

Higgs precision (new physics) at the ILC

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Osaka University, Osaka

Outline

- Higgs precision for cosmology (EW baryogenesis)
- Consequences of 1st-order EW phase transition (EWPT)
 - Higgs couplings & spectrum
 - Gravitational waves (GWs)
- Higgs CP nature ($h \rightarrow \tau\tau$)
- Summary

Report by the Committee on the Scientific Case of the ILC Operating at 250 GeV as a Higgs Factory (1710.08639)

ILC	Higgs & other SM precision measurements; electroweak baryogenesis; 2.1(b): higgsinos, and DM lighter than 62 GeV; 2.1(c): small $\tan\beta$.
HL-LHC	Higgs couplings; direct search of new phenomena; top quark mass; 2.1(a),(b): bino, wino; 2.1(c): large $\tan\beta$.
SuperKEKB	Additional CP violation in quark-sector; bottom quark mass; tau LFV (GUT); 2.1(c): large $\tan\beta$.
T2K, HK	CPV in neutrino-sector; leptogenesis; GUT.
LFV	Leptogenesis; right-handed neutrinos; GUT.
EDM	Flavor-conserving additional CP violation; electroweak baryogenesis.
LISA, DECIGO	First-order phase transition for electroweak baryogenesis: an alternative to the HHH coupling measurement.
Underground experiments	DM direct search; 2.1(b): heavy regions.

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EWBG tests

- We cannot redo EWPT in lab. exp. So, we test Sakharov cond. instead.

**Sakharov
conditions**

~~B~~

~~CP~~

out of equilibrium

sphaleron

CPV bubble-
particle ints.

1st-order EWPT
w/ bubbles

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Extended Higgs sector

ILC



spheron at colliders?

EDMs
b->s γ

h->ff

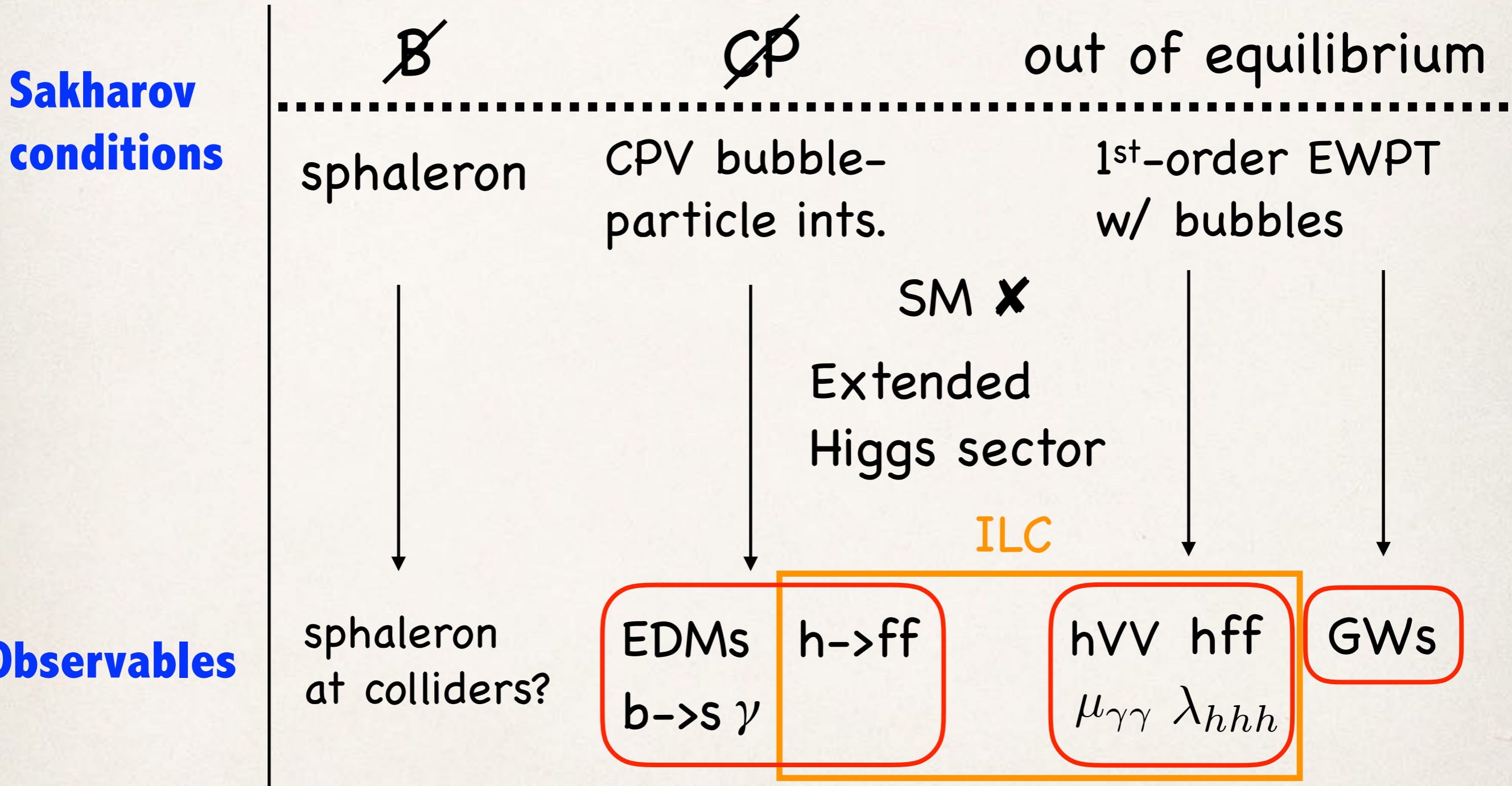
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- We cannot redo EWPT in lab. exp. So, we test Sakharov cond. instead.



- Sizes of the deviations in the Higgs couplings and Higgs spectrum are determined by "**B-preserving condition**".

EWBG mechanism

symmetric phase

$$\langle \Phi \rangle = 0$$

H: Hubble constant

$$\Gamma_B^{(s)} > H$$

$$f, \bar{f}$$

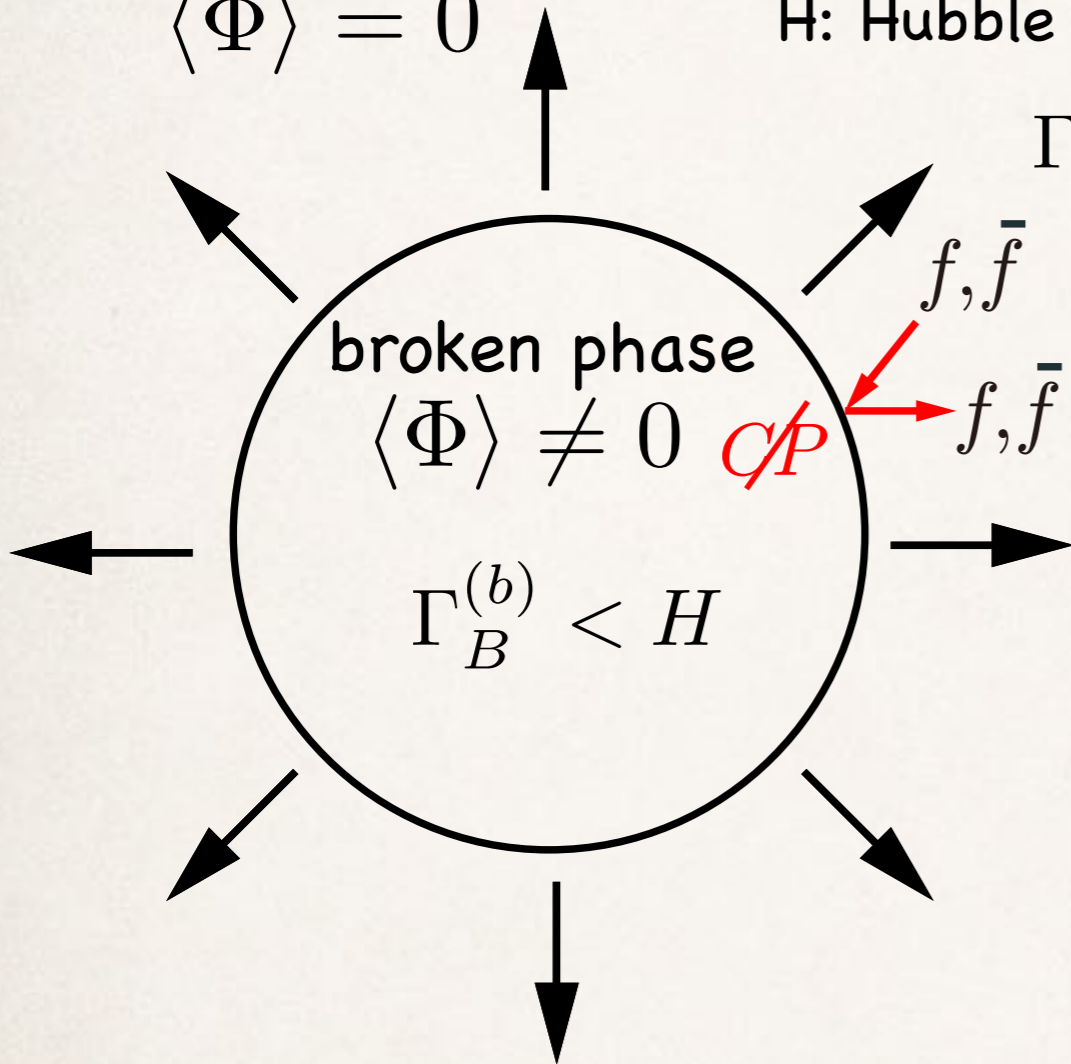
broken phase

$$\langle \Phi \rangle \neq 0$$

~~C/P~~

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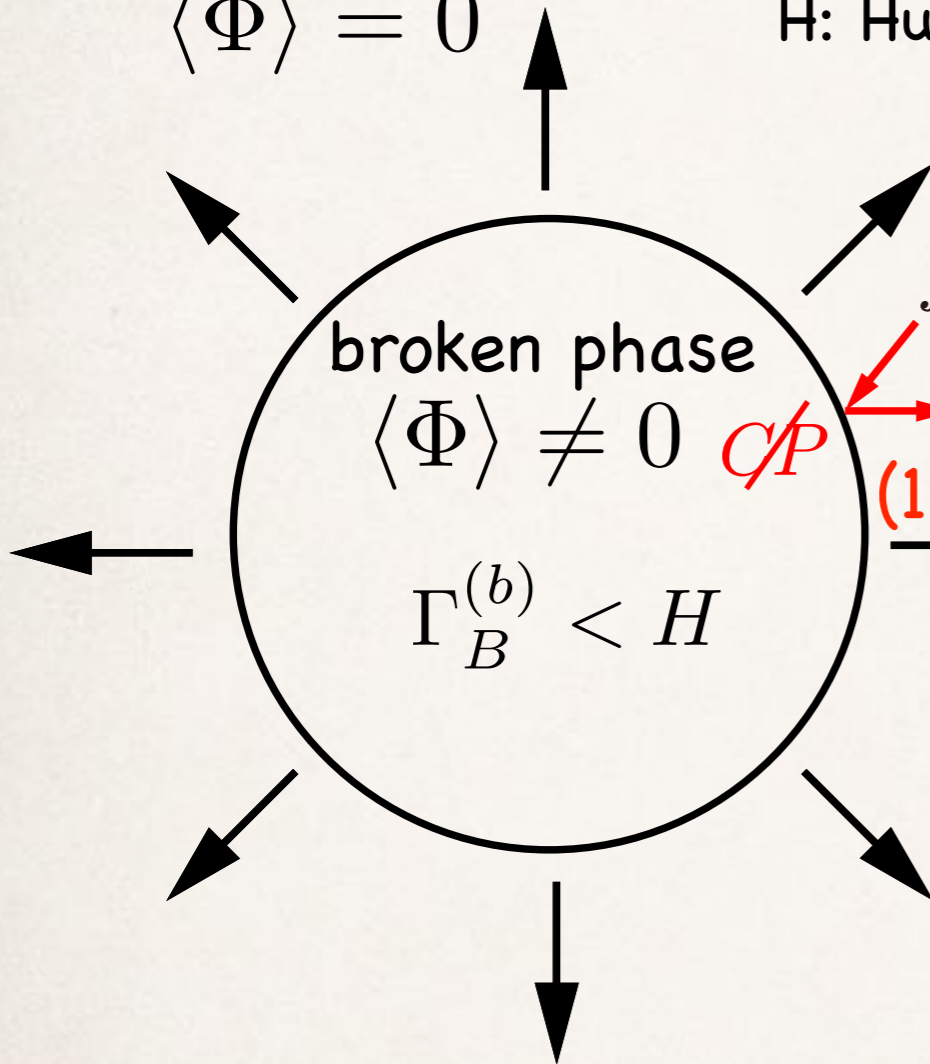
f, \bar{f}

$$(1) n_B = n_B^L + n_B^R = 0$$

$\neq 0 \quad \neq 0$

$$\Gamma_B^{(b)} < H$$

CP asymmetric but no B asymmetric

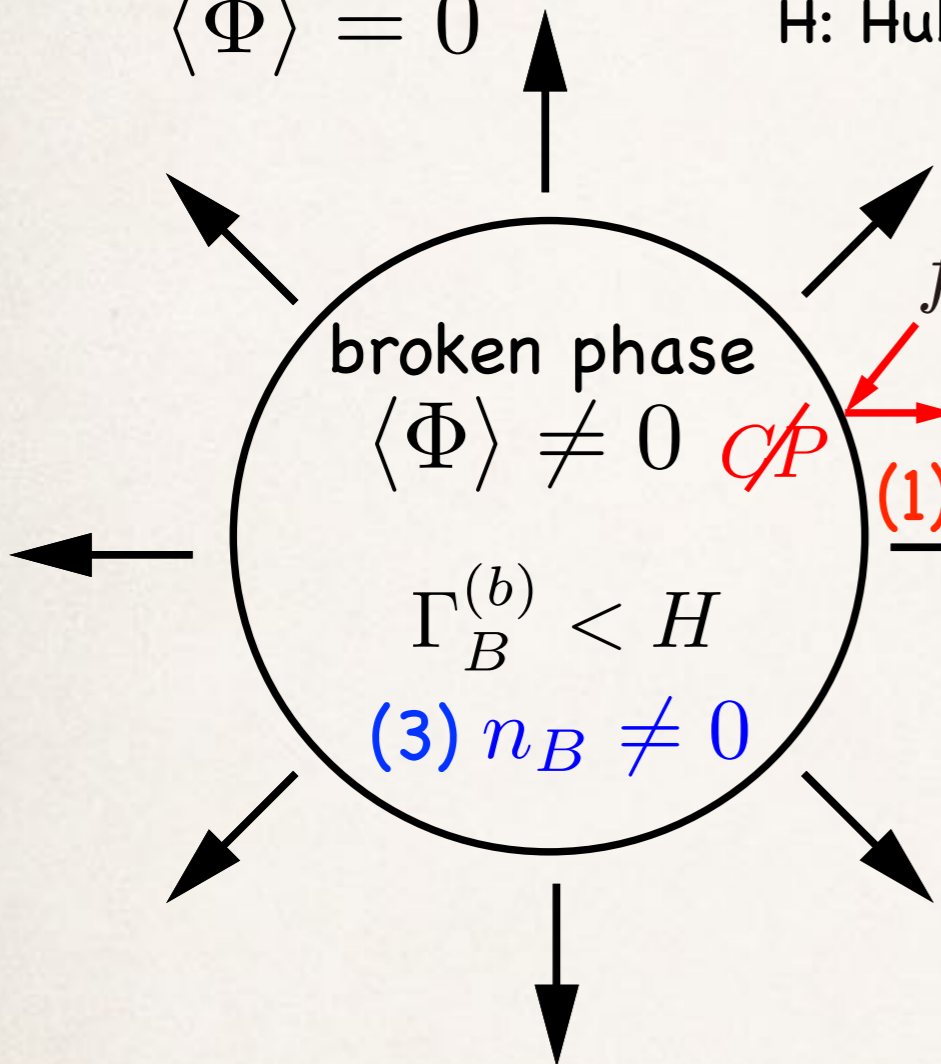


EWBG mechanism

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broken phase

$$\langle \Phi \rangle \neq 0$$

CP

$$\Gamma_B^{(b)} < H$$

$$(3) n_B \neq 0$$

$$\Gamma_B^{(s)} > H$$

changed by sphaleron. $t_{\text{wall}} < t_{\text{sph}}$

f, \bar{f}

$$(2) n_B = n_B^L + n_B^R \rightarrow n_B \neq 0$$

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baryogenesis!!

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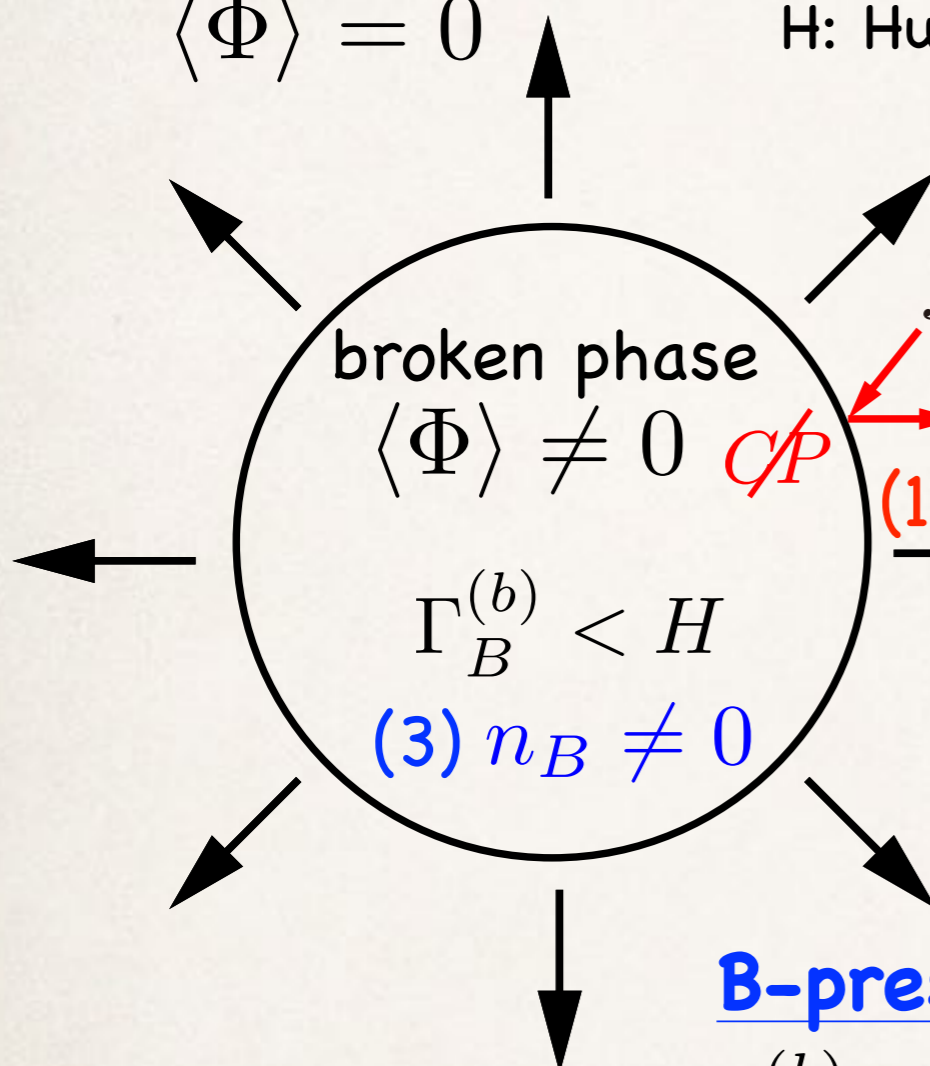
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B-preservation condition

$$\Gamma_B^{(b)} \sim e^{-4\pi \mathcal{E}_{\text{sph}} v / g_2 T} < H$$



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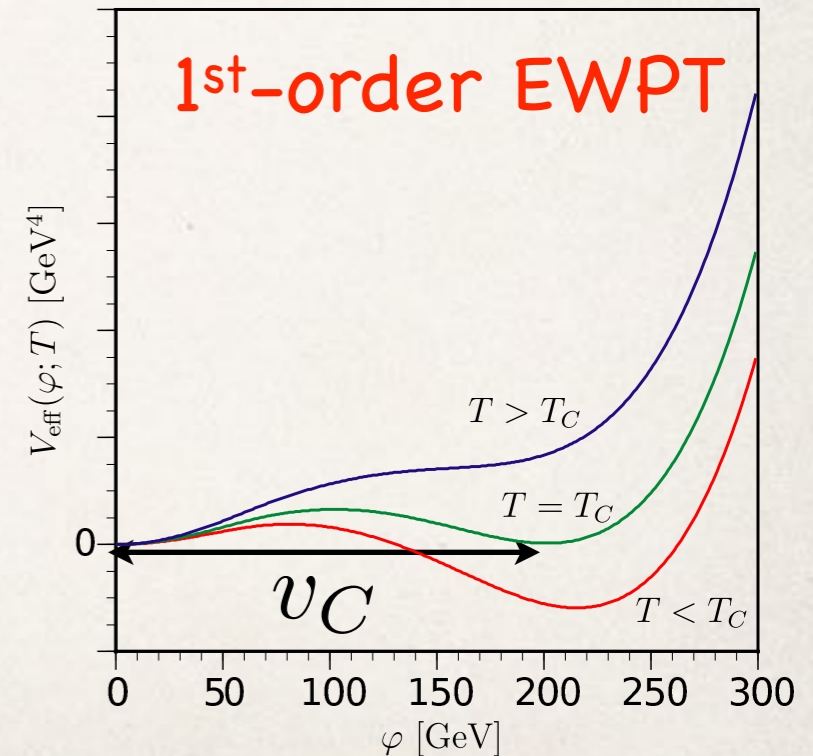
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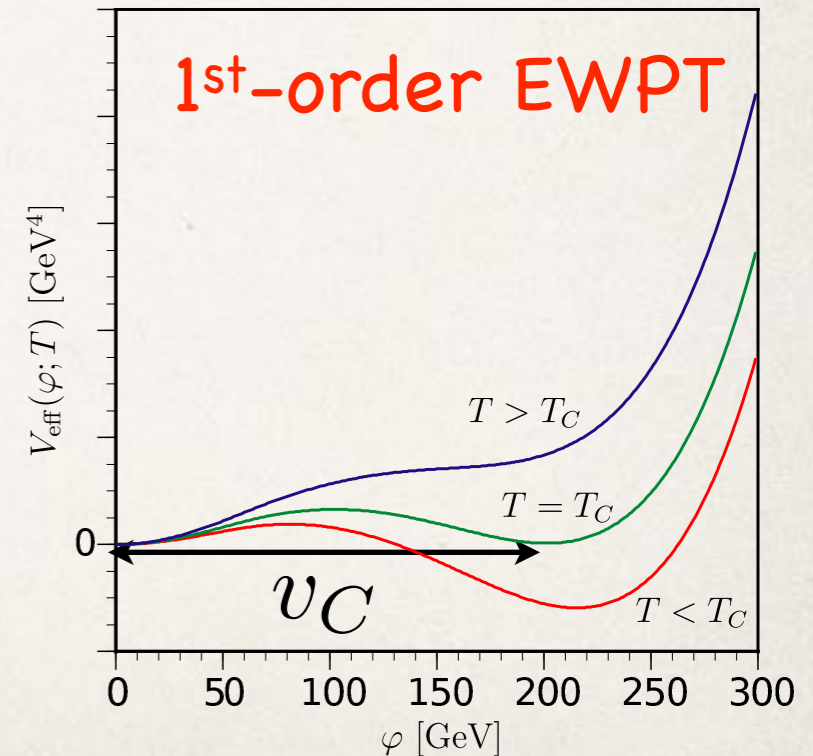
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Higgs spectrum



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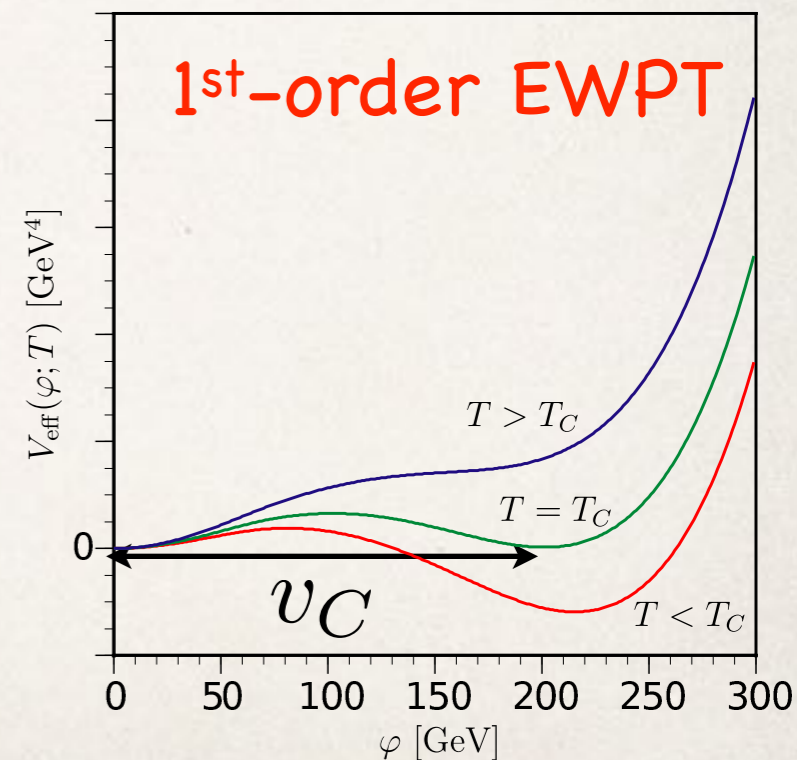
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model-dependent

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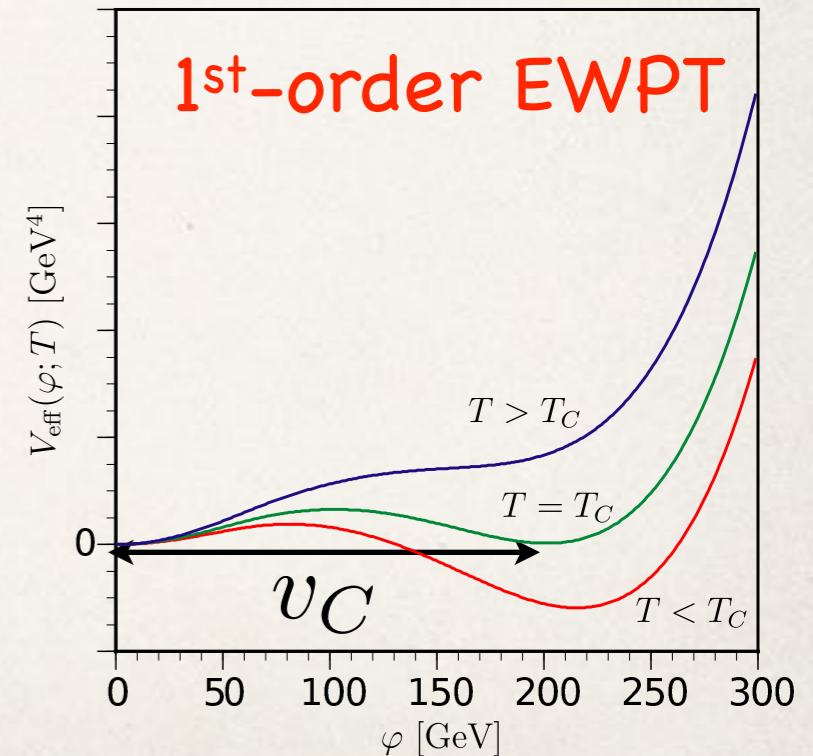
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Higgs spectrum

constrained by exp. data

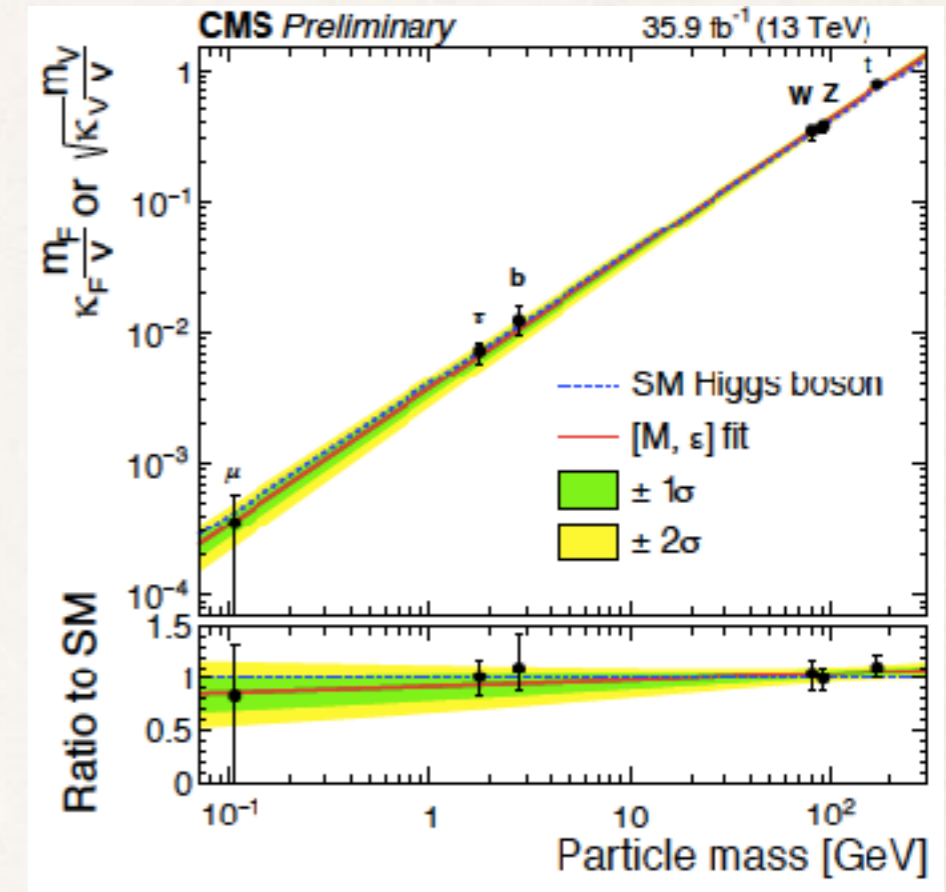


EWBG in our time

LHC data indicate

Higgs sector = SM-like

What is "SM-like Higgs sector"
compatible with EWBG?



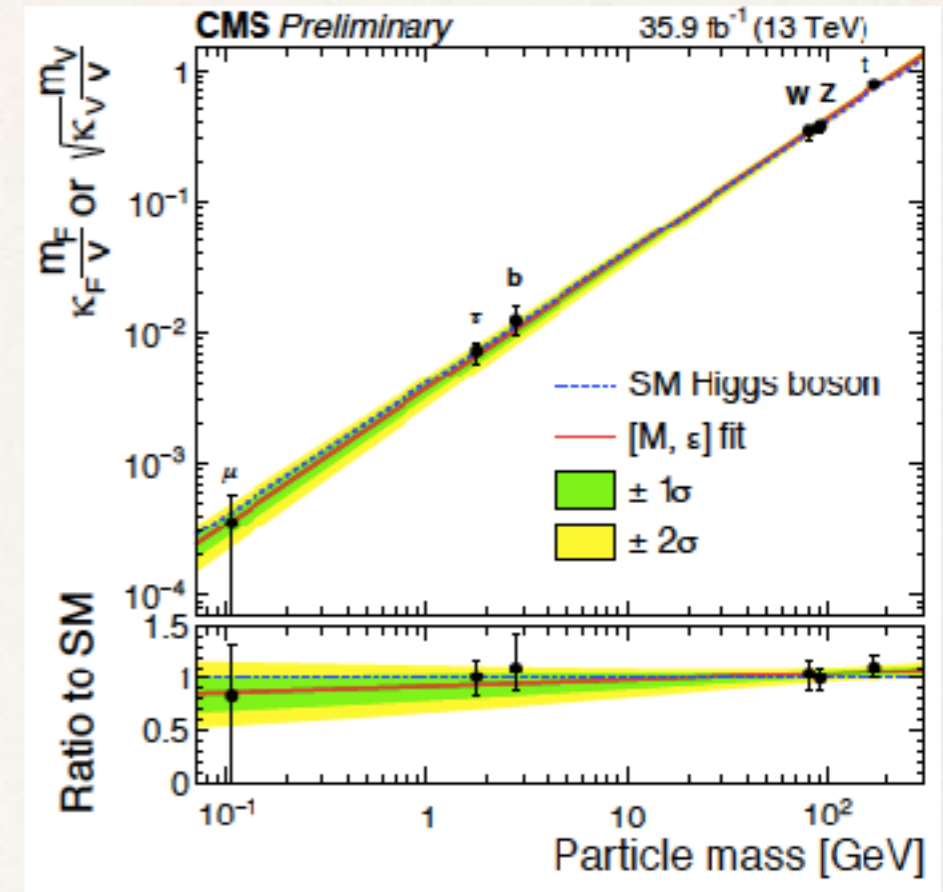
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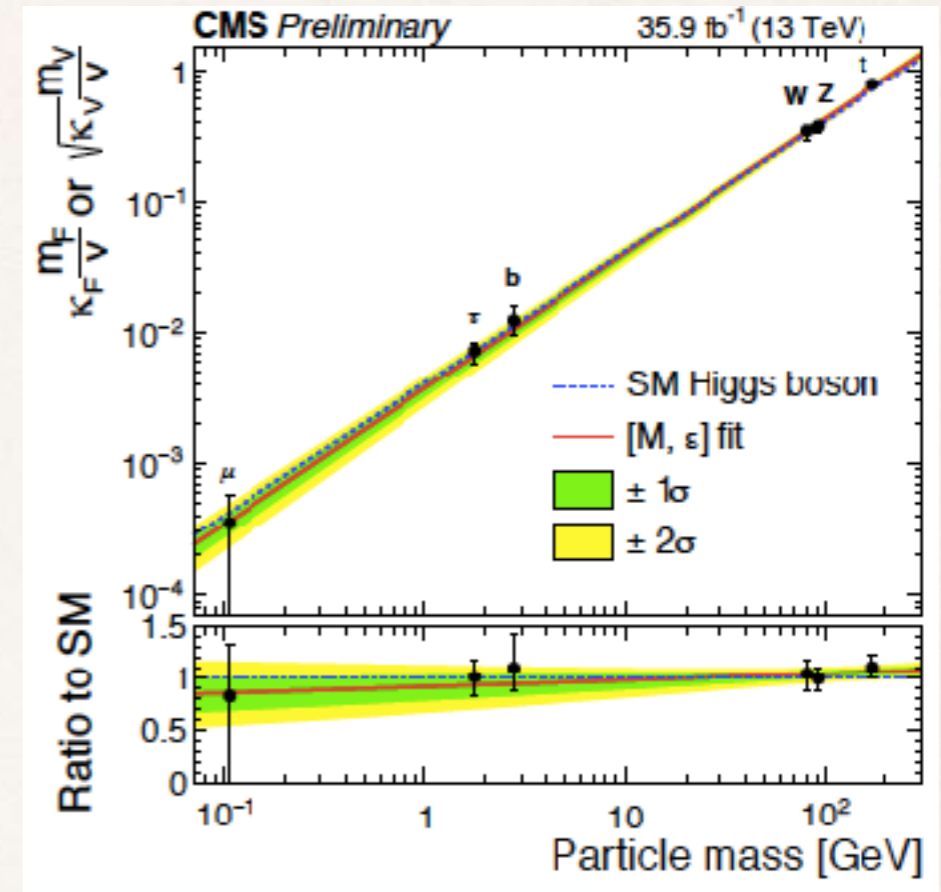
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e.g. 2HDM

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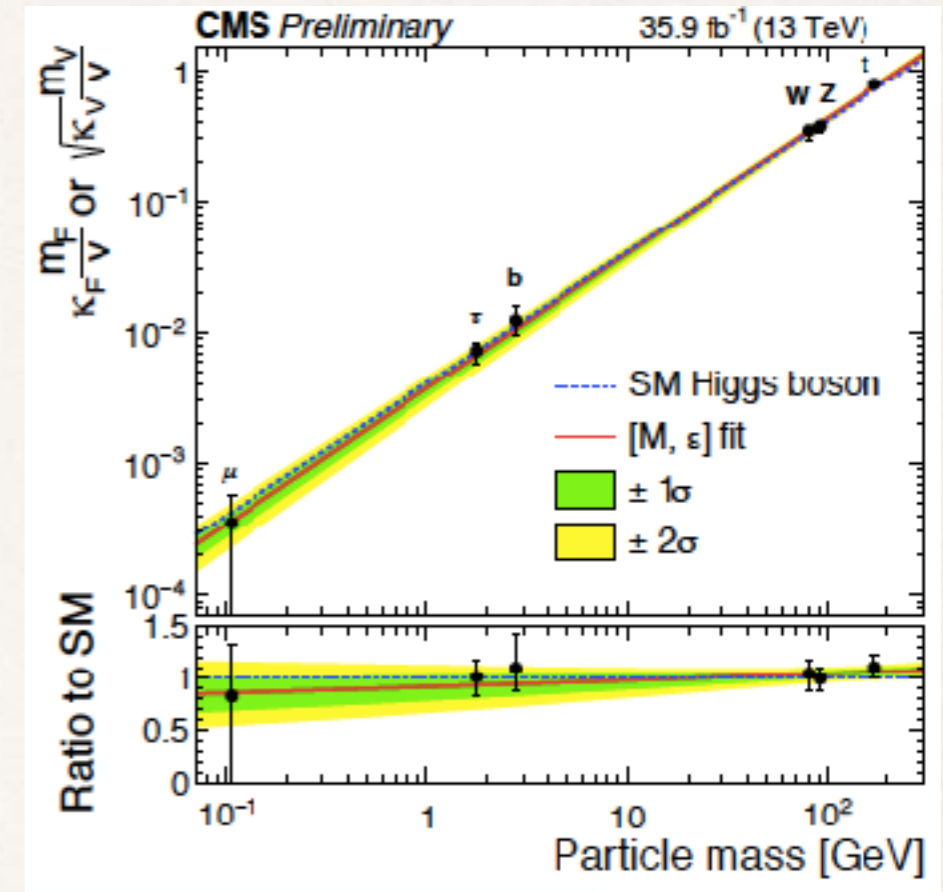
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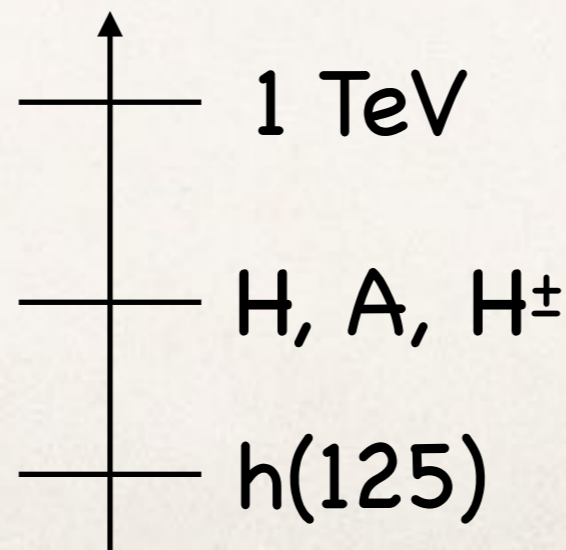
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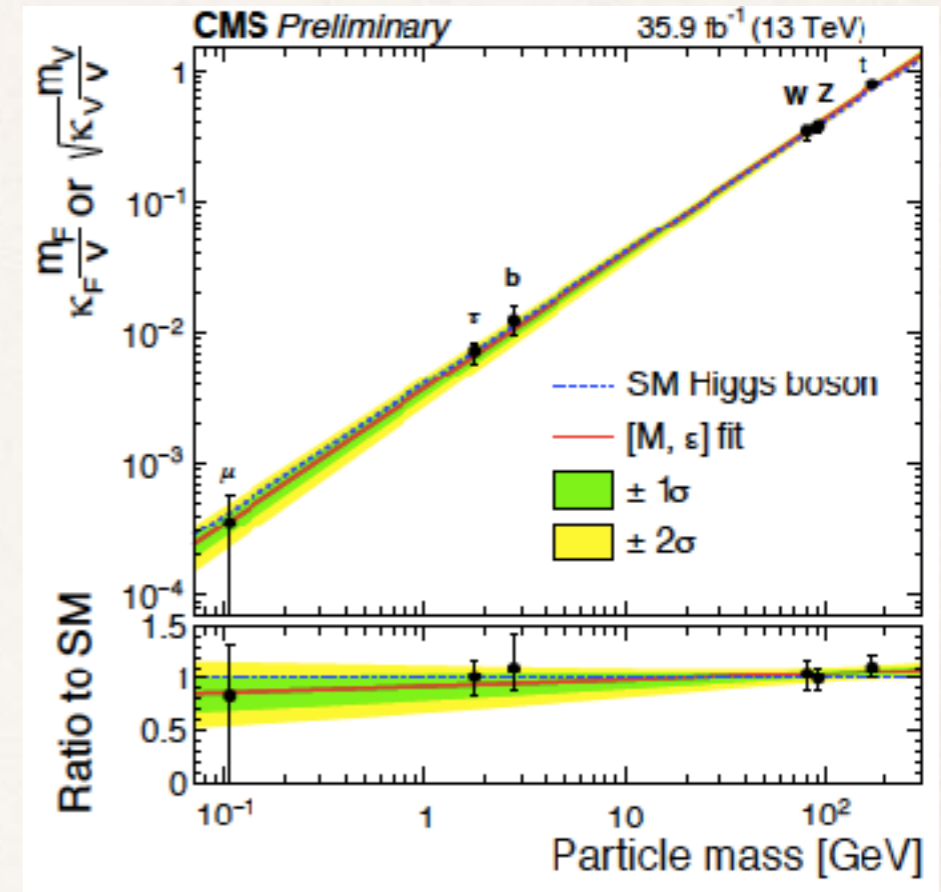
to satisfy $v_C/T_C \gtrsim 1$

$$\lambda_{h\phi\phi} = \mathcal{O}(1) \quad (\phi = H, A, H^\pm)$$



hhh = NonSM-like

[S.Kanemura, Y.Okada, E.S, hep-ph/0411354 (PLB)]



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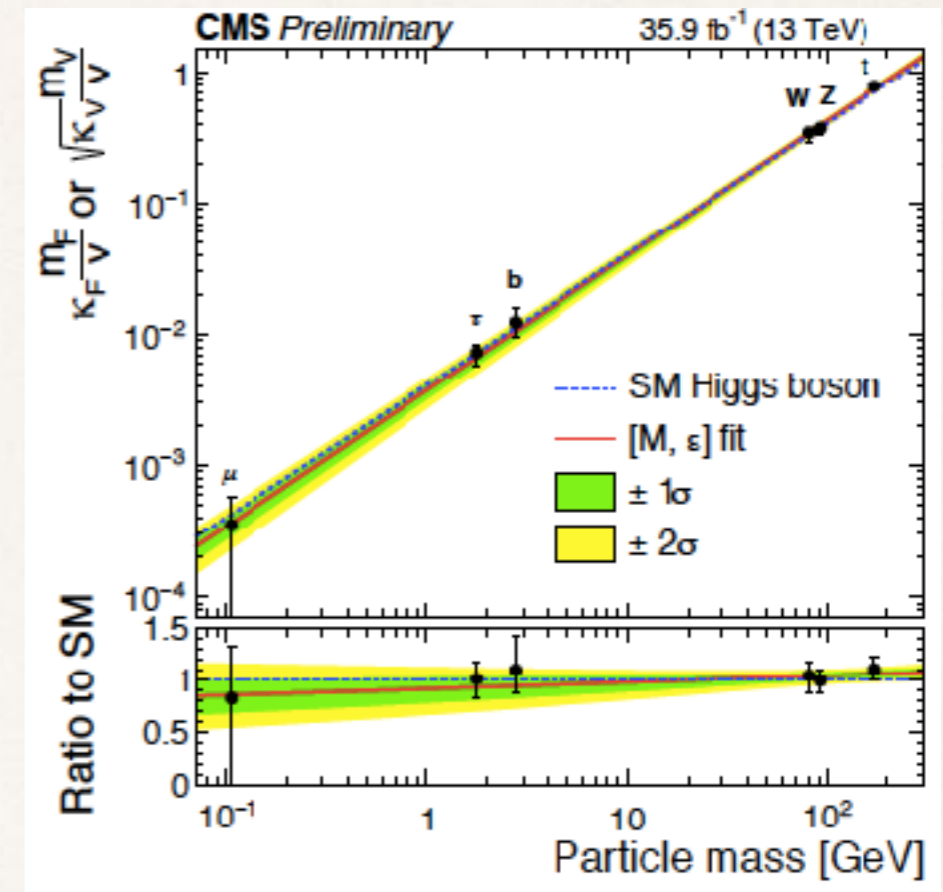
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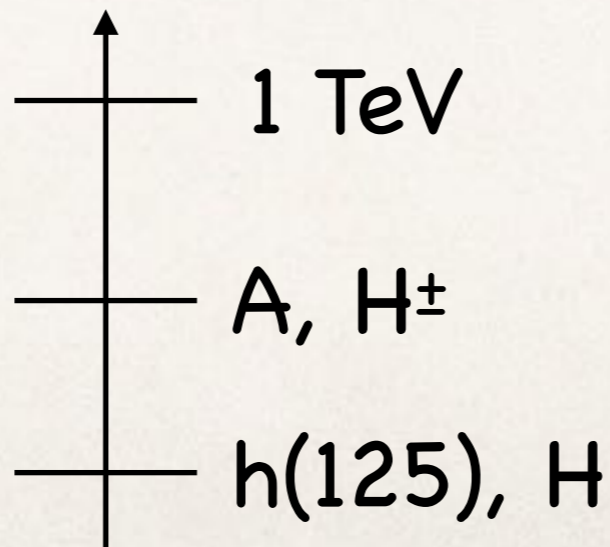
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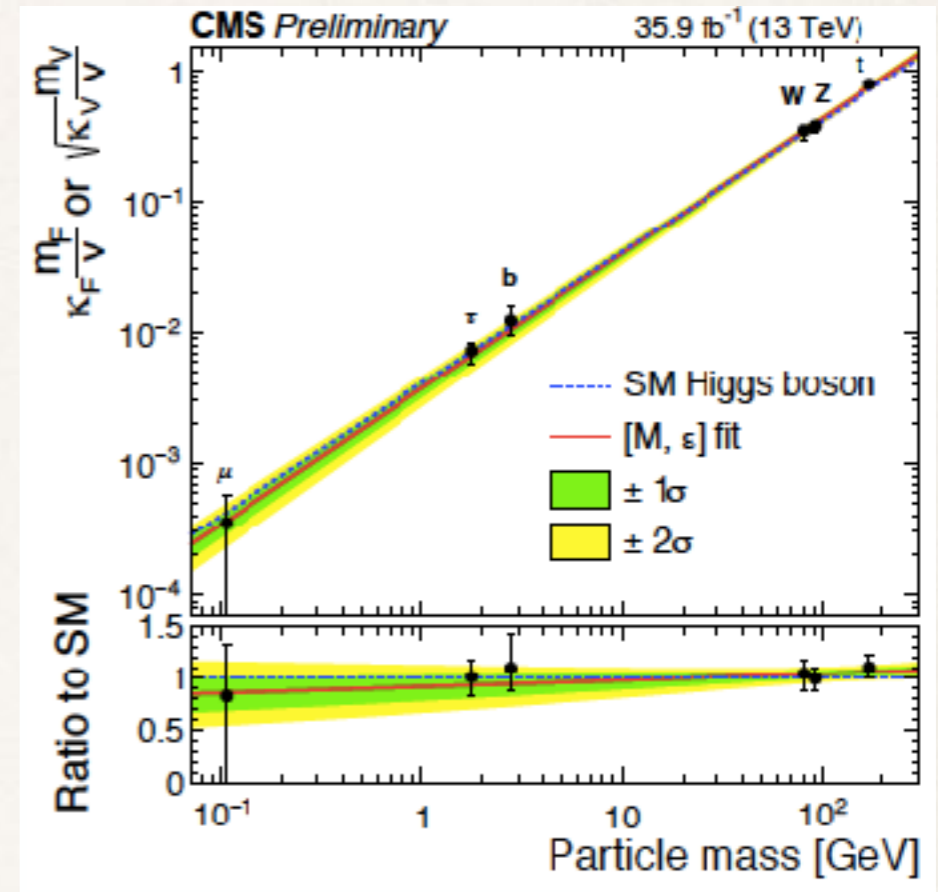
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$$\square A \rightarrow ZH \propto \sin(\beta - \alpha)$$

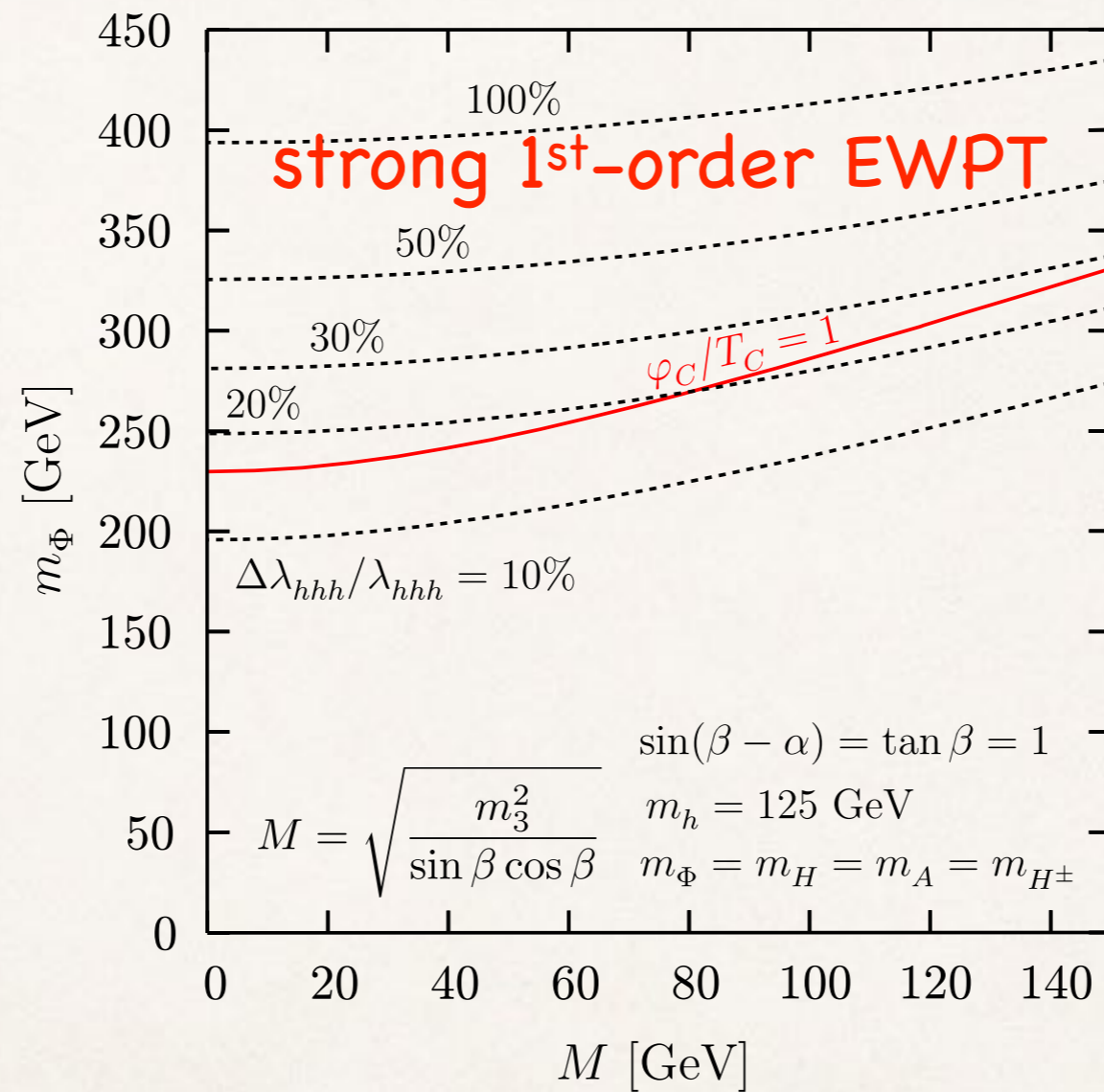
[G.C.Dorsch, S.J.Huber, K.Mimasu, J.M.No, 1405.4437(PRL)]



Parameter space of EWBG

2HDM

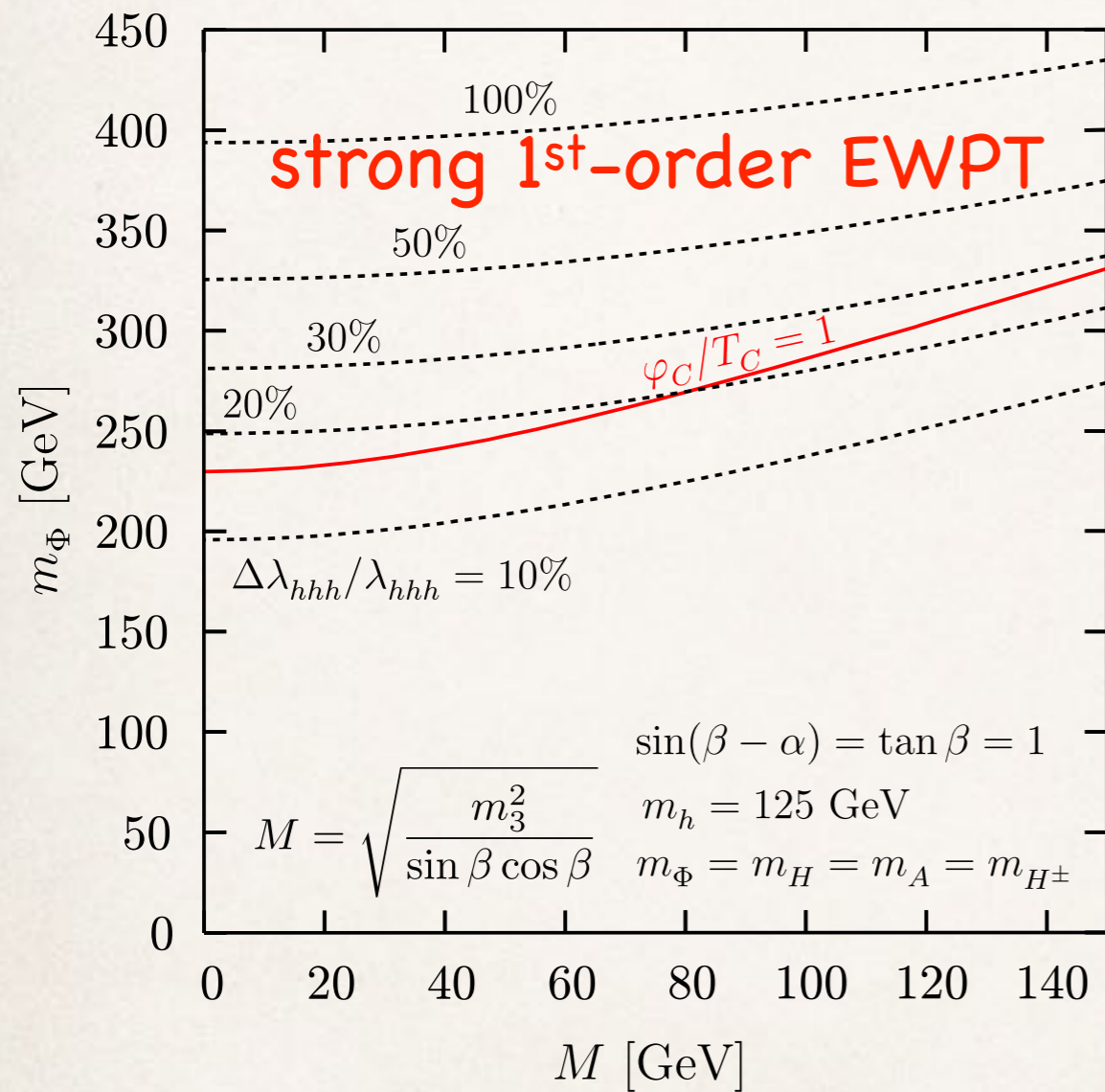
[Kanemura, Okada, E.S., PLB606,(2005)361]



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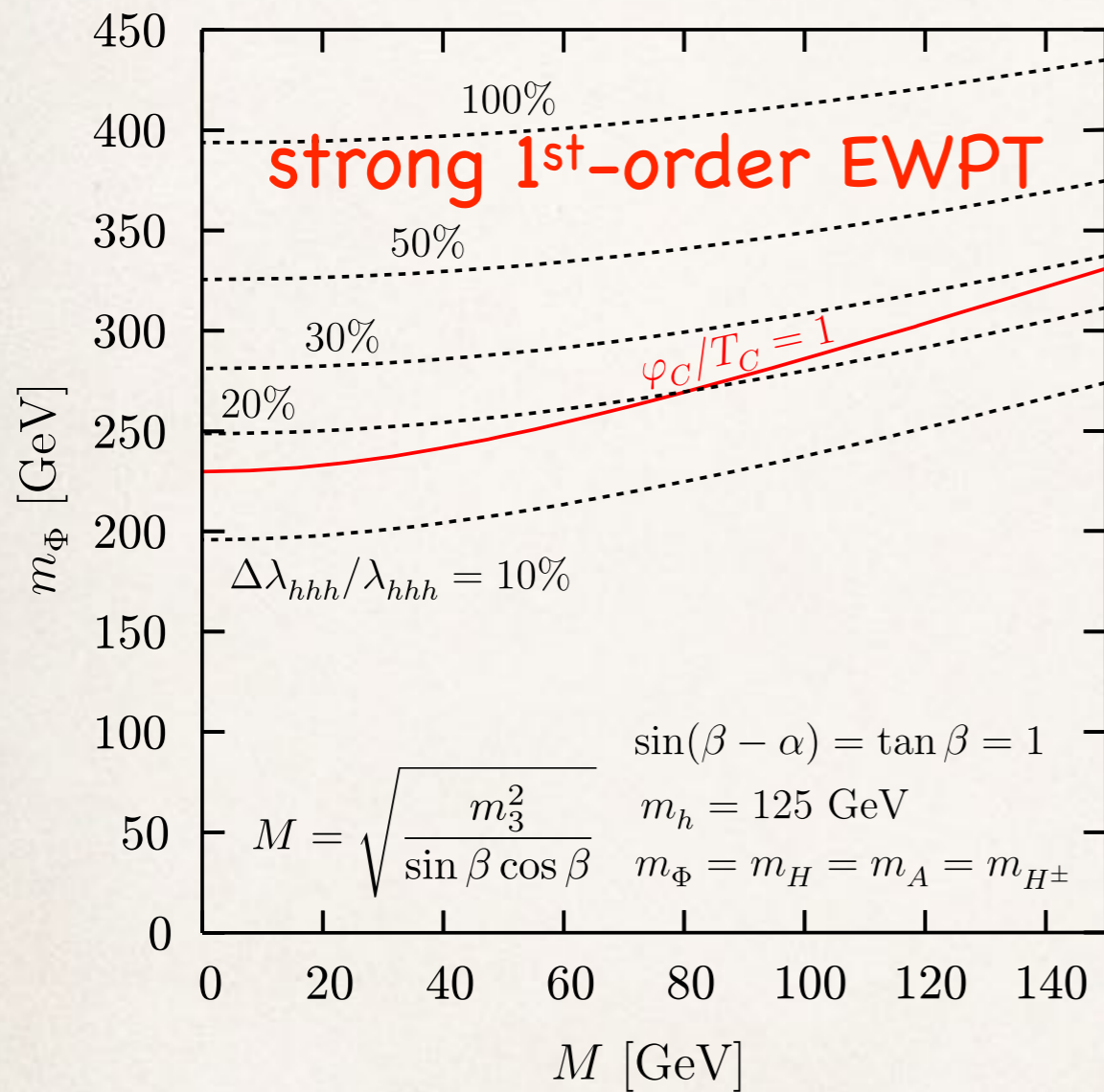
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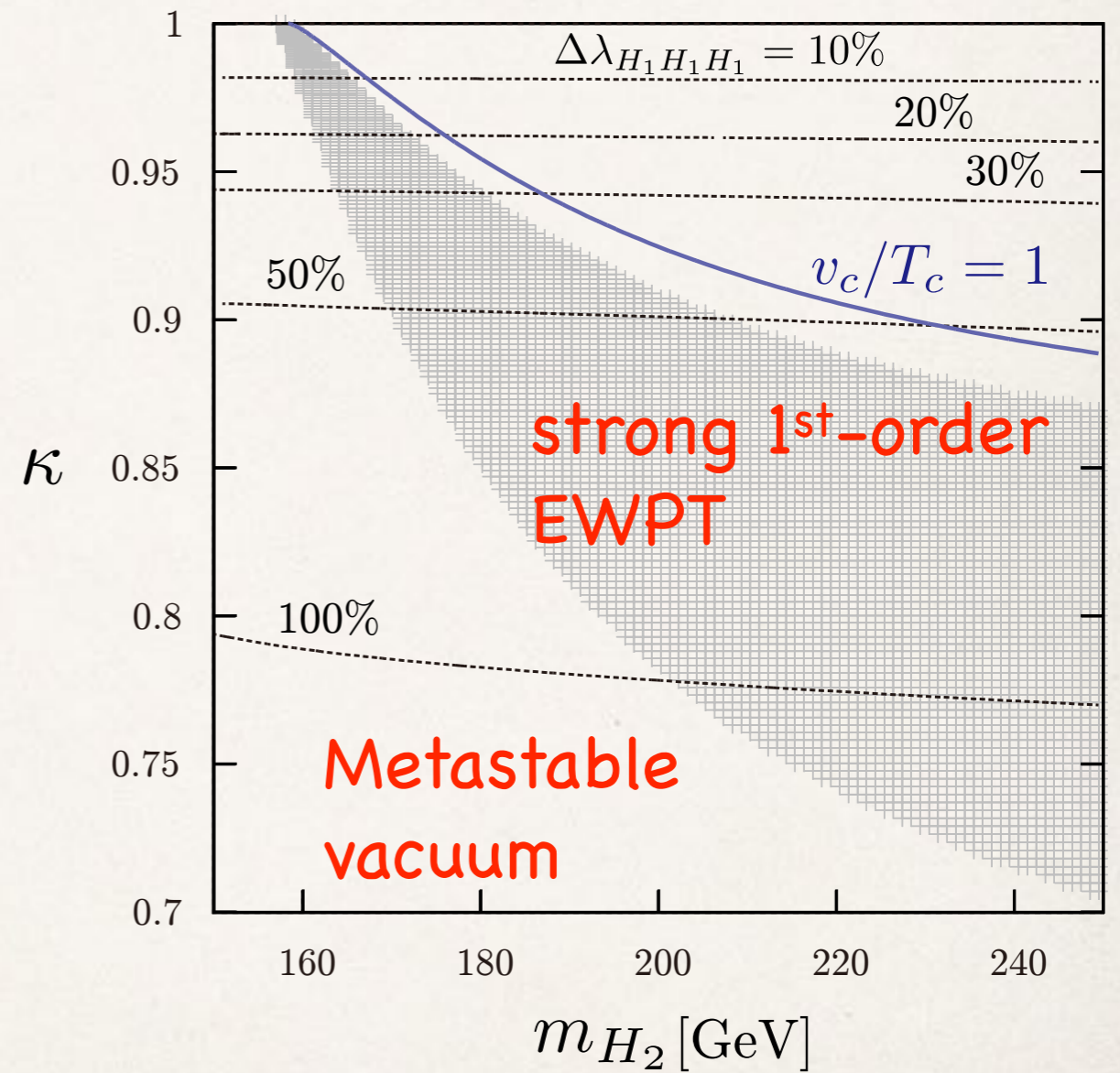
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SM+S

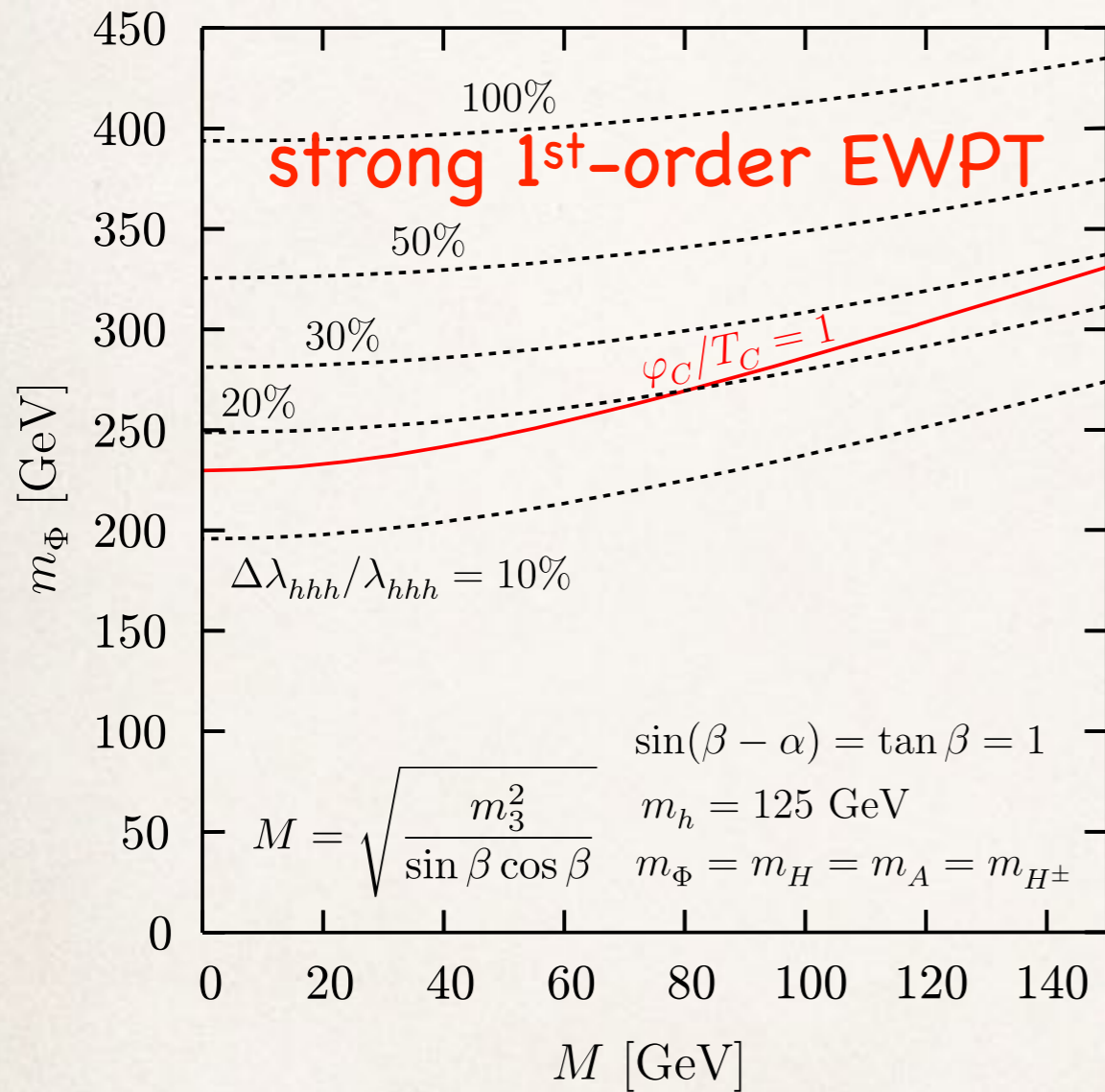
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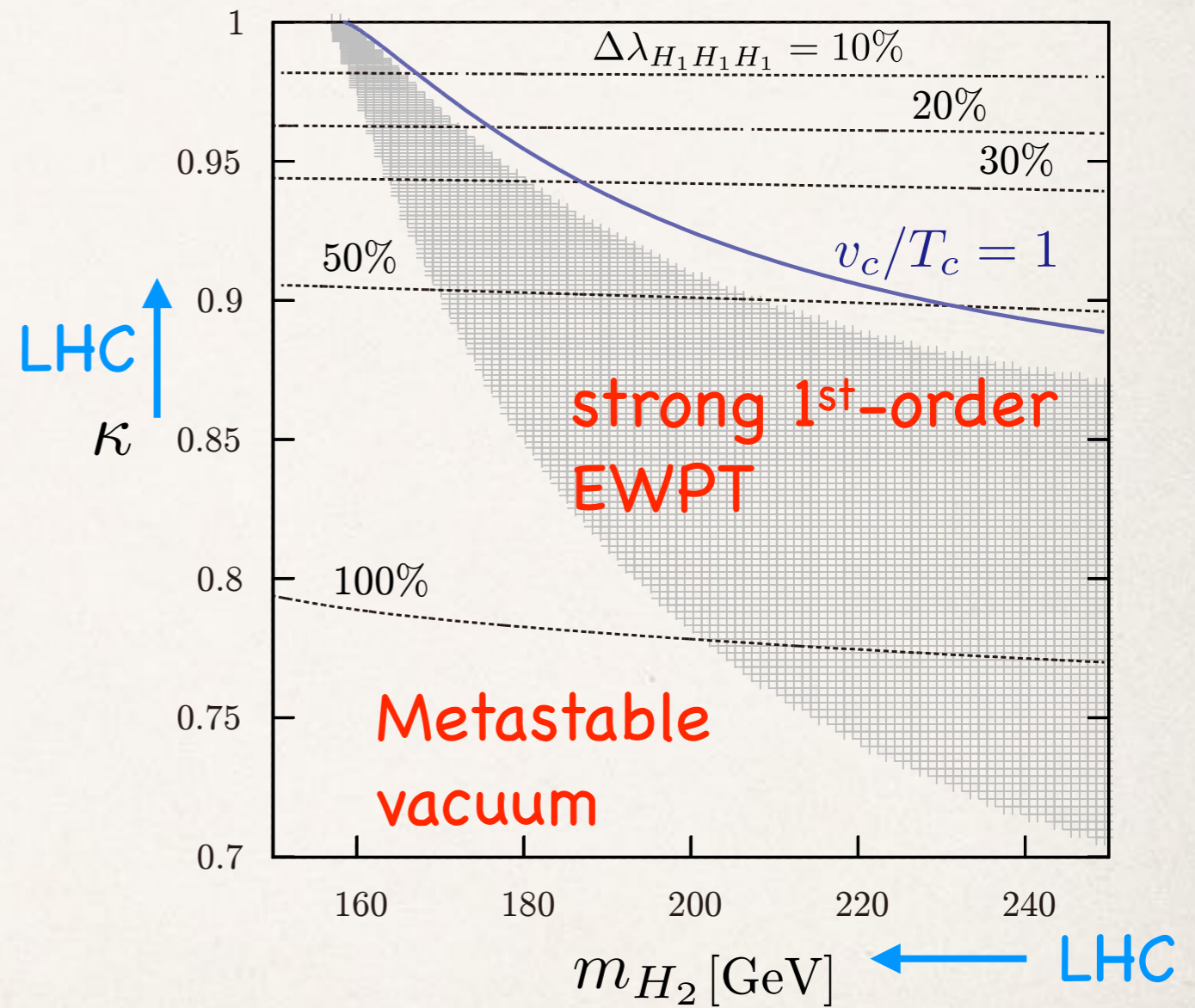
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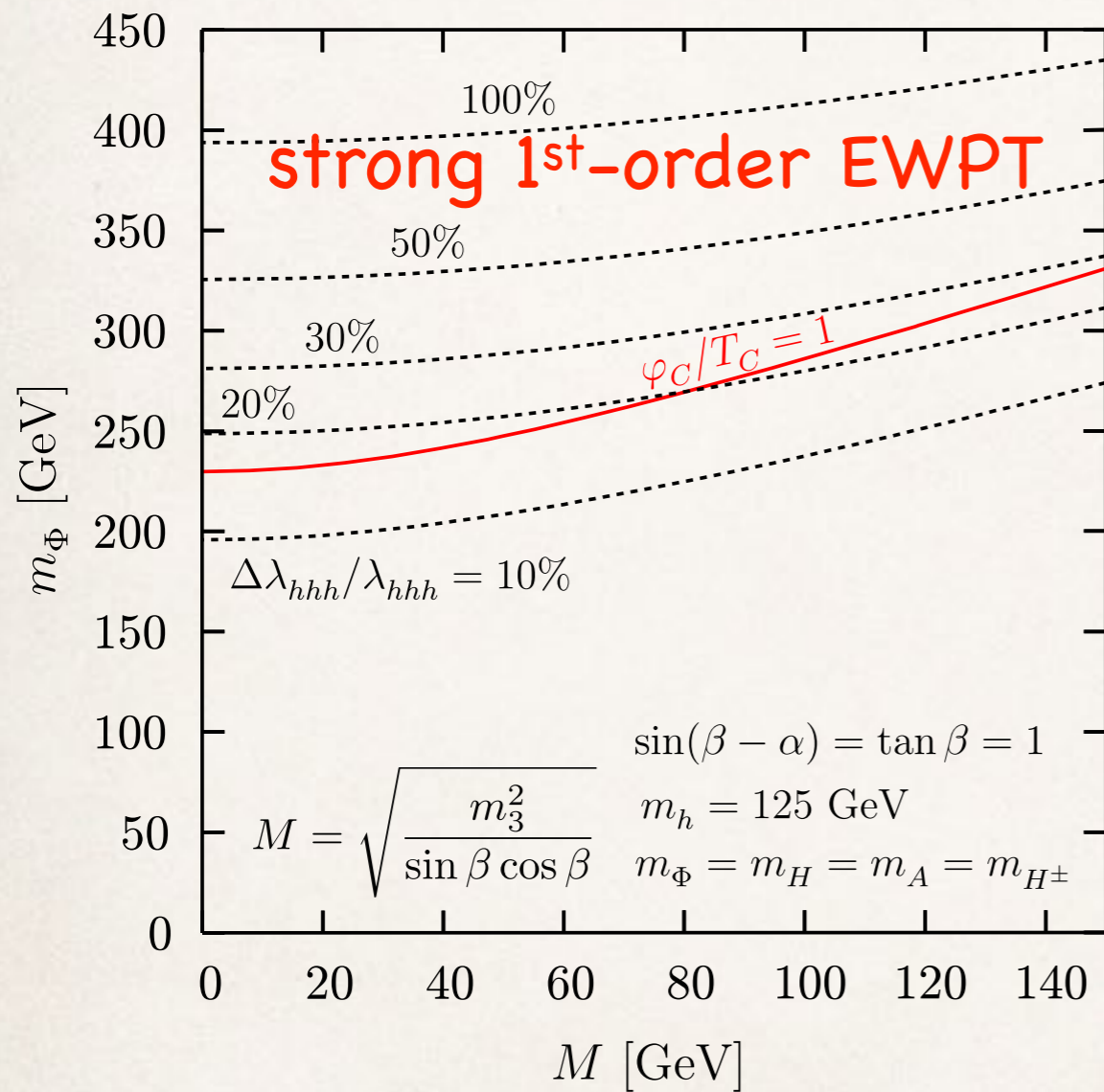
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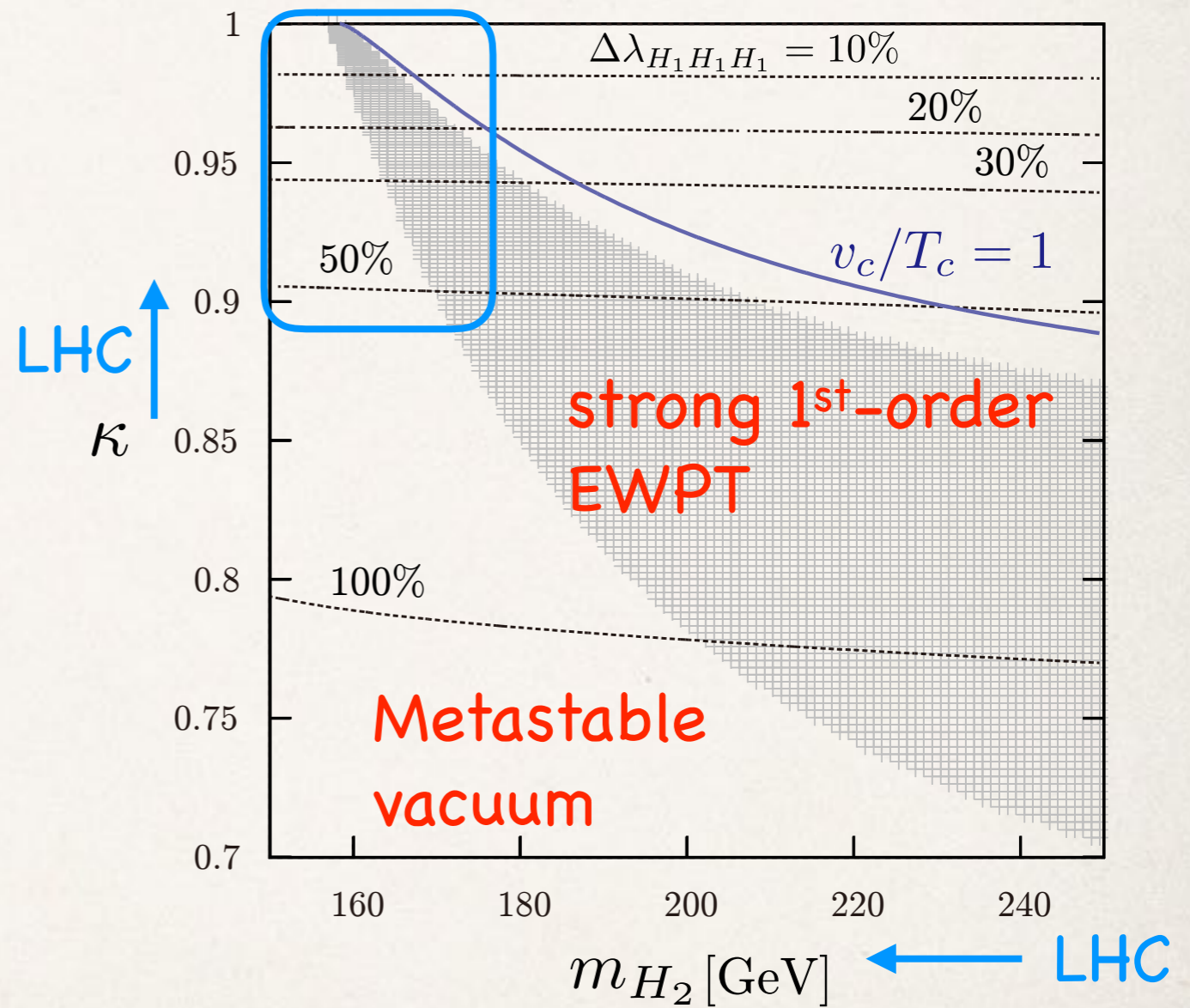
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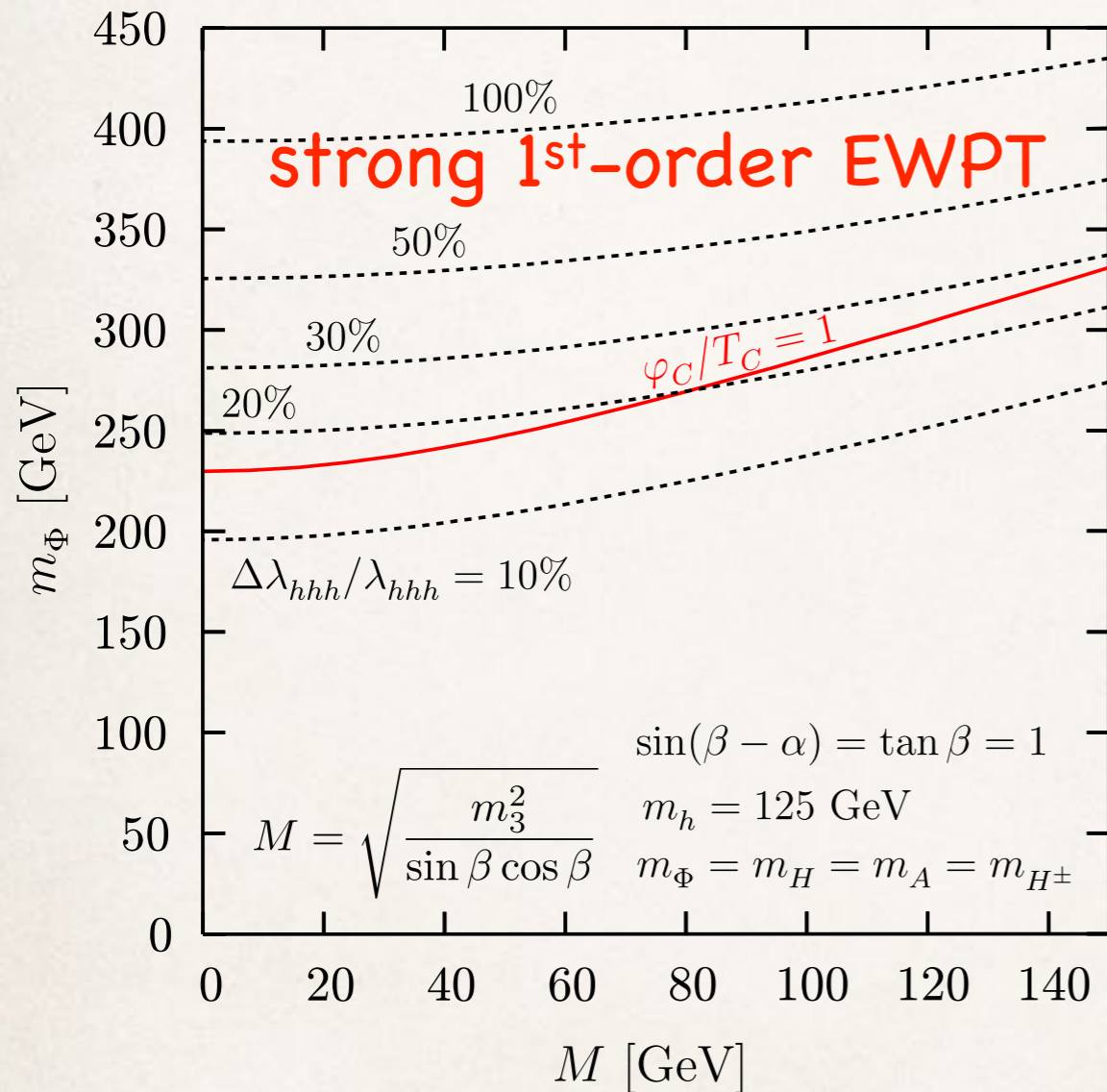
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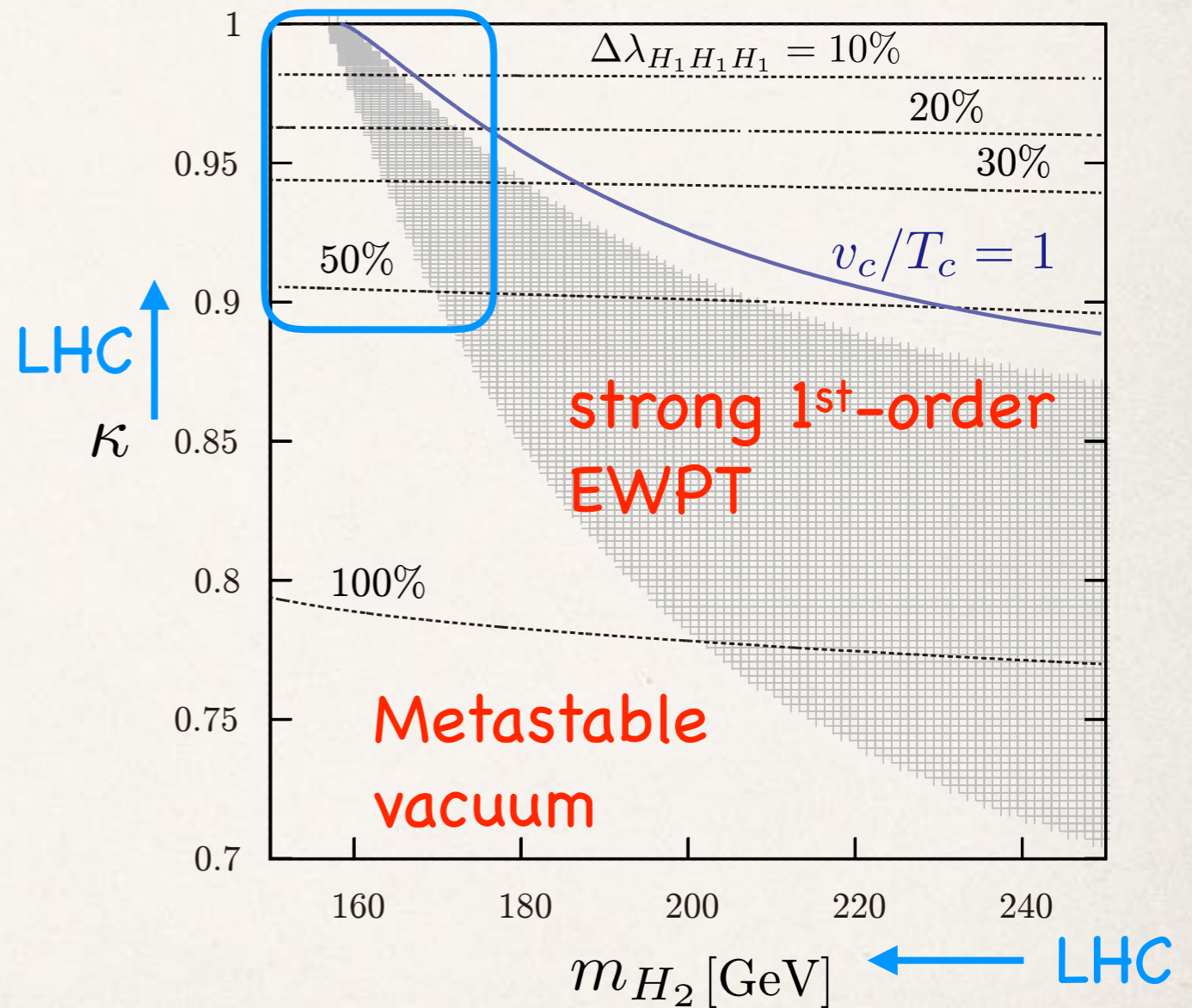
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[Kanemura, Okada, E.S., PLB606,(2005)361]



SM+S

[K.Fuyuto, E.S., PRD90, 015015 (2014)]

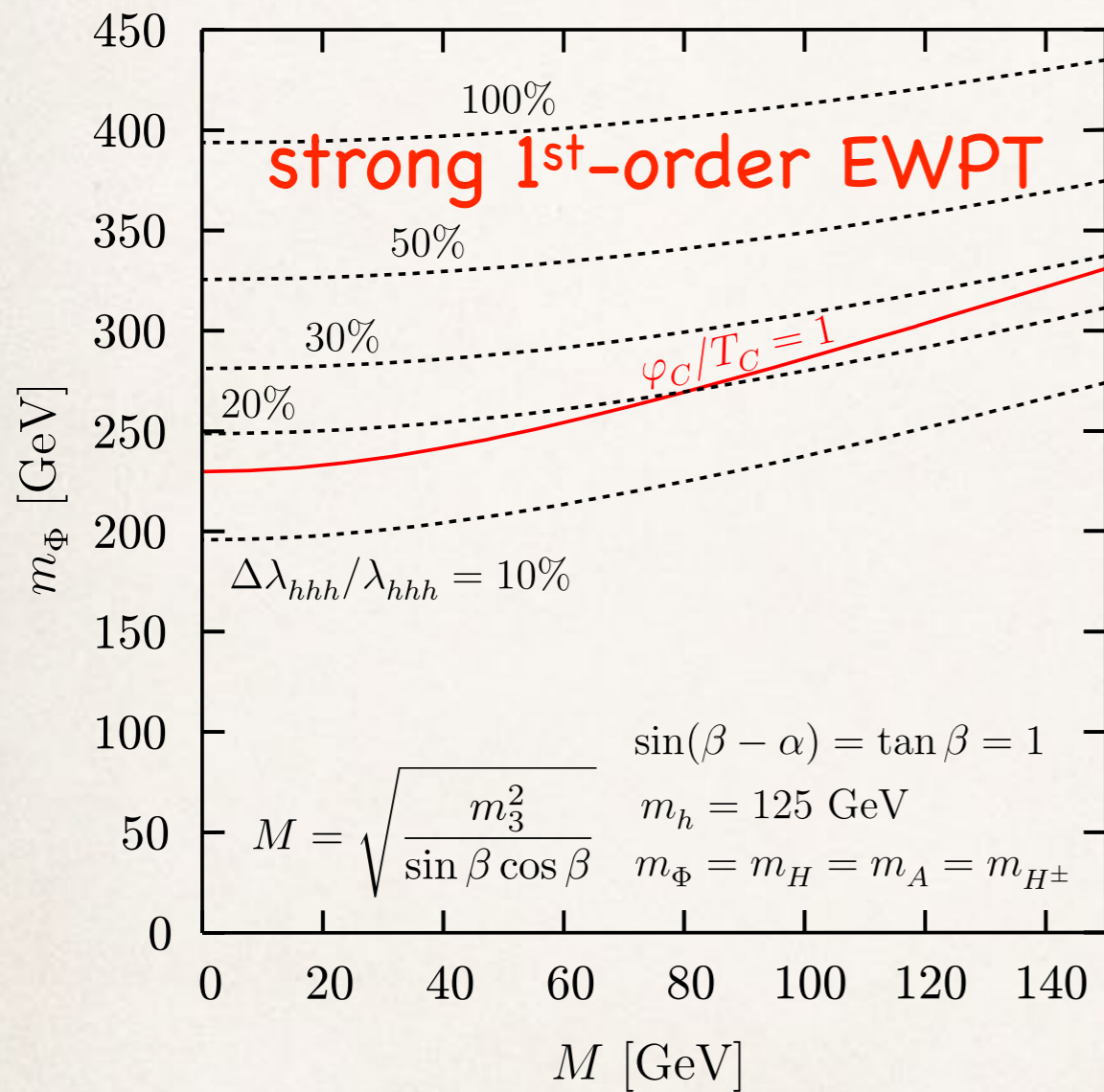


- Strong 1st-order EWPT leads to specific Higgs spectrum and couplings.

Parameter space of EWBG

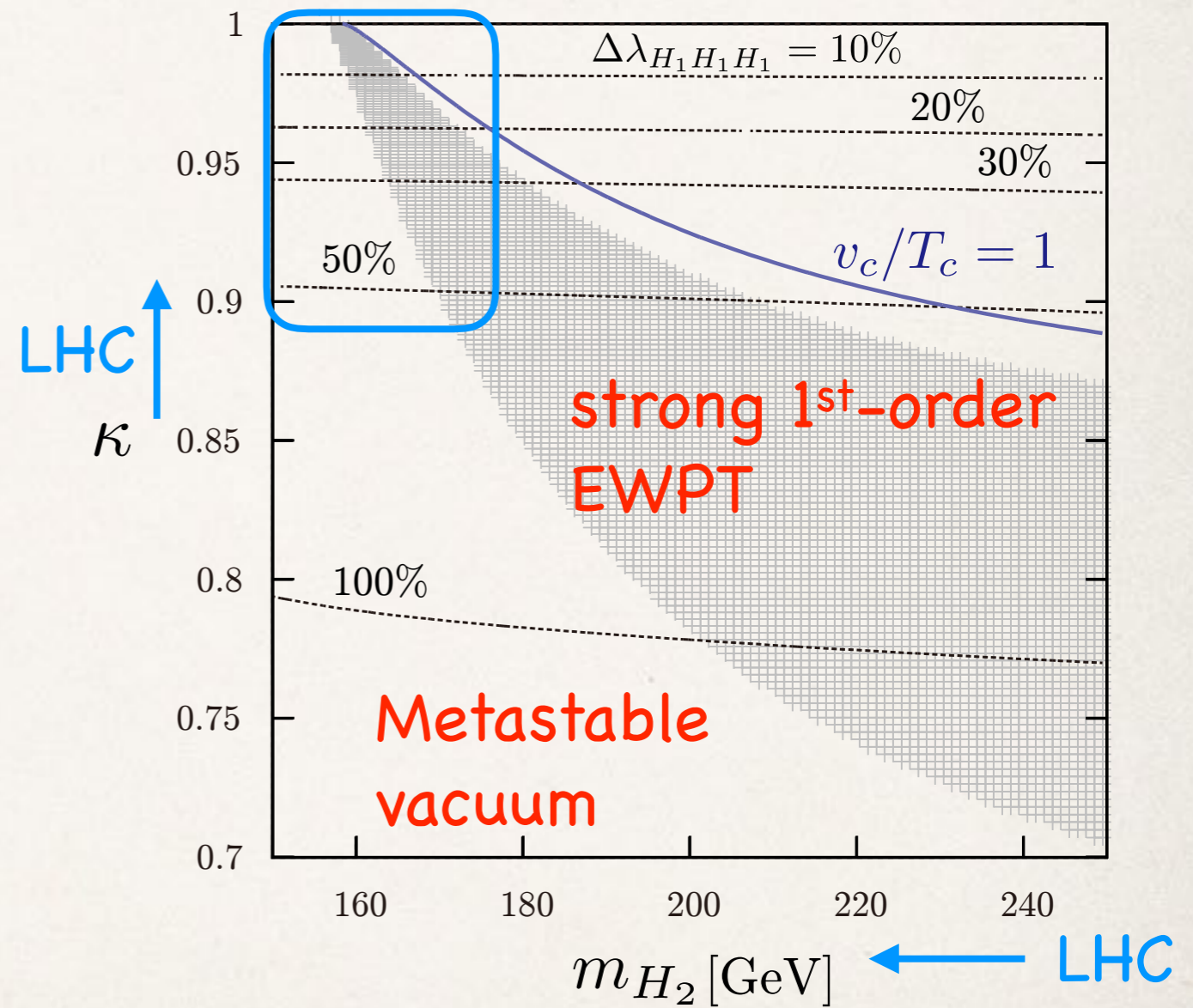
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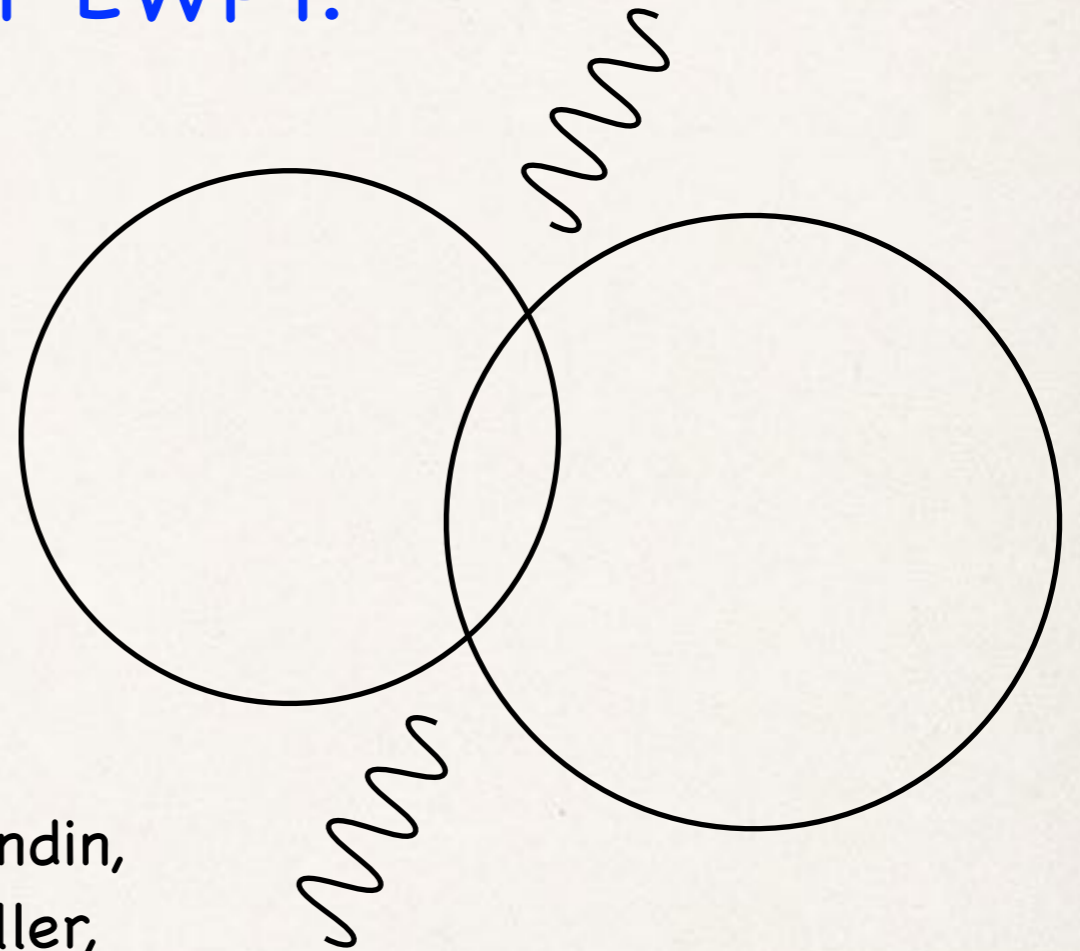
- Strong 1st-order EWPT leads to specific Higgs spectrum and couplings.
- $\Delta \lambda_{hhh}$ is not large enough to be detected at ILC250. -> probe by GWs

Gravitational Waves from 1st-order EWPT

GWs are induced by the 1st-order EWPT.

Sources of GW

- (1) Bubble collisions,
- (2) Sound waves,
- (3) Turbulence



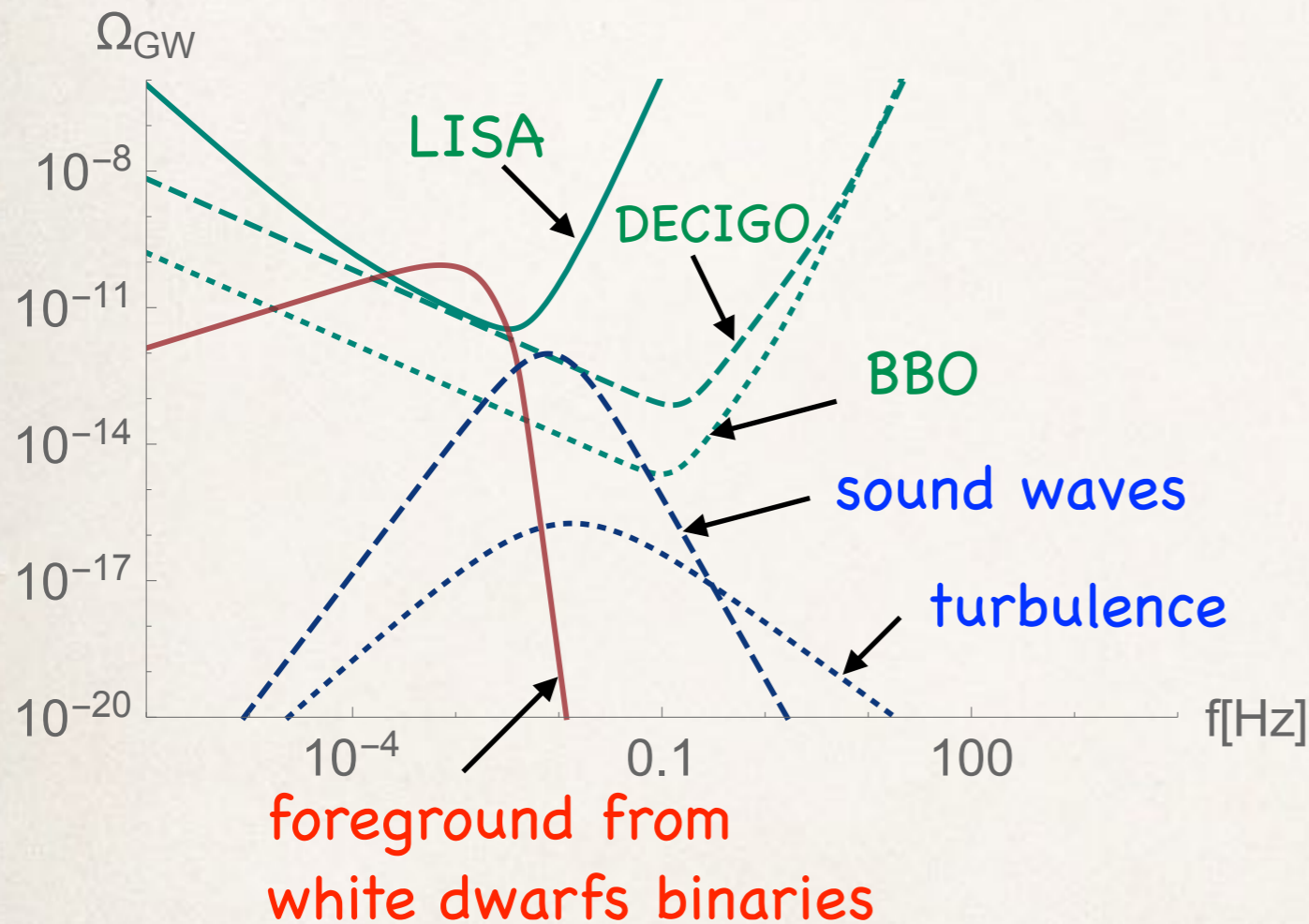
See Ref.[C.Caprini, M.Hindmarsh, S.Huber, T.Konstandin, J.Kozaczuk, G.Nardini, J.M.No, A.Petiteau, P.Schwaller, G.Servant, 1512.06239(JCAP)]

- GWs play a complementary role in probing Higgs sector.

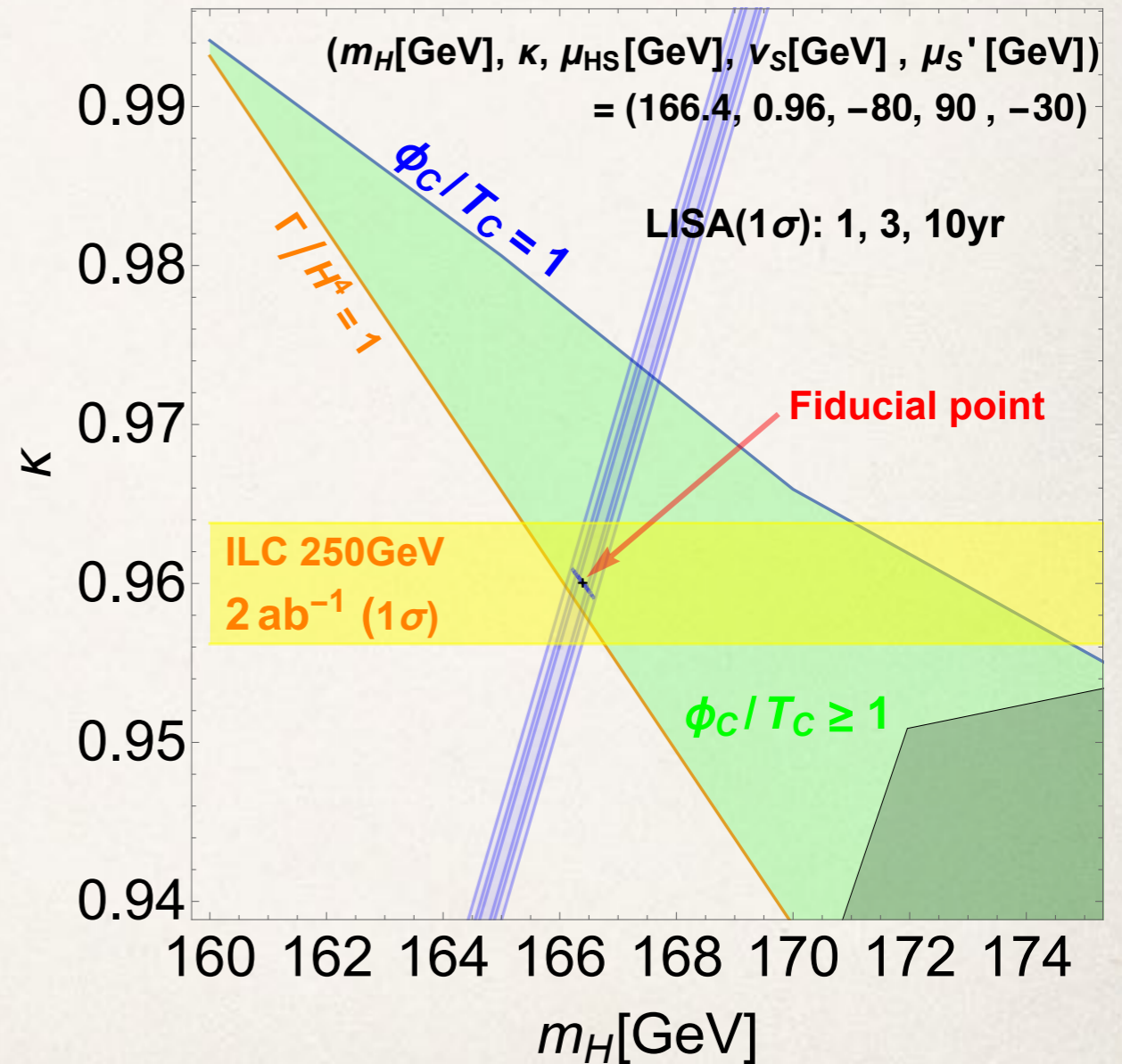
Gravitational Waves from 1st-order EWPT

[K.Hashino, R.Jinno, M.Kakizaki, S.Kanemura, T.Takahashi, M.Takimoto, 1809.04994]

e.g. SM+S



For details, see Hashino's poster



GWs also provide exquisite probes of the Higgs sector!!

Higgs CP nature

CP-violating Higgs-fermion-fermion coupling

$$\mathcal{L}_{hff} = -\frac{\kappa_f y_f}{\sqrt{2}} h \bar{f} (\cos \Psi_{\text{CP}} + i\gamma_5 \sin \Psi_{\text{CP}}) f$$

$\Psi_{\text{CP}} = 0 \rightarrow h$ is pure CP-even

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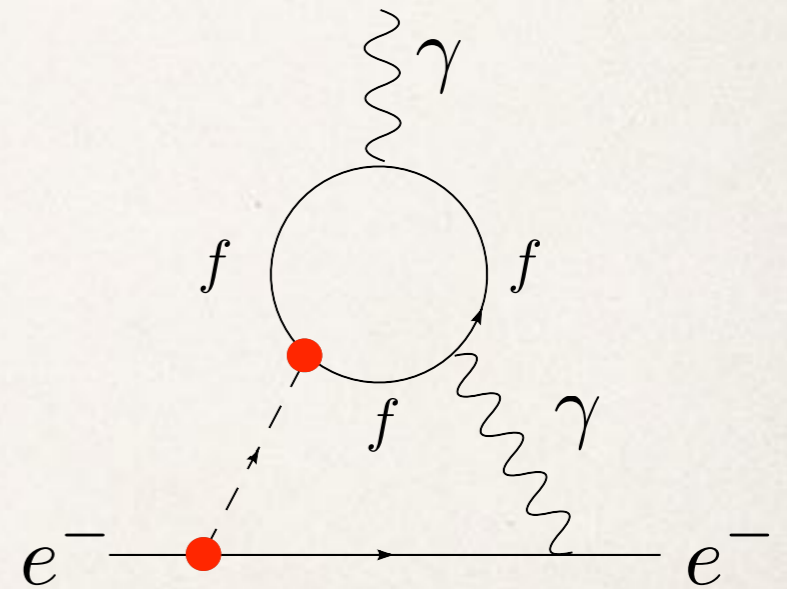
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CP phase is highly constrained by electric dipole moment (EDM) of electron.

$$|d_e| < 1.1 \times 10^{-29} \text{ e cm}$$

[ACME, Nature 562,355(2018)]



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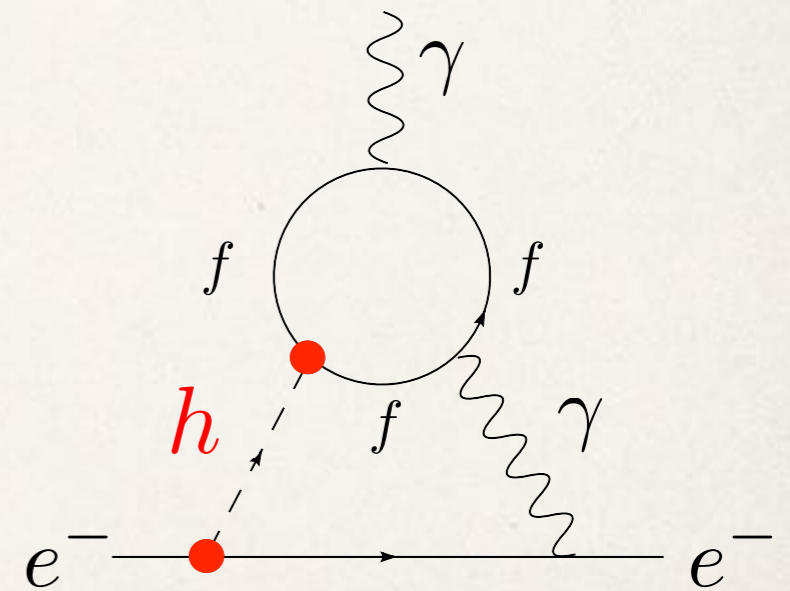
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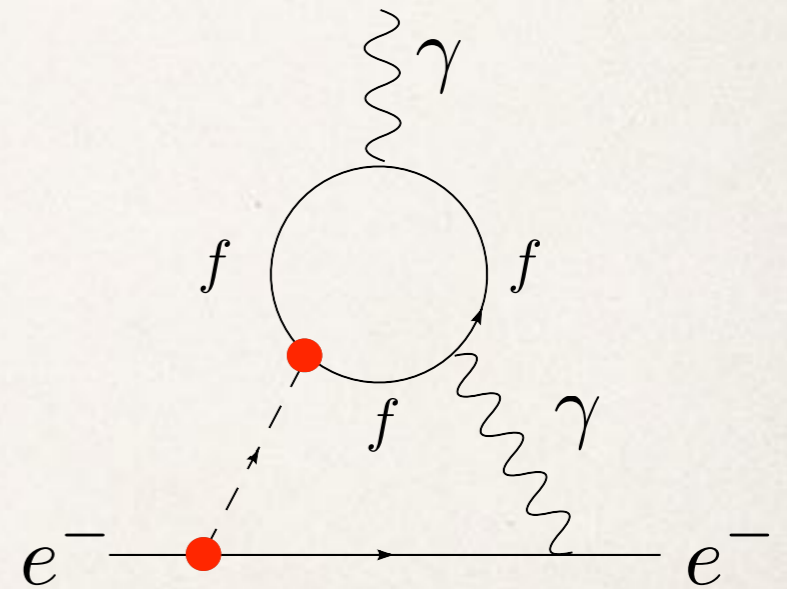
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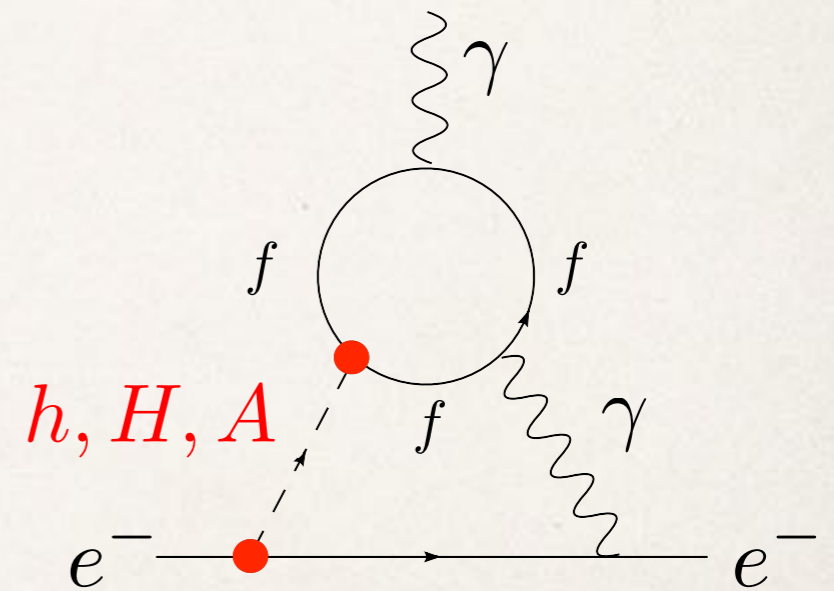
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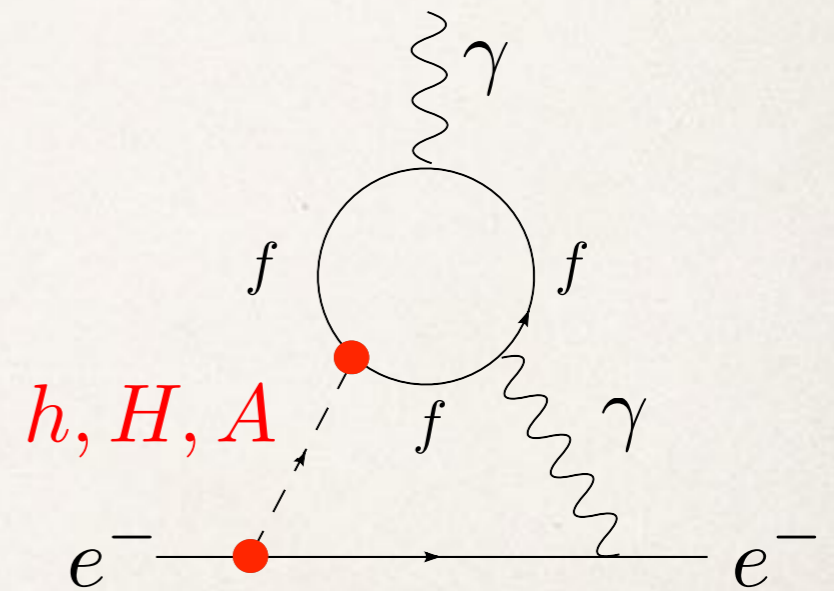
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[ACME, Nature 562,355(2018)]



However, this constraint can be avoidable if cancellation mechanism is at work. -> collider probes play a complementary role!

$h(125) \rightarrow \tau\tau$

CP-violating Higgs-tau-tau coupling:

$$\mathcal{L}_{h\tau\tau} = -\frac{\kappa_\tau y_\tau}{\sqrt{2}} h \bar{\tau} (\cos \Psi_{CP} + i\gamma_5 \sin \Psi_{CP}) \tau$$

□ LHC: $\sqrt{s} = 13$ TeV

[X.Chen, Y.Wu, PLB790(2019)332]

$\Psi_{CP} : 270$ mrad (15.5°) (300 fb^{-1})

$\Psi_{CP} : 90$ mrad (5.2°) (3000 fb^{-1})

□ ILC250 w/ 2000 fb^{-1}

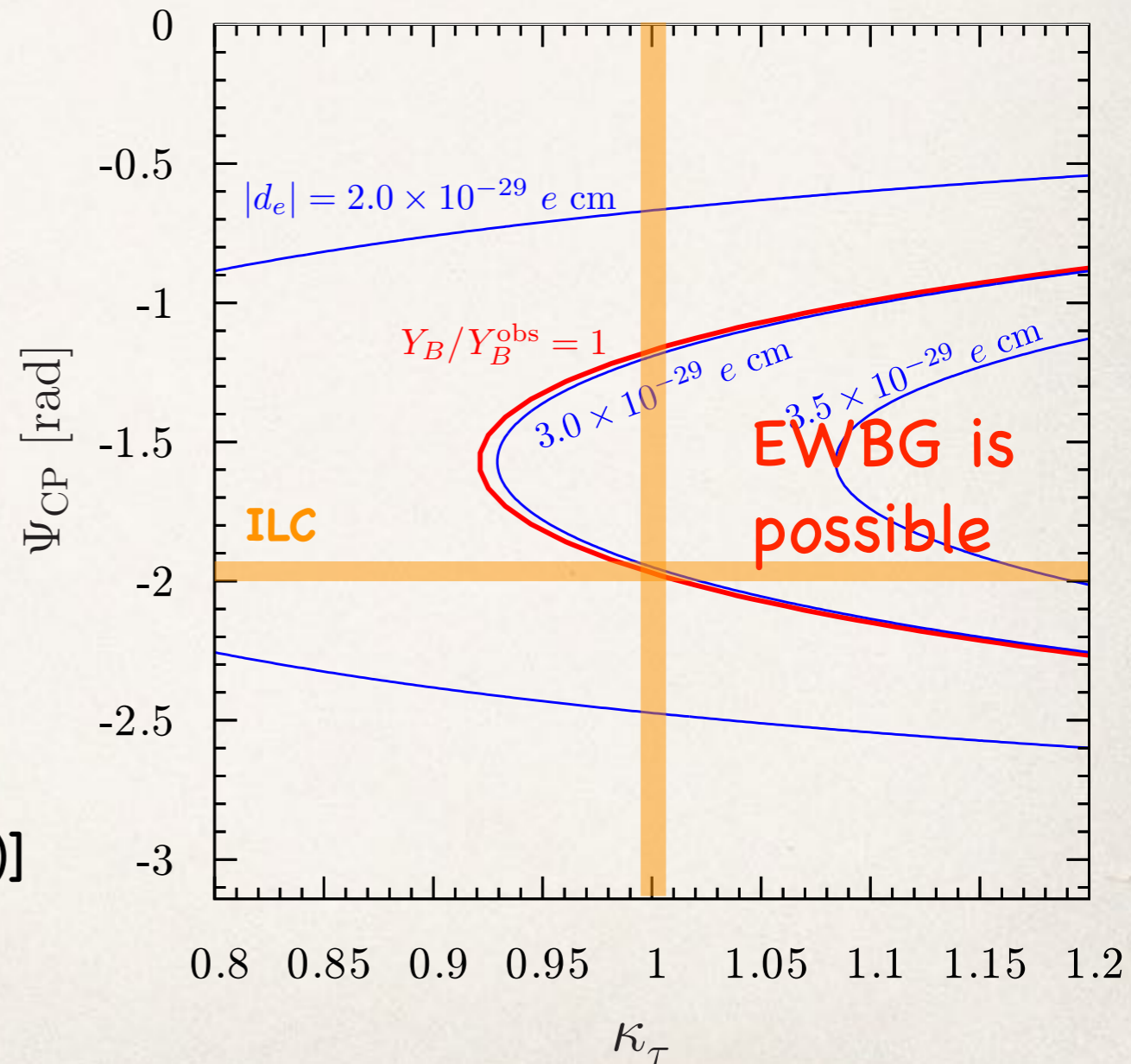
[D.Jeans, G.W. Wilson, PRD98,013007(2018)]

$\Psi_{CP} : 75$ mrad (4.3°)

EWBG driven by extra tau Yukawa:

e.g., general 2HDMs:

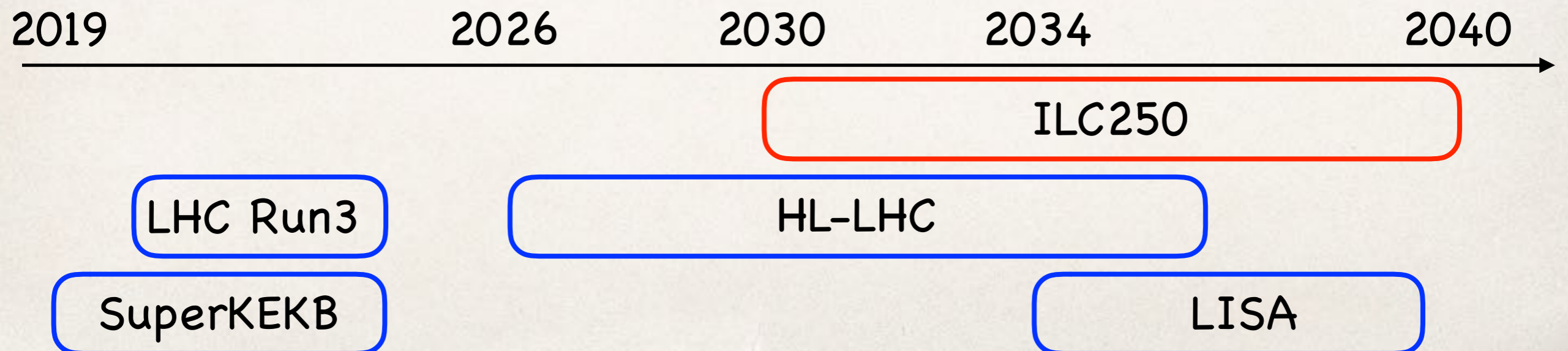
1607.07316(PLB), 1609.09849(PRD),



$\kappa_\tau \sim 1.0\%$ ILC250+HL-LHC

Summary

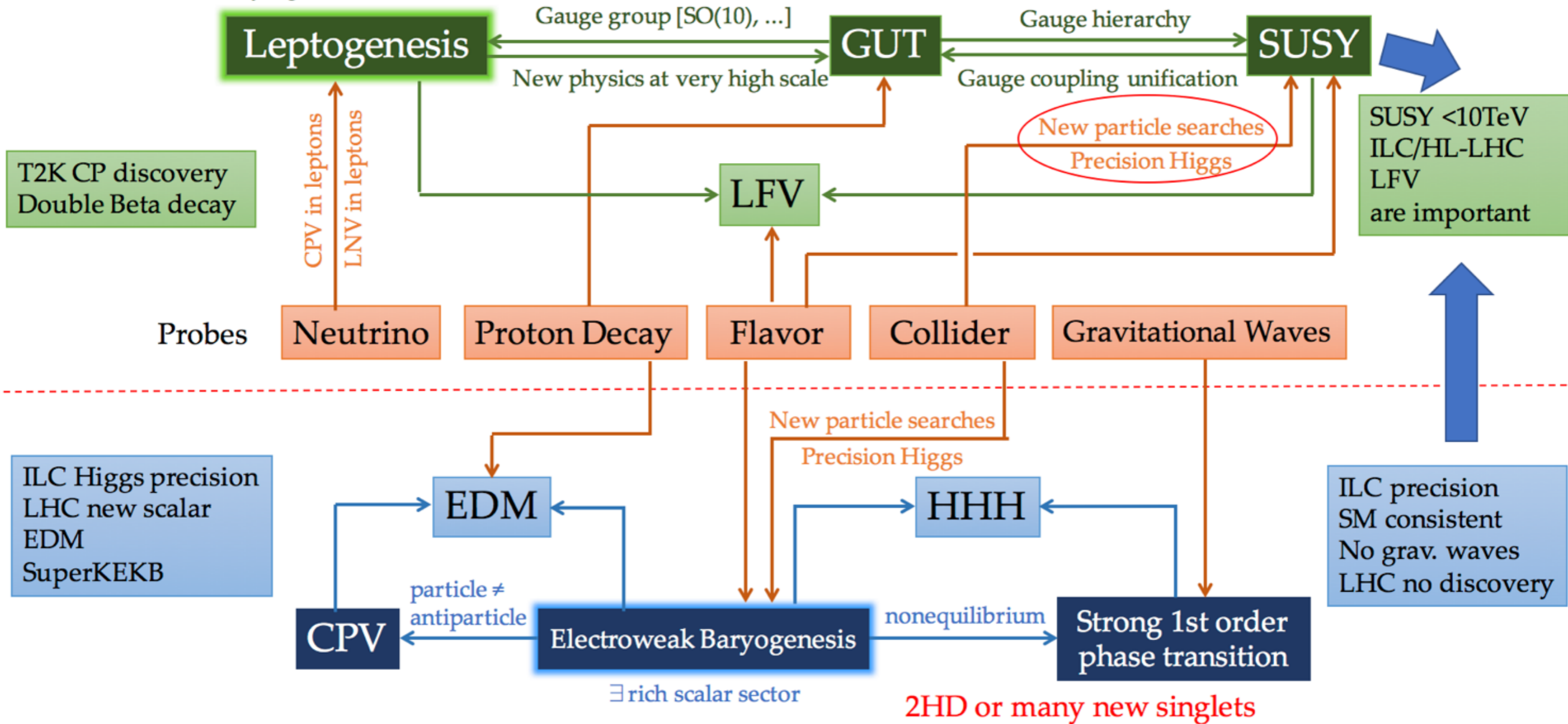
- Higgs precision measurements have huge impacts on probes of electroweak baryogenesis.
- Gravitational waves play a complimentary role in investigating nature of electroweak phase transition.
- $h(125) \rightarrow \tau\tau$ measurement is the powerful probe of CP violation regardless of accidental cancellation of electron EDM.



Backup

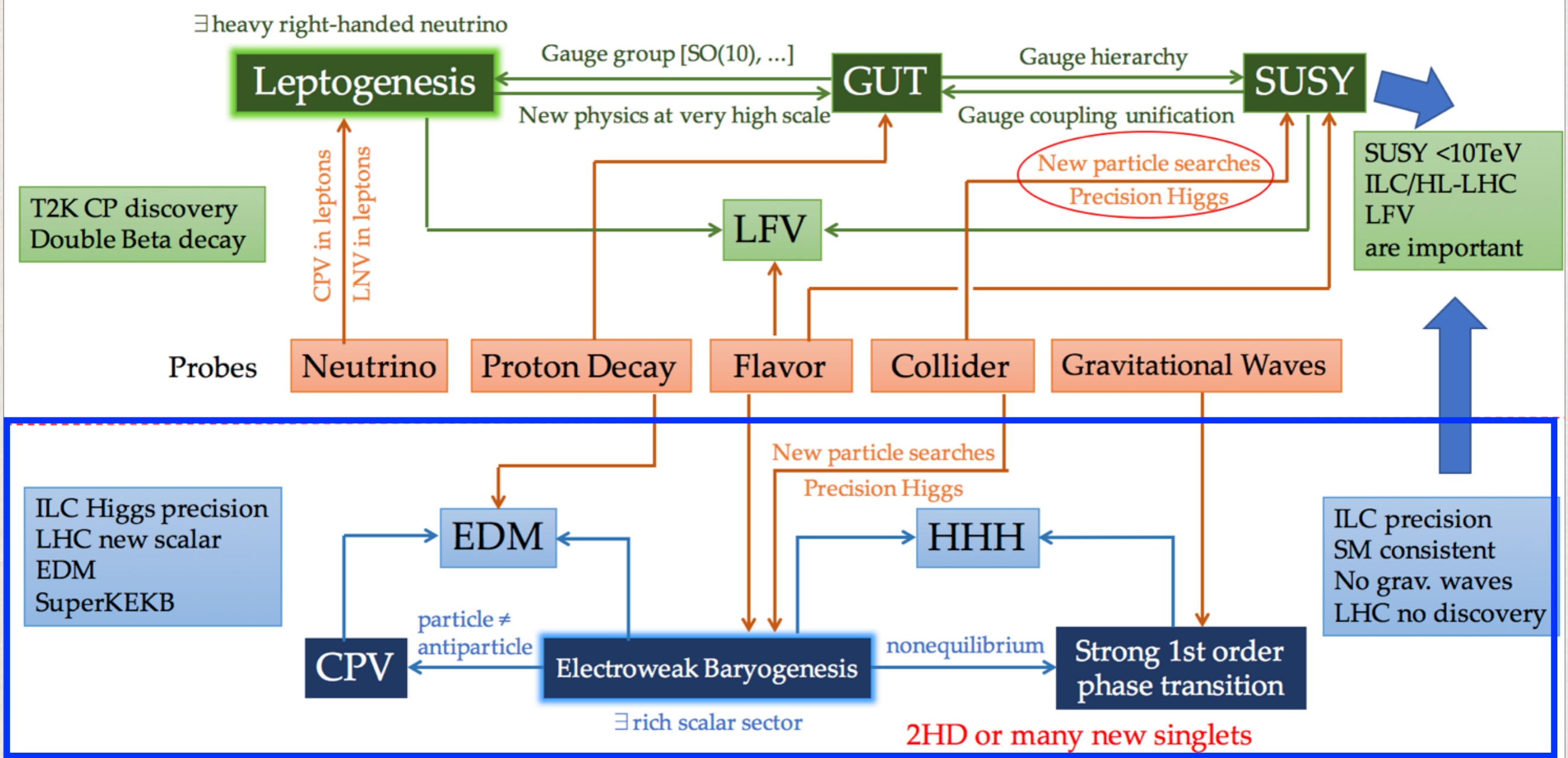
Origin of matter-antimatter asymmetry

\exists heavy right-handed neutrino



ILC (Higgs factory) provides exquisite probes of Electroweak Baryogenesis (EWBG).

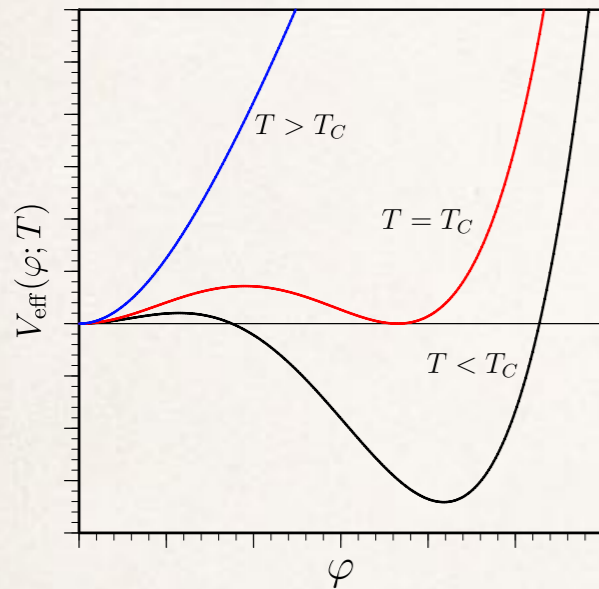
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λ_{hhh} -EWPT correlation

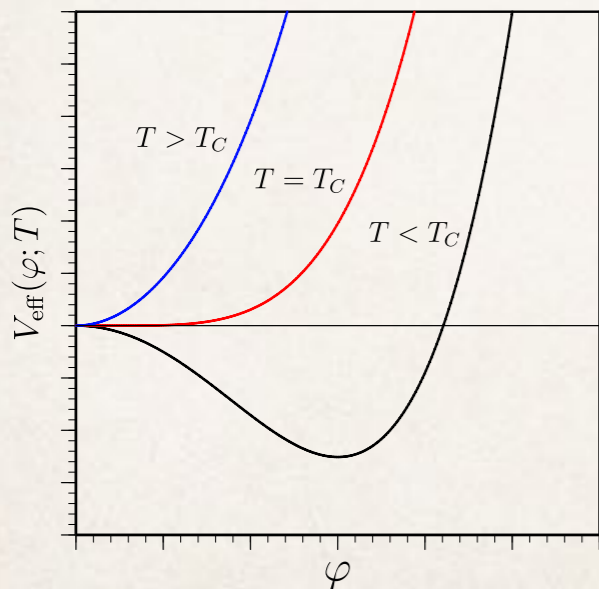
[S.Kanemura, Y.Okada, E.S., PLB606 (2005) 361;
C.Grojean, G.Servant, J.Wells, PRD71 (2005) 036001]



1st-order phase transition (needed for EW baryogenesis)



$$\lambda_{hhh} > \lambda_{hhh}^{\text{SM}}$$



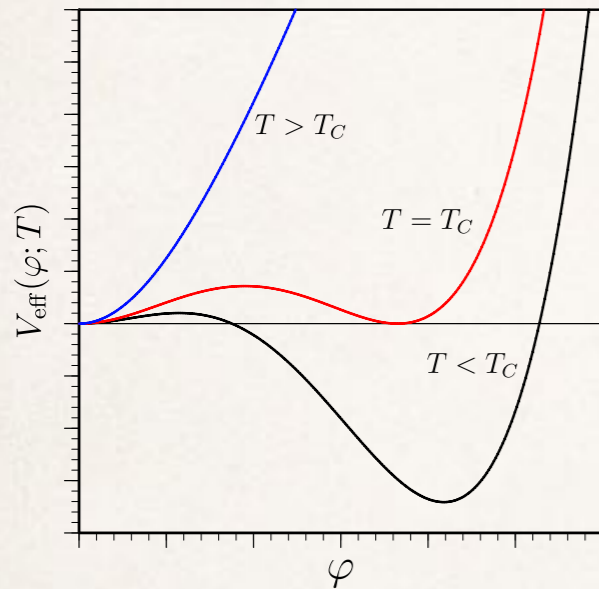
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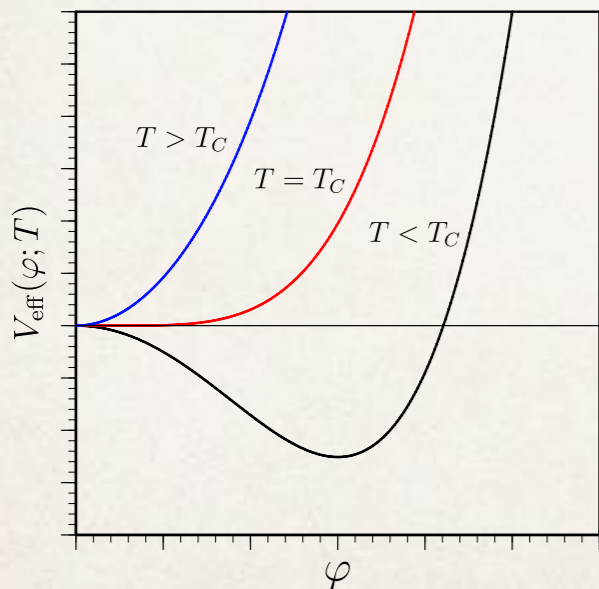


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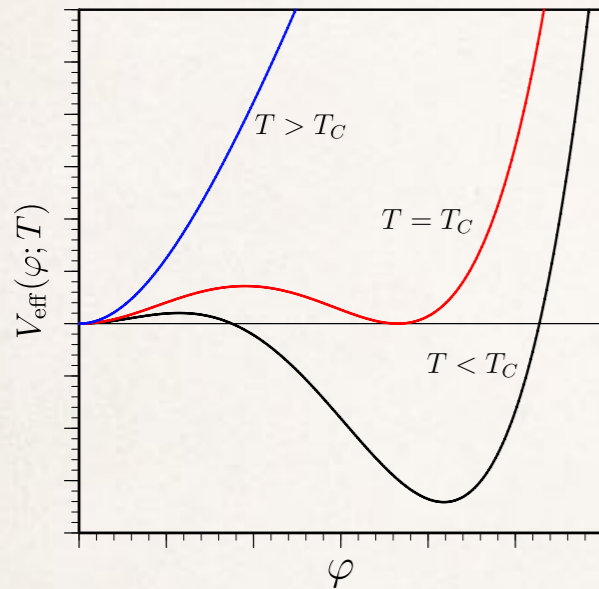
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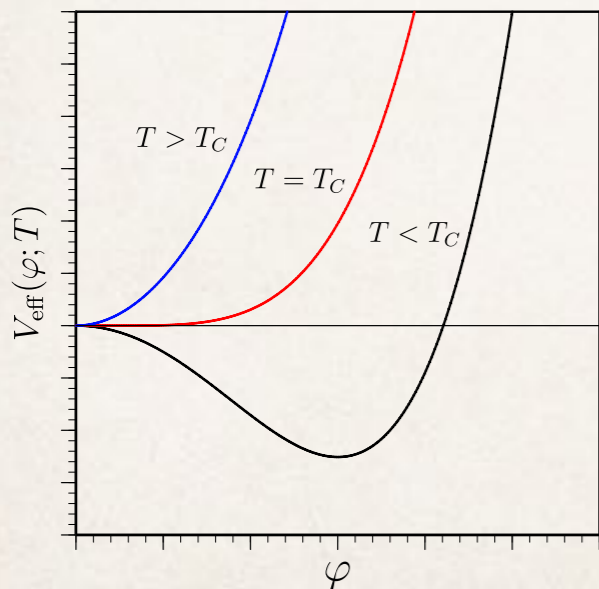


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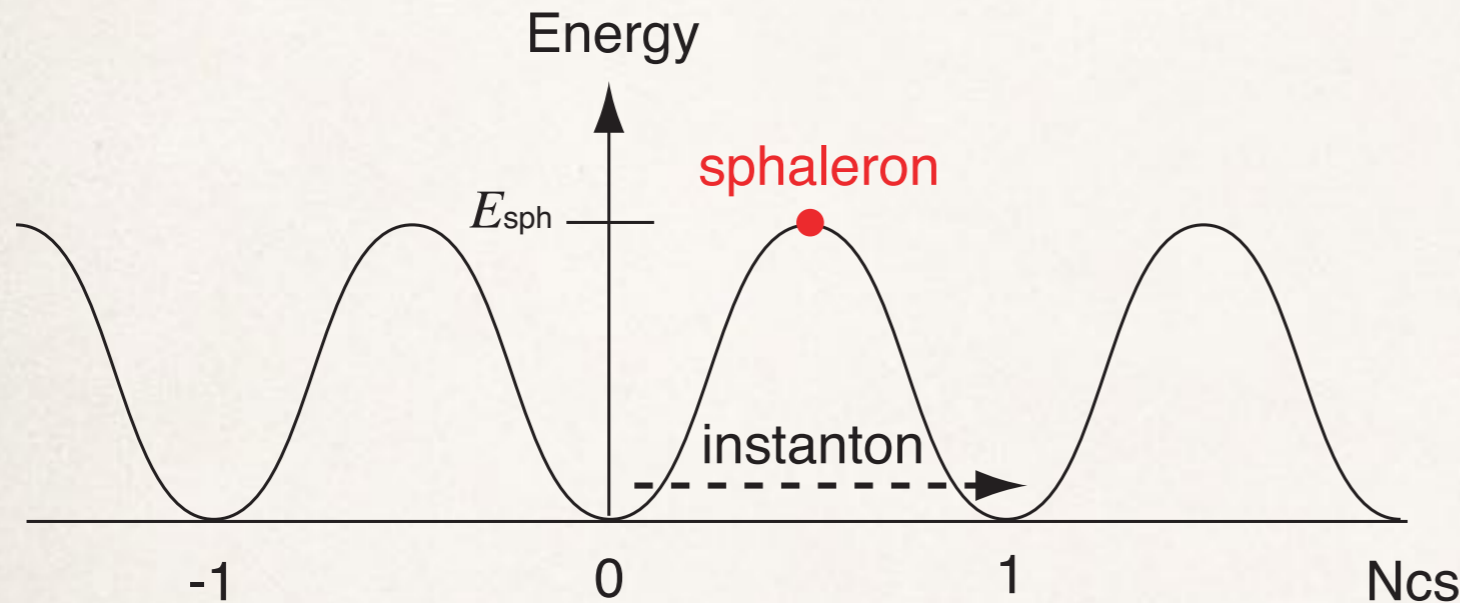


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B+L violation

- A static saddle point solution w/ finite energy of the gauge-Higgs system. [N.S. Manton, PRD28 ('83) 2019]



$$\Delta B \neq 0$$

Instanton: quantum tunneling

Sphaleron: thermal fluctuation

$$\Delta(B + L) = 3\Delta N_{CS}$$

B+L anomaly

$$\partial_\mu j_{B+L}^\mu = \frac{3}{16\pi^2} \left[g_2^2 \text{Tr}(F_{\mu\nu} \tilde{F}^{\mu\nu}) - g_1^2 B_{\mu\nu} \tilde{B}^{\mu\nu} \right],$$

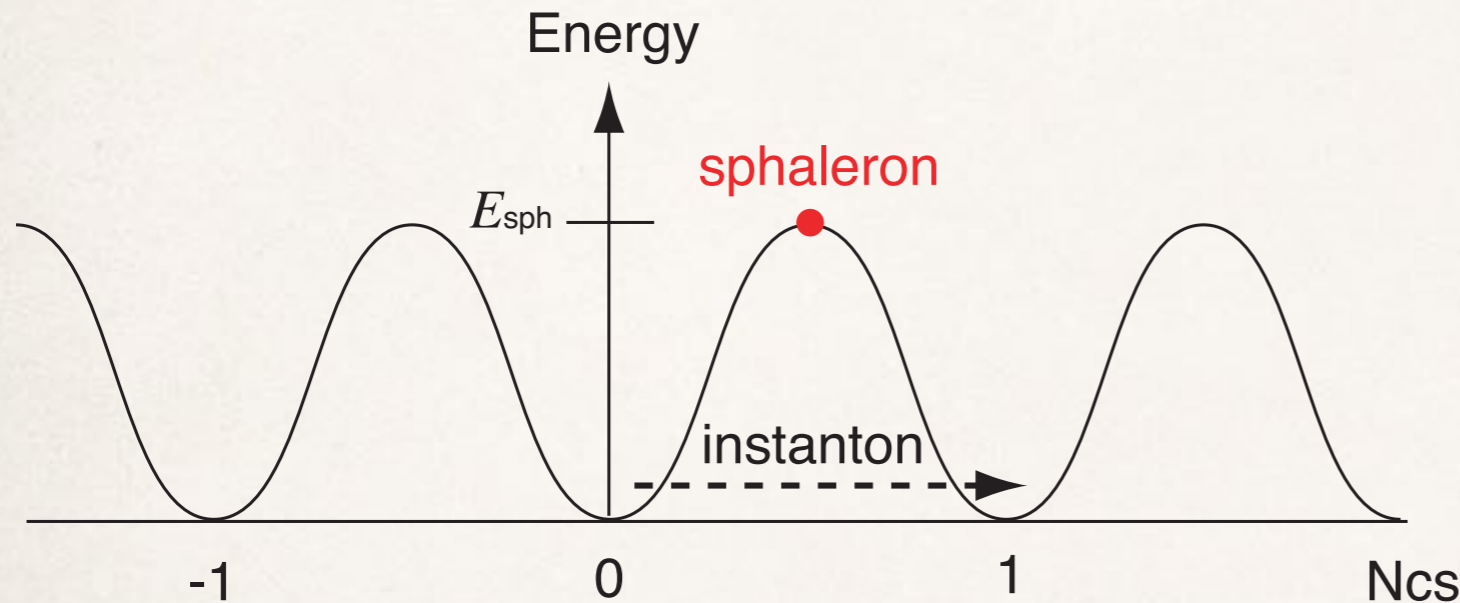
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$$0 \Leftrightarrow \sum_{i=1,2,3} (3q_L^i + l_L^i)$$

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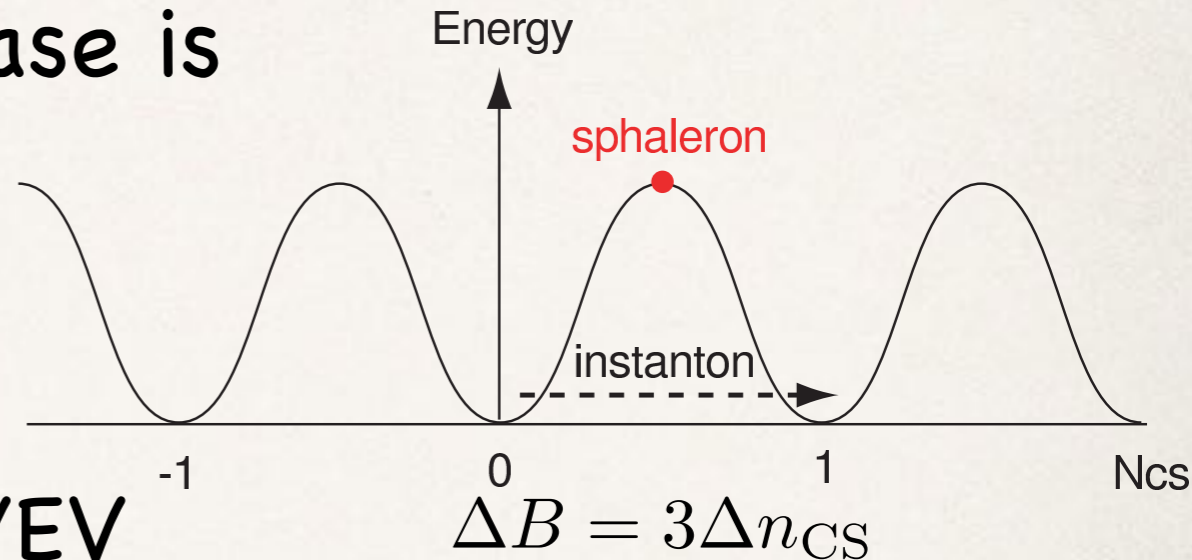
LHC can see this process?

still under debate...

$$\Gamma_B^{(b)} < H$$

B-changing rate in the broken phase is

$$\Gamma_B^{(b)} \simeq (\text{prefactor}) e^{-E_{\text{sph}}/T}$$



E_{sph} is proportional to the Higgs VEV

$$E_{\text{sph}} \propto v(T)$$

what we need is

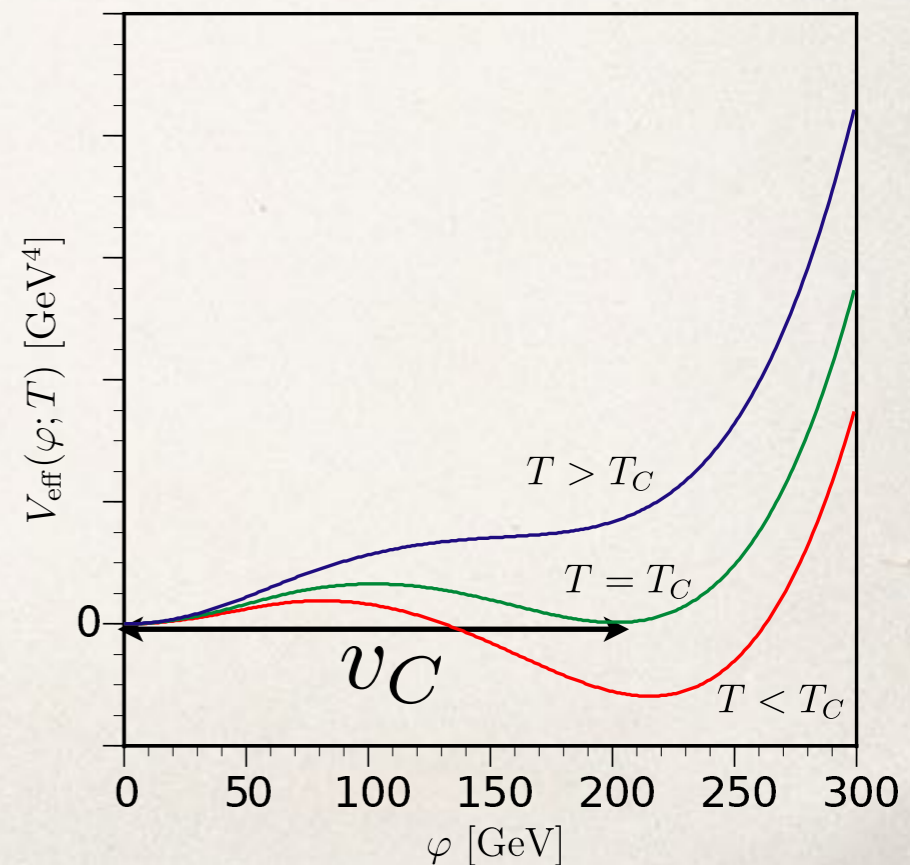
large Higgs VEV after the EWPT

➔ EWPT has to be "strong" 1st order!!

$$\Gamma_B^{(b)}(T_C) < H(T_C)$$



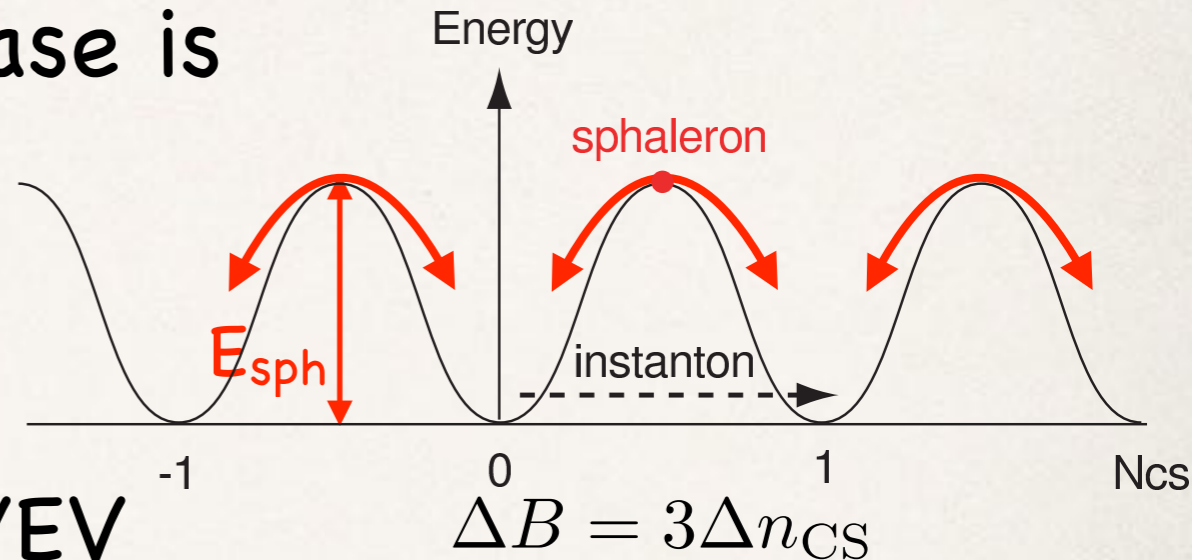
$$\frac{v_C}{T_C} \gtrsim 1$$



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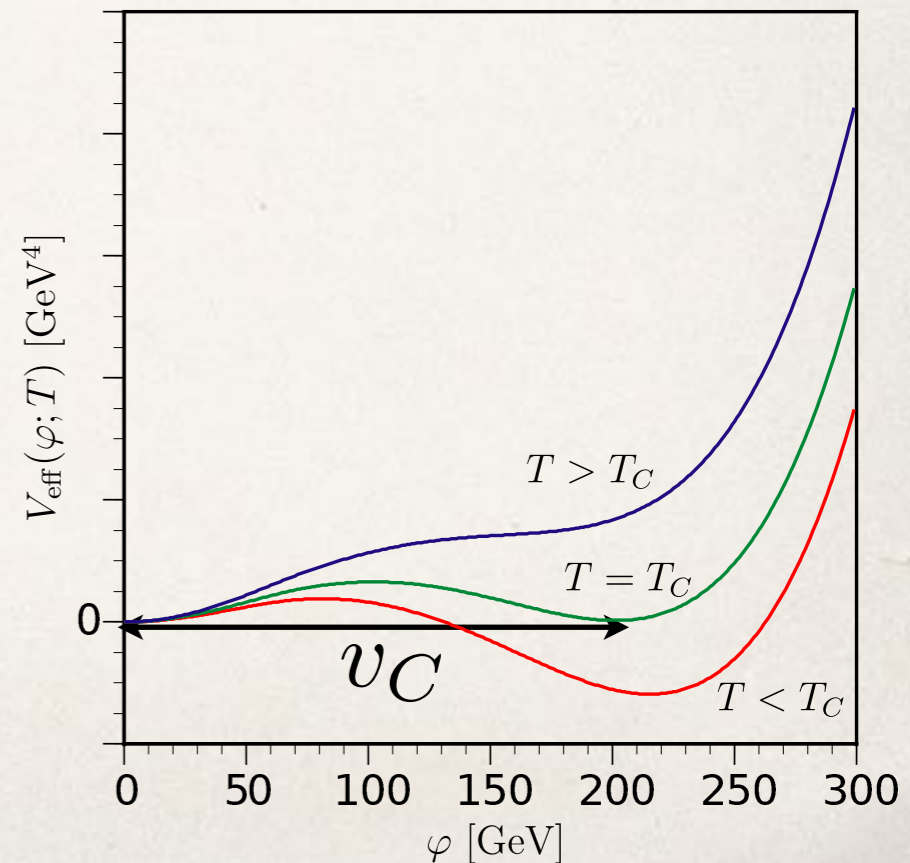
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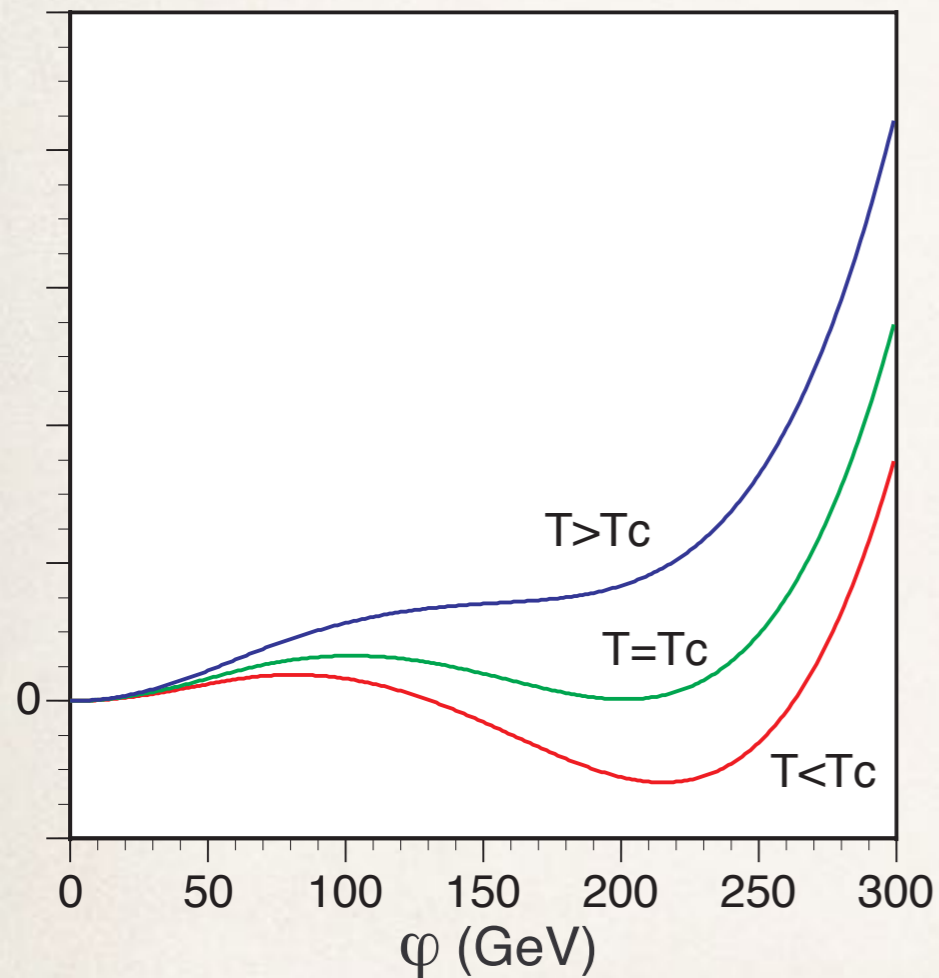
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$$V_{\text{eff}} \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4 \xrightarrow{T=T_C} \frac{\lambda_{T_C}}{4}\varphi^2(\varphi - v_C)^2$$

V_{eff}



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e.g., 2HDM

Heavy Higgs loops can enhance E .

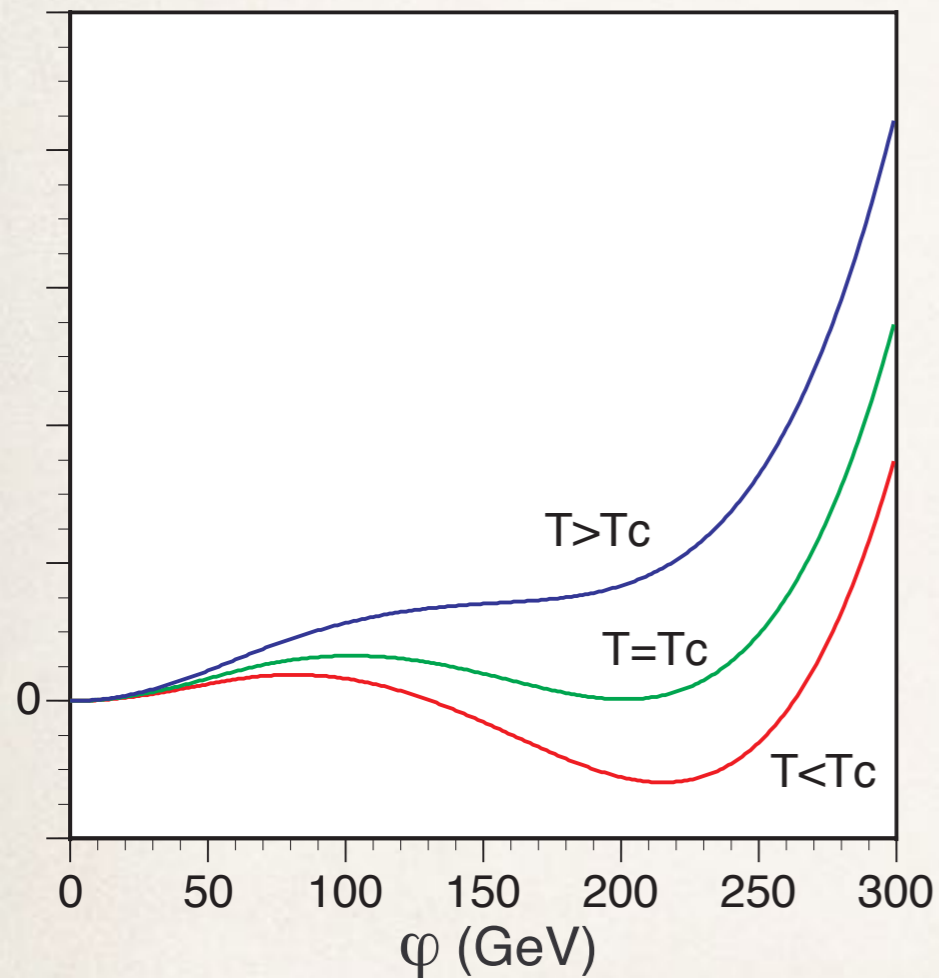
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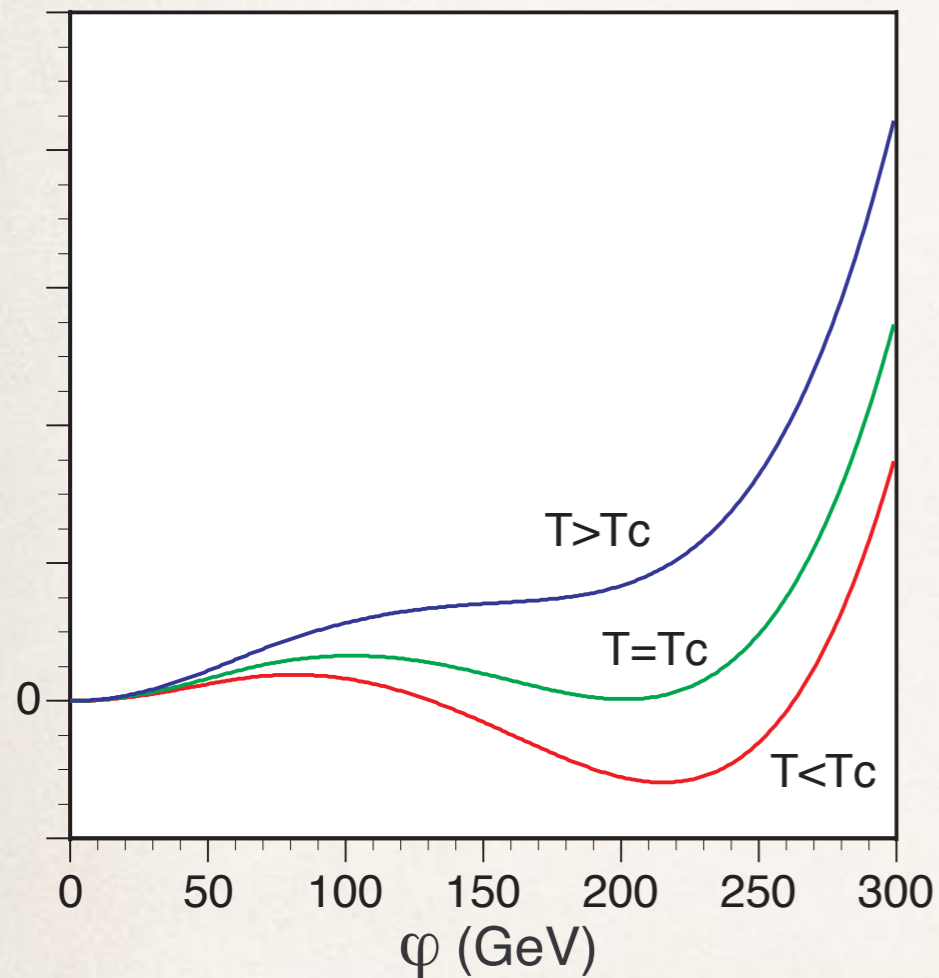
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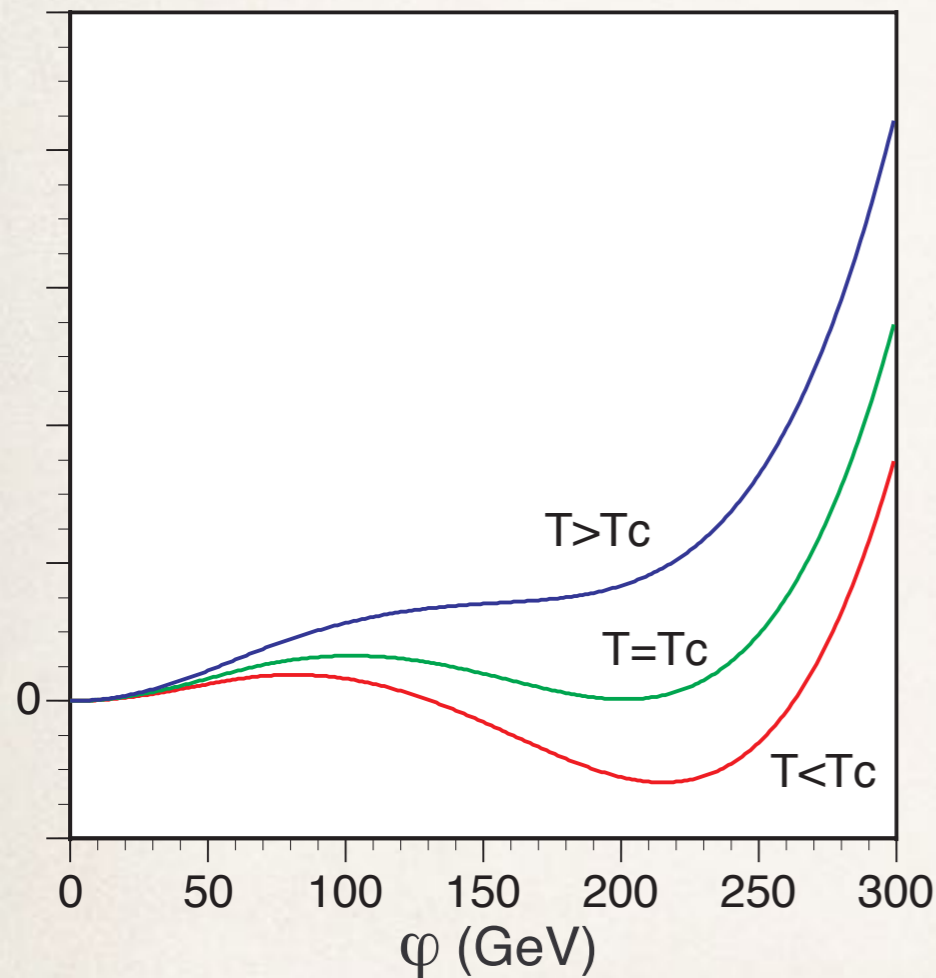
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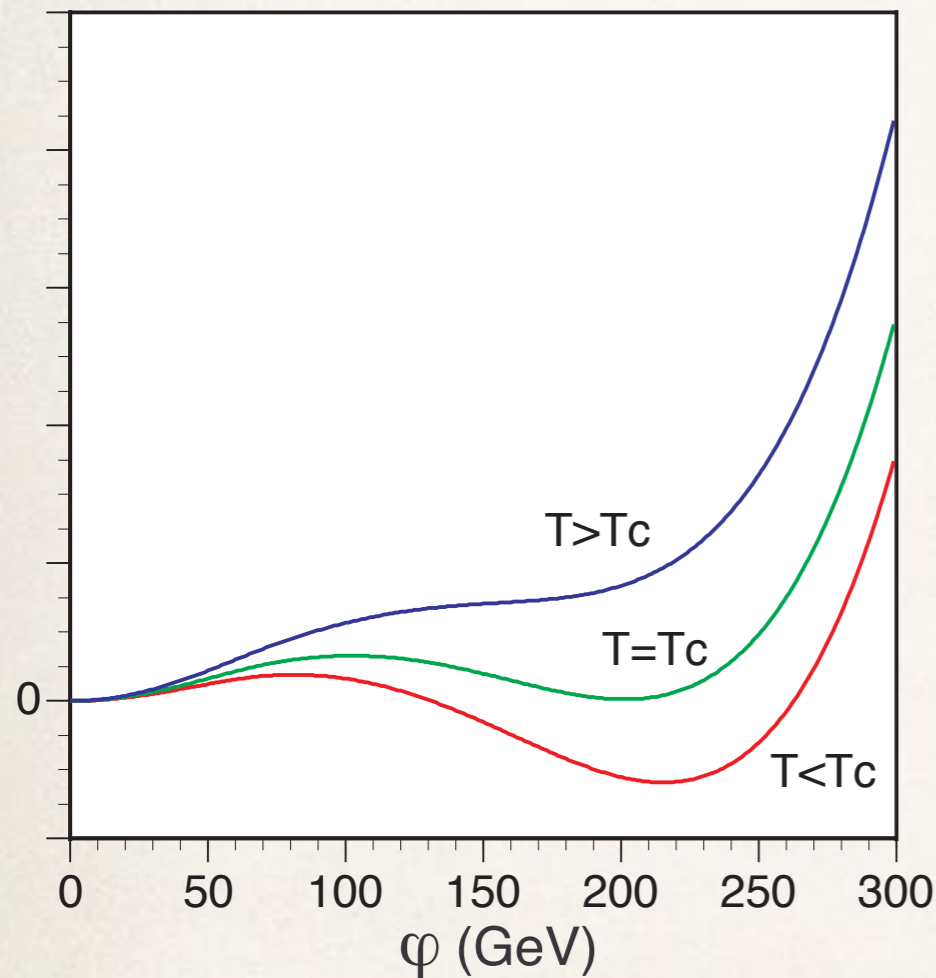
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non-decoupling

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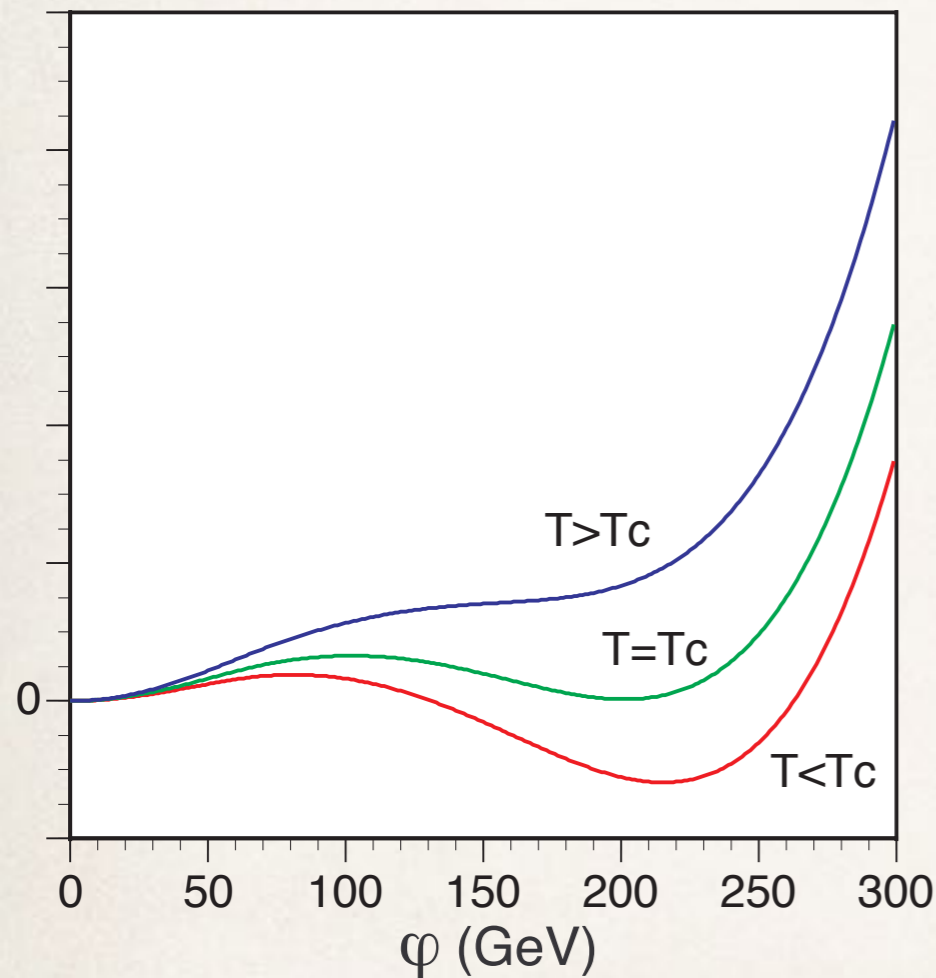
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$$V_{\text{eff}} \simeq D(T^2 - T_0^2)\varphi^2 - ET\varphi^3 + \frac{\lambda_T}{4}\varphi^4 \xrightarrow{T=T_C} \frac{\lambda_{T_C}}{4}\varphi^2(\varphi - v_C)^2$$

V_{eff}



$$v_C = \frac{2ET_C}{\lambda_{T_C}} \Rightarrow \frac{v_C}{T_C} = \frac{2E}{\lambda_{T_C}} \gtrsim 1$$

e.g., 2HDM

Heavy Higgs loops can enhance E .

$$m_{i=H,A,H^\pm}^2 = M^2 + \tilde{\lambda}_i \varphi^2$$

$$V_{\text{eff}} \ni \begin{cases} \text{non-decoupling} \\ -\tilde{\lambda}^{3/2} T \varphi^3 \left(1 + \frac{M^2}{\tilde{\lambda} \varphi^2}\right)^{3/2}, & \text{for } M^2 \ll \tilde{\lambda} \varphi^2, \\ \text{decoupling} \\ -|M|^3 T \left(1 + \frac{\tilde{\lambda} \varphi^2}{M^2}\right)^{3/2}, & \text{for } M^2 \gtrsim \tilde{\lambda} \varphi^2. \end{cases}$$

Non-decoupling heavy Higgs bosons play a central role in enhancing E .

EWBG-related CP violation

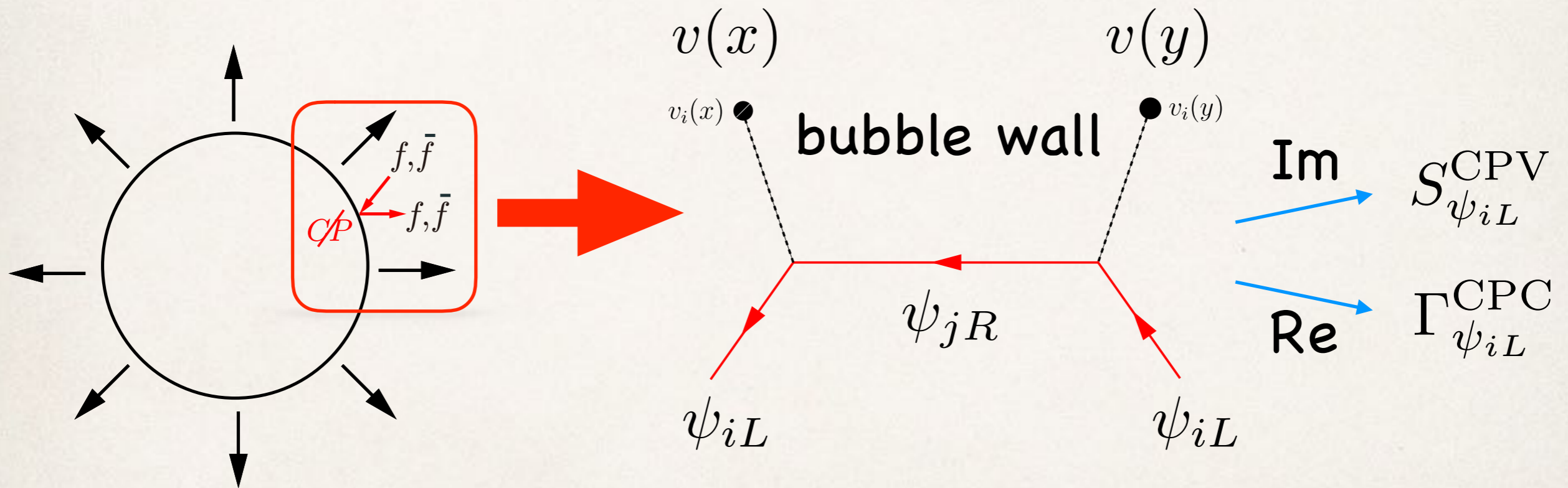
Diffusion eq. for n_B :

$\bar{z} < 0$: sym-phase, $\bar{z} > 0$: br-phase

$$D_Q n_B''(\bar{z}) - v_w n_B'(\bar{z}) - \theta(-\bar{z}) \mathcal{R} n_B(\bar{z}) = \theta(-\bar{z}) \frac{3}{2} \Gamma_B^{(\text{sym})} n_{\text{left}}(\bar{z})$$

diffusion const. wall velocity back reaction sph. rate

n_{left} is generated by scatterings b/w particles and bubbles.



$$n_B \propto n_{\text{left}} \propto S_{\psi_{iL}}^{\text{CPV}} / \sqrt{\Gamma_{\psi_{iL}}^{\text{CPC}}}$$

EWBG-related CP violation

If you have, e.g.,

$$-\mathcal{L}_Y = \bar{\psi}_i \left[c_L(x) P_L + c_R(x) P_R \right] \psi_j + \text{h.c.},$$

you could generate

$$S_{\psi_{iL}}^{\text{CPV}}(x) = C_{\text{BAU}} \left[c_R(x) \dot{c}_R^*(x) - c_R^*(x) \dot{c}_R(x) \right]$$

$$S_{\psi_{iR}}^{\text{CPV}}(x) = C_{\text{BAU}} \left[c_L(x) \dot{c}_L^*(x) - c_L^*(x) \dot{c}_L(x) \right]$$

$$S_{\psi_{iL}}^{\text{CPV}}(x) = -S_{\psi_{iR}}^{\text{CPV}}(x) \quad (i = j); \quad S_{\psi_{iL}}^{\text{CPV}}(x) = -S_{\psi_{jR}}^{\text{CPV}}(x) \quad (i \neq j)$$