

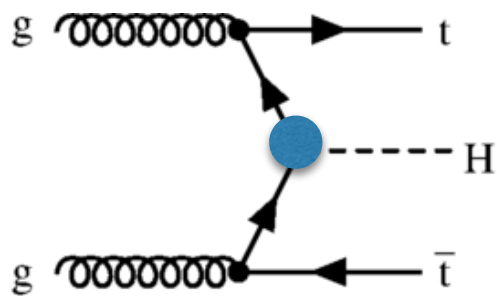
# **Limiting Top-Higgs Interaction and Higgs Width from multi-Top Productions**

Yandong Liu

Beijing Normal University

Based on Phys.Rev. D95 (2017) no.5, 053004 and arXiv: 1901.04567

# Observation of **Higgs-Top interaction** and **Higgs width**



Direct evidence on  
**Higgs-Top interaction**

$$\mu_{ttH} = 0.96^{+0.34}_{-0.31}$$

CMS-PAS-HIG-18-019

**Size, CP-phase**

## Higgs-boson width

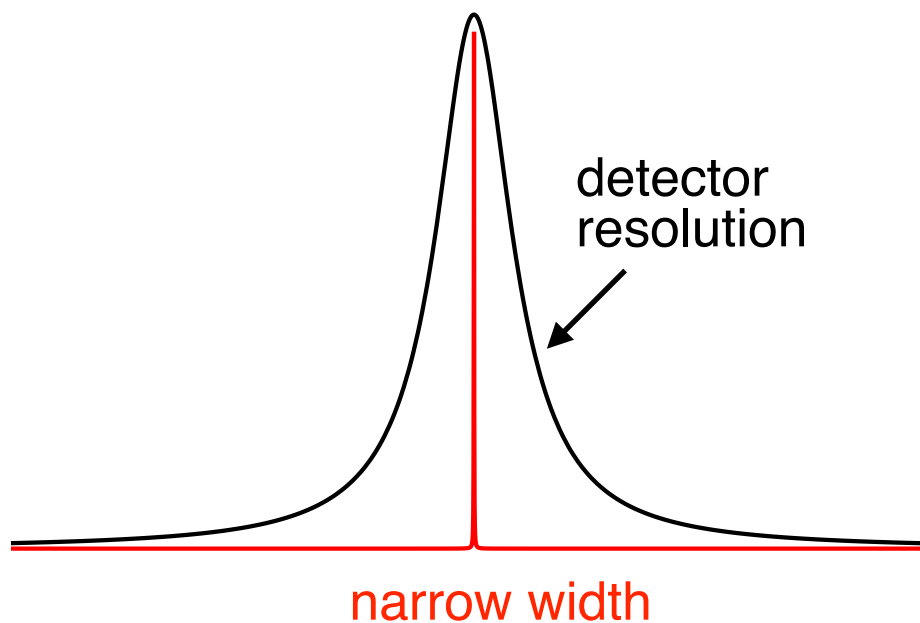
$$\begin{cases} \Gamma_H > \Gamma_H^{\text{SM}} \\ \Gamma_H < \Gamma_H^{\text{SM}} \end{cases}$$

**Invisible decay, scalar extension, ...**

**Scalar mixing, composite Higgs ...**

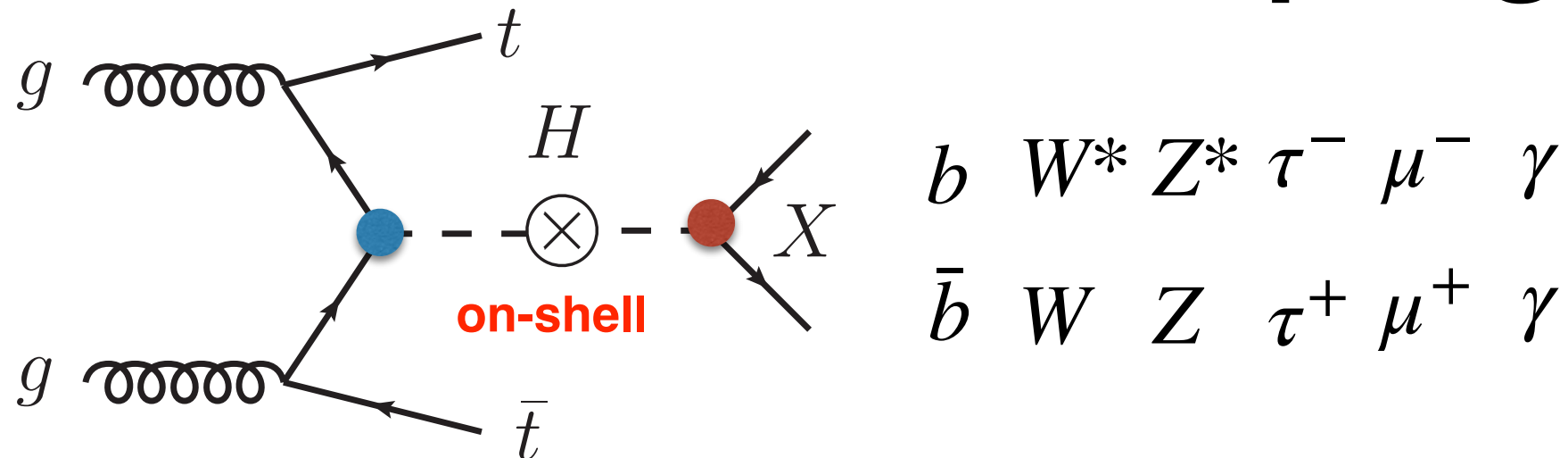
$$\Gamma_H^{\text{SM}} = 4 \text{ MeV}$$

$$\frac{\Gamma_H^{\text{SM}}}{m_H} = 0.000032$$



One can only obtain  
a range but not precise  
value of Higgs with

# Top-quark Yukawa coupling



Narrow width approximation

$$\hat{\sigma} = \sigma(gg \rightarrow t\bar{t}H) \times \frac{\Gamma(H \rightarrow X)}{\Gamma_H} = \frac{\kappa_t^2 \kappa_X^2}{\Gamma_H / \Gamma_H^{\text{SM}}} \hat{\sigma}_{\text{SM}}$$

$$\kappa_t = \frac{y_t}{y_t^{\text{SM}}}$$

$$\kappa_X = \frac{y_X}{y_X^{\text{SM}}}$$

signal strength  $\mu \equiv \frac{\hat{\sigma}}{\hat{\sigma}_{\text{SM}}} = \frac{\kappa_t^2 \kappa_X^2}{\Gamma_H / \Gamma_H^{\text{SM}}} \xrightarrow[\kappa_X = 1]{\Gamma_H = \Gamma_H^{\text{SM}}} \mu = \kappa_t^2$

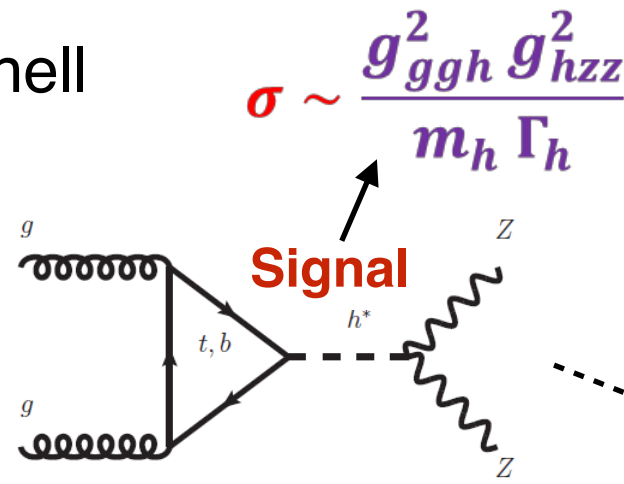
Higgs width affects all the Higgs measurements.

**Q1: can we determine  $\kappa_t$  without those assumptions?**

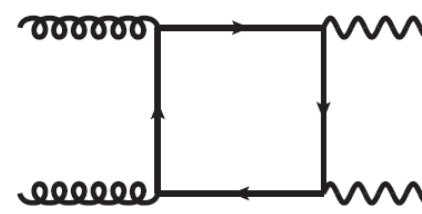
# Higgs boson width measurement

Caola, Melnikov (2013)

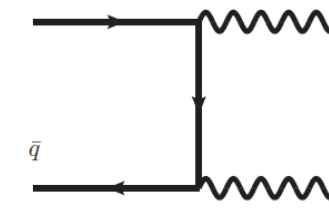
Higgs on-shell production



**Background**

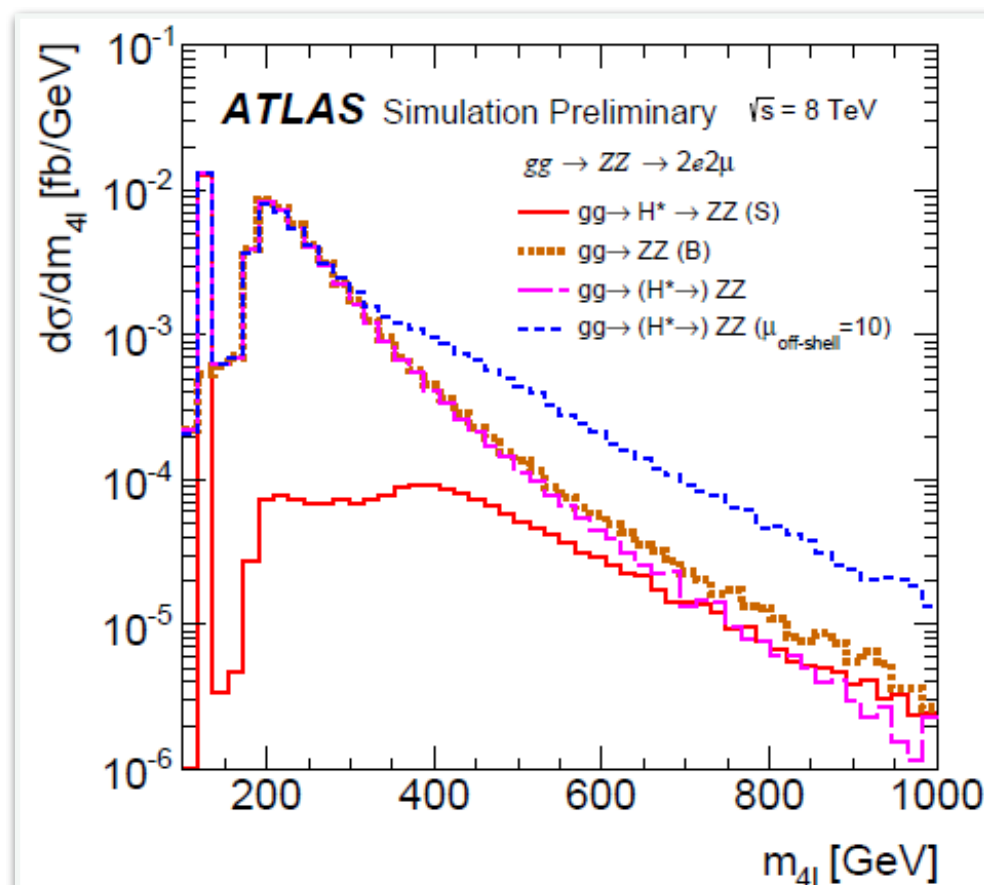


**Dominant background**



Higgs off-shell production

$$\frac{d\sigma}{dM_{ZZ}^2} \sim \frac{g_{ggh}^2 g_{hzz}^2}{(M_{ZZ}^2 - m_h^2)^2} |M_1|^2 + \frac{g_{ggh} g_{hzz}}{(M_{ZZ}^2 - m_h^2) M_{ZZ}^2} |M_1 M_2^*|$$



On-shell versus off-shell measurements of signal strength



a significant sensitivity to Higgs width

# Recent measurements of Higgs width

## Direct measurements:

CMS, 1706.09936  
(13TeV, 35.9fb<sup>-1</sup>)

$gg \rightarrow H \rightarrow ZZ^* \rightarrow 4\ell$

$$\Gamma_H < 1.10 \text{ GeV}$$

CMS, 1605.02329  
(7+8TeV)

$gg \rightarrow H \rightarrow WW^* \rightarrow 2\ell + \text{MET}$

$$\Gamma_H < 13 \text{ MeV}$$

ATLAS, 1808.01191  
(13TeV, 36.1fb<sup>-1</sup>)

$$\Gamma_H < 14.4 \text{ MeV}$$

## Indirect measurement through invisible decay:

ATLAS, 1809.06682 (13TeV, 36.1fb<sup>-1</sup>)

$$\text{Br}(H \rightarrow \text{inv}) \leq 0.37 \equiv \text{Br}_{\text{inv}}^{\text{Max}} \xrightarrow{\Gamma_H = \Gamma_H^{\text{known}} + \Gamma_H^{\text{inv}}} \Gamma_H \leq \frac{\Gamma_H^{\text{Known}}}{1 - \text{Br}_{\text{inv}}^{\text{Max}}}$$

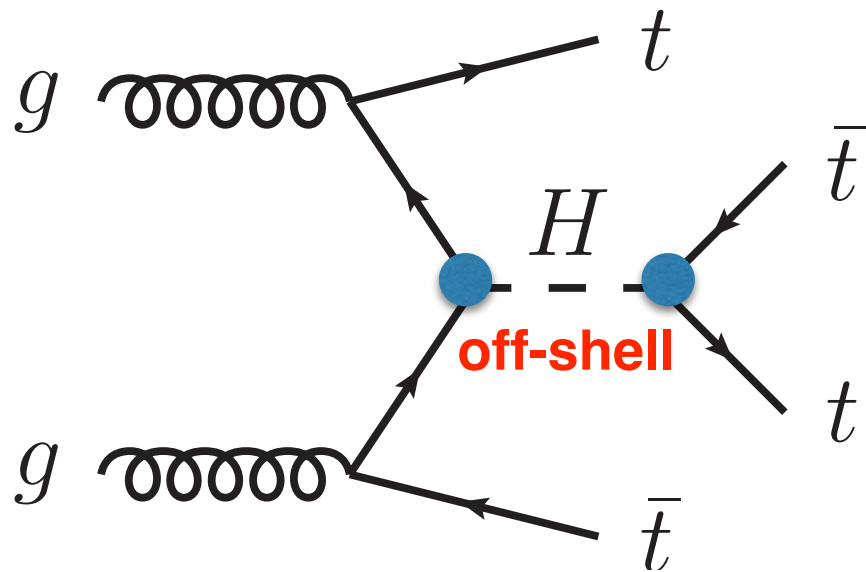
$$\downarrow \Gamma_H^{\text{Known}} = \Gamma_H^{\text{SM}}$$

$$\Gamma_H \leq \frac{\Gamma_H^{\text{SM}}}{1 - \text{Br}_{\text{inv}}^{\text{Max}}} = 1.6\Gamma_H^{\text{SM}} = 6.4 \text{ MeV}$$

Q2: alternative way to measure Higgs width?

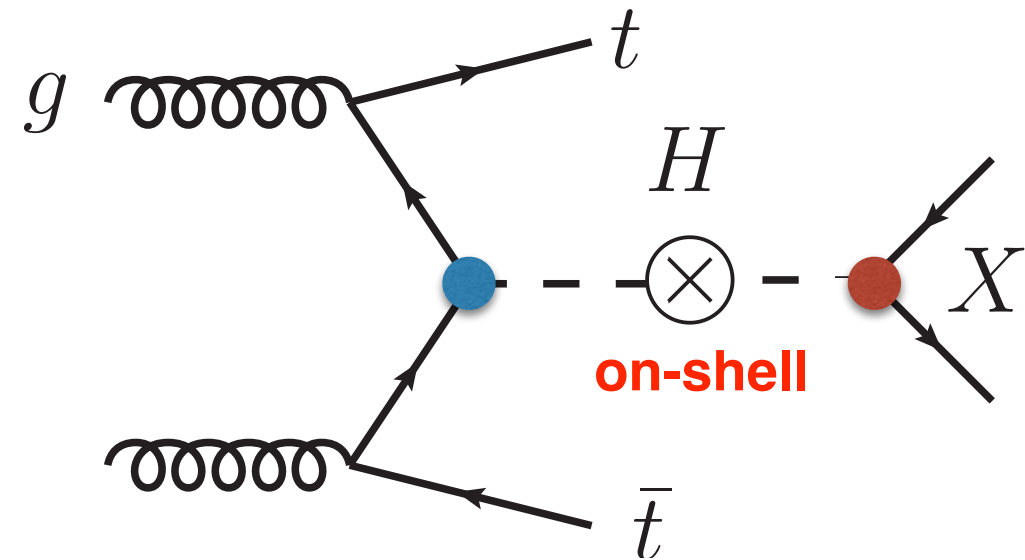
# Four top-quark production

Cao, Chen, YDL  
PRD95 (2017) 053004



$$\hat{\sigma}(pp \rightarrow t\bar{t}H \rightarrow t\bar{t}t\bar{t})$$

$$\propto \kappa_t^4 \times \hat{\sigma}(pp \rightarrow t\bar{t}H \rightarrow t\bar{t}t\bar{t})_{\text{SM}}$$

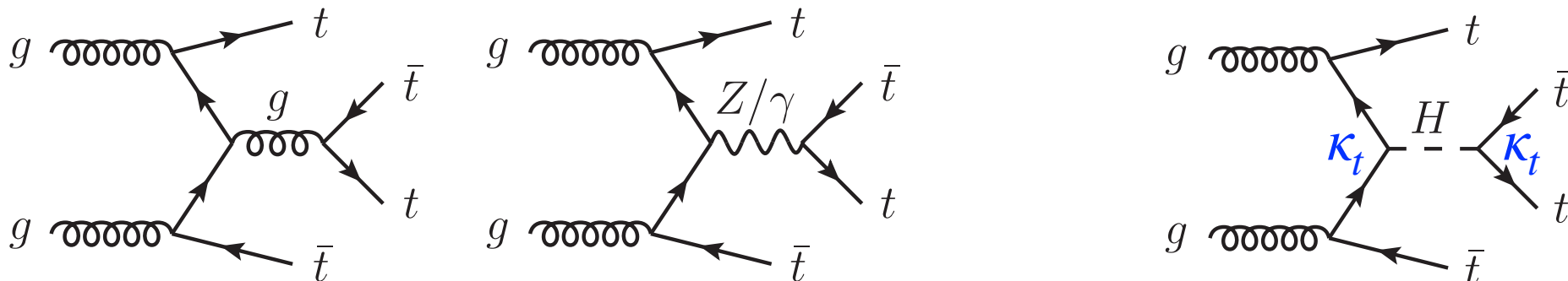


$$\hat{\sigma}(pp \rightarrow t\bar{t}H \rightarrow t\bar{t}X)$$

$$\propto \underbrace{\frac{\kappa_t^2 \kappa_X^2}{\Gamma_H / \Gamma_H^{\text{SM}}}}_{\mu_{t\bar{t}H}^X} \times \hat{\sigma}(pp \rightarrow t\bar{t}H \rightarrow t\bar{t}X)_{\text{SM}}$$

$$\mu_{t\bar{t}H}^X \equiv \frac{\kappa_t^2 \kappa_X^2}{\Gamma_H / \Gamma_H^{\text{SM}}} = \frac{\kappa_t^2 \kappa_X^2}{R_\Gamma} \xrightarrow{\kappa_X \simeq 1} \frac{\kappa_t^2}{R_\Gamma} = \mu_{t\bar{t}H}^X$$

# Measuring $\kappa_t$ from four top-quark production



$$\sigma(t\bar{t}t\bar{t}) = \underbrace{\sigma^{\text{SM}}(t\bar{t}t\bar{t})_{g/Z/\gamma}}_{\text{LO}} + \kappa_t^2 \underbrace{\sigma_{\text{int}}^{\text{SM}}}_{\text{NLO}} + \kappa_t^4 \underbrace{\sigma^{\text{SM}}(t\bar{t}t\bar{t})_H}_{\text{NLO}}$$

**LO**

8 TeV	1.344	-0.224	0.171	in unit of fb
13 TeV	9.997	-1.547	1.108	

$\sigma_g^{\text{SM}} = 1.216$        $\sigma_{g+Z/\gamma}^{\text{SM}} = -0.262$   
 $\sigma_{Z/\gamma}^{\text{SM}} = 0.412$

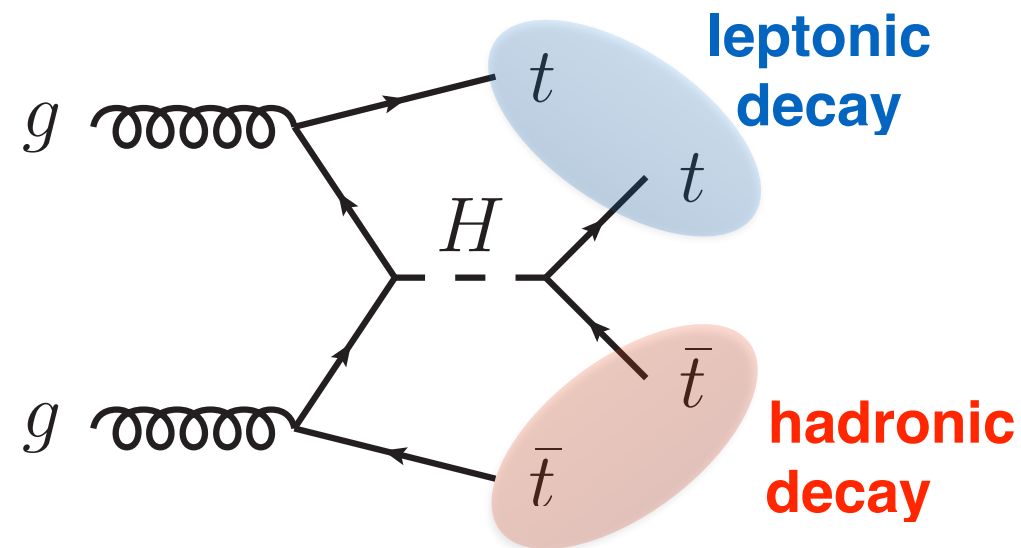
**NLO corrections:**  
 Bevilacqua, Worek (2012)  
 Alwall et al (2014)  
 Frederix, Pagani, Zaro (2017)

$K_{\text{factor}} = 1.58$

**significant cancellations between strong and weak interactions**  
**→ large scale dependence**

# Collider simulation

Event Topology: **same-sign charged leptons plus multi-jet (b-jet)**



Event selections:

$$p_T^{j,l} \geq 20\text{GeV}$$

$$|\eta^{j,l}| < 2.5$$

$$N_{l^\pm} = 2$$

$$N_{b\text{-jets}} \geq 3$$

	<b>13-14TeV</b>	<b>27TeV</b>	<b>100TeV</b>
$N_{\text{jets}} \geq 5$		$N_{\text{jets}} \geq 6$	$N_{\text{jets}} \geq 6$
$\cancel{E}_T \geq 100\text{GeV}$		<b>150GeV</b>	150GeV
$M_T \geq 100\text{GeV}$			
$H_T \geq 700\text{GeV}$		<b>700GeV</b>	800GeV

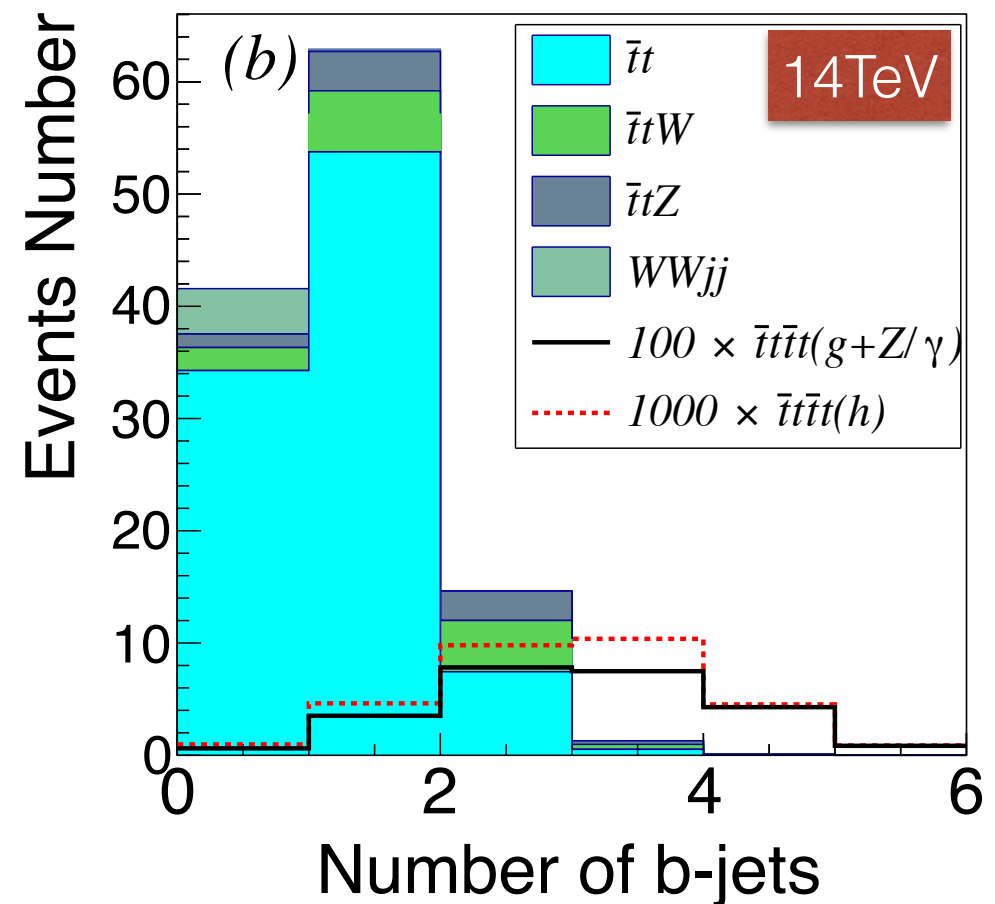
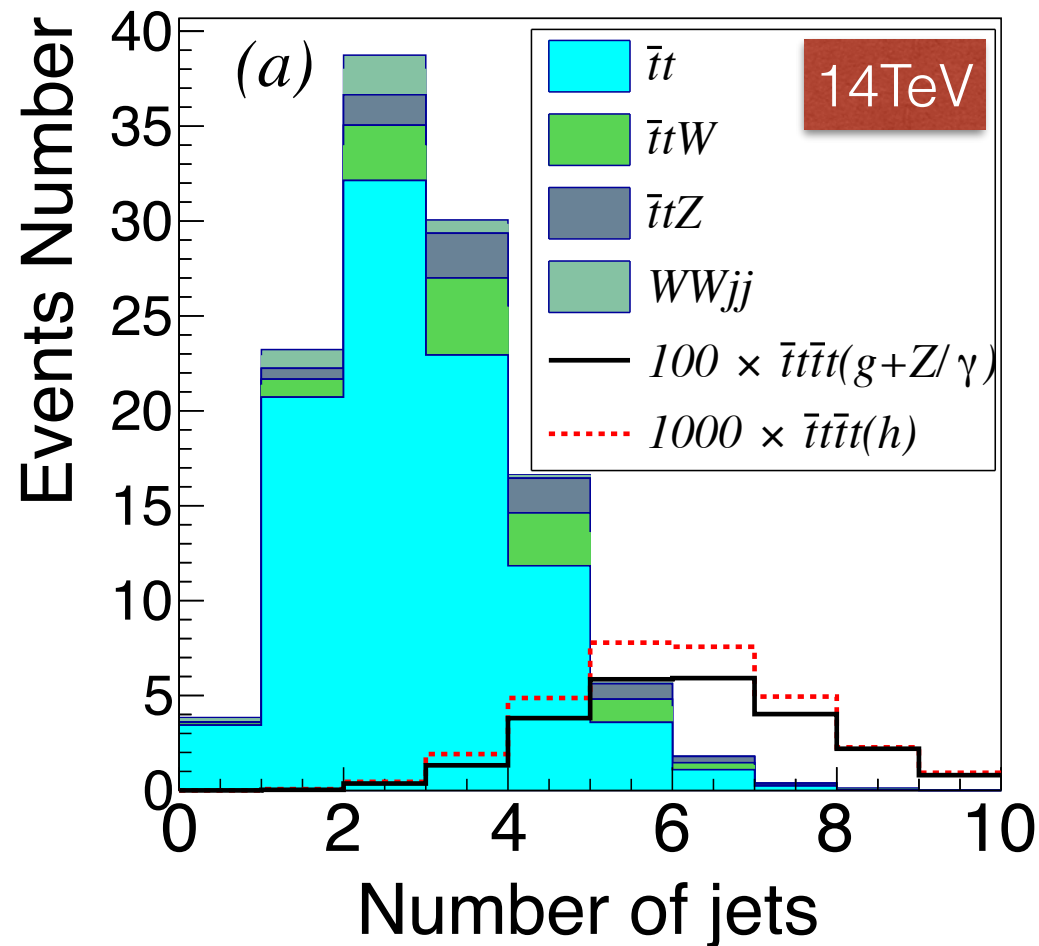
Backgrounds:  $t\bar{t}Z$ ,  $t\bar{t}W^\pm$ ,  $W^\pm W^\pm jj$ ,  $t\bar{t}$

$$K_F^{t\bar{t}W^+} = 1.22 \quad K_F^{t\bar{t}W^-} = 1.27 \quad K_F^{t\bar{t}Z} = 1.49 \quad K_F^{W^+W^+jj} = 0.9 \quad K_F^{t\bar{t}} = 1.4 \quad @14\text{TeV}$$



# Collider simulation

Event Topology: **same-sign charged leptons plus multi-jet (b-jet)**

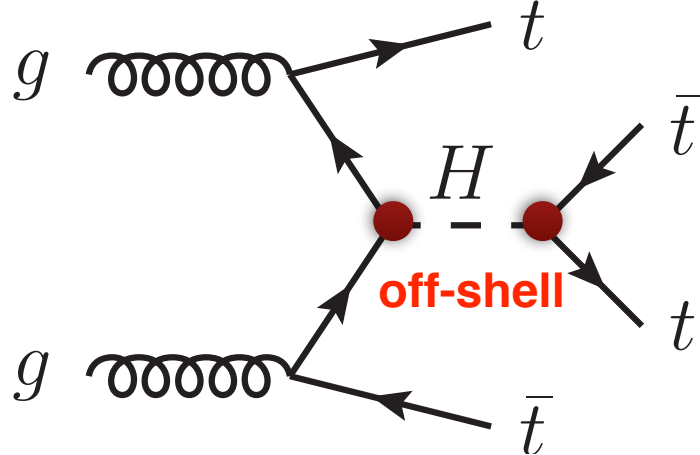


Not adequate to claim a discovery of  $\kappa_t$  at LHC but could set a bound

$$\kappa_t \leq 1.34 \text{ @ 13 TeV LHC (300fb}^{-1}\text{)}$$

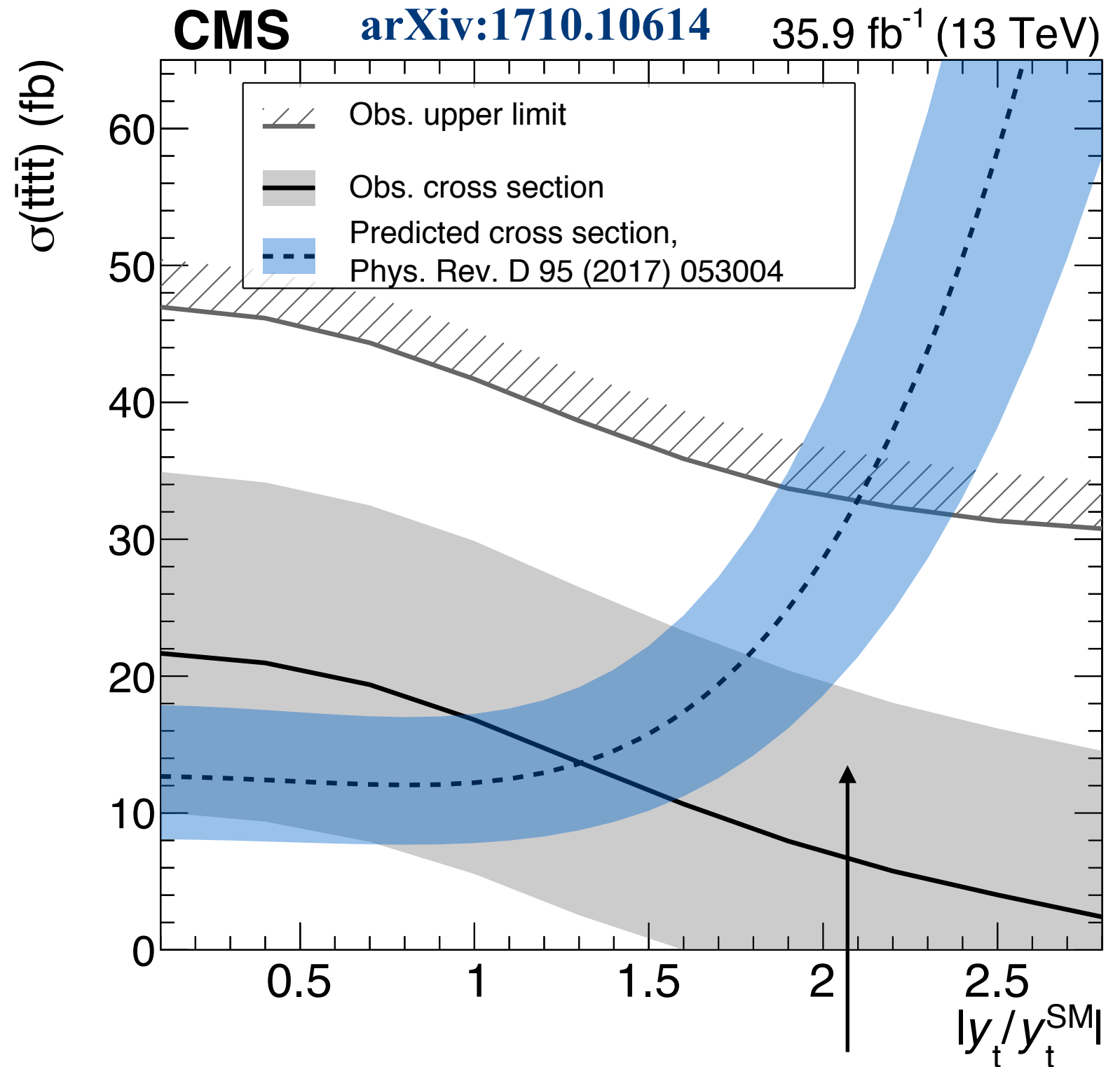
# Sizing up top-quark interaction with Higgs

Four-top production



Cao, Chen, YDL  
PRD95 (2017) 053004

No assumptions  
made on how  
Higgs-boson decays



$$y_t/y_t^{\text{SM}} \leq 2.1$$

$$\frac{\kappa_t^2}{R_\Gamma} = \mu_{t\bar{t}H} \quad \text{assume } \kappa_X \simeq 1 \text{ and invisible width}$$

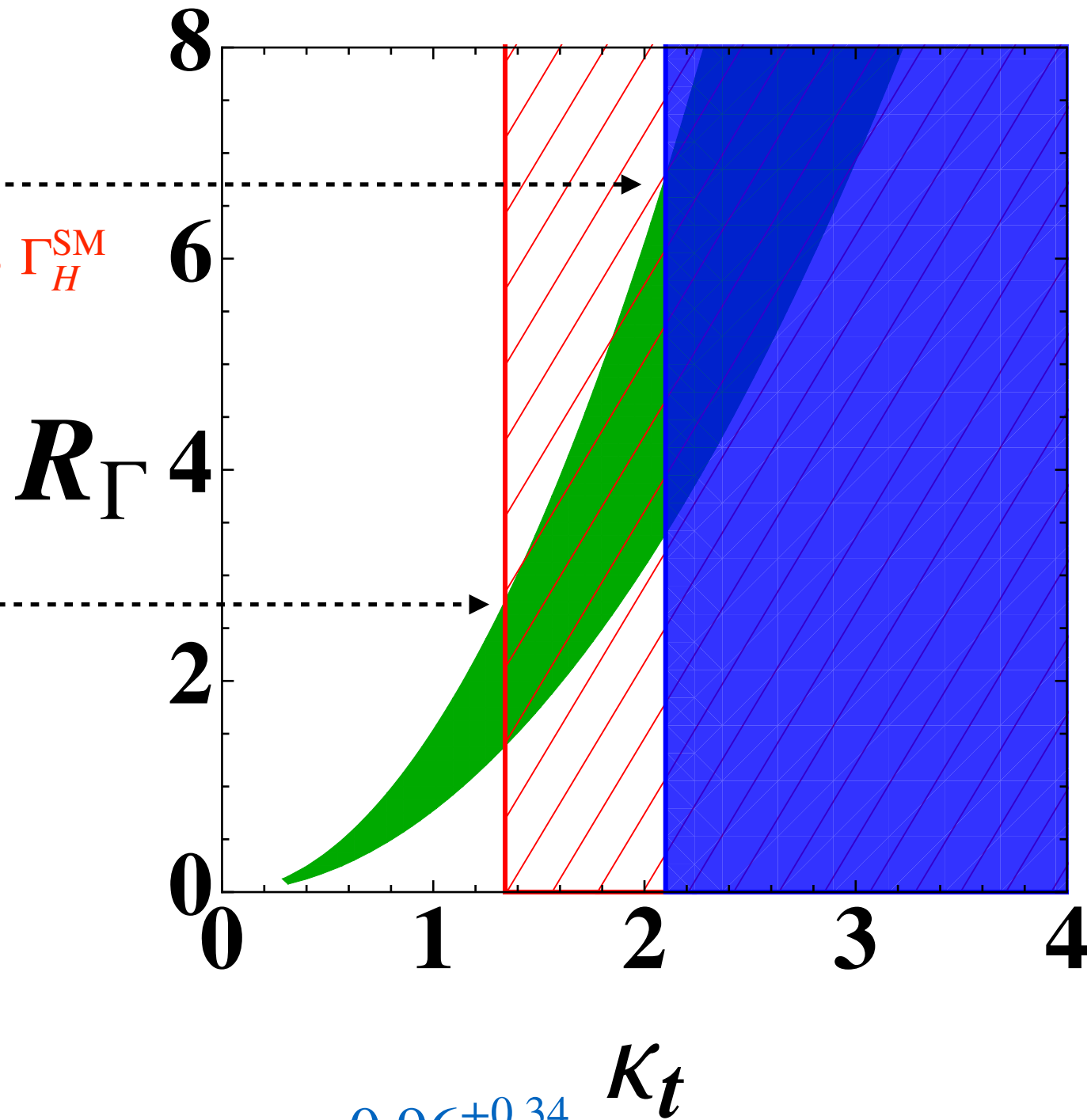
**13TeV LHC  
(35.9fb<sup>-1</sup>)**  
 $\kappa_t \leq 2.1$

**13TeV LHC  
(300fb<sup>-1</sup>)**  
 $\kappa_t \leq 1.34$

$$\Gamma_H \leq 6.8 \Gamma_H^{\text{SM}}$$

$$\Gamma_H \leq 2.8 \Gamma_H^{\text{SM}}$$

$\sim 10\text{MeV}$



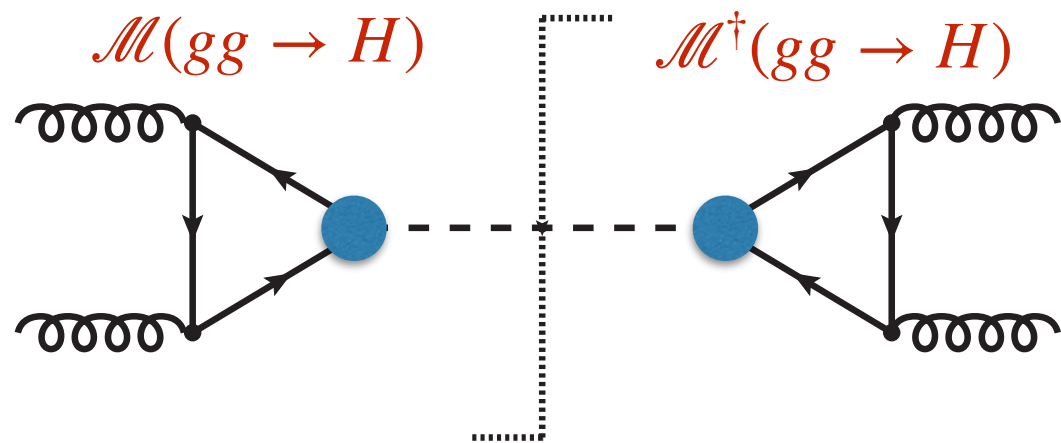
$$\mu_{t\bar{t}H} = 0.96^{+0.34}_{-0.31}$$

CMS-PAS-HIG-18-019

# Q3: CP property of top-Higgs interaction

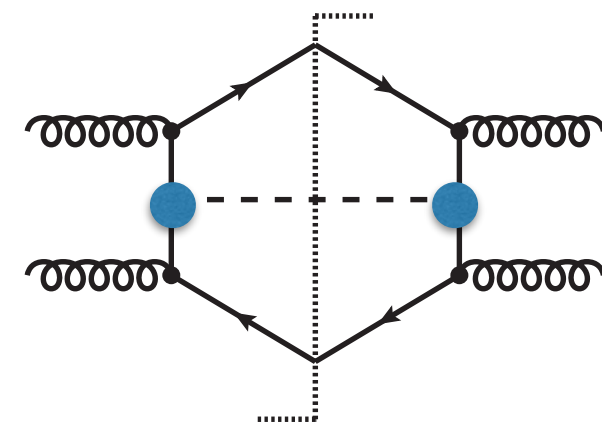
$$\mathcal{L}_{Ht\bar{t}} = -\frac{m_t}{v} H \bar{t} (a_t + i b_t \gamma_5) t$$

Boudjema, Godbole, Guadagnoli, Mohan,  
1501.03157



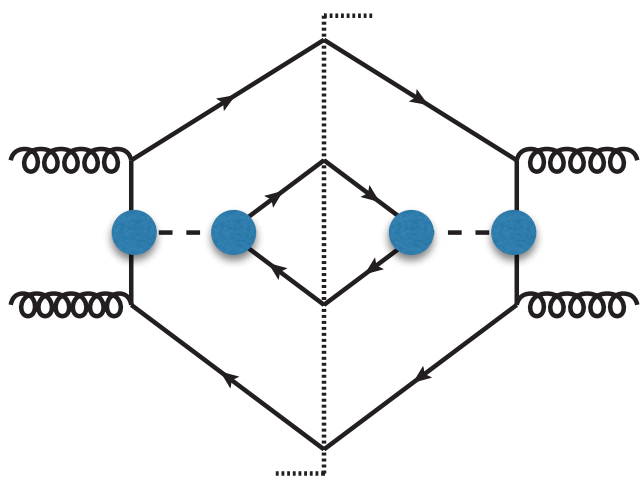
$$\frac{\sigma(gg \rightarrow H)}{\sigma(gg \rightarrow H)_{\text{SM}}} \sim a_t^2 + 2.26 b_t^2$$

pseudo-scalar dominates



$$\frac{\sigma(gg \rightarrow t\bar{t}H)}{\sigma(gg \rightarrow t\bar{t}H)_{\text{SM}}} \sim a_t^2 + 0.46 b_t^2 \quad @13\text{TeV}$$

scalar dominates



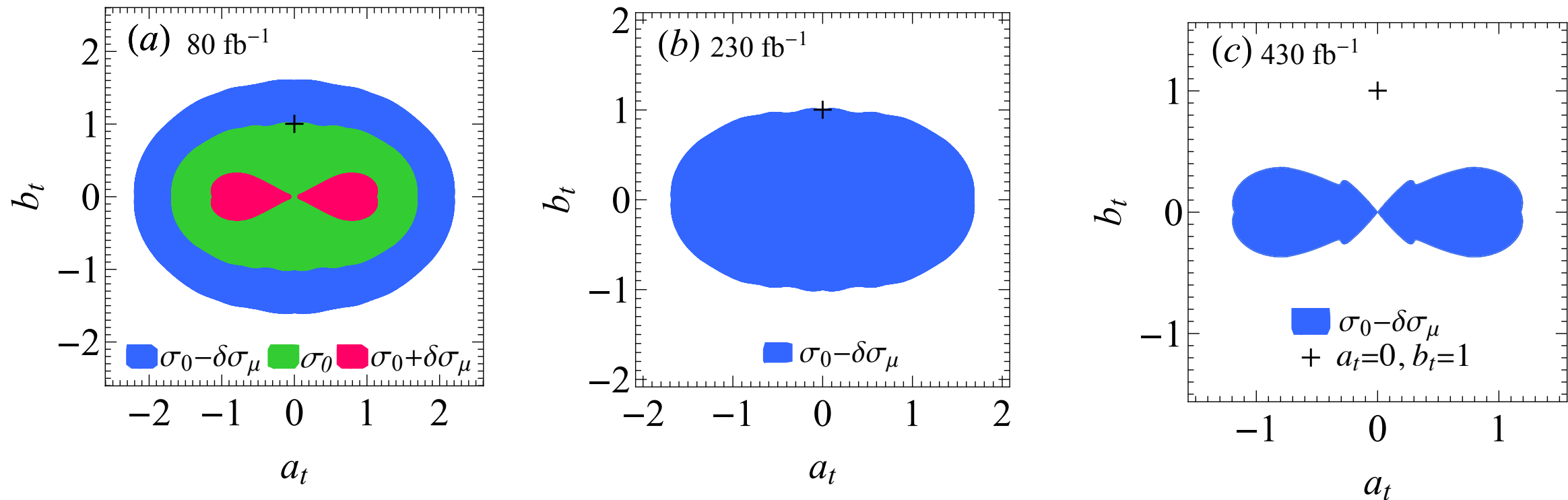
CP-odd  
( $a_t=0, b_t=1$ )

$$\sigma(t\bar{t}t\bar{t}) = 9.997 + 2.807 \times b_t^2 + 1.788 \times b_t^4$$

CP-even  
( $a_t=1, b_t=0$ )

$$\sigma(t\bar{t}t\bar{t}) = 9.997 - 1.547 \times a_t^2 + 1.108 \times a_t^4$$

# Potential of four-top measurements

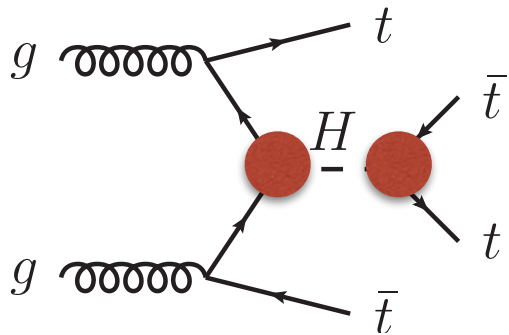


**13TeV**  **$230 \text{ fb}^{-1}$ : excludes a pure CP-odd Htt coupling with  $b_t=1$**   
 **$430 \text{ fb}^{-1}$ : excludes a pure CP-odd Htt coupling entirely ( $-5 < b_t < 5$ )**

even considering lower value of production rate  $\delta\sigma_\mu = 0.5\sigma_0$

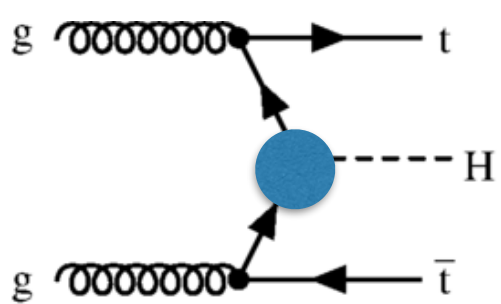
# Global analysis of multi-top productions

13TeV LHC



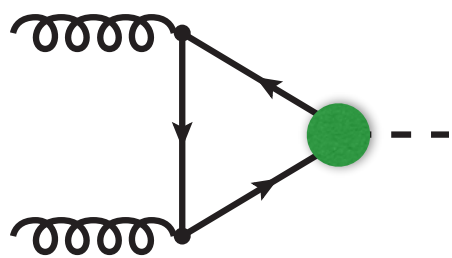
$$\sigma(t\bar{t}t\bar{t}) = 9.998 - 1.522a_t^2 + 2.883b_t^2 + 1.173a_t^4 + 2.713a_t^2b_t^2 + 1.827b_t^4$$

$$R_\Gamma = \Gamma_H / \Gamma_H^{\text{SM}}$$



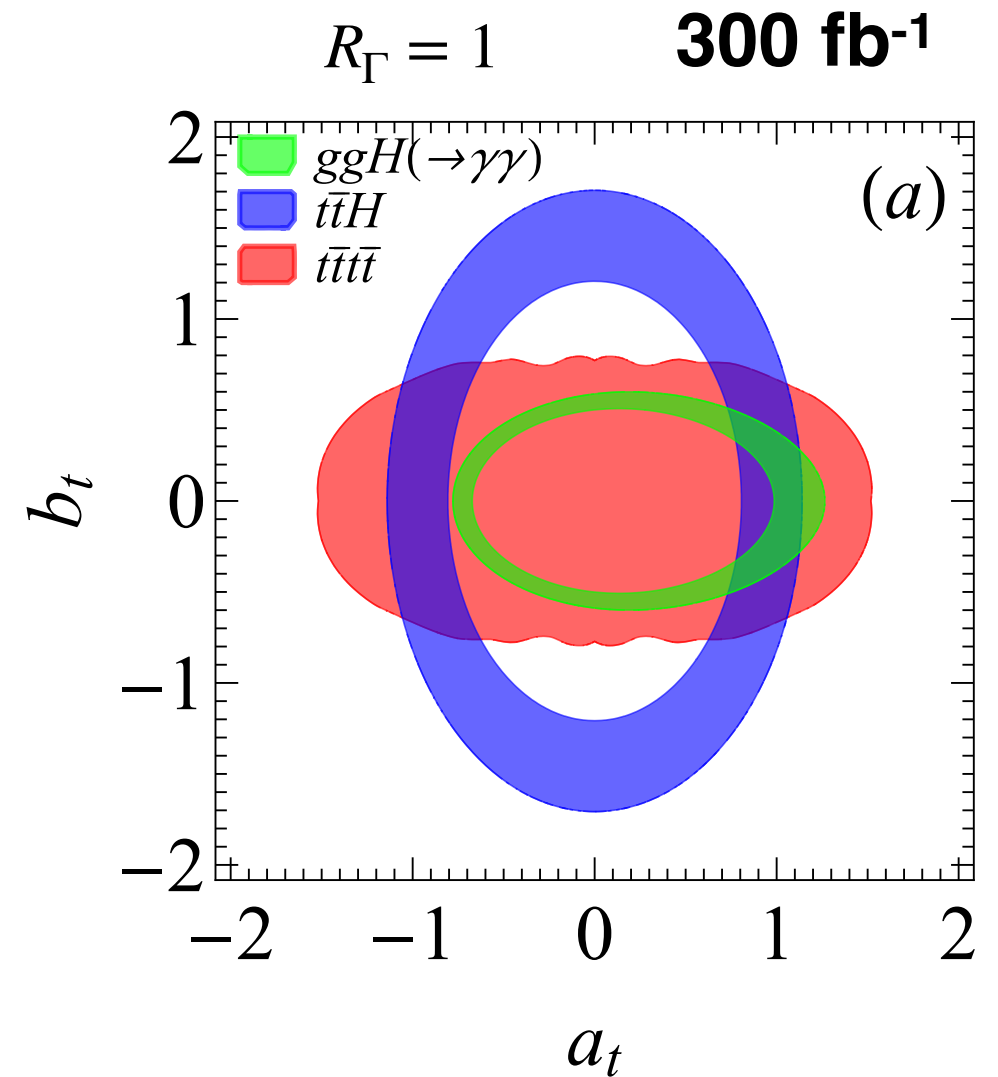
$$\frac{\sigma(gg \rightarrow t\bar{t}H)}{\sigma(gg \rightarrow t\bar{t}H)_{\text{SM}}} = (a_t^2 + 0.46b_t^2) \frac{1}{R_\Gamma}$$

$$\mu_{t\bar{t}H} = 0.96^{+0.34}_{-0.31}$$



$$\begin{aligned} & \frac{\sigma(gg \rightarrow H \rightarrow \gamma\gamma)}{\sigma(gg \rightarrow H \rightarrow \gamma\gamma)_{\text{SM}}} \\ &= (a_t^2 + 2.26b_t^2) \\ & \times \frac{0.035(-7.2 + 1.83a_t^2) + 0.27b_t^2}{R_\Gamma} \end{aligned}$$

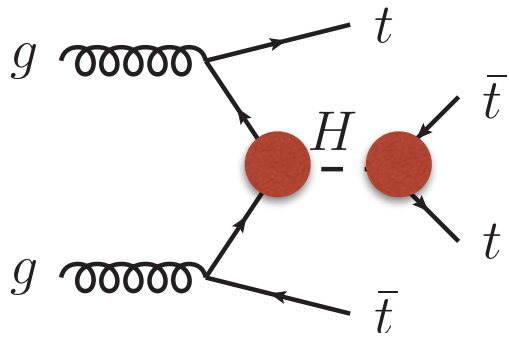
$$\mu_{gg \rightarrow H \rightarrow \gamma\gamma} = 1.16^{+0.21}_{-0.18}$$



$$\begin{aligned} 0.73 < a_t < 1.14 \\ -0.51 < b_t < 0.51 \end{aligned}$$

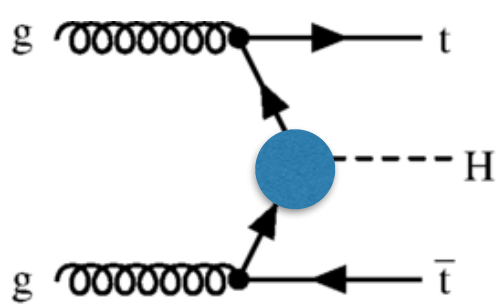
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13TeV LHC



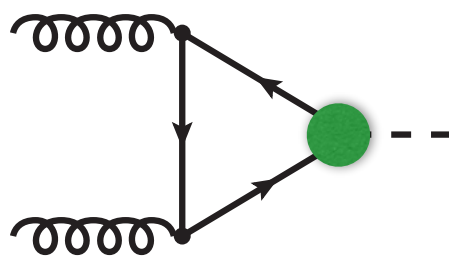
$$\sigma(t\bar{t}t\bar{t}) = 9.998 - 1.522a_t^2 + 2.883b_t^2 + 1.173a_t^4 + 2.713a_t^2b_t^2 + 1.827b_t^4$$

$$R_\Gamma = \Gamma_H / \Gamma_H^{\text{SM}}$$



$$\frac{\sigma(gg \rightarrow t\bar{t}H)}{\sigma(gg \rightarrow t\bar{t}H)_{\text{SM}}} = (a_t^2 + 0.46b_t^2) \frac{1}{R_\Gamma}$$

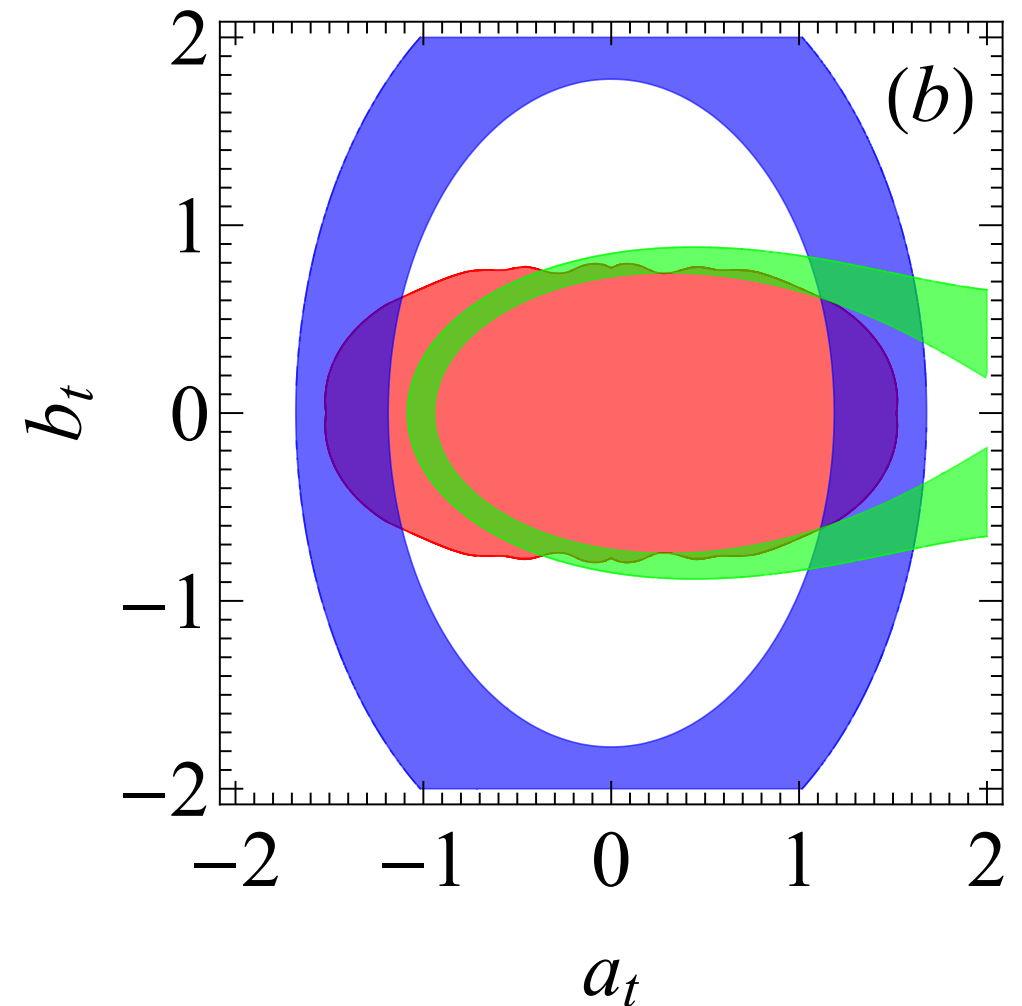
$$\mu_{t\bar{t}H} = 0.96^{+0.34}_{-0.31}$$



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$$\mu_{gg \rightarrow H \rightarrow \gamma\gamma} = 1.16^{+0.21}_{-0.18}$$

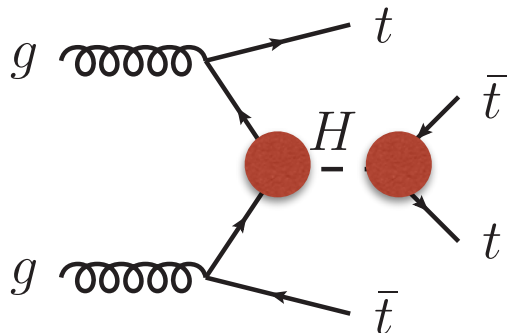
300 fb<sup>-1</sup>



$$R_\Gamma < 2.17$$

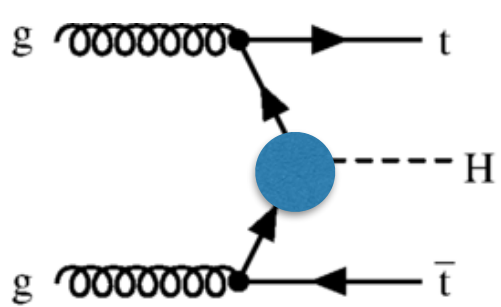
# Global analysis of multi-top productions

@ HL-LHC



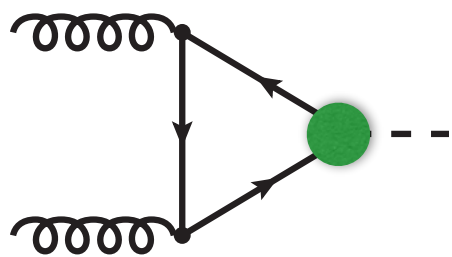
$$\sigma(t\bar{t}t\bar{t}) = 9.998 - \frac{1.522a_t^2 + 2.883b_t^2 + 1.173a_t^4 + 2.713a_t^2b_t^2 + 1.827b_t^4}{R_\Gamma}$$

assume  $\mu_{t\bar{t}t\bar{t}}^H = 1.00^{+0.50}_{-0.50}$



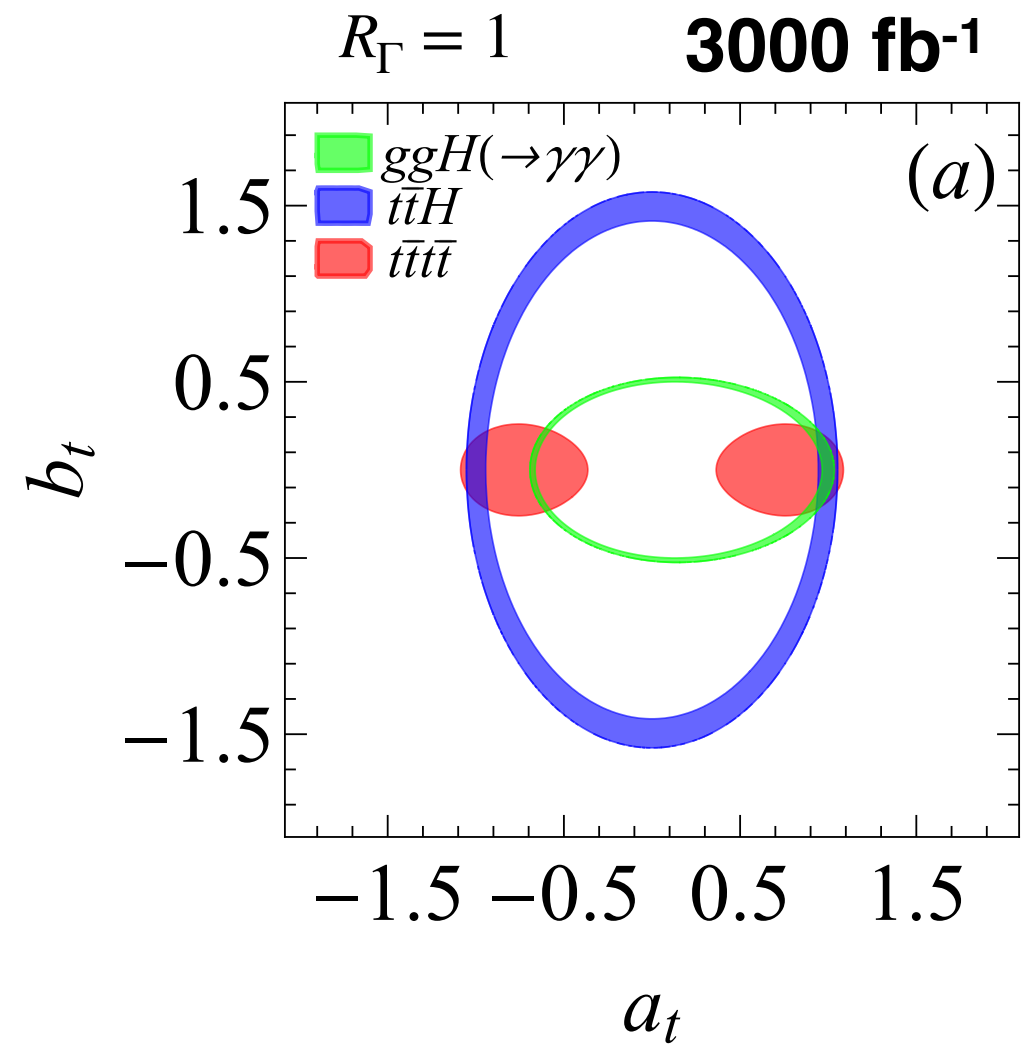
$$\frac{\sigma(gg \rightarrow t\bar{t}H)}{\sigma(gg \rightarrow t\bar{t}H)_{\text{SM}}} = (a_t^2 + 0.46b_t^2) \frac{1}{R_\Gamma}$$

$$\mu_{t\bar{t}H} = 1.00^{+0.11}_{-0.11}$$



$$\frac{\sigma(gg \rightarrow H \rightarrow \gamma\gamma)}{\sigma(gg \rightarrow H \rightarrow \gamma\gamma)_{\text{SM}}} = (a_t^2 + 2.26b_t^2) \times \frac{0.035(-7.2 + 1.83a_t)^2 + 0.27b_t^2}{R_\Gamma}$$

$$\mu_{gg \rightarrow H \rightarrow \gamma\gamma} = 1.00^{+0.05}_{-0.05}$$



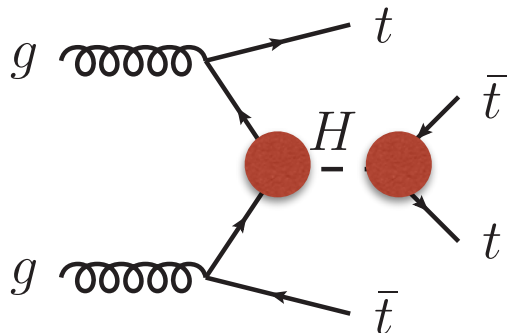
$$0.93 < a_t < 1.03$$

$$-0.22 < b_t < 0.22$$



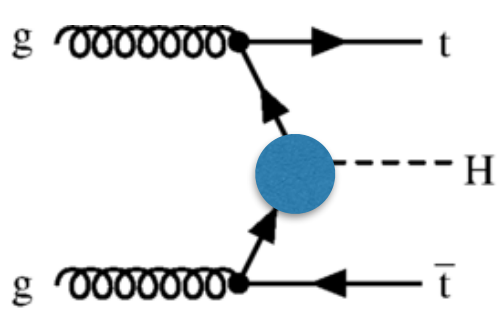
# Global analysis of multi-top productions

@ HL-LHC



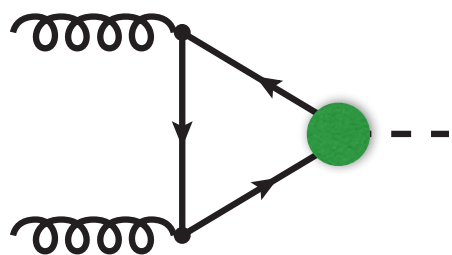
$$\sigma(t\bar{t}t\bar{t}) = 9.998 - 1.522a_t^2 + 2.883b_t^2 + 1.173a_t^4 + 2.713a_t^2b_t^2 + 1.827b_t^4$$

assume  $\mu_{t\bar{t}t\bar{t}}^H = 1.00^{+0.5}_{-0.5}$



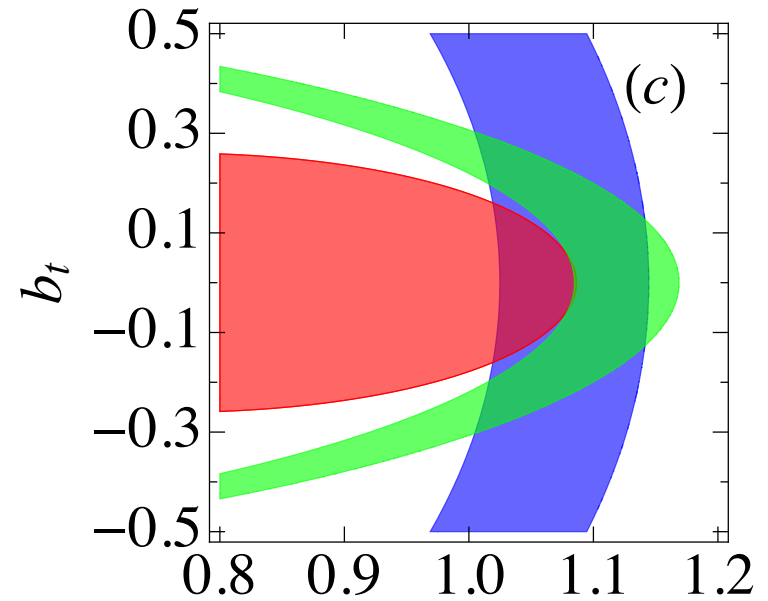
$$\frac{\sigma(gg \rightarrow t\bar{t}H)}{\sigma(gg \rightarrow t\bar{t}H)_{\text{SM}}} = (a_t^2 + 0.46b_t^2) \frac{1}{R_\Gamma}$$

$\mu_{t\bar{t}H} = 1.00^{+0.11}_{-0.11}$

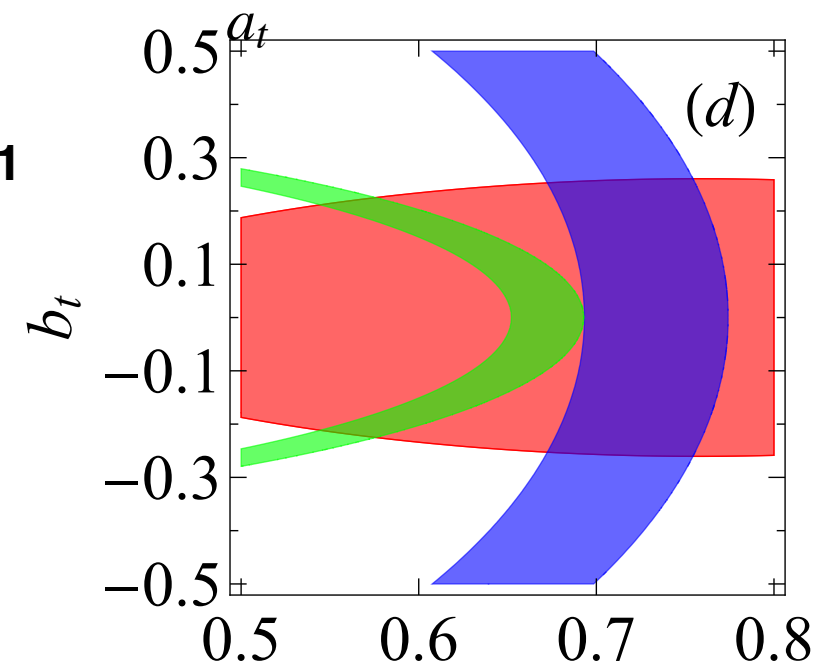


$$\frac{\sigma(gg \rightarrow H \rightarrow \gamma\gamma)}{\sigma(gg \rightarrow H \rightarrow \gamma\gamma)_{\text{SM}}} = (a_t^2 + 2.26b_t^2) \times \frac{0.035(-7.2 + 1.83a_t^2) + 0.27b_t^2}{R_\Gamma}$$

$\mu_{gg \rightarrow H \rightarrow \gamma\gamma} = 1.00^{+0.05}_{-0.05}$



3000 fb<sup>-1</sup>



$0.54 < R_\Gamma < 1.18$

$a_t$

# Summary

The four top-quark production can constrain top-quark Yukawa coupling without assumptions on Higgs boson width or decay branching ratios.

The four top-quark production is sensitive to the CP property of top-Higgs interaction.

$$\mathcal{L}_{Ht\bar{t}} = -\frac{m_t}{v} H\bar{t}(a_t + ib_t\gamma_5)t$$

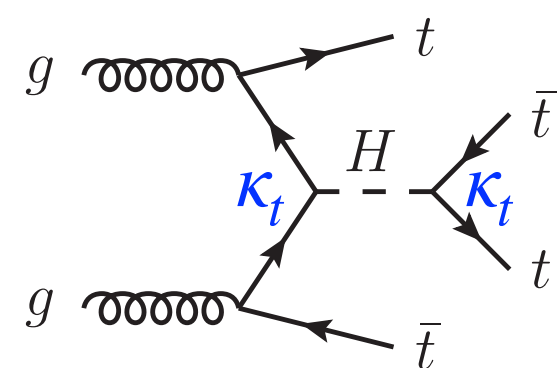
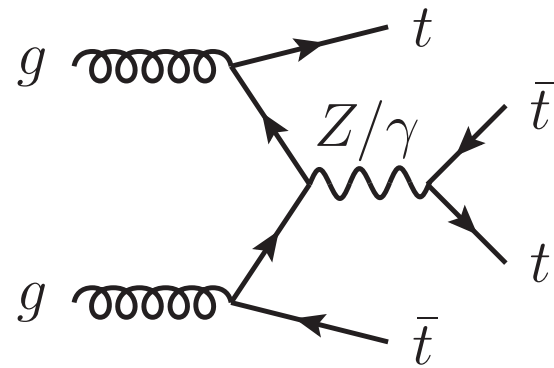
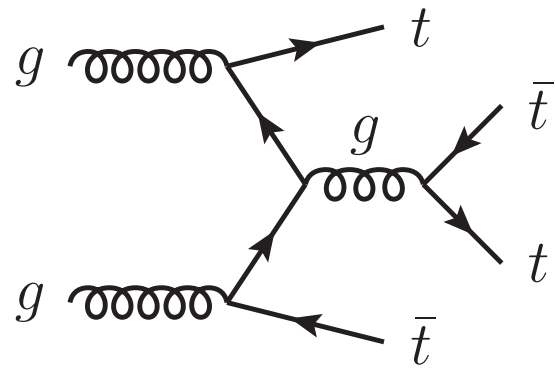
Global fitting of single-Higgs,  $t\bar{t}t\bar{t}$  and  $t\bar{t}h$  channels yields

$$0.93 < a_t < 1.13, \quad -0.22 < b_t < 0.22$$

$$0.54\Gamma_H^{\text{SM}} < \Gamma_H \leq 1.18\Gamma_H^{\text{SM}}$$

# Backup Slides

# Measuring $\kappa_t$ from four top-quark production



$$\sigma(t\bar{t}t\bar{t}) = \underbrace{\sigma^{\text{SM}}(t\bar{t}t\bar{t})_{g/Z/\gamma}} + \underbrace{\kappa_t^2 \sigma_{\text{int}}^{\text{SM}}}_{-1.3} + \underbrace{\kappa_t^4 \sigma^{\text{SM}}(t\bar{t}t\bar{t})_H}_{1}$$

**LO**

8 TeV	1.344	-0.224	0.171	in unit of fb
13 TeV	9.997	-1.547	1.108	
14 TeV	13.14	-2.007	1.515	
27 TeV	115.1	-15.57	11.73	
100 TeV	3276	-356.9	273.1	
Relative ratio	<b>8~12</b>	<b>-1.3</b>	<b>1</b>	

cancel out around SM  $\kappa_t = 1$