

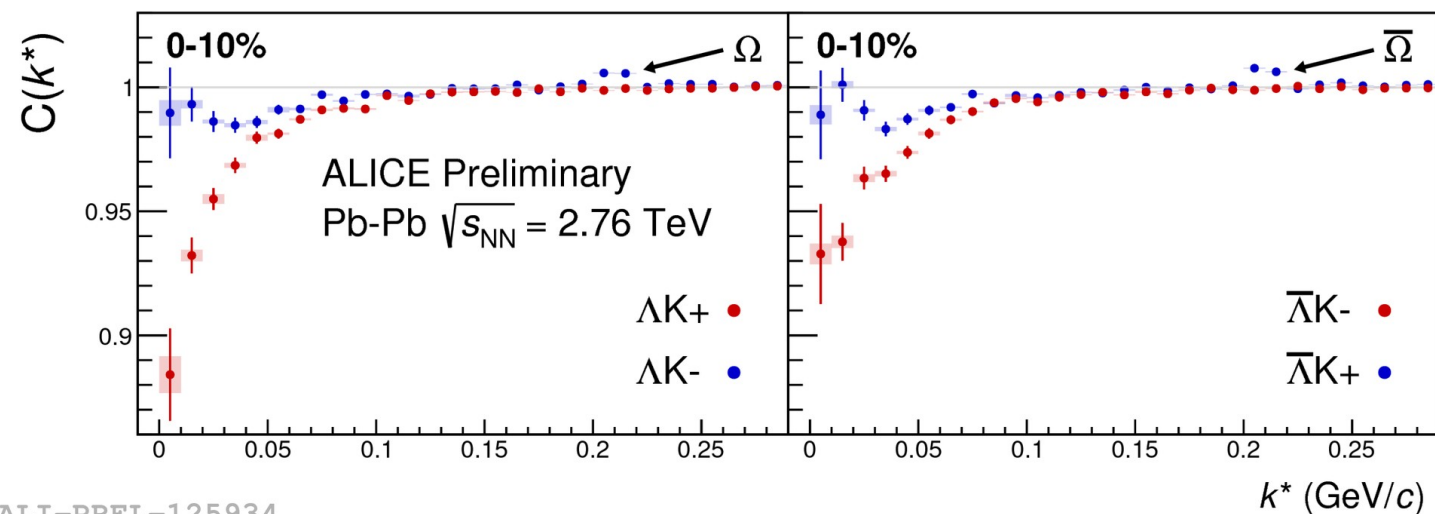
ΛK and $\Xi^- K^+$ femtoscopy in Pb-Pb collisions at 2.76 TeV from ALICE



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on behalf of the ALICE Collaboration

- Study femtoscopic ΛK correlations
 - ◆ Result from strong final-state interactions (FSI)
- Characterize ΛK pair emission region
- Extract ΛK interaction scattering parameters
 - ◆ **Never before measured**
- $\Xi^- K^\pm$ study to investigate difference in ΛK^+ and ΛK^-

ΛK^+	$uds + u\bar{s}$	$S=0$
ΛK^-	$uds + \bar{u}s$	$S=-2$
$\Xi^- K^+$	$dss + u\bar{s}$	$S=-1$
$\Xi^- K^-$	$dss + \bar{u}s$	$S=-3$



ALI-PREL-125934

- Exploit two-particle correlations of hadrons
- Probe space-time freeze-out structure at femtometer scale (10^{-15} m)
- Measure “regions of homogeneity” ^[1]
- **Unique environment to measure nuclear scattering parameters**

Theory

- Koonin-Pratt Equation ^[2,3]

$$C(\mathbf{P}, \mathbf{k}^*) = \int S_{\mathbf{P}}(\mathbf{r}^*) |\Psi(\mathbf{k}^*, \mathbf{r}^*)|^2 d^3 r^*$$

- $S_{\mathbf{p}}(\mathbf{r}^*)$ = source distribution
- $\Psi(\mathbf{k}^*, \mathbf{r}^*)$ = two-particle wave-function
- $k^* = |\mathbf{k}^*|$ = momentum of one particle in pair rest frame

Experiment

$$C(k^*) = \frac{A(k^*)}{B(k^*)}$$

- $A(k^*)$: signal distribution (same-event)
- $B(k^*)$: reference distribution (mixed events)

- Lednický and Lyuboshitz formulation [4]
 - ◆ Isotropic Gaussian profile & effective range approximation

$$\Psi(\mathbf{k}^*, \mathbf{r}^*) = e^{-i\mathbf{k}^* \cdot \mathbf{r}^*} + f^S(k^*) \frac{e^{ik^* r^*}}{r^*}$$

$$f^S(k^*) = \left(\frac{1}{f_0^S} + \frac{1}{2} d_0^S k^{*2} - ik^* \right)^{-1}$$

$$\sigma = 4\pi |f^2|$$

- Nice analytic form

$$C(k^*) = 1 + \sum_S \rho_S \left[\frac{1}{2} \left| \frac{f^S(k^*)}{R} \right|^2 \left(1 - \frac{d_0^S}{2\sqrt{\pi}R} \right) + \frac{2\Re f^S(k^*)}{\sqrt{\pi}R} F_1(2k^*R) - \frac{\Im f^S(k^*)}{R} F_2(2k^*R) \right]$$

- ◆ f_0^S – complex scattering length
- ◆ d_0^S – effective range of interaction
- ◆ R – source size

- Measured CF is combination of primary signal and transformed residuals [5]
- λ_{ij} control strength of contribution

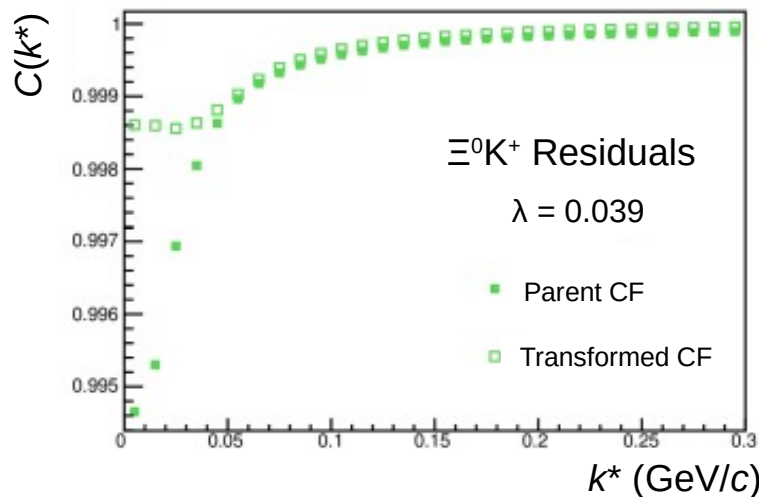
- Modeling parent CF
 - ◆ Assume same R, f_0^S, d_0^S as ΛK system
 - ◆ $\Xi^- K^+$ data or Coulomb-only simulation

$$C_{\text{measured}}(k_{\Lambda K}^*) = \mathcal{N} \left(1 + \lambda'_{\Lambda K} [C_{\Lambda K}(k_{\Lambda K}^*) - 1] + \sum_{i,j} \lambda'_{ij} [C_{ij}(k_{\Lambda K}^*) - 1] \right)$$

$$\lambda'_{ij} = \lambda_{\text{Fit}} \lambda_{ij}$$

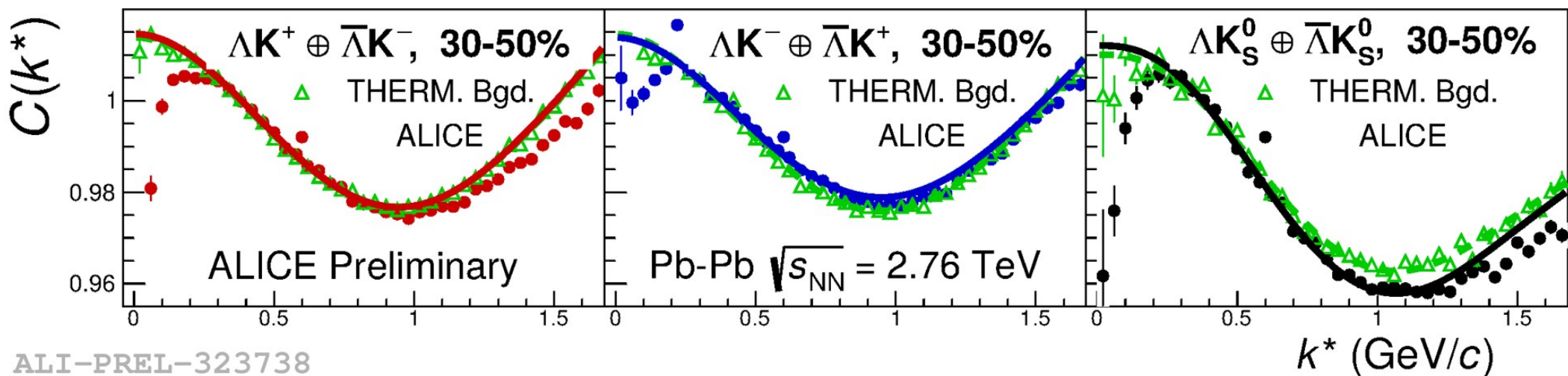
$$\sum_{i,j} \lambda'_{ij} = \lambda_{\text{Fit}} \sum_{i,j} \lambda_{ij} = \lambda_{\text{Fit}}$$

$$C_{ij}(k_{\Lambda K}^*) \equiv \frac{\sum_{k_{ij}^*} C_{ij}(k_{ij}^*) T(k_{ij}^*, k_{\Lambda K}^*)}{\sum_{k_{ij}^*} T(k_{ij}^*, k_{\Lambda K}^*)}$$



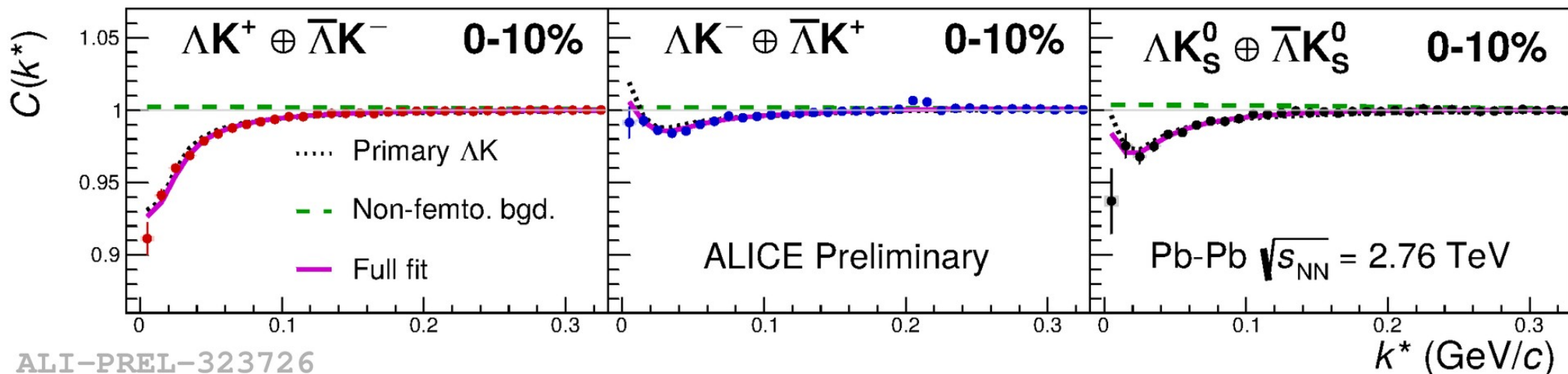
Pair System	<u>λ-factor</u>
Primary	0.527
$\Sigma^0 K^+$	0.111
$\Xi^0 K^+$	0.039
$\Xi^- K^+$	0.050
Other	0.226
Fakes	0.048

- Significant non-femtoscopic background at large k^*
- Effect due primarily to particle collimation associated with elliptic flow [6]
 - Results from mixing events with unlike event-plane angles
- THERMINATOR 2 simulation to model and account for in fit



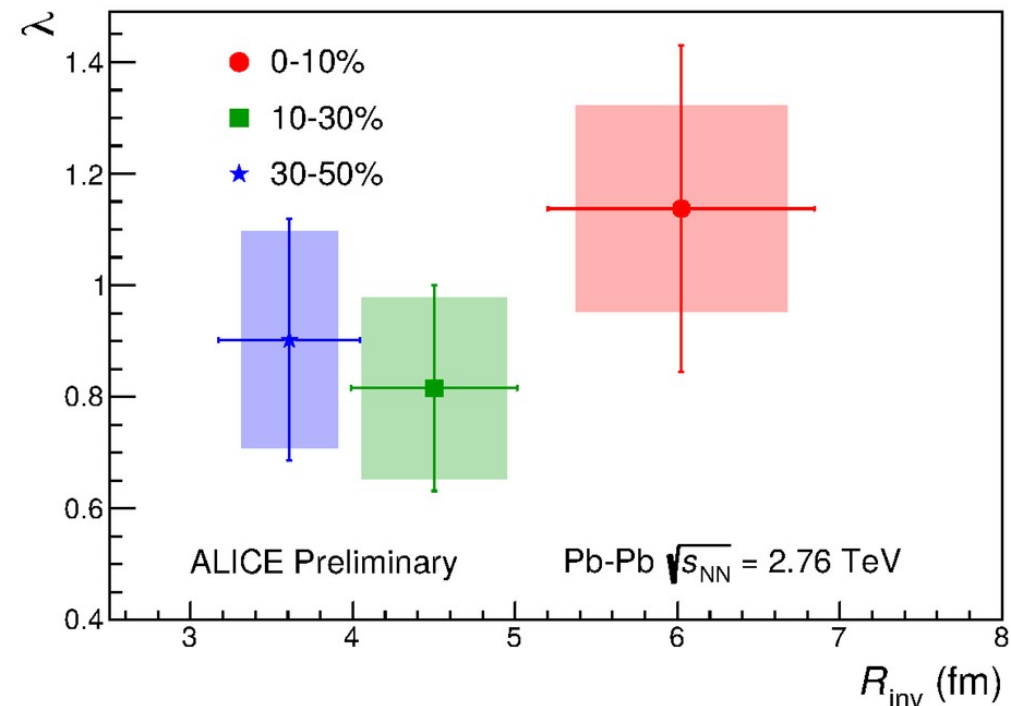
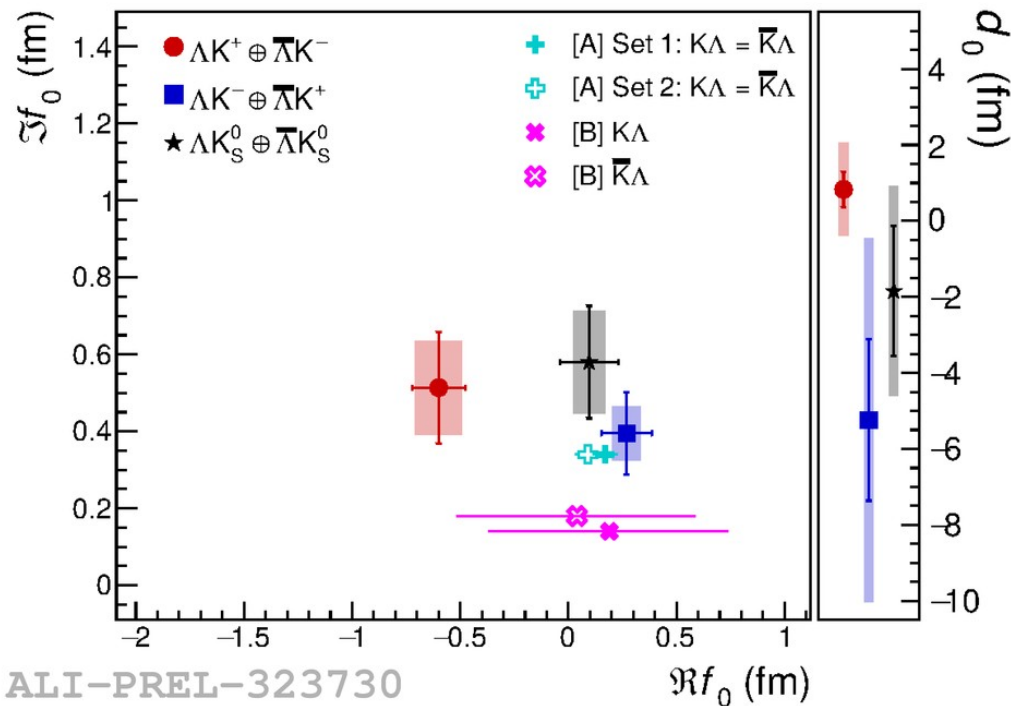
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- All analyses fit simultaneously across all centralities
 - ◆ For each centrality R and λ_{Fit} shared among all systems
 - ◆ Unique set of scattering parameters for each ΛK charge combination (ΛK^+ , ΛK^- , ΛK^0_S)
- Residual contributions from resonance feed-down included
- Non-femtoscopic background and momentum resolution corrections applied



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- $\Re f_0$ is **positive** for ΛK^- and ΛK_s^0 → **attractive** strong interaction
- $\Re f_0$ is **negative** for ΛK^+ → **repulsive** strong interaction

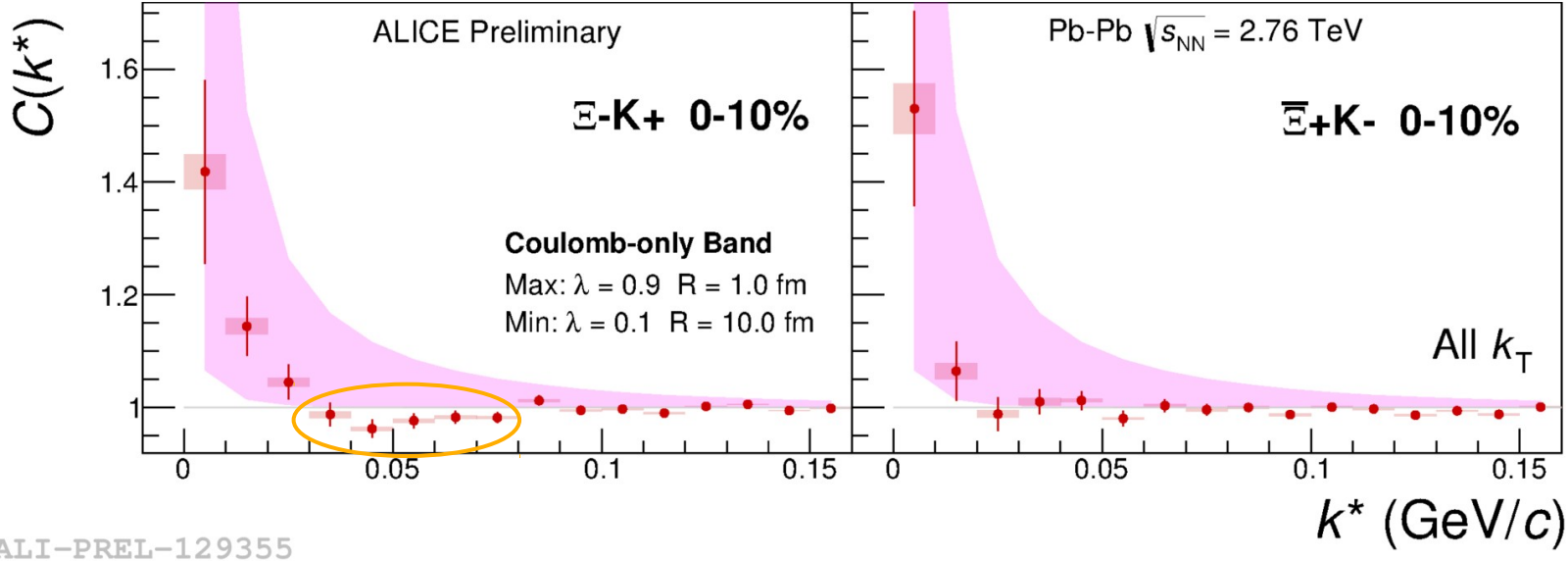


$\Xi^- K^\pm$ Analysis

Ξ^-K^+ Data vs. Coulomb Only

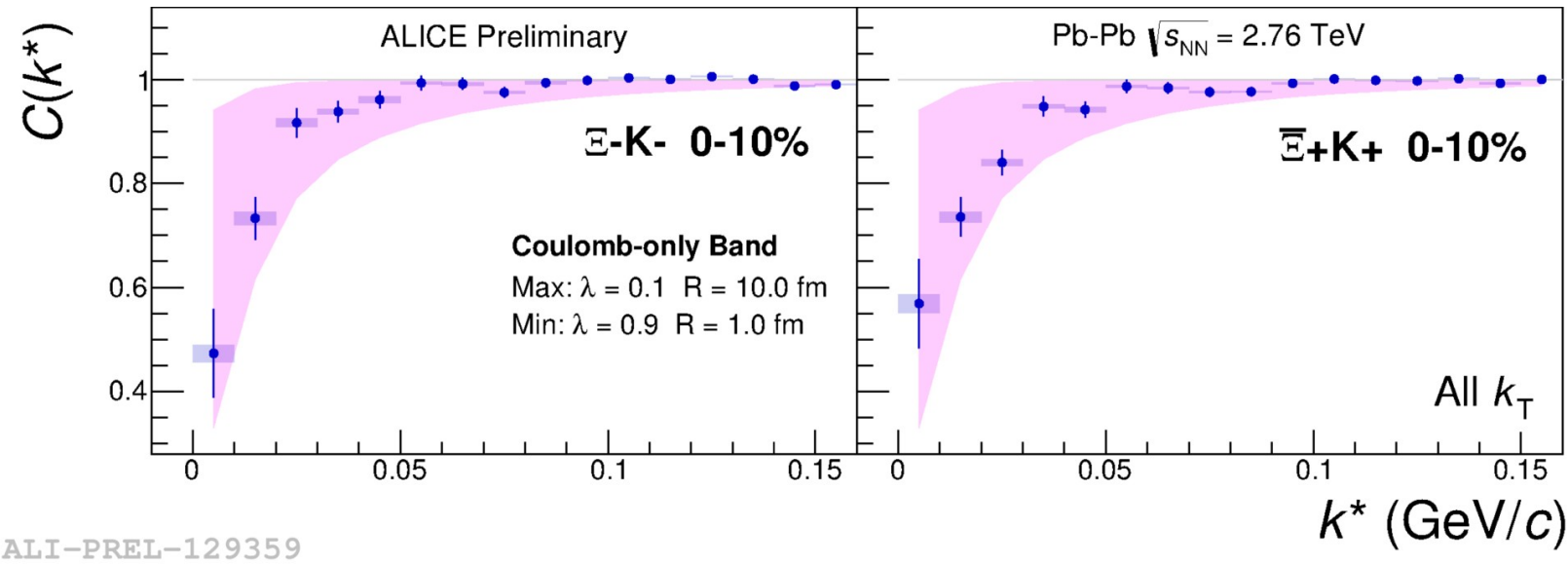
➤ **Magenta** = Coulomb-only band

- Spanned by two Coulomb-only CFs



➤ Ξ^-K^+ cannot be described with only Coulomb

- **Strong force showing?**

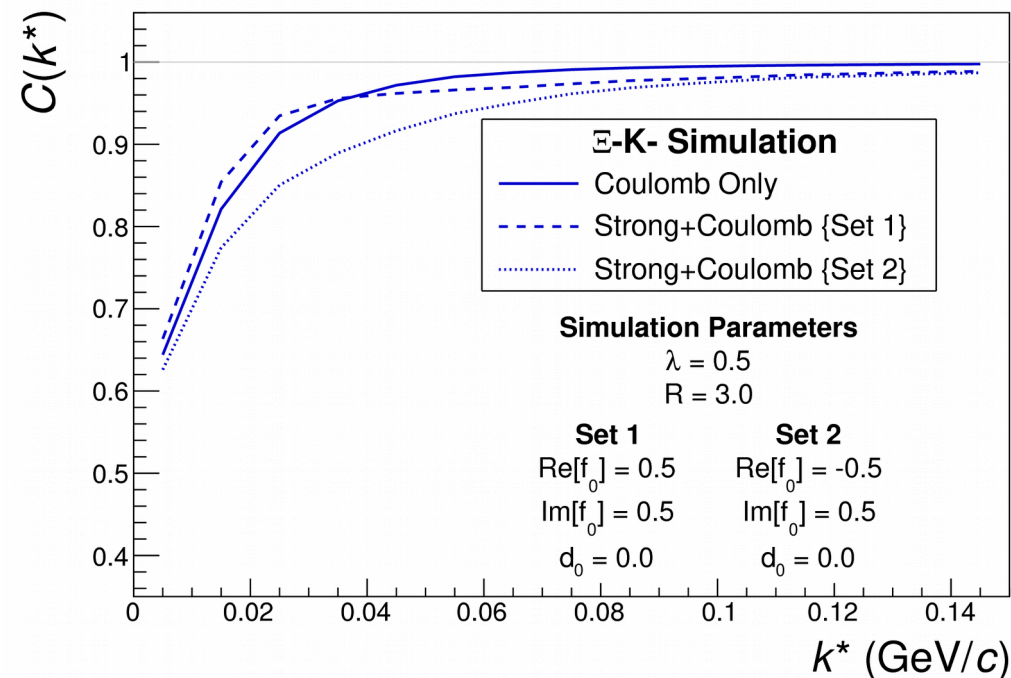
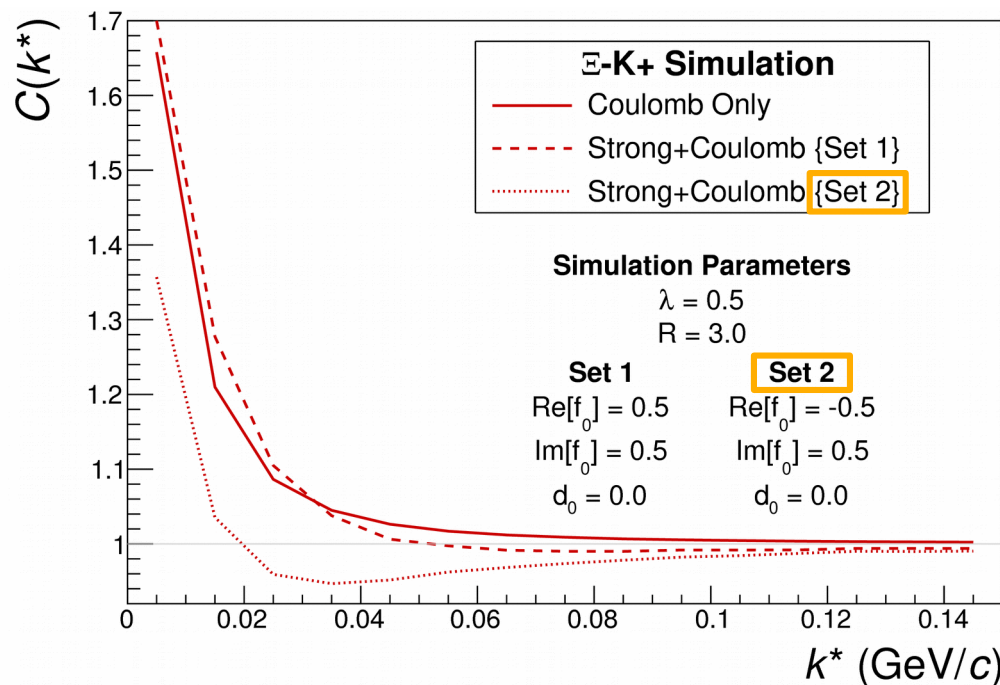


➤ Inclusion of strong and Coulomb interactions

- ◆ No nice analytic form
- ◆ Must integrate by hand

$$\Psi_{\mathbf{k}^*}(\mathbf{r}^*) = e^{i\delta_c} \sqrt{A_c(\eta)} \left[e^{-i\mathbf{k}^* \cdot \mathbf{r}^*} F(-i\eta, 1, i\xi) + f_c(k^*) \frac{\tilde{G}(\rho, \eta)}{r^*} \right]$$

$$f_c(k^*) = \left[\frac{1}{f_0} + \frac{1}{2} d_0 k^{*2} - \frac{2}{a_c} h(\eta) - ik^* A_c(\eta) \right]^{-1}$$



- ΛK femtoscopic analysis presented for Pb-Pb collisions at 2.76 TeV
 - ◆ First measurement of ΛK scattering parameters
 - ◆ Pair emission source radii extracted for 0-10%, 10-30%, and 30-50% centralities
- $\Xi^- K^\pm$ femtoscopic analysis introduced for Pb-Pb collisions at 2.76 TeV
 - ◆ Goal to help explain striking difference in ΛK^+ and ΛK^- correlations observed at low k^*
 - ◆ A Coulomb-only fit cannot describe the data



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Thank you

- [1] S. Akkelin and Y. Sinyukov, “The HBT-interferometry of expanding sources,” *Physics Letters* **B356** (1995) 525 – 530.
- [2] S. E. Koonin, “Proton Pictures of High-Energy Nuclear Collisions,” *Phys. Lett.* **B70** (1977) 43–47.
- [3] S. Pratt, T. Csorgo, and J. Zimanyi, “Detailed predictions for two pion correlations in ultrarelativistic heavy ion collisions,” *Phys. Rev.* **C42** (1990) 2646–2652.
- [4] R. Lednicky and V. L. Lyuboshits, “Final State Interaction Effect on Pairing Correlations Between Particles with Small Relative Momenta,” *Sov. J. Nucl. Phys.* **35** (1982) 770.
- [5] A. Kisiel, H. Zbroszczyk, and M. Szymaski, “Extracting baryon-antibaryon strong interaction potentials from $p\bar{\Lambda}$ femtosopic correlation functions,” *Phys. Rev.* **C89** no. 5, (2014) 054916, arXiv:1403.0433 [nucl-th].
- [6] A. Kisiel, “Non-identical particle correlation analysis in the presence of non-femtoscopic correlations,” *Acta Physica Polonica B* **48** (04, 2017) 717.
- [7] A. Kisiel, “Non-identical particle correlation analysis in the presence of non-femtoscopic correlations,” *XII Workshop on Particle Correlations and Femtoscopy*, 12-16 June 2017, Nikhef, Amsterdam, The Netherlands. Conference Talk.
- [8] M. A. Lisa, S. Pratt, R. Soltz, and U. Wiedemann, “Femtoscopic in relativistic heavy ion collisions,” *Ann. Rev. Nucl. Part. Sci.* **55** (2005) 357–402, arXiv:nucl-ex/0505014 [nucl-ex].

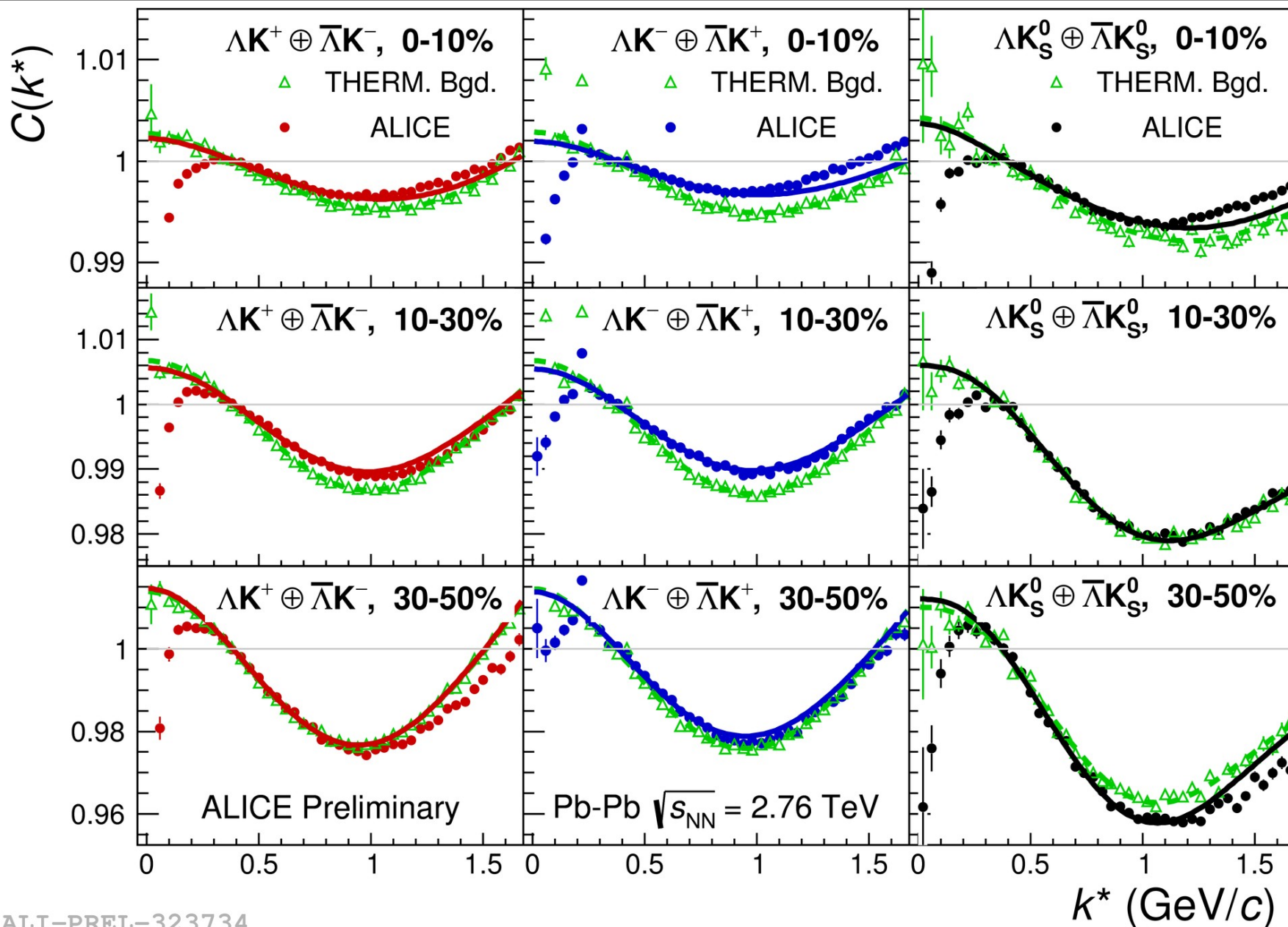


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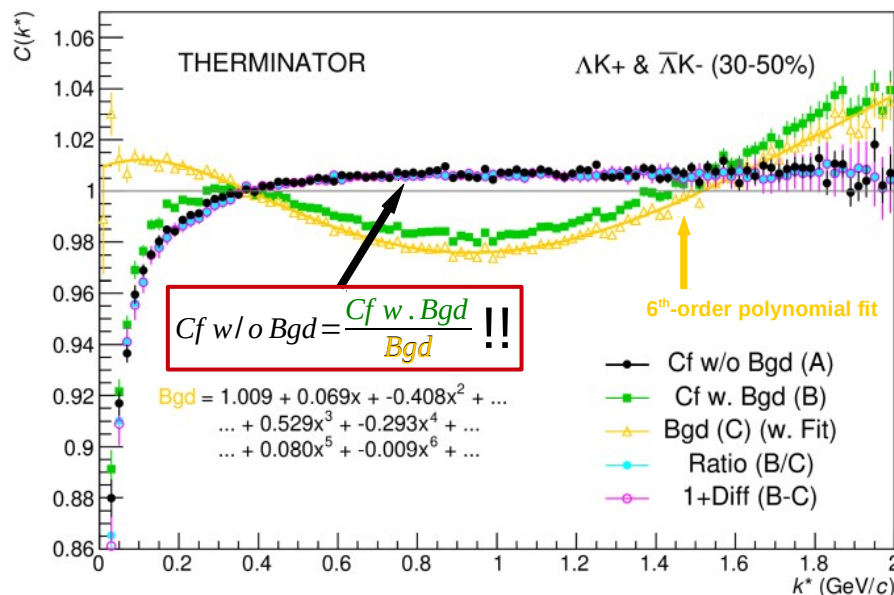
BACKUP



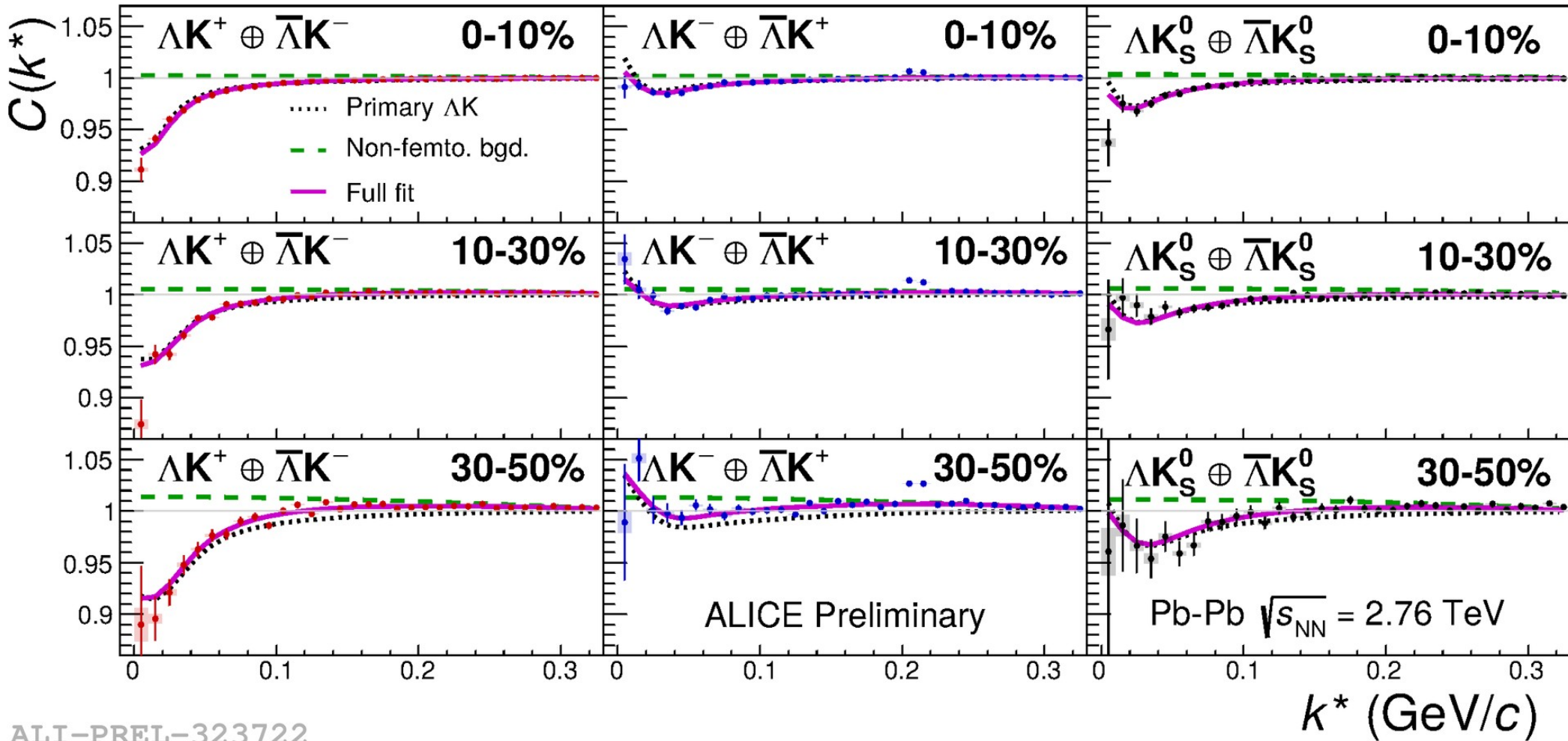
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- THERMINATOR 2: THERMal heavy IoN geneATOR 2
 - ◆ Statistical hadronization in relativistic heavy-ion collisions
 - ◆ Any freeze-out hypersurface + expansion velocity field can be implemented
- Demonstrates background is scale factor

$$Cf_{w/o\ Bgd} = \frac{Cf_w \cdot Bgd}{Bgd} \longrightarrow Cf_{th} = \frac{Cf_{exp}}{F_{Bgd}} \longrightarrow Cf_{exp} = Cf_{th} \cdot F_{Bgd}$$



Simulation Only:
Interaction achieved by assuming scattering parameters, and weighting the numerators in the simulation



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- Expect asymmetry μ_{out} in the outward direction
- Hydrodynamic response on higher m_T particles
 - ◆ confines them to smaller homogeneity regions
 - ◆ pushes them further in the out direction
- Within 1D model used, a non-zero μ_{out} induces larger extracted source radii

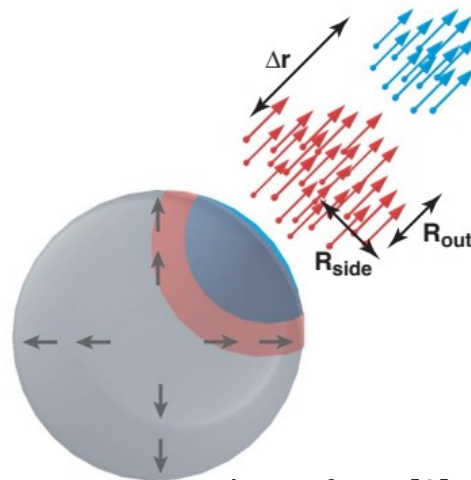
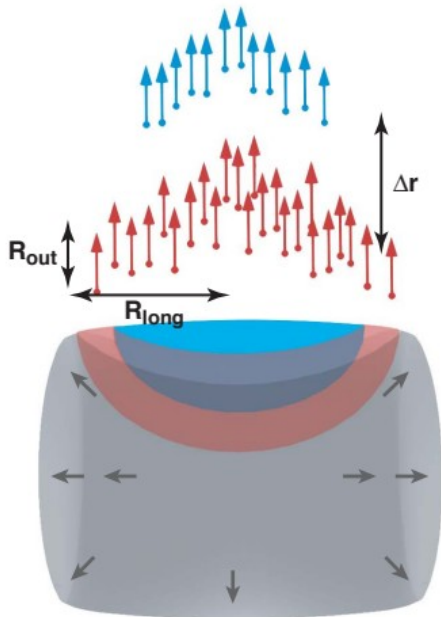


Figure from [8]

$$S_{ab}(\mathbf{r}) \propto \exp\left(-\frac{[r_{out} - (\mu_{a,out} - \mu_{b,out})]^2}{2(R_{a,out}^2 + R_{b,out}^2)}\right) \times \dots$$

$$\times \exp\left(-\frac{r_{side}^2}{2(R_{a,side}^2 + R_{b,side}^2)}\right) \times \dots$$

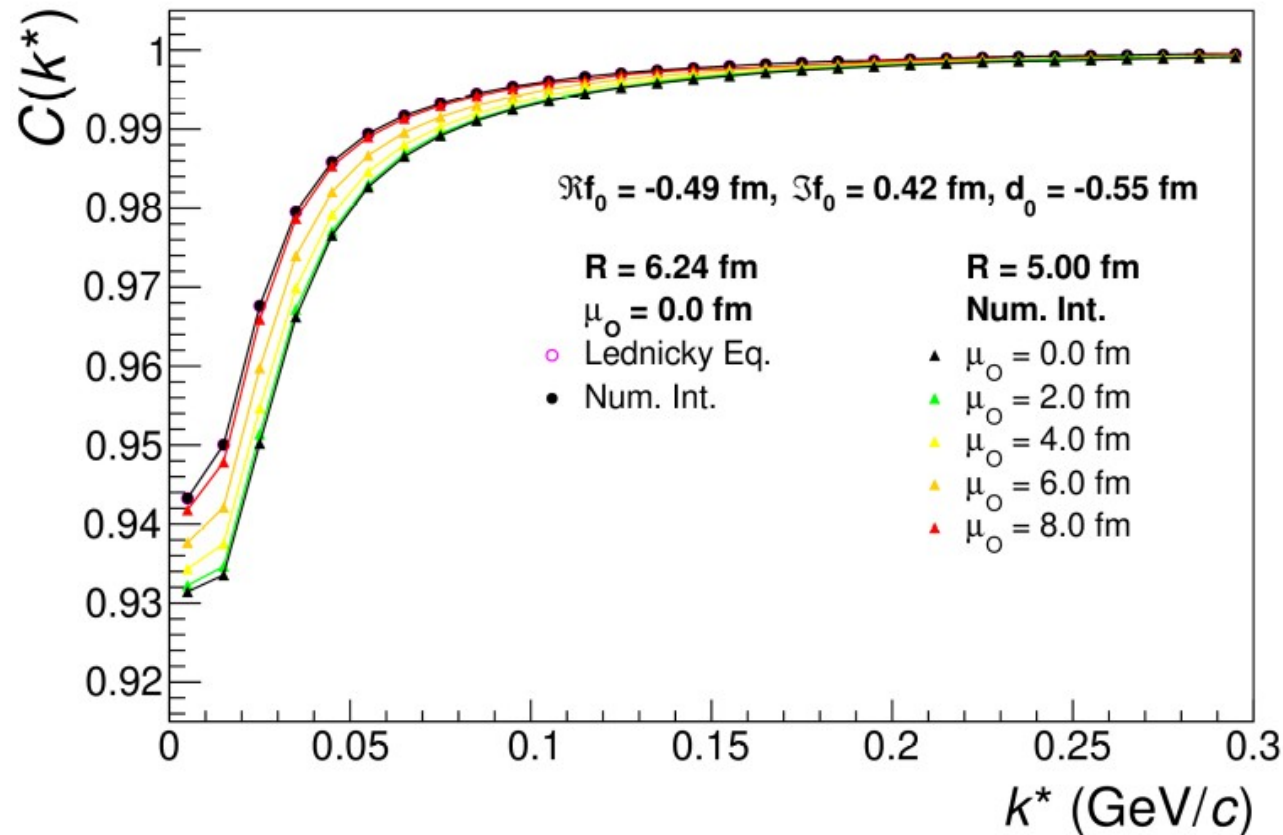
$$\times \exp\left(-\frac{r_{long}^2}{2(R_{a,long}^2 + R_{b,long}^2)}\right)$$

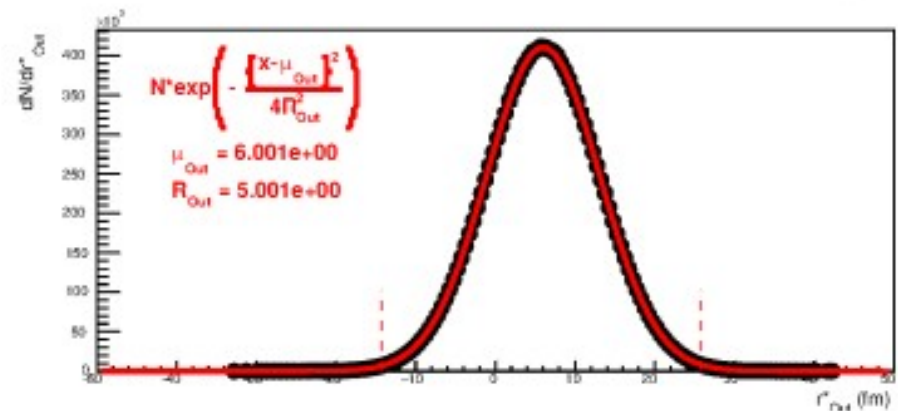
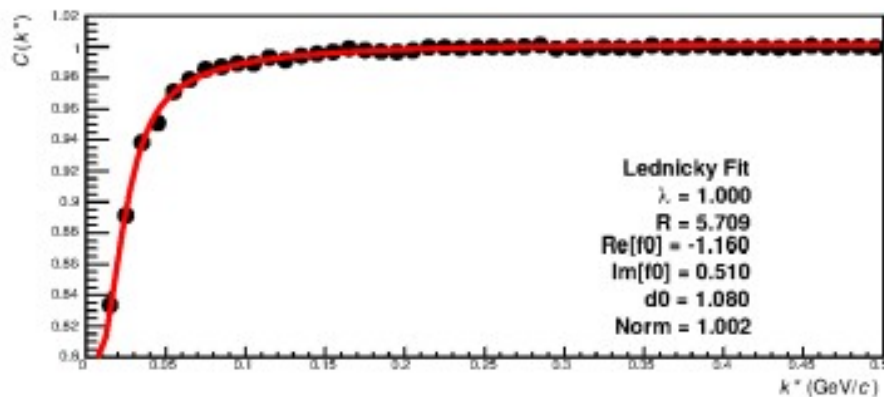
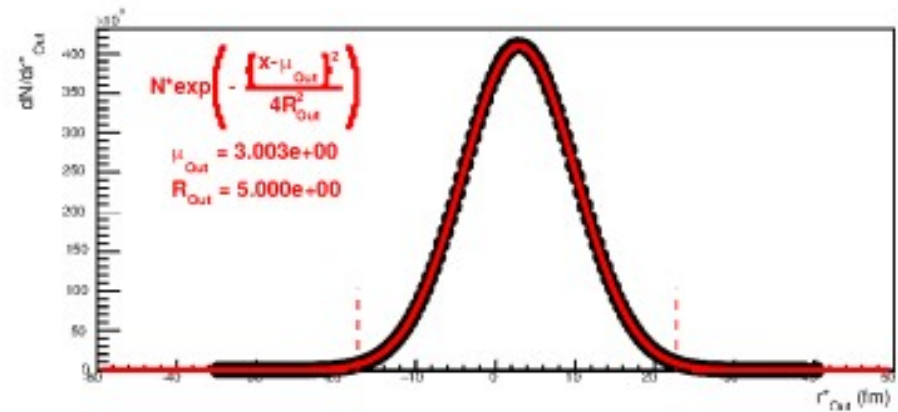
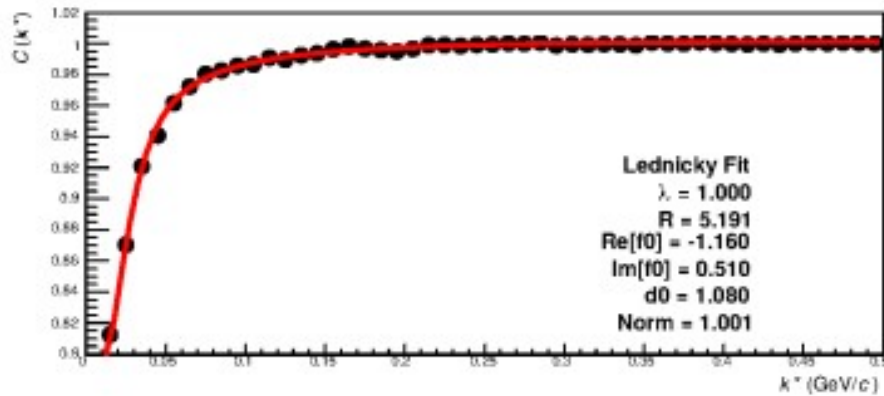
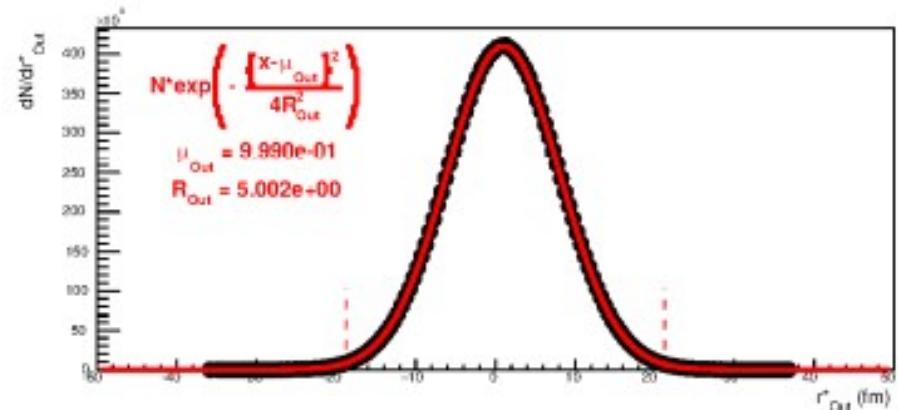
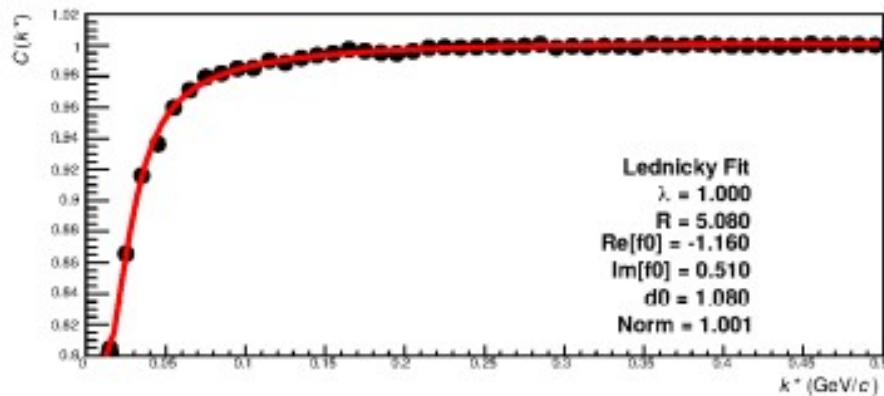
- Numerically integrate Koonin-Pratt equation
 - ◆ Allows for offset μ_{out} to be implemented
- Increasing μ_{out} makes source appear larger

$$C(\mathbf{P}, \mathbf{k}^*) = \int S_{\mathbf{P}}(\mathbf{r}^*) |\Psi(\mathbf{k}^*, \mathbf{r}^*)|^2 d^3 \mathbf{r}^*$$

$$\Psi(k^*, x^*) = e^{-ik^* \cdot x^*} + f(k^*) \frac{e^{ik^* x^*}}{x^*}$$

$$S_{ab}(\mathbf{r}) \propto \prod_{i=0,s,l} \exp\left(-\frac{[r_i - (\mu_{a,i} - \mu_{b,i})]^2}{2(R_{a,i}^2 + R_{b,i}^2)}\right)$$





$$\Psi_{\mathbf{k}^*}(\mathbf{r}^*) = e^{i\delta_c} \sqrt{A_c(\eta)} \left[e^{-i\mathbf{k}^* \cdot \mathbf{r}^*} F(-i\eta, 1, i\xi) + f_c(k^*) \frac{\tilde{G}(\rho, \eta)}{r^*} \right]$$

$$f_c(k^*) = \left[\frac{1}{f_0} + \frac{1}{2} d_0 k^{*2} - \frac{2}{a_c} h(\eta) - ik^* A_c(\eta) \right]^{-1}$$

$$h(\eta) = 0.5[\psi(i\eta) + \psi(-i\eta) - \ln(\eta^2)]$$

$$\psi(z) = \Gamma'(z)/\Gamma(z)$$

$$\rho = k^* r^*$$

$$\eta = (k^* a_c)^{-1}$$

$$\begin{aligned} \xi &= \mathbf{k}^* \cdot \mathbf{r}^* + k^* r^* \\ &= \rho(1 + \cos \theta^*) \end{aligned}$$

$$a_c = (\mu z_1 z_2 e^2)^{-1}$$

δ_c = Coulomb s-wave phase shift

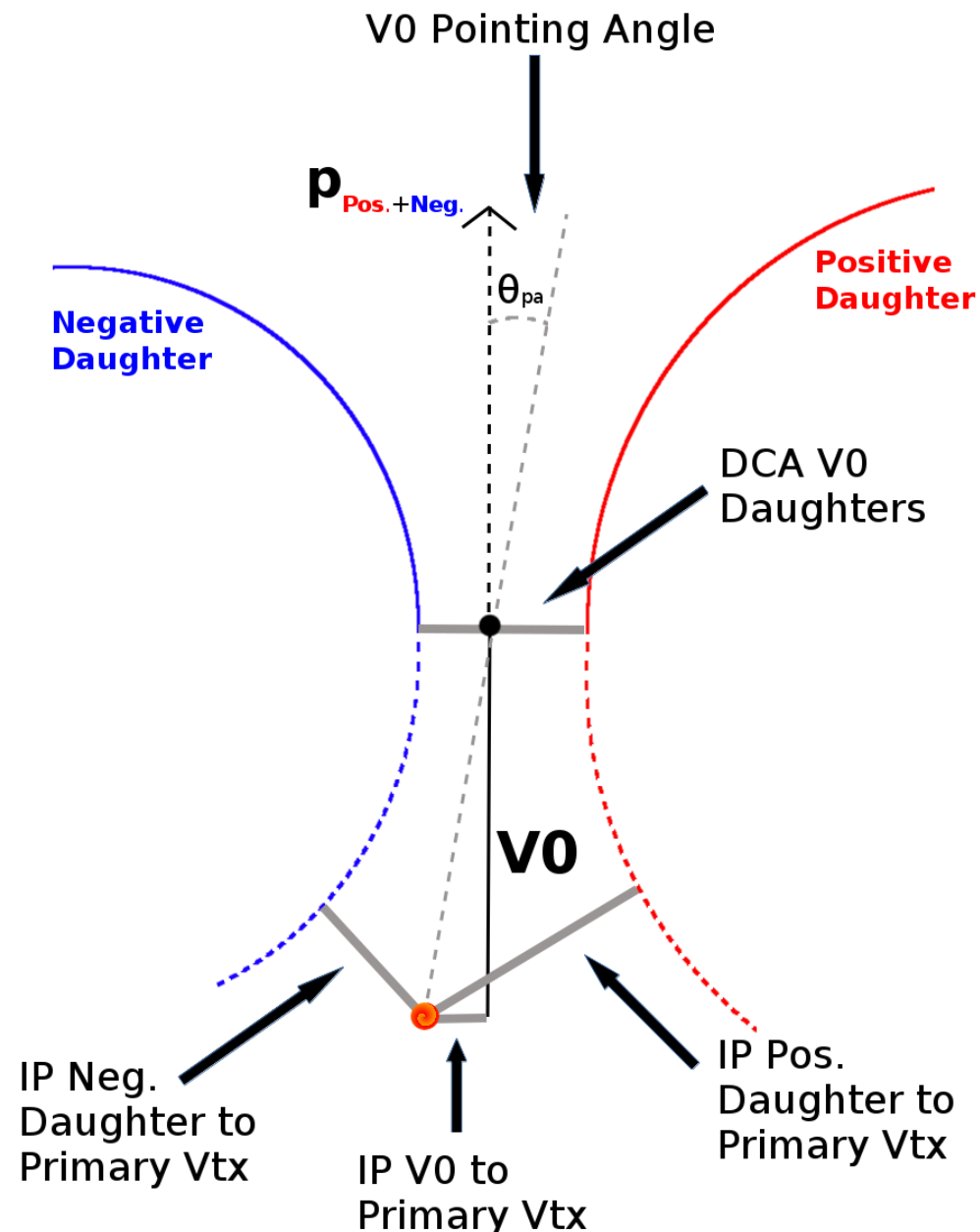
$A_c(\eta)$ = Coulomb penetration factor

$$\tilde{G} = \sqrt{A_c}(G_0 + iF_0)$$

F_0 (G_0) = regular (singular) s-wave Coulomb functions

Analysis Details

- Charged tracks identified with TPC and TOF detectors
 - Purity $K^\pm \approx 97\%$
- Neutral V0s identified from decay products
 - $\Lambda \rightarrow p\pi^-$ (Purity $\approx 95\%$)
 - $K_S^0 \rightarrow \pi^+\pi^-$ (Purity $\approx 98\%$)
- Misidentification cuts
 - Remove K_S^0 contamination in $\Lambda(\bar{\Lambda})$ and vice versa
- V0 shared daughter cut
- Pair cuts
 - Shared daughter
 - Average separation
 - V0 Daughter-V0 Daughter (ΛK_S^0)
 - V0 Daughter-Track (ΛK^\pm)



K[±] selection

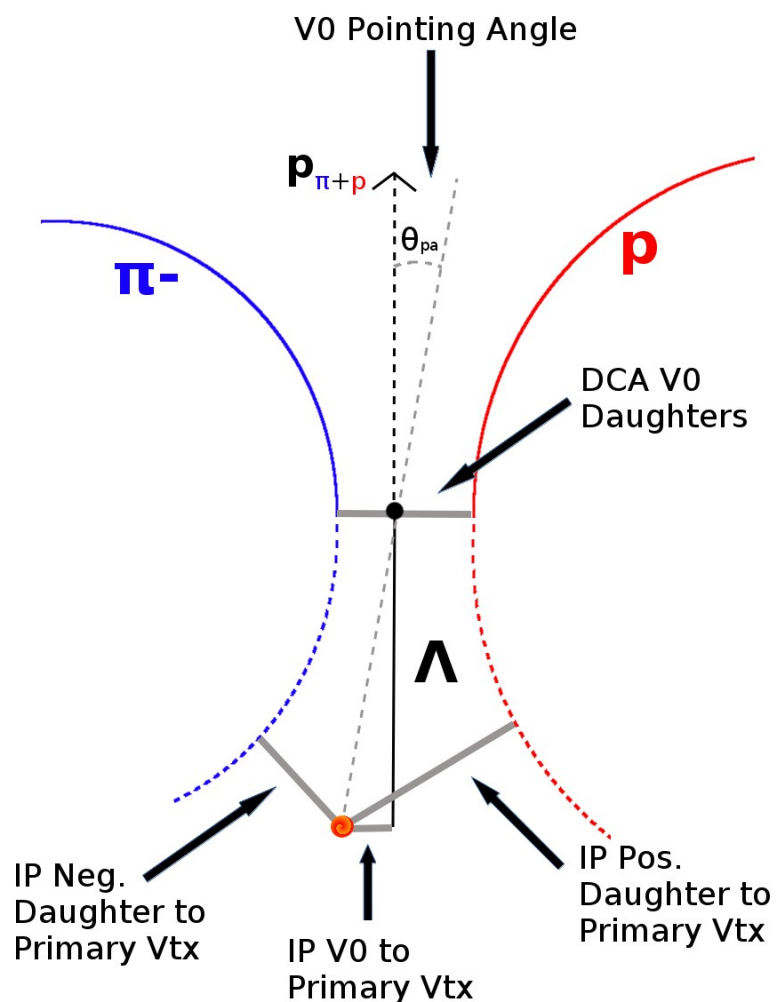
Kinematic range	
$ \eta $	< 0.8
p_T	$0.14 < p_T < 1.5 \text{ GeV}/c$
Track quality and selection	
FilterBit	7
Number of clusters in the TPC	> 80
χ^2/N_{DOF} for (ITS, TPC) clusters	$< (3.0, 4.0)$
DCA to primary vertex (XY, Z)	$< (2.4, 3.0) \text{ cm}$
Remove particles with any kink labels	true
$N\sigma$ to primary vertex	< 3.0
K[±] identification	
PID Probabilities	
K	> 0.2
(π, μ, p)	$< (0.1, 0.8, 0.1)$
Most probable particle type (fMostProbable =)	Kaon (3)
TPC and TOF $N\sigma$ Cuts	
$p < 0.4 \text{ GeV}/c$	$N_{\sigma K, TPC} < 2$
$0.4 < p < 0.45 \text{ GeV}/c$	$N_{\sigma K, TPC} < 1$
$0.45 < p < 0.80 \text{ GeV}/c$	$N_{\sigma K, TPC} < 3$
	$N_{\sigma K, TOF} < 2$
$0.80 < p < 1.0 \text{ GeV}/c$	$N_{\sigma K, TPC} < 3$
	$N_{\sigma K, TOF} < 1.5$
$p > 1.0 \text{ GeV}/c$	$N_{\sigma K, TPC} < 3$
	$N_{\sigma K, TOF} < 1$

K[±] selection - Misidentification Cuts

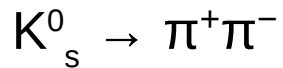
Electron Rejection: Reject if		$N_{\sigma e^-, \text{TPC}} < 3$
Pion Rejection: Reject if:		
$p < 0.65 \text{ GeV}/c$	TOF and TPC available	$N_{\sigma\pi, \text{TPC}} < 3$ $N_{\sigma\pi, \text{TOF}} < 3$
	Only TPC available	$p < 0.5 \text{ GeV}/c$ $N_{\sigma\pi, \text{TPC}} < 3$
$0.5 < p < 0.65 \text{ GeV}/c$		$N_{\sigma\pi, \text{TPC}} < 2$
$0.65 < p < 1.5 \text{ GeV}/c$		$N_{\sigma\pi, \text{TPC}} < 5$ $N_{\sigma\pi, \text{TOF}} < 3$
$p > 1.5 \text{ GeV}/c$		$N_{\sigma\pi, \text{TPC}} < 5$ $N_{\sigma\pi, \text{TOF}} < 2$

$\Lambda \rightarrow p\pi^-$ ($\bar{\Lambda} \rightarrow \bar{p}\pi^+$)

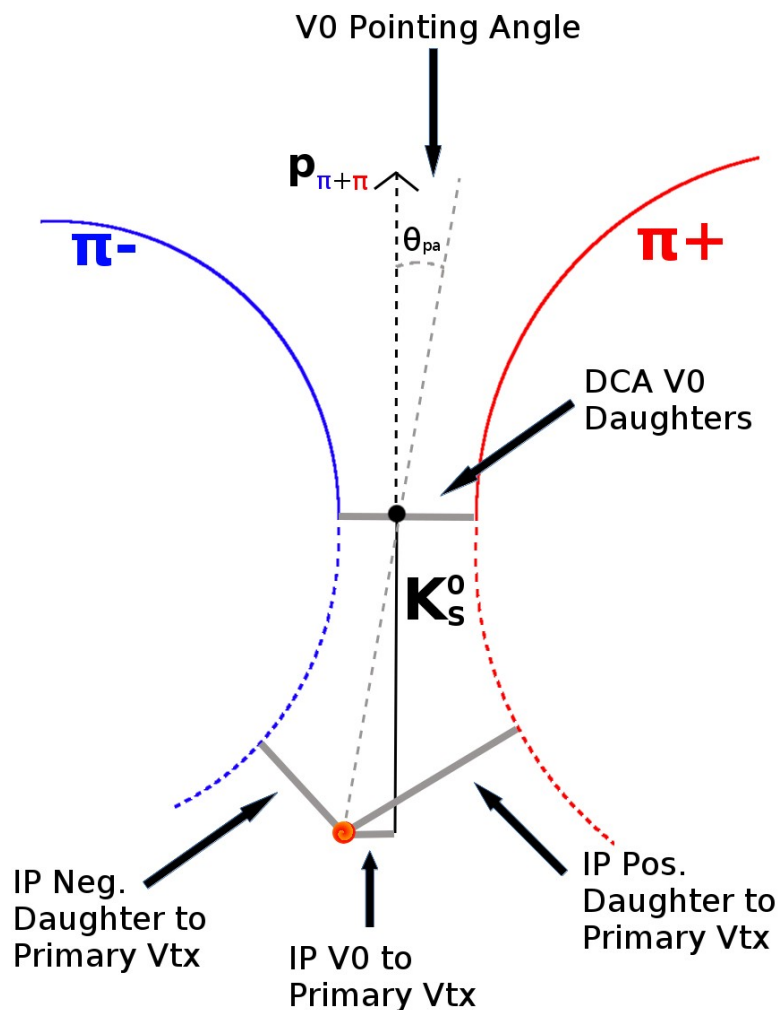
- $c\tau = 7.9$ cm
- Branching ratio $\sim 64\%$
- **Purity(Λ) \sim Purity($\bar{\Lambda}$) $\sim 95\%$**



Λ reconstruction		
$ \eta $		< 0.8
p_T		> 0.4 GeV/c
$ m_{\text{inv}} - m_{\text{PDG}} $		< 3.8 MeV
DCA to prim. vertex		< 0.5 cm
Cosine of pointing angle		> 0.9993
OnFlyStatus		false
Decay Length		< 60 cm
Shared Daughter Cut		true
Misidentification Cut		true
Daughter Cuts (π and p)		
$ \eta $		< 0.8
Number of clusters in the TPC		> 80
Daughter status		kTPCcredit
DCA πp Daughters		< 0.4 cm
π -specific cuts		
p_T		> 0.16 GeV/c
DCA to prim vertex		> 0.3 cm
TPC and TOF $N\sigma$ Cuts		
$p < 0.5$ GeV/c		$N\sigma_{\text{TPC}} < 3$
$p > 0.5$ GeV/c	if TOF & TPC available	$N\sigma_{\text{TPC}} < 3$ & $N\sigma_{\text{TOF}} < 3$
	else	$N\sigma_{\text{TOF}} < 3$
p -specific cuts		
p_T		$> 0.5(p)$ [$0.3(\bar{p})$] GeV/c
DCA to prim vertex		> 0.1 cm
TPC and TOF $N\sigma$ Cuts		
$p < 0.8$ GeV/c		$N\sigma_{\text{TPC}} < 3$
$p > 0.8$ GeV/c	if TOF & TPC available	$N\sigma_{\text{TPC}} < 3$ & $N\sigma_{\text{TOF}} < 3$
	else	$N\sigma_{\text{TOF}} < 3$



- $c\tau = 2.7$ cm (15 m for K_L^0)
- Branching ration $\sim 70\%$
- **Purity(K_S^0) $\sim 98\%$**

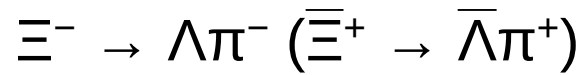


K_S^0 reconstruction		
$ \eta $	< 0.8	
p_T	> 0.2 GeV/c	
$m_{PDG} - 13.677$ MeV $< m_{inv} < m_{PDG} + 2.0323$ MeV		
DCA to prim. vertex	< 0.3 cm	
Cosine of pointing angle	> 0.9993	
OnFlyStatus	false	
Decay Length	< 30 cm	
Shared Daughter Cut	true	
Misidentification Cut	true	
π^\pm Daughter Cuts		
$ \eta $	< 0.8	
Number of clusters in TPC	> 80	
Daughter Status	kTPCrefit	
DCA $\pi^+\pi^-$ Daughters	< 0.3 cm	
p_T	> 0.15 GeV/c	
DCA to prim vertex	> 0.3 cm	
TPC and TOF $N\sigma$ Cuts		
$p < 0.5$ GeV/c	$N\sigma_{TPC} < 3$	
$p > 0.5$ GeV/c	if TOF & TPC available	$N\sigma_{TPC} < 3$ & $N\sigma_{TOF} < 3$
	else	$N\sigma_{TOF} < 3$

- Remove K^0_S contamination from $\Lambda(\bar{\Lambda})$ sample
 - ◆ Reject candidate if all of the following are satisfied (essentially, reject if candidate would pass as K^0):
 - ➔ $\left| m_{inv, K^0_S \text{ Hypothesis}} - m_{PDG, K^0_S} \right| < 9.0 \text{ MeV} / c^2$
 - ➔ Pos. and neg. daughters pass π cuts from K^0_S reconstruction
 - ➔ $\left| m_{inv, K^0_S \text{ Hypothesis}} - m_{PDG, K^0_S} \right| < \left| m_{inv, \Lambda(\bar{\Lambda}) \text{ Hypothesis}} - m_{PDG, \Lambda(\bar{\Lambda})} \right|$
- Remove $\Lambda(\bar{\Lambda})$ contamination from K^0_S sample
 - ◆ Similar to Λ procedure above, reject if:
 - ➔ $\left| m_{inv, \Lambda(\bar{\Lambda}) \text{ Hypothesis}} - m_{PDG, \Lambda(\bar{\Lambda})} \right| < 9.0 \text{ MeV} / c^2$
 - ➔ Pos. daughter passes $p+(\pi+)$ cut from $\Lambda(\bar{\Lambda})$ reconstruction
 - ➔ Neg. daughter passes $\pi-(\bar{p}-)$ cut from $\Lambda(\bar{\Lambda})$ reconstruction
 - ➔ $\left| m_{inv, \Lambda(\bar{\Lambda}) \text{ Hypothesis}} - m_{PDG, \Lambda(\bar{\Lambda})} \right| < \left| m_{inv, K^0_S \text{ Hypothesis}} - m_{PDG, K^0_S} \right|$

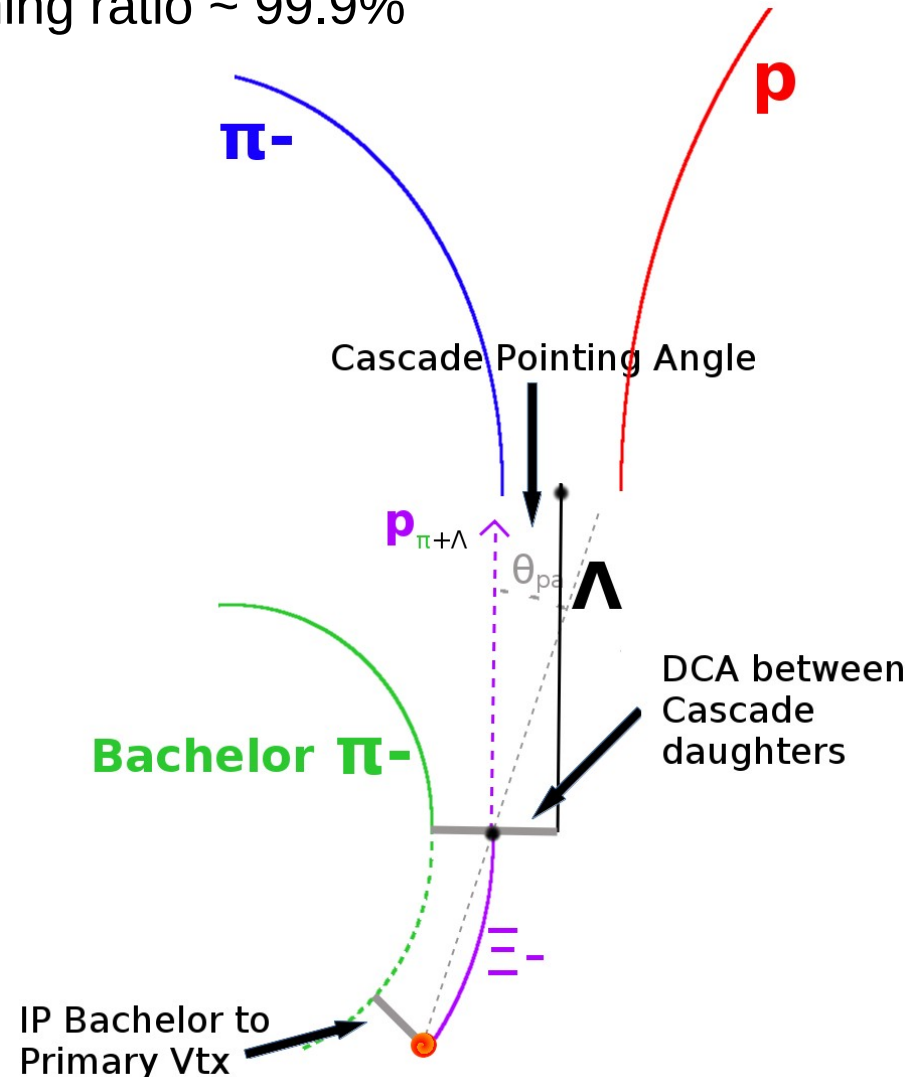
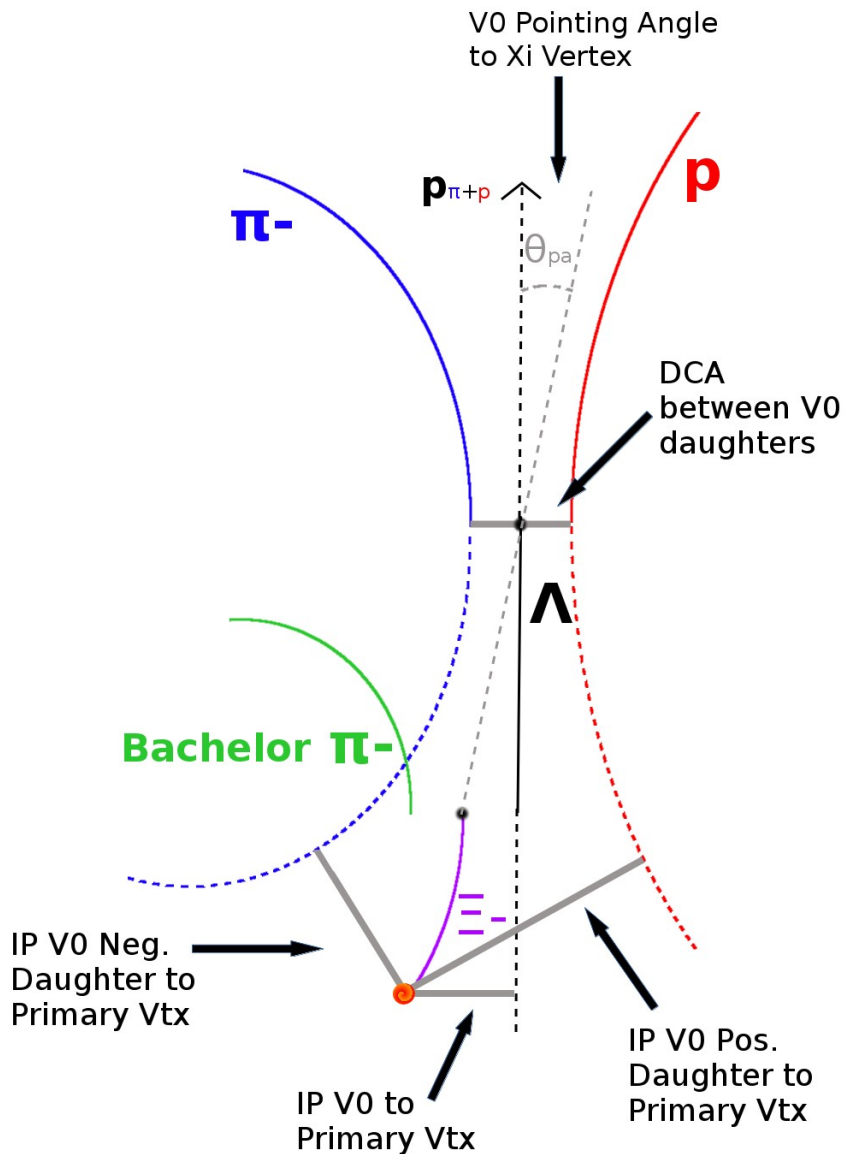
- Shared daughter cut for pairs
 - ◆ V0-V0 Pairs (i.e. ΛK^0_s analyses)
 - ➔ Remove all pairs which share a daughter
 - ➔ Ex. Λ and K^0_s particles which share a π^- daughter are excluded
 - ◆ V0-Track Pairs (i.e. ΛK^\pm analyses)
 - ➔ Remove pairs if K^\pm track is also used as V0 daughter
 - ➔ Only occurs if, for instance, K^\pm is misidentified as π or p in the V0 reconstruction
- Average separation cuts
 - ◆ ΛK^0_s
 - ➔ $\overline{\Delta r} > 6.0$ cm for like sign daughters
 - ➔ No requirement, unlike signs
 - ◆ ΛK^\pm
 - ➔ $\overline{\Delta r} > 8.0$ cm for like sign daughter and track
 - ➔ No requirement, unlike signs

Ξ^- Reconstruction



- $c\tau = 4.9$ cm
- Branching ratio $\sim 99.9\%$

Purity(Ξ^-) $\sim 90\%$
 Purity(Ξ^+) $\sim 92\%$



Ξ^- reconstruction		
$ \eta $		< 0.8
p_T		$> 0.8 \text{ GeV}/c$
$ m_{\text{inv}} - m_{\text{PDG}} $		$< 3.0 \text{ MeV}$
DCA to prim. vertex		$< 0.3 \text{ cm}$
Cosine of pointing angle		> 0.9992
Λ daughter cuts		
DCA to prim. vertex		$> 0.2 \text{ cm}$
Cosine of pointing angle		> 0.0
Cosine of pointing angle to Ξ^- decay vertex		> 0.9993
OnFlyStatus		false
All other Λ and corresponding (π and p) daughter cuts are same as in primary Λ selection		
Bachelor π cuts		
$ \eta $		< 0.8
p_T		$> 0.0 \text{ GeV}/c$
DCA to prim. vertex		$> 0.1 \text{ cm}$
Number of clusters in the TPC		> 70
Daughter status		kTPCrefit
TPC and TOF $N\sigma$ Cuts		
$p < 0.5 \text{ GeV}/c$		$N\sigma_{\text{TPC}} < 3$
$p > 0.5 \text{ GeV}/c$	if TOF & TPC available	$N\sigma_{\text{TPC}} < 3 \ \& \ N\sigma_{\text{TOF}} < 3$
	else	$N\sigma_{\text{TOF}} < 3$

- Pair fails if
 - ◆ K^\pm is a (misidentified) daughter of the Ξ^-
 - ◆ Bachelor π is also a daughter of the Λ
- Ξ shared daughter cut
 - ◆ Iterates through Ξ collection to ensure no daughter is used by more than one Ξ
- Average separation cut for all daughters
 - ◆ $\overline{\Delta r} > 8.0$ cm for daughters of Ξ^- and K^\pm sharing the same charge
 - ◆ No requirement for unlike-charges

- Study how different anisotropic flow affects background
- THERM. 2 model includes flow effects in standard implementation (left)
- Introduce strong artificial anisotropic flow signals for more controlled study (right)
 - ◆ Sample emission angles from: $P(\phi) = \frac{1}{2}[1 + \cos(n\phi)]$
- Flow signal killed by randomizing emission

