

25th International Summer Institute on Phenomenology of  
Elementary Particle Physics and Cosmology (SI 2019)  
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**Entropy production from decay**  
**of the GeV scale right-handed neutrinos**  
**and the primordial gravitational wave**

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In preparation

**NiiGATA**  
**UNIVERSITY**

# Outline

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- 1. Introduction**
- 2. Entropy production**
- 3. Primordial gravitational wave**
- 4. Summary**

# GeV scale right-handed neutrinos

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- **Seesaw mechanism that can explain tiny neutrino masses**

Minkowski '77 Yanagida '79 Gell-mann, Ramona, Slansky '79 Glashow '79

- **Baryogenesis via neutrino oscillation**

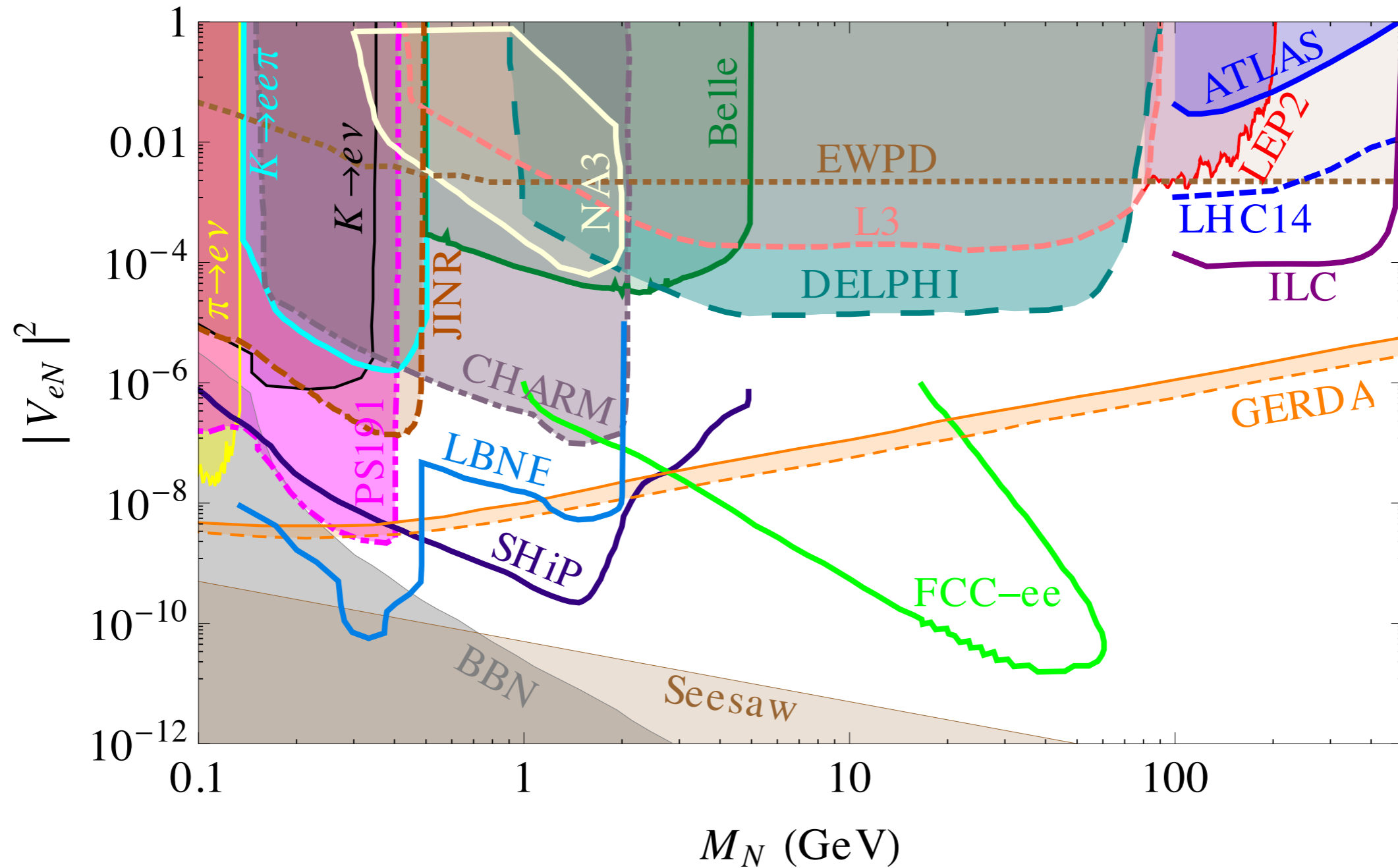
Akhmedov, Rubakov, Smirnov '98 Asaka, Shaposhnikov '05

- **Testability**

F.F.Deppisch, P.S.Bhupal Dev, A.Pilaftsis '15

# HNL search

F.F.Deppisch, P.S.Bhupal Dev, A.Pilaftsis '15



# Motivation

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**Are there any other methods  
for exploring RH neutrinos ?**

- Entropy production due to decay of RHvs that modifies the gravitational wave spectrum.

# Seesaw mechanism

## Extension by right-handed neutrinos

$$\mathcal{L} = \mathcal{L}_{SM} + i\bar{\nu}_R \partial_\mu \gamma^\mu \nu_R - F \bar{L} \nu_R \Phi - \frac{M_M}{2} \bar{\nu}_R \nu_R^c + h.c.$$

## Seesaw mechanism (type I)

$$-\mathcal{L}_M = \frac{1}{2} (\bar{\nu}_L, \bar{\nu}_R^c) \begin{pmatrix} 0 & M_D \\ M_D^T & M_M \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \nu_R \end{pmatrix} + h.c. = \frac{1}{2} (\bar{\nu}, \bar{N}) \begin{pmatrix} M_\nu & 0 \\ 0 & M_M \end{pmatrix} \begin{pmatrix} \nu^c \\ N \end{pmatrix}$$

$$M_\nu = -M_D^T M_M^{-1} M_D \quad (M_\nu \ll M_D)$$

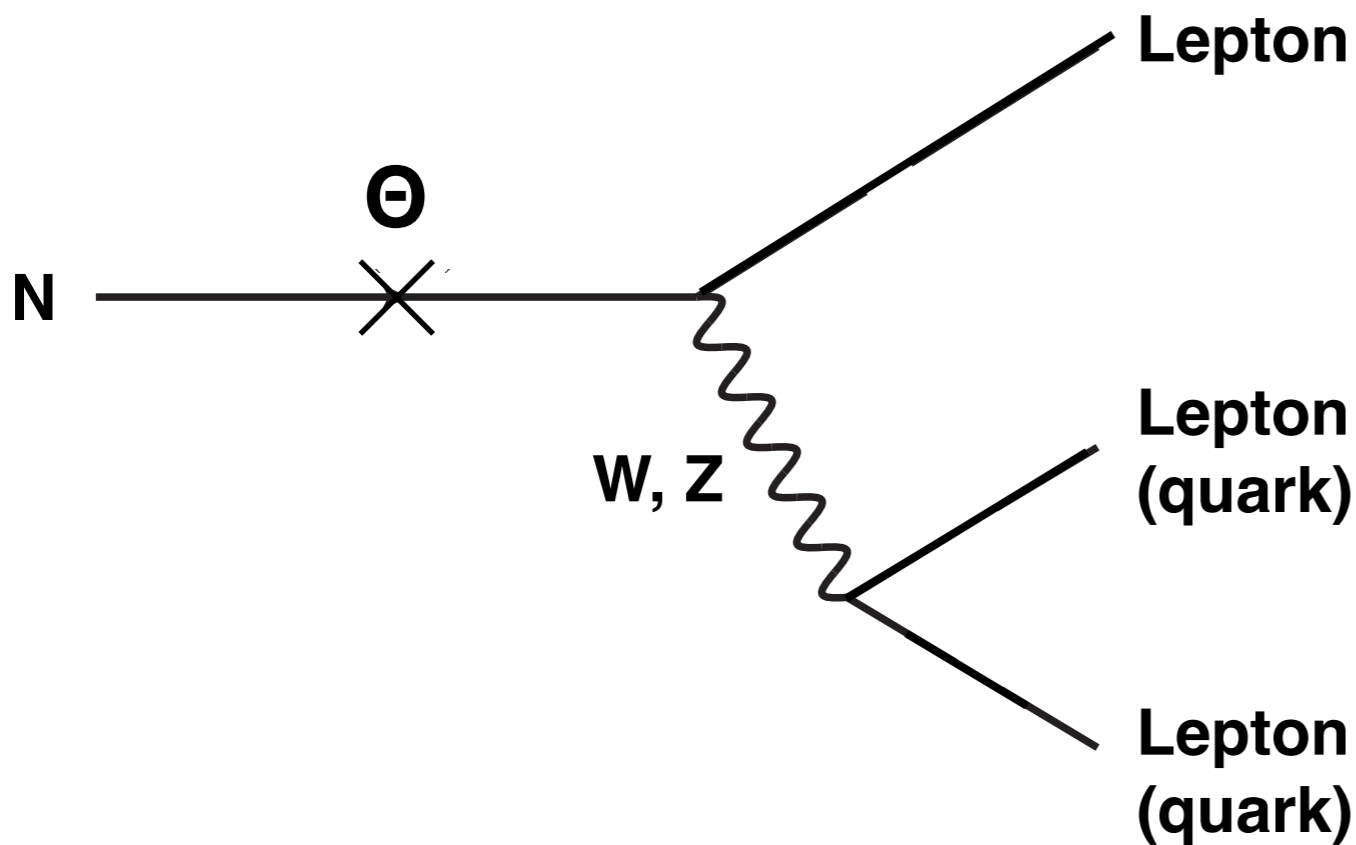
## Mixing of light neutrinos and heavy neutrinos

$$\nu_L = U \nu + \Theta N^c$$

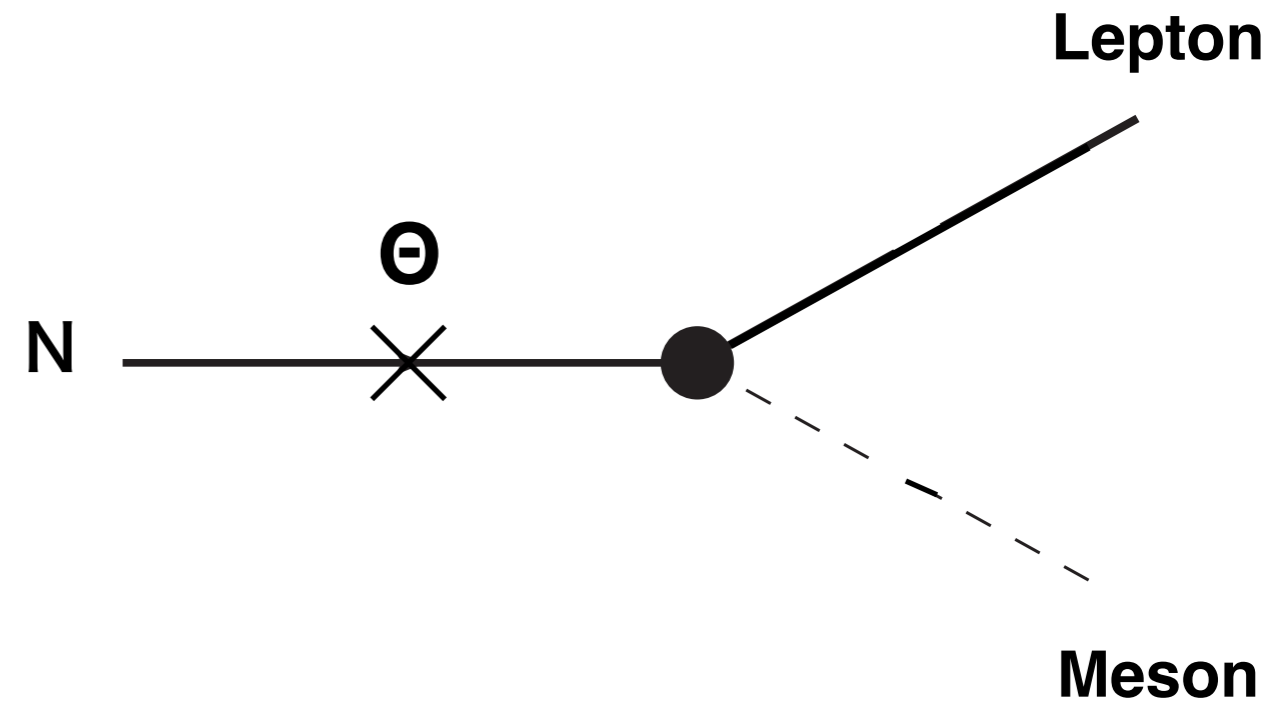
$$\Theta = \frac{M_D}{M_M} = \frac{F \langle \Phi \rangle}{M_M}$$

# Decay of right-handed neutrinos

## 3 Body decay



## 2 Body decay



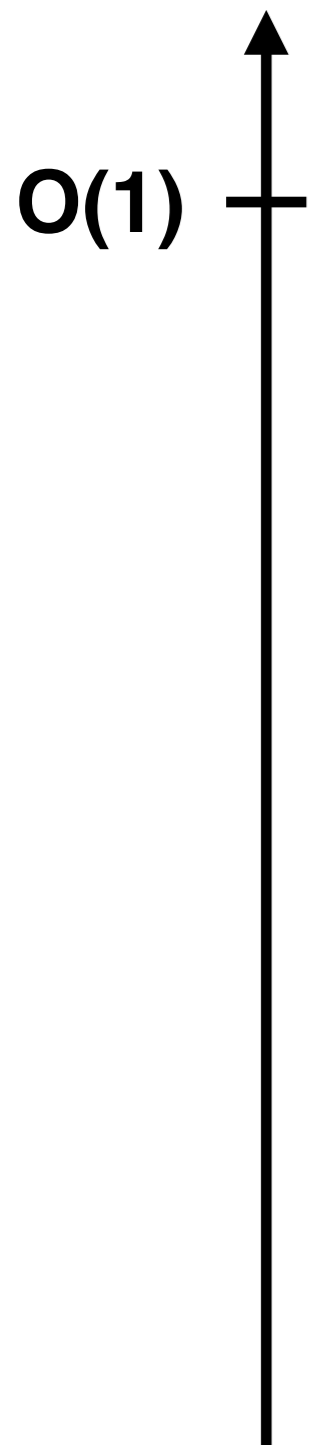
Lifetime can be  
 $\tau \sim O(0.1)$  sec

@  $M = 1$  GeV

✧ near BBN bound

# Scenario

Temperature [GeV]



▶  $T = T_{\text{dec}}$

**RHv decouples from thermal equilibrium ( $\Gamma_N < H$ ).**

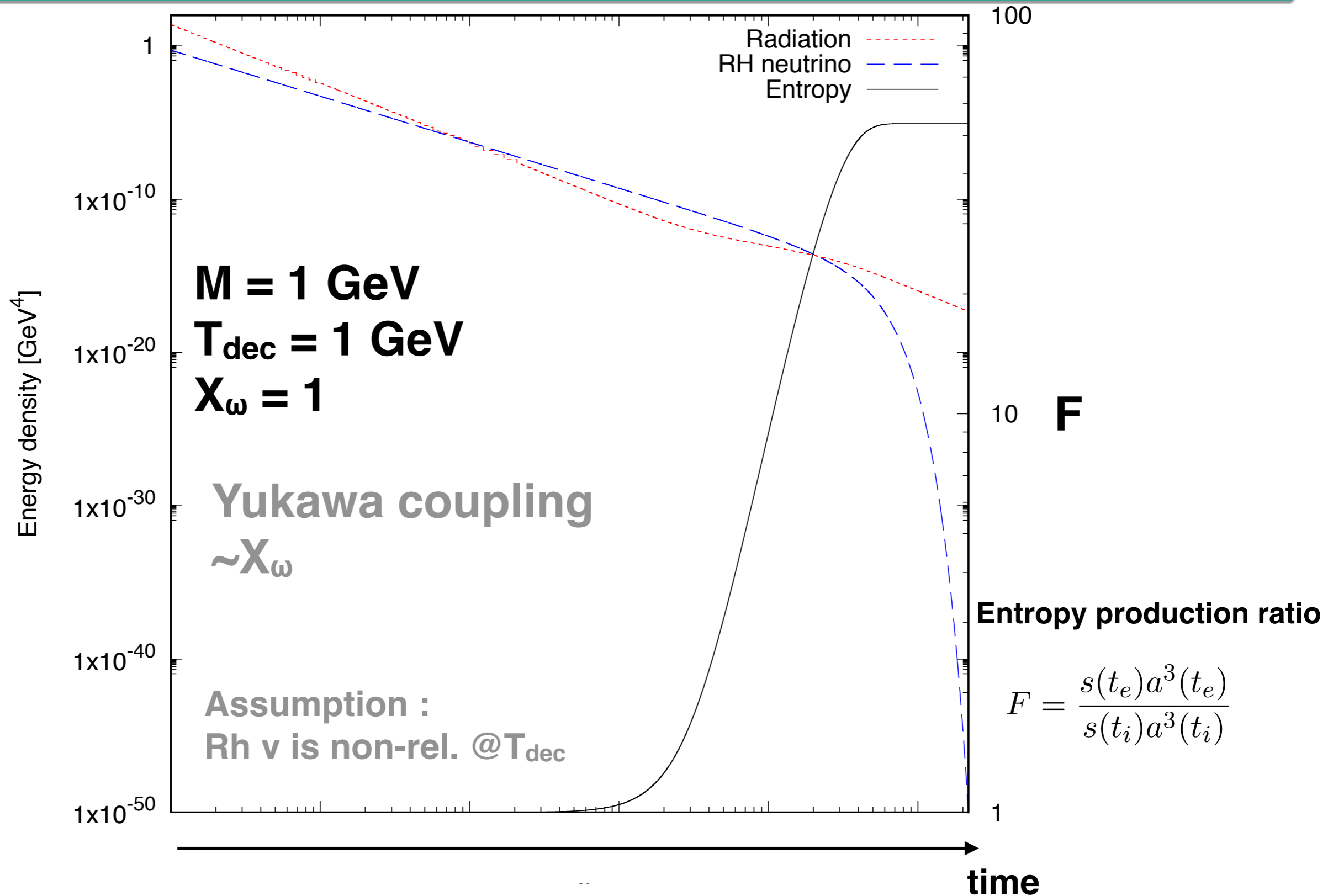
**The number of RHv will freeze out.**

**RHv will decay.**

**If RHv is non-relativistic particles with sufficient lifetime and the energy density of RHv dominates the universe, the entropy production occurs and changes the thermal history of universe.**

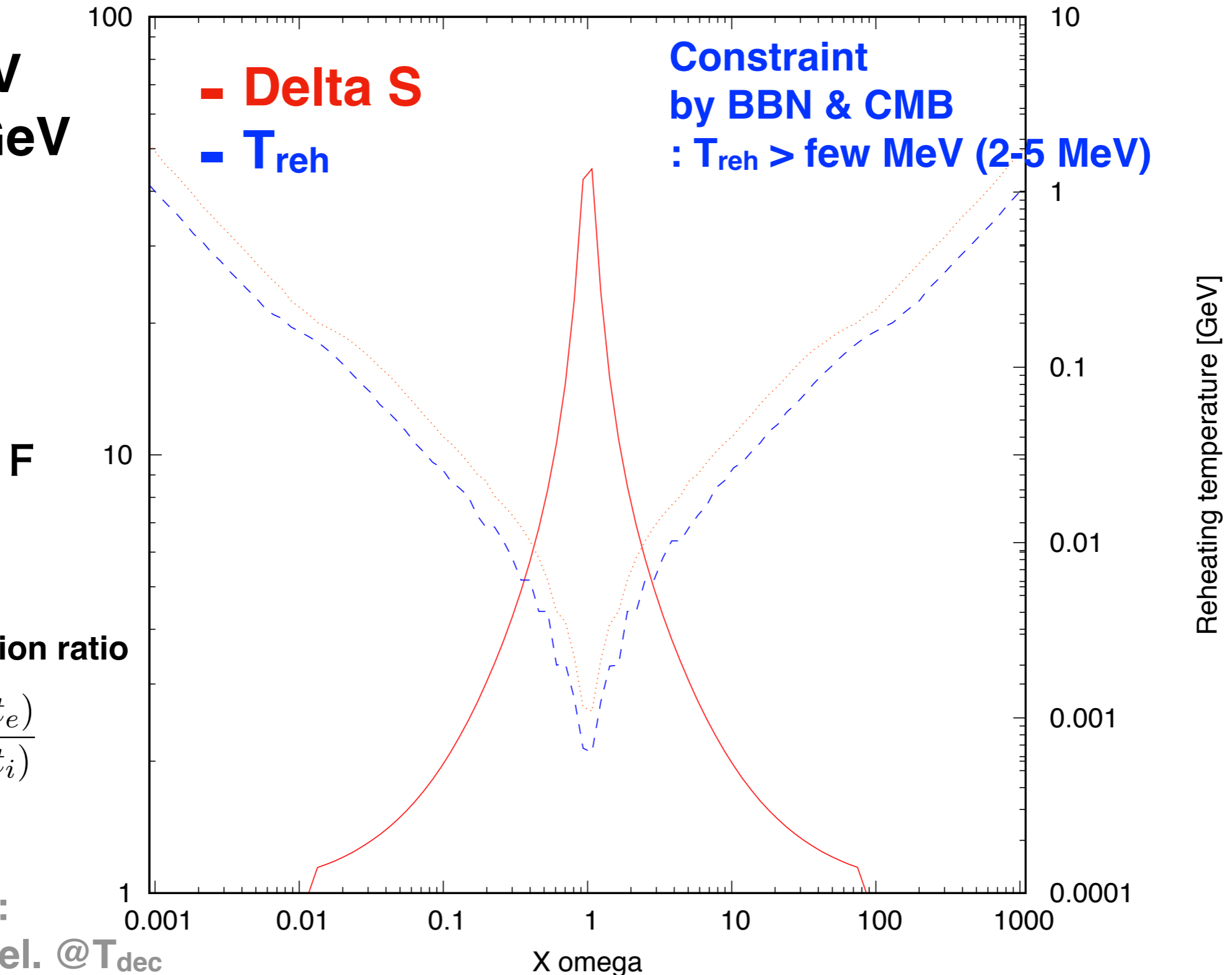


# Entropy production



# Entropy production

**M = 1 GeV**  
**T<sub>dec</sub> = 1 GeV**



# Primordial gravitational wave

$$\Omega_{GW} = \frac{1}{\rho_{cr}} \frac{d\rho_{GW}}{d \ln k}$$

$$\frac{d \ln \Omega_{GW}(f, a)}{d \ln a} = 3w(a) - 1$$

$$w = p / \rho$$

$$T \sim 3 \times 10^6 \text{ GeV}$$

$$\Gamma_X = 10^{-7} \sim 10^{-5} \text{ GeV}$$

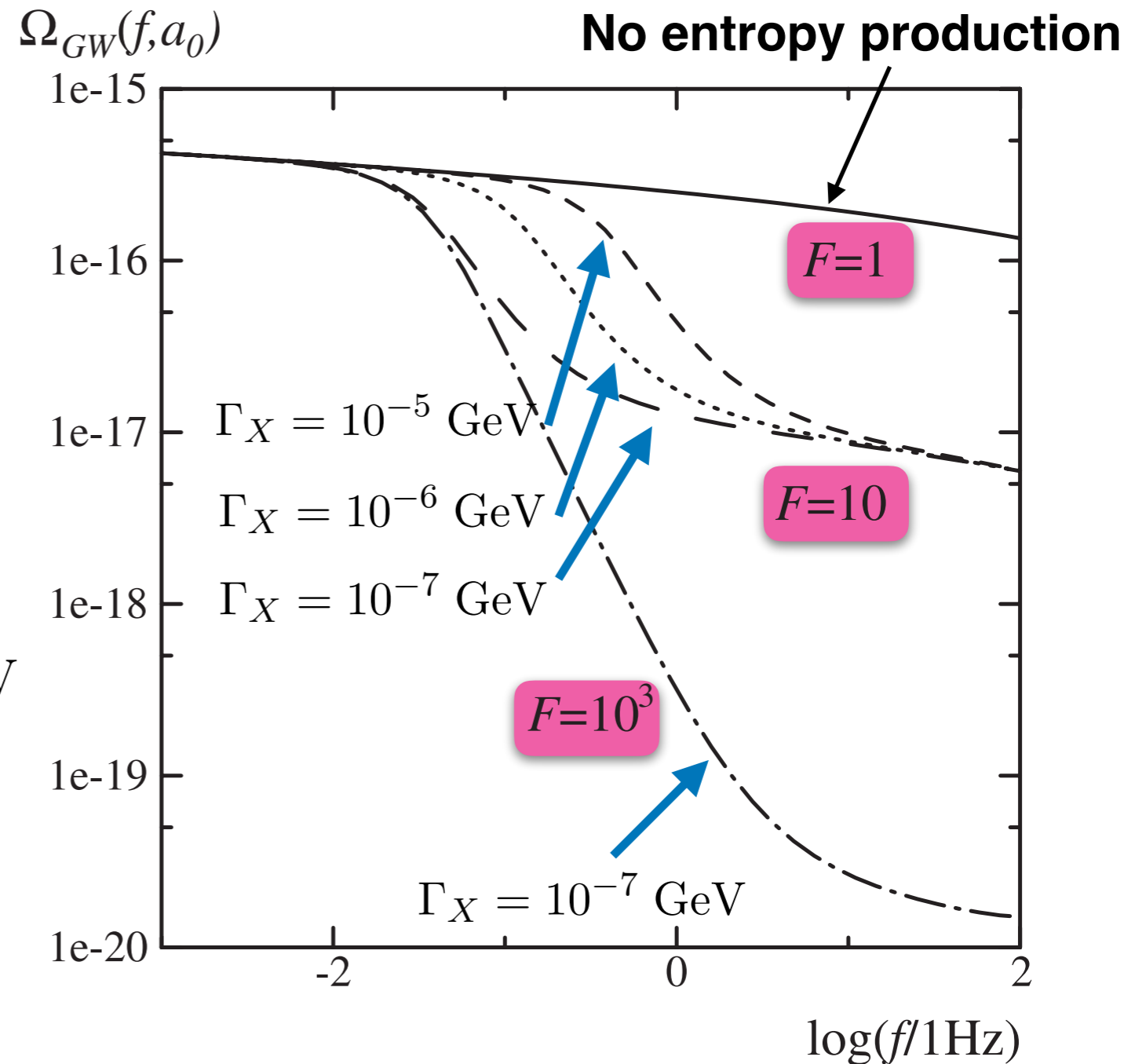
$$m_X \sim (0.8 \sim 4) \times 10^{10} \text{ GeV}$$

**(Approximated) modified GW spectrum**

$$\Omega_{GW}^{SM'}(a_0) = F^{-\frac{4}{3}} \Omega_{GW}^{SM}(a_0)$$

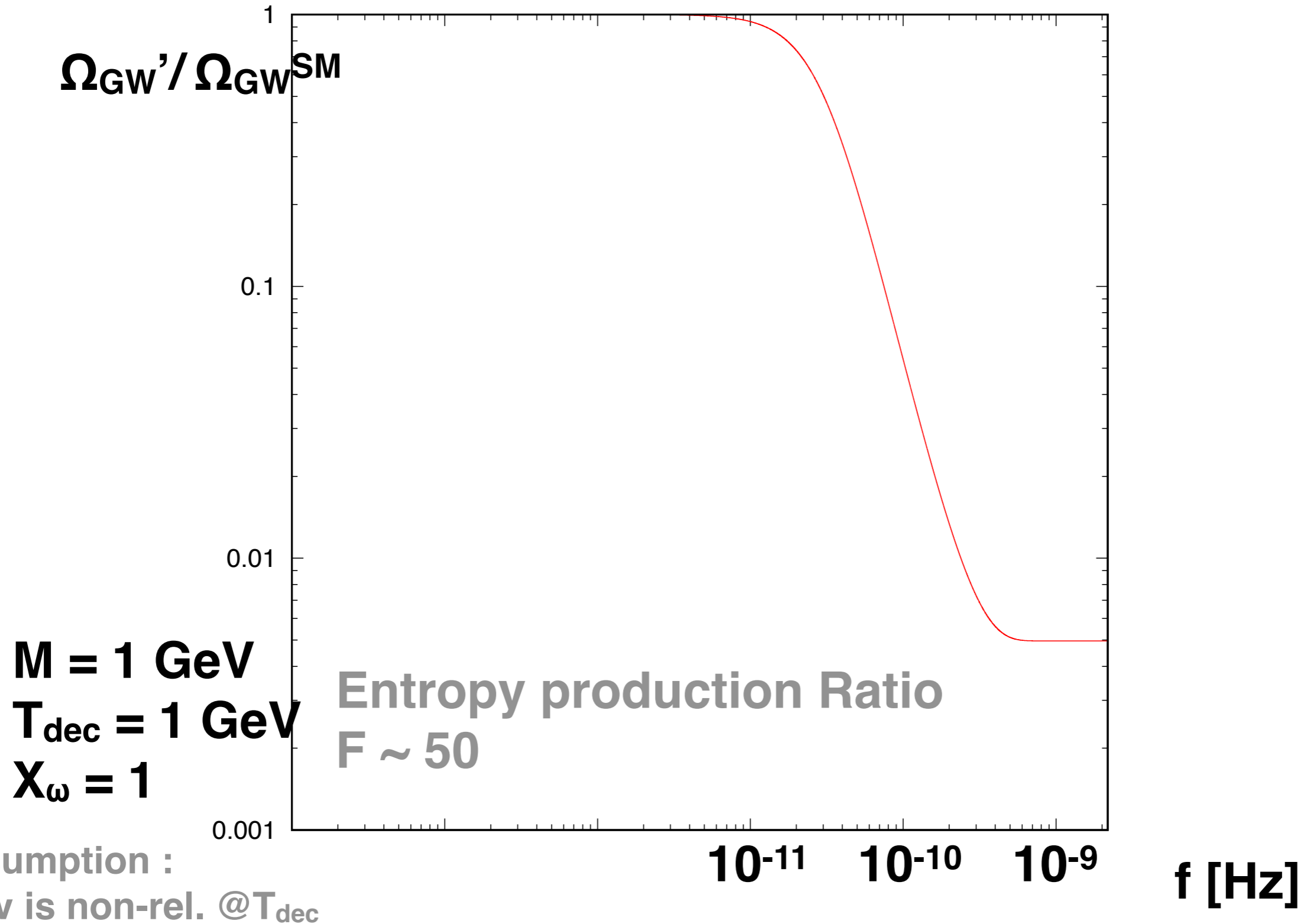
**Dilution factor**

$$F = \frac{s(t_e) a^3(t_e)}{s(t_i) a^3(t_i)}$$

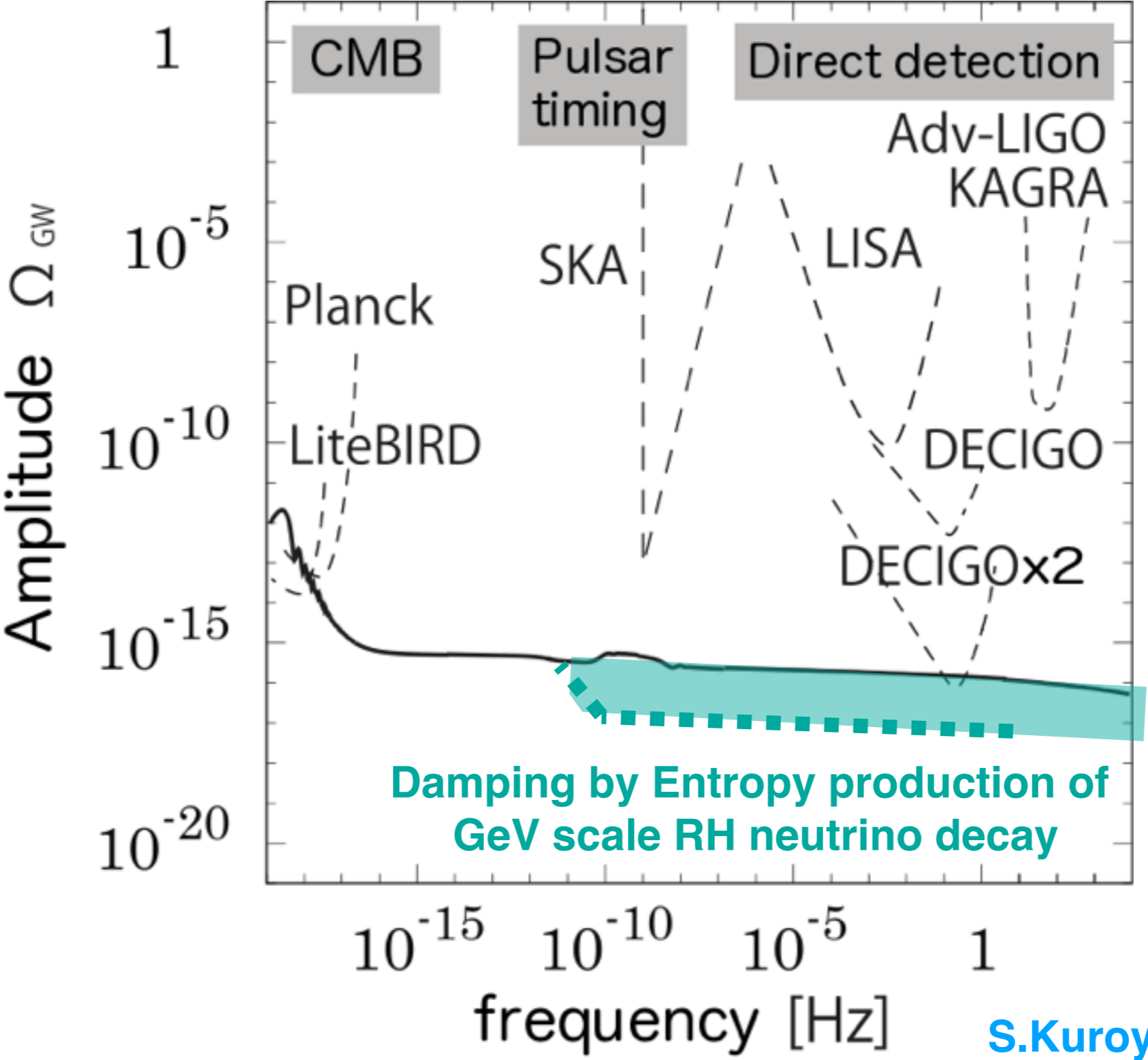


[Seto, Yokoyama, J.Phys.Soc.Jap. 72 \(2003\) 3082-3086](#)

# Modified spectrum by GeV scale RH neutrino



# Primordial gravitational wave



[S.Kuroyanagi, SI2017 slide](#)

# Summary

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- **If the lifetime of the right-handed neutrino is long enough, the right-handed neutrinos can realize the entropy production in the early universe.**
- **The entropy production changes the thermal history of the universe and affects the primordial gravitational spectrum.**
- **Dilution of primordial gravitational wave spectrum by entropy production of right-handed neutrinos starts to occur from about  $10^{-11}$  -  $10^{-8}$  Hz (SKA range).**