

# CP-violation at the LHC

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# Outline

- 🍪 A complex 2HDM
- 🍪 CP-violation in the bosonic Higgs couplings
- 🍪 CP-violation in the combination of Higgs decays
- 🍪 Some variables to probe CP-violation
- 🍪 CP-violation in the triple gauge boson couplings
- 🍪 CP-violation in the Yukawa couplings
- 🍪 CP-violation - a strange scenario
- 🍪 Conclusions

## A complex 2HDM

$$V = m_{11}^2 |\Phi_1|^2 + m_{22}^2 |\Phi_2|^2 - m_{12}^2 (\Phi_1^\dagger \Phi_2 + h.c.)$$

$$+ \frac{\lambda_1}{2} (\Phi_1^\dagger \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^\dagger \Phi_2)^2 + \lambda_3 (\Phi_1^\dagger \Phi_1) (\Phi_2^\dagger \Phi_2) + \lambda_4 (\Phi_1^\dagger \Phi_2) (\Phi_2^\dagger \Phi_1) + \frac{\lambda_5}{2} [(\Phi_1^\dagger \Phi_2) + h.c.]$$

and CP is explicitly and not spontaneously broken

$$\langle \Phi_1 \rangle = \begin{pmatrix} 0 \\ \frac{v_1}{\sqrt{2}} \end{pmatrix} \quad \langle \Phi_2 \rangle = \begin{pmatrix} 0 \\ \frac{v_2}{\sqrt{2}} \end{pmatrix}$$

•  $m_{12}^2$  and  $\lambda_5$  real    2HDM

•  $m_{12}^2$  and  $\lambda_5$  complex    C2HDM

➔  $\tan \beta = \frac{v_2}{v_1}$  ratio of vacuum expectation values

➔ 2 charged,  $H^\pm$ , and 3 neutral    CP-conserving - h, H and A

CP-violating -  $h_1, h_2$  and  $h_3$

➔ rotation angles in the neutral sector    CP-conserving -  $\alpha$

➔ soft breaking parameter    CP-violating -  $\alpha_1, \alpha_2$  and  $\alpha_3$

CP-conserving -  $m_{12}^2$

CP-violating -  $\text{Re}(m_{12}^2)$

# $h_{125}$ couplings

$$g_{2HDM}^{hVV} = \sin(\beta - \alpha) g_{SM}^{hVV}$$

$$g_{C2HDM}^{hVV} = \cos \alpha_2 g_{2HDM}^{hVV}$$

**CP-VIOLATING 2HDM**

"PSEUDOSCALAR" COMPONENT (DOUBLET)

$|s_2| = 0 \Rightarrow h_1$  is a pure scalar,

$|s_2| = 1 \Rightarrow h_1$  is a pure pseudoscalar

**Type I**

$$\kappa_U' = \kappa_D' = \kappa_L' = \frac{\cos \alpha}{\sin \beta}$$

**Type II**

$$\kappa_U'' = \frac{\cos \alpha}{\sin \beta}$$

$$\kappa_D'' = \kappa_L'' = -\frac{\sin \alpha}{\cos \beta}$$

$$Y_{C2HDM} = \cos \alpha_2 Y_{2HDM} \pm i \gamma_5 \sin \alpha_2 \tan \beta (1/\tan \beta)$$

**Type F(Y)**

$$\kappa_U^F = \kappa_L^F = \frac{\cos \alpha}{\sin \beta}$$

$$\kappa_D^F = -\frac{\sin \alpha}{\cos \beta}$$

**Type LS(X)**

$$\kappa_U^{LS} = \kappa_D^{LS} = \frac{\cos \alpha}{\sin \beta}$$

$$\kappa_L^{LS} = -\frac{\sin \alpha}{\cos \beta}$$

**THREE NEUTRAL STATES MIX**

**CP-VIOLATING 2HDM**

$$[h_i]_{mass} = [R_{ij}][h_j]_{gauge}$$

$$[R_{ij}] = \begin{pmatrix} c_1 c_2 & s_1 c_2 & s_2 \\ -(c_1 s_2 s_3 + s_1 c_3) & c_1 c_3 - s_1 s_2 s_3 & c_2 s_3 \\ -c_1 s_2 c_3 + s_1 s_3 & -(c_1 s_3 + s_1 s_2 c_3) & c_2 c_3 \end{pmatrix}$$

# 🍪 CP-violation in bosonic decays

## Correlations in the momentum distributions of leptons produced in the decays

$$h \rightarrow ZZ^* \rightarrow \bar{l}l\bar{l}l$$

$$h \rightarrow WW^* \rightarrow (l_1\nu_1)(l_2\nu_2)$$

CHOI, MILLER, MÜHLLEITNER, ZERWAS, PLB553, 61 (2003).

BUSZELLO, FLECK, MARQUARD, VAN DER BIJ, EPJC32, 209 (2004)

$$\mathcal{L}_{hZZ}^{\text{ATLAS}} = \kappa \frac{m_Z^2}{v} h Z_\mu Z^\mu + \frac{\alpha}{v} h Z_\mu \partial_\alpha \partial^\alpha Z^\mu + \frac{\beta}{v} h Z_{\mu\nu} Z^{\mu\nu} + \frac{\gamma}{v} h Z_{\mu\nu} \tilde{Z}^{\mu\nu}$$

**ONLY TERM IN THE 2HDM AT TREE-LEVEL**  $\kappa = \sin(\beta - \alpha)$

**ONLY TERM IN THE C2HDM AT TREE-LEVEL**  $\kappa = \cos \alpha_2 \sin(\beta - \alpha)$

Obtained 95% CL intervals on the *allowed* couplings of alternative, not SM-like, spin-zero states with respect to those of the SM scalar state.

	$\alpha/\kappa$	$\beta/\kappa$	$\gamma/\kappa$
ATLAS	not tested	[-2.5, 0.75]	[-0.95, 2.9]
CMS	[-1.2, 1.5]	[-∞, 0.69] [1.9, 2.3]	[-2.2, 2.1]
ATLAS	not tested	[-0.4, 0.85] [1, 2.2]	[-5, 6]
CMS	[-∞, +∞]	[-∞, 0.71] [1.2, +∞]	[-∞, +∞]
ATLAS	not tested	[-0.63, 0.73]	[-0.83, 2.2]
CMS	[-1.7, 1.6]	[-0.76, 0.58]	[-1.6, 1.5]

H→ZZ→4l

H→WW→2l2ν

**8 TeV results**

**EXPECTED FOR THE SM**

$$\beta/\kappa < 10^{-2}; \quad \gamma/\kappa < 10^{-7}$$

KARYTOV - TALK AT HIGGSDAYS 2015

# SENSITIVITY PROJECTIONS FOR HIGGS BOSON PROPERTIES MEASUREMENTS AT THE HL-LHC

CMS PAS FTR-18-011

Table 10: Summary of the 95% CL intervals for  $f_{a3} \cos(\phi_{a3})$ , under the assumption  $\Gamma_H = \Gamma_H^{\text{SM}}$ , and for  $\Gamma_H$  under the assumption  $f_{ai} = 0$  for projections at  $3000 \text{ fb}^{-1}$ . Constraints on  $f_{a3} \cos(\phi_{a3})$  are multiplied by  $10^4$ . Values are given for scenarios S1 (with Run 2 systematic uncertainties [47]) and the approximate S2 scenario, as described in the text.

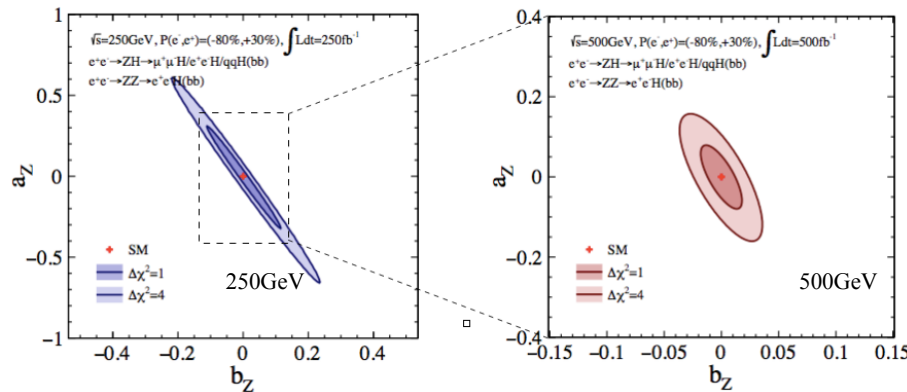
Parameter	Scenario	Projected 95% CL interval
$f_{a3} \cos(\phi_{a3}) \times 10^4$	S1, only on-shell	$[-1.8, 1.8]$
$f_{a3} \cos(\phi_{a3}) \times 10^4$	S1, on-shell and off-shell	$[-1.6, 1.6]$
$\Gamma_H$ (MeV)	S1	$[2.0, 6.1]$
$\Gamma_H$ (MeV)	S2	$[2.0, 6.0]$

$$\gamma/\kappa \lesssim 0.034$$

## Anomalous ZZH/ $\gamma$ ZH couplings 3-parameter fit



$$\mathcal{L}_{ZZH} = M_Z^2 \left( \frac{1}{v} + \frac{a_Z}{\Lambda} \right) Z_\mu Z^\mu H + \frac{b_Z}{2\Lambda} \hat{Z}_{\mu\nu} \hat{Z}^{\mu\nu} H + \frac{\tilde{b}_Z}{2\Lambda} \hat{Z}_{\mu\nu} \tilde{Z}^{\mu\nu} H \quad (\Lambda=1\text{TeV})$$



$$\gamma/\kappa \lesssim 0.022$$

SLIDE FROM KEISUKE FUJII'S  
PRESENTATION AT HIGGS  
COUPLINGS 2018, TOKYO

## 5-parameter fit

$1\sigma$  bounds  
including 500 GeV operation

ZH + ZZ at 250 + 500 GeV with  $H_{20}$

<https://arxiv.org/abs/1506.07830>

**ZZH /  $\gamma$ ZH structures  
can be measured to ~0.5%**

$$\left\{ \begin{array}{l} a_Z = \pm 0.0223 \quad (\eta_Z = \pm 0.5\%) \\ \zeta_{ZZ} = \pm 0.0067 \\ \zeta_{AZ} = \pm 0.0024 \\ \tilde{\zeta}_{ZZ} = \pm 0.0109 \end{array} \right., \quad \rho = \begin{pmatrix} 1 & -.837 & -.134 & -.009 & -.010 \\ - & 1 & .040 & .008 & .013 \\ - & - & 1 & .006 & -.0012 \\ - & - & - & 1 & .600 \\ - & - & - & - & 1 \end{pmatrix}$$

**CAN BE USED TO  
CONSTRAINT THE C2HDM AT  
LOOP-LEVEL**



## CP-violation in a combination of three decays

$$h_1 \rightarrow ZZ (+) h_2 \rightarrow ZZ (+) h_2 \rightarrow h_1 Z$$

Combinations of three decays

Many other combinations

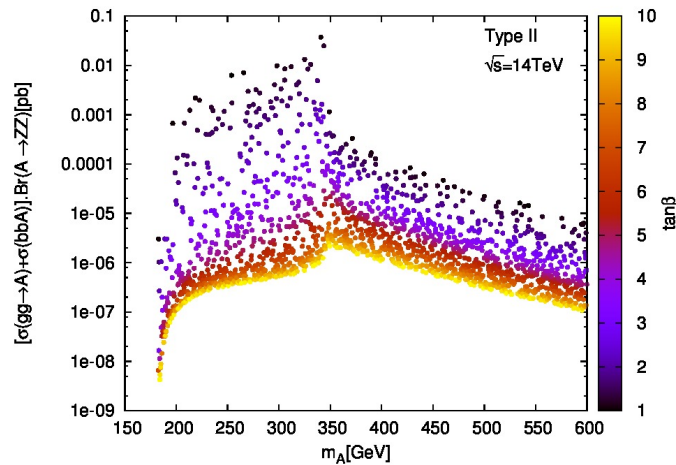
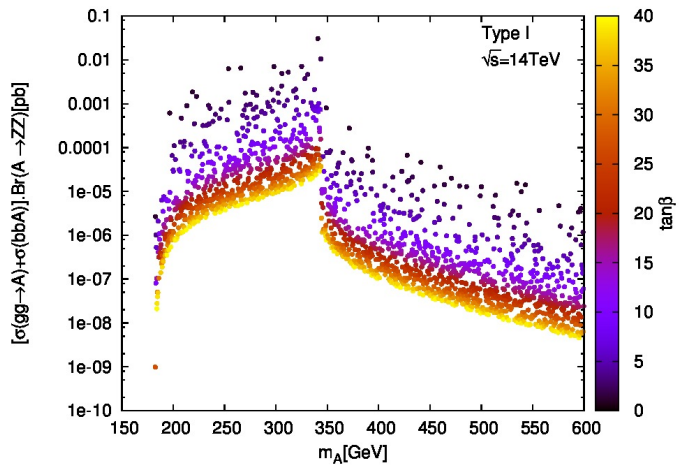
$$h_1 \rightarrow ZZ \Leftarrow CP(h_1) = 1$$

$$h_3 \rightarrow h_2 h_1 \Rightarrow CP(h_3) = CP(h_2)$$

Decay	CP eigenstates	Model
$h_3 \rightarrow h_2 Z$ $CP(h_3) = -CP(h_2)$	None	C2HDM, other CPV extensions
$h_{2(3)} \rightarrow h_1 Z$ $CP(h_{2(3)}) = -1$	2 CP-odd; None	C2HDM, NMSSM, 3HDM...
$h_2 \rightarrow ZZ$ $CP(h_2) = 1$	3 CP-even; None	C2HDM, cxSM, NMSSM, 3HDM...

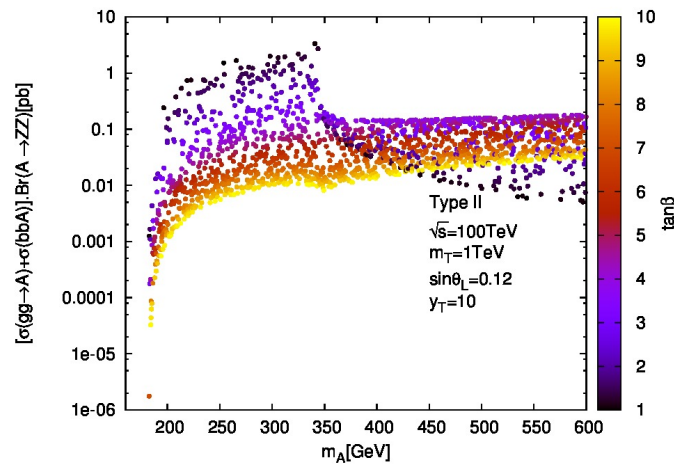
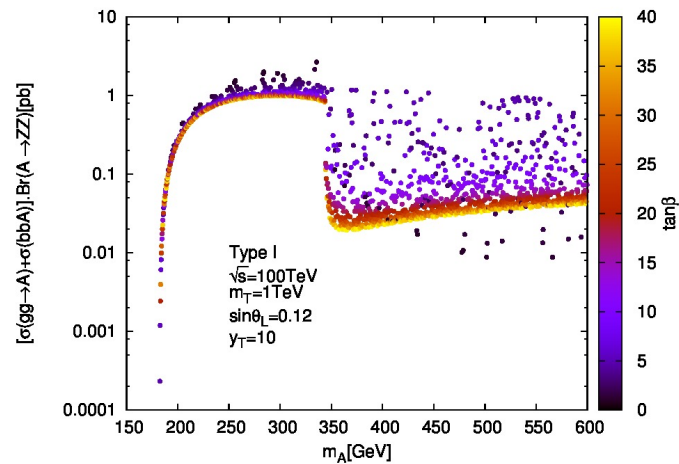
# CP-violation in a combination of three decays

But if something is found, a more detail studied is needed



Problem 1 - scalar is found in ZZ with very low rates - it could be a pseudoscalar plus in the 2HDM, in the exact alignment limit:

$$\Gamma(A \rightarrow ZZ) \sim \Gamma(H \rightarrow ZZ)$$



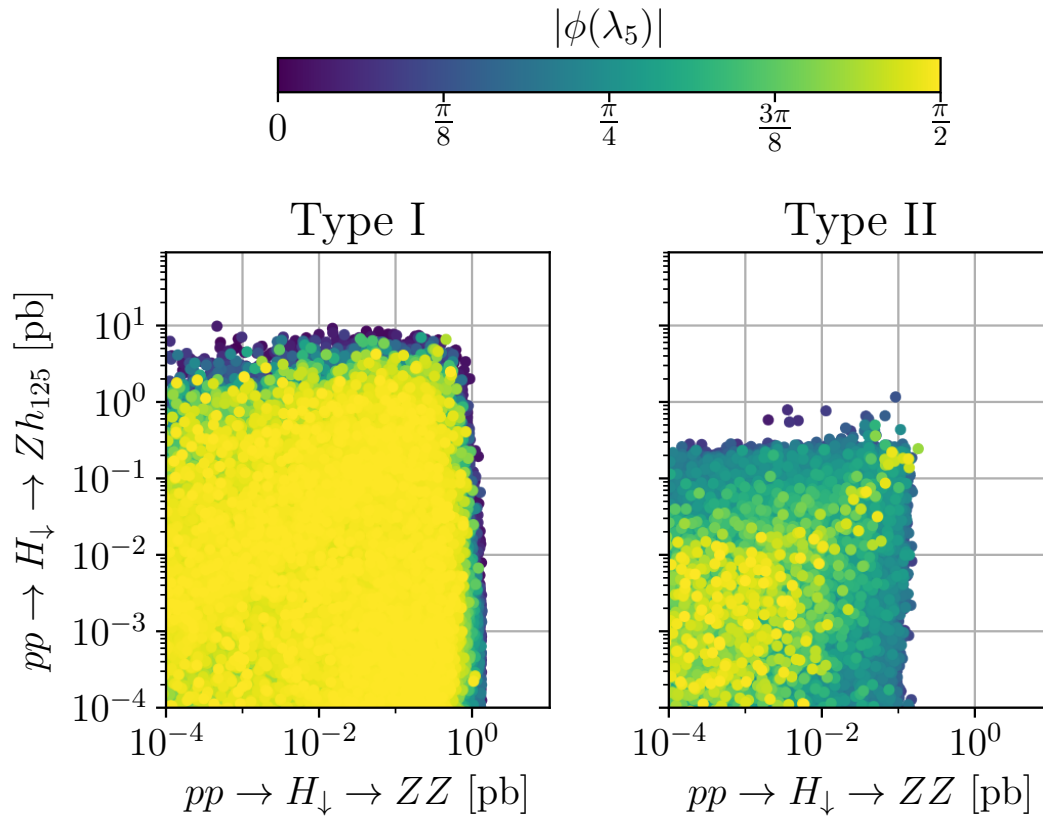
Problem 2 - with extra vector like quarks the rates could be higher even for a pseudoscalar





# Variables to probe CP-violation

Compare variables that probe CP-violation with the set of processes that together could signal CP-violation.



$h_{125} \rightarrow ZZ$       **MEASURED**

The first variable is just the phase

$$\lambda_5 = |\lambda_5| e^{i\phi(\lambda_5)}$$

**MORE YELLOW MEANS  
LARGER CP-VIOLATING  
PHASE**

There is no correlation between the high rates of CP-violating decays and the CP-violating phase.

# Variables to probe CP-violation

Variable involving Higgs couplings to gauge bosons

$$\xi_V = 27 \prod_{i=1}^3 c^2(H_i VV) \quad c(H_i VV) = R_{i1} c_\beta + R_{i2} s_\beta \quad [R_{ij}] = \begin{pmatrix} c_1 c_2 & s_1 c_2 & s_2 \\ -(c_1 s_2 s_3 + s_1 c_3) & c_1 c_3 - s_1 s_2 s_3 & c_2 s_3 \\ -c_1 s_2 c_3 + s_1 s_3 & -(c_1 s_3 + s_1 s_2 c_3) & c_2 c_3 \end{pmatrix}$$

MENDEZ, POMAROL, PLB272 (1991) 313.

$c(H_i VV)$  is the coupling relative to the SM Higgs coupling; variables are normalised

$$0 < \xi_V \leq 1$$

which is related with the simplest CP-odd invariant that can be build from the mass matrix

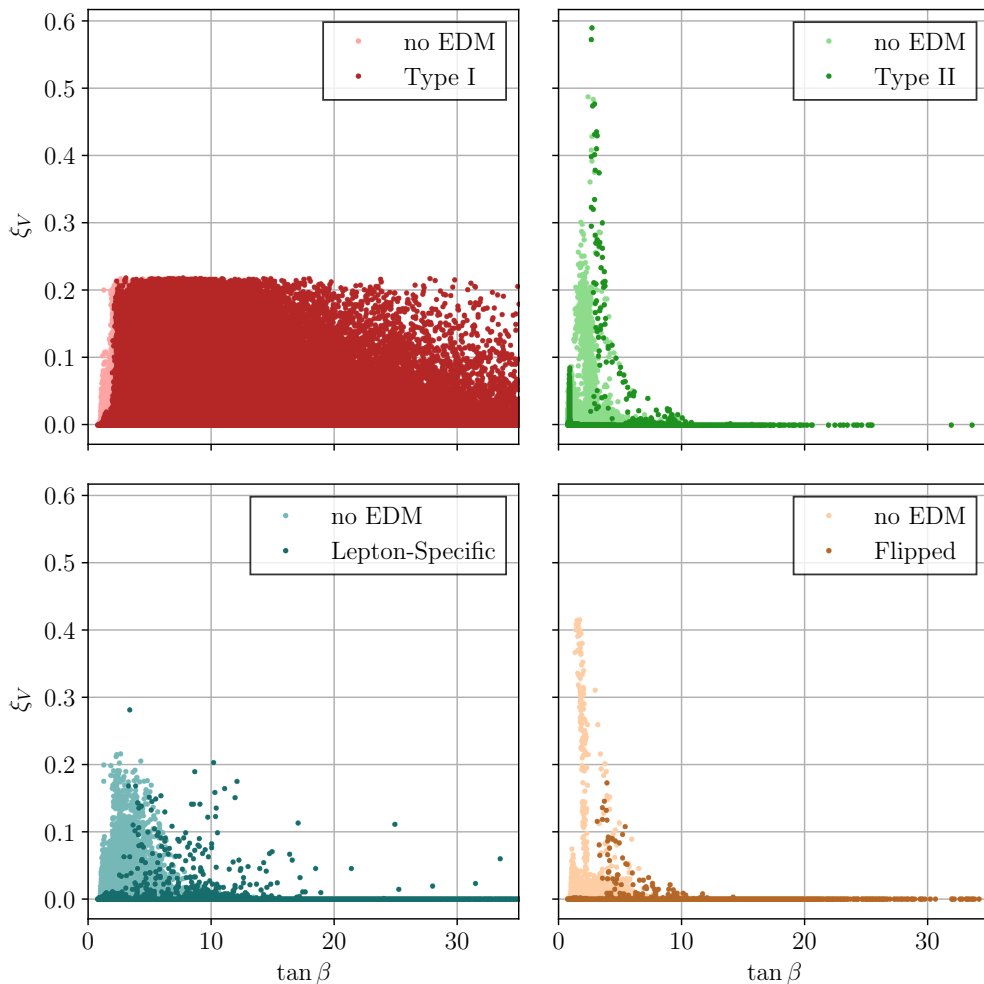
$$J_1^2 = [(m_2^2 - m_1^2)(m_3^2 - m_1^2)(m_3^2 - m_2^2)] \frac{\xi_V}{27}$$

LAVOURA, SILVA, PRD50 (1994) 4619.

Note that in the CP-conserving 2HDM,

$$c(AVV) = 0 \implies \xi_V = 0$$

## Variables vs. $\tan\beta$



CP-violating parameter  $\xi_V$  as a function of  $\tan\beta$  for all types.

Lighter points have passed all constraints except EDM, darker points have passed all constraints.

Type I: no special regions regarding the allowed values of  $\tan\beta$ . Also, the maximum value for  $\xi_V$  is around 0.2 almost independently of  $\tan\beta$ .

Type II: ,after EDM, we end with two almost straight lines (one for  $\tan\beta \approx 1$  and the other for  $\xi_V \approx 0$ ), as well as a region around  $\tan\beta \approx 3$  with  $\xi_V$  up to 0.6.

Points with significant CP-violation can occur for  $\tan\beta \approx 1$  in the alignment limit or for large  $\tan\beta$  for the wrong sign limit.

$$\kappa_D \kappa_W < 0 \quad \text{or} \quad \kappa_U \kappa_W < 0$$

The situation in Flipped is similar to Type II, with a maximum value of  $\xi_V \sim 0.2$ .

FERREIRA, GUNION, HABER, RS, PRD89 (2014)

FONTES, MÜHLEITNER, ROMÃO, RS, SILVA, WITTBRODT, JHEP 1802 (2018) 073.

Let us consider now the Yukawa couplings. As an example consider a Type II up-quark coupling

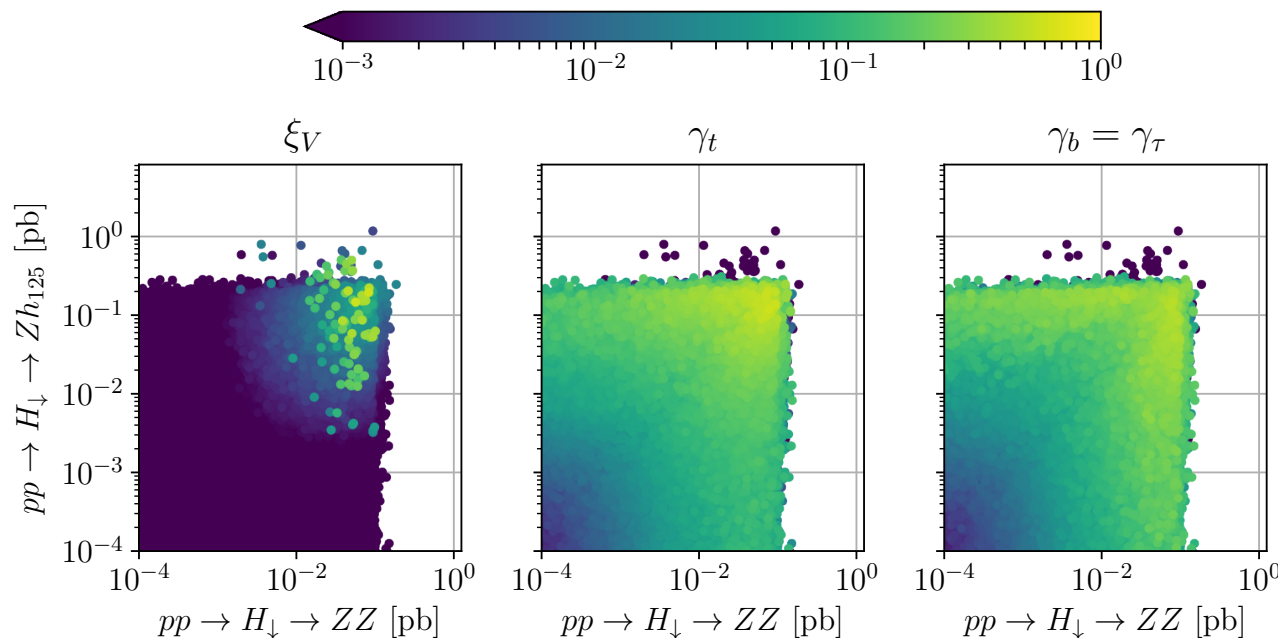
$$c(H_i \bar{t} t) = \frac{1}{s_\beta} (R_{i2} - i\gamma_5 R_{i3})$$

we defined the normalised variables

$$\gamma_t = 1024 \prod_{i=1}^3 (R_{i2} R_{i3})^2 \quad \gamma_b = 1024 \prod_{i=1}^3 (R_{i1} R_{i3})^2$$

KHATER, OSLAND, APP B34 (2003) 4531.

Similar variables can be defined for the sum.



Results for Type II  
(where some correlation  
seems to exist)

But in most cases  
we found no  
correlation.

## 🍪 CP-violation in the triple gauge bosons coupling

$$h_2 \rightarrow h_1 Z \quad CP(h_2) = -CP(h_1)$$

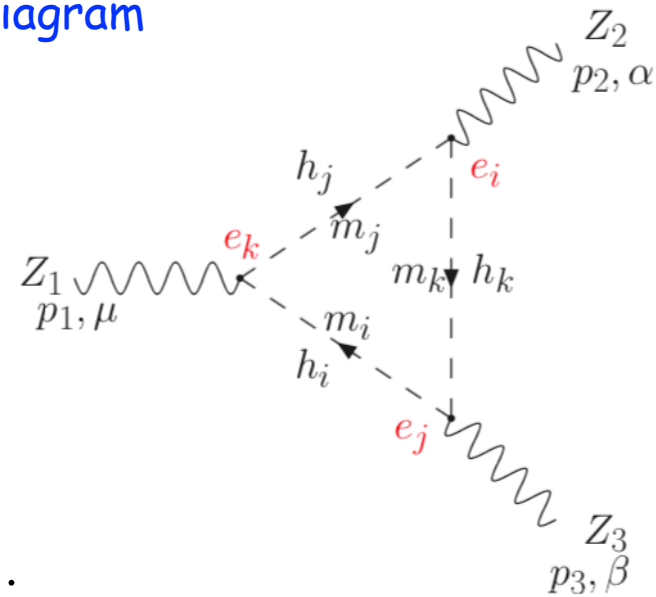
$$h_3 \rightarrow h_1 Z \quad CP(h_3) = -CP(h_1)$$

$$h_3 \rightarrow h_2 Z \quad CP(h_3) = -CP(h_2)$$

Is there CP-violation here? Now let us take these three processes and build a nice Feynman diagram

With one Z off-shell the most general ZZZ vertex has a CP-odd term of the form

$$i\Gamma_{\mu\alpha\beta} = -e \frac{p_1^2 - m_Z^2}{m_Z^2} f_4^Z (g_{\mu\alpha} p_{2,\beta} + g_{\mu\beta} p_{3,\alpha}) + \dots$$



For a model with only this type of diagrams

GAEMERS, GOUNARIS, ZPC1 (1979) 259

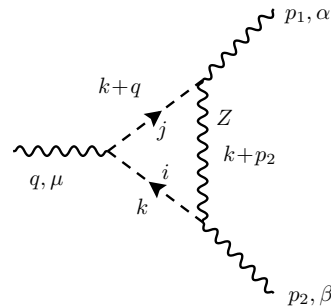
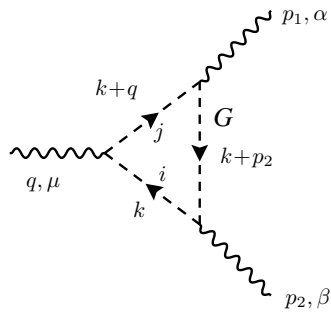
HAGIWARA, PECCEI, ZEPPENFELD, HIKASA, NPB282 (1987) 253

GRZADKOWSKI, OGREID, OSLAND, JHEP 05 (2016) 025

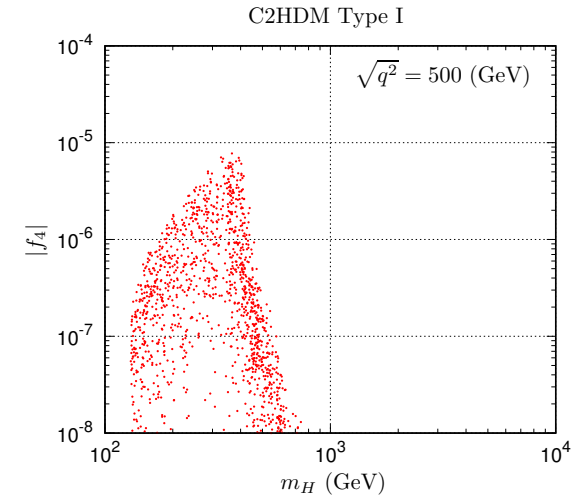
**DO NOT MISS  
PEDRO FERREIRA'S CP IN THE  
DARK tomorrow at 10.45**

# In the C2HDM there are two more types of diagrams

PLOT FROM JHEP 04 (2018) 002



$$\begin{aligned}
 h_1 &\rightarrow ZZ & CP(h_1) &= 1 \\
 h_2 &\rightarrow ZZ & CP(h_2) &= 1 \\
 h_2 &\rightarrow h_1 Z & CP(h_2) &= -CP(h_1)
 \end{aligned}$$



GRZĄDKOWSKI, OGREID, OSLAND, JHEP 05 (2016) 025.

BÉLUSCA-MAÍTO, FALKOWSKI, FONTES, ROMÃO, SILVA, JHEP 04 (2018) 002

The typical maximal value for  $f_4$  seems to be below  $10^{-4}$ .

Present measurements by ATLAS and CMS - still two orders of magnitude away

CMS COLLABORATION, EPJC78 (2018) 165.

$$-1.2 \times 10^{-3} < f_4^Z < 1.0 \times 10^{-3}$$

ATLAS COLLABORATION, PRD97 (2018) 032005.

$$-1.5 \times 10^{-3} < f_4^Z < 1.5 \times 10^{-3}$$

How far can we go in constraining  $f_4$ ?

TABLE III. Simultaneous limits ( $10^{-3}$ ) on anomalous couplings in ZZ production at LHC at  $\sqrt{s} = 13$  TeV for various luminosity from MCMC

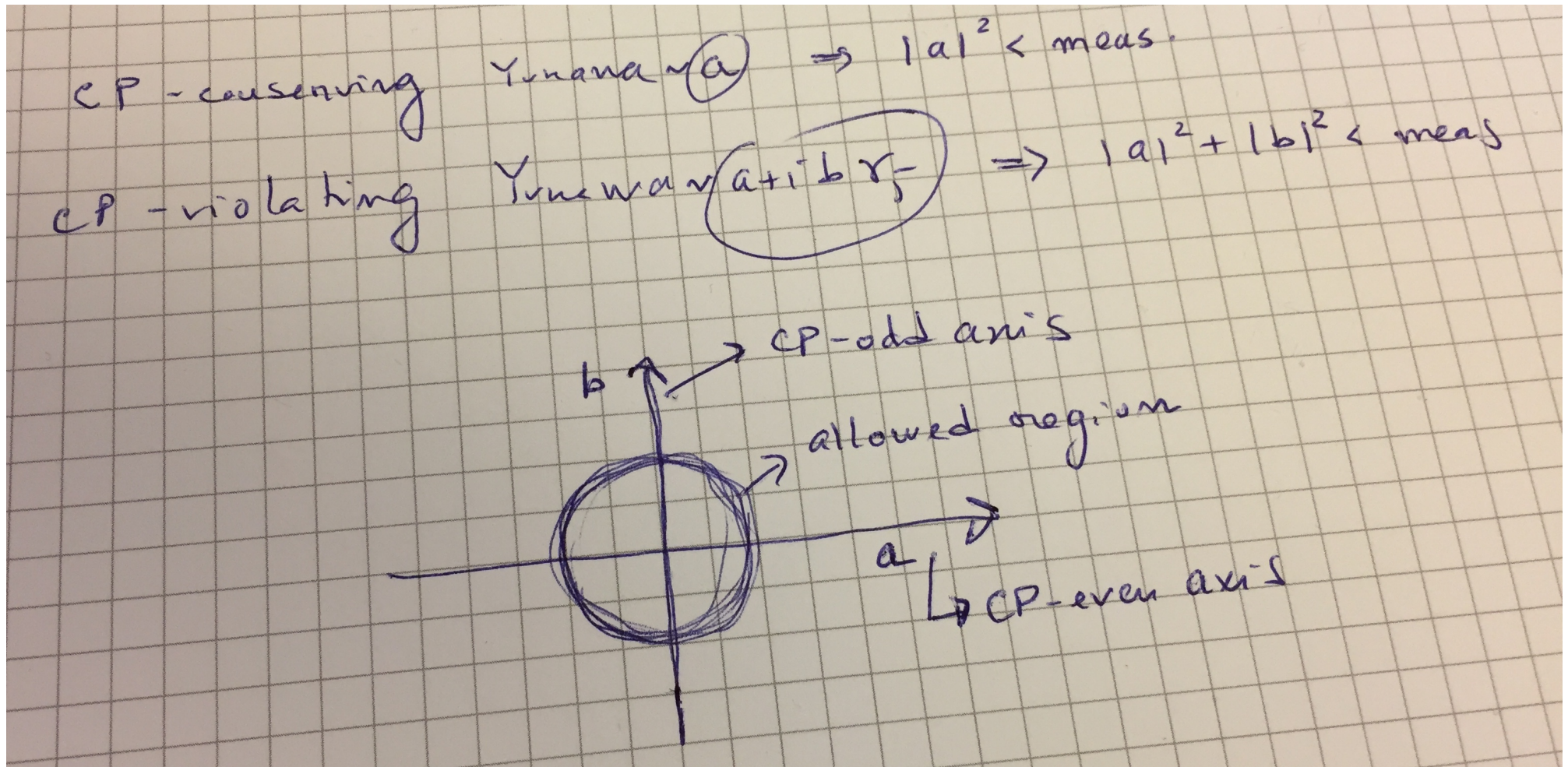
param / $\mathcal{L}$	35.9 fb <sup>-1</sup>	150 fb <sup>-1</sup>	300 fb <sup>-1</sup>	1000 fb <sup>-1</sup>
$f_4^Y$	+1.12 -1.11	+0.78 -0.78	+0.66 -0.66	+0.50 -0.50
$f_5^Y$	+1.10 -1.13	+0.77 -0.80	+0.65 -0.67	+0.47 -0.50
$f_4^Z$	+0.95 -0.95	+0.67 -0.67	+0.57 -0.57	+0.41 -0.41
$f_5^Z$	+0.95 -0.97	+0.67 -0.68	+0.56 -0.58	+0.41 -0.42

RAHAMAN, SINGH, 1810.11657.

## 🍪 CP-violation in the Yukawa couplings

$$Y_{C2HDM}^{TypeII} = a_d + i\gamma_5 b_d = c_2 Y_{2HDM}^{TypeII} - i\gamma_5 s_2 t_\beta \quad \text{bottom, tau}$$

$$Y_{C2HDM}^{TypeII} = a_u + i\gamma_5 b_u = c_2 Y_{2HDM}^{TypeII} - i\gamma_5 \frac{s_2}{t_\beta} \quad \text{top}$$



# Bounds on the Yukawa couplings

With the most relevant experimental and theoretical constraints

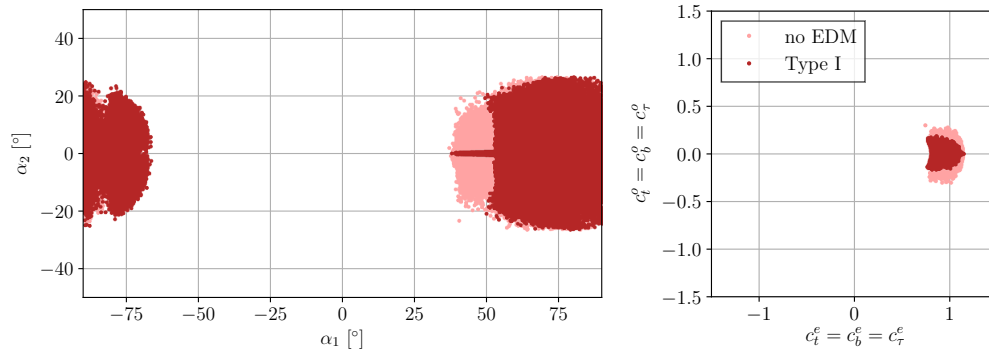
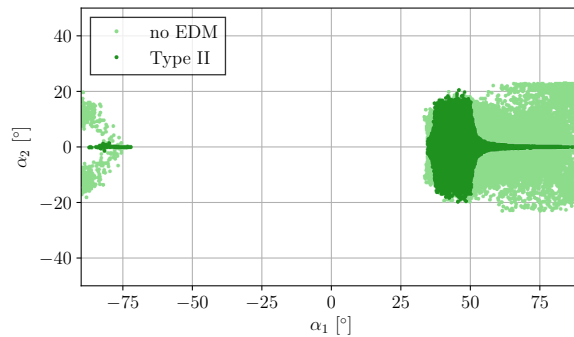


Figure 1. C2HDM Type I: for sample 1 (dark) and sample 2 (light) left: mixing angles  $\alpha_1$  and  $\alpha_2$  of the C2HDM mixing matrix  $R$  only including scenarios where  $H_1 = h_{125}$ ; right: Yukawa couplings.

$$g_{C2HDM}^{hVV} = \cos \alpha_2 \cos(\beta - \alpha_1) g_{SM}^{hVV}$$

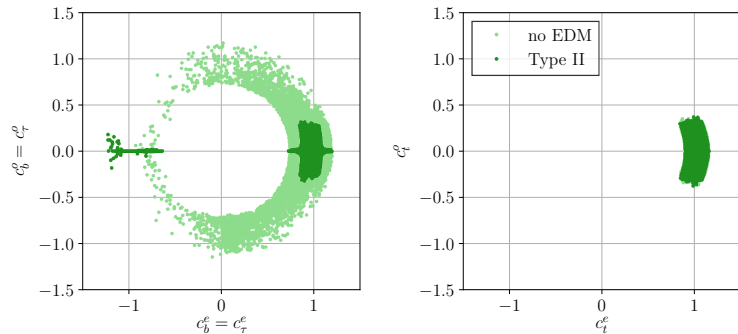
$$g_{C2HDM}^{huu} = \left( \cos \alpha_2 \frac{\sin \alpha_1}{\sin \beta} - i \frac{\sin \alpha_2}{\tan \beta} \gamma_5 \right) g_{SM}^{hff}$$

$$\mu_{VV} > 0.79 \Rightarrow \cos \alpha_2 > 0.89 \Rightarrow \alpha_2 < 27^\circ$$



$$\cos 20^\circ = 0.94 \quad \sin 20^\circ = 0.34$$

$$\tan \beta > 1$$



$$g_{C2HDM}^{hbb} = \left( \cos \alpha_2 \frac{\cos \alpha_1}{\cos \beta} - i \sin \alpha_2 \tan \beta \gamma_5 \right) g_{SM}^{hff}$$

EDM

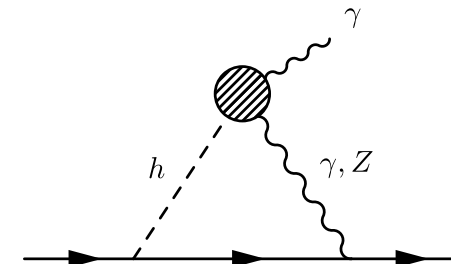
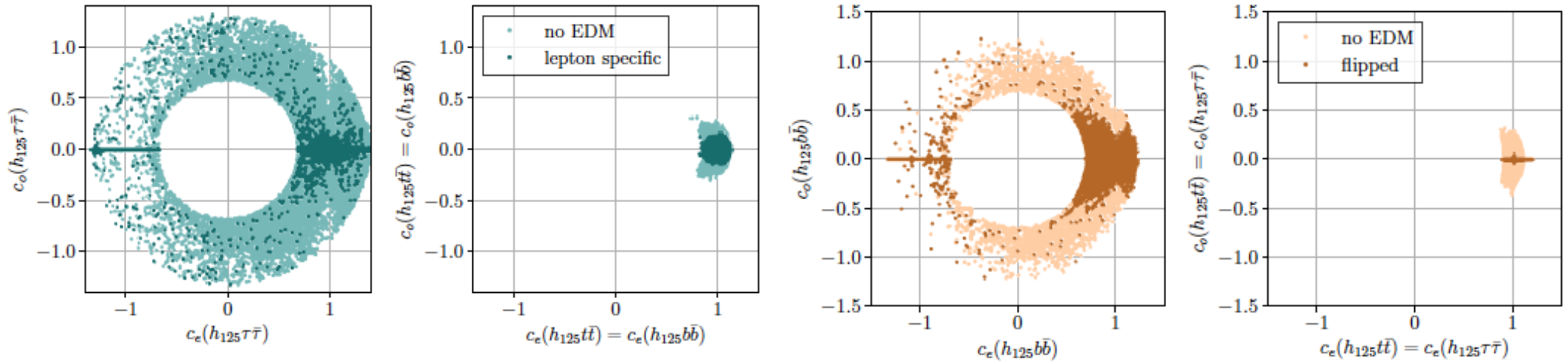


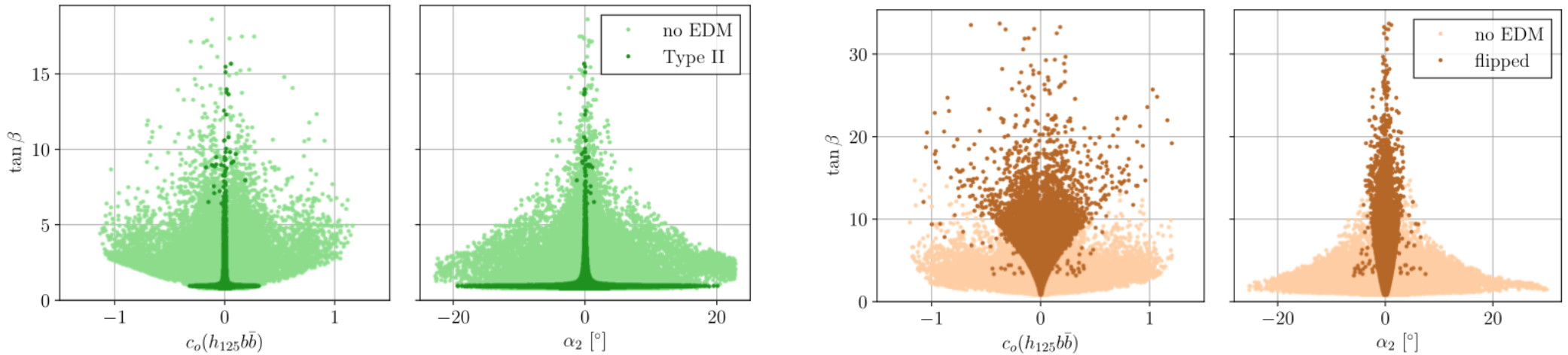
Figure 3. C2HDM Type II,  $h_{125} = H_1$ : Yukawa couplings to bottom quarks and tau leptons (left) and top quarks (right) for sample 1 (dark) and sample 2 (light).



**EDM constraints completely kill large pseudoscalar components in Type II.  
Not true in Flipped and Lepton Specific.**



CP-odd coupling proportional to  $\sin\alpha_2 \tan\beta$



EDMs act differently in the different Yukawa versions of the model.  
 Cancellations between diagrams occur.

The relevant quantity for the pseudoscalar component is

$$C_o = \sin(\alpha_2) \tan(\beta)$$

# How will it look in the future?

ABRAMOWICZ EAL, 1307.5288.

CLICDP, SICKING, NPPP, 273-275, 801 (2016)

Parameter	Relative precision [76, 77]		
	350 GeV 500 fb <sup>-1</sup>	+1.4 TeV +1.5 ab <sup>-1</sup>	+3.0 TeV +2.0 ab <sup>-1</sup>
$\kappa_{HZZ}$	0.43%	0.31%	0.23%
$\kappa_{HWW}$	1.5%	0.15%	0.11%
$\kappa_{Hbb}$	1.7%	0.33%	0.21%
$\kappa_{Hcc}$	3.1%	1.1%	0.75%
$\kappa_{Htt}$	—	4.0%	4.0%
$\kappa_{H\tau\tau}$	3.4%	1.3%	<1.3%
$\kappa_{H\mu\mu}$	—	14%	5.5%
$\kappa_{Hgg}$	3.6%	0.76%	0.54%
$\kappa_{H\gamma\gamma}$	—	5.6%	< 5.6%

**Predicted precision for CLIC**

$\Psi_i^{C2HDM}$

C2HDM - pseudoscalar component.

LHC today

$\Psi_i^{C2HDM} = R_{i3}^2$

C2HDM II	C2HDM I
10%	20%

CLIC@350GeV (500/fb)

$\Psi_i^{C2HDM} \leq 0.85\%$  from  $\kappa_{ZZ}$

If no new physics is discovered and the measured values are in agreement with the SM predictions, the pseudoscalar components (from the C2HDM) will be below the % level.

Not taking into account radiative corrections

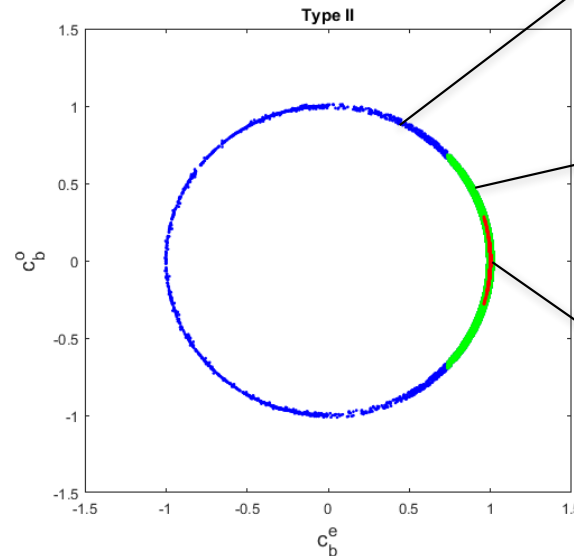
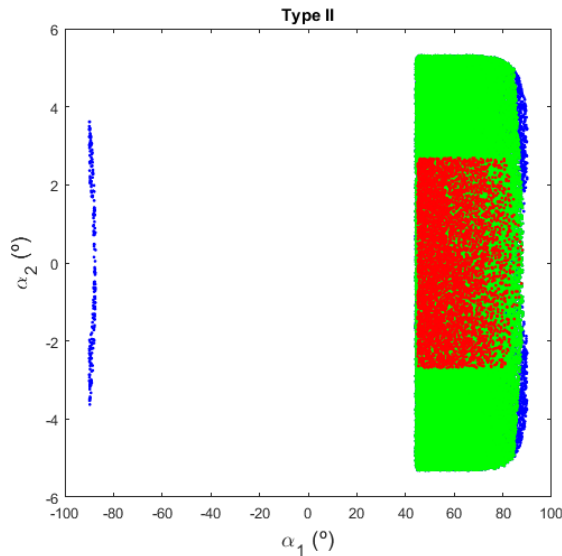
# How will it look in the future?

Using the bounds for  $\kappa_i$  the Yukawa allowed circle looks like

**Unitarity**  $\Rightarrow \kappa_{ZZ,WW}^2 + \Psi_i^{C2HDM} \leq 1$

$$\Psi_i^{C2HDM} = R_{i3}^2$$

350 GeV and no  
 $K_{gg} , K_{\gamma\gamma}$



350 GeV with  
 $K_{gg} , K_{\gamma\gamma}$

3 TeV with  
 $K_{gg} , K_{\gamma\gamma}$

The deviations can be written in terms of the rotation matrix from gauge to mass eigenstates.

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix} = R \begin{pmatrix} \rho \\ \eta \\ \rho_S \end{pmatrix} \quad R = [R_{ij}] = \begin{pmatrix} c_1 c_2 & s_1 c_2 & s_2 \\ -(c_1 s_2 s_3 + s_1 c_3) & c_1 c_3 - s_1 s_2 s_3 & c_2 s_3 \\ -c_1 s_2 c_3 + s_1 s_3 & -(c_1 s_3 + s_1 s_2 c_3) & c_2 c_3 \end{pmatrix}$$



# CP-violation - a strange scenario

	Type I	Type II	Lepton Specific	Flipped
Up	$\frac{R_{12}}{s_\beta} - ic_\beta \frac{R_{13}}{s_\beta}$	$\frac{R_{12}}{s_\beta} - ic_\beta \frac{R_{13}}{s_\beta}$	$\frac{R_{12}}{s_\beta} - ic_\beta \frac{R_{13}}{s_\beta}$	$\frac{R_{12}}{s_\beta} - ic_\beta \frac{R_{13}}{s_\beta}$
Down	$\frac{R_{12}}{s_\beta} + ic_\beta \frac{R_{13}}{s_\beta}$	$\frac{R_{11}}{c_\beta} - is_\beta \frac{R_{13}}{c_\beta}$	$\frac{R_{12}}{s_\beta} + ic_\beta \frac{R_{13}}{s_\beta}$	$\frac{R_{11}}{c_\beta} - is_\beta \frac{R_{13}}{c_\beta}$
Leptons	$\frac{R_{12}}{s_\beta} + ic_\beta \frac{R_{13}}{s_\beta}$	$\frac{R_{11}}{c_\beta} - is_\beta \frac{R_{13}}{c_\beta}$	$\frac{R_{11}}{c_\beta} - is_\beta \frac{R_{13}}{c_\beta}$	$\frac{R_{12}}{s_\beta} + ic_\beta \frac{R_{13}}{s_\beta}$

There is only one way to make the pseudoscalar component to vanish

$$c_1 = 0 \implies R_{11} = 0$$

and for instance in type II

$$c_1 = 0 \implies R_{11} = 0 \implies a_D = a_L = 0$$

and

**A scalar that is also a pseudoscalar**

$$b_D = b_L = -s_2 t_\beta$$

$$b_D^2 = b_L^2 \approx 1$$

$$0 + i\gamma_5 b_D$$

$$b_U = s_2 / t_\beta$$

$$b_U \approx 0$$

for large  $\tan\beta$

$$a_U + i\gamma_5 \times 0$$

## Possible for all Yukawa types except Type I

Can be achieved

$$a_i + i\gamma_5 b_i \quad (i = U, D, L)$$

$$c_1 = 0 \Rightarrow R_{11} = 0$$

and

$$a_U^2 = \frac{c_2^2}{s_\beta^2}; \quad b_U^2 = \frac{s_2^2}{t_\beta^2}; \quad C^2 = s_\beta^2 c_2^2$$

**Type I**

$$a_U = a_D = a_L = \frac{c_2}{s_\beta}$$

$$b_U = -b_D = -b_L = -\frac{s_2}{t_\beta}$$

**Type II**

$$a_D = a_L = 0$$

$$b_D = b_L = -s_2 t_\beta$$

**Type F**

$$a_D = 0$$

$$b_D = -s_2 t_\beta$$

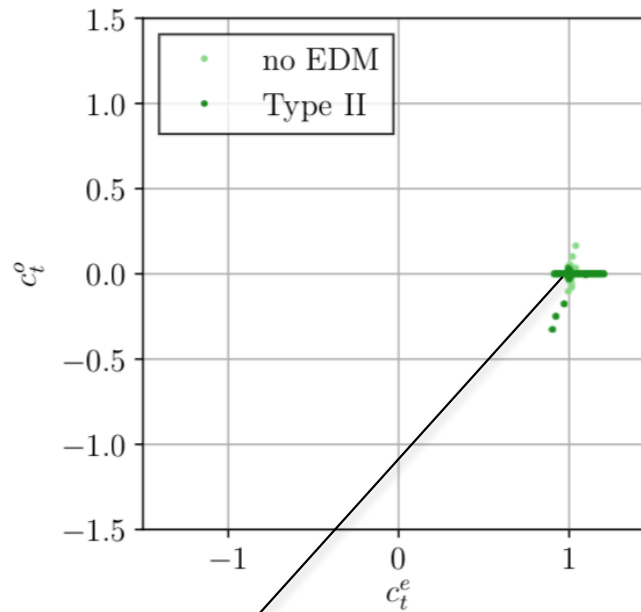
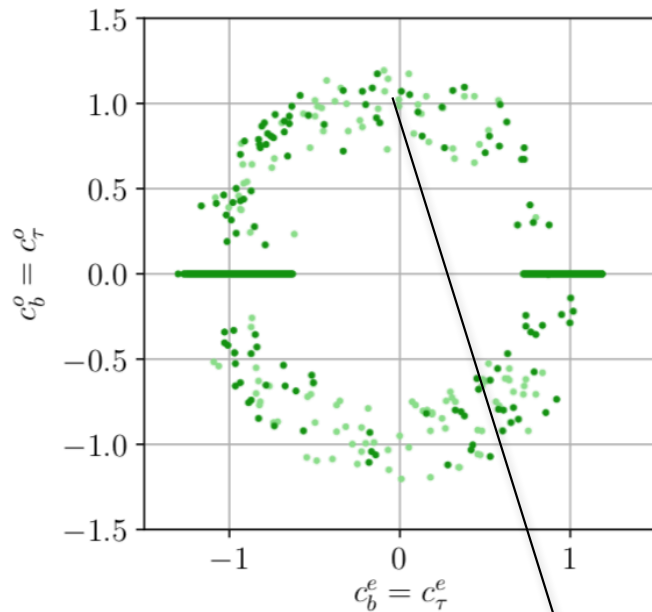
**Type LS**

$$a_L = 0$$

$$b_L = -s_2 t_\beta$$

Even if the CP-violating parameter is small, large  $\tan\beta$  can lead to large values of  $b$ .

# Which means CP-violation in a strange way



$$Y_{C2HDM} = a_F + i\gamma_5 b_F$$

$$b_U \approx 0; a_D \approx 0$$

**A Type II model  
where  $H_2$  is the SM-  
like Higgs.**

**Find two particles of the same mass one decaying  
to tops as CP-even**

$$h_2 = H; pp \rightarrow Ht\bar{t}$$

**and the other decaying to taus as CP-odd**

$$h_2 = A \rightarrow \tau^+\tau^-$$

**Probing one Yukawa coupling is not enough!**

Type II	BP2m	BP2c	BP2w
$m_{H_1}$	94.187	83.37	84.883
$m_{H_2}$	125.09	125.09	125.09
$m_{H^\pm}$	586.27	591.56	612.87
$\text{Re}(m_{12}^2)$	24017	7658	46784
$\alpha_1$	-0.1468	-0.14658	-0.089676
$\alpha_2$	-0.75242	-0.35712	-1.0694
$\alpha_3$	-0.2022	-0.10965	-0.21042
$\tan \beta$	7.1503	6.5517	6.88
$m_{H_3}$	592.81	604.05	649.7
$c_b^e = c_\tau^e$	0.0543	0.7113	-0.6594
$c_b^o = c_\tau^o$	1.0483	0.6717	0.6907
$\mu_V / \mu_F$	0.899	0.959	0.837
$\mu_{VV}$	0.976	1.056	1.122
$\mu_{\gamma\gamma}$	0.852	0.935	0.959
$\mu_{\tau\tau}$	1.108	1.013	1.084
$\mu_{bb}$	1.101	1.012	1.069

## The LS and F benchmark points

LS	BPLSm	BPLSc	BPLSw	Flipped	BPFm	BPFc	BPFw
$m_{H_1}$	125.09	125.09	91.619	$m_{H_1}$	125.09	125.09	125.09
$m_{H_2}$	138.72	162.89	125.09	$m_{H_2}$	154.36	236.35	148.75
$m_{H^\pm}$	180.37	163.40	199.29	$m_{H^\pm}$	602.76	589.29	585.35
$\text{Re}(m_{12}^2)$	2638	2311	1651	$\text{Re}(m_{12}^2)$	10277	8153	42083
$\alpha_1$	-1.5665	1.5352	0.0110	$\alpha_1$	-1.5708	1.5277	-1.4772
$\alpha_2$	0.0652	-0.0380	0.7467	$\alpha_2$	-0.0495	-0.0498	0.0842
$\alpha_3$	-1.3476	1.2597	0.0893	$\alpha_3$	0.7753	0.4790	-1.3981
$\tan \beta$	15.275	17.836	9.870	$\tan \beta$	18.935	14.535	8.475
$m_{H_3}$	206.49	210.64	177.52	$m_{H_3}$	611.27	595.89	609.82
$c_\tau^e$	-0.0661	0.6346	-0.7093	$c_b^e$	-0.0003	0.6269	-0.7946
$c_\tau^o$	0.9946	0.6780	-0.6460	$c_b^o$	-0.9369	0.7239	0.7130
$\mu_V / \mu_F$	0.980	0.986	0.954	$\mu_V / \mu_F$	0.927	0.964	0.844
$\mu_{VV}$	1.014	1.029	1.000	$\mu_{VV}$	1.154	1.091	0.998
$\mu_{\gamma\gamma}$	0.945	1.018	0.879	$\mu_{\gamma\gamma}$	1.027	0.986	0.874
$\mu_{\tau\tau}$	1.007	0.880	0.943	$\mu_{\tau\tau}$	1.148	1.084	1.039
$\mu_{bb}$	1.013	1.020	1.025	$\mu_{bb}$	1.001	0.992	1.170

Almost CP-odd in the coupling to taus. Almost CP-even in the coupling to quarks.

$$h_1 = A \rightarrow \tau^+ \tau^-$$

$$h_1 = H; pp \rightarrow Ht\bar{t}$$

Same but with a CP-odd coupling to b quarks.

$$h_1 = A \rightarrow \bar{b}b$$

$$h_1 = H; pp \rightarrow Ht\bar{t}$$

The other scenarios are for maximal  $c^o * c^e$  with all possible signs combination.

## CP from direct measurements at the LHC ( $\tau\tau h$ )

$$pp \rightarrow h \rightarrow \tau^+ \tau^-$$

BERGE, BERNREUTHER, ZIETHE PRL 100 (2008) 171605

BERGE, BERNREUTHER, NIEPELT, SPIESBERGER, PRD84 (2011) 116003

- A measurement of the angle

$$\tan \Phi_\tau = \frac{b_L}{a_L}$$

can be performed  
with the accuracies

$$\Delta\Phi_\tau = 15^\circ \Leftrightarrow 150 \text{ fb}^{-1}$$

$$\Delta\Phi_\tau = 9^\circ \Leftrightarrow 500 \text{ fb}^{-1}$$

**NUMBERS FROM:** BERGE, BERNREUTHER, KIRCHNER  
PRD92 (2015) 096012

$$\tan \Phi_\tau = -\frac{\sin \beta}{\cos \alpha_1} \tan \alpha_2 \Rightarrow \tan \alpha_2 = -\frac{\cos \alpha_1}{\sin \beta} \tan \Phi_\tau$$

- It is not a direct measurement of the CP-violating angle  $\alpha_2$ .



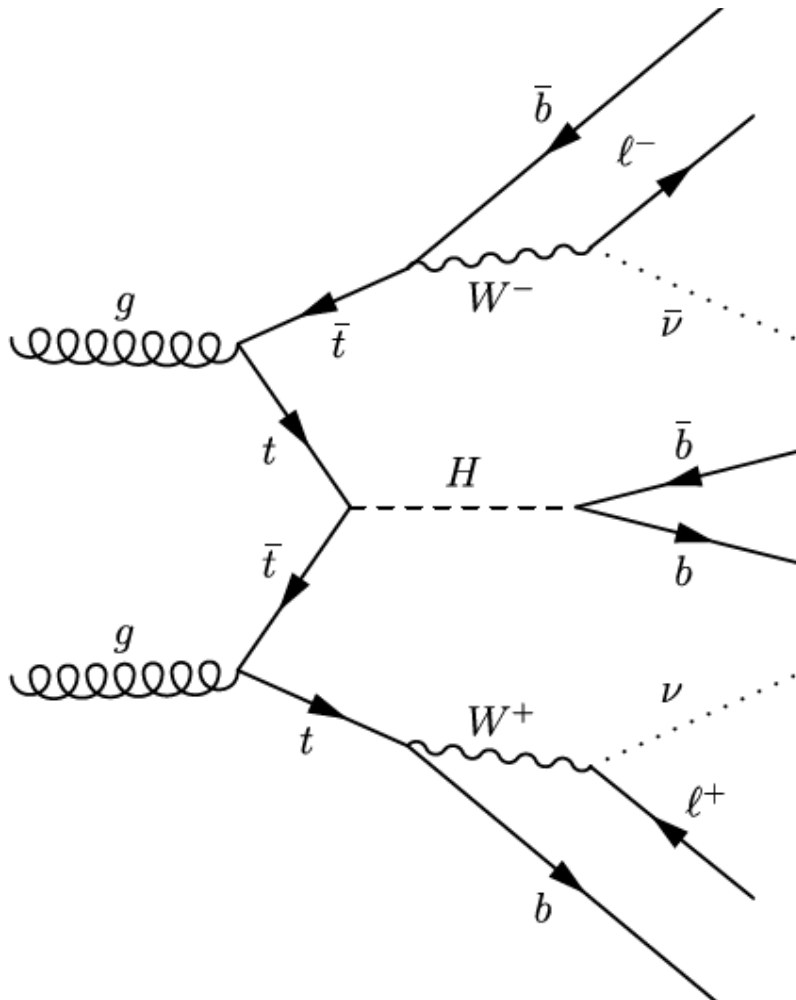
# CP from direct measurements at the LHC (tth)

$$pp \rightarrow h\bar{t}t$$

GUNION, HE, PRL77 (1996) 5172

BOUDJEMA, GODBOLE, GUADAGNOLI, MOHAN, PRD92 (2015) 015019

AMOR DOS SANTOS EAL PRD96 (2017) 013004



$$\mathcal{L}_{H\bar{t}t} = -\frac{y_t}{\sqrt{2}}\bar{t}(a + ib\gamma_5)th$$

**Signal:** tt fully leptonic (or semi-leptonic) and  $H \rightarrow bb$

**Background:** most relevant is the irreducible tt background

## Probing the nature of h in tth

The spin averaged cross section of tth productions has terms proportional to  $a^2+b^2$  and to  $a^2-b^2$ . Terms  $a^2-b^2$  are proportional to the top quark mass. We can define

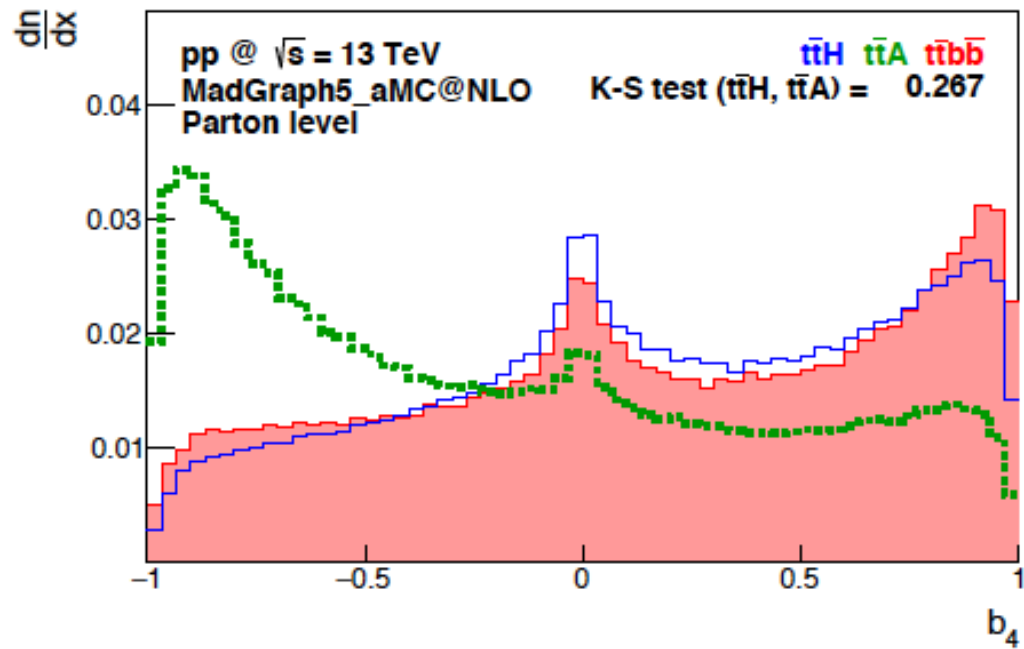
$$\alpha[\mathcal{O}_{CP}] \equiv \frac{\int \mathcal{O}_{CP} \{d\sigma(pp \rightarrow tth)/dPS\}dPS}{\int \{d\sigma(pp \rightarrow tth)/dPS\}dPS} \quad \mathcal{L}_{H\bar{t}t} = -\frac{y_t}{\sqrt{2}}\bar{t}(a + ib\gamma_5)th$$

where the operator is chosen to maximise the sensitivity of  $\alpha$  to the  $a^2-b^2$  term. The best operator from the ones proposed is

$$b_4 = \frac{p_t^z p_{\bar{t}}^z}{p_t p_{\bar{t}}}$$

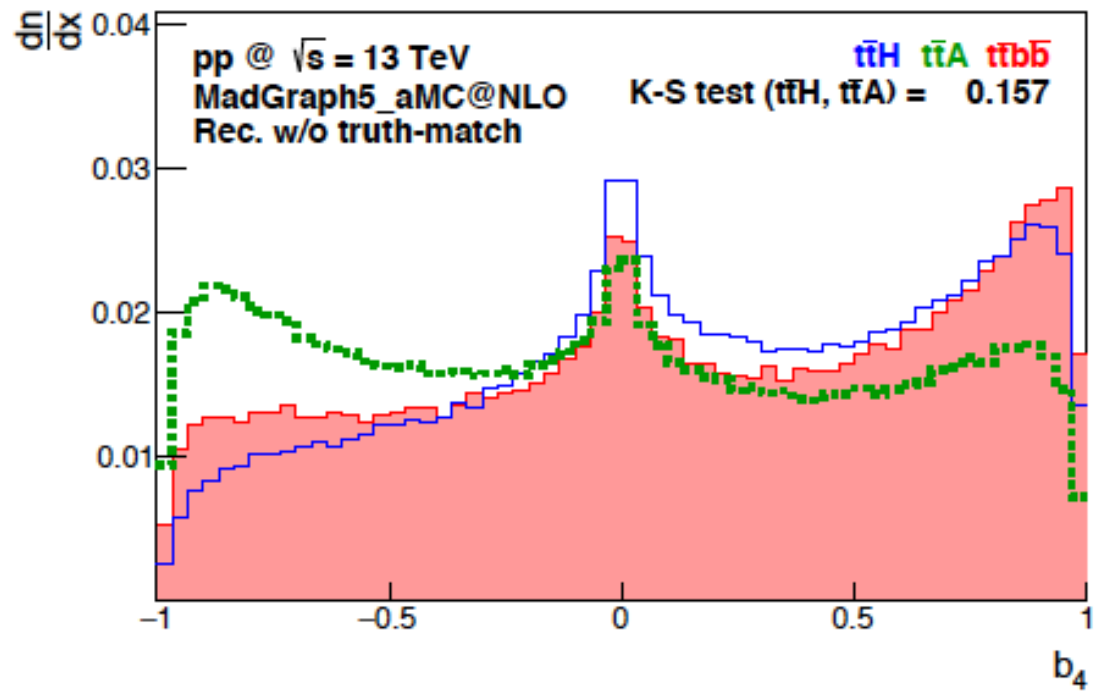
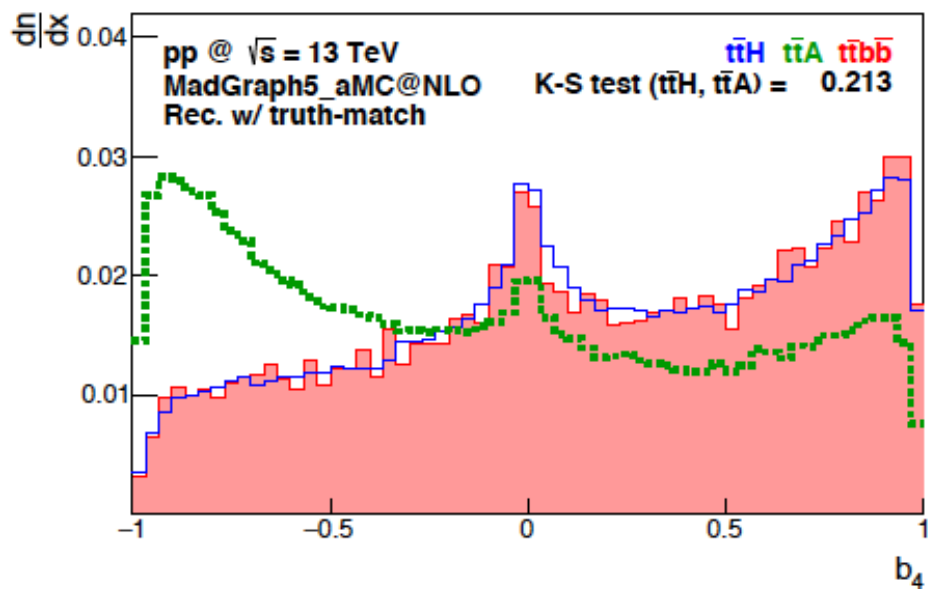
GUNION, HE, PRL77 (1996) 5172

Another option is to use angular distributions for which the CP-even and the CP-odd terms behave differently.



GUNION, HE, PRL77 (1996) 5172  
 AMOR DOS SANTOS EAL PRD96 (2017) 013004

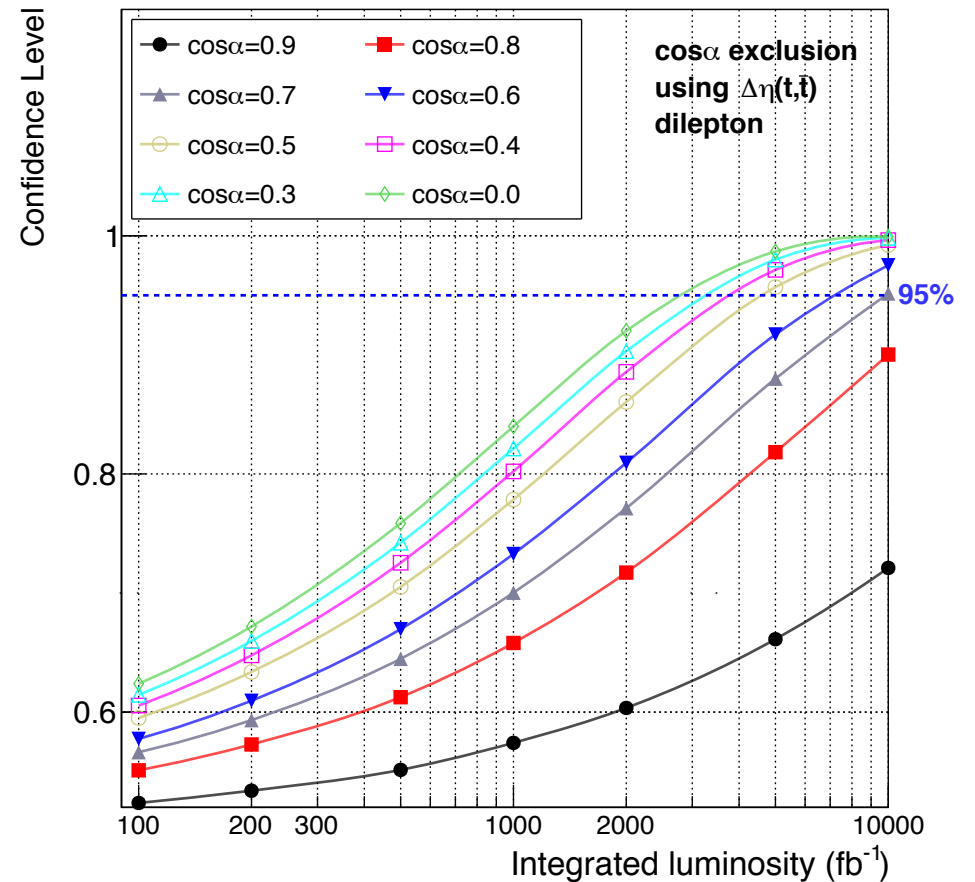
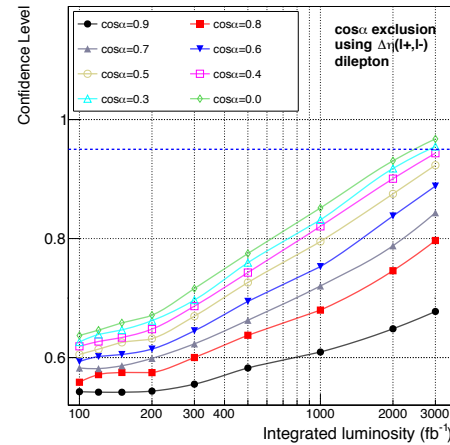
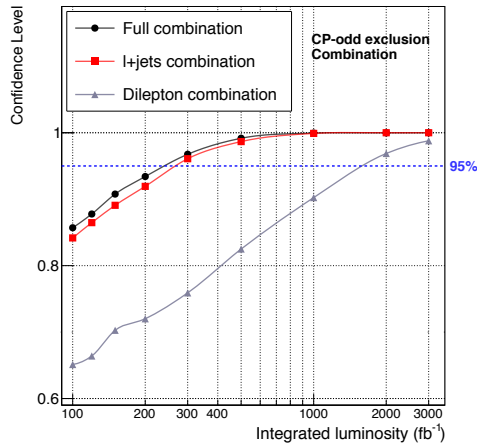
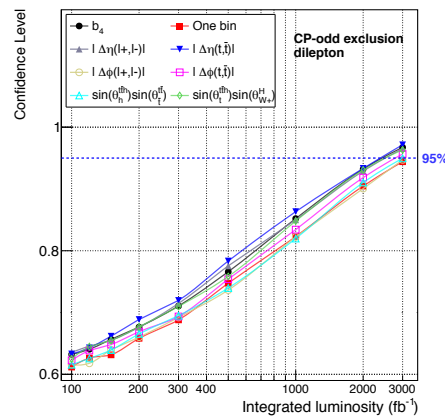
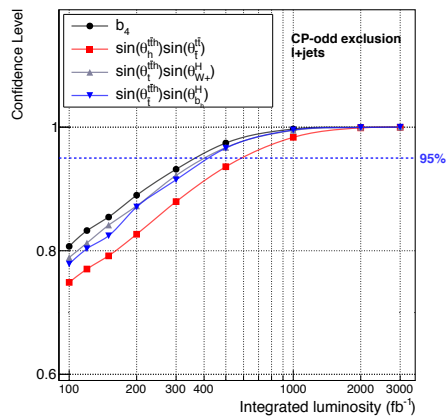
$$b_4 = \frac{p_t^z p_{\bar{t}}^z}{p_t p_{\bar{t}}}$$



$$\mathcal{L}_{H\bar{t}t} = \kappa y_t \bar{t}(\cos \alpha + i \sin \alpha \gamma_5) t h$$

$$\cos \alpha = 1 \quad \text{pure scalar}$$

So, what is bound on the pseudoscalar component of the  $t\bar{t}h$  coupling at the end of the high luminosity LHC?



For  $\cos \alpha = 0.7$  the limit on  $\alpha_2$  is  $46^\circ$  for  $\tan \beta = 1$  while for  $\cos \alpha = 0.9$  is  $26^\circ$  - close to what we have today from indirect measurements.

The difference is that the bound is now directly imposed on the Yukawa coupling.

many other proposals...

$$pp \rightarrow jjh$$

HANKELE, KLAMKE, ZEPPENFELD, 0605117

Using the azimuthal angle between  
the two jets.

Corresponds to the C2HDM in the limit

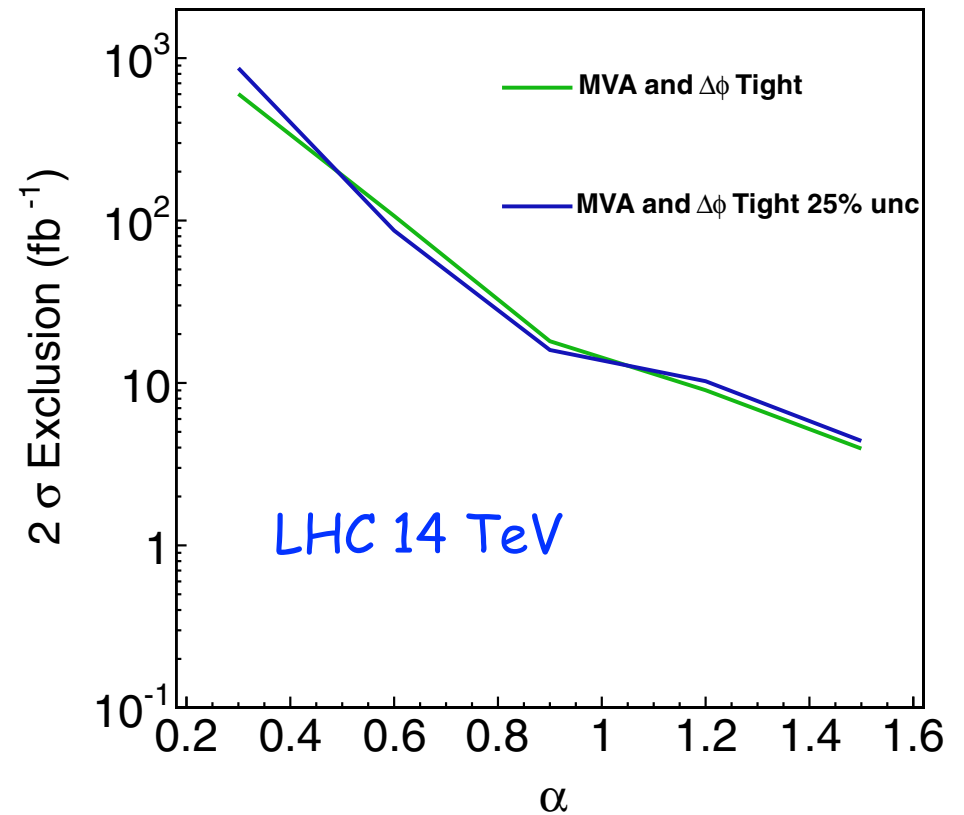
$$\cos(\beta - \alpha_1) = 1; \tan \beta = 1$$

In this case

$$\Phi_\tau = \alpha_2$$

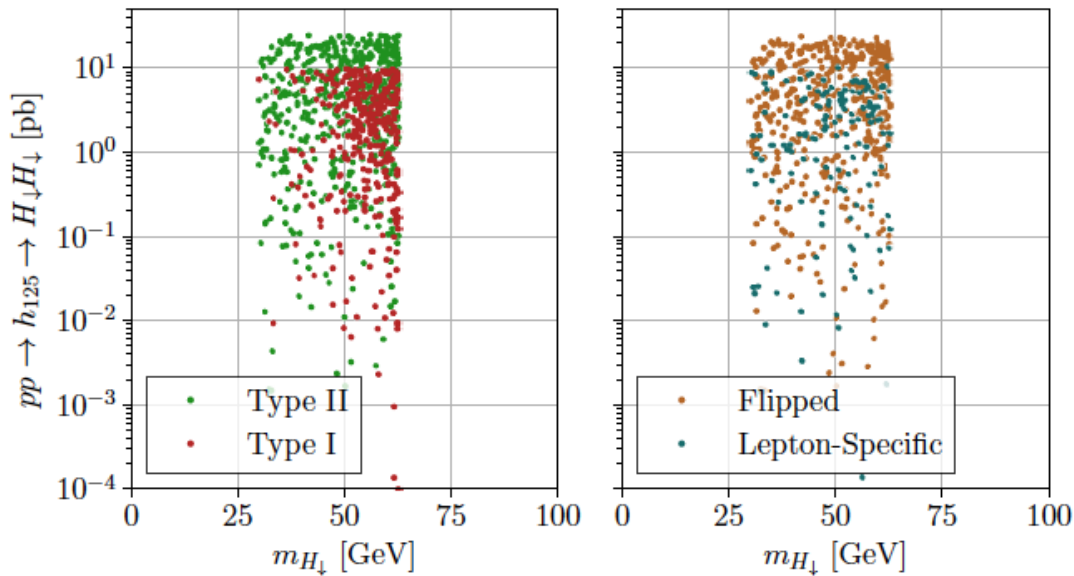
$$\Delta\Phi_\tau = 40^\circ \Leftrightarrow 50 \text{ fb}^{-1}$$

$$\Delta\Phi_\tau = 25^\circ \Leftrightarrow 300 \text{ fb}^{-1}$$

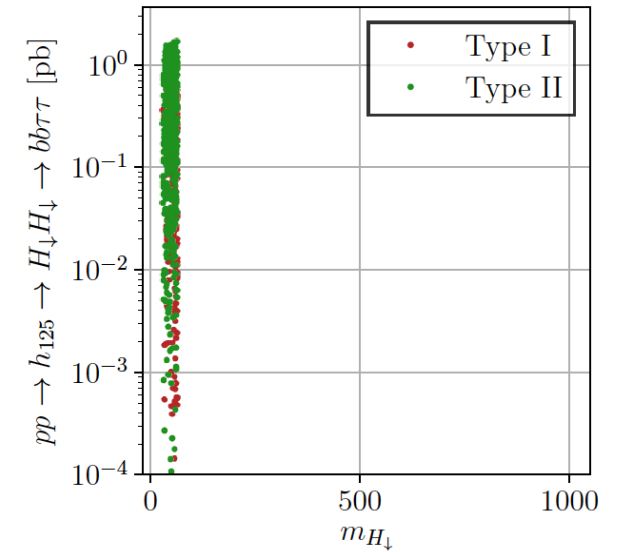


PLOT FROM: DOLAN, HARRIS, JANKOWIAK, SPANNSKY PRD90 (2014) 073008

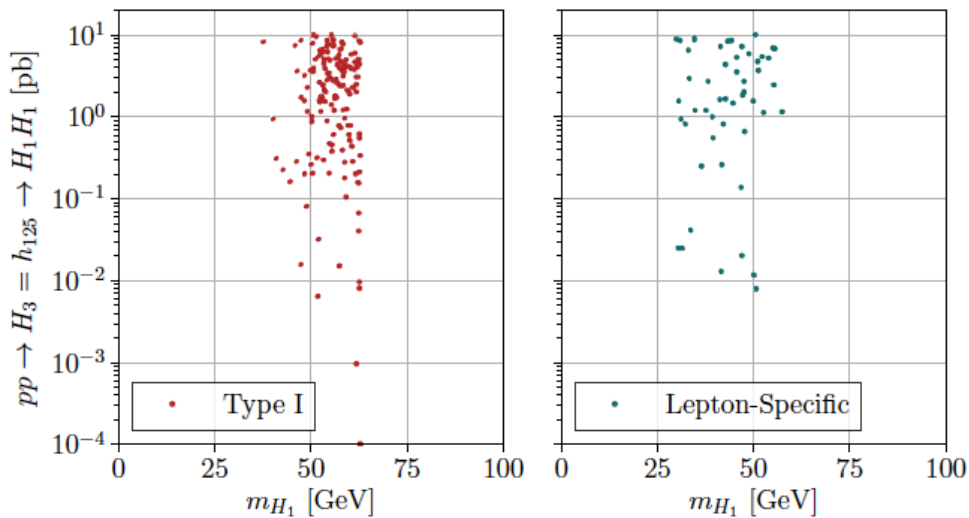
## Signal rates - $h_{125}$ ( $h_3$ or $h_2$ ) to $H_{\downarrow}H_{\downarrow}$ for all types



Maximal rates range from 10 to 30 pb. As an example the final state  $bb\tau\tau$  is still above the pb level.

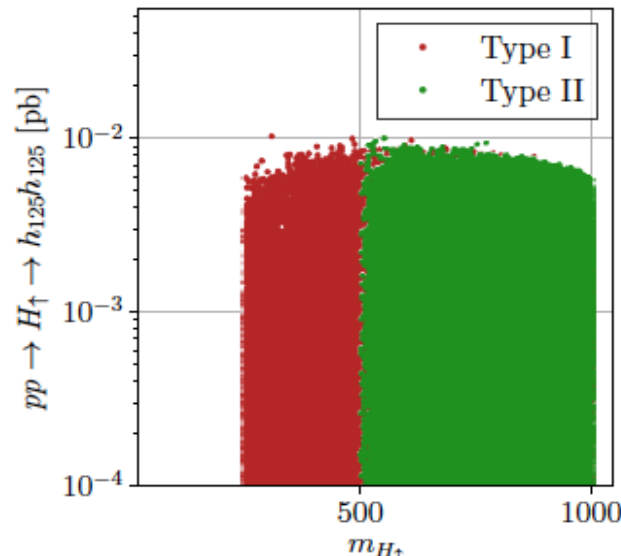
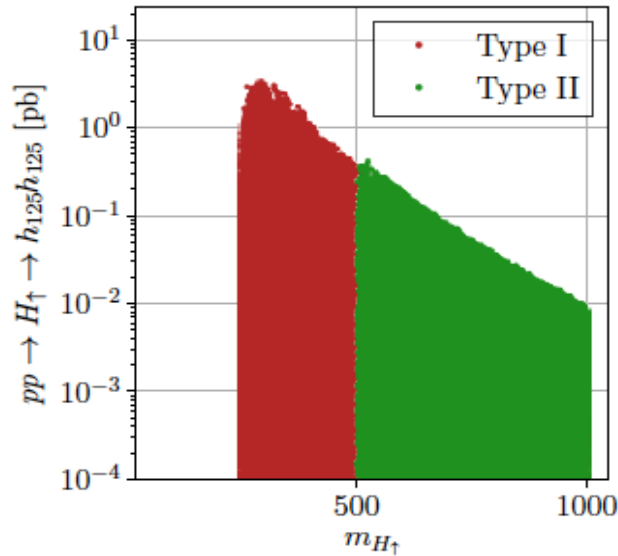
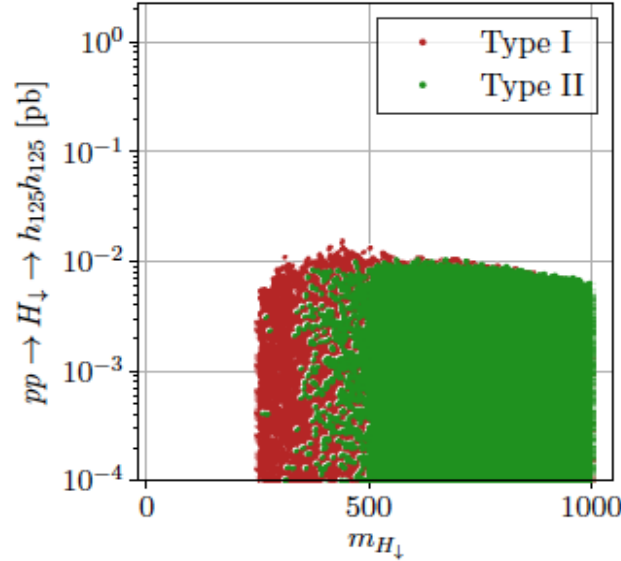
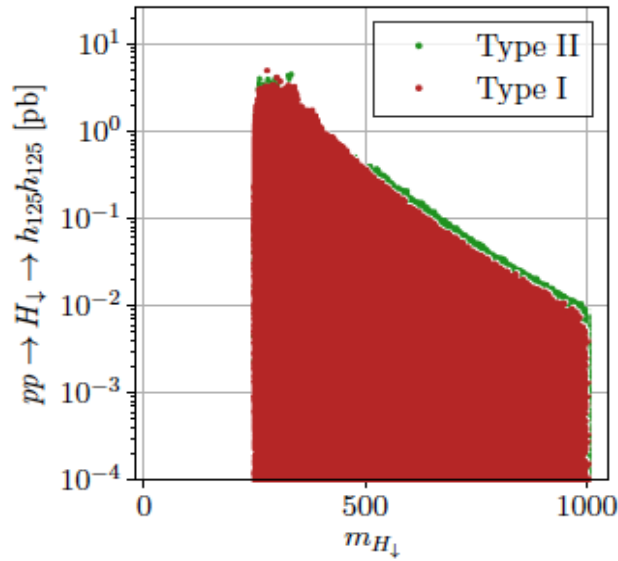


## Decays of $h_{125}$ (just $h_3$ ) to $H_{\downarrow}H_{\downarrow}$ for all types



In the case of the heaviest being the 125 GeV Higgs, signal rates can still be large but only for Type I and LS due to a combination of the bound on the charged Higgs mass and STU.

# Decays to $h_{125} h_{125}$ in Types I and II



**Left** - Signal rates for the production of  $H_{\downarrow}$  (upper) and  $H_{\uparrow}$  (lower) decaying to  $h_{125} h_{125}$  for 13 TeV as a function of  $m_H$ .

**Right** - Same as left with the extra conditions

$$\sigma(pp \rightarrow H_{\downarrow} \rightarrow ZZ) < 1 \text{ fb}$$

$$\sigma(pp \rightarrow H_{\uparrow} \rightarrow ZZ) < 1 \text{ fb}$$

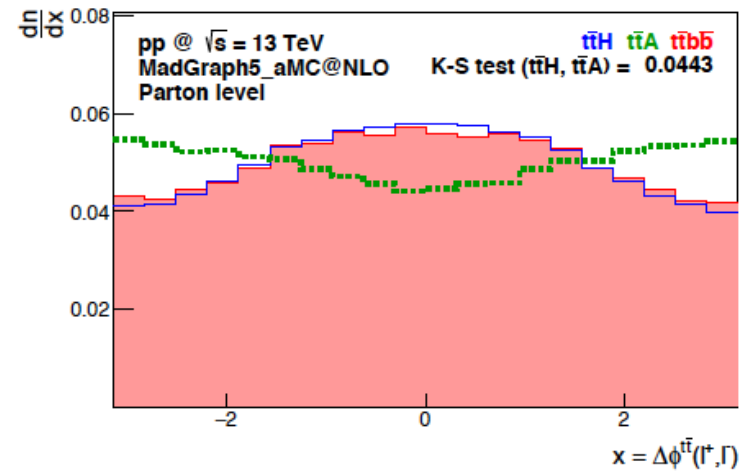
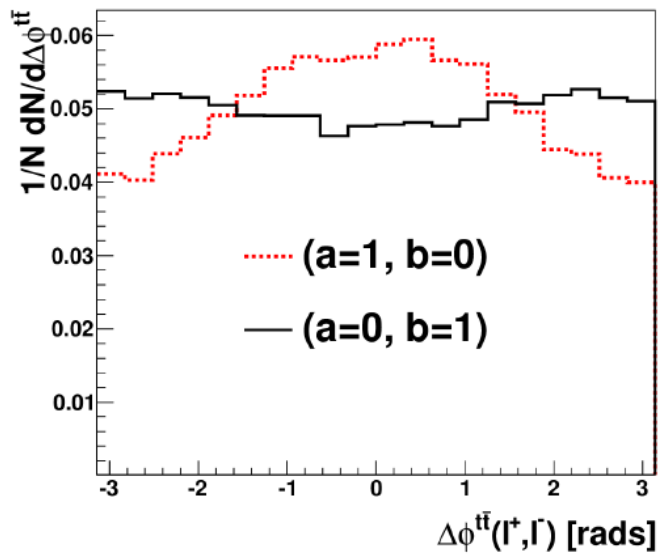
Rates can be above the pb level but are at most 10 fb if we restrict the decays to ZZ to be below 1 fb. Reference cross section for the SM di-Higgs production is about 30 fb.

# Conclusions

- 🍪 The closer we get to the situation where the Higgs couplings to fermions and gauge bosons are very *SM*-like, the harder will be to probe *CP*-violation using decays to *Z* bosons, if a new scalar is found.
- 🍪 Anomalous triple *Z* couplings would be an important measurement in the future if we could increase precision.
- 🍪 There is still a lot to do in the Yukawa sector...
- 🍪 ... and if not at the *LHC*, perhaps at the future *ILC*.
- 🍪 There are still scalars to be discovered with very large production rates.

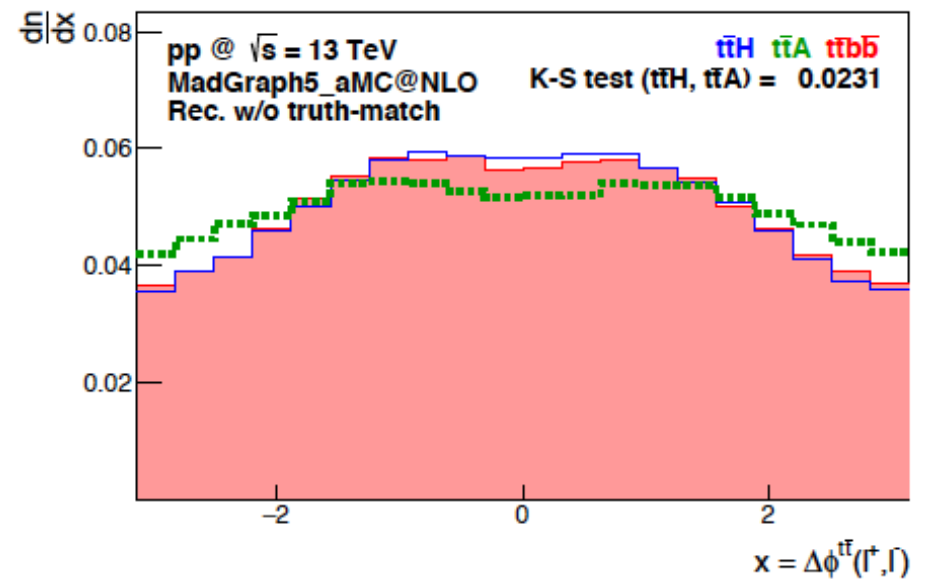
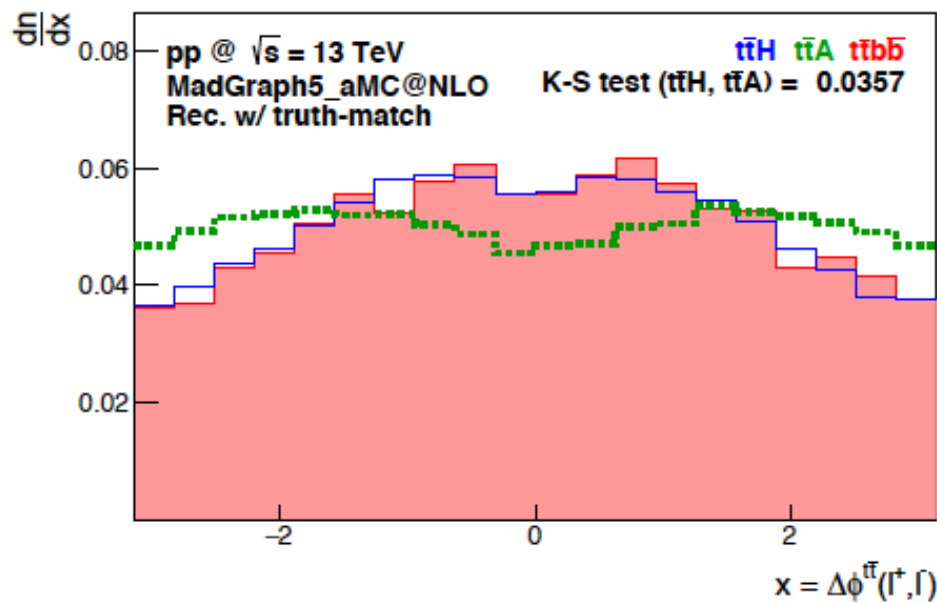


**The end**



BOUDJEMA, GODBOLE, GUADAGNOLI, MOHAN 2015

Azimuthal difference between  $l^+$  in the  $t$  rest frame and  $l^-$  in the  $t\bar{b}$  rest frame



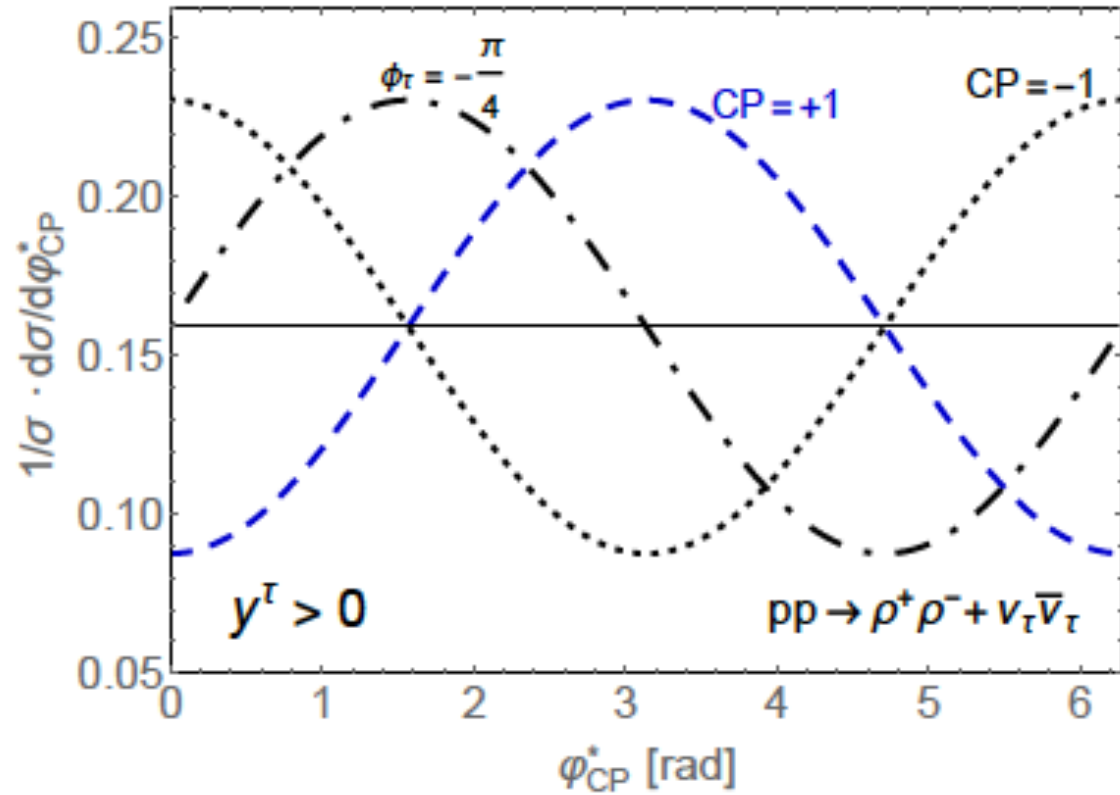
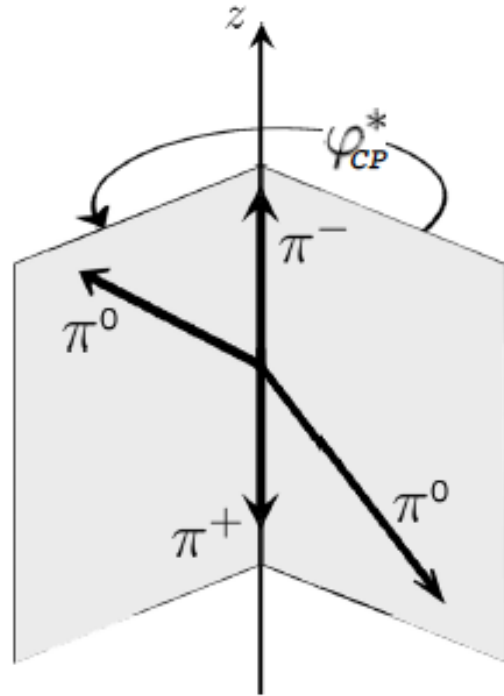


Illustration of  $\varphi_{CP}^*$  in the  $\rho$  decay-plane method as defined in (14) for  $pp \rightarrow h^0 \rightarrow \tau^- \tau^+ \rightarrow \rho^- \rho^+ + 2\nu$ .

## Direct probing at the LHC

- For the C2HDM we need three independent measurements

$$\tan\phi_i = \frac{b_i}{a_i}; \quad i = U, D, L$$

- Just one measurement for type I ( $U = D = L$ ), two for the other three types. At the moment there are studies for  $t\bar{t}h$  and  $\tau\bar{\tau}h$ .
- If  $\phi_{\dagger} \neq \phi_{\tau}$  type I and F ( $Y$ ) are excluded.
- To probe model F ( $Y$ ) we need the  $bbh$  vertex.

## What if the 125 GeV reveals different CP behaviour in two decay channels?

The SM-like Higgs coupling to ZZ(WW) relative to the corresponding SM coupling is

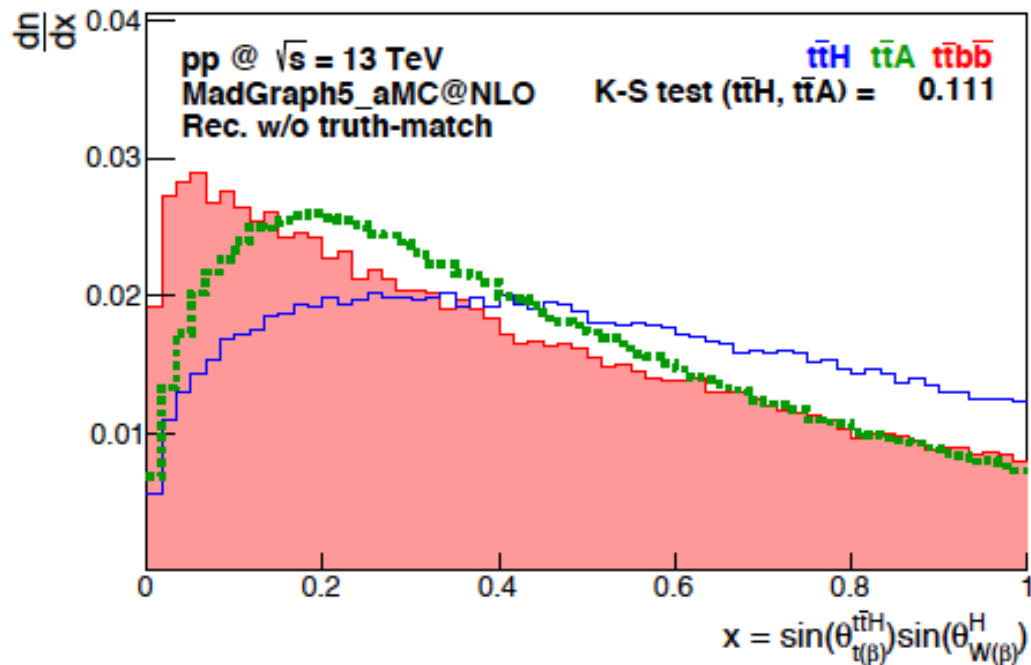
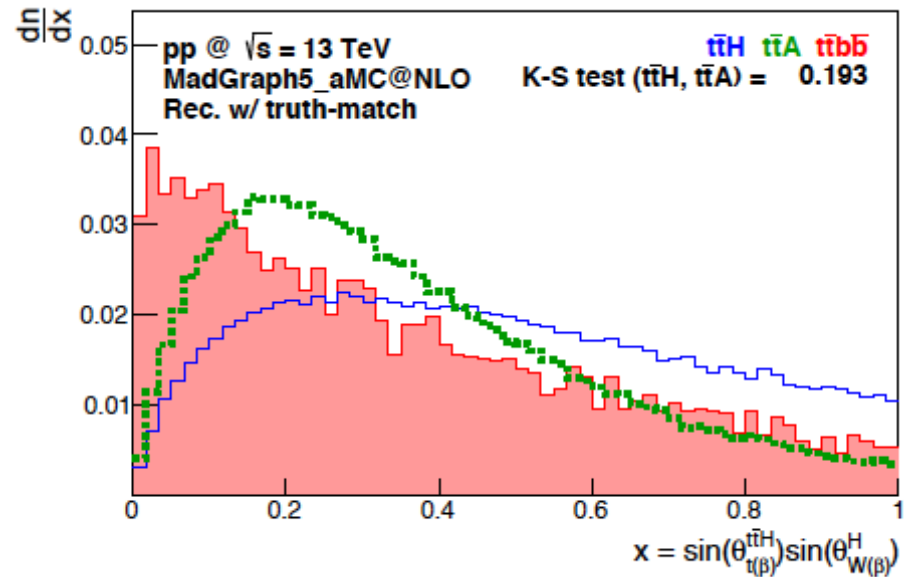
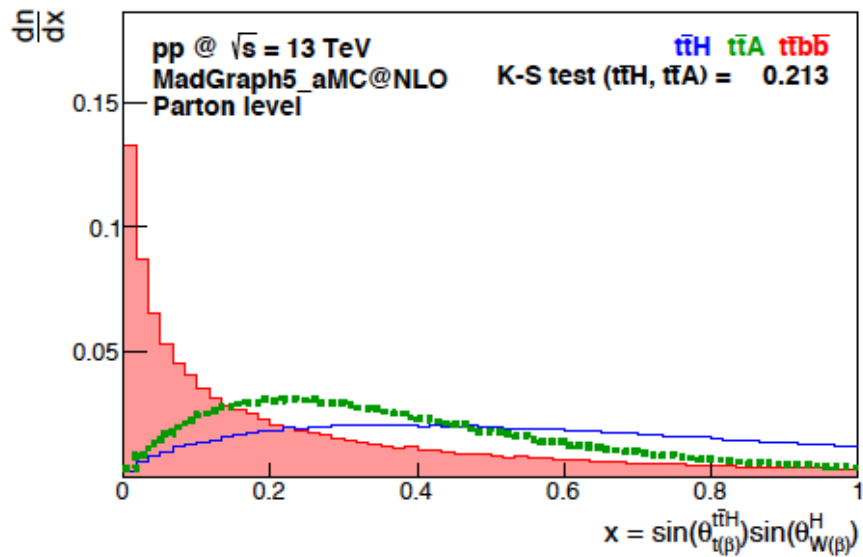
$$\kappa_{C2HDM}^{h_{125}WW} = c_2 \sin(\beta - \alpha)$$

and  $c_2$  cannot be far from 1. But  $\alpha_2$  is the CP-violating angle and therefore it should be small. However, the CP-odd component has an extra  $\tan\beta$  factor for down quarks and leptons, but not for the up quarks

$$Y_{C2HDM}^{TypeII} = c_2 Y_{2HDM}^{TypeII} - i\gamma_5 s_2 t_\beta \quad \text{bottom, tau}$$

$$Y_{C2HDM}^{TypeII} = c_2 Y_{2HDM}^{TypeII} - i\gamma_5 \frac{s_2}{t_\beta} \quad \text{top}$$

Thus, the SM-like Higgs couplings to the tops could be mainly CP-even while couplings to the bottoms and taus could be mainly CP-odd.



AMOR DOS SANTOS EAL 2015

Combinatorial background plays a very important role.