

Hyperon interaction with dense nuclear matter and link to neutron stars



Laura Tolós

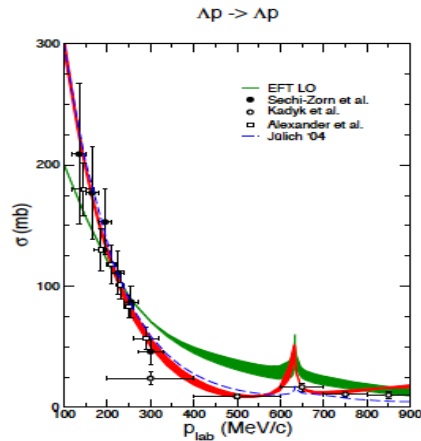
Institute of
Space Sciences



The 18th International Conference on
Strangeness in Quark Matter (SQM 2019)
10-15 June 2019, Bari (Italy)

Outline

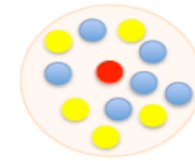
- YN and YY interactions
- Theoretical approaches to YN and YY
- YN and YY interactions in χ EFT
- Hyperons and Neutron Stars
- Summary



YN and YY interactions

- Study strangeness in nuclear physics
- Provide input for hypernuclear physics and astrophysics

hiperon ($\Lambda, \Sigma, \Xi \dots$)



hypernucleus

Scarce YN scattering data due to the short life of hyperons and the low-density beam fluxes

ΛN and ΣN : < 50 data points

ΞN very few events

NN : > 5000 data
for $E_{\text{lab}} < 350$ MeV

Data from hypernuclei:

- more than 40 Λ -hypernuclei (ΛN attractive)
- few $\Lambda \Lambda$ -hypernuclei ($\Lambda \Lambda$ weak attraction)
- single Ξ -hypernuclei (ΞN attractive)
- no evidence of Σ -hypernuclei (ΣN repulsive)

Theoretical approaches to YN and YY

- Meson meson-exchange models (Juelich/Nijmegen models)

To build YN and YY from a NN meson-exchange model imposing

$SU(3)_{\text{flavor}}$ symmetry

Juelich: Holzenkamp, Holinde, Speth '89; Haidenbauer and Meißner '05

Nijmegen: Maesen, Rijken, de Swart '89; Rijken, Nagels and Yamamoto '10

- Chiral effective field theory approach (Juelich-Bonn-Munich group)

To build YN and YY from a chiral effective Lagrangian similarly to NN interaction

Juelich-Bonn-Munich: Polinder, Haidenbauer and Meißner '06; Haidenbauer, Petschauer, Kaiser, Meißner, Nogga and Weise '13

Kohnno '10; Kohnno '18

This talk!

- Quark model potentials

To build YN and YY within constituent quark models

Fujiwara, Suzuki, Nakamoto '07

Garcilazo, Fernandez-Carames and Valcarce '07 '10

- $V_{\text{low } k}$ approach

To calculate a “universal” effective low-momentum potential for YN and YY using RG techniques

Schaefer, Wagner, Wambach, Kuo and Brown '06

- Lattice calculations (HALQCD/NPLQCD) **T. Hatsuda (HALQCD) talk**

To solve YN and YY interactions on the lattice

HALQCD: Ishii, Aoki, Hatsuda '07; Aoki, Hatsuda and Ishii '10; Aoki et al '12

NPLQCD: Beane, Orginos and Savage '11; Beane et al '12

YN and YY interactions in χ EFT

Baryon-Baryon interaction in SU(3) χ EFT **a la Weinberg** (1990);

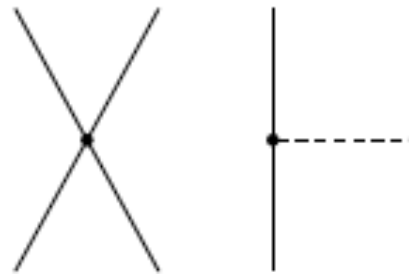
- **Power counting** allowing for a **systematic improvement** by going to higher order
- Derivation of **two- and three-baryon forces** in a consistent way

Degrees of freedom: **octet of baryons** (N, Λ , Σ , Ξ) & **pseudoscalar mesons** (π , K, η)

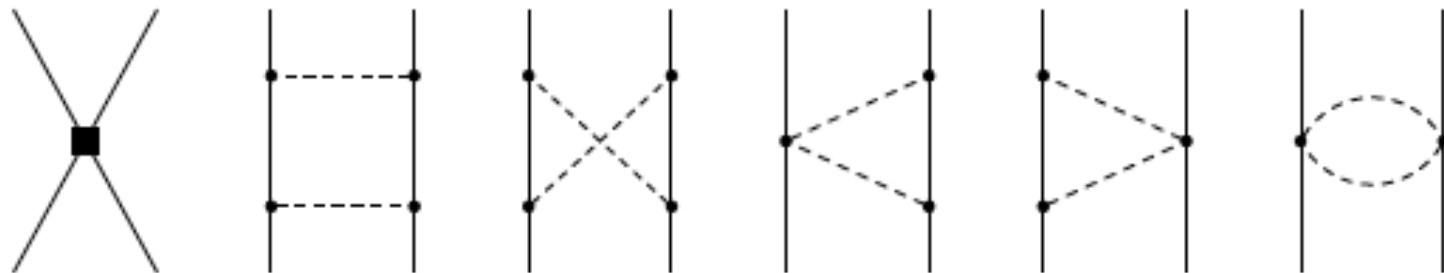
Diagrams: **pseudoscalar-meson exchanges and contact terms**

credit: Haidenbauer

LO :



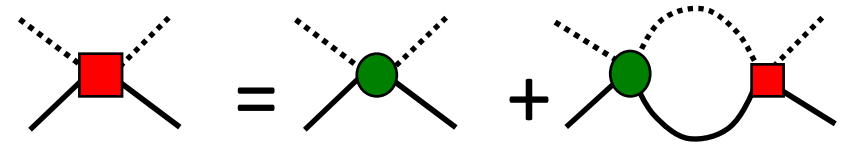
NLO :



LO: H. Polinder, J.H., U. Meißner, NPA 779 (2006) 244

NLO: J.H., N. Kaiser, U.-G. Meißner, A. Nogga, S. Petschauer, W. Weise, NPA 915 (2013) 24

ΛN and ΣN scattering data: the coupled-channel Lippman-Schwinger Equation

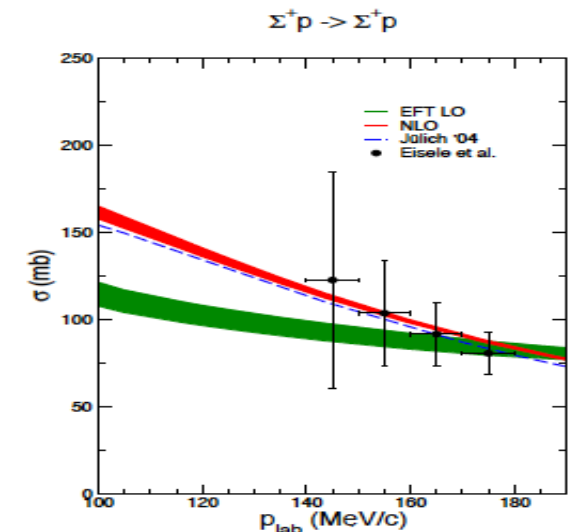
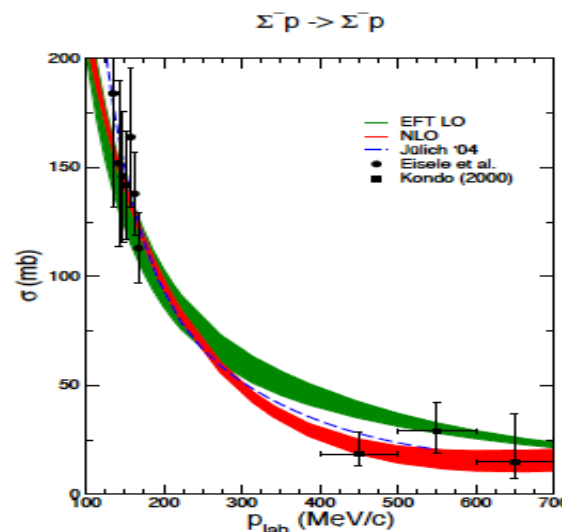
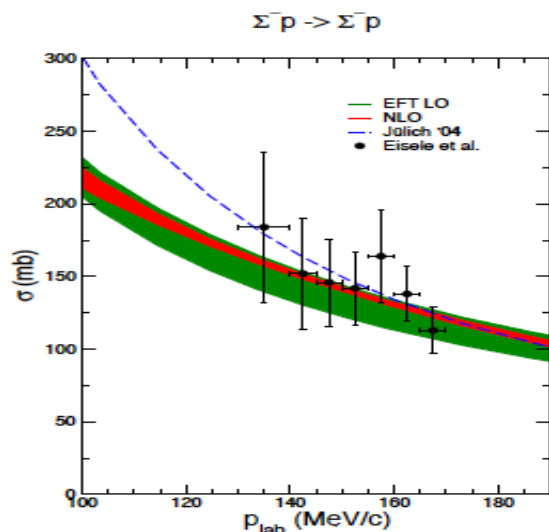
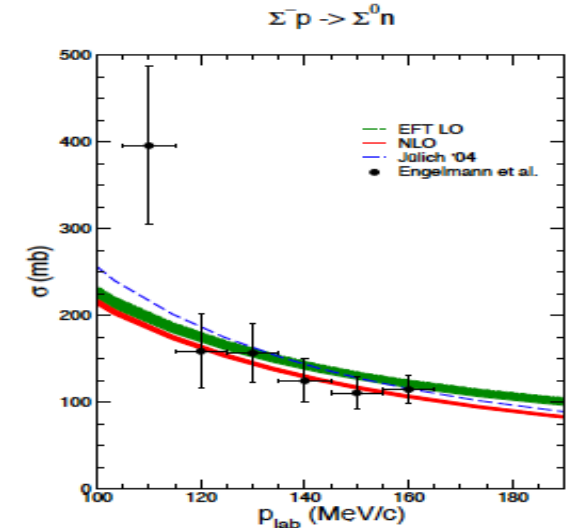
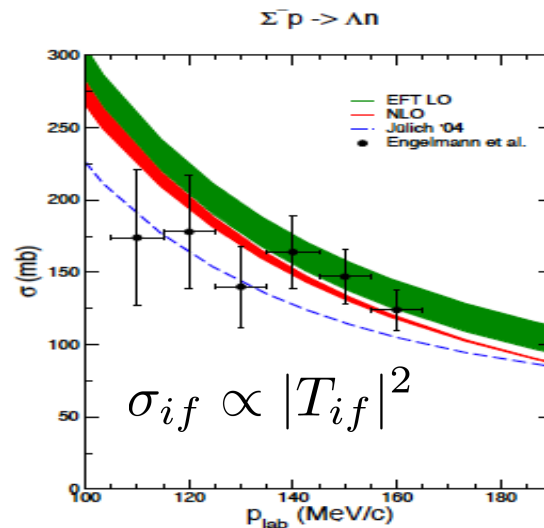
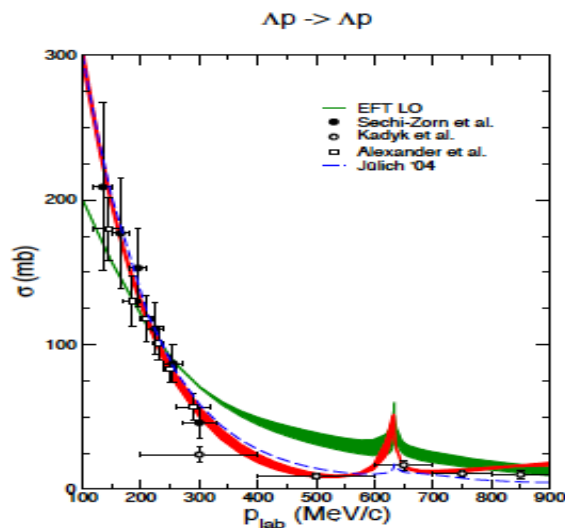


$$T = V + V \frac{1}{E_0 - H_0 + i\eta} T$$

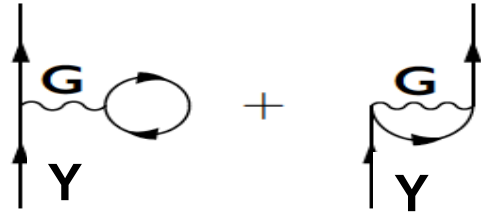
LO: H. Polinder, J.H., U. Meißner, NPA 779 (2006) 244

NLO: J.H., N. Kaiser, et al., NPA 915 (2013) 24

Jülich '04: J.H., U.-G. Meißner, PRC 72 (2005) 044005



Λ and Σ in dense matter: Brueckner-Hartree-Fock



$$G = V + V \frac{Q_{\text{pauli}}}{E_0 - H_0} G$$

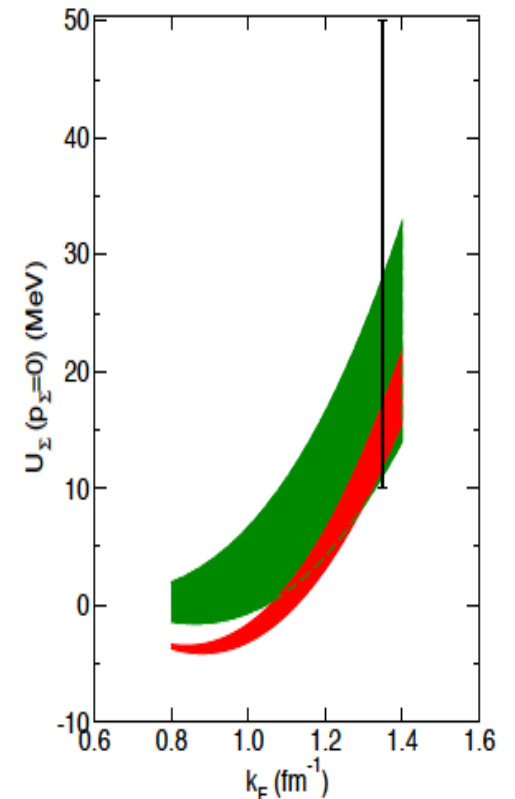
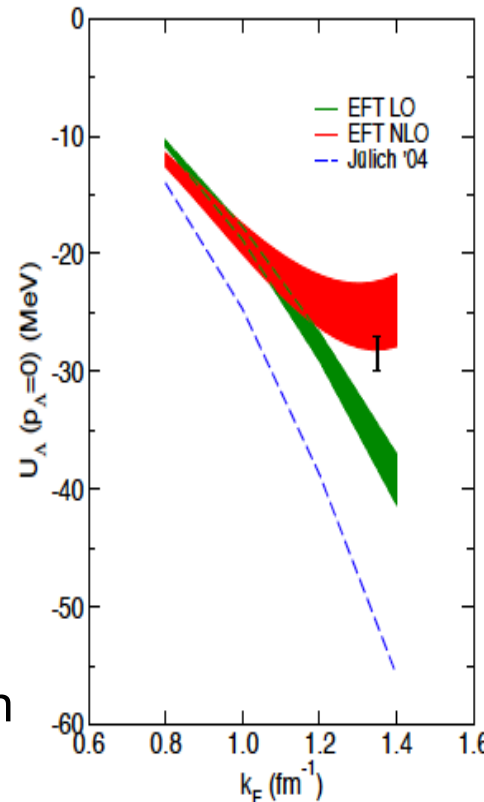
$$k_F = 1.35 \text{ fm}^{-1} \quad (\rho_0 = 0.166 \text{ fm}^{-3})$$

	EFT LO	EFT NLO
Λ [MeV]	550 ... 700	500 ... 650
$U_\Lambda(0)$	-38.0 ... -34.4	-28.2 ... -22.4
$U_\Sigma(0)$	28.0 ... 11.1	17.3 ... 11.9

- Empirical value of Λ binding in nuclear matter $\sim 27\text{-}30$ MeV

- ΣN ($I=3/2$): 3S_1 - 3D_1 decisive for Σ properties in nuclear matter. YN data can be reproduced with attractive and repulsive 3S_1 - 3D_1 interaction. It is chosen to be repulsive in accordance to data on Σ^- atoms and (π, K^+) inclusive spectra for Σ^- formation in heavy nuclei.

Lattice* supports repulsion!



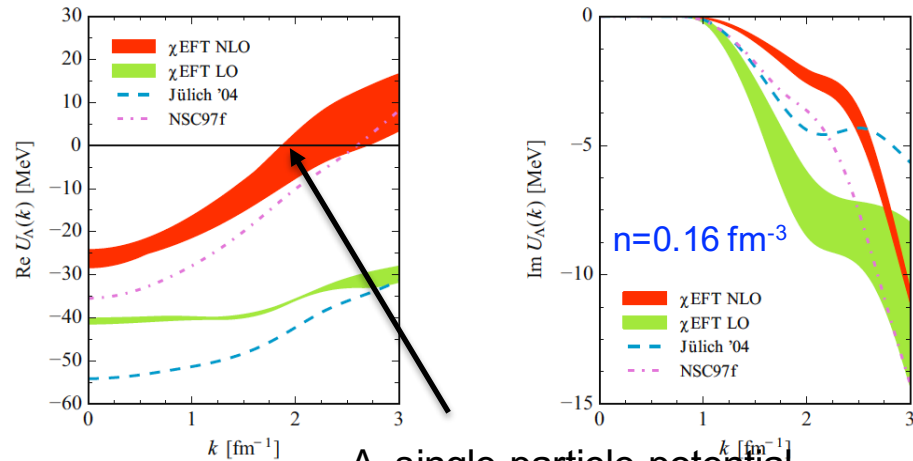
Haidenbauer and Meißner, NPA 936 (2015) 29

* Nemura et al EPJ Web of Conferences 175 (2018) 05030; Hatsuda (HALQCD) SQM2019

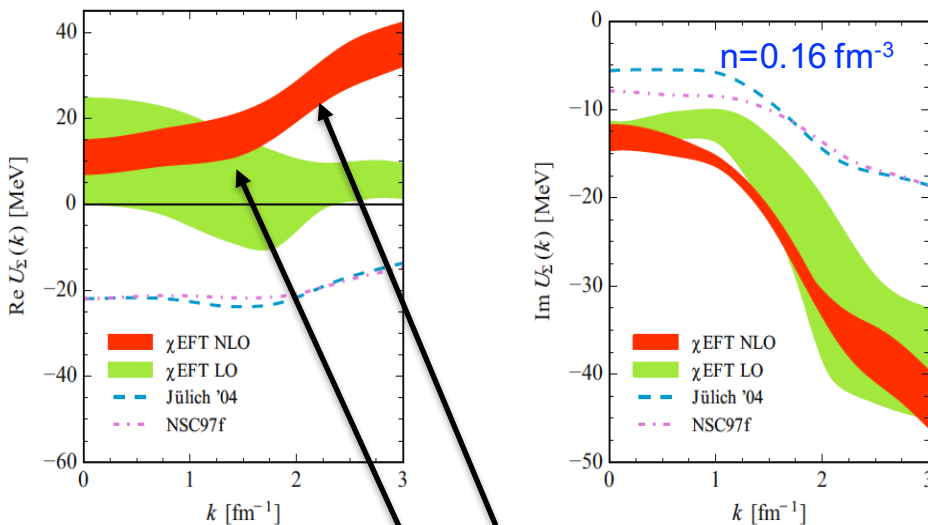
Improving on the calculation by using χ EFT NN interaction and continuous choice in Brueckner-Hartree-Fock approach while investigating isospin-asymmetric matter

S. Petschauer, J. Haidenbauer, N. Kaiser, U.G. Meißner and W. Weise EPJA 52 (2016) 15

symmetric nuclear matter

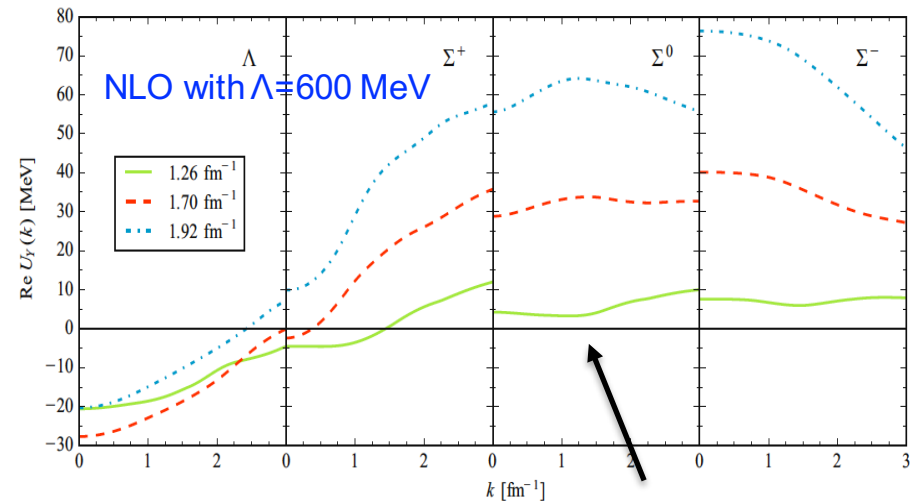


Λ single-particle potential at NLO turns repulsive $k \sim 2 \text{ fm}^{-1}$

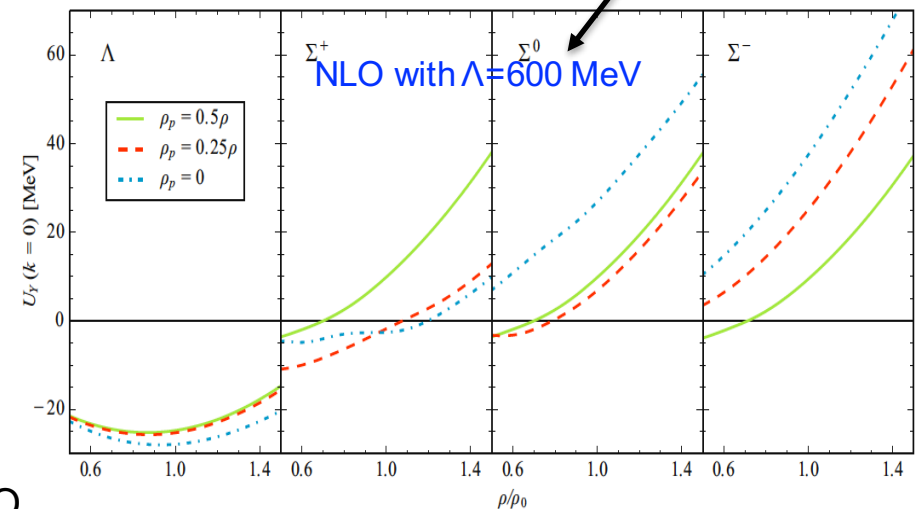


Σ -nuclear potential is moderately repulsive for LO and NLO

neutron matter



strong isospin dependence of the Σ N interaction

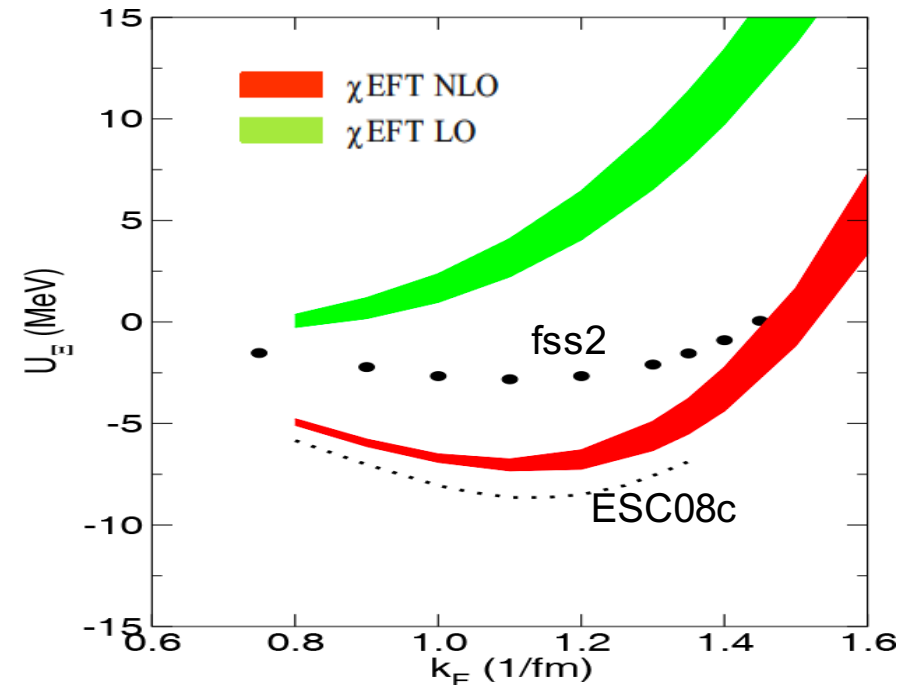
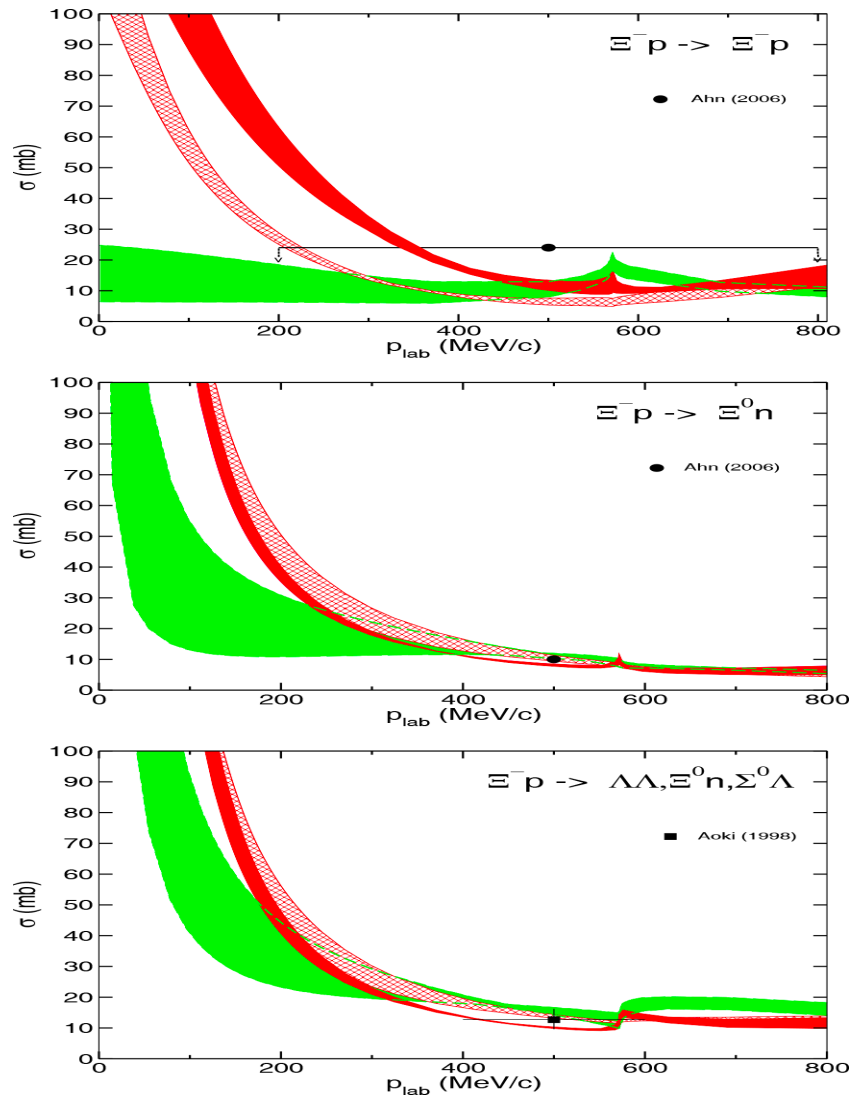


ΞN scattering and Ξ in dense matter

J. Haidenbauer and
U.G. Meißner EPJA 55 (2019) 23

Using experimental constraints on $\Lambda\Lambda$ scattering length to be mildly attractive, whereas ΞN cross sections are small

Ξ in dense matter

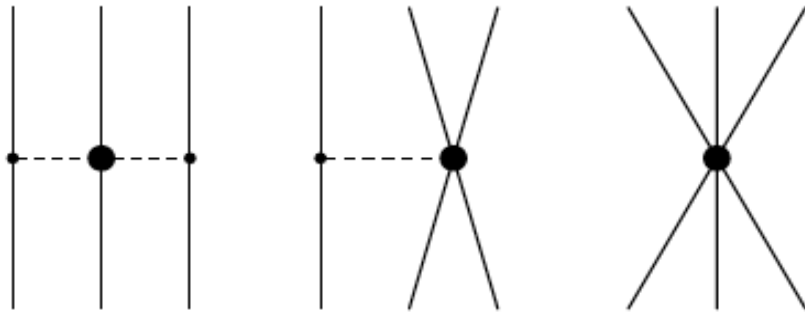


Moderately attractive Ξ -nuclear interaction, with $U_{\Xi}(0) \sim -3$ to -5 MeV.
Smaller than $U_{\Xi}(n_0) \sim -14$ MeV Khaustov et al'00 and in line with other BHF studies with phenomenological ΞN potentials

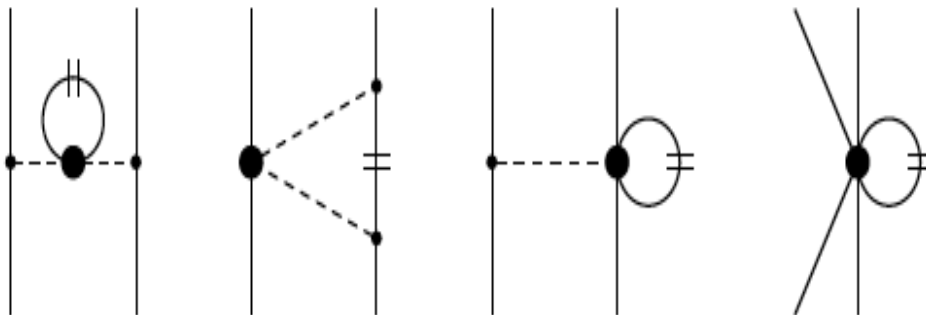
Λ in dense matter: including three-body forces

Three-body forces are required to reproduce few-nucleon binding energies, scattering observables and nuclear saturation in non-relativistic many-body approaches

Three-body force (nominally at N²LO)



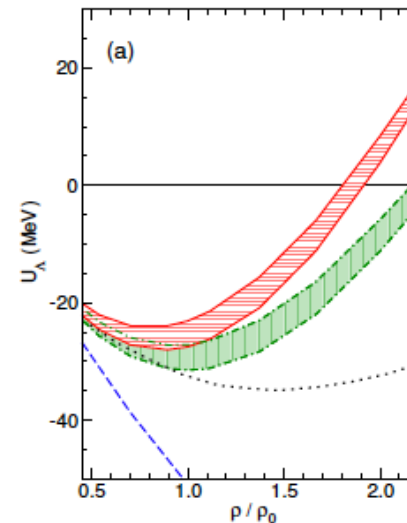
To use it in many-body calculations, such as BHF, one has to construct a density-dependent two-body interaction



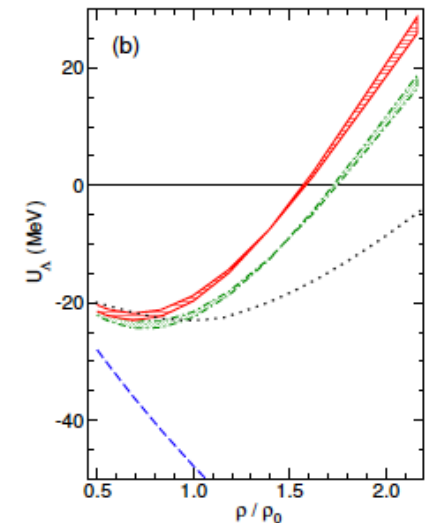
closing two baryon lines summing over the Fermi sea
credit: Haidenbauer

Λ in dense matter

symmetric matter



neutron matter



--- χ EFT at NLO
 --- χ EFT at NLO + density-dependent ΛN interaction derived from chiral $\Lambda N N$ 3BFs
 - - - Jülich '04; ··· Nijmegen NSC97f

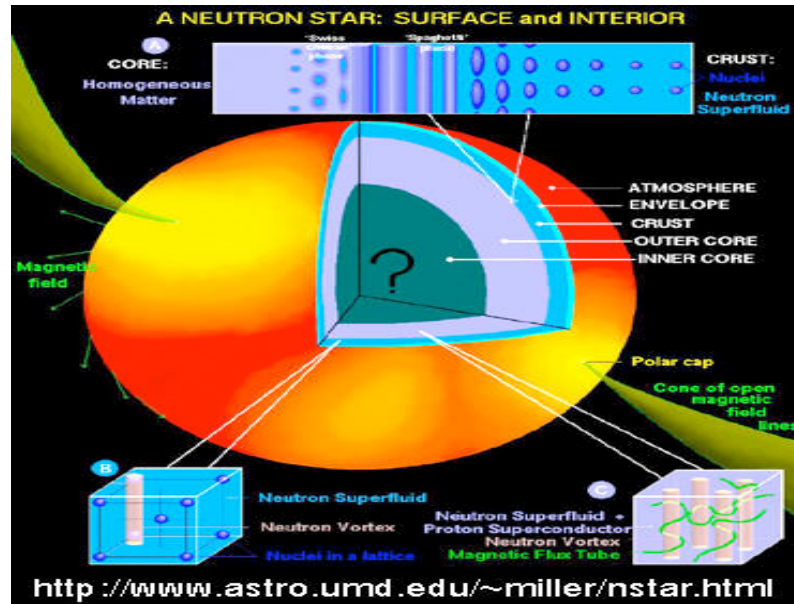
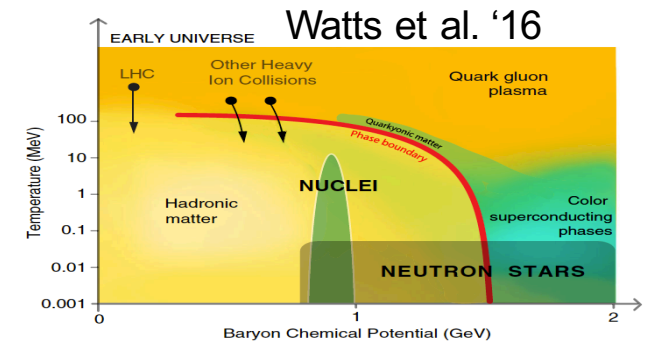
χ EFT gives little attraction or even repulsion for $n > n_0$

In neutron stars, hyperons will appear at high density!!

Solution of the Hyperon Puzzle?

J. Haidenbauer, U.G. Meißner, N. Kaiser and W. Weise EPJA 53 (2017) 121

Hyperons and Neutron Stars



- produced in core collapse supernova explosions, usually observed as pulsars

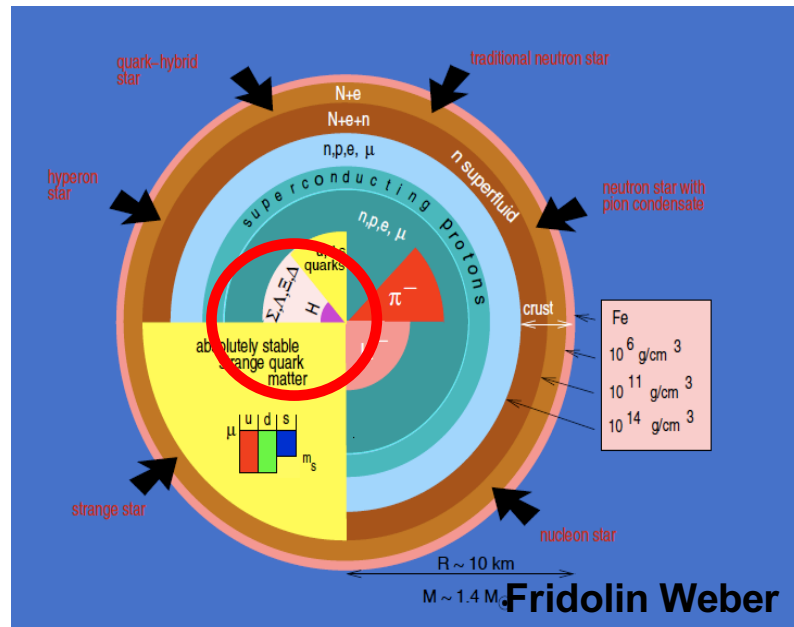
- usually refer to compact objects with $M \approx 1-2 M_{\odot}$ and $R \approx 10-12 \text{ Km}$

- extreme densities up to $5-10 \rho_0$ ($n_0 = 0.16 \text{ fm}^{-3} \Rightarrow \rho_0 = 3 \cdot 10^{14} \text{ g/cm}^3$)

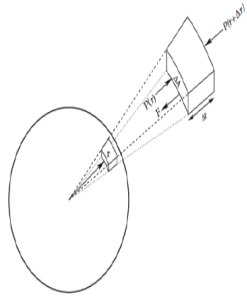
- magnetic field : $B \sim 10^{8..16} \text{ G}$

- temperature: $T \sim 10^{6..11} \text{ K}$

- observations: masses, radius (?), gravitational waves, cooling...



Mass-Radius Relation

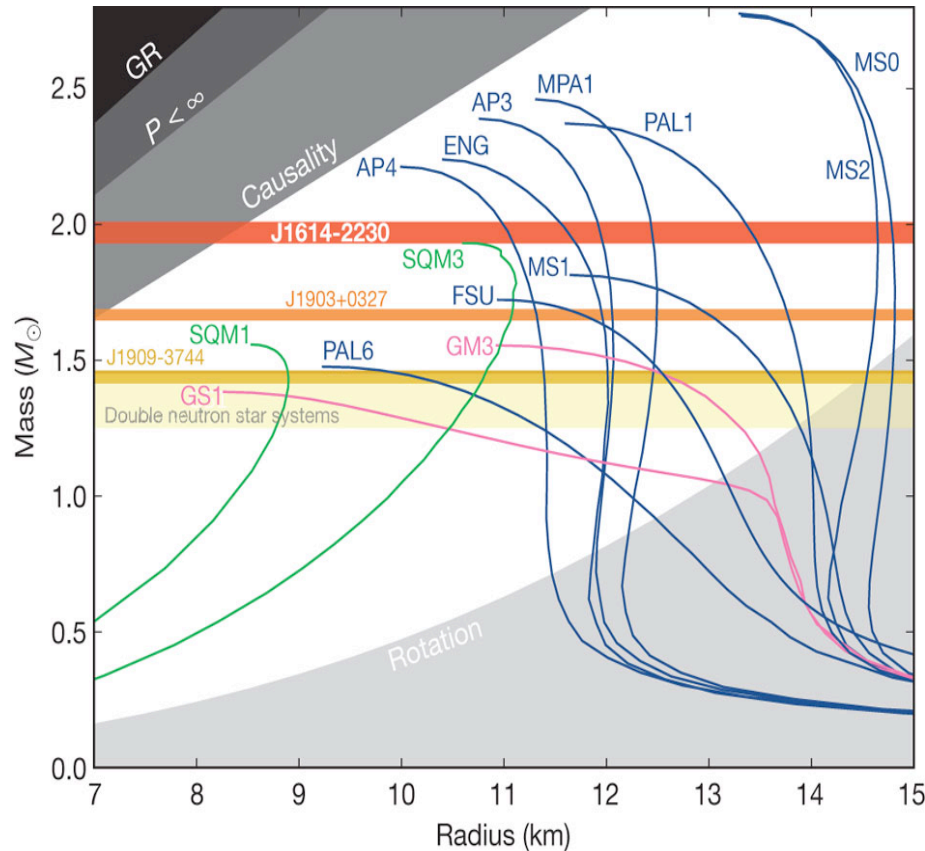


$$\frac{dP}{dr} = -\frac{Gm\epsilon}{c^2 r^2} \left(1 + \frac{P}{\epsilon}\right) \left(1 + \frac{4\pi r^3 P}{c^2 m}\right) \left(1 - \frac{2Gm}{c^2 r}\right)^{-1}$$

$$\frac{dm}{dr} = \frac{4\pi r^2 \epsilon}{c^2}$$

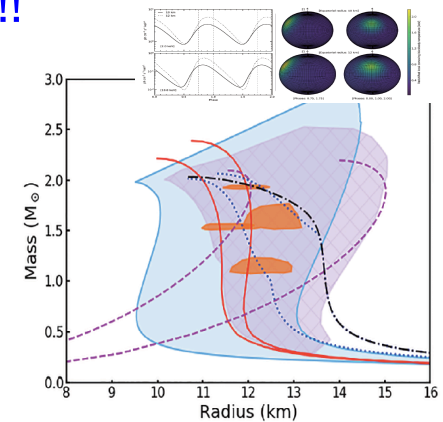
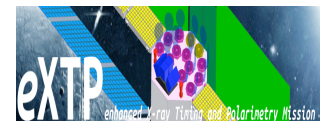
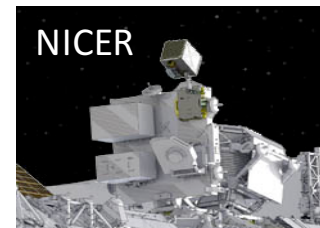
- primary ingredient:
EoS: $\epsilon(n)$, $P(n)$, $P(\epsilon)$
in charge neutral β -stable matter

- some constraints:
 - Schwarzschild limit (GR)
 $R \geq 2 GM/c^2$
 - causality limit for EoS
 $R \geq 2.9 GM/c^2$
 - mass-shedding limit
 $R < (GM/2\pi)^{1/3}/\nu^{2/3}$



Ozel et al '16

Need of simultaneous mass-radius measurements to constrain EoS !!!



Watts et al. (LT) '19

The Nucleonic Equation of State

The Equation of State (EoS) is a relation between thermodynamic variables describing the state of matter

Microscopic Ab-initio Approaches:

based on solving the many-body problem starting from two- and three-body interactions

- *Variational method: APR, CBF,..*
- *Quantum Montecarlo : AFDMC..*
- *Coupled cluster expansion*
- *Diagrammatic: BBG (BHF), SCGF..*
- *Relativistic DBHF*
- *RG methods: SRG from χ EFT..*
- *Lattice methods*

Advantage: systematic addition of higher-order contributions

Disadvantage: applicable up to?
(SRG from χ EFT \sim 1-2 n_0)

Phenomenological Approaches:

based on density-dependent interactions adjusted to nuclear observables and neutron star observations

- *Non-relativistic EDF: Skyrme..*
- *Relativistic Mean-Field (RMF) and Relativistic Hartree-Fock (RHF)*
- *Liquid Drop Model: BPS, BBP,..*
- *Thomas-Fermi model: Shen*
- *Statistical Model: HWN, RG, HS..*

Advantage: applicable to high densities beyond n_0

Disadvantage: not systematic

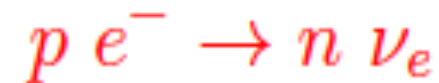
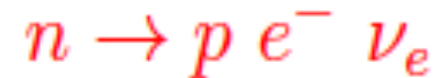
What about Hyperons?

credit: Vidana

First proposed in 1960 by
Ambartsumyan & Saakyan

Hyperon	Quarks	$I(J^P)$	Mass (MeV)
Λ	uds	$0(1/2^+)$	1115
Σ^+	uus	$1(1/2^+)$	1189
Σ^0	uds	$1(1/2^+)$	1193
Σ^-	dds	$1(1/2^+)$	1197
Ξ^0	uss	$1/2(1/2^+)$	1315
Ξ^-	dss	$1/2(1/2^+)$	1321
Ω^-	sss	$0(3/2^+)$	1672

Traditionally neutron stars were modeled by a uniform fluid of neutron rich matter in β -equilibrium



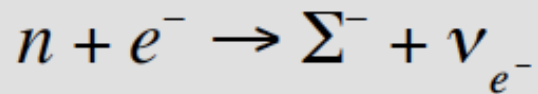
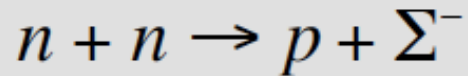
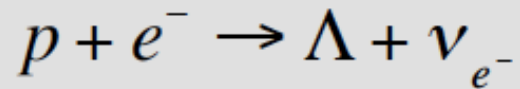
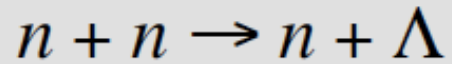
but more exotic degrees of freedom are expected, such as **hyperons**, due to:

- high value of density at the center and
- the rapid increase of the nucleon chemical potential with density

Hyperons might be present at $n \sim (2-3)n_0$!!!

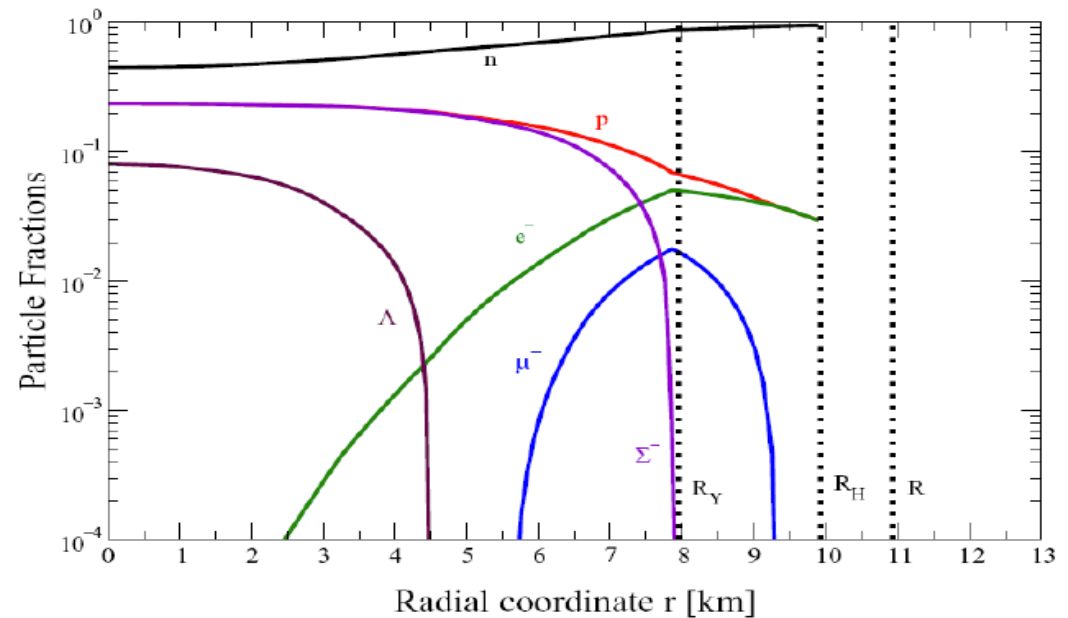
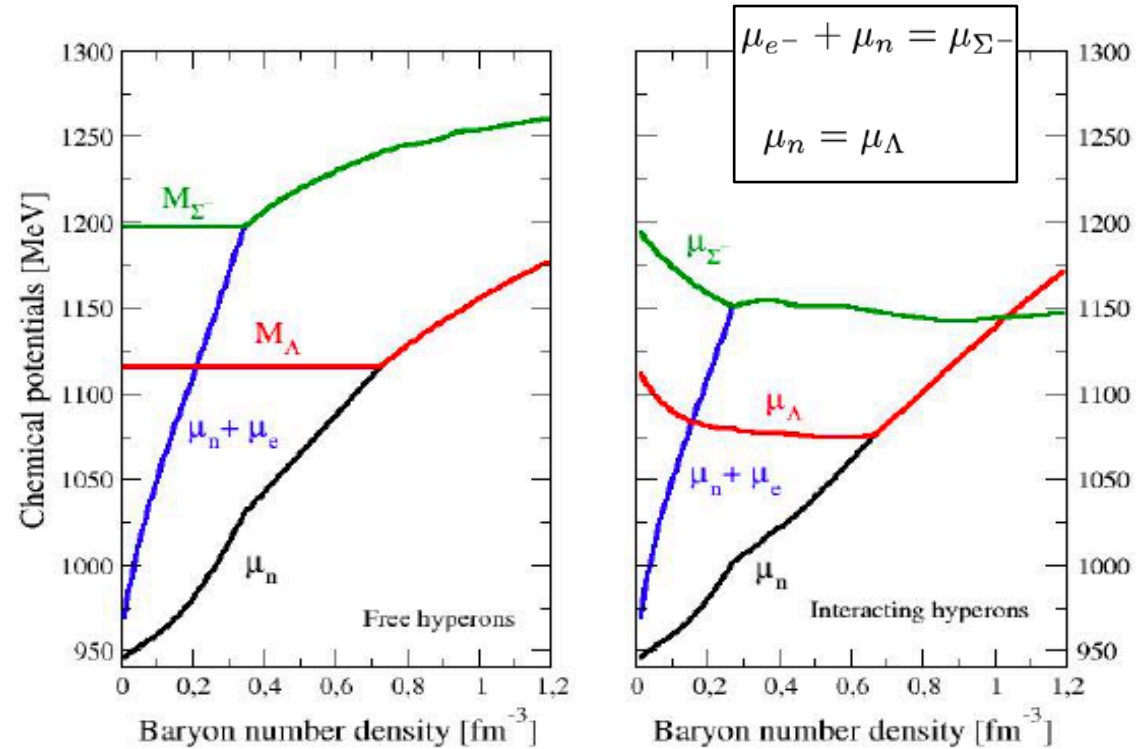
β -stable hyperonic matter

μ_N is large enough to make $N \rightarrow Y$ favorable



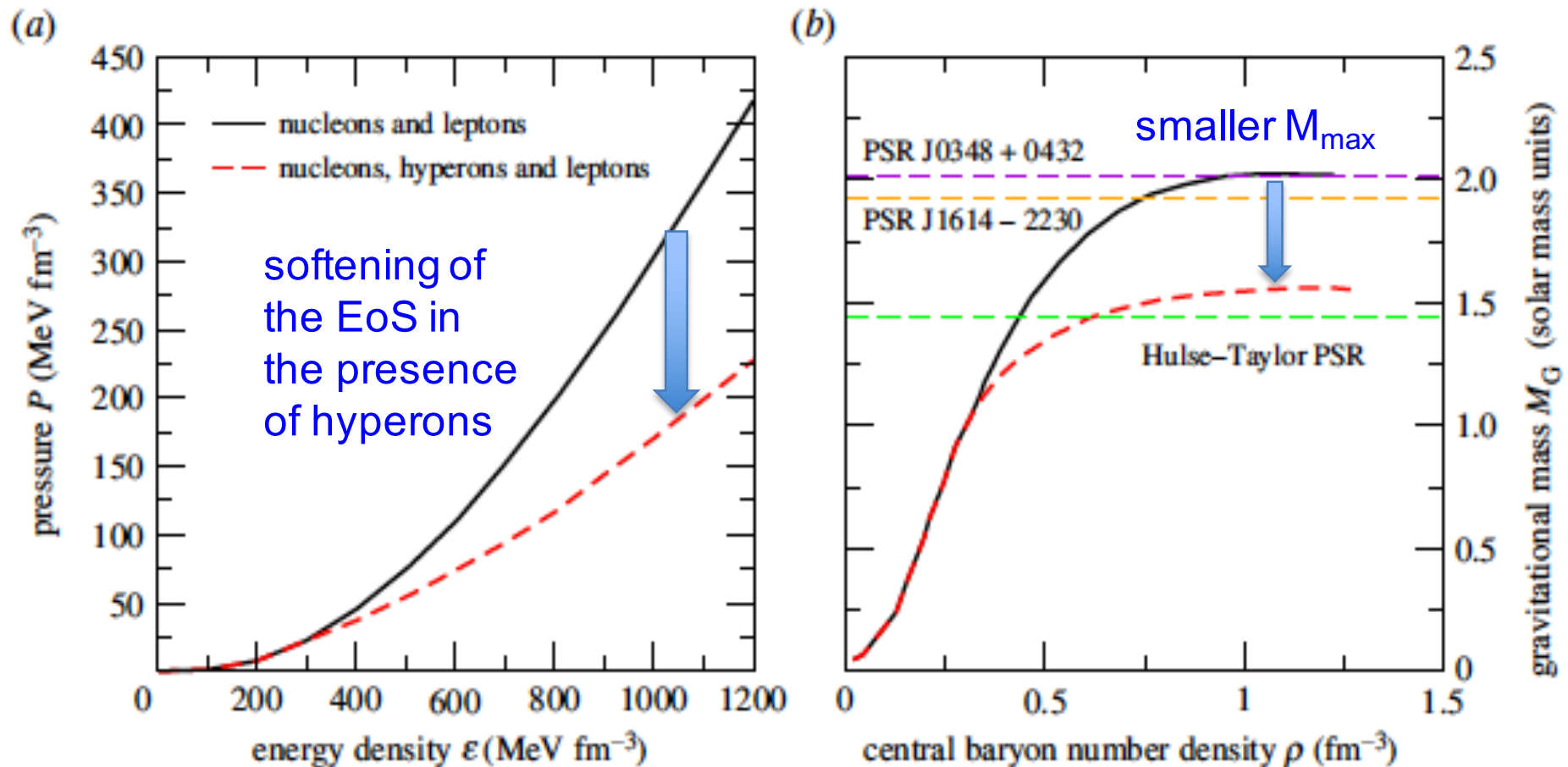
$$\mu_i = b_i \mu_n - q_i \mu_e$$

$$\sum_i x_i q_i = 0$$



credit: Vidana

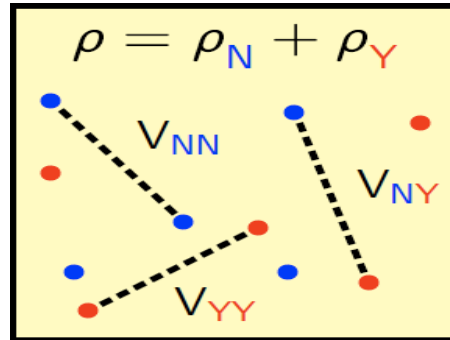
Inclusion of hyperons....



..... induces a strong softening of the EoS
that leads to $M_{\max} < 2M_{\text{sun}}$



Experimental Data from YN scattering and hypernuclei



Theoretical models for hyperons in neutron stars

- **YN**: < 50 scattering data points
- **N Λ** : Λ -hypernuclei for $A=3-209$, $U_{\Lambda}(n_0) = -30$ MeV
- **N Σ** : Σ^- atoms but no Σ -hypernuclei, $U_{\Sigma}(n_0) = 30$ MeV ?
- **N Ξ** : one Ξ hypernuclei $U_{\Xi}(n_0) = -14/-18/-28$ MeV ?
- **$\Lambda\Lambda$** : few $\Lambda\Lambda$ hypernuclear events, slightly attractive ?
- **YY** with Λ , Σ , Ξ **unknown!**

- **Relativistic mean field models**
Glendenning '85; Knorren, Prakash & Ellis '95; Schaffner & Mishustin '96..
- **Non-relativistic potential model**
Balberg & Gal '97...
- **Quark-meson coupling model**
Pal et al '99..
- **Chiral effective lagrangians**
Hanuske et al. '00...
- **Density dependent hadron field model** Hofmann, Keil & Lenske '01..
- **DBHF/BHF approaches**
Brockmann & Machleidt '90; Baldo, Burgio, Schulze '00; Vidana et al. '00; Jong and Lenske '98..
- **Low-momentum interactions**
Schwenk, Pethick, Hebeler, Friman, LT, Djapo..
- **Quantum Montecarlo**
Leonardi et al '14..

Solutions to the Hyperon Puzzle?

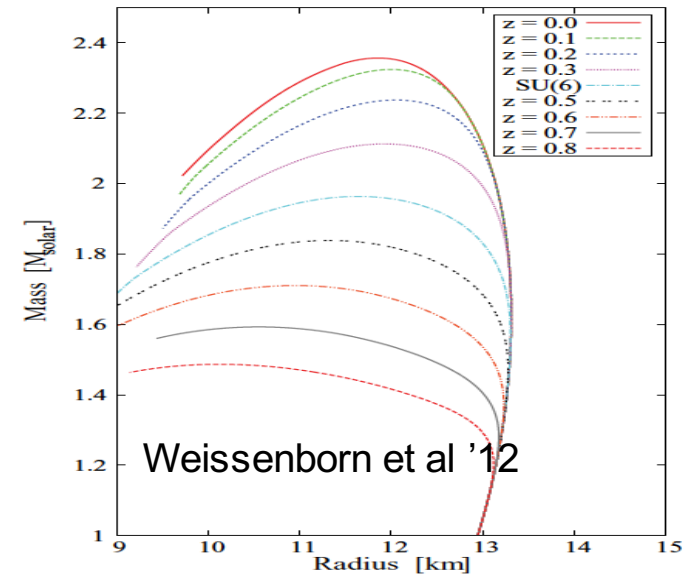
I. Stiffer YN and YY interactions

mainly explored in RMF models:

coupling of ϕ to hyperons to shift the onset of hyperons to higher densities

Bednarek et al '12; Weissenborn et al '12;
Oerte et al '15; Maslov et al '15..

results still compatible with $\Delta B_{\Lambda\Lambda}({}^6\text{He}_{\Lambda\Lambda})$
Fortin et al '17



II. Hyperonic 3-body forces

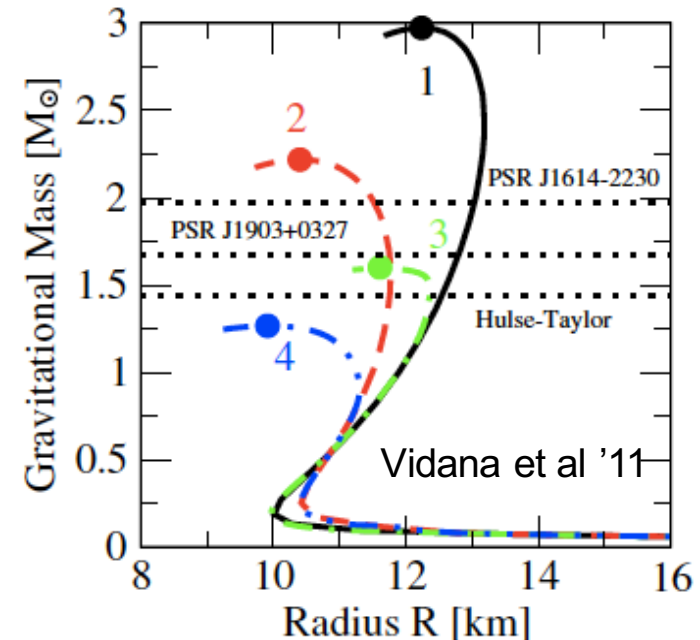
not yet a general consensus:

while for some models 2Msun are reached,
Taktasuka et al '02 '08; Yamamoto et al '13 '14..

for others M_{max} is $1.6M_{\text{sun}}$ Vidana et al '11

while Lonardonì et al '15

shows no a conclusive outcome due to
the strong dependence on ΛNN force



Solution from point of view of $\chi\text{EFT!!}$

Solutions to the Hyperon Puzzle?

III. Push of Y onset by Δ -isobars or meson condensates

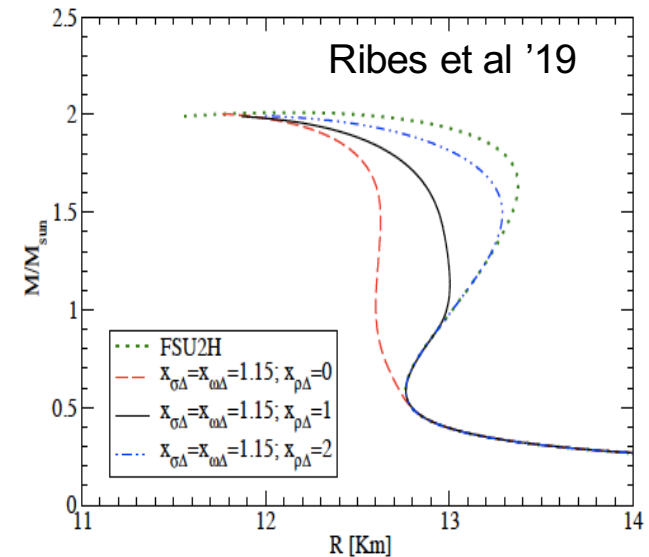
appearance of another degree of freedom that push Y onset to higher densities.
It might (or not) reach $2M_{\text{sun}}$

Δ

Drago et al '14 '15, Jie Li et al '19 ; Ribes et al '19...

K condensate

Kaplan et al' 86, Brown et al '94; Thorsson et al '94; Lee '96; Glendenning et al '98..

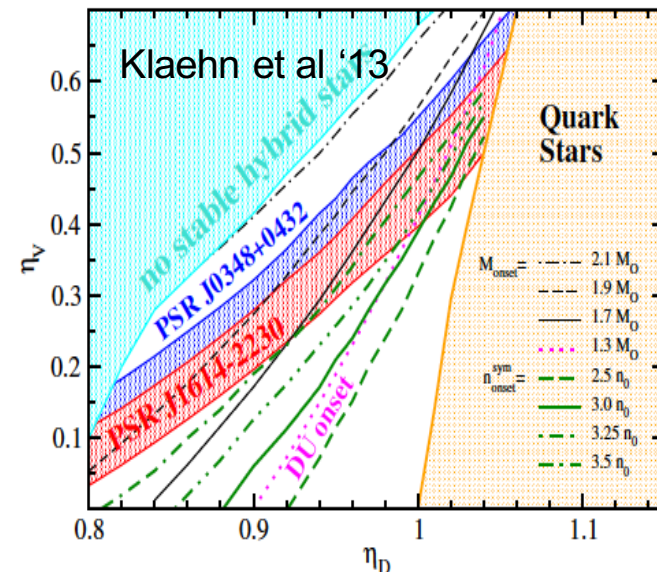


IV. Quark matter below Y onset

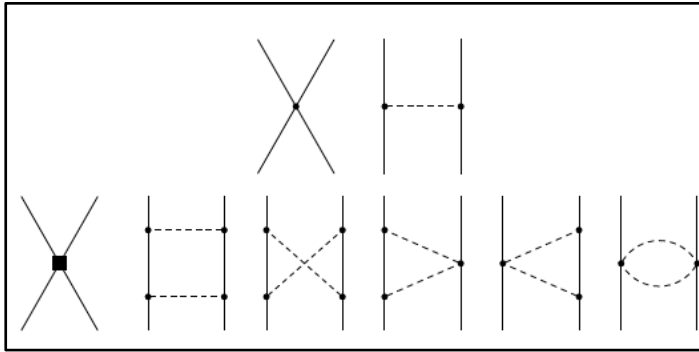
early transition to quark matter below Y onset, with quarks providing enough repulsion to reach $2M_{\text{sun}}$

Weissenborn et al '11; Klaehn et al '13;

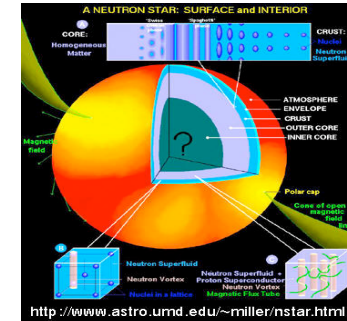
Bonanno et al '12; Lastowiecki et al '12...



V. Others: modified gravity...



Summary



- We have presented the **YN and YY interactions** in dense matter for different approaches and, in particular, for χ EFT
- **Λ , Σ and Ξ interactions** in nuclear matter have been investigated from χ EFT at NLO (and with density-dependent 2-body forces for Λ NN), showing attraction for Λ , and repulsion for Σ and Ξ at low densities
- **Λ feels little attraction or even repulsion for $n > n_0$ in χ EFT**, pointing to a possible solution of the Hyperon Puzzle in neutron stars
- We have discussed the **presence of hyperons in neutron stars** and the **possible solutions to the Hyperon Puzzle**