

Anomalous quartic gauge couplings and unitarization for VBS

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Outline of talk:

- Introduction
- Effective Lagrangian for VBS
- Unitarization and off-shell $VV \rightarrow VV$
- Results for same sign W scattering
- Conclusions

- For details see **arXiv:1807.02707**

BSM effects in VBS: EFT expansion

- Concentrate on quartic gauge couplings (QGC):
trilinear couplings already probed in $qq \rightarrow VV$ or $h \rightarrow VV$
at much better statistics
- Dimension 6 operators do affect QGC, but they all also
contribute to trilinear WWV or hVV couplings \rightarrow allowed
values after $qq \rightarrow VV$ or $h \rightarrow VV$ constraints affect VBS at
modest level only
- Consider mainly dimension 8 operators in effective
Lagrangian in the following

Going beyond dimension 6

Reason for dimension 8 operators like

$$\begin{aligned}\mathcal{L}_{S,0} &= \left[(D_\mu \Phi)^\dagger D_\nu \Phi \right] \times \left[(D^\mu \Phi)^\dagger D^\nu \Phi \right] \\ \mathcal{L}_{M,1} &= \text{Tr} \left[\hat{W}_{\mu\nu} \hat{W}^{\nu\beta} \right] \times \left[(D_\beta \Phi)^\dagger D^\mu \Phi \right] \\ \mathcal{L}_{T,1} &= \text{Tr} \left[\hat{W}_{\alpha\nu} \hat{W}^{\mu\beta} \right] \times \text{Tr} \left[\hat{W}_{\mu\beta} \hat{W}^{\alpha\nu} \right]\end{aligned}$$

- Dimension 6 operators only do not allow to parameterize $VVVV$ vertex with arbitrary helicities of the four gauge bosons

For example: $\mathcal{L}_{S,0}$ is needed to describe $V_L V_L \rightarrow V_L V_L$ scattering

- New physics may appear at 1-loop level for dimension 6 operators but at tree level for some dimension 8 operators

Building blocks:

$$D_\mu \Phi \equiv \left(\partial_\mu + i \frac{g'}{2} B_\mu + i g W_\mu^i \frac{\tau^i}{2} \right) \Phi \quad \text{with} \quad \Phi = \begin{pmatrix} 0 \\ \frac{v+H}{\sqrt{2}} \end{pmatrix}$$

$$W_{\mu\nu} = \frac{i}{2} g \tau^I (\partial_\mu W_\nu^i - \partial_\nu W_\mu^i - g \epsilon_{ijk} W_\mu^j W_\nu^k),$$

$$B_{\mu\nu} = \frac{i}{2} g' (\partial_\mu B_\nu - \partial_\nu B_\mu).$$

Full set of dimension 8 operators (Eboli et al.)

- Distinguish by dominant set of vector boson helicities
- Longitudinal operators: derivatives of Higgs doublet field

$$\mathcal{O}_{S_0} = \left[(D_\mu \Phi)^\dagger D_\nu \Phi \right] \times \left[(D^\mu \Phi)^\dagger D^\nu \Phi \right]$$

$$\mathcal{O}_{S_1} = \left[(D_\mu \Phi)^\dagger D^\mu \Phi \right] \times \left[(D_\nu \Phi)^\dagger D^\nu \Phi \right]$$

$$\mathcal{O}_{S_2} = \left[(D_\mu \Phi)^\dagger D_\nu \Phi \right] \times \left[(D^\nu \Phi)^\dagger D^\mu \Phi \right]$$

Field strength \leftrightarrow transverse polarizations

Transverse operators

$$\mathcal{O}_{T_0} = \text{Tr} [W_{\mu\nu} W^{\mu\nu}] \quad \times \quad \text{Tr} [W_{\alpha\beta} W^{\alpha\beta}]$$

$$\mathcal{O}_{T_1} = \text{Tr} [W_{\alpha\nu} W^{\mu\beta}] \quad \times \quad \text{Tr} [W_{\mu\beta} W^{\alpha\nu}]$$

$$\mathcal{O}_{T_2} = \text{Tr} [W_{\alpha\mu} W^{\mu\beta}] \quad \times \quad \text{Tr} [W_{\beta\nu} W^{\nu\alpha}]$$

$$\mathcal{O}_{T_5} = \text{Tr} [W_{\mu\nu} W^{\mu\nu}] \quad \times \quad B_{\alpha\beta} B^{\alpha\beta} ,$$

$$\mathcal{O}_{T_6} = \text{Tr} [W_{\alpha\nu} W^{\mu\beta}] \quad \times \quad B_{\mu\beta} B^{\alpha\nu} ,$$

$$\mathcal{O}_{T_7} = \text{Tr} [W_{\alpha\mu} W^{\mu\beta}] \quad \times \quad B_{\beta\nu} B^{\nu\alpha} ,$$

$$\mathcal{O}_{T_8} = B_{\mu\nu} B^{\mu\nu} B_{\alpha\beta} B^{\alpha\beta} ,$$

$$\mathcal{O}_{T_9} = B_{\alpha\mu} B^{\mu\beta} B_{\beta\nu} B^{\nu\alpha} .$$

Mixed: transverse-longitudinal

$$\mathcal{O}_{M_0} = \text{Tr} [W_{\mu\nu} W^{\mu\nu}] \quad \times \quad \left[(D_\beta \Phi)^\dagger D^\beta \Phi \right] ,$$

$$\mathcal{O}_{M_1} = \text{Tr} [W_{\mu\nu} W^{\nu\beta}] \quad \times \quad \left[(D_\beta \Phi)^\dagger D^\mu \Phi \right] ,$$

$$\mathcal{O}_{M_2} = [B_{\mu\nu} B^{\mu\nu}] \quad \times \quad \left[(D_\beta \Phi)^\dagger D^\beta \Phi \right] ,$$

$$\mathcal{O}_{M_3} = [B_{\mu\nu} B^{\nu\beta}] \quad \times \quad \left[(D_\beta \Phi)^\dagger D^\mu \Phi \right] ,$$

$$\mathcal{O}_{M_4} = \left[(D_\mu \Phi)^\dagger W_{\beta\nu} D^\mu \Phi \right] \quad \times \quad B^{\beta\nu} ,$$

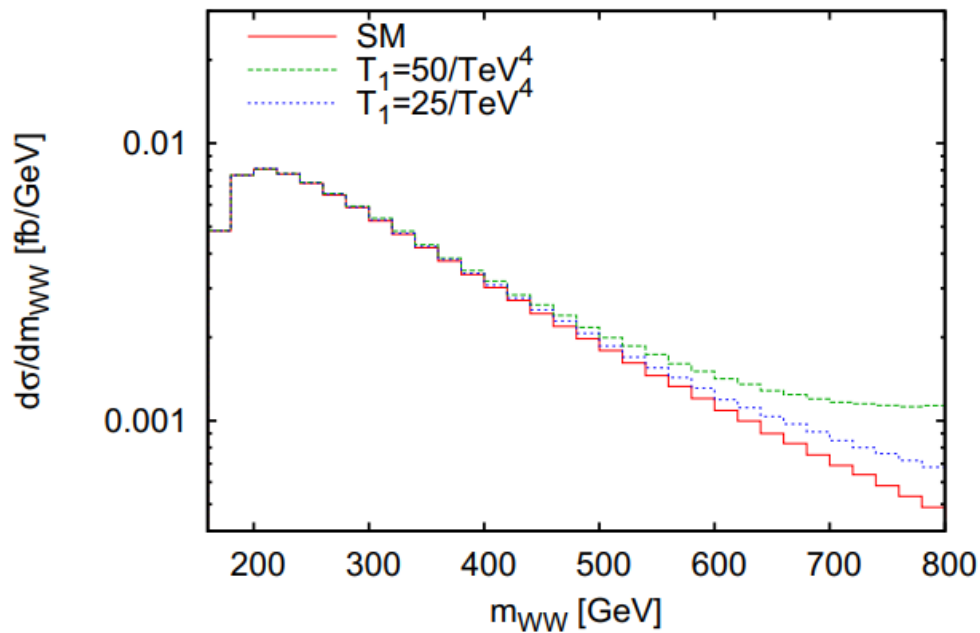
$$\mathcal{O}_{M_5} = \left[(D_\mu \Phi)^\dagger W_{\beta\nu} D^\nu \Phi \right] \quad \times \quad B^{\beta\mu} ,$$

$$\mathcal{O}_{M_7} = \left[(D_\mu \Phi)^\dagger W_{\beta\nu} W^{\beta\mu} D^\nu \Phi \right] .$$

$VV \rightarrow W^+W^-$ with dimension 8 operators

Effect of $\mathcal{L}_{eff} = \frac{f_{M,1}}{\Lambda^4} \text{Tr} [\hat{W}_{\alpha\nu} \hat{W}^{\mu\beta}] \times \text{Tr} [\hat{W}_{\mu\beta} \hat{W}^{\alpha\nu}]$

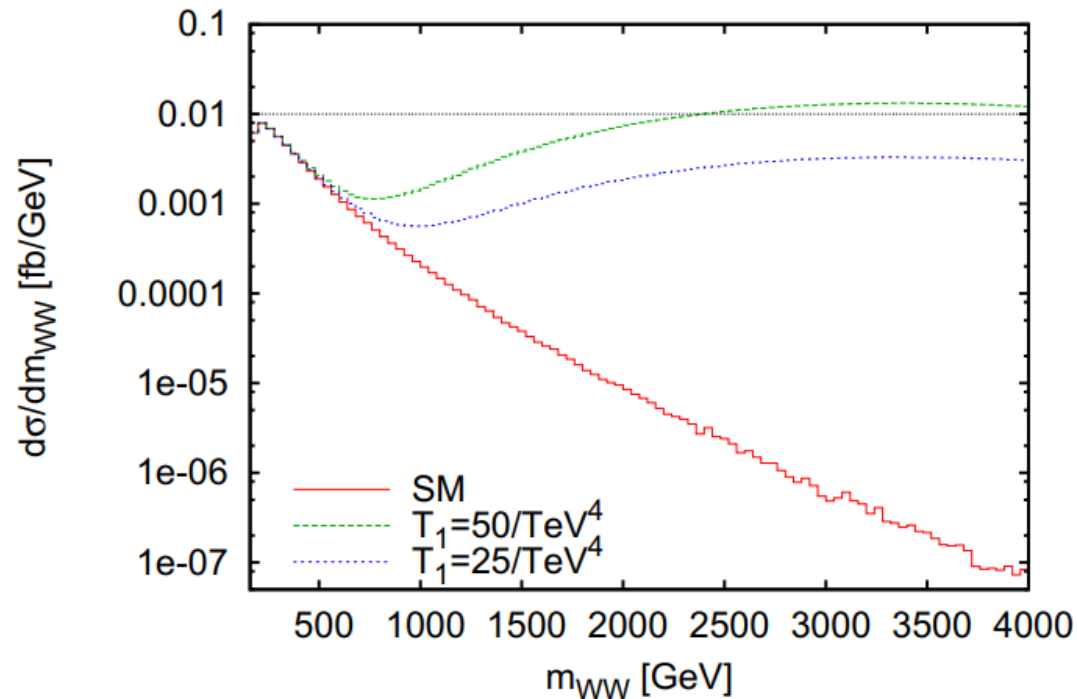
with $T_1 = \frac{f_{M,1}}{\Lambda^4}$ constant on $pp \rightarrow W^+W^- jj \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu jj$



- Small increase in cross section at high WW invariant mass??

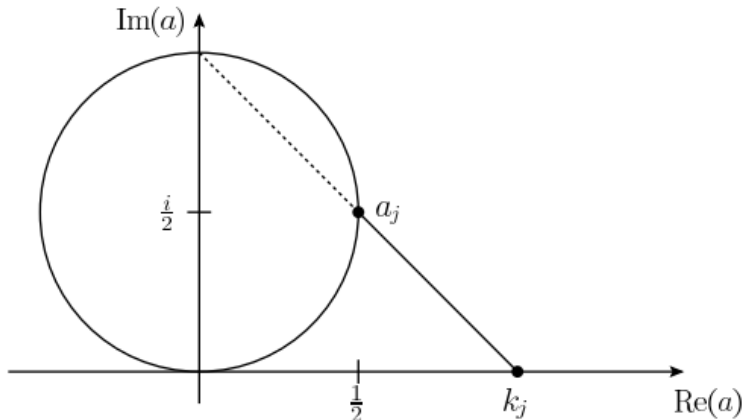
$VV \rightarrow W^+W^-$ with dimension 8 operators

Effect of constant $T_1 = \frac{f_{M,1}}{\Lambda^4}$ on $pp \rightarrow W^+W^- jj \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu jj$



- Huge increase in cross section at high m_{WW} is completely unphysical
- Need form factor for analysis or some other unitarization procedure

K matrix unitarization

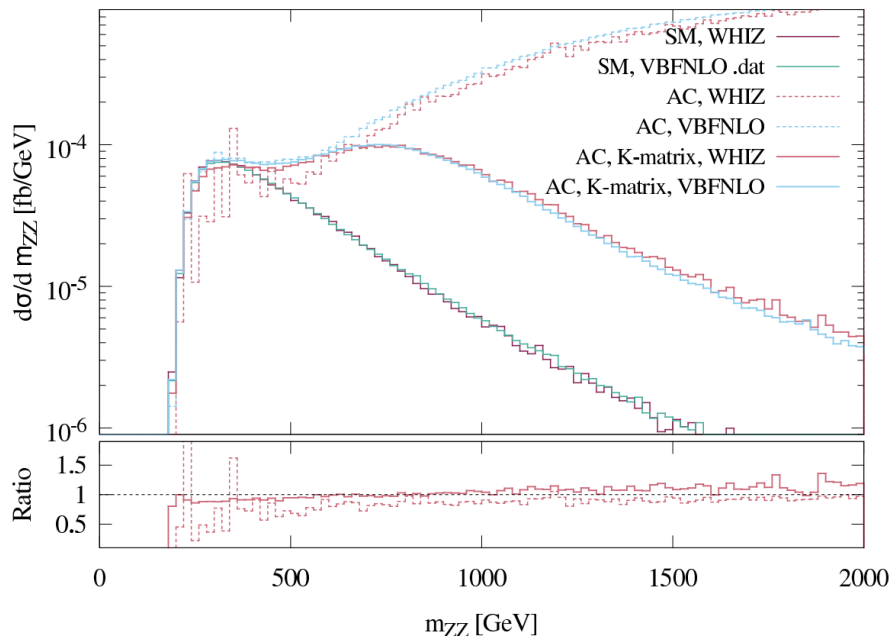


Project amplitude k_j , which exceeds (tree-level) unitarity, back onto Argand circle
 → K matrix unitarized amplitude a_j

[VBFNLO implementation: Löschner, Perez;

following: Alboteanu, Kilian, Reuter]

Comparison with Whizard, which has this method already implemented: [Kilian, Ohl, Reuter, Sekulla, et al.]



Example: VBF-ZZ ($e+e-\mu+\mu-$)
 good agreement between both codes
 for longitudinal ops. at LO

→ can now generate distributions
 also at NLO via VBFNLO

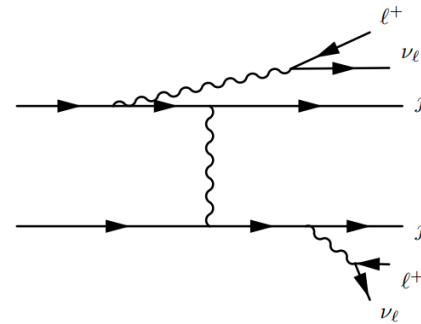
Extension to mixed and transverse
 operators not straight-forward: work with
Genessis Perez and **Marco Sekulla**

Off-shell VBS amplitude

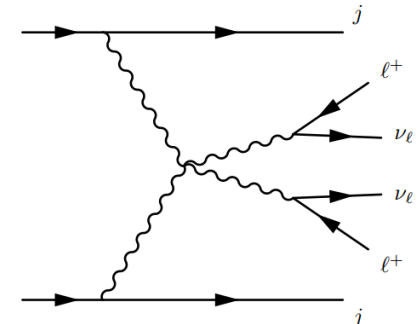
- Assume new physics in $VV \rightarrow VV$ only

$$\mathcal{M}_{pp \rightarrow 4fjj} = \mathcal{M}_{pp \rightarrow 4fjj}^{\text{SM}} + \mathcal{M}_{pp \rightarrow 4fjj}^{\text{BSM}}$$

- SM part alone has vector boson emission, triple gauge couplings, H-exchange etc. which interfere destructively



(a) Vector boson emission



(b) Quartic gauge interaction.

→ SM piece is unitary and small

- unitarize BSM piece only

$$\begin{aligned} \mathcal{M}_{pp \rightarrow 4fjj}^{\text{BSM}} &= J_{p_1 \rightarrow j V_1}^\mu J_{p_2 \rightarrow j V_2}^\nu D_{\mu\alpha}^{V_1}(q_1) D_{\nu\beta}^{V_2}(q_2) \\ &\quad \times \mathbf{M}_{V_1 V_2 \rightarrow V_3 V_4}^{\alpha\beta\gamma\delta} D_{\gamma\rho}^{V_3}(q_3) D_{\delta\sigma}^{V_4}(q_4) \\ &\quad \times J_{V_3 \rightarrow \bar{f}f}^\rho J_{V_4 \rightarrow \bar{f}f}^\sigma \end{aligned}$$

- V-propagators decompose into polarization sums

$$\begin{aligned} D_V^{\mu\nu}(q) &= \frac{-i}{q^2 - m_V^2 + i m_V \Gamma_V} \left(g^{\mu\nu} - \frac{q^\mu q^\nu}{q^2} \right) \\ &\equiv \frac{-i}{q^2 - m_V^2 + i m_V \Gamma_V} \sum_\lambda \epsilon_{J^\mu}^*(q, \lambda) \epsilon_{\mathcal{M}^\nu}^\nu(q, \lambda) \end{aligned}$$

- Defines $\mathcal{M}_{\lambda_3, \lambda_4; \lambda_1, \lambda_2}^{VBS}(q_1, q_2; q_3, q_4) = \epsilon_{\mathcal{M}, \alpha}(q_1, \lambda_1) \epsilon_{\mathcal{M}, \beta}(q_2, \lambda_2) \mathbf{M}_{V_1 V_2 \rightarrow V_3 V_4}^{\alpha\beta\gamma\delta} \epsilon_{\mathcal{M}, \gamma}^*(q_3, \lambda_3) \epsilon_{\mathcal{M}, \delta}^*(q_4, \lambda_4)$

Partial wave decomposition and unitarity relation

- S-matrix unitarity

$$\mathbf{S} = 1 + i\mathbf{T}, \quad \mathbf{T}_{fi} = (2\pi)^4 \delta(P_f - P_i) \mathcal{T}_{fi}$$

$$2\text{Im}\mathbf{T} = -i(\mathbf{T} - \mathbf{T}^\dagger) = \mathbf{T}^\dagger \mathbf{T} = \mathbf{T} \mathbf{T}^\dagger$$

- Implication for helicity amplitudes

$$\mathcal{M}_{\lambda_3 \lambda_4 \leftarrow \lambda_1 \lambda_2} = \mathcal{T}_{fi}$$

$$\mathcal{T}_{fi} - \mathcal{T}_{if}^* = i \sum_n \int \underbrace{\frac{d^3 \mathbf{q}_{n,3} d^3 \mathbf{q}_{n,4}}{(2\pi)^3 2q_{n,3}^0 (2\pi)^3 2q_{n,4}^0} (2\pi)^4 \delta(P_i - q_{n,3} - q_{n,4}) S_n \mathcal{T}_{nf}^* \mathcal{T}_{ni}}_{\frac{\lambda^{1/2}(s, q_{n,3}^2, q_{n,4}^2)}{8s(2\pi)^2} d\Omega}$$

- Projection onto $j \leq 2$ partial waves

$$\mathcal{M}_{\lambda_3 \lambda_4 \leftarrow \lambda_1 \lambda_2}(\Theta, \varphi) = 8\pi \mathcal{N}_{fi} \sum_{j=\max(|\lambda_{12}|, |\lambda_{34}|)}^{j_{\max}} (2j+1) \mathcal{A}_{\lambda_3 \lambda_4 \leftarrow \lambda_1 \lambda_2}^j d_{\lambda_{12} \lambda_{34}}^j(\Theta) e^{i\lambda_{34}\varphi}$$

- Partial wave unitarity relation

$$2\text{Im}(\mathcal{A}_{\lambda_3 \lambda_4 \leftarrow \lambda_1 \lambda_2}^j) = \sum_n \frac{\mathcal{N}_{ni} \mathcal{N}_{nf}}{\mathcal{N}_{fi}} \frac{\lambda^{1/2}(s, q_{n,3}^2, q_{n,4}^2)}{s} S_n \sum_{\lambda'_1, \lambda'_2} \mathcal{A}_{\lambda'_1 \lambda'_2 \leftarrow \lambda_3 \lambda_4}^{j*} \mathcal{A}_{\lambda'_1 \lambda'_2 \leftarrow \lambda_1 \lambda_2}^j$$

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- Partial wave unitarity relation

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Unitarization of tree level amplitude: $T_0 \rightarrow T_u$

- K-matrix (also called T-matrix) procedure for on-shell hermitian T_0

$$\mathbf{T}_L = \left(\mathbb{1} - \frac{i}{2} \mathbf{T}_0^\dagger \right)^{-1} \frac{1}{2} \left(\mathbf{T}_0 + \mathbf{T}_0^\dagger \right) = \left(\mathbb{1} + \frac{1}{4} \mathbf{T}_0 \mathbf{T}_0 \right)^{-1} \left(\mathbf{T}_0 + \frac{i}{2} \mathbf{T}_0 \mathbf{T}_0 \right)$$

- General virtualities $\rightarrow T_0$ not normal for off-shell $VV \rightarrow VV$

Must distinguish

$$\mathbf{A}_{t \leftarrow s} = \mathcal{M}_{\lambda_3, \lambda_4; \lambda_1, \lambda_2}(q_3, q_4; q_1, q_2)$$

$$\mathbf{A}_{s \leftarrow t} = \mathcal{M}_{\lambda_3, \lambda_4; \lambda_1, \lambda_2}(k_3, k_4; k_1, k_2)$$

$$\mathbf{A}_{t \leftarrow t} = \mathcal{M}_{\lambda_3, \lambda_4; \lambda_1, \lambda_2}(q_3, q_4; k_1, k_2)$$

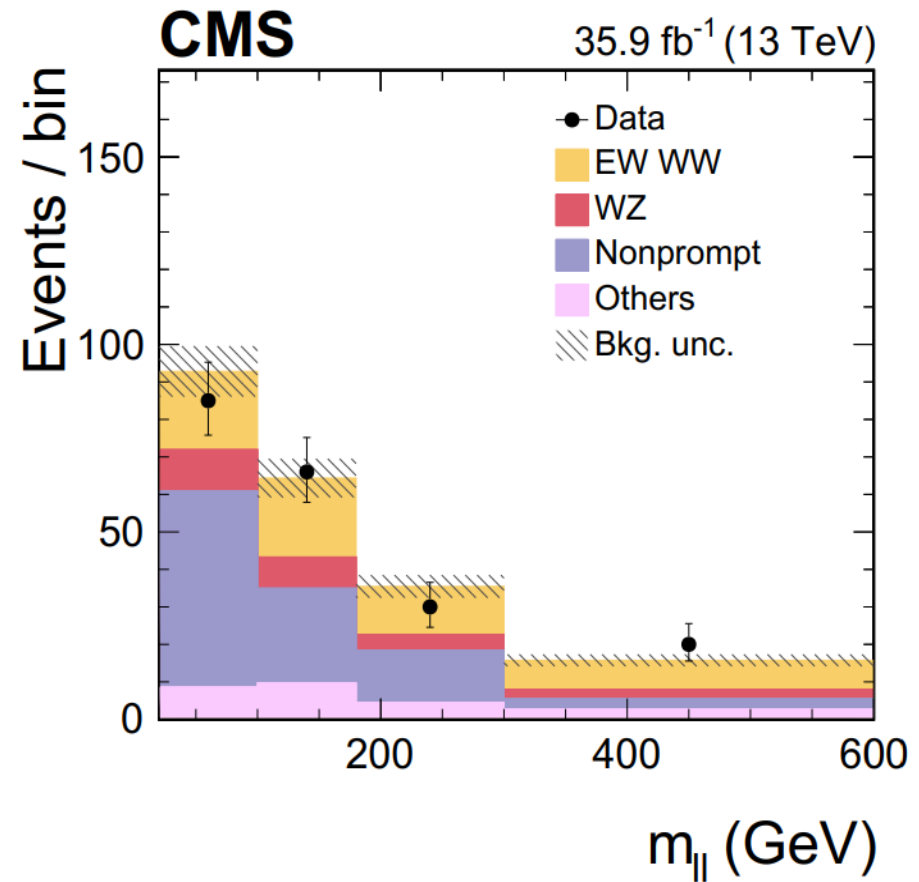
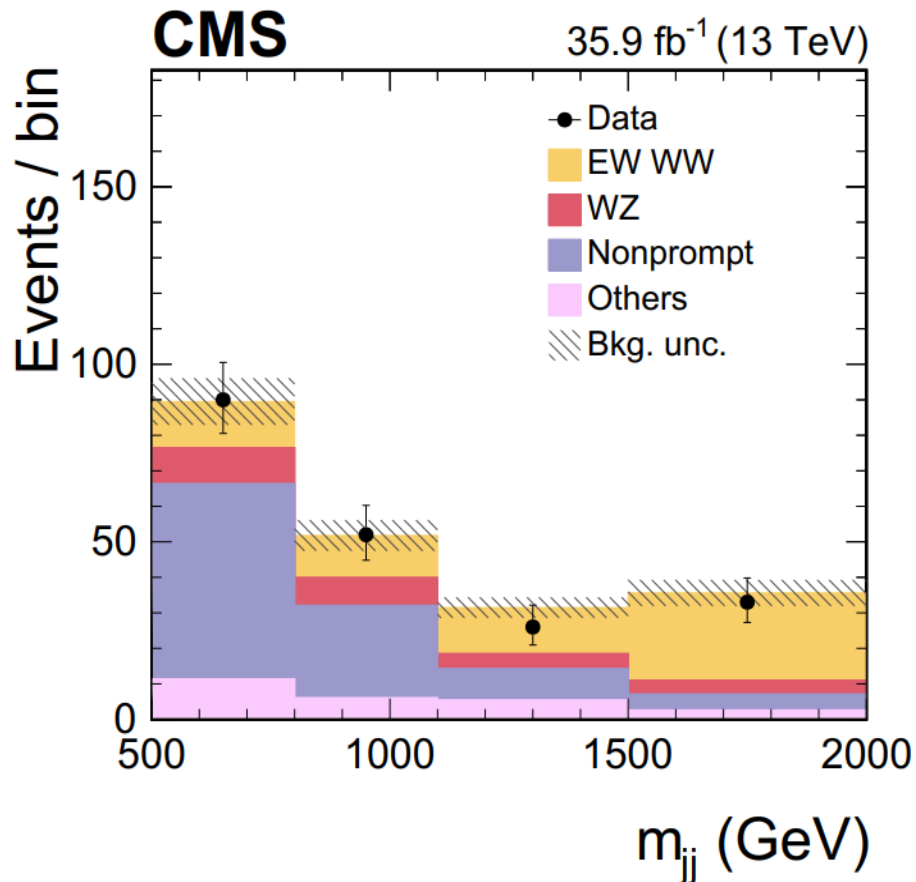
- Use
$$\mathbf{A}_{t \leftarrow s}^{\text{unit}} = \left(\mathbb{1} + \frac{1}{4} \mathbf{A}_{t \leftarrow s} \mathbf{A}_{s \leftarrow t} \right)^{-1} \left(\mathbf{A}_{t \leftarrow s} + \frac{i}{2} \mathbf{A}_{t \leftarrow t} \mathbf{A}_{t \leftarrow s} \right)$$

- Alignment problems avoided by using largest eigenvalue of denominator

$$\mathbf{A}_{t \leftarrow s}^{\text{unit}} = \left(\mathbb{1} + \frac{1}{4} a_{\text{max}}^2 \right)^{-1} \left(\mathbf{A}_{t \leftarrow s} + \frac{i}{2} \mathbf{A}_{t \leftarrow t} \mathbf{A}_{t \leftarrow s} \right)$$

Application to same sign W scattering

- Observed (with modest background) by ATLAS and CMS
- Useful bounds on Wilson coefficients of dim-8 operators



Definition of fiducial VBS cross sections

- Phase space cuts

$$m_{\ell\ell} > 20 \text{ GeV}, \quad m_{jj} > 500 \text{ GeV},$$

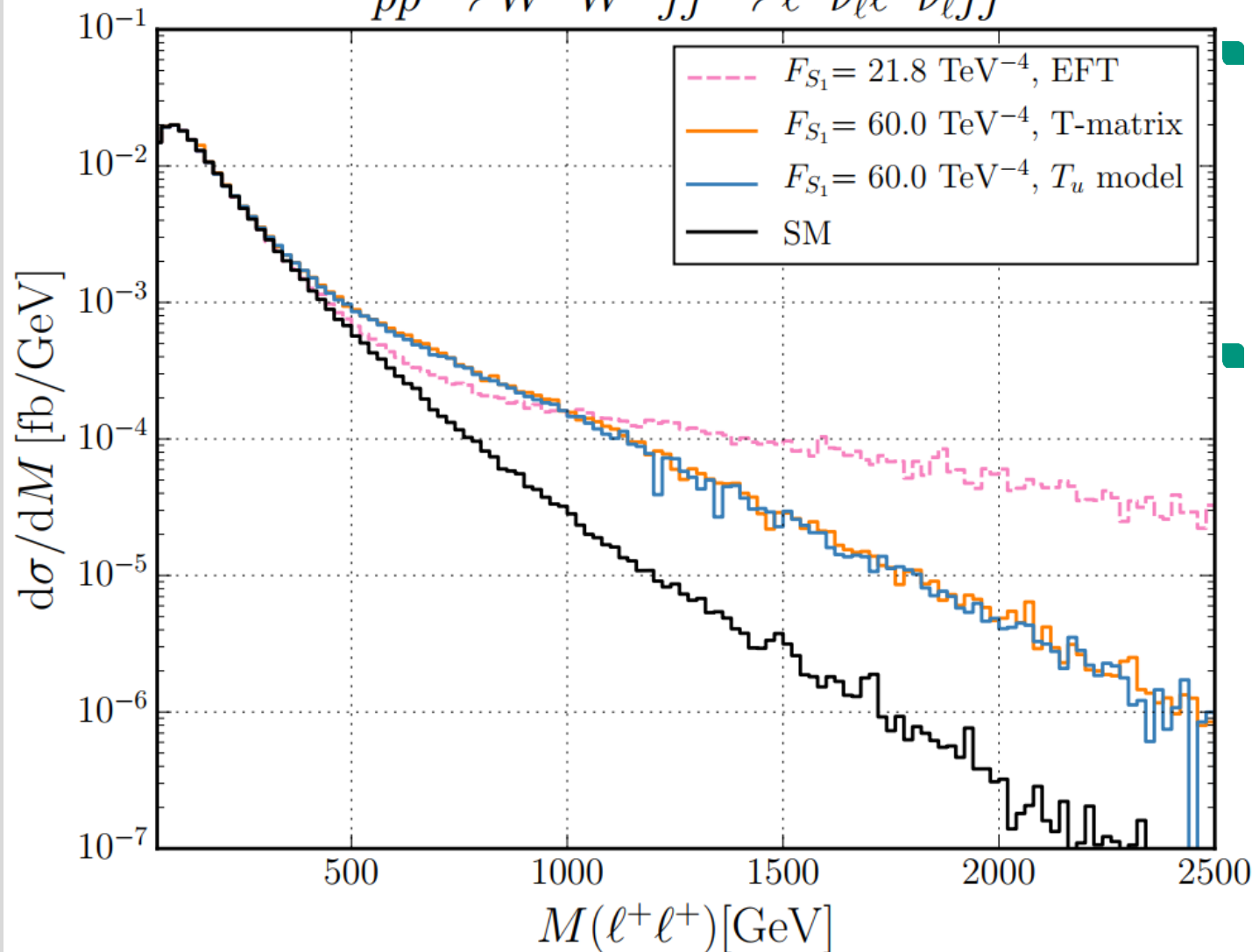
$$p_T^\ell > 20 \text{ GeV}, \quad p_T^j > 30 \text{ GeV}, \quad p_T^{\text{miss}} > 30 \text{ GeV}$$

$$|\eta_\ell| < 2.5, \quad |\eta_j| < 5, \quad \Delta\eta_{jj} > 2.5 .$$

- Jets defined with anti-kT clustering and R=0.4

Comparison to K-matrix

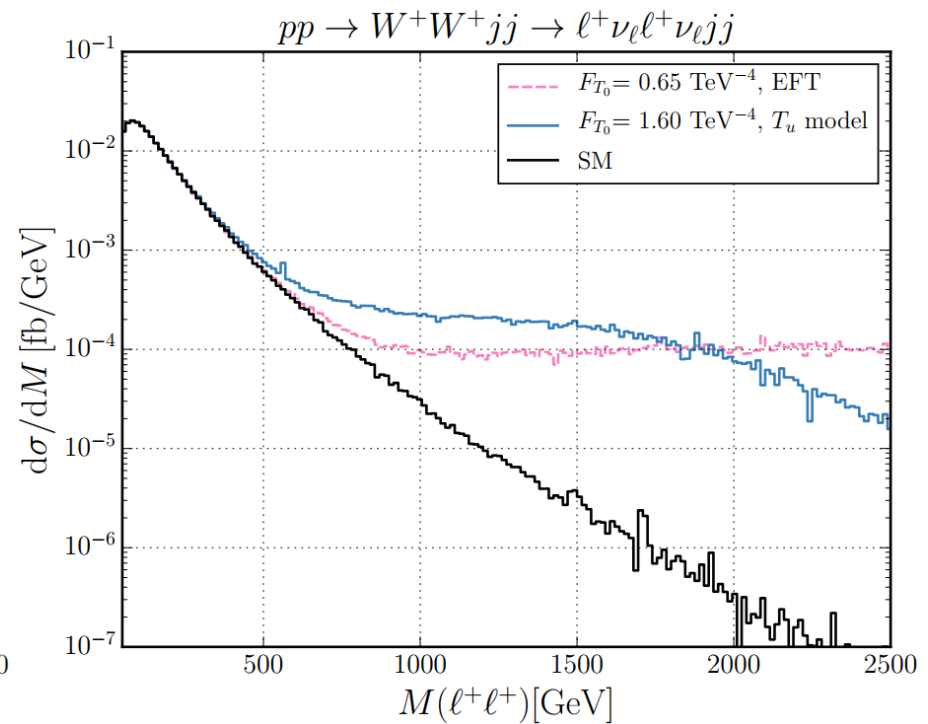
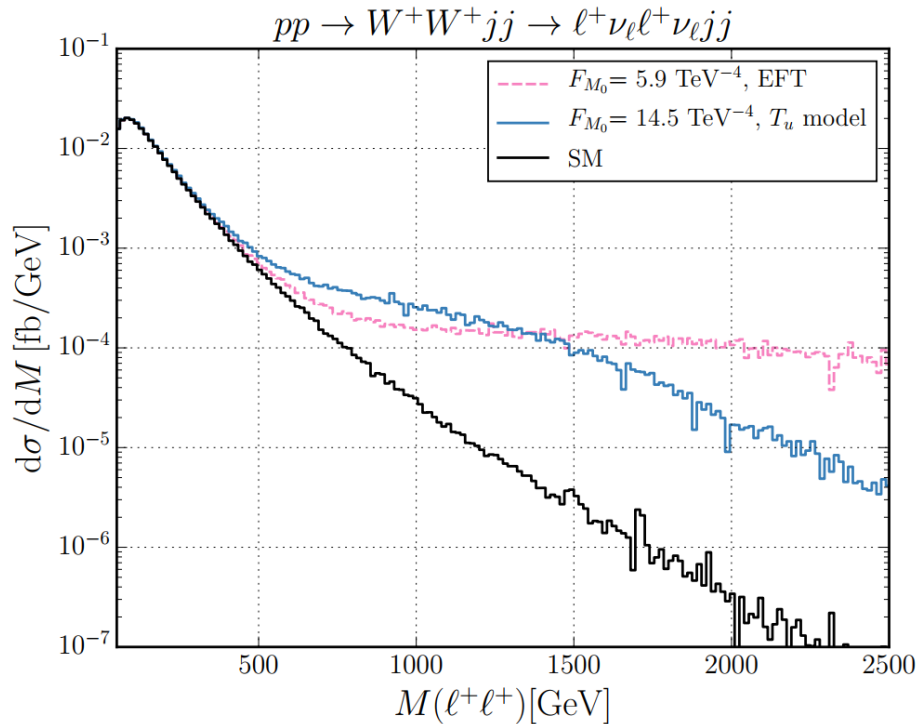
$$pp \rightarrow W^+W^+jj \rightarrow \ell^+\nu\ell^+\nu jj$$



Excellent agreement between different unitarization methods

$F_{S_1} = f_{S_1}/\Lambda^4$
coefficients adjusted for unitarized models to reproduce pure EFT cross section \leftrightarrow CMS limits on F

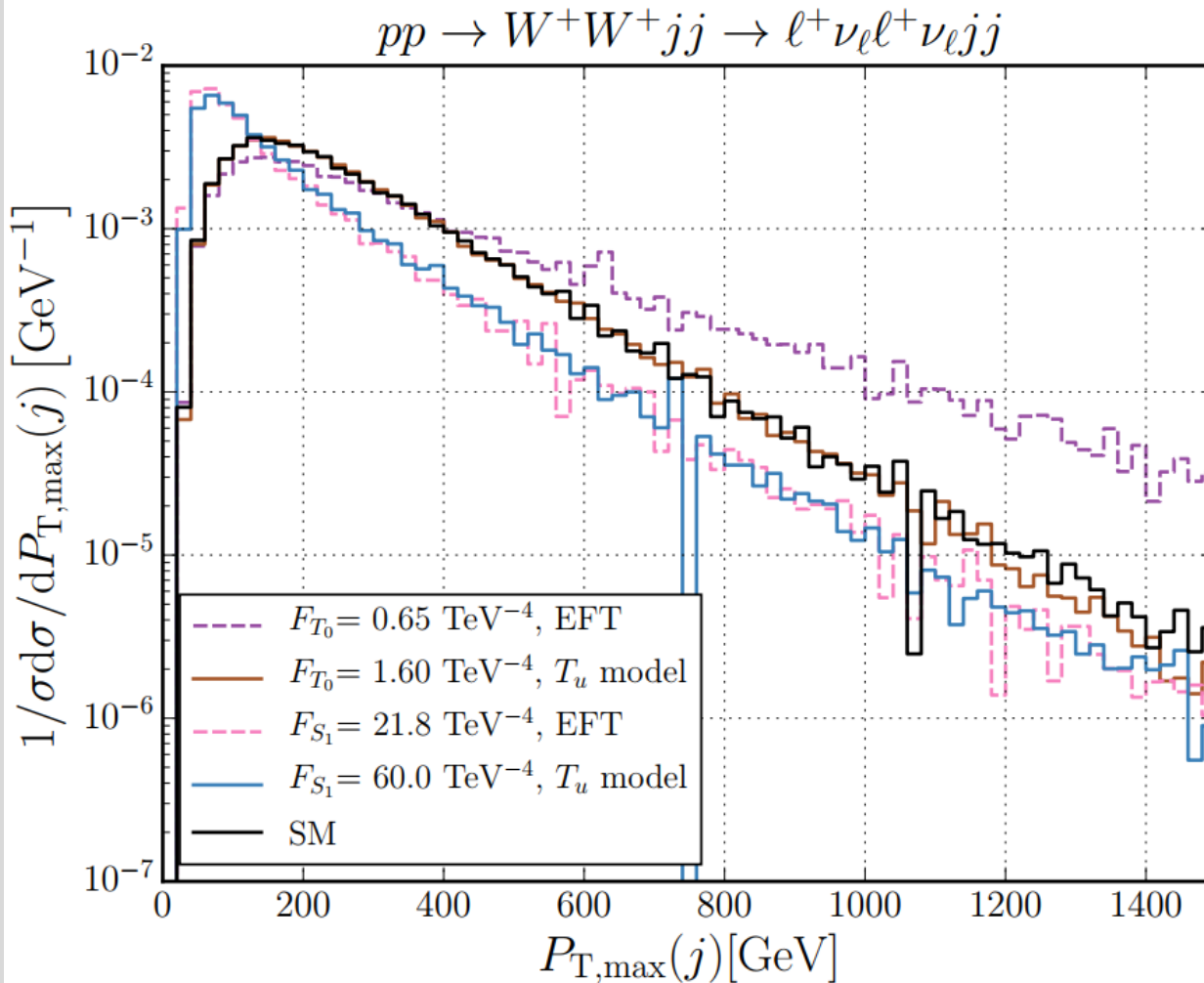
Mixed and transverse operators



Unitarity bound depends on whether $j=0,1$, or 2 partial waves dominate

Larger deviations allowed for transverse than for longitudinal operators

Incident W polarization: $p_T(j, \text{max})$



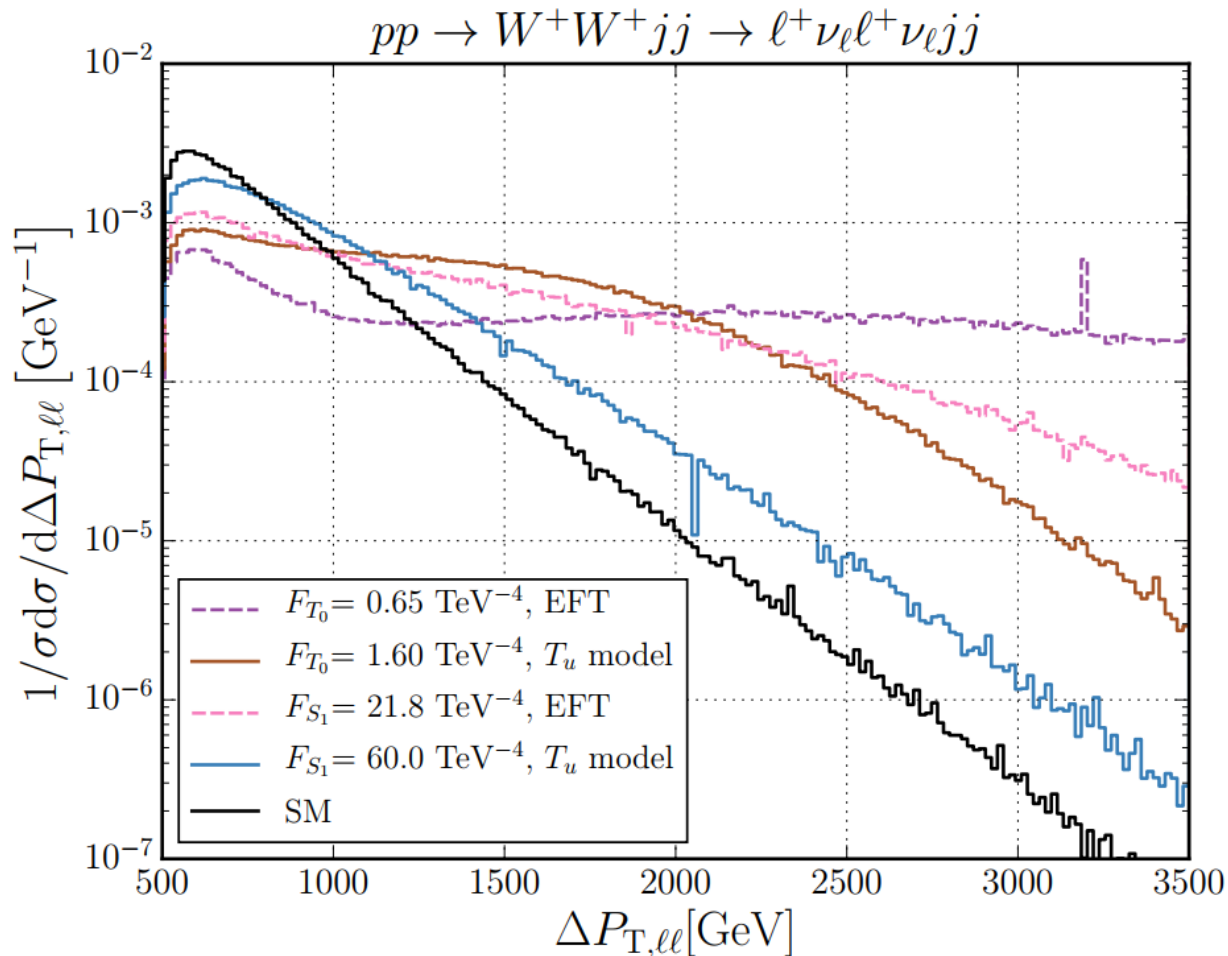
- Typical off-shell behavior

$$M \sim [s^2 + (q_1^2 + q_2^2 - q_3^2 - q_4^2) s]/\Lambda^4$$

- Unitarization suppresses large incident virtualities $\rightarrow p_T(j, \text{max})$ shapes depend on polarization only
- Enhancement at small $p_T(j, \text{max})$ is sign for enhanced longitudinal scattering

Lepton transverse momentum correlation

- $\Delta p_{T,\ell\ell} = |\mathbf{p}_{T,\ell_1} - \mathbf{p}_{T,\ell_2}|$ is sensitive to final W-polarization differences



Comments

- Unitarization changes shapes of distributions
- T_u model suppresses high VV invariant mass and large incident virtualities: similar to what one expects from loop functions
- Unitarization is not unique \rightarrow additional model dependence

Conclusions

- VBF and VBS provide powerful tests of electroweak symmetry breaking
- Pure EFT approach to parameterization of BSM effects is insufficient due to large energy reach of LHC and breakdown of unitarity at tree level
- Unitarization models provide improved tools for describing BSM VV scattering

Backup

Off-shell VBS amplitude: details

- Off shell polarization vectors

$$\epsilon_J^\mu(q, \pm) = \mp \frac{1}{\sqrt{2}\sqrt{q_x^2 + q_y^2}} \left(0; \frac{q_z q_x}{|\vec{q}|} \mp i q_y, \frac{q_y q_z}{|\vec{q}|} \pm i q_x, -\frac{q_x^2 + q_y^2}{|\vec{q}|} \right) = \epsilon_{\mathcal{M}}^\mu(q, \pm)$$

$$\epsilon_J^\mu(q, 0) = \mathcal{N}_J \left(|\vec{q}|, q_0 \frac{\vec{q}}{|\vec{q}|} \right), \quad \mathcal{N}_{\mathcal{M}} \left(|\vec{q}|, q_0 \frac{\vec{q}}{|\vec{q}|} \right) = \epsilon_{\mathcal{M}}^\mu(q, 0)$$

- Normalizaton factors

$$\mathcal{N}_J = \frac{m_V}{q^2}, \quad \mathcal{N}_{\mathcal{M}} = \frac{1}{m_V}, \quad \mathcal{N}_J \mathcal{N}_{\mathcal{M}} = 1/q^2$$

- Defines off shell tree-level amplitude

$$\mathcal{M}_{\lambda_3, \lambda_4; \lambda_1, \lambda_2}^{VBS}(q_1, q_2; q_3, q_4) = \epsilon_{\mathcal{M}, \alpha}(q_1, \lambda_1) \epsilon_{\mathcal{M}, \beta}(q_2, \lambda_2) \mathbf{M}_{V_1 V_2 \rightarrow V_3 V_4}^{\alpha \beta \gamma \delta} \epsilon_{\mathcal{M}, \gamma}^*(q_3, \lambda_3) \epsilon_{\mathcal{M}, \delta}^*(q_4, \lambda_4)$$

- Normalization of partial wave amplitudes

$$2\text{Im}(\mathcal{A}_{\lambda_3 \lambda_4 \leftarrow \lambda_1 \lambda_2}^j) = \sum_n \frac{\mathcal{N}_{ni} \mathcal{N}_{nf}}{\mathcal{N}_{fi}} \frac{\lambda^{1/2}(s, q_{n,3}^2, q_{n,4}^2)}{s} S_n \sum_{\lambda'_1, \lambda'_2} \mathcal{A}_{\lambda'_1 \lambda'_2 \leftarrow \lambda_3 \lambda_4}^{j*} \mathcal{A}_{\lambda'_1 \lambda'_2 \leftarrow \lambda_1 \lambda_2}^j$$

$$\mathcal{N}_{ni} = \frac{s}{\lambda^{1/4}(s, q_{n,3}^2, q_{n,4}^2) \lambda^{1/4}(s, q_1^2, q_2^2)} \frac{1}{\sqrt{S_n S_i}}$$