

# A Search for Sphalerons at the Large Hadron Collider

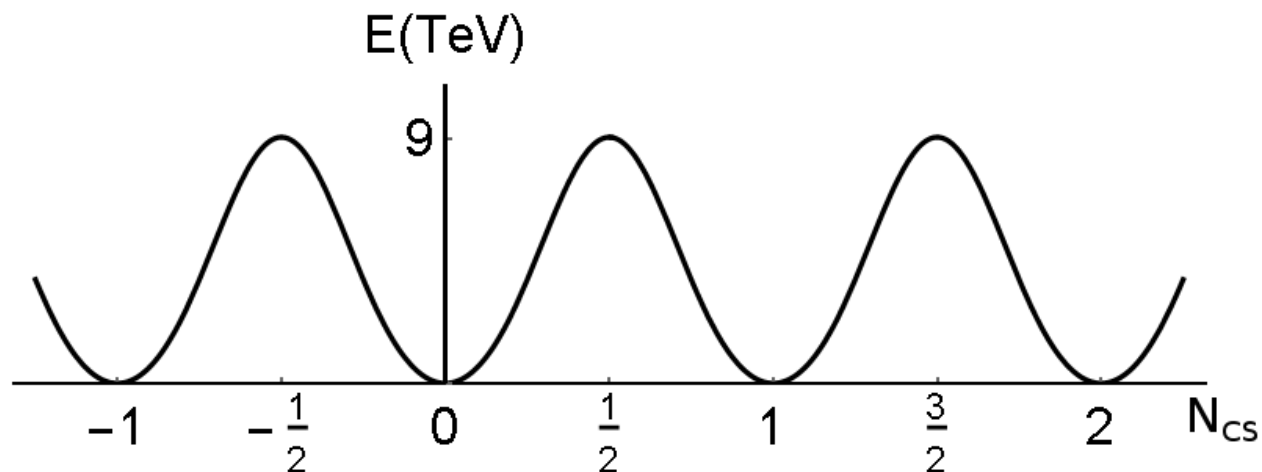
September 11, 2018  
Cameron Bravo

The UCLA logo consists of the letters "UCLA" in a white, bold, sans-serif font, centered within a solid blue rectangular background.

UCLA

# What is a Sphaleron?

- Non-abelian gauge field configuration
  - First proposed by 't Hooft in 1976
  - Sister to instantons
  - Potential in Chern-Simons number ( $N_{CS}$ ) of gauge field
- Not yet discovered, now know SM energy: **~9 TeV**
  - Higgs mass was the last piece needed to calculate
  - “Fireball” final states: around twelve 0.8 TeV particles
- **Violates B+L**
  - B-L is conserved
  - Potential piece of universal matter antimatter asymmetry
- **First dedicated EW sphaleron search**
  - Using full 2016 CMS dataset
  - QCD sphalerons violate chirality and searched for by ALICE (<https://indico.cern.ch/event/656773/>)

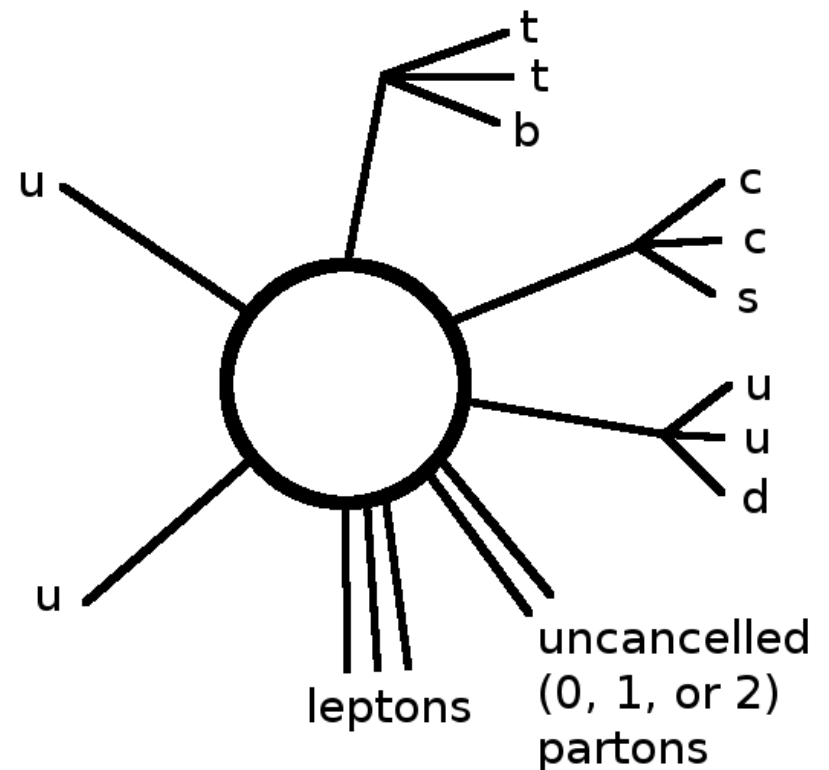


# Where to Begin?

- Phenomenology of B+L violating part of transitions has never been fully studied
- Only public generator makes complicated assumptions which include the generation of an additional  $O(30)$  electroweak gauge bosons
  - Theorists have a lot of disagreement
- What would a “minimal” model look like?
  - Want model focused on B+L violation
  - Distill complex parameter space into salient experimental signatures

# How to Build Final States?

- There are 12 different SM fermion doublets
  - One lepton doublet for each generation
  - Three quark doublets for each generation
  - All fermions of a given configuration are exclusively matter or anti-matter, corresponding to  $\Delta N_{CS} = 1$  or  $-1$
- Pair doublets and choose opposite SU(2) indices for each pair, this guarantees all relevant charges are conserved
  - 1,330,560 quantum mechanically unique fermionic configurations
- Cancel partons if any quark-antiquark pairs exist

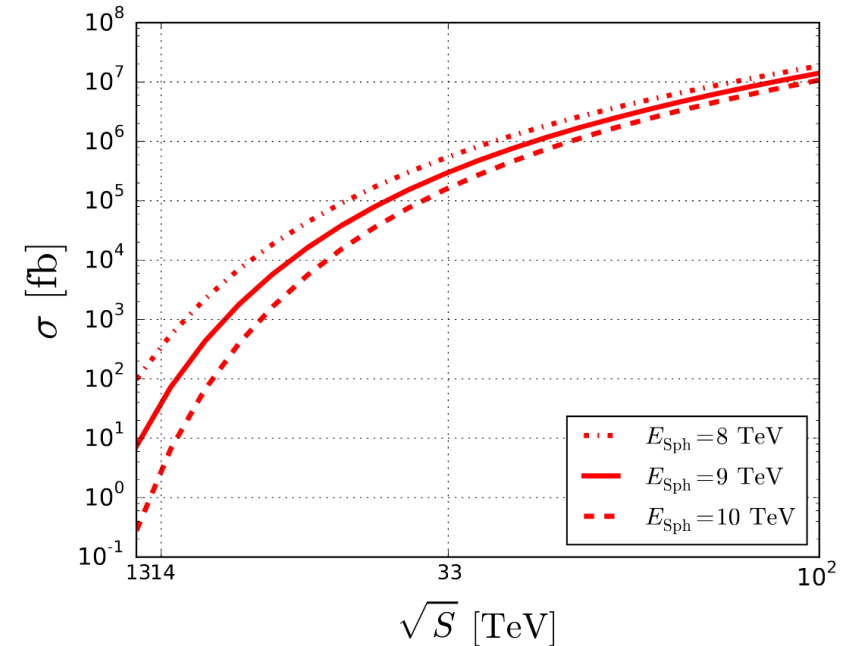


# Phenomenological Final States

- Many of the 1,330,560 different final states are phenomenologically identical in a collider experiment
  - e uud  $\mu$  ccs  $\tau$  ttb
  - e udu  $\mu$  csc  $\tau$  tbt these are different in QM (color charge)
- At CMS u, d, c, and s are difficult to distinguish from each other. There are 8 lepton configurations and 4 configurations of 3 3<sup>rd</sup> generation quarks, making **32** phenomenological final states
  - 1/8 have 3 neutrinos (before W decays)
  - ttt, ttb, tbb, and bbb 3<sup>rd</sup> generation quark configurations each characterize 1/8, 3/8, 3/8, 1/8 of the final states respectively

# Sphaleron Phenomenology

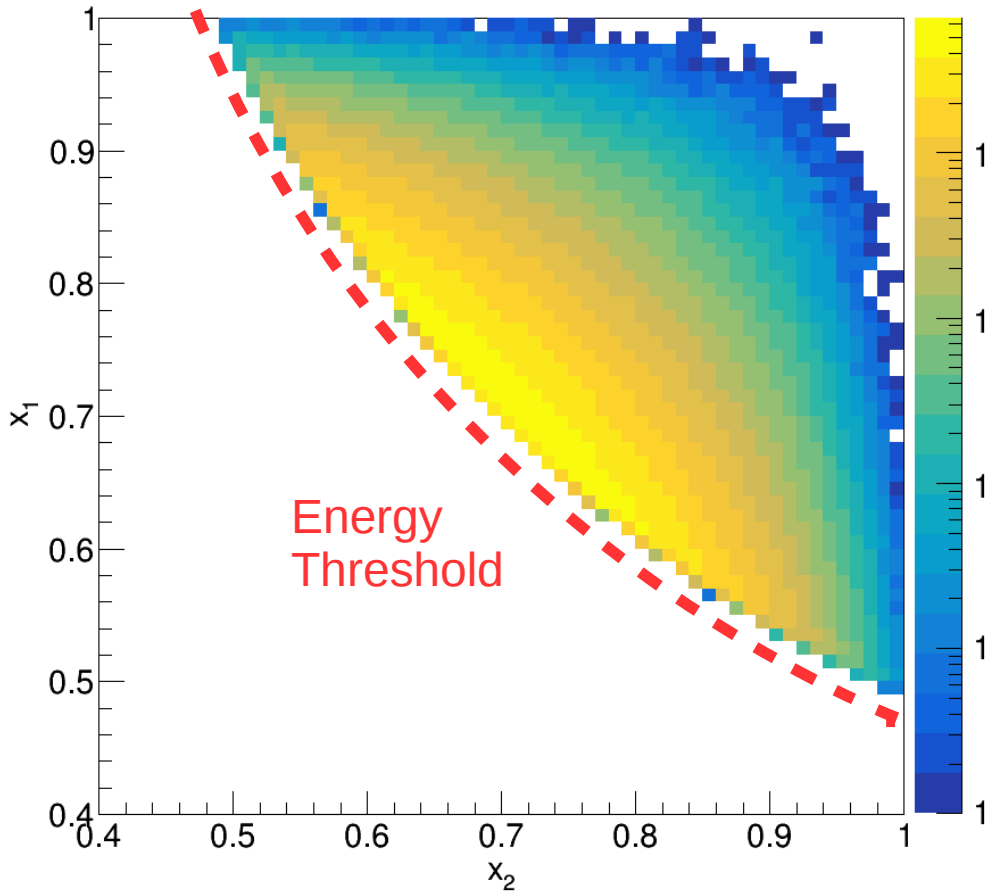
- 10/12/14 particles sharing 9 TeV so each has on average about 760 GeV
  - 4/6/8 light quark jets
  - There are always 3 b's, including b's from tops
  - $\leq 3$  W's all the same sign
  - 0 or 1 of each e,  $\mu$ , and  $\tau$ , which will all be the same sign
  - $\leq 3$   $\nu$ 's
  - Example: e uud  $\mu$  ccs  $\tau$  ttb uu



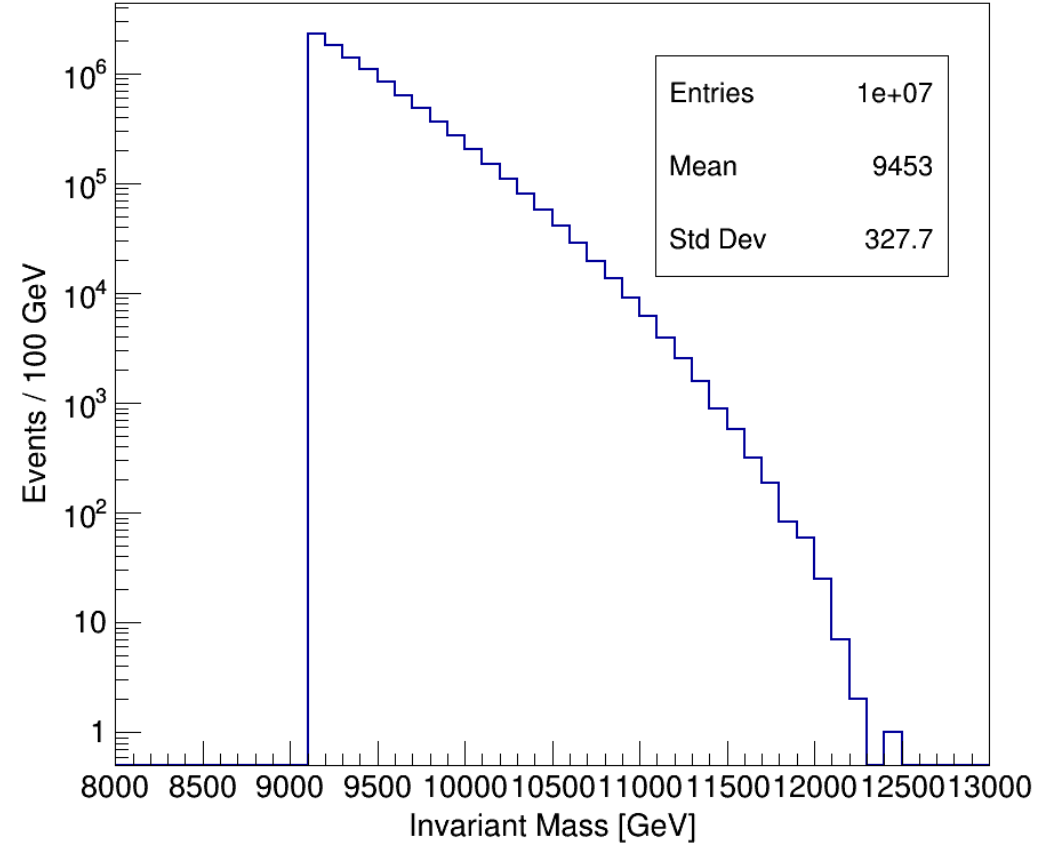
- $S_T = H_T + \text{Lepton } E_T + \text{Photon } E_T + MET$  is  $\sim 7$  TeV on average
- $\sigma = PEF * 10 \text{ fb}$ ,  $PEF = [0,1]$  is the pre-exponential factor for a threshold of 9 TeV at  $\text{sqrt}(s) = 13 \text{ TeV}$  [Ellis and Sakurai, [arXiv:1601.03654](https://arxiv.org/abs/1601.03654)]
  - The cross-section for  $PEF = 1$  corresponds to all quark-quark interactions over the energy threshold and comes from the parton distribution functions (PDF)

# BaryoGEN, a New MC Generator

Parton Momentum Fractions



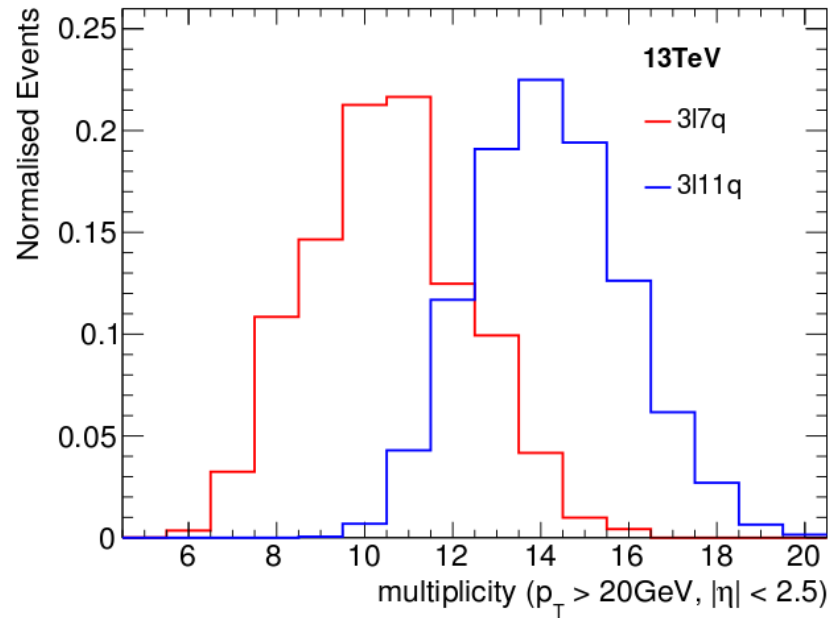
Sphaleron Mass



- Available on github: <https://github.com/cbravo135/BaryoGEN>
- Paper recently accepted at JHEP (C. Bravo and J. Hauser, arXiv:1805.02786)

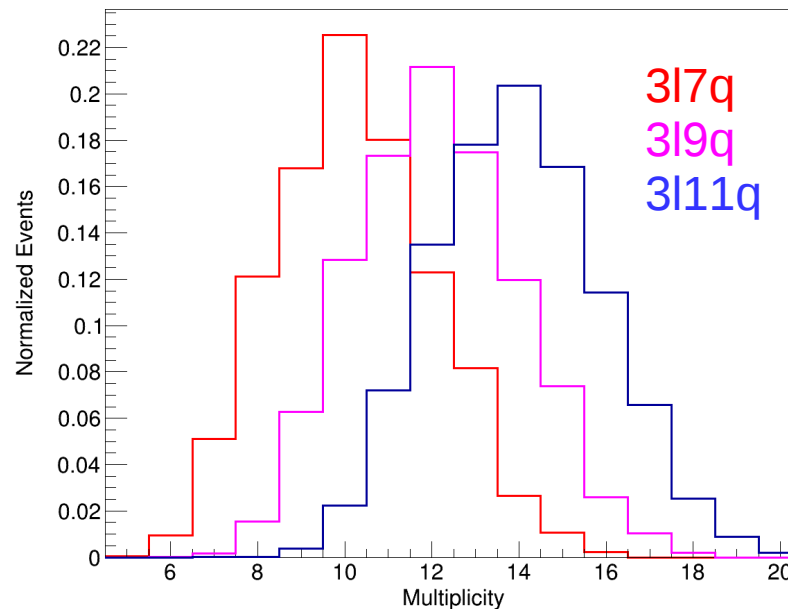
# Comparison with Ellis and Sakurai

3l7q, 3l9q, and 3l11q are different outgoing parton multiplicities due to cancellation with incoming states



Ellis and Sakurai

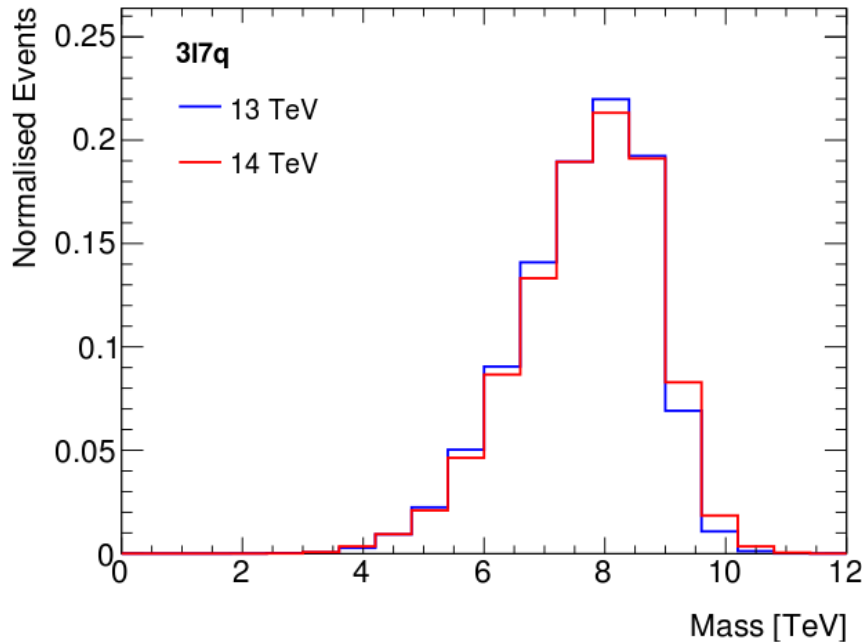
w.r.t. Ellis and Sakurai I am adding 3l9q and additional multiplicity category, which is the case of only one parton cancellation



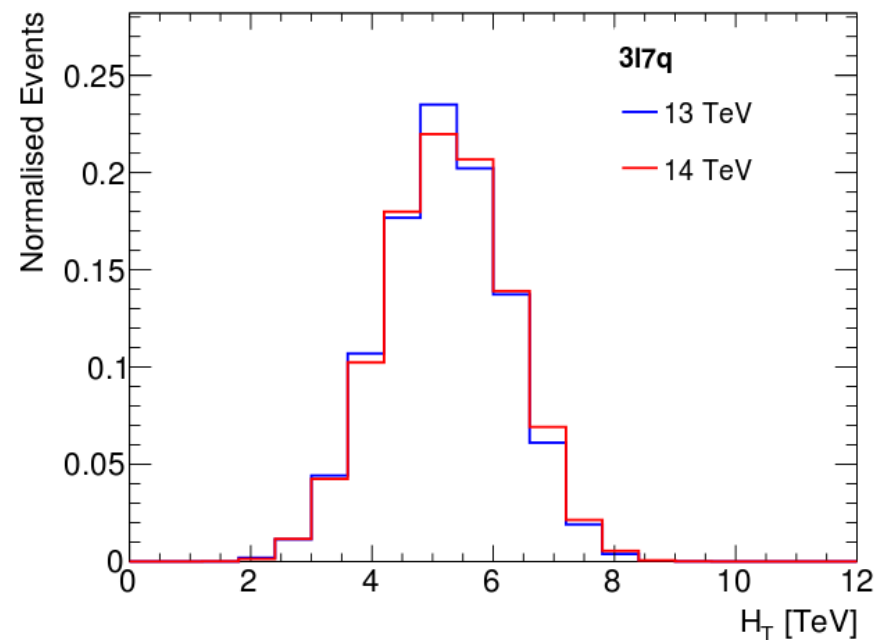
BaryoGEN  
13 TeV



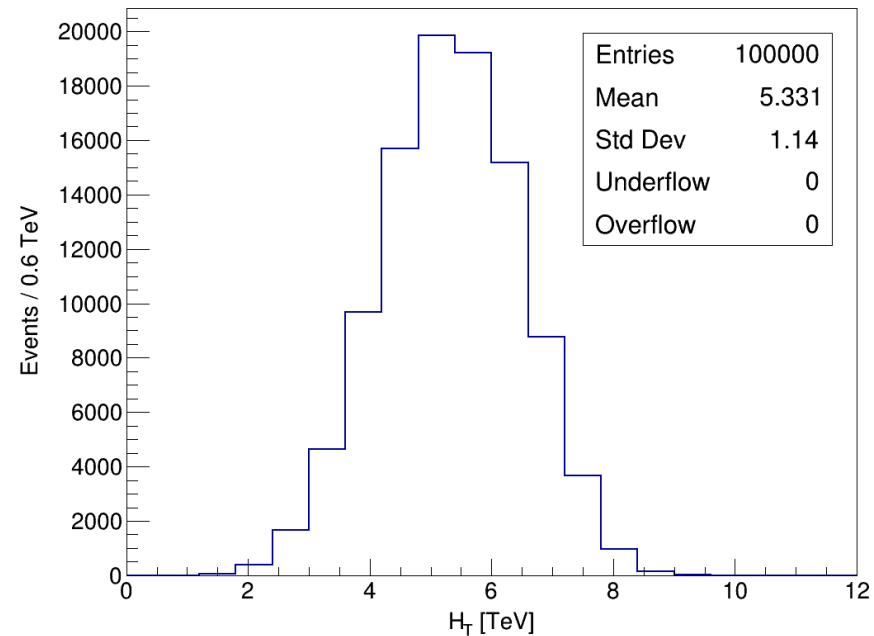
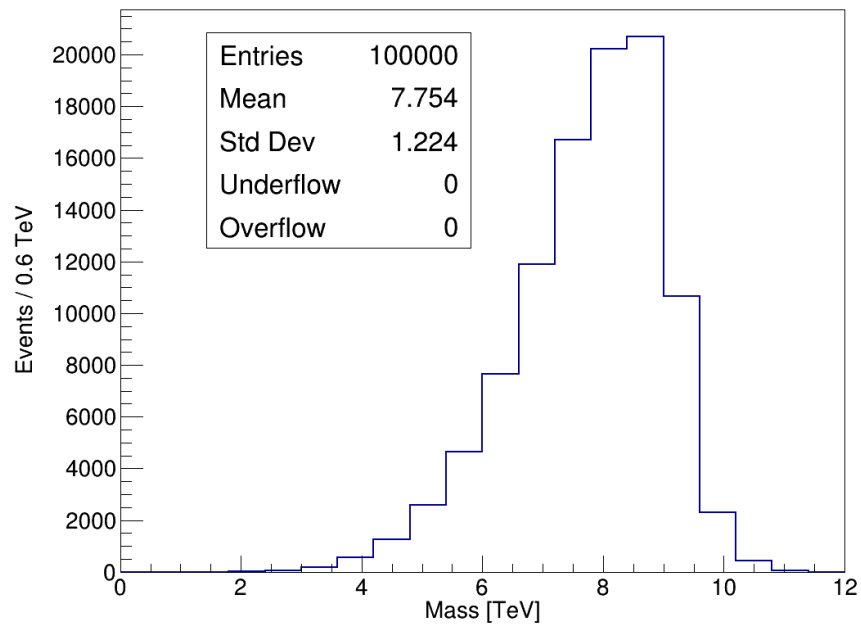
# Energy Comparison



Mass of Observable Particles ( $p_T > 20$  GeV and  $|\eta| < 2.5$ )



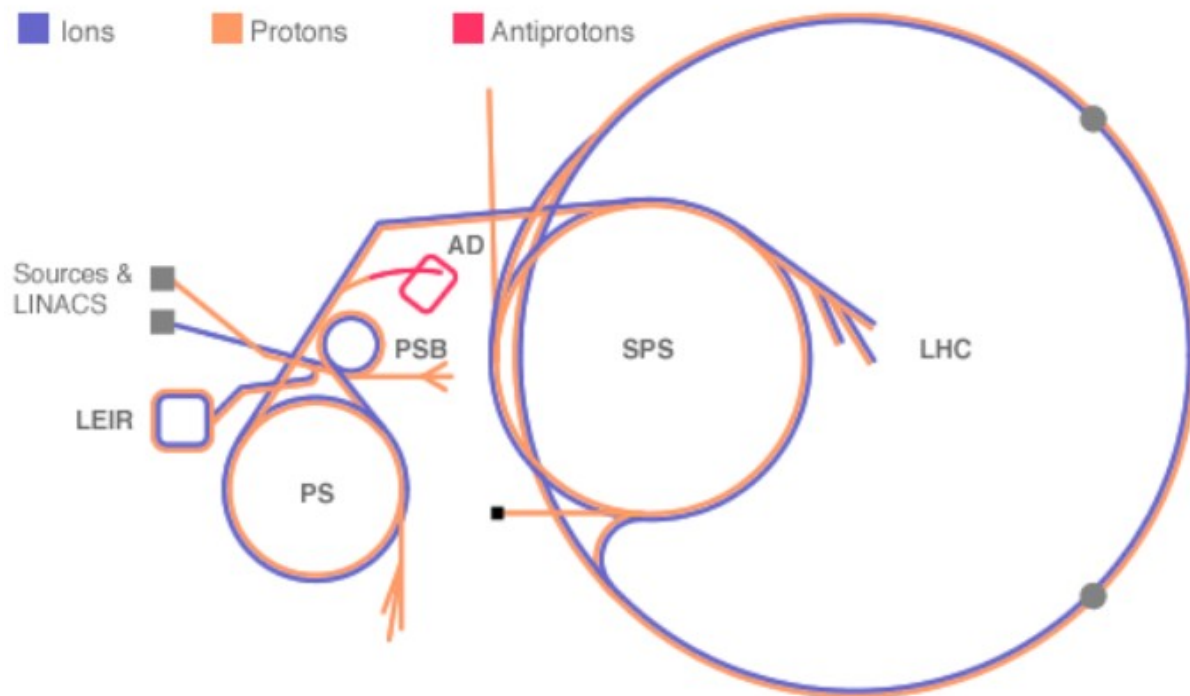
Ellis and Sakurai



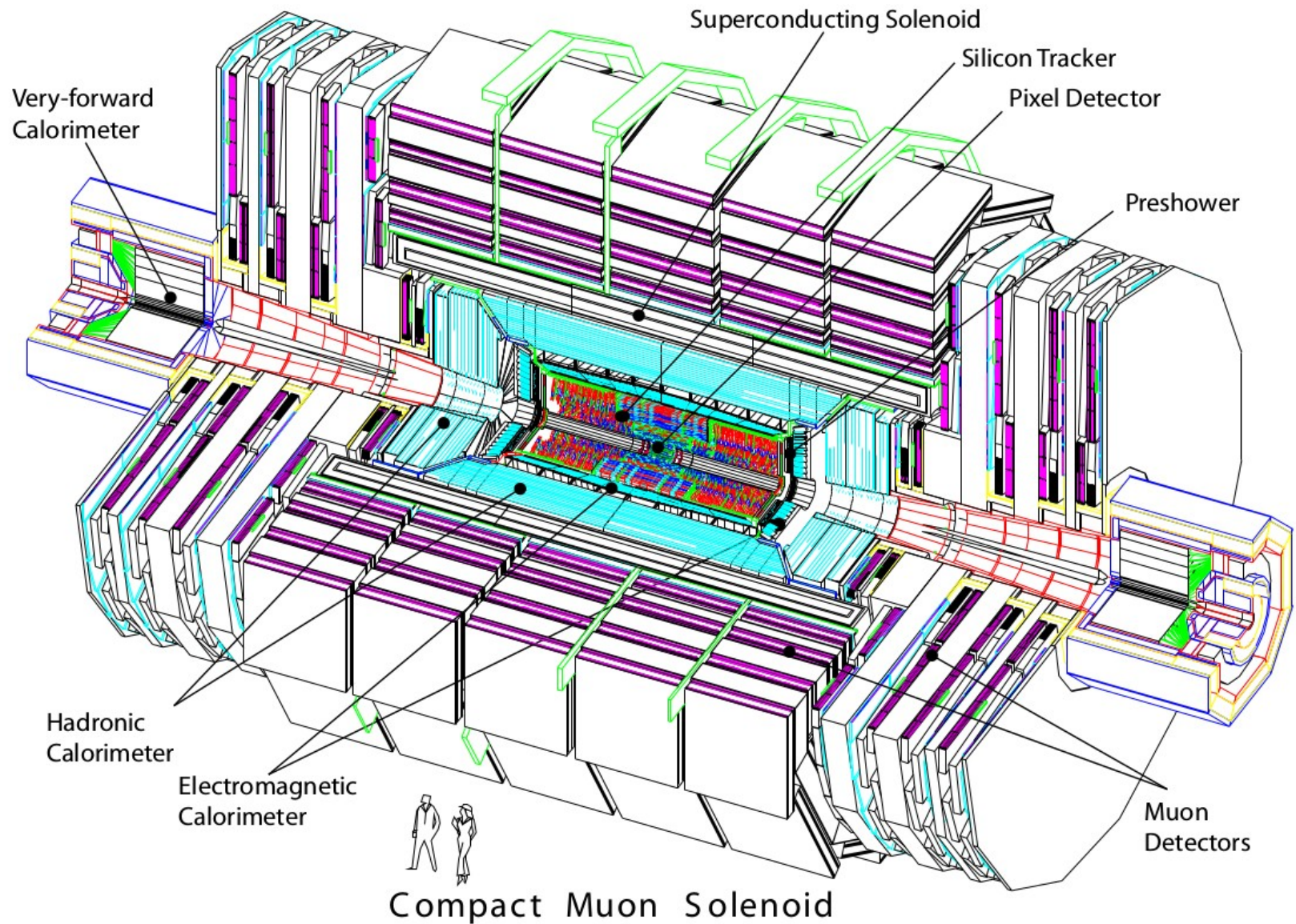
BaryoGEN  
13 TeV

# How do We Look for It?

- Need the worlds largest particle accelerator: LHC
  - Run 2 with  $\sqrt{s} = 13 \text{ TeV}$  is just at the production threshold
  - We can finally start making sphalerons
- Full 2016 CMS dataset
  - Integrated Luminosity:  $35.9 \text{ fb}^{-1}$

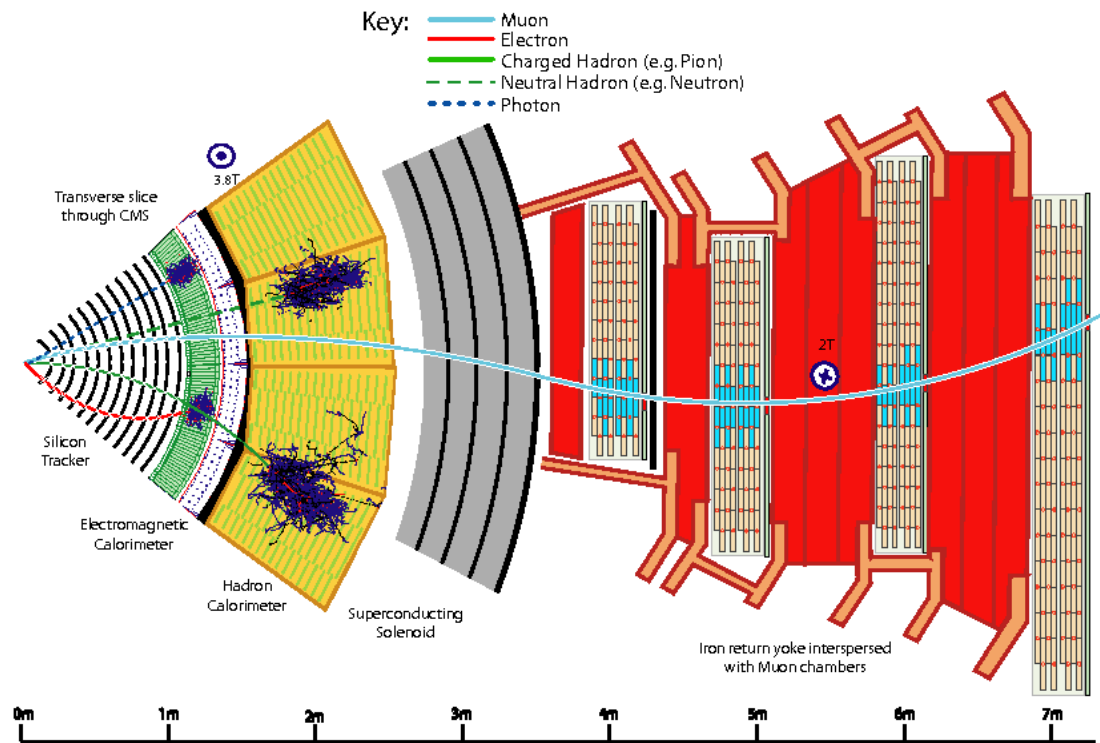


# The CMS Detector



# Event Reconstruction

- Build *physics objects* from digital signals: Particle Flow
- Jets
  - Hadrons and photons
  - Calorimeters
- Electrons and Photons
  - ECAL
  - Tracking and Isolation
- Muons
  - Gas detectors
  - Tracking

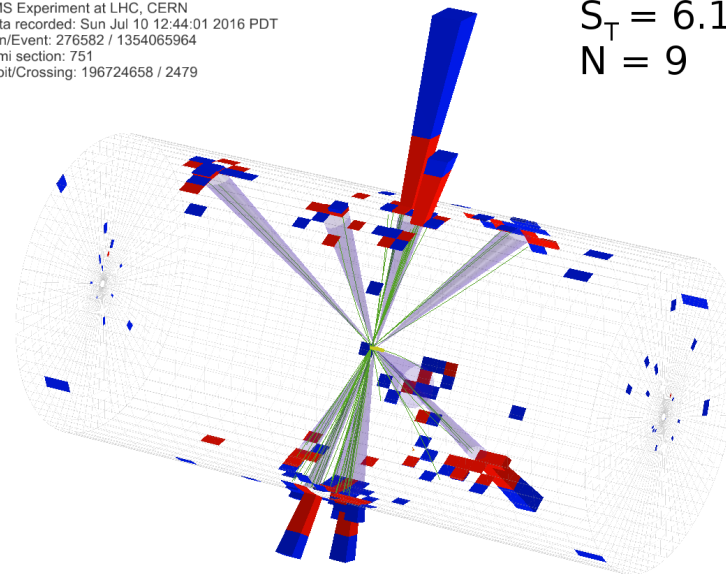


# Introduction to CMS Search

- High energy and high multiplicity search for new physics
- LHC could produce new physics with high ( $\sim$ TeV) mass and decaying into a high multiplicity of physics objects
  - Events with such objects would have high transverse energy, and possibly high MET
- Flagship analysis searching for microscopic black holes is a great fit
  - BH/Sphaleron search is born
- Multijet QCD is the dominant background
- Main results of analysis are model independent limits in case no significant excess is observed



CMS Experiment at LHC, CERN  
Data recorded: Sun Jul 10 12:44:01 2016 PDT  
Run/Event: 276582 / 1354065964  
Lumi section: 751  
Orbit/Crossing: 196724658 / 2479



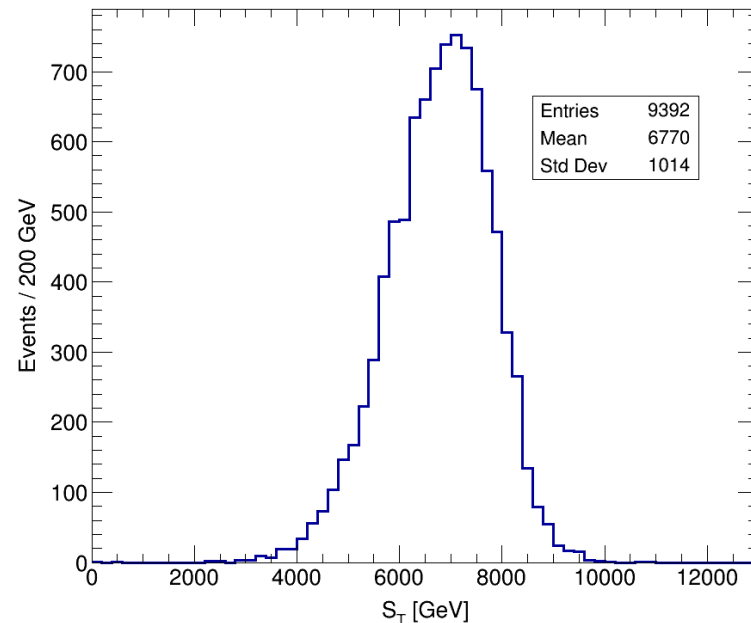
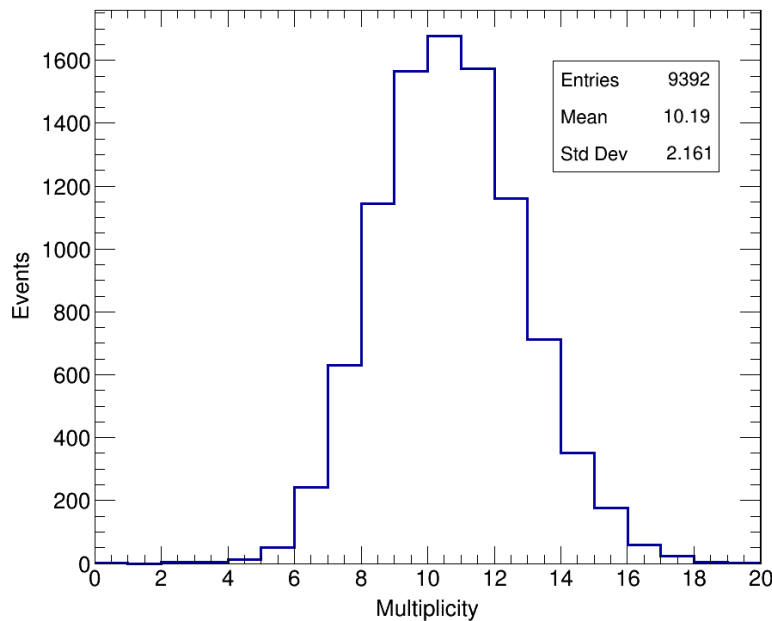
$S_T = 6.10$  TeV  
 $N = 9$



# The Data

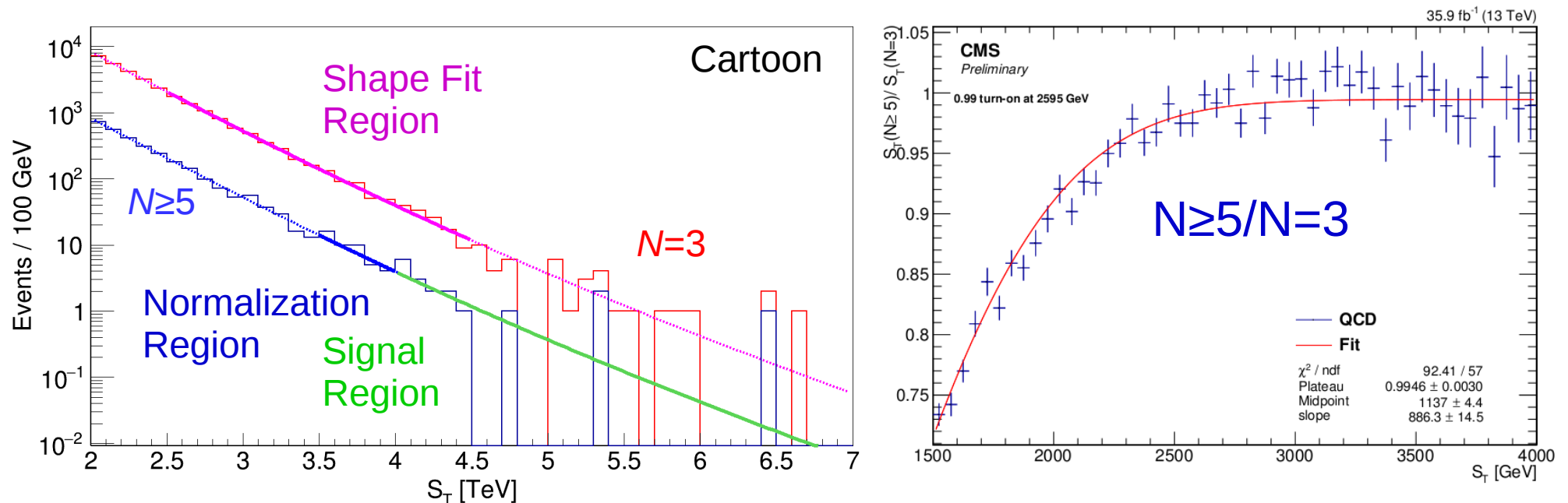
- Collect data with online high  $H_T$  triggers
- Inclusive search: two search variables
  - Multiplicity ( $N$ ) is defined as total number of physics objects over 70 GeV
  - $S_T = \left( \sum_{i=1}^N E_{T,i} \right) + E_T^{\text{miss}}$  summed over jets, photons, electrons, and muons
- Sensitive to a broad range of high-energy signatures

## Sphaleron Signal

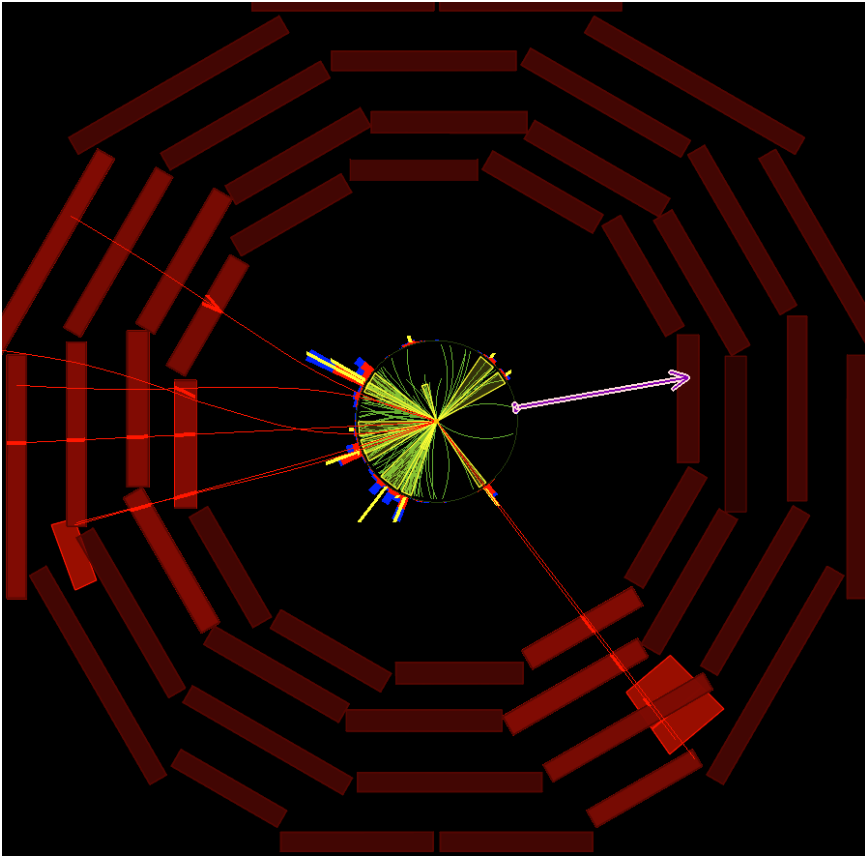


# Analysis Strategy

- Data driven background estimation takes advantage of the shape of the  $S_T$  spectrum being independent of  $N$ 
  - Fit shapes to data at low  $S_T$  for  $N=3$  and  $N=4$
  - For each  $N$  ( $\geq 3,4,5,6,\dots,11$ ) scale shape using signal-free normalization region
  - Procedure developed and validated on MC and then applied independently to data



# Background Estimation Procedure

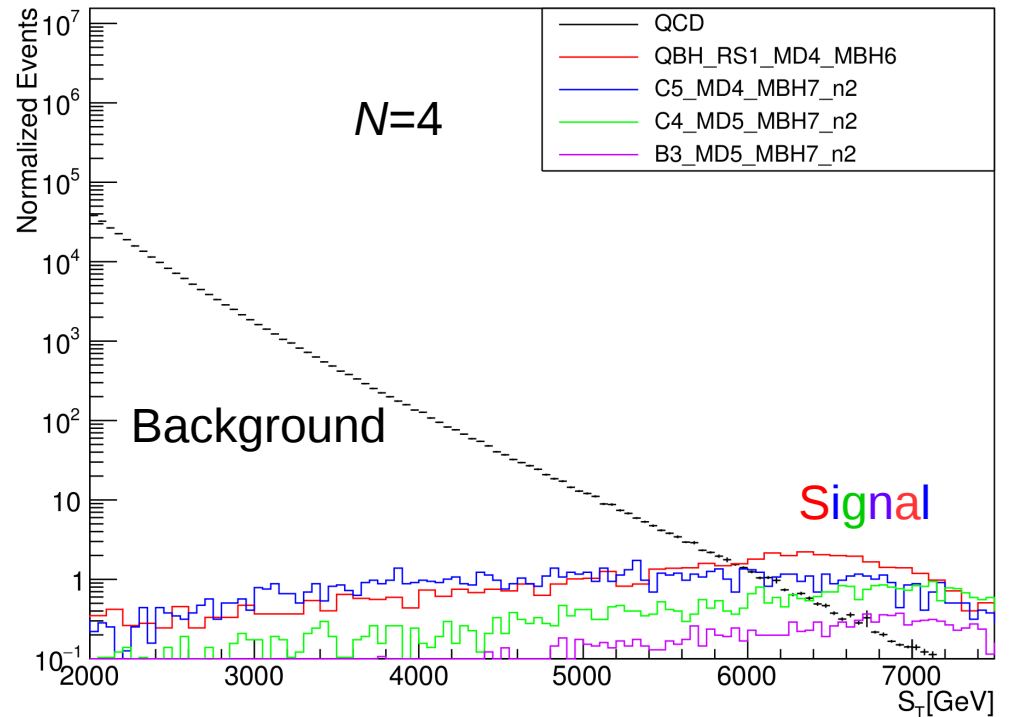
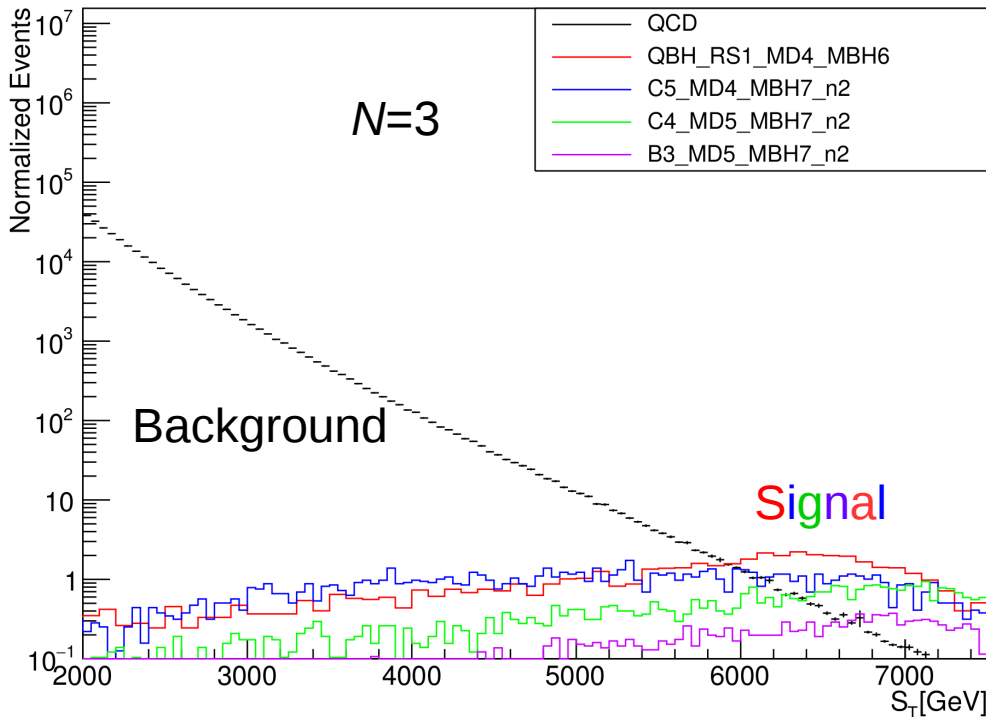


Sphaleron MC Event Display

- 1) Choose fit region
- 2) Choose fit functions
- 3) Fit background shape
- 4) Normalization



# Step 1: Choose Fit Region



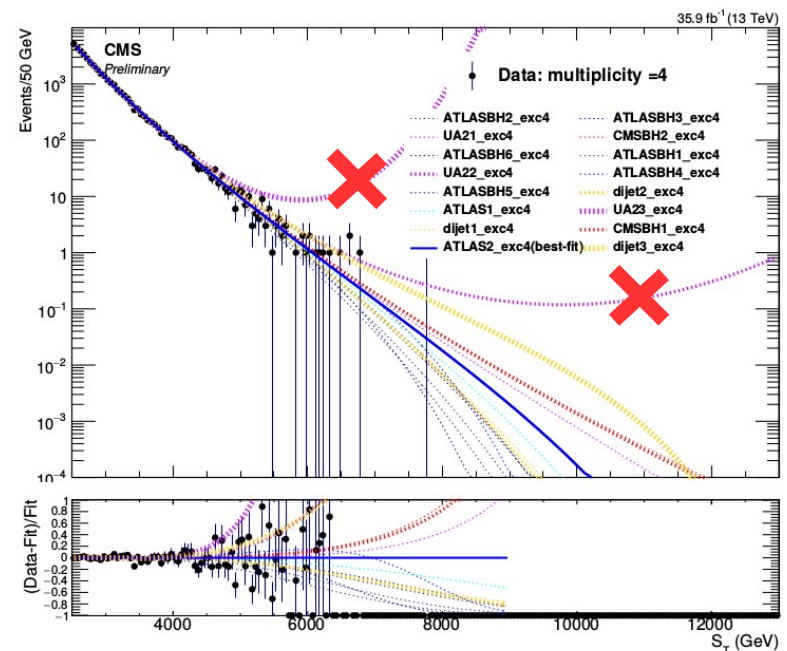
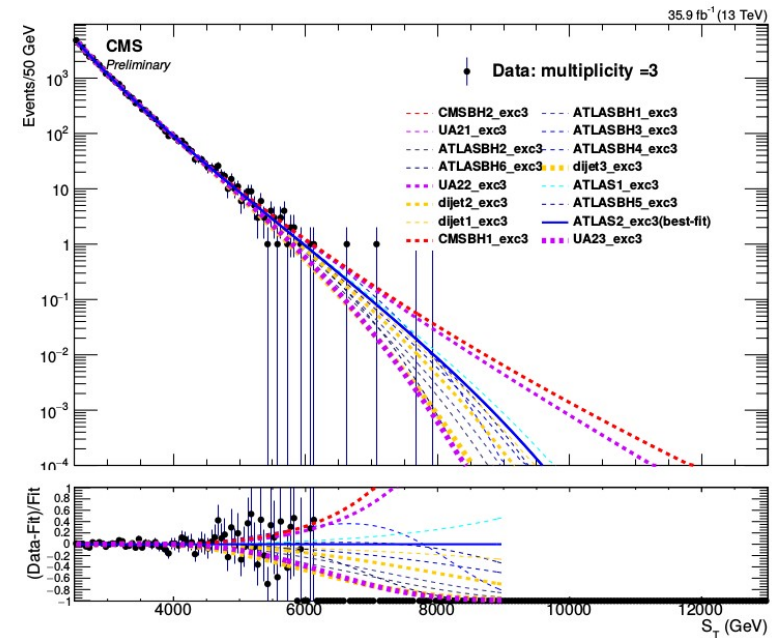
- Look at lowest unexcluded mass for each class of models from 2015
- Choose fit range  $2.5 \text{ TeV} < S_T < 4.3 \text{ TeV}$
- Less than 2% signal contamination in both  $N=3$  and  $N=4$  in any bin
- No signal contamination at these multiplicities from sphalerons

# Step 2: Choose Fit Functions

- Goal is to find steeply falling functions over a wide range
- Search literature for functions used in a reasonably similar setting
  - CMS and ATLAS BH searches
  - Dijet searches
  - All functions used are in backup

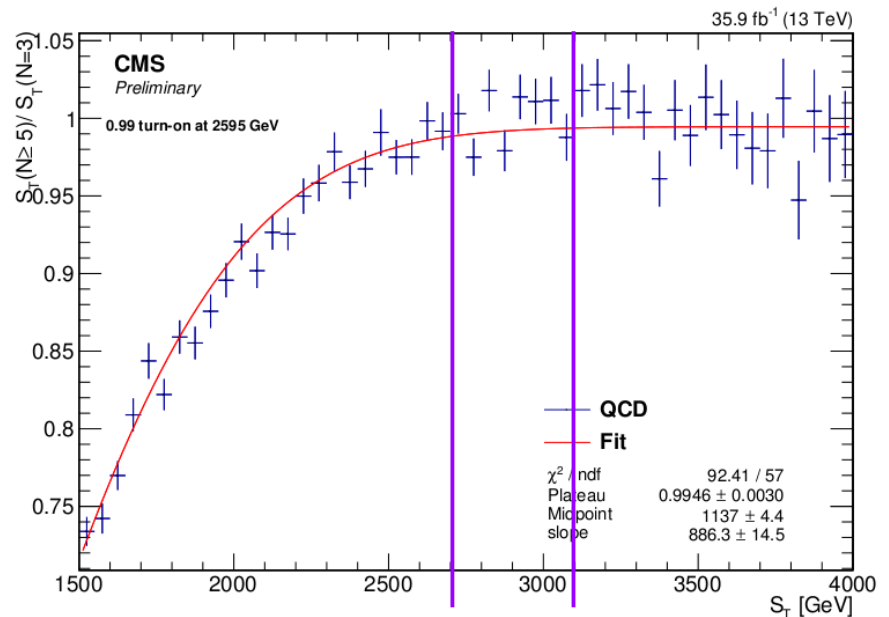
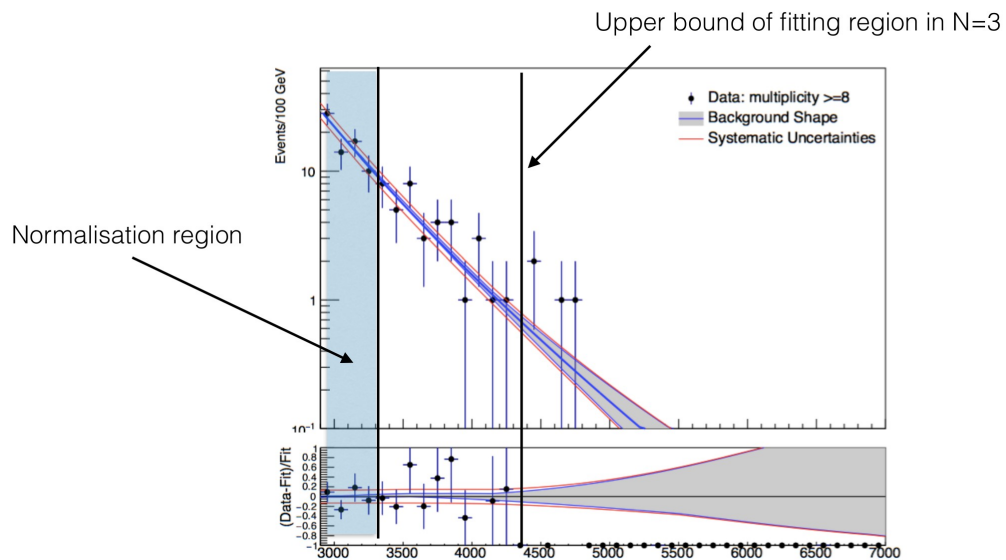
# Step 3: Background Shape

- Higher order functions can often diverge at high  $S_T$ 
  - Require functions to be monotonically decreasing up to 13 TeV
  - Remaining functions generally describe data well
  - Use collective results to build background prediction
- Choose central fit from ensemble of  $N = 3$  fits
- Shape systematic is taken as the maximum and minimum values at each  $S_T$  point
  - This step includes  $N=4$  fits

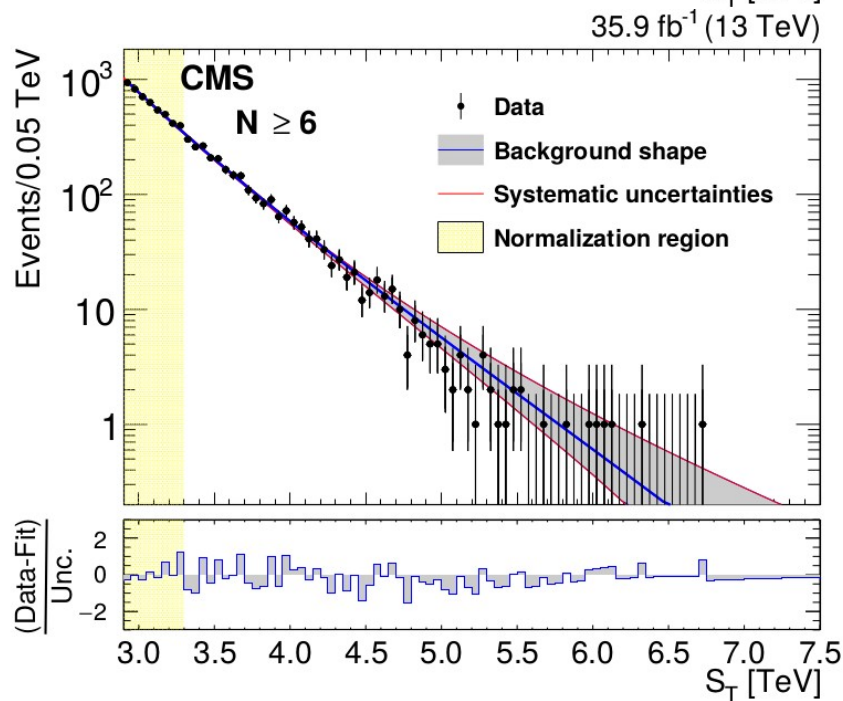
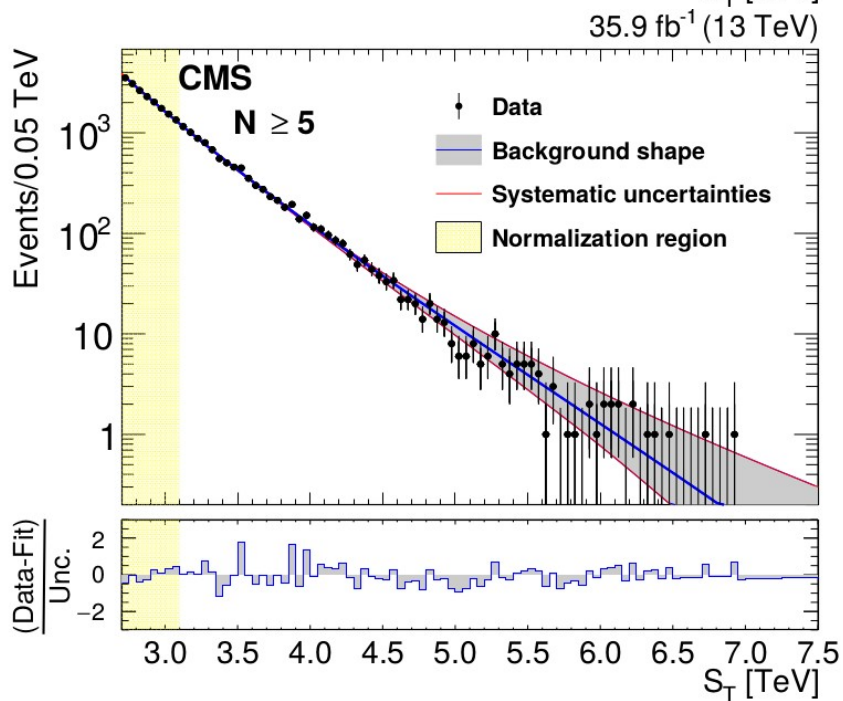
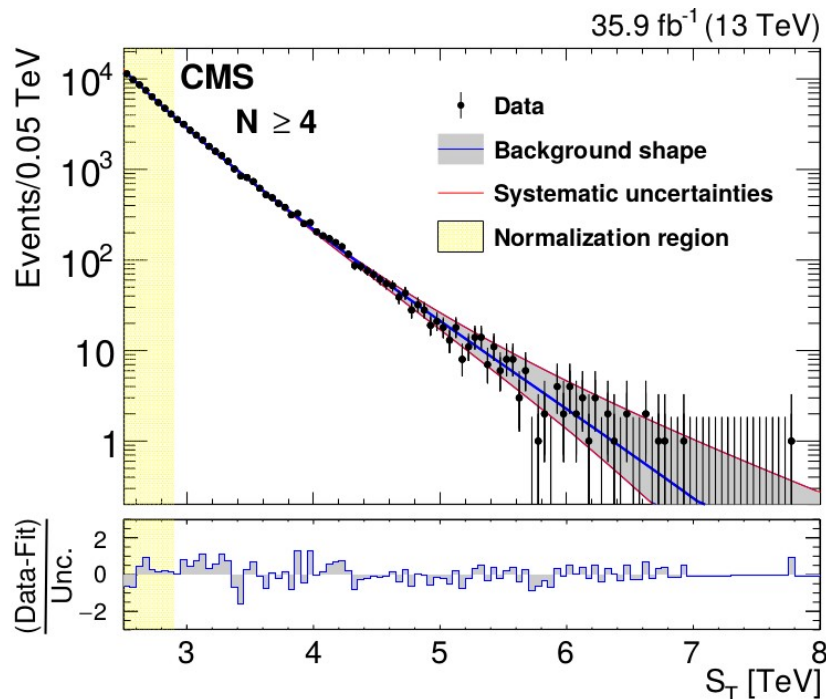
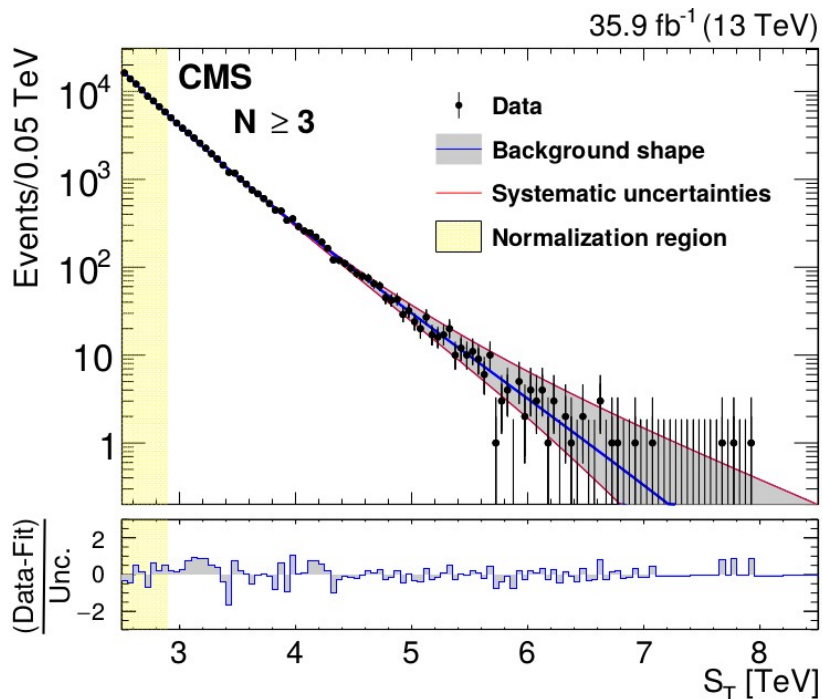


# Step 4: Background Normalization

- Study ratio of inclusive spectra to exclusive 3 spectrum
  - Determine the lower bound of normalization region
- All normalization regions are 400 GeV wide
- $s_{N \geq i} = (\#Events)_{N \geq i} / (\#Events)_{N=3}$
- At low  $S_T$  (inside fit region) the uncertainty is dominated by the uncertainty of  $s_{N \geq i}$

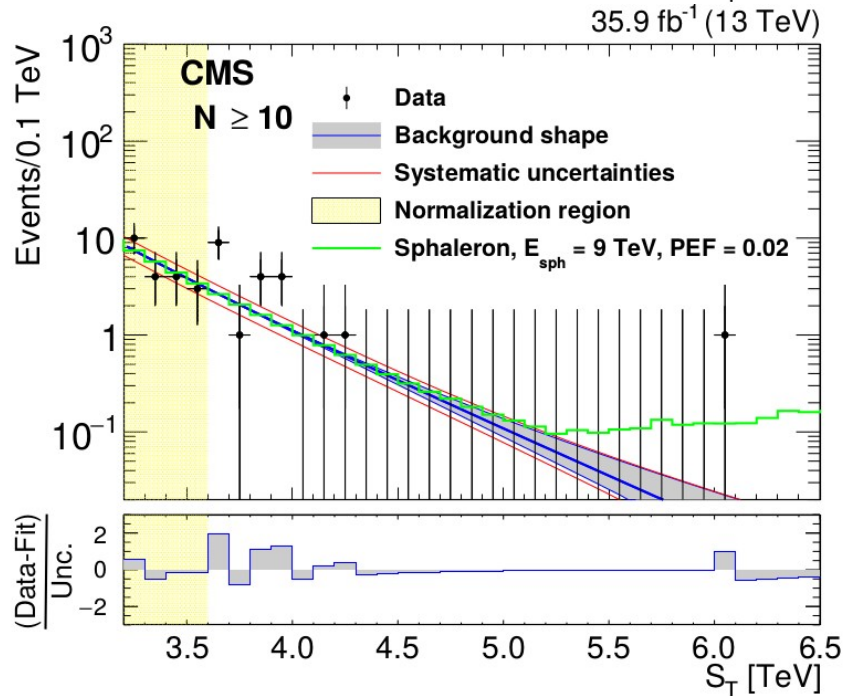
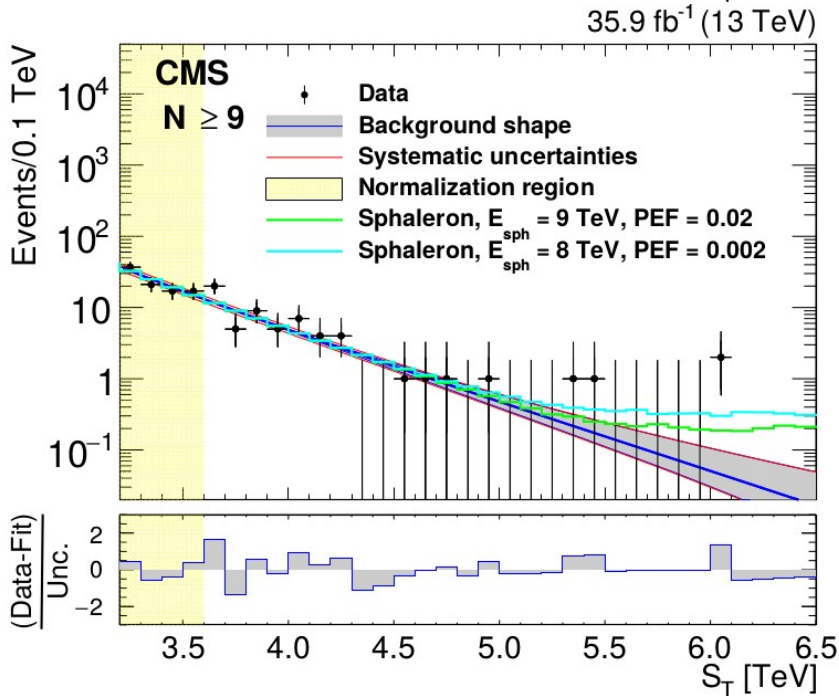
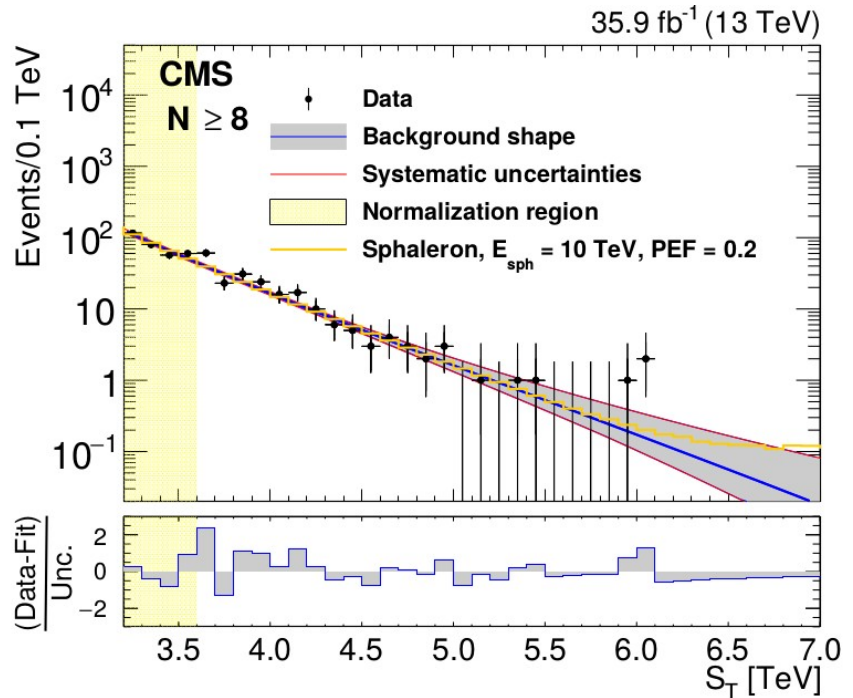
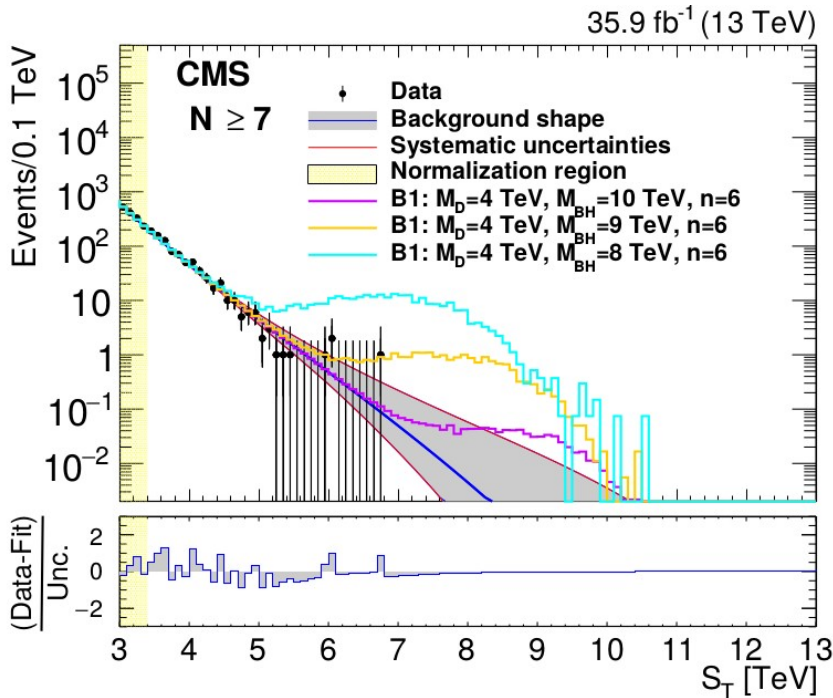


# Take a Look at the Data



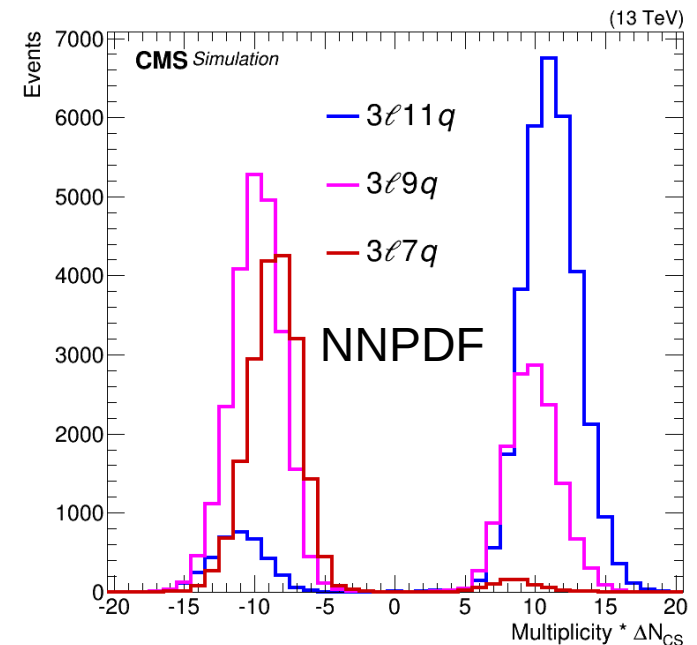
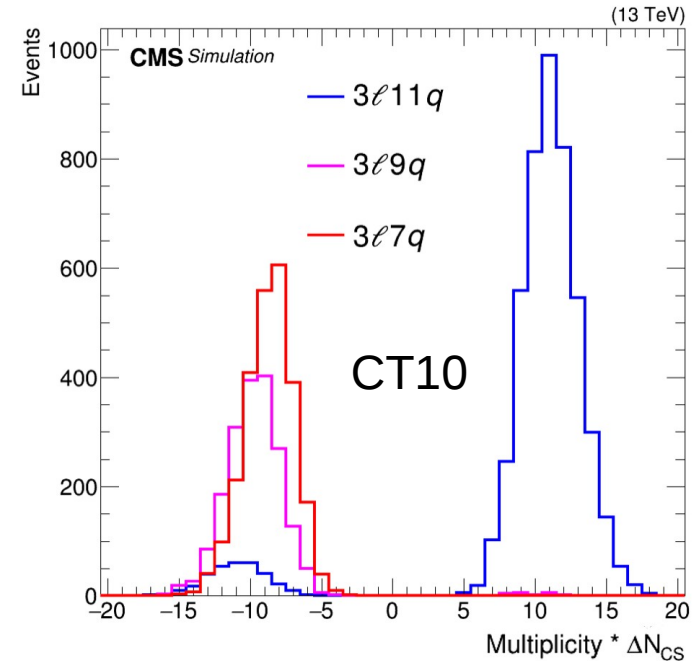


# No Excess Observed

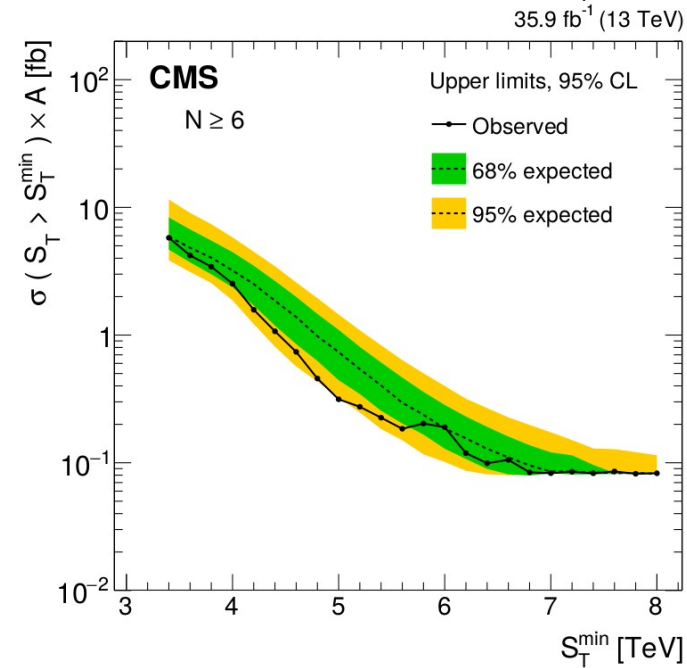
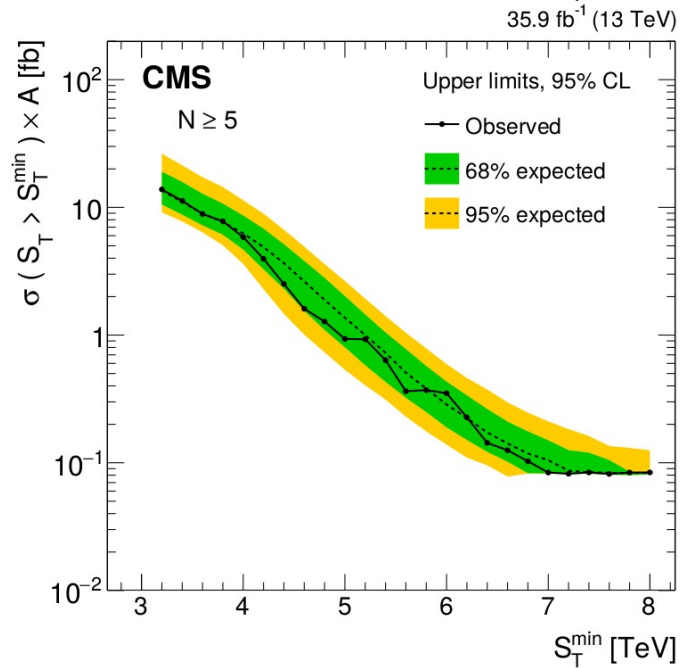
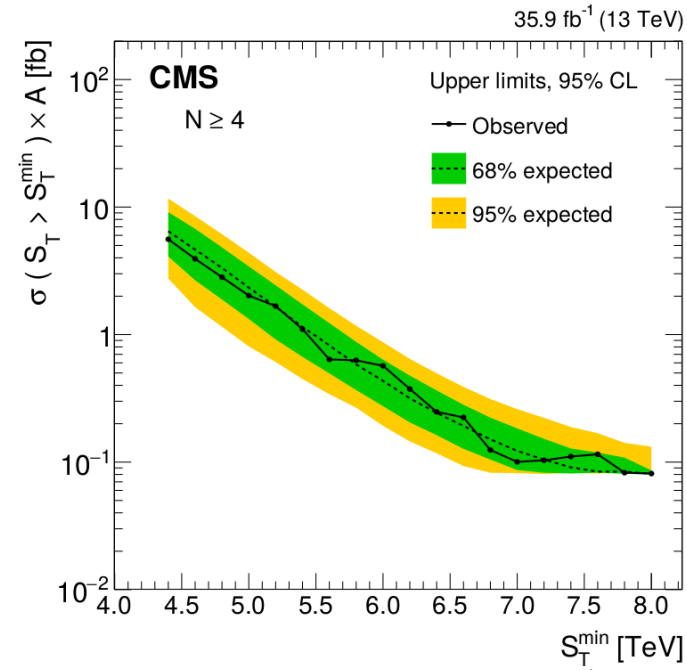
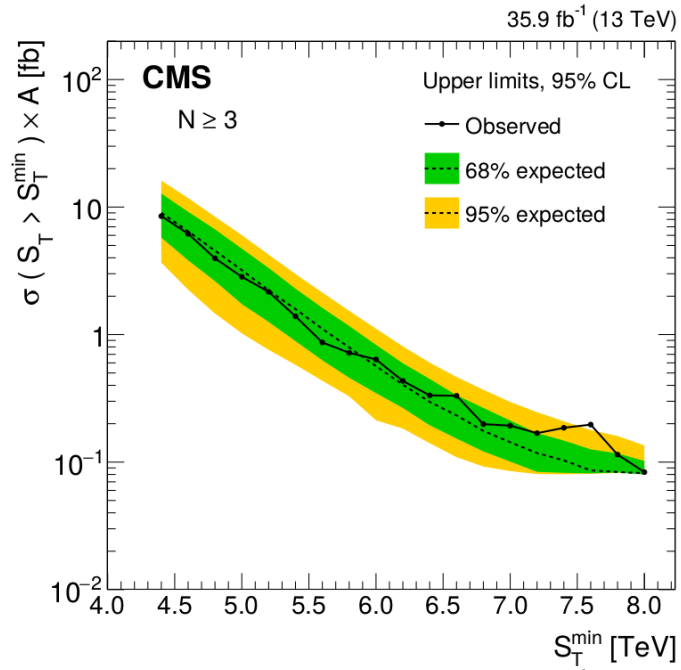


# No Excess, Set Limits

- Data shows no significant deviation from background prediction, proceed setting upper limits
- Full  $CL_s$  criterion to set 95% confidence level upper limit for each inclusive multiplicity for varying  $S_T$  cuts
- Systematics
  - Signal
    - Jet Energy Scale: 5%
    - Jet Energy Resolution: 4%
    - Parton Distribution Functions: 6%
    - Luminosity: 2.5%
  - Background
    - Shape: 1-1000%
    - Normalization: 4-23%

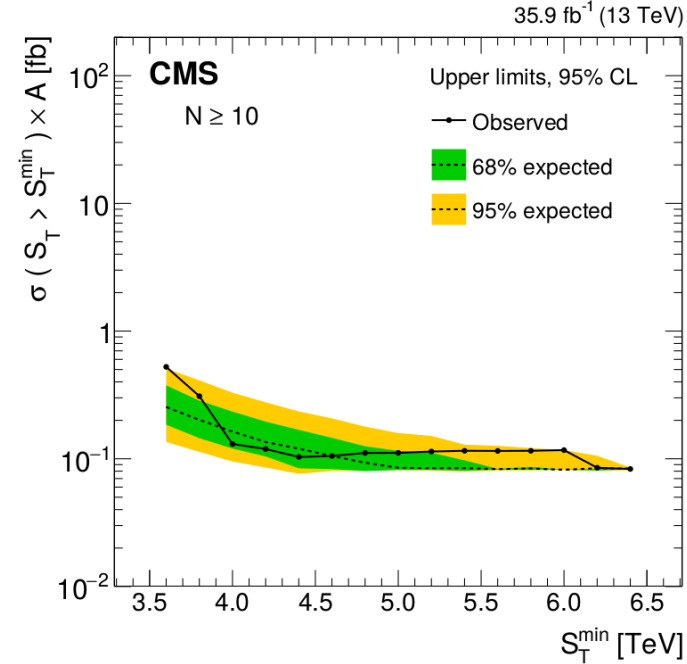
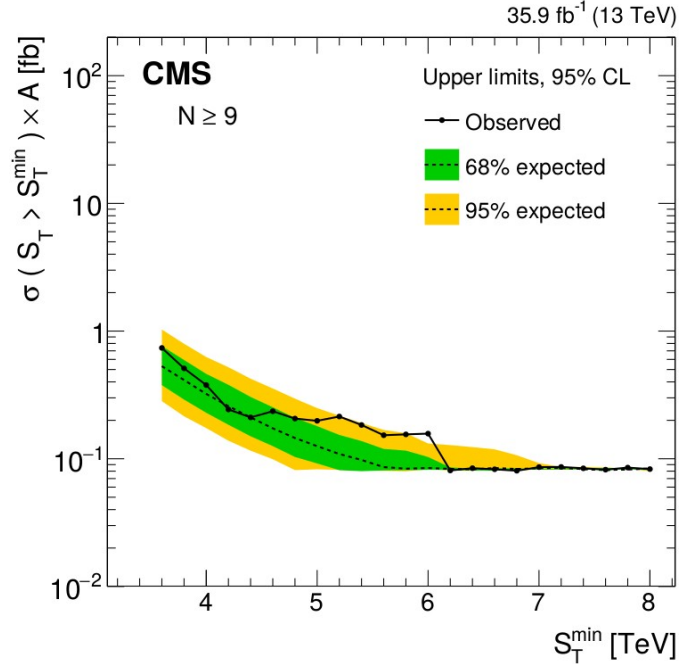
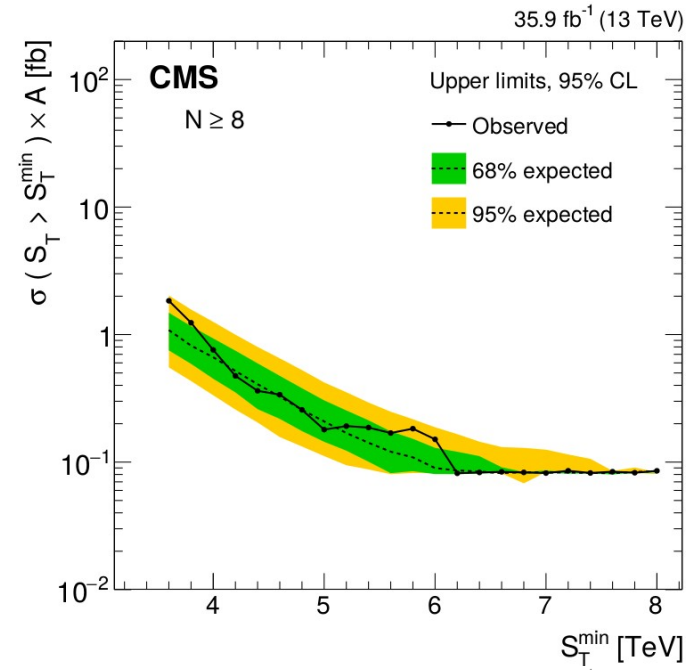
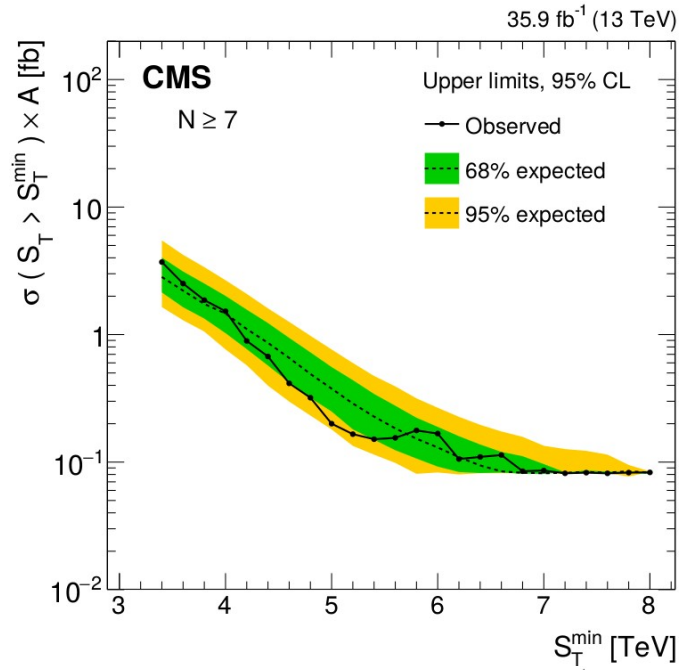


# Model Independent Limits



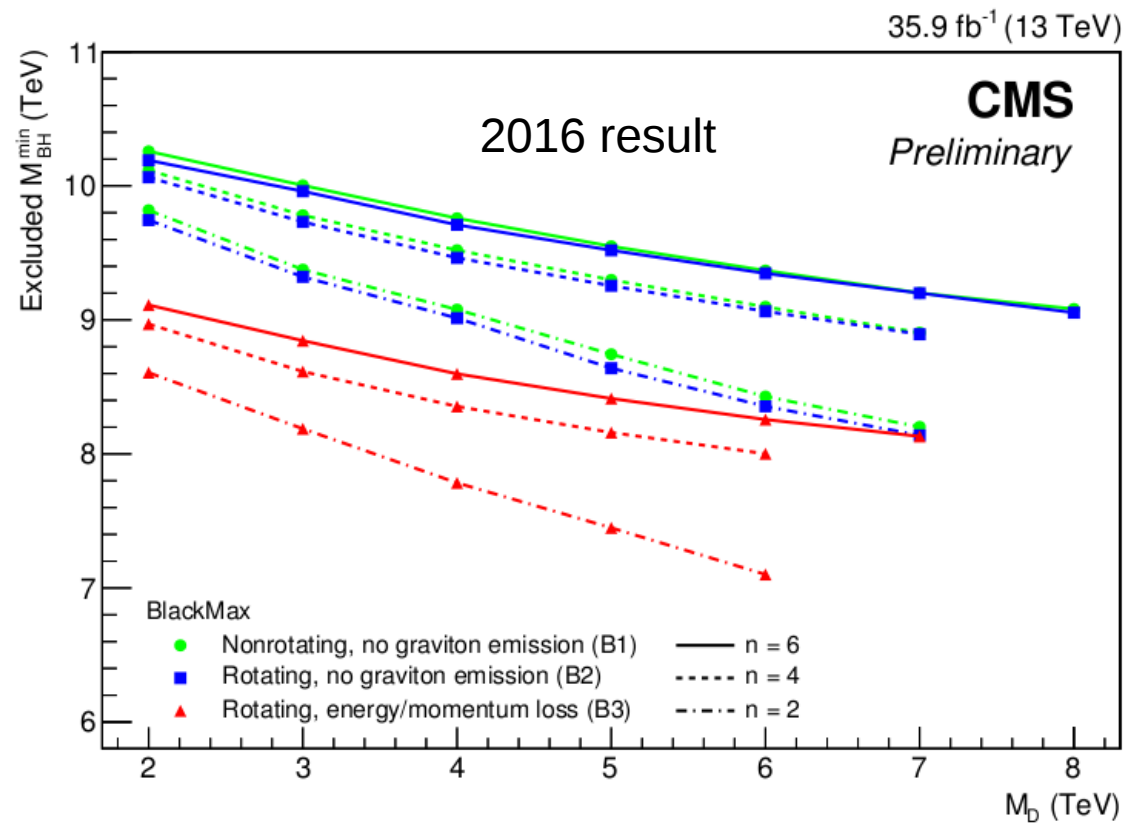
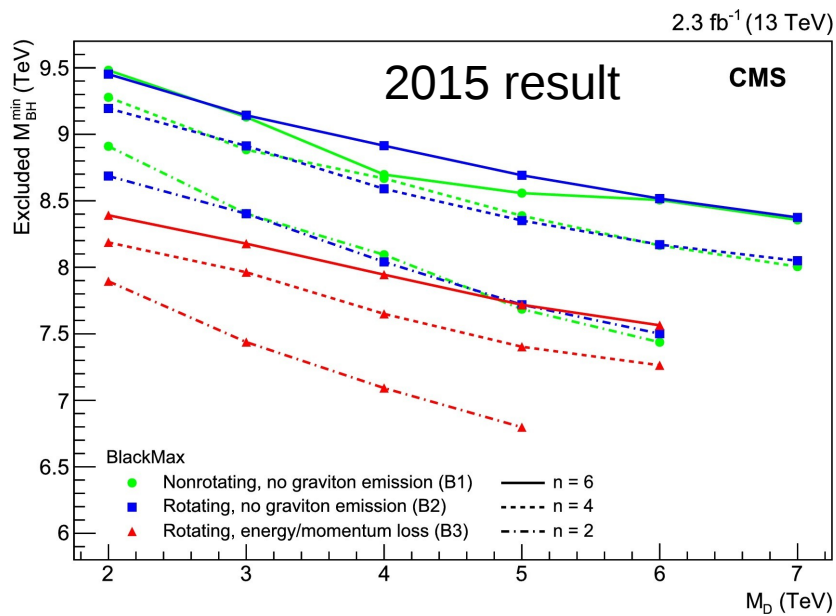


# Model Independent Limits



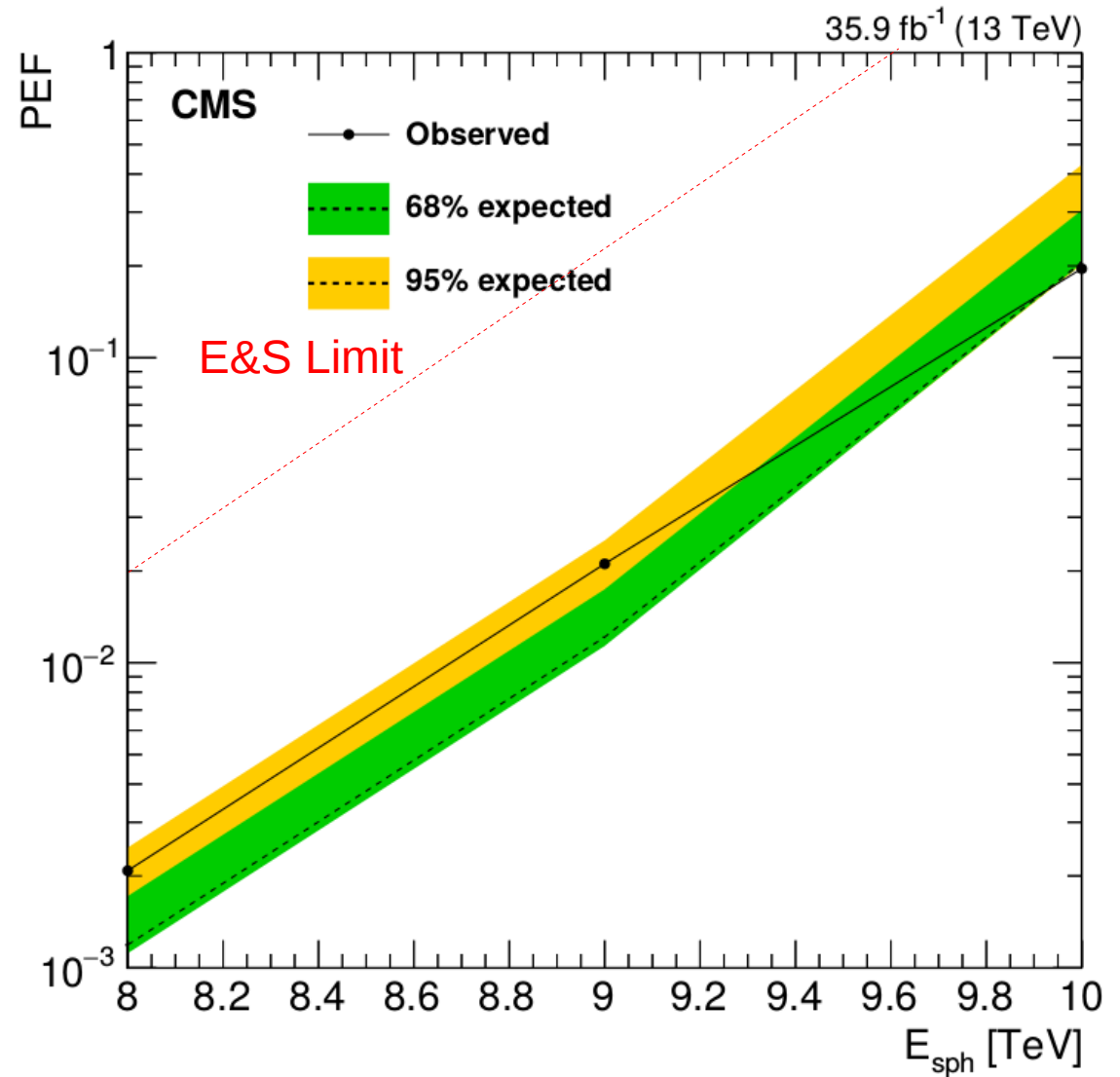
# Model Specific BH Interpretations

- Black Hole limits are pushed about 1 TeV beyond 2015 analysis
- Now including boiling remnant model limits which are nearly the same as the YR model limits



# Sphaleron Limit

- Limit improved by a factor of 10
- Previous limit is a phenomenological study
- First dedicated experimental limit



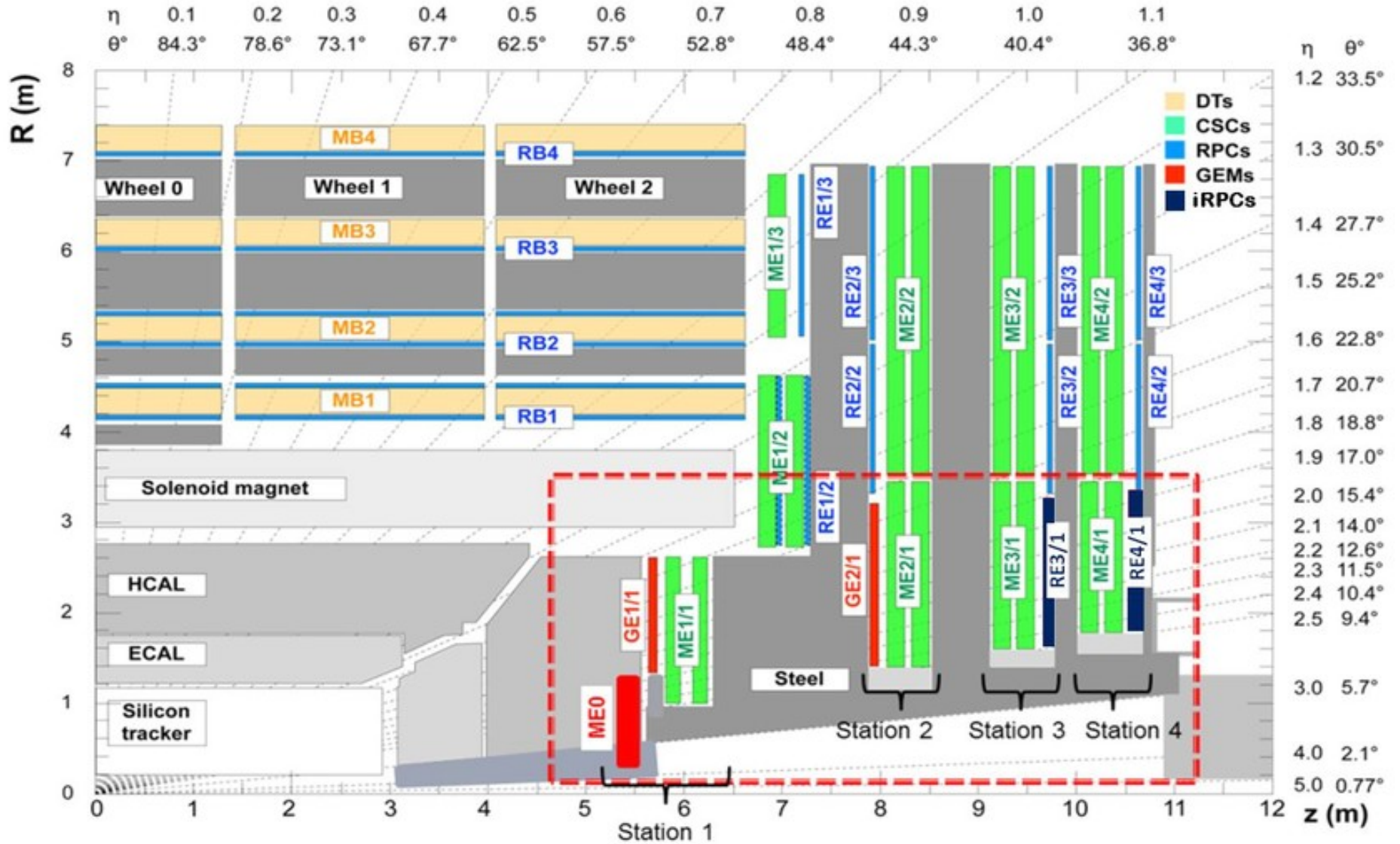
# Possibilities for Future

- Upgrade generator
  - Parameterize relative rates of different fermionic configurations in some reasonable manner
  - Include more specific models which have been proposed
- Build new dedicated analysis for sphalerons
  - Include larger scan of transition energies to also take into account possible BSM physics (arXiv:1611.05466)
  - Build set of more targeted analyses which each target one of the 32 phenomenological final states
    - Lower transition energies will have more background
    - More independent of which fermionic configurations sphaleron transitions “choose” in nature
- Increase beam energy
  - 13 TeV → 14 TeV gives 5x the cross section
  - 14 TeV → 28 TeV gives 2200x the cross section
- Add more integrated luminosity to analysis...

# HL-LHC

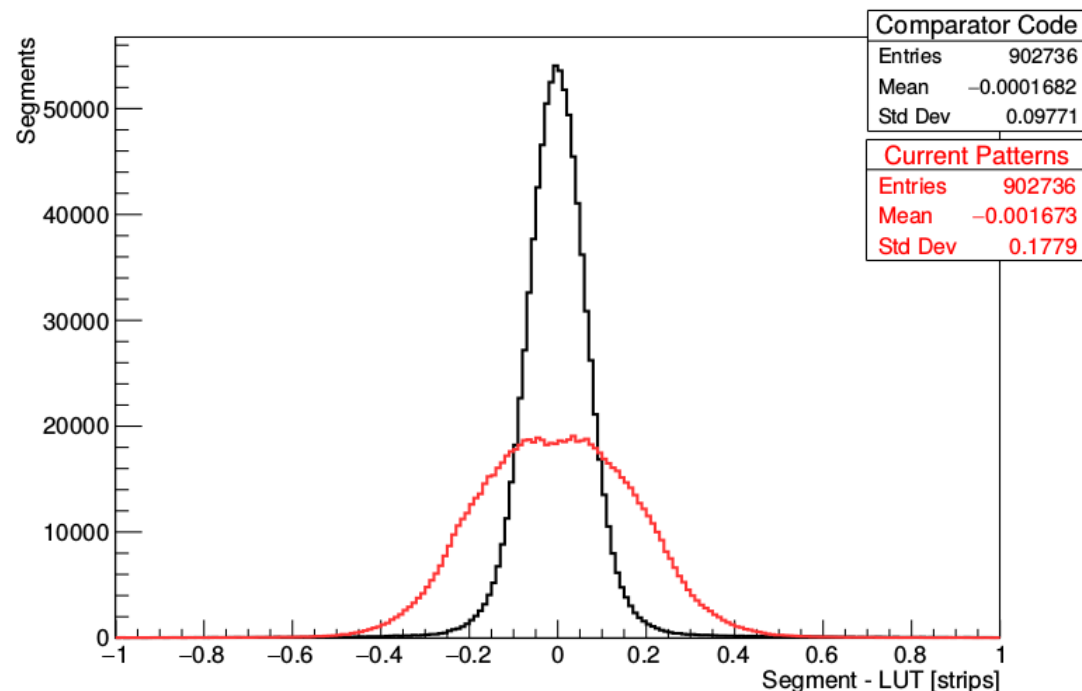
- Upgrade to LHC expected to be finished by 2026
- Expected to increase luminosity up to  $10^{35} \text{ cm}^{-2}\text{s}^{-1}$
- Great for sphalerons but there are challenges
  - More proton-proton interactions per bunch crossing
  - Longer trigger latency
  - Higher trigger frequency: 100 kHz  $\rightarrow$  1 MHz
  - Must upgrade electronics and trigger to keep up with higher demand
  - Detectors must be robust against higher backgrounds

# Muon System Upgrade



# CMS Cathode Strip Chambers

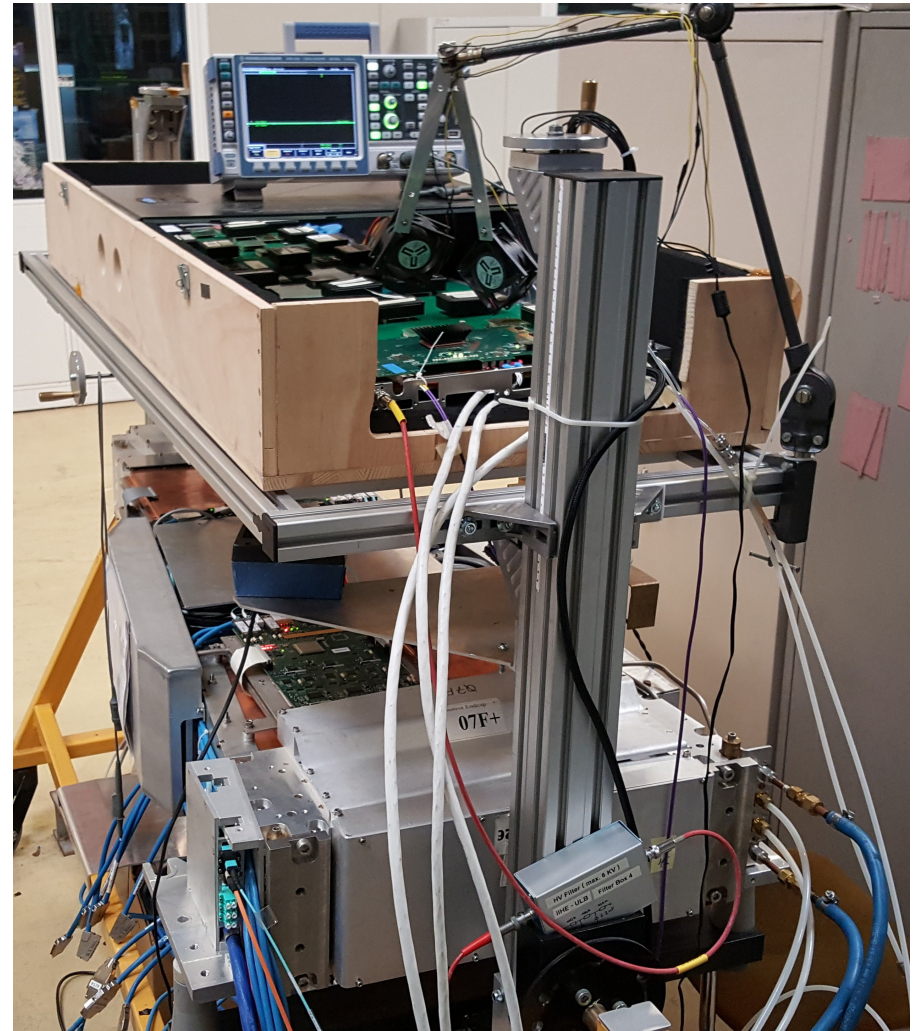
- Upgrade on-chamber electronics to increase bandwidth
- Studied performance of trigger primitives
- My focus has been upgrading local pattern recognition
  - Still a work in progress
  - We expect a factor of 2 better position resolution





# CMS Gas Electron Multipliers

- We installed demonstrator system onto CMS in 2017
  - A lot of effort in getting first generation operational
- My focus: DAQ Electronics
  - Prototype integration
  - DAQ SW/FW development
  - Calibration/Characterization analysis
  - ENC reduced to about 0.5 fC from up to 10 fC





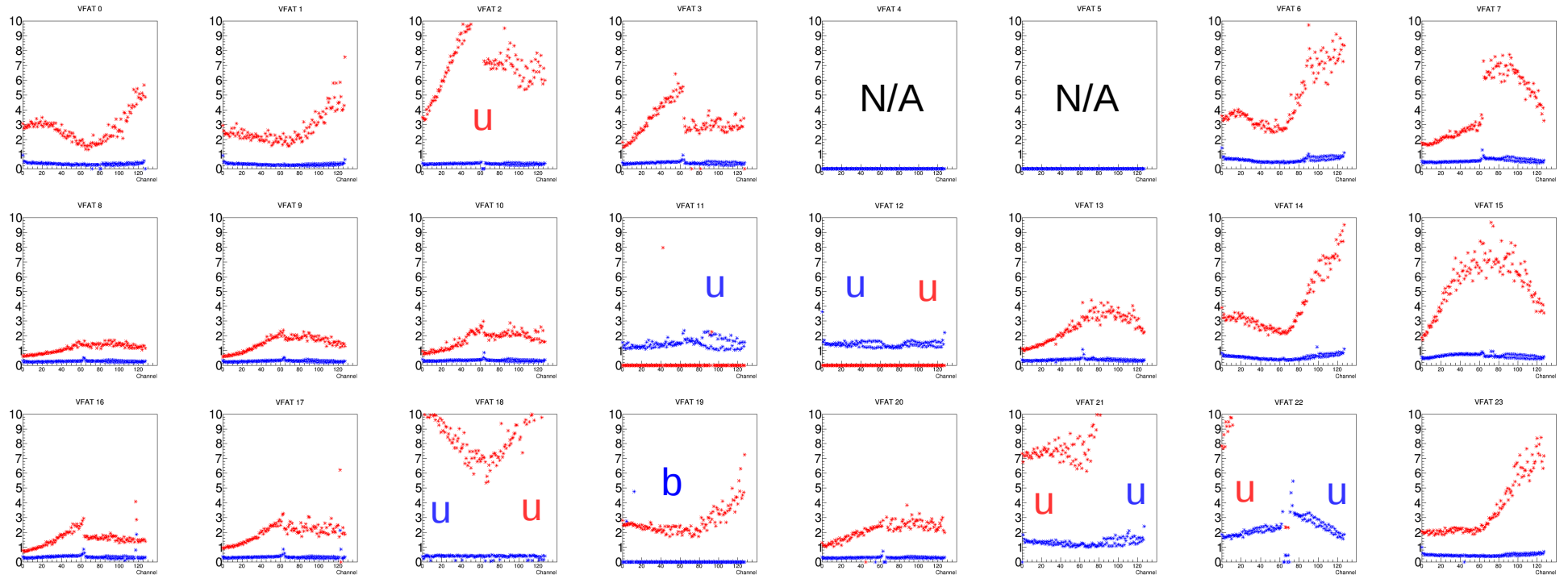
# Summary

- **First** dedicated result on Sphaleron production
  - $\text{PEF} < 0.021$  for  $E_{\text{sph}} = 9 \text{ TeV}$ 
    - Factor of 10 better than previous theorist reinterpretation
  - “Search for black holes and sphalerons in high-multiplicity final states in proton-proton collisions at  $\sqrt{s} = 13 \text{ TeV}$ ” (CMS Collaboration, arXiv:1805.06013) has been approved by CMS and submitted to JHEP
- Built “BaryoGEN, a Monte Carlo Generator for Sphaleron-Like Transitions in Proton-Proton Collisions” (C. Bravo and J. Hauser, arXiv:1805.02786)
  - Establishes a minimal phenomenological model
  - First to include a complete set of fermion configurations in final-state
  - Paper recently accepted for publication in JHEP
- This is just the beginning of sphalerons at the LHC
  - Stay tuned for more extensive searches
  - Just wait until HL-LHC
- Thanks to Jay Hauser, David Saltzberg, Graciela Gelmini, Doojin Kim, John Ellis, Kazuki Sakurai, and Steve Mrenna

Thank you for your attention

# Backup

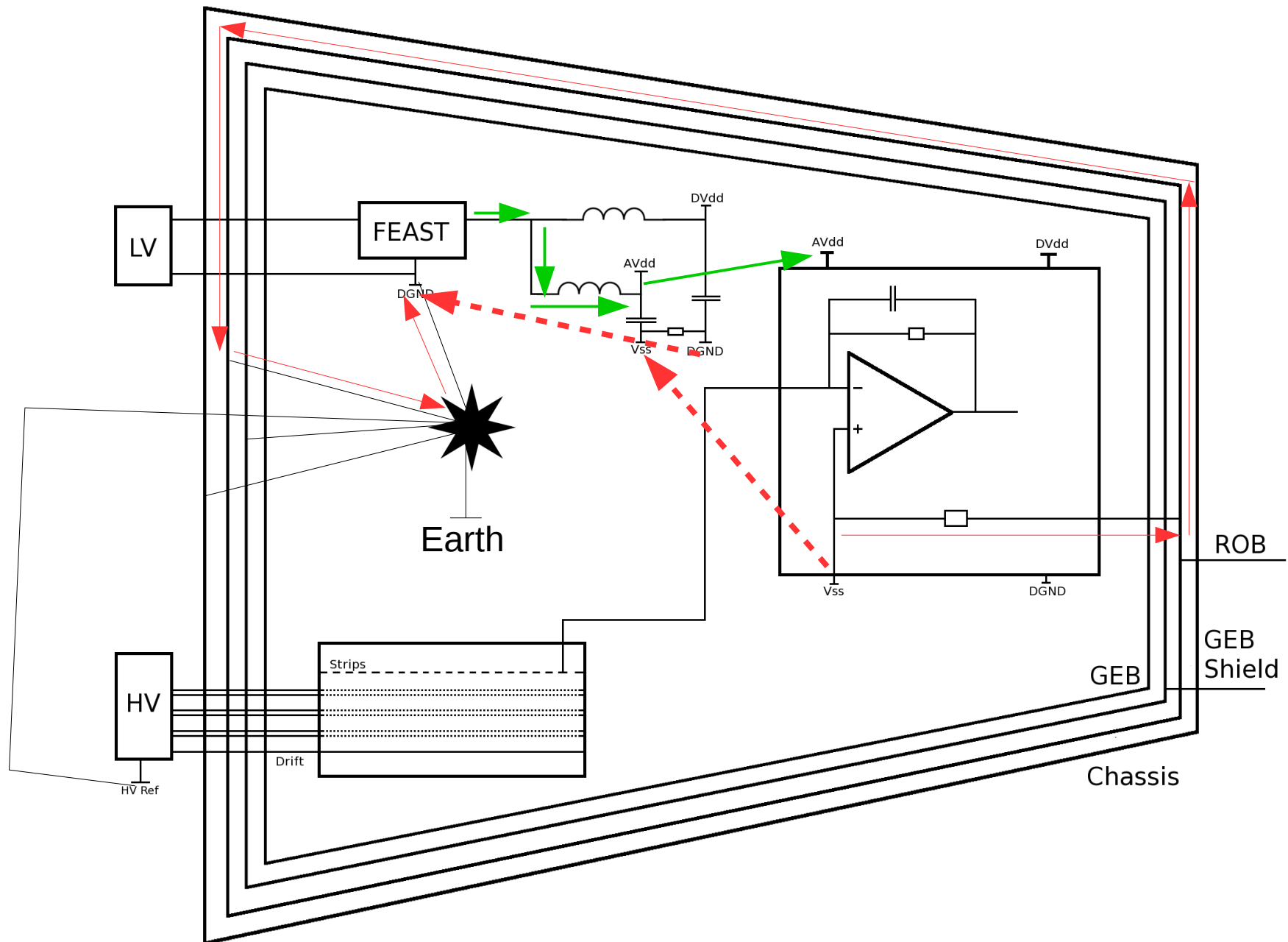
# Killing GEM Noise



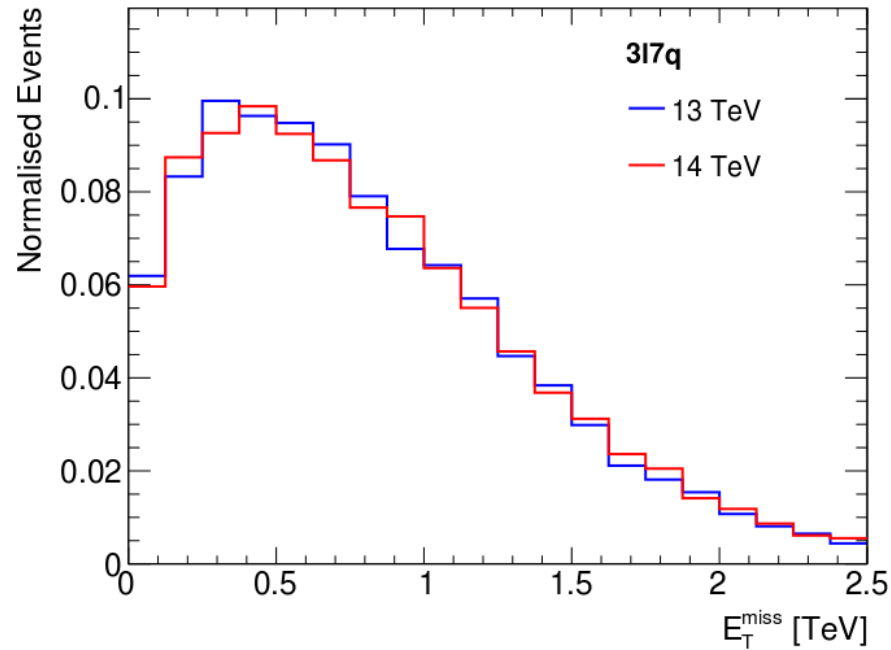
u = uncalibrated

b = broken VFAT

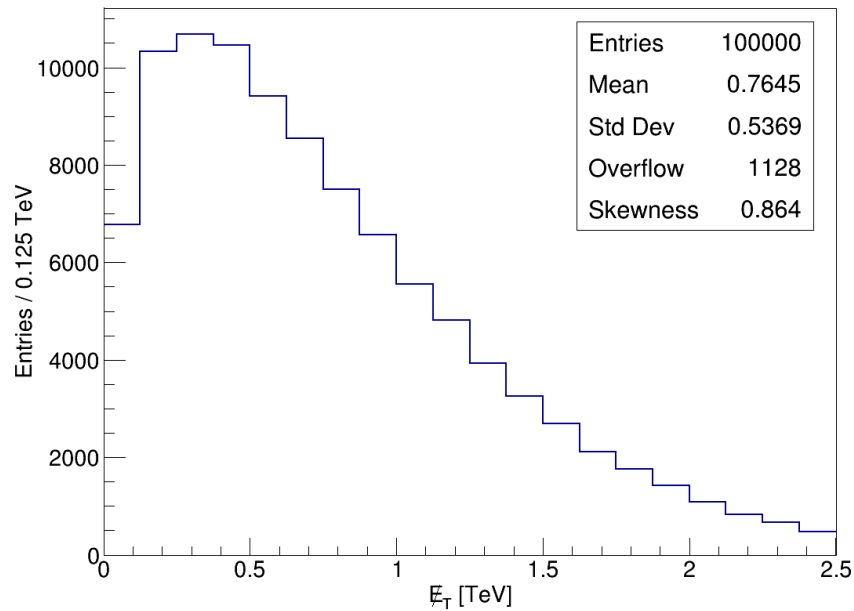
# Analog LV Current Paths



# Comparing MET



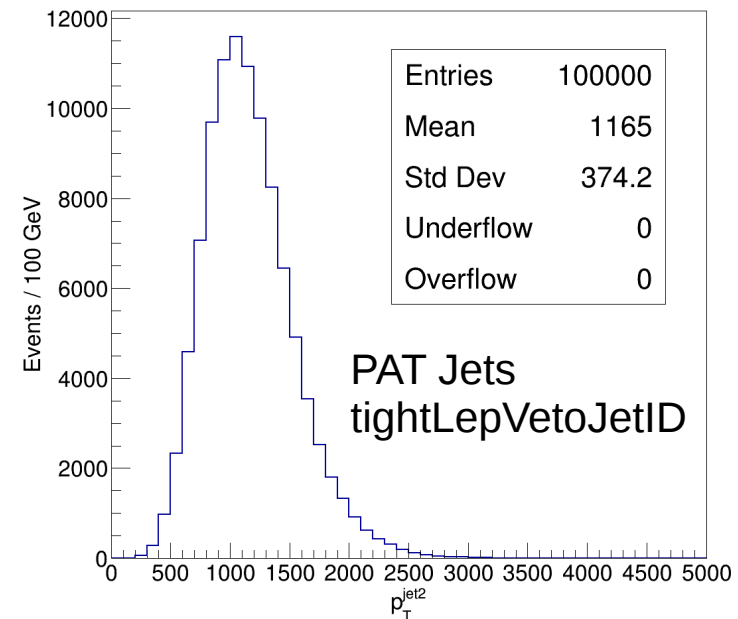
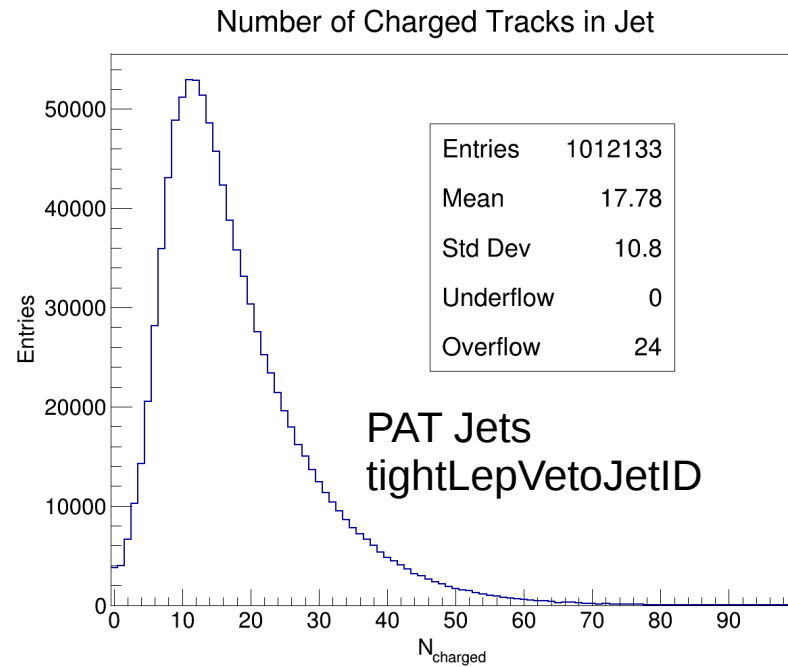
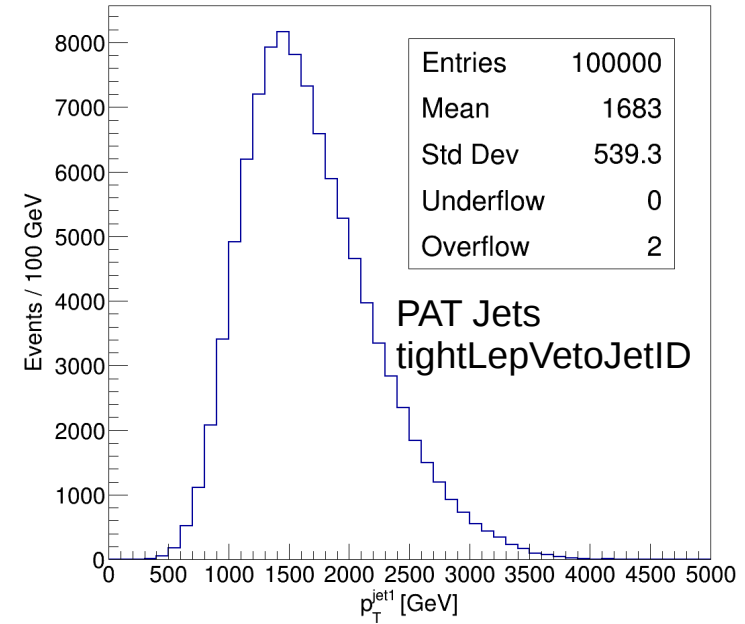
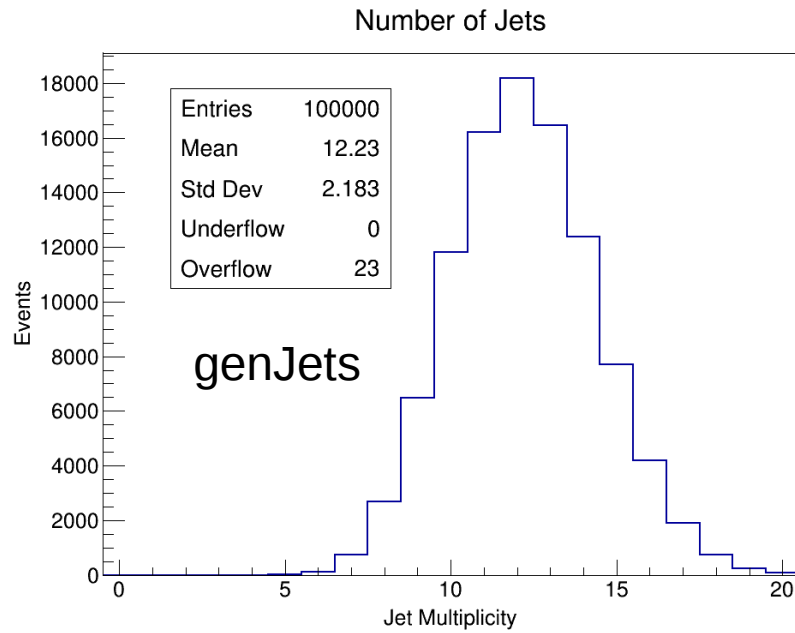
Ellis and  
Sakurai



Mine  
GEN-SIM  
genMET

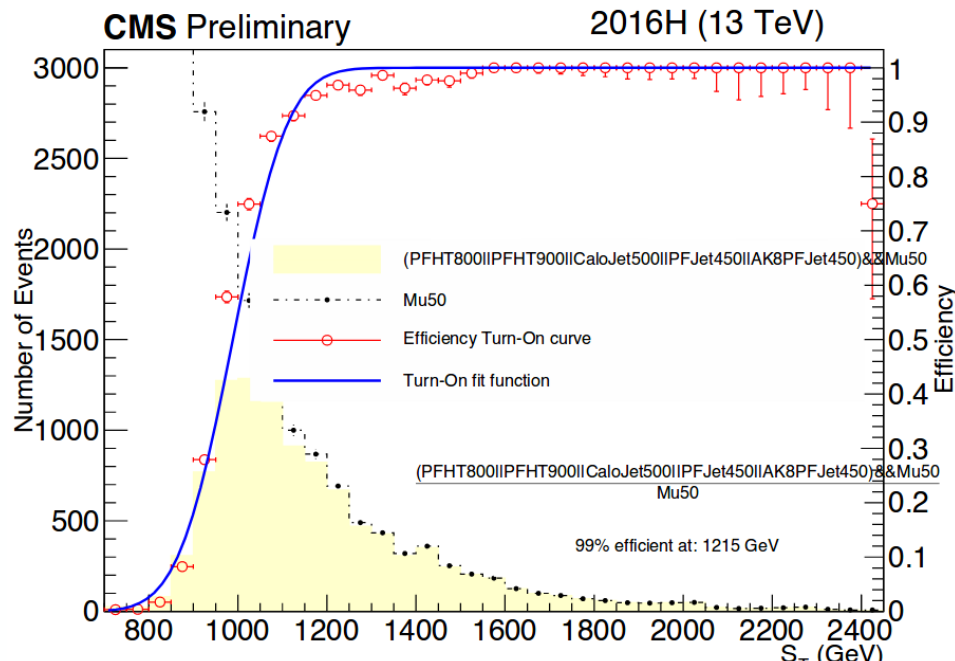
# Hadronic Quantities

$p_T > 50$  and  $|\eta| < 5.2$  everywhere



# Datasets and Triggers

- Primary dataset: JetHT, 03Feb2017 Re-MiniAOD, corresponding to 35.9/fb
  - /JetHT/Run2016B-03Feb2017\_ver2-v2/MINIAOD
  - /JetHT/Run2016C-03Feb2017-v1/MINIAOD
  - /JetHT/Run2016D-03Feb2017-v1/MINIAOD
  - /JetHT/Run2016E-03Feb2017-v1/MINIAOD
  - /JetHT/Run2016F-03Feb2017-v1/MINIAOD
  - /JetHT/Run2016G-03Feb2017-v1/MINIAOD
  - /JetHT/Run2016H-03Feb2017\_ver2-v1/MINIAOD
  - /JetHT/Run2016H-03Feb2017\_ver3-v1/MINIAOD
- Used the lowest un-prescaled HT trigger: HT800 (Except 2016H)
- “OR” of 4 triggers used for 2016H
  - HLT\_PFJET450, HLT\_AK8PFJET450, HLT\_CaloJet500\_NoJetID, HT900
- Full efficiency for  $S_T > 1.6$  TeV, measured w.r.t. Mu50



# Step 2: Choose Fit Functions

- Considered 5 classes of functions commonly used to fit high mass/ $S_\top/H_\top$  spectra
- Used multiple orders of each class of function
- $x = S_\top / 13 \text{ TeV}$  for all functions

CMSBH (from previous CMS BH searches) [\[link\]](#)

$$f_{cmsBH1}(x) = \frac{p_0(1+x)^{p_1}}{x^{p_2 \log x}}$$

$$f_{cmsBH2}(x) = \frac{p_0(1+x)^{p_1}}{x^{p_3+p_2 \log x}}$$

“ATLAS” (from Zgamma search) [\[link\]](#)

$$f_{ATLAS1}(x) = \frac{p_0(1-x^{1/3})^{p_1}}{x^{p_2}}$$

$$f_{ATLAS2}(x) = \frac{p_0(1-x^{1/3})^{p_1}}{x^{p_2+p_3 \log^2(x)}}$$

“UA2” (from UA2 dijet search) [\[link\]](#)

$$f_{UA2_1}(x) = p_0 x^{p_1} e^{p_2 x}$$

$$f_{UA2_2}(x) = p_0 x^{p_1} e^{p_2 x + p_3 x^2}$$

Standard dijet [\[link\]](#)

$$f_{dijet1}(x) = \frac{p_0(1-x)^{p_1}}{x^{p_2}}$$

$$f_{dijet2}(x) = \frac{p_0(1-x)^{p_1}}{x^{p_2+p_3 \log(x)}}$$

$$f_{dijet3}(x) = \frac{p_0(1-x)^{p_1}}{x^{p_2+p_3 \log(x)+p_4 \log^2(x)}}$$

ATLAS BH (3 parameters variants of dijet2) [\[link\]](#)

$$f_{ATLASBH1}(x) = p_0(1-x)^{p_1} x^{p_2 \log(x)}$$

$$f_{ATLASBH2}(x) = p_0(1-x)^{p_1} (1+x)^{p_2 \log(x)}$$

$$f_{ATLASBH3}(x) = p_0(1-x)^{p_1} e^{p_2 \log(x)}$$

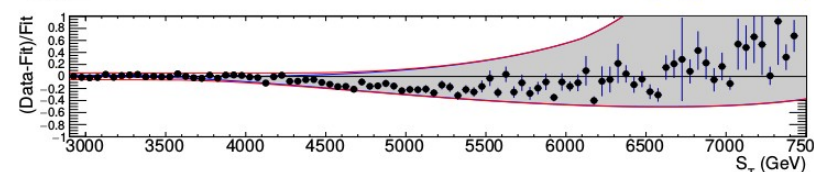
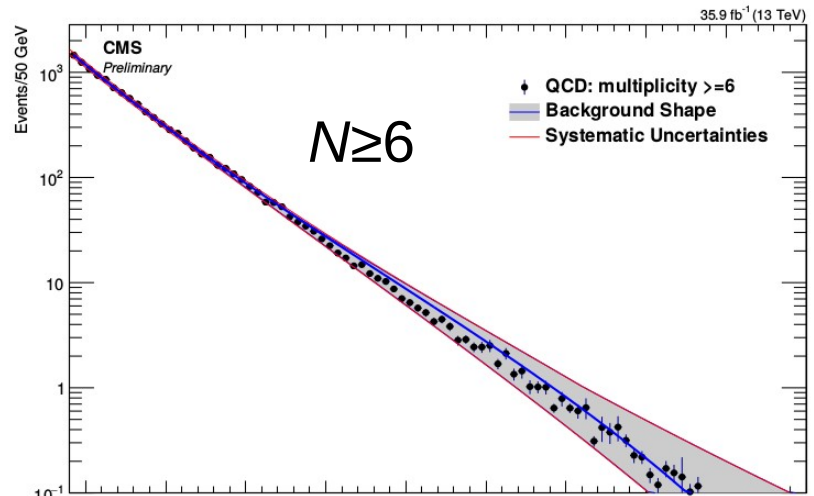
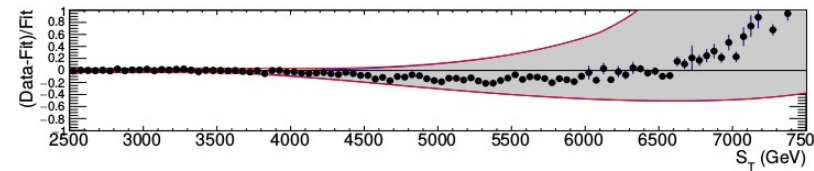
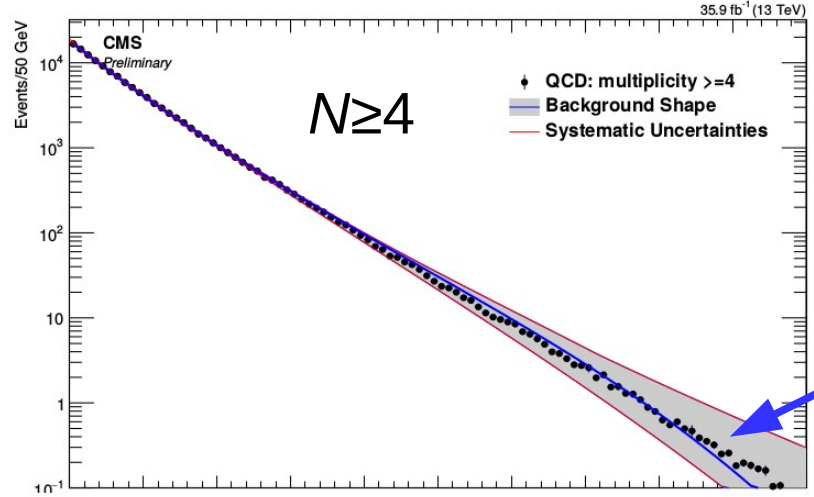
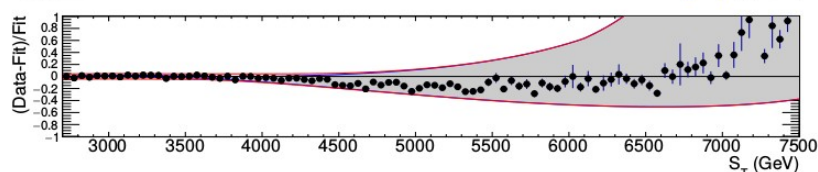
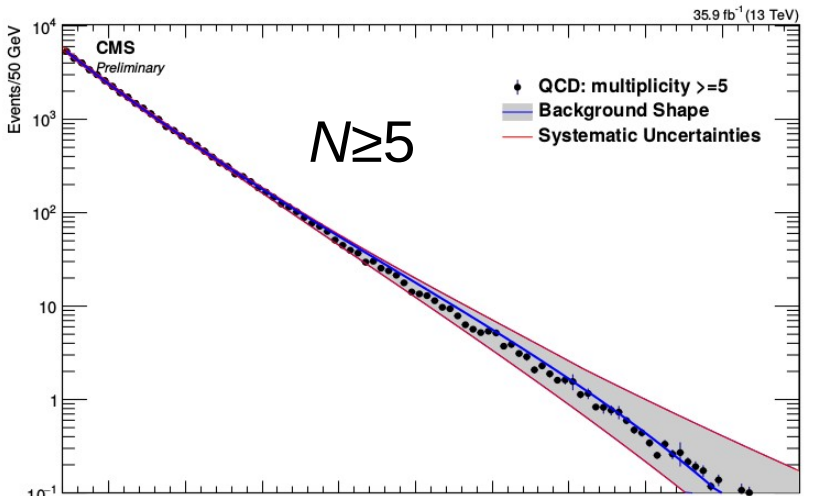
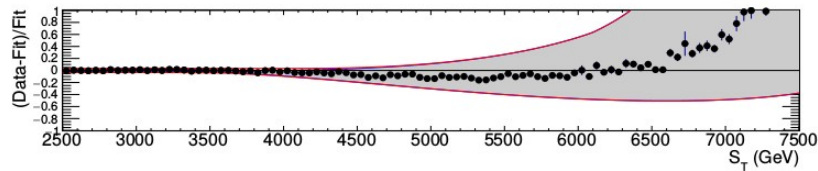
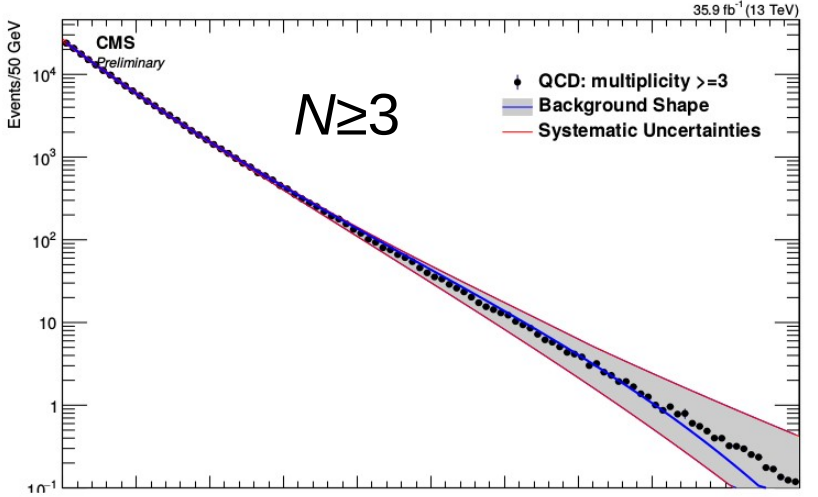
$$f_{ATLASBH4}(x) = p_0(1-x^{1/3})^{p_1} x^{p_2 \log(x)}$$

$$f_{ATLASBH5}(x) = p_0(1-x)^{p_1} x^{p_2 x}$$

$$f_{ATLASBH6}(x) = p_0(1-x)^{p_1} (1+x)^{p_2 x}$$

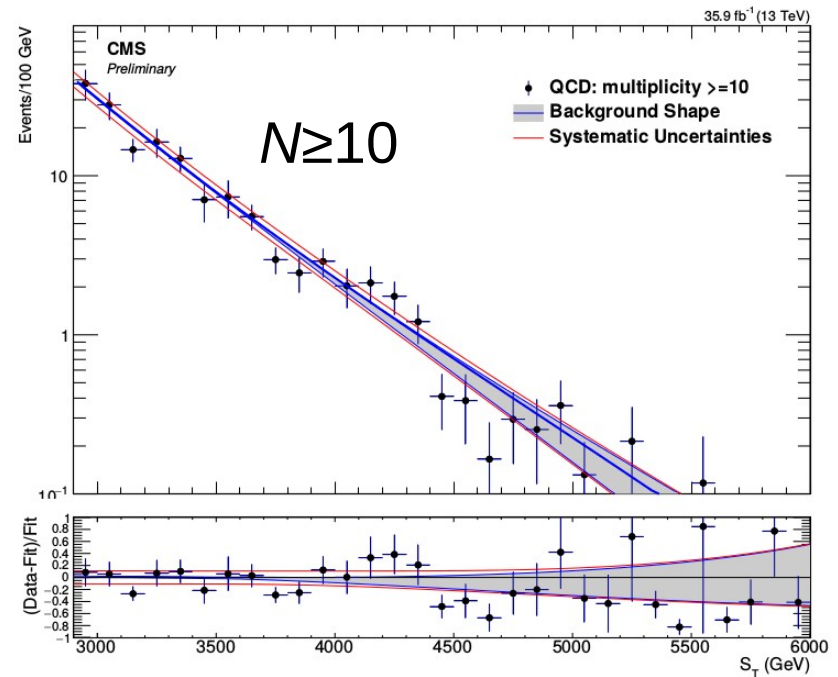
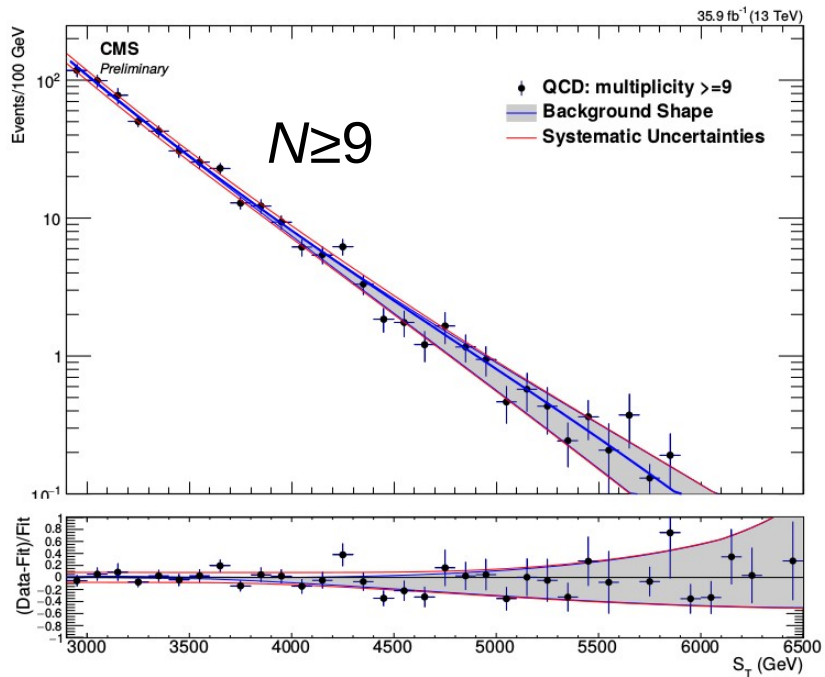
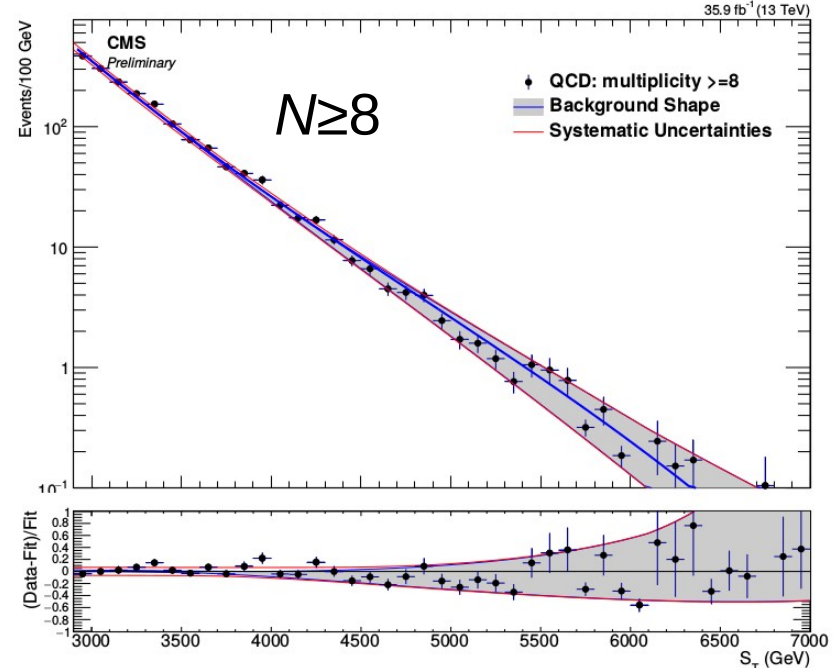
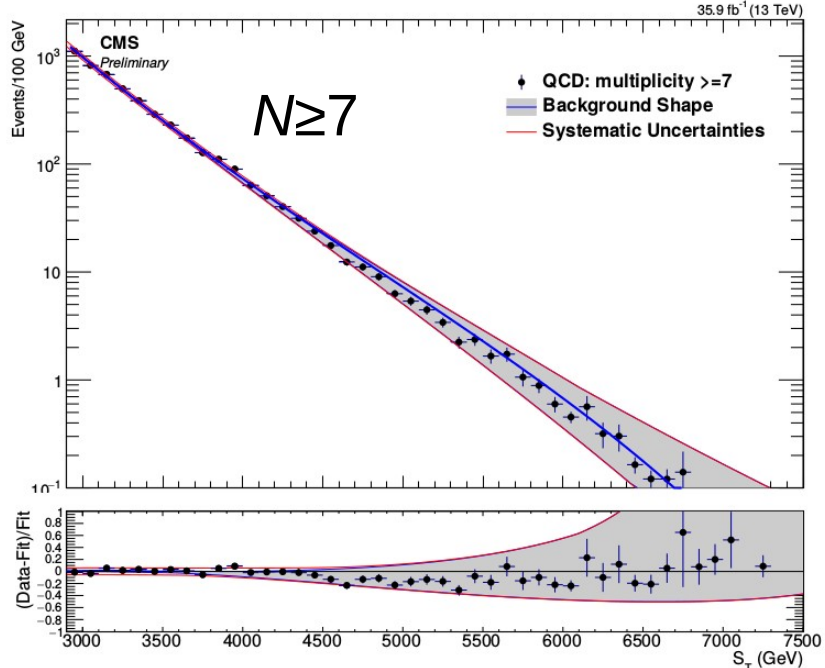


# Closure of Background Estimate using QCD MC



Shape systematics large compared to central prediction bias

# Closure of Background Estimate using QCD MC



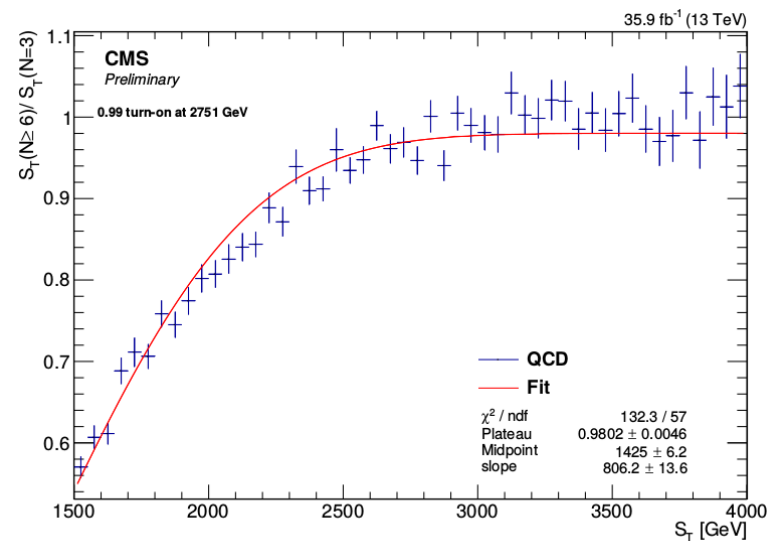
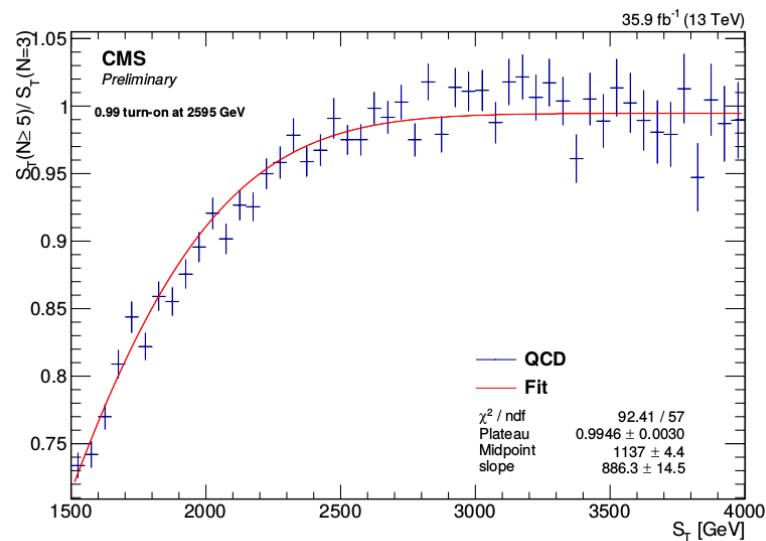
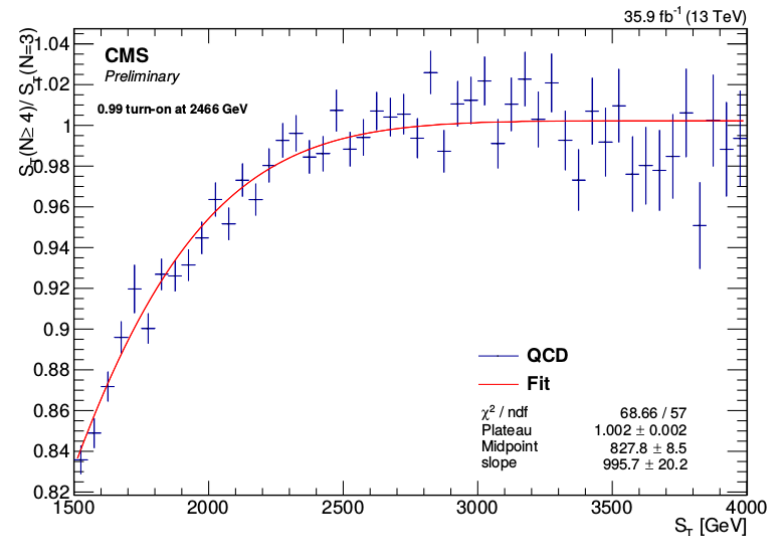
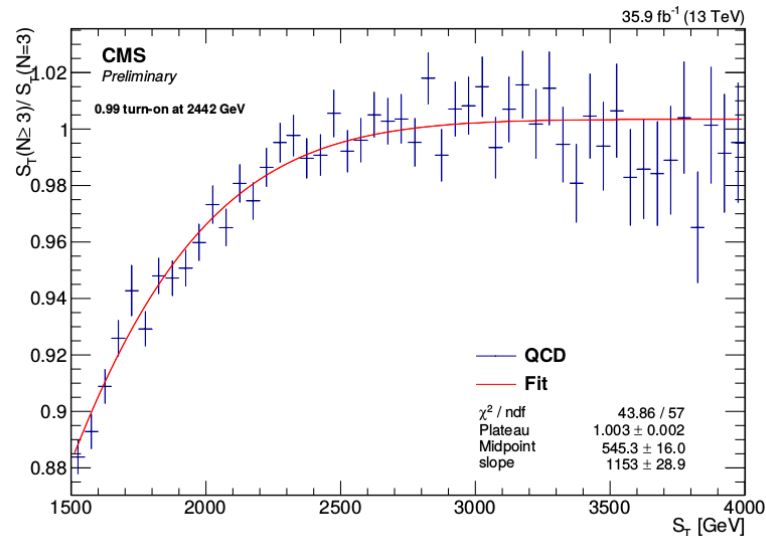
# Phenomenological Final States

- Choose an ordering of the doublets for labeling
  - I personally like **l1 q1 q1 q1 l2 q2 q2 q2 l3 q3 q3 q3**
- Many of the 1,330,560 different final states are phenomenologically identical
  - **e uud μ ccs τ ttb**
  - **e udu μ csc τ tbt** these are different in QM (color charge)
- At CMS u, d, c, and s are difficult to distinguish from each other. There are 8 lepton configurations and 4 configurations of 3 3<sup>rd</sup> generation quarks, making **32** phenomenological final states
  - 1/8 have 3 neutrinos (before W decays)
  - ttt, ttb, tbb, and bbb 3<sup>rd</sup> generation quark configurations each characterize 1/8, 3/8, 3/8, 1/8 of the final states respectively

# Background MC Samples

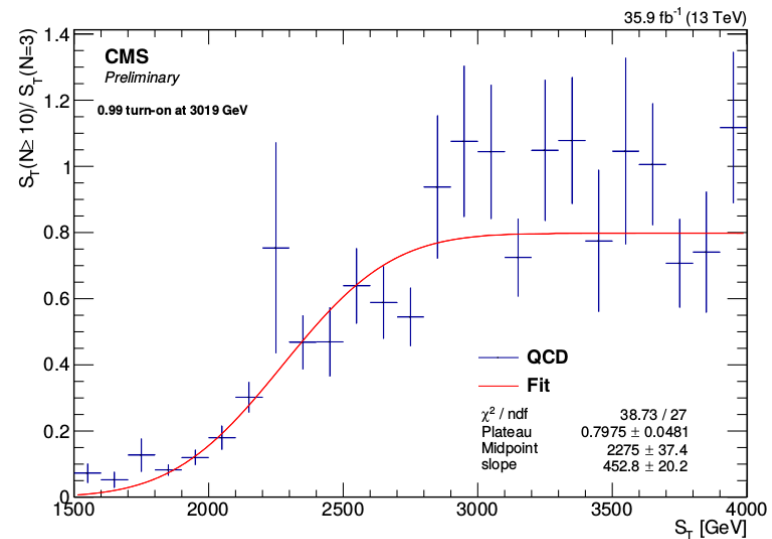
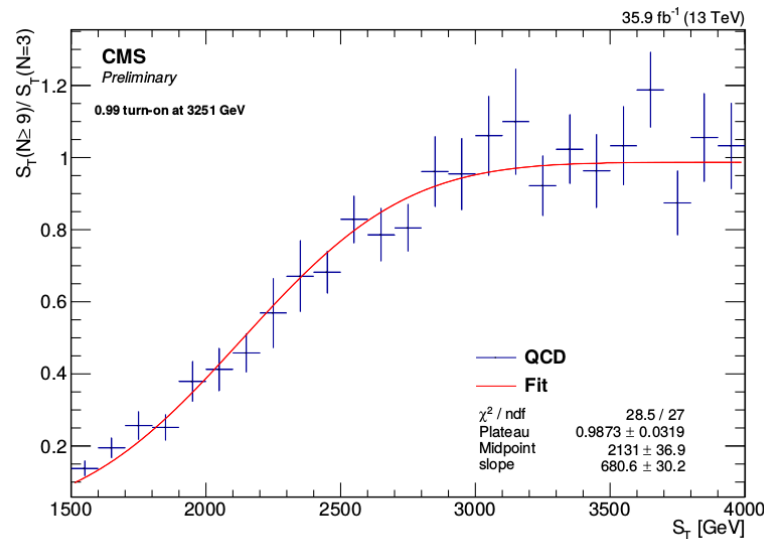
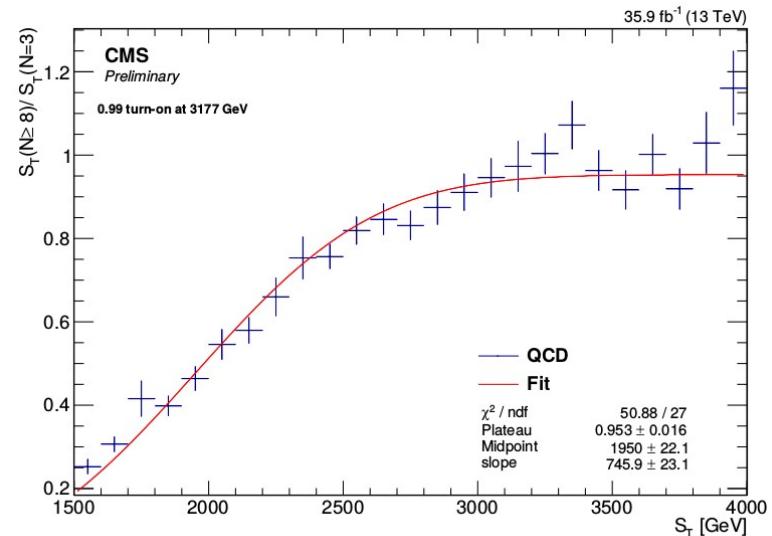
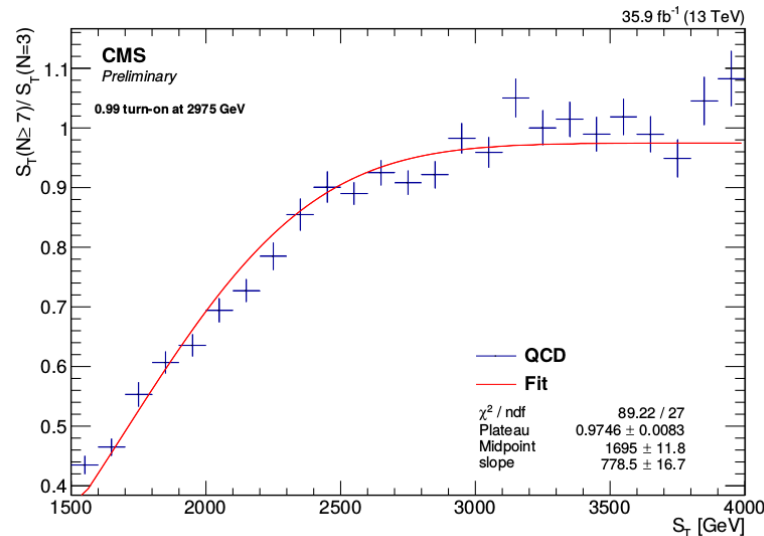
Sample	*/RunII Summer16 MiniAODv2-PUMoriond17_80X_mcRun2_asymptotic_2016_TracheIV_v6-v1/MINIAODSIM	Number of Events	Cross-section [pb]
y+jets	GJets_HT-600ToInf_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	2463946	93.38
	GJets_HT-400To600_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	2529729	277.4
	GJets_HT-200To400_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	10036487	2300
Drell-Yan	DYJetsToNuNu_PtZ-650ToInf_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	1022595	0.02639
+ Jets	DYJetsToNuNu_PtZ-400To650_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	1050705	0.2816
	DYJetsToNuNu_PtZ-250To400_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	1052985	2.082
	DYJetsToNuNu_PtZ-100To250_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	5353639	55.03
	DYJetsToNuNu_PtZ-50To100_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	21953584	593.9
	DYJetsToNuNu_Zpt-0To50_TuneCUETP8M1_13TeV-amcatnloFXFX-pythia8	47728607	3483
	DYJetsToQQ_HT180_13TeV-madgraphMLM-pythia8	12055100	1187
W+Jets	WJetsToLNu_HT-2500ToInf_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	253561	0.03216
	WJetsToLNu_HT-1200To2500_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	244532	1.329
	WJetsToLNu_HT-800To1200_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	1544513	5.501
	WJetsToLNu_HT-600To800_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	3779141	12.05
	WJetsToLNu_HT-400To600_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	1963464	48.91
	WJetsToQQ_HT180_13TeV-madgraphMLM-pythia8	22402469	2788
QCD	QCD_Pt_3200toInf_TuneCUETP8M1_13TeV_pythia8	391735	0.000165445
	QCD_Pt_2400to3200_TuneCUETP8M1_13TeV_pythia8	399226	0.00682981
	QCD_Pt_1800to2400_TuneCUETP8M1_13TeV_pythia8	397660	0.114943
	QCD_Pt_1400to1800_TuneCUETP8M1_13TeV_pythia8	396409	0.84265
	QCD_Pt_1000to1400_TuneCUETP8M1_13TeV_pythia8	2999069	9.4183
	QCD_Pt_800to1000_TuneCUETP8M1_13TeV_pythia8	3992112	32.293
	QCD_Pt_600to800_TuneCUETP8M1_13TeV_pythia8	3896412	186.9
	QCD_Pt_470to600_TuneCUETP8M1_13TeV_pythia8	3959986	648.2
	QCD_Pt_300to470_TuneCUETP8M1_13TeV_pythia8	4150588	7823
	QCD_Pt_170to300_TuneCUETP8M1_13TeV_pythia8	6958708	117276
	QCD_Pt_120to170_TuneCUETP8M1_13TeV_pythia8	6708572	471100
	QCD_Pt_80to120_TuneCUETP8M1_13TeV_pythia8	6986740	2.76253e+06
	QCD_Pt_50to80_TuneCUETP8M1_13TeV_pythia8	9954370	1.92043e+07
	QCD_Pt_300to470_TuneCUETP8M1_13TeV_pythia8	4150588	7823
tthbar	TTJets_TuneCUETP8M1_13TeV-madgraphMLM-pythia8	10139950	502.2

# MC $S_T$ Shape Invariance Turn-On



- Fit ratio of inclusive spectra to  $N=3$  spectrum and fit to error function to decide where normalization regions are for each multiplicity individually
- Normalization regions are determined based on MC

# MC $S_T$ Shape Invariance Turn-On



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# Counting Final States

- There are  $\frac{\prod_{n=1}^6 \binom{2n}{2}}{6!} = 10395$  doublet pairings
- There are also 7 factors of 2 , one for each pair (2 possible SU(2) index choices) and the 7<sup>th</sup> for the sign of the Chern-Simons Number, giving a total of 1,330,560 quantum mechanically unique final states

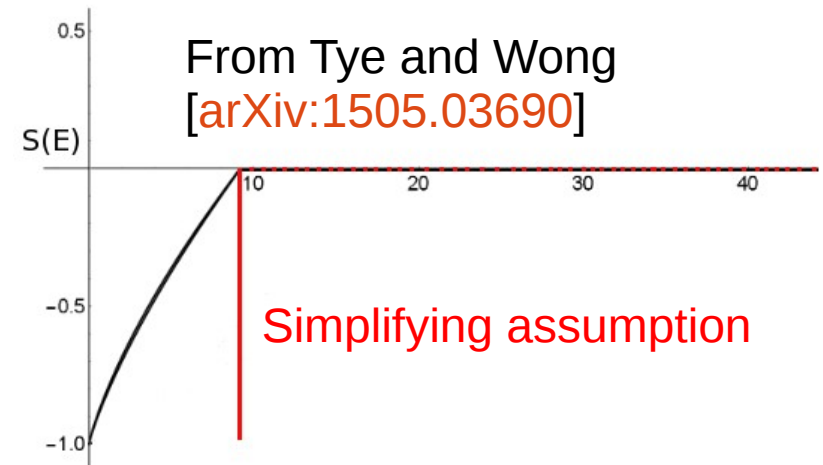


# Monte Carlo Integration

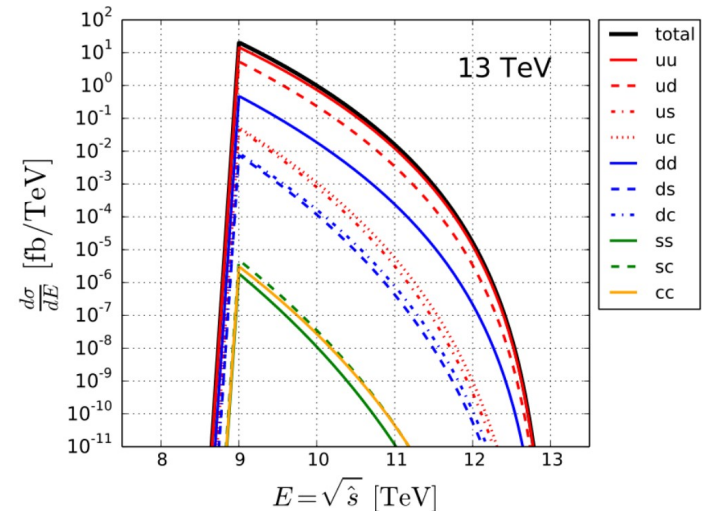
- I am approximating integrals I found in **Ellis and Sakurai**

$$\sigma(\Delta n = \pm 1) = \frac{1}{m_W^2} \sum_{ab} \int dE \frac{d\mathcal{L}_{ab}}{dE} p \exp\left(c \frac{4\pi}{\alpha_W} S(E)\right)$$

$$\frac{d\mathcal{L}_{ab}}{dE} = \frac{2E}{E_{\text{CM}}^2} \int_{\ln \sqrt{\tau}}^{-\ln \sqrt{\tau}} dy f_a(\sqrt{\tau} e^y) f_b(\sqrt{\tau} e^{-y})$$



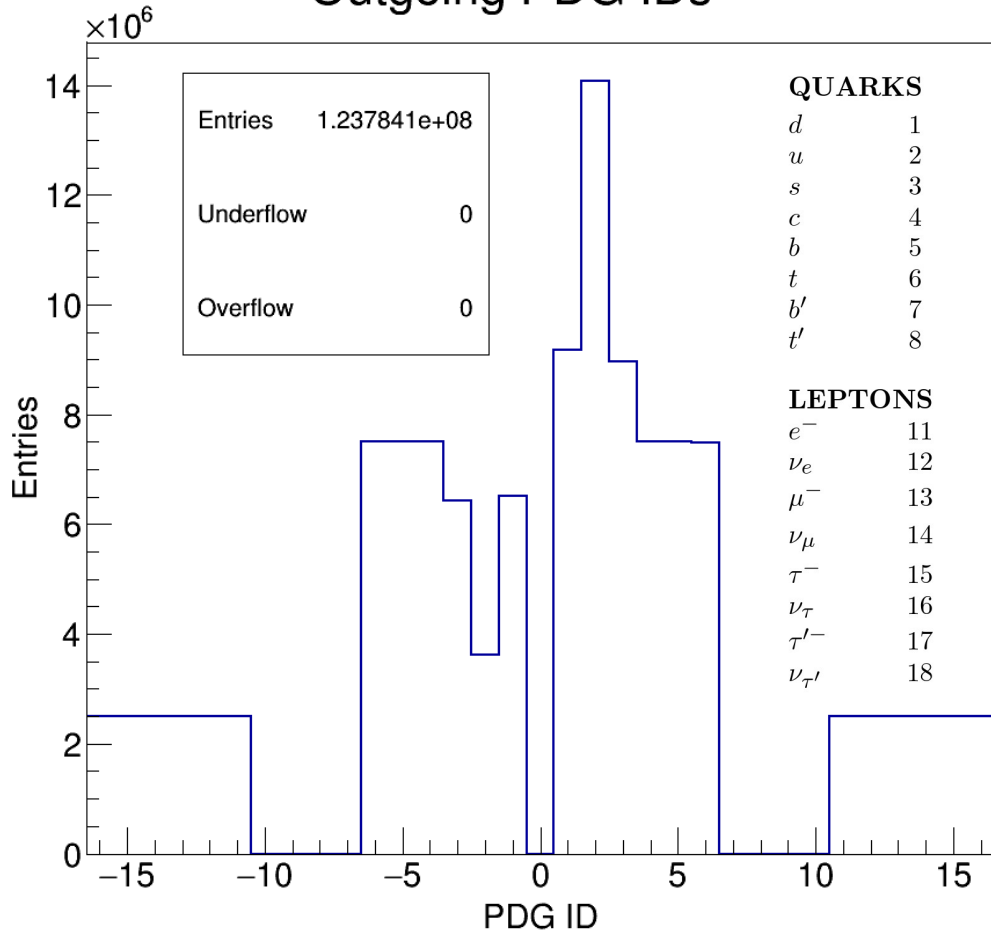
- Made a simplifying assumption to make the MC more efficient



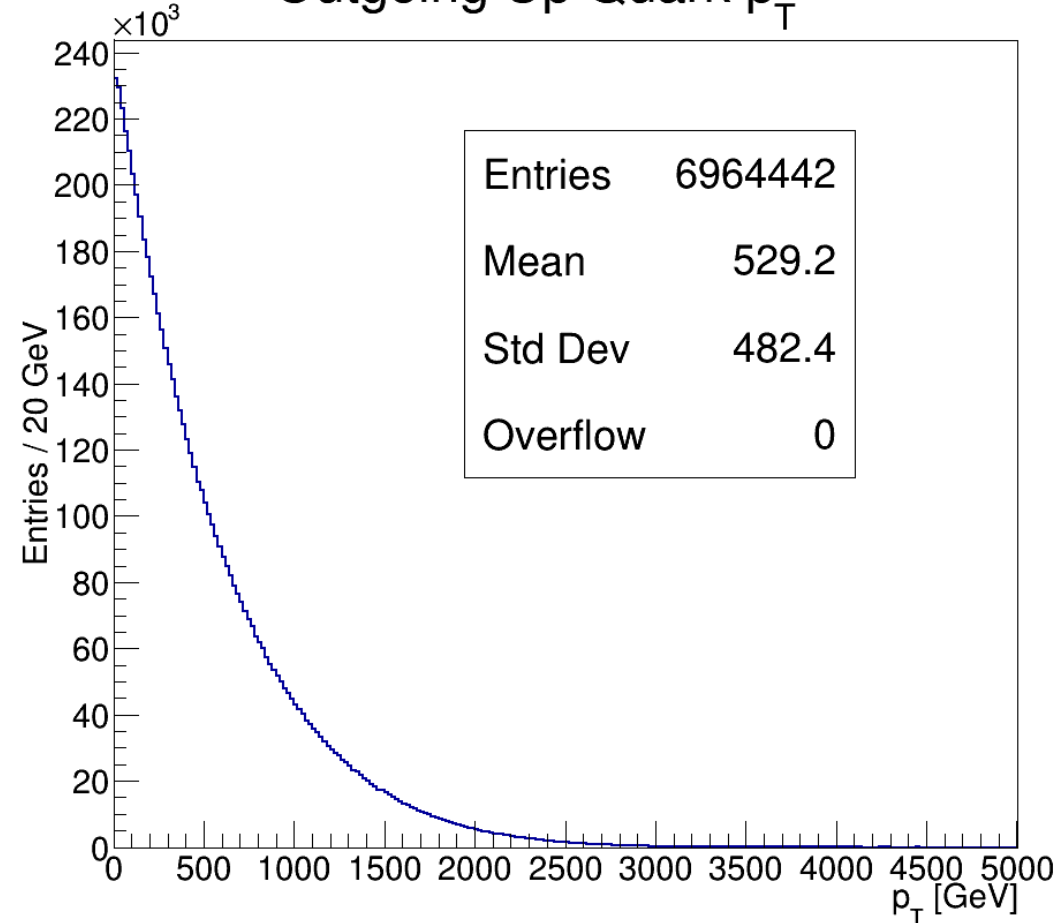


# Outgoing Particles

Outgoing PDG IDs



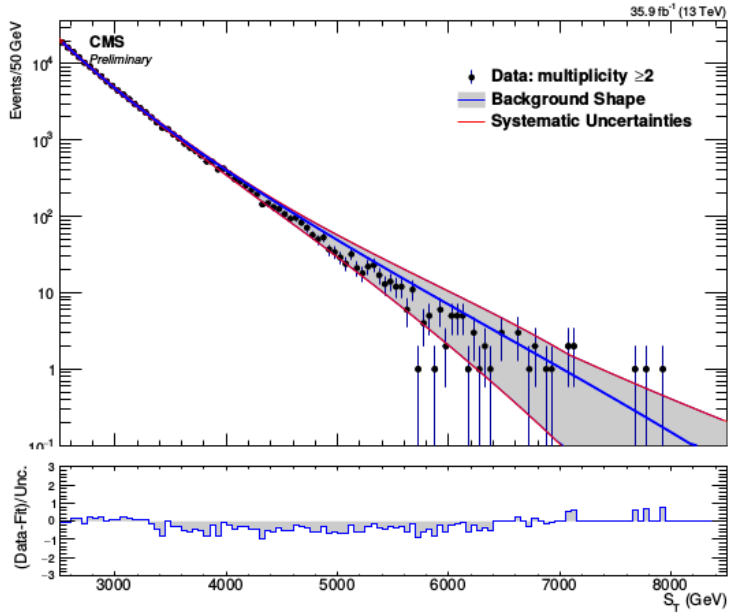
Outgoing Up Quark  $p_T$



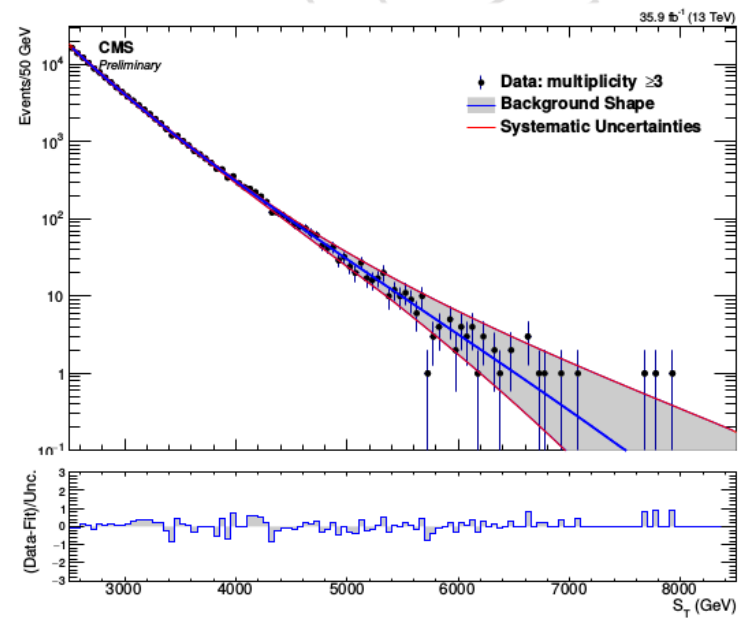
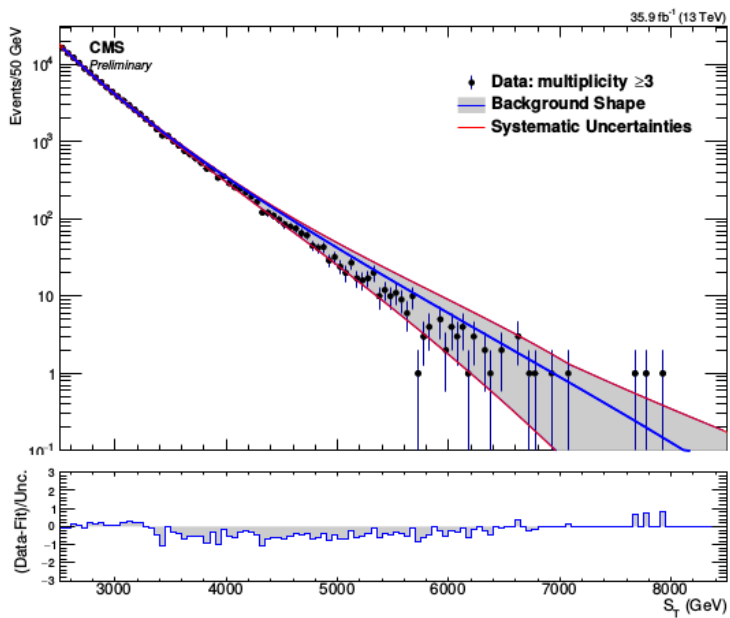
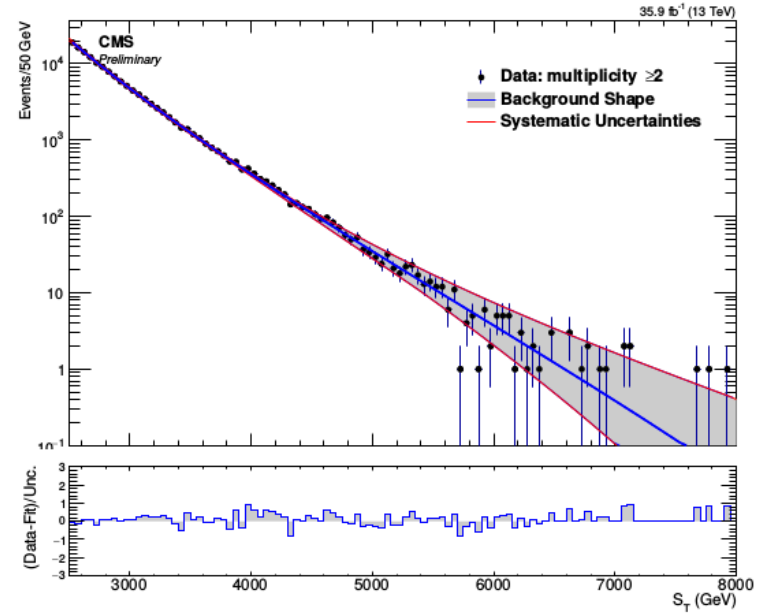
- Peak at two and dip at minus two makes sense because u quarks are most probable incoming type so anti-ups get canceled most often
- Have looked at kinematics of all outgoing particles and they all look reasonable

# Crosscheck with Fit to N=2

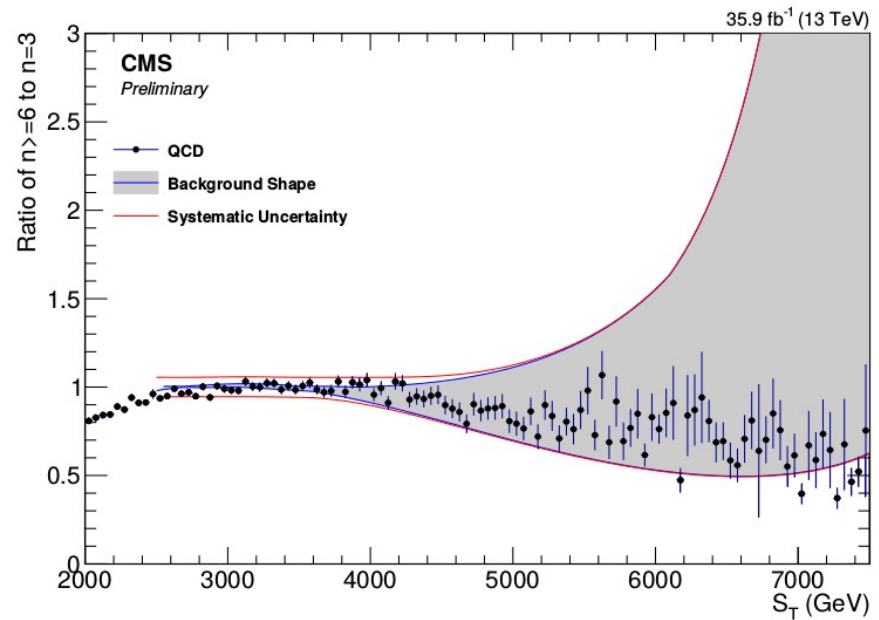
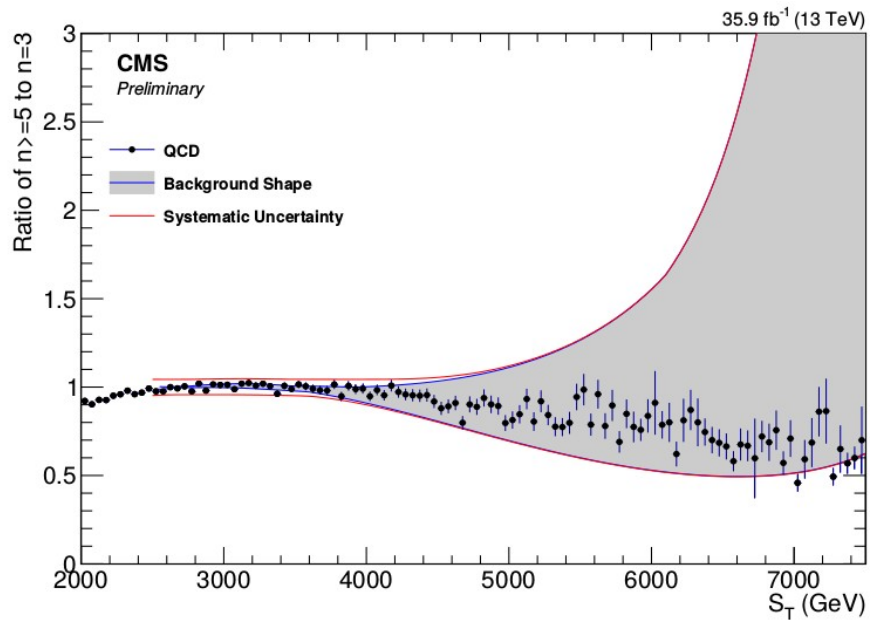
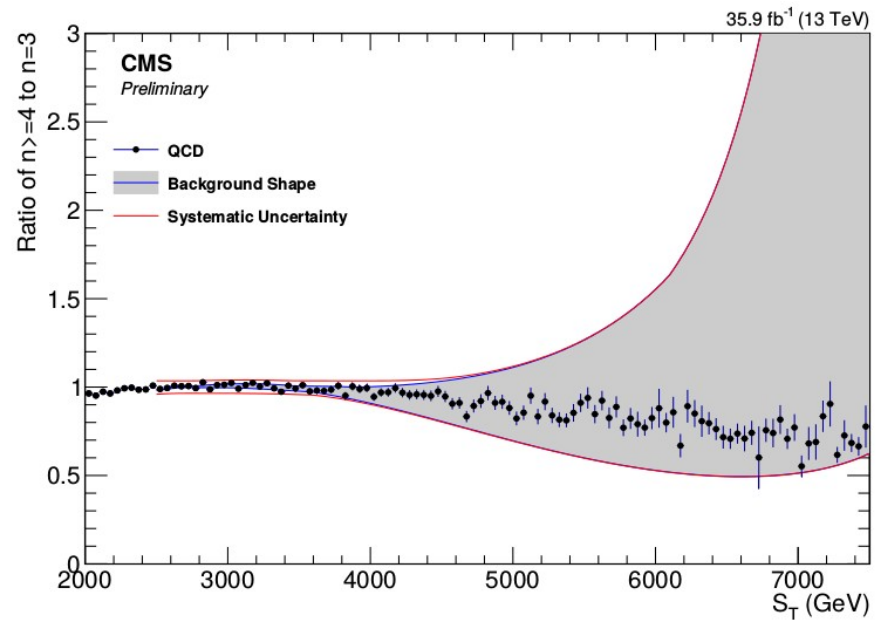
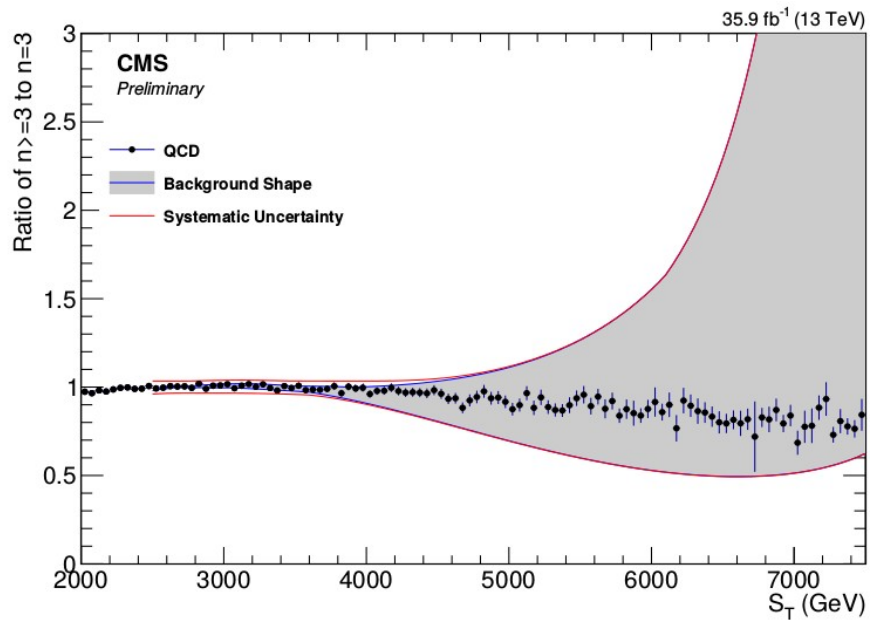
## Fit to N=2



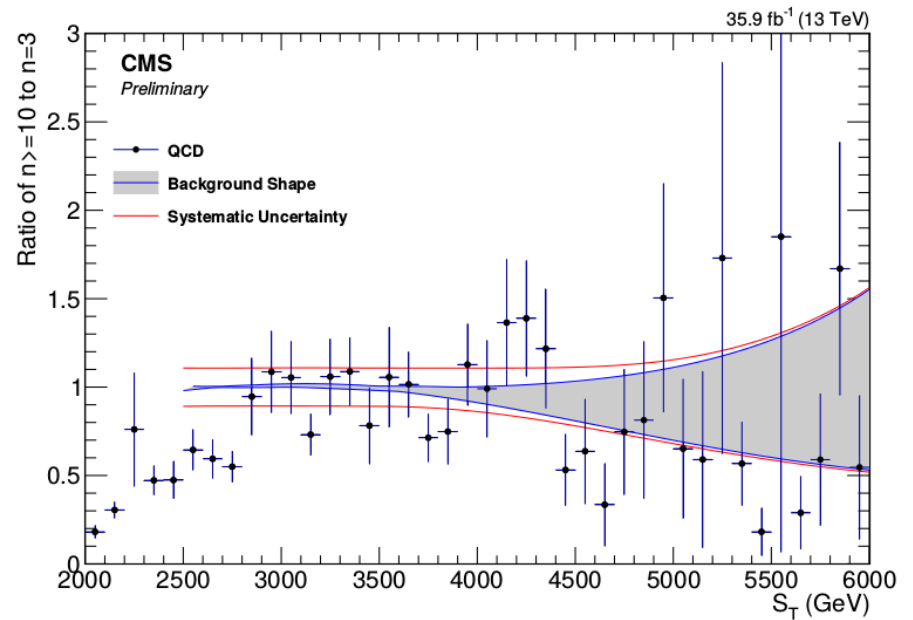
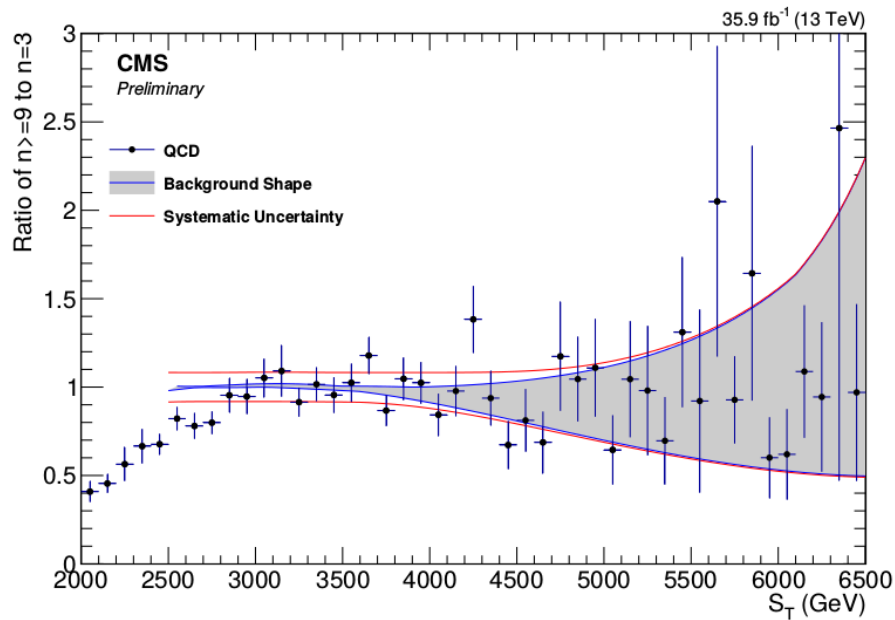
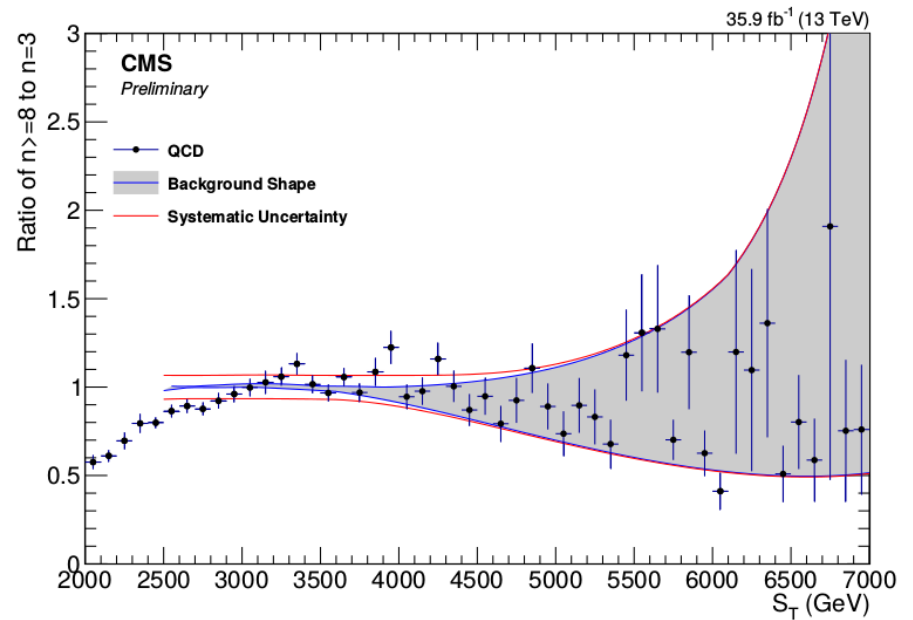
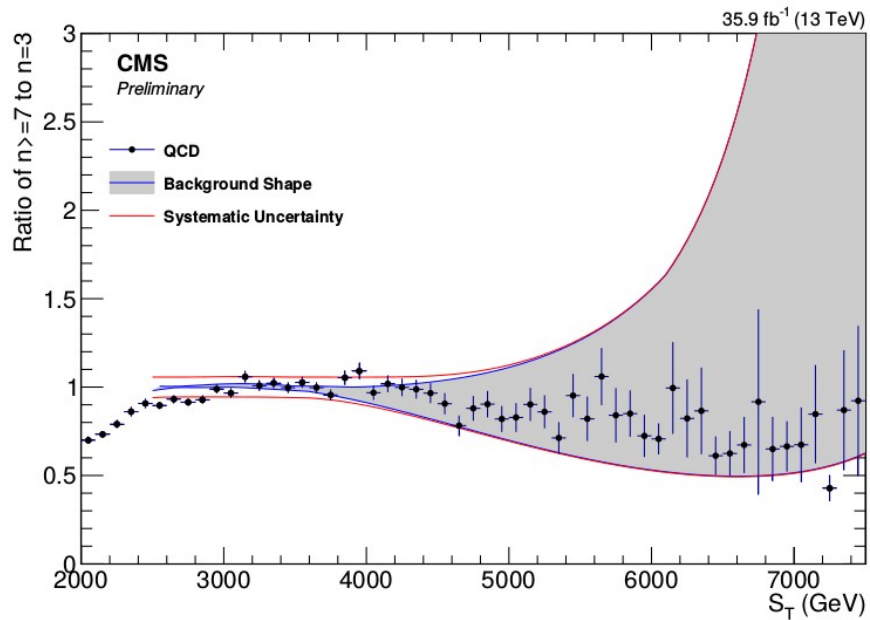
## Fit to N=3



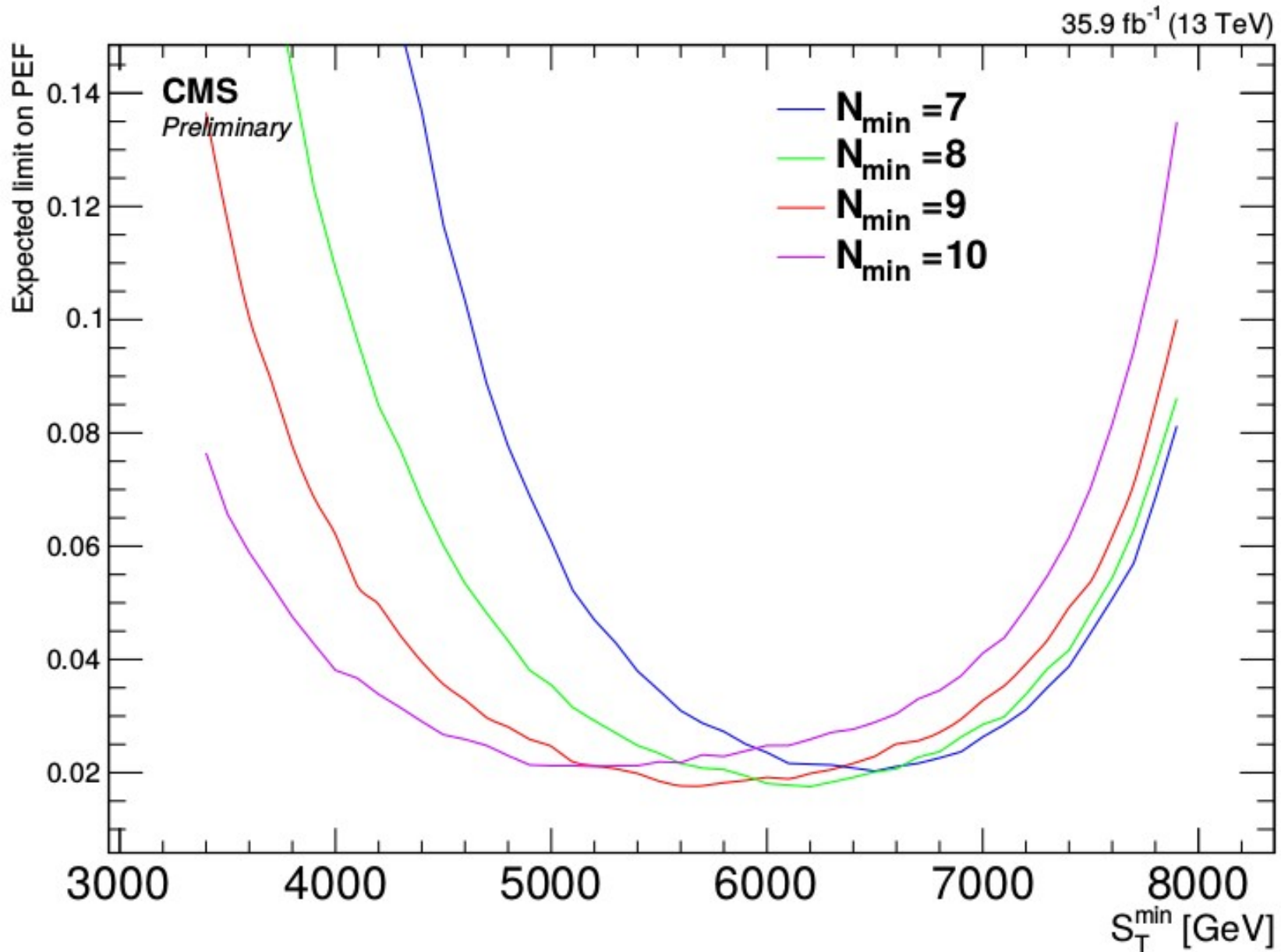
# MC $S_T$ Shape Invariance



# MC $S_T$ Shape Invariance



# Sphaleron Limit



# Normalization Details

Multiplicity	Normalization Region [ GeV ]	Normalization Scaling
$\geq 3$	2500 – 2900	$3.437 \pm 0.129$
$\geq 4$	2500 – 2900	$2.437 \pm 0.094$
$\geq 5$	2700 – 3100	$1.379 \pm 0.066$
$\geq 6$	2900 – 3300	$0.653 \pm 0.039$
$\geq 7$	3000 – 3400	$0.516 \pm 0.034$
$\geq 8$	3200 – 3600	$0.186 \pm 0.017$
$\geq 9$	3200 – 3600	$0.055 \pm 0.006$
$\geq 10$	3200 – 3600	$0.012 \pm 0.002$
$\geq 11$	3200 – 3600	$0.0024 \pm 0.0005$