

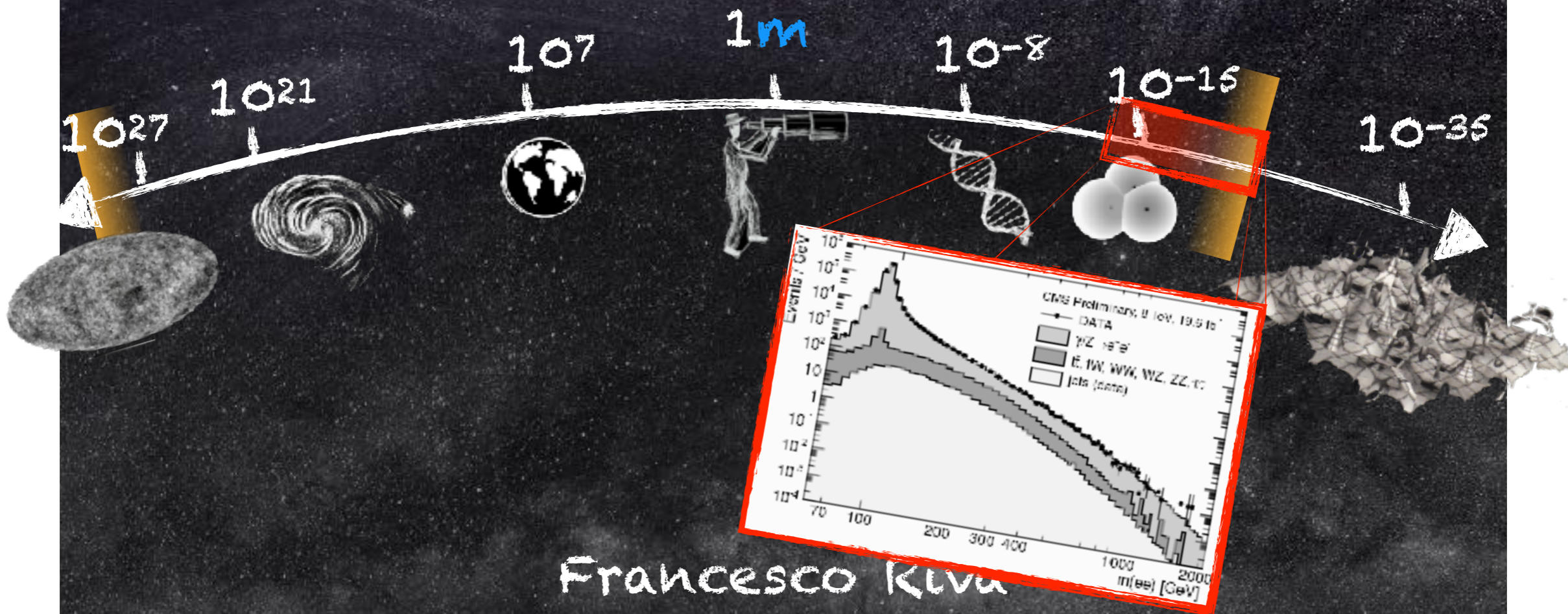
High-Energy Tests of a Low-Energy Theory -Transverse Vectors-



Francesco Riva
(Université de Genève)

In collaboration with
Bellazzini 1806.09640
Bellazzini, Serra, Sgarlata, 1706.03070
Panico, Wulzer 1708.07823,
Azatov, Contino, Machado 1607.05236
Liu, Pomarol, Rattazzi, 1603.03064

High-Energy Tests of a Low-Energy Theory -Transverse Vectors-

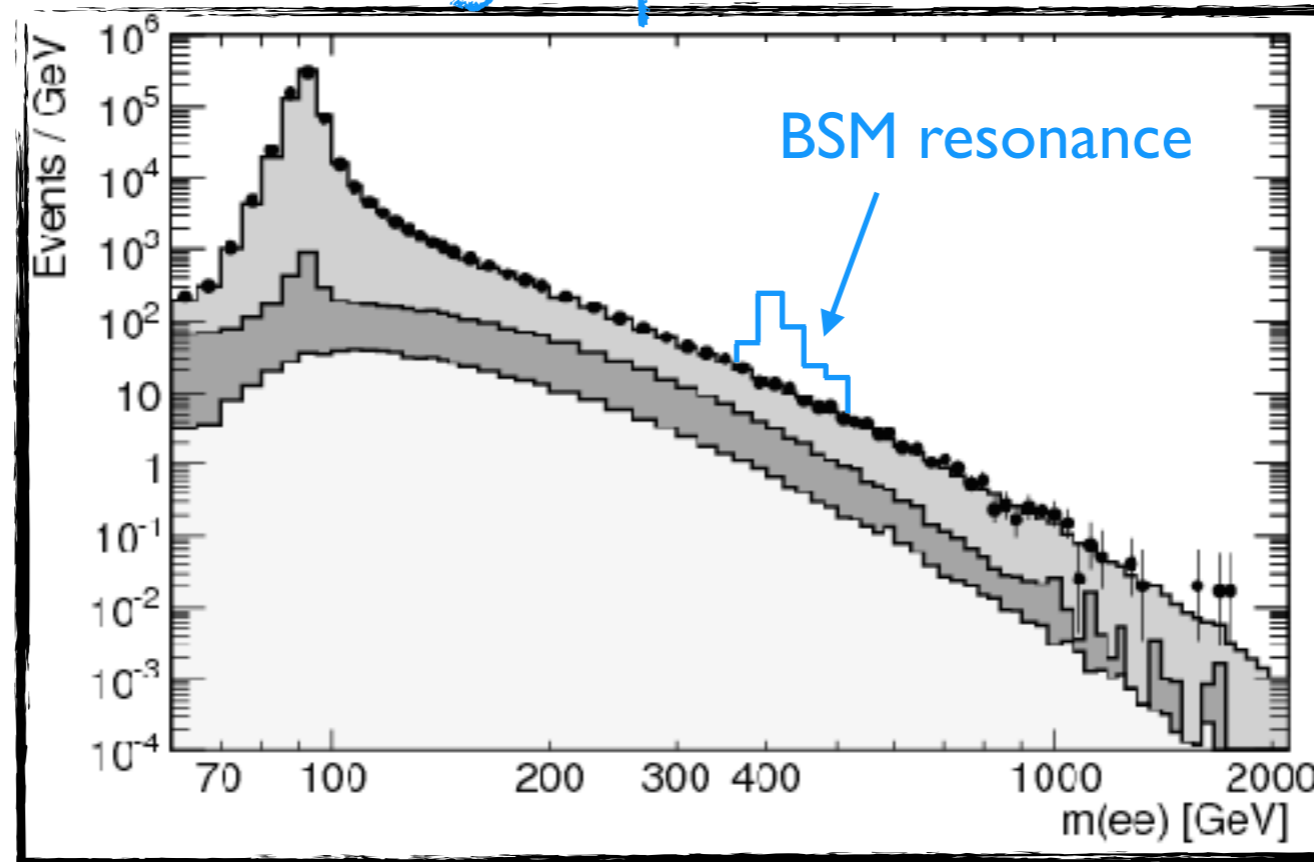


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Collider Exploration (so far)

Focus: Search for new light particles



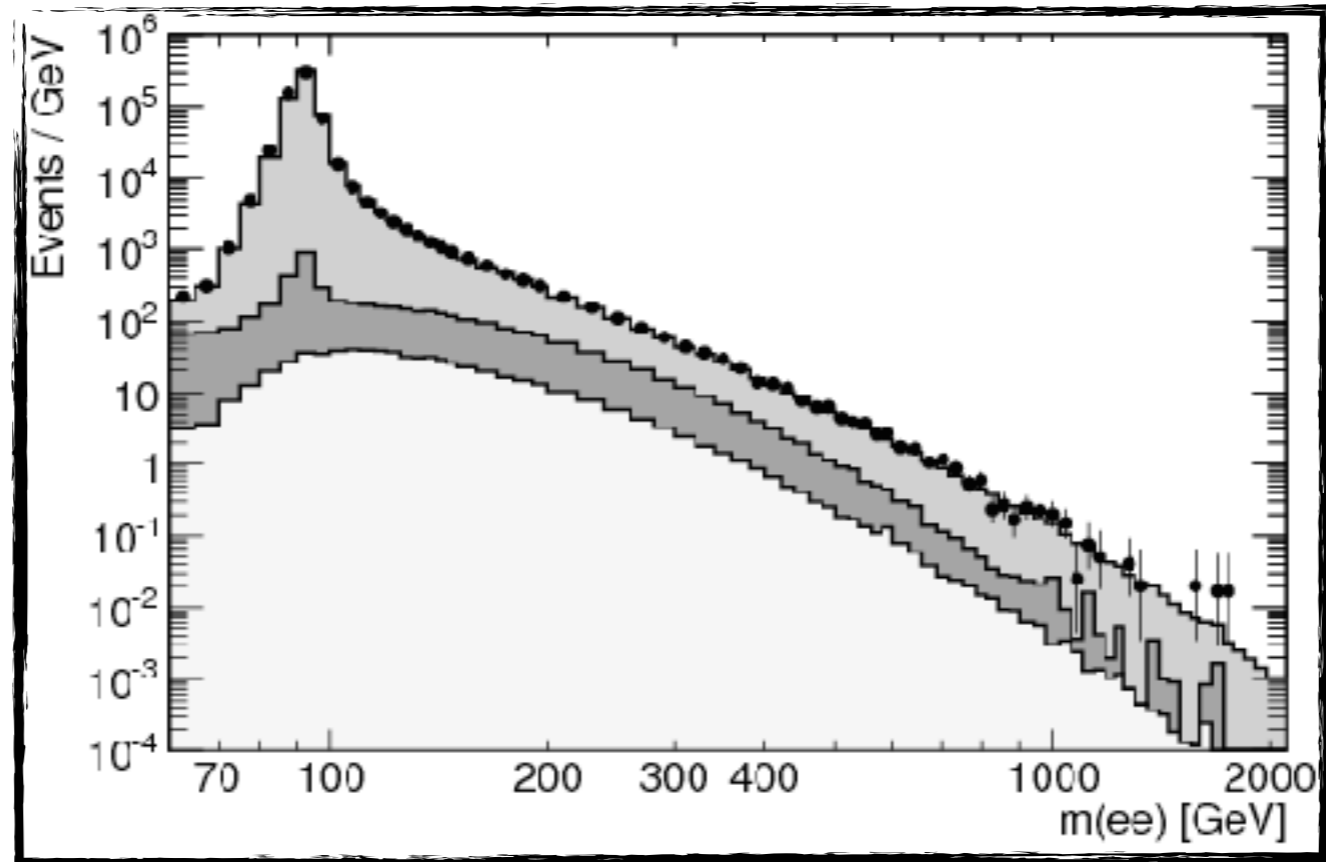
Energy frontier (13 TeV)

Collider Exploration (from now)

Focus: Standard Model Precision Tests

(2035: 3000 fb⁻¹)

intensity
frontier

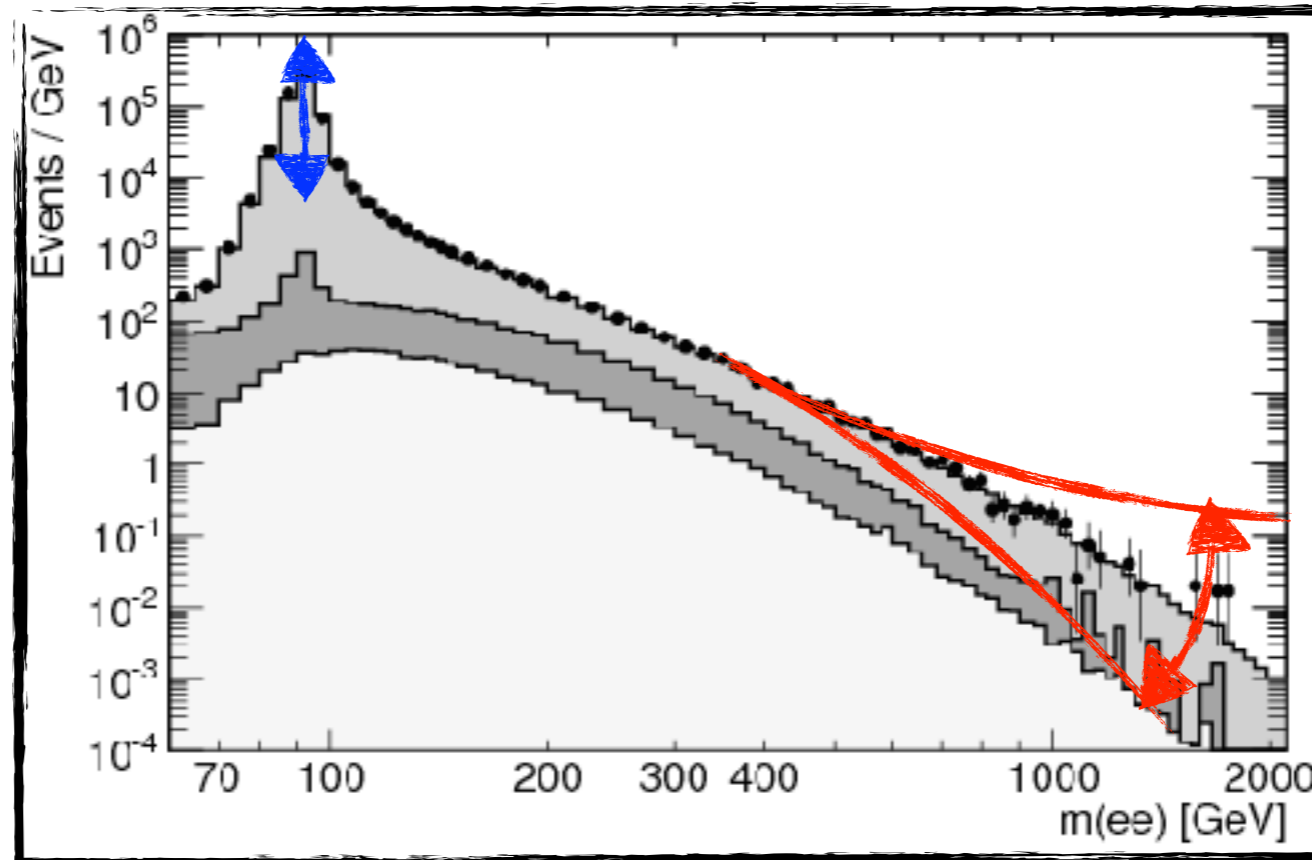


Collider Exploration (from now)

Focus: Standard Model Precision Tests

(2035: 3000 fb⁻¹)

intensity
frontier

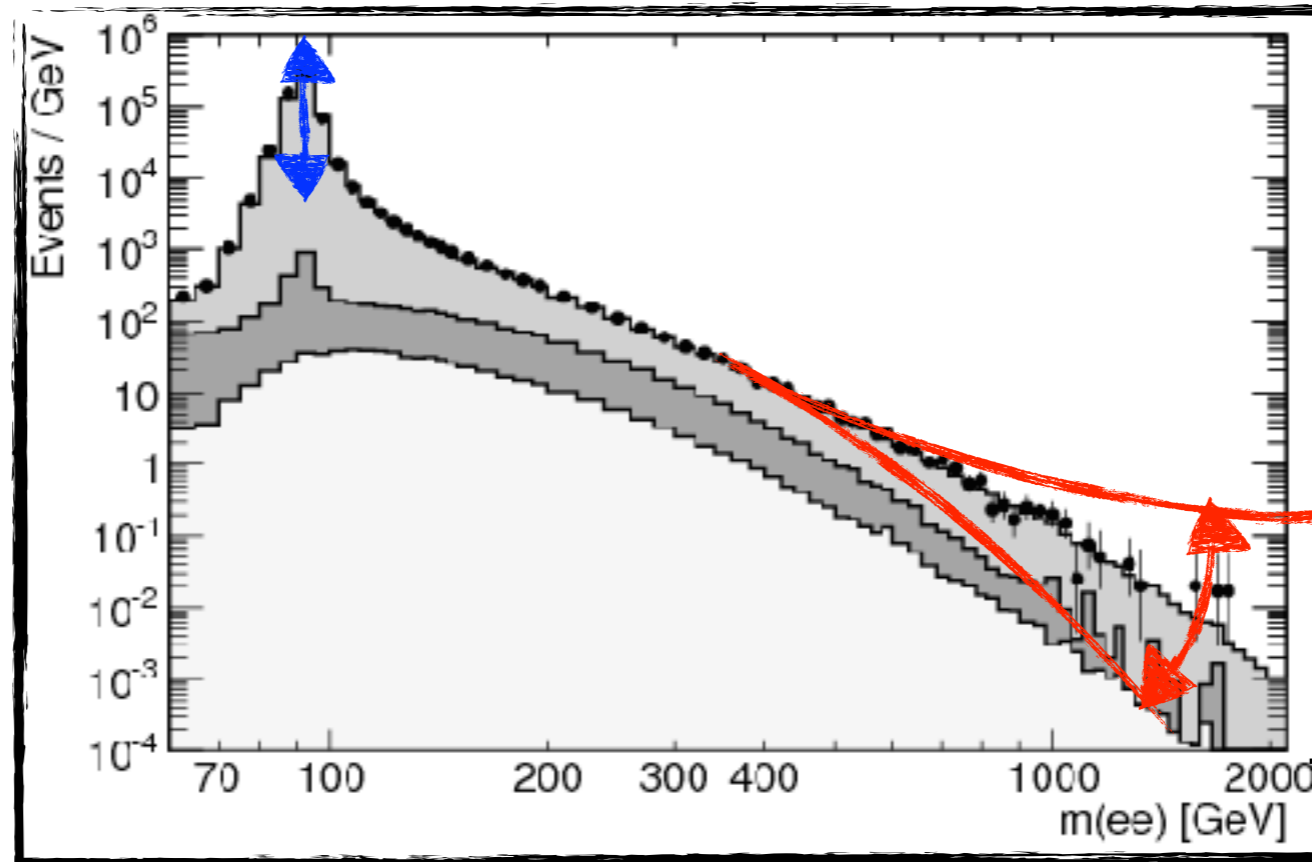


Collider Exploration (from now)

Focus: Standard Model Precision Tests

(2035: 3000 fb⁻¹)

intensity
frontier



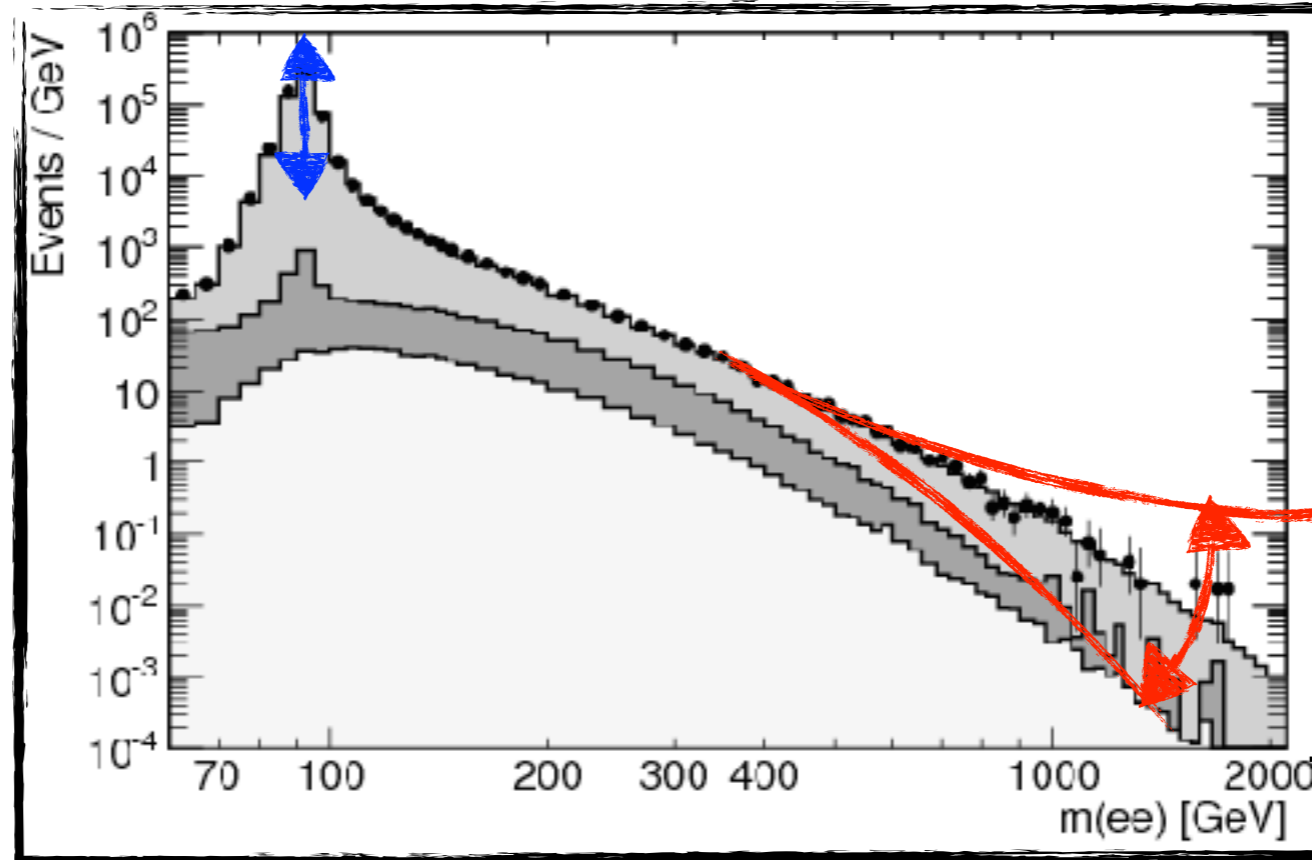
10-100 TeV

Collider Exploration (from now)

Focus: Standard Model Precision Tests

(2035: 3000 fb⁻¹)

intensity
frontier



10-100 TeV
 M

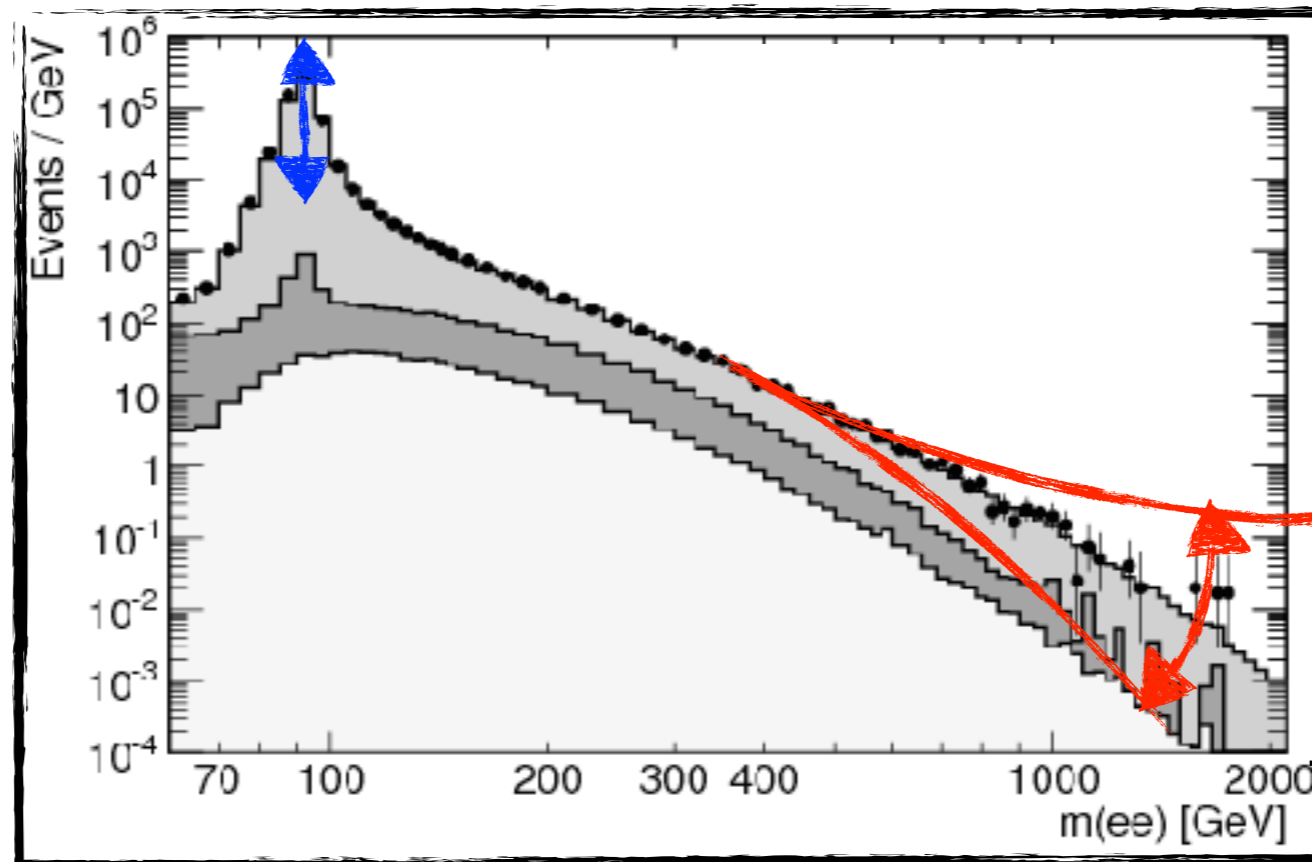
Effective
Field
Theory

Collider Exploration (from now)

Focus: Standard Model Precision Tests

(2035: 3000 fb⁻¹)

intensity
frontier



10-100 TeV
 M

Effective
Field
Theory

► Experimentally: Larger couplings → more visible effects

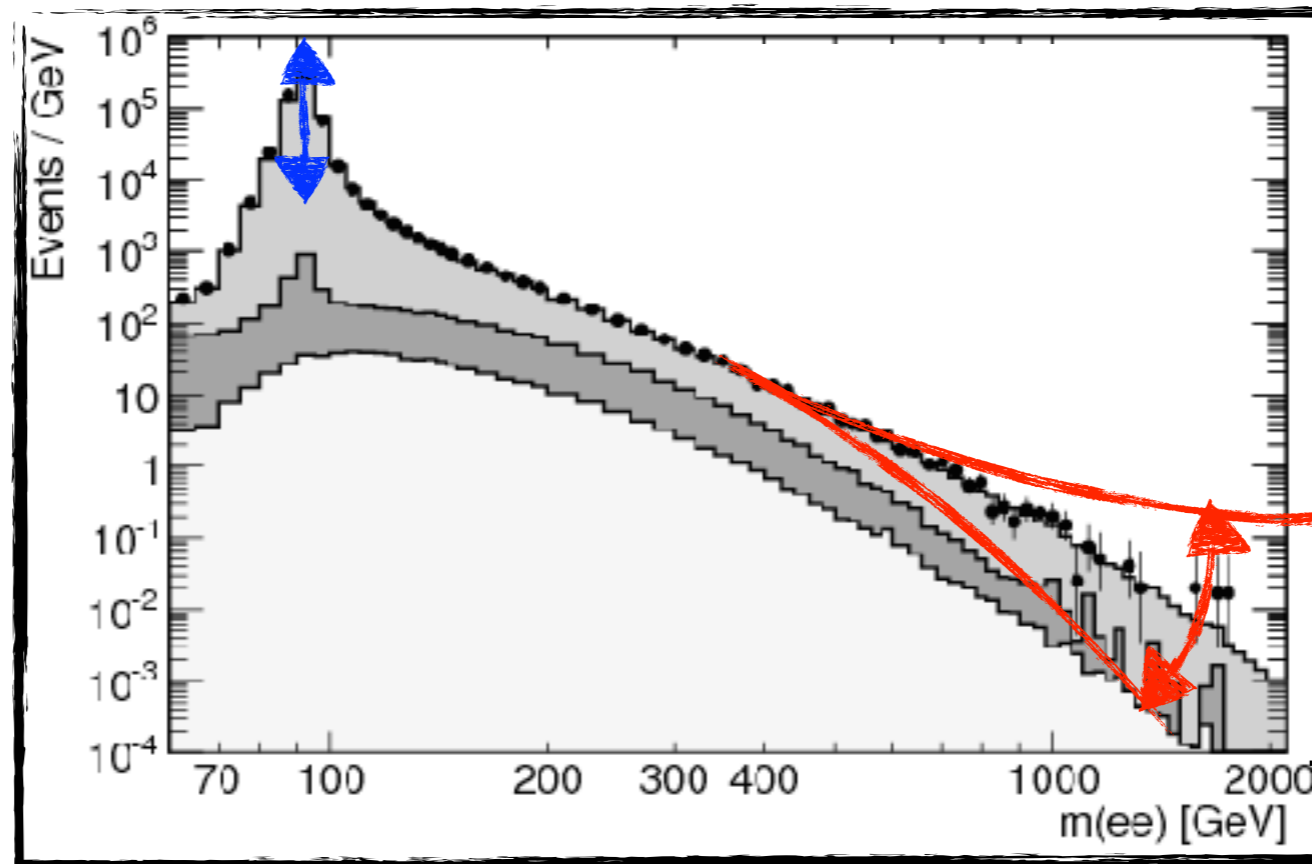
► Theoretically: strong coupling → radical departures from SM

Collider Exploration (from now)

Focus: Standard Model Precision Tests

(2035: 3000 fb⁻¹)

intensity
frontier



Effective
Field
Theory

(UV dof \neq IR dof)

- ▶ Experimentally: Larger couplings → more visible effects
- ▶ Theoretically: strong coupling → radical departures from SM

Transverse Vectors => High Energy

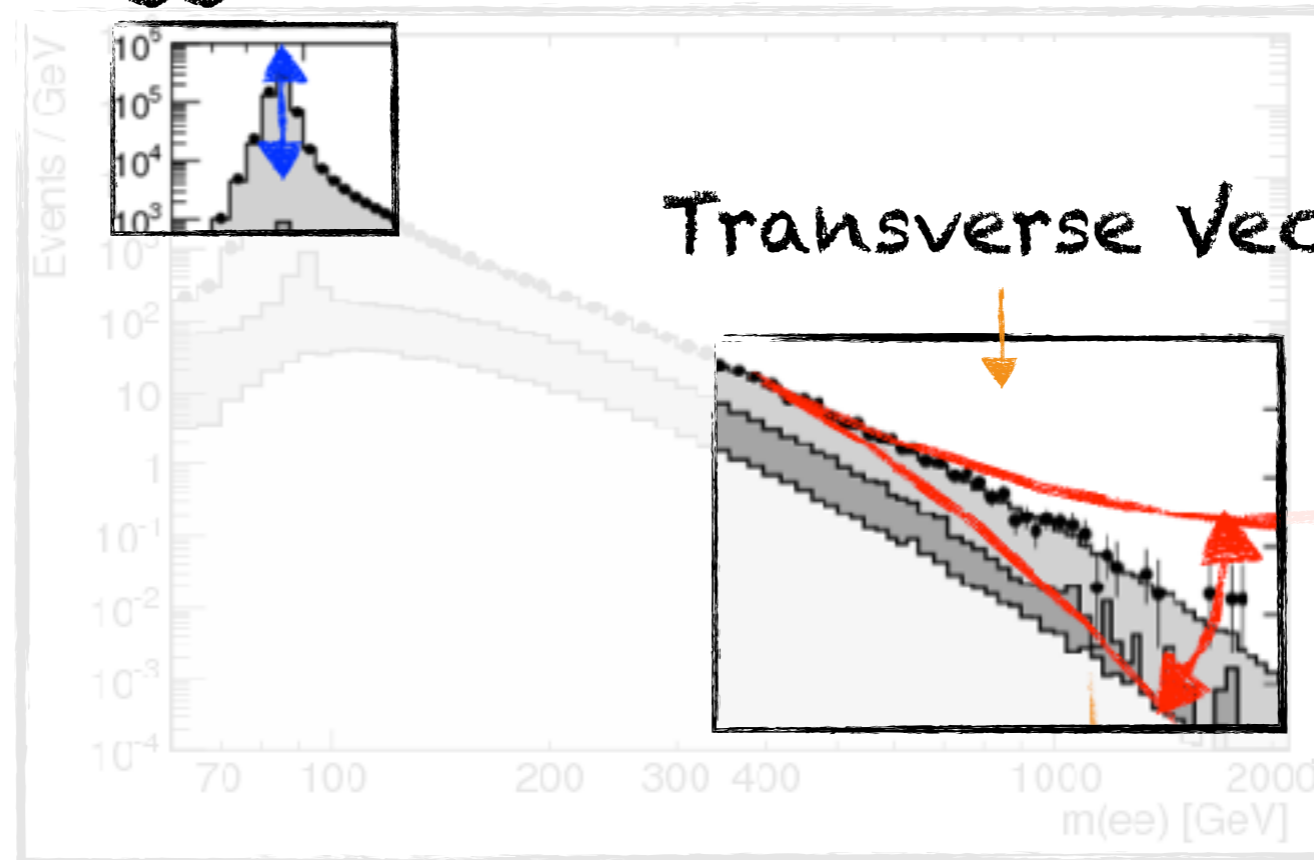
Couplings $\sim \frac{v^2}{M^2}$ (now $v^2 \rightarrow$ 2030's)

Focus: Standard Model Precision Tests

(2035: 3000 fb⁻¹)

intensity frontier

(2016: 40 fb⁻¹)



10-100 TeV

$$Amp = SM \left(1 + c \frac{E^2}{M^2} \right)$$

M

Effective Field Theory

- Outline:
- No Interference and Resurrections (WW, WZ, WY)
 - 8: before 6 (ZZ, ZY)

Transverse Vectors and Non-Interference

$$\sigma \propto |Amp|^2 \simeq SM^2 (1 + \delta_{BSM} + \delta_{BSM}^2)$$

$\delta_{BSM} = c \frac{E^2}{M^2}$

Leading for
 $1 \gg \delta_{BSM}$

Transverse Vectors and Non-Interference

$$\sigma \propto |Amp|^2 \simeq SM^2 \left(1 + \cancel{\delta_{BSM}} + \delta_{BSM}^2 \right)$$

$\delta_{BSM} = c \frac{E^2}{M^2}$

Leading for $1 \gg \delta_{BSM}$

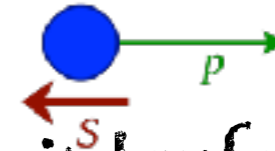
Small effects \rightarrow smaller $\delta_{BSM} \gg \delta_{BSM}^2$

Non-Interference

(2→2, high-E, tree-level)

Azatov, Contino, Machado, FR'16

For $E \gg m_W$ states have well defined helicity



Amplitudes for 2→2 with different total h don't interfere

SM

Any BSM
dim-6 operator

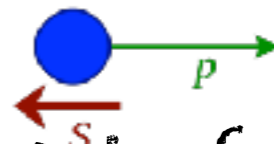
A_4	$ h(A_4^{\text{SM}}) $	$ h(A_4^{\text{BSM}}) $
VVVV	0	4,2
VV $\phi\phi$	0	2
VV $\psi\psi$	0	2
V $\psi\psi\phi$	0	2
$\psi\psi\psi\psi$	2,0	2,0
$\psi\psi\phi\phi$	0	0
$\phi\phi\phi\phi$	0	0

helicity

Non-Interference

(2→2, high-E, tree-level)

Azatov, Contino, Machado, FR'16

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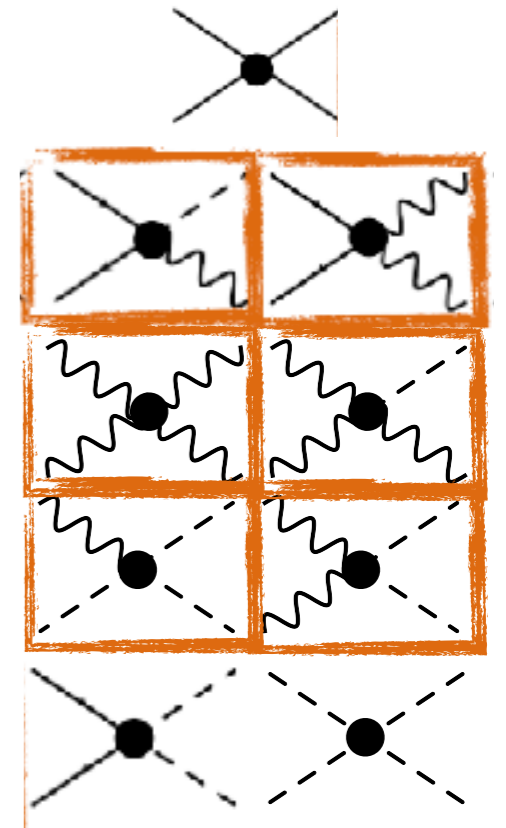
Any BSM dim-6 operator

Different helicity

No-Interference

Poor Measurement

A_4	$ h(A_4^{\text{SM}}) $	$ h(A_4^{\text{BSM}}) $
VVVV	0	4,2
VV $\phi\phi$	0	2
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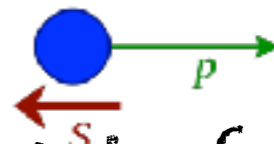


helicity

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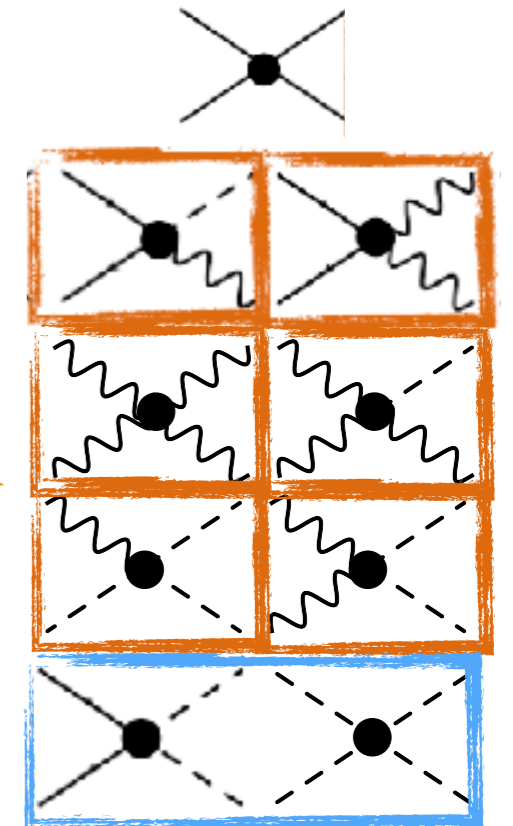
Different helicity

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$\psi\psi\phi\phi$	0	0
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helicity

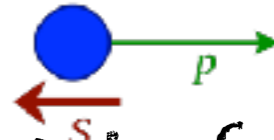


Small in inclusive xsec

Non-Interference

Azatov, Contino, Machado, FR'16

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dim-6 operator

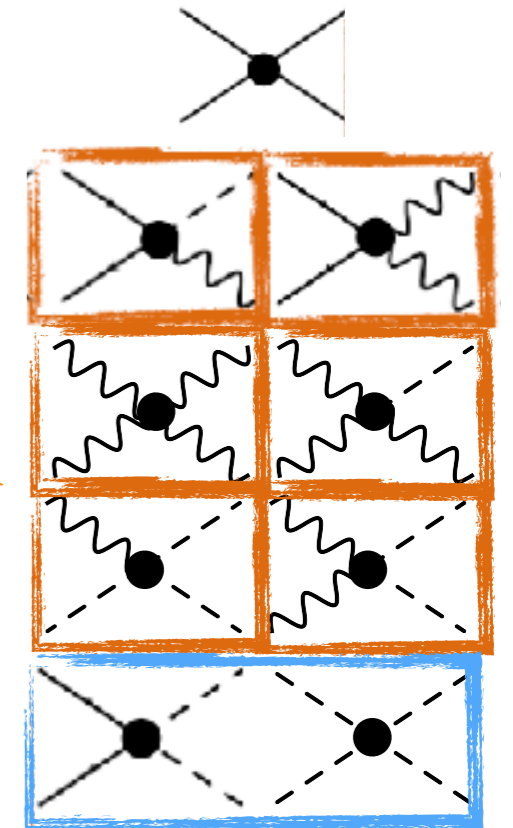
Different helicity

No-Interference

Poor Measurement

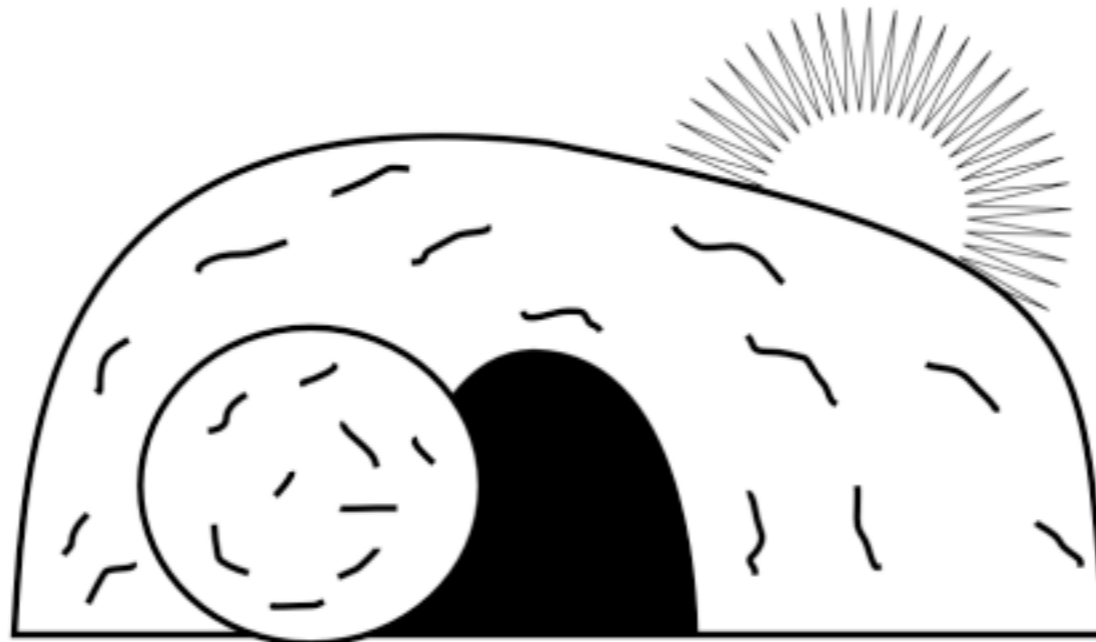
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helicity



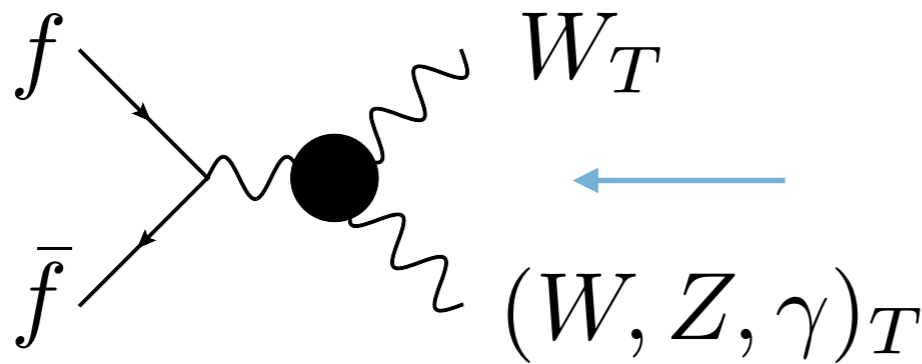
Small in inclusive xsec
(See Wulzer's talk)

WW, WZ, WY and their resurrection



Interference Resurrection

Focus on **dibosons**, with these operators that do not interfere with the SM



$$\epsilon_{abc} W_{\mu}^{a\nu} W_{\nu\rho}^b W^{c\rho\mu}$$
$$\epsilon_{abc} W_{\mu}^{a\nu} W_{\nu\rho}^b \widetilde{W}^{c\rho\mu}$$

CP-even

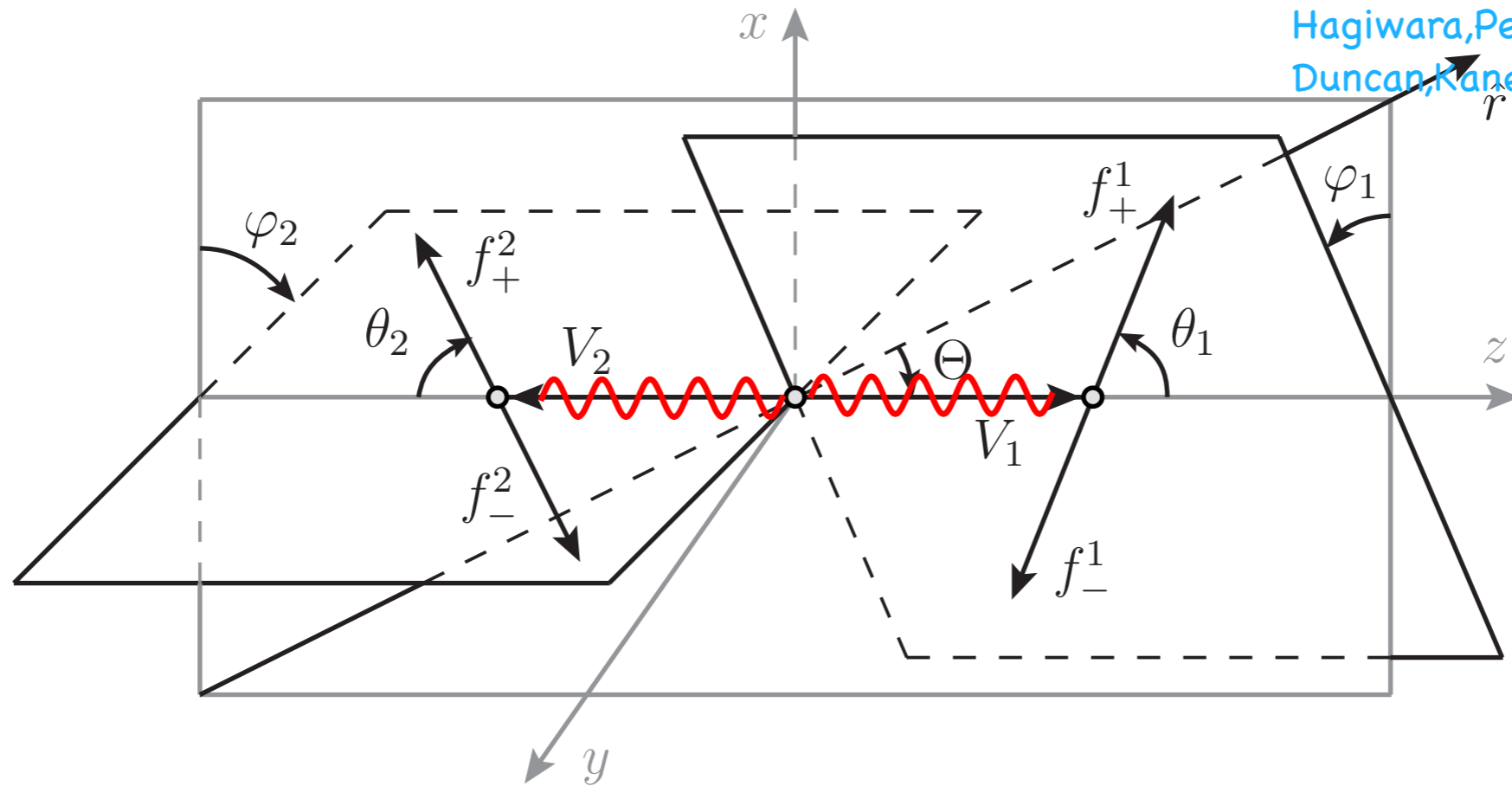
CP-odd

Differential measurements WW, WZ

Panico,FR,Wulzer'17,

Hagiwara,Peccei,Zeppenfeld,Hikasa'86

Duncan,Kane,Repko'86



$V_{1,2}$: Helicity $\pm\mp/\pm\pm$ in SM/BSM

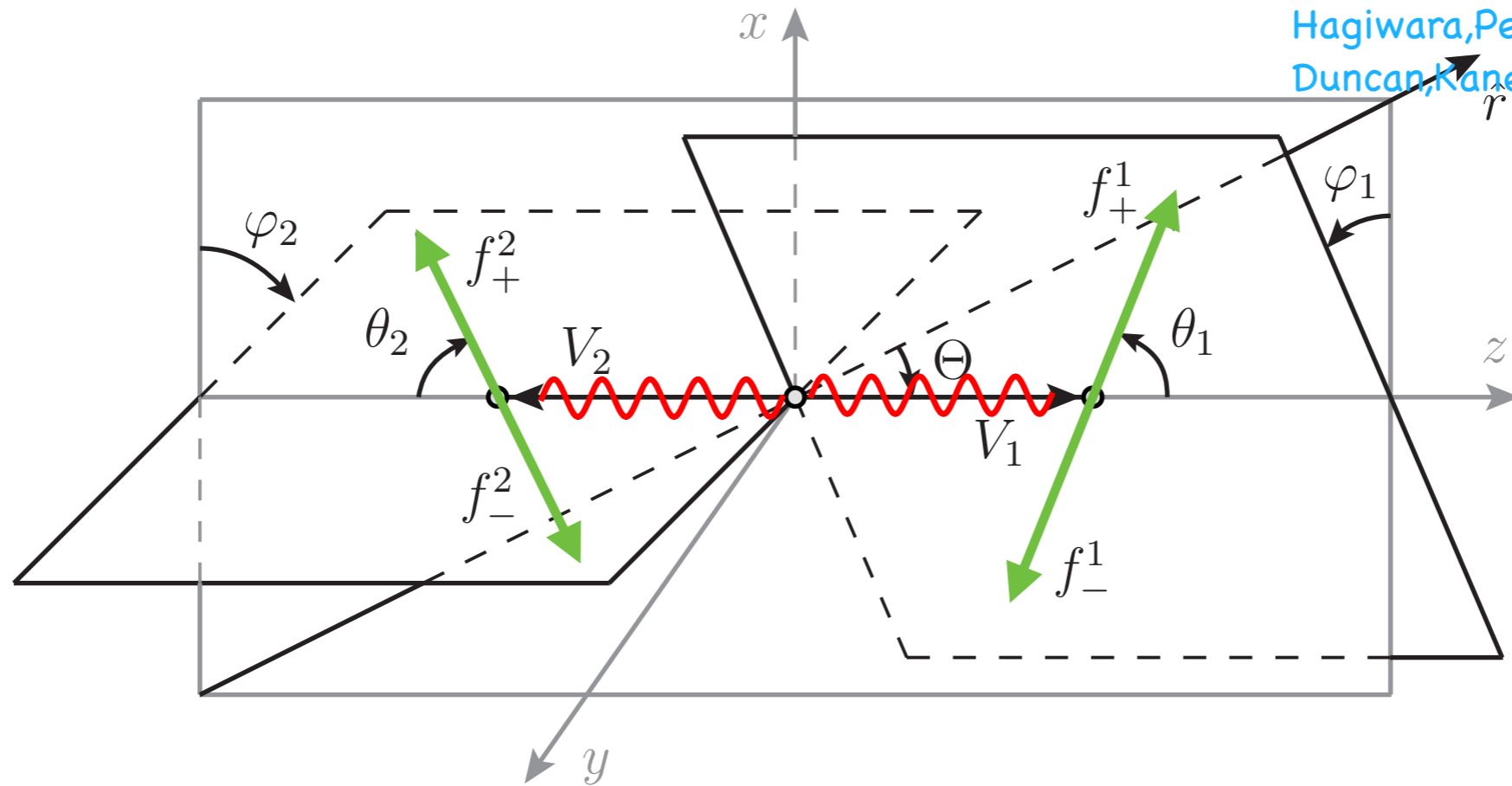
► Quantum mechanically different, no interference

Differential measurements WW, WZ

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$V_{1,2}$: Helicity $\pm\mp/\pm\pm$ in SM/BSM

▶ Quantum mechanically **different**, **no** interference

$f_{(1,3)} f_{(2,4)}$: Helicity $+1/2 -1/2$ in SM **and** in BSM

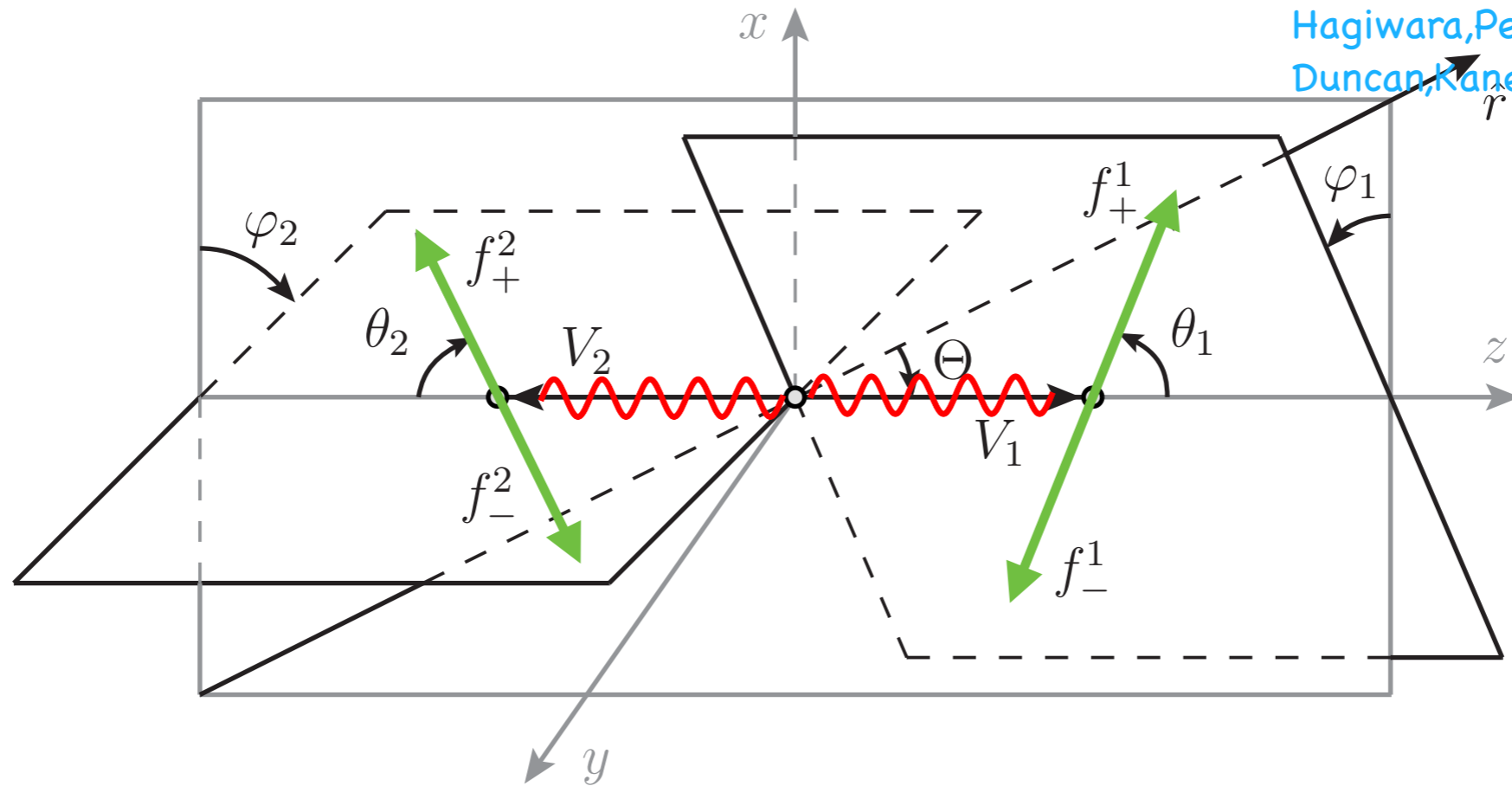
▶ QM **same**, interference possible

Differential measurements WW, WZ

Panico,FR,Wulzer'17,

Hagiwara,Peccei,Zeppenfeld,Hikasa'86

Duncan,Kane,Repko'86



$$Int^{CP} \propto \mathcal{A}_{\mathbf{h}}^{SM (+1, -1)} \mathcal{A}_{\mathbf{h}'}^{BSM+ (+1, +1)} \cos [\Delta \mathbf{h} \cdot \boldsymbol{\varphi}]$$

$(h_1 - h'_1, h_2 - h'_2)$
 (φ_1, φ_2)

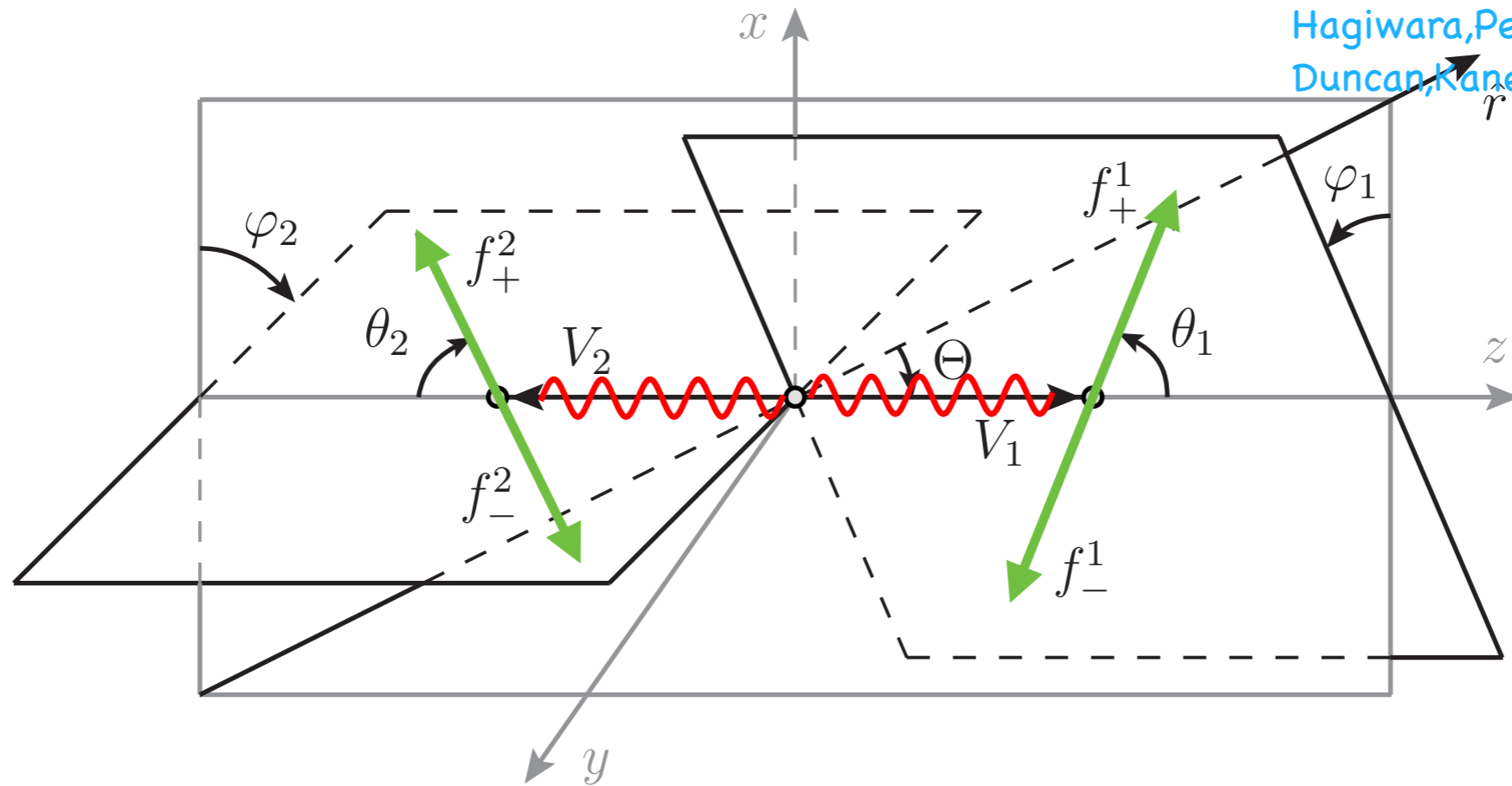
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 (φ_1, φ_2)

$$Int^{CP} \propto \mathcal{A}_{\mathbf{h}}^{SM} \mathcal{A}_{\mathbf{h}'}^{BSM-} \sin [\Delta \mathbf{h} \cdot \boldsymbol{\varphi}]$$

► Cancels when integrated over $\varphi \in [-\pi, \pi]$

Differential measurements $W\gamma$

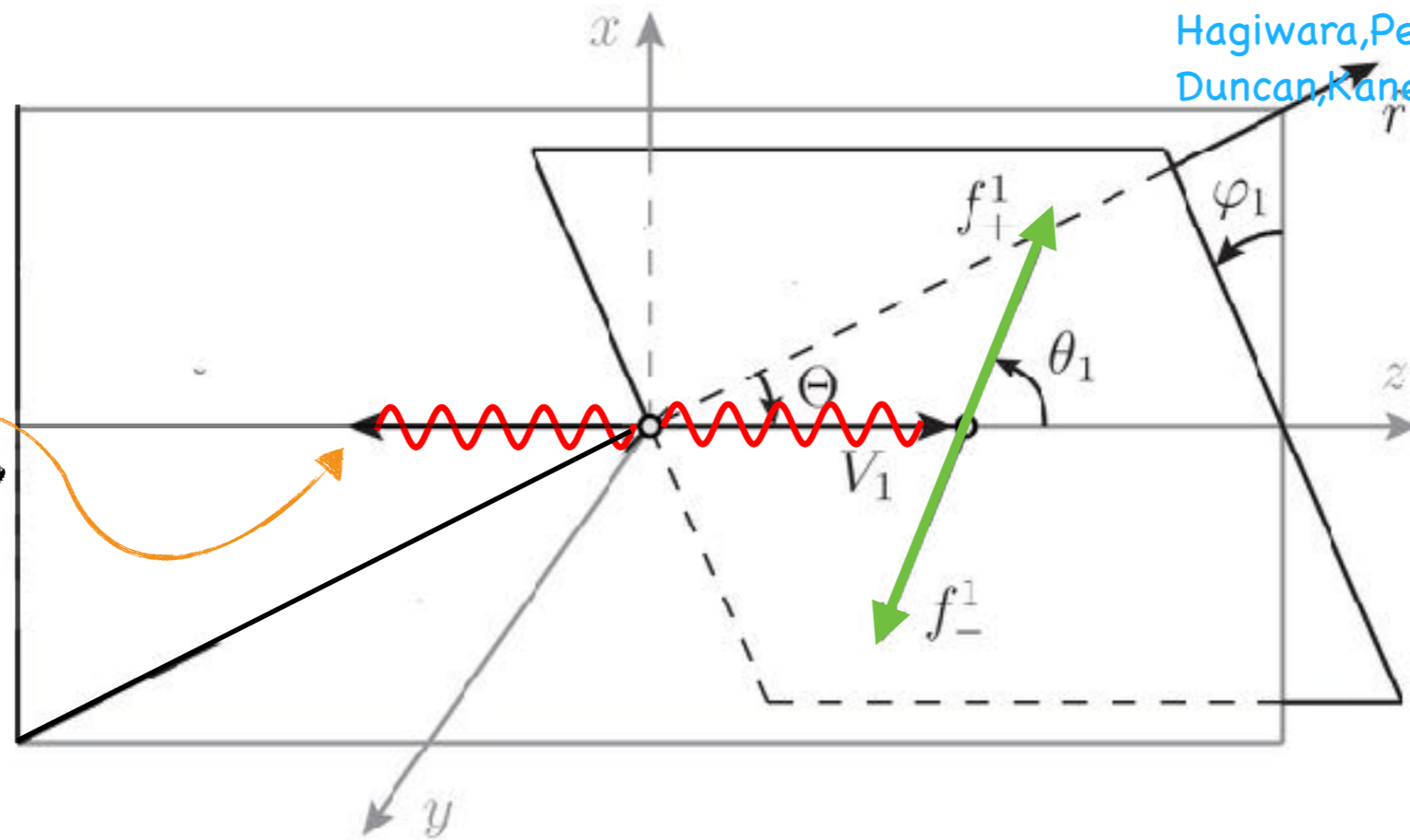
Panico,FR,Wulzer'17,

Hagiwara,Peccei,Zeppenfeld,Hikasa'86

Duncan,Kane,Repko'86

$W\gamma$

No (leptonic)
Branching Ratio



$$Int^{CP} = 2g^2 \sin^2 \theta \mathcal{A}_{++}^{BSM+} [\mathcal{A}_{-++}^{SM} + \mathcal{A}_{+-}^{SM}] \cos 2\varphi ,$$

$$Int^{CP} = 2ig^2 \sin^2 \theta \mathcal{A}_{++}^{BSM-} [\mathcal{A}_{-+-}^{SM} - \mathcal{A}_{+-}^{SM}] \sin 2\varphi$$

Differential measurements $W\gamma$

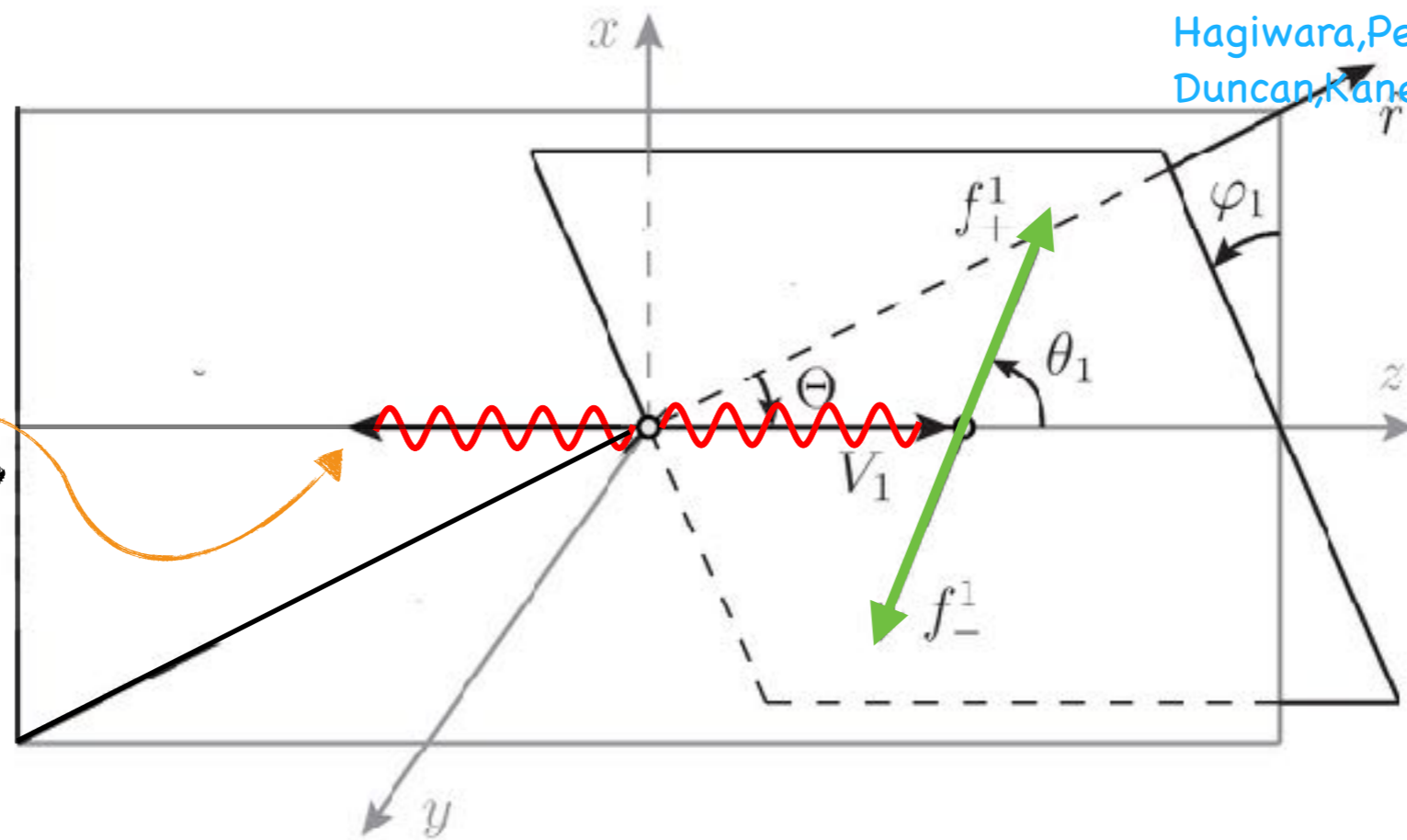
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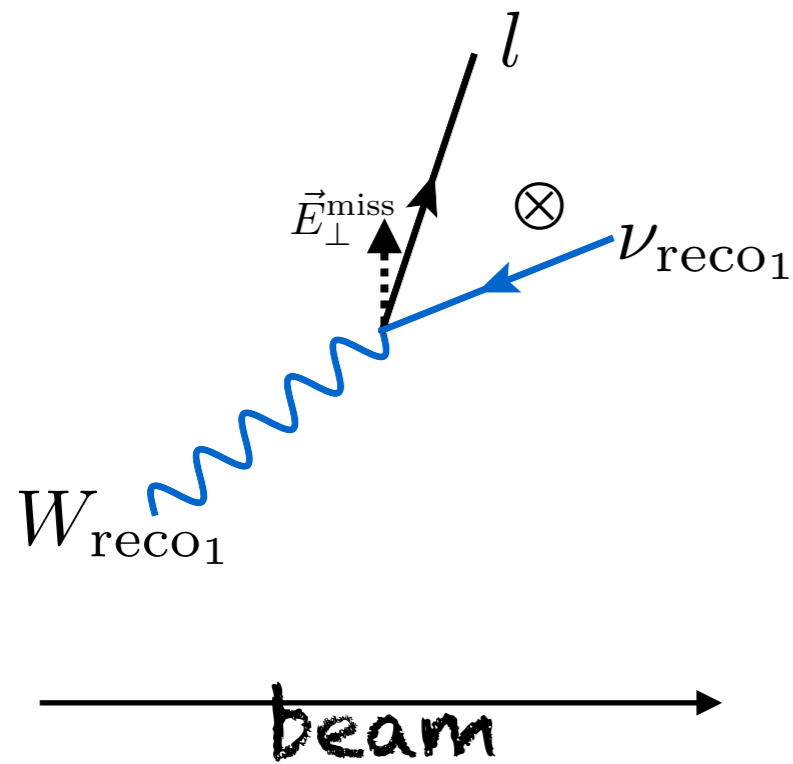
$$Int^{CP} = 2ig^2 \sin^2 \theta \mathcal{A}_{++}^{BSM-} [\mathcal{A}_{-+}^{SM} - \mathcal{A}_{+-}^{SM}] \sin 2\varphi$$

Differential azimuthal distributions = SM-BSM interference

Azimuthal Angle... in reality

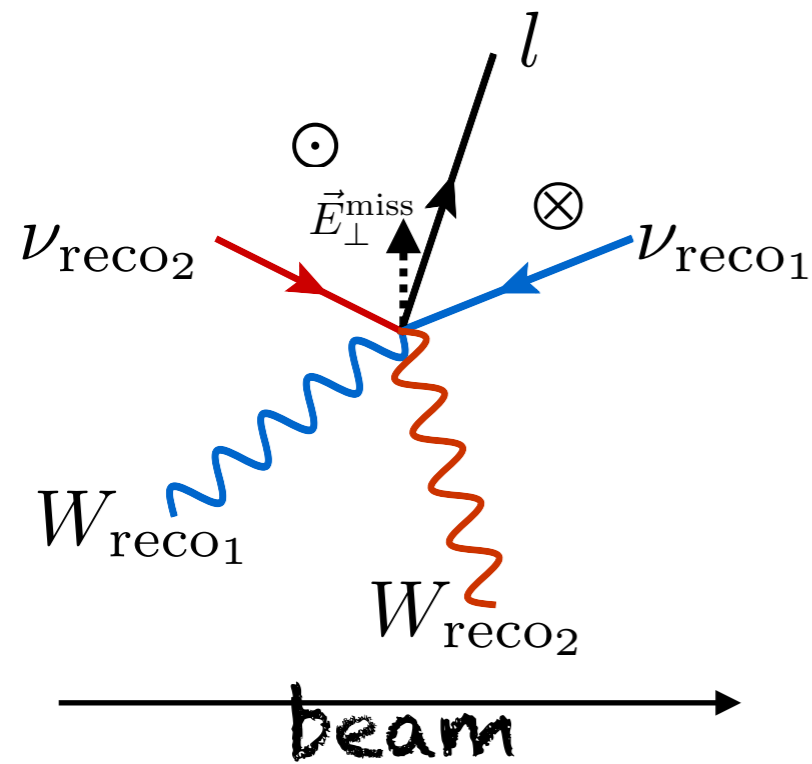
Neutrino: from missing energy + reconstruct W mass

1)



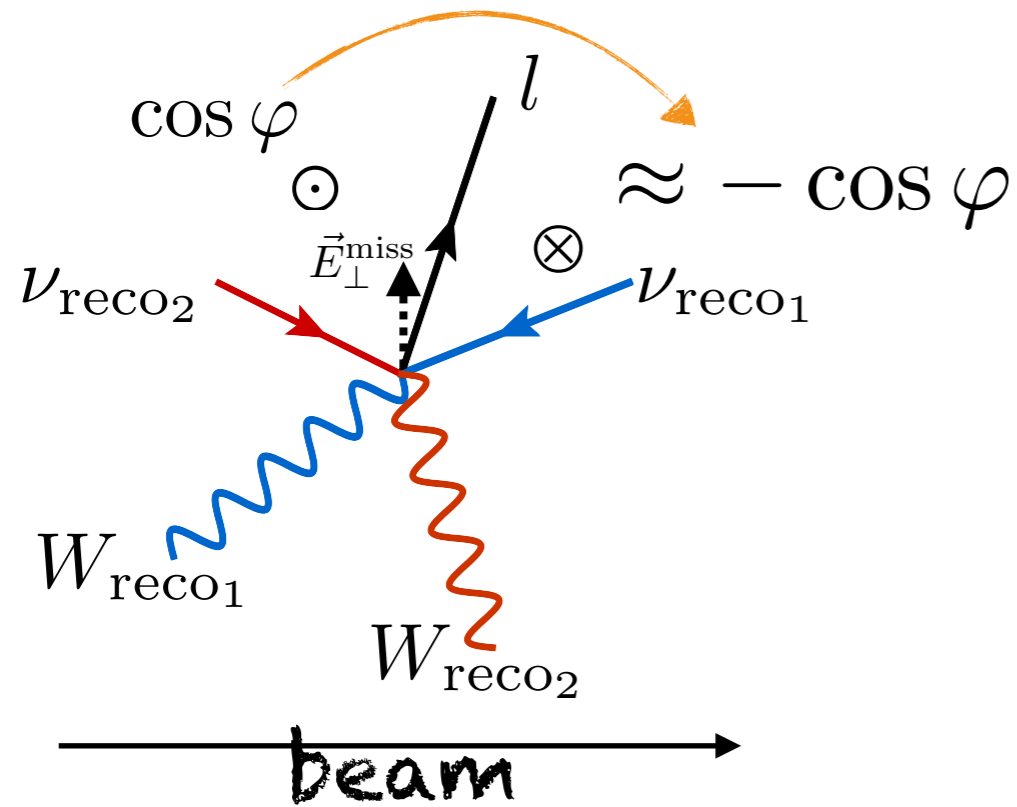
Azimuthal Angle... in reality

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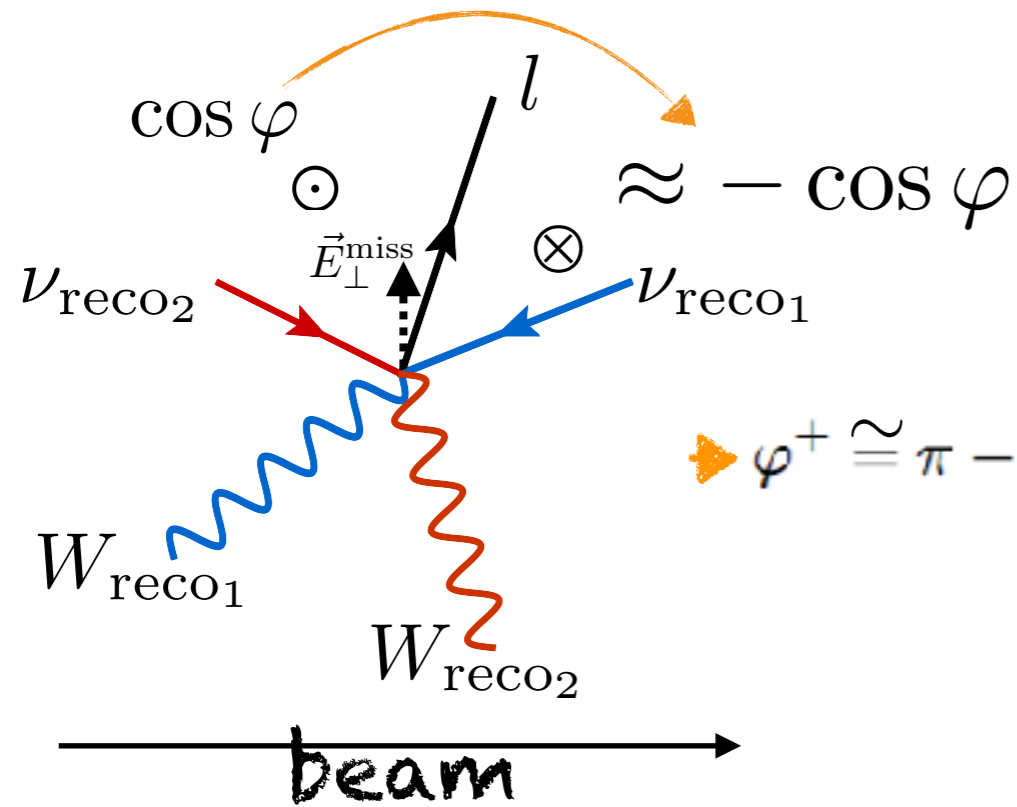
Azimuthal Angle... in reality

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Azimuthal Angle... in reality

Neutrino: from missing energy + reconstruct W mass

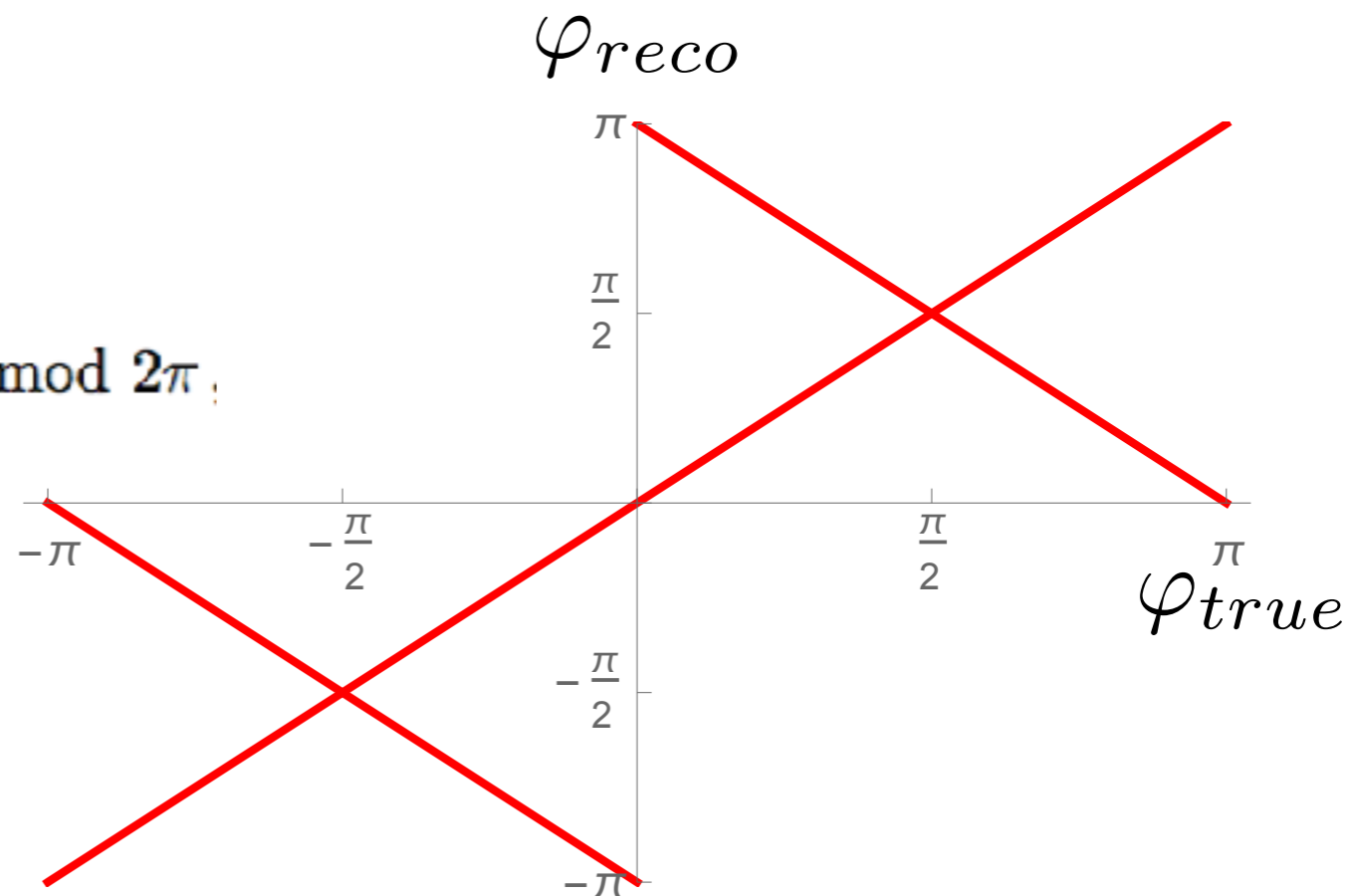
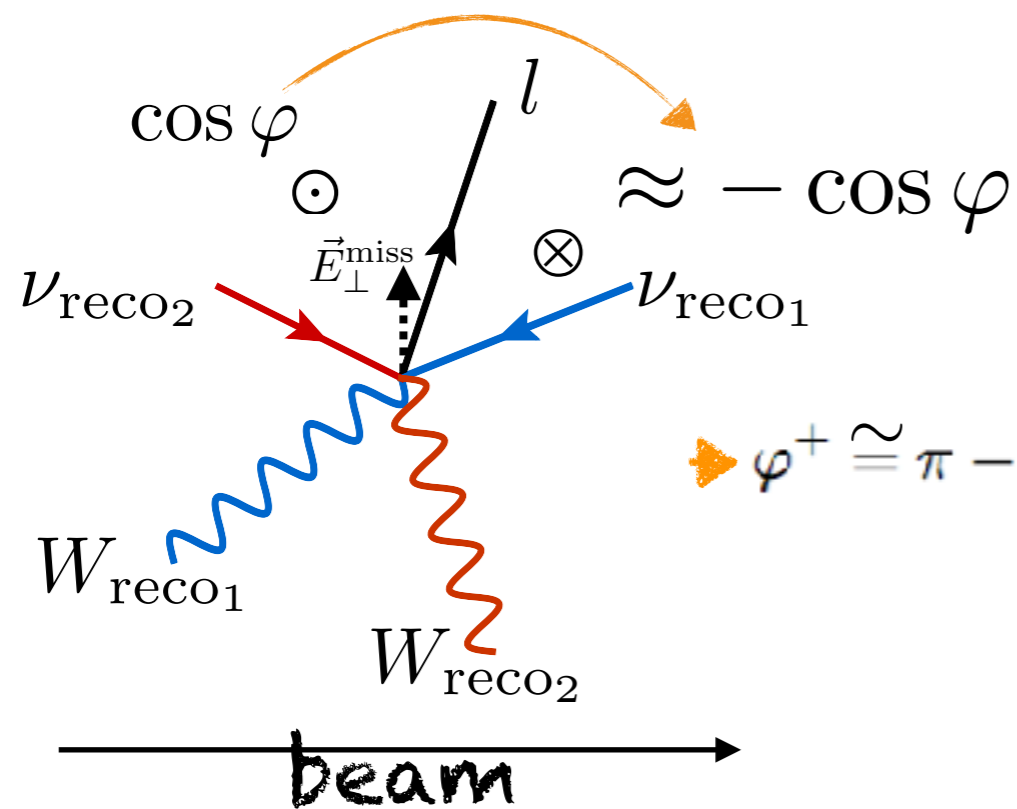


φ_{reco}

φ_{true}

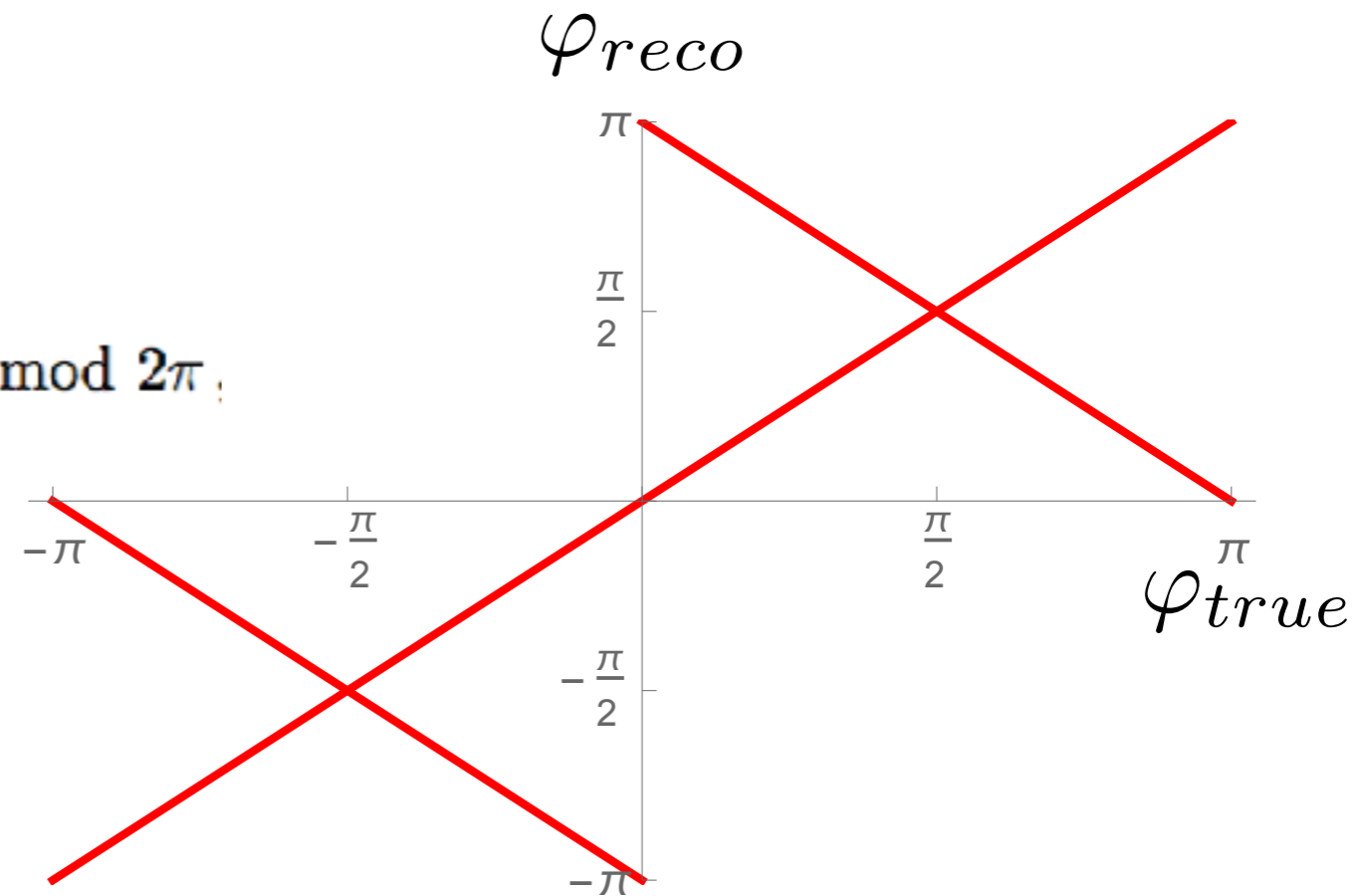
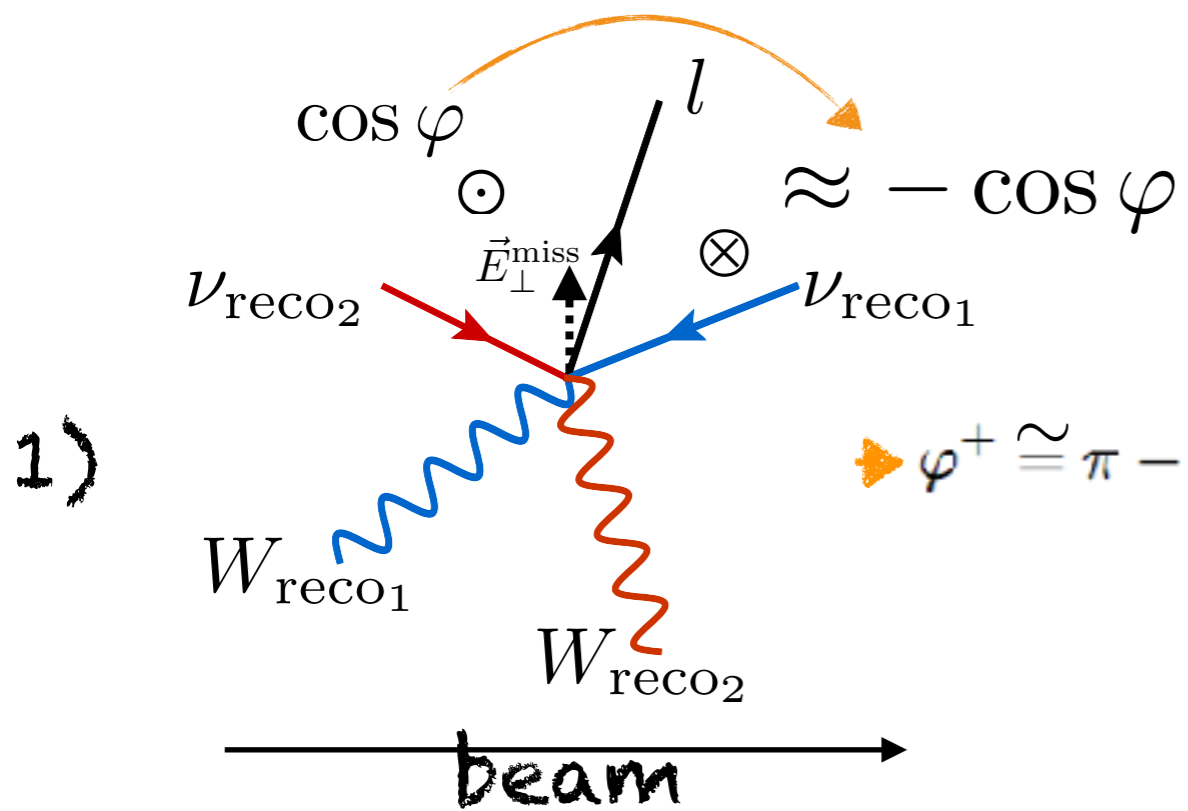
Azimuthal Angle... in reality

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Azimuthal Angle... in reality

Neutrino: from missing energy + reconstruct W mass



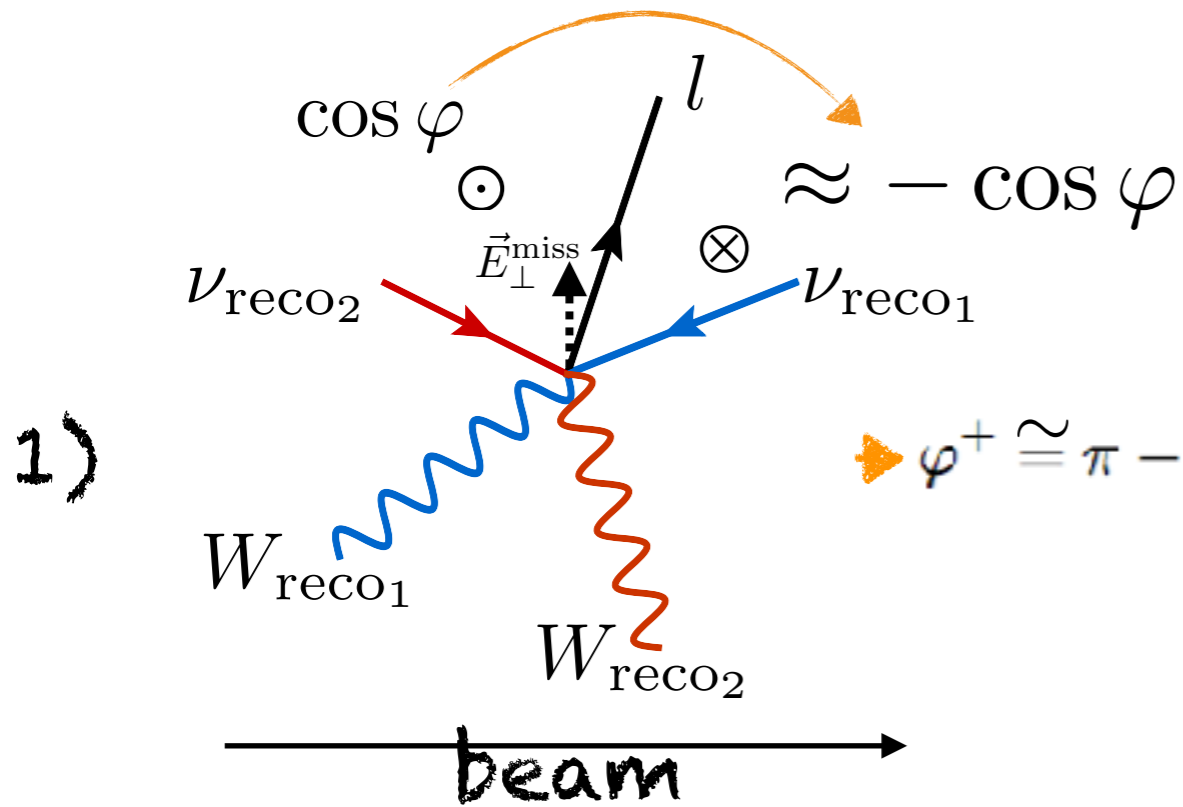
2) Some events: $m_{\perp}^2 > m_W^2$
(off-shell, exp.error)

reconstructed as $m_{\text{inv}}^2 = m_W^2$

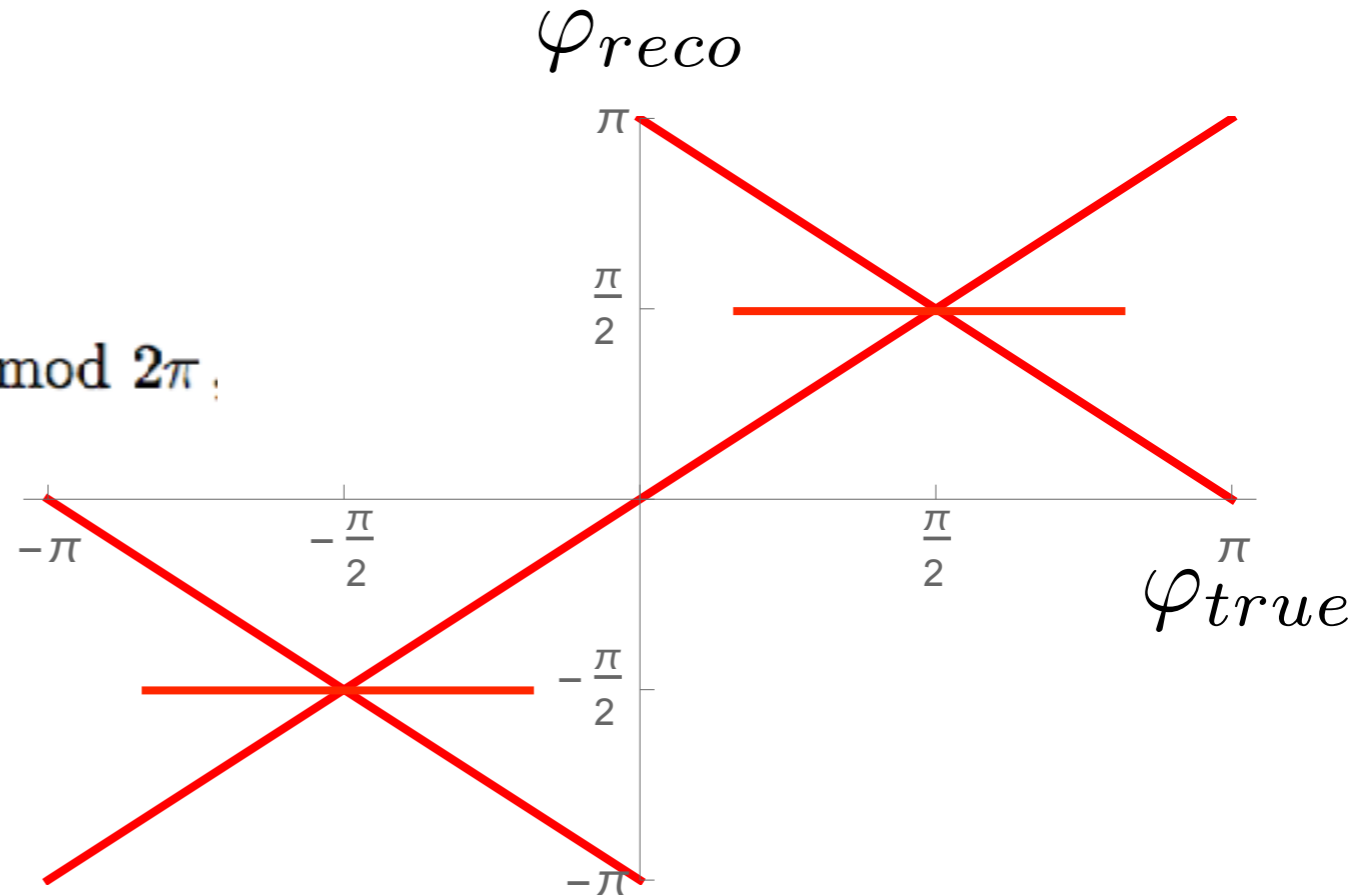
$\varphi = \pi/2$ or $\varphi = -\pi/2$.

Azimuthal Angle... in reality

Neutrino: from missing energy + reconstruct W mass



$\varphi^+ \approx \pi - \varphi^- \pmod{2\pi}$



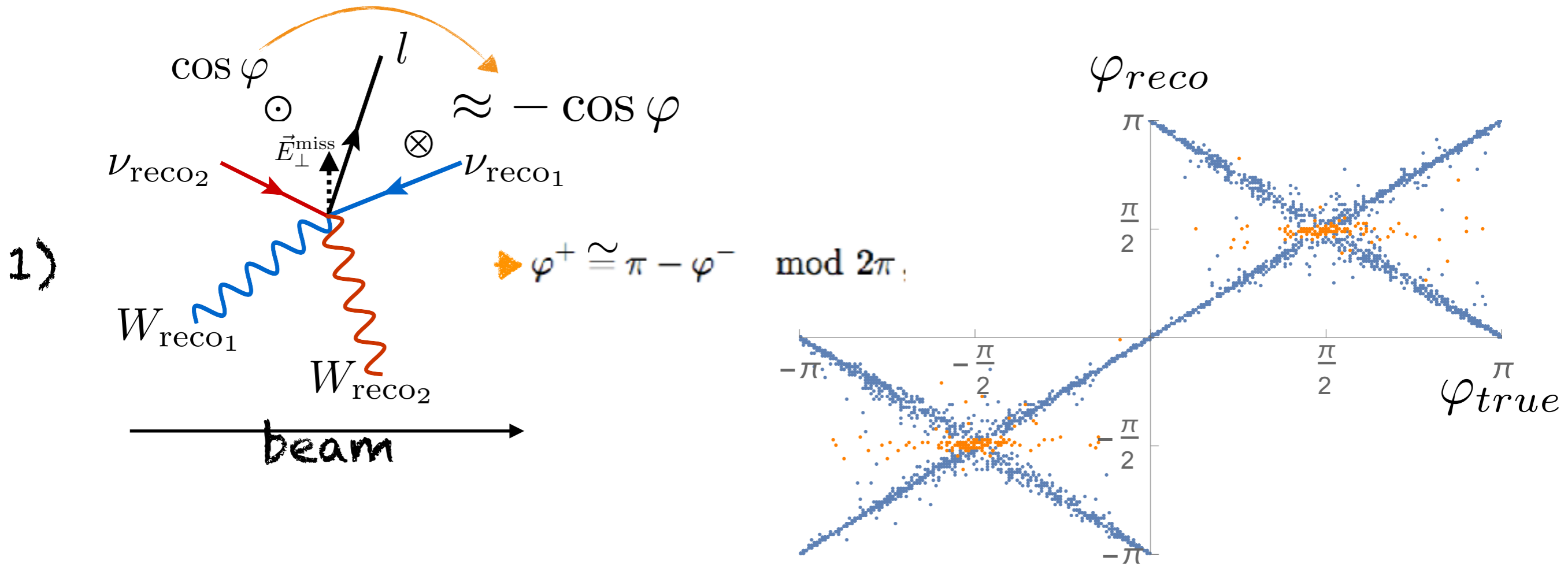
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Azimuthal Angle... in reality

Neutrino: from missing energy + reconstruct W mass



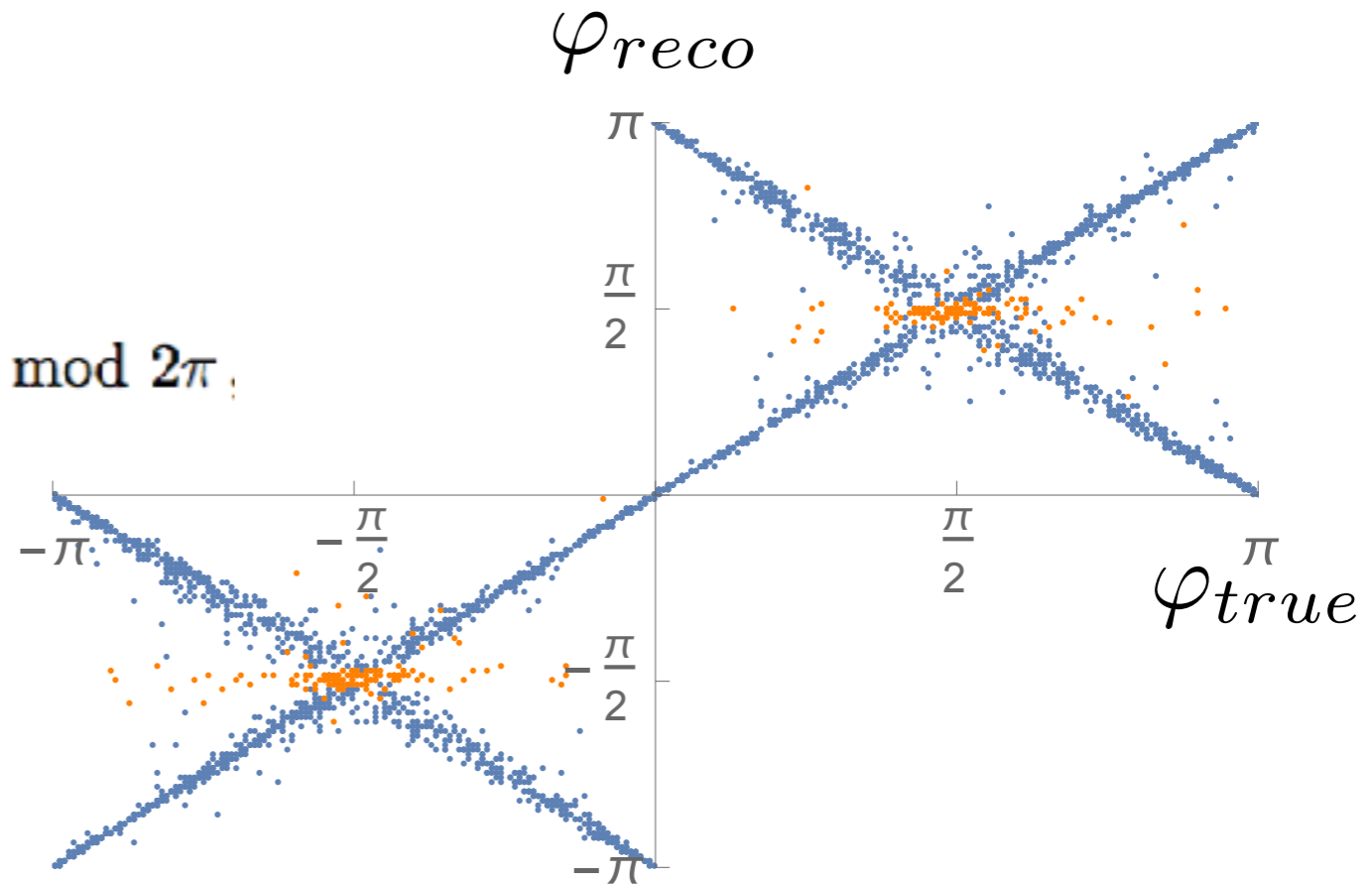
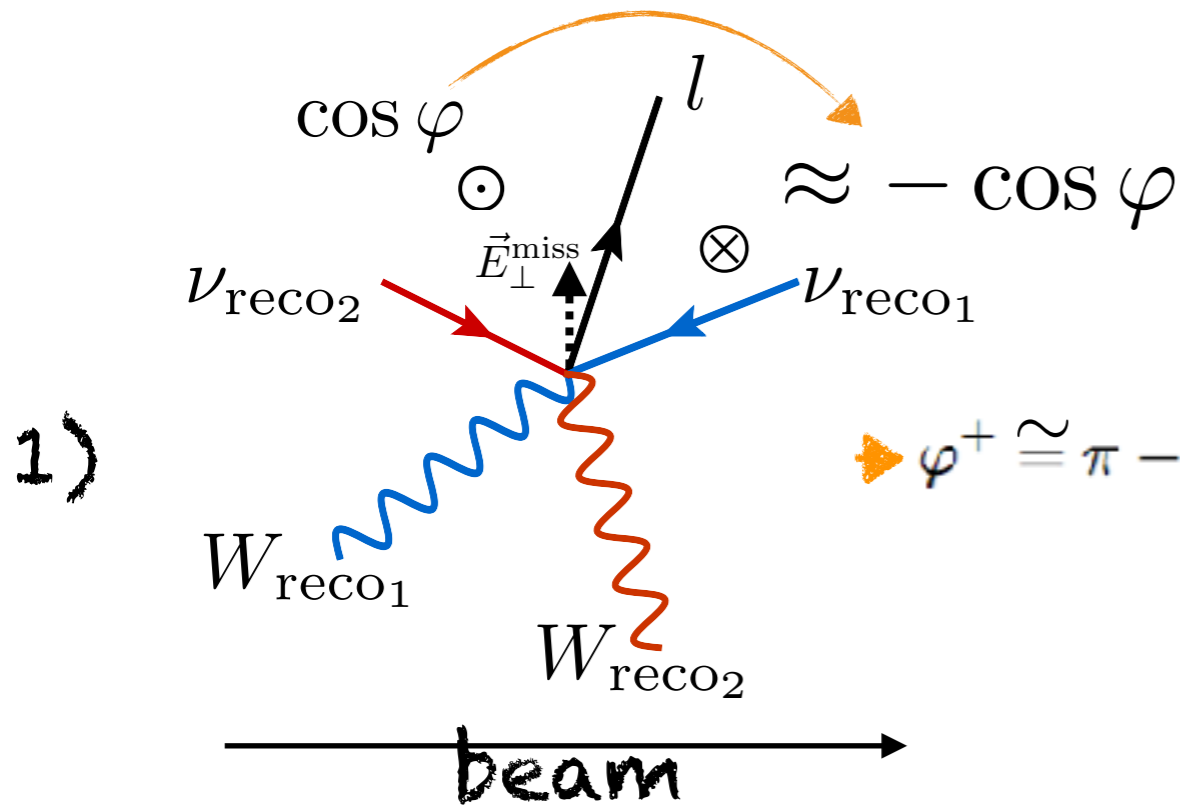
2) Some events: $m_{\perp}^2 > m_W^2$
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► $\varphi = \pi/2$ or $\varphi = -\pi/2$.

Azimuthal Angle... in reality

Neutrino: from missing energy + reconstruct W mass



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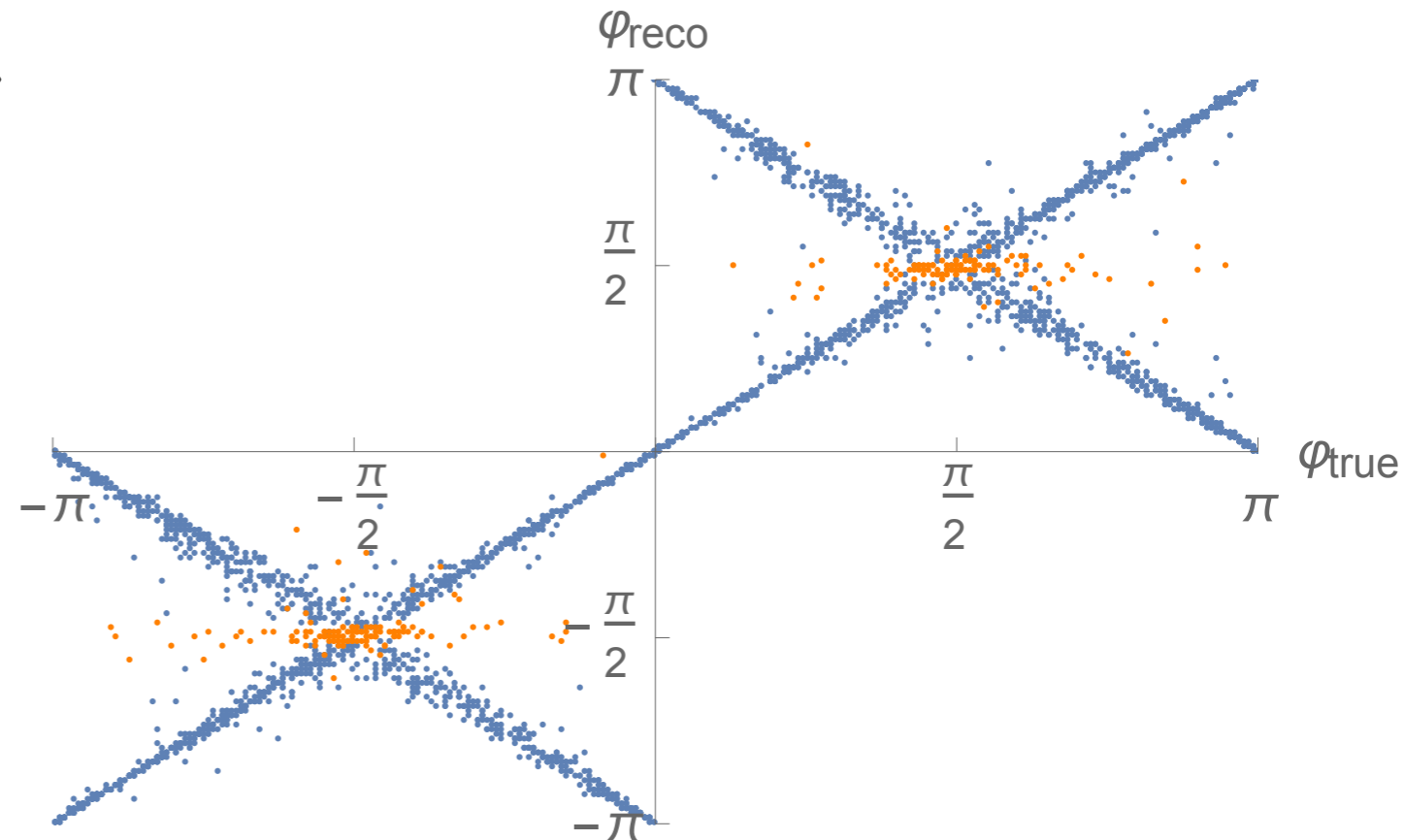
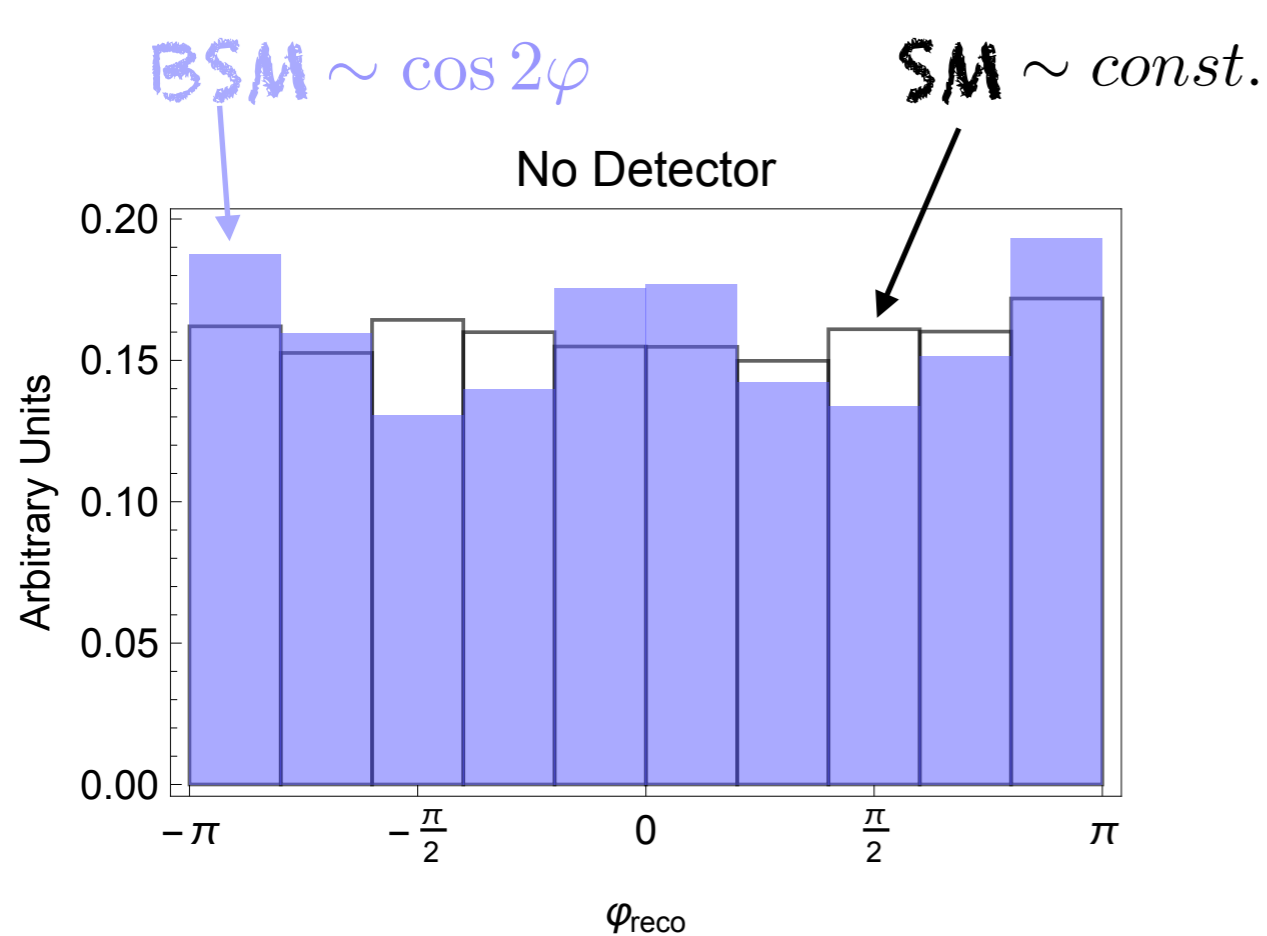
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CP-odd inaccessible!

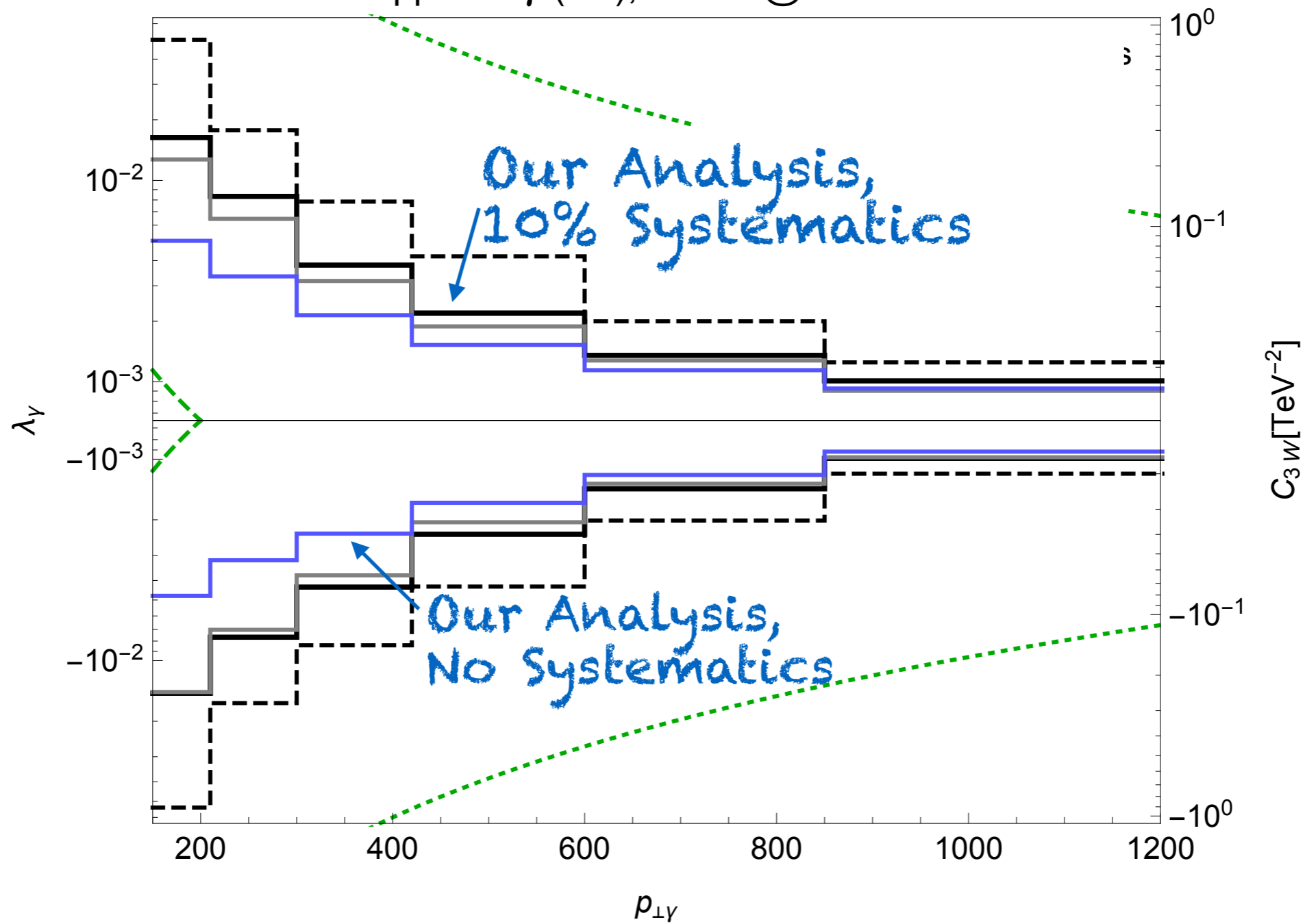
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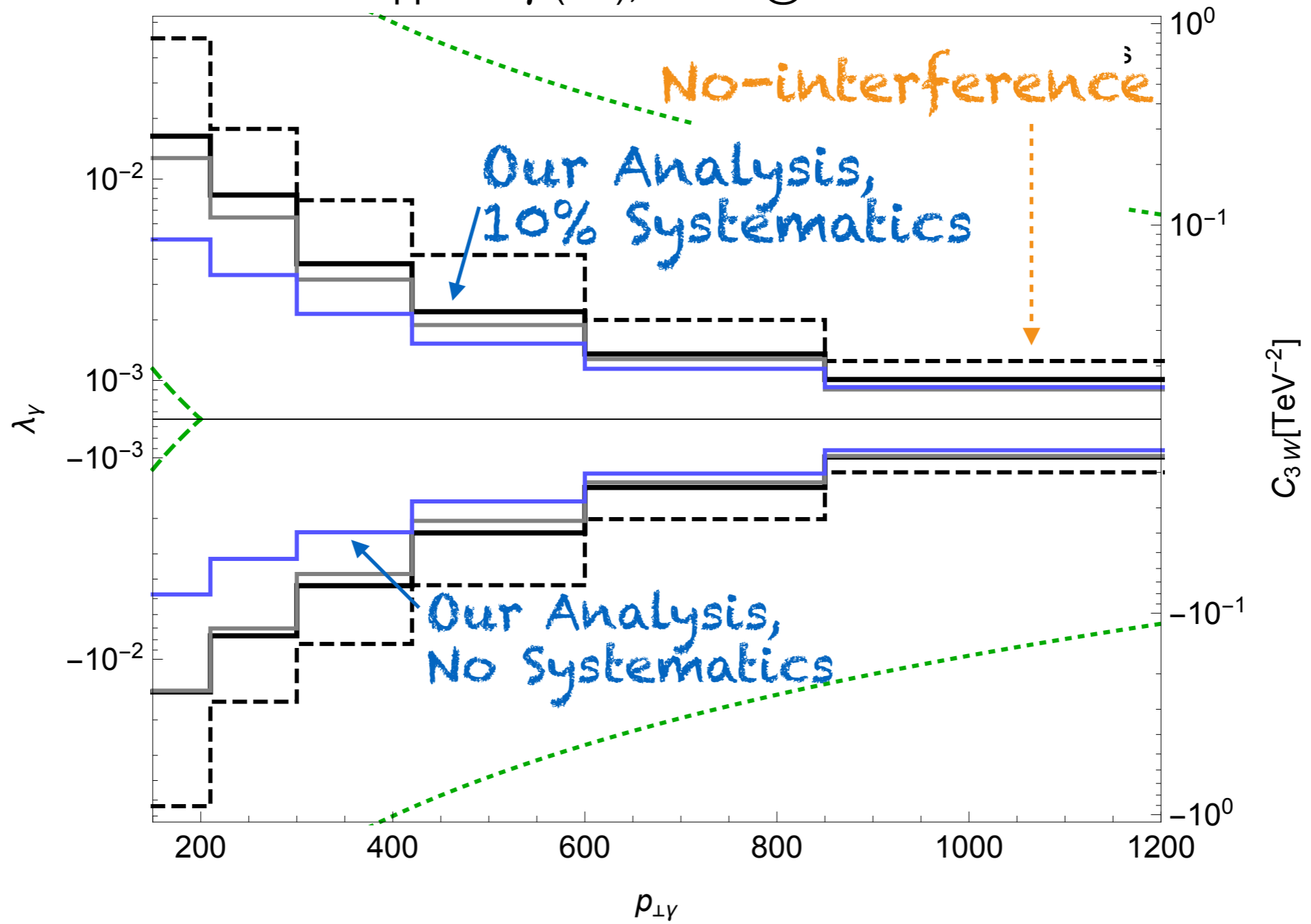
Results

$pp \rightarrow W\gamma$ (LO), 3ab^{-1} @14 TeV



Results

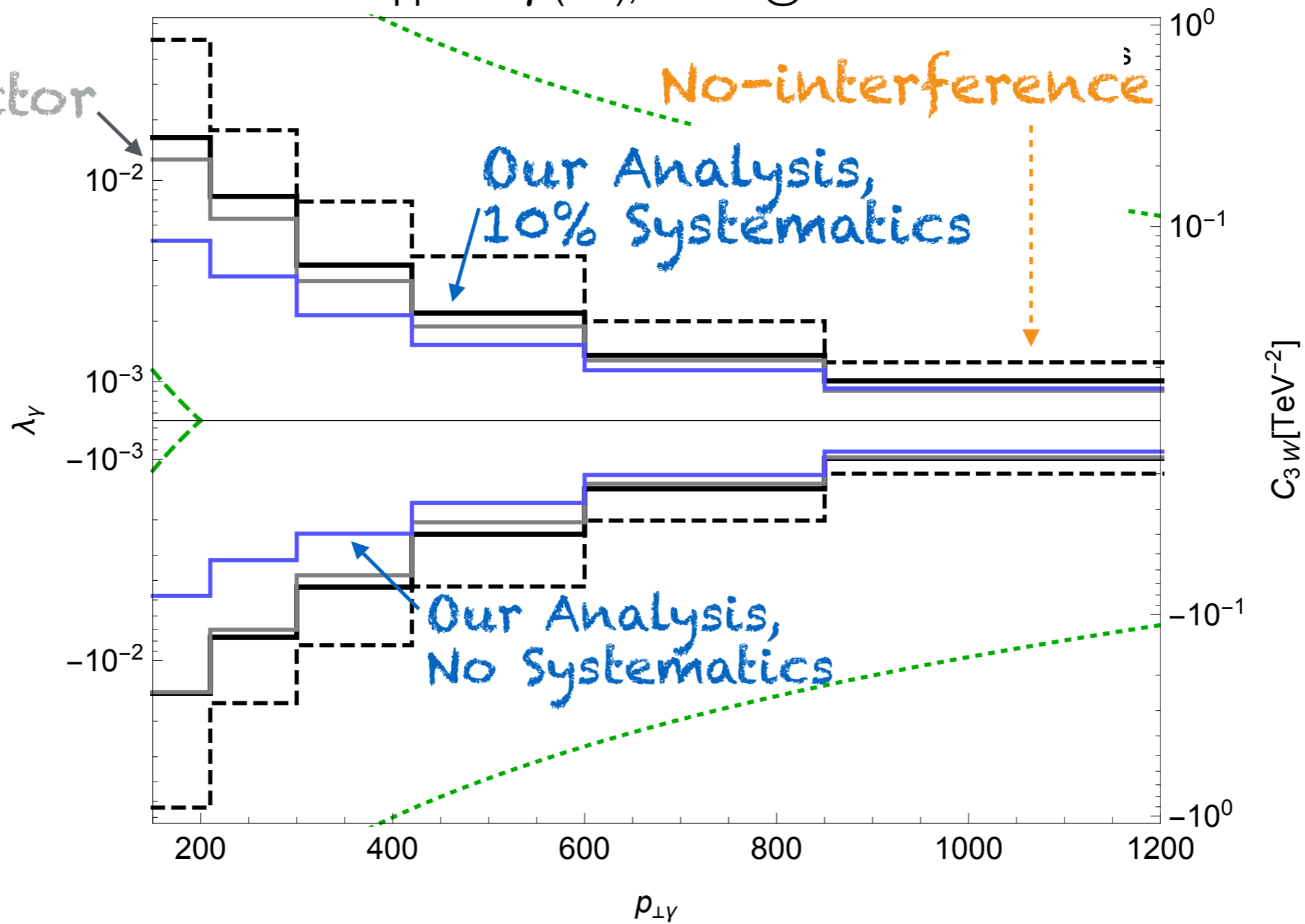
$pp \rightarrow W\gamma$ (LO), 3ab^{-1} @14 TeV



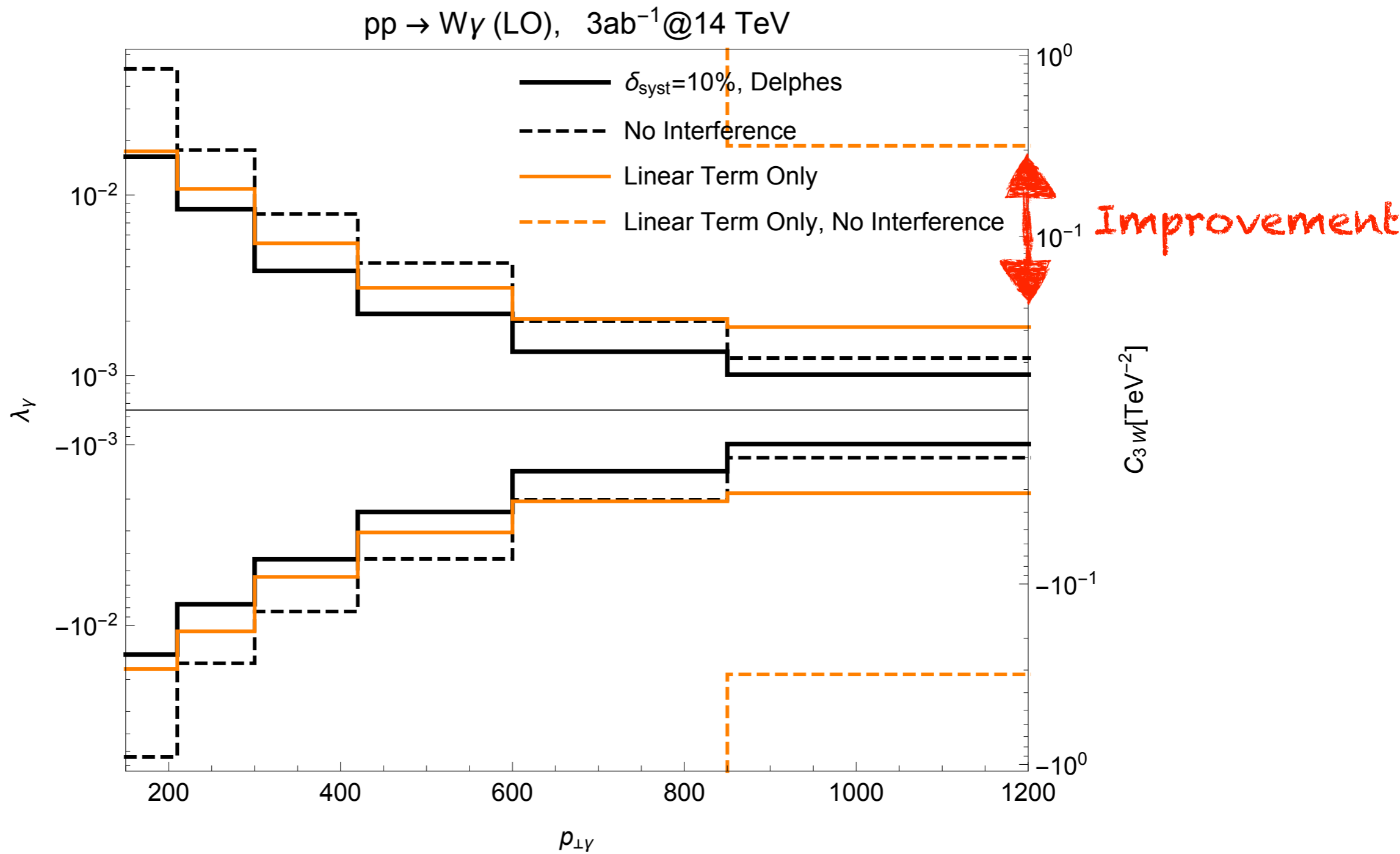
Results

pp \rightarrow W γ (LO), 3ab⁻¹@14 TeV

No detector effects



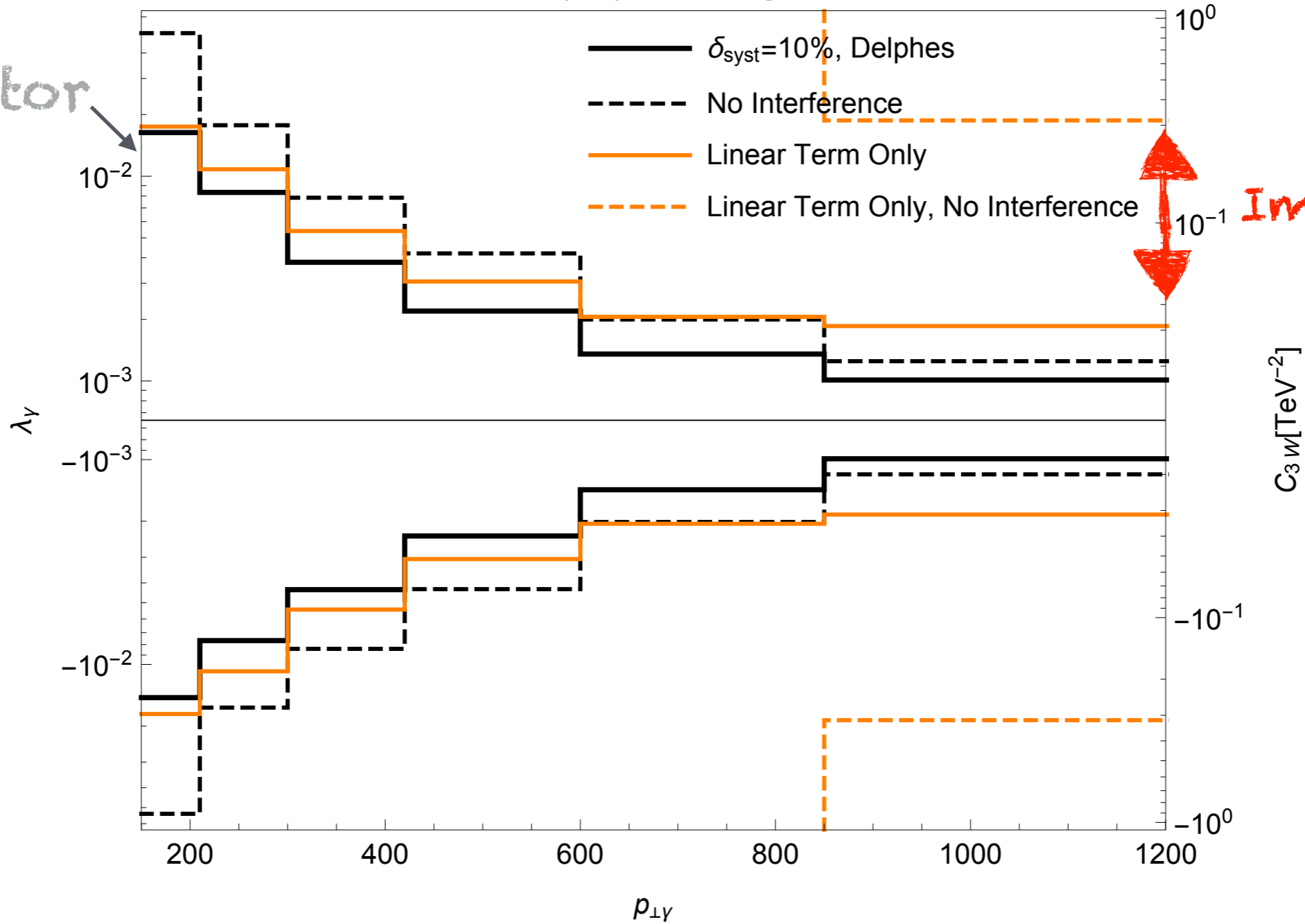
Results



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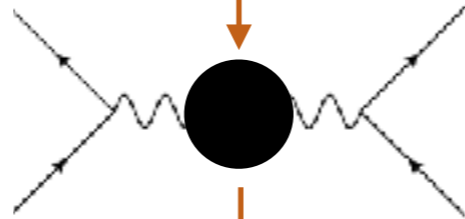


Improvement

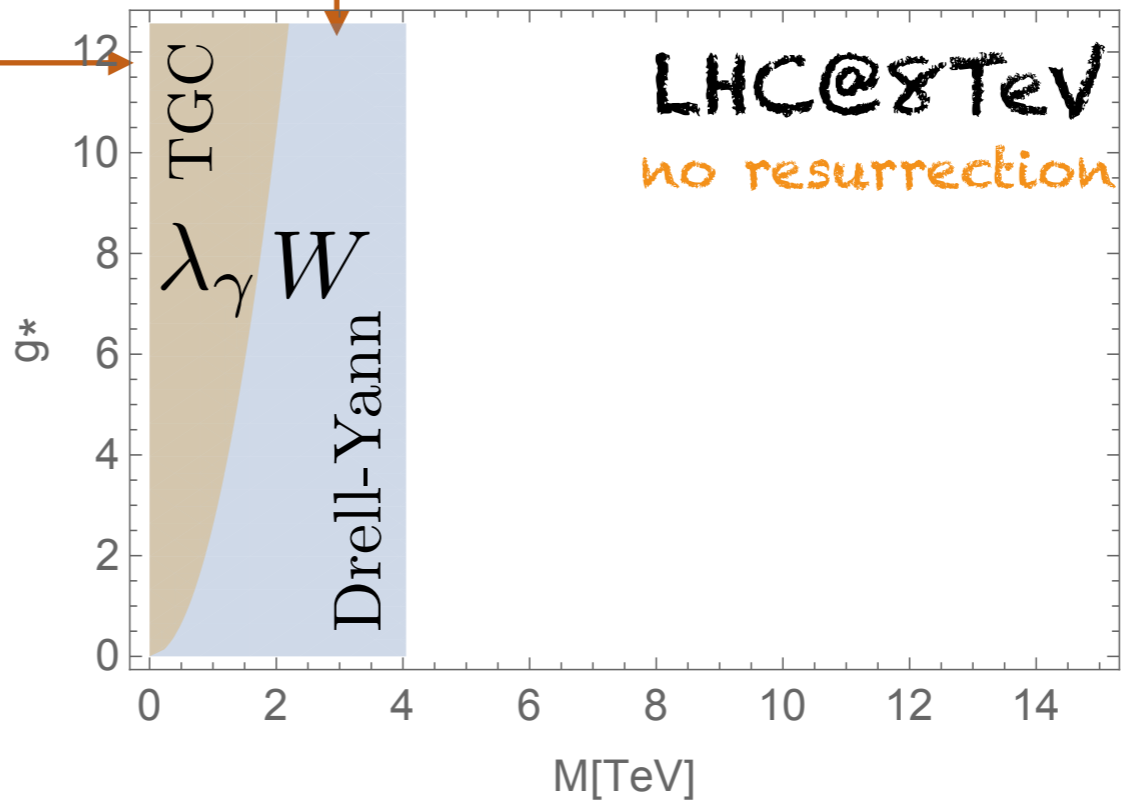
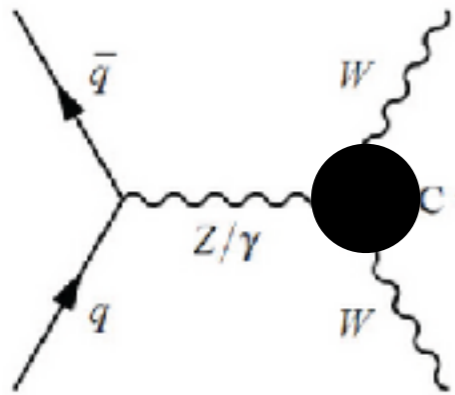
Explicit Model (Remedios)

Remedios Scenario
Liu, Pomarol, Rattazzi, FR'16

$$\frac{1}{M^2} (D_\rho W_\mu^{a,\nu})^2$$



$$\frac{g_*}{M^2} \epsilon_{abc} W_\mu^{a,\nu} W_{\nu\rho}^b W^{c\rho\mu}$$



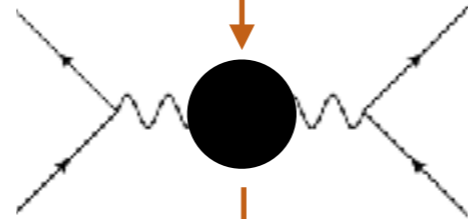
Interference Resurrection makes the difference.

Explicit Model (Remedios)

Liu, Pomarol, Rattazzi, FR'16

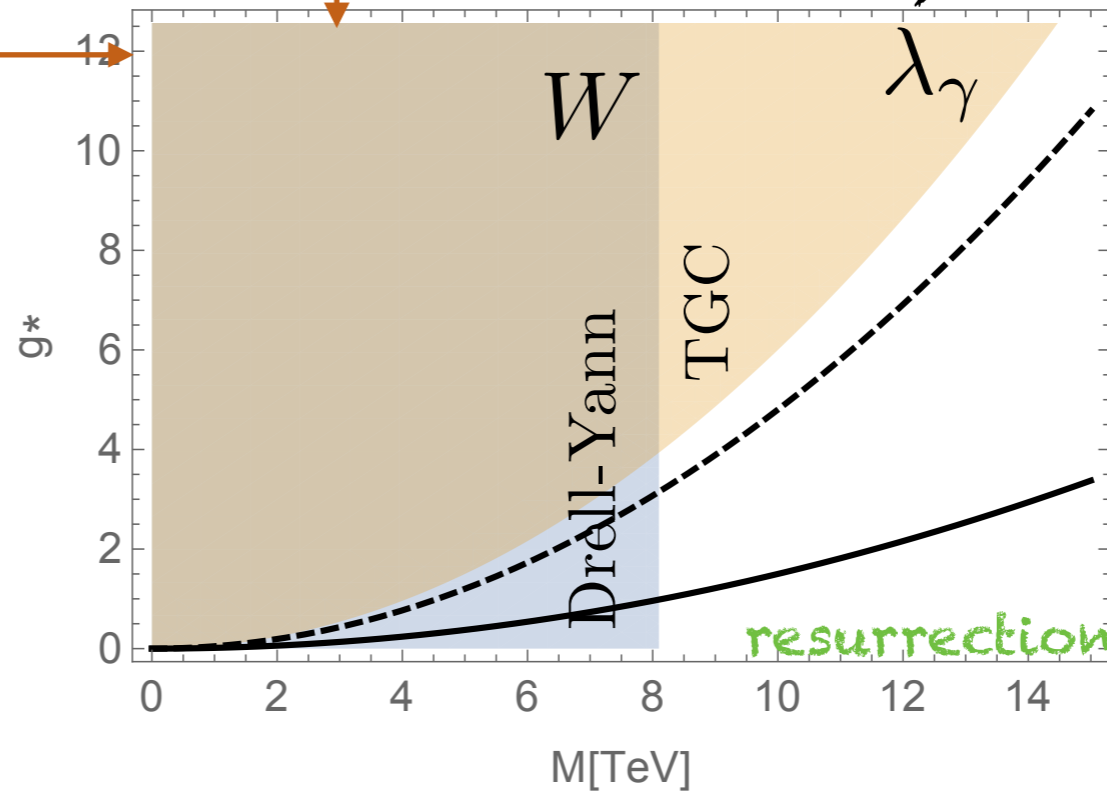
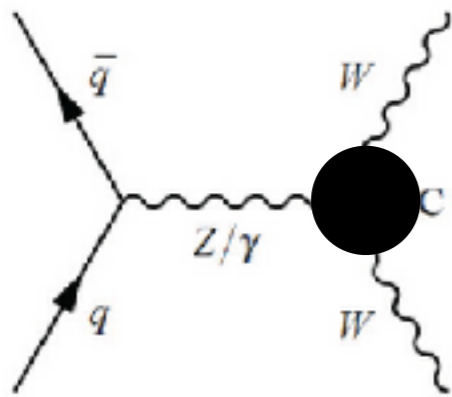
Remedios Scenario
Liu, Pomarol, Rattazzi, FR'16

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LHC@14TeV, 3ab⁻¹

$$\frac{g_*}{M^2} \epsilon_{abc} W_\mu^{a,\nu} W_{\nu\rho}^b W^{c\rho\mu}$$



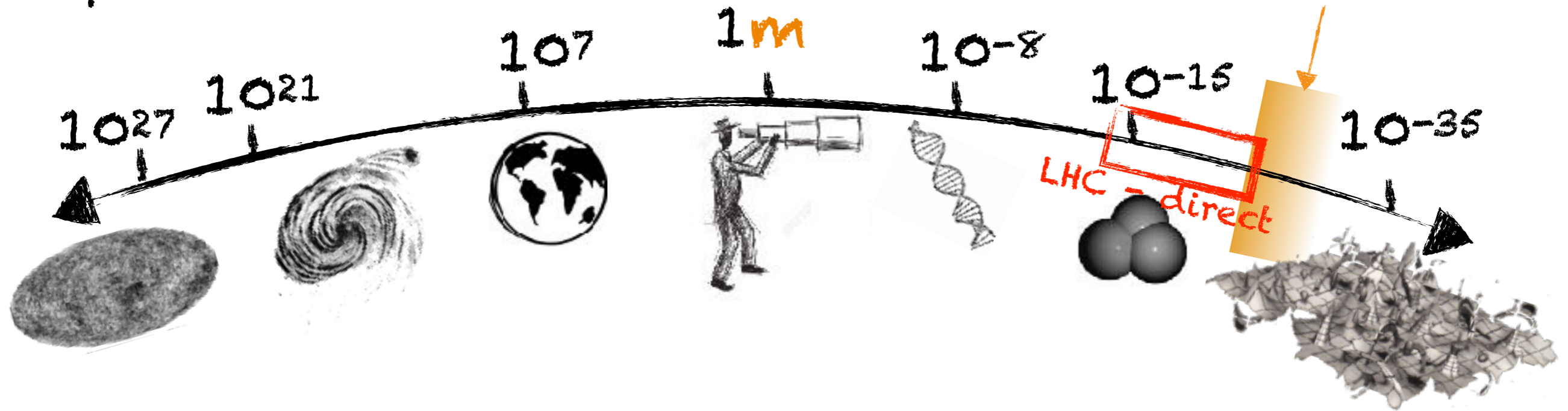
FCCee

CLIC (3TeV)

Interference Resurrection makes the difference.

Message

SM precision tests will define the new distance frontier



Precision: qualitative change in BSM searches

- ▶ New search strategies become possible
- ▶ Precise measurements inspire new model building

Beyond the SM EFT₆: ZZ, Zγ

No dimension-6 E-growing effects in pp → ZZ, Zγ!

What is being looked for so far: nTGC

Anomalous Couplings

$$\begin{aligned} \mathcal{L}_{NP} = & \frac{e}{m_Z^2} \left[- [f_4^\gamma (\partial_\mu F^{\mu\beta}) + f_4^Z (\partial_\mu Z^{\mu\beta})] Z_\alpha (\partial^\alpha Z_\beta) + [f_5^\gamma (\partial^\sigma F_{\sigma\mu}) + f_5^Z (\partial^\sigma Z_{\sigma\mu})] \tilde{Z}^{\mu\beta} Z_\beta \right. \\ & - [h_1^\gamma (\partial^\sigma F_{\sigma\mu}) + h_1^Z (\partial^\sigma Z_{\sigma\mu})] Z_\beta F^{\mu\beta} - [h_3^\gamma (\partial_\sigma F^{\sigma\rho}) + h_3^Z (\partial_\sigma Z^{\sigma\rho})] Z^\alpha \tilde{F}_{\rho\alpha} \\ & - \left\{ \frac{h_2^\gamma}{m_Z^2} [\partial_\alpha \partial_\beta \partial^\rho F_{\rho\mu}] + \frac{h_2^Z}{m_Z^2} [\partial_\alpha \partial_\beta (\square + m_Z^2) Z_\mu] \right\} Z^\alpha F^{\mu\beta} \\ & \left. + \left\{ \frac{h_4^\gamma}{2m_Z^2} [\square \partial^\sigma F^{\rho\alpha}] + \frac{h_4^Z}{2m_Z^2} [(\square + m_Z^2) \partial^\sigma Z^{\rho\alpha}] \right\} Z_\sigma \tilde{F}_{\rho\alpha} \right], \end{aligned} \quad (3)$$

Gounaris,Laysacc,Renard'99

EFT

$$\frac{iH^\dagger \overset{\leftrightarrow}{D}_\mu H D^\nu B_{\nu\rho} B^{\mu\rho}}{\Lambda^4}$$

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Gounaris, Laysacc, Renard'99

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(Longitudinal+Transverse)

► Modifies only the **LT** amplitude:

At high-Energy, every amplitude with odd number of L is suppressed by $m_Z/E \rightarrow$ not maximally growing! ☹️

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► Contributes to **+0/-0** helicity, while SM mainly in **+-**
nTGC don't modify the majority of the process ☹️

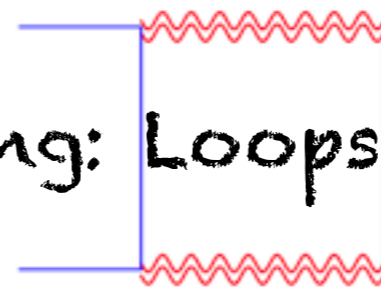
When do dimension-8 make sense?

Symmetries or selection rules can give $C_6 \ll C_8$

Massive spin-2 (KK graviton)

$$\mathcal{L}_g = -\frac{m_g^2}{2} h^{\mu\nu} P_{\mu\nu\rho\sigma} h^{\rho\sigma} - \frac{1}{\bar{M}_p} h^{\mu\nu} T_{\mu\nu} \xrightarrow{E \ll m_g} \mathcal{L}_g^{eff} = \frac{1}{2m_g^2 \bar{M}_p^2} [(T^{\mu\nu} T_{\mu\nu}) - \frac{1}{3} (T^\mu{}_\mu)^2] + \dots$$

But only for weak coupling: Loops generate dim-6!



dim-8!

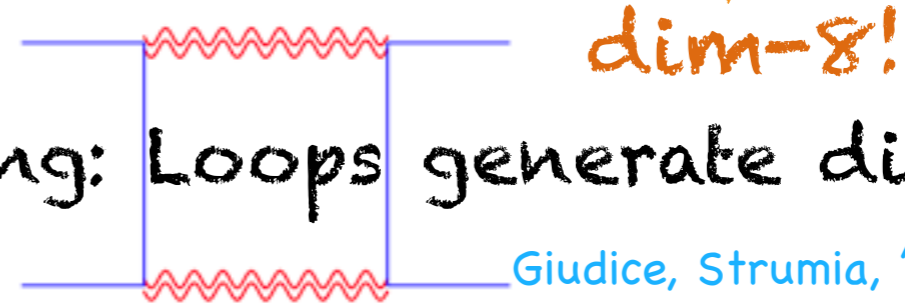
Giudice, Strumia, '03

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(Non-linear) Symmetries (at strong coupling)

► U(1) Goldstone-Boson: $\mathcal{L} = (\partial\phi)^2 + c \frac{(\partial\phi)^4}{\Lambda^4} + \dots$

dim-8

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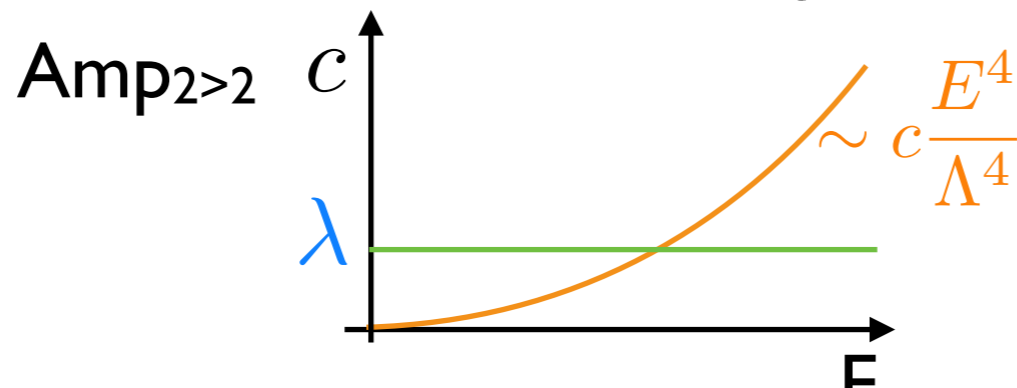


But only for weak coupling: Loops generate dim-6!

(Non-linear) Symmetries (at strong coupling)

► U(1) pseudo Goldstone-Boson: $\mathcal{L} = (\partial\phi)^2 + \lambda\phi^4 + c \frac{(\partial\phi)^4}{\Lambda^4} + \dots$ dim-8

small λ visible at low-E, big c visible at High-E $\lesssim \Lambda$



Dimension-8 and ZZ, Zγ

(Non-linear) Symmetries (at strong coupling)

► Fermions as pseudogoldstini: $g^{\mu\nu} = \eta^{\mu\nu} + \frac{1}{2F^2} (i\bar{\chi}\gamma^\mu\partial^\nu\chi + i\bar{\chi}\gamma^\nu\partial^\mu\chi + \text{h.c.}) + \dots$

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Bardeen, Visnjic'81,
Liu, Pomaral, Rattazzi, FR'16,
Bellazzini, Serra, Sgarlata, FR'17

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Bardeen, Visnjic'81,
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What is the EFT? ...surprise...

$\frac{1}{2\Lambda^4} (i\bar{\psi}\gamma^{\{\mu}\partial^{\nu\}}\psi + \text{h.c.}) D_{\mu}H^{\dagger}D_{\nu}H$	$-\frac{1}{4\Lambda^4} B_{\mu\nu}B^{\mu\rho} (i\bar{\psi}\gamma^{\{\rho}\partial^{\nu\}}\psi + \text{h.c.})$
$\frac{1}{2\Lambda^4} (i\bar{Q}\sigma^a\gamma^{\{\mu}\partial^{\nu\}}Q + \text{h.c.}) D_{\mu}H^{\dagger}\sigma^a D_{\nu}H$	$-\frac{1}{4\Lambda^4} W_{\mu\nu}^a W_{\rho}^{a\mu} (i\bar{\psi}\gamma^{\{\rho}\partial^{\nu\}}\psi + \text{h.c.})$
$\psi = Q, u_R, d_R$	$-\frac{1}{4\Lambda^4} B_{\mu\nu}W_{\rho}^{a\mu} (i\bar{Q}\sigma^a\gamma^{\{\rho}\partial^{\nu\}}Q + \text{h.c.})$

very different from uTGC parametrization!

Energy-Growth

$\frac{1}{2\Lambda^4} \left(i\bar{\psi}\gamma^{\{\mu}\partial^{\nu\}}\psi + \text{h.c.} \right) D_\mu H^\dagger D_\nu H$	$-\frac{1}{4\Lambda^4} B_{\mu\nu} B^\mu{}_\rho \left(i\bar{\psi}\gamma^{\{\rho}\partial^{\nu\}}\psi + \text{h.c.} \right) .$
$\frac{1}{2\Lambda^4} \left(i\bar{Q}\sigma^a\gamma^{\{\mu}\partial^{\nu\}}Q + \text{h.c.} \right) D_\mu H^\dagger \sigma^a D_\nu H$	$-\frac{1}{4\Lambda^4} W_{\mu\nu}^a W^a{}_\rho \left(i\bar{\psi}\gamma^{\{\rho}\partial^{\nu\}}\psi + \text{h.c.} \right) .$
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LL final states (ZZ only)

TT final states (ZZ, ZY, YY)

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LL final states (ZZ only)

TT final states (ZZ, ZY, YY)

▶ No LT (no m_Z/E suppression)

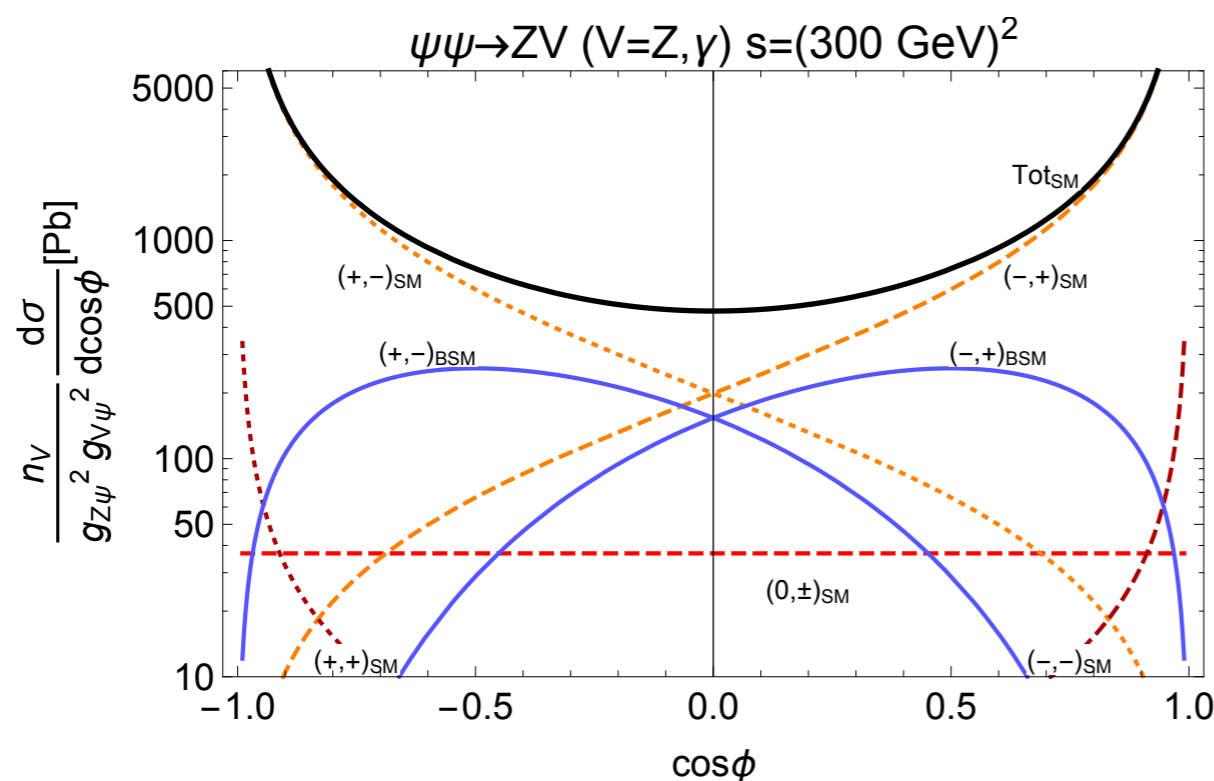
▶ Both grow as E^4/Λ^4 in amplitude

Helicity

$\frac{1}{2\Lambda^4} \left(i\bar{\psi}\gamma^{\{\mu}\partial^{\nu\}}\psi + \text{h.c.} \right) D_\mu H^\dagger D_\nu H$	$-\frac{1}{4\Lambda^4} B_{\mu\nu} B^\mu{}_\rho \left(i\bar{\psi}\gamma^{\{\rho}\partial^{\nu\}}\psi + \text{h.c.} \right) .$
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00

+-



- **Interferes** with largest SM contribution
- **Sensitivity enhanced!**

Positivity Constraints

Fundamental principles from unitarity/analyticity imply constraints on coefficient in front! unique of these dimension-8

Adams, Arkani-Hamed, Dubovsky, Nicolis, Rattazzi' hep-th/0602178
Bellazzini' 1605.06111

$\frac{1}{2\Lambda^4} \left(i\bar{\psi}\gamma^{\{\mu}\partial^{\nu\}}\psi + \text{h.c.} \right) D_\mu H^\dagger D_\nu H$	$-\frac{1}{4\Lambda^4} B_{\mu\nu} B^\mu{}_\rho \left(i\bar{\psi}\gamma^{\{\rho}\partial^{\nu\}}\psi + \text{h.c.} \right) .$
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$c=0$

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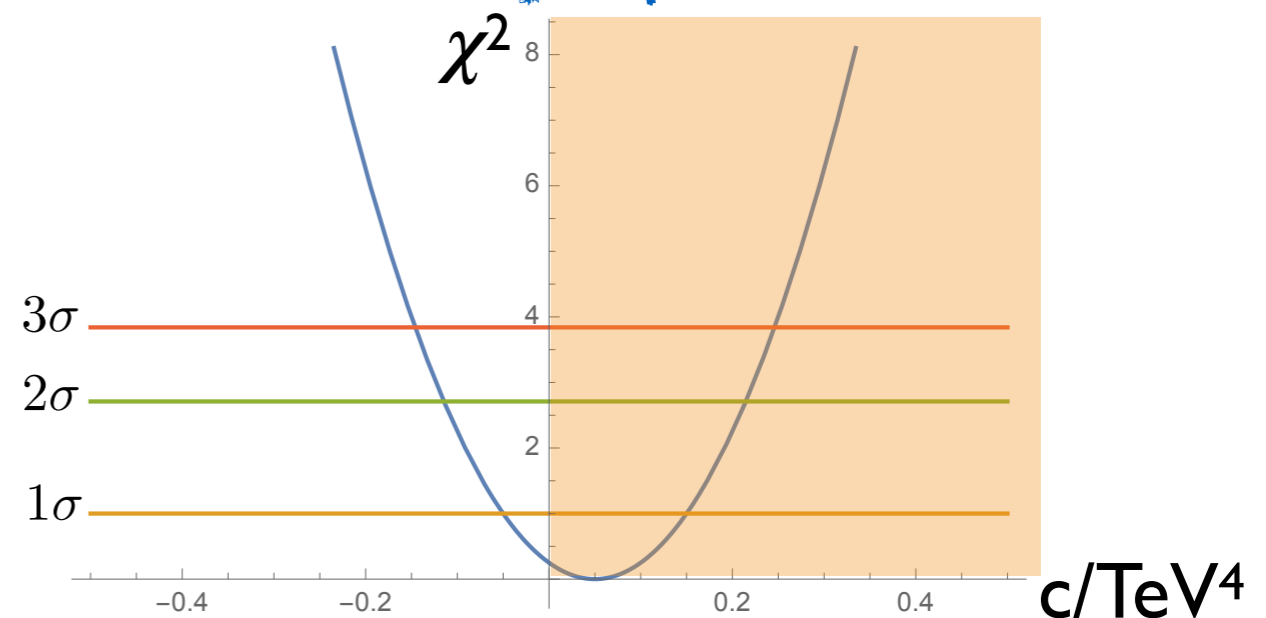
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$c=0$

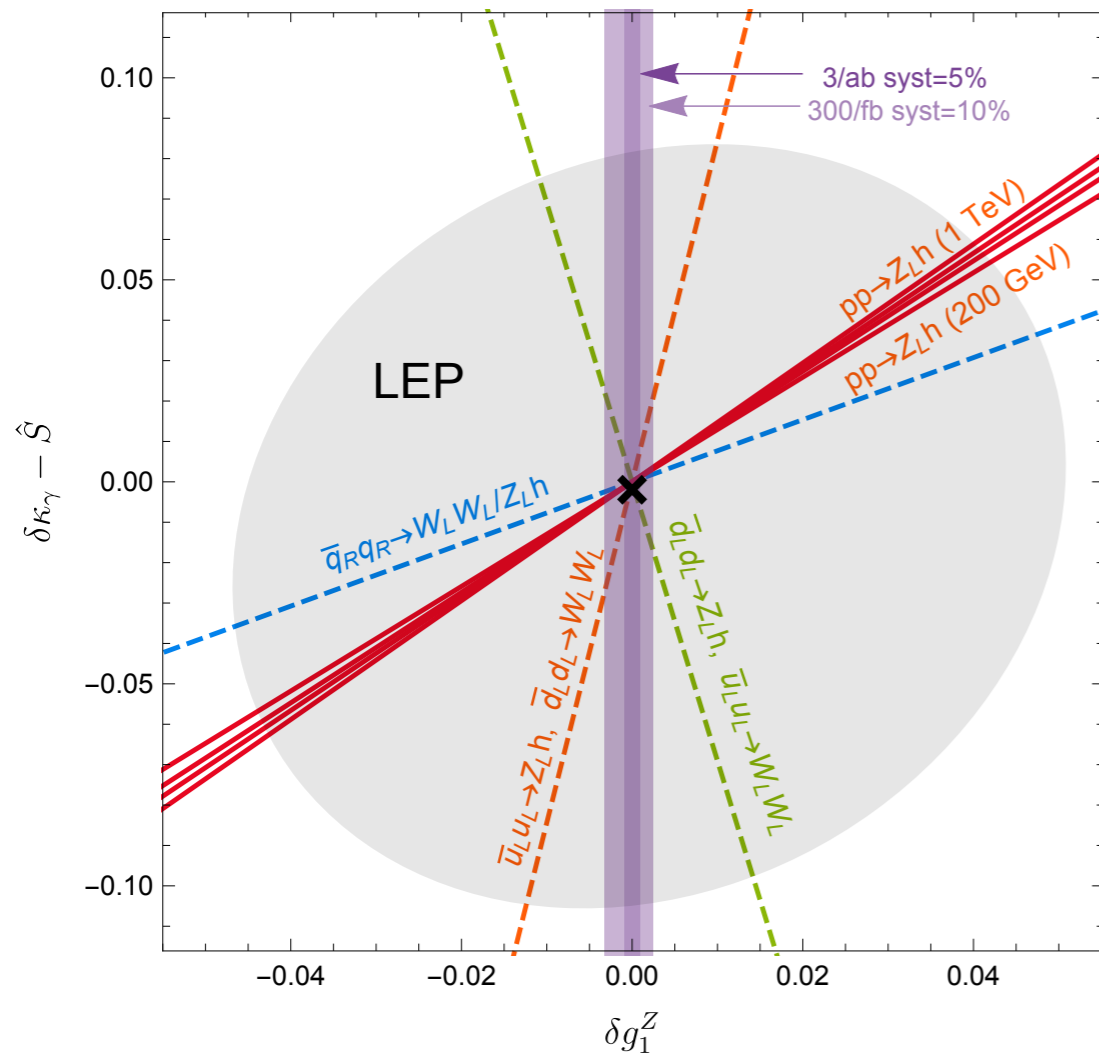
$c>0$ (always positive!)

Smaller viable parameter space

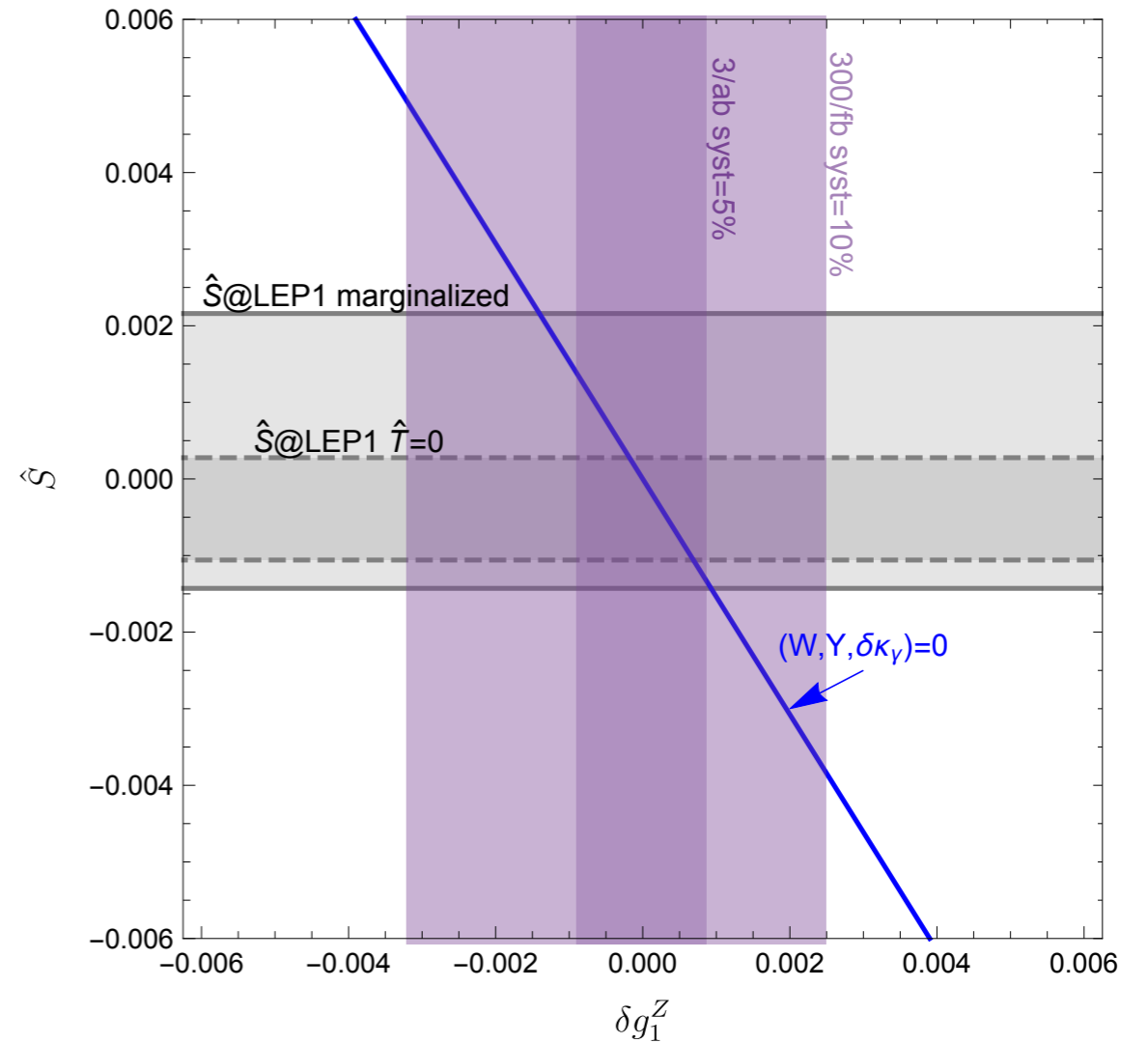


Comparisons

high-E is unique, but it compares at lower-E with different effects:



...with TGCs at LEP2



...with S-parameter at LEP1

▶ Genuine SM precision test

Why Interference?

When SM and BSM contribute to the same amplitude:

$$\text{Amp} = SM + BSM = SM(1 + \delta_{BSM})$$

$\delta_{BSM} = c \frac{E^2}{M^2}$

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$$Amp = SM + BSM = SM(1 + \delta_{BSM})$$

$\delta_{BSM} = c \frac{E^2}{M^2}$

► $\sigma \propto |Amp|^2 \simeq SM^2(1 + \delta_{BSM} + \delta_{BSM}^2)$

For **small** BSM effects $1 \gg \delta_{BSM}$,

interference dominates $\delta_{BSM} \gg \delta_{BSM}^2$

Non-Interference?

If SM and BSM contribute to different amplitudes:

$$\sigma \propto \sum |Amp|^2 \simeq SM^2 \left(1 + \cancel{c_i \frac{E^2}{\Lambda^2}} + c_i^2 \frac{E^4}{\Lambda^4} \right)$$

interference vanishes

Non-Interference?

If SM and BSM contribute to different amplitudes:

interference vanishes

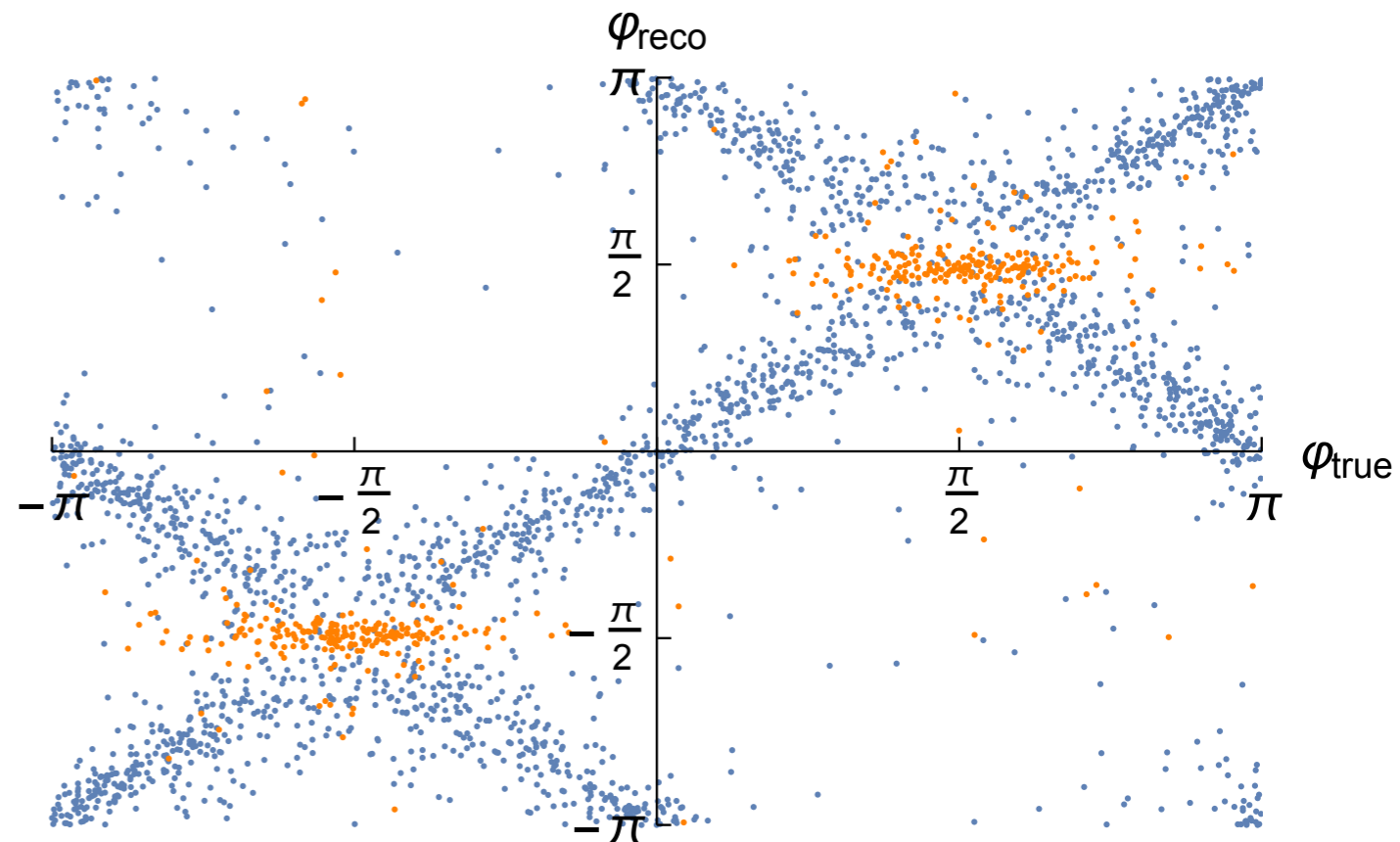
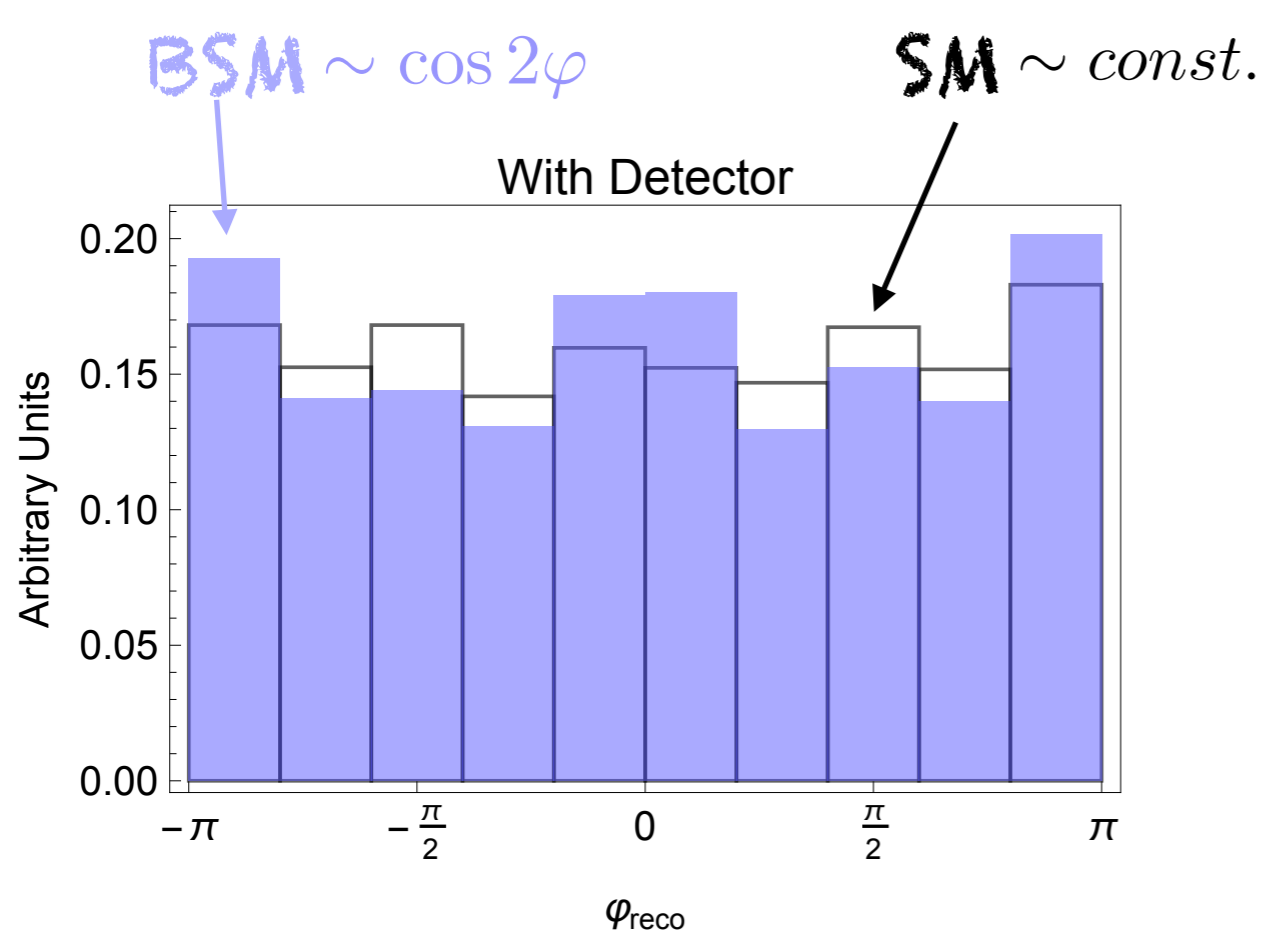
$$\sigma \propto \sum |Amp|^2 \simeq SM^2 \left(1 + \cancel{c_i \frac{E^2}{\Lambda^2}} + c_i^2 \frac{E^4}{\Lambda^4} \right)$$

The leading effects BSM are $O\left(\frac{1}{\Lambda^4}\right)$

► Small effects, even smaller!

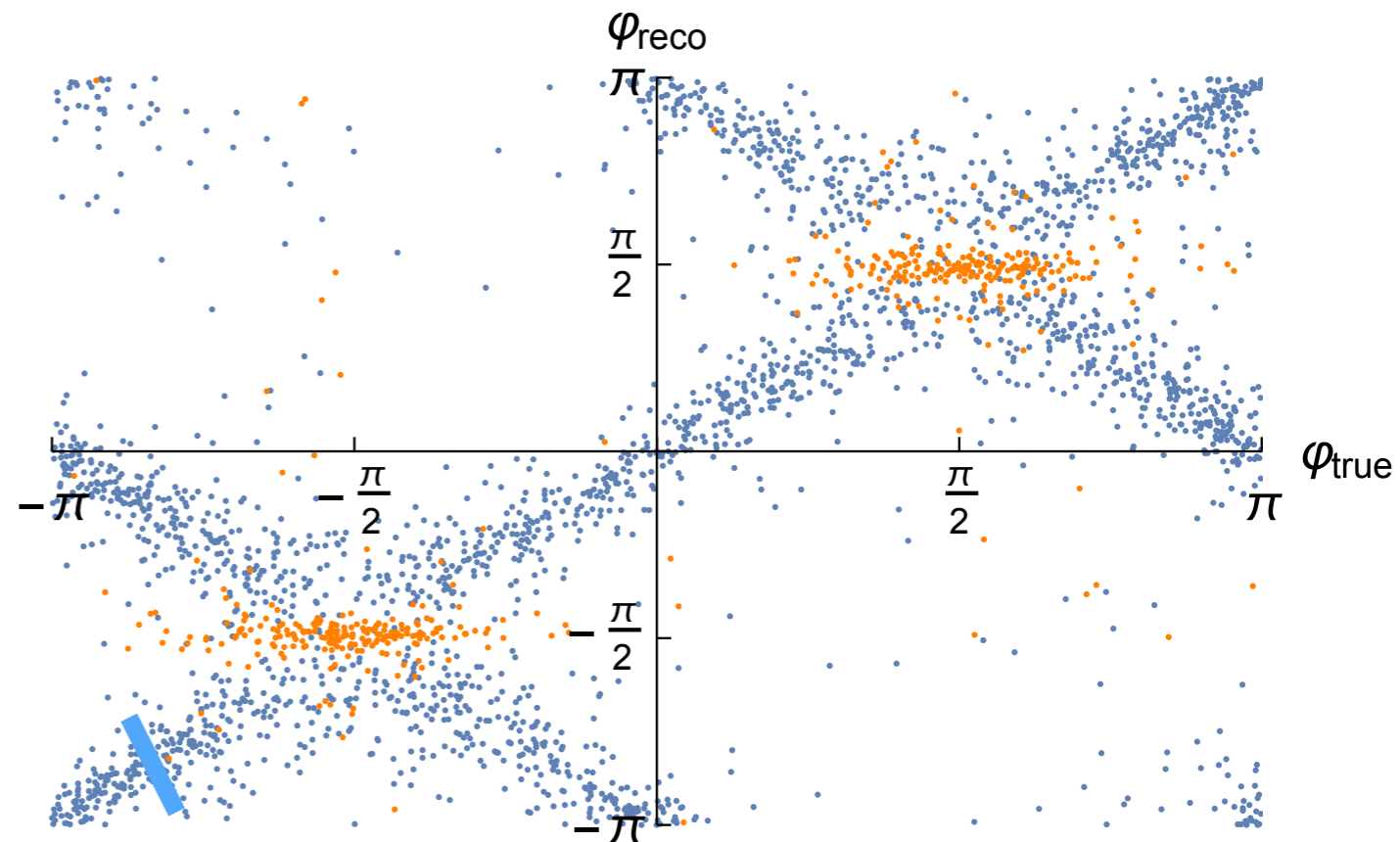
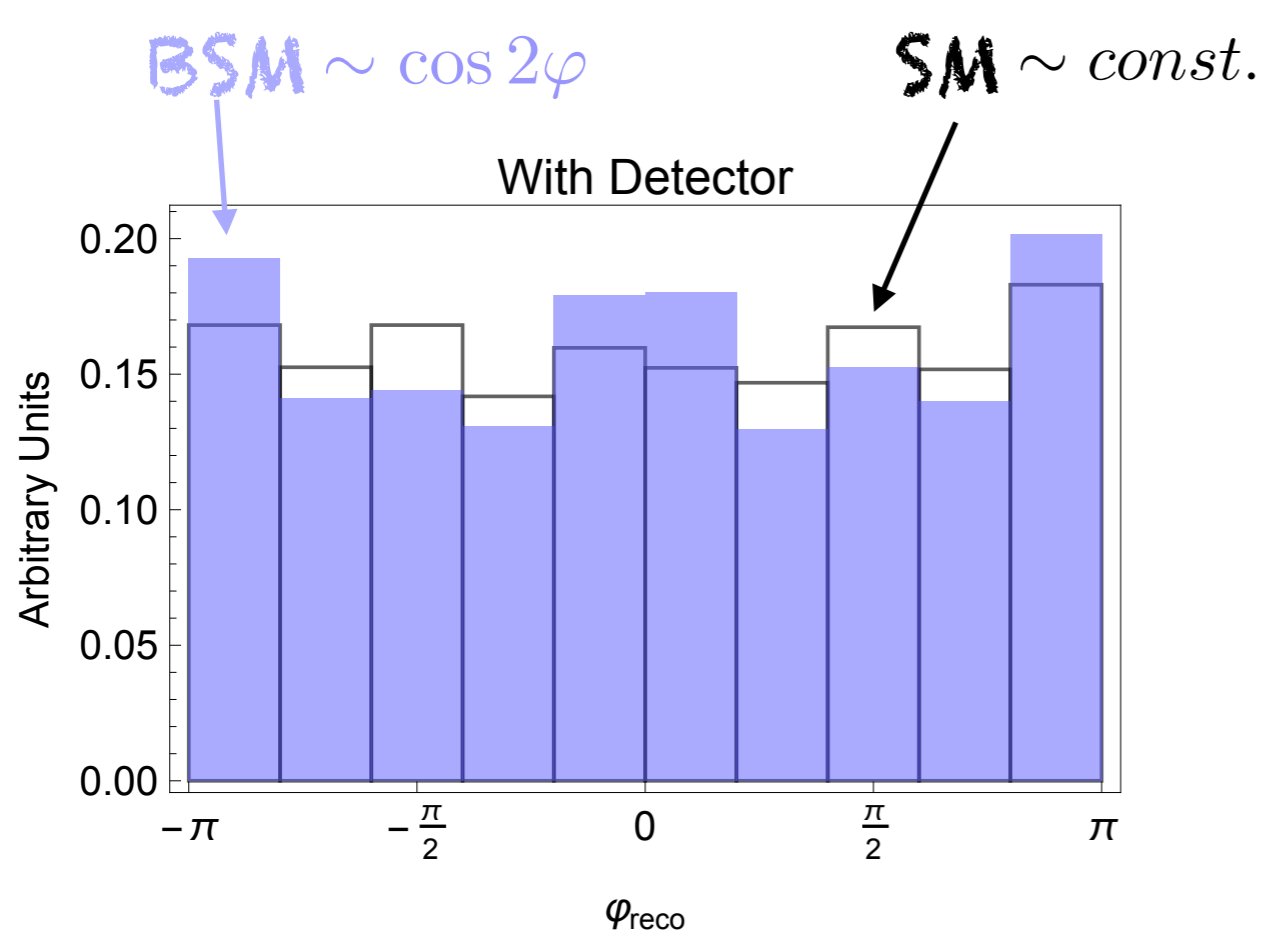
Azimuthal Angle... **more** in reality

Neutrino: from missing energy + reconstruct W mass
With (DELPHES) detector simulation



Azimuthal Angle... **more** in reality

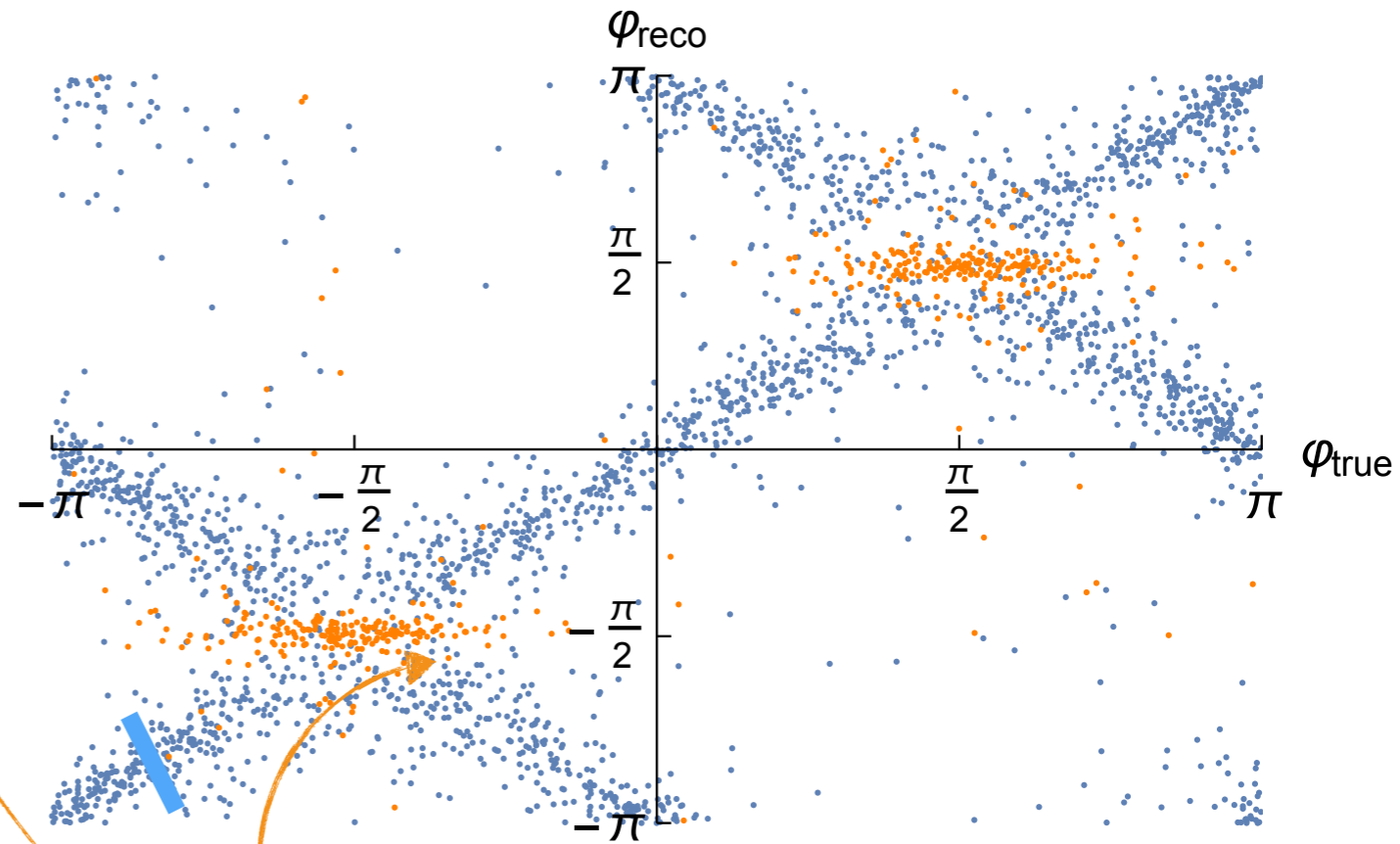
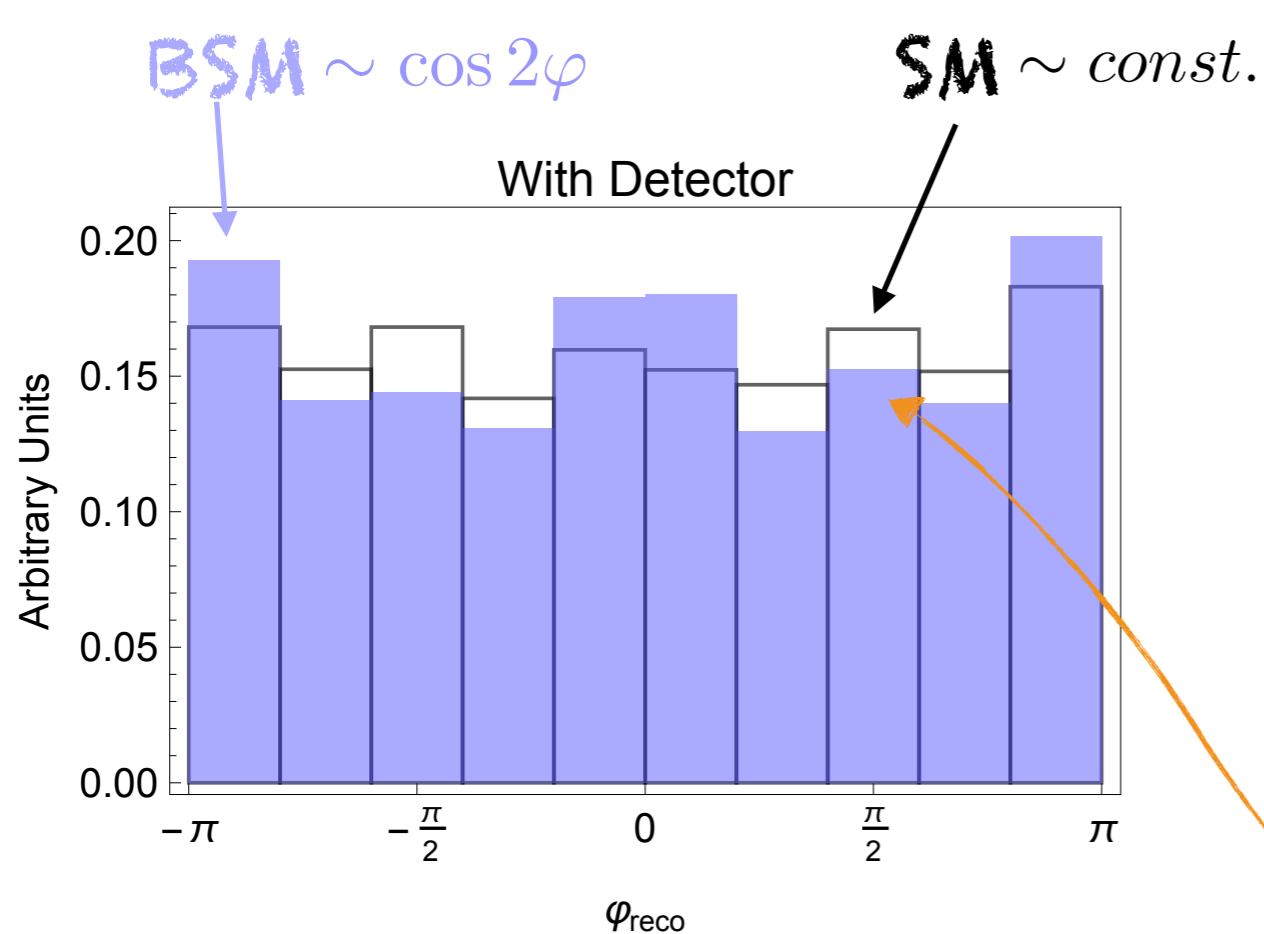
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Spread under control

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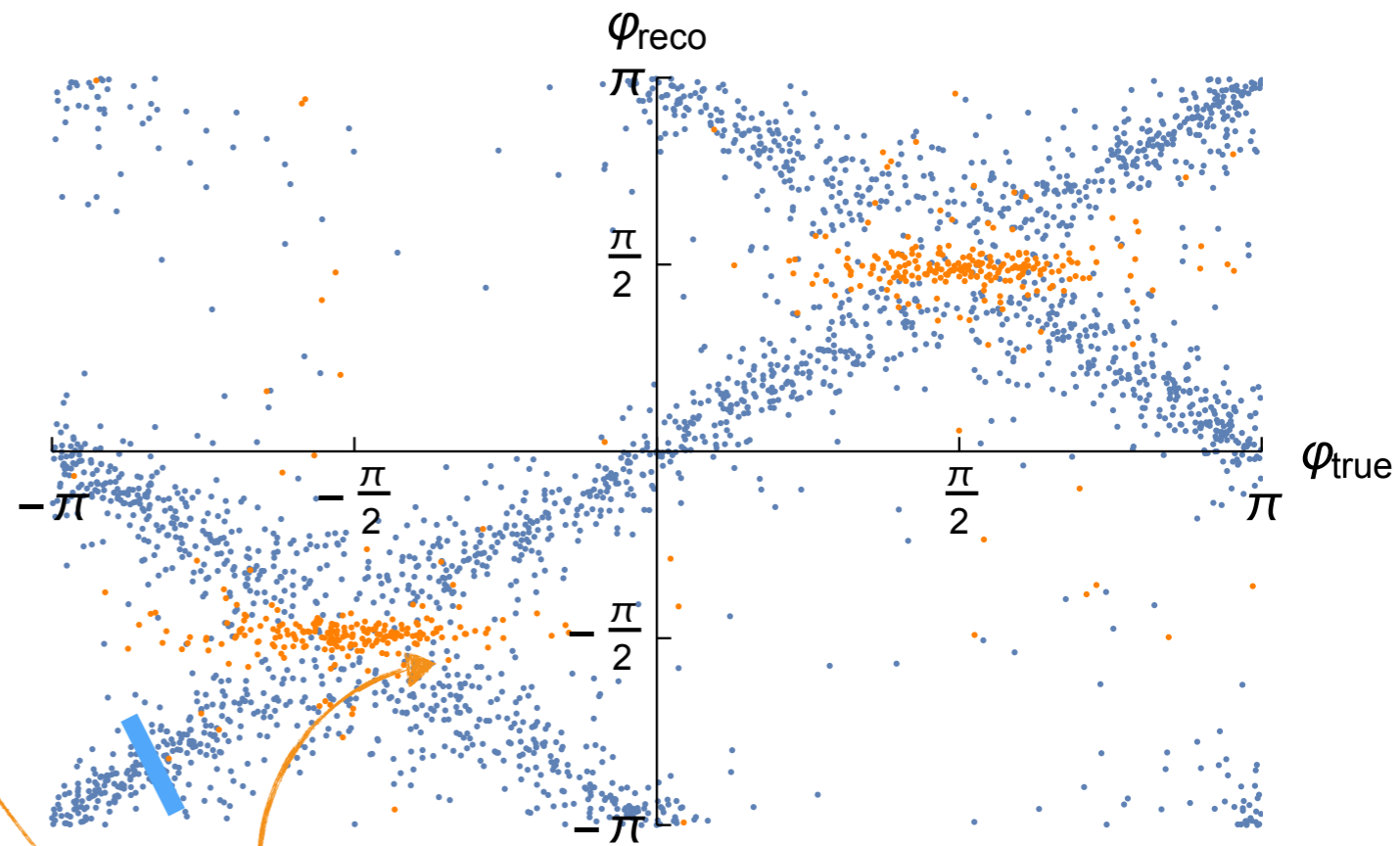
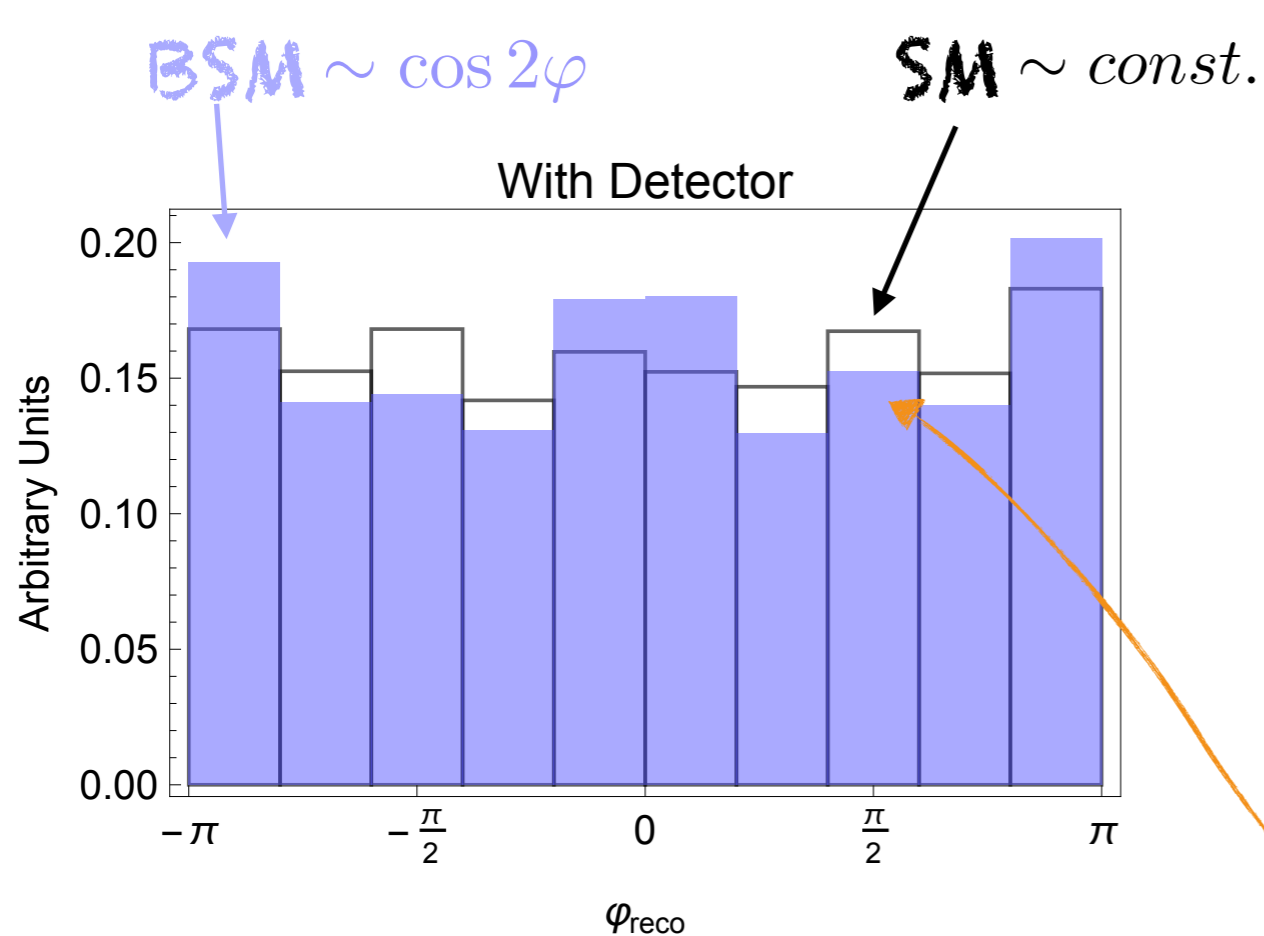


Spread under control

More events with $m_{\perp}^2 > m_W^2$

Azimuthal Angle... **more** in reality

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Spread under control

More events with $m_{\perp}^2 > m_W^2$

► Resurrection is real