

# *B*-meson anomalies and Higgs physics in flavored $U(1)'$ model

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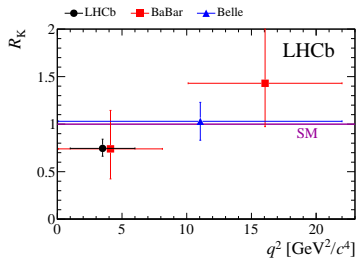
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Ref: [L. Bian, H. M. Lee, CBP, EPJC78, 306 \(2018\)](#)

# B-meson anomalies: $R_K$ and $R_{K^*}$



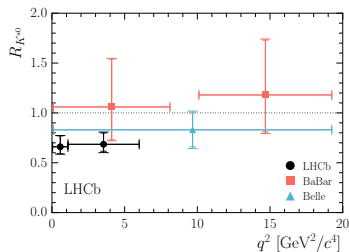
$$R_K \equiv \frac{\mathcal{B}(B \rightarrow K \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K e^+ e^-)}$$

$$= 0.745^{+0.090}_{-0.074}(\text{stat}) \pm 0.036(\text{syst})$$

(1 GeV<sup>2</sup> <  $q^2$  < 6 GeV<sup>2</sup>).

**2.6 $\sigma$**

LHCb, PRL 113, 151601 (2014)



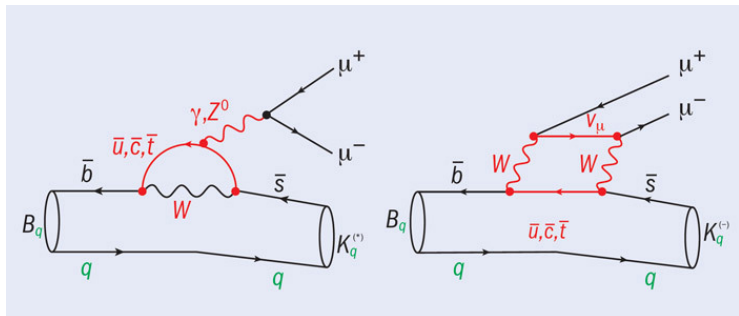
$$R_{K^*} \equiv \frac{\mathcal{B}(B \rightarrow K^* \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^* e^+ e^-)}$$

$$= \begin{cases} 0.66^{+0.11}_{-0.07}(\text{stat}) \pm 0.03(\text{syst}) \\ (0.045 \text{ GeV}^2 < q^2 < 1.1 \text{ GeV}^2), \\ 0.69^{+0.11}_{-0.07}(\text{stat}) \pm 0.05(\text{syst}) \\ (1.1 \text{ GeV}^2 < q^2 < 6.0 \text{ GeV}^2). \end{cases}$$

**2.5 $\sigma$**

LHCb, JHEP 08, 055 (2017)

## B-meson anomalies: $R_K$ and $R_{K^*}$



- Assuming the **lepton flavor universality (LFU)**,

$$R_{K^{(*)}} = \frac{\mathcal{B}(B \rightarrow K^{(*)} \mu^+ \mu^-)}{\mathcal{B}(B \rightarrow K^{(*)} e^+ e^-)} = 1 + \mathcal{O}(m_\mu^2/m_b^2)$$

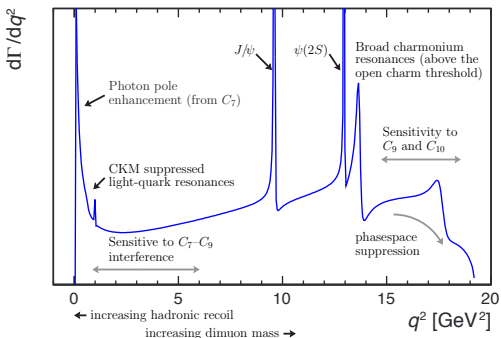
- Theoretical predictions in the SM for  $R_{K^{(*)}}$  are very accurate: hadronic uncertainties cancel.

► Theoretical uncertainties are  $\mathcal{O}(1\%)$  (M. Bordone et al, arXiv:1605.07633).

# B-meson anomalies: effective operators

$$\mathcal{H}_{\text{eff}}^{\text{NP}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \sum_{i,\ell} (\mathcal{C}_i^\ell \mathcal{O}_i^\ell + \mathcal{C}_i^{\ell'} \mathcal{O}_i^{\ell'}) + \text{h.c.}$$

- vector coupling:  $\mathcal{O}_9^\ell = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \ell)$ ,  $\mathcal{O}_9^{\ell'} = (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \ell)$ ,
- axialvector coupling:  $\mathcal{O}_{10}^\ell = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \gamma^5 \ell)$ ,  $\mathcal{O}_{10}^{\ell'} = (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \gamma^5 \ell)$ .



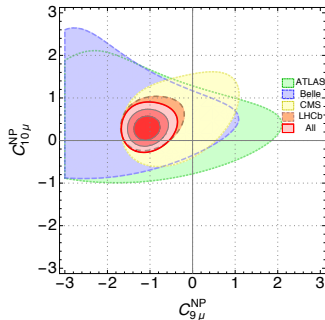
# B-meson anomalies: effective operators

$$\mathcal{H}_{\text{eff}}^{\text{NP}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \sum_{i,\ell} (\mathcal{C}_i^\ell \mathcal{O}_i^\ell + \mathcal{C}_i^{\prime\ell} \mathcal{O}_i^{\prime\ell}) + \text{h.c.}$$

- vector coupling:  $\mathcal{O}_9^\ell = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \ell)$ ,  $\mathcal{O}_9^{\prime\ell} = (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \ell)$ ,
- axialvector coupling:  $\mathcal{O}_{10}^\ell = (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \gamma^5 \ell)$ ,  $\mathcal{O}_{10}^{\prime\ell} = (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \gamma^5 \ell)$ .

Global fit results (B. Capdevila, arXiv:1704.05340):

$$\mathcal{C}_9^\mu = -1.11 \quad \text{or} \\ (\mathcal{C}_9^\mu, \mathcal{C}_{10}^\mu) = (-1.01, 0.29).$$



## $B$ -meson anomalies: effective operators

$$\mathcal{H}_{\text{eff}}^{\text{NP}} = -\frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \frac{e^2}{16\pi^2} \sum_{i,\ell} (\mathcal{C}_i^\ell \mathcal{O}_i^\ell + \mathcal{C}_i^{\ell\prime} \mathcal{O}_i^{\ell\prime}) + \text{h.c.}$$

For an effective Hamiltonian,

$$\mathcal{H}_{\text{eff}}^{\text{NP}} = -\sum_i \frac{1}{\Lambda_i^2} \mathcal{O}_i^\ell$$

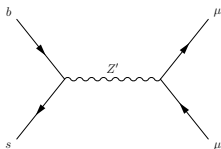
we find

$$\Lambda_i = \frac{4\pi}{e} \frac{1}{\sqrt{|V_{tb} V_{ts}^*|}} \frac{1}{\sqrt{|\mathcal{C}_i|}} \frac{v}{\sqrt{2}} \simeq \frac{35 \text{ TeV}}{\sqrt{|\mathcal{C}_i|}}.$$

- For  $|\mathcal{C}_i| = \mathcal{O}(1)$ ,

$$\Lambda_{\text{NP}} \lesssim 35 \text{ TeV}$$

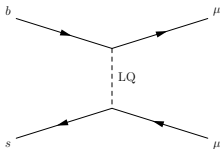
# $B$ -meson anomalies: new physics models



$Z'$

- Flavored  $Z'$  model:

$$-\mathcal{L}_{Z'} \supset \left( g_L^{sb} Z'_\rho \bar{s} \gamma^\rho P_L b + \text{h.c.} \right) + g_L^{\mu\mu} Z'_\rho \bar{\mu} \gamma^\rho P_L \mu$$



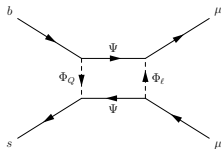
Leptoquark

- Leptoquark model (For  $S_3$  being  $(\bar{3}, 3, 1/3)$  triplet scalar):

$$-\mathcal{L}_{LQ} \supset y_3 Q L S_3 + y_q Q Q S_3^\dagger + \text{h.c.}$$

- Loop mediators (For a fermion  $\Psi$  and two scalars  $\Phi_Q$  and  $\Phi_\ell$ ):

$$-\mathcal{L}_{\text{int}} \supset \Gamma_i^Q \bar{Q}_i P_R \Psi \Phi_Q + \Gamma_i^L \bar{L}_i P_R \Psi \Phi_\ell + \text{h.c.}$$



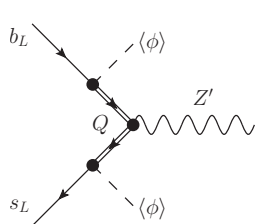
Loop mediators

See G. D'Amico et al, arXiv:1704.05438 and references therein.

# B-meson anomalies: flavored $Z'$ models

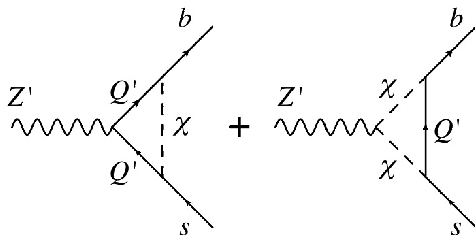
$L_\mu - L_\tau$

- The  $U(1)'$  interactions must be flavor-dependent (*flavored  $Z'$* ).
- The anomaly-free condition restricts the viable classes of  $U(1)'$  models.
- The simplest model with LFU is  $U(1)_{L_\mu - L_\tau}$ .
  - ▶ Extra matters such as vector-like quarks are required.



W. Altmannshofer et al,

arXiv:1403.1269, 1508.07009



P. Ko et al, arXiv:1702.02699



# $B$ -meson anomalies: flavored $Z'$ models

$B_3 - L_3$

- $U(1)'_{B-L}$  with three  $\nu_R$ 's.
  - ▶ gauge anomalies cancel within each generation.
  - ▶ generation of neutrino masses requires at least two  $\nu_R$ 's.
  - ▶ **flavored  $B-L$** :  $B_i - L_i$  ( $i = 1, 2, 3$ ), in particular  $B_3 - L_3$  for  $B$ -anomalies  
(R. Alonso et al, arXiv:1705.03858)

**BUT**, the extra vector-like quarks and leptons are still required to have mixing between the third generation and the first two.

# The flavored $Z'$ model

Consider the linear combination of  $L_\mu - L_\tau$  and  $B_3 - L_3$ .\*

(L. Bian, S.-M. Choi, Y.-J. Kang, H. M. Lee, arXiv:1707.04811)

$$Q_{Z'} = y(L_\mu - L_\tau) + x(B_3 - L_3)$$

( $x$  and  $y$  are real parameters)<sup>†</sup>

- Two Higgs doublets  $H_1$  and  $H_2$  are necessary to have quark masses and mixings.
  - ▶ Only  $H_2$  has the  $U(1)'$  charge. The off-diagonal components of quark mass matrices are obtained from  $\langle H_2 \rangle$ .
- A complex singlet scalar  $S$  is necessary to have the Higgs bilinear term  $H_1^\dagger H_2$ .
- The neutrino masses are generated by extra singlet scalars,  $\Phi_a$  ( $a = 1, 2, 3$ ).

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\*cf. linear combinations of  $L_\mu - L_\tau$  and  $B_1 + B_2 - 2B_3$  (A. Crivellin et al, arXiv:1503.03477) or  $B_3 - L_1$  (P. Ko et al, arXiv:1701.05788)

<sup>†</sup> $y$  could be removed by rescaling the  $Z'$  coupling  $g_{Z'}$ .

# The flavored $Z'$ model

	$q_{3L}$	$u_{3R}$	$d_{3R}$	$\ell_{2L}$	$e_{2R}$	$\nu_{2R}$	$\ell_{3L}$	$e_{3R}$	$\nu_{3R}$
$Q_{Z'}$	$\frac{1}{3}x$	$\frac{1}{3}x$	$\frac{1}{3}x$	$y$	$y$	$y$	$-x-y$	$-x-y$	$-x-y$

	$S$	$H_1$	$H_2$	$\Phi_1$	$\Phi_2$	$\Phi_3$
$Q_{Z'}$	$\frac{1}{3}x$	$0$	$-\frac{1}{3}x$	$-y$	$x+y$	$x$

$$\begin{aligned}
 -\mathcal{L}_Y^q &= \bar{q}_i \left[ \begin{pmatrix} y_{11}^u & y_{12}^u & 0 \\ y_{21}^u & y_{22}^u & 0 \\ 0 & 0 & y_{33}^u \end{pmatrix} \tilde{H}_1 + \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ h_{31}^u & h_{32}^u & 0 \end{pmatrix} \tilde{H}_2 \right] u_j \\
 &+ \bar{q}_i \left[ \begin{pmatrix} y_{11}^d & y_{12}^d & 0 \\ y_{21}^d & y_{22}^d & 0 \\ 0 & 0 & y_{33}^d \end{pmatrix} H_1 + \begin{pmatrix} 0 & 0 & h_{13}^d \\ 0 & 0 & h_{23}^d \\ 0 & 0 & 0 \end{pmatrix} H_2 \right] d_j \quad (\tilde{H}_i = i\sigma_2 H_i^*).
 \end{aligned}$$

- If  $H_1 \leftrightarrow H_2$  and  $h_{ij}^{u,d} = 0$ , the model corresponds to the type-I 2HDM.

## The flavored $Z'$ model

$$(M_u)_{ij} = \frac{\nu \cos \beta}{\sqrt{2}} \begin{pmatrix} y_{11}^u & y_{12}^u & 0 \\ y_{21}^u & y_{22}^u & 0 \\ 0 & 0 & y_{33}^u \end{pmatrix} + \frac{\nu \sin \beta}{\sqrt{2}} \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ h_{31}^u & h_{32}^u & 0 \end{pmatrix}$$
$$(M_d)_{ij} = \frac{\nu \cos \beta}{\sqrt{2}} \begin{pmatrix} y_{11}^d & y_{12}^d & 0 \\ y_{21}^d & y_{22}^d & 0 \\ 0 & 0 & y_{33}^d \end{pmatrix} + \frac{\nu \sin \beta}{\sqrt{2}} \begin{pmatrix} 0 & 0 & h_{13}^d \\ 0 & 0 & h_{23}^d \\ 0 & 0 & 0 \end{pmatrix} \quad (\tan \beta = \nu_2/\nu_1).$$

Diagonalization of quark matrices:

$$U_L^\dagger M_u U_R = M_u^D = \text{diag}(m_u, m_c, m_t),$$

$$D_L^\dagger M_d D_R = M_d^D = \text{diag}(m_d, m_s, m_b).$$

and  $V_{\text{CKM}} = U_L^\dagger D_L$ .

■  $h_{31}^u$  and  $h_{32}^u$  correspond to the right-handed rotations.

►  $U_L \simeq \mathbb{1}$ , so  $V_{\text{CKM}} \simeq D_L$ .

## $B$ -meson anomalies: the flavored $Z'$ model

For  $D_L = V_{\text{CKM}}$ ,

$$\begin{aligned}\mathcal{L}_{Z'} &\supset \frac{1}{2} m_{Z'}^2 Z_\mu'^2 + g_{Z'} Z'_\mu \left[ \frac{x}{3} \bar{d}_i \gamma^\mu V_{\text{CKM}}^\dagger \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 1 \end{pmatrix} V_{\text{CKM}} P_L d_j + y \bar{\mu} \gamma^\mu \mu \right] \\ &= \frac{1}{2} m_{Z'}^2 Z_\mu'^2 + g_{Z'} Z'_\mu \left( \frac{x}{3} V_{ts}^* V_{tb} \bar{s} \gamma^\mu P_L b + \text{h.c.} + y \bar{\mu} \gamma^\mu \mu \right) + \dots\end{aligned}$$

Integrating out  $Z'$  by the equation of motion,

$$-\mathcal{L}_{\text{eff}} = \frac{xyg_{Z'}^2}{3m_{Z'}^2} V_{ts}^* V_{tb} (\bar{s} \gamma^\mu P_L b) (\bar{\mu} \gamma_\mu \mu) + \text{h.c.}$$

Thus,

$$\mathcal{C}_9^\mu = -\frac{8xy\pi^2 \alpha_{Z'}}{3\alpha} \left( \frac{v}{m_{Z'}} \right)^2$$

- The  $b$ -quark transition is only through CKM.

The best-fit value  $\mathcal{C}_9^\mu = -1.10$

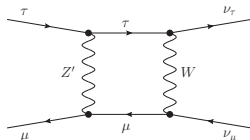
(B. Capdevila, arXiv:1704.05340) gives us

$$m_{Z'} = 1.2 \text{ TeV} \times \left( xy \frac{\alpha_{Z'}}{\alpha} \right)^{1/2}$$

# The flavored $Z'$ model: constraints

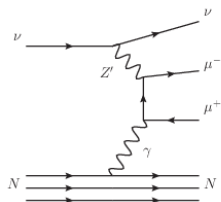
Important bounds include:

- $B_s^0 - \bar{B}_s^0$  mixing and  $B \rightarrow X_s \gamma$ ,
- $\tau \rightarrow \mu \nu_\tau \bar{\nu}_\mu$ ,



$$\frac{\Delta \mathcal{B}(\tau \rightarrow \mu \nu_\tau \bar{\nu}_\mu)}{\mathcal{B}(\tau \rightarrow \mu \nu_\tau \bar{\nu}_\mu)_{\text{SM}}} = \frac{3y(x+y)g_{Z'}^2}{4\pi^2} \frac{\ln(m_W^2/m_{Z'}^2)}{1 - m_{Z'}^2/m_W^2}$$

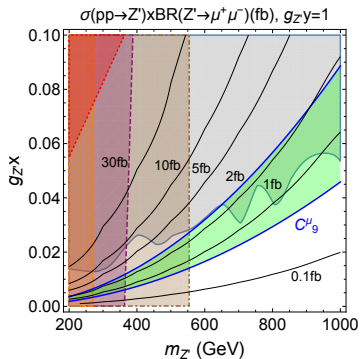
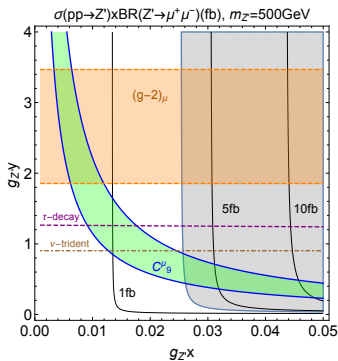
- Neutrino trident production at CHARM-II, CCFR, and NuTeV,



$$\frac{\sigma}{\sigma_{\text{SM}}} \simeq \frac{1 + (1 + 4s_W^2 + 2y^2 g_{Z'}^2 v^2 / m_{Z'}^2)^2}{1 + (1 + 4s_W^2)^2}$$

- $pp \rightarrow Z' \rightarrow \mu^+ \mu^-$  at ATLAS and CMS.

# The flavored $Z'$ model: constraints



from L. Bian et al, arXiv:1707.04811

## The flavored $Z'$ model: Higgs sector

Two Higgs doublets  $H_1, H_2$  + singlet scalar  $S$ :

$$\begin{aligned} V(H_1, H_2, S) = & \mu_1^2 |H_1|^2 + \mu_2^2 |H_2|^2 - (\mu S H_1^\dagger H_2 + \text{h.c.}) \\ & + \lambda_1 |H_1|^4 + \lambda_2 |H_2|^4 + 2\lambda_3 |H_1|^2 |H_2|^2 + 2\lambda_4 (H_1^\dagger H_2)(H_2^\dagger H_1) \\ & + 2|S|^2(\kappa_1 |H_1|^2 + \kappa_2 |H_2|^2) + m_S^2 |S|^2 + \lambda_S |S|^4 \end{aligned}$$

with

$$H_j = \begin{pmatrix} \phi_j^+ \\ (v_j + \rho_j + i\eta_j)/\sqrt{2} \end{pmatrix} \quad (j=1, 2), \quad S = \frac{v_S + S_R + iS_I}{\sqrt{2}}.$$



## The flavored $Z'$ model: Higgs sector

$$H_j = \begin{pmatrix} \phi_j^+ \\ (v_j + \rho_j + i\eta_j)/\sqrt{2} \end{pmatrix} \quad (j=1, 2), \quad S = \frac{v_S + S_R + iS_I}{\sqrt{2}}.$$

- $v_S$  determines the  $Z'$  mass,
- $G^0 = \cos\beta\eta_1 + \sin\beta\eta_2$  is eaten by the  $Z$  boson.
- The mass of the CP-odd scalar  $A^0 = \sin\beta\eta_1 - \cos\beta\eta_2$  is

$$m_A^2 = \frac{\mu \sin\beta \cos\beta}{\sqrt{2}v_S} \left( v^2 + \frac{v_S^2}{\sin^2\beta \cos^2\beta} \right).$$

- And, the charged Higgs boson  $H^+ = \sin\beta\phi_1^+ - \cos\beta\phi_2^+$  is

$$m_{H^+}^2 = m_A^2 - \left( \frac{\mu \sin\beta \cos\beta}{\sqrt{2}v_S} + \lambda_4 \right) v^2.$$

# The flavored $Z'$ model: Higgs sector

For CP-even scalars:

$$M_S = \begin{pmatrix} 2\lambda_1 v_1^2 + \frac{\mu v_2 v_s}{\sqrt{2} v_1} & 2v_1 v_2 (\lambda_3 + \lambda_4) - \frac{\mu v_s}{\sqrt{2}} & 2\kappa_1 v_1 v_s - \frac{\mu v_2}{\sqrt{2}} \\ 2v_1 v_2 (\lambda_3 + \lambda_4) - \frac{\mu v_s}{\sqrt{2}} & 2\lambda_2 v_2^2 + \frac{\mu v_1 v_s}{\sqrt{2} v_2} & 2\kappa_2 v_2 v_s - \frac{\mu v_1}{\sqrt{2}} \\ 2\kappa_1 v_1 v_s - \frac{\mu v_2}{\sqrt{2}} & 2\kappa_2 v_2 v_s - \frac{\mu v_1}{\sqrt{2}} & 2\lambda_S v_s^2 + \frac{\mu v_1 v_2}{\sqrt{2} v_s} \end{pmatrix}$$

Suppose that mixing with singlet scalar is negligible. Then,

$$\begin{pmatrix} h_1 \\ h_2 \\ h_3 \end{pmatrix} = \begin{pmatrix} \cos \alpha & \sin \alpha & 0 \\ -\sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} \rho_1 \\ \rho_2 \\ S_R \end{pmatrix}.$$

And, for  $h = h_1$  and  $H = h_2$ ,

$$\lambda_1 \approx \frac{2(m_h^2 \cos^2 \alpha + m_H^2 \sin^2 \alpha) - \sqrt{2} \mu v_s \tan \beta}{4v^2 \cos^2 \beta},$$

$$\lambda_2 \approx \frac{2(m_h^2 \sin^2 \alpha + m_H^2 \cos^2 \alpha) - \sqrt{2} \mu v_s \cot \beta}{4v^2 \sin^2 \beta},$$

$$\lambda_3 + \lambda_4 \approx \frac{(m_h^2 - m_H^2) \sin 2\alpha + \sqrt{2} \mu v_s}{4v^2 \sin 2\beta}.$$

If  $m_h = 125$  GeV, the input parameters for the CP-even Higgses are

$$m_H, \mu v_s, \tan \beta, \sin \alpha.$$

## The flavored $Z'$ model: quarks

Recall the quark mass matrices:

$$M_u = \begin{pmatrix} y_{11}^u \langle \tilde{H}_1 \rangle & y_{12}^u \langle \tilde{H}_1 \rangle & 0 \\ y_{21}^u \langle \tilde{H}_1 \rangle & y_{22}^u \langle \tilde{H}_1 \rangle & 0 \\ h_{31}^u \langle \tilde{H}_2 \rangle & h_{32}^u \langle \tilde{H}_2 \rangle & y_{33}^u \langle \tilde{H}_1 \rangle \end{pmatrix},$$
$$M_d = \begin{pmatrix} y_{11}^d \langle H_1 \rangle & y_{12}^d \langle H_1 \rangle & h_{13}^d \langle H_2 \rangle \\ y_{21}^d \langle H_1 \rangle & y_{22}^d \langle H_1 \rangle & h_{23}^d \langle H_2 \rangle \\ 0 & 0 & y_{33}^d \langle H_1 \rangle \end{pmatrix}$$

The mixing with the third generation is induced by  $H_2$ .

## The flavored $Z'$ model: quarks

For  $V_{\text{CKM}} = D_L$  and  $D_R = \mathbb{1}$ , the flavor-violating couplings are determined by  $V_{\text{CKM}}$ ,  $\tan \beta$ , and  $y_{33}^u$ .

$$h_{13}^d = \frac{\sqrt{2}m_b}{\nu \sin \beta} V_{ub}, \quad h_{23}^d = \frac{\sqrt{2}m_b}{\nu \sin \beta} V_{cb},$$

$$|y_{33}^u|^2 + \tan^2 \beta (|h_{31}^u|^2 + |h_{32}^u|^2) = \frac{2m_t^2}{\nu^2 \cos^2 \beta},$$

$$y_{21}^u (h_{31}^u)^* + y_{22}^u (h_{32}^u)^* = 0, \quad y_{11}^u (h_{31}^u)^* + y_{12}^u (h_{32}^u)^* = 0.$$

The physical couplings are  $\tilde{h}^d = D_L^\dagger h^d D_R$  and  $\tilde{h}^u = U_L^\dagger h^u U_R$ :

$$\tilde{h}_{33}^u = \frac{\sqrt{2}m_t}{\nu \sin \beta} \left( 1 - \frac{\nu^2 \cos^2 \beta}{2m_t^2} |y_{33}^u|^2 \right), \quad \tilde{h}_{13}^d = 1.80 \times 10^{-2} \left( \frac{m_b}{\nu \sin \beta} \right),$$
$$\tilde{h}_{23}^d = 5.77 \times 10^{-2} \left( \frac{m_b}{\nu \sin \beta} \right), \quad \tilde{h}_{33}^d = 2.41 \times 10^{-3} \left( \frac{m_b}{\nu \sin \beta} \right).$$

- small  $\tan \beta \Rightarrow$  large flavor violation.

## The flavored $Z'$ model: leptons

The mass matrix for charged leptons are diagonal:

$$M_\ell = \begin{pmatrix} y_{11}^\ell \langle H_1 \rangle & 0 & 0 \\ 0 & y_{22}^\ell \langle H_1 \rangle & 0 \\ 0 & 0 & y_{33}^\ell \langle H_1 \rangle \end{pmatrix}.$$

On the other hand, the neutrinos are

$$-\mathcal{L}_Y^\nu = \bar{\ell} M_D \nu_R + \overline{(\nu_R)^c} M_R \nu_R + \text{h.c.},$$

with

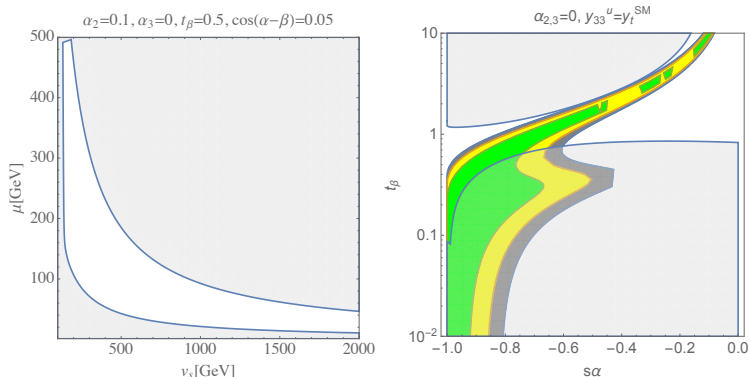
$$M_D = \begin{pmatrix} y_{11}^\nu \langle \tilde{H}_1 \rangle & 0 & 0 \\ 0 & y_{22}^\nu \langle \tilde{H}_1 \rangle & 0 \\ 0 & 0 & y_{33}^\nu \langle \tilde{H}_1 \rangle \end{pmatrix}, \quad M_R = \begin{pmatrix} M_{11} & z_{12}^{(1)} \langle \Phi_1 \rangle & z_{13}^{(2)} \langle \Phi_2 \rangle \\ z_{21}^{(1)} \langle \Phi_1 \rangle & 0 & z_{23}^{(3)} \langle \Phi_3 \rangle \\ z_{31}^{(2)} \langle \Phi_2 \rangle & z_{32}^{(3)} \langle \Phi_3 \rangle & 0 \end{pmatrix}.$$

- The neutrino masses arise via the seesaw mechanism,

$$m_\nu \simeq -M_D M_R^{-1} M_D^T.$$

# Constraints on the Higgs sector

Theoretical bounds from the perturbative unitarity and stability and experimental bounds from the Higgs data at the LHC

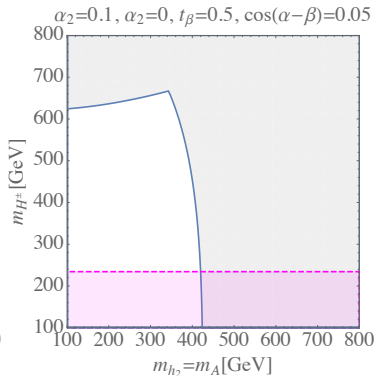
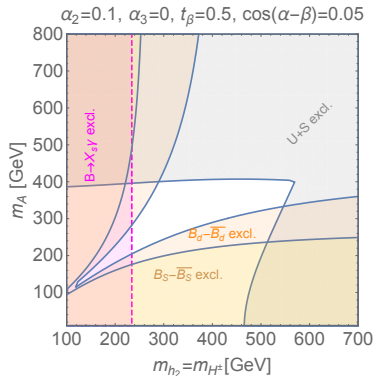


The EWPT constraint (assuming negligible kinetic mixing):

$$\Delta\rho = \frac{m_W^2}{m_{Z'}^2 \cos^2 \theta_W} - 1 \simeq 10^{-4} \left( \frac{x}{0.05} \right)^2 g_{Z'}^2 \sin^4 \beta \left( \frac{400 \text{ GeV}}{m_{Z'}} \right)^2.$$

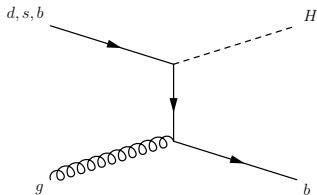
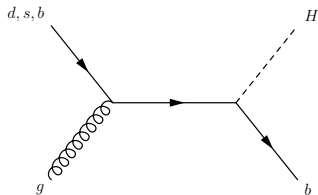
# Constraints on the Higgs sector

$B$ -physics bounds:  $B_s \rightarrow \mu^+ \mu^-$ ,  $B_s - \bar{B}_s$  mixing,  $B \rightarrow X_s \gamma$  for the heavy Higgses as well as  $Z'$



# Higgs productions and decays at the LHC: neutral

- The standard channels for neutral Higgs production are  $gg \rightarrow H$  and  $b\bar{b} \rightarrow H$ .
- Productions through the flavor-violating couplings,  $b\bar{d}_i/d_i\bar{b} \rightarrow H$  ( $d_i = d, s$ ).
- $b$ -quark associated productions:  $bg \rightarrow bH$  and  $d_i g \rightarrow bH$ .





## Higgs productions and decays at the LHC: neutral

$$-\mathcal{L}_Y^H \supset \frac{\lambda_t^H}{\sqrt{2}} \bar{t}_R t_L H + \frac{\lambda_b^H}{\sqrt{2}} \bar{b}_R b_L H + \frac{\sin(\alpha - \beta)}{\sqrt{2} \cos \beta} \bar{b}_R (\tilde{h}_{13}^{d*} d_L + \tilde{h}_{23}^{d*} s_L) H + \text{h.c.},$$

where

$$\lambda_t^H = \frac{\sqrt{2} m_t \cos \alpha}{v \cos \beta} + \frac{\tilde{h}_{33}^u \sin(\alpha - \beta)}{\cos \beta}, \quad \lambda_b^H = \frac{\sqrt{2} m_b \cos \alpha}{v \cos \beta} + \frac{\tilde{h}_{33}^d \sin(\alpha - \beta)}{\cos \beta}$$

with

$$\tilde{h}_{13}^d = \frac{\sqrt{2} m_b}{v \sin \beta} (V_{ud}^* V_{ub} + V_{cd}^* V_{cb}), \quad \tilde{h}_{23}^d = \frac{\sqrt{2} m_b}{v \sin \beta} (V_{us}^* V_{ub} + V_{cs}^* V_{cb}),$$

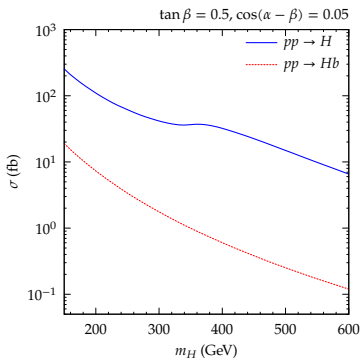
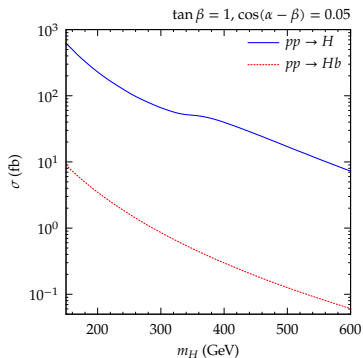
$$\tilde{h}_{33}^d = \frac{\sqrt{2} m_b}{v \sin \beta} (|V_{ub}|^2 + |V_{cb}|^2), \quad \tilde{h}_{33}^u = \frac{\sqrt{2} m_t}{v \sin \beta} \left( 1 - \frac{v^2 \cos^2 \beta}{2 m_t^2} |y_{33}^u|^2 \right).$$

If  $y_{33}^u = y_t^{\text{SM}}$ ,

$$\lambda_t^H = y_t^{\text{SM}} \cos(\alpha - \beta) \xrightarrow{\alpha = \beta - \pi/2} 0.$$

The gluon-fusion process is suppressed compared to the SM case.

# Higgs productions and decays at the LHC: neutral



For  $m_H = 200$  GeV and  $\tan \beta = 1$  (0.5),  $\sigma_{pp \rightarrow H} \simeq 225.2$  (110.5) fb.

$$(\sigma_{b\bar{d}_i \rightarrow H} + \sigma_{d_i \bar{b} \rightarrow H}) / \sigma_{gg \rightarrow H} \simeq 0.62\% (1.6\%),$$

$$(\sigma_{b\bar{d}_i \rightarrow H} + \sigma_{d_i \bar{b} \rightarrow H}) / \sigma_{b\bar{b} \rightarrow H} \simeq 1.6\% (10.9\%).$$

- The gluon-fusion process is still the most dominant.

## Higgs productions and decays at the LHC: neutral

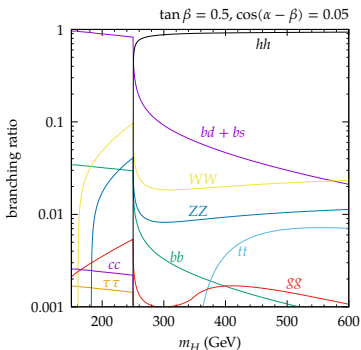
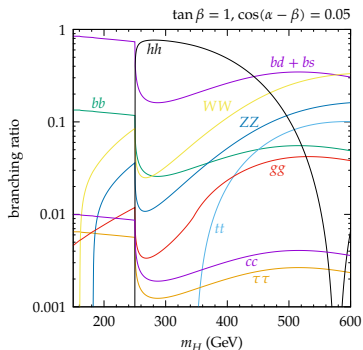
The most important decay modes of the heavy neutral Higgs are  $H \rightarrow b\bar{d}_i$  and  $H \rightarrow hh$ .

$$\Gamma(H \rightarrow b\bar{d}_i) = \Gamma(H \rightarrow d_i\bar{b}) = \frac{3|\tilde{h}_{i3}^d|^2 \sin^2(\alpha - \beta)}{32\pi \cos^2 \beta} m_H \left(1 - \frac{m_b^2}{m_H^2}\right)^2,$$
$$\Gamma(H \rightarrow hh) = \frac{g_{Hhh}^2 v^2}{32\pi m_H} \left(1 - \frac{4m_h^2}{m_H^2}\right)^{1/2},$$

where

$$\tilde{h}_{13}^d = 1.80 \times 10^{-2} \left(\frac{m_b}{v \sin \beta}\right), \quad \tilde{h}_{23}^d = 5.77 \times 10^{-2} \left(\frac{m_b}{v \sin \beta}\right),$$
$$g_{Hhh} = 3(\lambda_1 \sin \alpha \cos \beta + \lambda_2 \cos \alpha \sin \beta) \sin(2\alpha) \\ + (\lambda_3 + \lambda_4) [3 \cos(\alpha + \beta) \cos(2\alpha) - \cos(\alpha - \beta)].$$

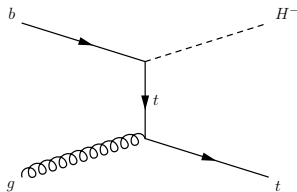
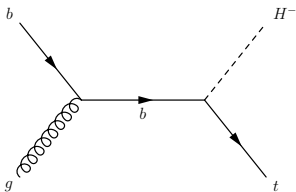
# Higgs productions and decays at the LHC: neutral



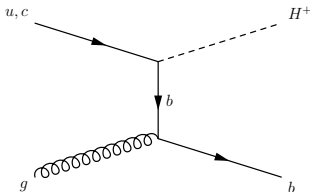
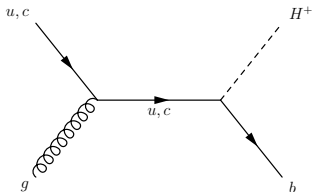
- If  $m_H < 2m_{hh}$ ,  $H \rightarrow bq$  is the most dominant channel.
- If  $m_H > 2m_{hh}$ ,  $H \rightarrow hh$  up to accidental cancellation in the trilinear coupling  $g_{Hhh}$ .

# Higgs productions and decays at the LHC: charged

- The standard channels for charged Higgs production are top quark associated process,  $bg \rightarrow tH^-$ .



- The bottom quark associated production is possible:  $u_i g \rightarrow bH^+$  ( $u_i = u, c$ )



# Higgs productions and decays at the LHC: charged

$$-\mathcal{L}_Y^{H^-} \supset \bar{b}(\lambda_{t_L}^{H^-} P_L + \lambda_{t_R}^{H^-} P_R)tH^- + \bar{b}(\lambda_{c_L}^{H^-} P_L + \lambda_{c_R}^{H^-} P_R)cH^- + \lambda_{u_L}^{H^-} \bar{b}P_L uH^- + \text{h.c.},$$

where

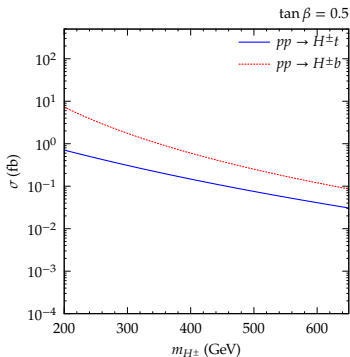
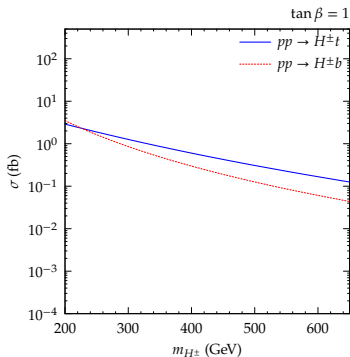
$$\lambda_{t_L}^{H^-} = \frac{\sqrt{2}m_b \tan \beta}{v} V_{tb}^* - \frac{(V_{\text{CKM}} \tilde{h}^d)_{33}^*}{\cos \beta}, \quad \lambda_{t_R}^{H^-} = -\left( \frac{\sqrt{2}m_t \tan \beta}{v} - \frac{\tilde{h}_{33}^u}{\cos \beta} \right) V_{tb}^*,$$

$$\lambda_{c_L}^{H^-} = \frac{\sqrt{2}m_b \tan \beta}{v} V_{cb}^* - \frac{(V_{\text{CKM}} \tilde{h}^d)_{23}^*}{\cos \beta}, \quad \lambda_{c_R}^{H^-} = -\frac{\sqrt{2}m_c \tan \beta}{v} V_{cb}^*,$$

$$\lambda_{u_L}^{H^-} = \frac{\sqrt{2}m_b \tan \beta}{v} V_{ub}^* - \frac{(V_{\text{CKM}} \tilde{h}^d)_{13}^*}{\cos \beta}.$$

- If  $y_{33}^u = y_t^{\text{SM}}$ ,  $\lambda_{t_R}^{H^-} = 0$ .

# Higgs productions and decays at the LHC: charged



- The bottom-quark associated production can be dominant process for the charged Higgs if  $\tan \beta$  is small.

# Higgs productions and decays at the LHC: charged

The most important decay modes of the heavy charged Higgs are  $H^+ \rightarrow W^+ h$  and  $H^+ \rightarrow t\bar{b}$ .

$$\Gamma(H^+ \rightarrow W^+ h) = \Gamma(H^- \rightarrow W^- h)$$

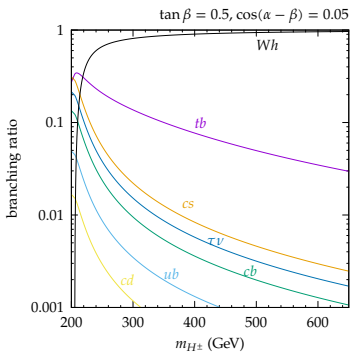
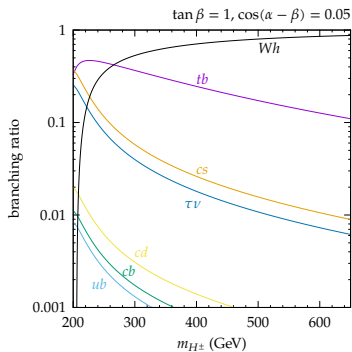
$$= \frac{g^2 \cos^2(\alpha - \beta) m_{H^\pm}^3}{64\pi m_W^2} \left[ \left( 1 - \frac{m_W^2}{m_{H^\pm}^2} - \frac{m_h^2}{m_{H^\pm}^2} \right)^2 - \frac{4m_W^2 m_h^2}{m_{H^\pm}^4} \right]^{3/2},$$

$$\Gamma(H^+ \rightarrow t\bar{b}) = \Gamma(H^- \rightarrow b\bar{t})$$

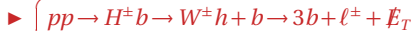
$$= \frac{3|\lambda_{t_L}^{H^-}|^2 m_{H^\pm}}{16\pi} \left[ \left( 1 - \frac{(m_t + m_b)^2}{m_{H^\pm}^2} \right) \left( 1 - \frac{(m_t - m_b)^2}{m_{H^\pm}^2} \right) \right]^{1/2} \\ \times \left( 1 - \frac{m_t^2 + m_b^2}{m_{H^\pm}^2} \right) \quad (y_{33}^\mu = y_t^{\text{SM}}, \lambda_{t_R}^{H^-} = 0).$$



# Higgs productions and decays at the LHC: charged



- If kinematically allowed,  $H^+ \rightarrow W^+ h$  is always the most dominant channel.



will be the smoking gun signal at the LHC and future hadron colliders.

# Summary and conclusion

- The  $B$ -meson anomalies at LHCb indicate BSM, which could be the flavored  $Z'$ .
  - ▶ We studied  $U(1)'_{\gamma(L_\mu - L_\tau) + \kappa(B_3 - L_3)}$ .
- Various theoretical and experimental bounds are important.
  - ▶ Perturbative unitarity and stability, electroweak precision and Higgs data,  $B$ -meson mixing,  $B_s \rightarrow \mu^+ \mu^-$ ,  $b \rightarrow s \gamma$ , rare decays, ...
- Direct signals can be probed via  $Z' \rightarrow \mu \mu$  and flavor-violating decays of heavy Higgs bosons at the LHC.
  - ▶  $pp \rightarrow H^\pm + b \rightarrow W^\pm h + b$  will be the smoking gun signal.