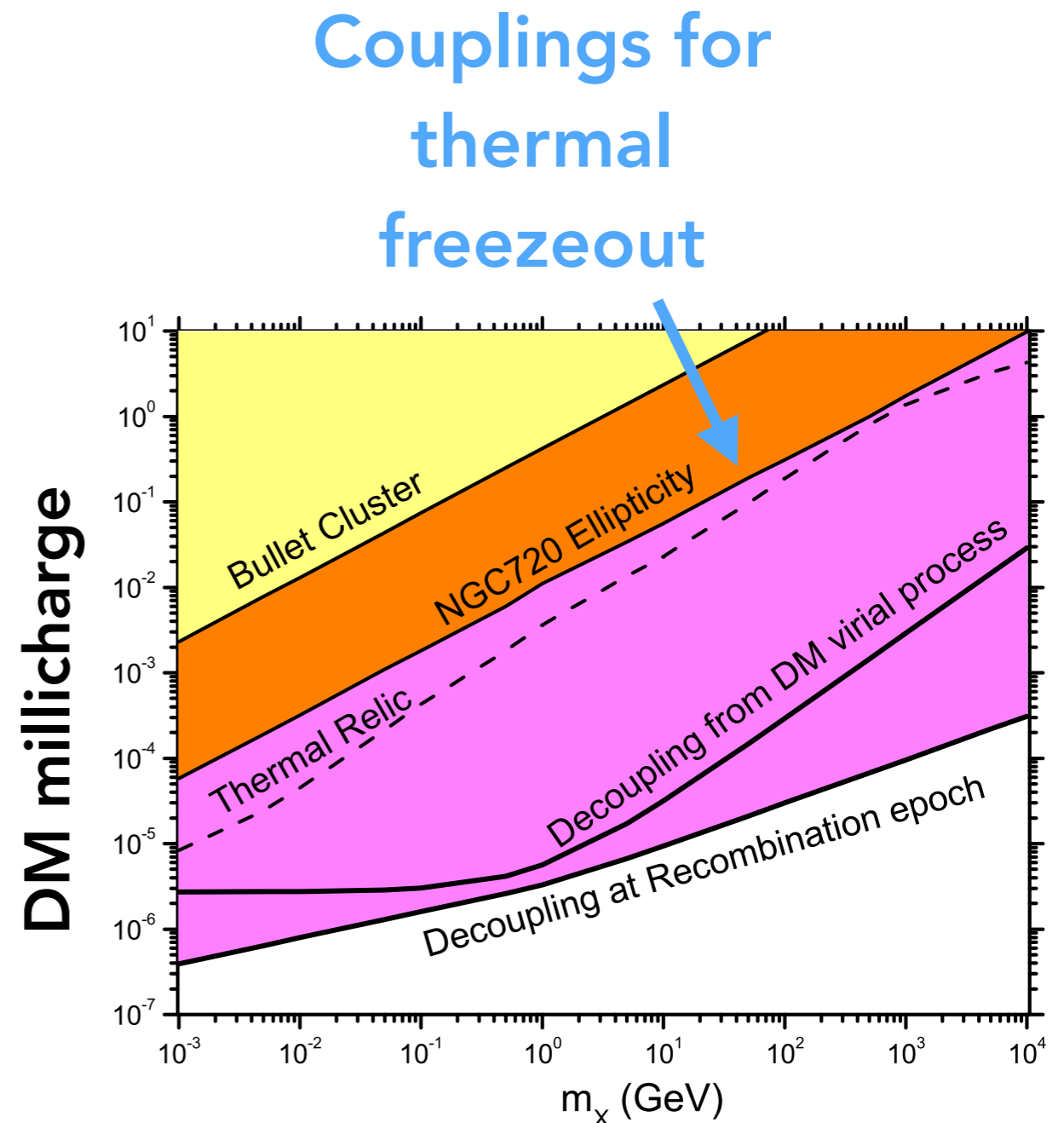
The ultralight mediator limit

For dark photon masses below $\sim eV$, define effective millicharge

$$Q = \frac{\kappa g_X}{e}$$

Self-interaction bounds on g_X push us to large κ and thus to the ultralight mediator mass limit

—> Can be considered specific realization of millicharged DM

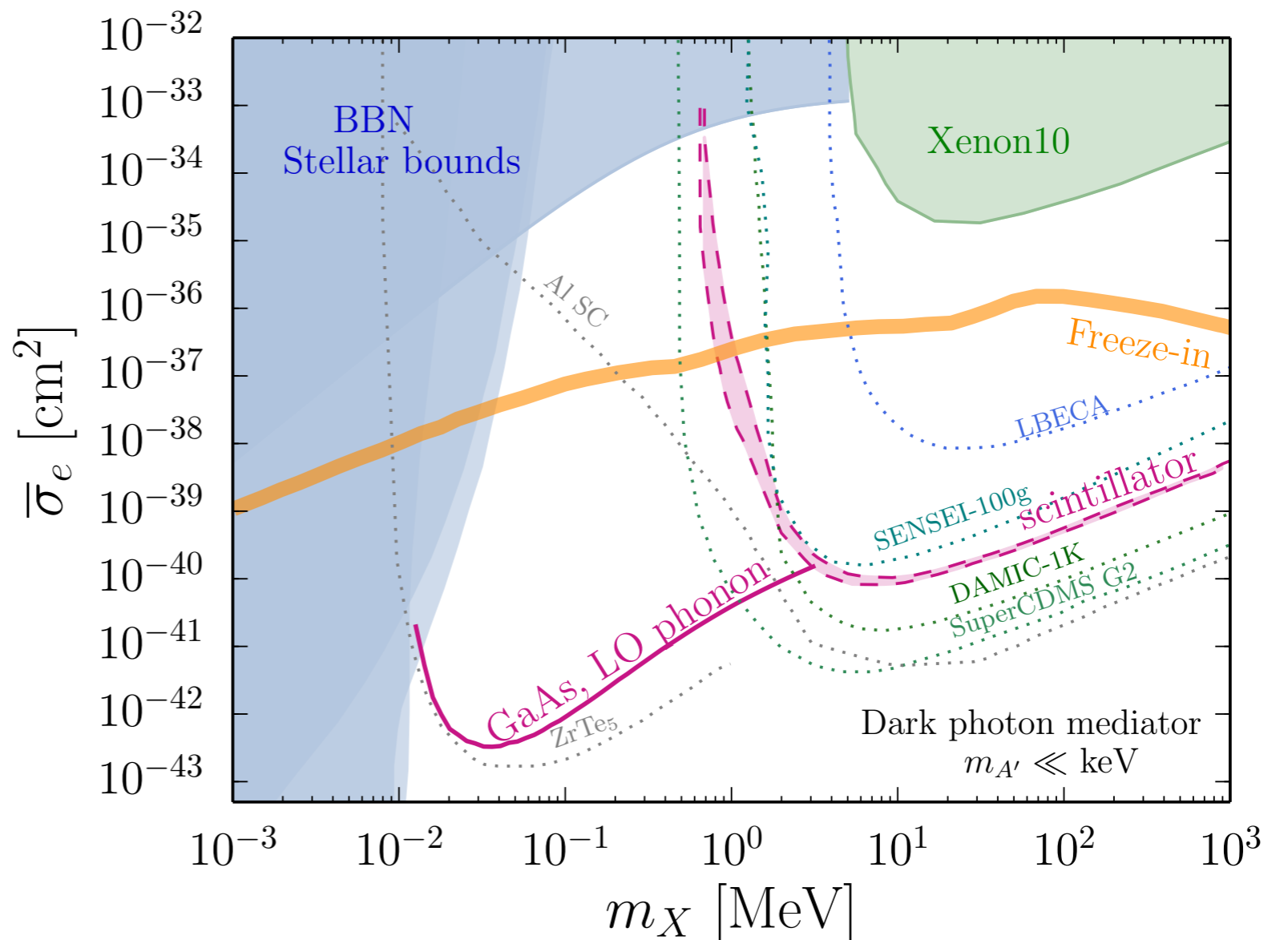


Thermal freeze-in benchmark

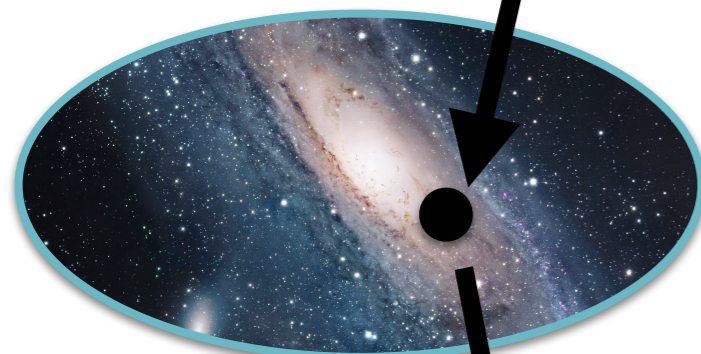
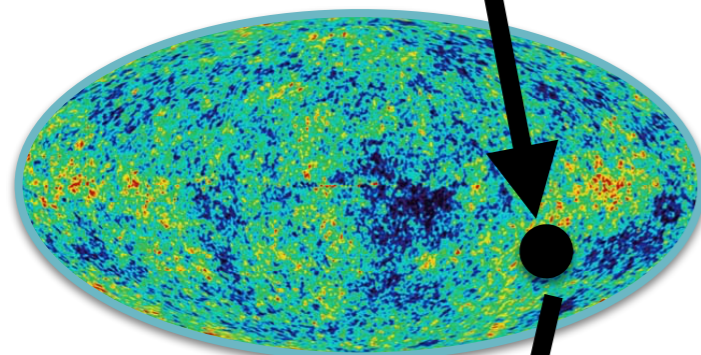
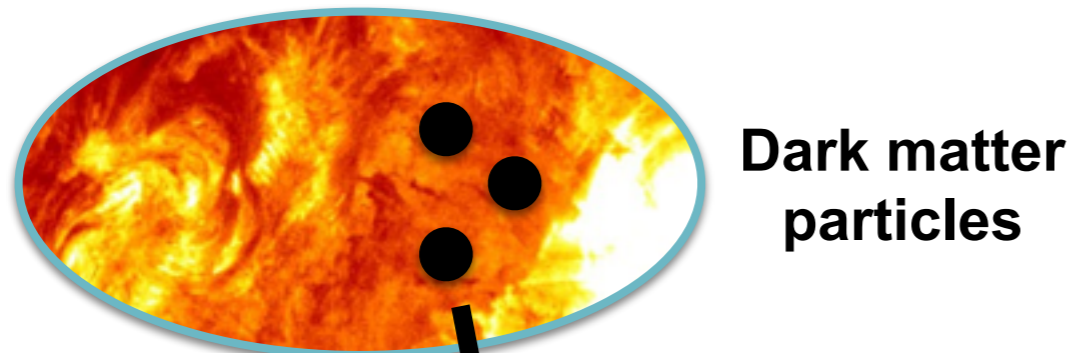
DM has millicharge $Q = \frac{\kappa g_X}{e} \sim 10^{-11}$

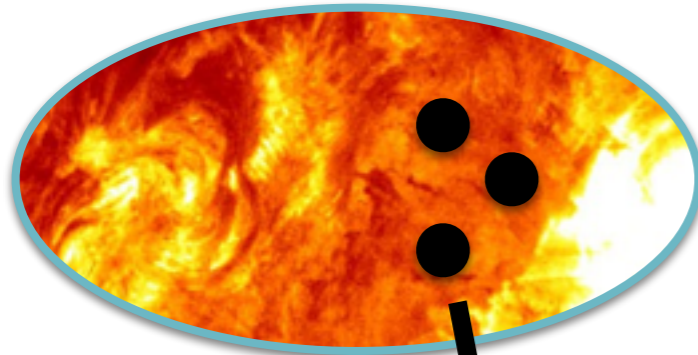
Electron scattering cross section is also maximized for freeze-in through a light mediator

$$\bar{\sigma}_e \equiv \frac{16\pi\alpha_\chi\alpha_{em}\kappa^2\mu_{\chi e}^2}{(m_V^2 + \alpha_{em}^2 m_e^2)^2}$$



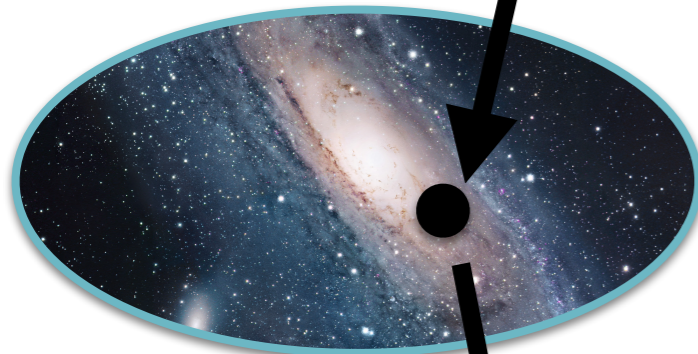
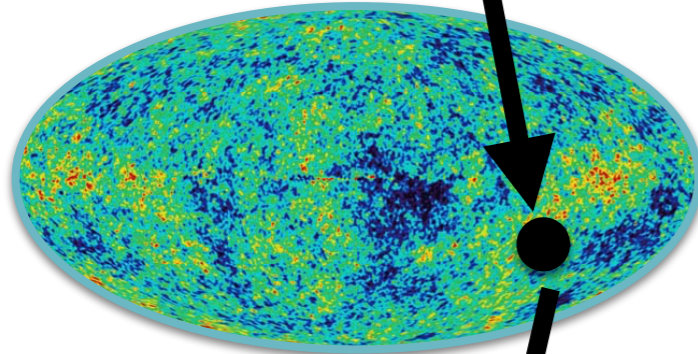
Cosmology of sub-MeV freeze-in DM





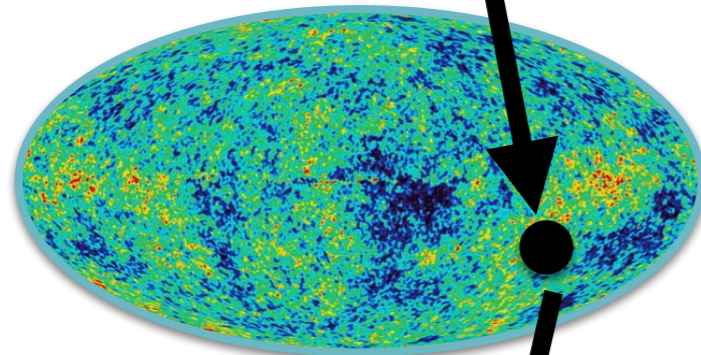
Dark matter particles

First minute: In-medium photon decays to DM, which can then free-stream

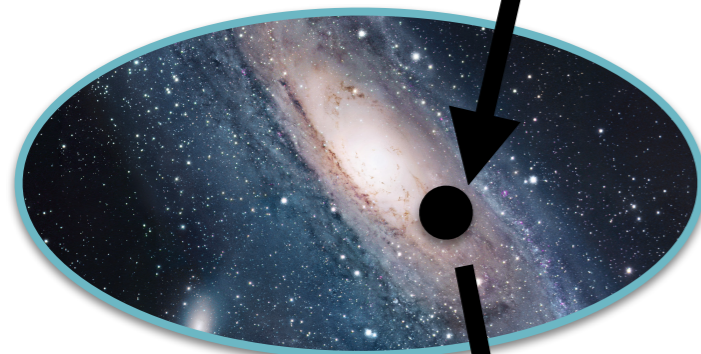




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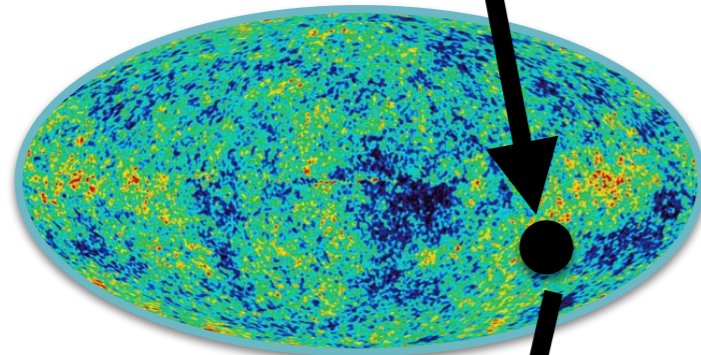


Recombination: Dark matter scatters against the baryon-photon fluid (drag effect).

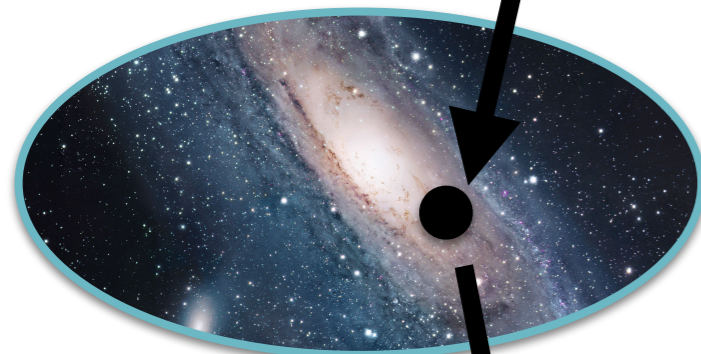




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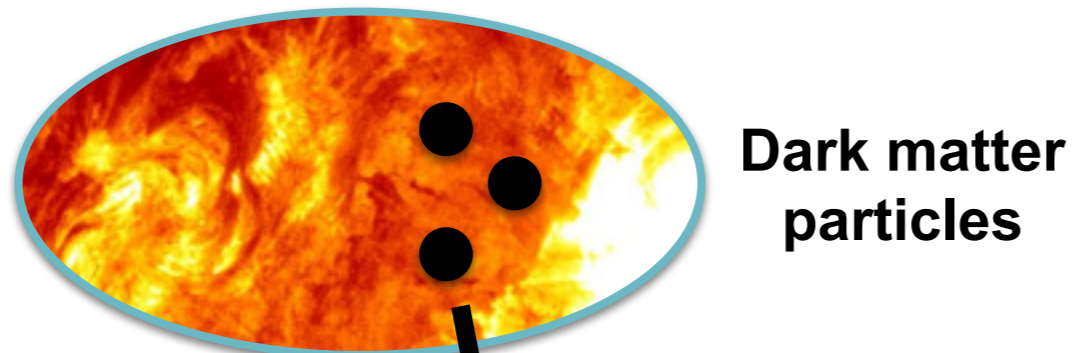


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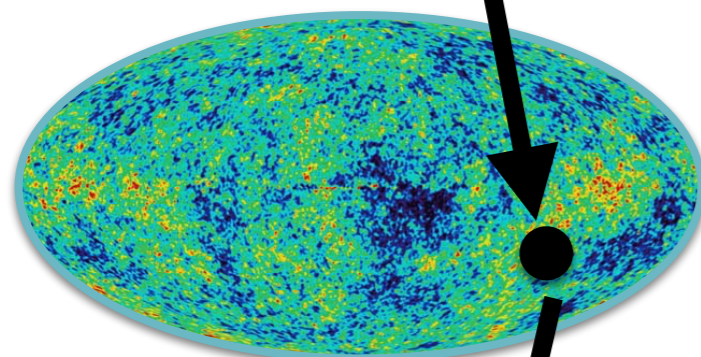


Galactic dynamics: Dark matter interacts with particles, fields within galaxies

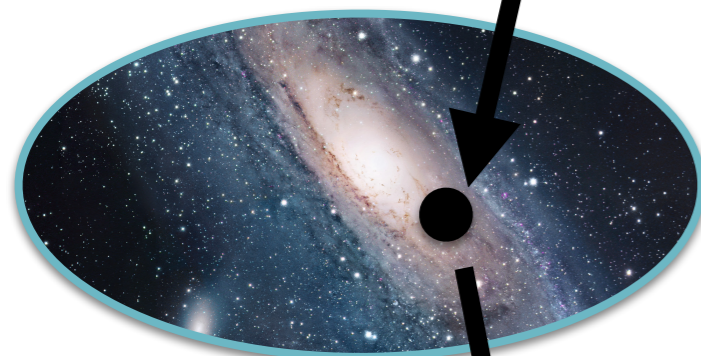




First minute: In-medium photon decays to DM, which can then free-stream



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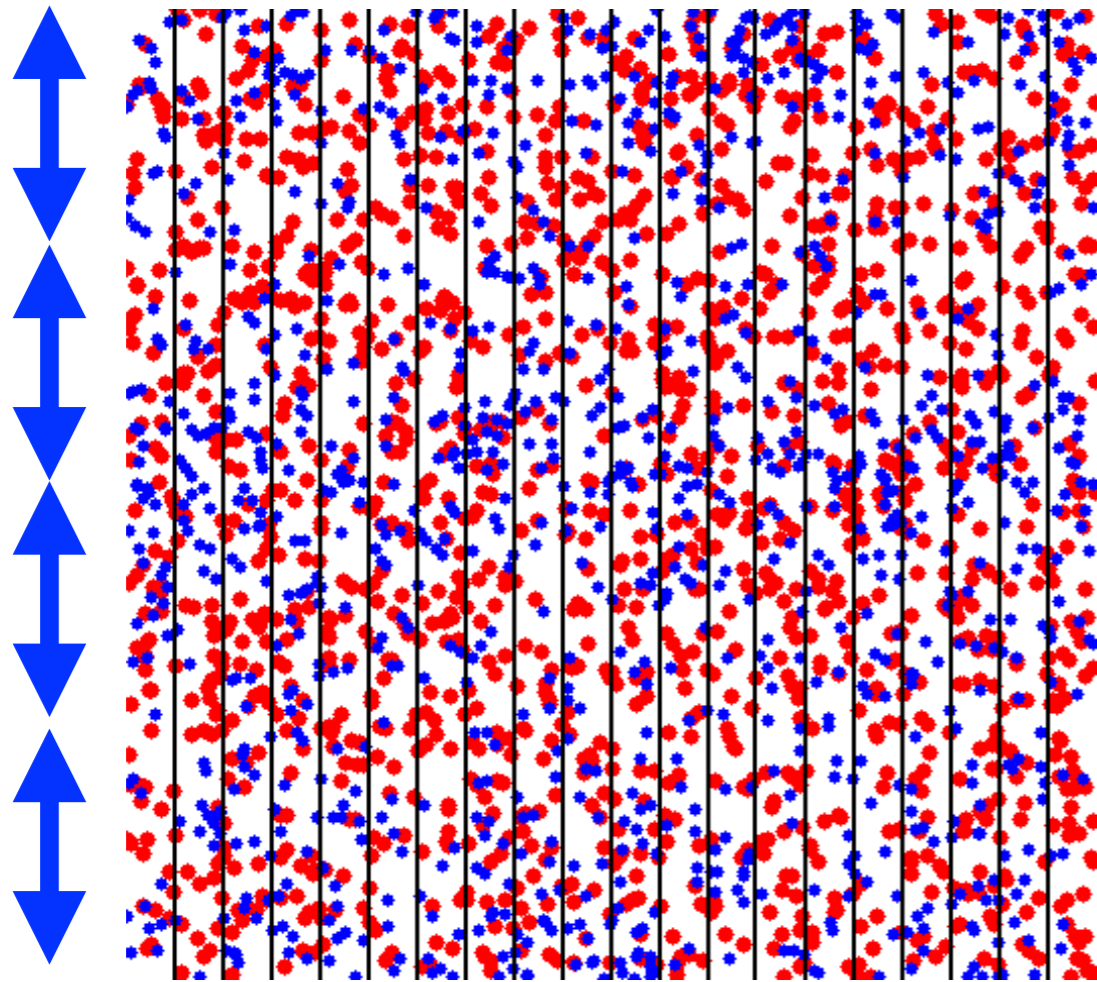


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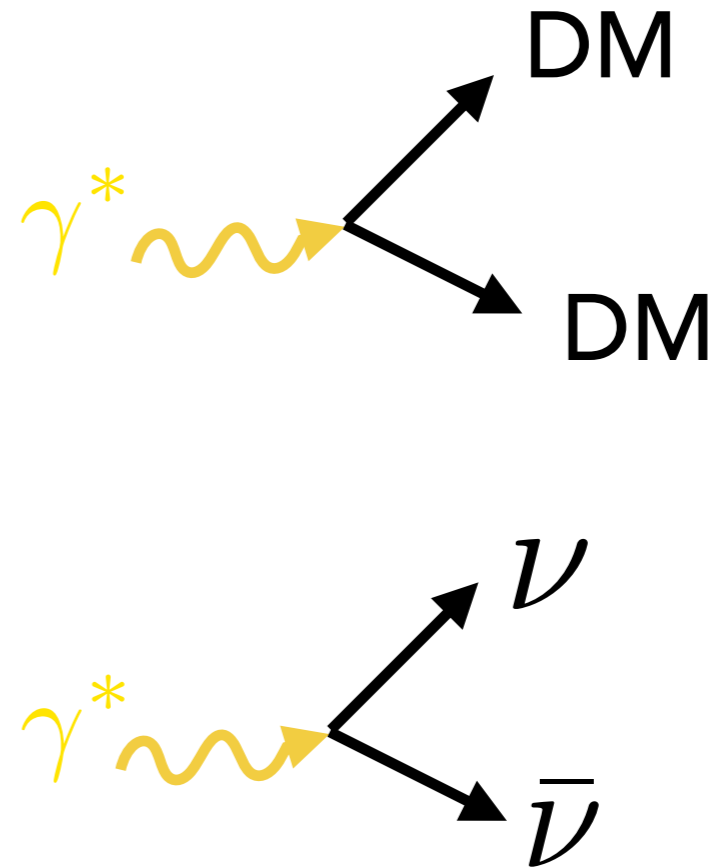


Future lab: DM scatters and creates phonon (or electron) excitations in a crystal target

Plasma oscillations

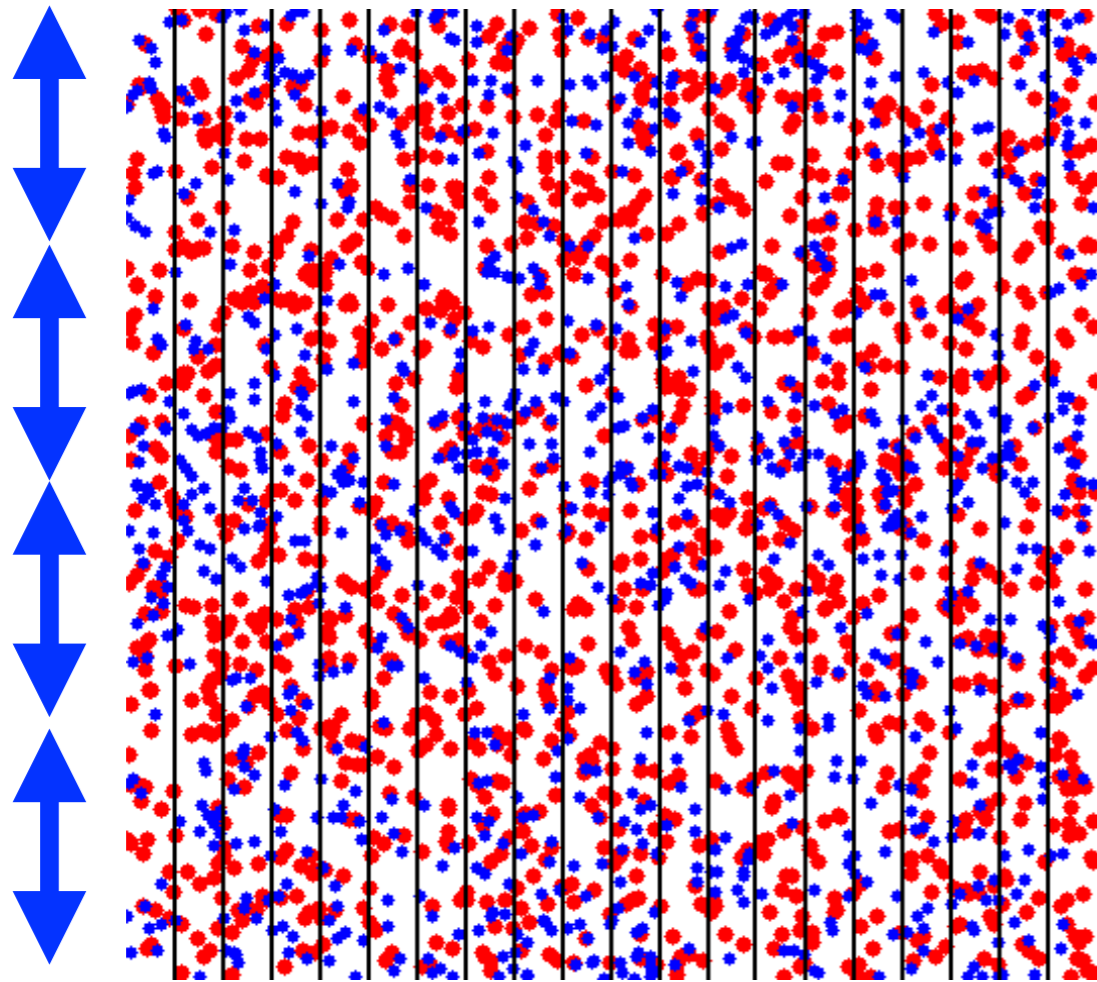


red: ion blue: electron

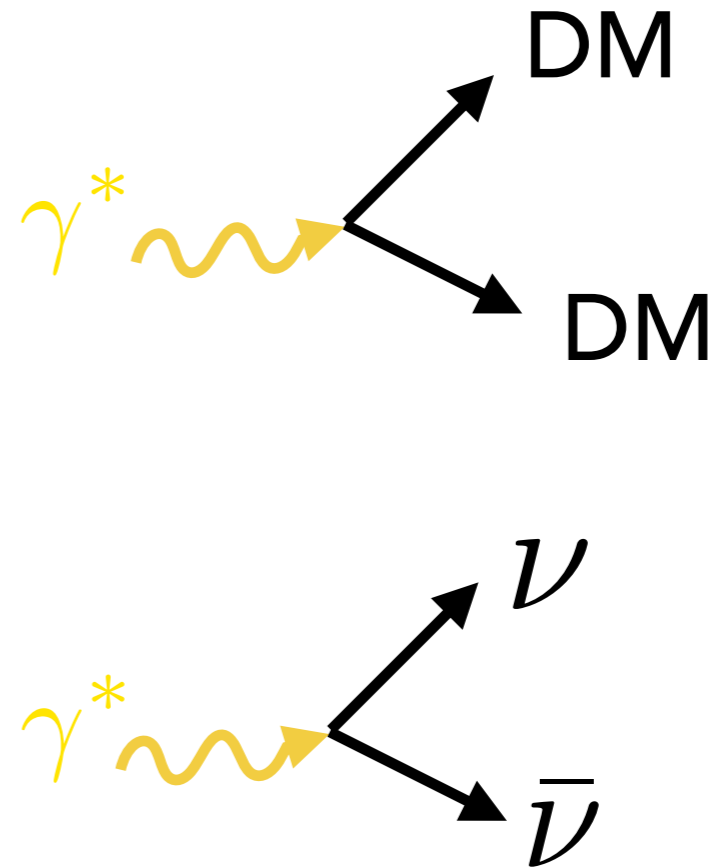


Dark matter created from plasma oscillations as long as plasma frequency $\omega_p \approx 0.1 k_B T$ is greater than $2m_{DM}$

Plasma oscillations



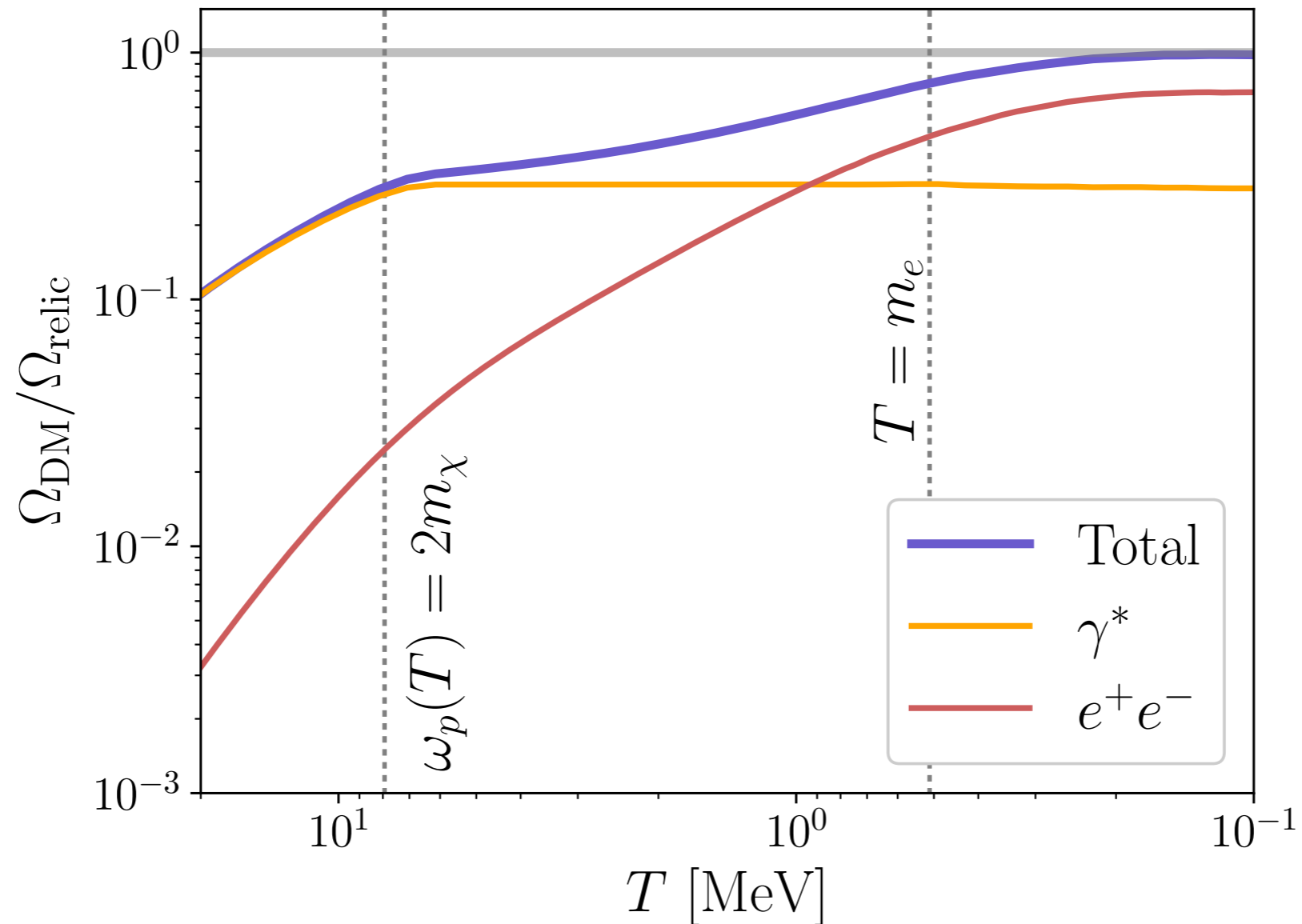
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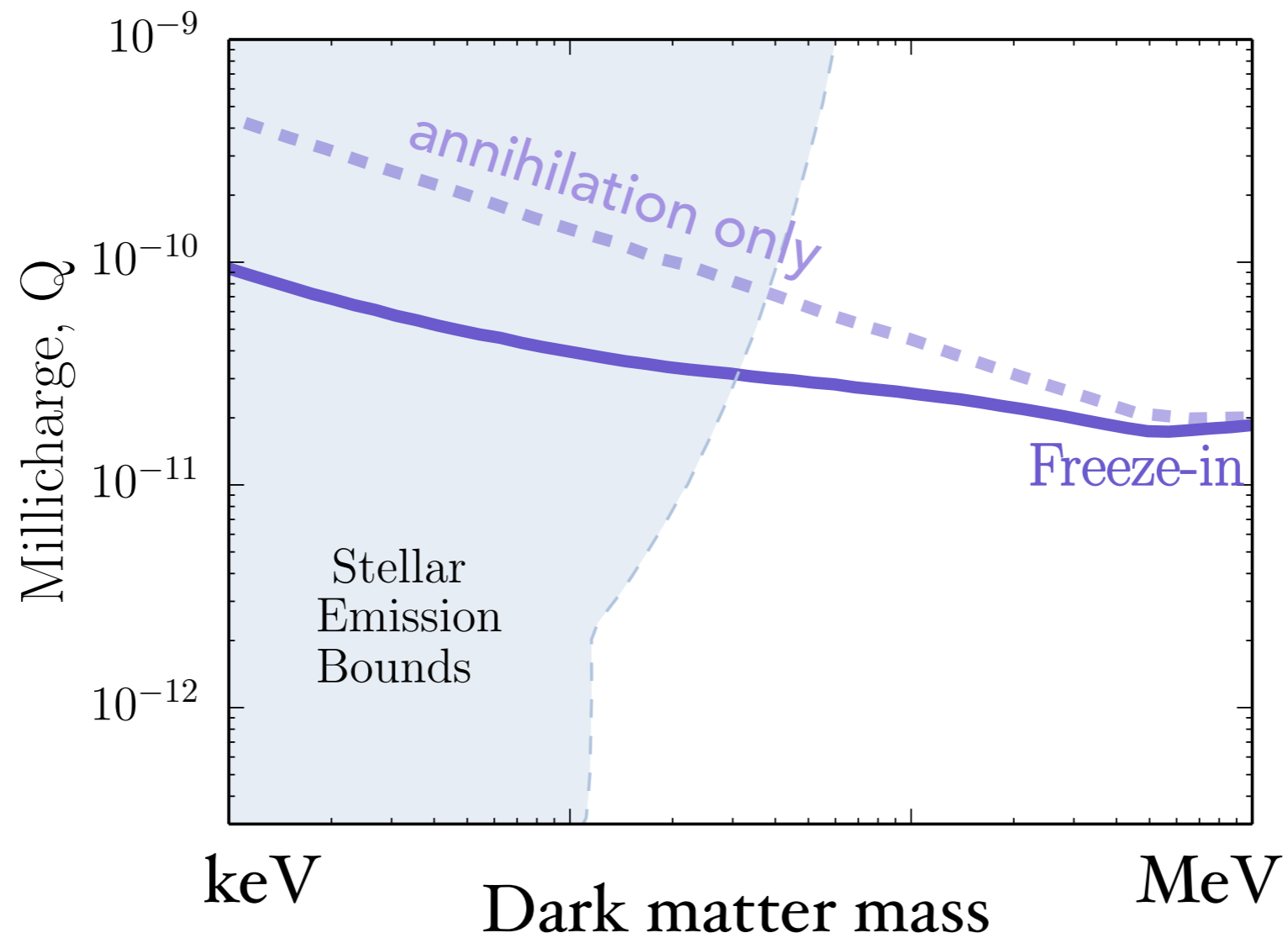
Freeze-in

$$m_\chi = 400 \text{ keV}$$

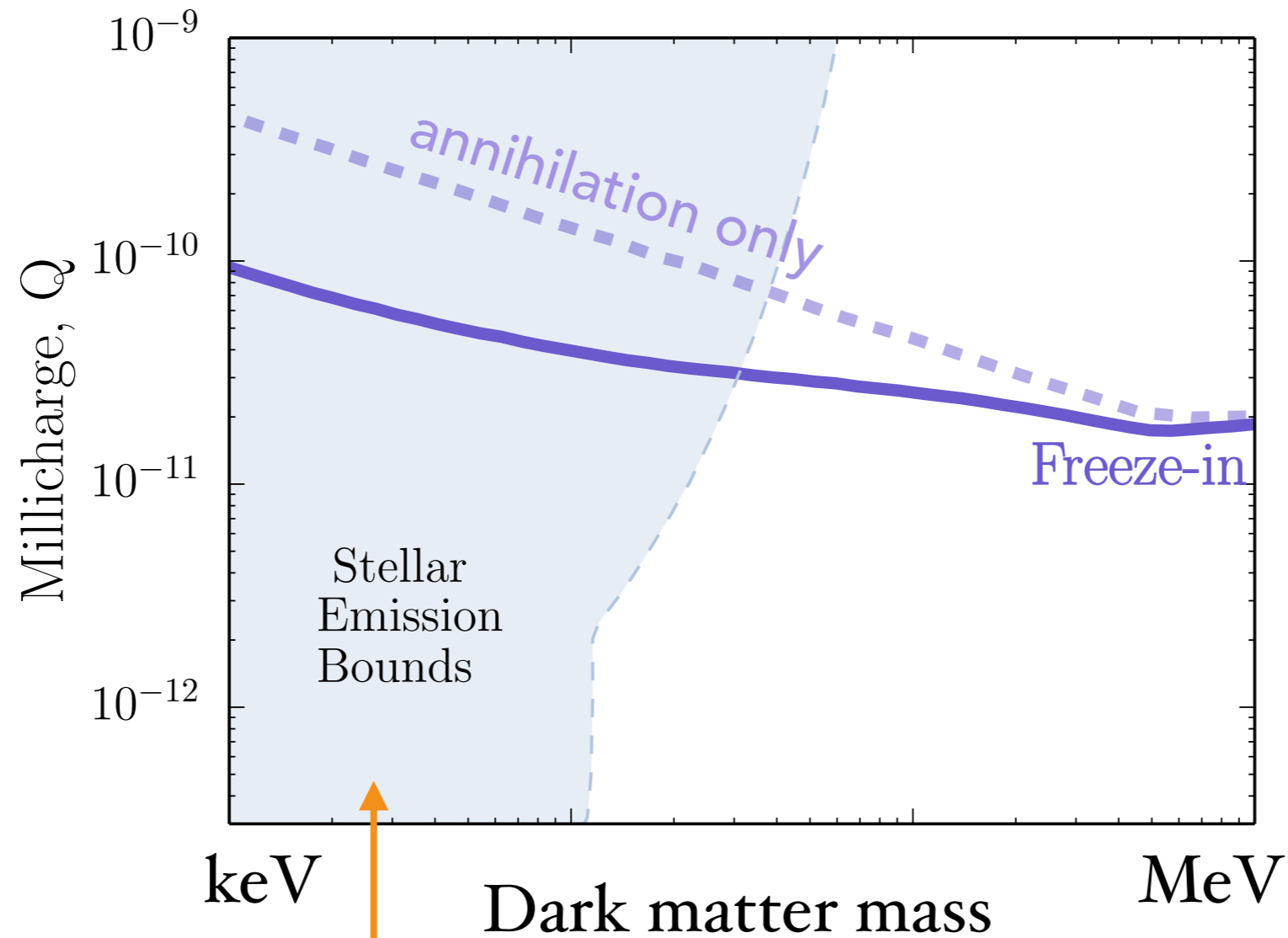


Plasma effects most important for lower DM masses
since $\omega_p \approx 0.1 k_B T$

Sub-MeV freeze-in DM



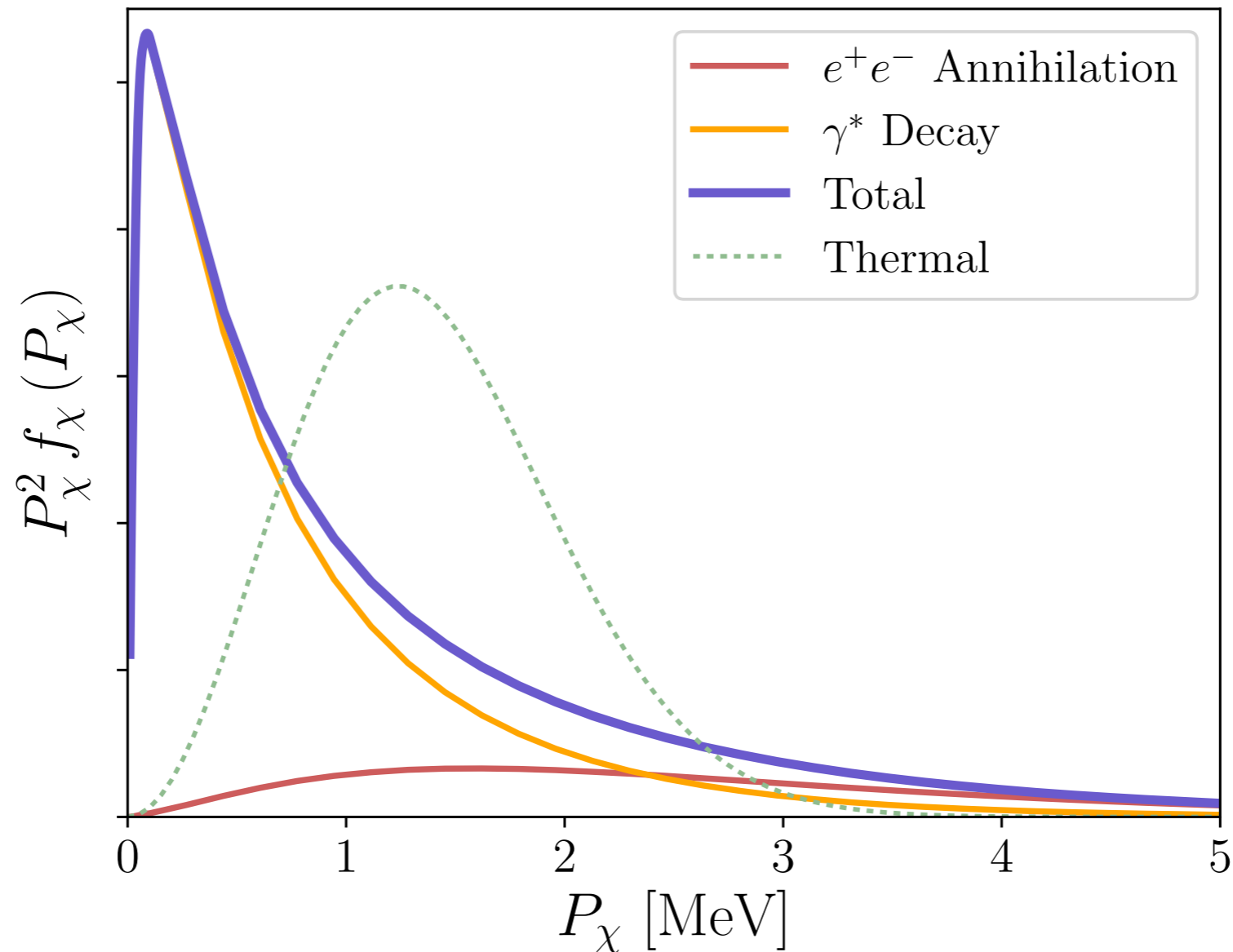
Sub-MeV freeze-in DM



Stellar bounds from Vogel and Redondo 2013; High mass part sensitive to temps, models

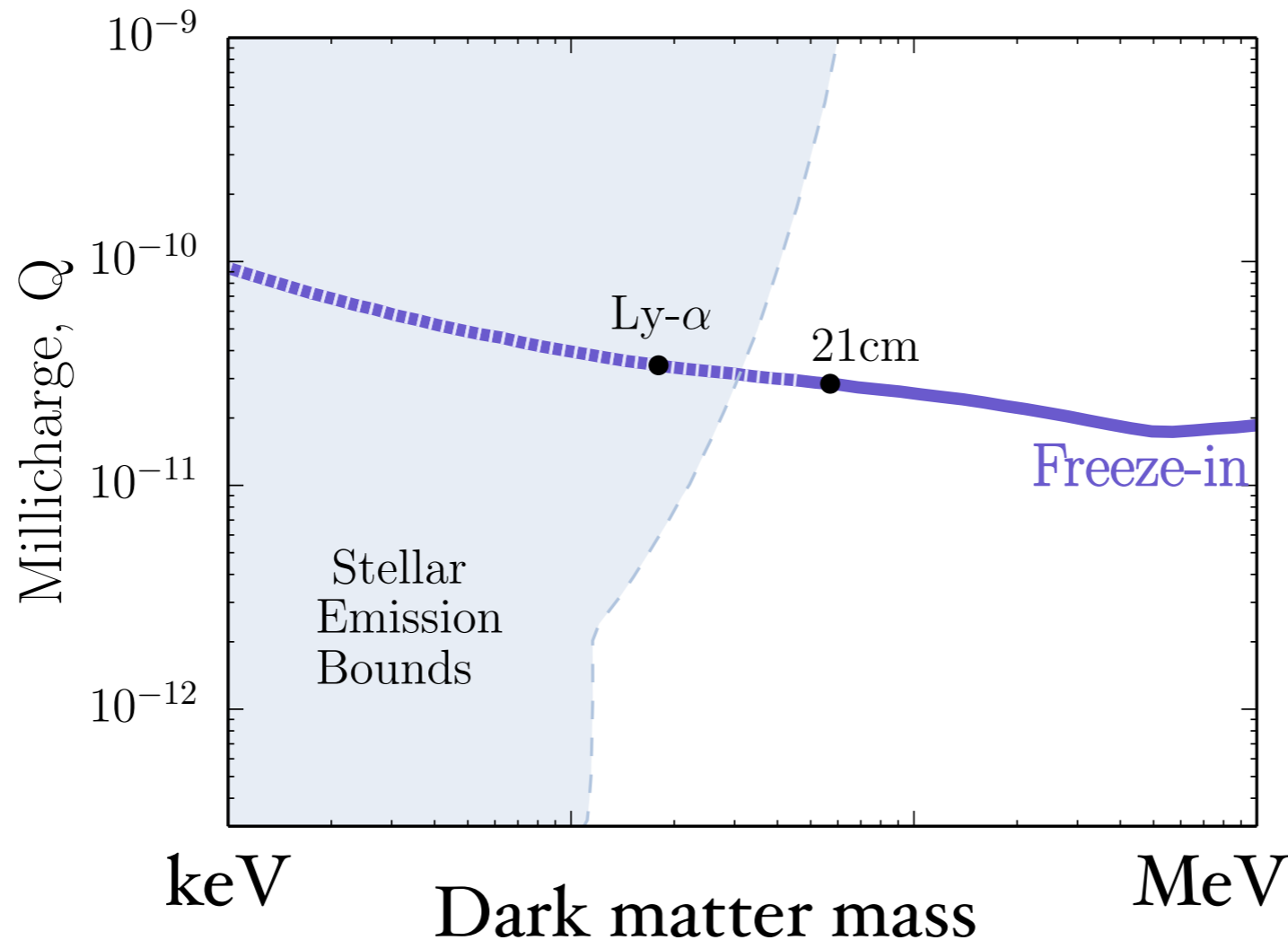
Dark matter phase space

$$m_\chi = 40 \text{ keV}$$



Dark matter is produced hot, but with highly non thermal phase space

Free-streaming of freeze-in DM

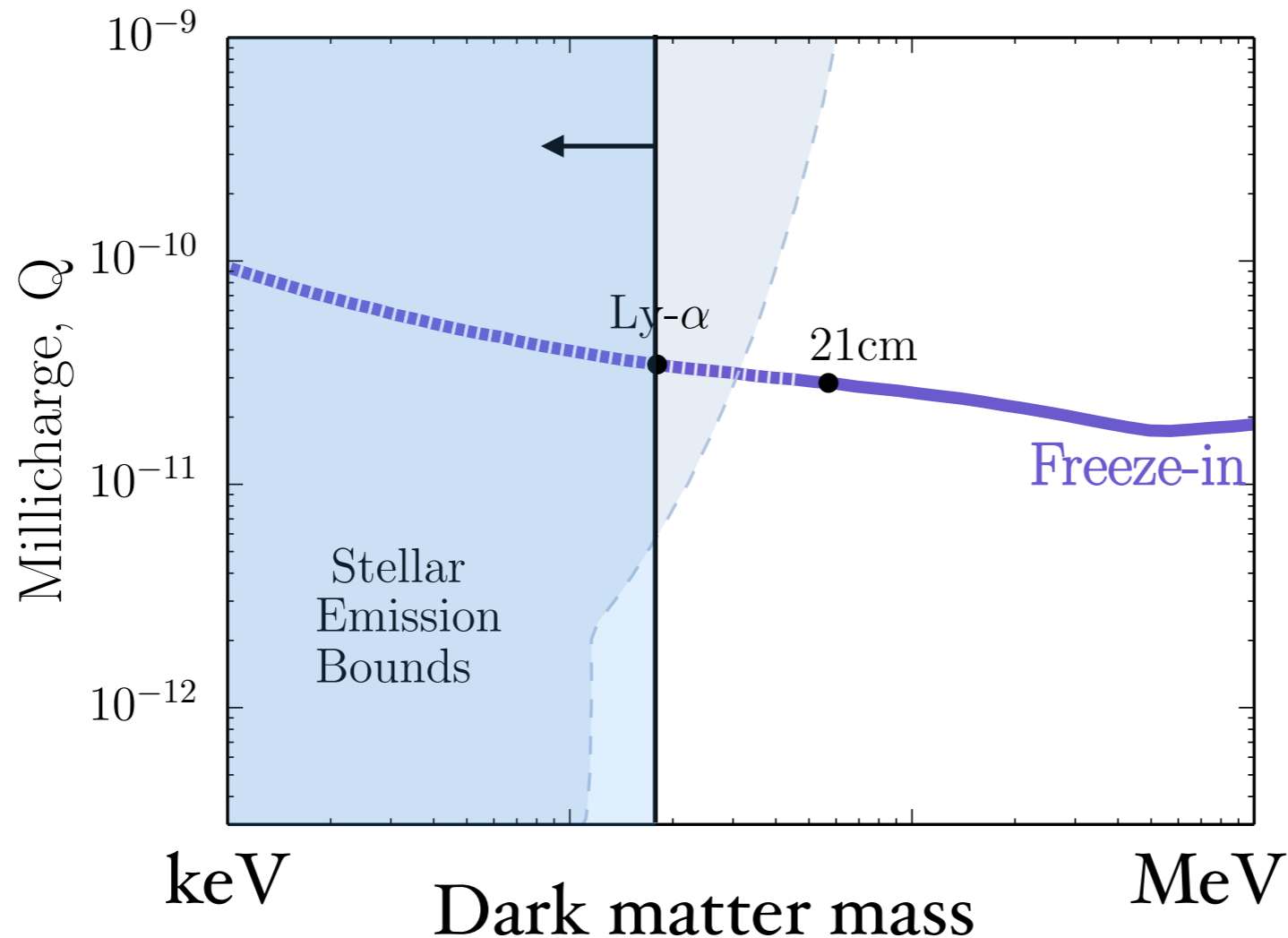


Lyman- α bound:
Yeche et al. 2017
21cm projection:
Sitwell et al. 2013

Bounds for non thermal DM distribution.

Sensitivity improves by $O(30\%)$ for DM with dark photon self-interactions

Free-streaming of freeze-in DM

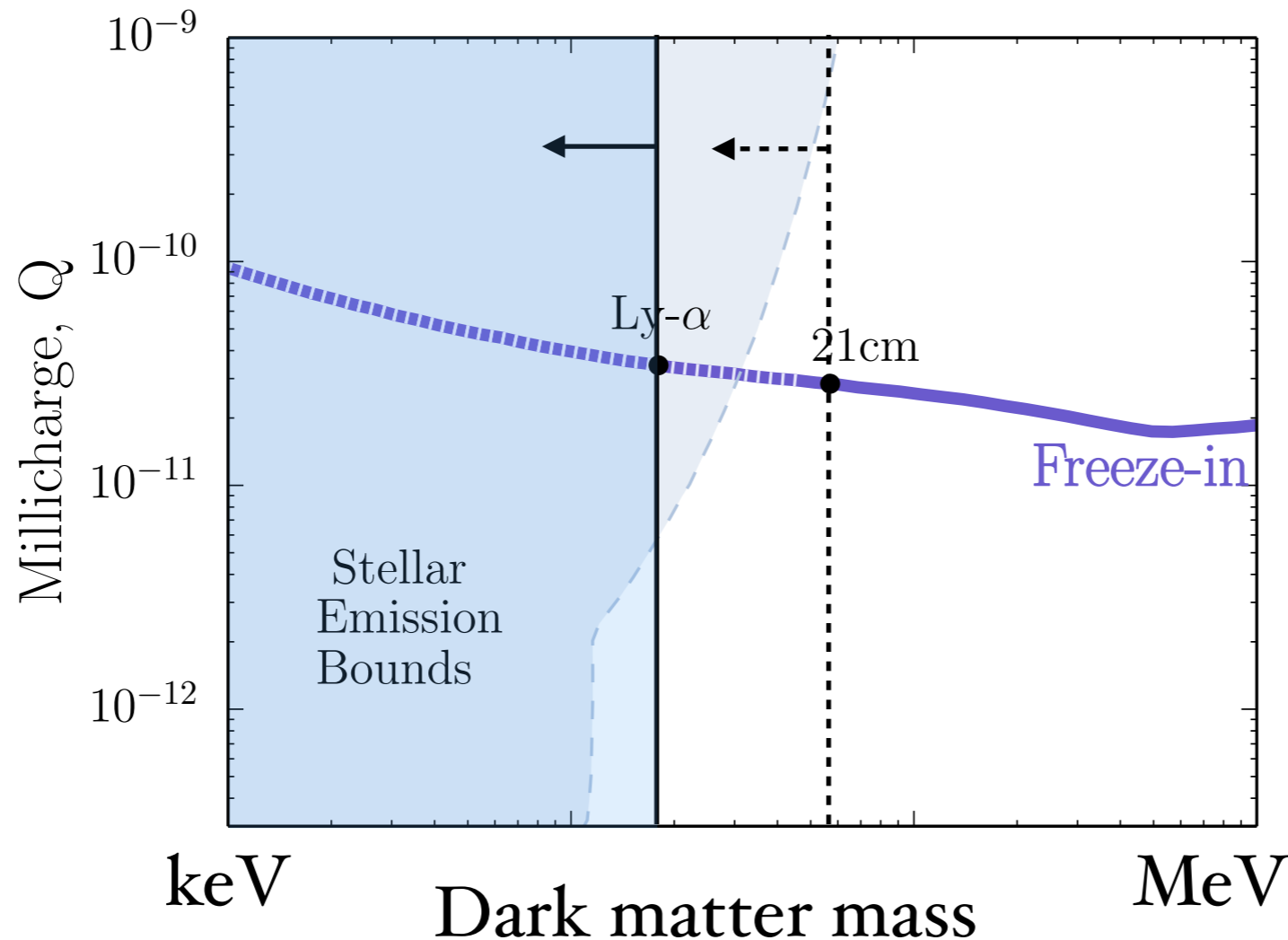


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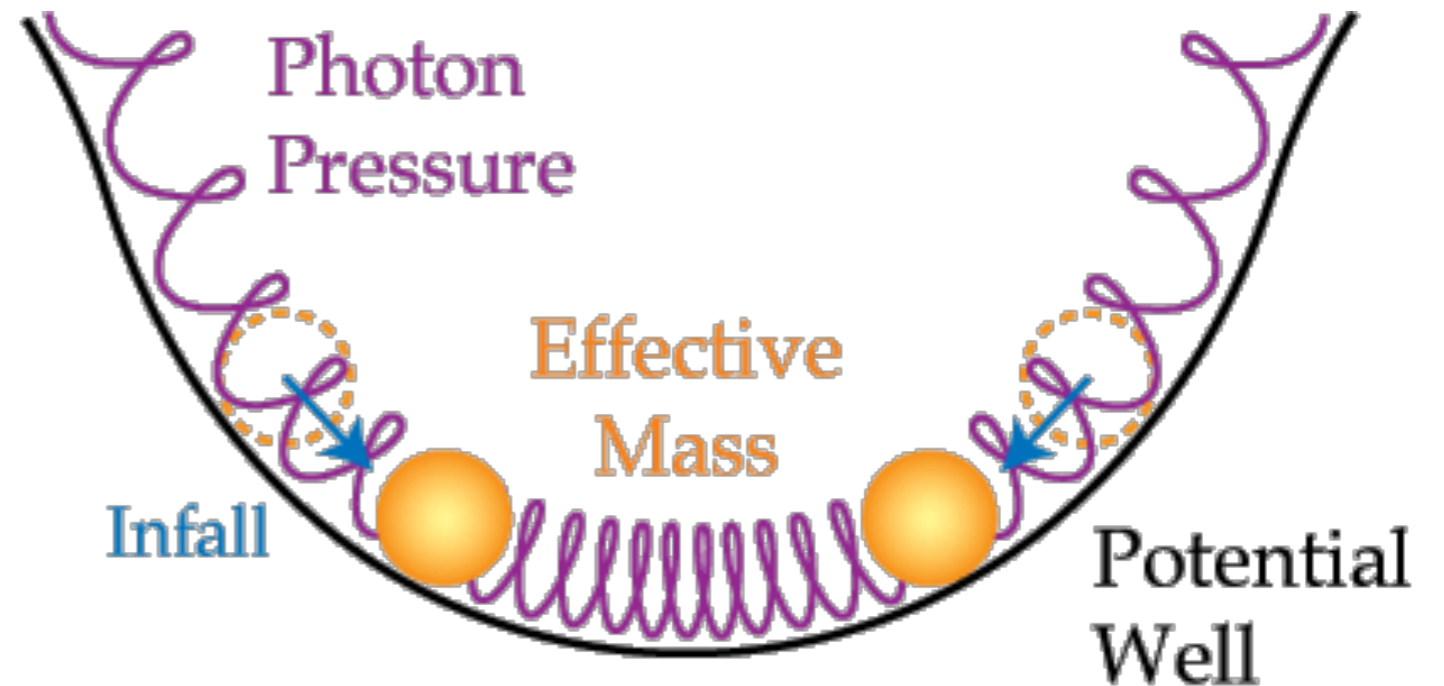
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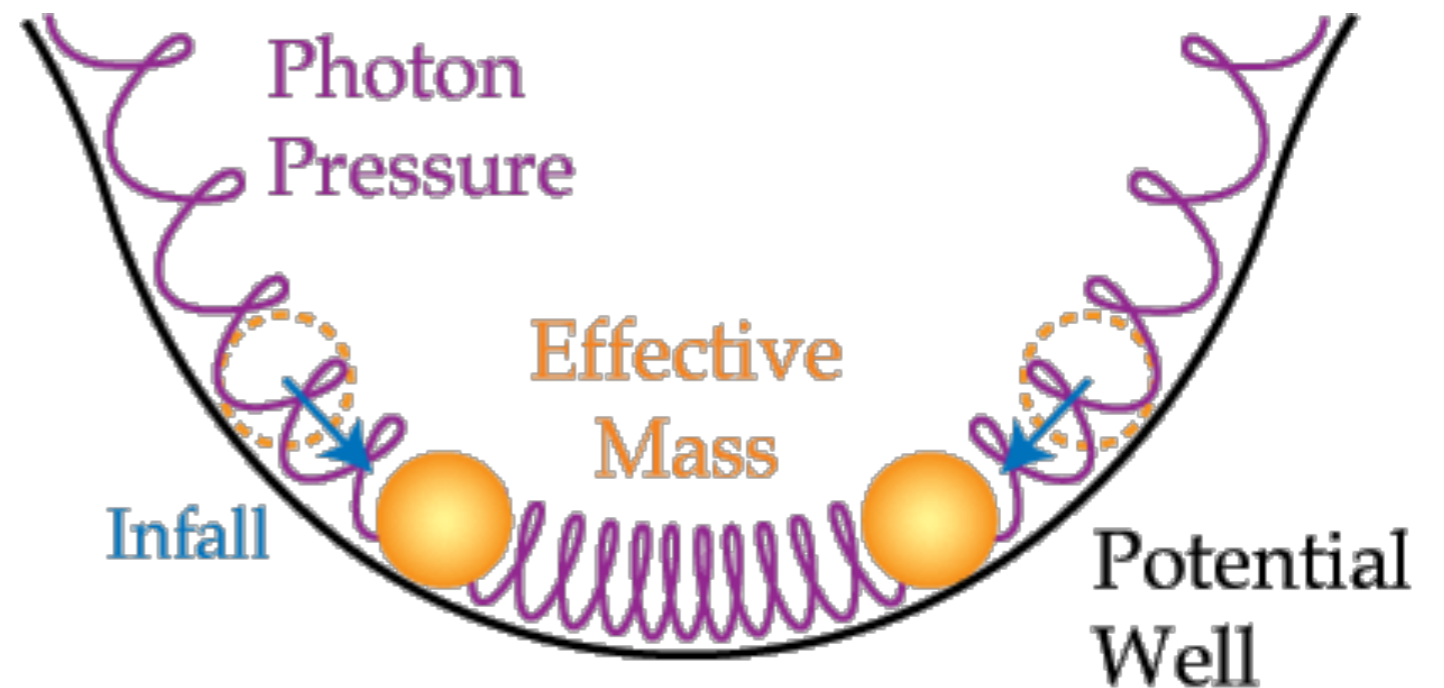
Acoustic oscillations

Dark matter is a cold and clumpy fluid, while the baryon-photon fluid oscillates in and out of the gravitational potential.



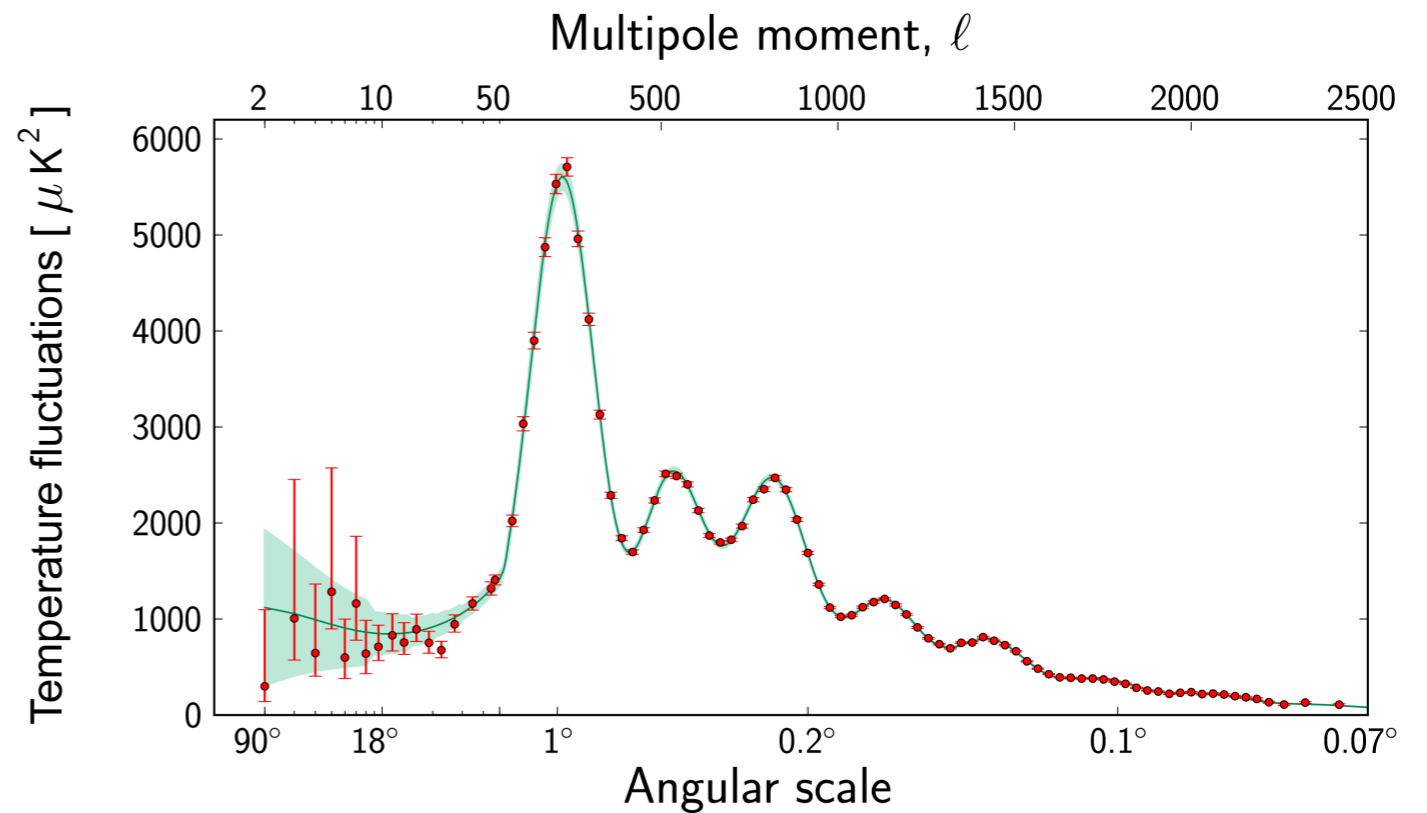
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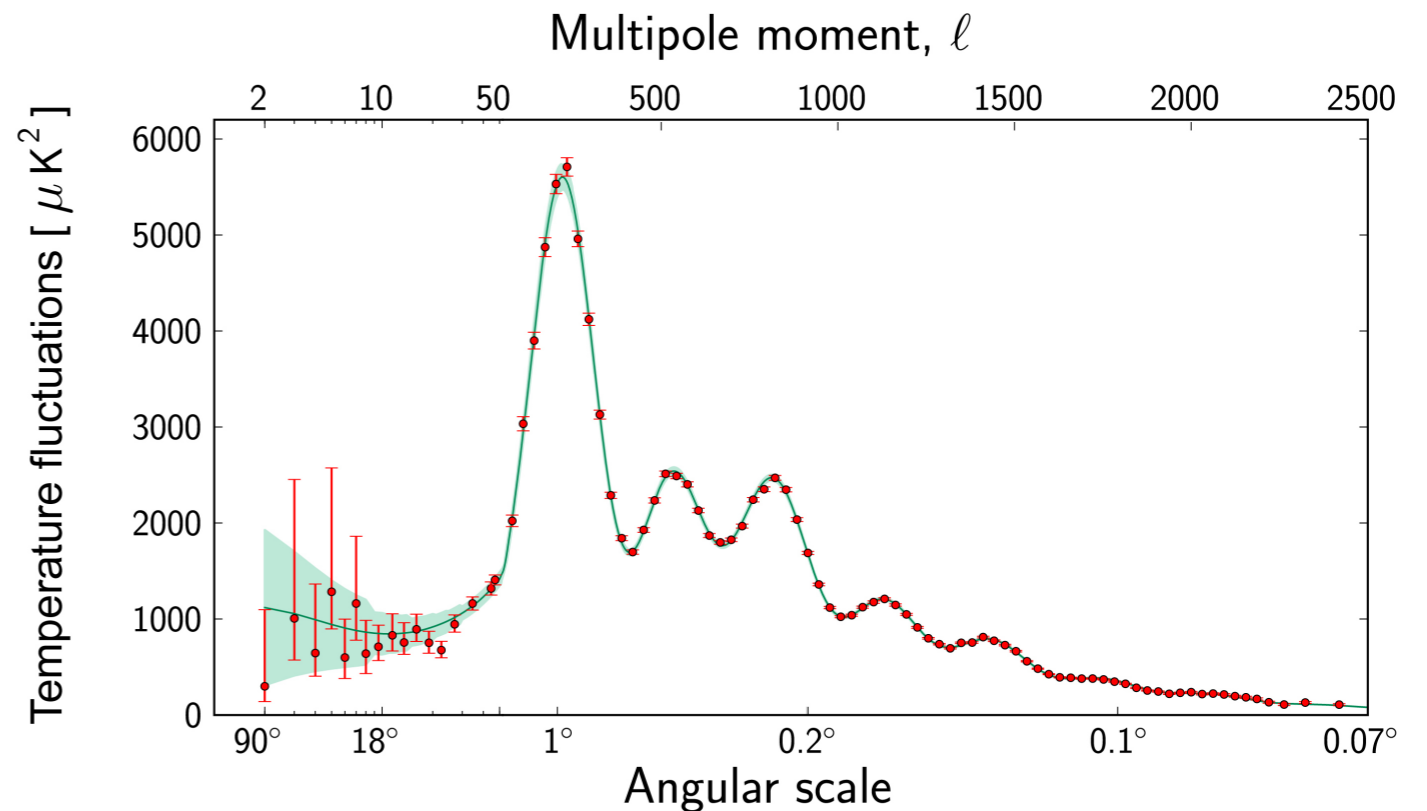


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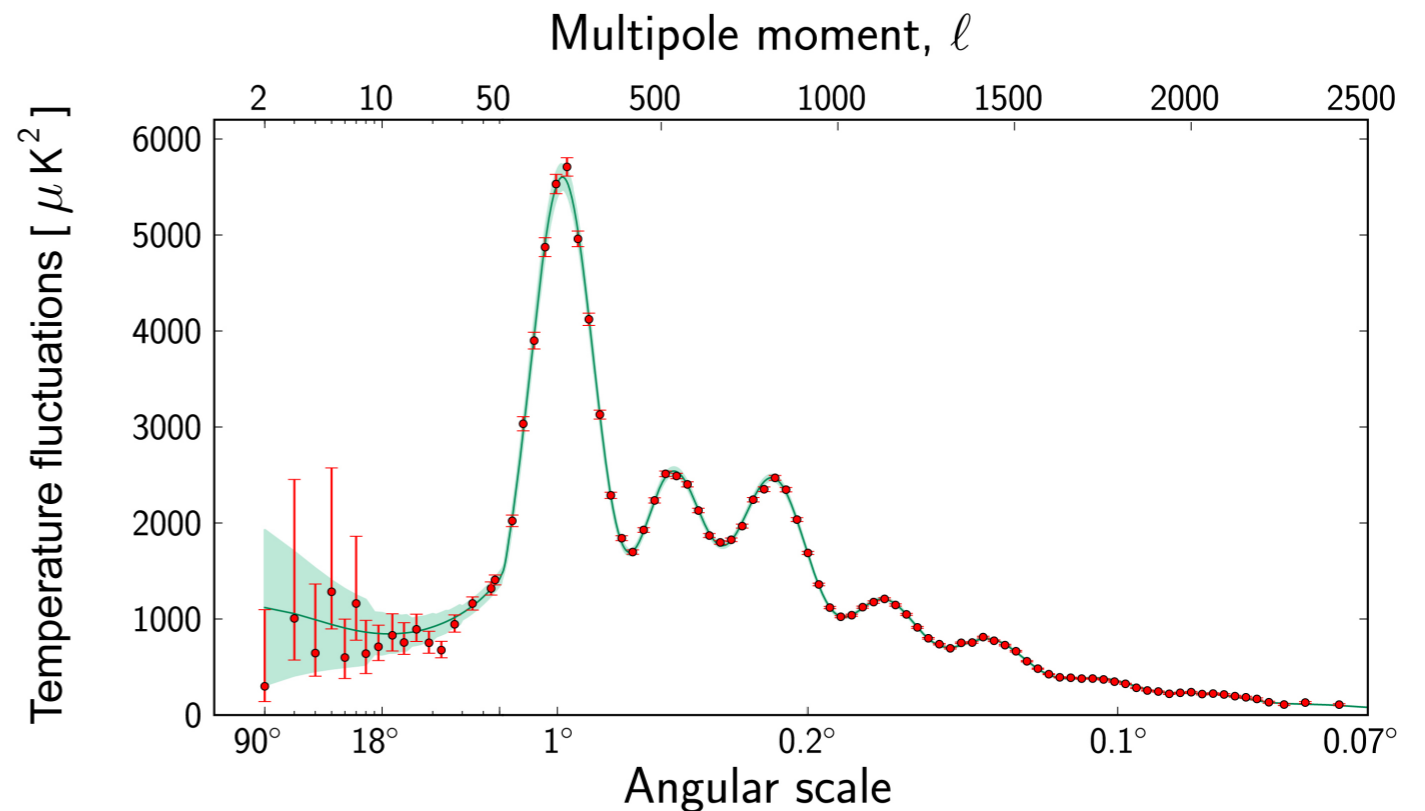
Momentum transfer cross section $\sigma_T \propto \frac{\pi Q_\chi^2 \alpha^2}{m_{\text{DM}}^2 v^4}$

Drag rate between bulk fluid motions $\approx n_b \sigma_T v_{\text{rel}}$



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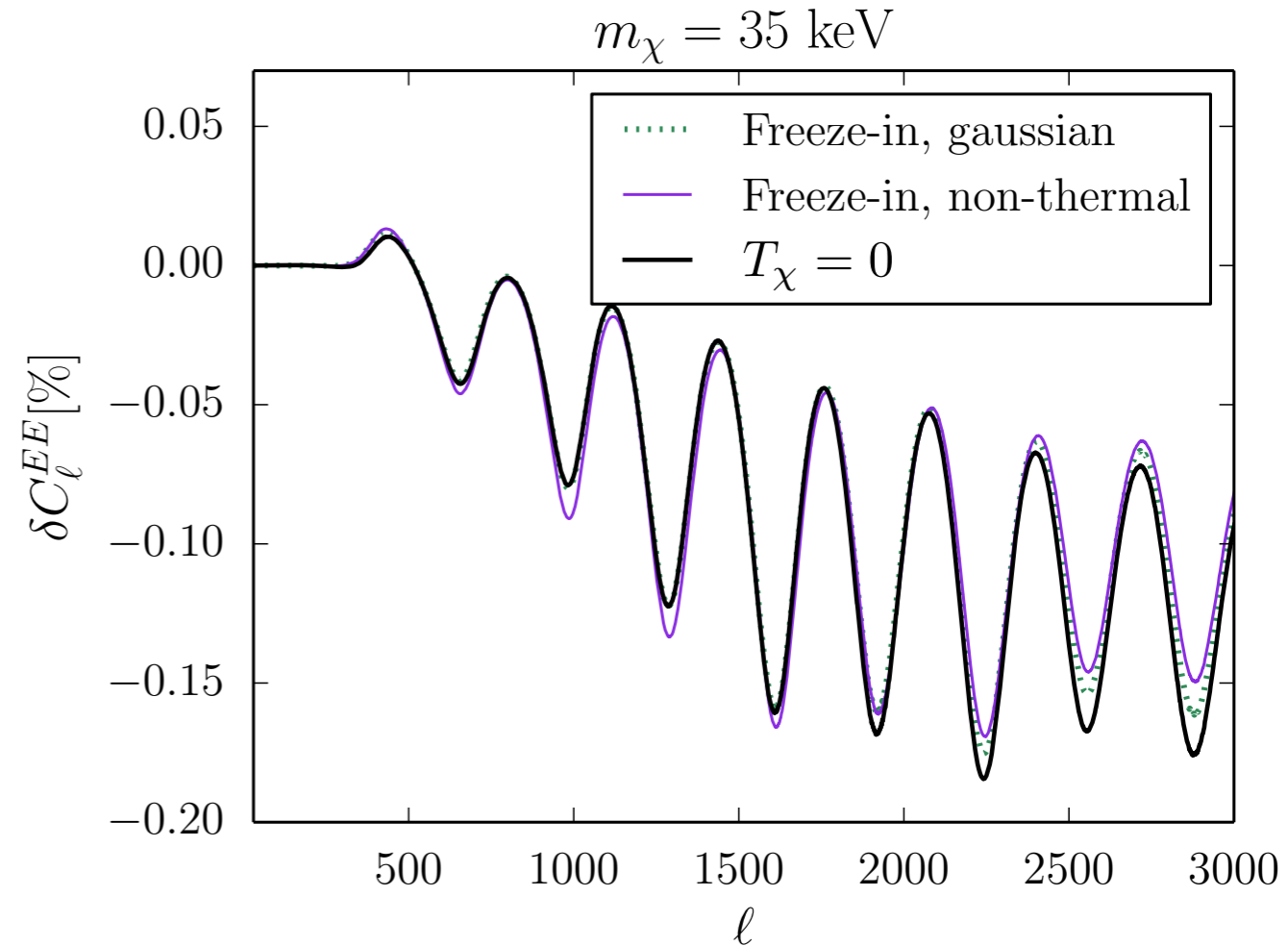
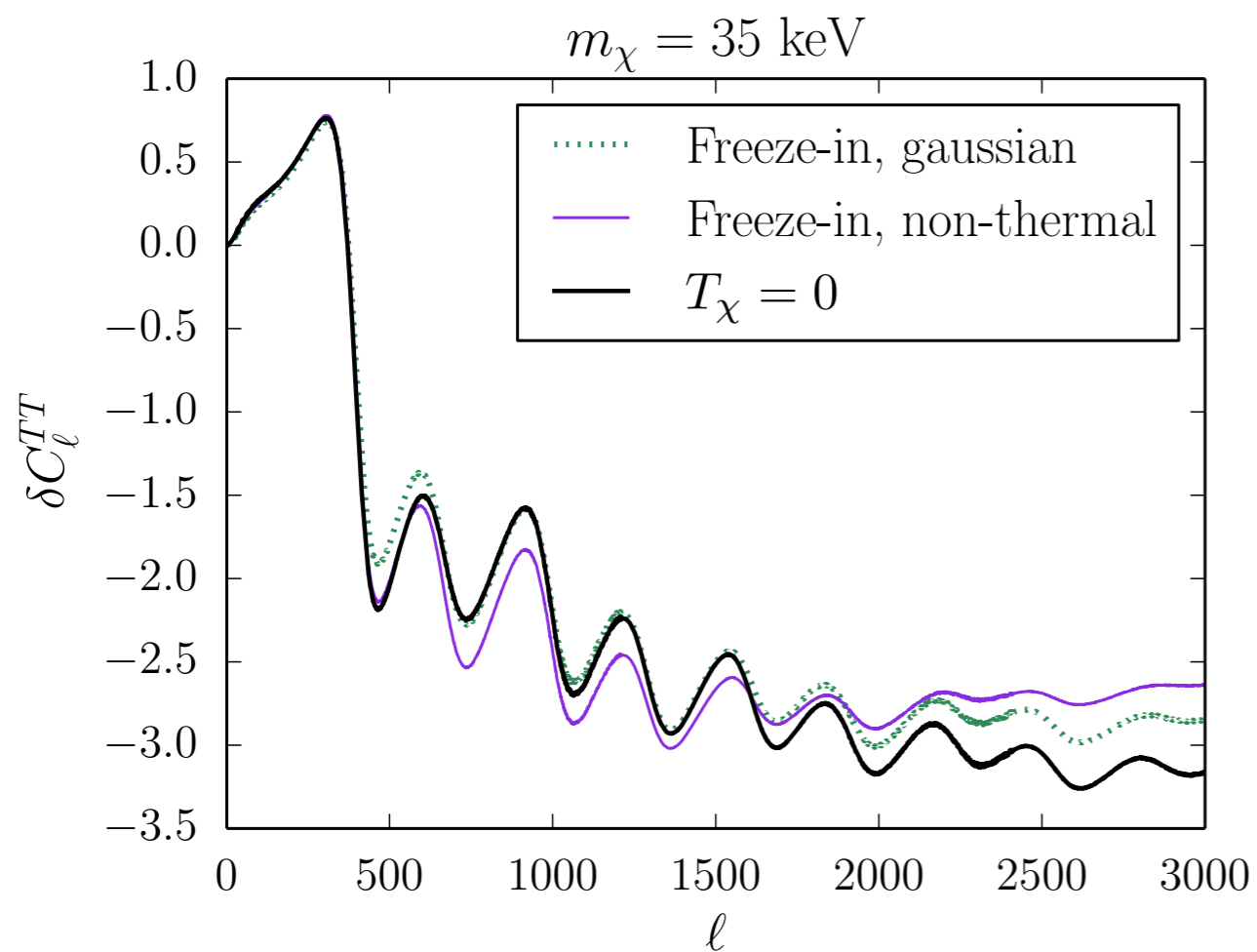


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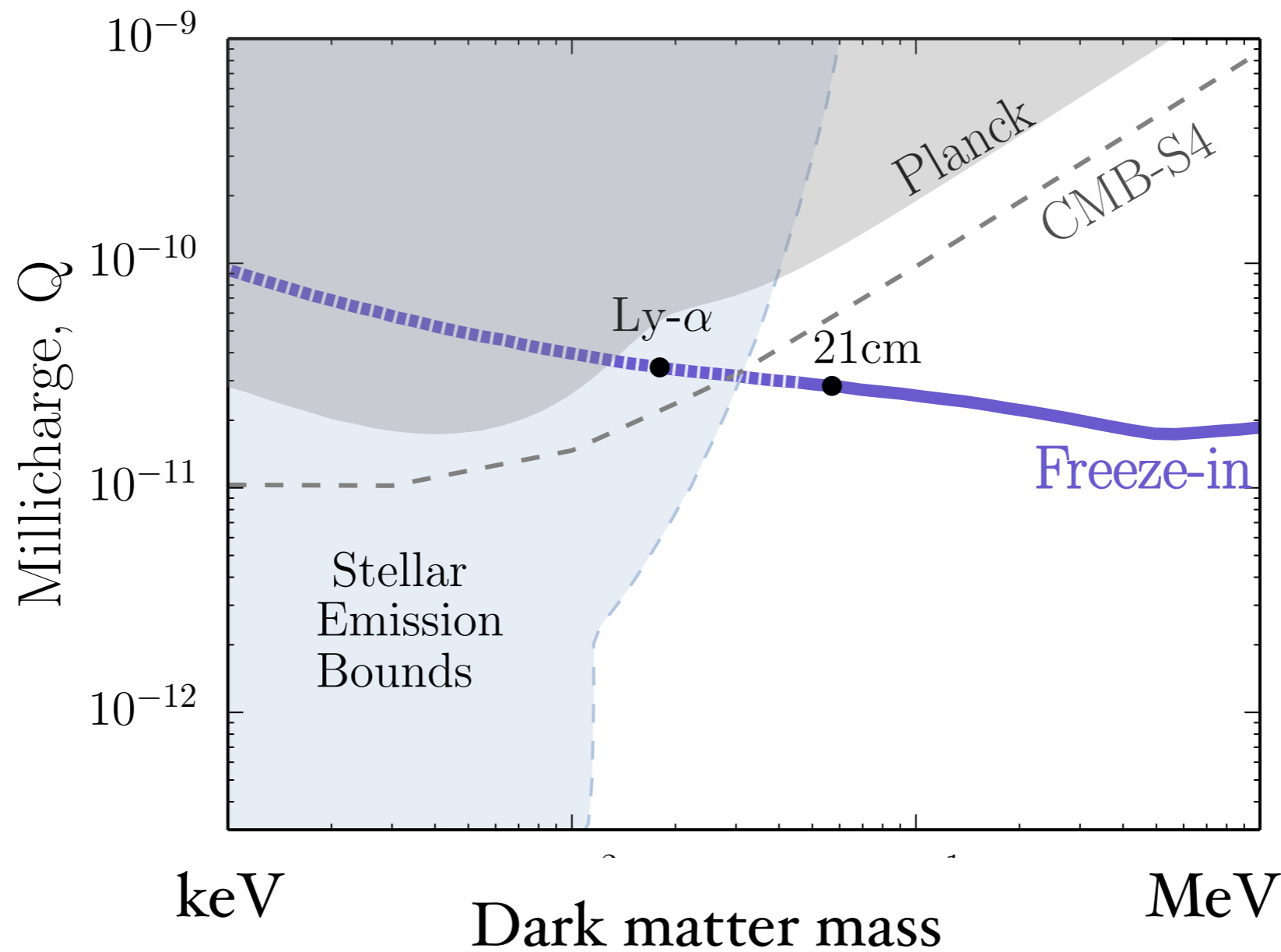
Extra DM-baryon drag force changes the characteristic size of sound waves in the baryon-photon fluid → modify CMB peaks

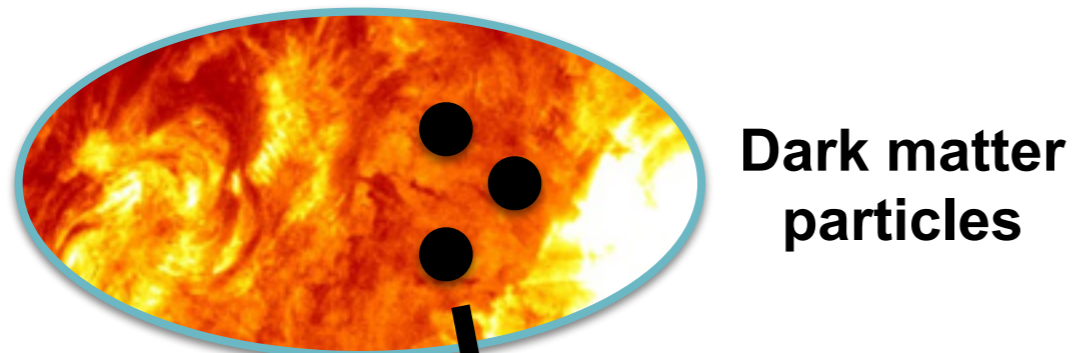
Effect on CMB anisotropies



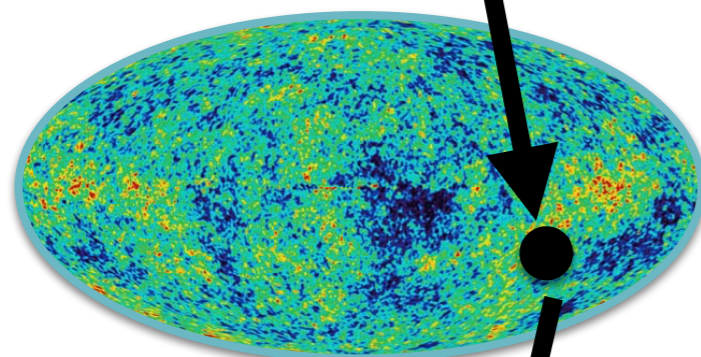
Drag force leads to
damped perturbations, shifted peaks

Using the CMB as a cosmic detector for dark matter scattering

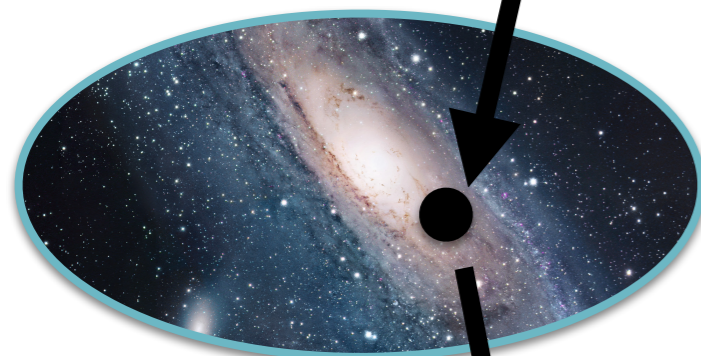




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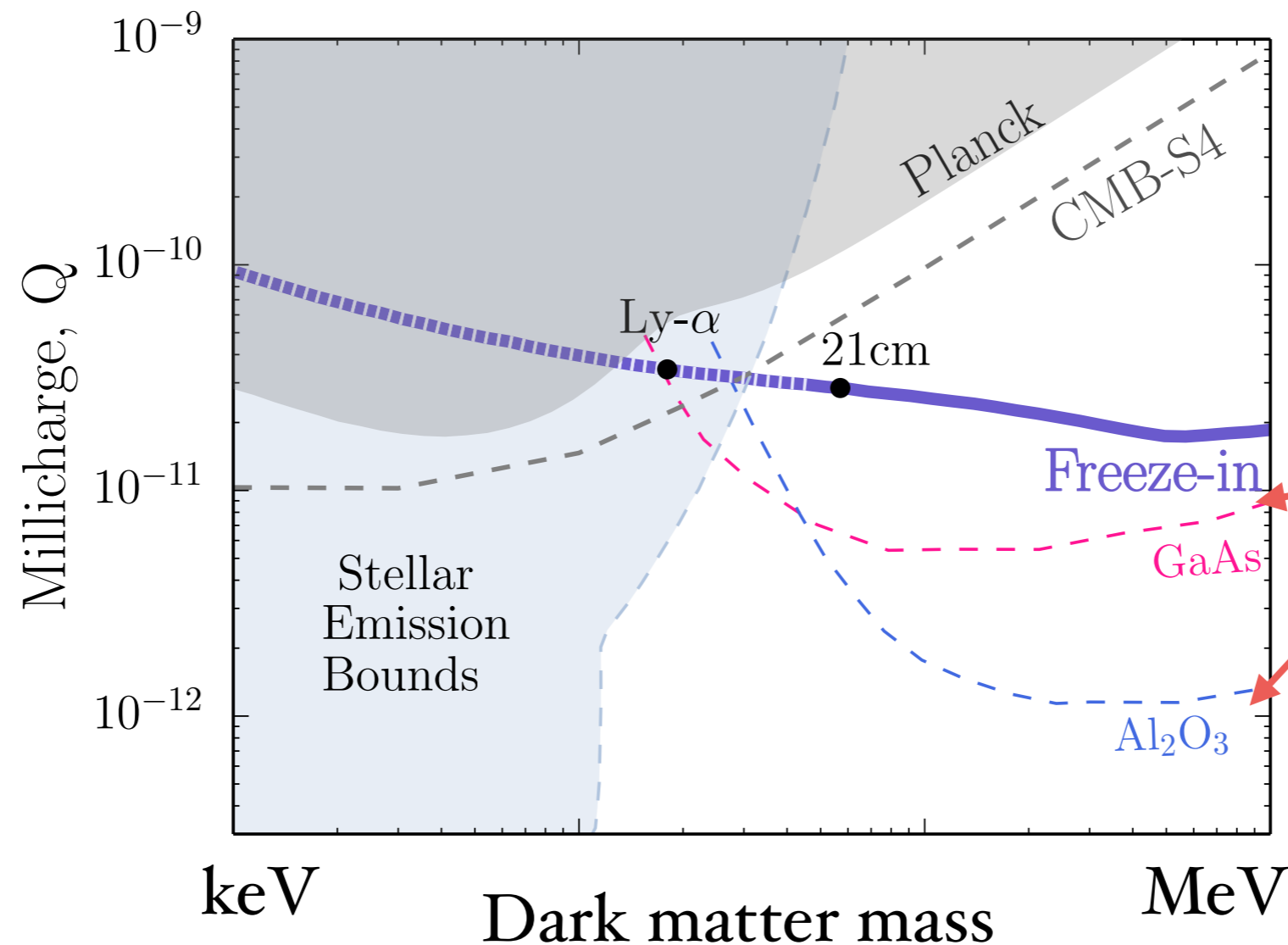


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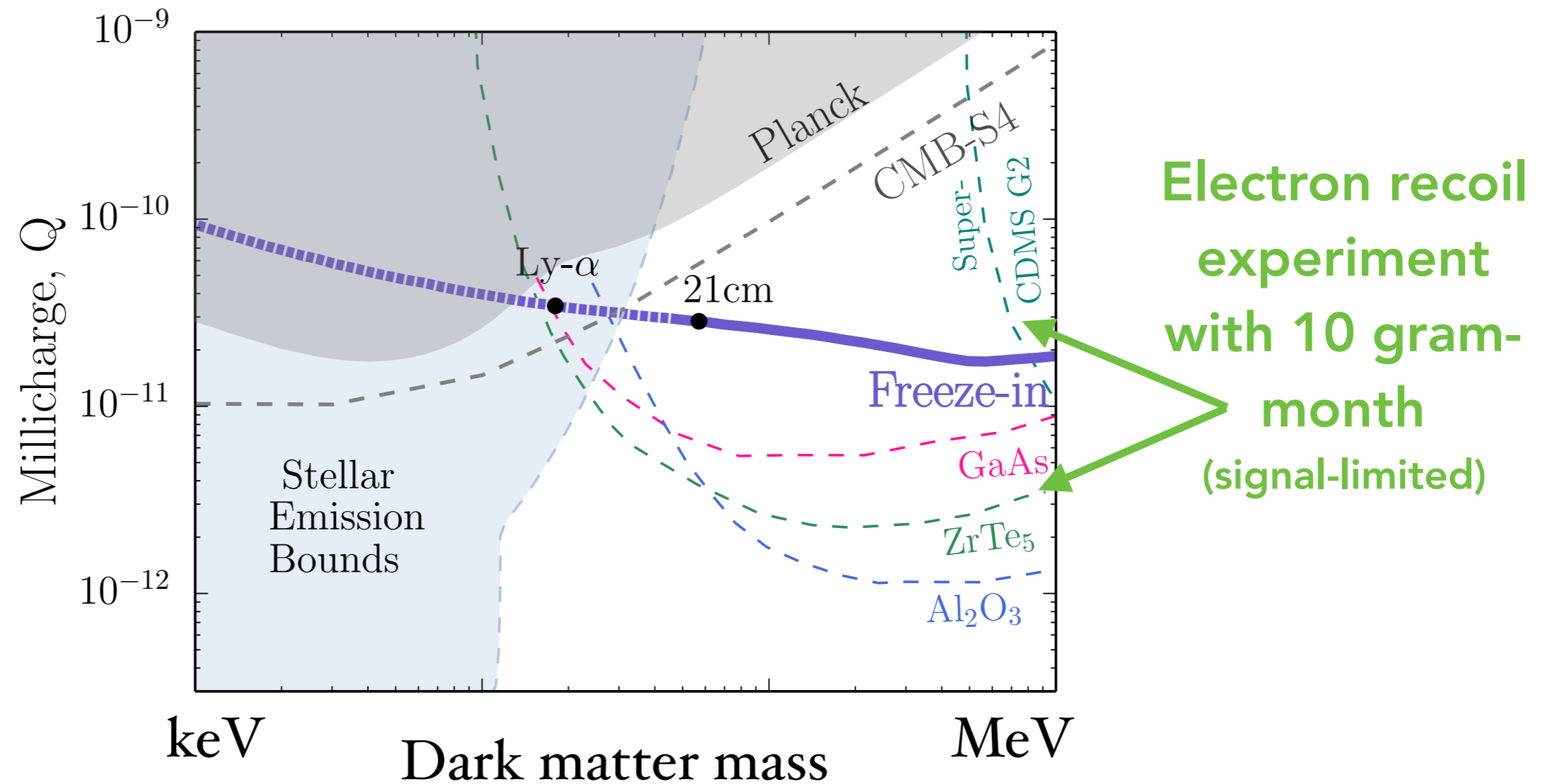
Direct detection of freeze-in DM



Phonon-based
experiment
with 10 grams
running for
1 month
(signal-limited)

DM-induced optical phonon excitations in polar crystal targets

Direct detection of freeze-in DM



Electron scattering in materials with small electron band gap

Summary

Simplest scalar & vector dark sector portals give rise to direct detection signatures for $m_X > \text{MeV}$.

We learned “The Standard Model is fragile” ... ΛCDM is also fragile! Sub-MeV dark matter faces cosmological constraints.

For $m_X < \text{MeV}$, the most compelling scenario is freeze-in through an ultralight vector mediator. Fortunately, this can be tested with a combination of methods in cosmology and in the lab.