

Implications of Vector Boson Scattering Unitarity in Composite Higgs Models

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arXiv:1705.02787, DBF, Piero Ferrarese

arXiv:1809.09146, DBF, Giacomo Cacciapaglia, Aldo Deandrea

- Despite its incredible success, the **SM is plagued** by several problems.
- **Composite Higgs** (CH) models are among the most promising alternatives,
- dynamically generating the EW scale through a vacuum condensate misaligned with the vacuum that breaks EW symmetry

$$v = f \sin \theta$$

- and at the same time explaining the mass gap between the Higgs and the other composite states \rightarrow Higgs = Goldstone boson of spontaneous symmetry G/H.

- A striking evidence of strong dynamics is the growing (with E^2) behavior of **Goldstone Boson Scattering (GBS)** amplitudes

$$\mathcal{A}(\pi\pi \rightarrow \pi\pi) \sim \frac{s}{f^2} = \frac{s}{v^2} \sin^2 \theta,$$

- controlled by strong effects at high energies, **broad continuum** or **composite resonances**, saturating unitarity - similar to hadron physics.
- **Perturbative unitarity** is a powerful tool to assess the **scale of strong effects** and properties of the composite spectrum.

- The **(pseudo-)Goldstone bosons** can be described by the CCWZ construction, at $d = 2$,

$$\mathcal{L}_2 = \frac{1}{2} f^2 \langle x_\mu x^\mu \rangle$$

- Higgs coupling deviations conflict with EWPO and direct measurements, leading to fine-tuned parameters
- The emergence of heavy excitations can help alleviating these tensions leading to natural theories of CH.

$$\sin \theta \lesssim 0.2 \rightarrow \sin \theta \lesssim 0.6 \quad (\text{EWPO})$$

- To analyze perturbative unitarity it is imperative to include higher order terms \rightarrow together with high dimensional operators. At $d = 4$,

$$\begin{aligned} \mathcal{L}_4 &= L_0 \langle x^\mu x^\nu x_\mu x_\nu \rangle + L_1 \langle x^\mu x_\mu \rangle \langle x^\nu x_\nu \rangle \\ &+ L_2 \langle x^\mu x^\nu \rangle \langle x_\mu x_\nu \rangle + L_3 \langle x^\mu x_\mu x^\nu x_\nu \rangle \end{aligned}$$

Unitarity of GBS amplitudes

- Consider $\pi^a \pi^b \rightarrow \pi^c \pi^d$ scattering amplitude in $SU(4)/Sp(4)$. Expand in $Sp(4)$ channels $\mathbf{5} \otimes \mathbf{5} = \mathbf{1} \oplus \mathbf{10} \oplus \mathbf{14} \equiv \mathbf{A} \oplus \mathbf{B} \oplus \mathbf{C}$ and partial waves, J
- Example scalar \mathbf{A} $J = 0$ channel
- In this basis, elastic unitarity condition read

$$\text{Im} a_J(s) = |a_J(s)|^2$$

$$a_{A0}(s) = a_{A0}^{(0)}(s) + a_{A0}^{(1)}(s) + \dots$$

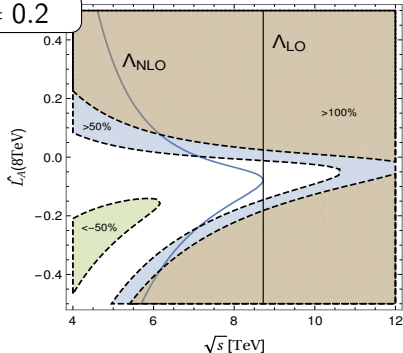
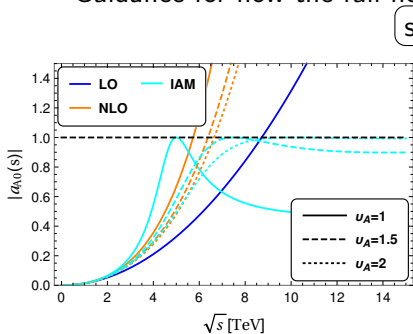
$$\text{Im} a_J^{(1)}(s) = |a_J^{(0)}(s)|^2$$

$$a_{A0}^{(0)}(s) = \frac{s}{16\pi f^2}$$

$$a_{A0}^{(1)}(s) = \frac{s^2}{32\pi f^4} \left[\frac{1}{16\pi^2} \left(\frac{29}{12} + \frac{46}{18} \log \left(\frac{s}{\mu^2} \right) + 2\pi i \right) + \frac{2}{3} \widehat{L}_A(\mu) \right]$$

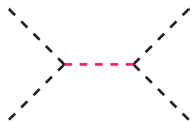


- **Unitarity/Perturbativity test** $|a(s)| < 1$.
- LO prediction is conservative. NLO corrections anticipate unitarity violation.
- Unitarity implies an eventual resonance is lighter than $M_\sigma \lesssim 1.75/\sin\theta$ TeV.
- Lattice results $M_\sigma = 4.7(2.6)/\sin\theta$ TeV (2 Dirac fermions in fundamental of SU(2), Arthur, Drach, Hansen, Hietanen, Pica, Sannino 16')
- **Inverse Amplitude Method (IAM)** is an Unitarization Model. Guidance for how the full non-perturbative amplitude could look like.



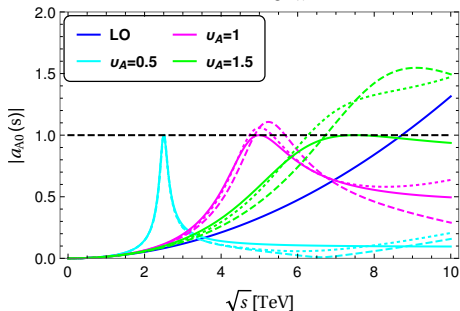
The σ resonance

$$\mathcal{L}_\sigma = \frac{1}{2}\kappa(\sigma)f^2\langle x_\mu x^\mu \rangle + \frac{1}{2}\partial_\mu\sigma\partial^\mu\sigma - \frac{1}{2}M_\sigma^2\sigma^2$$



$$a_{A0}^\sigma(s) = \frac{g_\sigma^2}{32\pi f^2} \left(\frac{5s^2}{m_\sigma^2 - i\Gamma_\sigma m_\sigma - s} - 2m_\sigma^2 + \frac{2m_\sigma^4 \log\left(\frac{s}{m_\sigma^2} + 1\right)}{s} + s \right)$$

$$v_A \equiv \frac{m_\sigma \sin\theta}{\text{TeV}}, \quad \Gamma_\sigma \sim 5 \frac{g_\sigma^2 m_\sigma^3}{32\pi f^2}, \quad \kappa(\sigma) = 1 + \kappa'\sigma/f + \kappa''\sigma^2/(2f) + \dots$$



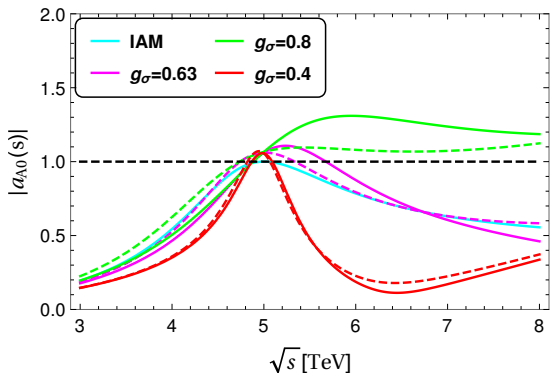
$$g_\sigma \equiv \kappa'/2 \sim \sqrt{2/5} \sim 0.63$$

Dashed: Fixed width

Dotted: Running width

Solid: IAM

$\sin\theta = 0.2$



$v = 1$

Solid: Fixed width

Dashed: Running width

$\sin \theta = 0.2$

Unitarity and perturbativity give further information about effective Lagrangian beyond pure dimensional analysis:

$$g_\sigma \lesssim 0.8 \text{ and } M_\sigma \lesssim \frac{1.2}{\sin \theta} \text{ TeV}$$

Composite vector resonances

Hidden Local Gauge prescription:

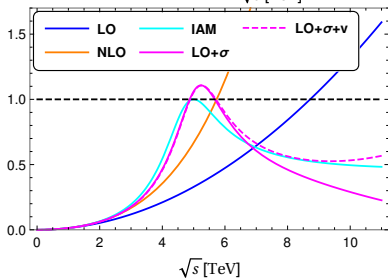
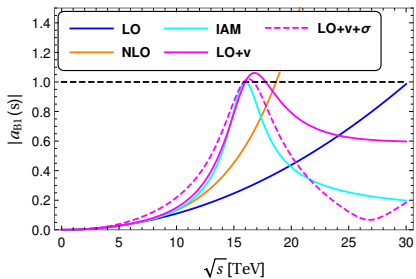
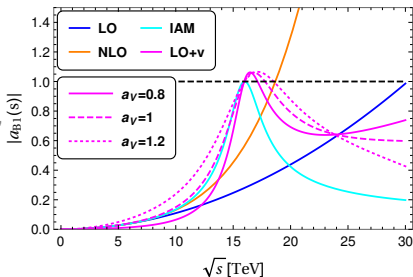
$$\begin{aligned}\mathcal{L}_V &= -\frac{1}{2\tilde{g}^2} \langle \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu} \rangle + \frac{1}{2} f_0^2 \langle x_{0\mu} x_0^\mu \rangle + \frac{1}{2} f_1^2 \langle x_{1\mu} x_1^\mu \rangle \\ &+ r f_1^2 \langle x_{0\mu} K x_1^\mu K^\dagger \rangle + \frac{1}{2} f_K^2 \langle D^\mu K D_\mu K^\dagger \rangle\end{aligned}$$

$$\pi_a(p_1) \pi_b(p_2) \mathcal{V}_\mu^c : i g_V (p_1 - p_2) \Xi^{abc}, \quad g_V = -\frac{M_V}{2f} a_V = -\frac{M_V^2 (1 - r^2)}{\sqrt{2} \tilde{g} f^2},$$

$$a_{B1}^V(s) = \frac{g_V^2}{32\pi} \left[\frac{s}{3(s - M_V^2)} - \frac{s}{2M_V^2} - \left(\frac{M_V^2}{s} + 2 \right) \left(2 - \left(2 \frac{M_V^2}{s} + 1 \right) \log \left(1 + \frac{s}{M_V^2} \right) \right) \right].$$

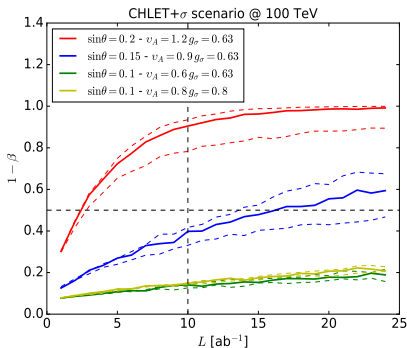
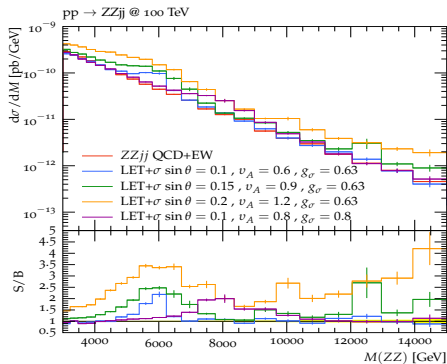


- $M_V = 13f = 3.2 \text{ TeV} / \sin \theta$ from lattice
(R. Arthur, V. Drach, M. Hansen, A. Hietanen, C. Pica, F. Sannino)
- $|a_V| \approx 1$, also from width bounds DBF, Cacciapaglia, Cai, Deandrea, Frandsen 16'



Strong VBS in $pp \rightarrow jjZZ \rightarrow jj4\ell$

- High compositeness scale $f \gtrsim 1.2$ TeV: **Scalar σ resonance at 100 TeV**
- Typical VBS kinematical cuts applied.
- Mixing $h - \sigma$ very small $\alpha \sim \frac{2m_h^2}{m_\sigma^2}$, suppressed gluon fusion.



Sigma assisted Composite Higgs model, low compositeness scale $f \gtrsim 500 \text{ GeV}$

DBF, Cacciapaglia, Deandrea 18'

- One of the most promising candidates to provide mass to the top quark in the CH paradigm is the partial compositeness mechanism, $m_t \propto f s_{2\theta}$.
- This is also a natural candidate of CH because if the potential is dominated by top loops $V \sim m_t^2$, its natural minimum is $s_\theta = 1/\sqrt{2}$, thus EW broken w/ the presence of a CH doublet.
- Common lore: EWPO and Higgs couplings measurements $s_\theta \lesssim 0.2$ (fine-tuning)

$$\kappa_V = \frac{\partial_\theta V}{V} = c_\theta, \quad \kappa_t = \frac{v}{f m_t} \partial_\theta m_t = \frac{c_{2\theta}}{c_\theta}.$$

- We will show how a light σ (and vectors), with dynamically inspired profile, alleviate these constraints.

Minimal model set-up

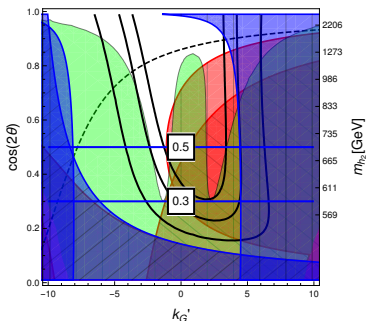
- Minimal model: $SU(4)/Sp(4)$ coset and fermionic operators in two-index representations of $SU(4)$ (symmetric \mathbf{S} or anti-symmetric \mathbf{A}).
- Underlying: $G_{TC} = Sp(2N_c)$, 4 Weyl fermions ψ fundamental representation (Ryttov, Sannino 08, Galloway et al. 10), $+\chi$ carrying QCD colour and hypercharge are needed to generate top partners ($\psi\chi\chi$) (Barnard 13, Ferretti 13)
- Effective Lagrangian (adding potential)

$$\begin{aligned}\mathcal{L} \supset & k_t(\sigma) \frac{y_{LYR} f C_y}{4\pi} (Q_\alpha t^c)^\dagger \text{Tr} [(P_Q^\alpha \Sigma^\dagger P_t \Sigma^\dagger)] \\ & - k_t^2(\sigma) V_t - k_G^2(\sigma) V_g - k_m(\sigma) V_m\end{aligned}$$

- $\sigma - h$ mix and change predictions.

Constraints

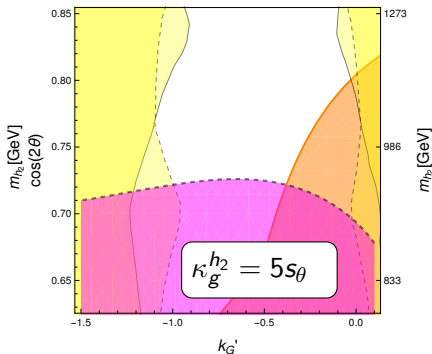
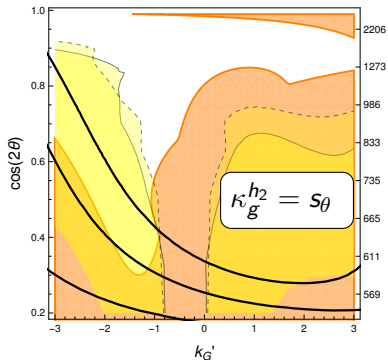
- **Perturbativity**, $|k'_i| < 4\pi$, pert. unitarity $\gamma = \frac{m_{h_2}}{4\sqrt{\pi}f} \lesssim 1$ ($\gamma = 0.2$ in the plot), $\Gamma/m_{h_2} \lesssim 1$ (black curves, 0.3, 0.5, 1)
- **EWPO**, σ creates the valleys and vectors shift and broaden them.



- **Higgs measurements**, $\kappa_{t,V}$. $\Gamma(h \rightarrow \eta\eta)$ (dashed line) for $m_\eta = 0$ - larger masses (m_ψ or **A** rep.) opens parameters space and interesting experimental signatures.
- Dynamically inspired composite resonance profile works nicely. σ : $|k'_G| \sim 1.2$. v_μ : $r = 1.1 \rightarrow |a_V| = 1$, with $M_V = 4\pi f$, $\tilde{g} = 3$.

Direct searches

- $pp \rightarrow h_2 \rightarrow ZZ$ (CMS 18') and $pp \rightarrow h_2 \rightarrow t\bar{t}$ (from DBF, Fabbri, Schumman 17')
- $\sigma = \sigma_0^{gg} \frac{|\kappa_t^{h_2} A_F(\tau_t) + \kappa_g^{h_2}|^2}{|A_F(\tau_t)|^2} + \sigma_0^{VBF} (\kappa_V^{h_2})^2$ gg: Anastasiou et al. 16', VBF: Bolzoni, Maltoni, Moch, Zaro 11'
- VBF contribution small ($f_{VBS} \lesssim 0.003$ for $\cos 2\theta = 0.6$)



Conclusion

- Perturbative unitarity gives valuable information about spectrum and couplings of composite sector in CH models. Beyond simple dimensional analysis.
- Scalar sector: σ resonance, $k'_G \lesssim 1.2$ and $M_\sigma \lesssim 1.2/\sin\theta$ TeV or *continuum* dominates.
- For high compositeness scale main process is VBS - 100 TeV collider more appropriate to observe strong effects.
- Low scale feasible aided by composite states - high contribution in σ production from gluon fusion in top PC. Details of potential important and LHC can probe the scenario.
- Other interesting signatures are also present, e.g. $h \rightarrow \eta\eta \rightarrow Z\gamma Z\gamma$, vector production.

- Vacuum $\Sigma_0 = \cos \theta \Sigma_B + \sin \theta \Sigma_H$.
- Minimization $\cos \theta_{min} = \frac{2C_m}{y'_t C_t}$, for $y'_t C_t > 2|C_m|$.
- Generators

$$\begin{aligned} V^a \cdot \Sigma_0 + \Sigma_0 \cdot V^{aT} &= 0, & S^a \cdot \Sigma_B + \Sigma_B \cdot S^{aT} &= 0, \\ Y^a \cdot \Sigma_0 - \Sigma_0 \cdot Y^{aT} &= 0. & X^a \cdot \Sigma_B - \Sigma_B \cdot X^{aT} &= 0, \end{aligned}$$

$$U = \exp \left[\frac{i\sqrt{2}}{f} \sum_{a=1}^5 \pi^a Y^a \right],$$

$$\begin{aligned} \omega_\mu &= U^\dagger D_\mu U, \\ D_\mu &= \partial_\mu - ig W_\mu^i S^i - ig' B_\mu S^6, \\ x_\mu &= 2\text{Tr}[Y_a \omega_\mu] Y^a, \\ s_\mu &= 2\text{Tr}[V_a \omega_\mu] V^a. \end{aligned}$$

Hidden Local Symmetry (HLS)

- Enhance the symmetry group $SU(4)_0 \times SU(4)_1$, and embed the SM gauge bosons in $SU(4)_0$ and the heavy resonances in $SU(4)_1$. $SU(4)_i \rightarrow Sp(4)_i$.
 $Sp(4)_0 \times Sp(4)_1 \rightarrow Sp(4)$ by a sigma field K

$$U_0 = \exp \left[\frac{i\sqrt{2}}{f_0} \sum_{a=1}^5 (\pi_0^a Y^a) \right], \quad U_1 = \exp \left[\frac{i\sqrt{2}}{f_1} \sum_{a=1}^5 (\pi_1^a Y^a) \right]. \quad (1)$$

$$\begin{aligned} D_\mu U_0 &= (\partial_\mu - igW_\mu^i S^i - ig' B_\mu S^6) U_0, \\ D_\mu U_1 &= (\partial_\mu - i\tilde{g}\mathcal{V}_\mu^a V^a - i\tilde{g}\mathcal{A}_\mu^b Y^b) U_1. \end{aligned} \quad (2)$$

$$\begin{aligned} K &= \exp [ik^a V^a / f_K], \\ D_\mu K &= \partial_\mu K - iv_{0\mu} K + iKv_{1\mu} \end{aligned} \quad (3)$$

$$\mathcal{F}_\mu = \mathcal{V}_\mu + \mathcal{A}_\mu = \sum_{a=1}^{d_H} \mathcal{V}_\mu^a V_a + \sum_{a=1}^{d_G - d_H} \mathcal{A}_\mu^a Y_a,$$

$$\begin{aligned} \mathcal{L}_v &= -\frac{1}{2\tilde{g}^2} \langle \mathcal{F}_{\mu\nu} \mathcal{F}^{\mu\nu} \rangle + \frac{1}{2} f_0^2 \langle x_{0\mu} x_0^\mu \rangle + \frac{1}{2} f_1^2 \langle x_{1\mu} x_1^\mu \rangle \\ &+ r f_1^2 \langle x_{0\mu} K x_1^\mu K^\dagger \rangle + \frac{1}{2} f_K^2 \langle D^\mu K D_\mu K^\dagger \rangle. \end{aligned}$$

- $\pi\pi \rightarrow \pi\pi$ scattering amplitudes expanded in partial wave amplitudes

$$\mathcal{A}(s, t) = 32\pi \sum_{J=0}^{\infty} a_J(s)(2J+1)P_J(\cos\theta)$$

- In order to force elasticity (at least below new heavy states appear), decompose amplitude in conserved quantum number
- **Template: SU(4)/Sp(4), FMCHM**, decompose in multiplets of Sp(4) (very good symmetry at high energy)

$$\mathbf{5} \otimes \mathbf{5} = \mathbf{1} \oplus \mathbf{10} \oplus \mathbf{14} \equiv \mathbf{A} \oplus \mathbf{B} \oplus \mathbf{C}$$

Inverse Amplitude Method

- Phenomenological approach to describe the physics beyond unitarity violation, successful in describing lightest mesonic resonances in pion-pion and pion-kaon scattering up to 1.2 GeV

$$a_{IJ}^{IAM}(s) = \frac{a_{IJ}^{(0)}(s)}{1 - \frac{a_{IJ}^{(1)}(s)}{a_{IJ}^{(0)}(s)}}$$

- Use with caution, not a QFT!
- Generate poles interpreted as dynamically generated resonances in each channel, e.g.

$$M_A^2 = \frac{2f^2}{\frac{1}{16\pi^2} \left(\frac{29}{12}\right) + \frac{2}{3} \widehat{L}_A(M_A)}, \quad \Gamma_A = \frac{M_A^3}{16\pi f^2}$$

- Normalized mass: $v_I \equiv \frac{M_I \sin \theta}{\text{TeV}}$, $I = A, B, C$.

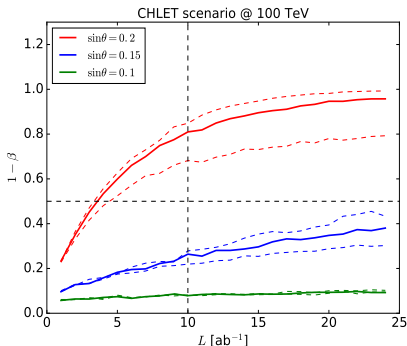
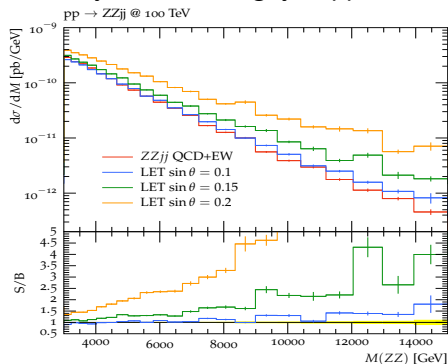
Cuts:

cut	100 TeV	14 TeV
2 jets	$p_T > 30 \text{ GeV}, \eta > 3.5, \eta_1 \cdot \eta_2 < 0$	$p_{T,j} > 30 \text{ GeV}, \eta_j > 3., \eta_{j1} \cdot \eta_{j2} < 0$
ZZ invariant mass	$m_{ZZ} > 3\text{TeV}$	$m_{ZZ} > 3\text{TeV}$
di-jet invariant mass	$m_{jj} > 1 \text{ TeV}$	$m_{jj} > 1 \text{ TeV}$
Zs centrality	$ \eta_{Z_i} < 2.$	$ \eta_{Z_i} < 2.$
Zs momentum	$p_{T,Z_i} > 1 \text{ TeV}$	$p_{T,Z_i} > 0.5 \text{ TeV}$

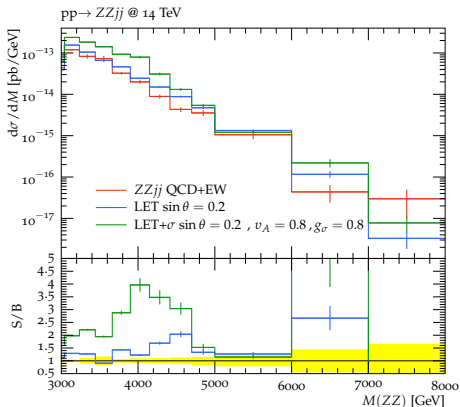
Probability distribution:

$$\mathcal{P}(k; \lambda, \epsilon) = \frac{1}{2\epsilon} \int_{1-\epsilon}^{1+\epsilon} dx e^{-x\lambda} \frac{(x\lambda)^k}{k!}$$

LET no-resonant enhancement at 100 TeV: Conservative scenario, unitarity violation highly suppressed for $\sin \theta < 0.2$

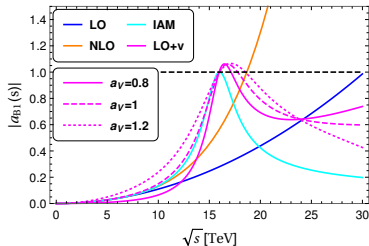


σ resonance at the LHC



- $\sigma \sim 2.9 \times 10^{-4}$ ab very small.
- Other VBS channels imperative for this search.
- Gluon fusion contribution could help.

Vector Analysis



$$g_V = -\frac{M_V}{2f} a_V = -\frac{M_V^2(1-r^2)}{\sqrt{2}\tilde{g}f^2},$$

$$\mathcal{A}(s, t, u) = -g_V^2 \left(\frac{s-u}{t-M_V^2} + \frac{s-t}{u-M_V^2} + \frac{3s}{M_V^2} \right)$$

