# ATALS-LHCf joint analysis Single diffractive fraction 

11/26 LHCf collaboration meeting
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## LHCf - ATLAS joint analysis

- Conf. note (Nov. 2017)
- LHCf photon spectrum with ATLAS inner tracker veto
- Next goal
- LHCf photon spectrum produced by single diffractive with $\log (\xi)<-5$.
- Correction factor:
- $C^{\log _{10} \xi}:$ Nch $=0 \rightarrow \log _{10} \xi$ event selection
- $C^{C \tau}: \mathrm{c}^{*}$ tau $<140 \mathrm{~m} \rightarrow \mathrm{c}^{*}$ tau $<1 \mathrm{~cm}$ (+ magnet effect)
- $C^{S D}$ : single diffractive fraction in ATLAS veto spectrum.
- In this presentation, I report details about $C^{S D}$


## content

- the effect of diffractive events on the air shower development ( using COSMOS 8.035)
- the detail of Single diffractive fraction analysis


## diffractive events

## In this analysis, we focus on diffractive events



## diffractive events

20-30\% of inelastic collisions
diffractive event has large rapidity gap.

In conf. note of ATLAS-LHCf joint analysis
Select diffractive events using ATLASInner tracker which cover $|\eta|<2.5$.
Non-diffractive events (ND): events other than diffractive events

## diffractive mass and rapidity gap

$$
M_{X}^{2}=\left(\sum_{i} p_{i, X}\right)^{2} \sim s e^{-\Delta \eta}
$$

$\Delta \boldsymbol{\eta}$ :Rapidity gap, $\mathrm{s}=E_{c m}^{2}$

the effect of diffractive events on the air shower development

## interactions in air shower

toy model of Air shower
the primary particle $E_{0}$
first int.


Energy of most energetic
EM shower

Electromagnetic cascade shower (EM shower)

Most of charged particle are produced in EM shower
diffractive events : high elasticity
single diffractive single diffractive air proton dissociation nuclei dissociation

high $\boldsymbol{K}_{\text {el }}$

very high $K_{\text {el }}$
nucleonother hadrons
air nuclei

## the effect of diffractive events on the shower development

## Air shower simulation

- using the air shower simulation package COSMOS
- 50000 events ( 30000 events for EPOSLHC)
- $10^{15} \mathrm{eV}$, proton ( $\left.\sqrt{S_{N N}}=1.3[\mathrm{TeV}]\right)$
- diffractive flag from the first interaction
- simulate shower development

From the first interaction information,

1. divide events into 4 or 5 type

- Non-diff, Single diff. with projectile proton dissociation, Single diff. with target air nucleon dissociation, double diff, central diff. (EPOS only)

2. calculate diffractive mass of SD (proton dissociation)

## the effect of diffractive events 1. fraction of single diffraction

|  |  | Non- <br> diffractive | SD, projectile <br> proton dis. | SD, target <br> dis. | DD | CD | total |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| SIBYLL | mean $X_{\max }$ | 577.0 | 609.9 | 648.1 | 605.7 | 583.8 |  |
| 2.3c | fraction [\%] | 84.2 | 10.5 | 4.2 | 1.1 |  |  |
| QGSJet | mean $X_{\max }$ | 561.5 | 612.4 | 634.8 | 602.8 | 569.9 |  |
| II-04 | fraction [\%] | 84.6 | 7.2 | 4.2 | 4.0 |  |  |
| EPOS | mean $X_{\max }$ | 565.2 | 613.8 | 634.9 | 605.9 | 624.1 | 576.0 |
| LHC | fraction [\%] | 78.9 | 4.6 | 5.0 | 9.1 | 2.4 |  |
|  |  |  | Unit of mean Xmax : $\left[\mathrm{g} / \mathrm{cm}^{2}\right]$ |  |  |  |  |

## the effect of diffractive events 2. diffractive mass

projectile single diffractive (proton dissociation)


$X_{1}=X_{\max }-X_{0}$,
$X_{0}$ : depth of the first interaction
the shower development is deep at low-mass region, where model discrepancy is large.

## the effect of diffractive events 2. diffractive mass

projectile single diffractive (proton dissociation)

$$
\text { p- Air, } \sqrt{S_{N N}}=1.3 \text { [TeV] }
$$




Qi-Dong Zhou et al.,
Eur. Phys. J. C 77212 (2017)
$X_{1}=X_{\text {max }}-X_{0}$,
$X_{0}$ : depth of the first interaction
the shower development is deep at low-mass region, where model discrepancy is large.

# Single diffractive fraction 

## LHCf - ATLAS joint analysis

- $C^{S D}$ : single diffractive fraction in ATLAS veto spectrum.
- MC-based correction factor
- small statistics of Arm1-Arm2 coincidence events
- In MC, SD fraction is 0.4 (PYTHIA) or 0.9 (SIBYLL)
- Energy dependence of SD fraction is small, and SD fraction of Region $A$ is very similar with that of Region $B$

SD fraction of photon spectrum with ATLAS veto
Large model discrepancy



## LHCf - ATLAS joint analysis

- $C^{S D}$ : single diffractive fraction in ATLAS veto spectrum.
- Energy dependence of SD fraction is small, and SD fraction of Region $A$ is very similar with that of Region $B$
- => ignore energy dependence of SD fraction, and assume that SD fraction is same between Region $A$ and $B$

SD fraction of photon spectrum with ATLAS veto
Large model discrepancy



## concept

To measure single diffractive fraction, we introduce ATLAS Minimum-bias trigger scintillator (MBTS).

If we measure particles created by dissociation with both side of rapidity-gap, that event is a double diffractive event.


But, MBTSs only cover part of the gap between ATLAS-Inner tracker and LHCf detectors, so we unfold detector effects using MC simulation.

## concept

Using MBTS, we can select part of double diffractive events.


Exp. data
Two samples DD-enriched and SD-enriched

Response Matrix $R^{\text {MBTS }}$

- MBTS detection efficiency
- photon production
- LHCf detector response
without detector effect

$$
\begin{aligned}
& \text { true } N_{S D}^{N_{c h}=0} \\
& \text { and } N_{D D}^{N_{c h}=0}
\end{aligned}
$$

Unfolding

## ATLAS MBTS

ATLAS Minimum-bias trigger scintillator(MBTS) is forward detectors which cover $2.08<|\eta|<3.86$.


MBTS event selection


OFF Arm1 side Nhit
double diffraction


## Two samples

sample I: B (SD-enriched) sample II: C + D (DD-enriched)

A: Arm1side OFF, Arm2side OFF (SD and DD mixed sample)
B: Arm1side ON, Arm2side OFF (SD and DD mixed sample)
C:Arm1side OFF, Arm2side ON (DD sample)
D:Arm1side ON, Arm2side ON (DD sample)

## method



## For energy dependence

In unfolding calculation, we ignore energy dependence.
For energy dependence, we introduce parameter $X$.

$$
C^{S D}=\frac{X \int N_{S D}(E) d E}{\int N_{\text {all }}(E) d E}
$$

Then, scale true SD fraction using X and get $C_{A}^{S D}(E)$ for region A. For region B , assume same parameter X and calculate $C_{B}^{S D}(E)$ for region B.

## test of unfolding

## generator level

after unfolding
unfolding
inverse matrix

$$
C^{S D}=\frac{X \int N_{S D}(E) d E}{\int N_{\text {all }}(E) d E} \quad \begin{aligned}
& \text { model for } \\
& \text { response matrix }
\end{aligned}
$$

result: $C_{A}^{S D}$

## test of unfolding

Using MC simulation with detector for instead of exp. data, check the performance of this method.
If method is ideal, all results with same input should be same despite of the model for response matrix.
with detector response
Non-diff. subtraction assumption: all ND events -> MBTS selection D

## MC simulation (instead of data)

$N_{I}^{\text {Data }}, N_{I I}^{\text {Data }}$
I: Nch=0 and MBTS selection B and LHCf Arm1 photon hit (Region A)
II: Nch=0 and MBTS selection C\&D and LHCf Arm1 photon hit (Region A)
model for input

## test of unfolding

Calculate SD fraction after ND correction using MC simulation as input. (substitute MC simulation for Exp. data)

The average of SD fraction model for response

| $\boldsymbol{C}_{A}^{S D}$ | PYTHIA | EPOSLHC | QGSJET | SIBYLL |
| :---: | :---: | :---: | :---: | :---: |
| PYTHIA | 0.404 | 0.444 | 0.487 | 0.488 |

If the method is ideal, results with different model for response matrix should be same, but the results are not same.

## test of unfolding

Calculate SD fraction after ND correction using MC simulation as input. (substitute MC simulation for Exp. data)

The average of SD fraction model for response

| $C_{A}^{S D}$ | PYTHIA | EPOSLHC | QGSJET | SIBYLL |
| :---: | :---: | :---: | :---: | :---: |
| PYTHIA | 0.404 | 0.444 | 0.487 | 0.488 |
| $\frac{\text { for input }}{}$ EPOSLHC | 0.436 | 0.484 | 0.530 | 0.517 |
| QGSJET | 0.591 | 0.641 | 0.670 | 0.649 |
| SIBYLL | 0.862 | 0.891 | 0.906 | 0.883 |

With other inputs, results with different model for response matrix are different. And these difference has clear tendency, the results with pythia response always show smaller results compare to EPOS or QGSJET.
=> This method has some biases due to the model for response matrix.
This bias should be included in systematic uncertainty.

## Results

The average of SD fraction
Using exp. data as input of unfolding


## Bias of method

## Bias of SD fraction

$C^{S D}$ : the fraction of $S D$ in Nch=0 events
( Nch=0 and LHCf photon (generator level))
Region A
response

| input | $C_{A}^{S D}$ | PYTHIA | EPOSLHC | QGSJET | SIBYLL | TRUE |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | PYTHIA | 0.404 | 0.444 | 0.487 | 0.488 | 0.404 |
|  | EPOSLHC | 0.436 | 0.484 | 0.530 | 0.517 | 0.484 |
|  | QGSJET | 0.591 | 0.641 | 0.670 | 0.649 | 0.670 |
|  | SIBYLL | 0.862 | 0.891 | 0.906 | 0.883 | 0.883 |
| $\kappa=\frac{C_{\text {results }}^{S D}-C_{\text {true }}^{S D}}{C_{\text {true }}^{S D}}$ |  | $\kappa$ [\%] | PYTHIA | EPOSLHC | QGSJET | SIBYLL |
|  |  | PYTHIA | 0.0 | 10.0 | 20.5 | 20.8 |
| ```Cresults: calculated results Ctrue: true SD fraction``` |  | EPOSLHC | -9.9 | 0.0 | 9.5 | 6.8 |
|  |  | QGSJET | -11.7 | -4.3 | 0.0 | -3.1 |
|  |  | SIBYLL | -2.4 | 0.8 | 2.6 | 0.0 |

## To calculate syst. uncertainty from the bias of method

Region A
response

| $C_{A}^{S D}$ | PYTHIA | EPOSLHC | QGSJET | SIBYLL | TRUE |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PYTHIA | 0.404 | 0.444 | 0.487 | 0.488 | 0.404 |
| input EPOSLHC | 0.436 | 0.484 | 0.530 | 0.517 | 0.484 |
| QGSJET | 0.591 | 0.641 | 0.670 | 0.649 | 0.670 |
| SIBYLL | 0.862 | 0.891 | 0.906 | 0.883 | 0.883 |
| Introduce $\Delta$$\Delta=\frac{C_{\text {true }}^{S D}-C_{\text {results }}^{S D}}{C_{\text {results }}^{S D}}$ | $\Delta$ [\%] | PYTHIA |  |  |  |
|  | PYTHIA |  |  | 0.0 |  |
| $C_{\text {results }}^{S D}$ : <br> calculated results <br> $C_{\text {true }}^{S D}$ : <br> true SD fraction <br> $\Delta$ : Size of difference <br> from $C_{\text {results }}^{S D}$ | EPOSLHC | upper one and |  | 11.0 |  |
|  | QGSJET |  | r one | 13.3 |  |
|  | SIBYLL |  |  | 2.5 |  |
|  | Bias upper |  |  | 13.3 |  |
|  | Bias lower |  |  | 0.0 | 25 |

## To calculate syst. uncertainty from the bias of method

Region A
response

| $C_{A}^{S D}$ | PYTHIA | EPOSLHC | QGSJET | SIBYLL | TRUE |
| :---: | :---: | :---: | :---: | :---: | :---: |
| PYTHIA | 0.404 | 0.444 | 0.487 | 0.488 | 0.404 |
| input EPOSLHC | 0.436 | 0.484 | 0.530 | 0.517 | 0.484 |
| QGSJET | 0.591 | 0.641 | 0.670 | 0.649 | 0.670 |
| SIBYLL | 0.862 | 0.891 | 0.906 | 0.883 | 0.883 |
| Introduce $\Delta$$\Delta=\frac{C_{\text {true }}^{S D}-C_{\text {results }}^{S D}}{C_{\text {results }}^{S D}}$ | $\Delta$ [\%] | PYTHIA | EPOSLHC | QGSJET | SIBYLL |
|  | PYTHIA | 0.0 | -9.1 | -17.0 | -17.2 |
| $C_{\text {results }}^{S D}:$ <br> calculated results <br> $C_{\text {true }}^{S D}$ : <br> true SD fraction <br> $\Delta$ : Size of difference from $C_{\text {results }}^{S D}$ | EPOSLHC up | per one and | 0.0 | -8.7 | -6.4 |
|  | QGSJET | 13.3 | 4.4 | 0.0 | 3.2 |
|  | SIBYLL | $\downarrow 2.5$ | -0.8 | -2.5 | 0.0 |
|  | Bias upper | ${ }^{1} 3.3$ | 4.4 | 0.0 | 3.2 |
|  | Bias lower | 0.0 | -9.1 | -17.0 | -17.2 |

## To calculate syst. uncertainty from the bias of method

## Region A

 response model results with exp. data

## syst. uncertainty from the bias of method

| Region A | response model |  |  | ND subtraction: method 2. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $C_{A}^{S D}$ | PYTHIA | EPOSLHC | QGSJET | SIBYLL | Method A |
| Data | 0.452 | 0.502 | 0.546 | 0.531 | 0.508 |
| Result +Bias upper | 0.512 | 0.524 | est one <br> 0.546 | 0.548 | Max. of <br> 'Result + Bias upper' |
| Result + Bias |  | lowest one |  |  | Min. of 'Result + Bias lower' |
| lower | 0.452 | 0.456 | 0.453 | 0.440 |  |

center value: simple average (just for simplicity) in real case, weighted average
Bias: Maximum of 'Result + Bias upper' and Minimum of 'Result + Bias lower'

## uncertainties

## uncertainty

- uncertainty
- MBTS response
- LHCf response function
- Non-diffractive events
- model discrepancy + bias of the method
- statistical error


## syst. uncertainty

- MBTS response function
- MC model for MBTS response function calculation
- MBTS threshold
- LHCf response function
- difference between response function and full simulation
- Non-diffractive events
- Non-diffractive sys. uncertainty is calculated with extreme assumption
- From ATLAS full simulation, almost 100 \% of Non-diff. events make a hit in both MBTS. We assume $100 \%$ and take syst. uncertainty of ND events as $80 \%$ of events make a hit in a MBTS.


## uncertainties of $C_{A}^{S D}$

response

|  | PYTHIA | EPOSLHC | QGSJET | SIBYLL |
| :--- | ---: | ---: | ---: | ---: | ---: |
| $C_{A}^{S D}$ | 0.452 | 0.502 | 0.546 | 0.531 |
|  | 2.37 | 2.84 | 2.00 | 2.31 |
| statistical (+/-) [\%] | 2.62 | 2.72 | 1.72 | 1.45 |
| MBTS threshold upper [\%] | -1.84 | -1.13 | -2.07 | -0.99 |
| lower[\%] | 1.78 | 2.62 |  |  |
| Model for MBTS response function [\%] | 0.06 | 0.19 | -0.04 | 0.08 |
| LHCf response func. upper[\%] | -0.21 | -0.65 | -0.02 | -0.40 |
| lower[\%] | -0.67 | -1.79 | -2.95 | -0.91 |
| Non-diffractive [\%] | 3.95 | 4.73 | 2.64 | 2.72 |
| total upper [\%] | 3.08 | 3.60 | 4.12 | 2.70 |
| total lower[\%] |  |  |  |  |

Note: As shown in p.24, $\quad \boldsymbol{C}_{\boldsymbol{A}}^{S D}$
average

| Data | 0.508 |  |
| :--- | ---: | ---: |
| biases and model discrepancies: upper | 0.548 | $+7.9[\%]$ |
| biases and model discrepancies: lower | 0.440 | $-13.4[\%]$ |

## summary

- For final result, we need Single diffractive fraction of ATLAS veto spectrum, but there is large model discrepancy in MC.
- To measure SD fraction, we introduce ATALS Minimum-bias trigger scintillator (MBTS), and unfold detector effects.
- SD fraction is about 0.5.
- the study of uncertainty is on going and still need some update.


## backup

## single diffractive fraction

true single diffractive fraction with $\mathrm{Nch}=0$

histogram of single diffractive events with Nch=0 and LHCf Arm1 photon-like hit


The fraction of single diffraction is diffractive-mass dependent. In our analysis, most of detected events are low-mass events $\left(\log _{10} \xi<-7\right)$.

## detail of unfolding

## SD fraction measurement

- Measure SD (DD) fraction based on the data and MC simulation.
- Using ATLAS-MBTS detectors, we divide exp. data into the DD-enriched sample and the SD-enriched sample, and "unfold" SD fraction using response matrixes calculated by MC simulation.
- update from the report at analysis meeting on Jul. 25
- New method: Unfolding (An Idea and calculation is same as previous, but easier to understand)


## Non-diff. subtraction

assumption: all Non-diff. events make a hit in MBTSs ( MBTS selection D)

- two method
- Method 1. $N_{I I}^{M B T S}=N_{I I}^{\text {Data }} \times R$
- $R=\frac{N_{M C, N D}^{M B T S I I}}{N_{M C, S D}^{M B T S}{ }^{I I}+N_{M C, D D}^{M B T S I I}+N_{M C, N D}^{M B T S I I}}$
- Method 2. $N_{I I}^{M B T S}=N_{I I}^{D a t a}-N^{N D}$
- $N^{N D}=N_{N c h=0}^{D a t a} \times \frac{N_{M C, N D}^{N c h=0}}{N_{M C, S D}^{N c h=0}+N_{M C, D D}^{N c h}=0+N_{M C, N D}^{N c h=0}}$


## Input - Response test

To decide Non-diff. subtract method
$C^{S D}$ : the fraction of $S D$ in $\mathrm{Nch}=0$ events
method 1. ( LHCf Arm1 photon-like)

| input | $C^{S D}$ | PYTHIA | EPOSLHC | QGSJET | SIBYLL |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | PYTHIA | 0.402 | 0.449 | 0.483 | 0.498 |
|  | EPOSLHC | 0.429 | 0.478 | 0.509 | 0.520 |
|  | QGSJET | 0.587 | 0.639 | 0.655 | 0.653 |
|  | SIBYLL | 0.857 | 0.880 | 0.879 | 0.877 |

method 2.
response

|  | $\boldsymbol{C}^{\boldsymbol{S D}}$ | PYTHIA | EPOSLHC | QGSJET | SIBYLL |
| :--- | :--- | :--- | :--- | :--- | :--- |
| input | PYTHIA | 0.402 | 0.441 | 0.471 | 0.474 |
|  | EPOSLHC | 0.431 | 0.478 | 0.511 | 0.501 |
|  | QGSJET | 0.589 | 0.638 | 0.655 | 0.637 |
|  | SIBYLL | 0.861 | 0.888 | 0.895 | 0.877 |

## difference $\boldsymbol{C}^{\boldsymbol{S D}}-\boldsymbol{C}_{\text {true }}^{\boldsymbol{S D}}$ (\% of $C_{\text {true }}^{S D}$ )

LHCf Arm1 photon-like

| method | $1 . \quad$ response |  |  |  | LHCf Arm1 photon-like |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $C^{S D}$-true | PYTHIA | EPOSLHC | QGSJET | SIBYLL | $C_{\text {true }}^{S D}$ |
| input | PYTHIA | 0.02 | 11.71 | 20.17 | 23.90 | 0.4019 |
|  | EPOSLHC | -10.26 | -0.01 | 6.47 | 8.77 | 0.4781 |
|  | QGSJET | -10.34 | -2.40 | 0.04 | -0.26 | 0.6547 |
|  | SIBYLL | -2.31 | 0.32 | 0.20 | -0.03 | 0.8772 |

method 2.
response

| input | $C^{S D}$-true | PYTHIA | EPOSLHC | QGSJET | SIBYLL | $C_{\text {true }}^{S D}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | PYTHIA | 0.02 | 9.72 | 17.19 | 17.93 | 0.4019 |
|  | EPOSLHC | -9.85 | -0.01 | 6.89 | 4.80 | 0.4781 |
|  | QGSJET | -10.04 | -2.56 | 0.04 | -2.71 | 0.6547 |
|  | SIBYLL | -1.85 | 1.23 | 2.03 | -0.03 | 0.8772 |

=> Method 2 is better than method 1.
Bias?? Results with the PYTHIA response are smaller than others.

## uncertainty

## syst. uncertainty

- MBTS response function
- MC model for MBTS response function
- MBTS threshold
- normal and sys up, down
- 0.15 pC, 0.27pC (up) , 0.07pC (down)



## LHCf response sys. uncertainty

difference between LHCf detector response and
full simulation is already calculated by zhou-san.
$\kappa=\frac{a-b}{b}$,a: using Response, b : full simulation
Table 4: Parameter $\kappa$ of each cases

| Model | QGSJET-II-04 |  | EPOS-LHC |  |
| :--- | :---: | :---: | :---: | :---: |
| Fiducial area | Region A | Region B | Region A | Region B |
| Single photon | -0.0057 | -0.0169 | -0.0003 | -0.0108 |
| Single neutron | -0.0059 | 0.3785 | 0.0478 | 0.0766 |
| Two photons | -0.0057 | 0.0231 | -0.0057 | -0.0175 |
| Photon \& hadron | -0.0537 | 0.0219 | 0.1964 | -0.0376 |


| EPOS LHC, Region A |  |  |
| :---: | :--- | :--- |
| $N_{B}^{M C, S D}$ | Single photon | 3028 |
|  | Single neutron | 94 |
|  | Two photon | 99 |
|  | Photon \& hadron | 149 |
|  | total | 4070 |

shift these number of events by $\Delta$ of each type
total number of events shift from 4070 to 4042.94 (EPOSLHC full simulation)

## LHCf response sys. uncertainty

difference between Response and full simulation
$\kappa=\frac{a-b}{b}$,a: using Response, b: full simulation calculated by zhou-san
Table 4: Parameter $\kappa$ of each cases

| Model | QGSJET-II-04 |  | EPOS-LHC |  |
| :--- | :---: | :---: | :---: | :---: |
| Fiducial area | Region A | Region B | Region A | Region B |
| Single photon | -0.0057 | -0.0169 | -0.0003 | -0.0108 |
| Single neutron | -0.0059 | 0.3785 | 0.0478 | 0.0766 |
| Two photons | -0.0057 | 0.0231 | -0.0057 | -0.0175 |
| Photon \& hadron | -0.0537 | 0.0219 | 0.1964 | -0.0376 |


| EPOS LHC <br> Region A | normal | sys. modified <br> (EPOSLHC) | sys. modified <br> (QGSJET II-04) |
| :---: | :--- | :--- | :--- |
| $N_{B}^{M C, S D}$ | 4070 | 4042.94 | 4100.95 |
| $N_{B}^{M C, D D}$ | 3726 | 3695.77 | 3755.9 |
| $N_{C}^{M C, D D}$ | 5794 | 5696.29 | 5855.27 |
| $N_{D}^{M C, D D}$ | 1390 | 1377.23 | 1401.55 |

## ultra-high energy cosmic ray and

 air showera primary particle proton or nuclei
$X_{\text {max }}$

Air shower

key information of cosmic rays

- flux
- species of nuclei
- anisotropy
(ultrahigh-energy)
the depth of maximum of shower development $X_{\text {max }}$ an indicator of species of a primary particle


## Air Shower

CORSIKA web page
https://www-zeuthen.desy.de/~jknapp/fs/protonshowers.html

## air shower simulation and data



FIG. 13. Energy evolution of the first two central moments of the $X_{\text {max }}$ distribution compared to air-shower simulations for proton and iron primaries [80,81,95-98].
A. Aab et al. (Pierre Auger Collaboration)

Phys. Rev. D 90, 122005
the simulation of $X_{\text {max }}$ has model discrepancy caused by hadronic interaction models, that make difficult to interpret primary particles.

