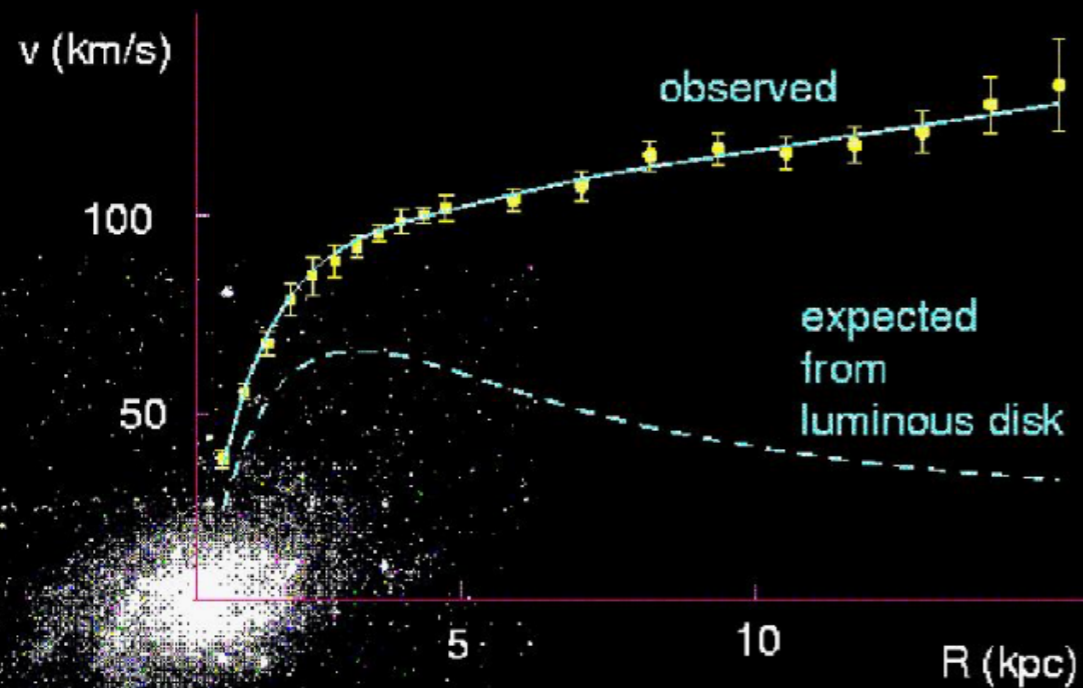


# Phenomenology of dark gauge group at the LHC

박명훈



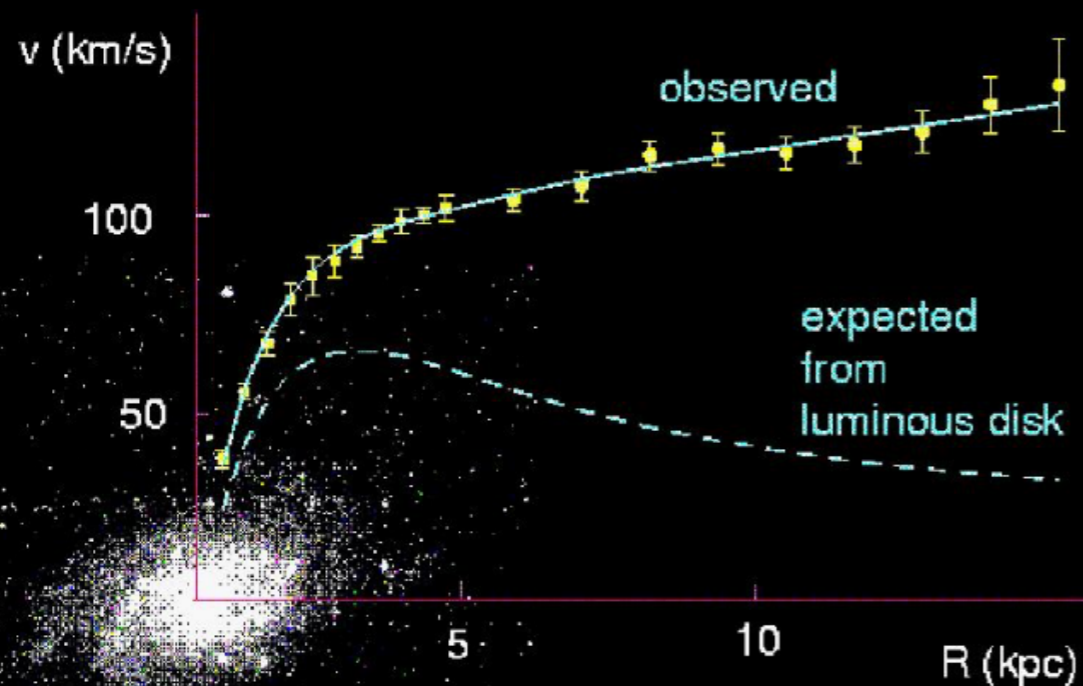
# Dark Matter is neutral



M33 rotation curve

- We know that we **can not** see dark matter directly

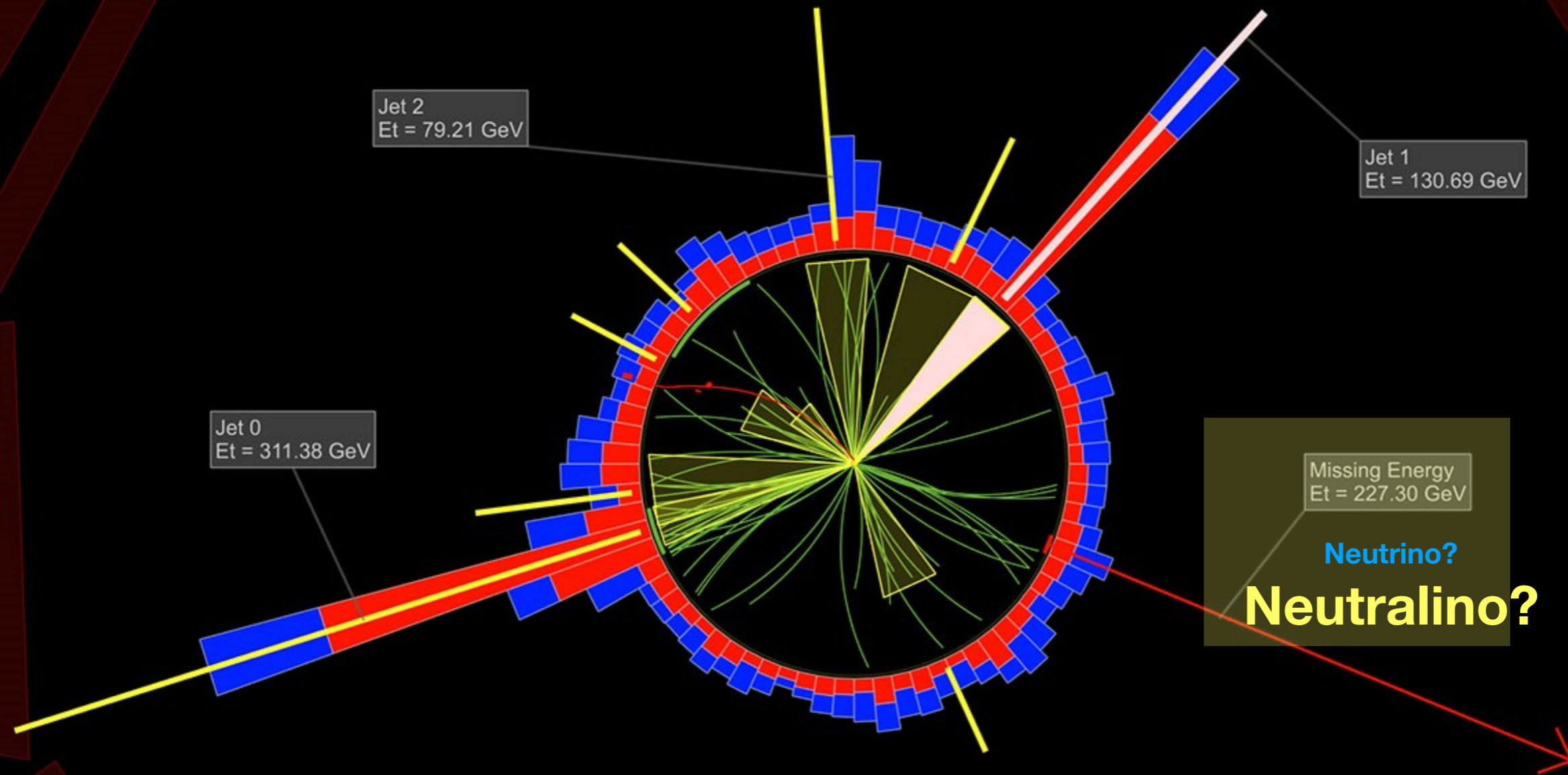
# Dark Matter is neutral



M33 rotation curve

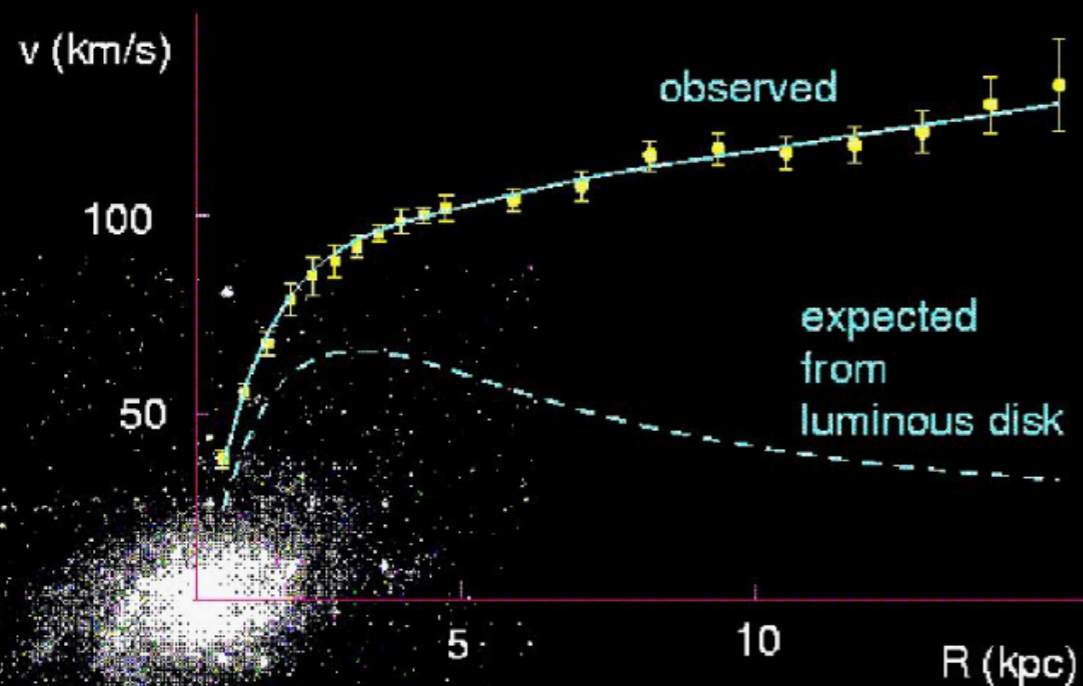
- We know that we **can not** see dark matter directly
- ↓
- Dark Matter is **Neutral** under **Standard Model  $U(1)_{EM}$**

# Collider signature for neutral Dark Matter



SUSY simulated by CMS

# Is Dark Matter neutral under ...?



M33 rotation curve

- We know that we **can not** see dark matter directly



- Dark Matter is Neutral under Standard Model  $U(1)_{EM}$

- But it **does not** mean that Dark Matter is neutral under “**Dark Gauge Group(s)**”

- What would be the **phenomenological consequences** of “dark charged” dark matter ?
- How we can **check** whether dark matter is “dark charged” or not.

# Particle under Gauge Group

- In the Standard Model, **fermions** get masses due to **a Higgs [designed to break SU(2)]**
- In the Standard Model, proton/neutron get masses due to **non-abelian gauge-charged**.

- Fermion, Gauge particle and Higgs
  - Dark Matter, Dark Gauge particle and Dark Higgs



# U(1) Dark photon and DM

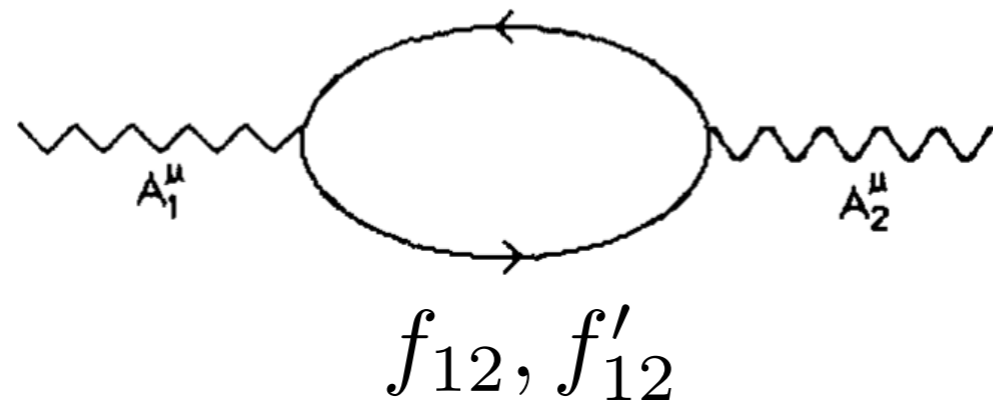
- Dark matter may have a dark-U(1) charge (good to have proper relic density)
- dark-U(1) can mix with SM U(1)-hyper through a Gauge-kinetic mixing : Gauge-invariant term

$$\mathcal{L} \ni \epsilon F'_{\mu\nu} F_Y^{\mu\nu} \quad \begin{array}{c} \gamma_d \\ \text{~~~~~} \end{array} \times \begin{array}{c} \gamma \\ \text{~~~~~} \end{array}$$

- If dark-U(1) is massless (unbroken), then a dark matter can have a milli-charged under SM U(1)
- If dark-U(1) is massive, dark matter would be totally neutral under SM U(1) (Holdom 1986)
- **If this additional U(1) exists, it can be a portal to DM sector**

# Small mixing

- There may be loop-induced diagram, mediated particles charged under two U(1)

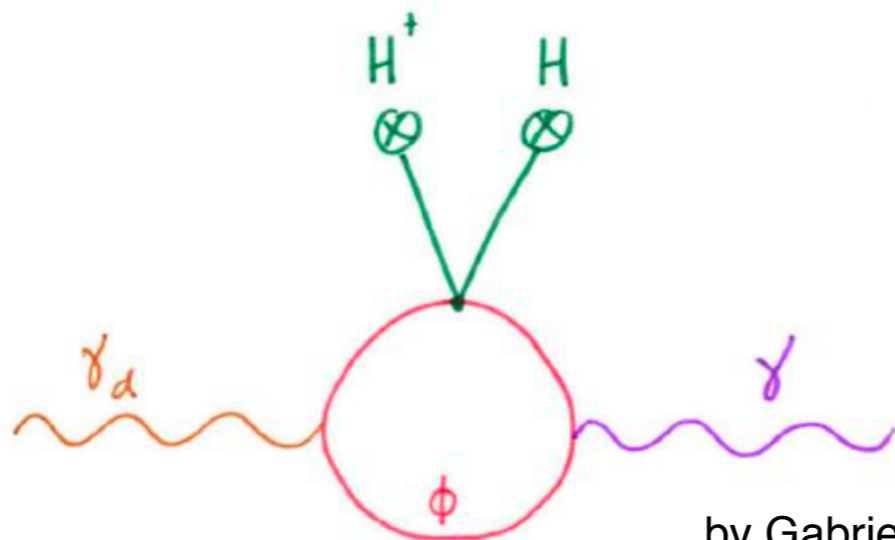


Holdom 1986

$$\epsilon \propto \frac{Q_1 Q_2}{\pi^2} \ln \left( \frac{m'_{12}}{m_{12}} \right)$$

- Higher dimensional operator, induced from Standard Model SU(2) and dark U(1)

Spencer Chang et.al. 2015



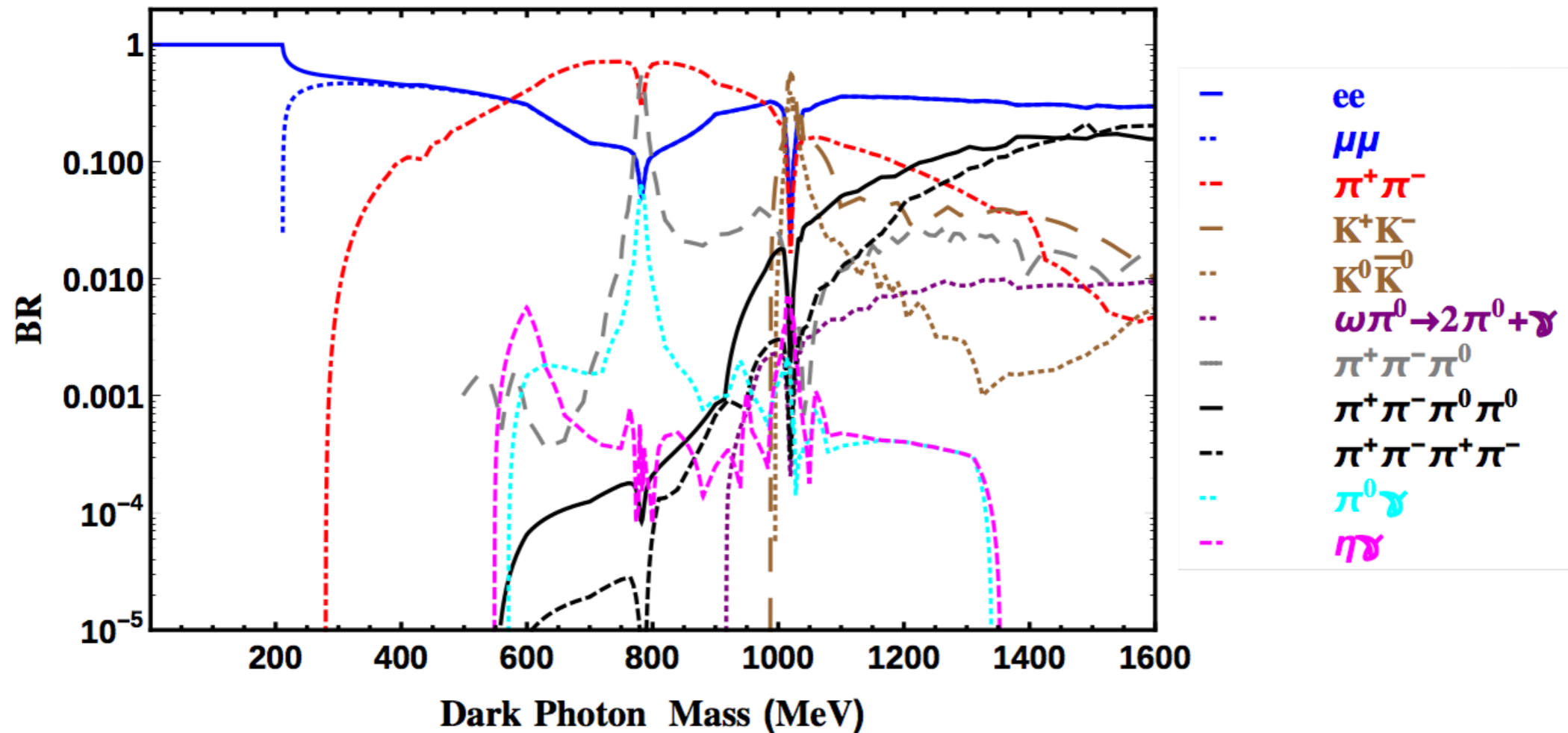
by Gabriel Barello

$$\frac{c}{16\pi^2 m_\phi^2} (H^\dagger \tau^a H) W_{\mu\nu}^a F_D^{\mu\nu}$$

- mediated by SU(2) triplet  $\phi$

# Dark photon decay

The decay of dark photon only depend on its mass:



There are just two parameters in this simple extension:  
**kinetic mixing** and **dark photon mass**.



life time



decay pattern

# DM with dark charge and dark-Higgs

- For a minimality, abelian U(1)-gauge on DM
  - Dark Matter, Gauge field and Dark-Higgs

$A'_\mu$	$\Phi$	$\chi_L$	$\chi_R$	• • •
	$Q'_\Phi$	$Q'_{\chi_L}$	$Q'_{\chi_R}$	

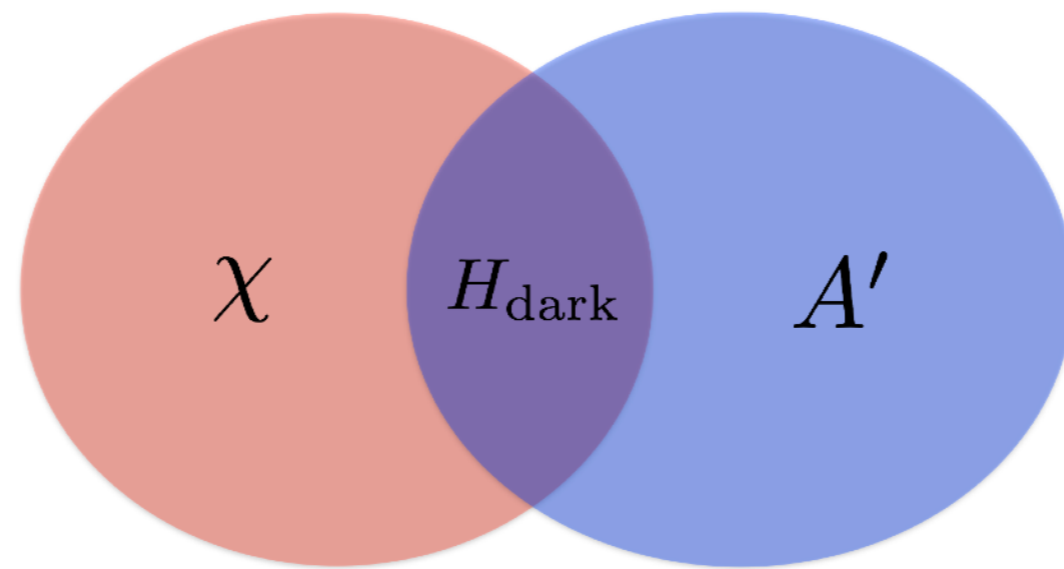
$$\mathcal{L}_{\text{matter}} \ni -g' Q'_V A'_\mu \bar{\chi} \gamma^\mu \chi - g' Q'_A A'_\mu \bar{\chi} \gamma^\mu \gamma_5 \chi$$

## Yukawa for mass

$$Q'_A = \frac{1}{2} (Q'_{\chi_R} - Q'_{\chi_L}) = \frac{Q'_\Phi}{2} \quad \leftarrow \quad \mathcal{L} \ni y_\chi \bar{\chi}_L \Phi^* \chi_R + h.c.$$

$$Q'_V = \frac{1}{2} (Q'_{\chi_R} + Q'_{\chi_L}) = \frac{Q'_\Phi}{2} + Q'_{\chi_L} \quad Q'_{\chi_L} - Q'_{\chi_R} + Q'_\Phi = 0$$

- Dark matter and dark-photon **share the same origin (Dark Higgs)** for their mass



Yukawa Interaction

$$\mathcal{L} \ni y_\chi \bar{\chi}_L \Phi^* \chi_R + h.c.$$

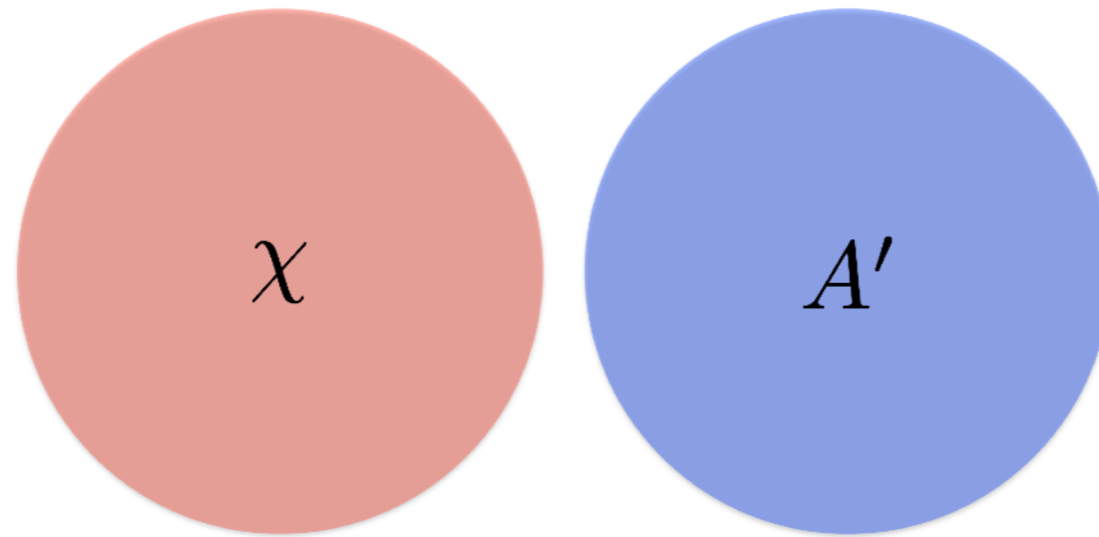
Dark-gauge breaking with non-zero charge  $Q'_\Phi$

$$Q'_{\chi_L} - Q'_{\chi_R} + Q'_\Phi = 0$$

- For maximal chirality:  $Q'_{\chi_R} = 0$  ,  $Q'_{\chi_L} = -Q'_\Phi$

$$Q'_A = \frac{1}{2} (Q'_{\chi_R} - Q'_{\chi_L}) = \frac{Q'_\Phi}{2}$$

- Dark matter and dark-photon **DO NOT share the a source** for their mass

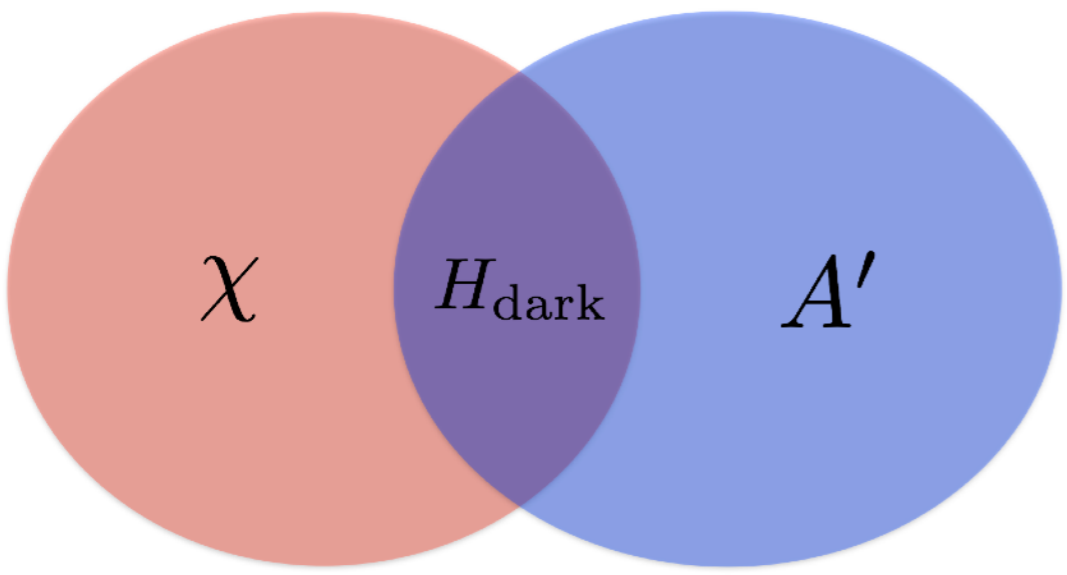


**No Yukawa Interaction: Vector-like DM**

$$Q'_{\chi L} = Q'_{\chi R}$$

- No axial vector coupling:

$$Q'_A = \frac{1}{2} (Q'_{\chi R} - Q'_{\chi L}) = 0$$



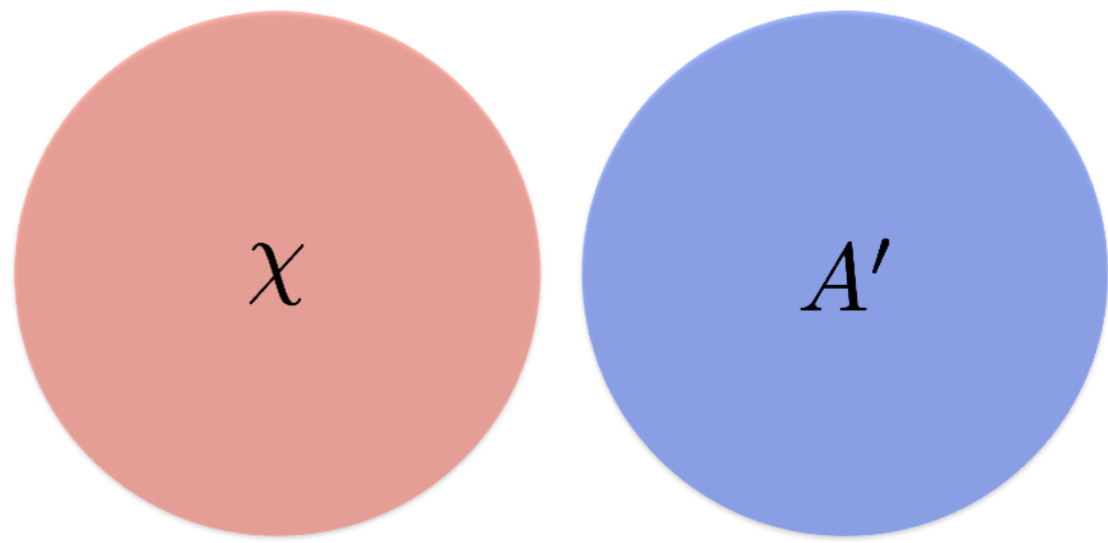
dark matter and dark-photon share the same origin for their mass

$$Q'_A = \frac{1}{2} (Q'_{\chi_R} - Q'_{\chi_L}) = \frac{Q'_\Phi}{2}$$

**with Dark-Higgs  
Chiral fermion**

# Can we see difference @ LHC ?

dark matter and dark-photon have their own mass mechanism

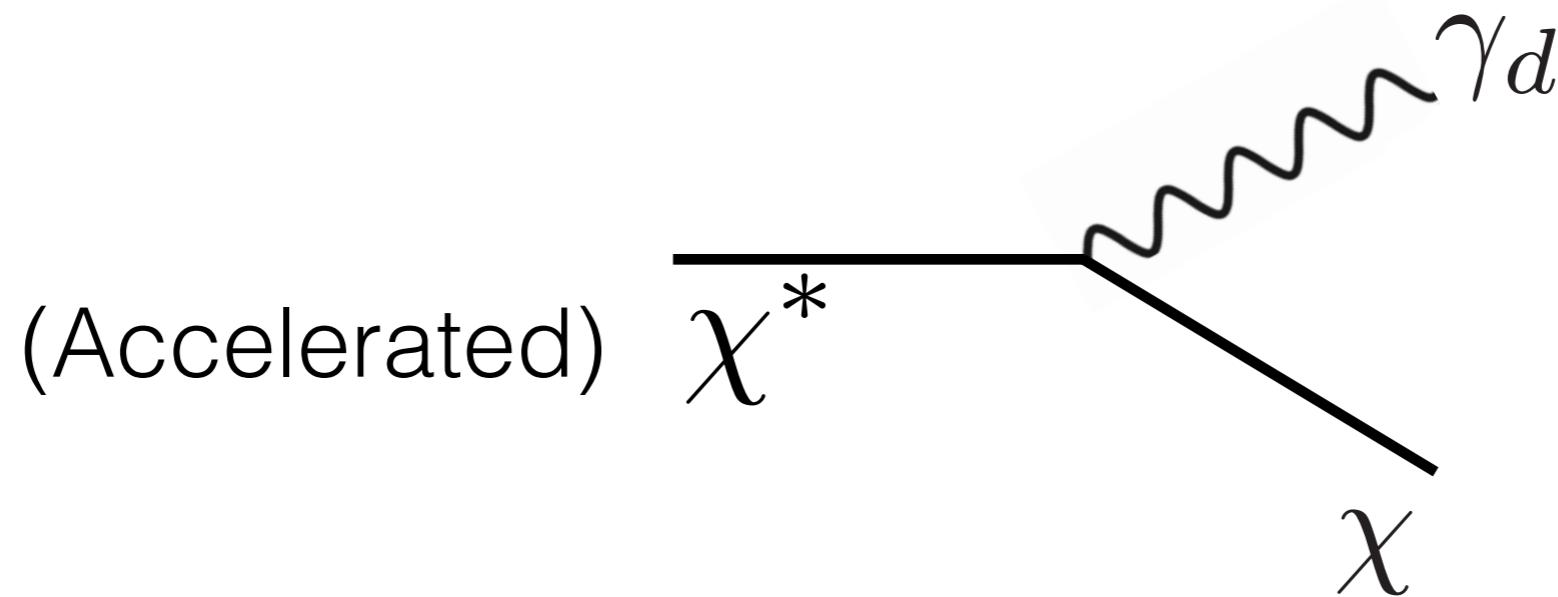


$$Q'_{\chi_L} = Q'_{\chi_R}$$

**No Dark-Higgs  
Vector-like fermion**

# How can we observe?

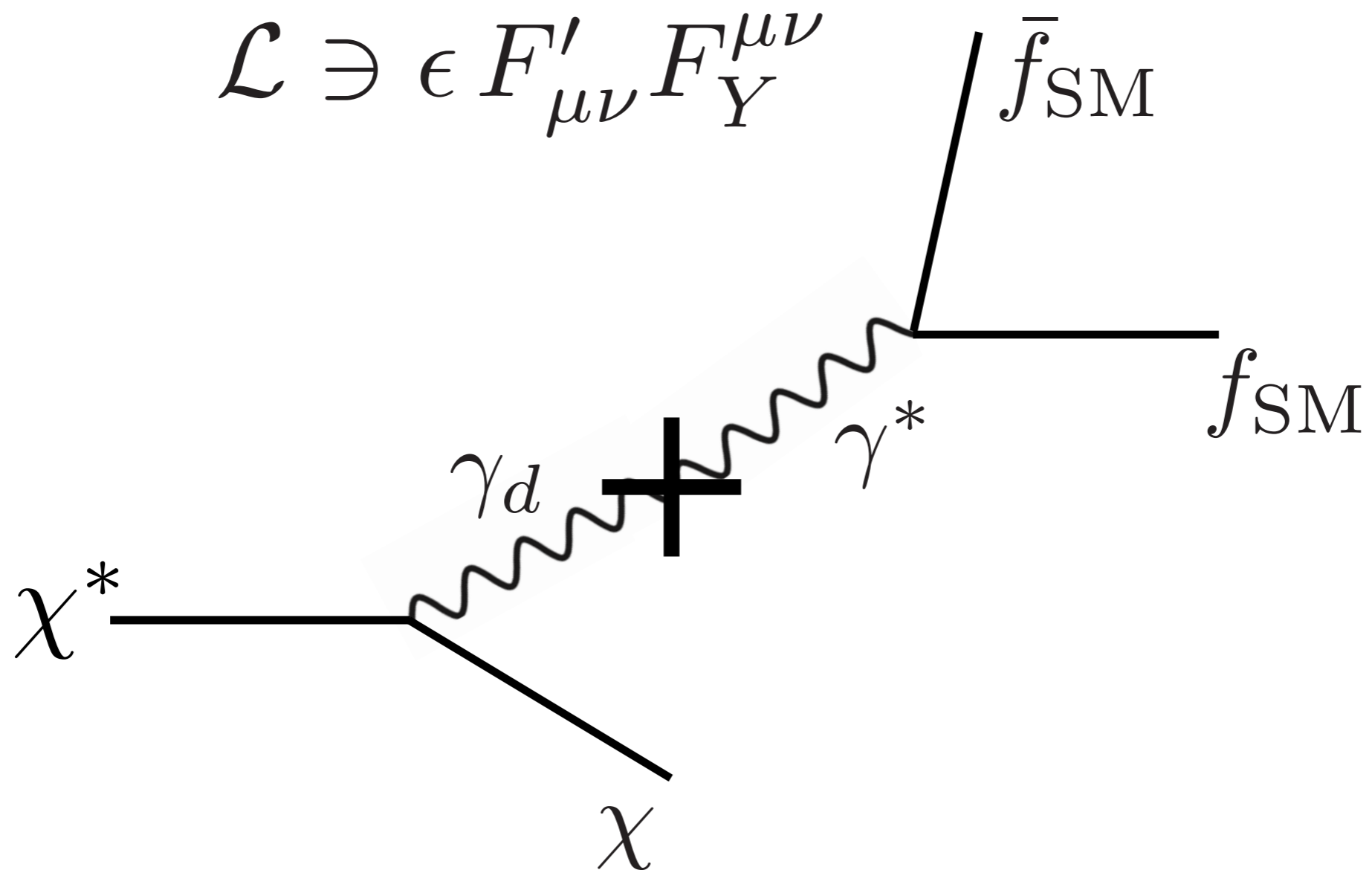
- **Dark Showering:** Accelerated "Dark Charged" particle radiates corresponding dark-gauge bosons





# How can we observe?

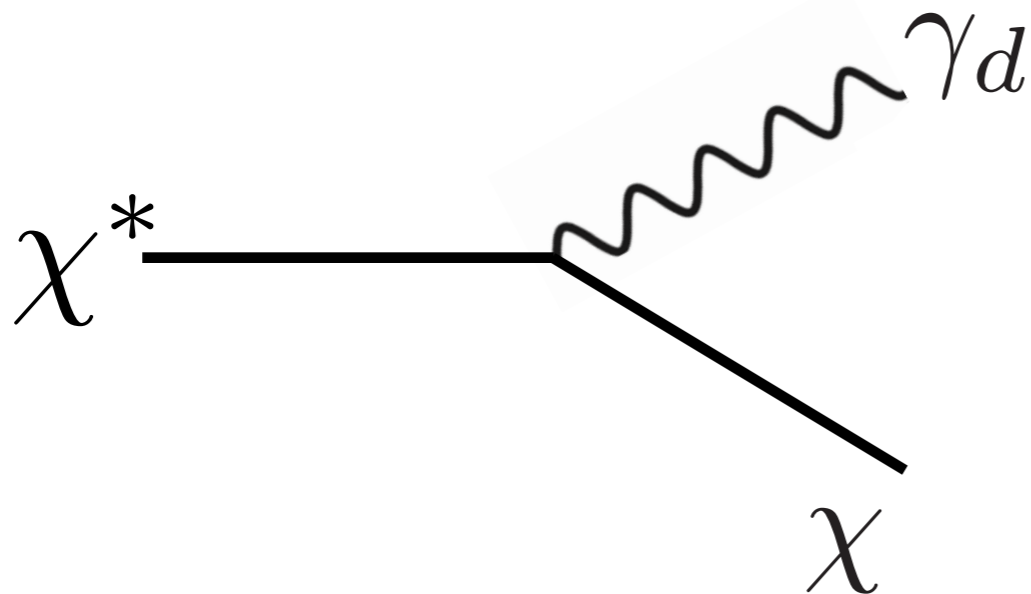
- dark-U(1) can mix with SM U(1)-hyper through a **Gauge-kinetic mixing** : Gauge-invariant term



# Showering process

Differential probability of a splitting process

$$\propto \frac{\alpha'}{2\pi} dx \frac{dt}{t} P_{\chi \rightarrow \chi \gamma_d}(x, t)$$



With  $x = \frac{E_{\chi, \text{out}}}{E_{\chi^*}}$

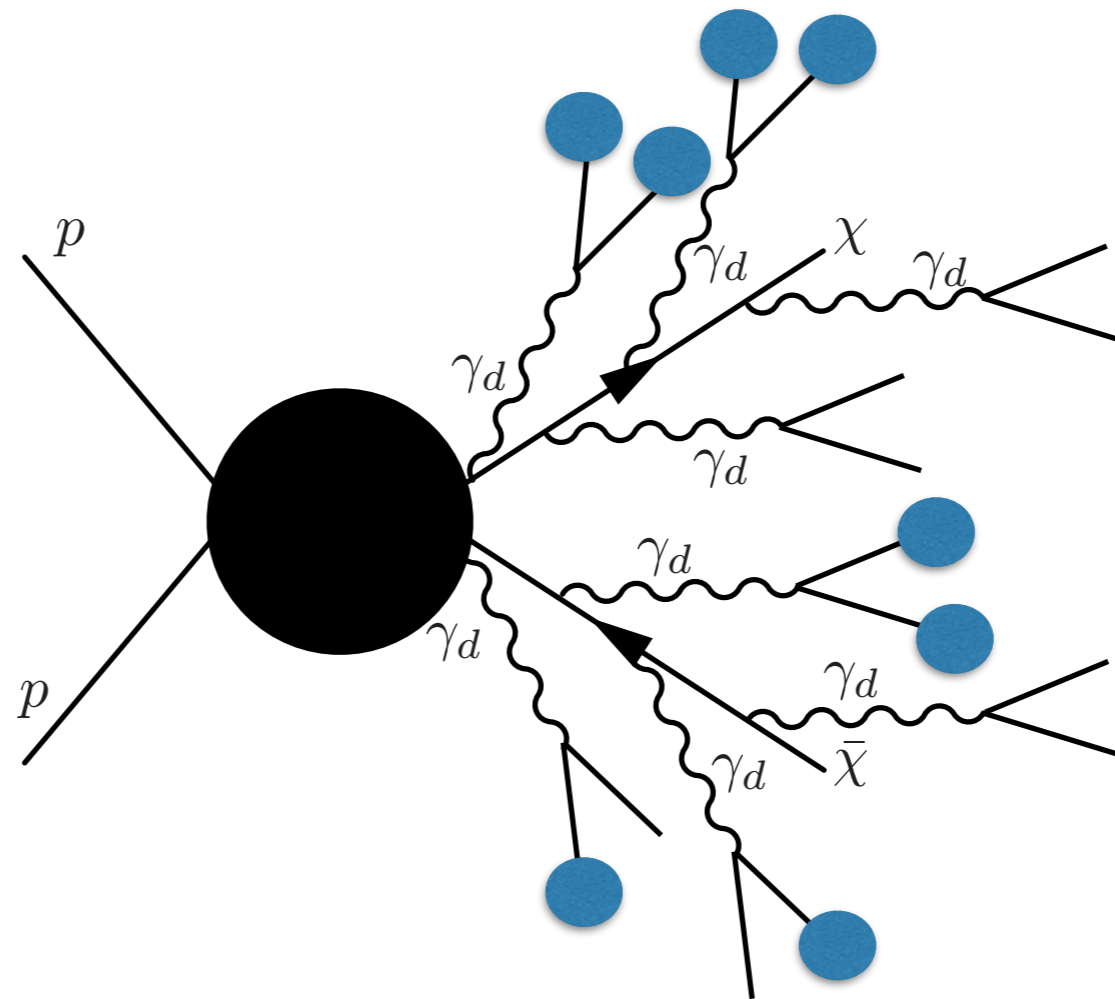
Splitting function

$$P_{\chi \rightarrow \chi \gamma_d}(x, t) \simeq Q_V'^2 \frac{1+x^2}{1-x}$$

- In a **chiral** case, the **longitudinal** component of a dark photon couples to a dark matter

$$P_{\chi \rightarrow \chi \gamma_d}(x, t) \simeq (Q_V'^2 + Q_A'^2) \frac{1+x^2}{1-x} + 2Q_A'^2 \frac{m_\chi^2}{m_{\gamma_d}^2}$$

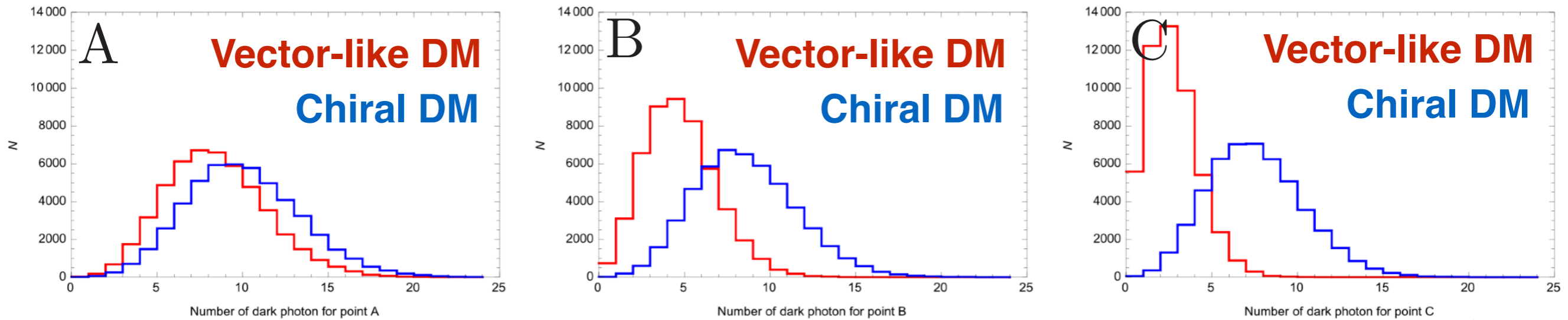
# Energetic DM @ Colliders



- **Radiations** from **Energetic** “dark charged” particles will acquire certain level of energy, enough to be “**tagged**”  
(detectable effect)

Benchmark Points (BP)	A	B	C
$\alpha'$	0.3	0.15	0.075
$m_\chi$ (GeV)	0.7	1.0	1.4
$m_{\gamma_d}$ (GeV)		0.4	

- Number of showered dark photons



weak coupling limit

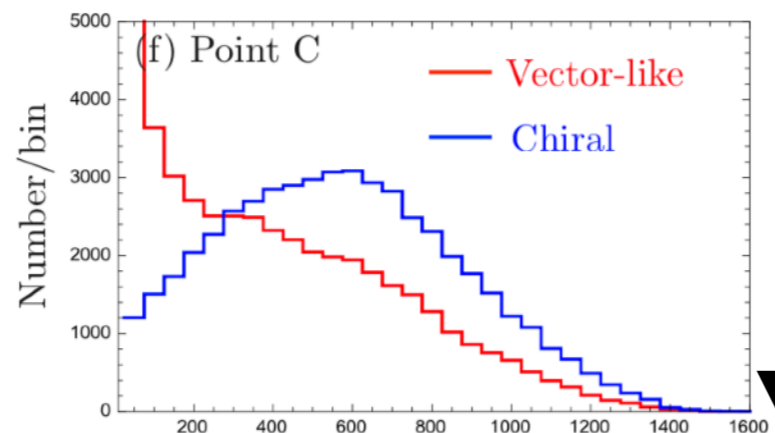
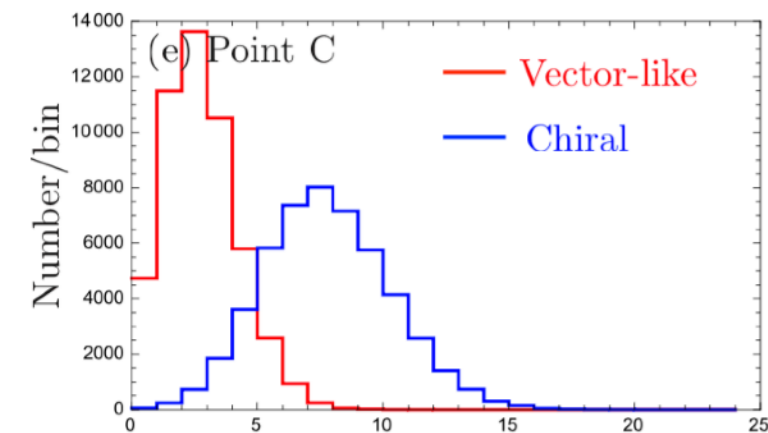
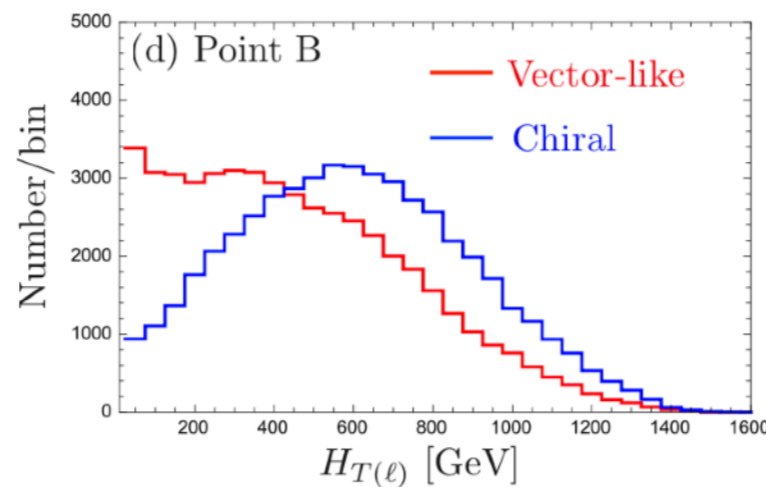
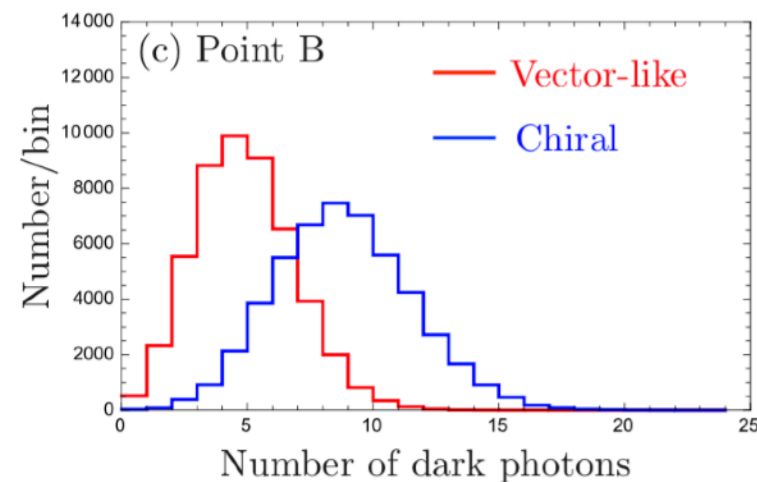
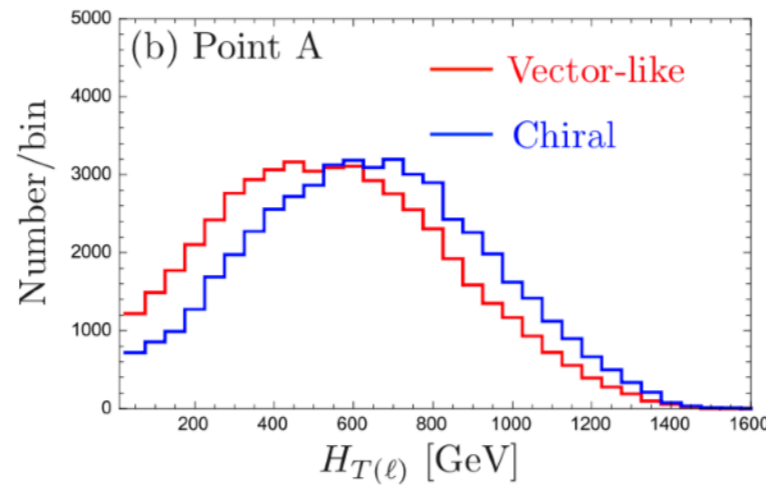
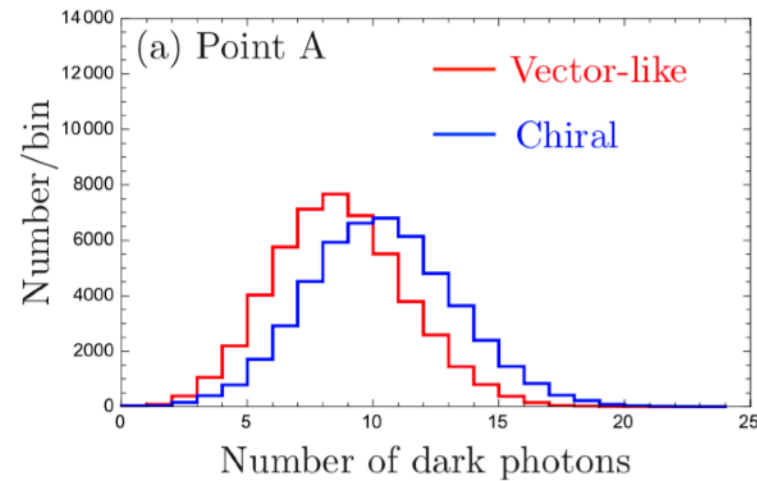
$$P_{\chi \rightarrow \chi \gamma_d}(x, t) \simeq (Q_V'^2 + Q_A'^2) \frac{1+x^2}{1-x} + 2Q_A'^2 \frac{m_\chi^2}{m_{\gamma_d}^2}$$

- In the weak gauge coupling limit,

$$\lim_{\alpha' \ll 1} \alpha' P_{\chi \rightarrow \chi \gamma_d} \simeq \alpha' \cdot 2Q_A'^2 \frac{m_\chi^2}{m_{\gamma_d}^2} \propto \frac{m_{\gamma_d}^2}{v_S^2} \cdot \frac{m_\chi^2}{m_{\gamma_d}^2} \sim y_\chi^2$$

# Quantify the difference

- We use the transverse energy deposits  $H_{T(\ell)} = \sum_{i=\mu^\pm, e^\pm} |p_{T_i}|$



- In a splitting function

$$P_{\chi \rightarrow \chi \gamma_d}(x, t) \simeq Q_V'^2 \frac{1+x^2}{1-x}$$

$x \simeq 1$  : Soft radiation

- In a chiral case, additional term:

$$P_{\chi \rightarrow \chi \gamma_d}(x, t) \ni 2Q_A'^2 \frac{m_\chi^2}{m_{\gamma_d}^2}$$

: **No singularity** at  $x \sim 1$

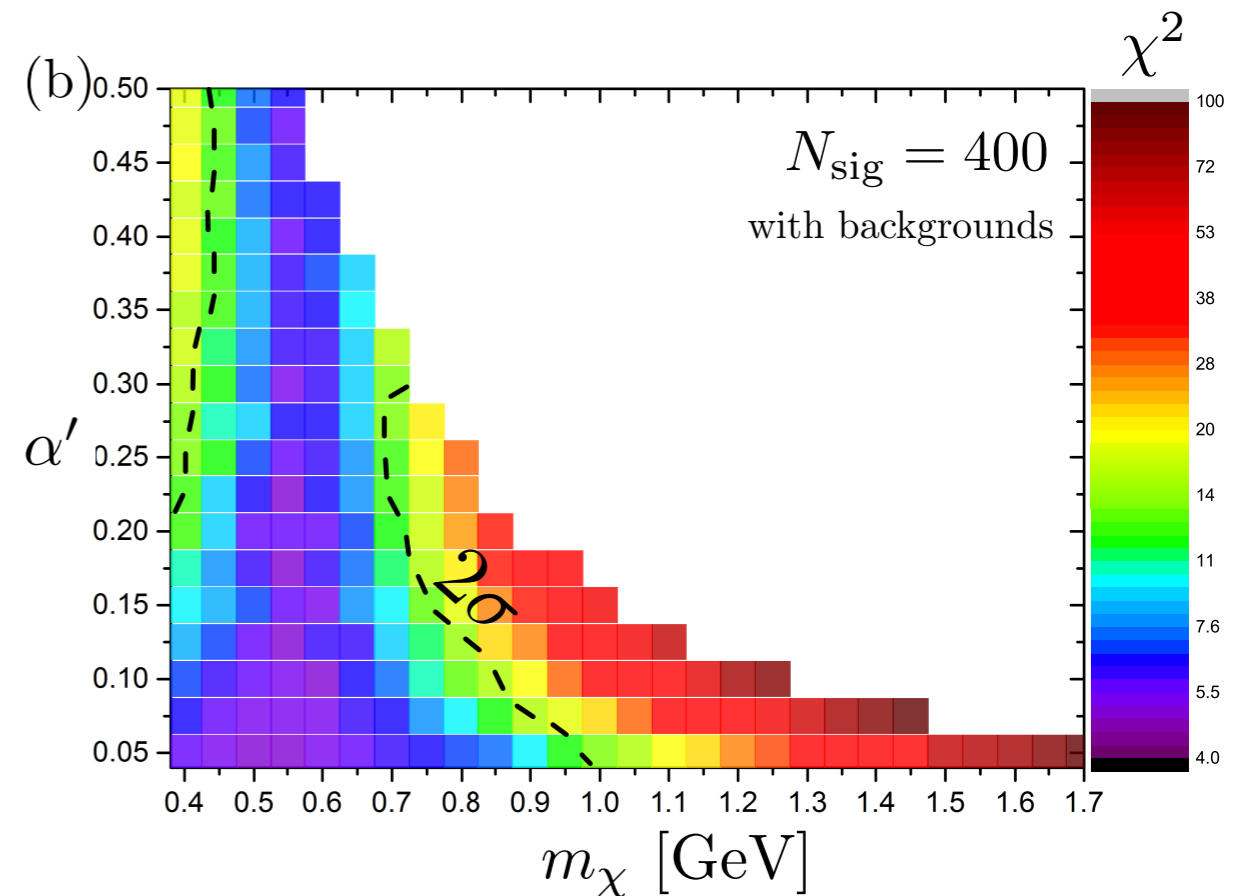
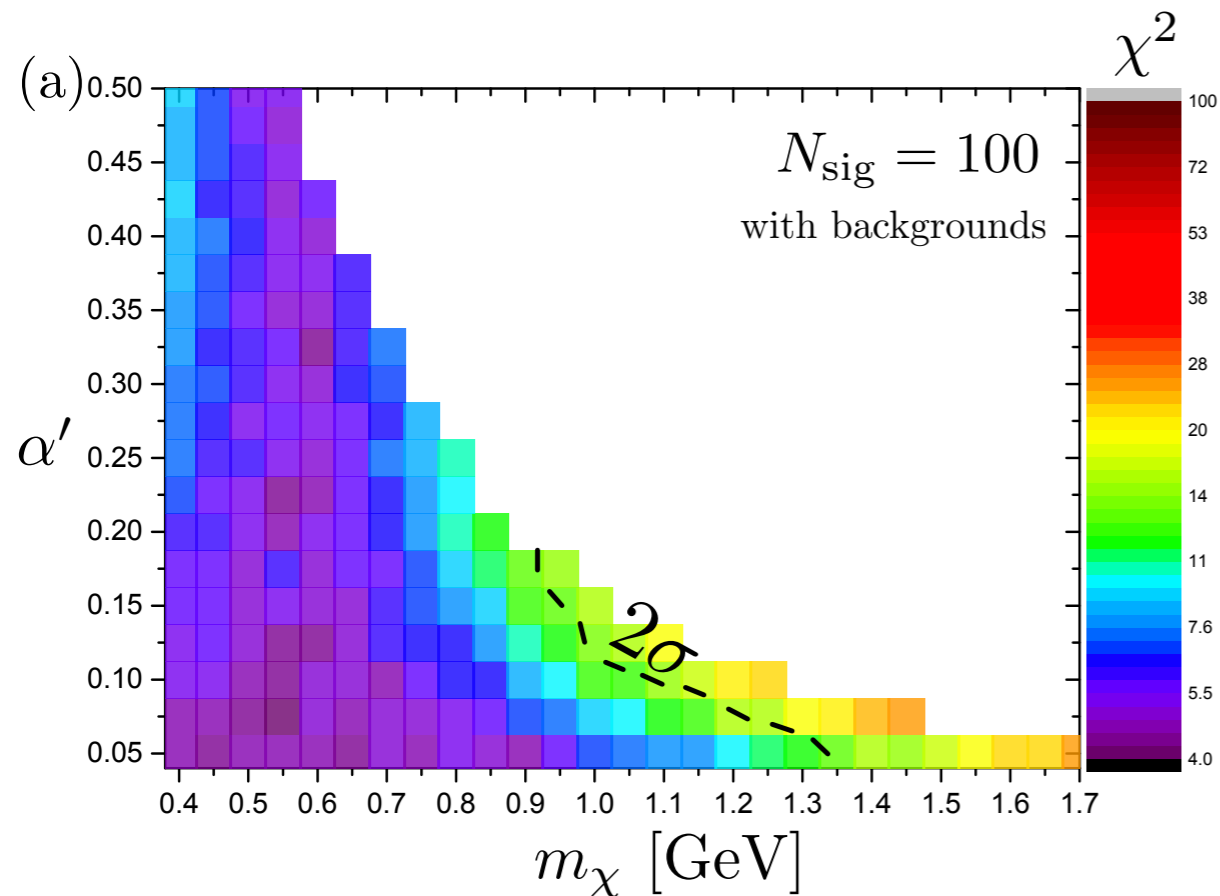
weak coupling limit

Number of dark photons

$H_{T(\ell)}$  [GeV]

# Checking chirality@ Collider

- After triggering signal events by tagging a collimated muon-jet (a jet only with muons)



with 100 , 400 signal events after cuts to reduce BKG

Number of BKG  $\sim O(1)$

# $SU(N)$ dark sector



**Where is from the stability of Dark matter ?**

**How does Dark matter become MASSIVE ?**

**= Dark "Baryon"**

# Dark Matter with $SU(N)$

- A new scale of confinement will be introduced  $\Lambda$
- "Composite" particle (baryon) under non-abelian gauge group
  - "Composite" Dark Matter under dark non-abelian gauge group



# Dark Matter with SU(2)

Timothy Cohen et.al 2015

- Dark sector in SU(2) with two fermionic quark flavors

$$\chi_i = \chi_{1,2}$$

- There are two accidental symmetries:

- A dark-isospin number  $U(1)_{1-2}$

- A dark-baryon number  $U(1)_{1+2}$

- Dark Matter is **Dark Baryon with two dark-quarks**

$$(\chi_1\chi_2, \chi_1^\dagger\chi_2^\dagger)$$

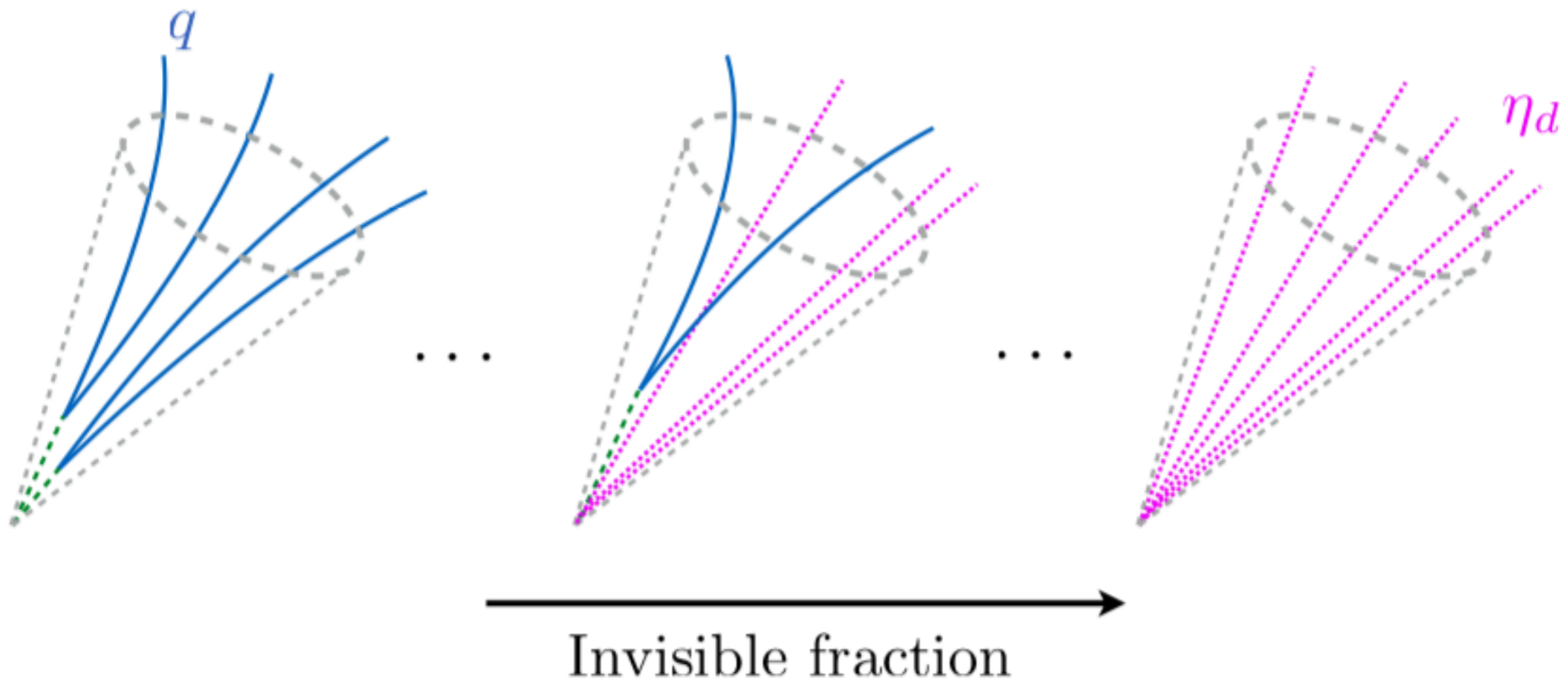
- Dark mesons are

- Stable mesons  $(\chi_1^\dagger\chi_2, \chi_1\chi_2^\dagger)$ , charged under  $U(1)_{1-2}$

- Unstable mesons  $(\chi_1^\dagger\chi_1, \chi_2^\dagger\chi_2)$ , neutral under  $U(1)_{1-2}$

# Dark Matter with $SU(2)$

Timothy Cohen et.al 2015

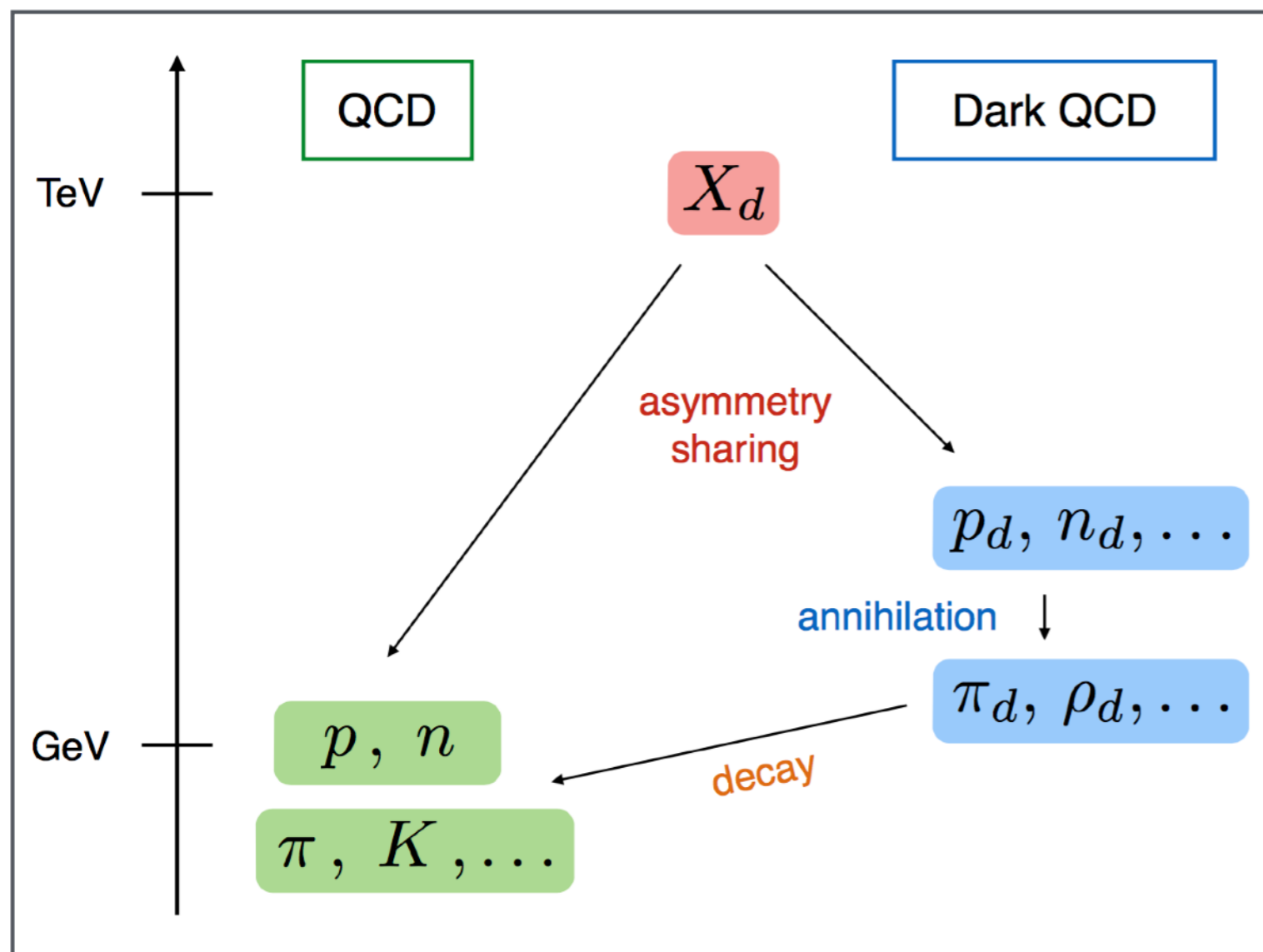


$$r_{\text{inv}} \equiv \left\langle \frac{\# \text{ of stable hadrons}}{\# \text{ of hadrons}} \right\rangle$$

# Dark Matter with SU(3)

- Hidden Valley type extension

Andreas Weiler et.al. 2015

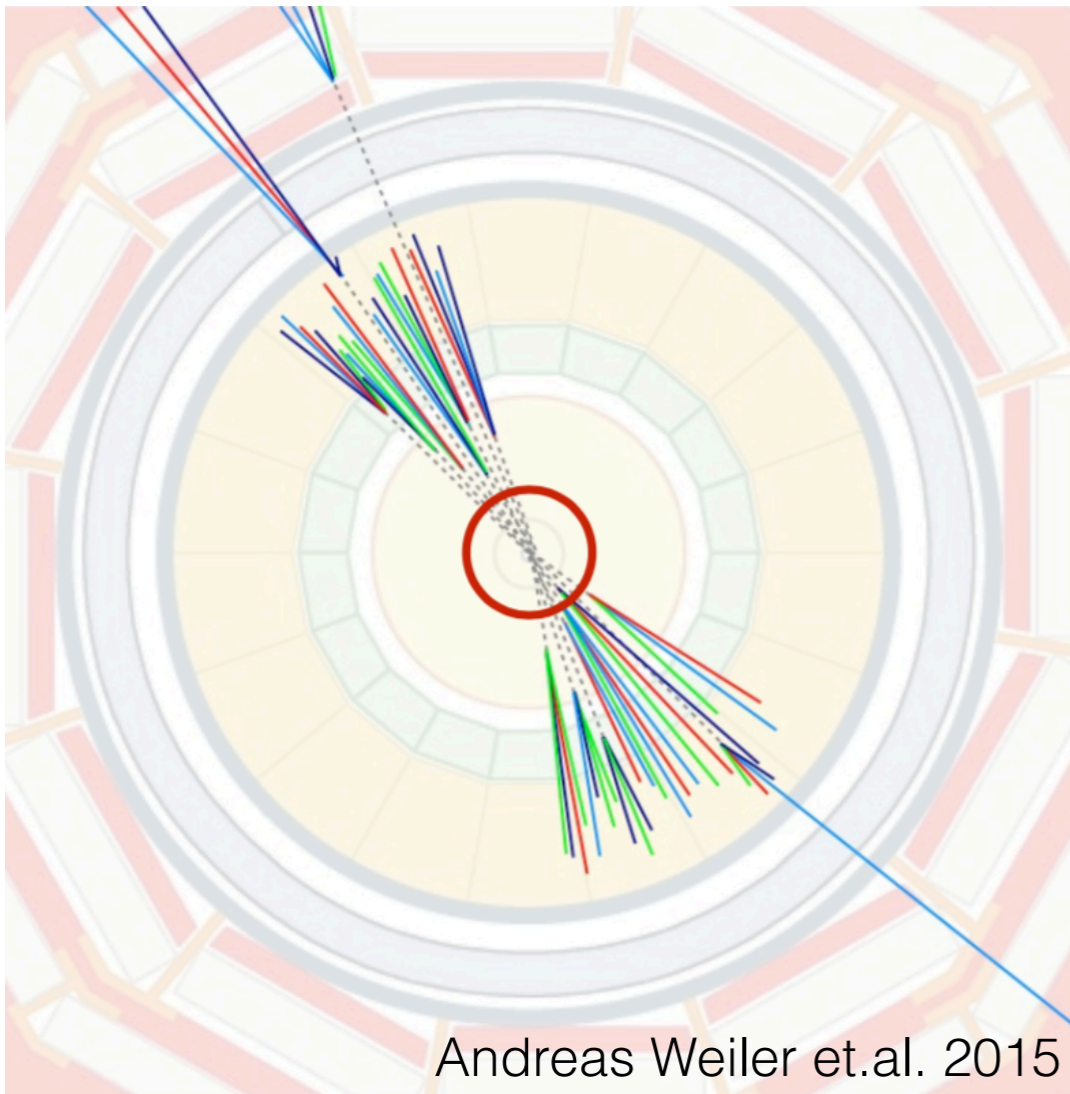


- Dark Matter is **Dark Baryon with three dark-quarks**
- Dark mesons can be easily produced

Field	$SU(3) \times SU(2) \times U(1)$	$SU(3)_{\text{dark}}$	Mass	Spin
$Q_d$	$(1, 1, 0)$	$(3)$	$m_d \mathcal{O}(\text{GeV})$	Dirac Fermion
$X_d$	$(3, 1, \frac{1}{3})$	$(3)$	$M_{X_d} \mathcal{O}(\text{TeV})$	Complex Scalar

# Dark Matter with SU(3)

Andreas Weiler et.al. 2015

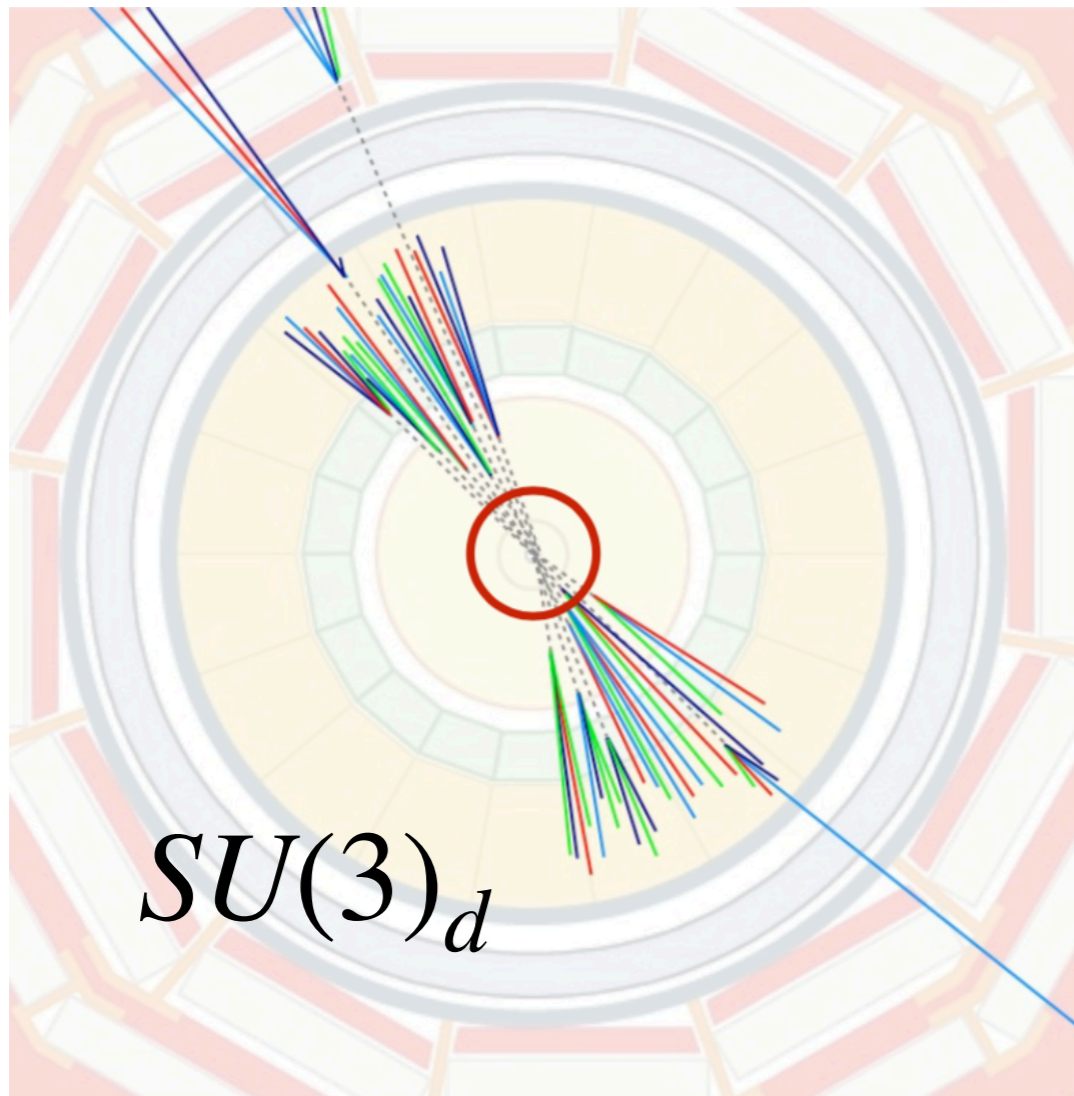


- Dark mesons can be easily produced and they will have a **finite life-time : Displaced Vertex**

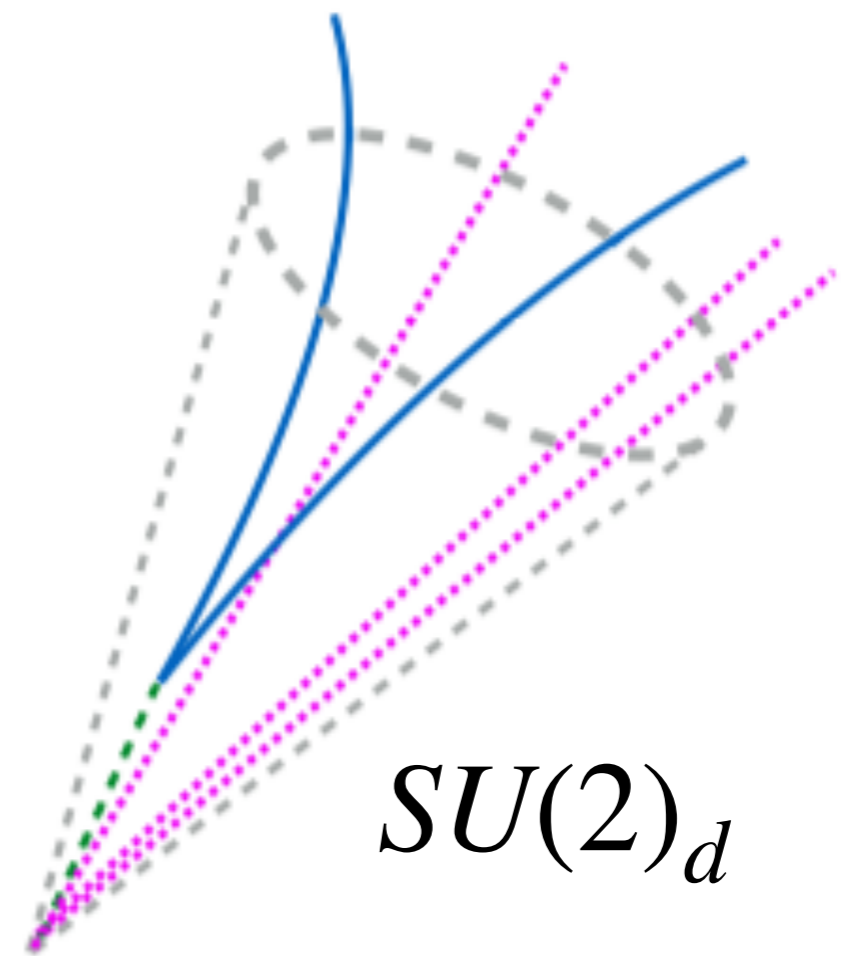
$$\Gamma(\pi_d \rightarrow \bar{d}d) = \frac{\kappa^4 N_c f_{\pi_d}^2 m_{\text{down}}^2}{32\pi M_{X_d}^4} m_{\pi_d}$$

$$c\tau_0 = \frac{c\hbar}{\Gamma} \approx 80 \text{ mm} \times \frac{1}{\kappa^4} \times \left(\frac{2 \text{ GeV}}{f_{\pi_d}}\right)^2 \left(\frac{100 \text{ MeV}}{m_{\text{down}}}\right)^2 \left(\frac{2 \text{ GeV}}{m_{\pi_d}}\right) \left(\frac{M_{X_d}}{1 \text{ TeV}}\right)^4$$

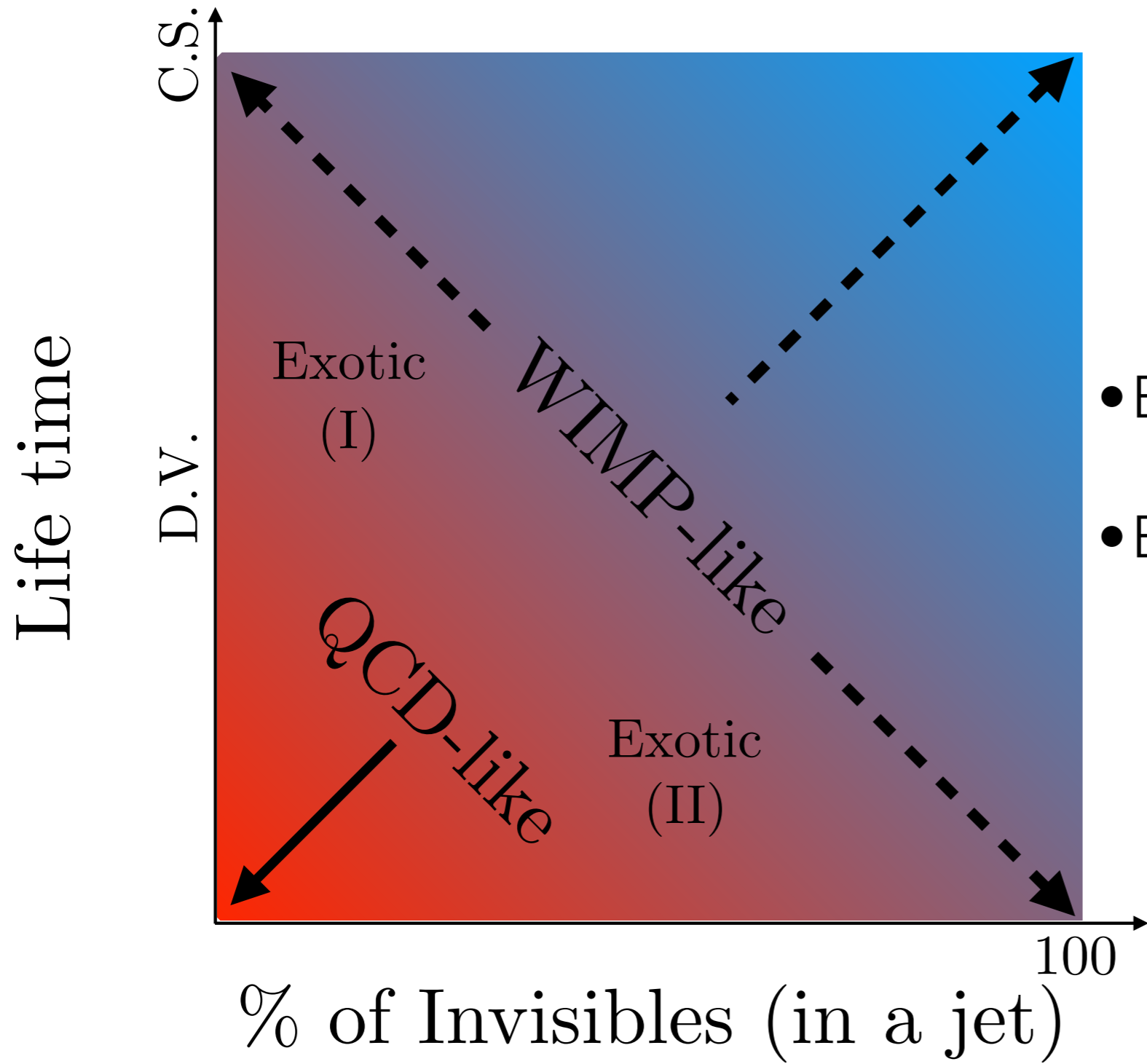
# Conventional-"exotic" searches for $SU(N)$ charged DM?



- Exotic (I) : Emerging jet



- Exotic (II) : Semi-invisible jet



- Exotic (I) : Emerging jet
- Exotic (II) : Semin-invisible jet

# Minimal setup

- Consider a minimal set up for Hadron Collider
  - SM Strong Sector - Mediator - Hidden Sector

to produce and detect signatures at hadron colliders

$$\mathcal{L}_d = \bar{q}' (i \not{D} - m_{q'}) q' - \frac{1}{4} G'^{\mu\nu} G'_{\mu\nu} \quad \vdots SU(N_d)$$

- A mediator which couples SM part and Dark part

$$\mathcal{L}_{med} = (D^\mu X)^\dagger (D_\mu X) - M_X^2 X^\dagger X + \kappa X \bar{q}' q + h.c.$$

**OR**

$$\mathcal{L}_{med} = -\frac{1}{4} Z'^{\mu\nu} Z'_{\mu\nu} - \frac{1}{2} M_{Z'}^2 Z'^\mu Z'_\mu + Z'_\mu (\bar{q}' \gamma^\mu q' + \bar{q} \gamma^\mu q)$$

- Dark pion: spin-0 pseudo-scalar. Due to chiral flipping suppression, dark pion tends to decay a heavy SM quark pair.

$$\Gamma(\pi_d \rightarrow q\bar{q}) = \frac{3\kappa^4 f_{\pi_d}^2 m_q^2}{32\pi M_X^4} m_{\pi_d}$$

or if there is U(1), dark pion would like to decay into two dark photons promptly.

- Dark rho meson: spin-1 vector meson
- Dark baryon: In SU(3), population ratio of baryons over mesons is O(10) %.
- Dark glue ball: In the case of  $m_{q_d} \gg \Lambda_d$ , the lightest dark hadron would be a "glue-ball"



	$N_d$	$n_f$	$\Lambda_d$ (GeV)	$m_{\pi_d}$ (GeV)	$m_{\rho_d}$ (GeV)	$\pi_d$ Decay Mode	$\rho_d$ Decay Mode
<i>A</i>	3	2	15	10	50	$\pi_d \rightarrow c\bar{c}$	$\rho_d \rightarrow \pi_d\pi_d$
<i>B</i>	3	6	2	2	4.67	$\pi_d \rightarrow s\bar{s}$	$\rho_d \rightarrow \pi_d\pi_d$
<i>C</i>	3	2	15	10	50	$\pi_d \rightarrow \gamma'\gamma'$ with $m_{\gamma'} = 4.0$ GeV	$\rho_d \rightarrow \pi_d\pi_d$
<i>D</i>	3	6	2	2	4.67	$\pi_d \rightarrow \gamma'\gamma'$ with $m_{\gamma'} = 0.7$ GeV	$\rho_d \rightarrow \pi_d\pi_d$

A, C : Large Lambda QCD

B, D : Small Lambda QCD

A, B : meson decays into HF

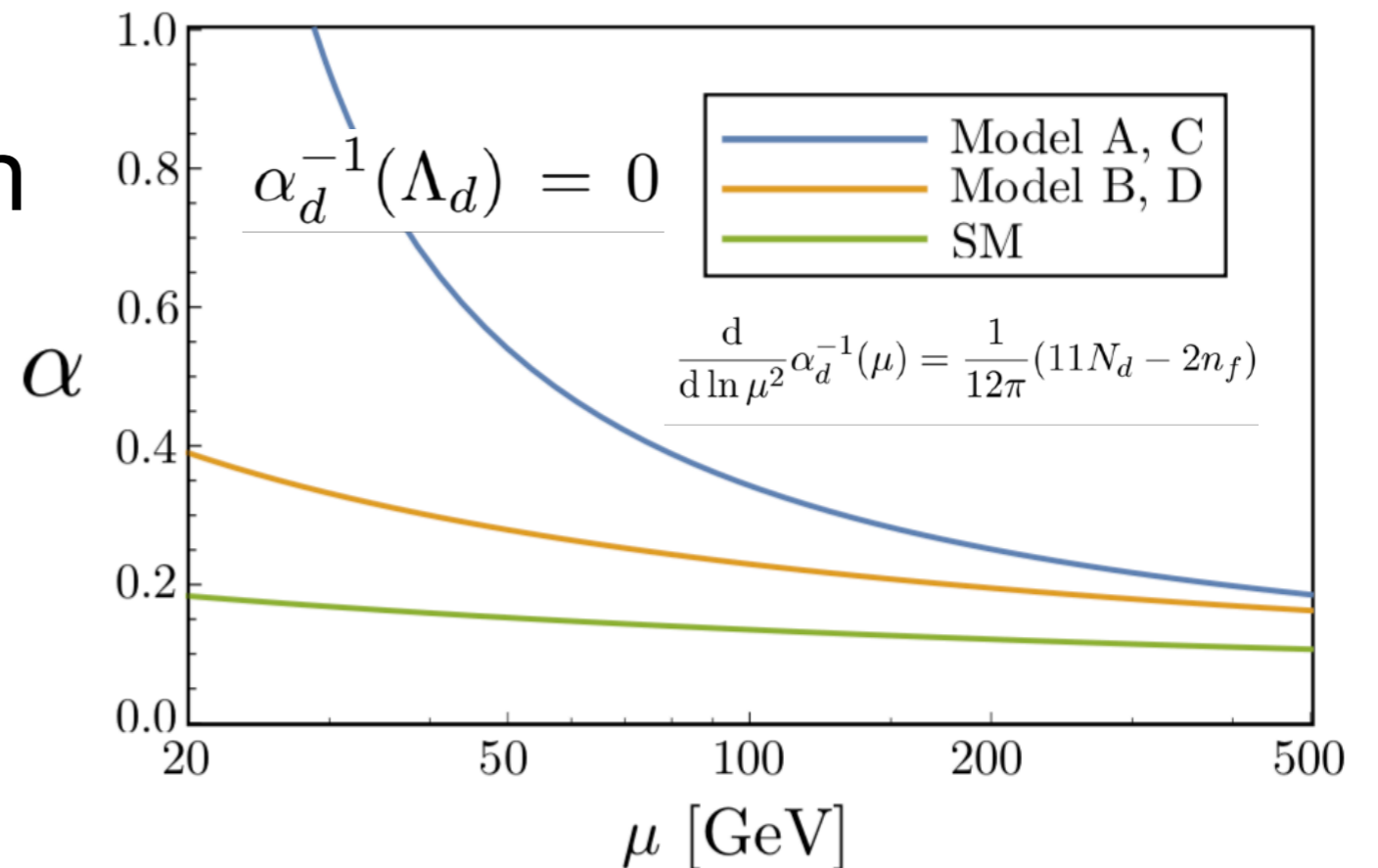
C, D : additional meson decay

Jet evolution depends on

1. Color factor


2. Coupling


Jet components depends on  
- decay mode.



# Color factor

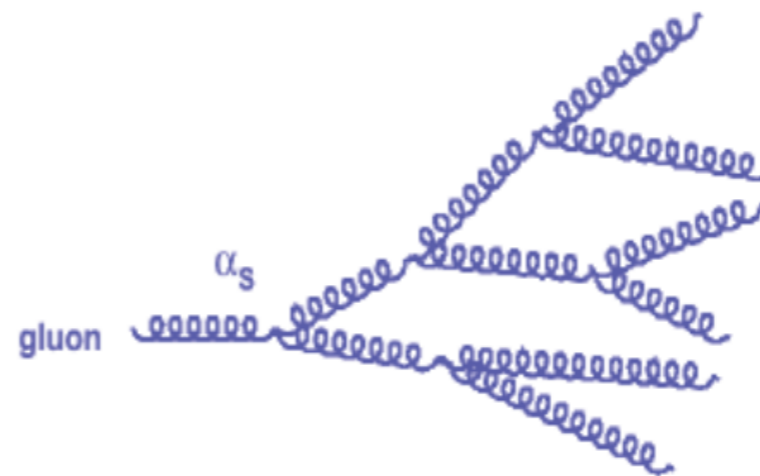
- What is the most significant difference between quark and gluon ?

$$\left| \text{q} \begin{array}{c} \text{g} \\ \text{q} \end{array} \right|^2 \sim C_F = 4/3$$


$$\left| \text{g} \begin{array}{c} \text{g} \\ \text{g} \end{array} \right|^2 \sim C_A = 3$$




quark jets



gluon jets

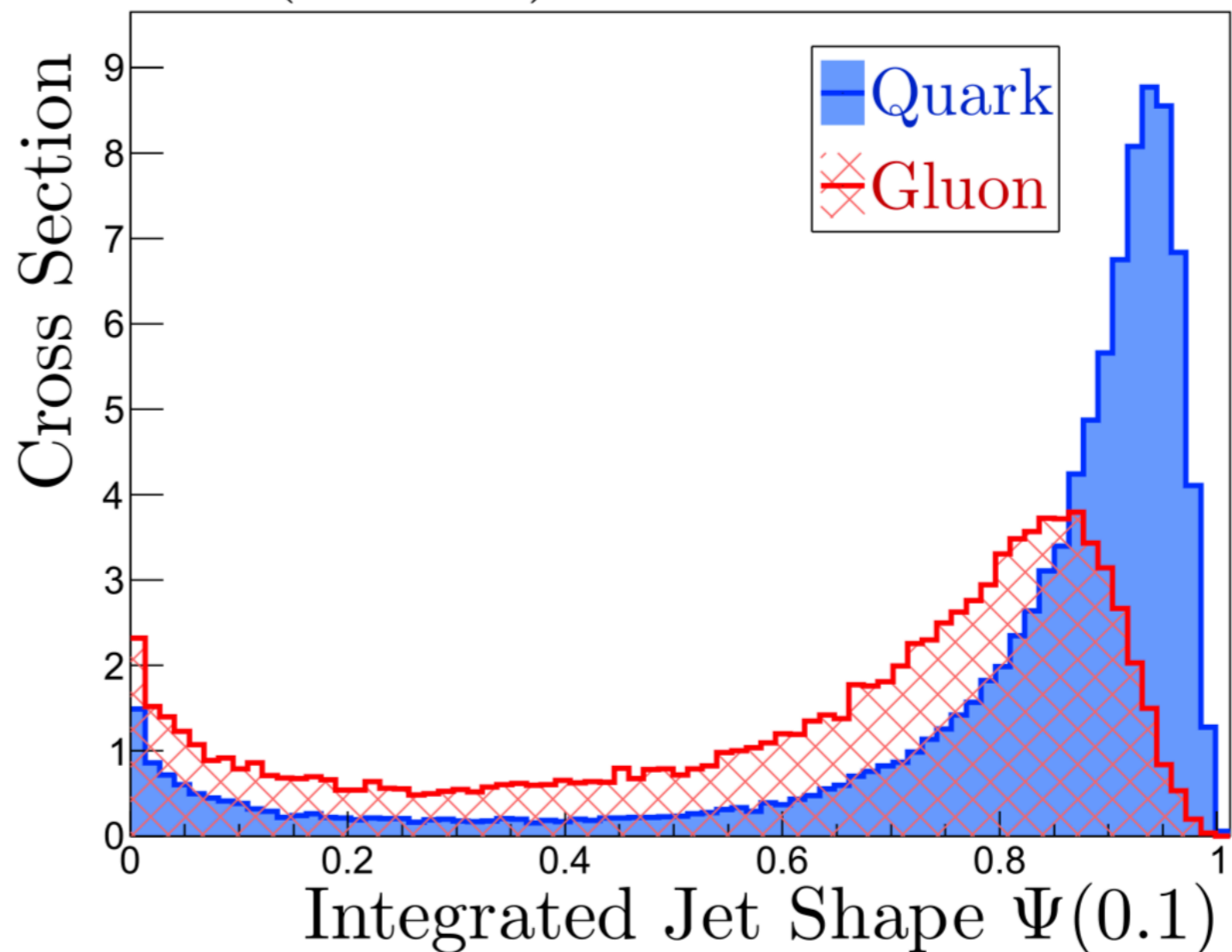
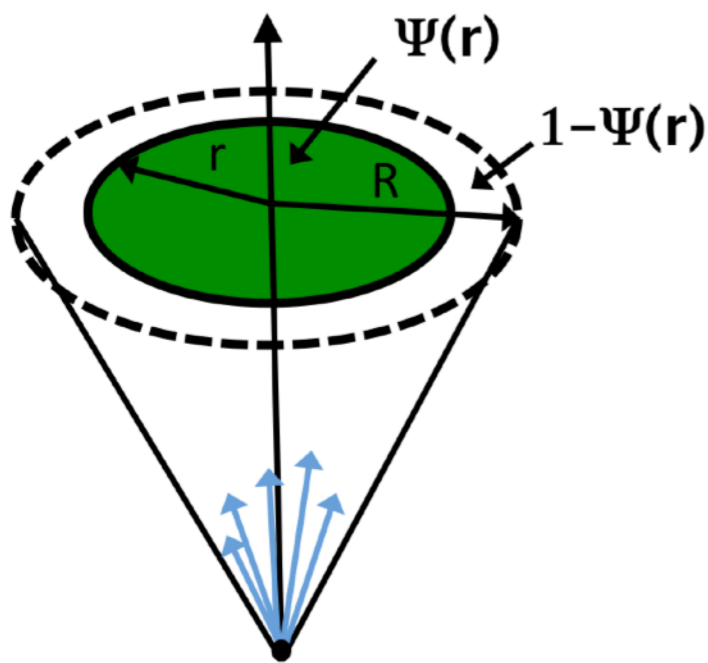
$$F_{q \rightarrow g}(z, \theta) = \frac{4}{N_c} \frac{\alpha_s}{\pi} \frac{1 + (1 - z)^2}{z} \frac{1}{\sin^2 \theta}$$

$$F_{g \rightarrow q}(z, \theta) = \frac{4}{N_c^2 - 1} \frac{\alpha_s}{\pi} \frac{z^2 + (1 - z)^2}{\sin^2 \theta}$$

# pencil (q) v.s. wide (g)

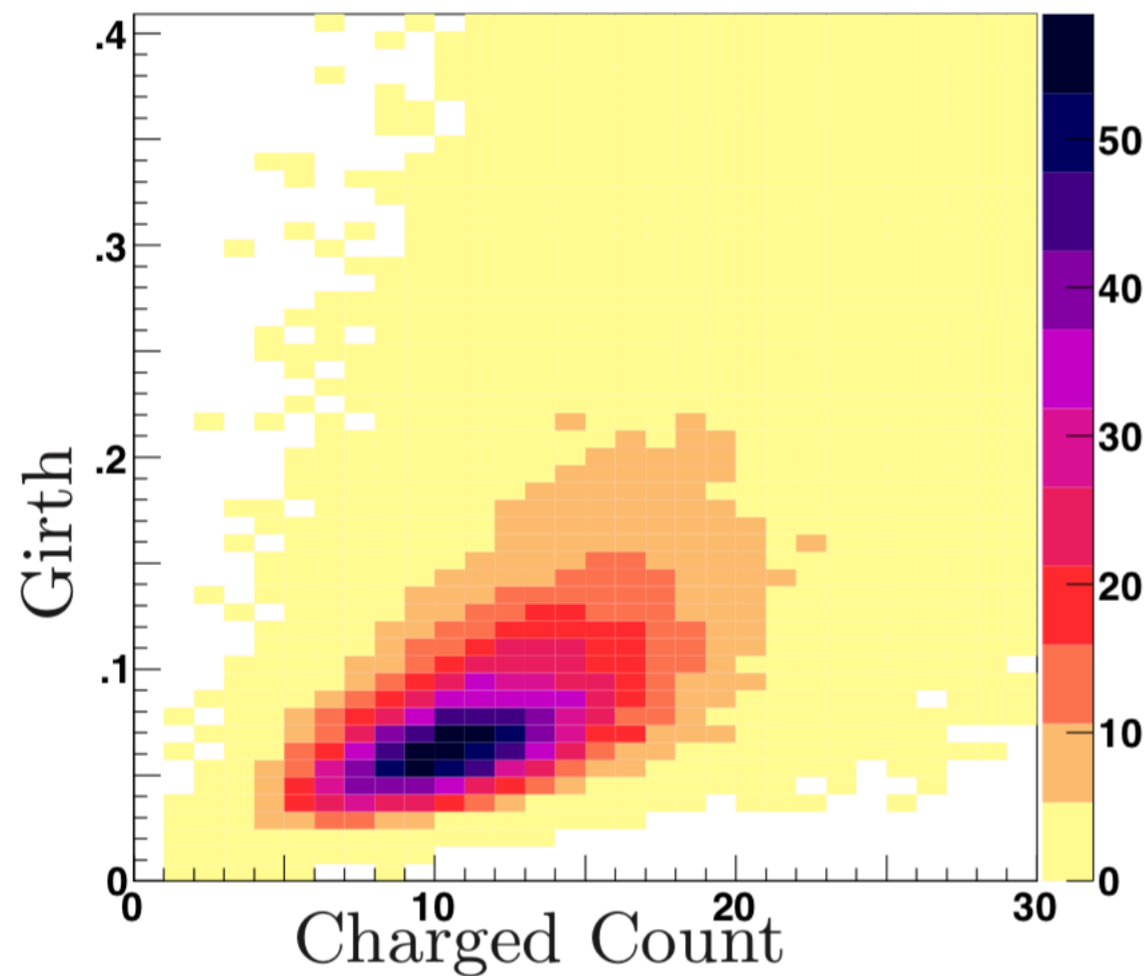
$$\Psi(r) = \frac{1}{N} \sum_J \sum_{i \in J} \frac{p_T(0 < r_i < r)}{p_{T,J}}$$

$\Psi(r = 0.1)$  for 200 GeV Jets

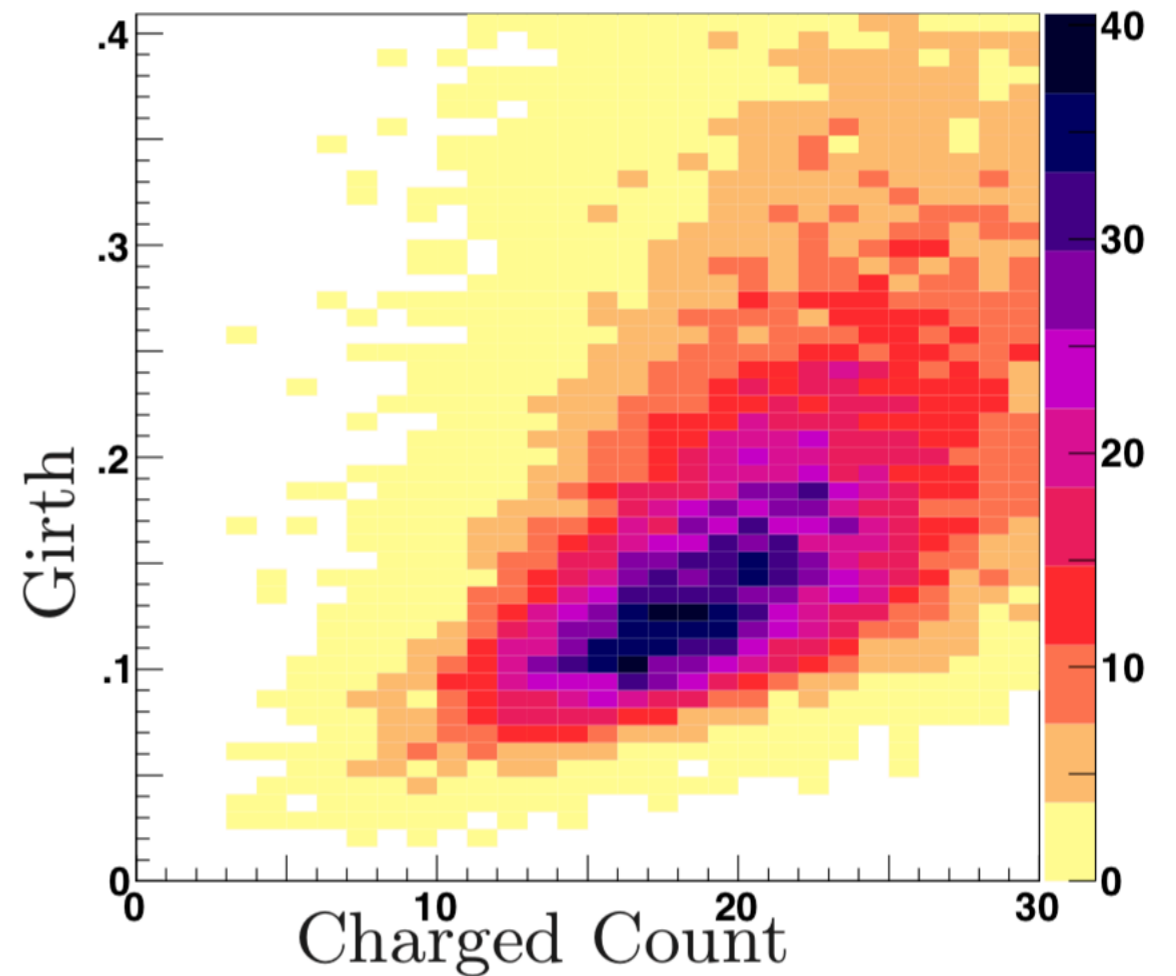


# Thin & Simple (q) v.s. Fat & Busy (g)

Quark



Gluon

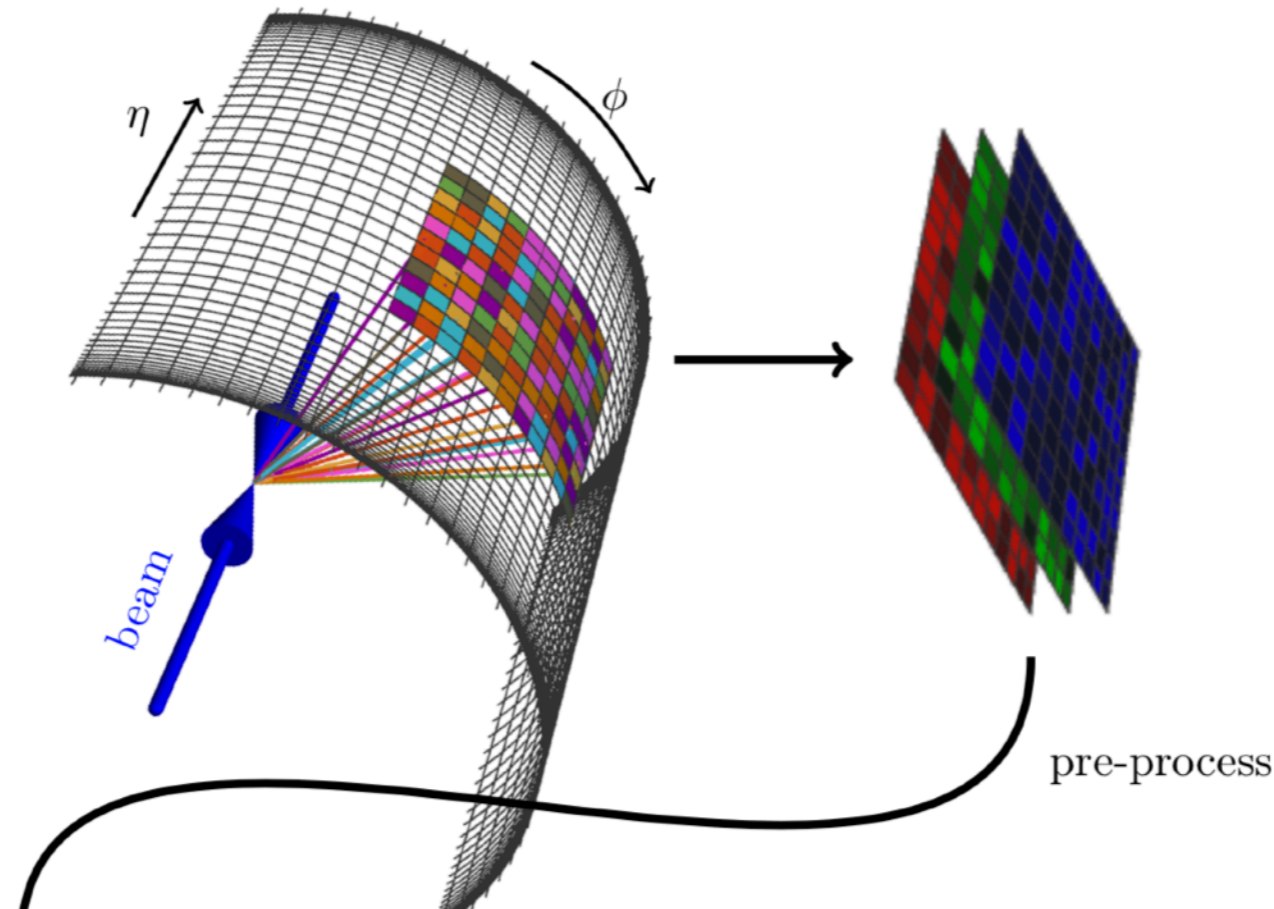


Matthew D. Schwartz et. al 2013

$$\text{girth} = \sum_{i \in J} \frac{p_{T_i}}{P_{T_J}} |r_i|$$

# Jet shape can be interpreted by image analysis

by Schwartz et.al. 2017



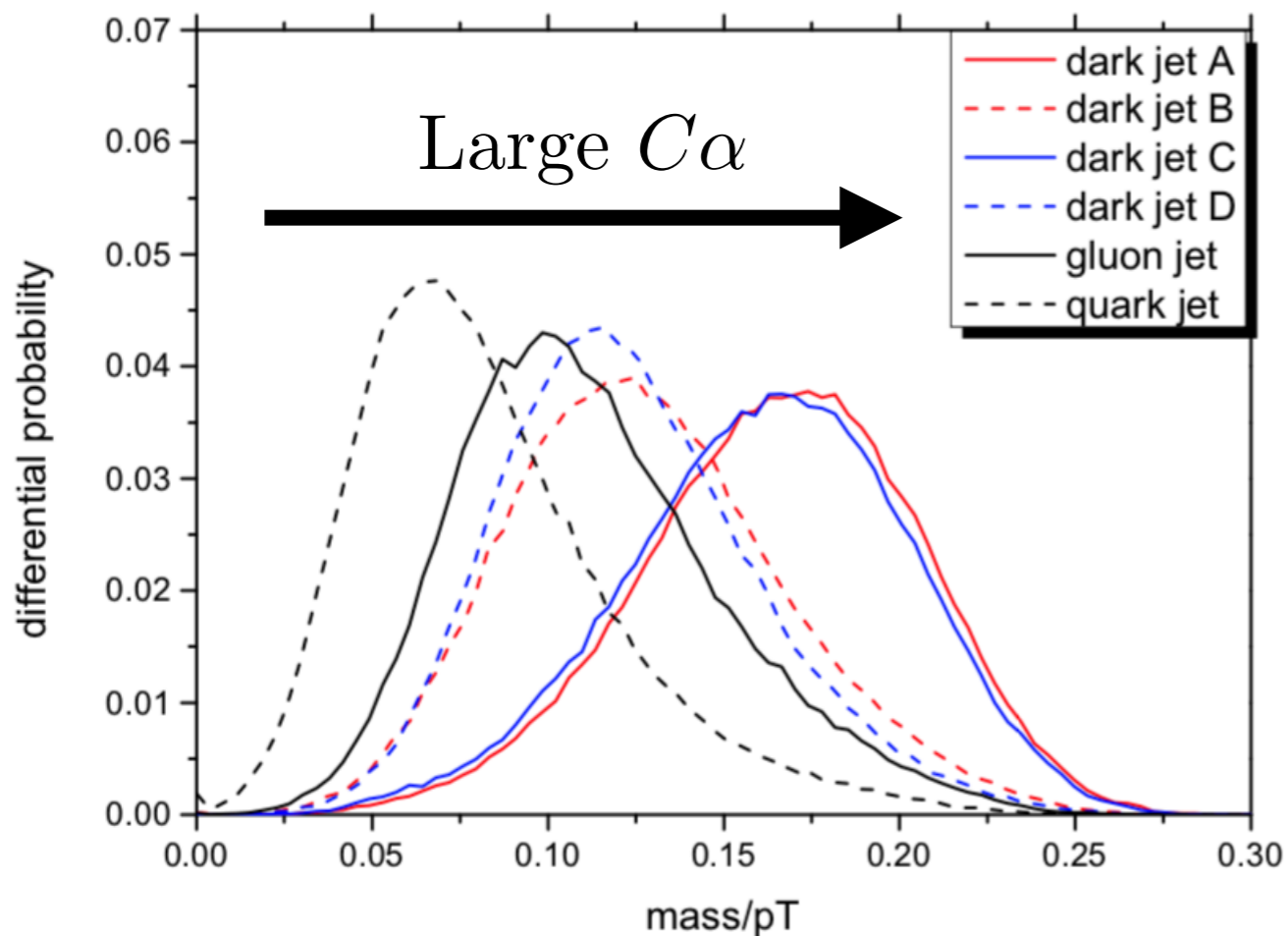
red = transverse momenta of charged particles

green = the transverse momenta of neutral particles

blue = charged particle multiplicity

**What's the case of jet  
evolved from Dark QCD ?**

# eg: jet mass



Large  $C\alpha$  pushes a distribution to the right

$$\frac{1}{\sigma_0} \frac{d\sigma}{d(p^2/Q^2)} \approx \frac{C\alpha}{\pi} \frac{Q^2}{p^2} \ln \frac{Q^2}{p^2} \exp \left\{ -\frac{C\alpha}{2\pi} \left( \ln \frac{Q^2}{p^2} \right)^2 \right\}$$

Gluon:  $C=3$

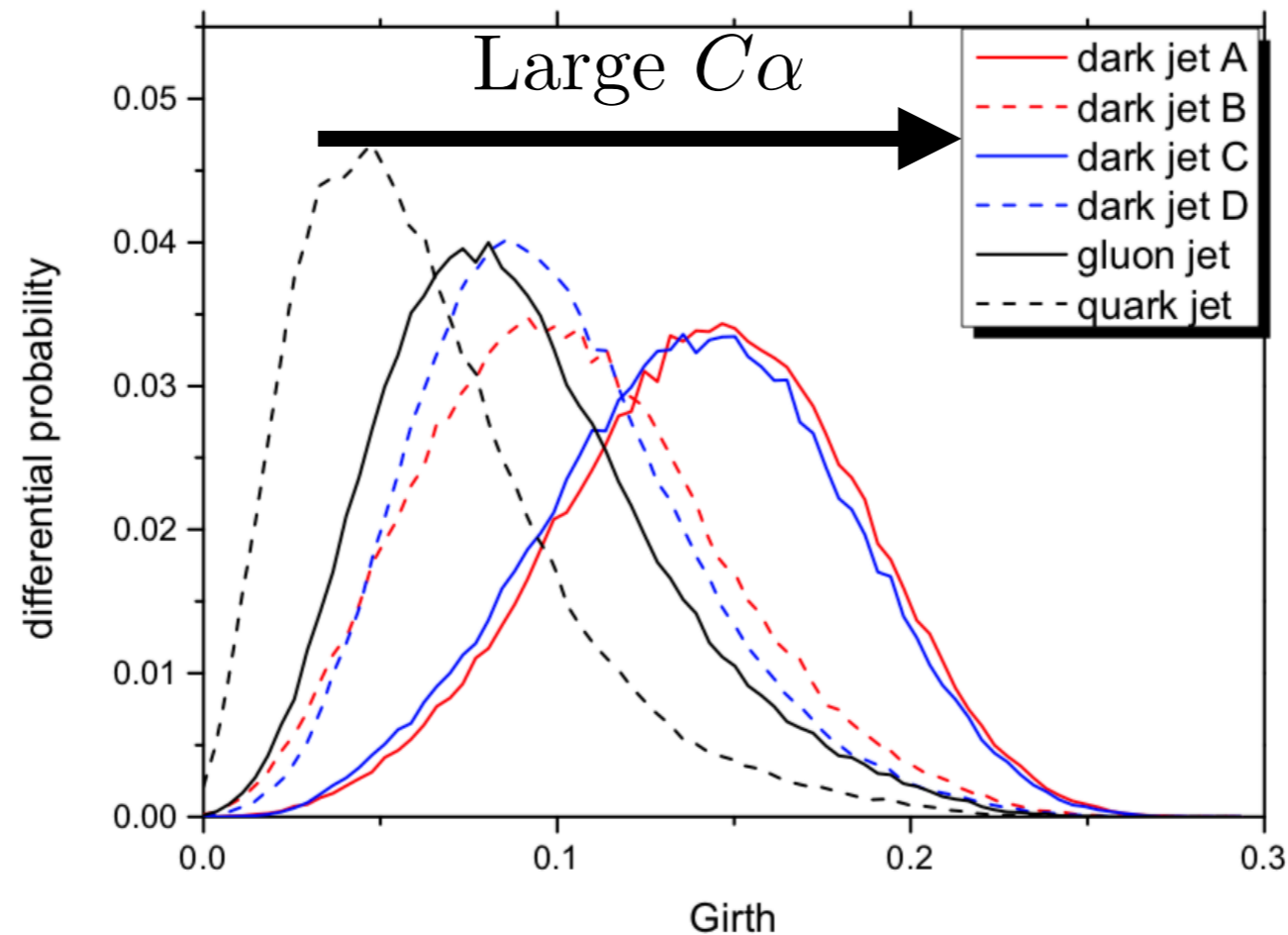
Quark:  $C=4/3$

: Coupling strengths of A and C are larger than the case of B and D

# eg: Girth

- A radial "spread", called girth is a good discriminator

$$\text{girth} = \sum_{i \in J} \frac{p_{T_i}}{P_{T_J}} |r_i|$$





# eg: Energy correlation

- Correlations among constitute particles would be interesting

$$C_1^{(\beta)} = \sum_{i < j \in J} z_i z_j (R_{ij})^\beta$$

$$\frac{1}{\sigma} \frac{d\sigma}{dC_1^{(\beta)}} = \frac{2\alpha C}{\pi\beta C_1^{(\beta)}} L(C_1^{(\beta)}) \exp\left(-\int_{C_1^{(\beta)}}^{R_0^\beta} d\tilde{C} \frac{2\alpha C}{\pi\beta\tilde{C}} L(\tilde{C})\right)$$

- As the mass of dark mesons  $>$  SM QCD  $\Lambda$ , dark mesons contributes large E-correlation for  $\beta > 0$

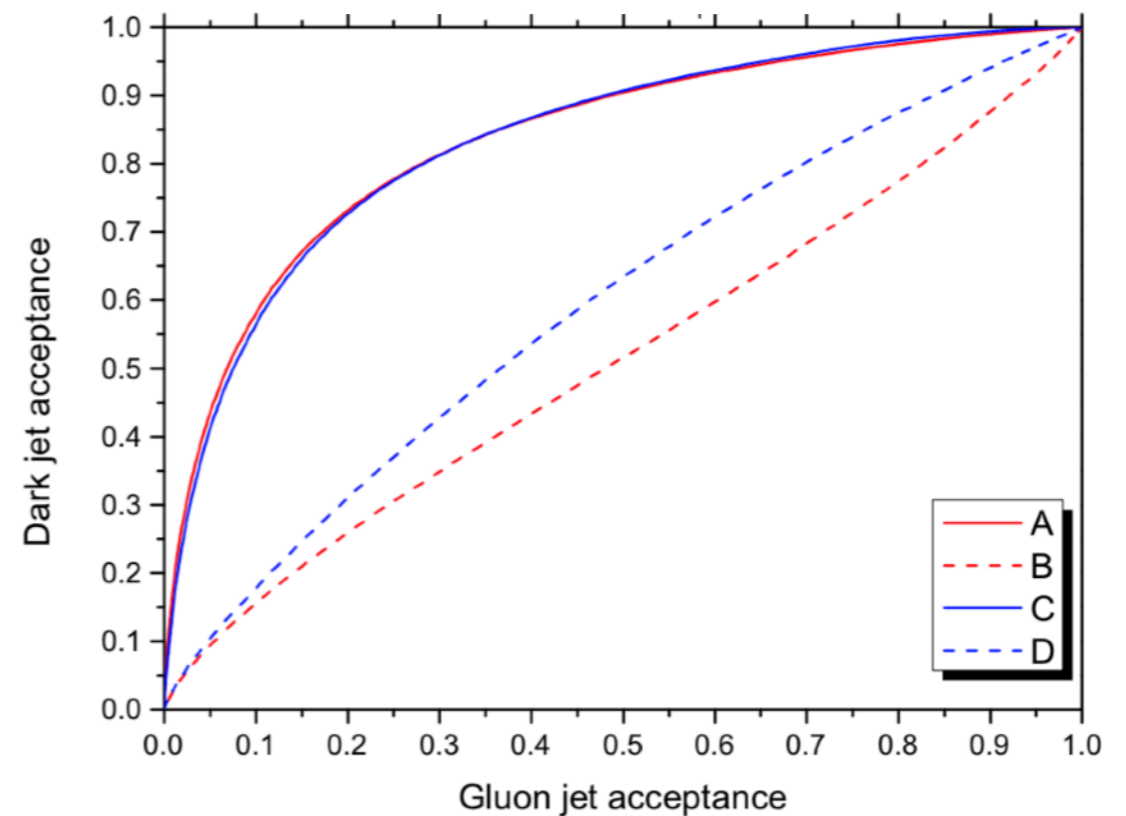
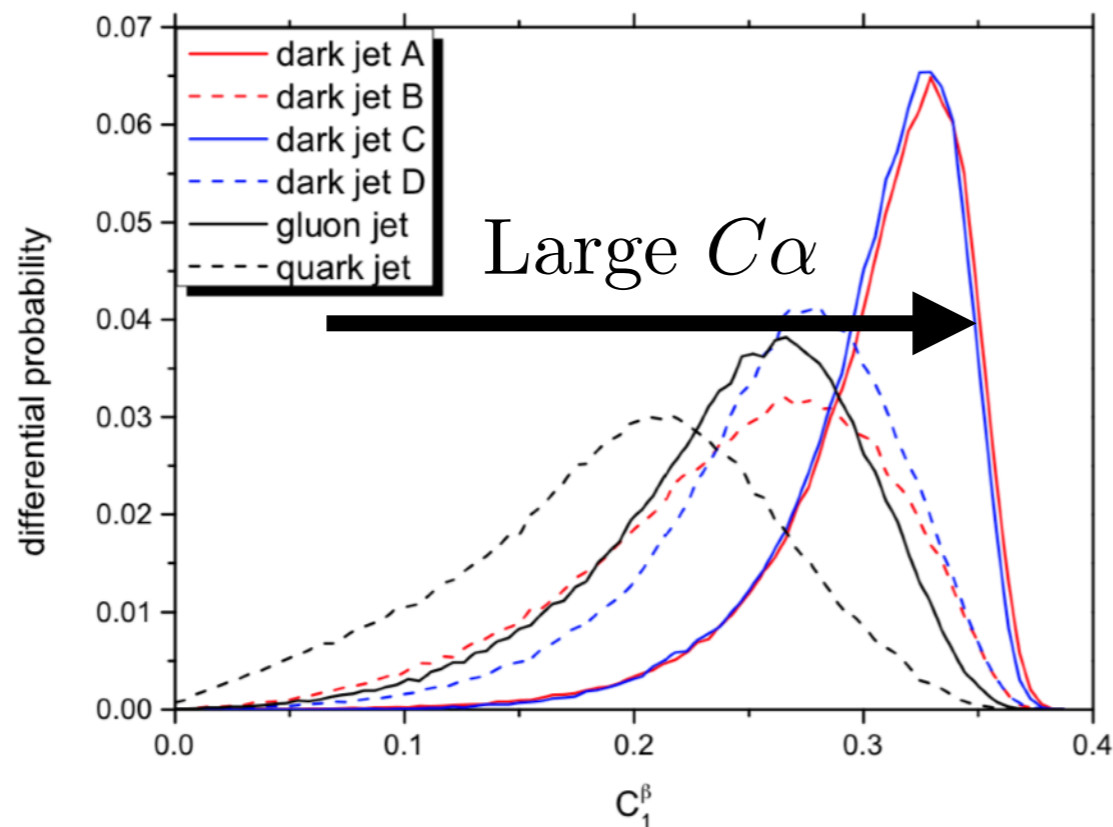
$$z_1 z_2 \theta^\beta \rightarrow \frac{1}{4} (z_1 + z_2)^2 \left(\frac{m_{\pi_d}}{p_T}\right)^\beta$$

---

# eg: Energy correlation

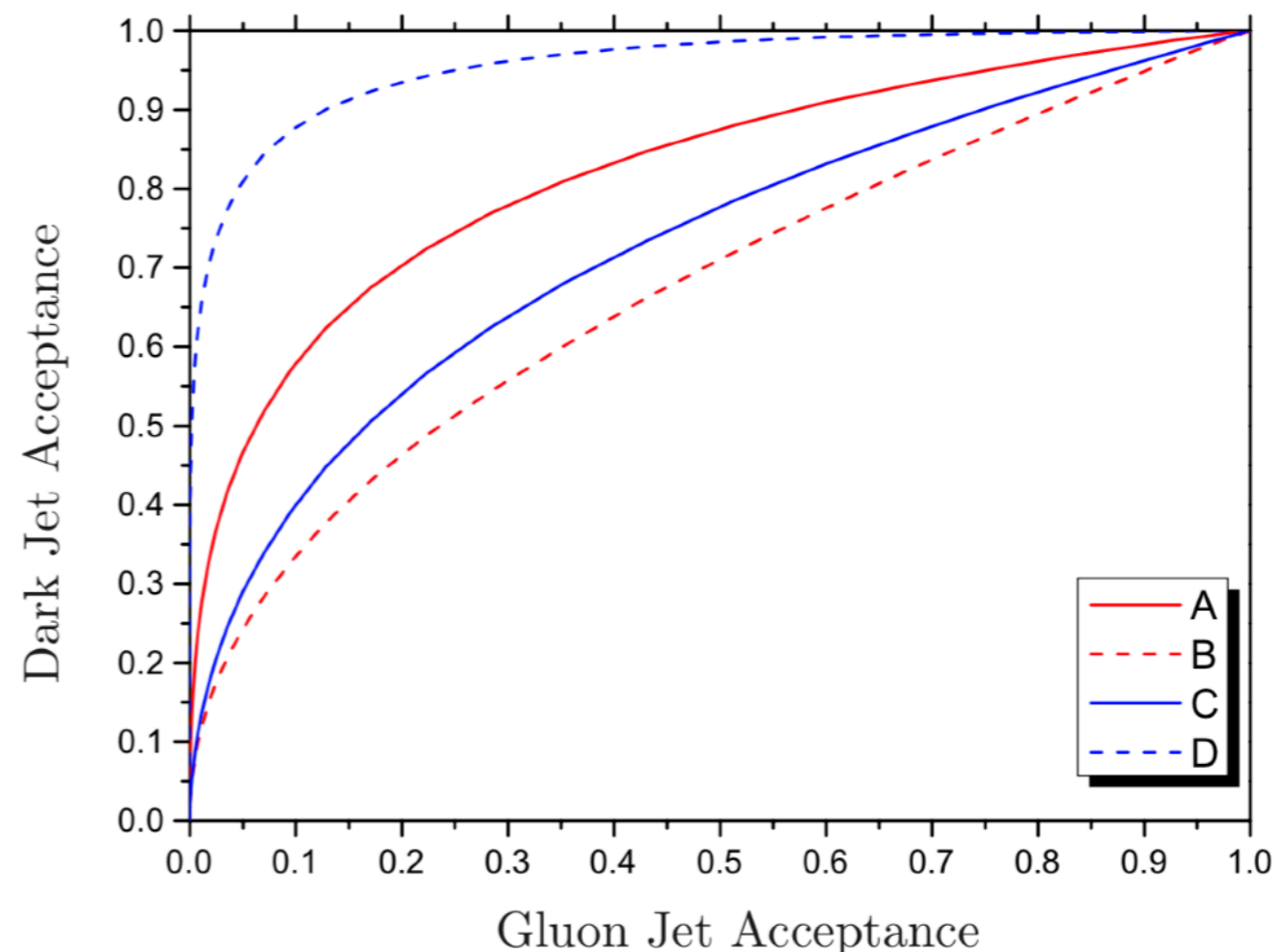
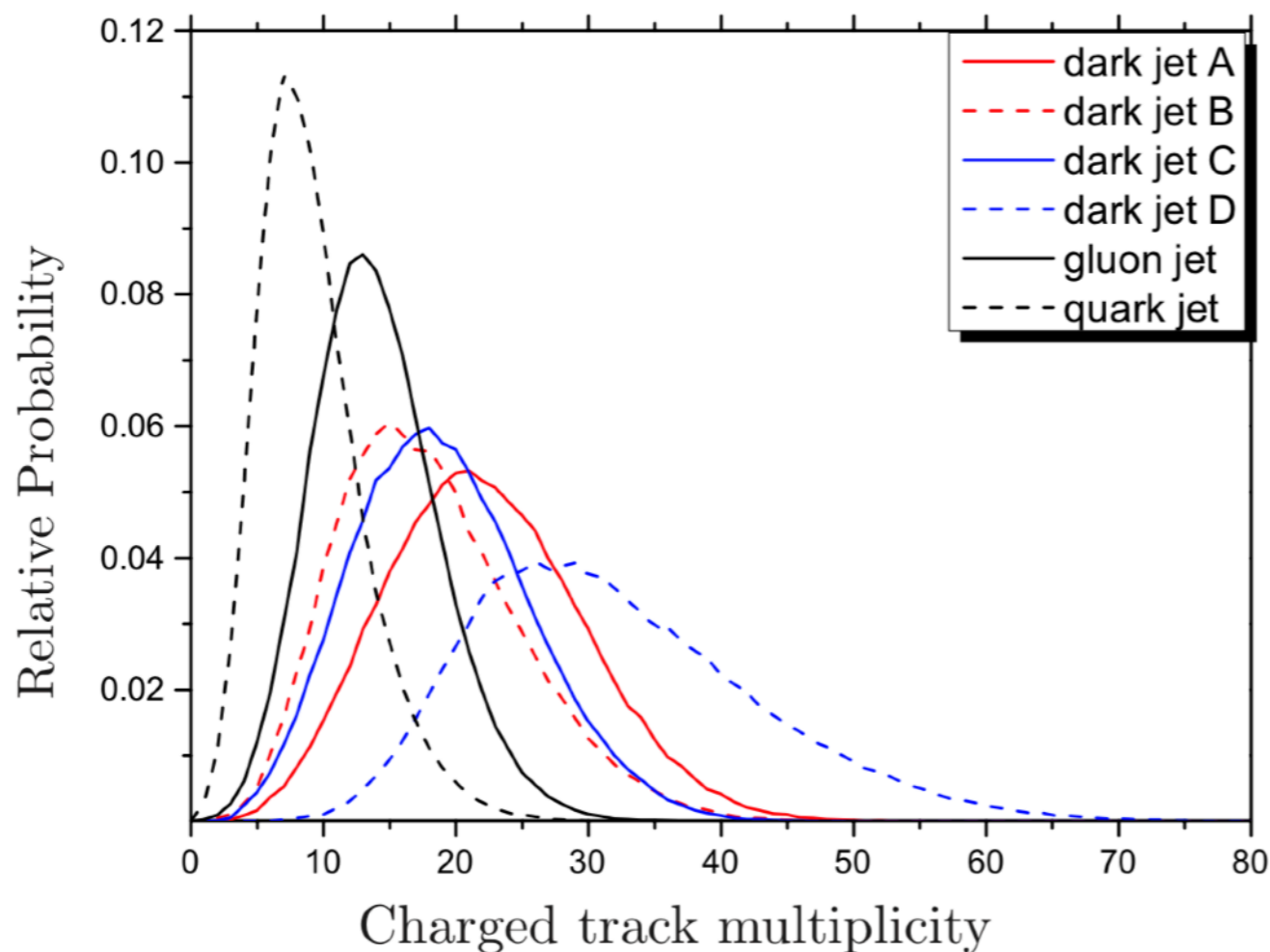
- Correlations among constitute particles would be interesting

$$C_1^{(\beta)} = \sum_{i < j \in J} z_i z_j (R_{ij})^\beta$$



# eg: Charged track multiplicity

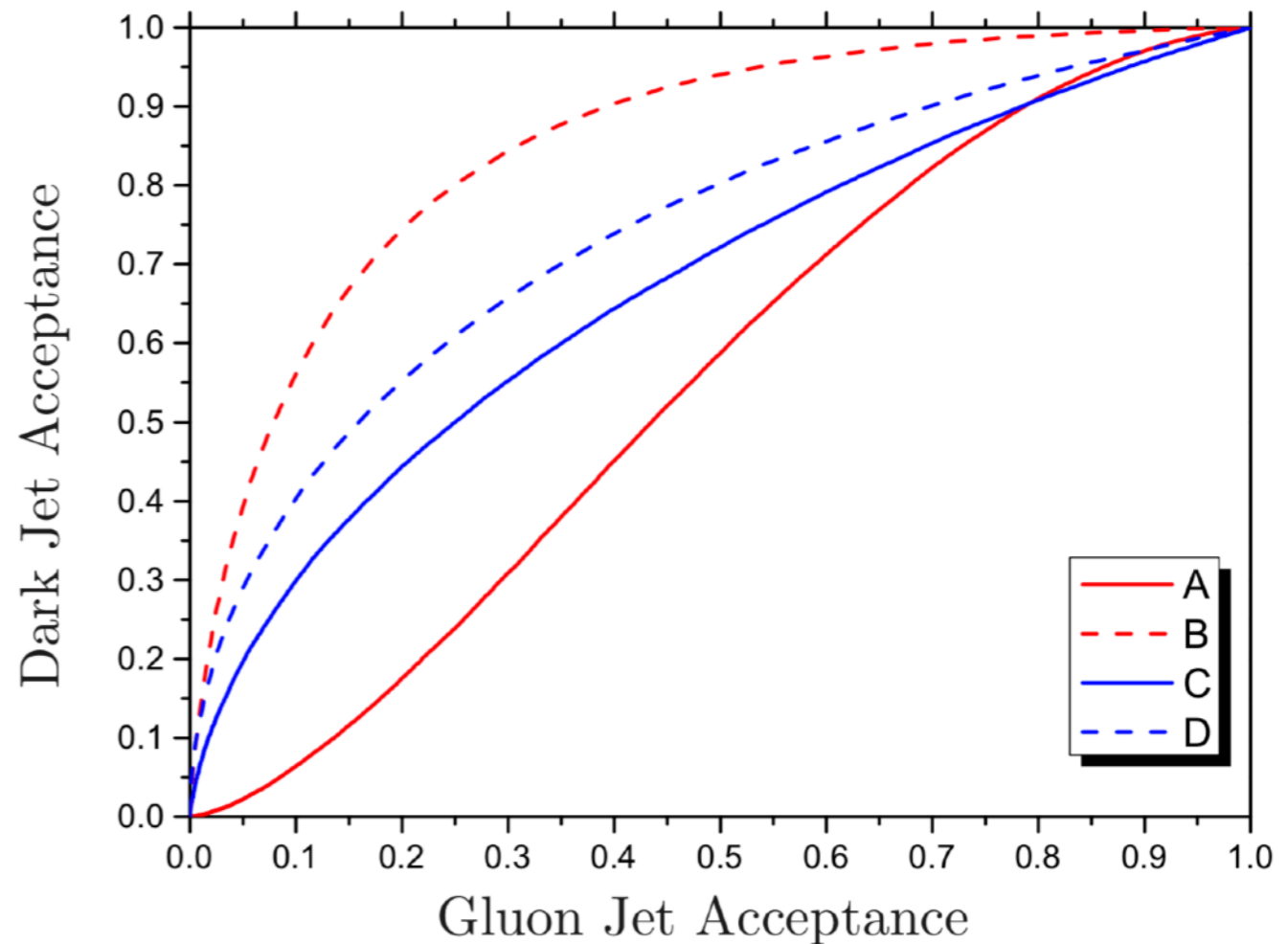
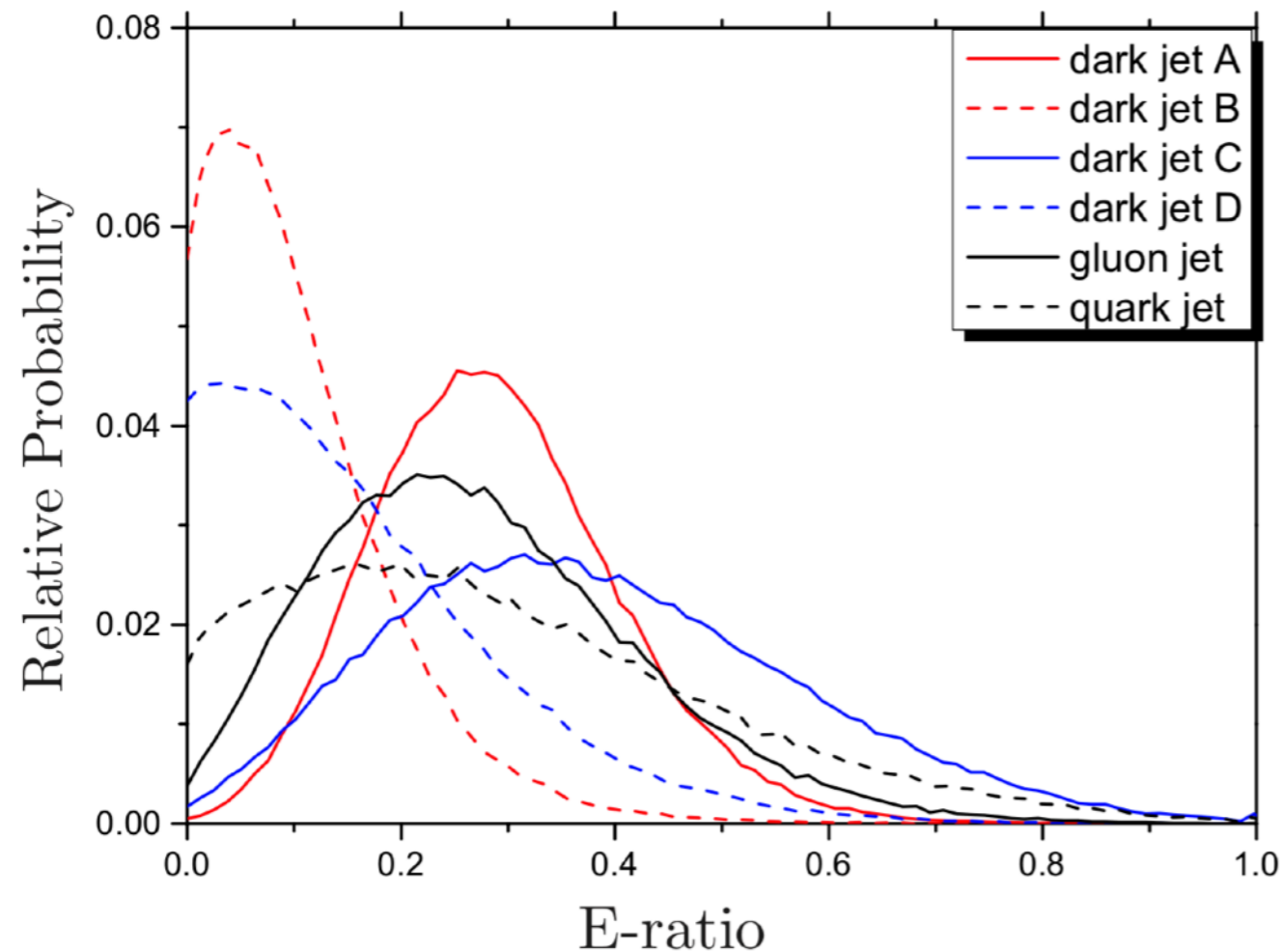
- Analyses with charged track multiplicity get benefits from the LHC track reconstruction performance.
- IRC-unsafe variables, but cut on  $p_t > 0.5$  GeV



# eg: E-ratio

- A variable which depends on the life-time of hadron;

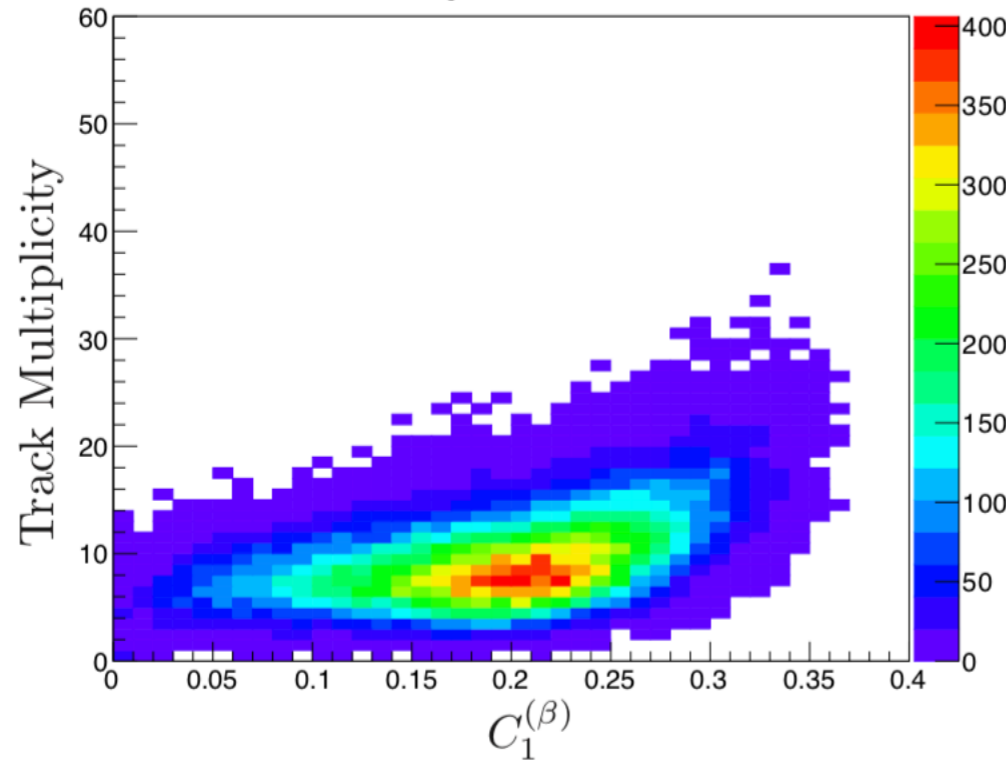
$$\text{E-ratio} = \frac{\text{Energy deposit on ECAL}}{\text{Jet's } p_T}.$$



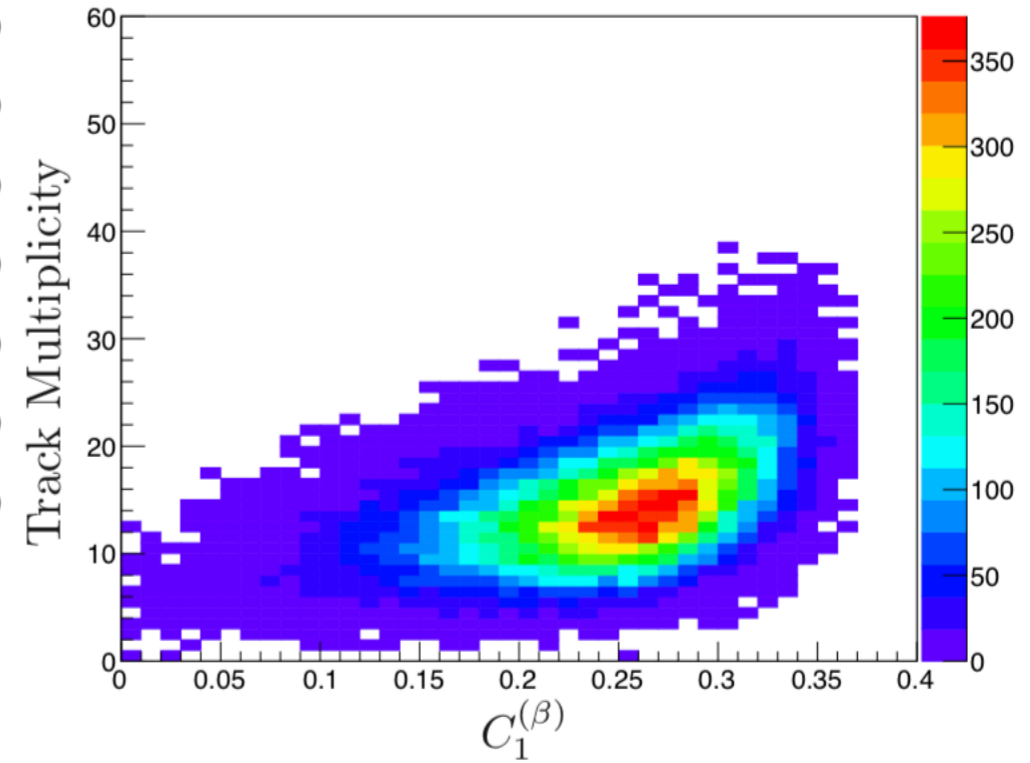
- A model with  $\pi_d \rightarrow s\bar{s}$ , which leads to K-Long.

# Different behavior of jet signals from dark QCD jet

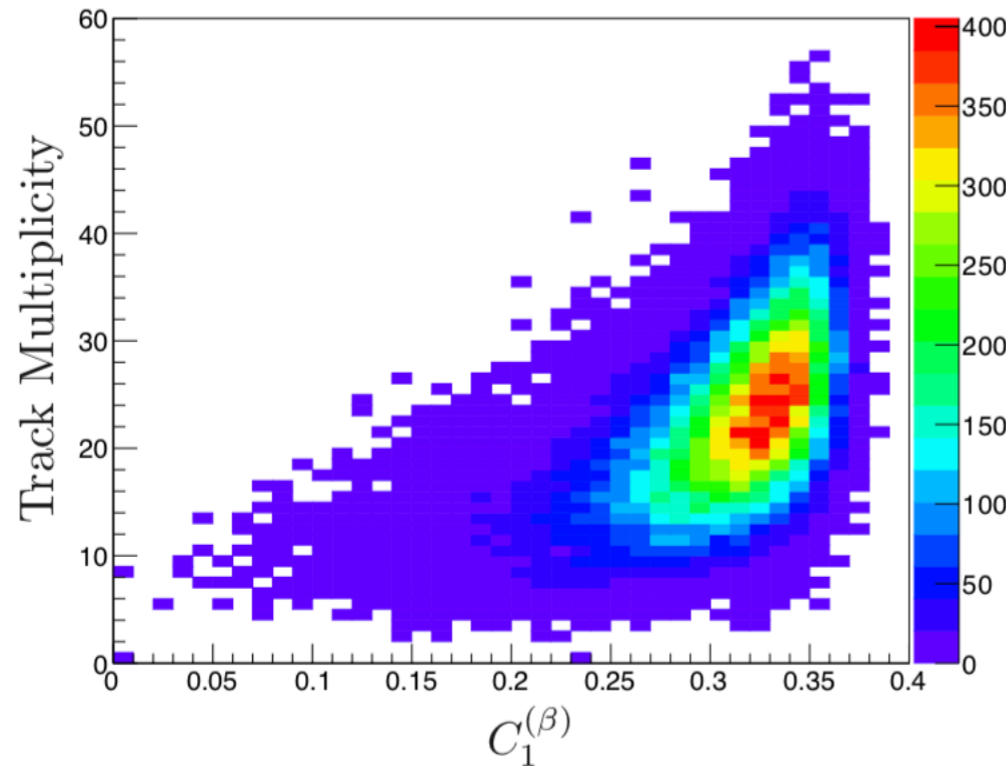
Quark Jet



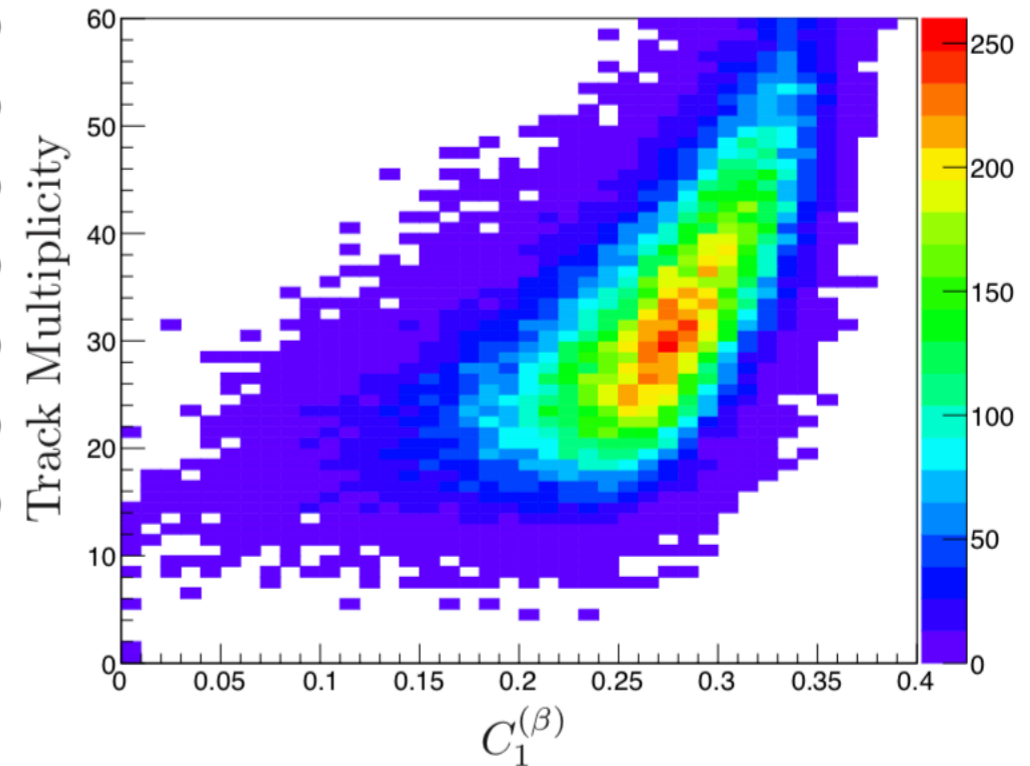
Gluon Jet



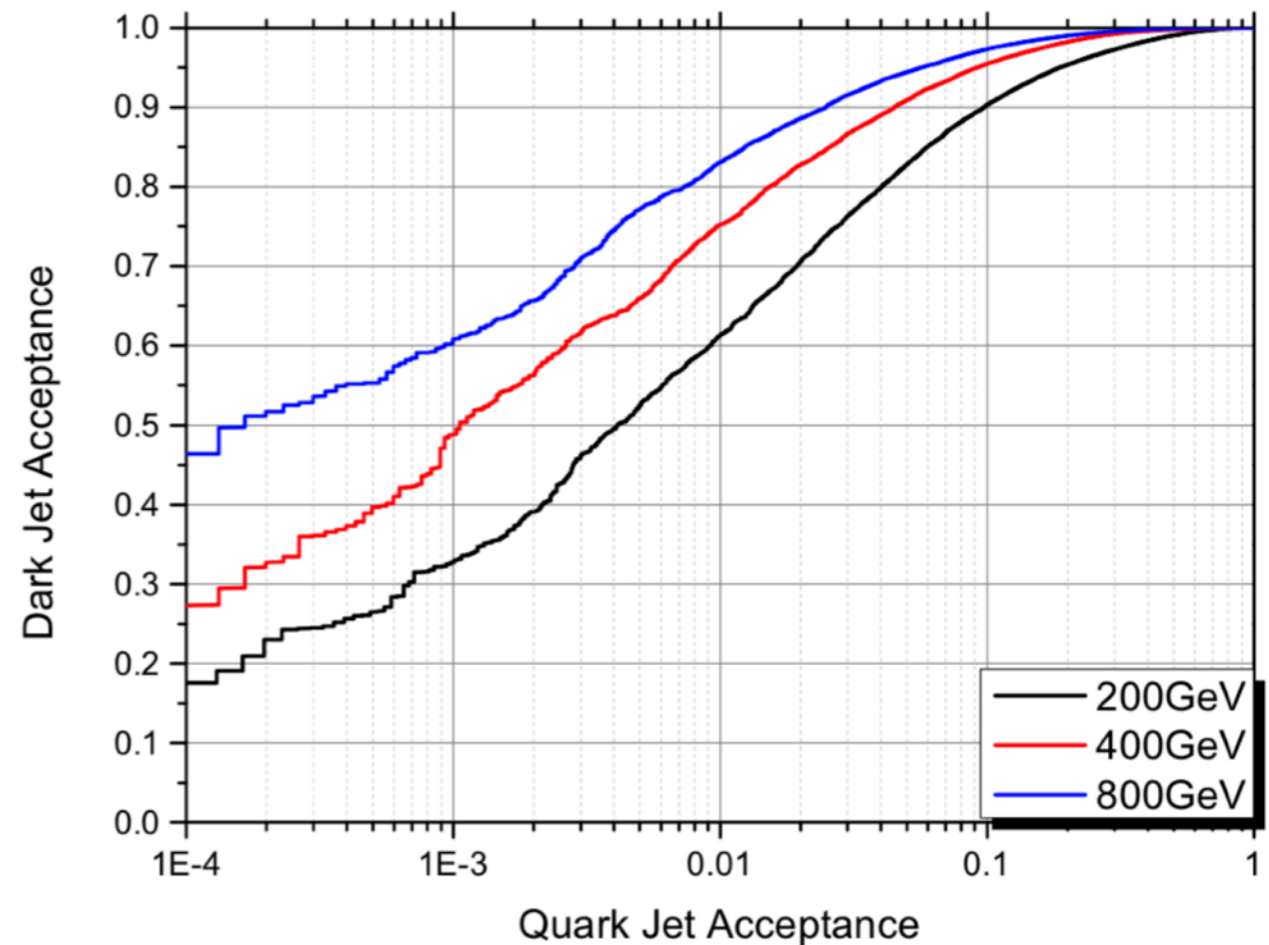
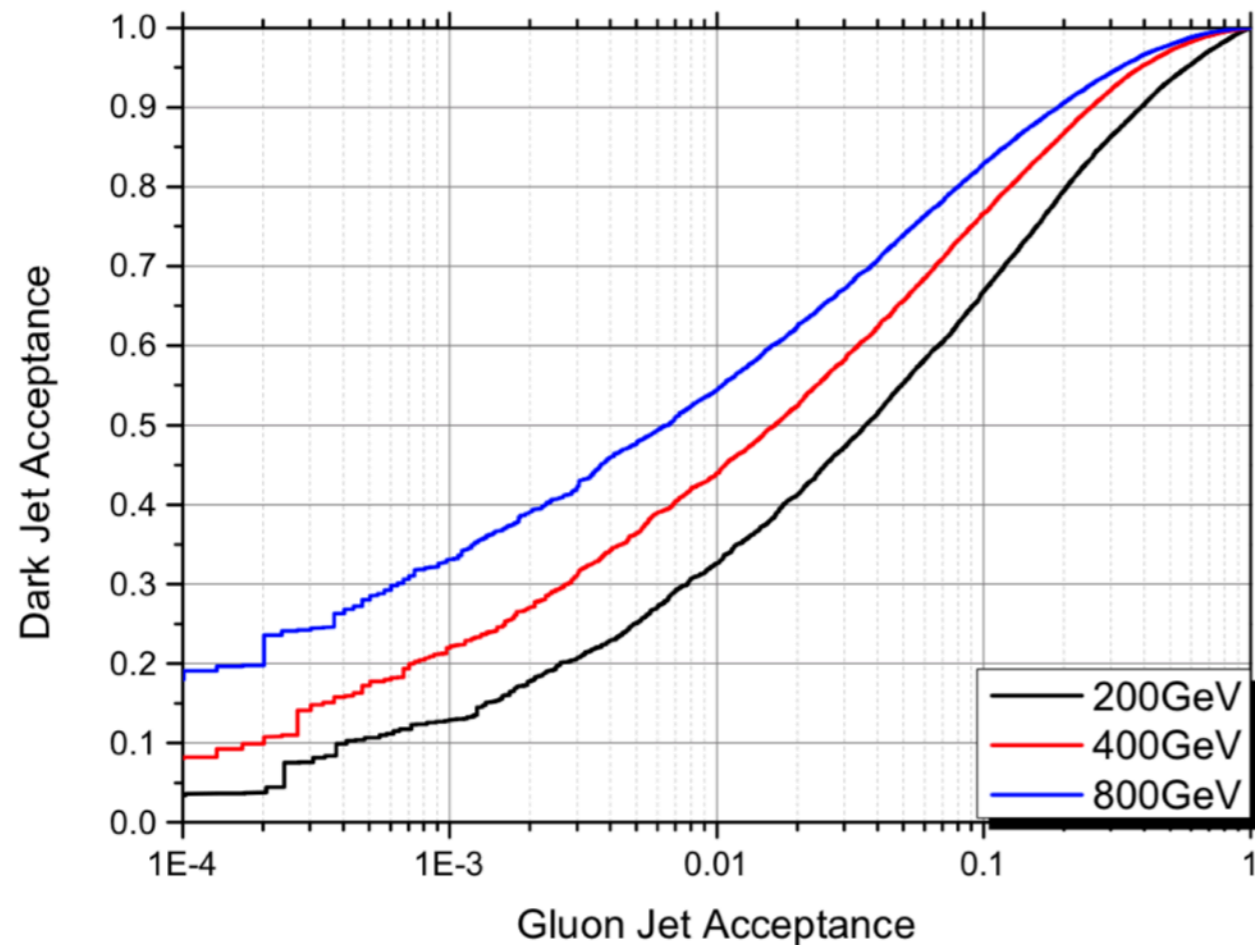
Dark Jet A



Dark Jet D

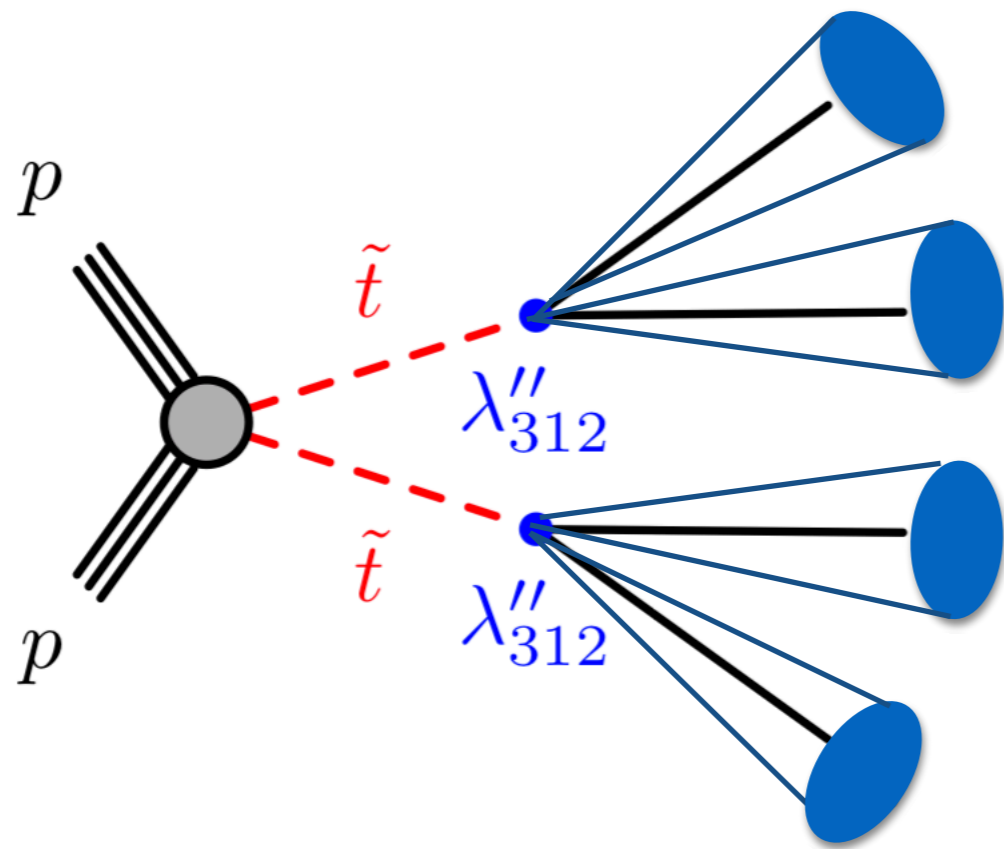


# Identify dark jet

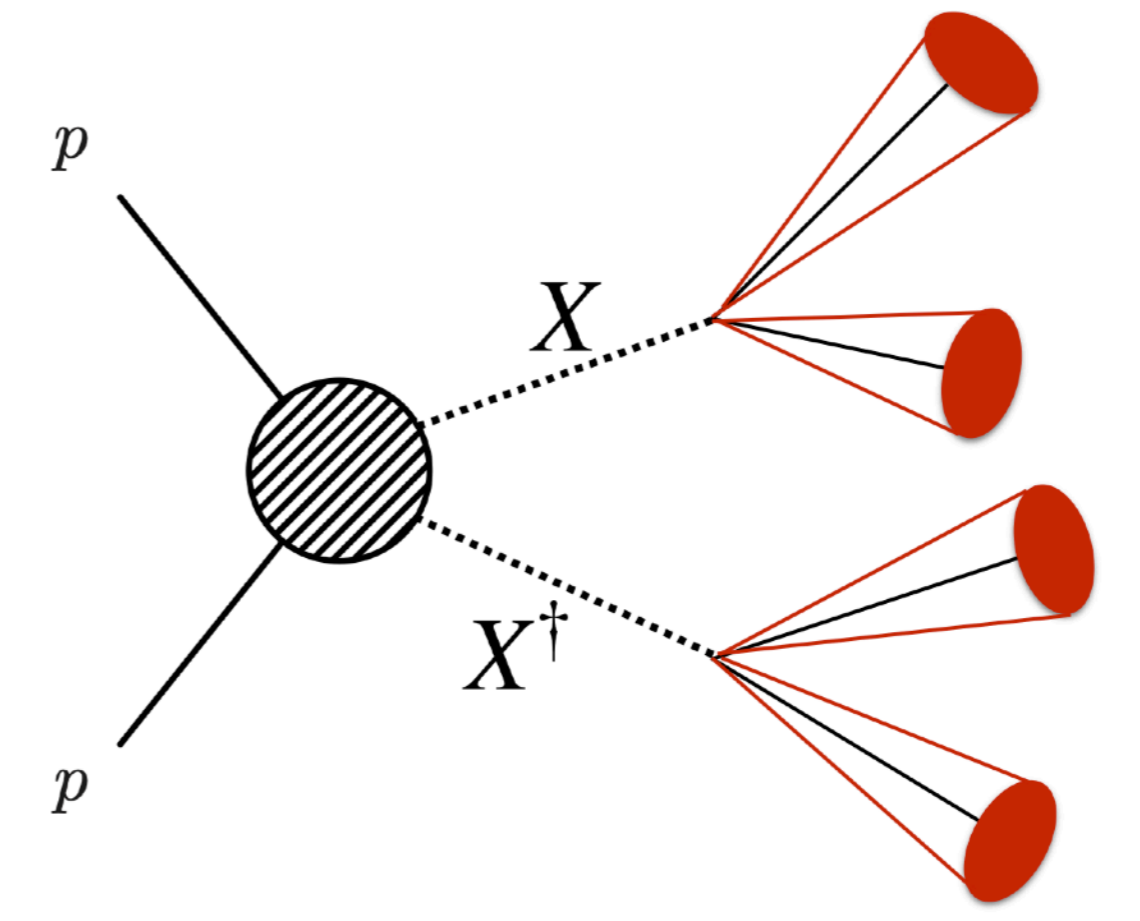


- Combining : Jet mass, Energy correlation function, girth, charged track multiplicity, # of subjects, ...
- High PT jet would be better to separate dark jet from SM QCD jets

# Comparison between conventional search and jet substructure method



**Normal QCD jet**



**Jet from Dark QCD**

# Conventional cuts

- Events are required to have at least 4 jets with  $p_T > 120\text{GeV}$  and  $|\eta| < 2.4$ .
- These 4 jets are paired by minimizing  $\Delta R_{\min} = \sum_{i=1,2} |\Delta R_i - 1|$ , with  $\Delta R_i$  the angular distance between two jets in a pair.
- Define  $m_{\text{avg}}$  as the average of the invariant masses of these two jets pair as  $m_{\text{avg}} = \frac{1}{2}(m_1 + m_2)$  with  $m_1$  and  $m_2$  are the invariant masses of two resonances. Discard events with large angular separation according to a resonant mass:

$$\begin{aligned} \Delta R_{\min} &> -0.002 \times (m_{\text{avg}}/\text{GeV} - 225) + 0.72 && \text{if } m_{\text{avg}} < 225\text{GeV} \\ \Delta R_{\min} &> +0.0013 \times (m_{\text{avg}}/\text{GeV} - 225) + 0.72 && \text{if } m_{\text{avg}} > 225\text{GeV} \end{aligned}$$

- Boosting the system of these two resonances (two jets pairs) to their centre-of-mass frame.  $\cos \theta^*$  is defined as the cosine of the angle between one of the resonance and the beam-line in the centre-of-mass frame. The mass asymmetry  $\mathcal{A}$  is defined as:

$$\mathcal{A} = \frac{|m_1 - m_2|}{m_1 + m_2},$$

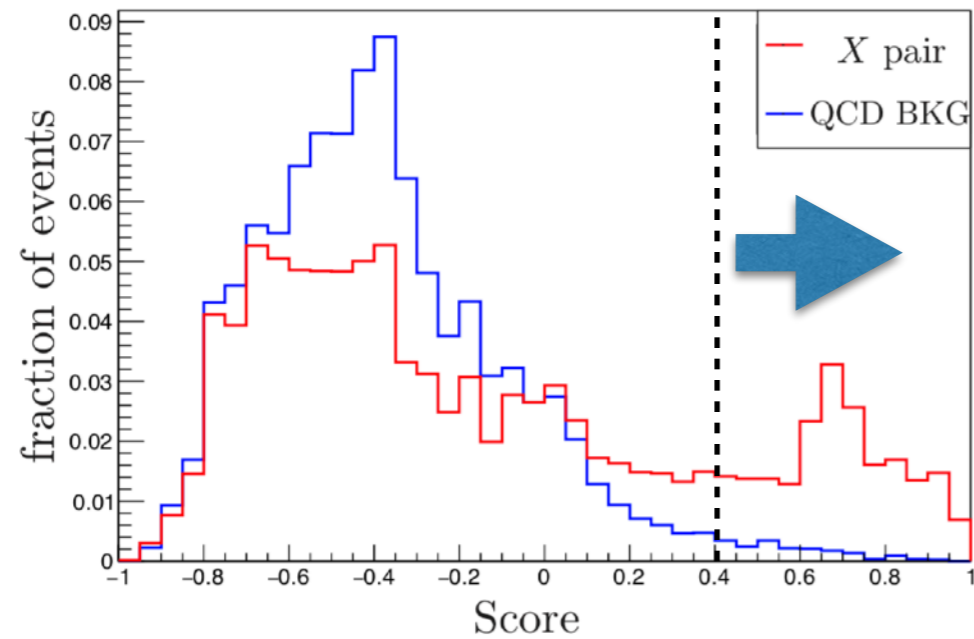
Events are cut by requiring  $\mathcal{A} < 0.05$  and  $|\cos \theta^*| < 0.3$ . This cut defines the inclusive signal region (SR) selection.

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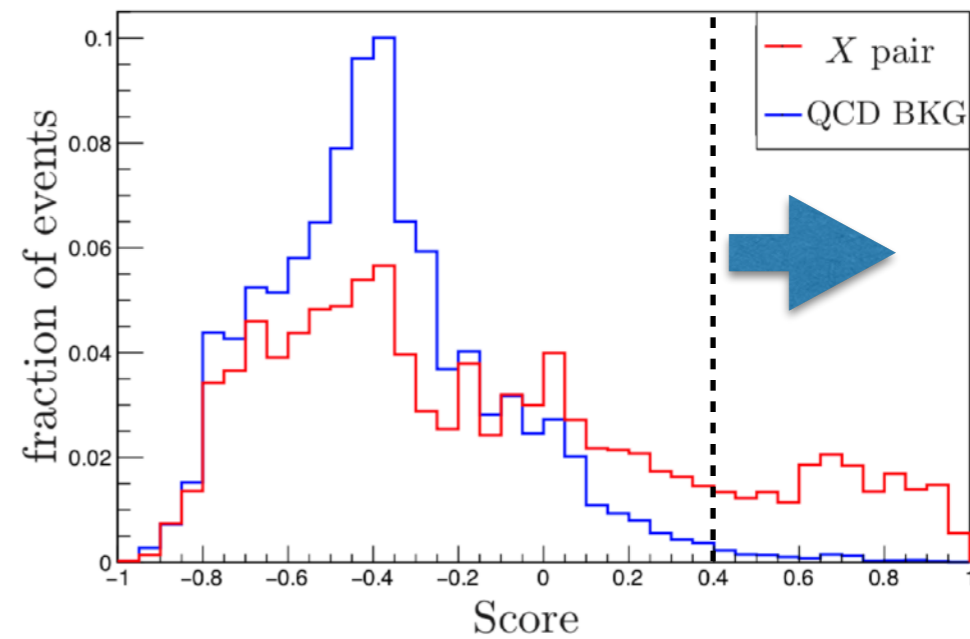


# BDT with $\{C_1^{(\beta)}, \text{E-ratio, Track Multiplicity}\}$

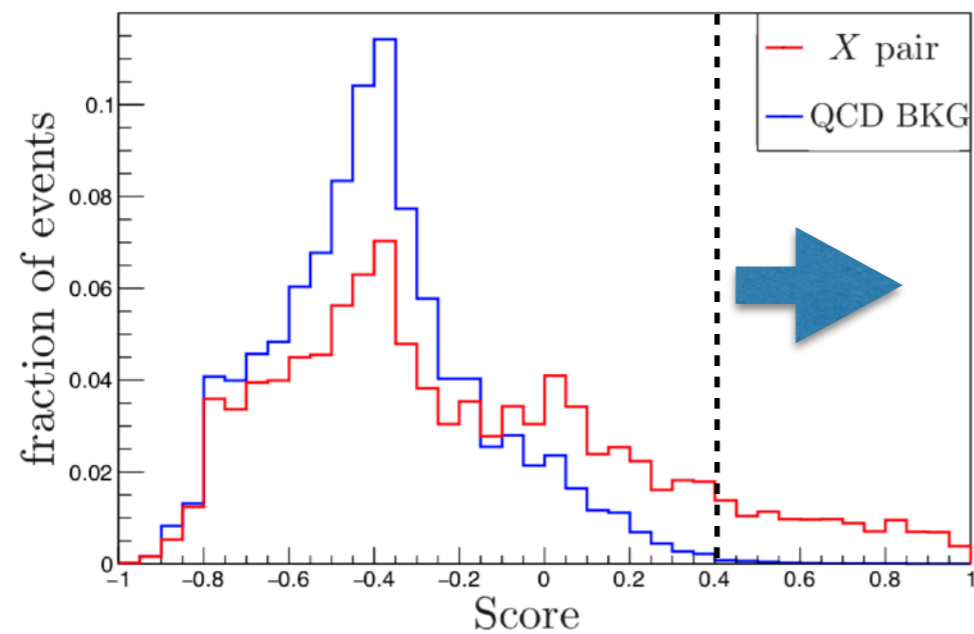
BDT score of hardest jet



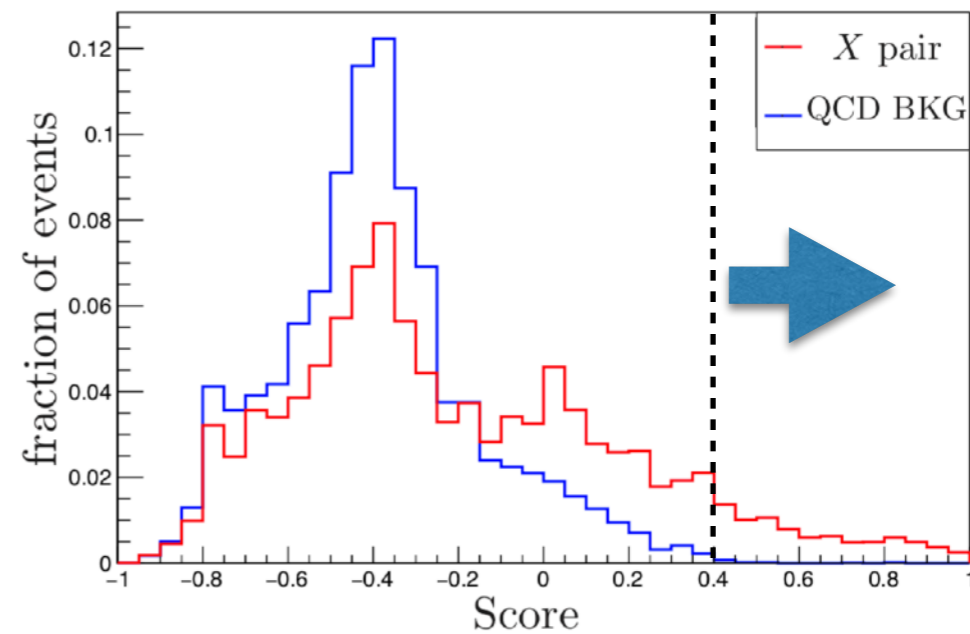
BDT score of 2nd hardest jet



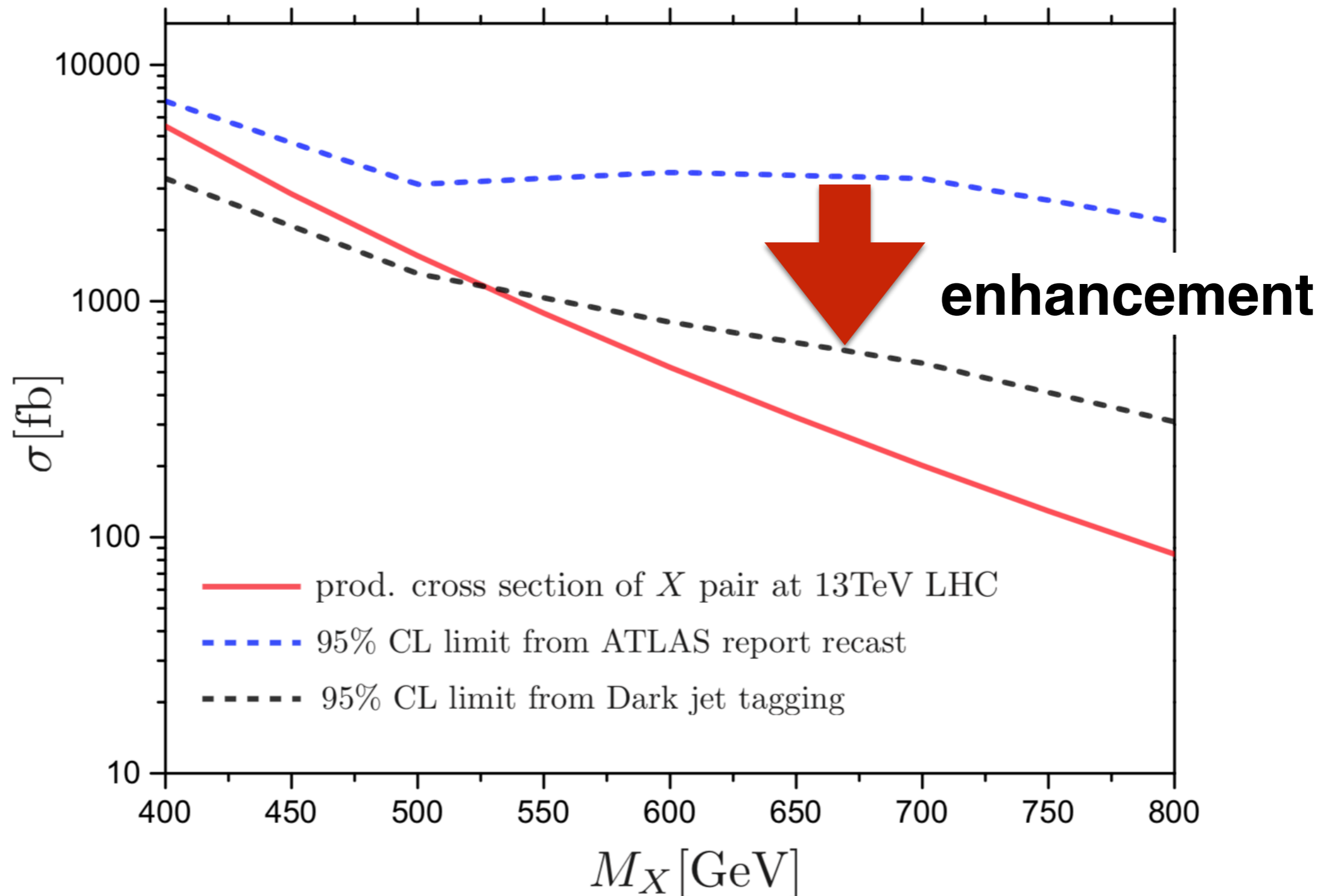
BDT score of 3rd hardest jet



BDT score of 4th hardest jet



# Comparison between conventional search and jet substructure method



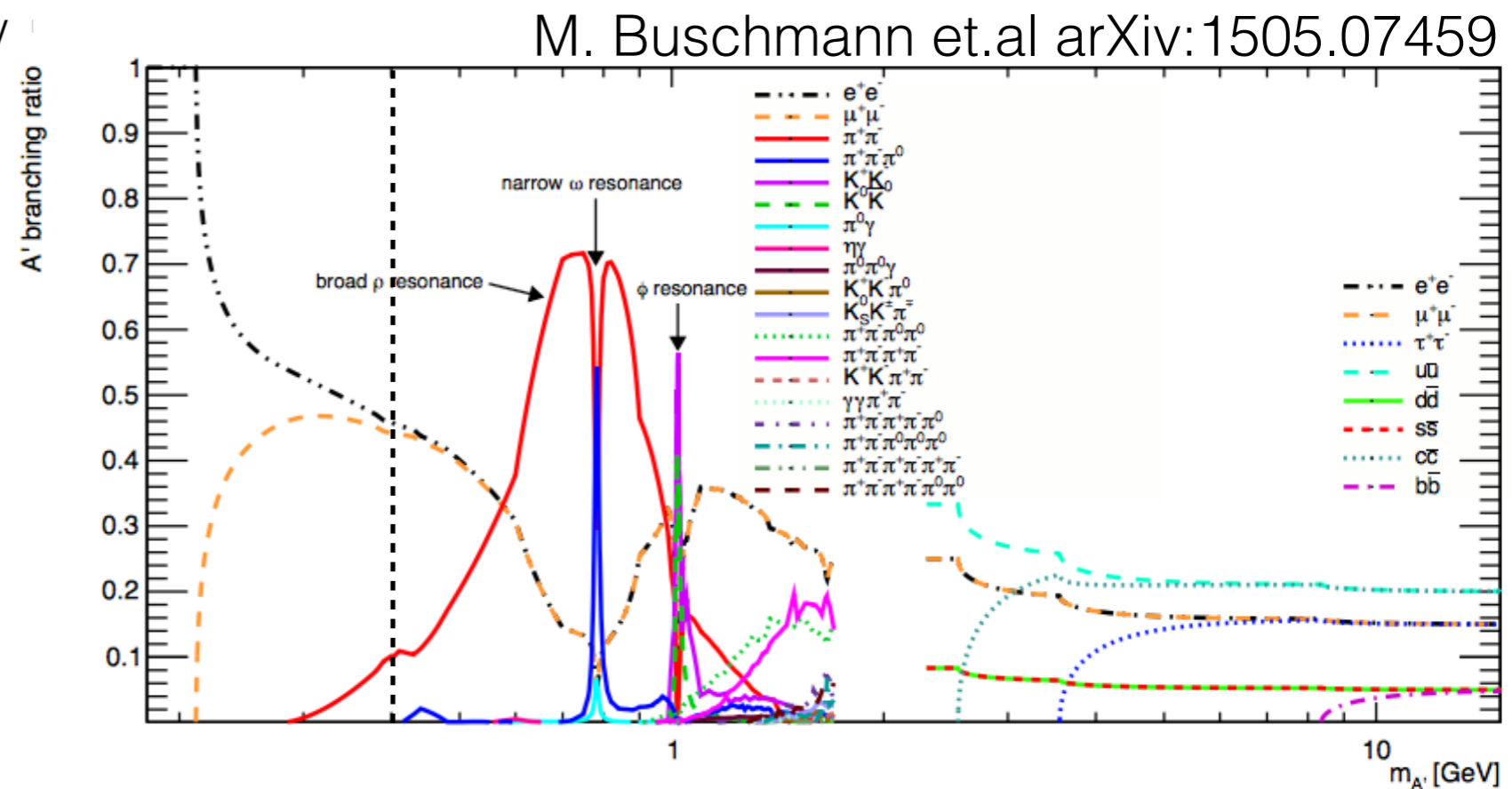
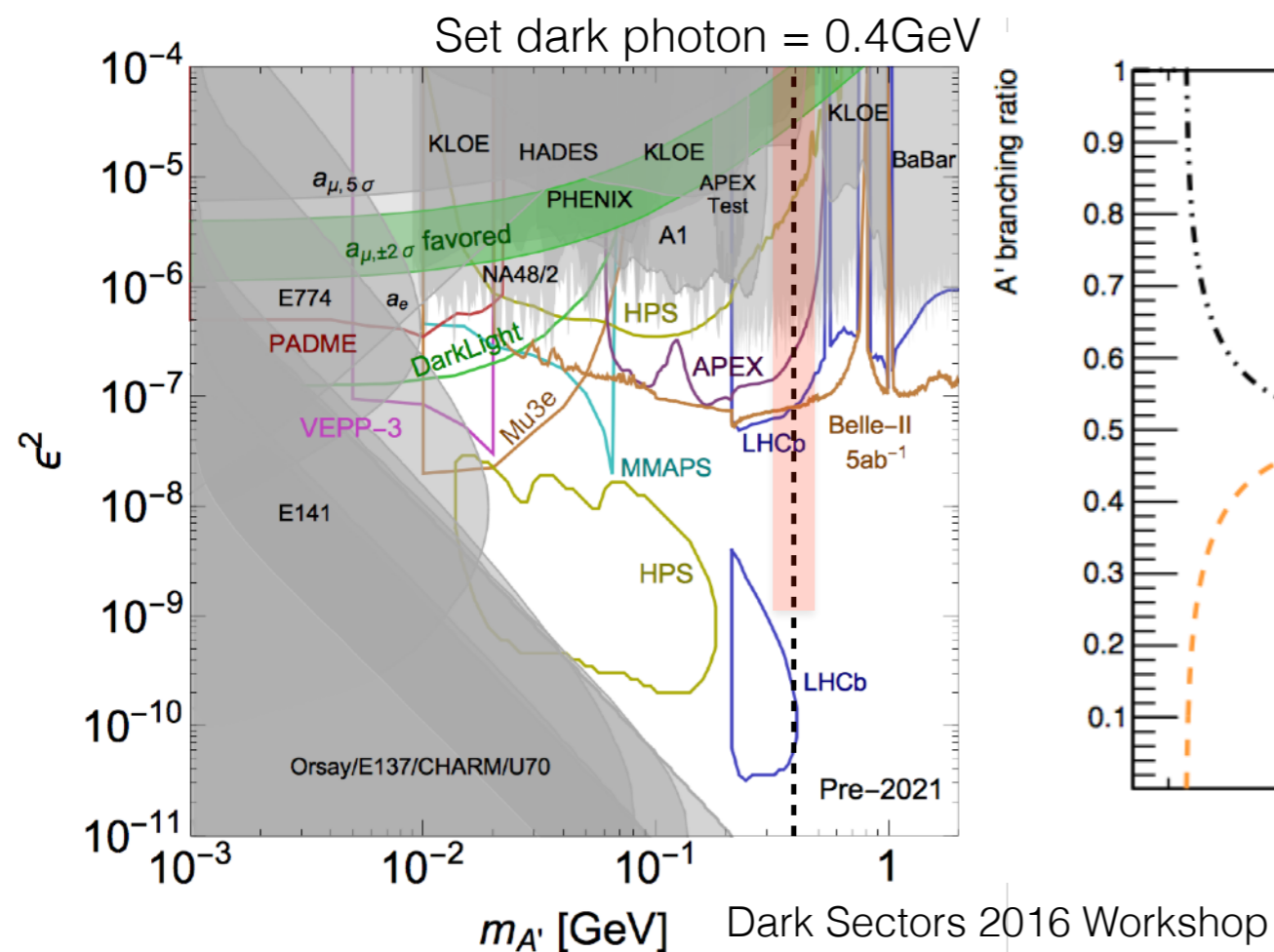
# Conclusion

- LHC program is an **active** experiment
  - to find dark sector ( dark matter ).
  - to measure properties of a dark sector.
- The **mass origin** in dark sector (like SM-Higgs mechanism) can strongly affect the dark photon showering in “**Energetic**” dark matter.
- Collider can probe the nature of dark matter by examine the **pattern** of dark photon **showering**
- LHC can probe the compositeness of dark matter using sophisticated **jet-substructure** techniques.

Back up

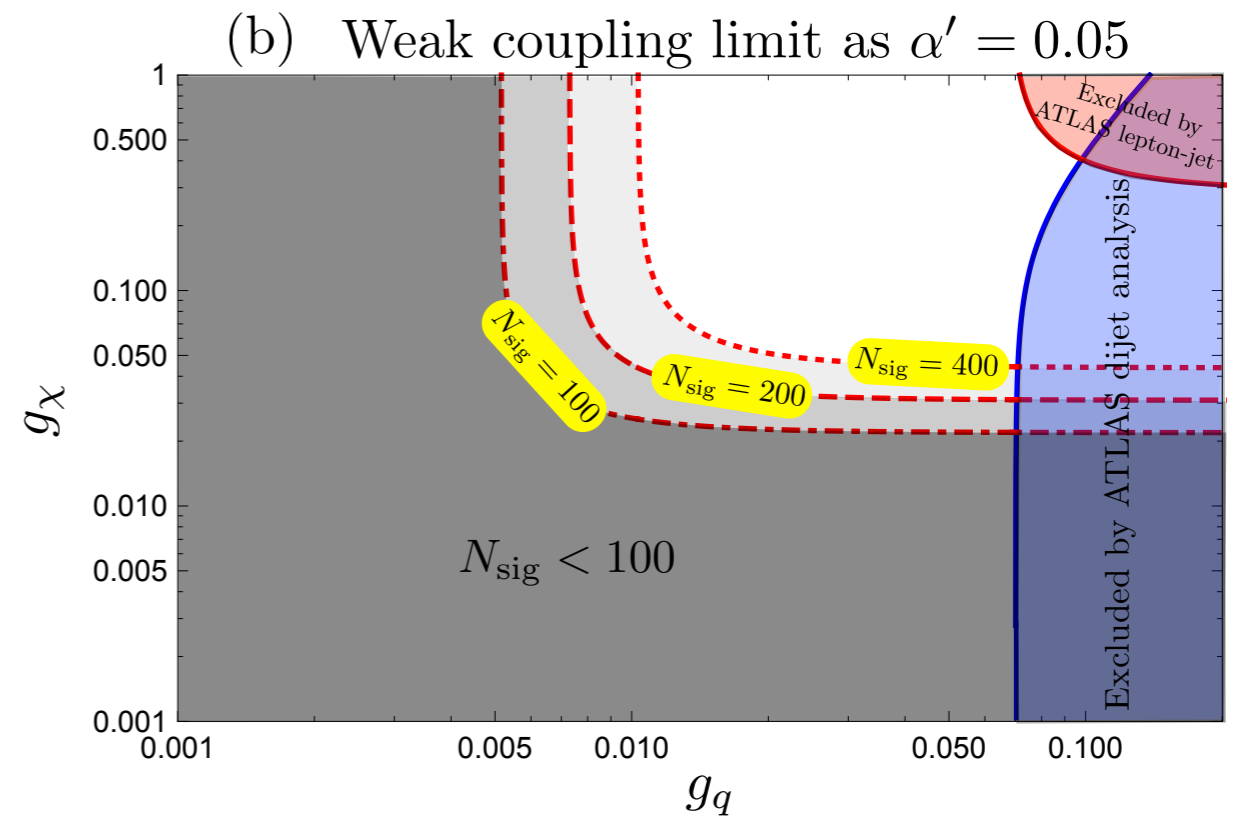
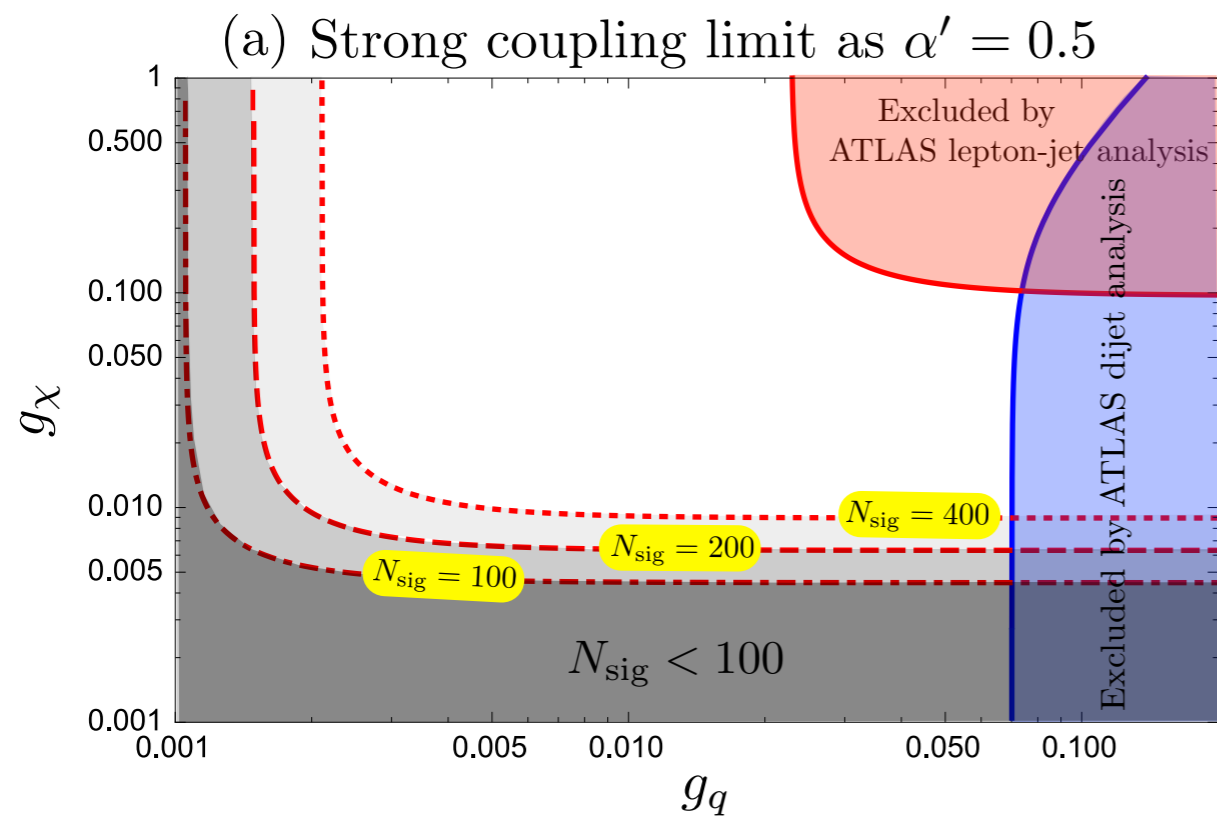
# Benchmark points

- We choose a bench mark point for
  - the prompt decays of a dark photon
  - Non-negligible decay mode into muons-pair to tag!



# Constraints from LHC

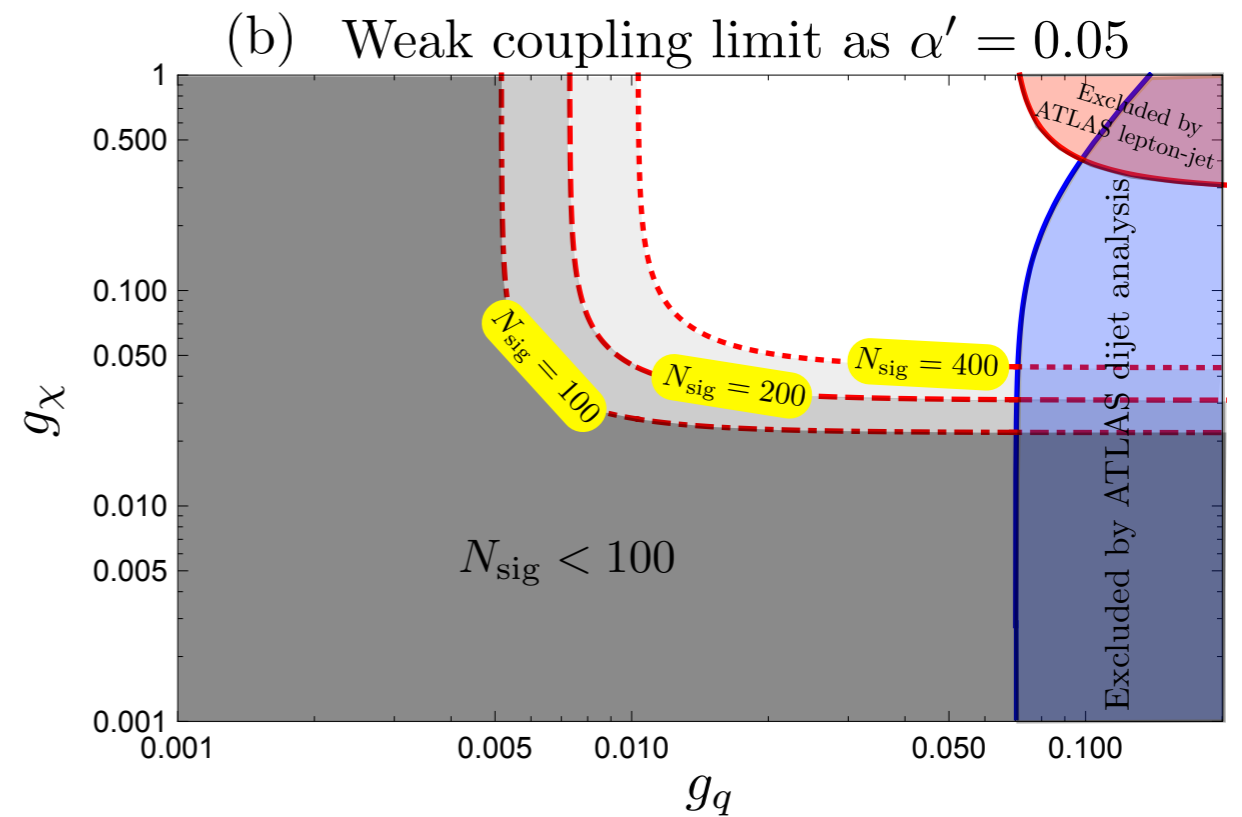
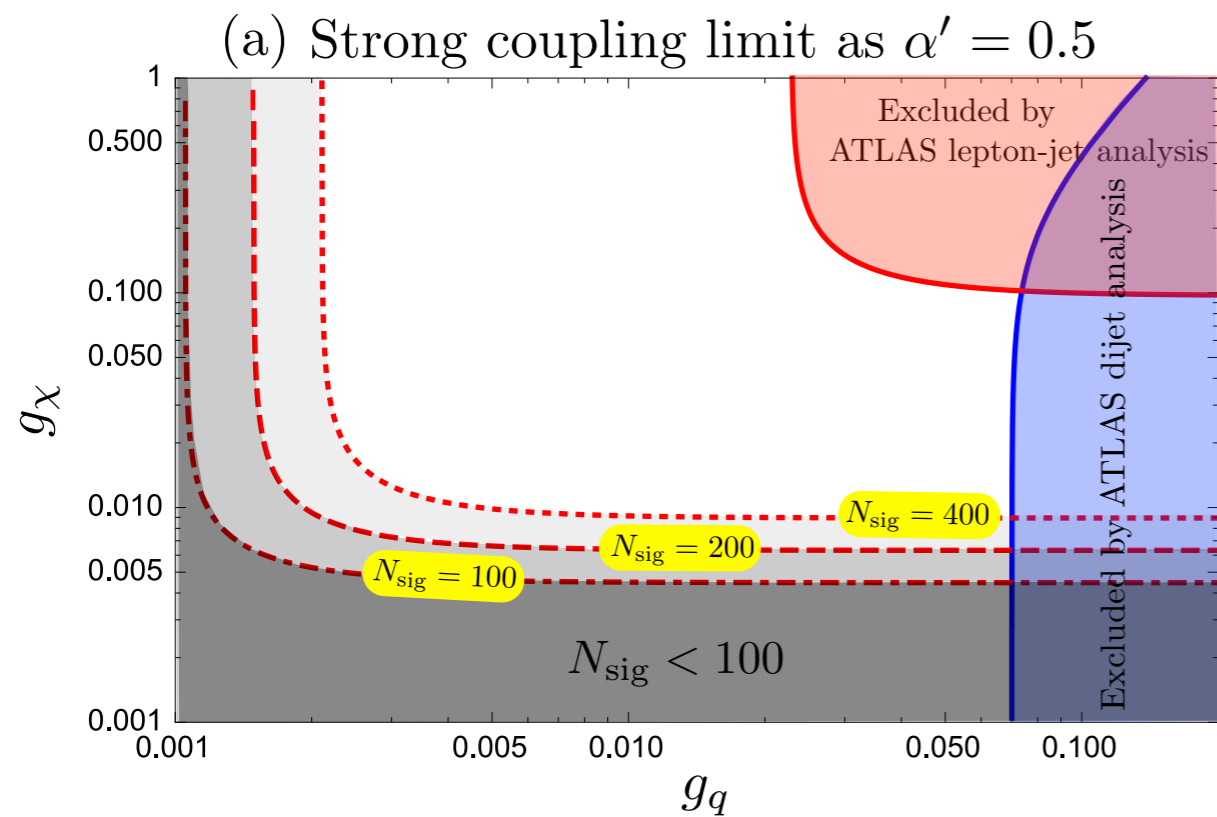
with  $M_{Z'} = 1.5 \text{ TeV}$  and  $m_{\gamma_d} = 0.4 \text{ GeV}$



Benchmark case	$\alpha'$	$m_\chi$ (GeV)	Model	$\epsilon_S$ (%)
(a) strong coupling limit	0.50	0.5	vector-like	3.68
(b) weak coupling limit	0.05	0.45	chiral	0.41

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