

# Determination of chemical freeze-out parameters from net-kaon fluctuations at RHIC

Jamie M. Stafford — University of Houston, USA

Collaborators: Claudia Ratti, Paolo Alba, Rene Bellwied,  
Jaki Noronha-Hostler, Paolo Parotto, Israel Portillo-Vazquez, Valentina Sarti

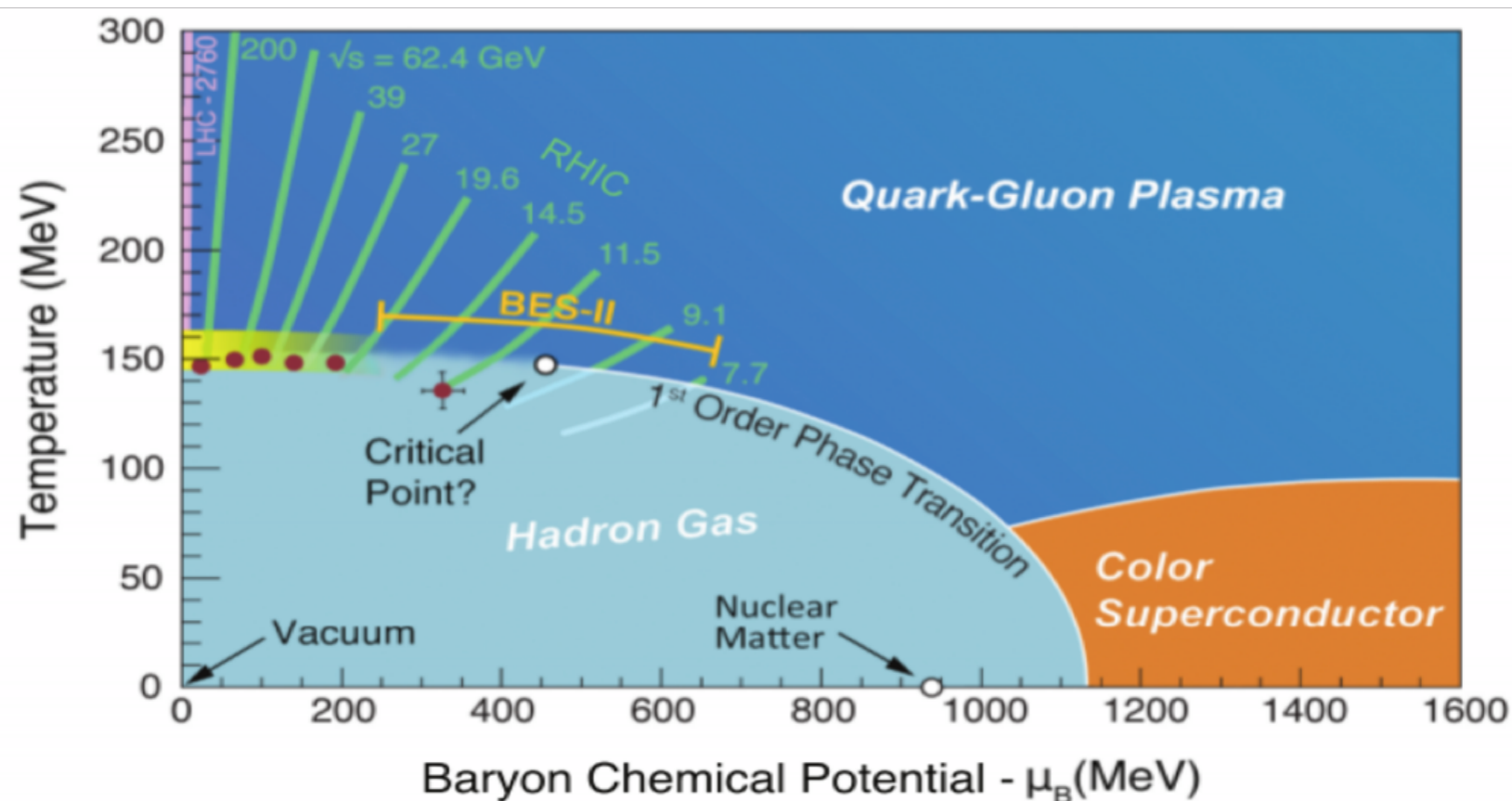


# QCD Phase Diagram



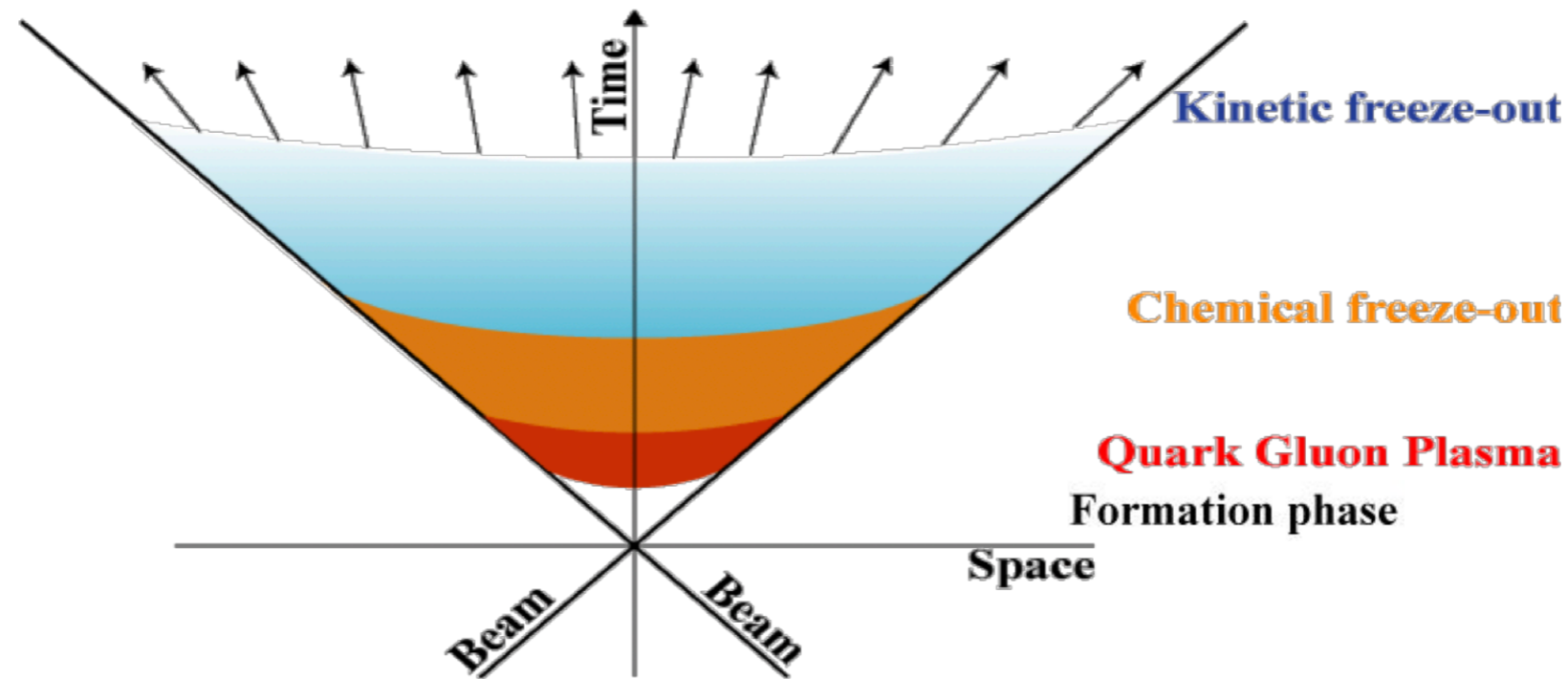
The different phases of QCD matter can be understood by studying the characteristics of the phase diagram

- ▶ QGP is formed at large  $T$ ,  $\mu_B$ ; ordinary hadronic matter at small  $T$ ,  $\mu_B$
- ▶ Crossover transition at  $T \sim 155\text{MeV}$ ; possible first order phase transition at high  $\mu_B$ 
  - ❖ Search for the critical point with the RHIC Beam Energy Scan (BES)



NSAC 2015 Long Range Plan for Nuclear Physics

# Evolution of a heavy-ion collision



- **Chemical freeze-out:** inelastic collisions cease; the chemical composition is fixed (particle yields and fluctuations)
- **Kinetic freeze-out:** elastic collisions cease; spectra and correlations are fixed

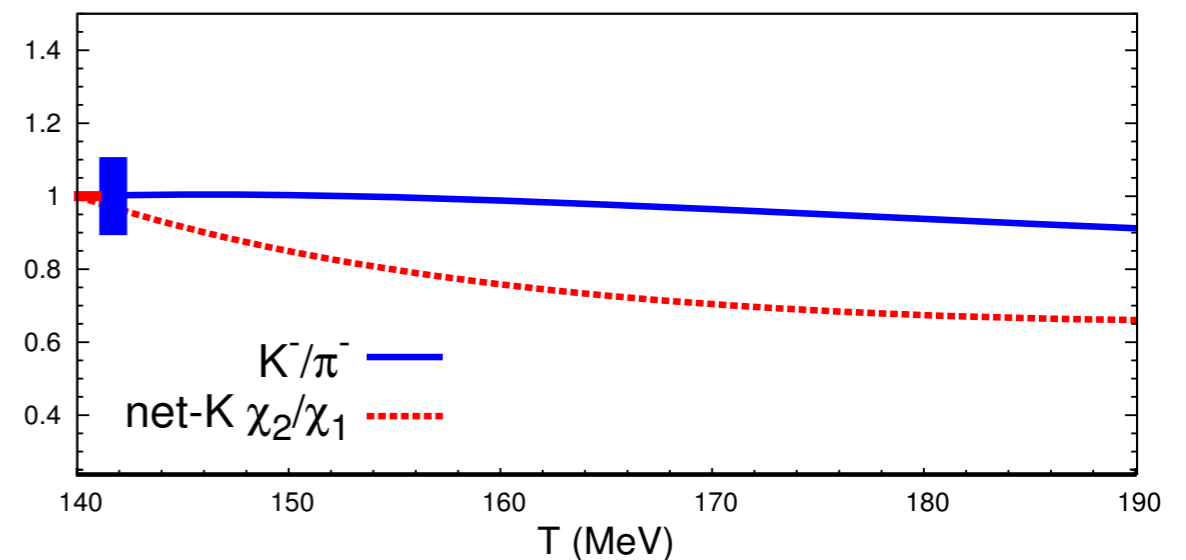
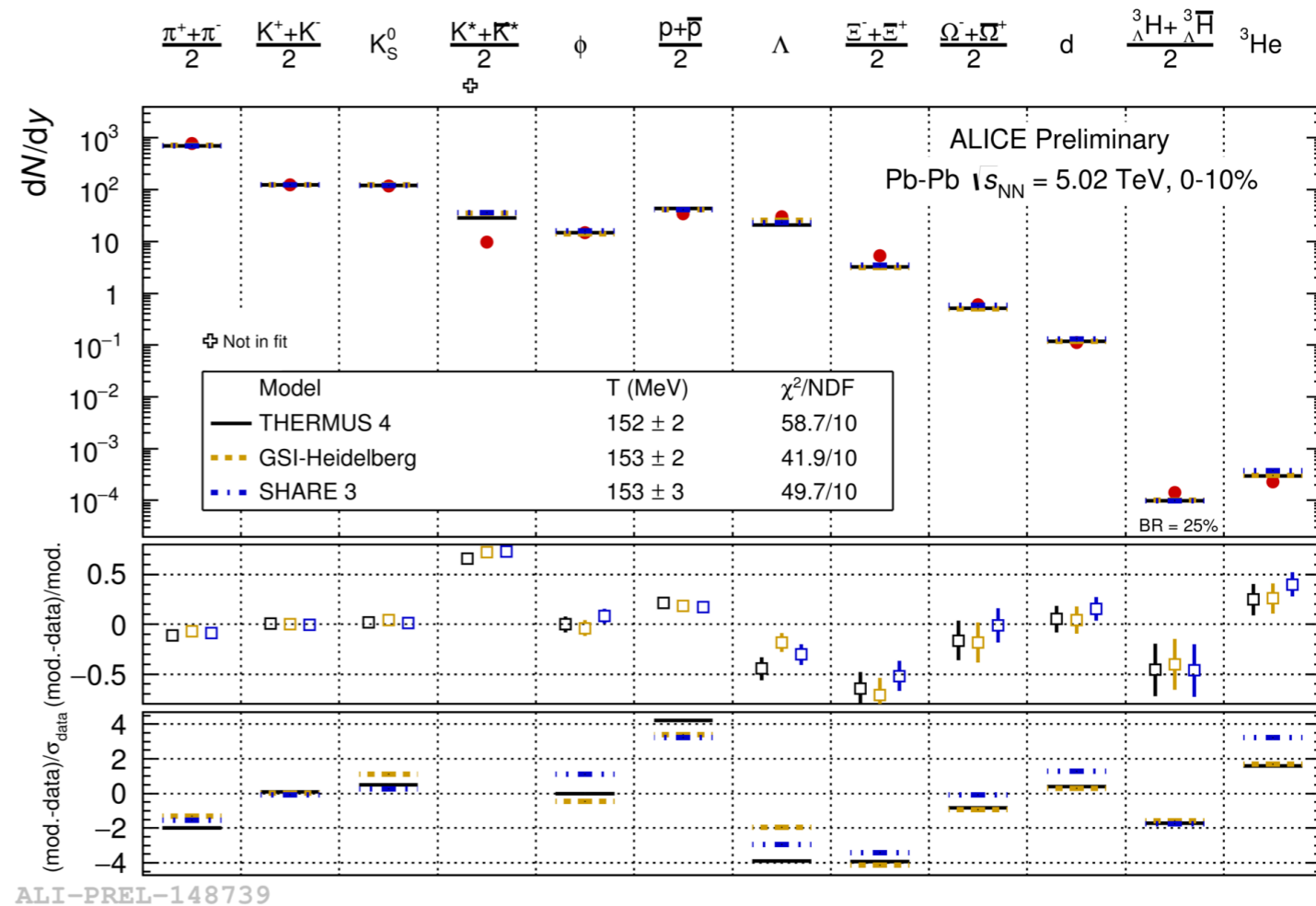
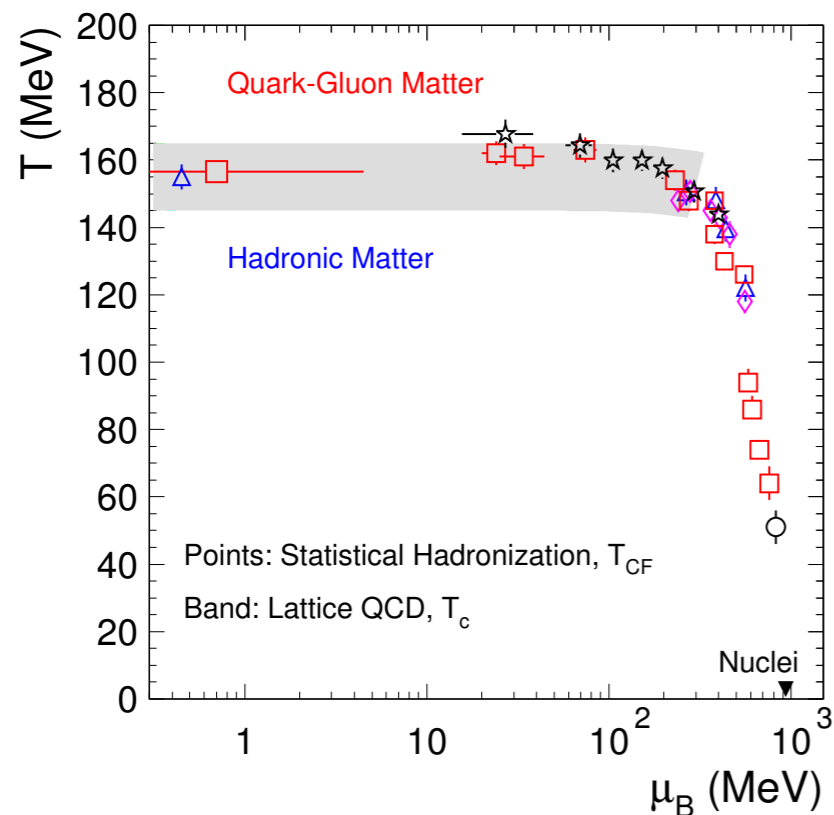
# Chemical freeze-out in HICs



The freeze-out parameters are determined by:

- ▶ Thermal fits of particle yields  $\{T_f, \mu_{B,f}, V_f\}$  or ratios  $\{T_f, \mu_{B,f}\}$
- ▶ Fits of the net-charge fluctuations

The hadron freeze-out curve can be drawn by scanning a range of collision energies



F. Bellini, Nucl.Phys. A (2019); A. Andronic, et al, Nature (2018); P. Alba, et al, PRC (2015)

# Fluctuations of Conserved Charges



$$\chi_{lmn}^{BSQ} = \frac{\partial^{l+m+n} p/T^4}{\partial(\mu_B/T)^l \partial(\mu_S/T)^m \partial(\mu_Q/T)^n}$$

mean :  $M = \chi_1$

variance :  $\sigma^2 = \chi_2$

skewness :  $S = \chi_3/\chi_2^{3/2}$

kurtosis :  $\kappa = \chi_4/\chi_2^2$

The volume-independent ratios are:

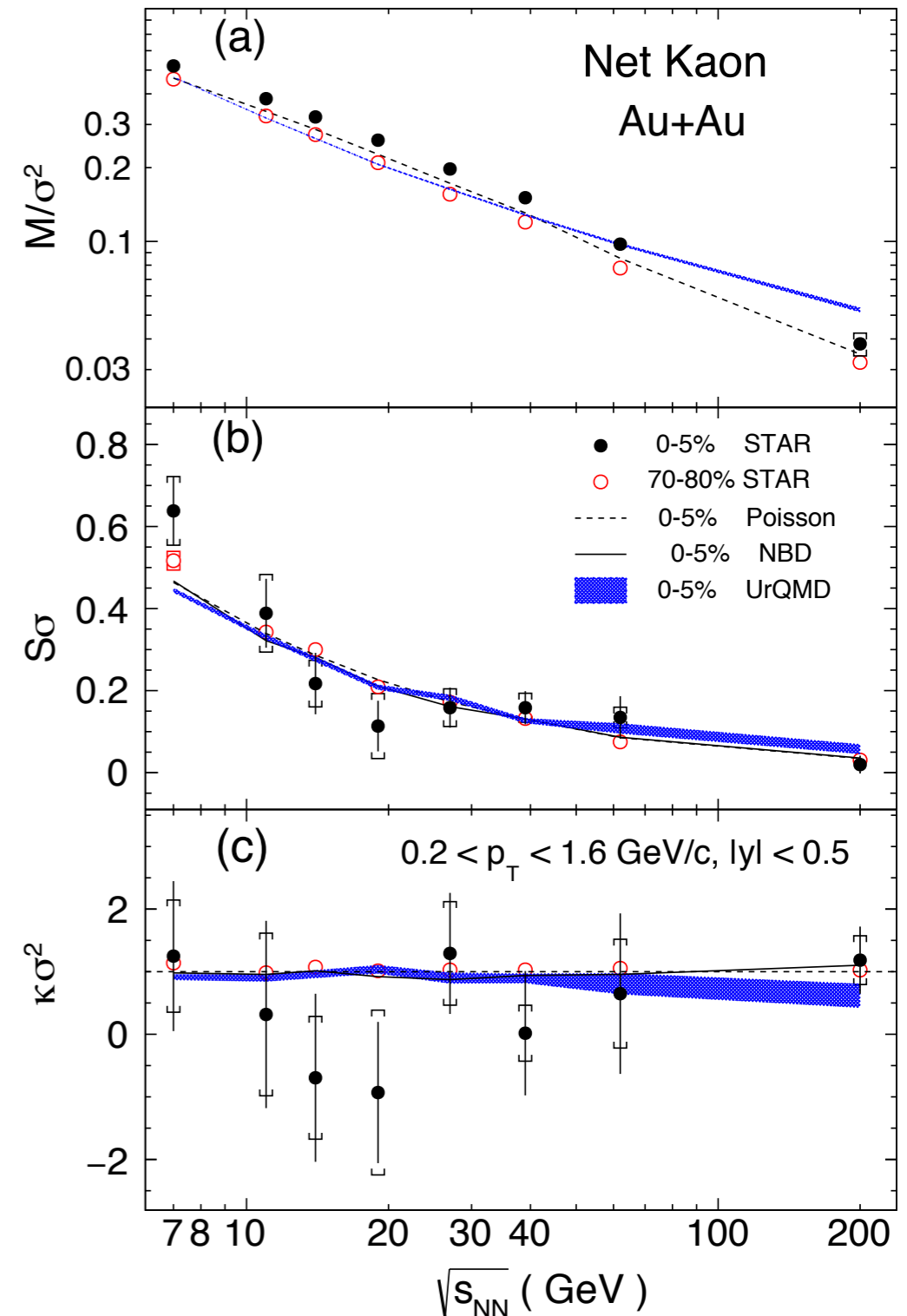
$$S\sigma = \chi_3/\chi_2$$

$$\kappa\sigma^2 = \chi_4/\chi_2^2$$

$$M/\sigma^2 = \chi_1/\chi_2$$

$$S\sigma^3/M = \chi_3/\chi_1$$

Directly compare HRG Model to experiment to identify chemical freeze-out conditions!



STAR Collaboration (Adamczyk, L. et al.) Phys.Lett. B (2018)

Kaon susceptibilities in the HRG Model are defined as:

$$\chi_n^{\text{net-K}} = \sum_{i \in \text{HRG}} \frac{(Pr_{i \rightarrow \text{net-K}})^n S_i^{1-n} d_i}{T^{3-(n-1)} 4\pi^2} \frac{\partial^{n-1}}{\partial \mu_S^{n-1}} \times \left\{ \int_{-0.5}^{0.5} dy \int_{0.2}^{1.6} dp_T \frac{p_T \sqrt{p_T^2 + m_i^2} \text{Cosh}[y]}{(-1)^{B_i+1} + \exp((\text{Cosh}[y] \sqrt{p_T^2 + m_i^2} - (B_i \mu_B + S_i \mu_S + Q_i \mu_Q))/T)} \right\}$$

- ☑ Limits of integration correspond to the acceptance cuts from the experiment
- ☑ Strangeness neutrality imposed on  $\mu_B, \mu_Q, \mu_S$  matches the experimental conditions:

$$\langle n_S \rangle = 0 \quad \langle n_Q \rangle = 0.4 \langle n_B \rangle$$

- ☑ Include feed-down from resonances by utilizing the branching ratios:

$$Pr_{i \rightarrow K_{net}} = Br_{i \rightarrow K_{net}} n_i(K_{net})$$



Is there a quark flavor hierarchy in chemical freeze-out?

What is the effect of additional states in the HRG model?

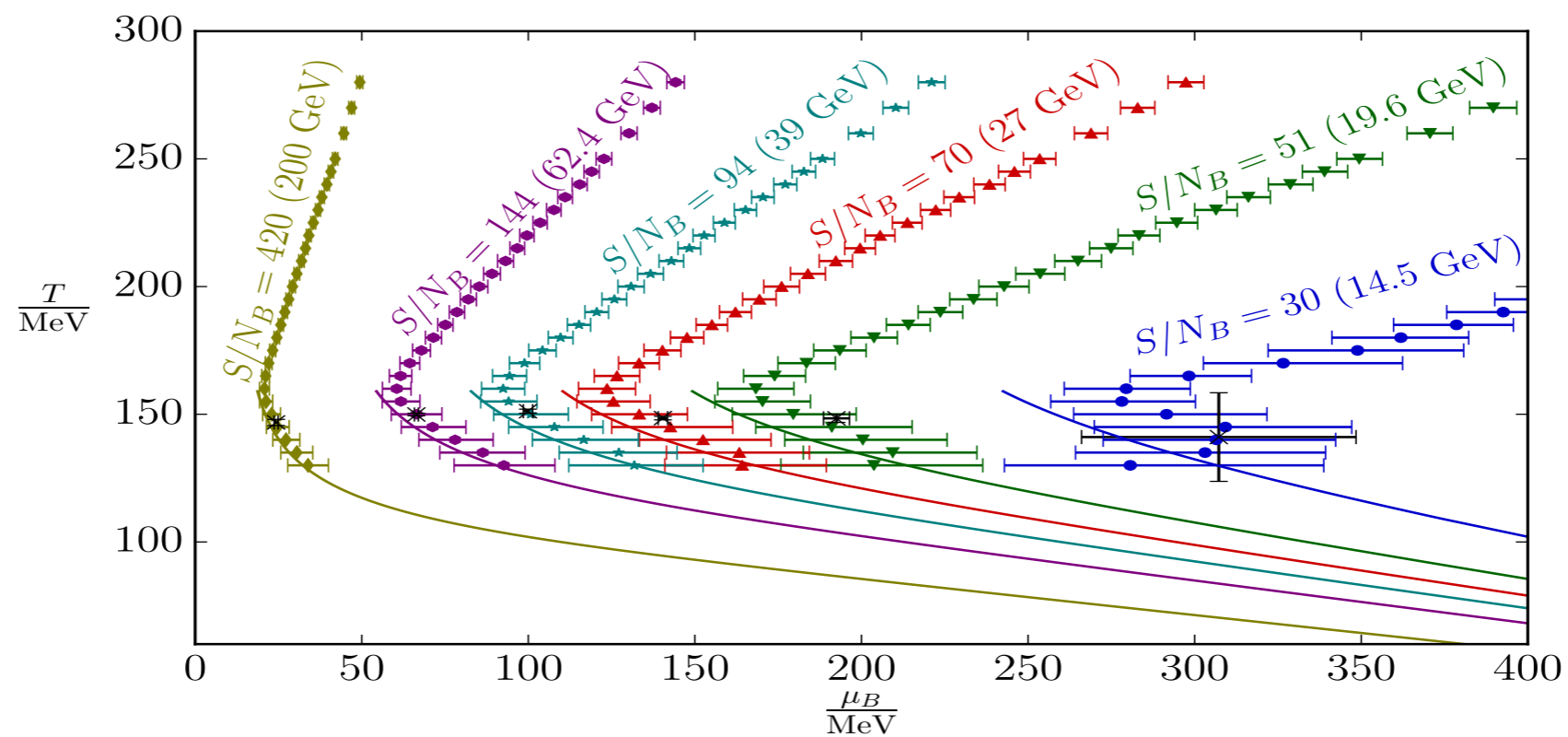
- ➔ Compare the HRG Model with experimental data from RHIC
  - ▶ Calculate  $\chi_1/\chi_2$  for net-kaons in the HRG model, including acceptance cuts and resonance decays
  - ▶ Find  $\chi_1/\chi_2$  along the lattice QCD isentropes
  - ▶ Fit HRG results with experiment to extract freeze-out temperature,  $T_f$
  - ▶ Obtain  $\mu_{B,f}$  from the isentropes

# Lattice QCD Isentropes



In order to extract the  $\{T_f, \mu_{B,f}\}$ , the isentropic trajectories from Lattice QCD are utilized

- ▶ Shows the path of the system across the phase diagram
- ▶  $S/N_B$  is conserved



Guenther, J. et al. Nucl.Phys. A (2017)

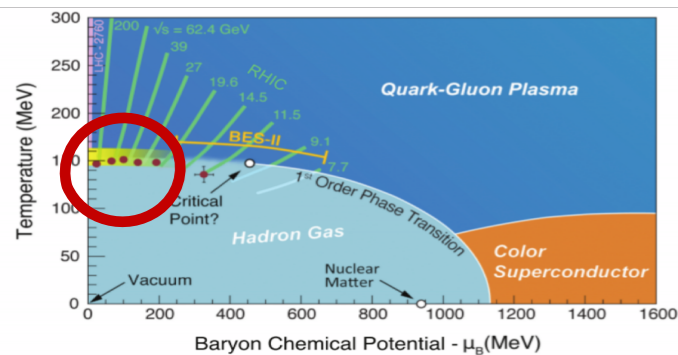
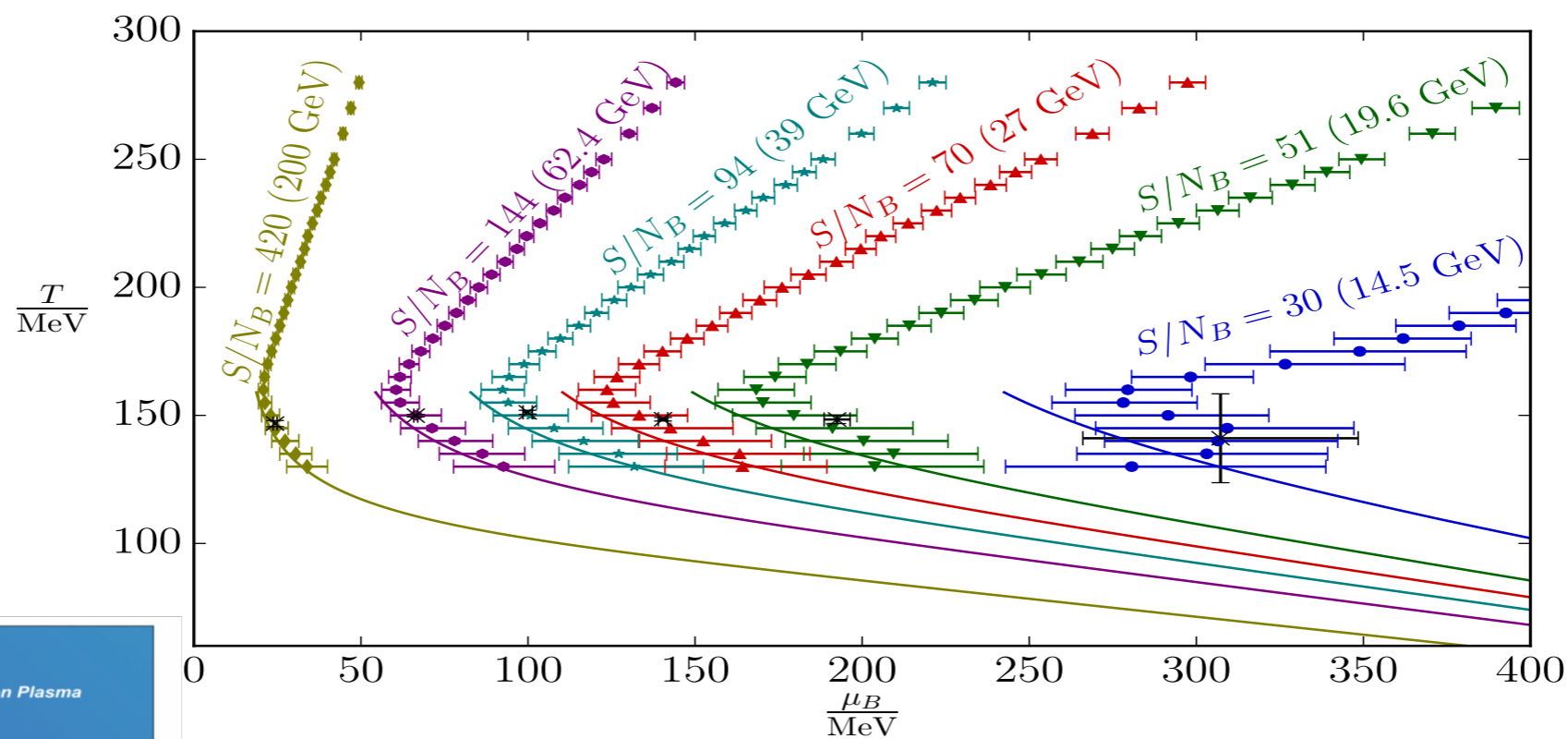


# Lattice QCD Isentropes



In order to extract the  $\{T_f, \mu_{B,f}\}$ , the isentropic trajectories from Lattice QCD are utilized

- ▶ Shows the path of the system across the phase diagram
- ▶  $S/N_B$  is conserved



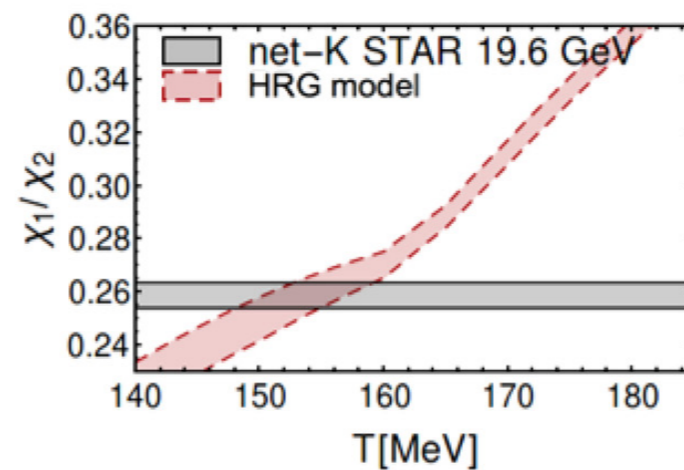
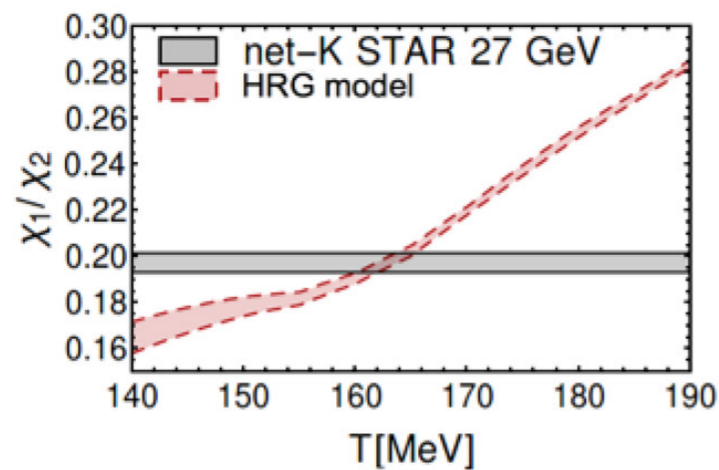
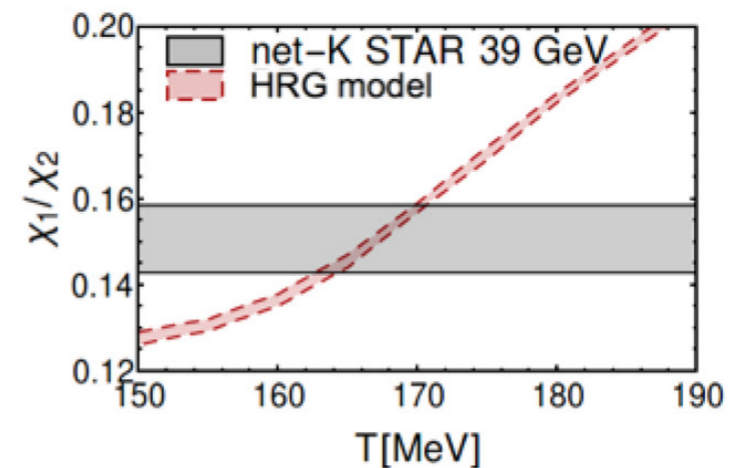
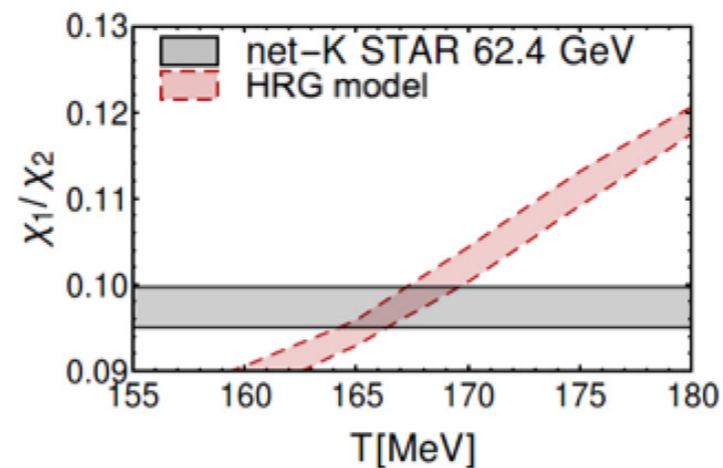
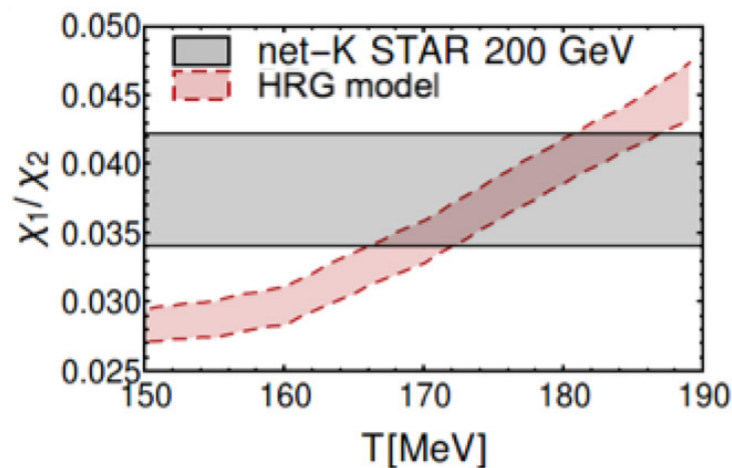
Guenther, J. et al. Nucl.Phys. A (2017)

# Results: Net-kaon fluctuations



Calculate  $\chi_1/\chi_2$  along the isentropes corresponding to the five highest energies of the Beam Energy Scan at RHIC

- ▶ Extract  $T_f$  by identifying the overlap regions



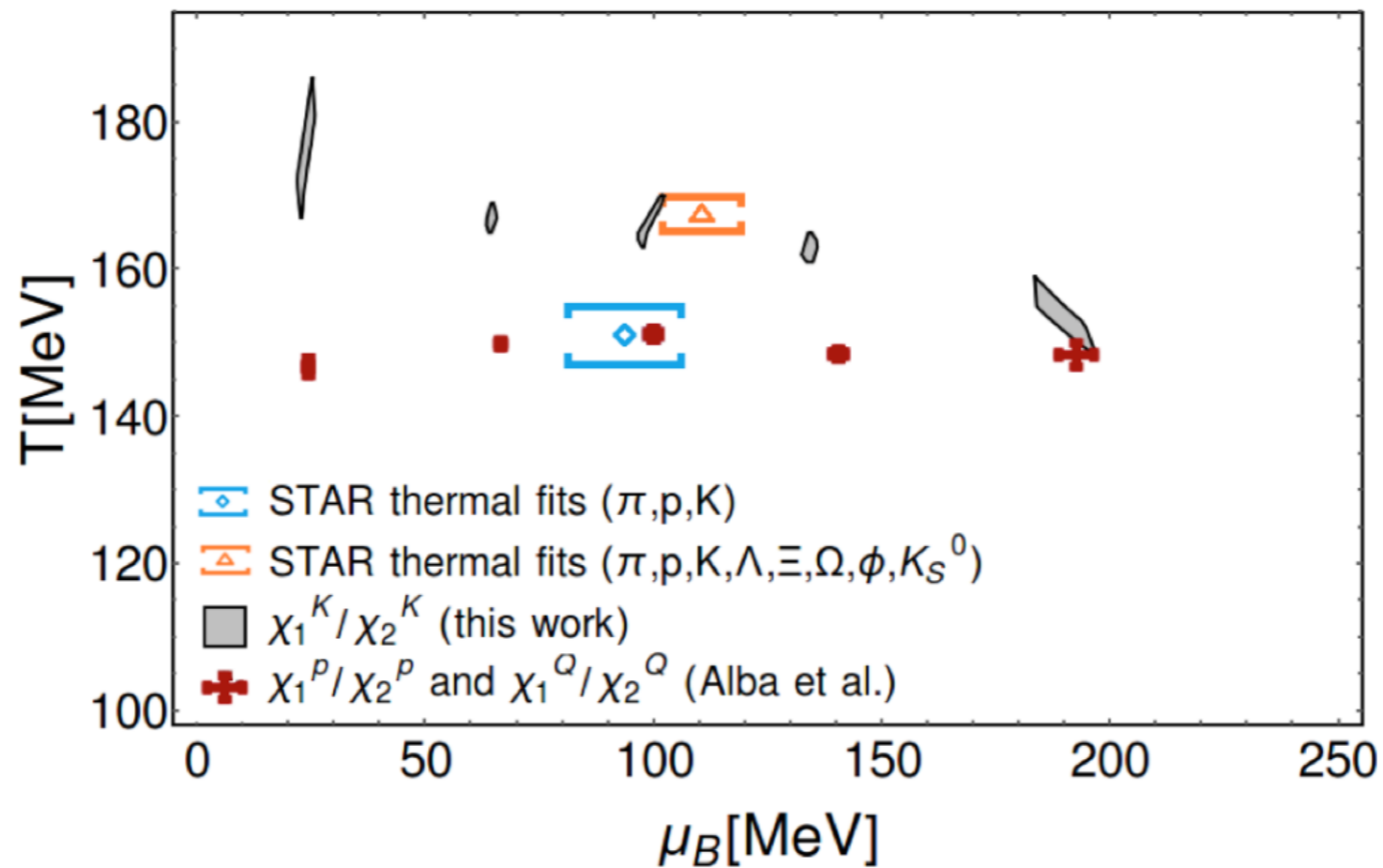
**At 200 GeV:**  
 **$T_f \gtrsim 163$  MeV**

# Results: Phase diagram



Compare the freeze-out parameters for net-kaon to:

- ▶ light freeze-out (combined fit of net-proton and net-electric charge)
- ▶ thermal fits from the experiment



*R. Bellwied, JS, et al., PRC (2019)*

Recall the pressure in the HRG Model:  $\frac{P}{T^4} = \frac{1}{VT^3} \sum_i \ln Z_i(T, V, \vec{\mu})$

Different PDG lists will yield different results for the freeze-out parameters

- ▶ **PDG2012: 319 species**
- ▶ **PDG2016: 608 species** (includes many more particles in the strange sector)
- ▶ **PDG2016+: 738 species** (includes all experimentally observed particles, i.e. \*, \*\*, \*\*\*, \*\*\*\*)

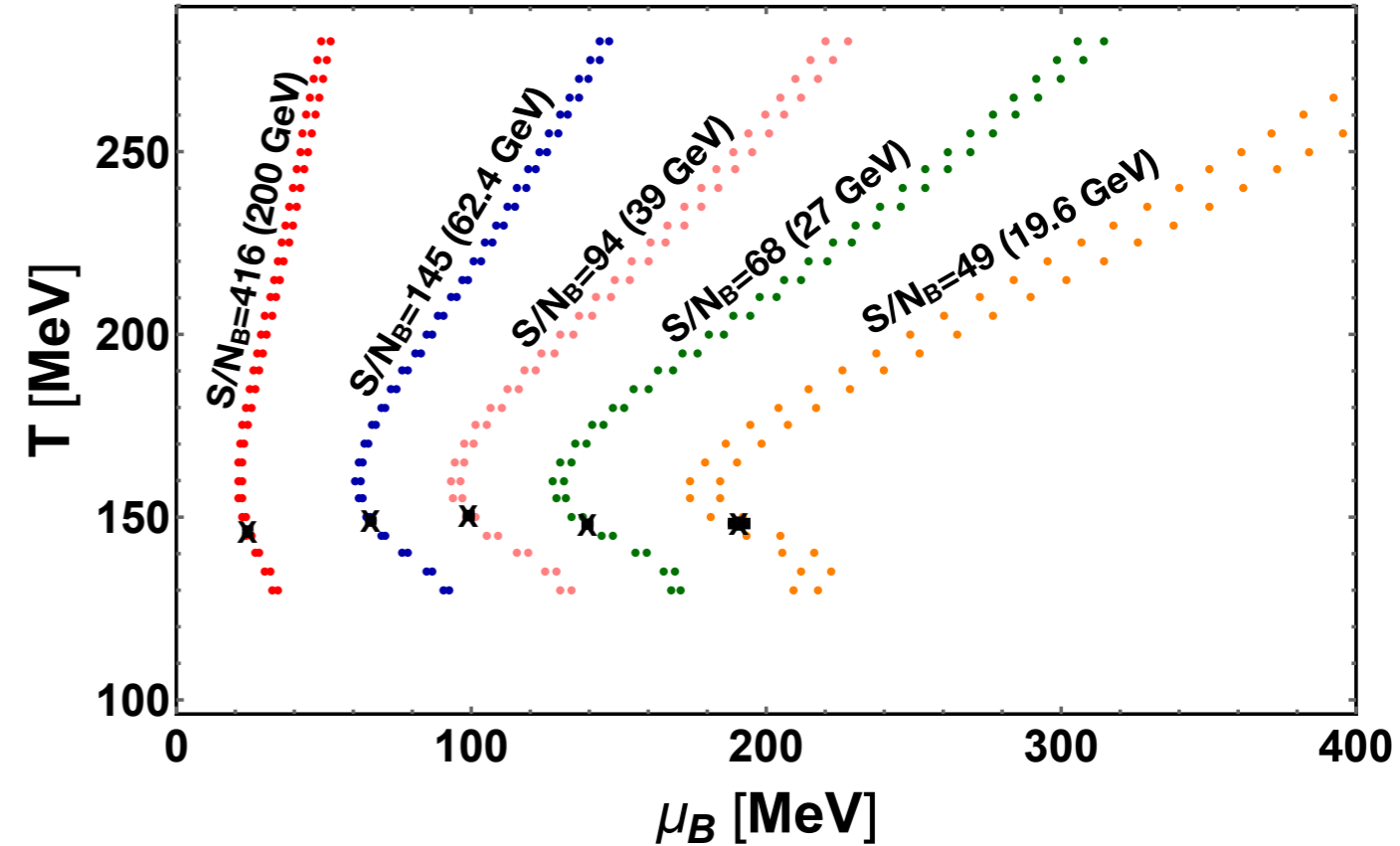
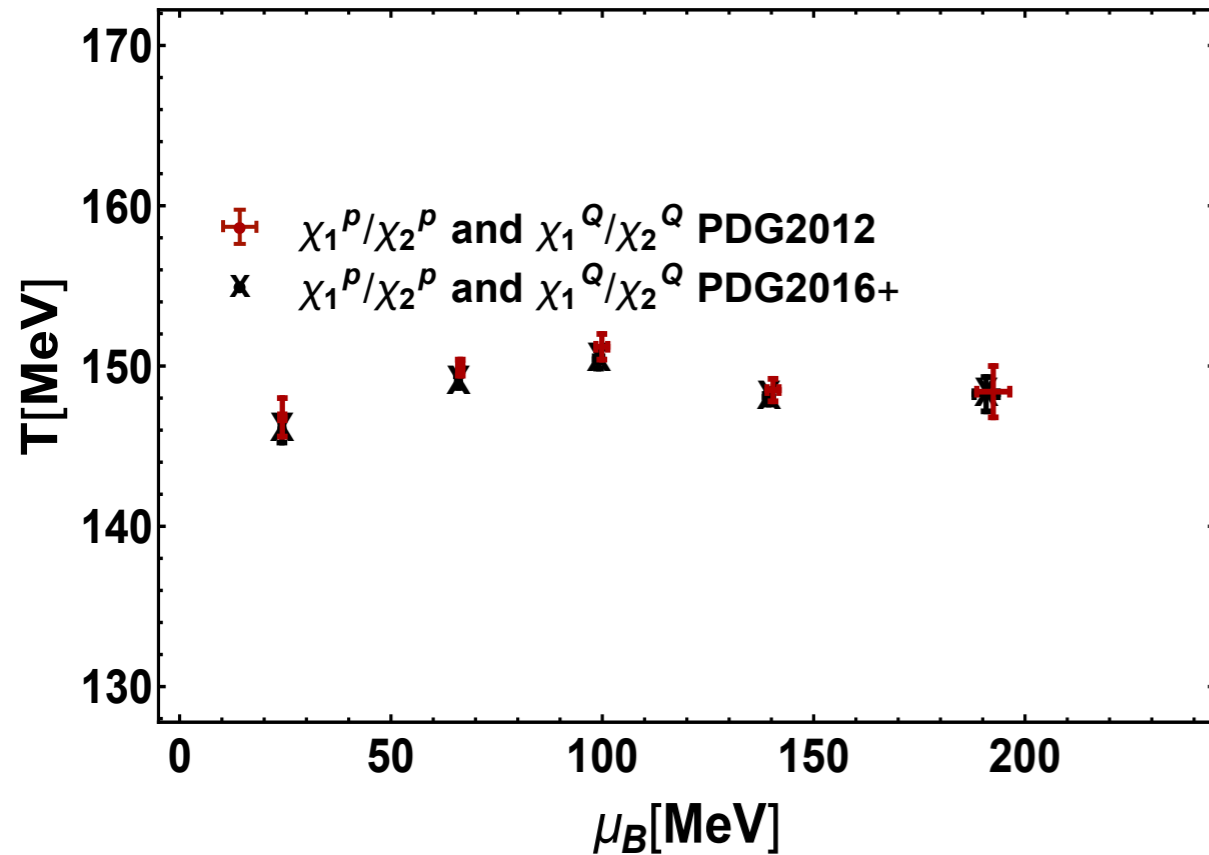
$p$	$1/2^+$	****
$n$	$1/2^+$	****
$N(1860)$	$5/2^+$	**
$N(1875)$	$3/2^-$	***
$\Delta(1232)$	$3/2^+$	****
$\Delta(1750)$	$1/2^+$	*

*P. Alba et al, PRD (2017); C. Patrignani et al. (Particle Data Group), Chin. Phys. C (2016)*

# Lattice QCD Isentropes with 2016+



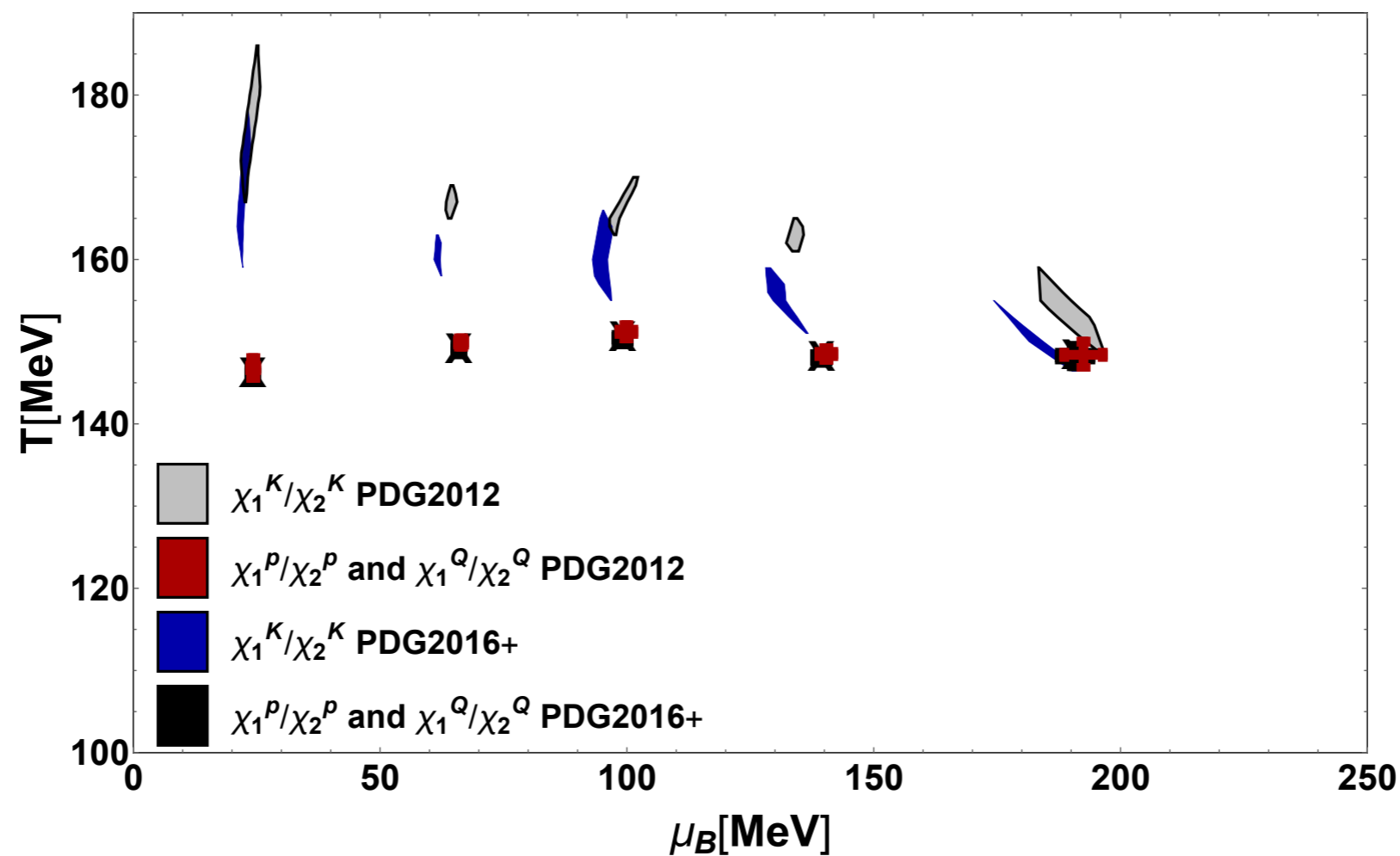
Calculate new isentropes from light particle freeze-out parameters determined by combined fit of net-p and net-Q with PDG2016+



# Results: PDG2012 and PDG2016+



Compare the freeze-out parameters for the kaons and light particles for the different lists in order to determine the effect of the number of resonant states:

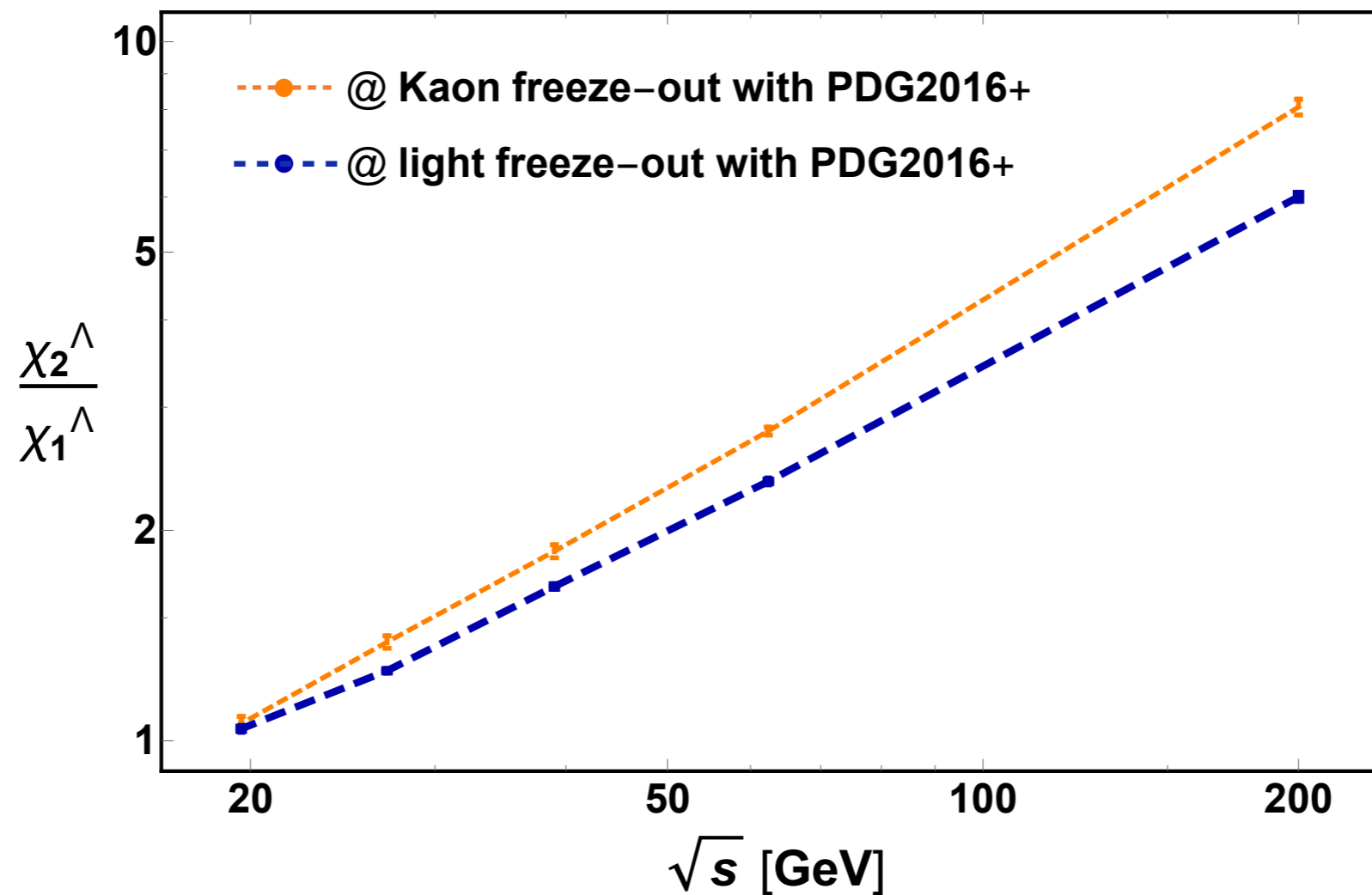


With the inclusion of more states in the HRG Model the kaon freeze-out temperature is decreased, but the separation remains

# Results: Net-lambda predictions with 2016+



Calculate fluctuations for net- $\Lambda$  using the kaon and light hadron freeze-out parameters.

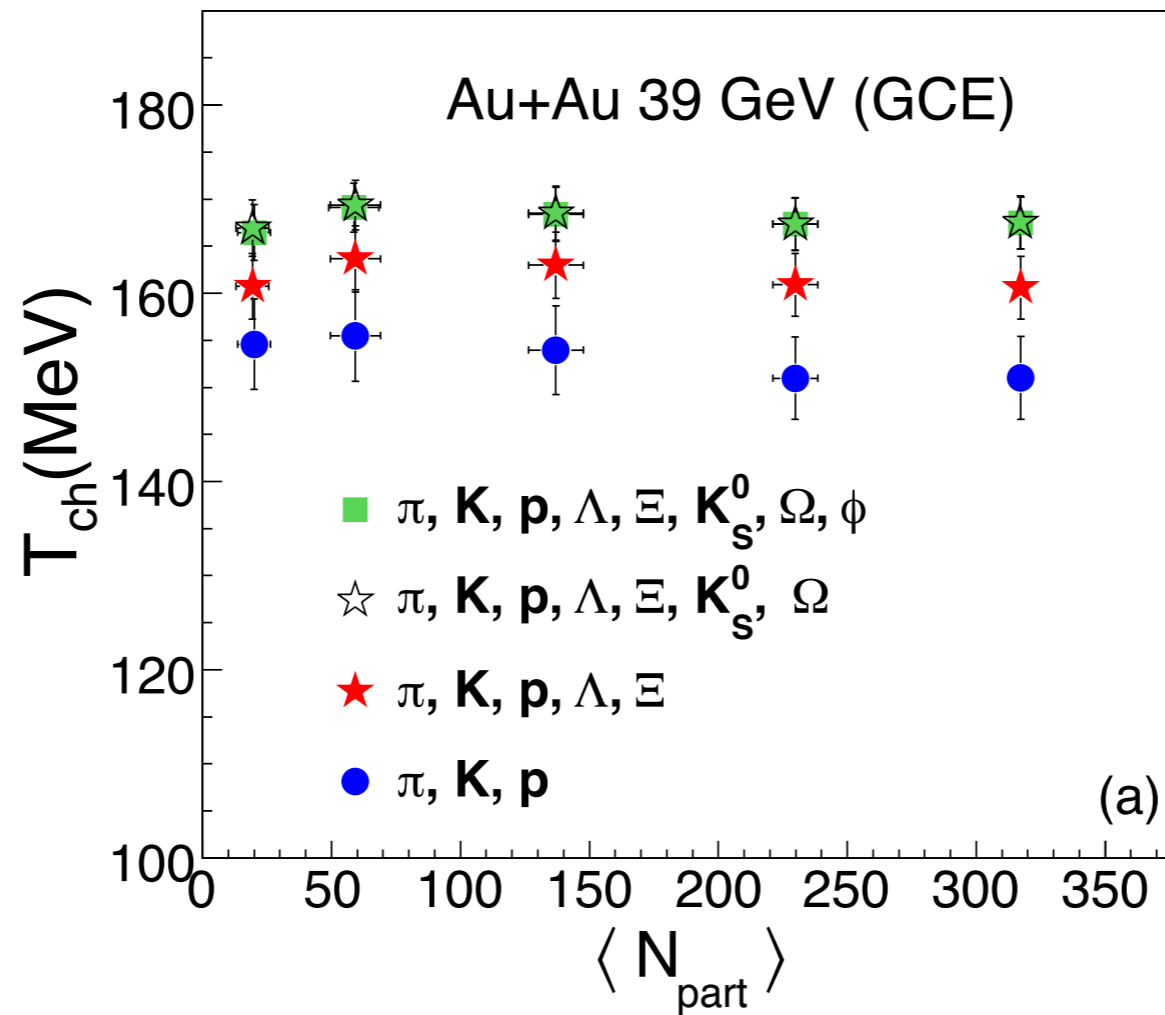


- The net-kaon fluctuation data from the STAR collaboration cannot be reproduced in the HRG model by using the **freeze-out** parameters obtained from the combined fit of  $\chi^P_1/\chi^P_2$  and  $\chi^Q_1/\chi^Q_2$ .
- At the highest collision energy, the kaon freeze-out with PDG2012 is above  $T=163$  MeV, about **10-15 MeV higher** than the light hadrons.
- With the inclusion of **more strange resonances** in the HRG Model, the kaon freeze-out temperature becomes  $T \gtrsim 160$  MeV at  $\sqrt{s_{NN}} = 200$  GeV.



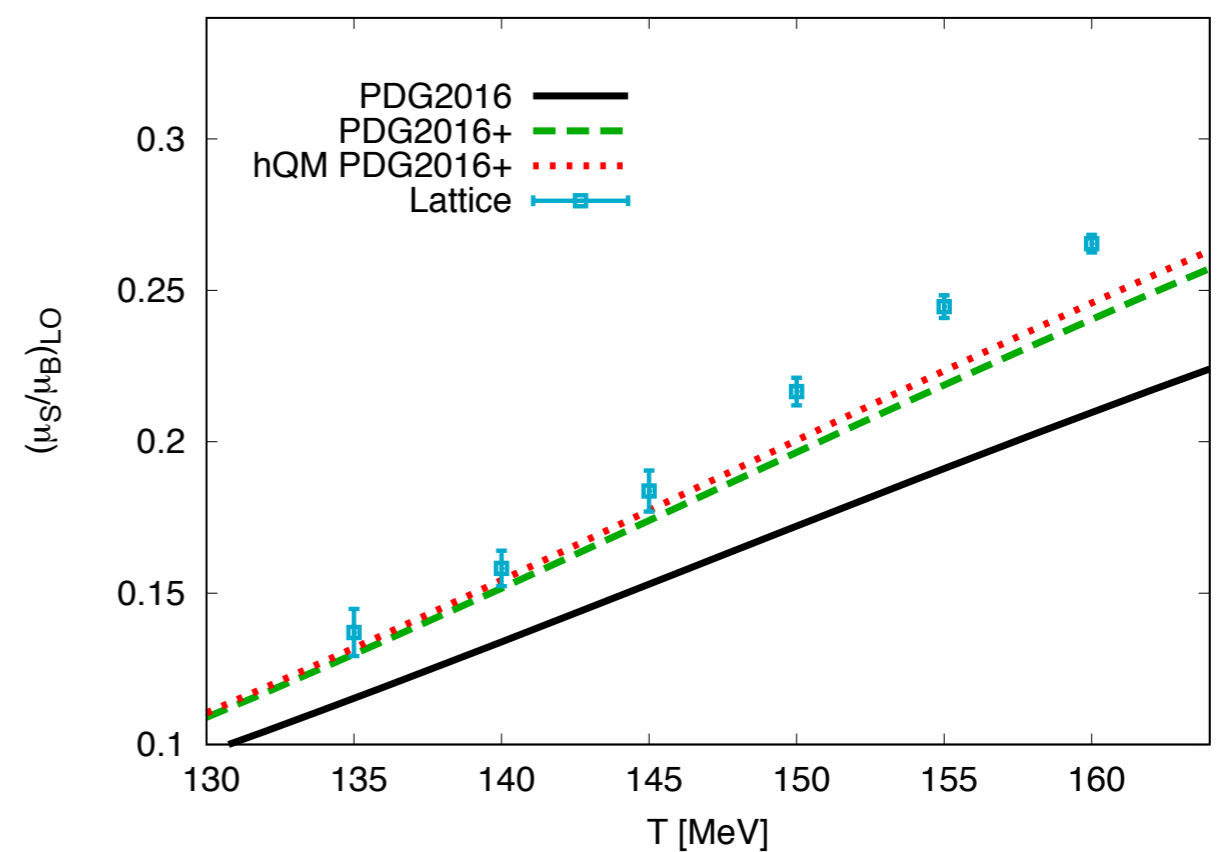
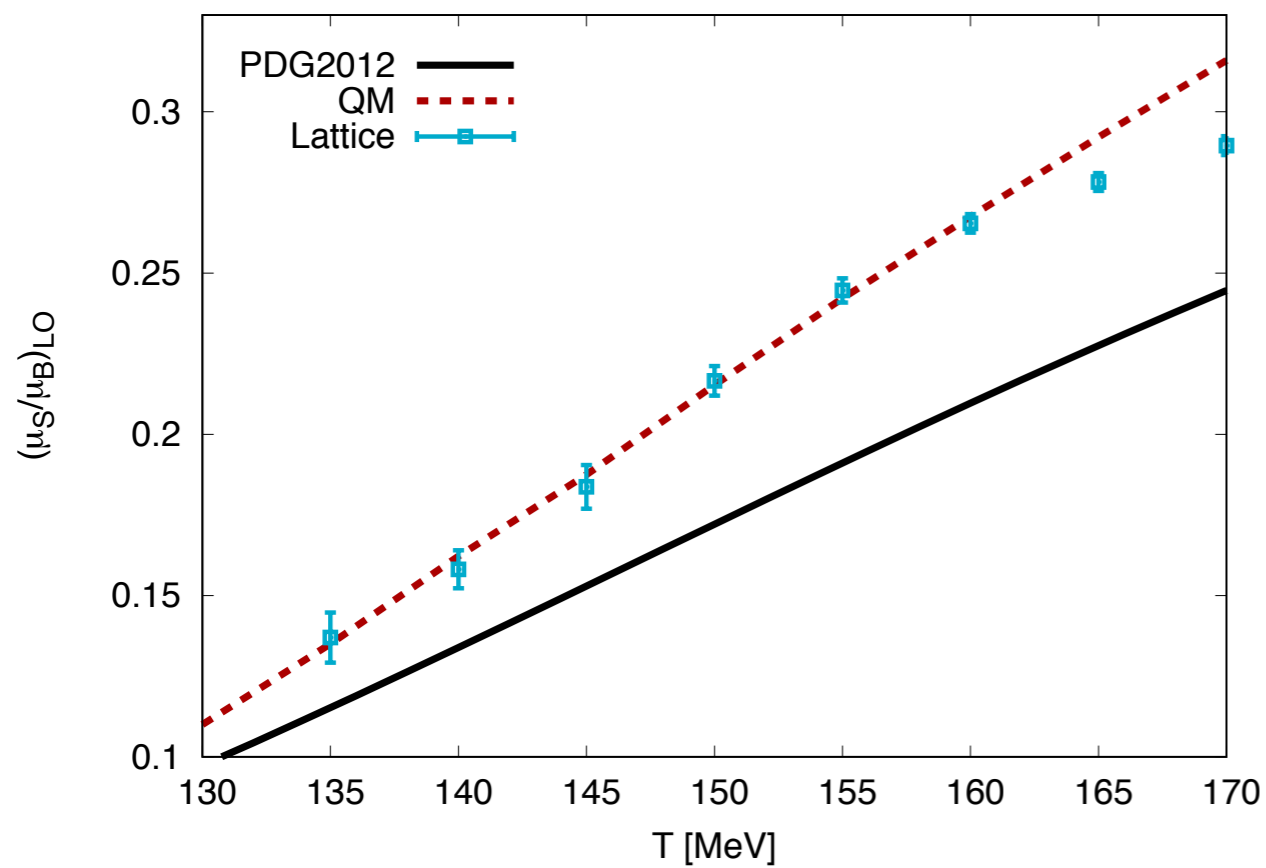
**Back-up slides**

# STAR THERMUS fits of particle yields



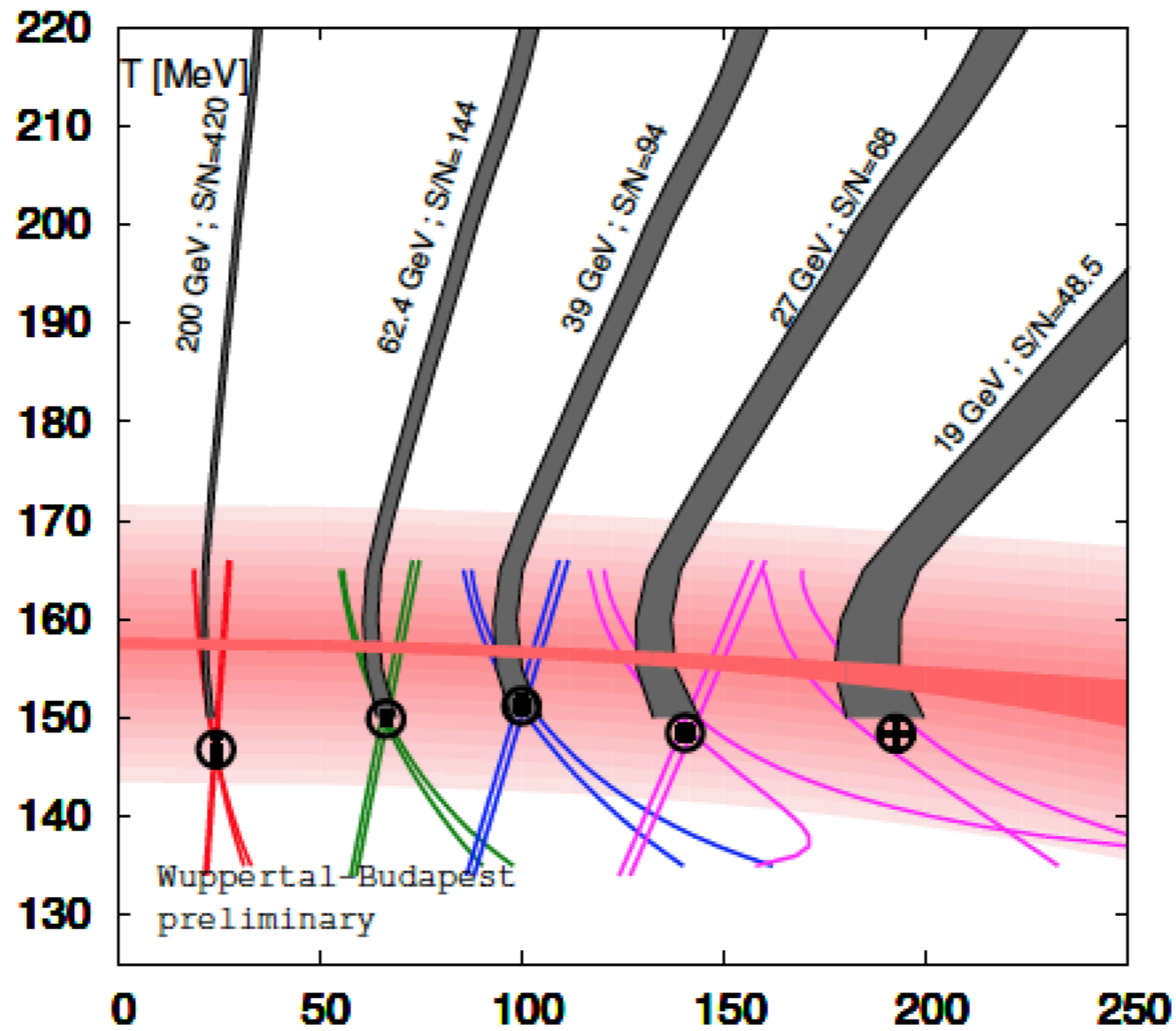
arXiv: 1701.07065

# Comparison of HRG & Lattice results



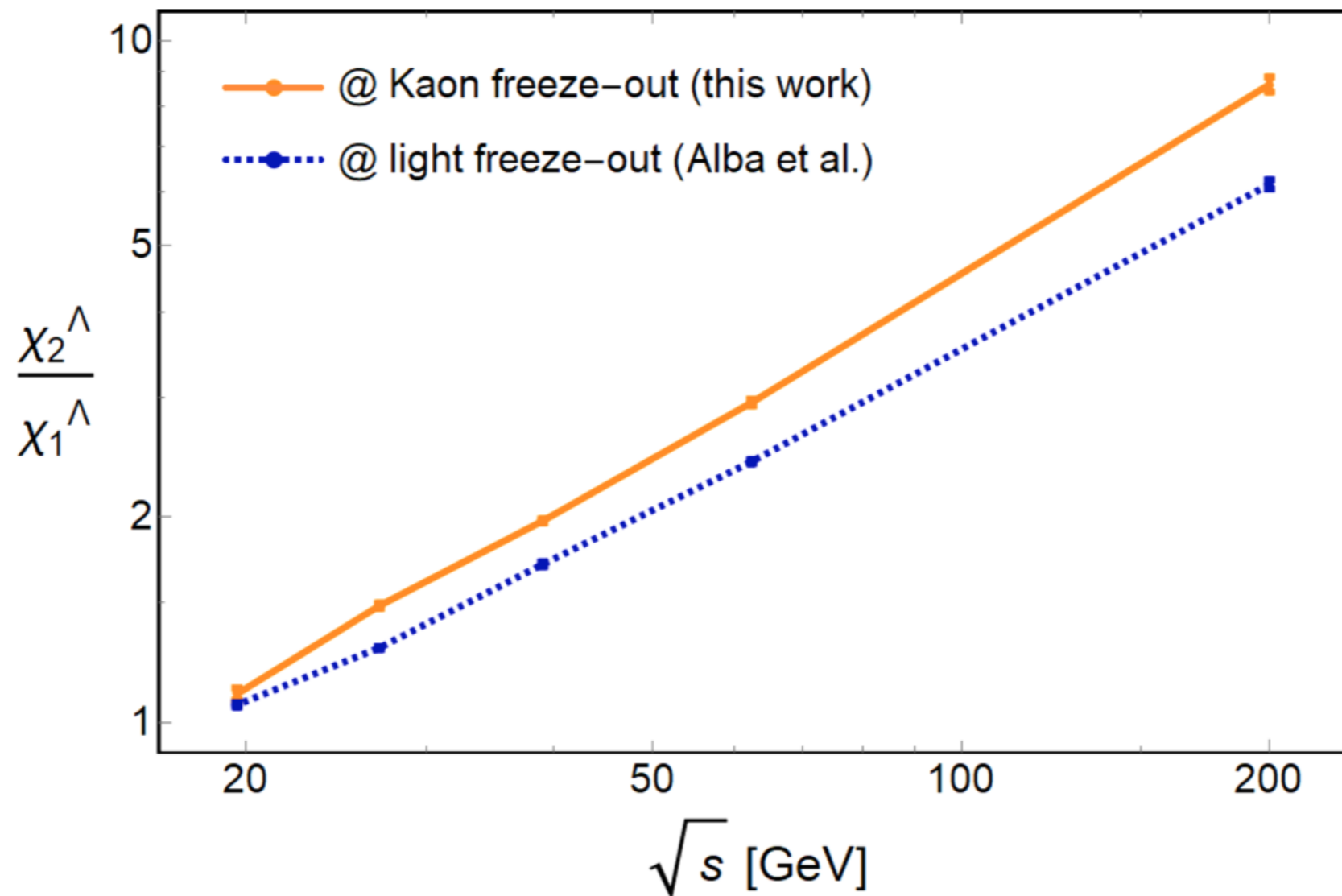
arXiv: 1702.01113

# Freeze-out from net-p & net-Q



arXiv: 1601.02367

# Net-lambda predictions with PDG2012



arXiv: 1805.00088