

# Update on BEST collaboration and status of lattice QCD



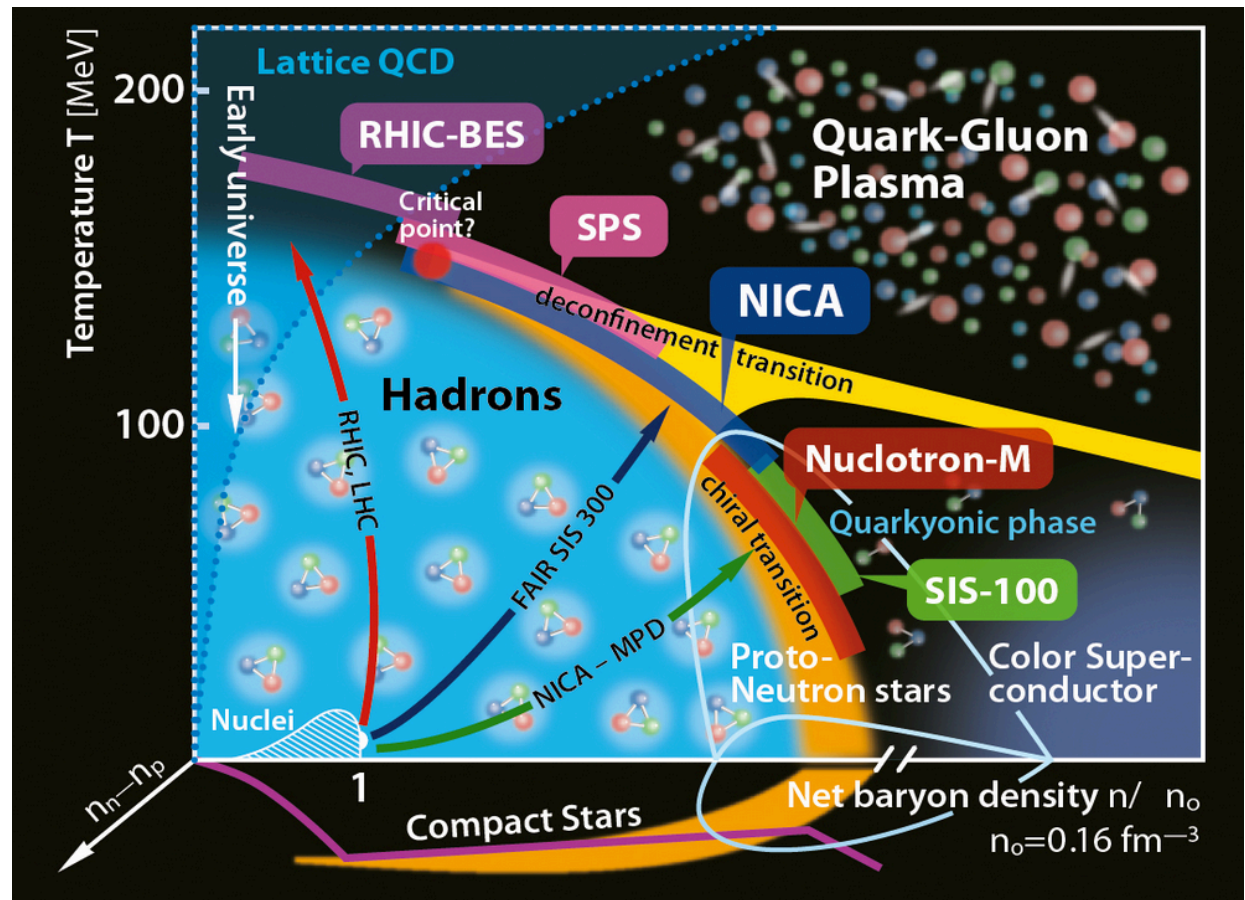
**CLAUDIA RATTI**  
**UNIVERSITY OF HOUSTON**



**BEST**  
COLLABORATION

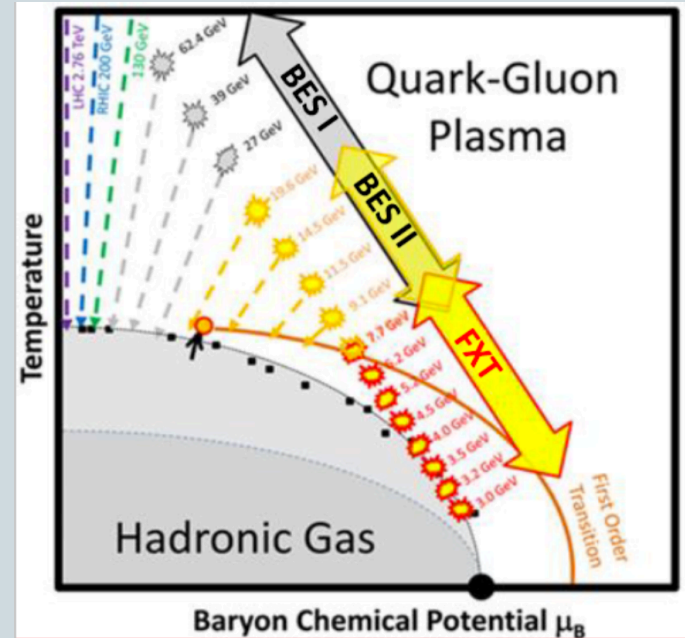
# Open Questions

- Is there a critical point in the QCD phase diagram?
- What are the degrees of freedom in the vicinity of the phase transition?
- Where is the transition line at high density?
- What are the phases of QCD at high density?
- Are we creating a thermal medium in experiments?



# Second Beam Energy Scan (BESII) at RHIC

- Planned for 2019-2020
- 24 weeks of runs each year
- Beam Energies have been chosen to keep the  $\mu_B$  step  $\sim 50$  MeV
- Chemical potentials of interest:  $\mu_B/T \sim 1.5 \dots 4$



$\sqrt{s}$ (GeV)	19.6	14.5	11.5	9.1	7.7	6.2	5.2	4.5
$\mu_B$ (MeV)	205	260	315	370	420	487	541	589
# Events	400M	300M	230M	160M	100M	100M	100M	100M

Collider

Fixed Target 03/30

# Comparison of the facilities

Compilation by D. Cebra

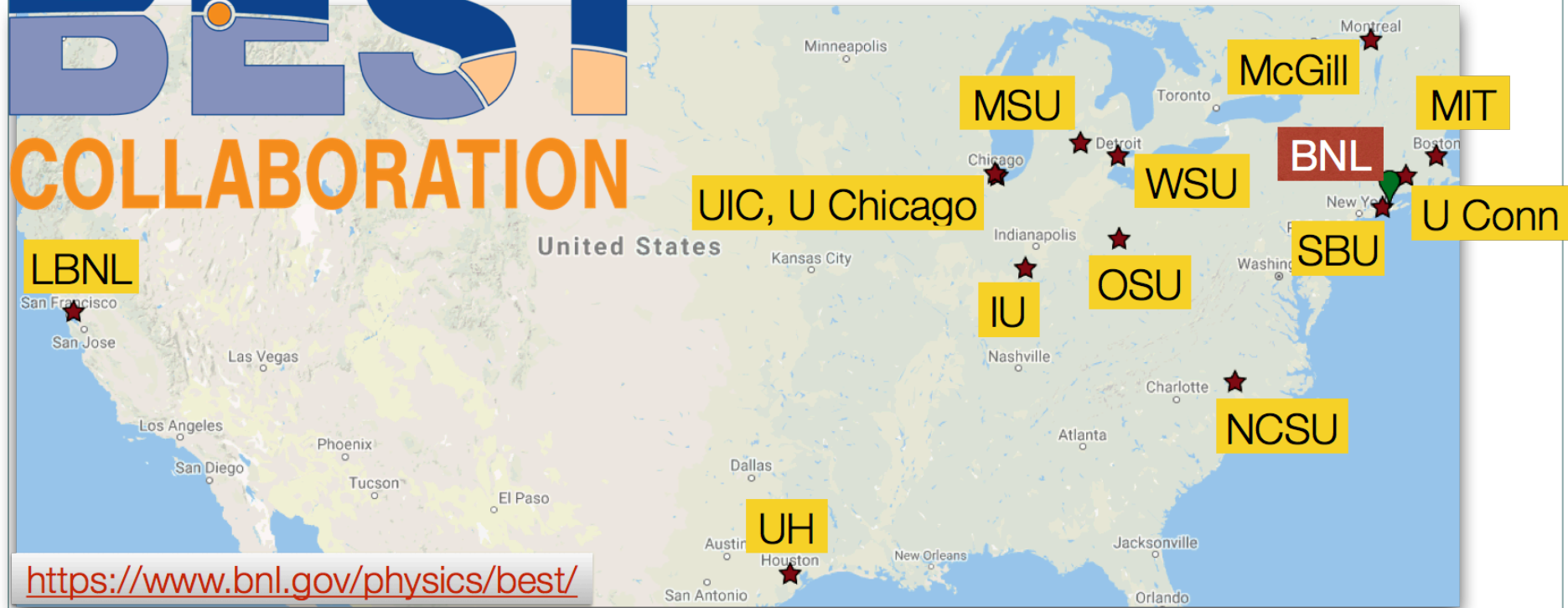
Facility	RHIC BESII	SPS	NICA	SIS-100 SIS-300	J-PARC HI
Exp.:	STAR +FXT	NA61	MPD + BM@N	CBM	JHITS
Start:	2019-20 2018	2009	2020 2017	2022	2025
Energy:	7.7– 19.6	4.9-17.3	2.7 - 11	2.7-8.2	2.0-6.2
$v_{sNN}$ (GeV)	2.5-7.7		2.0-3.5		
Rate:	100 HZ	100 HZ	<10 kHz	<10 MHZ	100 MHZ
At 8 GeV	2000 Hz				
Physics:	CP&OD	CP&OD	OD&DHM	OD&DHM	OD&DHM
	Collider Fixed target	Fixed target Lighter ion collisions	Collider Fixed target	Fixed target	Fixed target

CP=Critical Point    OD= Onset of Deconfinement    DHM=Dense Hadronic Matter



# BEST

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### objectives:

- constraints on the existence of a critical point in the QCD phase diagram
- properties of baryon-rich QGP
- probe chiral symmetry restoration through chiral anomaly induced phenomena

### path:

- construct a theoretical framework for interpreting the results from the BES @ RHIC

# BEST COLLABORATION



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# Hot and dense lattice QCD

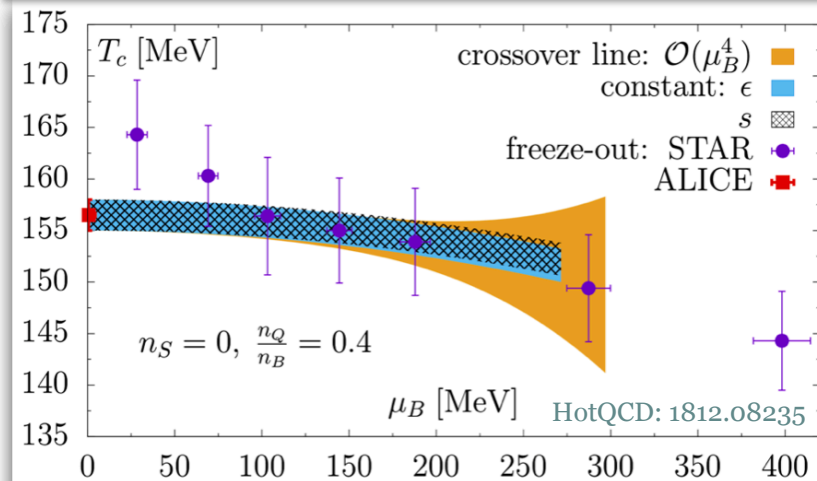
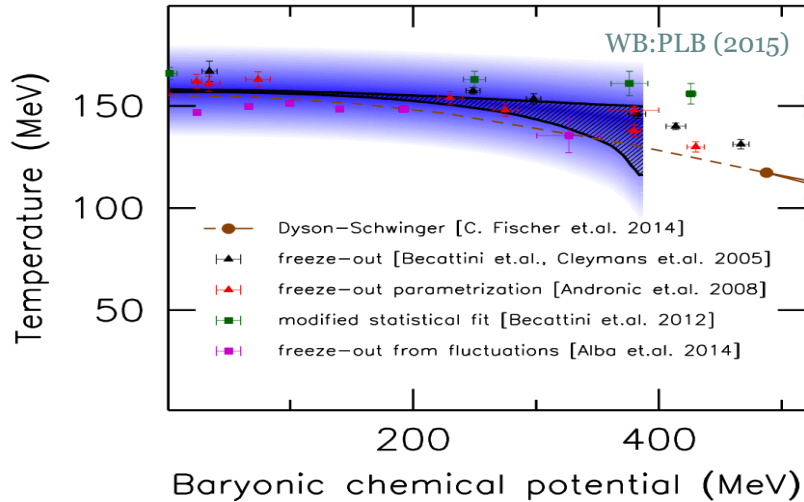


BNL, UH

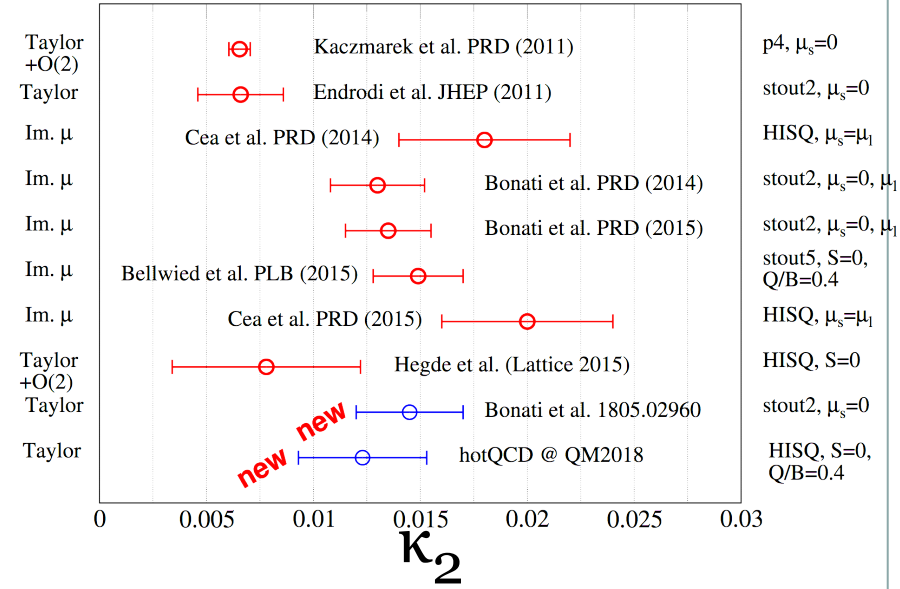
Major goals:

- **QCD crossover temperature  $T_c(\mu_B)$** 
  - switching temperature/energy density for fluid-dynamical modeling
- **QCD equation of state (EoS) for  $\mu_B > 0$** 
  - input for fluid-dynamical modeling & EoS with critical point
- **skewness and kurtosis of conserved charge fluctuations for  $\mu_B > 0$** 
  - equilibrium QCD baseline for the experimentally measured higher order cumulants of net proton, electric charge and kaon fluctuation

# QCD crossover temperature



Compilation by F. Negro



$$T_0 = 156.5 \pm 1.5 \text{ MeV}$$

$$\frac{T_c(\mu_B)}{T_0} = 1 - \kappa_2 \left( \frac{\mu_B}{T_0} \right)^2 - \kappa_4 \left( \frac{\mu_B}{T_0} \right)^4 + \mathcal{O}(\mu_B^6)$$

Curvature very small at  $\mu_B=0$

# QCD Equation of state for $\mu_B > 0$

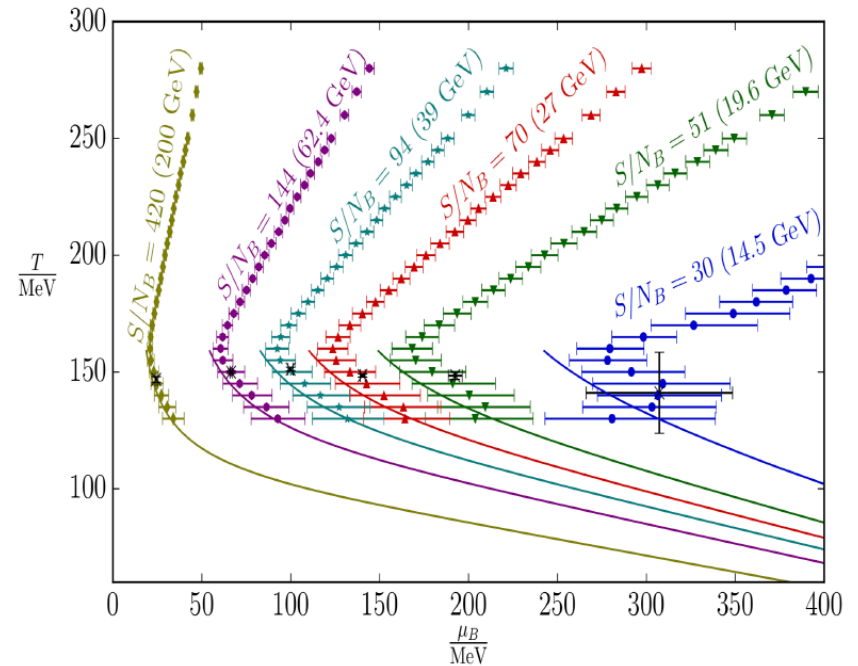
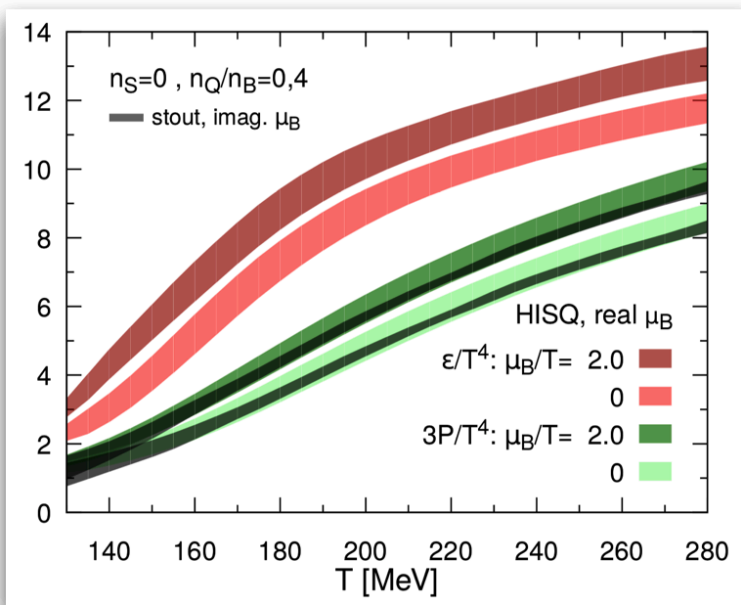


- Taylor expansion of the pressure:

$$\frac{p(T, \mu_B)}{T^4} = \frac{p(T, 0)}{T^4} + \sum_{n=1}^{\infty} \frac{1}{(2n)!} \frac{d^{2n}(p/T^4)}{d(\frac{\mu_B}{T})^{2n}} \Big|_{\mu_B=0} \left(\frac{\mu_B}{T}\right)^{2n} = \sum_{n=0}^{\infty} c_{2n}(T) \left(\frac{\mu_B}{T}\right)^{2n}$$

HotQCD: PRD (2017)

WB: NPA (2017)



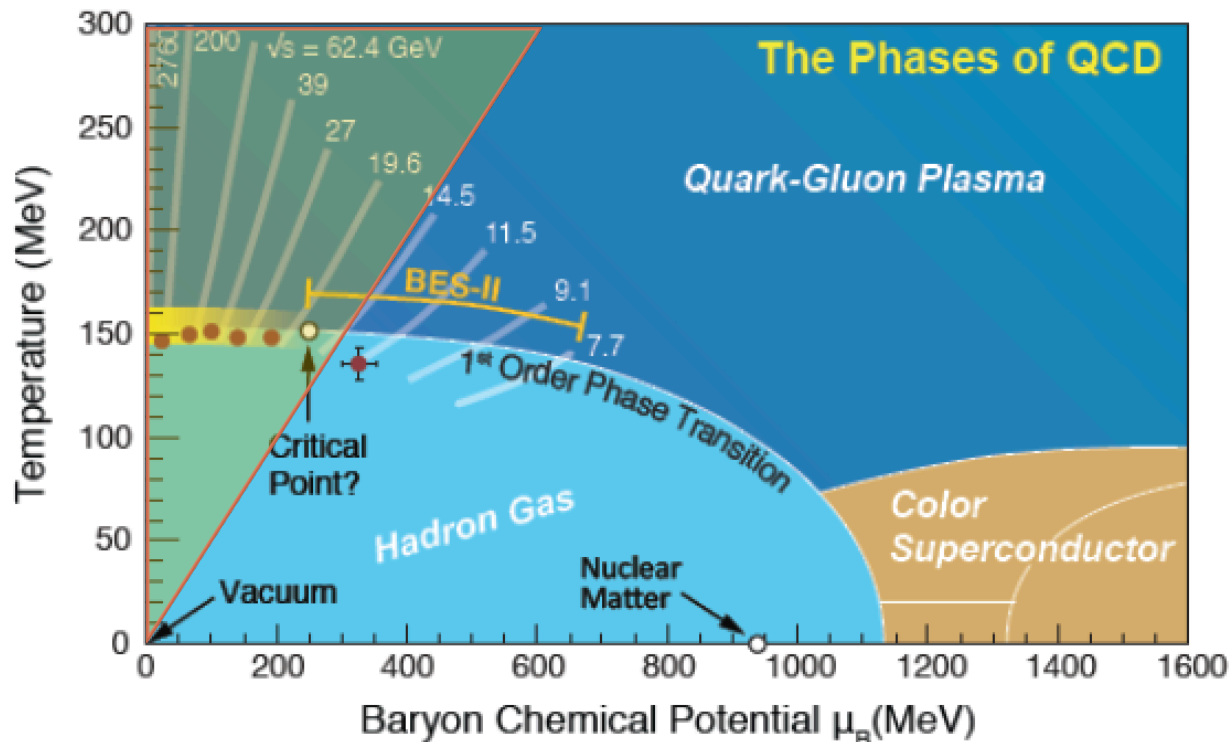


# QCD Equation of state for $\mu_B > 0$



- We now have the equation of state for  $\mu_B/T \leq 2$  or in terms of the RHIC energy scan:

$$\sqrt{s} = 200, 62.4, 39, 27, 19.6, 14.5 \text{ GeV}$$

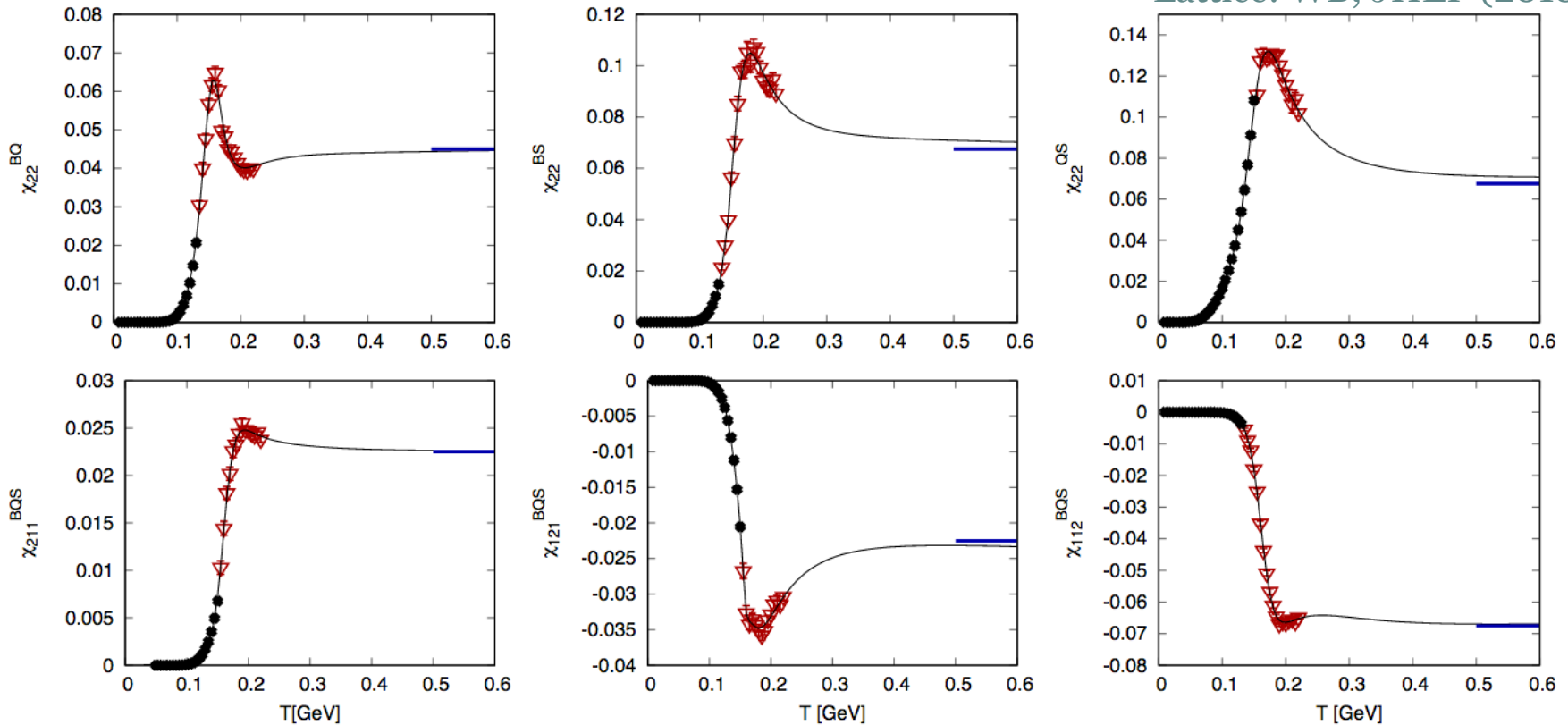


# QCD Equation of state for $\mu_B, \mu_S, \mu_Q > 0$

 Noronha-Hostler, C.R. et al., 1902.06723

$$\frac{p(T, \mu_B, \mu_Q, \mu_S)}{T^4} = \sum_{i,j,k} \frac{1}{i!j!k!} \chi_{ijk}^{BQS} \left(\frac{\mu_B}{T}\right)^i \left(\frac{\mu_Q}{T}\right)^j \left(\frac{\mu_S}{T}\right)^k$$

Lattice: WB, JHEP (2018)

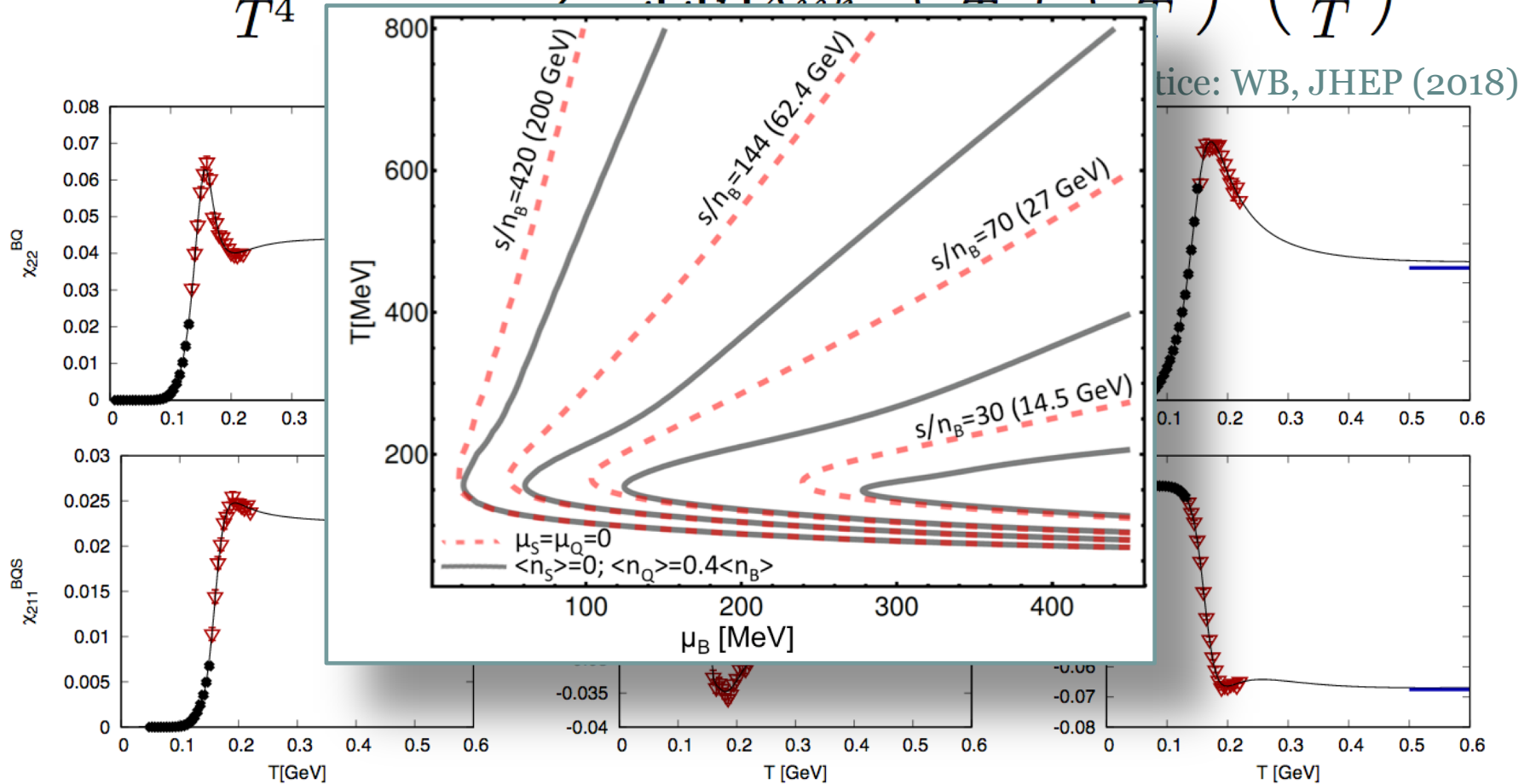


See also A. Monnai et al., 1902.05095

# QCD Equation of state for $\mu_B, \mu_S, \mu_Q > 0$

Noronha-Hostler, C.R. et al., 1902.06723

$$\frac{p(T, \mu_B, \mu_Q, \mu_S)}{T^4} = \sum_{i,j,k} \frac{1}{\chi_{ijk}^{BQS}} \left(\frac{\mu_B}{T}\right)^i \left(\frac{\mu_Q}{T}\right)^j \left(\frac{\mu_S}{T}\right)^k$$



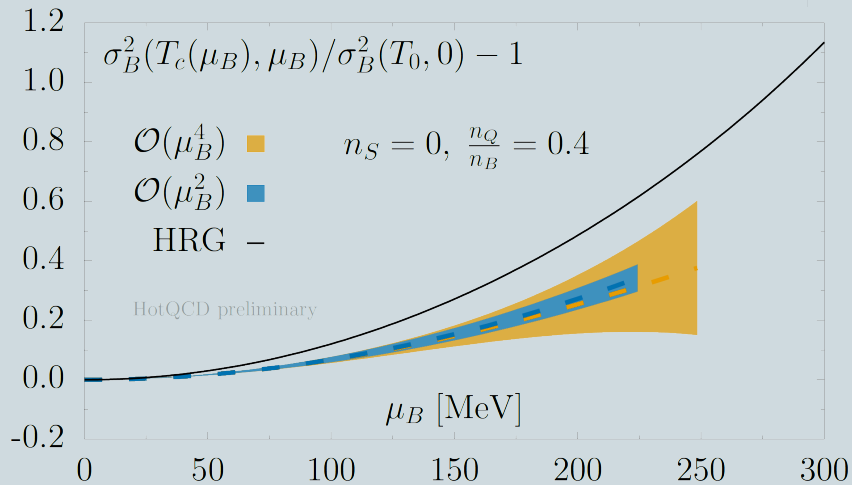
See also A. Monnai et al., 1902.05095

# Fluctuations along the QCD crossover

P. Steinbrecher for HotQCD, 1807.05607

## Net-baryon variance

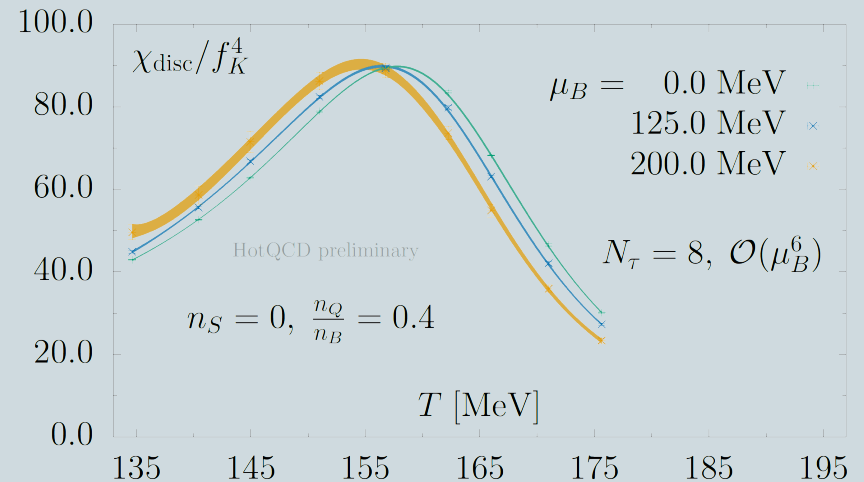
$$\frac{\sigma_B^2(T_c(\mu_B), \mu_B) - \sigma_B^2(T_0, 0)}{\sigma_B^2(T_0, 0)} = \lambda_2 \left(\frac{\mu_B}{T_0}\right)^2 + \lambda_4 \left(\frac{\mu_B}{T_0}\right)^4 + \mathcal{O}(\mu_B^6)$$



- Expected to be larger than HRG model result near the CP
- No sign of criticality

## Disconnected chiral susceptibility

$$\chi_{\text{sub}} \equiv \frac{T}{V} m_s \left( \frac{\partial}{\partial m_u} + \frac{\partial}{\partial m_d} \right) \left[ m_s (\Sigma_u + \Sigma_d) - (m_u + m_d) \Sigma_s \right]$$

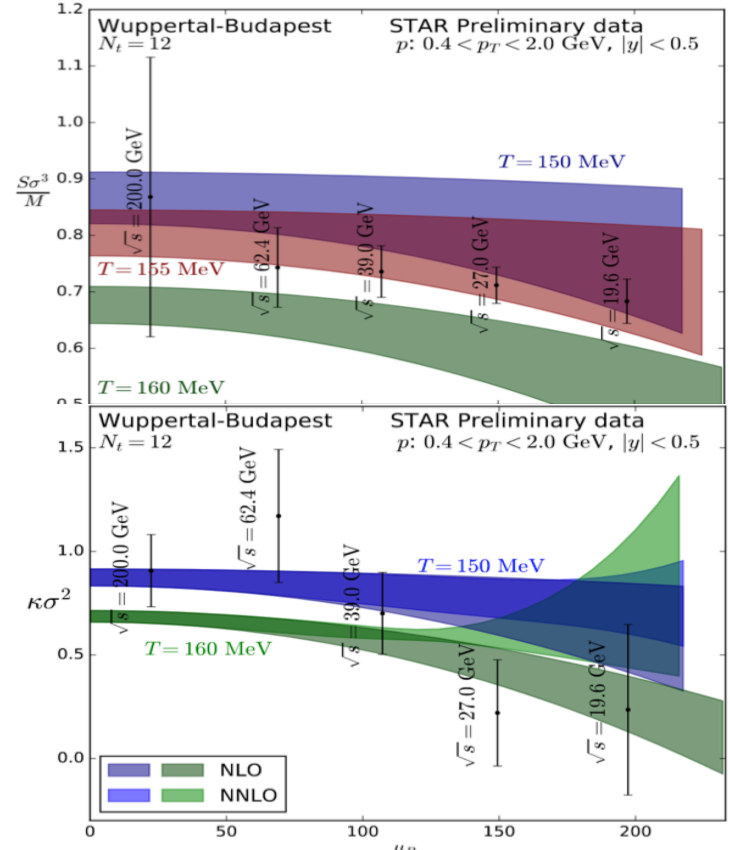
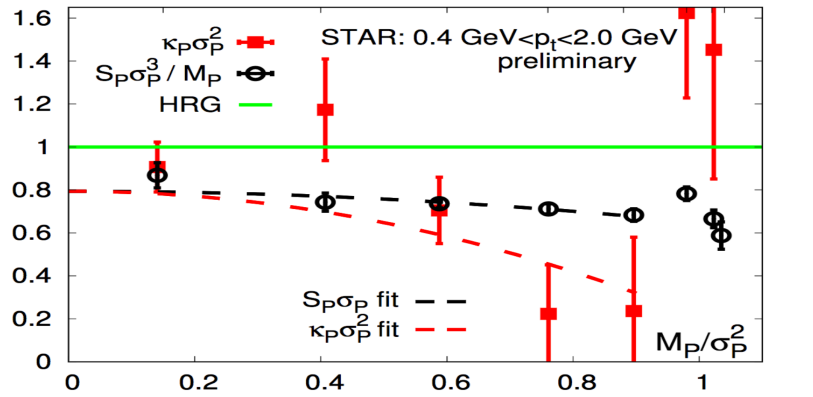
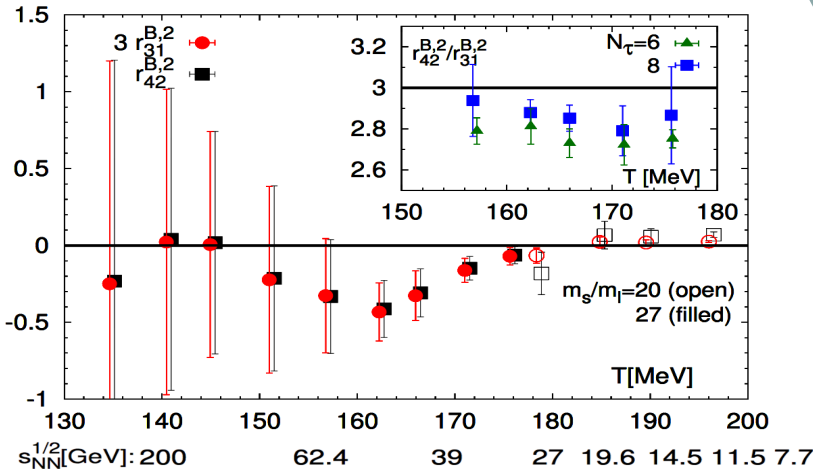


- Peak height expected to increase near the CP
- No sign of criticality

# Higher order fluctuations

HotQCD, PRD (2017)

WB, JHEP (2018)



$$\frac{S_B \sigma_B^3}{M_B} = \frac{\chi_3^B(T, \mu_B)}{\chi_1^B(T, \mu_B)} = \frac{\chi_4^B + s_1 \chi_{31}^{BS} + q_1 \chi_{31}^{BQ}}{\chi_2^B + s_1 \chi_{11}^{BS} + q_1 \chi_{11}^{BQ}} + \mathcal{O}(\mu_B^2) \equiv r_{31}^{B,0} + r_{31}^{B,2} \hat{\mu}_B^2 + \mathcal{O}(\mu_B^4)$$

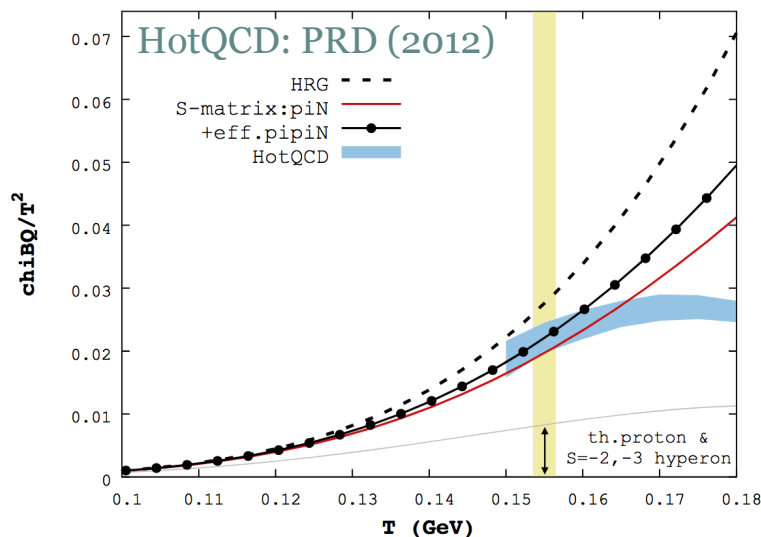
$$\kappa_B \sigma_B^2 = \frac{\chi_4^B(T, \mu_B)}{\chi_2^B(T, \mu_B)} = \frac{\chi_4^B}{\chi_2^B} + \mathcal{O}(\mu_B^2) \equiv r_{42}^{B,0} + r_{42}^{B,2} \hat{\mu}_B^2 + \mathcal{O}(\mu_B^4),$$

P. Braun Munzinger et al.,  
NPA (2017)

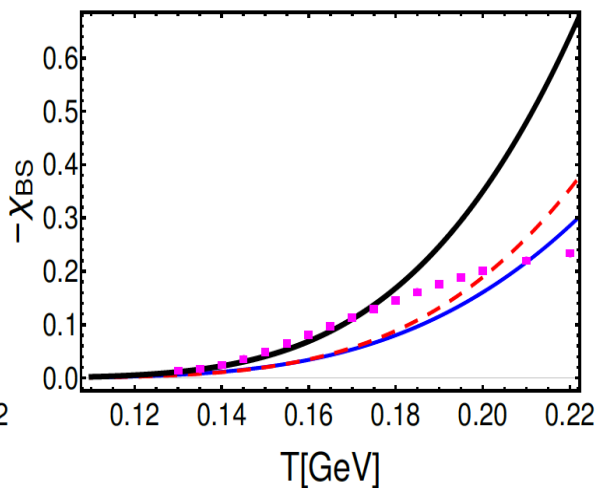
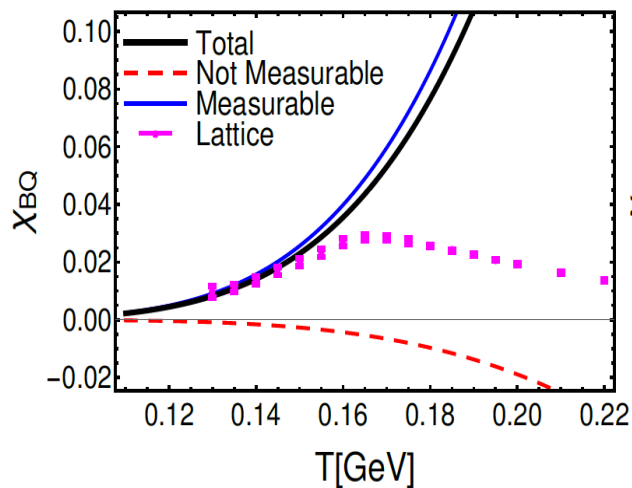
Alternative explanation:  
canonical suppression

# B, Q, S correlators

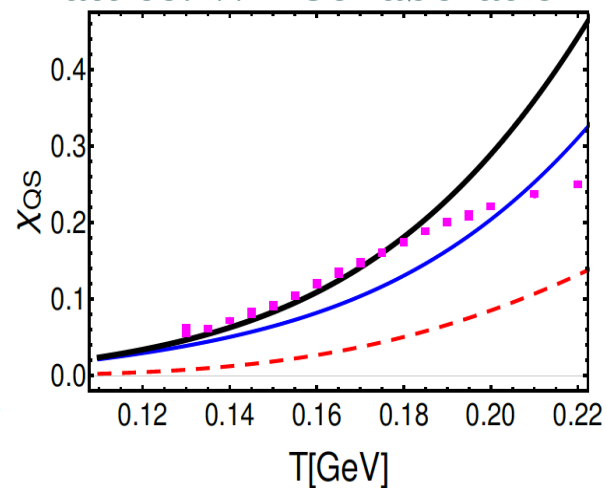
See talk by P. Parotto on Thursday



- Measurements from STAR are becoming available
- How to bring the experimental measurements close to lattice QCD?
- Calculate all measurable contributions

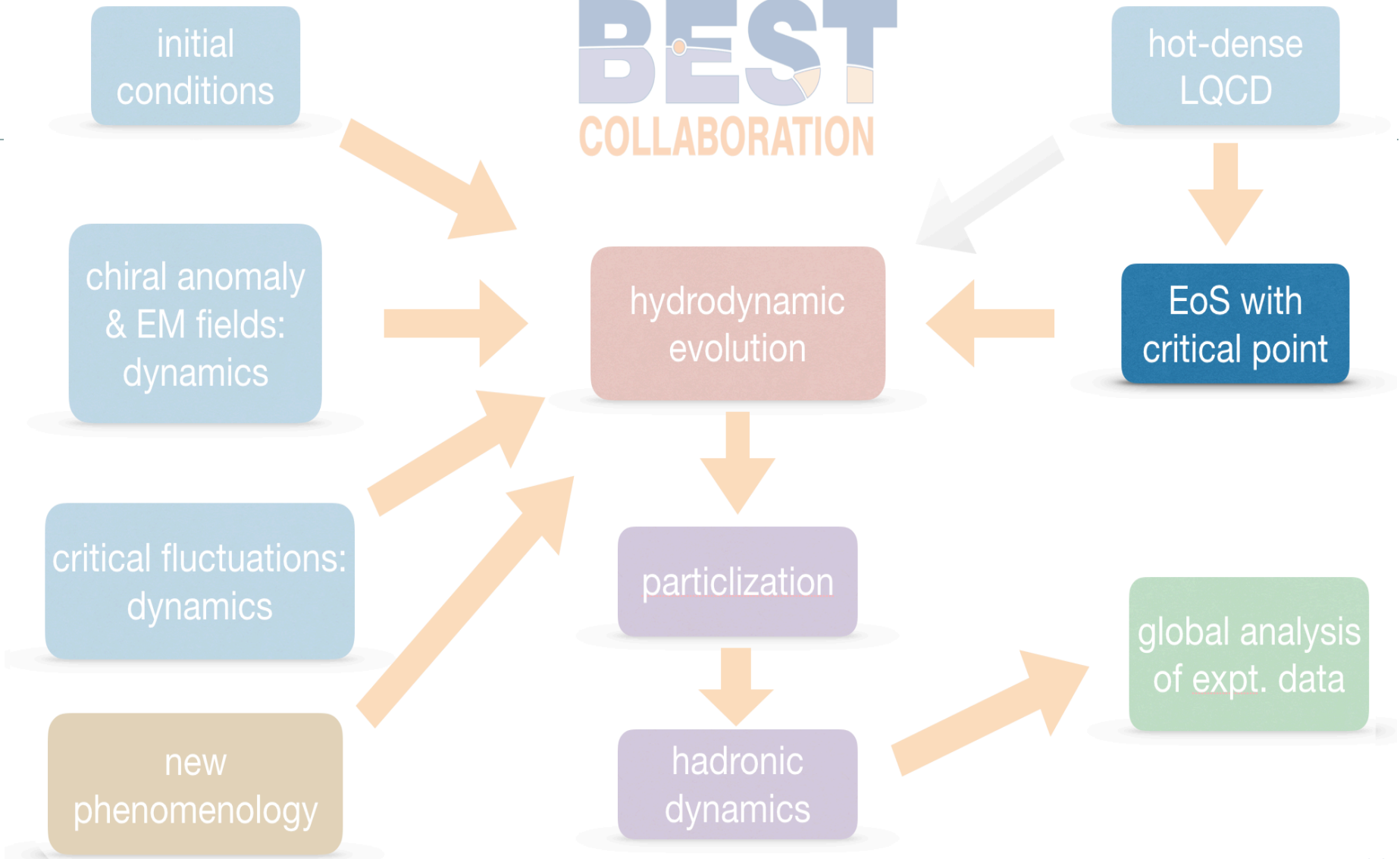


Lattice: WB Collaboration





# BEST COLLABORATION



# Strategy



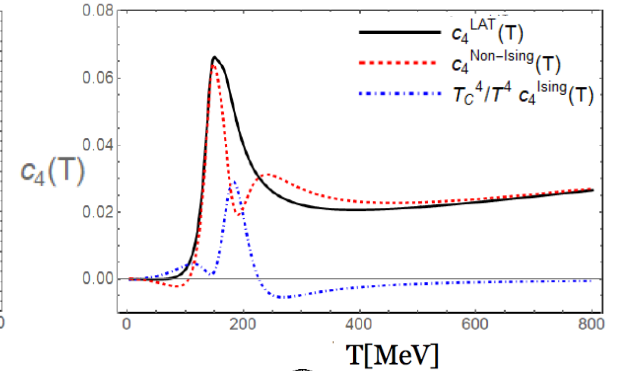
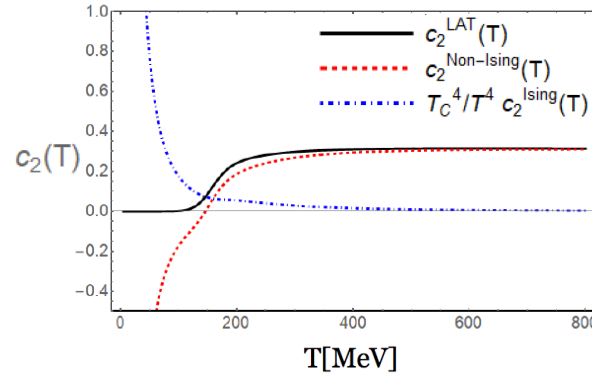
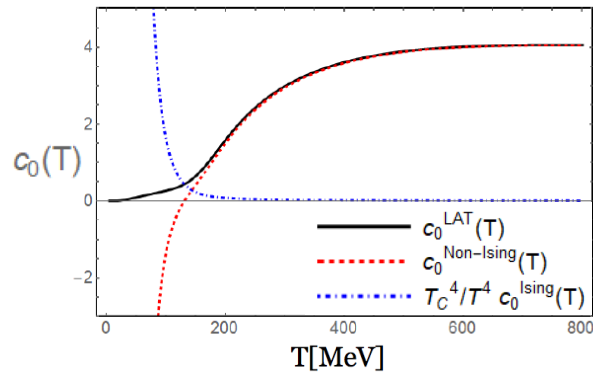
- ✓ We built an equation of state which:
  - ✓ Reproduces the one from lattice QCD up to  $O(\mu_B^4)$  (provided by the BEST lattice QCD effort)
  - ✓ Contains a critical point in the 3D Ising model universality class
  - ✓ Can be readily used as input for hydrodynamic simulations to test the effect of the critical point on observables (has already been tested by the BEST hydro working group)
- Future hydro simulations and comparison with BESII data will help to constrain the position of the critical point
- ✓ Code available for everybody to use  
(download from <https://www.bnl.gov/physics/best/resources.php>)

# Expansion coefficients and EoS

P. Parotto et al.: hep-ph/1805.05249

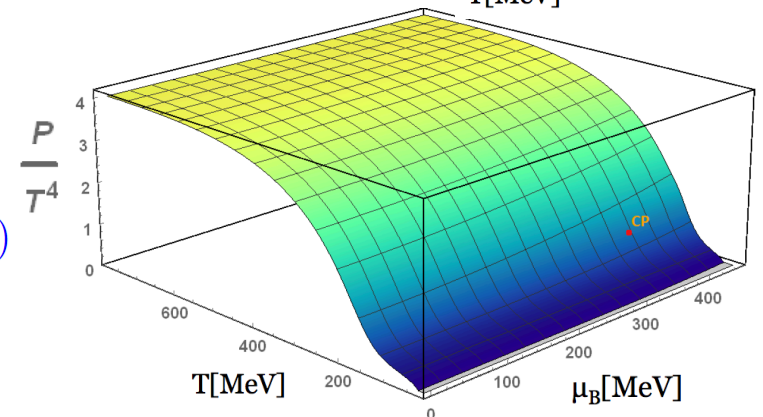
Extract the “regular” contribution as the difference between the lattice and Ising ones

$$T^4 c_n^{\text{LAT}}(T) = T^4 c_n^{\text{Non-Ising}}(T) + T_C^4 c_n^{\text{Ising}}(T)$$



Total pressure becomes:

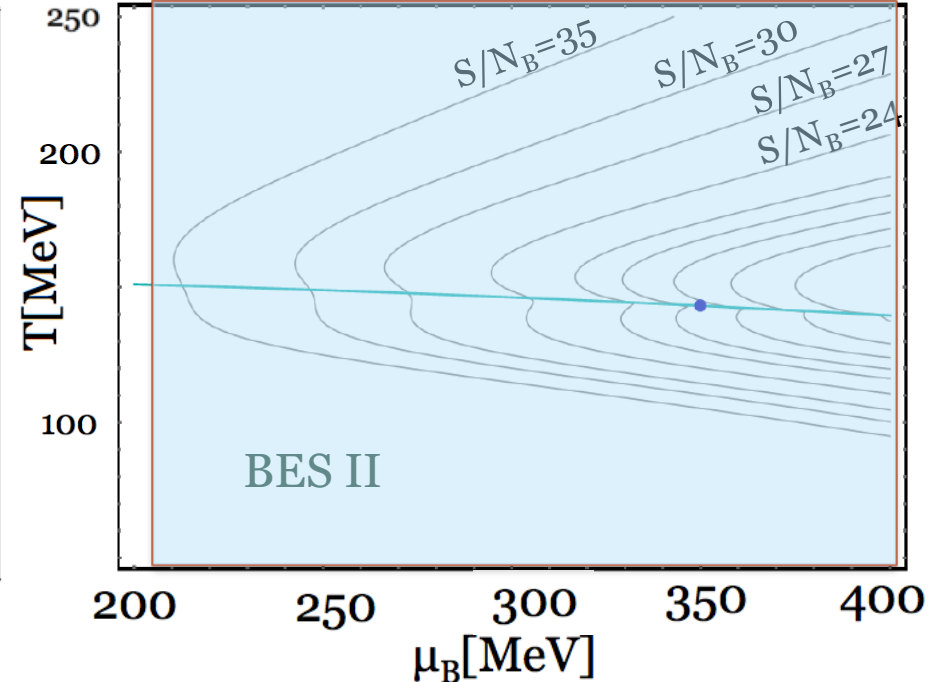
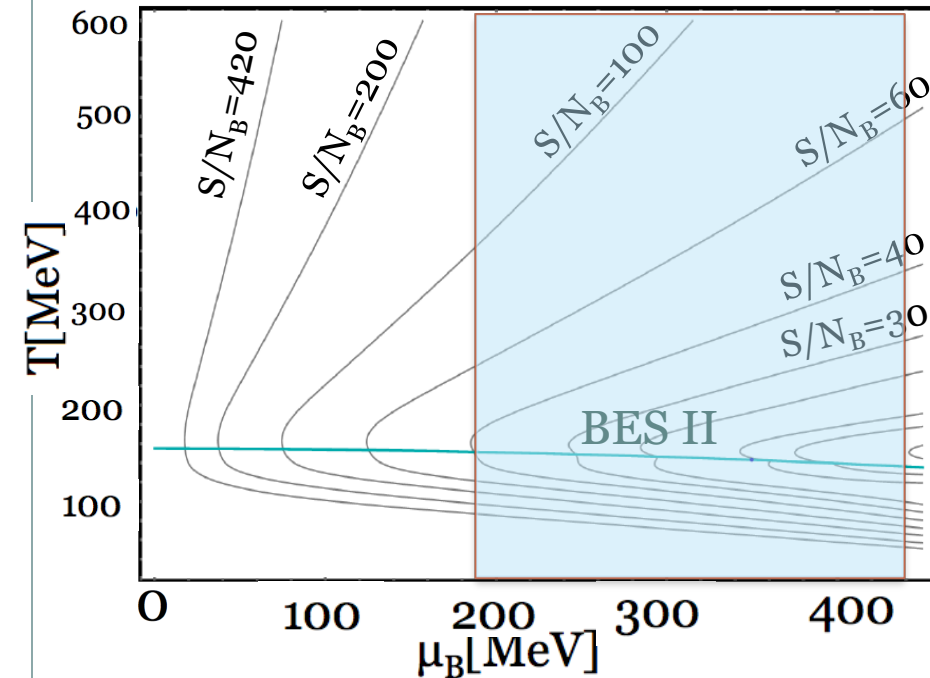
$$P(T, \mu_B) = T^4 \sum_n c_{\text{Non-Ising}}^n(T) \left(\frac{\mu_B}{T}\right)^n + T_C^4 P_{\text{Ising}}(T, \mu_B)$$



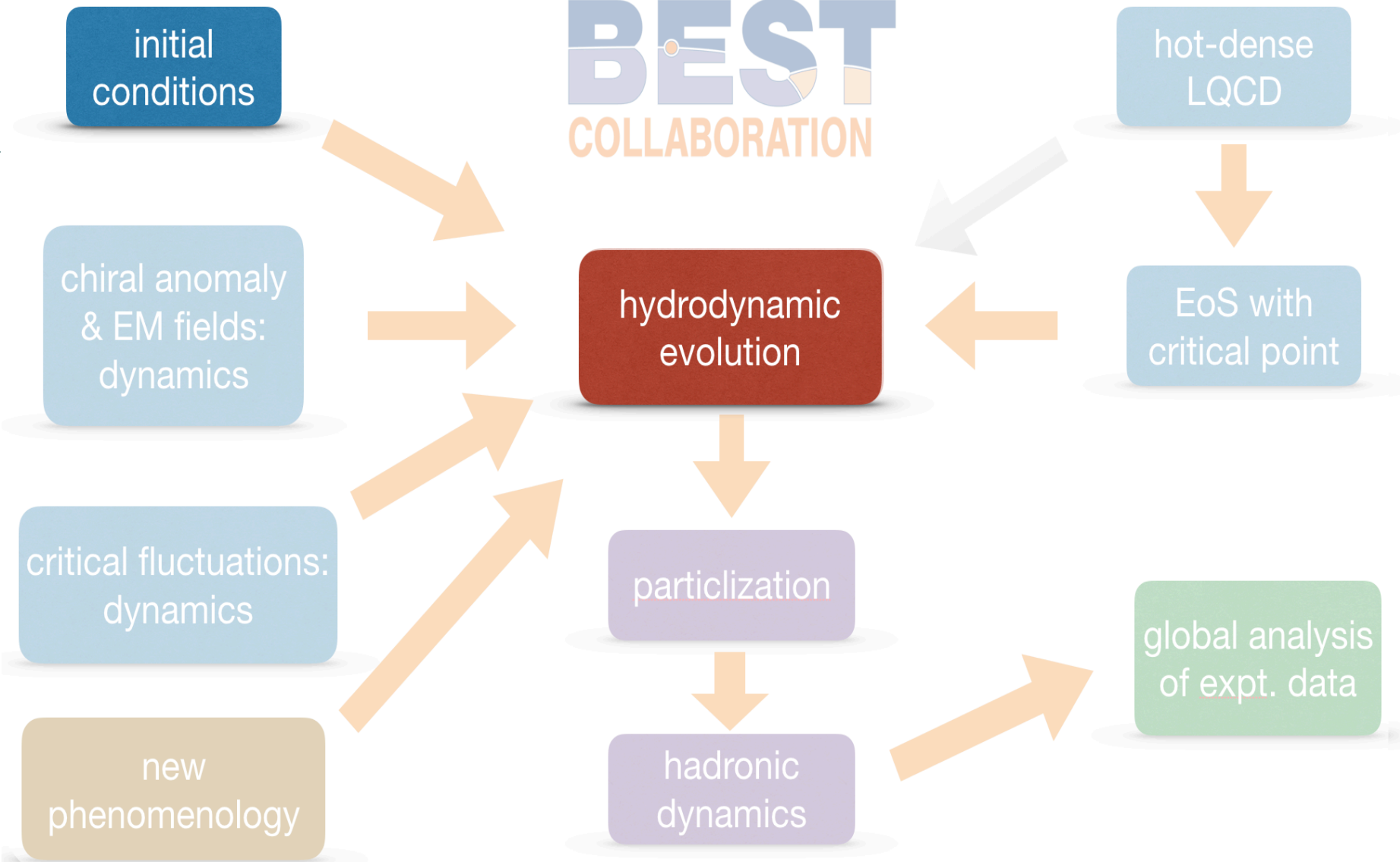
# Final EoS: Isentropic trajectories

P. Parotto et al.: hep-ph/1805.05249

- ▶ Relevant for hydrodynamic evolution are the lines of  $s/n_B = \text{const}$ :
  - ▶ Low- $\mu_B$ : match behavior from Lattice QCD
  - ▶ Close to the CP: some structure appears



# BEST COLLABORATION



# Scientific goals



- Model the fluctuating initial conditions for the baryon-asymmetric matter for baryon, electric charge, and strangeness  
C. Shen, B. Schenke, PRC (2018)  
C. Shen, B. Schenke, NPA (2019)
- Develop **(3+1)D** viscous hydrodynamic code which includes all conserved currents and connect it to model for initial conditions  
G. Denicol et al., PRC (2018)  
L. Du et al., NPA (2019)
- Extract transport properties of nuclear matter at finite baryon density  
M. Li, C. Shen, PRC (2018)  
C. Gale et al., NPA (2019)



# Hydrodynamics evolution

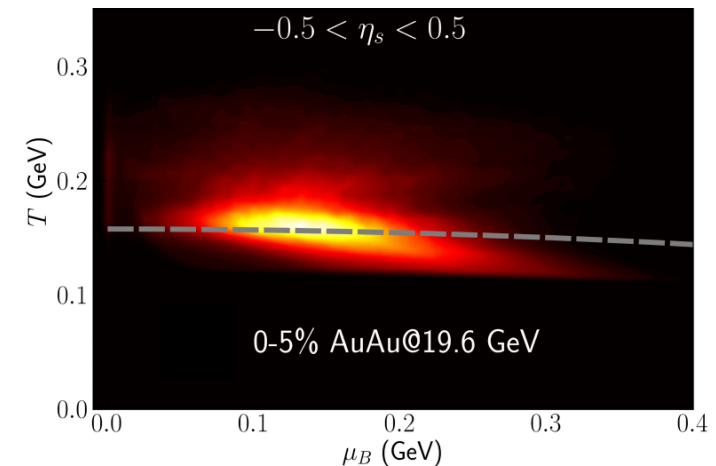
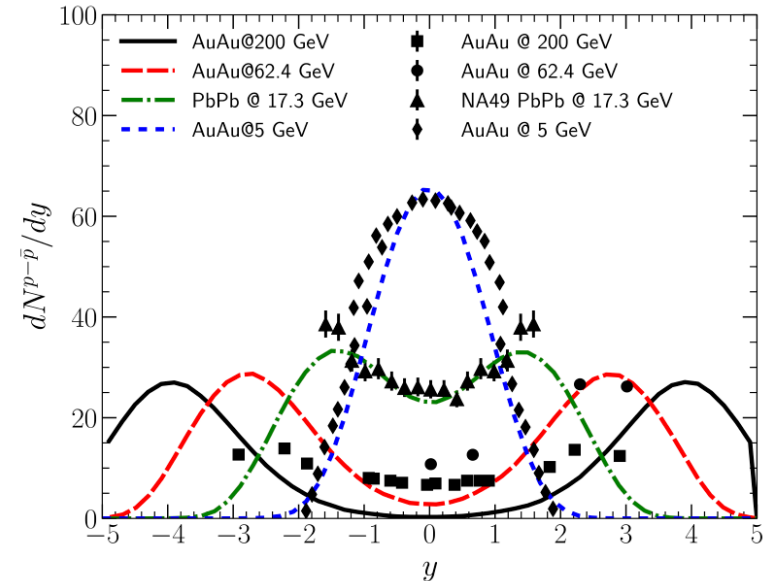
See talk by U. Heinz this afternoon

- The sequential collisions between nucleons contribute as energy-momentum and net-baryon density **sources** to the hydrodynamic fields

C. Shen, B. Schenke, PRC (2018);  
L. Du et al., NPA (2019)

- relativistic viscous hydrodynamic simulations extended to include the propagation of net baryon current including its dissipative diffusion

C. Shen, B. Schenke, NPA (2018)



# BEST COLLABORATION



# Scientific goals



One of the central goals of the BEST collaboration is to develop quantitative understanding of the fluctuations near the CP

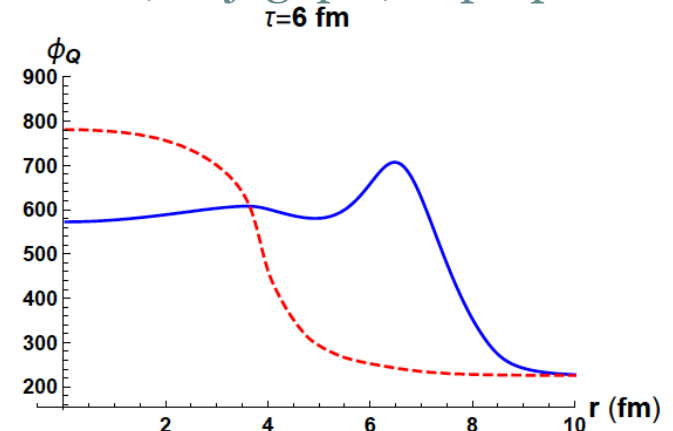
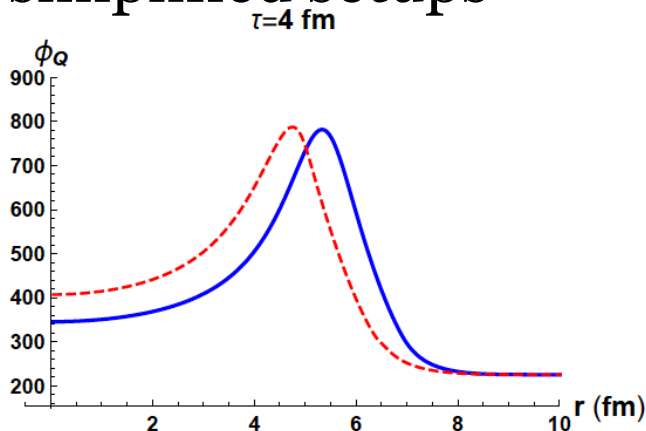
- Develop, implement and test a hydrodynamic formalism which incorporates hydrodynamic and critical fluctuations
- Incorporate hydro fluctuations into the evolution code and include the coupling of the hydro fluid to the chiral mean field
- Use the resulting stochastic hydro code to map out the effects of critical fluctuations on different fluctuation observables

Complementary approach: hydro with noise (Nahrgang, Bluhm, Schaefer, Bluhm)

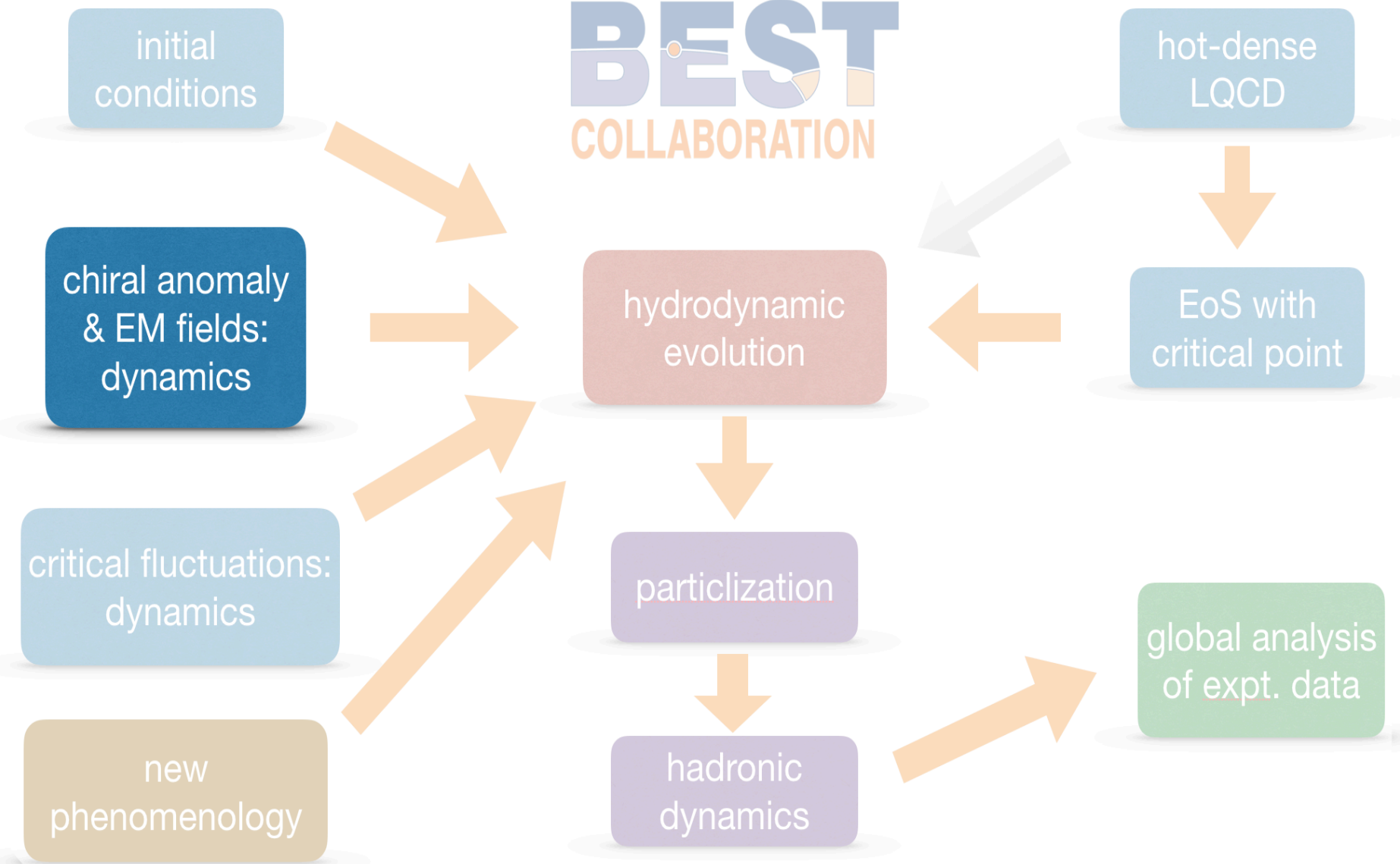
# Hydro+ and its implementation



- Consistent description of bulk hydrodynamics, out-of-equilibrium critical fluctuations, and the feedback between them  
M. Stephanov, Y. Yin, PRD (2018)
- Hydro+ equations for  $\epsilon$ ,  $n$ ,  $u$  and  $\phi_Q$  are deterministic and follow from 2PI-like entropy  $s_+(\epsilon, n; \phi_Q)$ .
- Hydro+ implemented in VH1+1 hydro code and tested in simplified setups  
Yin, Ridgway, Weller, Rajagopal, in preparation



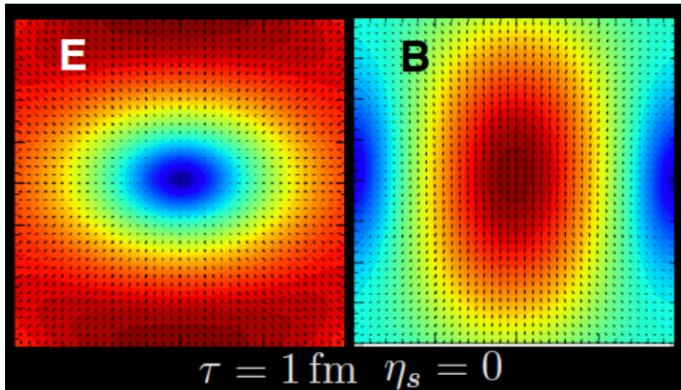
# BEST COLLABORATION



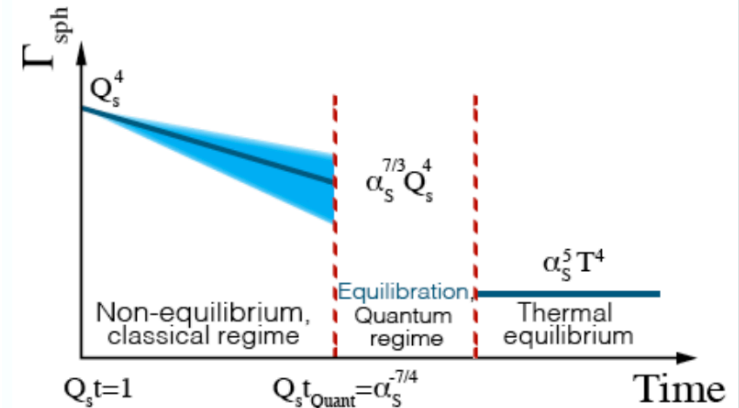
# Scientific goals and achievements

- Model fluctuating initial conditions for axial charges

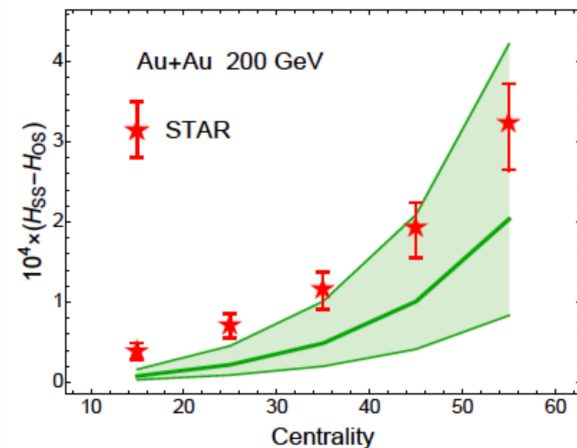
Mace et al., PRD (2016)



- Quantitatively characterize the experimental signals of CME
- Shi et al., Annals of Physics (2018)



- Develop magneto-hydro code and incorporate anomalous hydro terms
- Kharzeev et al., PRC (2018)





# BEST COLLABORATION



# Particlization



- Develop the interface between the hydrodynamic evolution and hadronic transport, such that it preserves fluctuations
- Standard procedure: Cooper-Frye

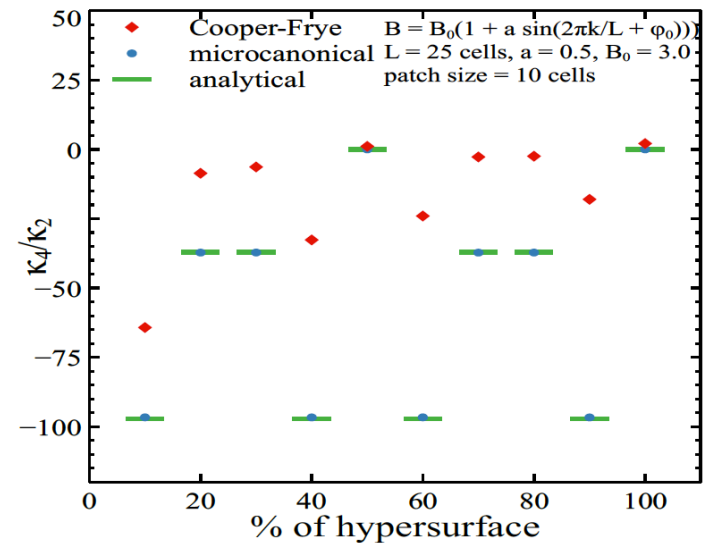
➡ additional (Poisson) fluctuations from Cooper-Frye freeze out  
adds extra (un-physical) fluctuations and washes out correlations

J. Steinheimer, V. Koch, PRC (2017)

- Solution: (micro-canonical) Metropolis sampling algorithm

- conserves all the charges as well as energy and momentum as given by hydrodynamics

D. Oliinychenko, V. Koch, 1902.09775



# Future plans

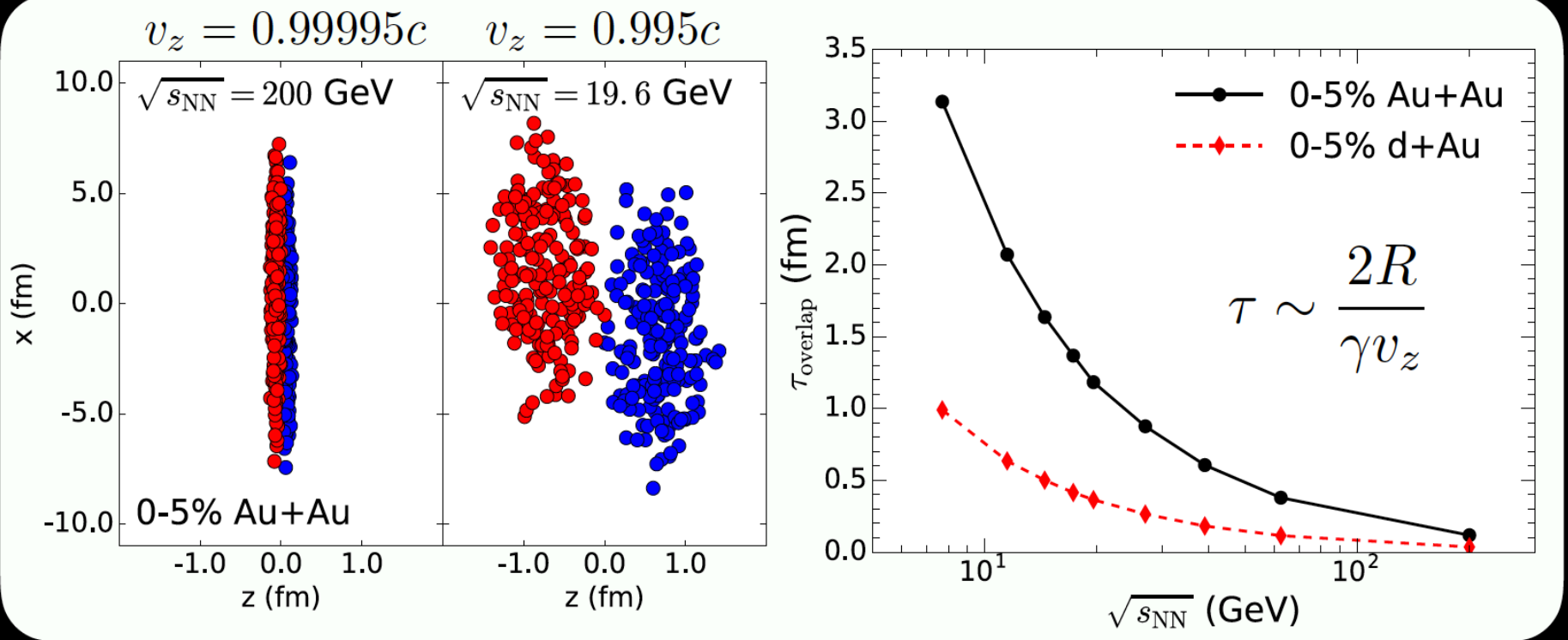


- Extend the lattice calculations to  $\mu_B \sim 400$  MeV
- Complete and integrate “hydro+” and/or stochastic hydrodynamics into the code base
- Combine the particlization and transport code SMASH with the bulk hydrodynamics code
- Perform large-scale numerical simulations with the Bayesian statistical approach to constrain the theoretical framework using the experimental measurements

# Backup Slides

# Heavy-ion collisions at RHIC BES

I. A. Karpenko, P. Huovinen, H. Petersen and M. Bleicher, Phys. Rev. C91 (2015) 064901  
C. Shen and B. Schenke, Phys. Rev. C97 (2018) 024907



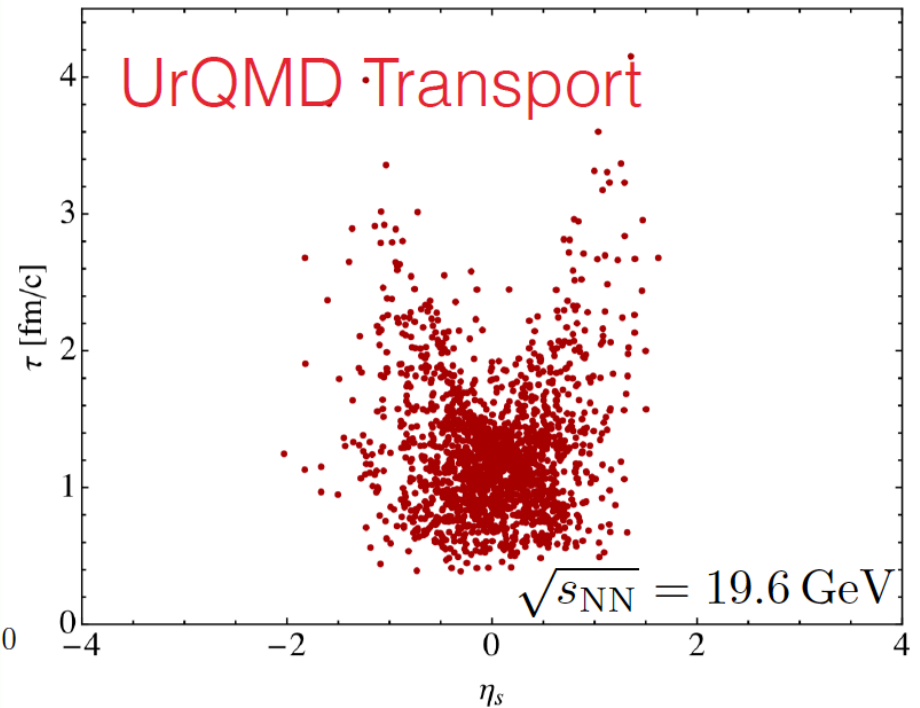
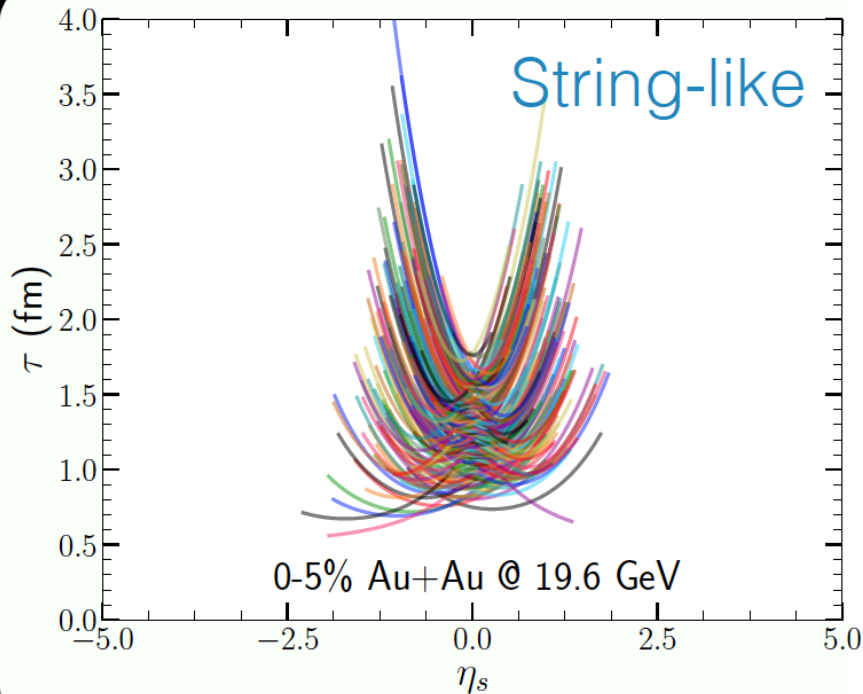
- Nuclei overlapping time is **large** at low collision energy
- **Pre-equilibrium dynamics** can play an important role

note: total evolution time  $\sim 10$  fm

# Energy-momentum space-time distribution

C. Shen and B. Schenke, Phys. Rev. C97 (2018) 024907

L. Du, U. Heinz and G. Vujanovic, Nucl. Phys. A982 (2019) 407-410

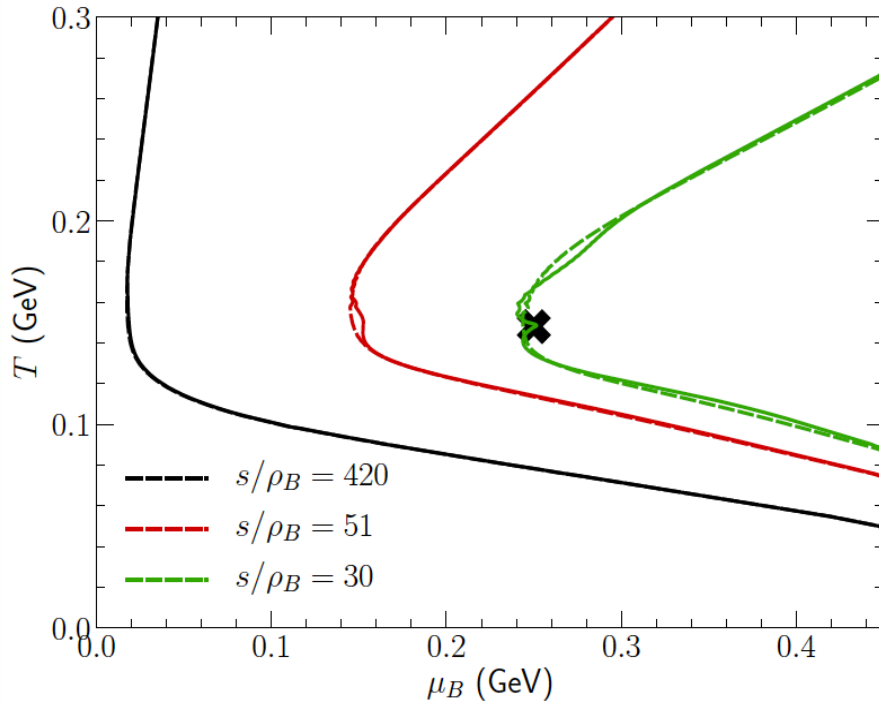


- An extended interaction zone for the energy-momentum sources from the 3D collision geometry

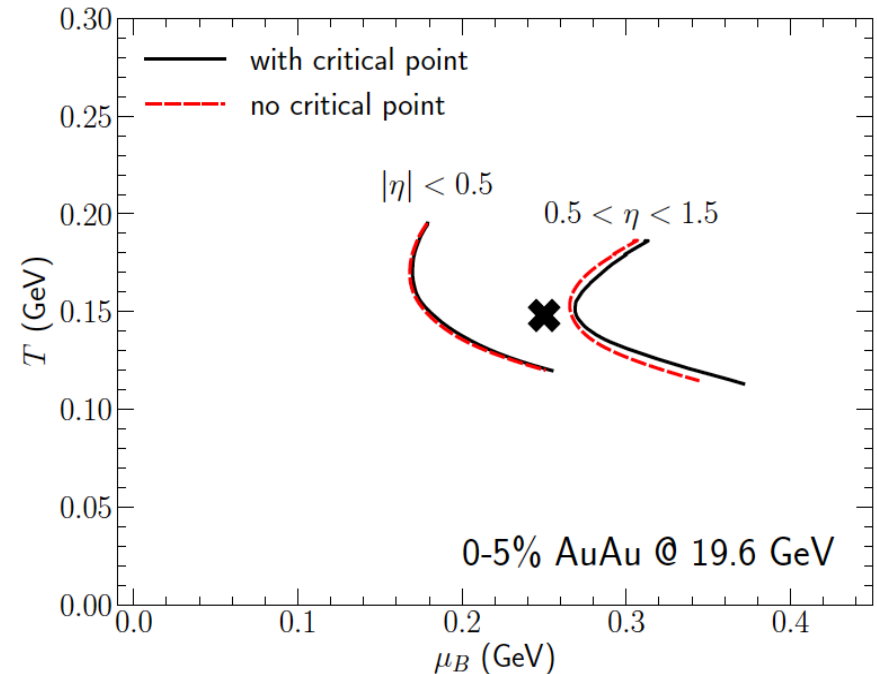
**Dynamically interweaves with hydrodynamics**

# BEST EOS with a critical point

P. Parotto et al., arXiv:1805.05249 [hep-ph]



B. Schenke and C. Shen, in preparation



- The BEST EOS is implemented in the state-of-the-art 3D hydrodynamic code (MUSIC)

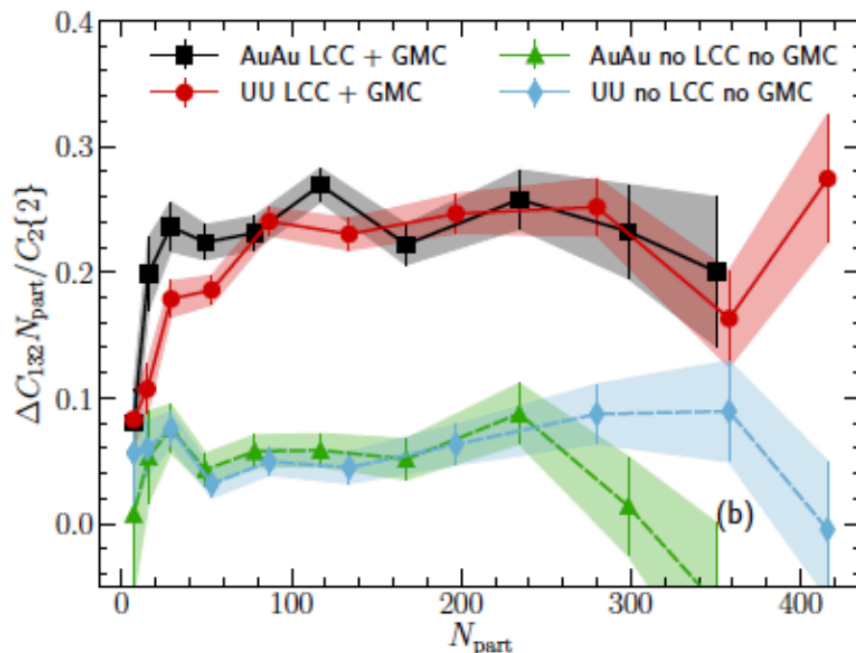
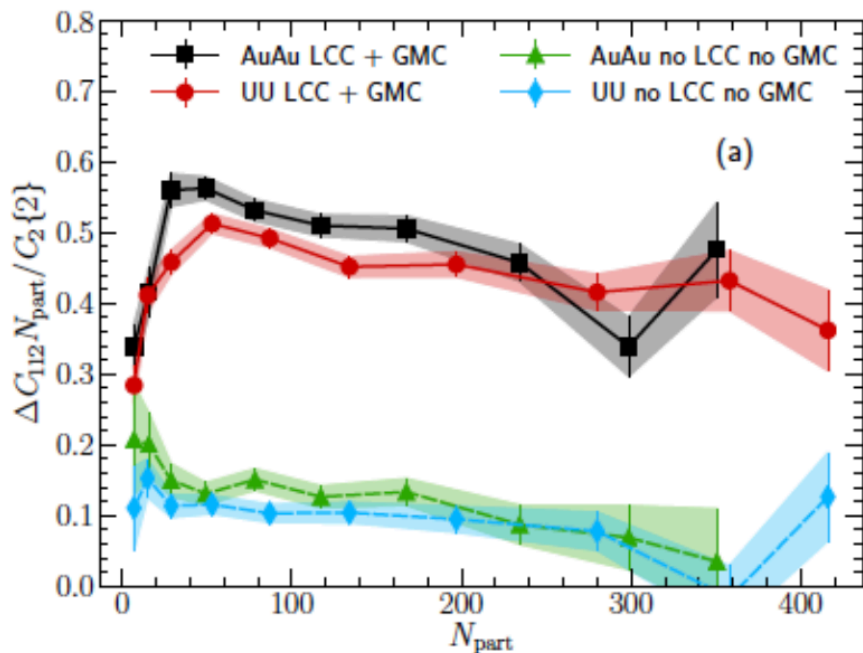
Visible difference in the fireball trajectories with a critical point



# CME Working Group Achievements

## Specific Goals #2 & #4:

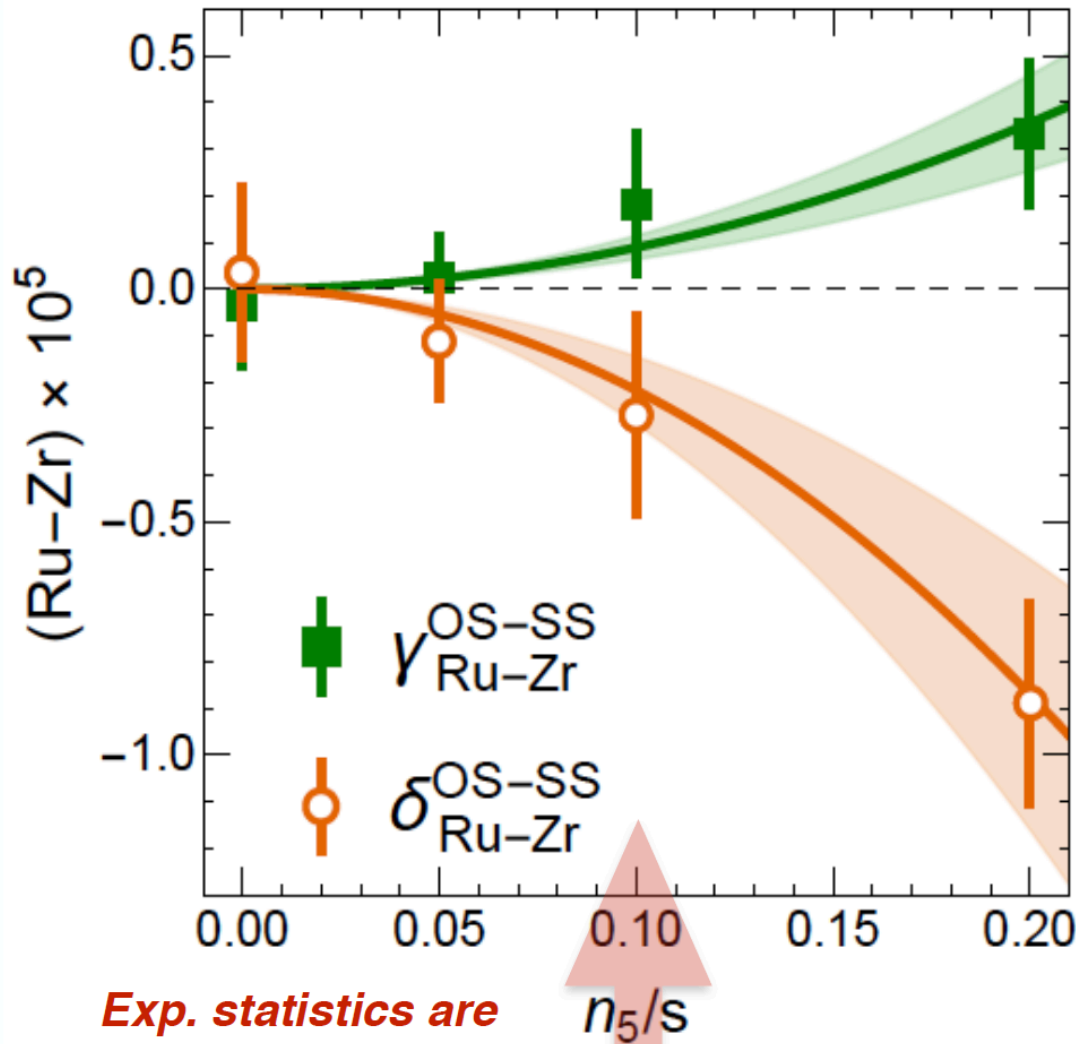
– “...backgrounds”



*A detailed quantification of various background correlations in the data-validated state-of-art hydrodynamic framework*

*[Schenke, Shen, Tribedy, 2019]*

# New Opportunity: Isobaric Collisions



*AVFD predictions for CME signals in isobars*

**EBE-AVFD:**  
*Include EBE fluctuations*

- ▶ Initial Conditions
- ▶ Statistic @ Freeze-out
- ▶ Hadron Cascade

*[Shi, JL, ..., QM2018]*  
*[BEST: IU-McGill]*

*Exp. statistics are expected to shrink error bar by a factor of ~10*

*Projected axial charge level based on comparison AuAu data*

# Data analysis

## GOAL: Bayesian Comparison of BEST models to BES data

- Collect and distill data (once BES data are available)
  - state uncertainties
- Parameterize BEST beginning-to-end model
  - a few dozen parameters; once model is available
- Construct and tune model emulator
  - Gaussian process or machine learning
  - Requires significant computational resources
- Determine (including uncertainty) likelihood of parameters
  - Markov Chain Monte Carlo
  - Parameters describe:
    - EoS, Viscosity, Diffusion constants....
    - and ultimately critical point and anomalous transport

# Progress



John Bower  
grad stud, MSU

- Emulators constructed:
  - Gaussian process
  - Machine-learning
  - Comparison underway
  - Strategies for expressing uncertainties are being developed
- Sample problem
  - Imaging charge correlations
  - Should also be applicable to BES data

$$B_{\pi,\pi}(\Delta y), B_{K,K}(\Delta y), B_{p,p}(\Delta y), B_{p,K}(\Delta y)$$

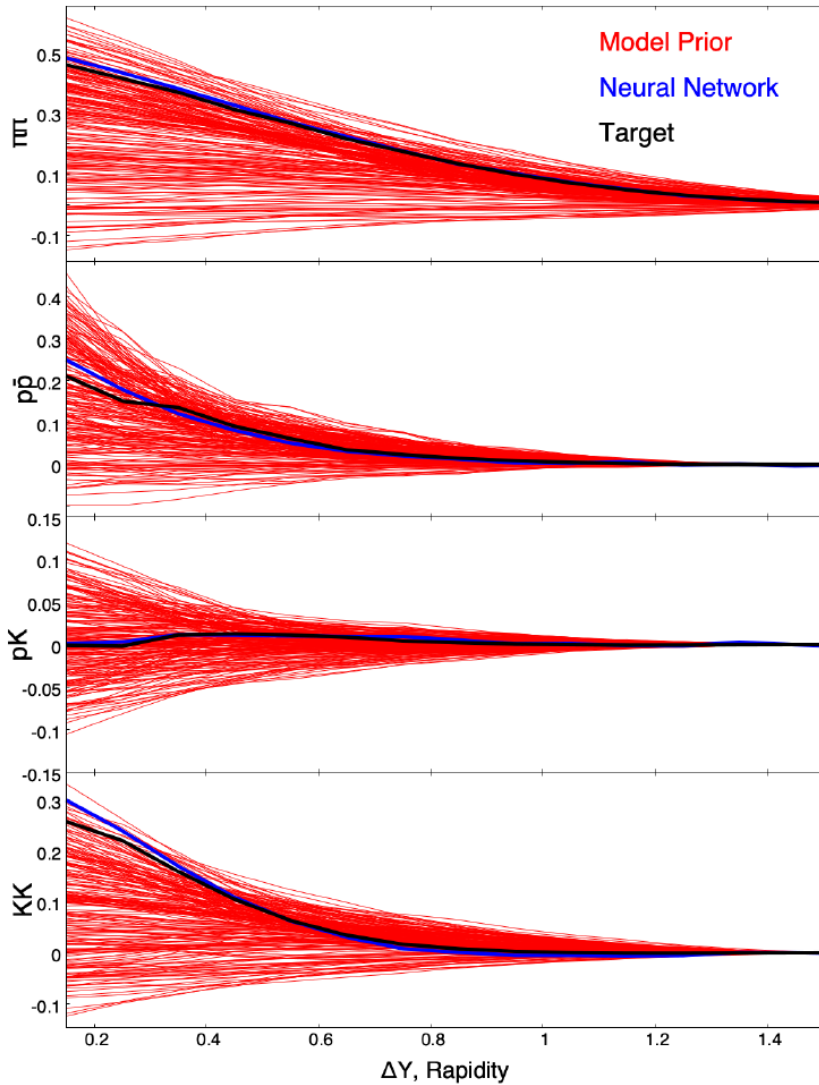
Measured by STAR

$$\rightarrow C_{uu}(\Delta\eta), C_{ud}(\Delta\eta), C_{ss}(\Delta\eta), C_{us}(\Delta\eta)$$

Correlations in coordinate space

# Progress

## Charge Balance Functions,



Two emulators constructed:  
1. Gaussian Process  
2. Neural network  
Currently being compared

### Test of Neural Network Emulator

Balance functions used for training

Balance function from trained Neural Network

True BF using full model

# Next steps

- Transport
  - Particlization for deterministic hydro (hydro+)
  - Connect particlization algorithm + SMASH to hydro; test
  - Implement mean field into SMASH transport; test
  - Run full code and calculate global observables such as flow
  - Connect to stochastic hydro; test
  - Match mean field to EOS
  - Ready to calculate fluctuations
- Data analysis
  - Finish warm-up projects
    - imaging
    - Machine learning vs Gaussian emulator comparison
  - Connect statistics codes with full BEST time evolution code
  - Collect statistics from experiments
  - Develop strategy for running, and allocate resources