

**HPNP 2019 - 4th International workshop on `Higgs as a  
probe of new physics 2019**

**Pursuing exotic  
decay channels of a  
charged Higgs boson**

**Jeonghyeon Song**  
(Konkuk University, Korea)

**work in progress w/ Yeo Woong Yoon**

**Osaka University, 2019. 2. 20.**

# HPNP 2019 - 4th International workshop on `Higgs as a probe of new physics 2019

$$H^{\pm} \rightarrow W^{\pm} \gamma$$

**Jeonghyeon Song**  
(Konkuk University, Korea)

Osaka University, 2019. 2. 20.

# Charged Higgs boson in the 2HDM

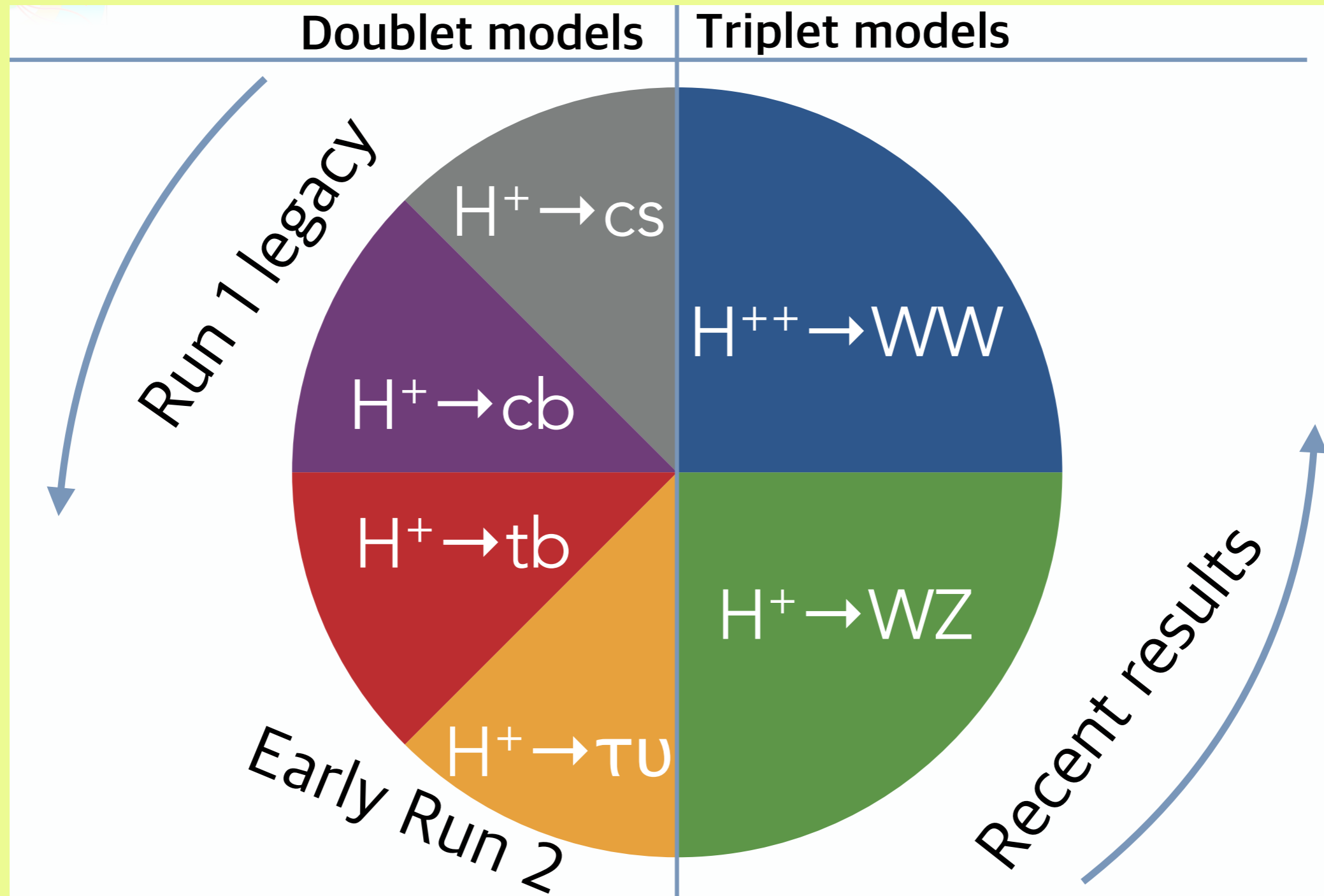
$\Phi_1$  and  $\Phi_2$

$$\Phi_a = \begin{pmatrix} \phi_a^+ \\ \frac{v_a + \rho_a + i\eta_a}{\sqrt{2}} \end{pmatrix}, \quad a = 1, 2.$$

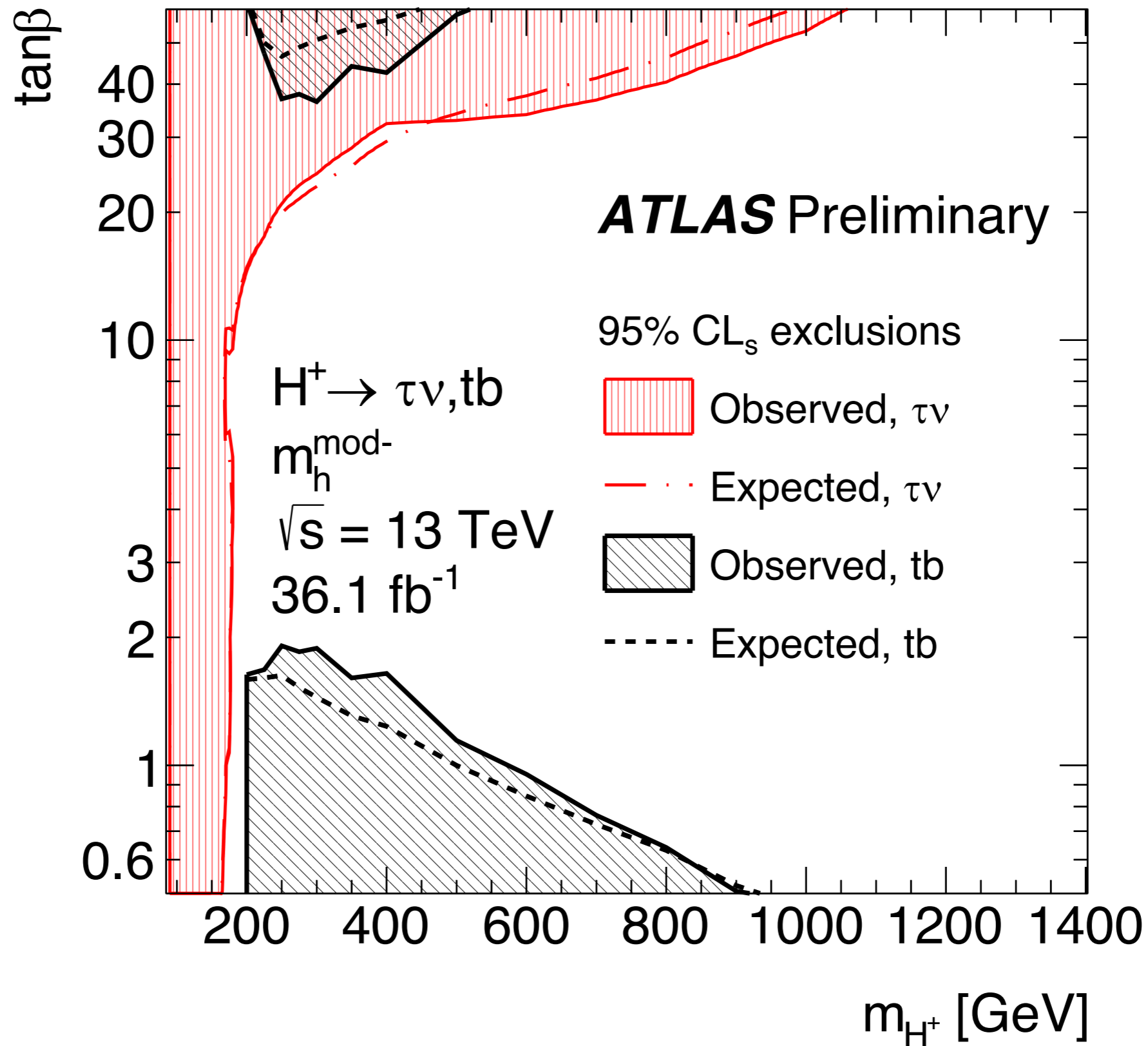
**Five physical Higgs bosons**

$h^0, H^0, A^0, H^\pm$

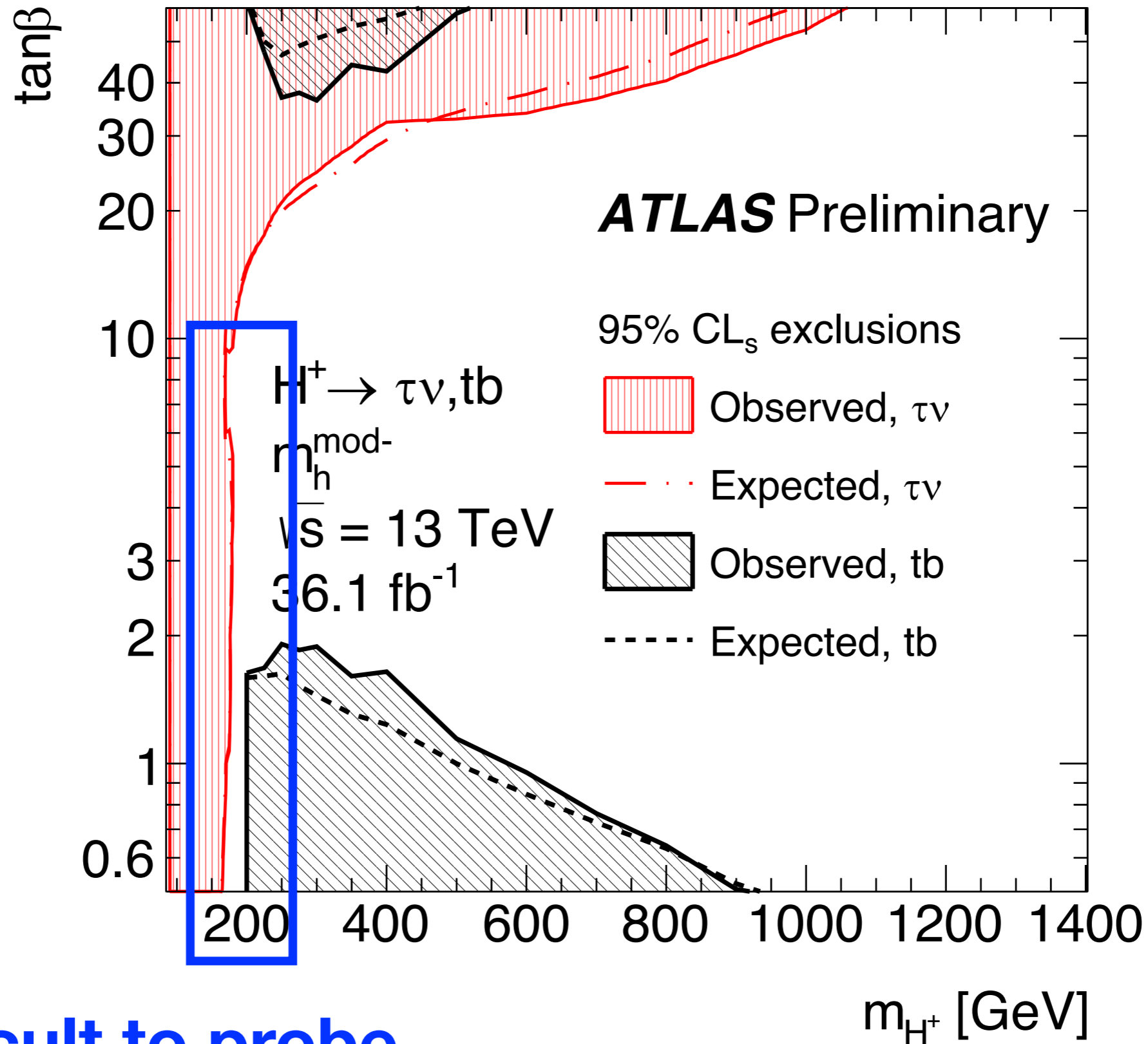
# Search for $H^\pm$ at the LHC



# $H^+ \rightarrow tb$ and $H^+ \rightarrow \tau\nu$ superposition



# $H^+ \rightarrow tb$ and $H^+ \rightarrow \tau\nu$ superposition



**Very difficult to probe**

# Possible?

$$M_{H^\pm} \simeq m_t$$



# Two Higgs doublets

$\Phi_1$  and  $\Phi_2$

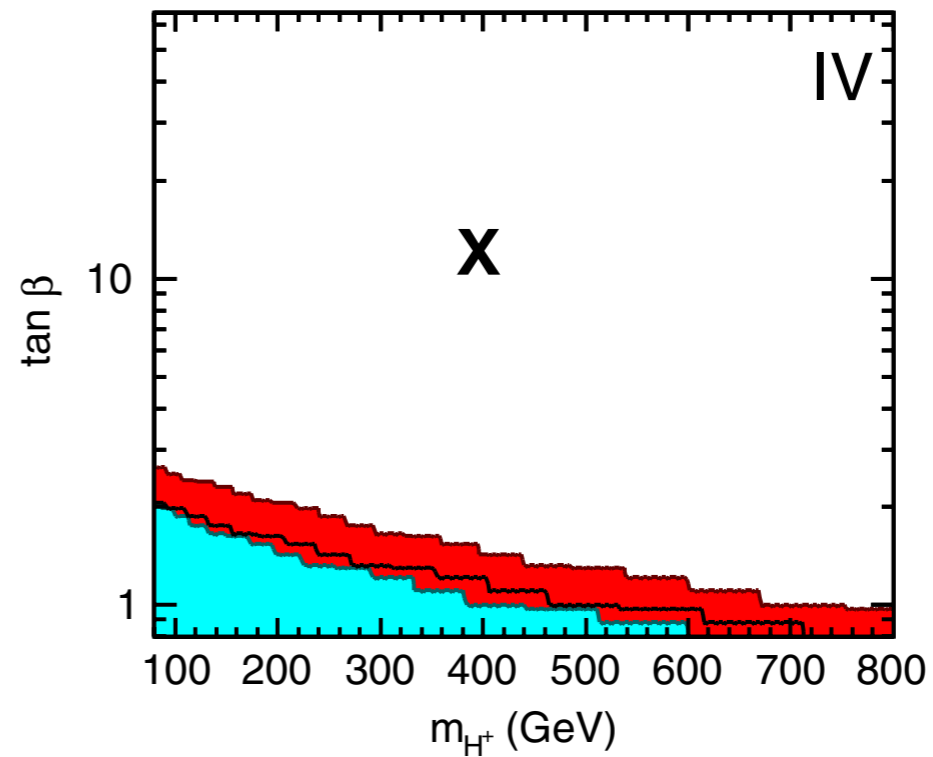
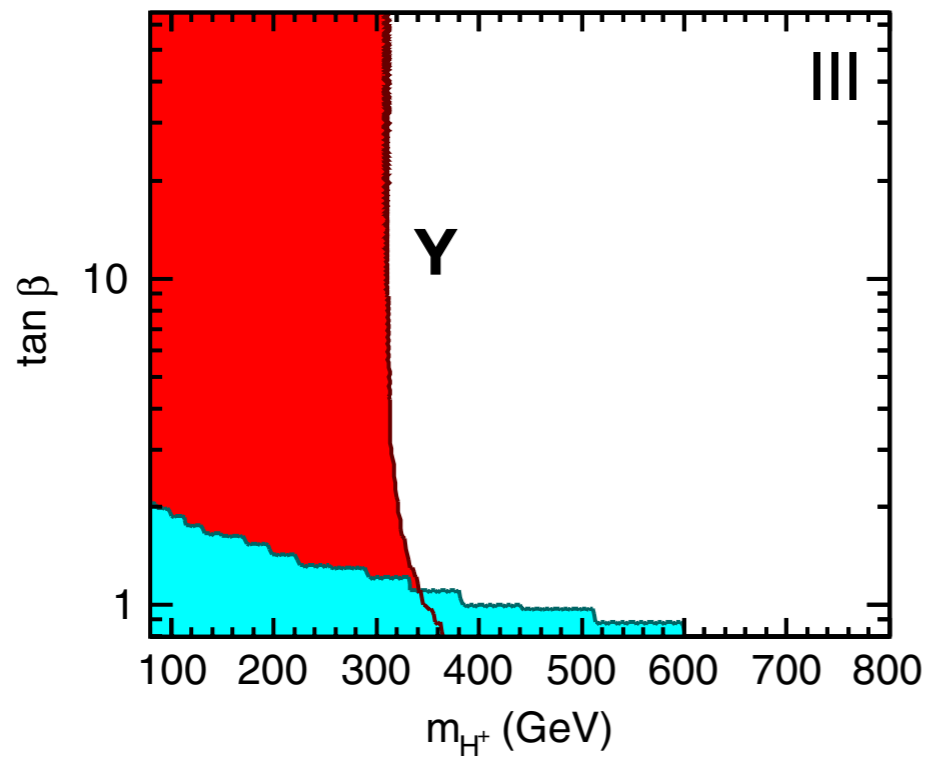
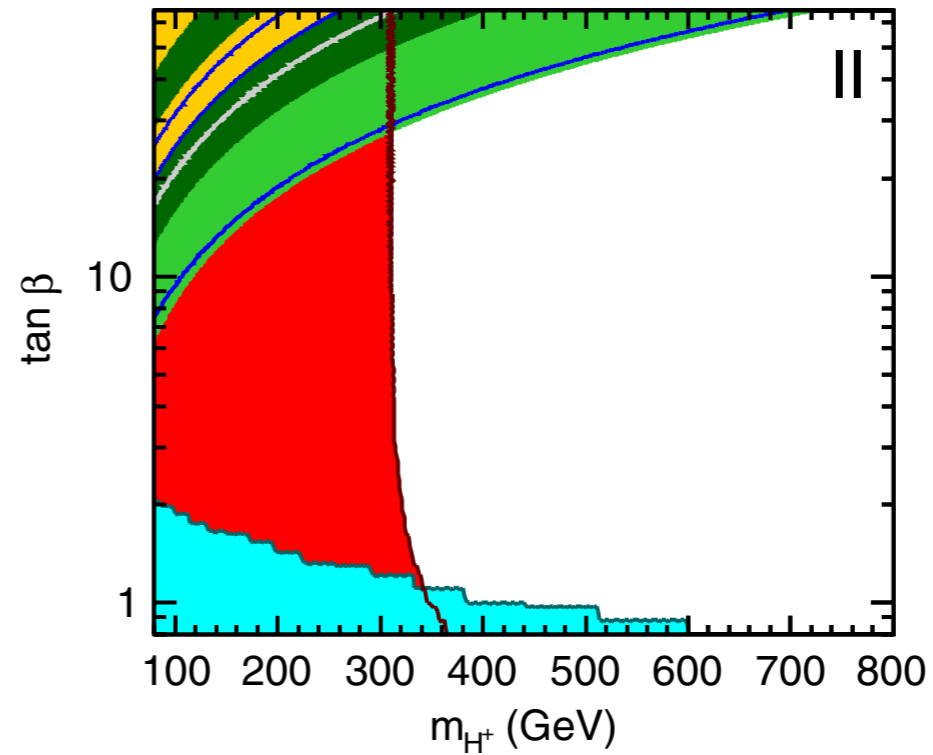
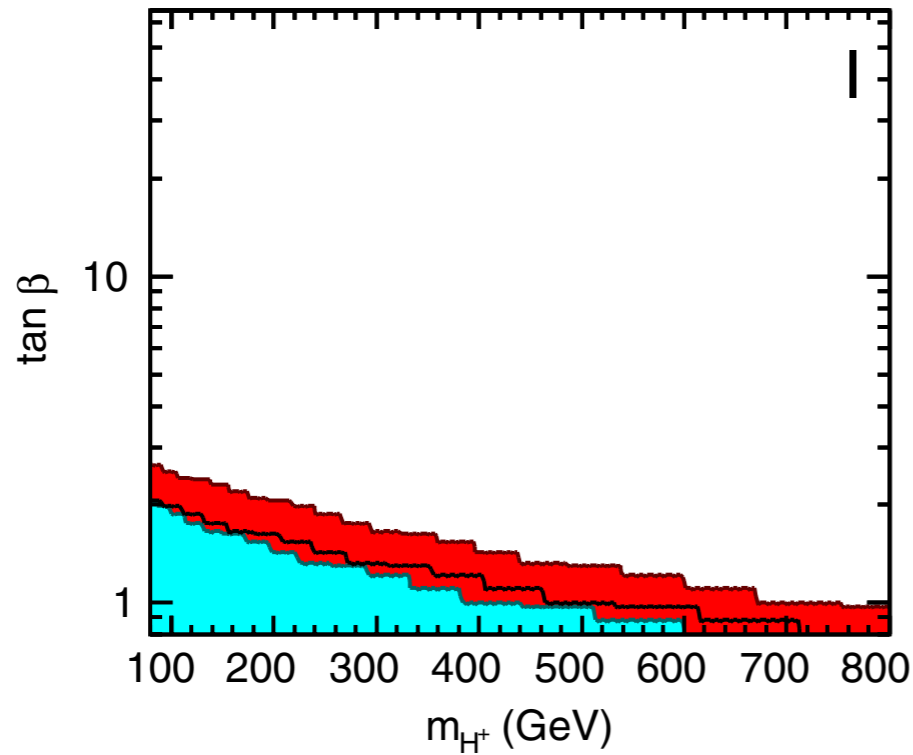
**In order to suppress FCNC at tree level,  
we impose Z2 symmetry**

$$\Phi_1 \rightarrow \Phi_1 \quad \text{and} \quad \Phi_2 \rightarrow -\Phi_2$$

# 4 types according to $Z_2$ parities

	$\Phi_1$	$\Phi_2$	$u_R$	$d_R$	$\ell_R$	$Q_L, L_L$
Type I	+	-	-	-	-	+
Type II	+	-	-	+	+	+
Type X	+	-	-	-	+	+
Type Y	+	-	-	+	-	+

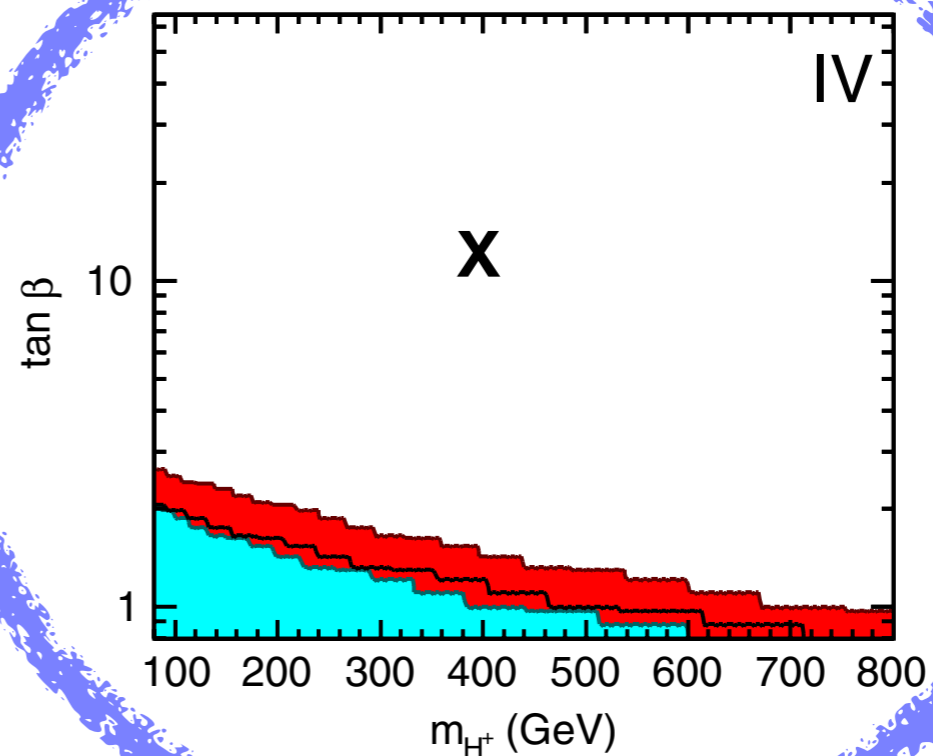
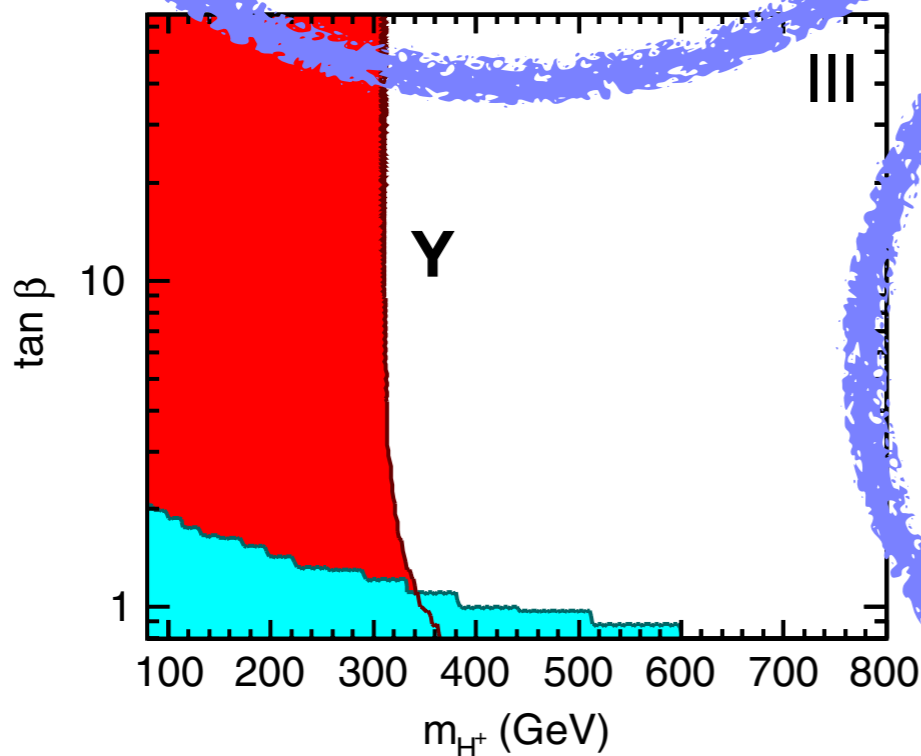
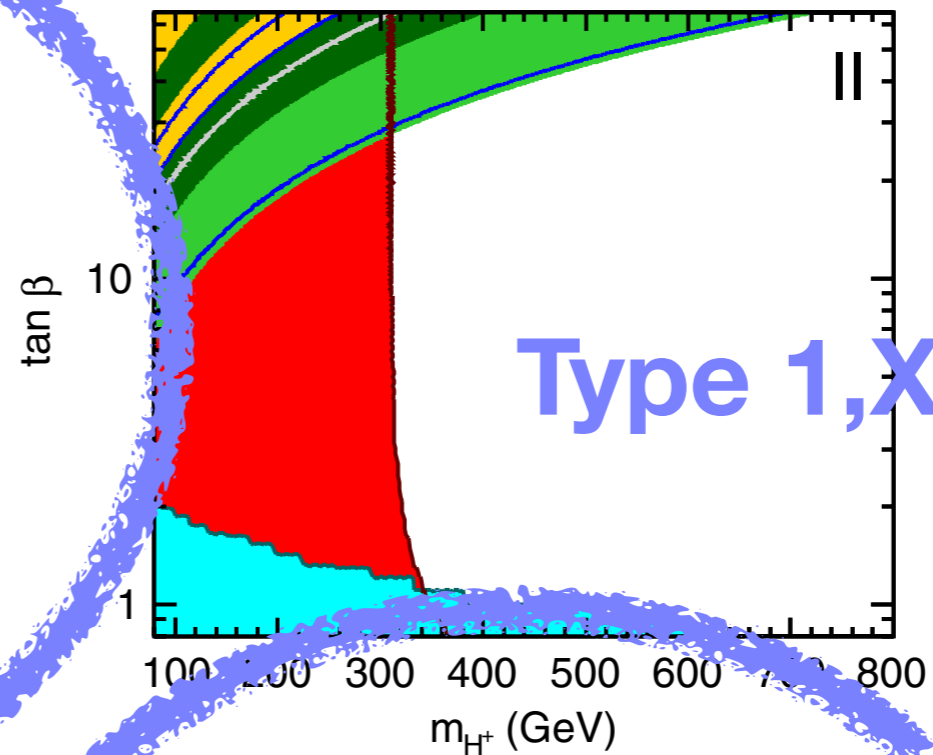
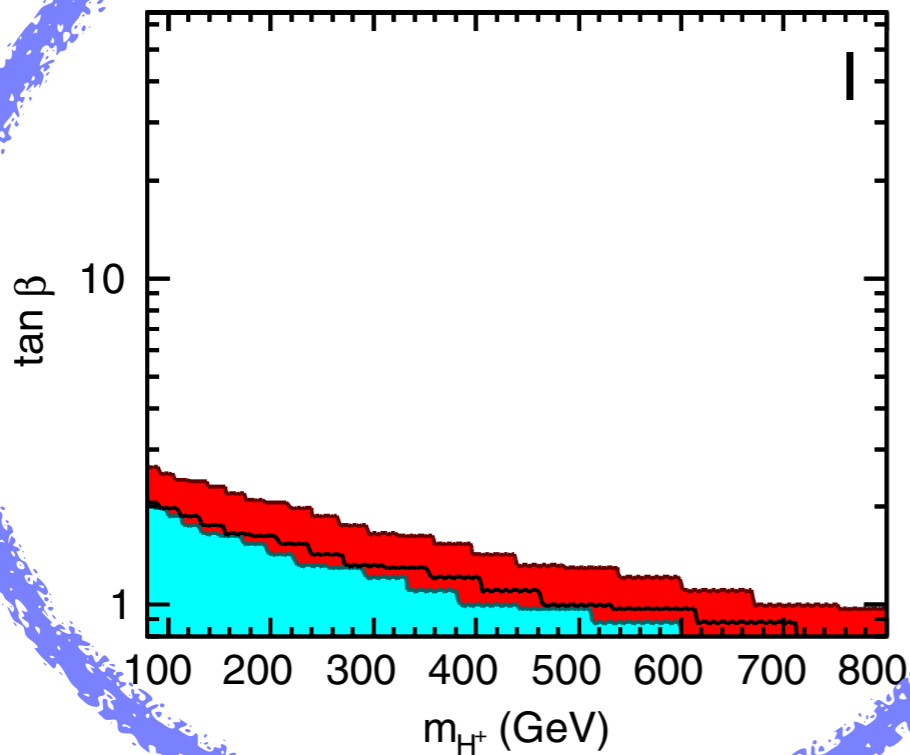
# FCNC constraint



Cyan:  $\Delta M_{bd}$

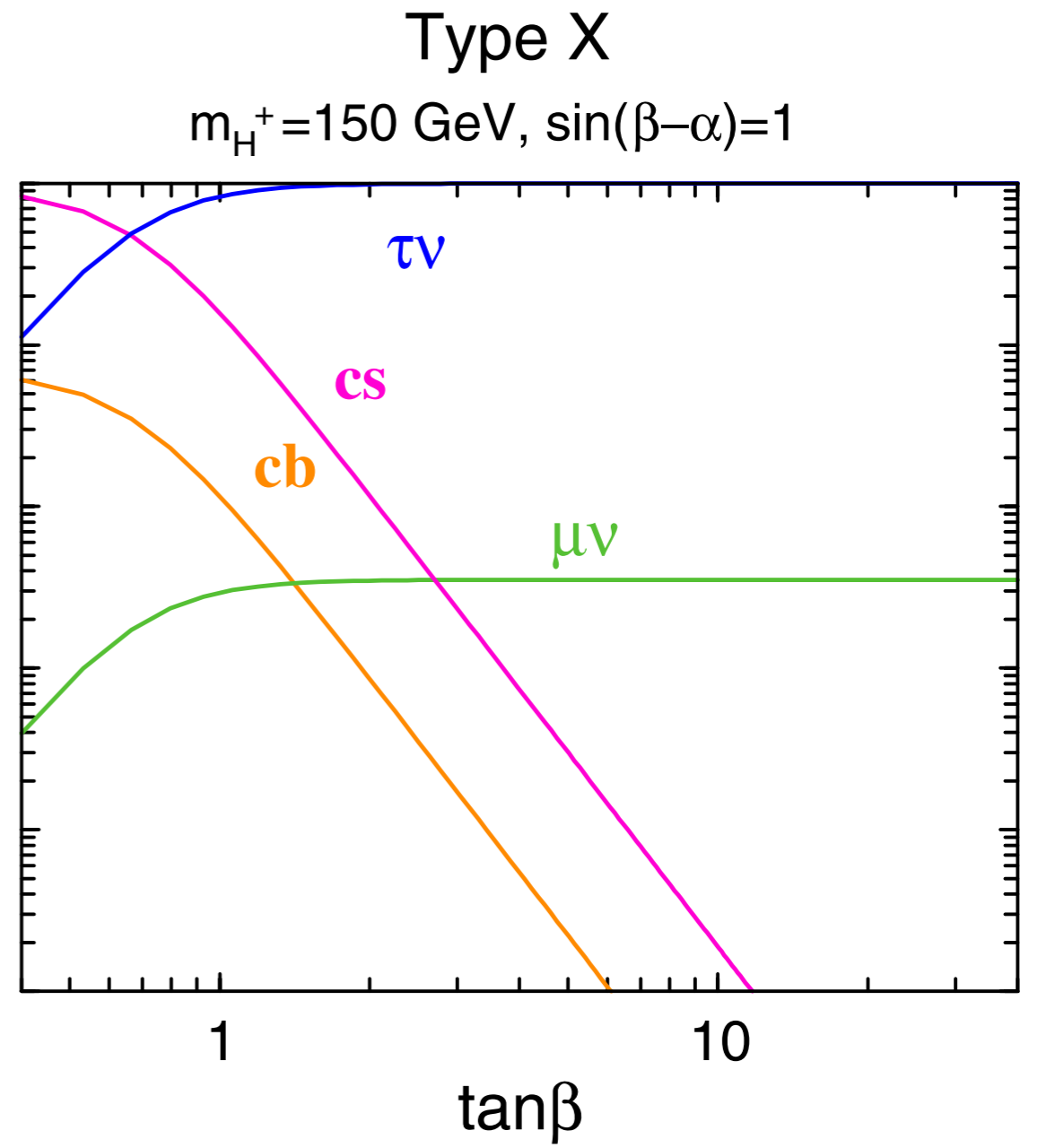
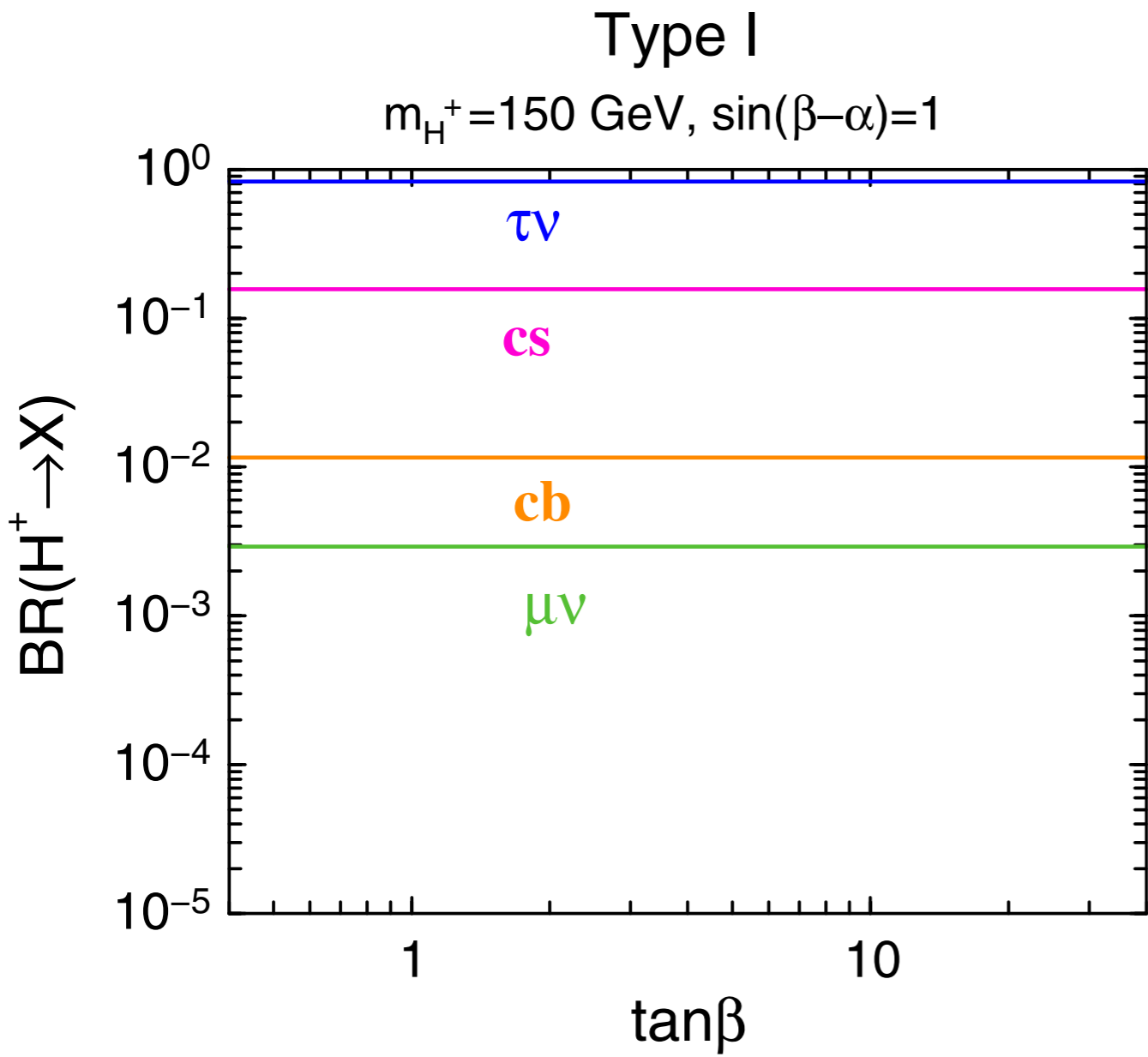
Red:  $b \rightarrow s\gamma$

# FCNC constraint



Cyan:  $\Delta M_{bd}$

Red:  $b \rightarrow s\gamma$



**Aoki et.al. PRD 80 (2009)**

# Question

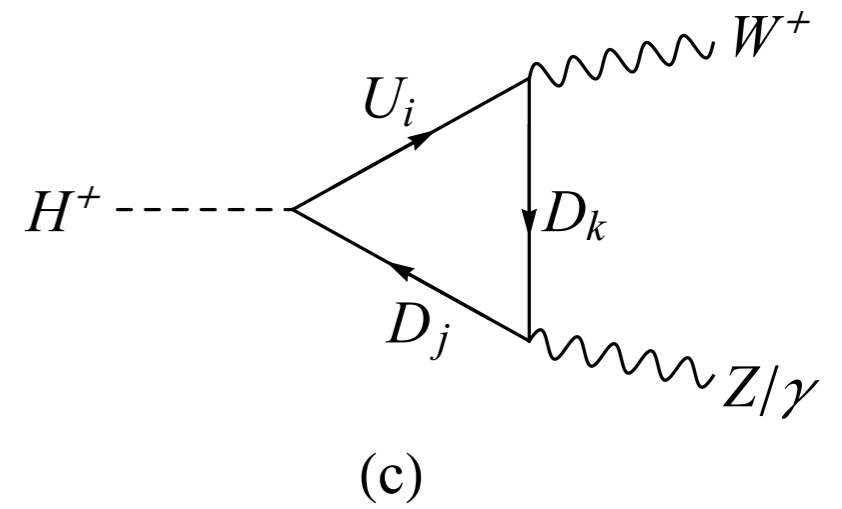
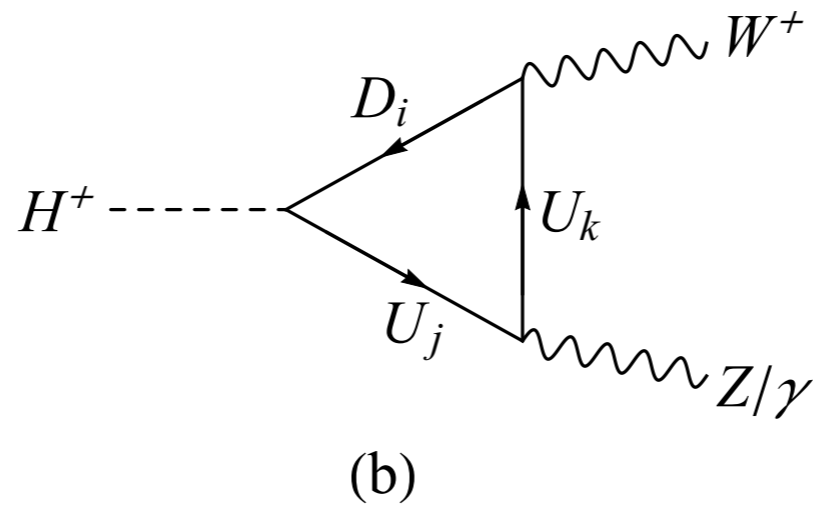
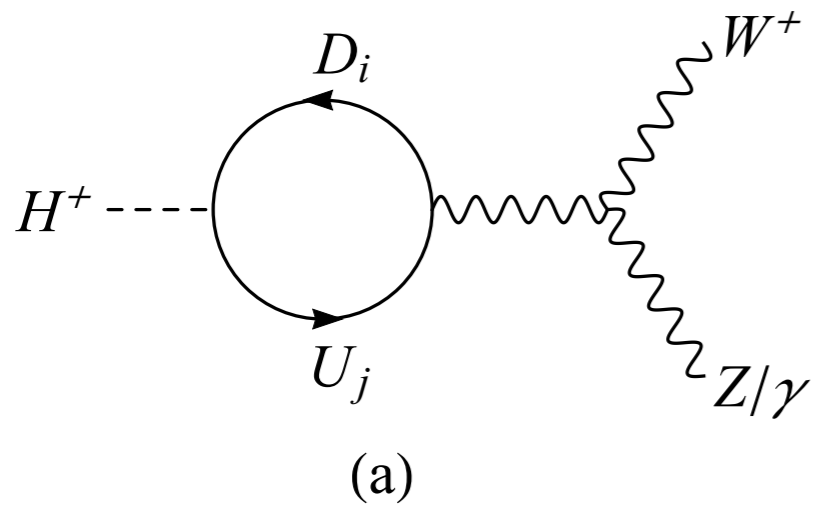
New search channel  
for this tricky  $H^\pm$ ?

$$M_{H^\pm} \simeq m_t$$

# Possible!

$$H^\pm \rightarrow W^\pm \gamma$$

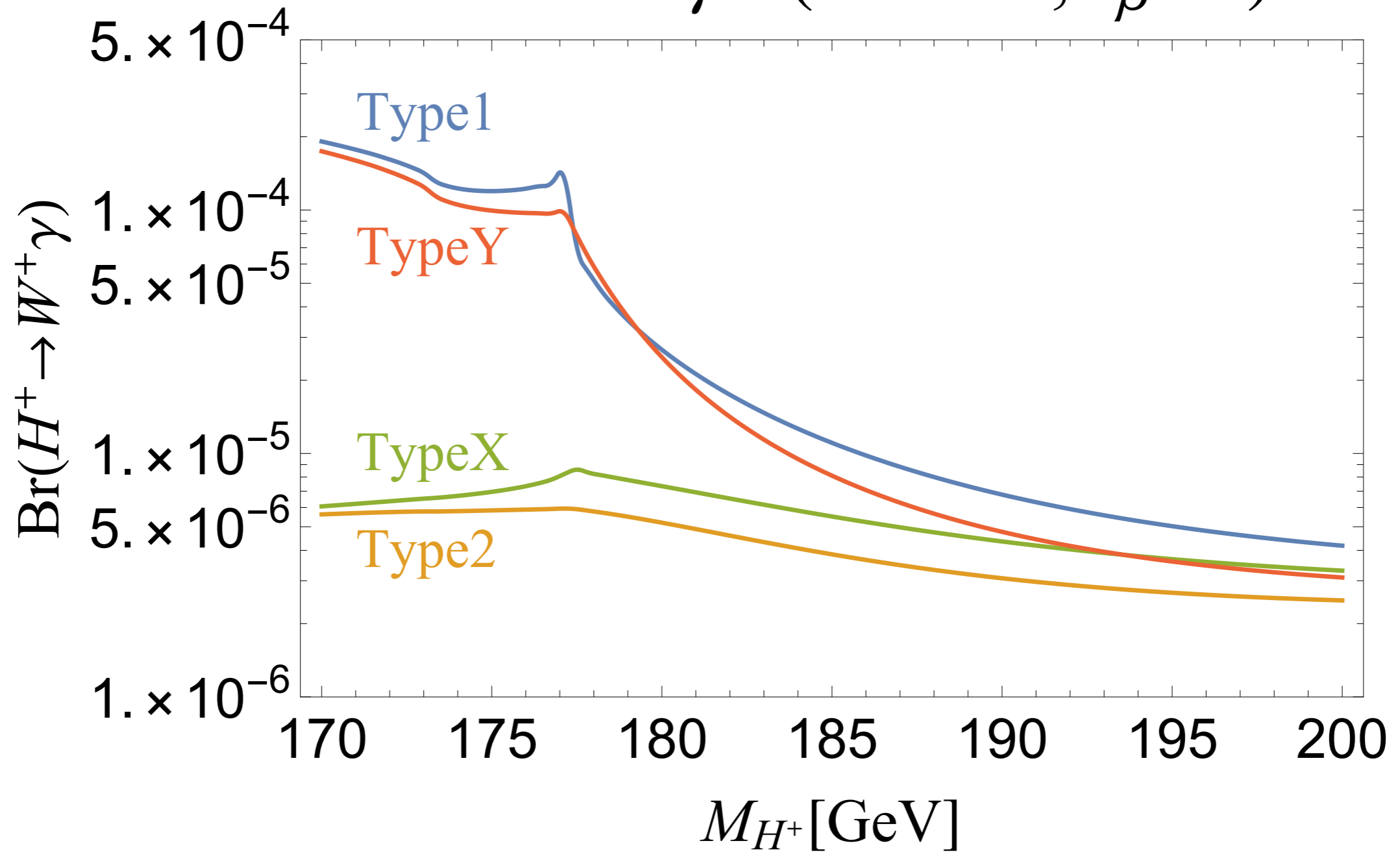
$$H^\pm \rightarrow W^\pm Z^{(*)}$$



**In a pure 2HDM,  
the branching ratio is  
too small!**



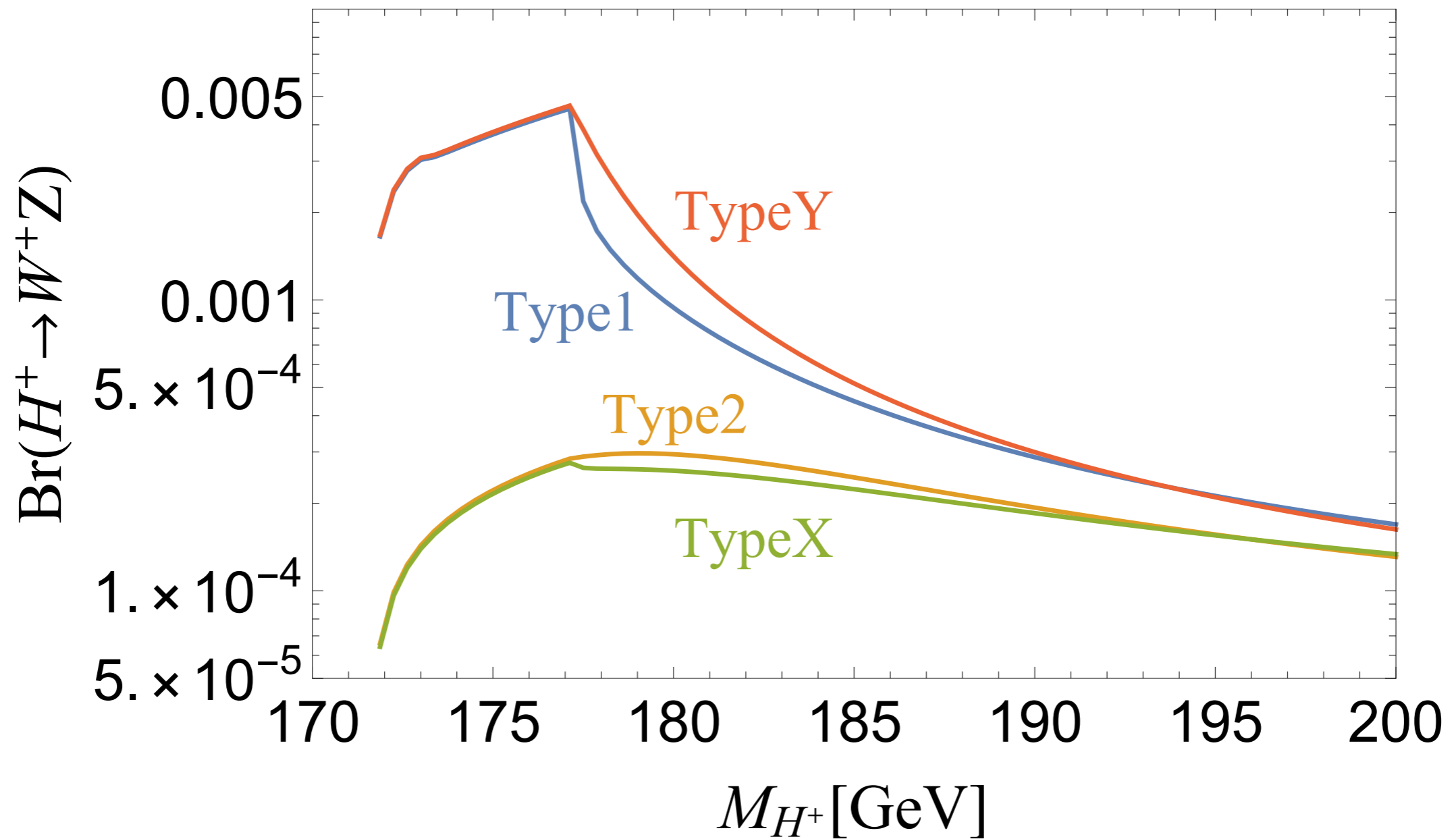
$$H^+ \rightarrow W^+ \gamma \quad (2\text{HDM}, t_\beta=5)$$



At most  $10^{-4}$

After  $M_{H^\pm} > m_t + m_b$ ,  $10^{-5}$

$$H^+ \rightarrow W^+ Z \quad (2\text{HDM}, t_\beta=5)$$



Further suppression if we want  $Z \rightarrow \ell\ell$

**Let's add new  
fermions in the loop:  
Vector-like fermions  
(VLF)**

# VLF

**Introduce both doublet and singlet**

$$\text{VLF doublet : } Q_L = \begin{pmatrix} \mathcal{U}'_L \\ \mathcal{D}'_L \end{pmatrix}, \quad Q_R = \begin{pmatrix} \mathcal{U}'_R \\ \mathcal{D}'_R \end{pmatrix},$$

$$\text{VLF singlets : } \mathcal{U}_L, \quad \mathcal{U}_R, \quad \mathcal{D}_L, \quad \mathcal{D}_R.$$

**Crucial to allow the Higgs Yukawa couplings**

# Strategy to enhance

$$\text{BR}(\mathbf{H}^\pm \rightarrow \mathbf{W}^\pm \gamma)$$

SM	$Q_L, L_L$	$u_R$	$d_R, \ell_R$
type-I	+	-	-
VLF	$Q_{L,R}$	$\mathcal{U}_{L,R}$	$\mathcal{D}_{L,R}$
type-II	+	-	+

# Yukawa Lagrangian

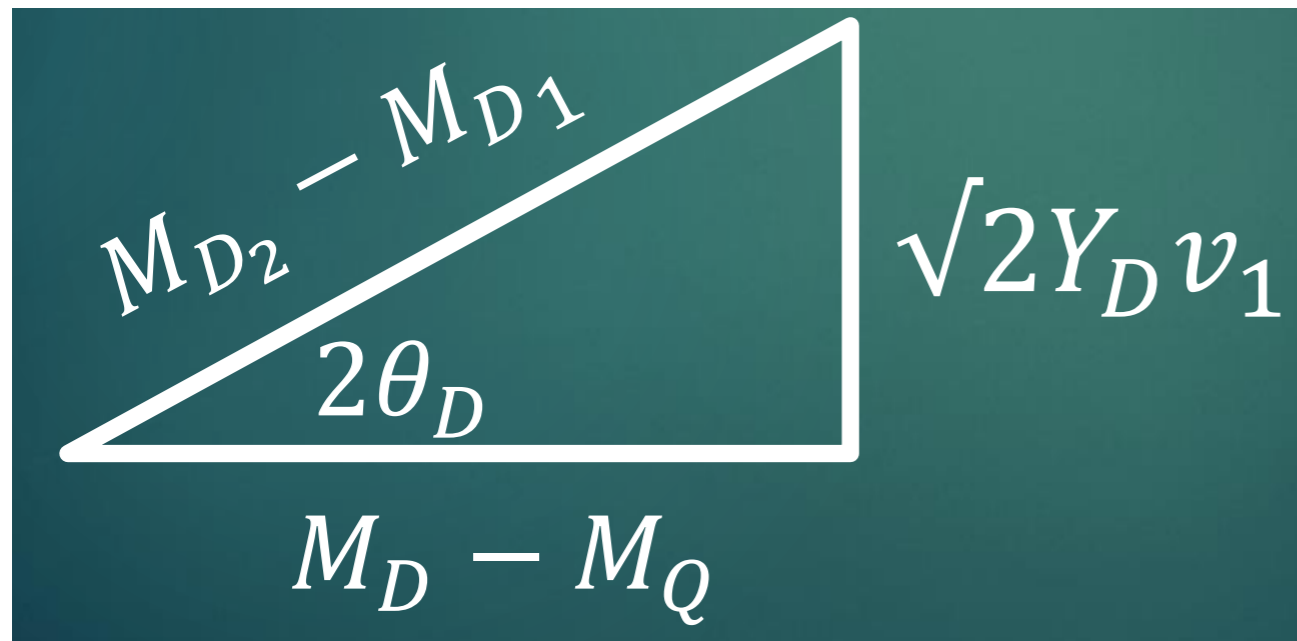
$$-\mathcal{L}_{\text{Yuk}} = M_{\mathcal{F}} \bar{\mathcal{Q}} \mathcal{Q} + M_{\mathcal{U}} \bar{\mathcal{U}} \mathcal{U} + M_{\mathcal{D}} \bar{\mathcal{D}} \mathcal{D} \\ + \left[ Y_{\mathcal{D}} \bar{\mathcal{Q}} \Phi_1 \mathcal{D} + Y_{\mathcal{U}} \bar{\mathcal{Q}} \tilde{\Phi}_2 \mathcal{U} + \text{h.c.} \right]$$

**For simplicity, we assume**

$$Y_{\mathcal{U}}^L = Y_{\mathcal{U}}^R \equiv Y_{\mathcal{U}}$$

# Mixing b/w doublet and singlet

$$M_D = \begin{pmatrix} M_Q & \frac{1}{\sqrt{2}} Y_D v c_\beta \\ \frac{1}{\sqrt{2}} Y_D v c_\beta & M_D \end{pmatrix}, \quad M_U = \begin{pmatrix} M_Q & \frac{1}{\sqrt{2}} Y_U v s_\beta \\ \frac{1}{\sqrt{2}} Y_U v s_\beta & M_U \end{pmatrix}.$$



$$V_D = \begin{pmatrix} \cos \theta_D & -\sin \theta_D \\ \sin \theta_D & \cos \theta_D \end{pmatrix}$$

# Higgs couplings with the VLF mass eigenstates

$$y_{\mathcal{F}_1\mathcal{F}_1}^\phi = -y_{\mathcal{F}_2\mathcal{F}_2}^\phi = -\frac{1}{\sqrt{2}} Y_{\mathcal{F}} \xi_\phi^{\mathcal{F}} s_{2\mathcal{F}},$$

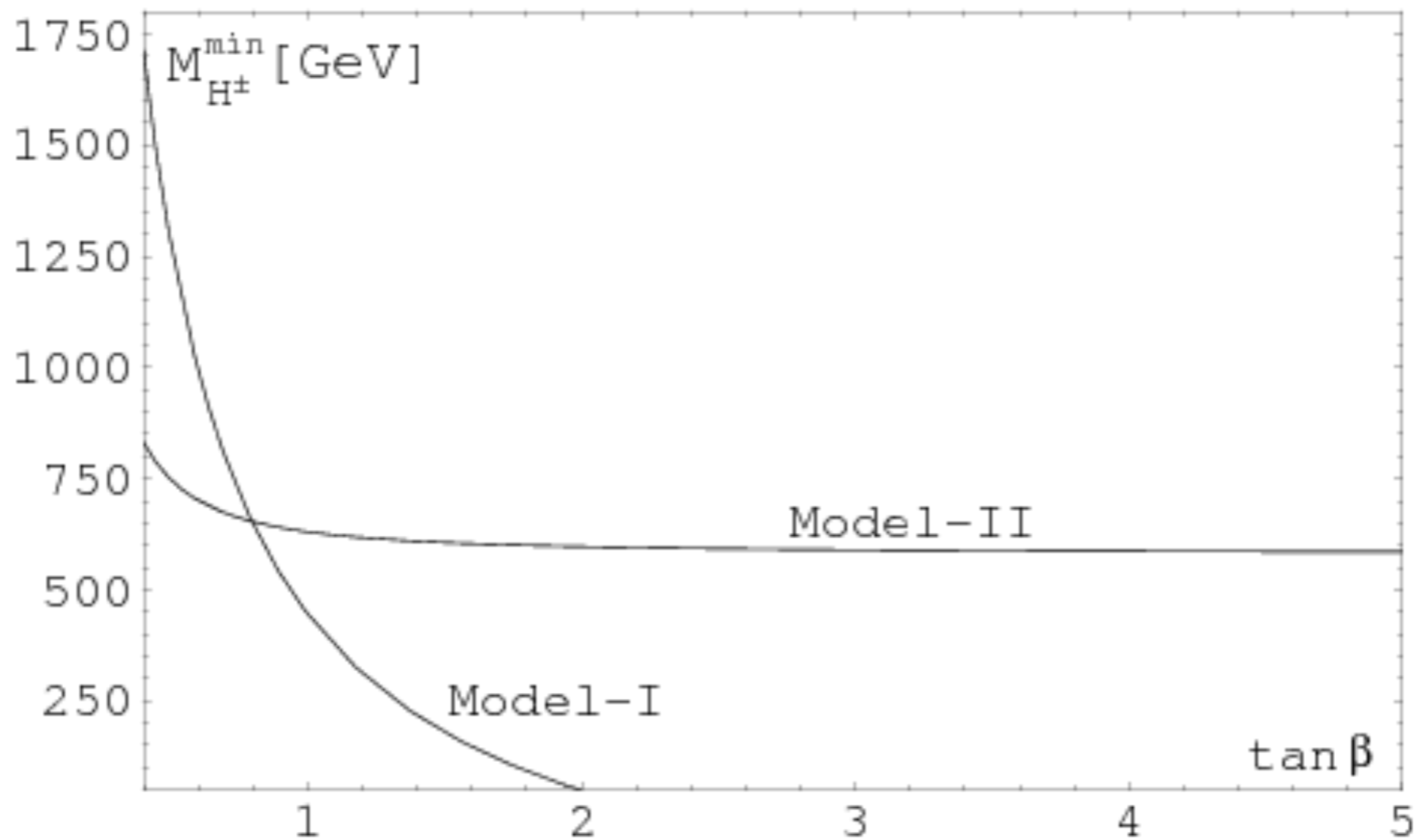
$$y_{\mathcal{F}_1\mathcal{F}_2}^\phi = y_{\mathcal{F}_2\mathcal{F}_1}^\phi = \frac{1}{\sqrt{2}} Y_{\mathcal{F}} \xi_\phi^{\mathcal{F}} c_{2\mathcal{F}},$$

**Where**  $\mathcal{F} = \mathcal{U}, \mathcal{D}$ ,  $\phi = h, H$



# Constraints

# A. Constraints from $b \rightarrow s\gamma$ .



For  $t_\beta > 2$ ,  $M_{H^\pm} \sim m_t$  is possible in Type I

## B. Constraints from Higgs precision

$$0.6 < |\kappa_g| < 1.12.$$

$$\kappa_g = 1 + \frac{\sum_{q=VLQs} y_{hqq} v / m_q A_{1/2}^H(\tau_q)}{A_{1/2}^H(\tau_t)}$$

**OK!**

## B. Constraints from Higgs precision

$$0.6 < |\kappa_g| < 1.12.$$

$$\kappa_g = 1 + \frac{\sum_{q=VLQs} y_{hqq} v / m_q A_{1/2}^H(\tau_q)}{A_{1/2}^H(\tau_t)}$$

$$y_{\mathcal{F}_1 \mathcal{F}_1}^\phi = -y_{\mathcal{F}_2 \mathcal{F}_2}^\phi \quad \text{Cancellation!}$$

## C. Constraints from $\hat{T}$ parameter



Oblique parameters: **S, T, U**

$$S \approx \frac{1}{6\pi},$$

$$T \approx \frac{1}{12\pi s^2 c^2} \left[ \frac{(\Delta m)^2}{m_Z^2} \right],$$

$$U \approx \frac{2}{15\pi} \left[ \frac{(\Delta m)^2}{m_N^2} \right].$$

**In the SM!**

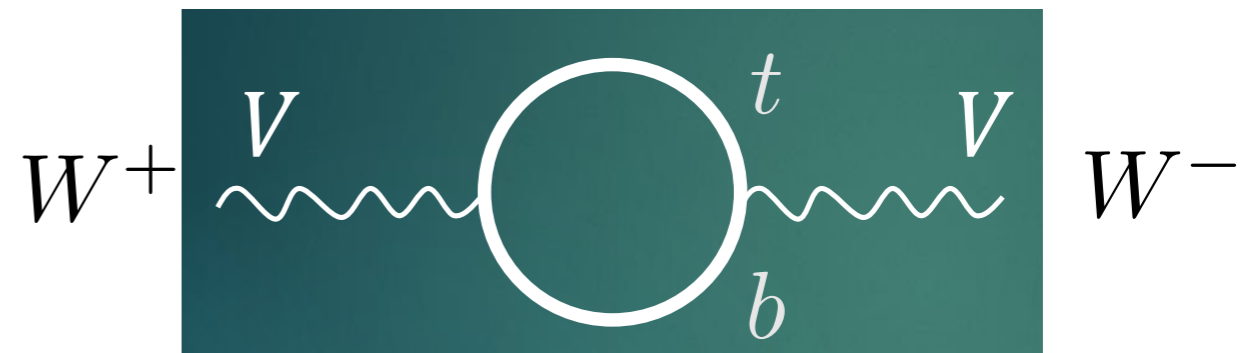
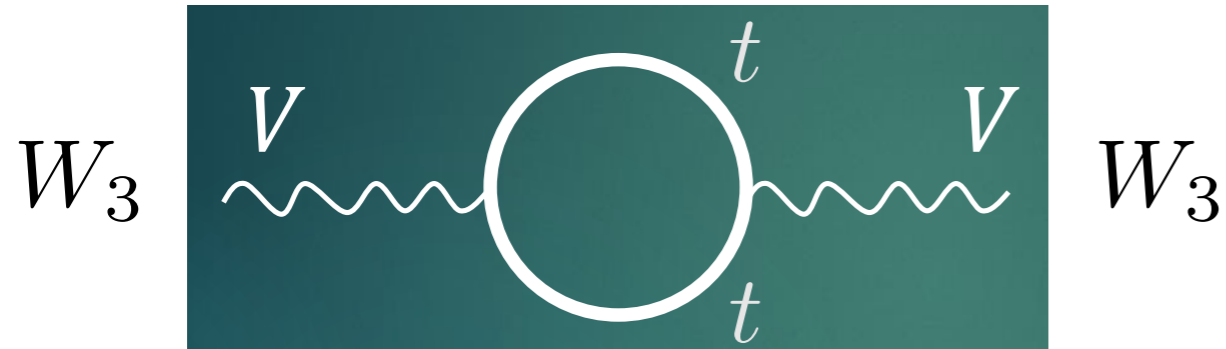
**Later we shall consider large  
mass difference like 500 GeV**

**Why is this allowed in our  
model?**

$$M_W^2 \hat{T} = \Pi_{W_3 W_3}(0) - \Pi_{W^+ W^-}(0),$$

SM?

$$M_W^2 \hat{T} = \Pi_{W_3 W_3}(0) - \Pi_{W^+ W^-}(0),$$

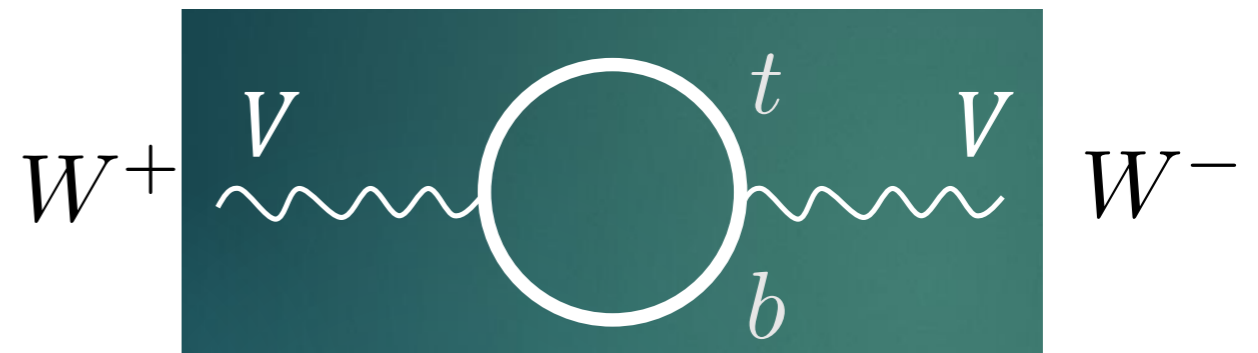
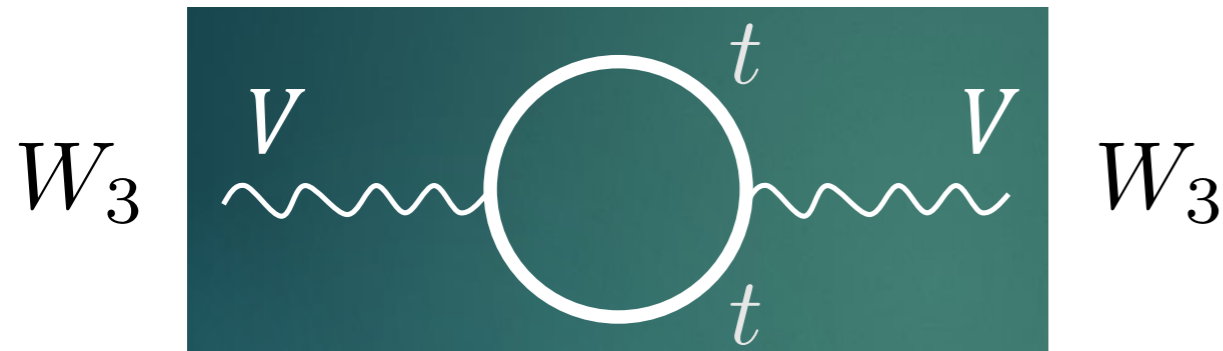




SM?

$$M_W^2 \hat{T} = \Pi_{W_3 W_3}(0) - \Pi_{W^+ W^-}(0),$$

$$\Delta M = 0 \rightarrow \Pi_{VV}(0) = 0$$



$$M_W^2 \hat{T} = \Pi_{W_3 W_3}(0) - \Pi_{W^+ W^-}(0),$$

$\nearrow 0$        $\nearrow \propto \Delta M^2$

# One VLQ doublet + one VLQ singlet

**Mixing**



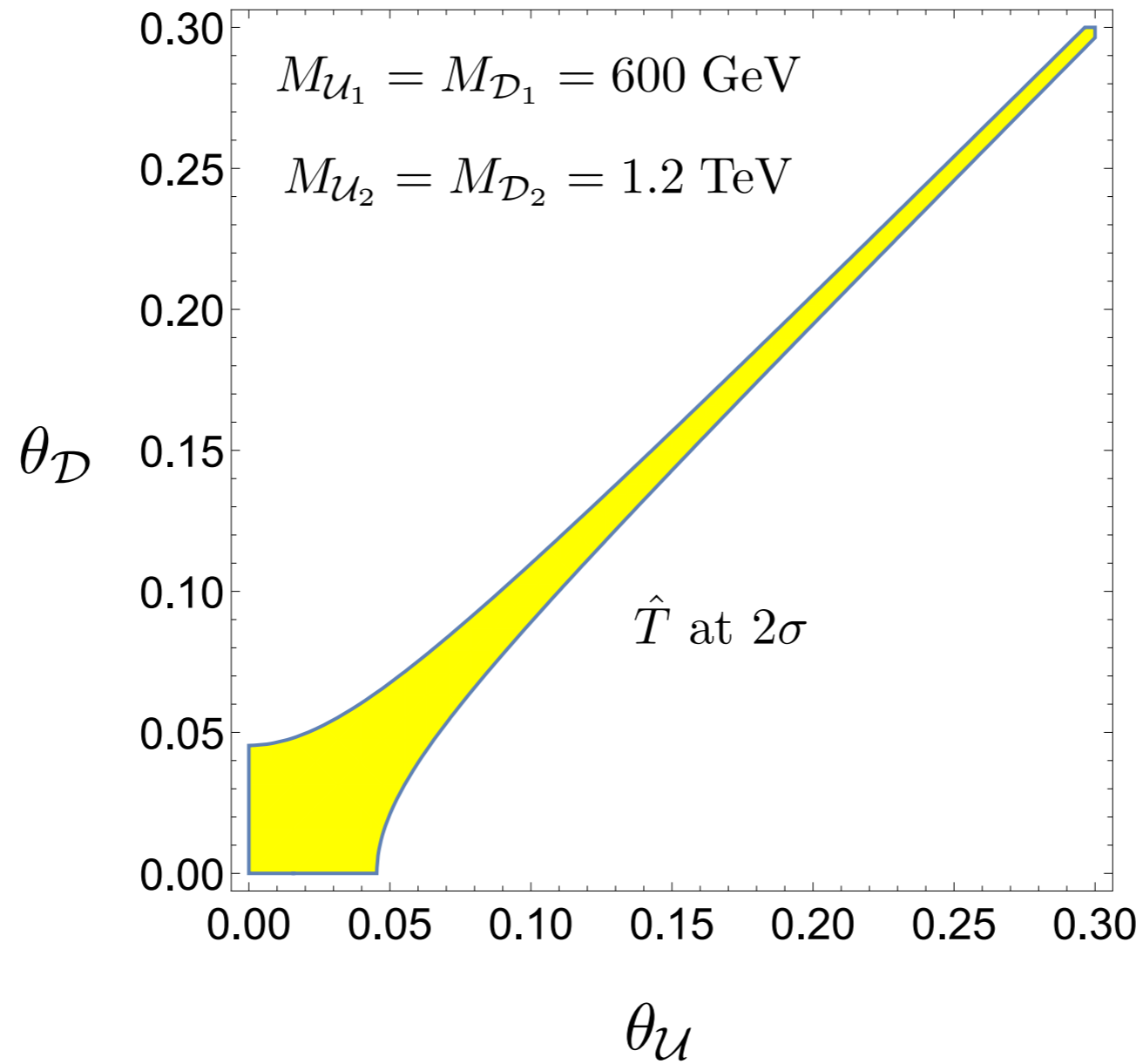
$\propto \Delta M^2$

$\propto \Delta M^2$

$$M_W^2 \hat{T} = \Pi_{W_3 W_3}(0) - \Pi_{W^+ W^-}(0),$$

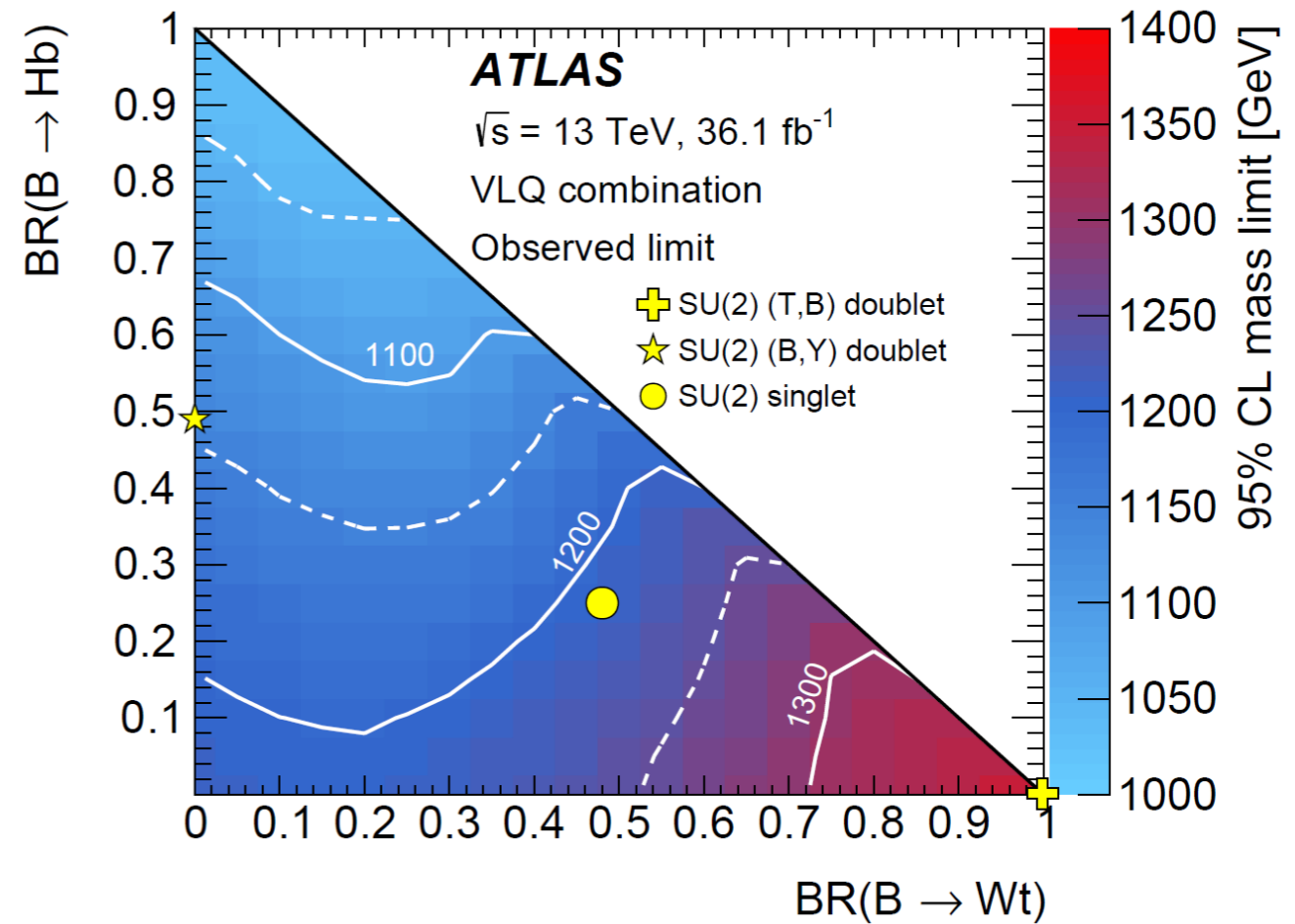
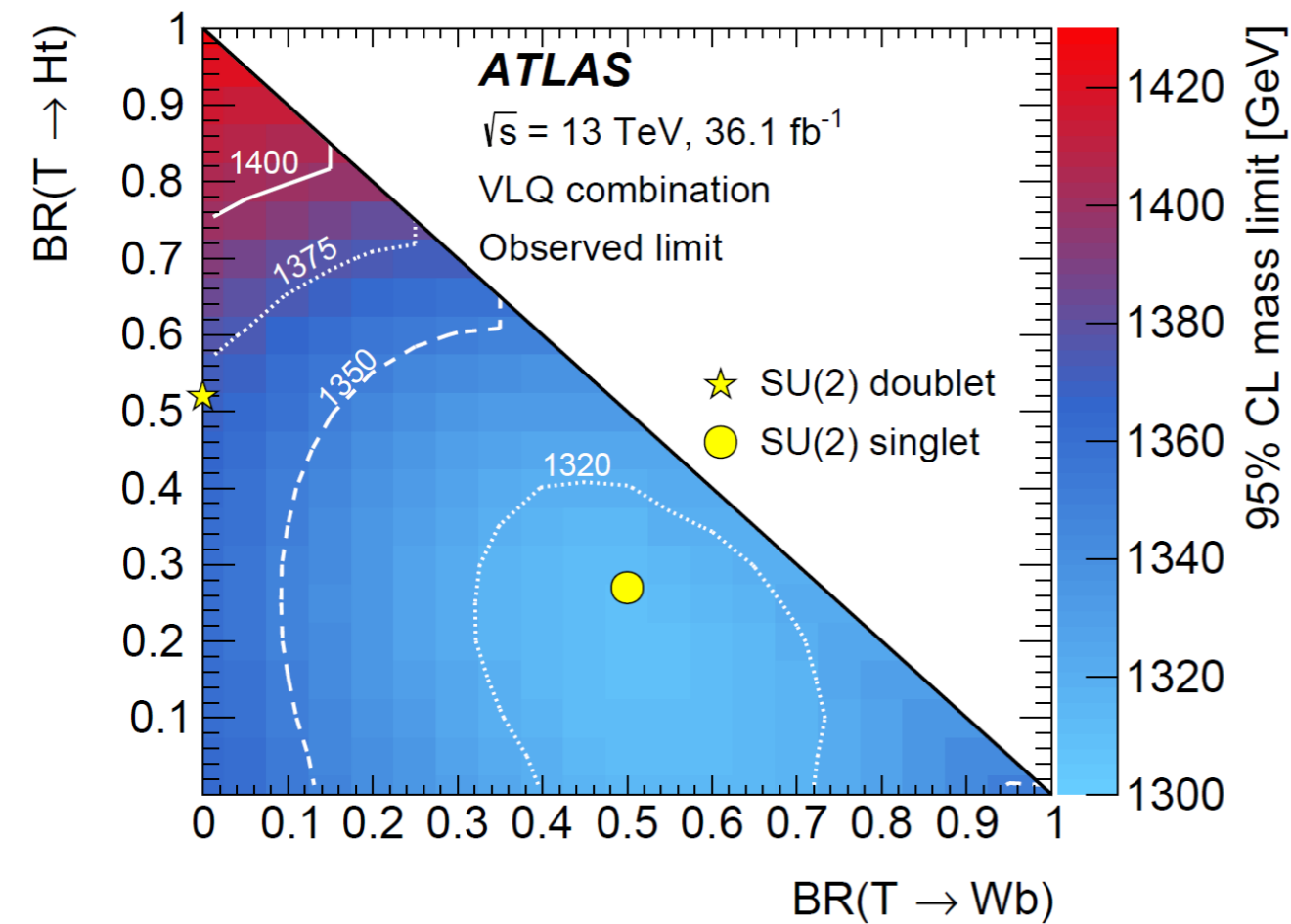
**Cancellation!**

# Cancellation happens when



$$M_{U_1} = M_{D_1}, \quad M_{U_2} = M_{D_2}, \quad \theta_U = \theta_D.$$

# Direct constraints on the VL fermion masses



$$M_T > 1.31 \text{ TeV}$$

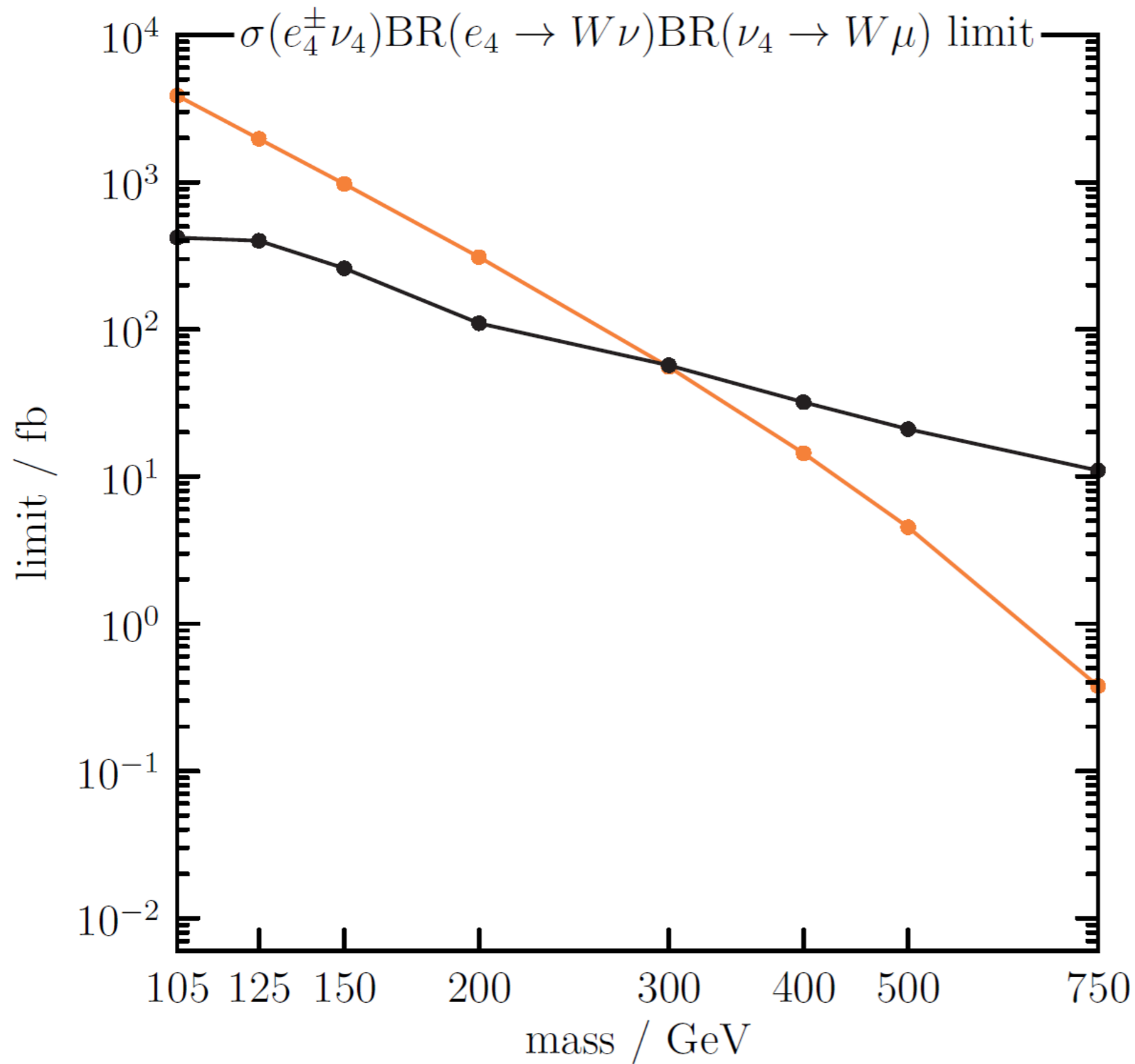
$$M_B > 1.03 \text{ TeV}$$

$$T \rightarrow Zt/Wb/Ht$$

$$B \rightarrow Hb/Zb/Wt$$

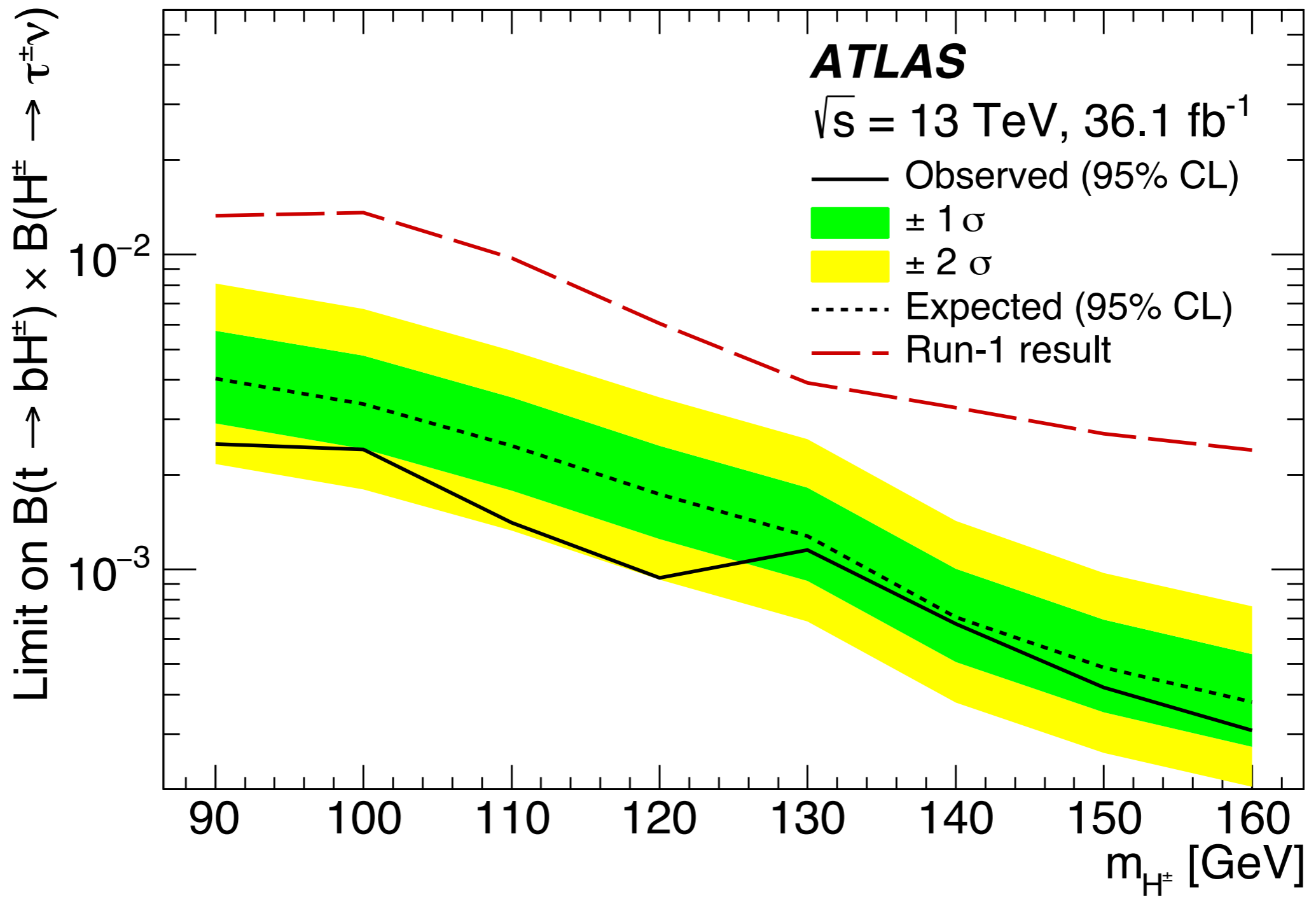
The bounds can be relaxed if the VLQs decay into light quarks.

# Dermisek, Hall, Lunghi, Shin, 1408.3123

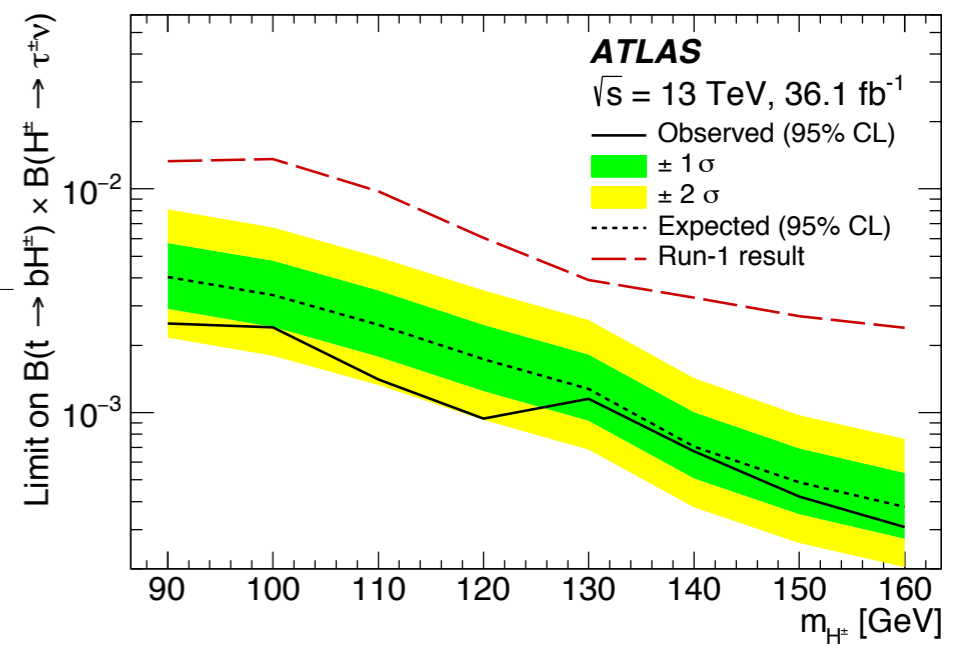
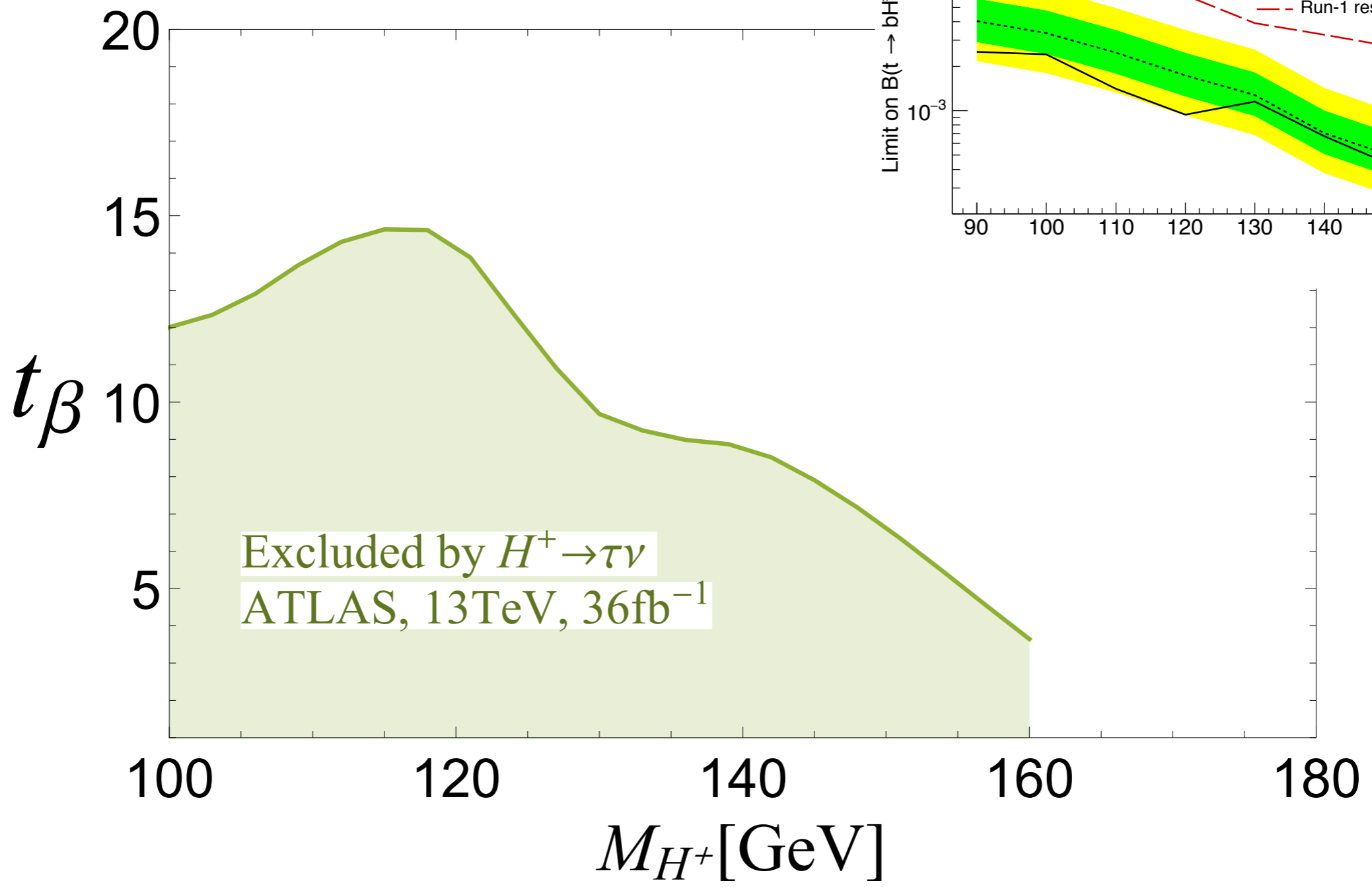


$M_E > 300 \text{ GeV}$

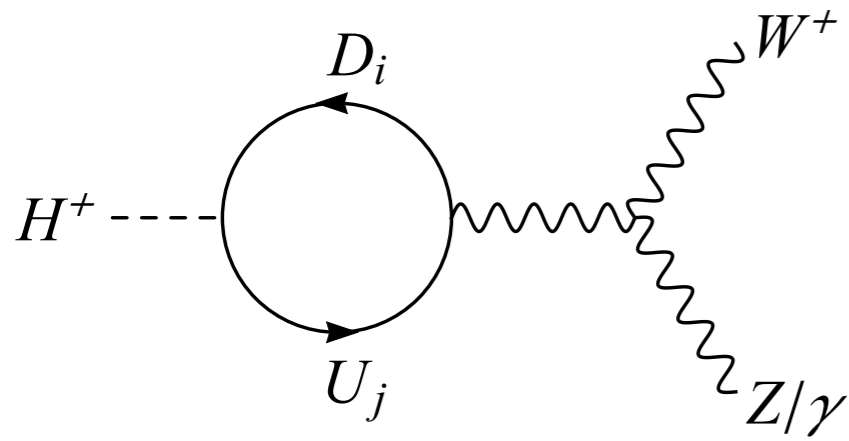
# Constraints from the direct searches for the charged Higgs boson at the LHC



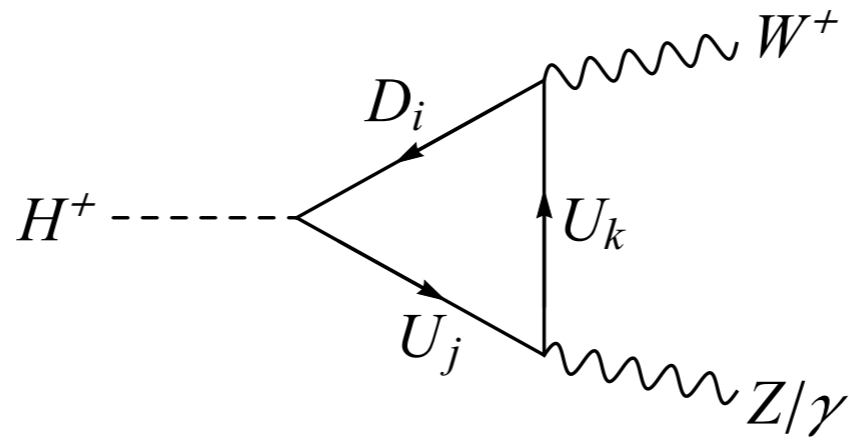




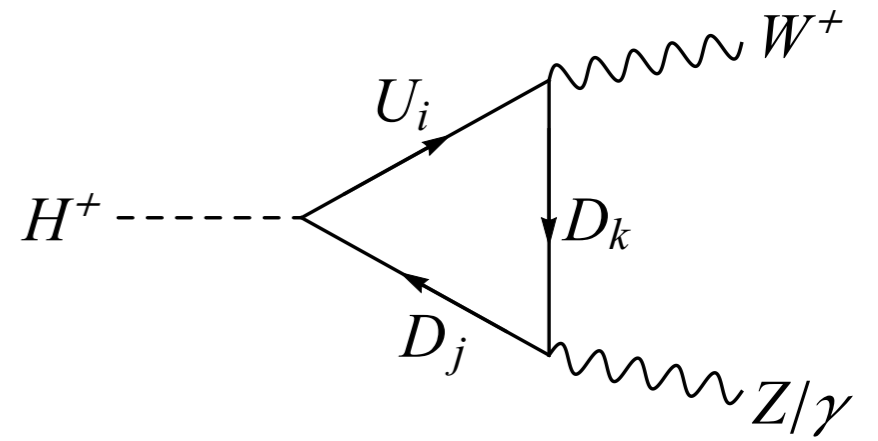
$$BR(H^\pm \rightarrow W^\pm \gamma / W^\pm Z)$$



(a)



(b)



(c)

$$\mathcal{M} = \frac{g^2 N_c M_{H^+}}{(16\pi^2) \sqrt{2} c_W} \epsilon_W^{\mu*} \epsilon_V^{\nu*} \mathcal{M}_{\mu\nu},$$

$$\mathcal{M}_{\mu\nu} = g_{\mu\nu} \mathcal{M}_1 + \frac{p_{2\mu} p_{1\nu}}{M_{H^-}^2} \mathcal{M}_2 + i \epsilon_{\mu\nu\rho\sigma} \frac{p_{2\rho} p_{1\sigma}}{M_{H^-}^2} \mathcal{M}_3$$

For  $W^+\gamma$  decay, the Ward-identity  $p_2^\nu M_{\mu\nu} = 0$

$$\mathcal{M}_1 = -\frac{1}{2} \left( 1 - \frac{m_W^2}{M_{H^+}^2} \right) \mathcal{M}_2, \quad (\text{for } H^+ \rightarrow W^+\gamma)$$

$$\Gamma(H^+ \rightarrow W^+\gamma) = \frac{M_{H^+}}{32\pi} \left( 1 - \frac{m_W^2}{M_{H^+}^2} \right)^3 [ |\mathcal{M}_2|^2 + |\mathcal{M}_3|^2 ]$$

for  $H^+ \rightarrow W^+ Z$

$$\Gamma(H^+ \rightarrow W^+ Z) = \frac{\beta M_{H^+}}{32\pi} \left[ \left( 6 + \frac{\beta^2 M_{H^+}^4}{2m_W^2 m_Z^2} \right) |\mathcal{M}_1|^2 + \frac{\beta^4 M_{H^+}^4}{8m_W^2 m_Z^2} |\mathcal{M}_2|^2 + \beta^2 |\mathcal{M}_3|^2 \right. \\ \left. + \frac{\beta^2}{2} \left( \frac{M_{H^+}^4}{m_W^2 m_Z^2} - \frac{M_{H^+}^2}{m_W^2} - \frac{M_{H^+}^2}{m_Z^2} \right) \text{Re}(\mathcal{M}_1 \mathcal{M}_2^*) \right],$$

# Benchmark point

$$s_{\beta-\alpha} = 1, \quad (\text{alignment limit}),$$

$$M_{\mathcal{U}_1} = M_{\mathcal{D}_1} = \begin{cases} 600 \text{ GeV or } 1.3 \text{ TeV, for VLQ;} \\ 300 \text{ GeV, for VLL,} \end{cases}$$

$$(Q_{\mathcal{U}}, Q_{\mathcal{D}}) = \begin{cases} \text{VLQ:} & \begin{bmatrix} (X, T) : (5/3, 2/3); \\ (T, B) : (2/3, -1/3); \\ (B, Y) : (-1/3, -4/3); \end{bmatrix} \\ \text{VLL:} & (N, E) : (0, -1), \end{cases}$$

$$\Delta M \equiv M_{\mathcal{U}_2} - M_{\mathcal{U}_1} = M_{\mathcal{D}_2} - M_{\mathcal{D}_1} \subset [0, 1.5] \text{ TeV}$$

$$\theta_{\mathcal{U}} = \theta_{\mathcal{D}} = 0.2,$$

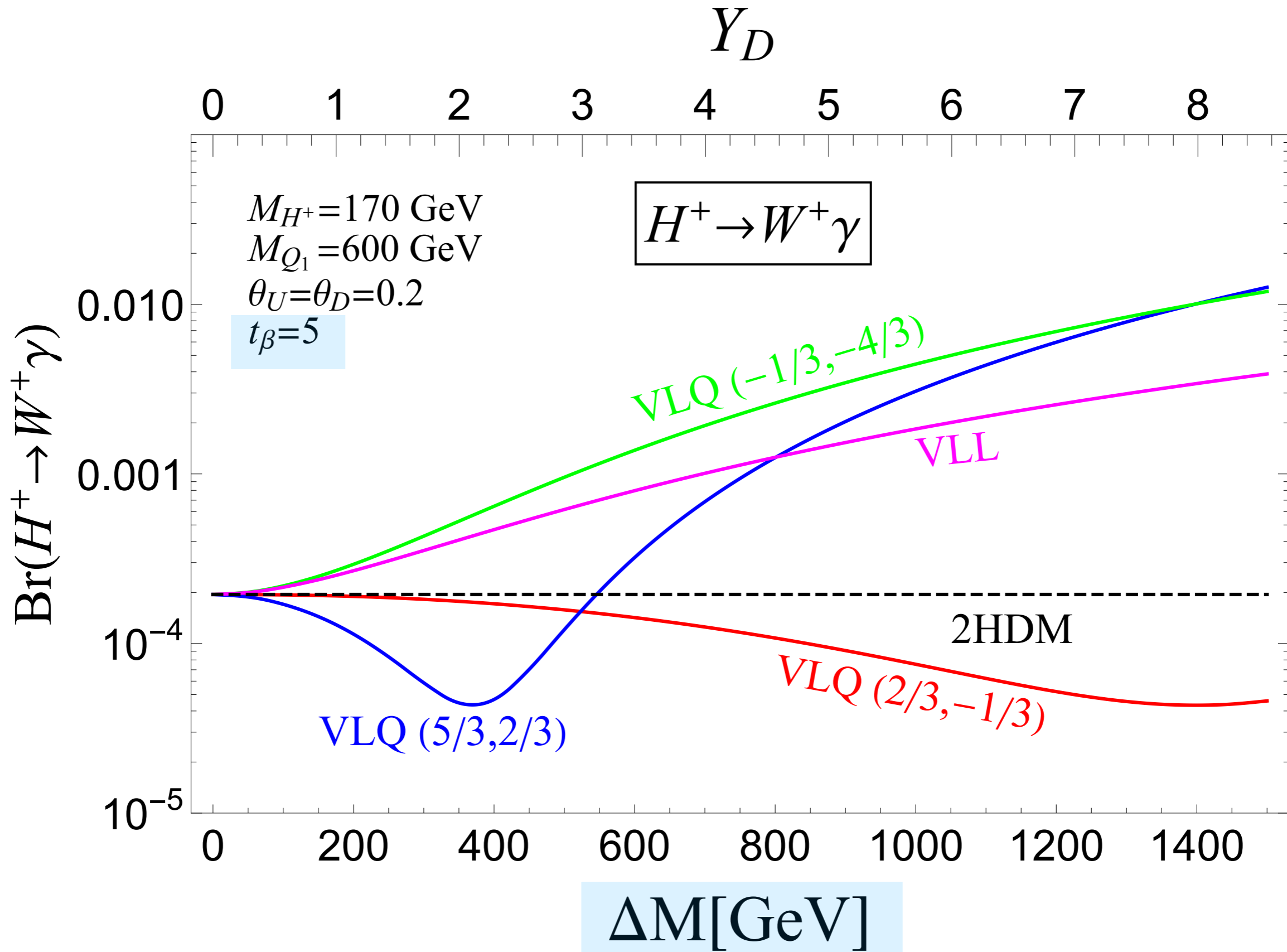
# Decays of VLF (X,T)

$$-\mathcal{L} = \delta Y_{4u} \bar{Q} \Phi_2 u_R + \delta Y_{4d} \bar{Q}_L \Phi_1 \mathcal{D} + h.c.,$$

$$X \rightarrow H^+ u_i, \quad X \rightarrow W^+ u_i$$

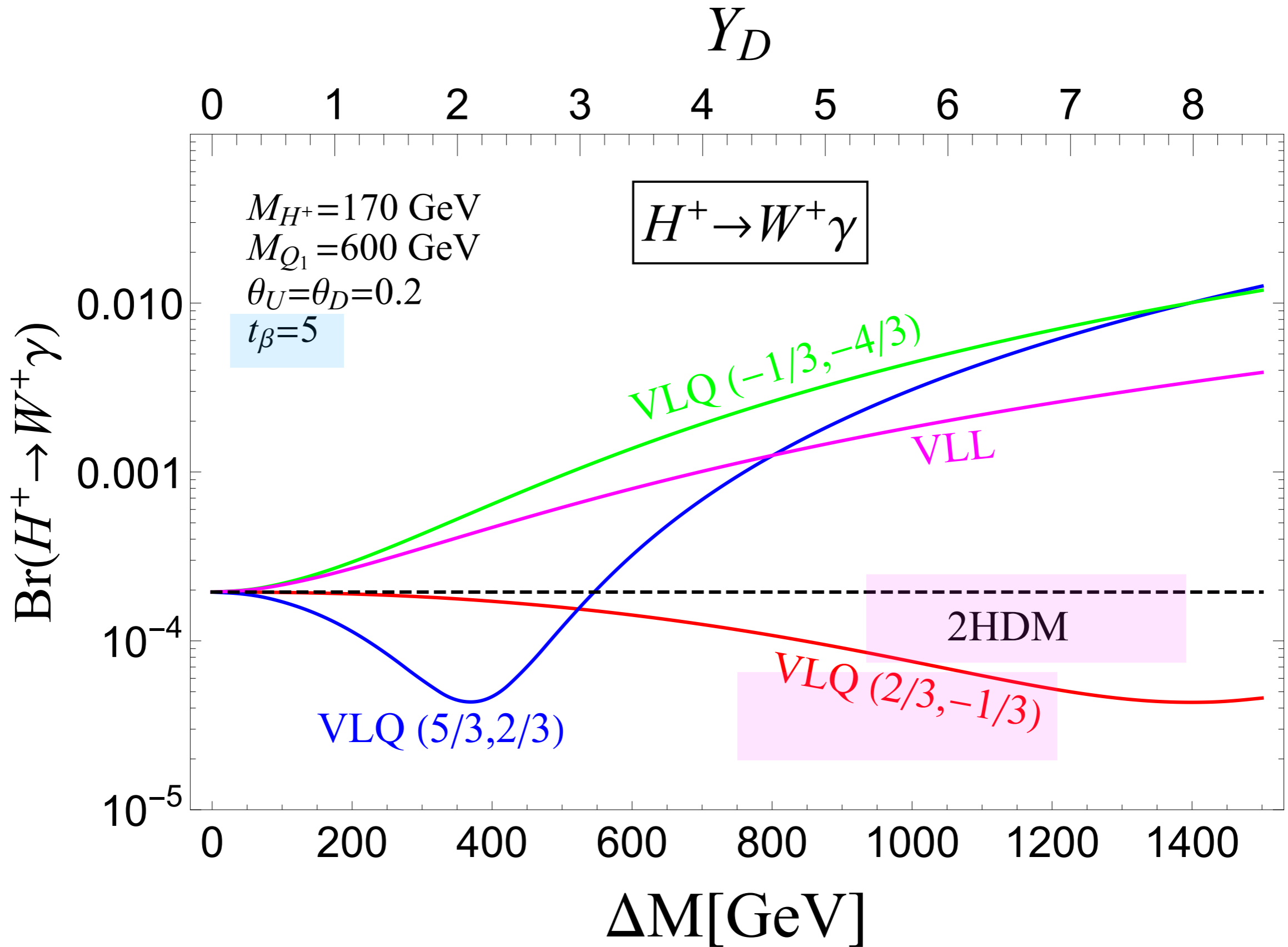
$$Q_X = \frac{5}{3}$$

# Low mass of the VLFs

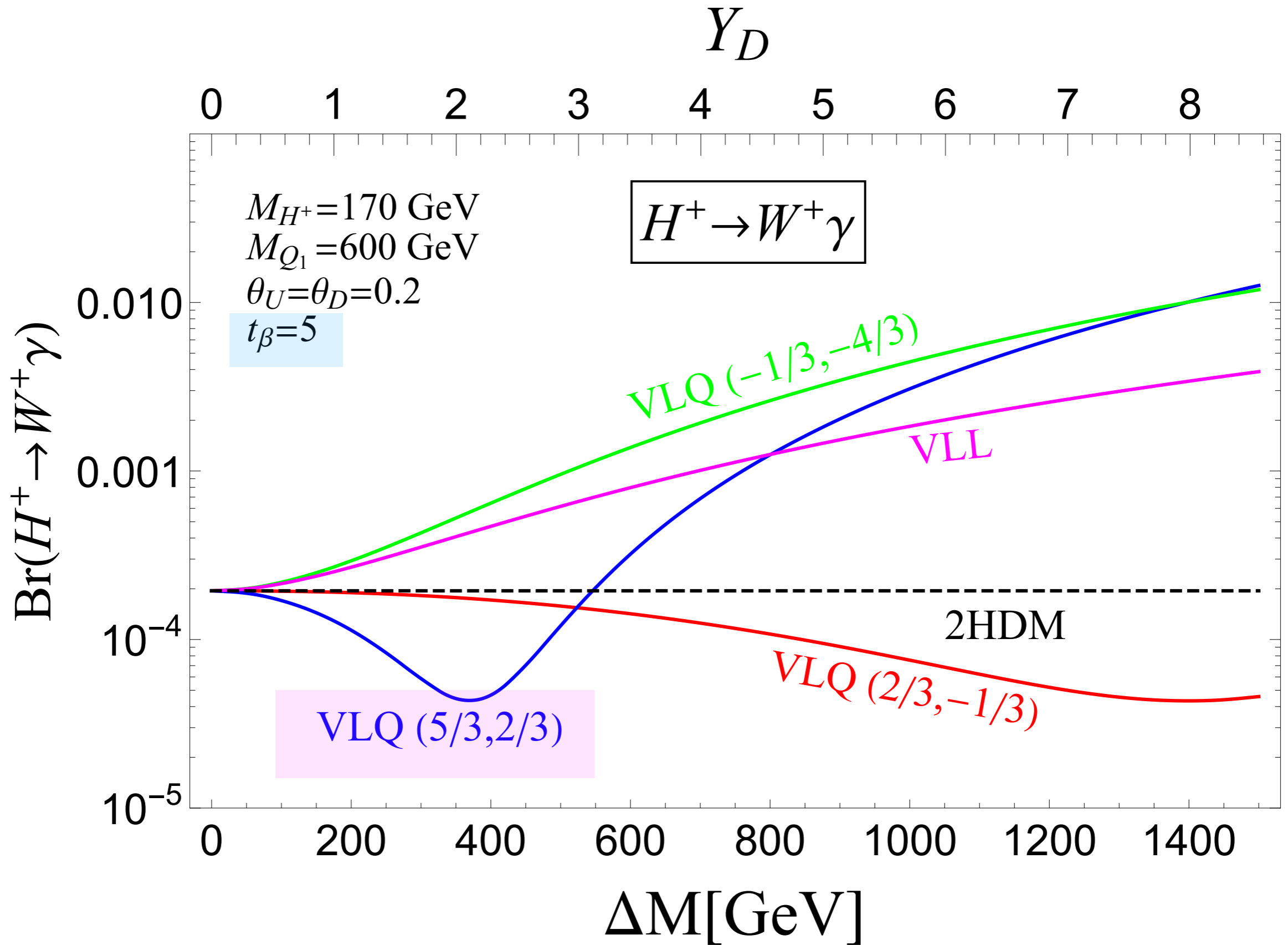




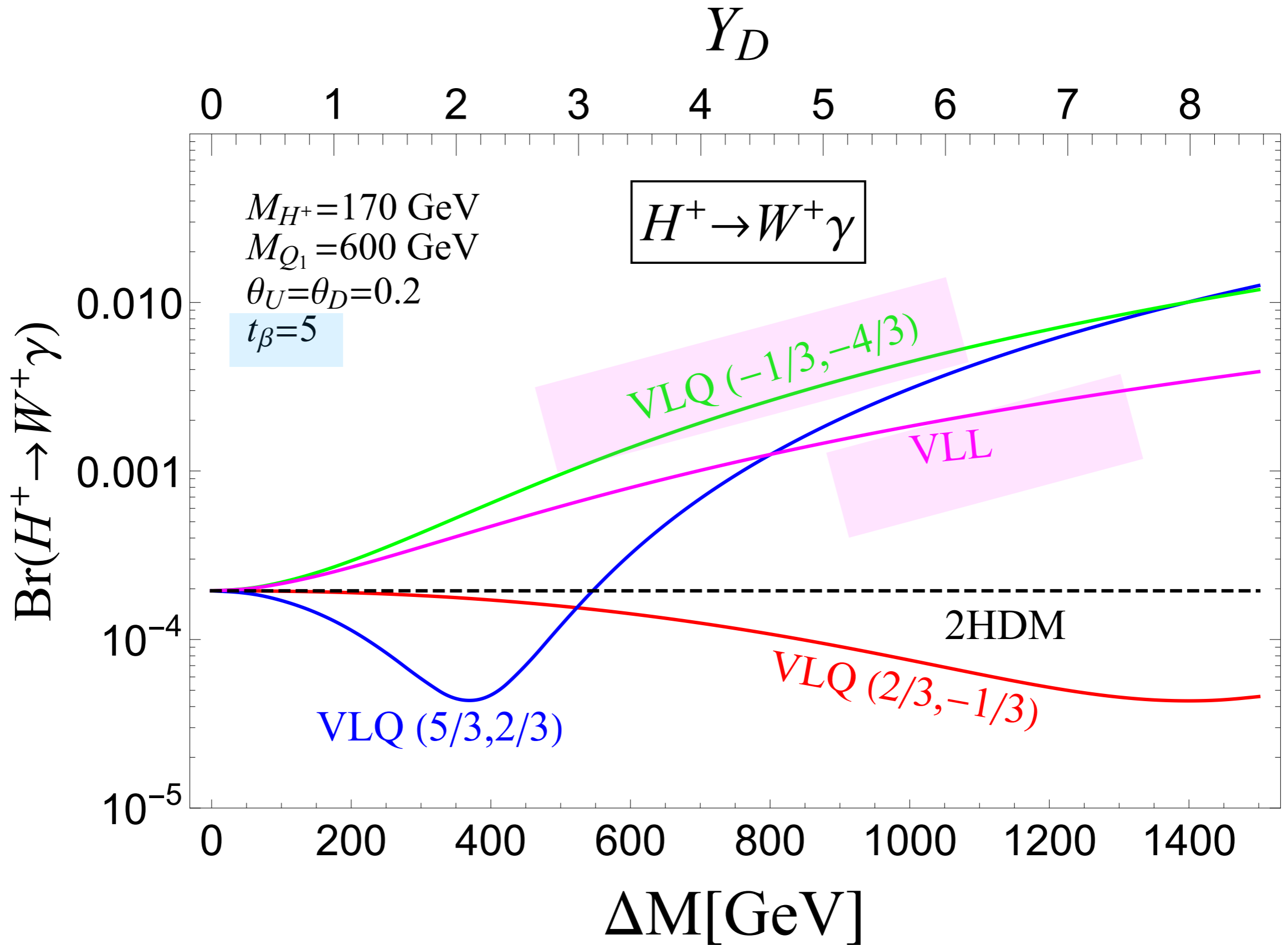
# Low mass of the VLFs



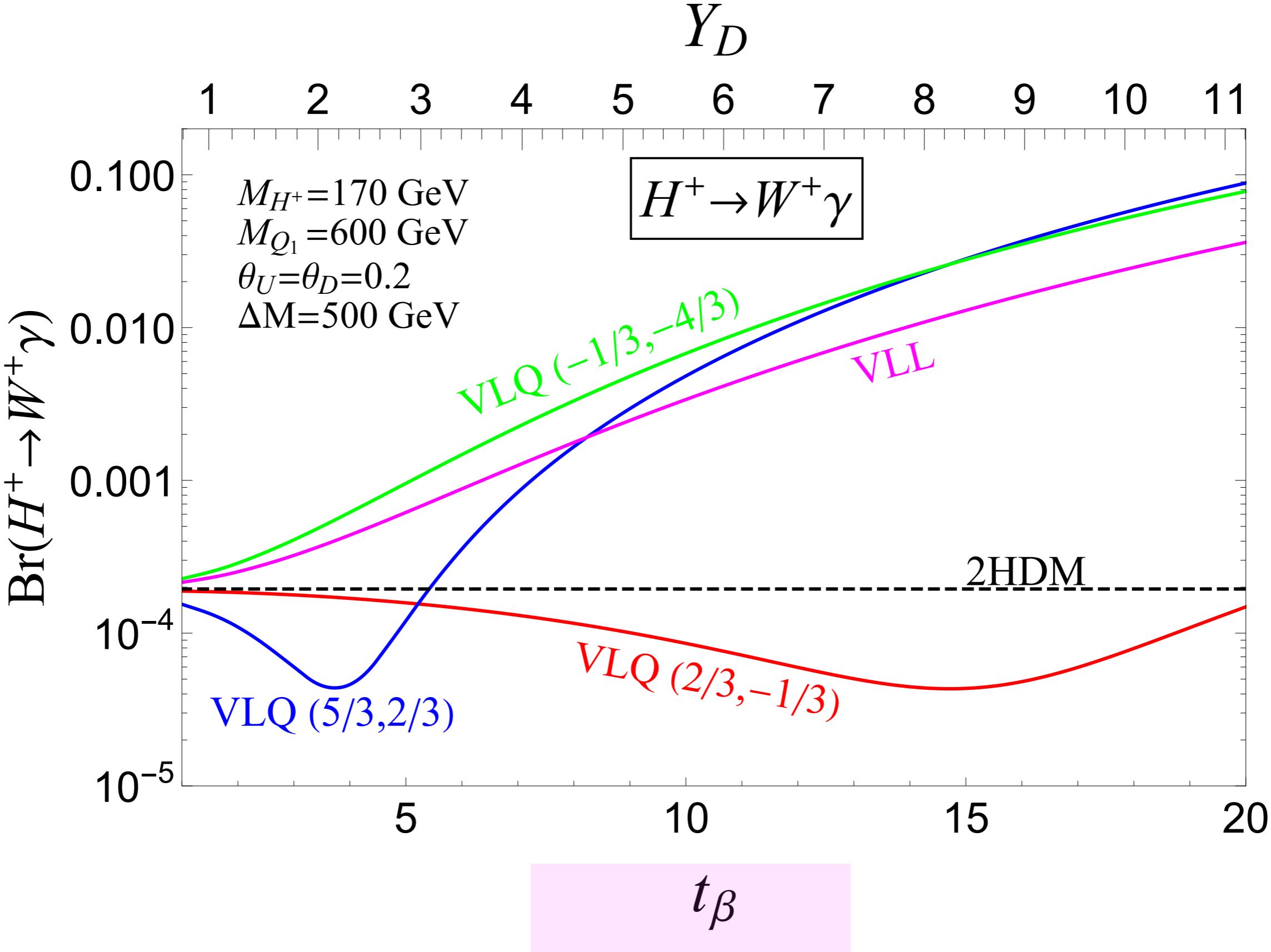
# Low mass of the VLFs



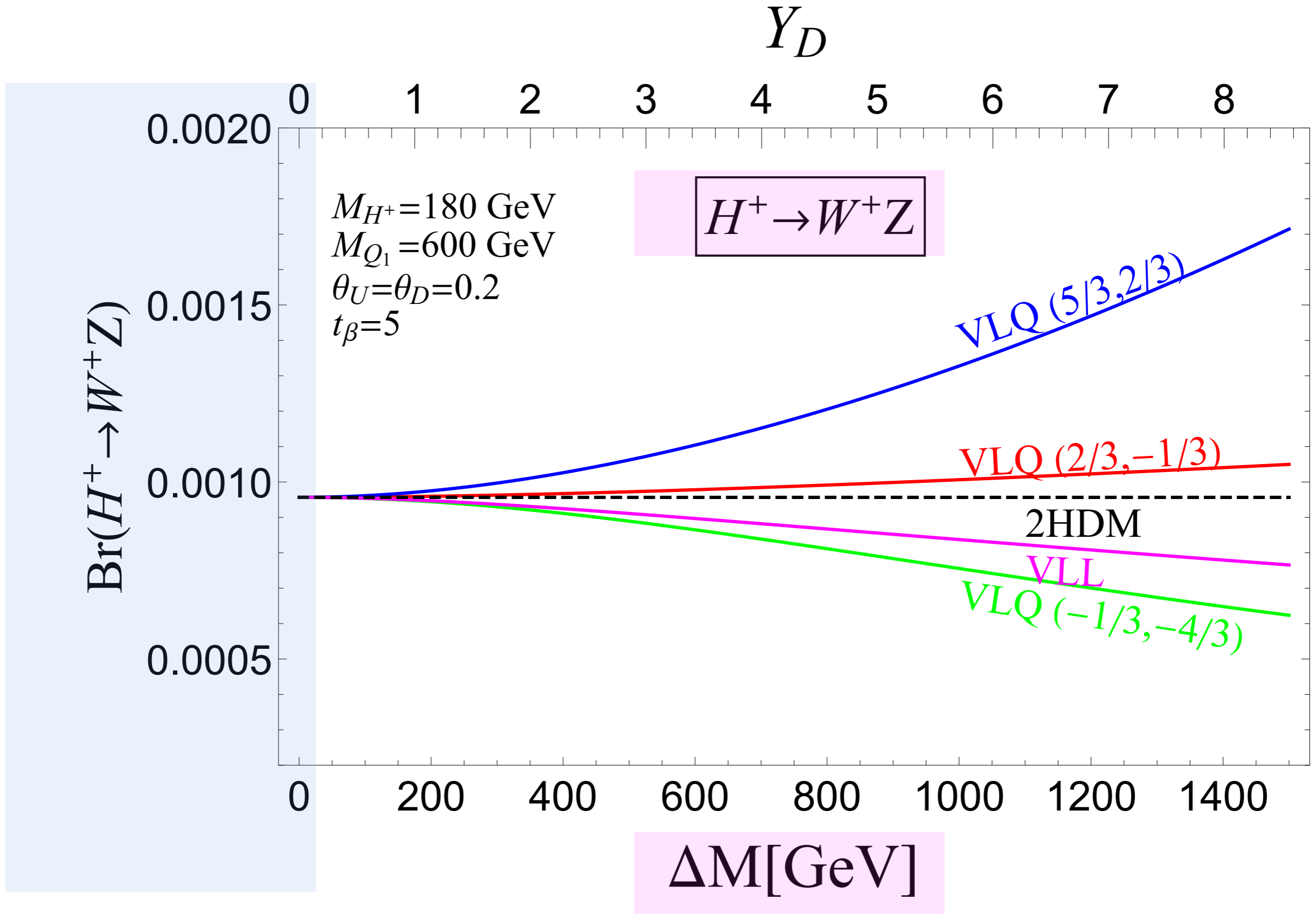
# Low mass of the VLFs



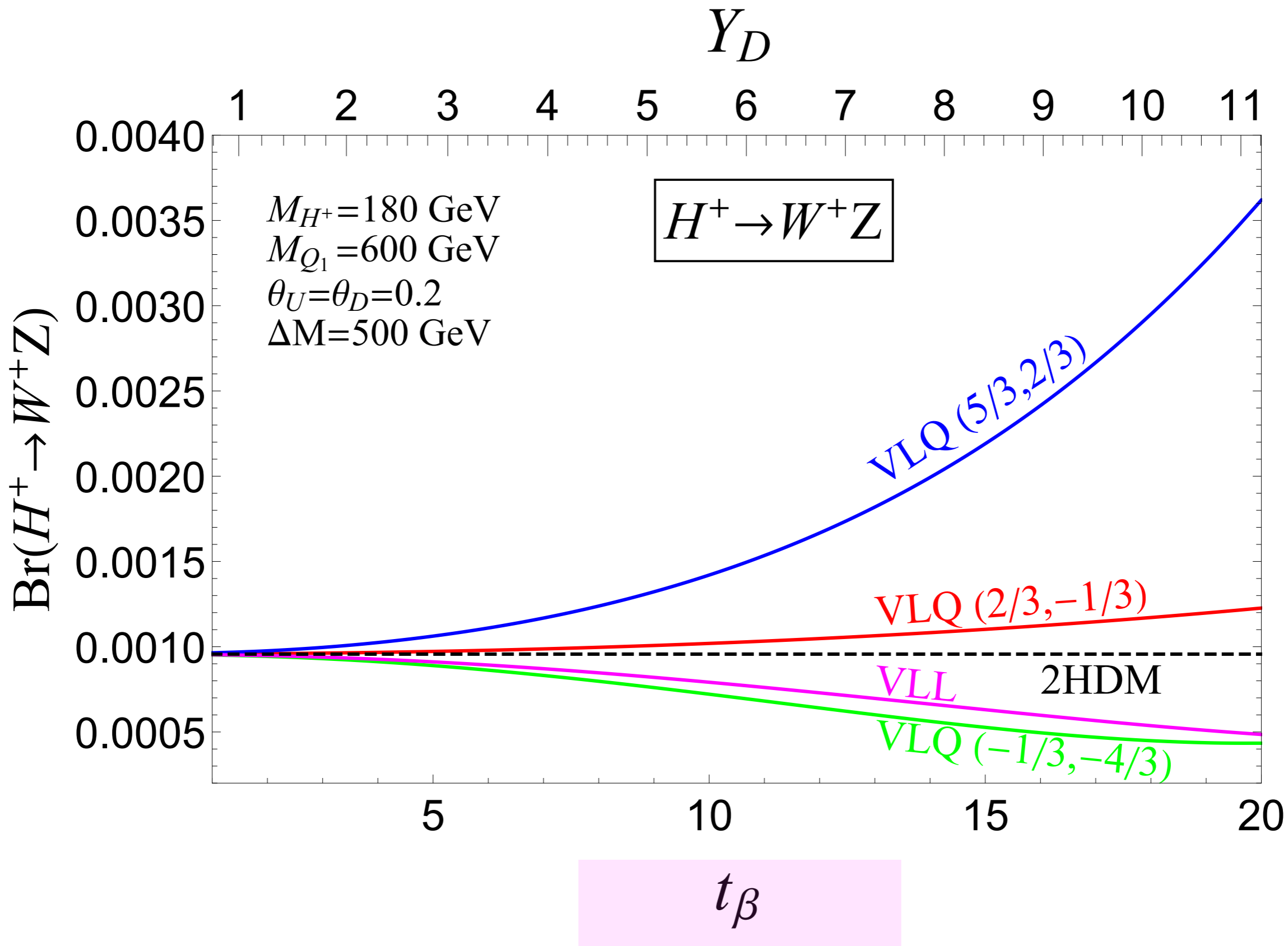
# Low mass of the VLFs



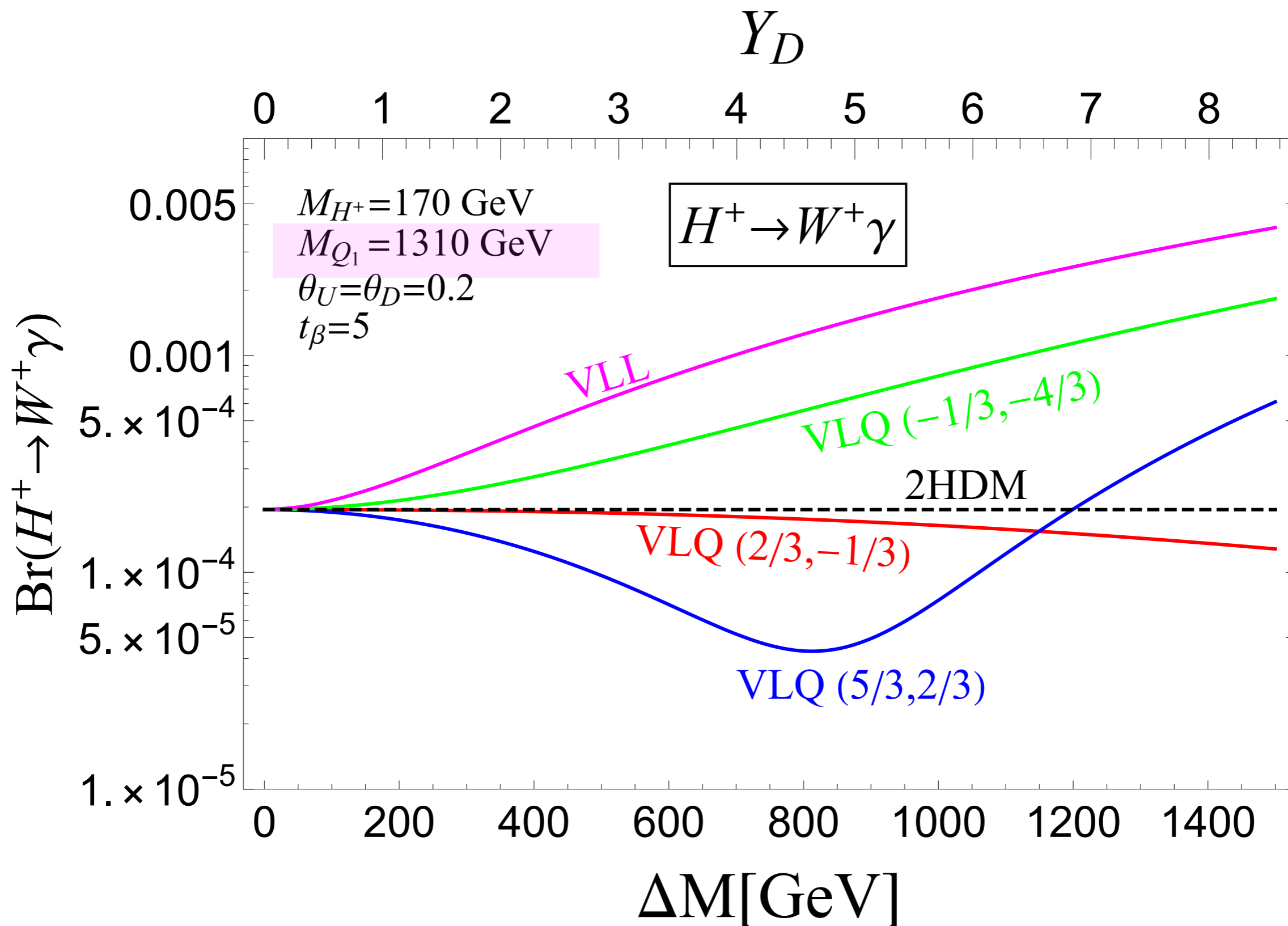
# Low mass of the VLFs



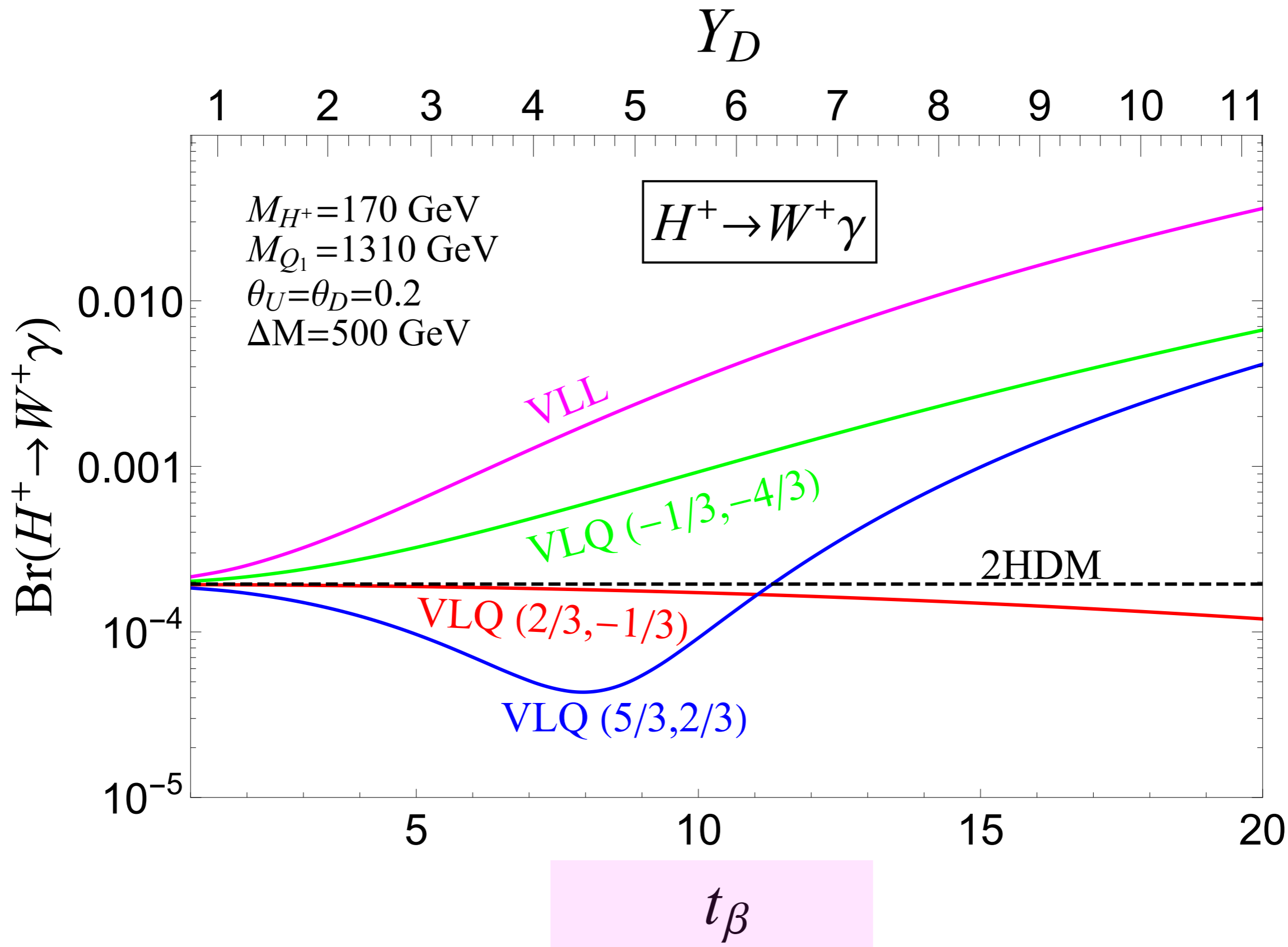
# Low mass of the VLFs



# High mass of the VLFs



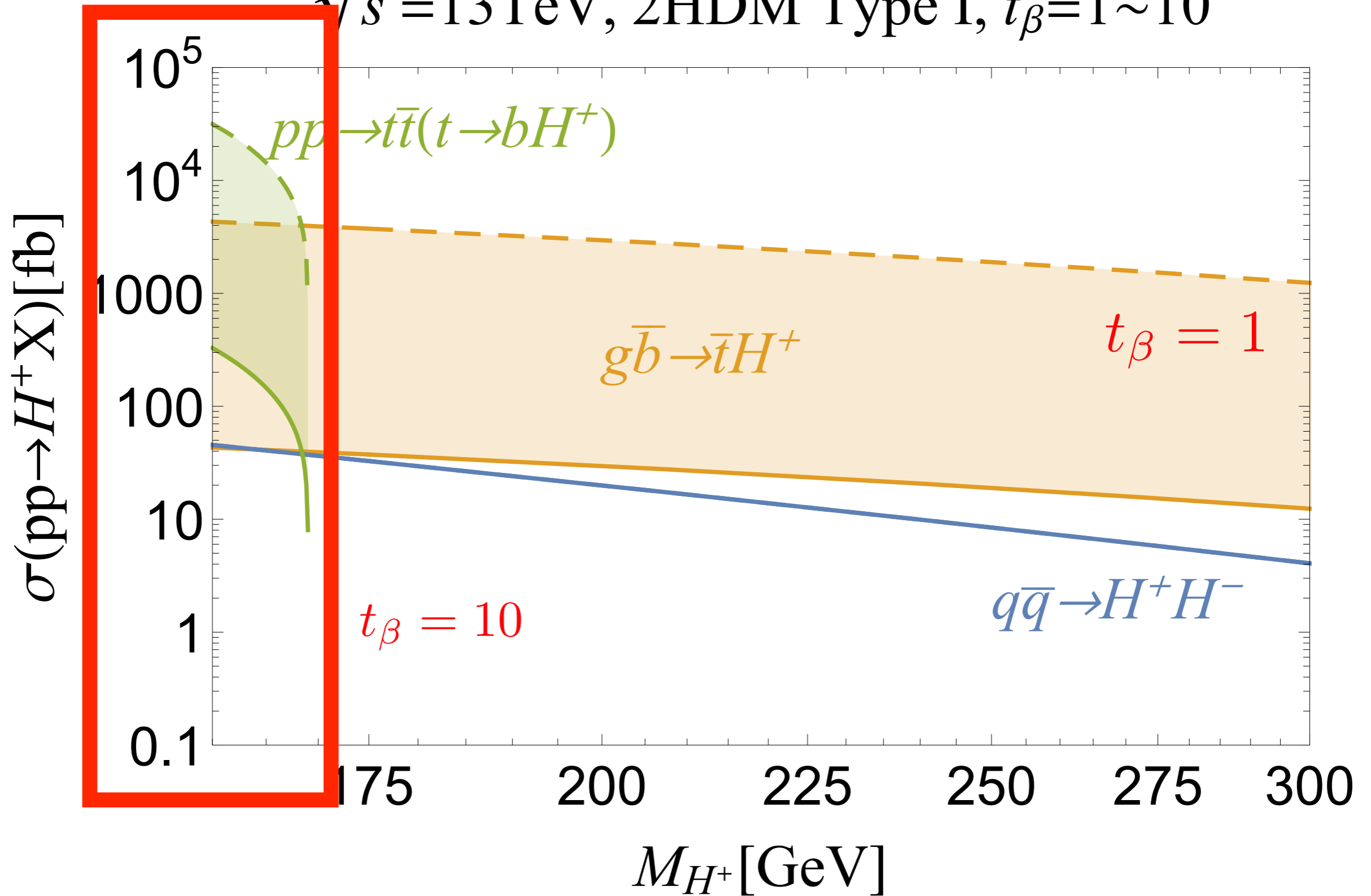
# High mass of the VLFs



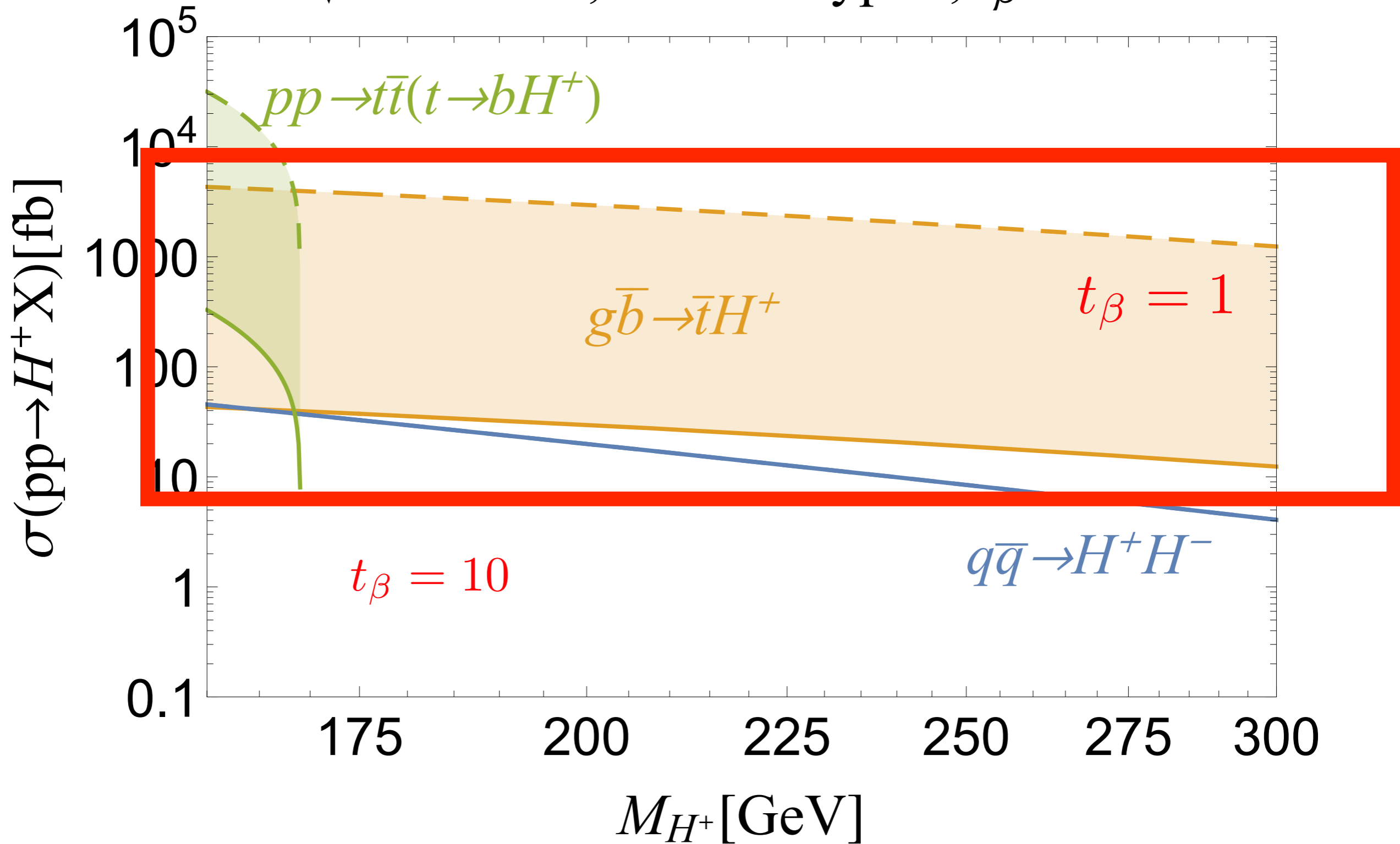


# Production of the charged Higgs boson

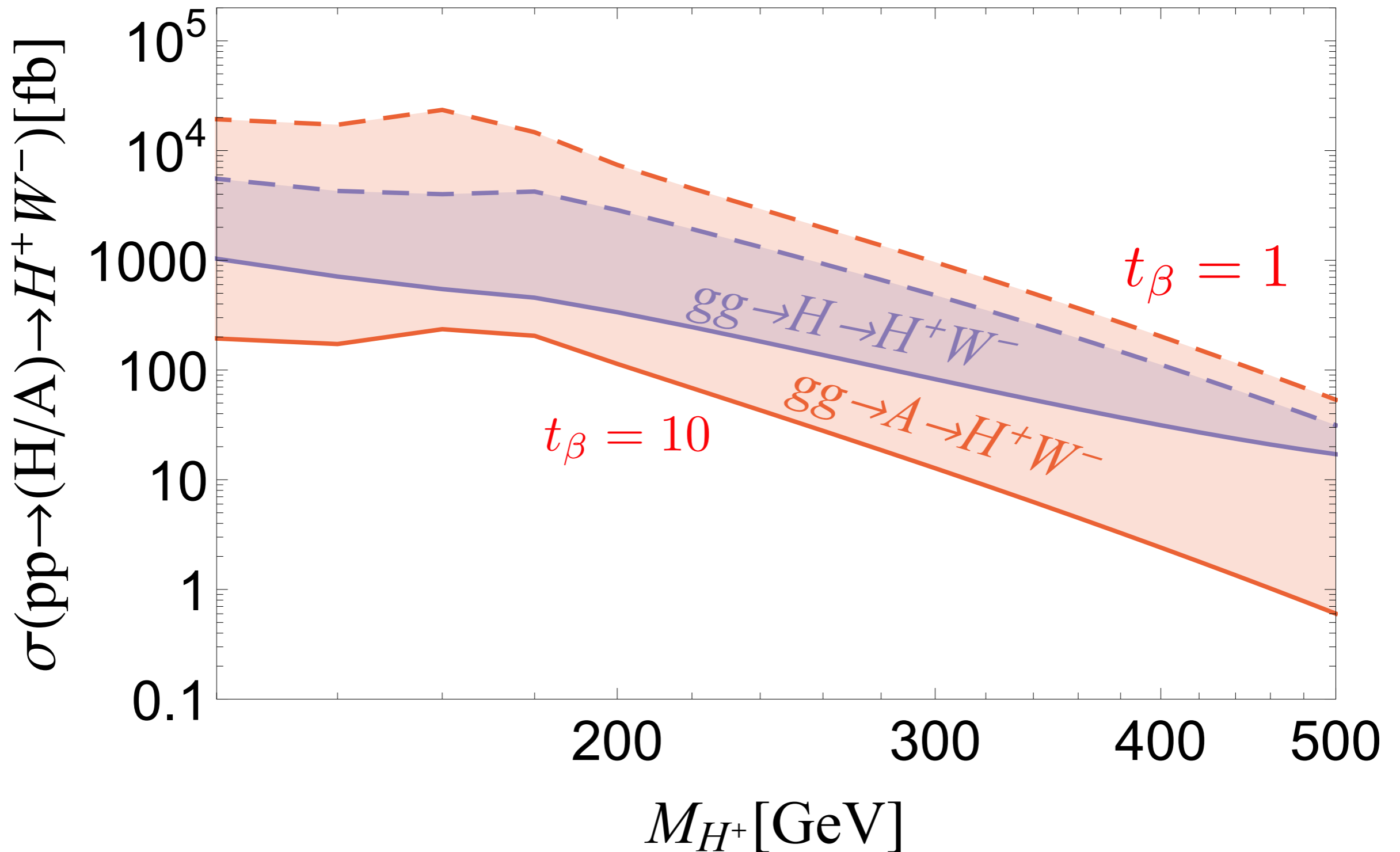
$\sqrt{s} = 13\text{TeV}$ , 2HDM Type I,  $t_\beta = 1 \sim 10$



$\sqrt{s} = 13\text{TeV}$ , 2HDM Type I,  $t_\beta = 1 \sim 10$

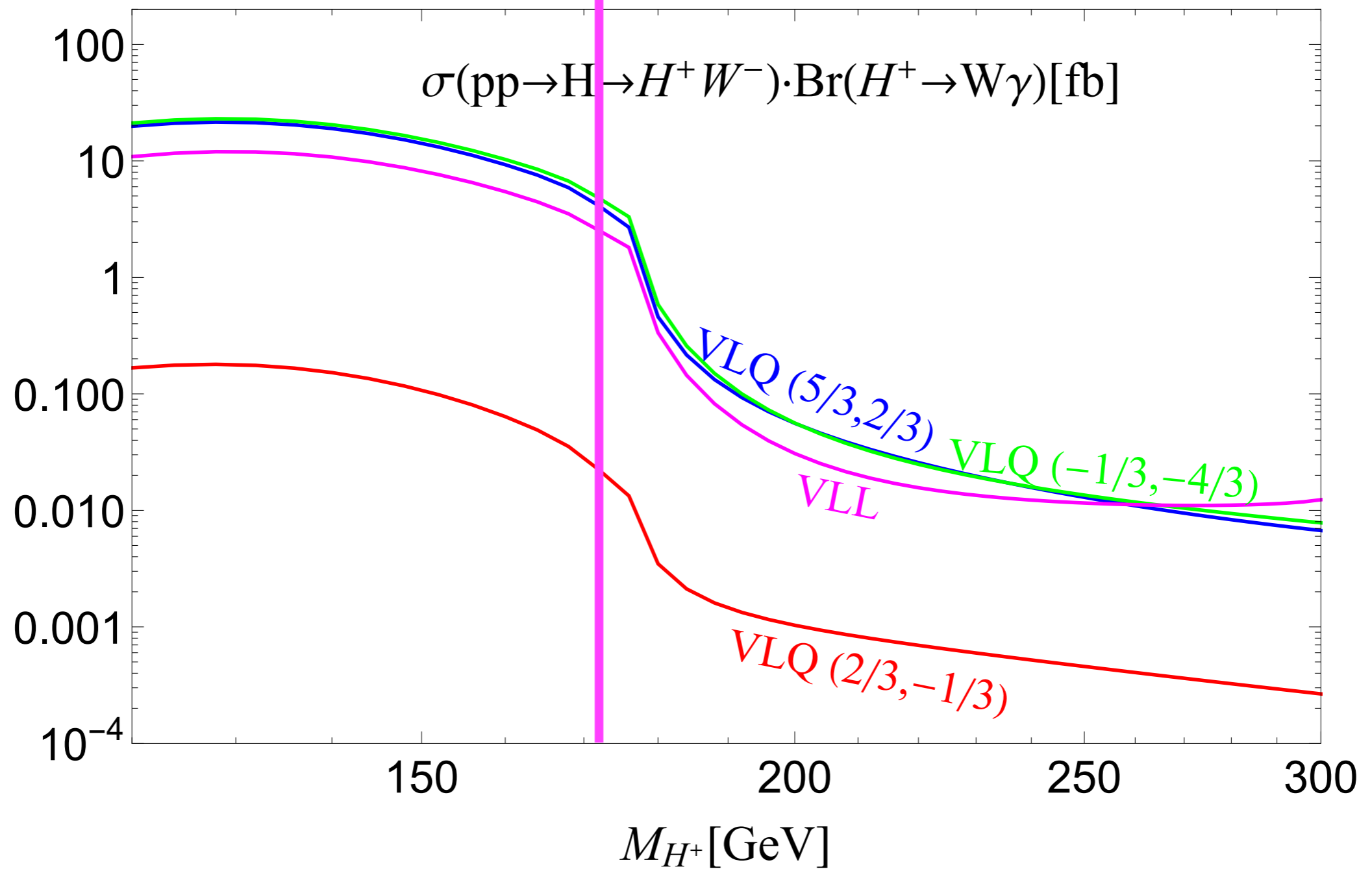


$\sqrt{s} = 13\text{TeV}, M_{H/A} = 2M_{H^+}, t_\beta = 1 \sim 10,$



**NOTE: Negligible VLQ contributions**

$\sqrt{s} = 13\text{TeV}, M_H = 2M_{H^+}, t_\beta = 10$

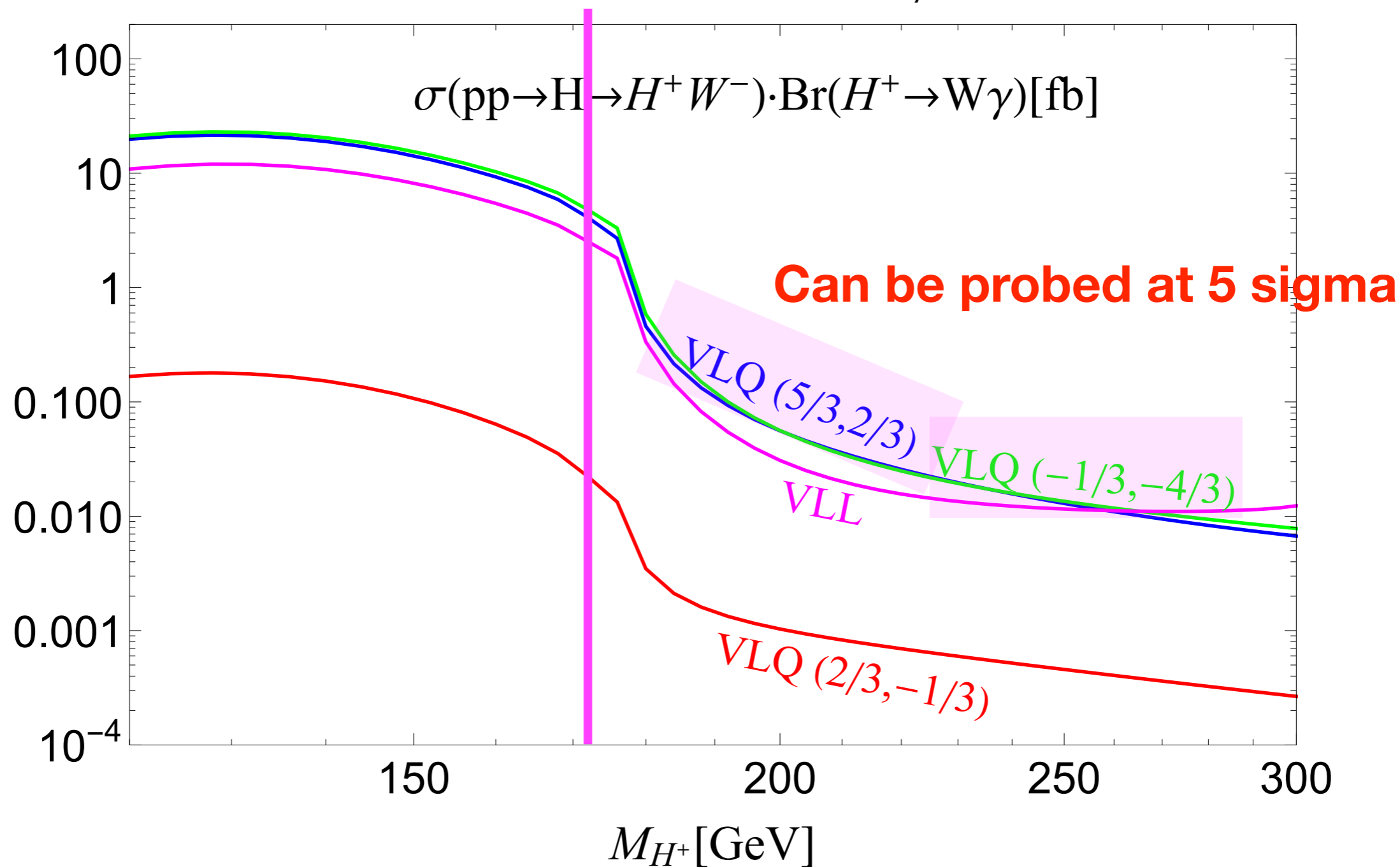


$\sigma_{\text{SM}}(pp \rightarrow W^+ W^- \gamma) = 14 \text{ fb}$

with  $|M_{W+\gamma}| < (170 \pm 10) \text{ GeV}$

# NOTE: No VLQ contributions to $gg \rightarrow A$

$$\sqrt{s} = 13 \text{ TeV}, M_H = 2M_{H^+}, t_\beta = 10$$



$$\sigma_{\text{SM}}(pp \rightarrow W^+ W^- \gamma) = 14 \text{ fb}$$

$$\text{with } |M_{W+\gamma}| < (170 \pm 10) \text{ GeV}$$

# Conclusions

- The charged Higgs boson with  $M_{H^\pm} \sim m_t$  is tricky to probe at the LHC.
- $H^\pm \rightarrow W^\pm \gamma$  can serve as a complementary channel.
- The branching ratio can be enhanced in a 2HDM with the VLFs.