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The Low-Energy Frontier of the Standard Model & Precision Hadron Physics

***The basic ideas and concepts behind the modern High-Energy Physics and Cosmology
Truskavets (Ukraine), October 5 - 16, 2018***

Outline of the lectures

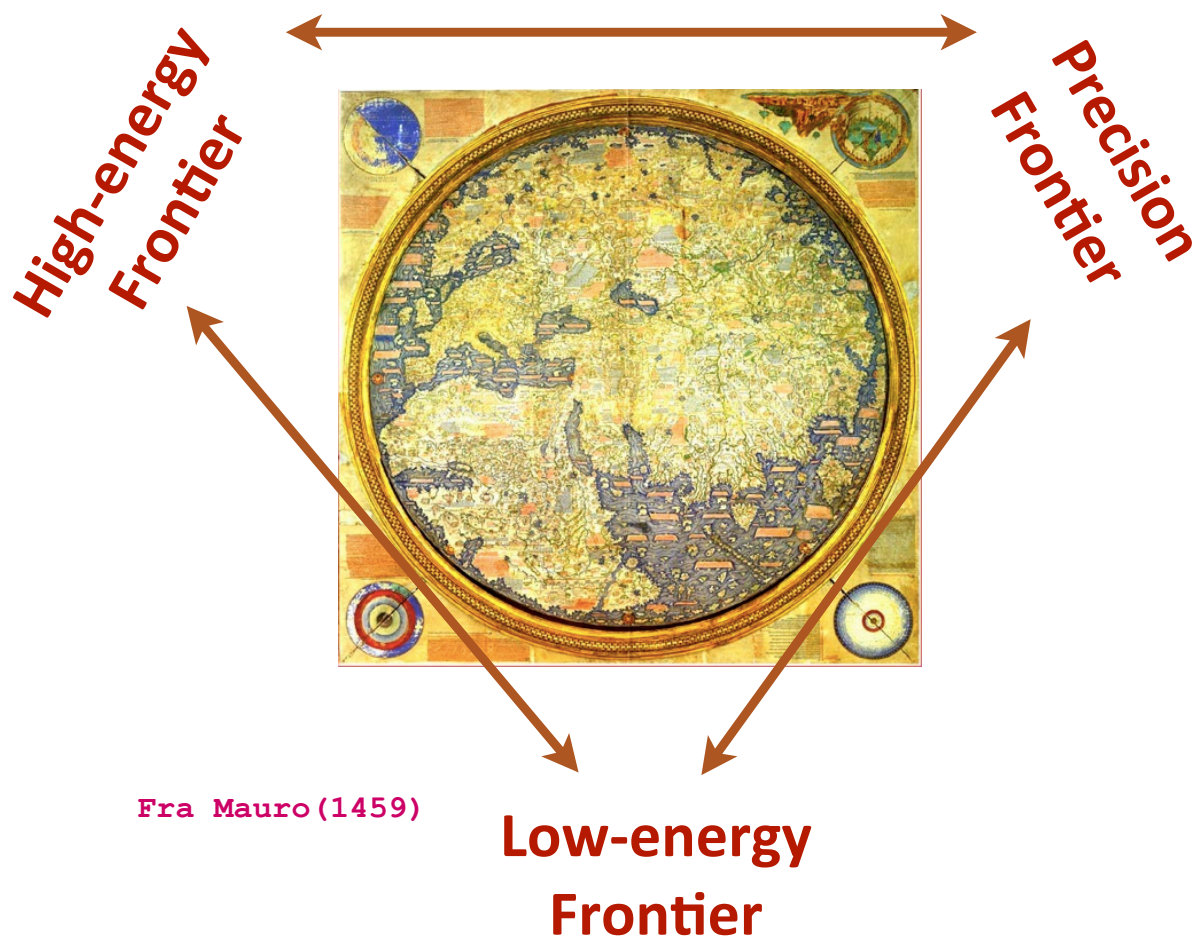
Lecture 1: Tests of the Standard Model at low-energies

- Introduction: Frontiers of the Standard Model
- Low-energy tests of the weak mixing angle
- Search for a dark photon and light dark matter

Lecture 2: Modern Topics in Precision Hadron Physics

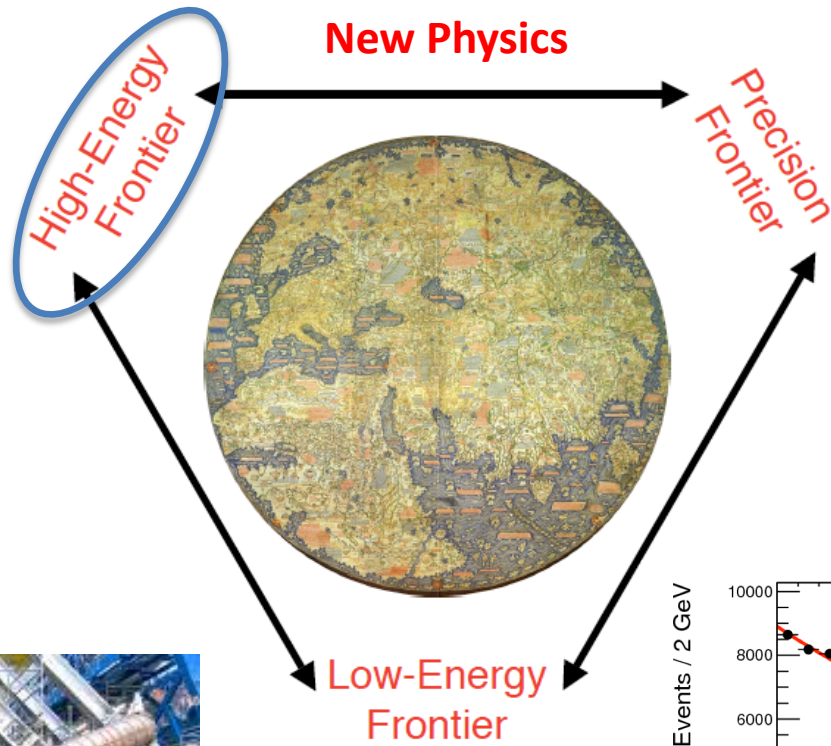
Lecture 3: given by Dr. Vladyslav Pauk **Precision physics: the anomalous magnetic moment of the muon**

Frontiers of the Standard Model

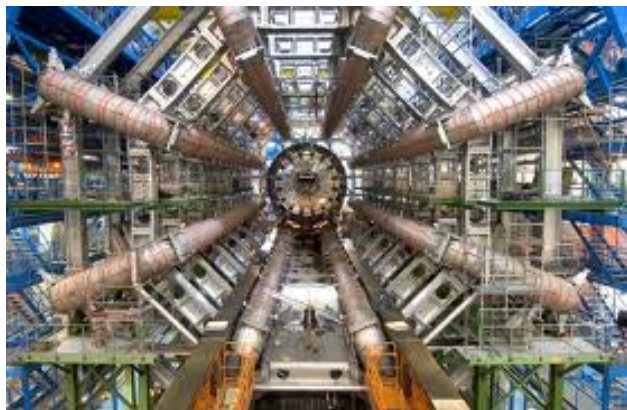


Fra Mauro (1459)

Frontiers of the Standard Model

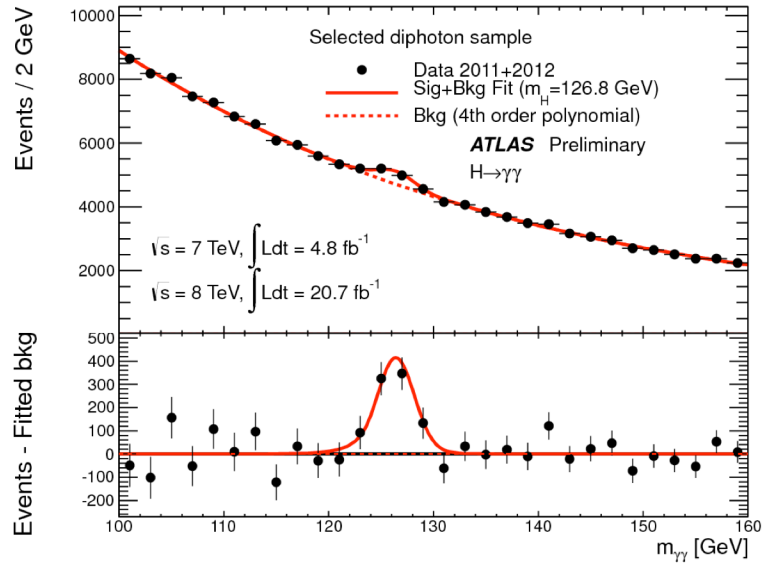


LHC
 Higgs discovery
 Production of new physics particles
 Later: ILC

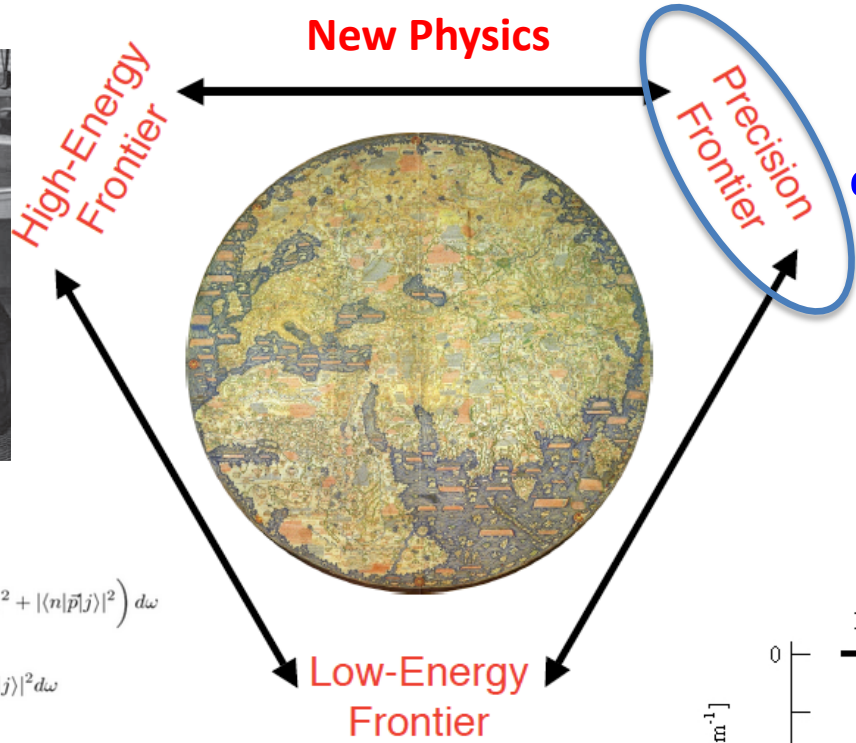


Englert, Higgs
 Nobel prize 2013

Higgs discovery



Frontiers of the Standard Model



New Physics

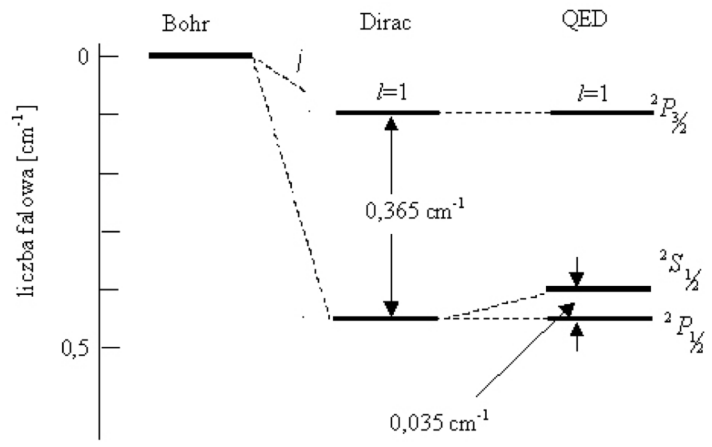
Testing SM at low energies, quantum loop corrections

- $\sin^2\theta_W$
- $(g-2)\mu$
- EDM

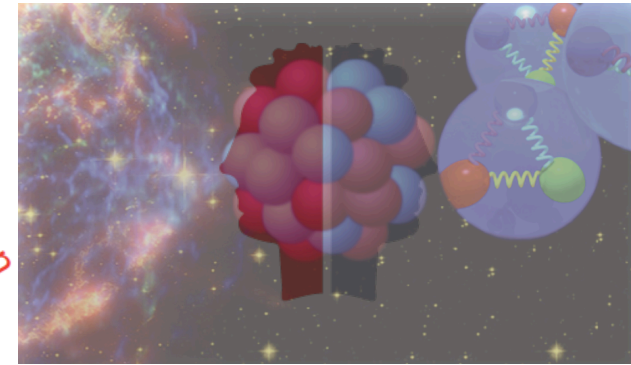
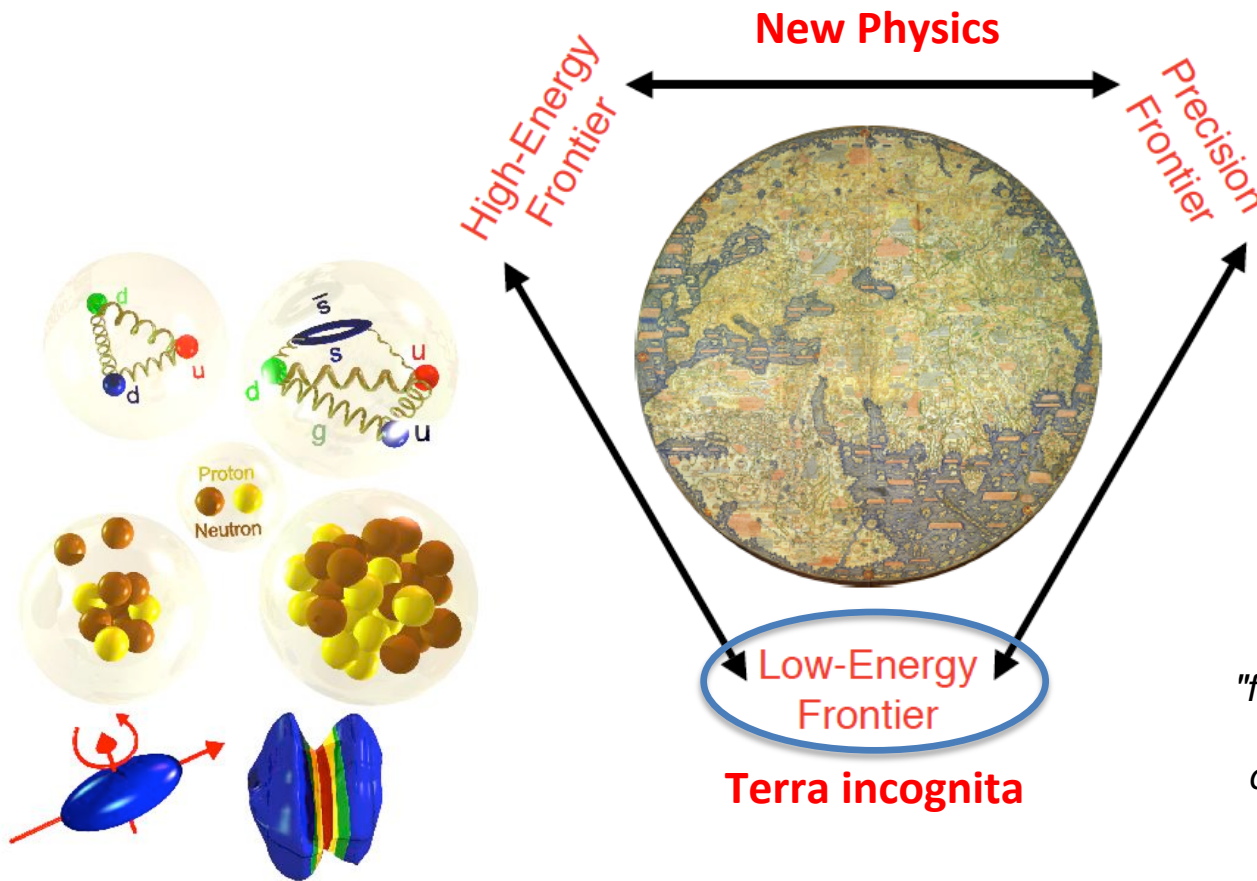
Flavor physics
Atomic physics

$$\begin{aligned} \Delta E_n^{(obs)} &= \frac{2\alpha\hbar}{3\pi m^2 c^2} \int_0^{\omega_{cut-off}} \sum_j \left(\frac{\omega}{(\omega_{nj} - \omega)} |\langle n|\vec{p}|j\rangle|^2 + |\langle n|\vec{p}|j\rangle|^2 \right) d\omega \\ &= \frac{2\alpha\hbar}{3\pi m^2 c^2} \int_0^{\omega_{cut-off}} \sum_j \frac{\omega + (\omega_{nj} - \omega)}{(\omega_{nj} - \omega)} |\langle n|\vec{p}|j\rangle|^2 d\omega \\ &= -\frac{2\alpha\hbar}{3\pi m^2 c^2} \sum_j \int_0^{\omega_{cut-off}} \frac{\omega_{nj}}{\omega - \omega_{nj}} |\langle n|\vec{p}|j\rangle|^2 d\omega \\ &= -\frac{2\alpha\hbar}{3\pi m^2 c^2} \sum_j \omega_{nj} [\log(\omega - \omega_{nj})]_0^{\omega_{cut-off}} |\langle n|\vec{p}|j\rangle|^2 \\ &= \frac{2\alpha\hbar}{3\pi m^2 c^2} \sum_j \omega_{nj} [\log(|\omega_{nj}|) - \log(\omega_{cut-off} - \omega_{nj})] |\langle n|\vec{p}|j\rangle|^2 \\ &\approx \frac{2\alpha\hbar}{3\pi m^2 c^2} \sum_j \omega_{nj} [\log(|\omega_{nj}|) - \log(\omega_{cut-off})] |\langle n|\vec{p}|j\rangle|^2 \\ &= \frac{2\alpha\hbar}{3\pi m^2 c^2} \sum_j \omega_{nj} \log\left(\frac{|\omega_{nj}|}{\omega_{cut-off}}\right) |\langle n|\vec{p}|j\rangle|^2 \end{aligned}$$

H. Bethe (1947)



Frontiers of the Standard Model



from quarks to stars:

looking outward
vs looking inward

Hans Bethe:
Nobel prize 1967

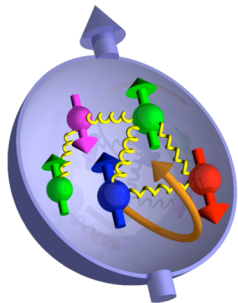
"for his contributions to the theory of nuclear reactions, especially his discoveries concerning the energy production in stars"

Hadron physics: Strong interactions, Complex systems

How do quarks/gluons merge into hadrons (mass, spin,...) ?

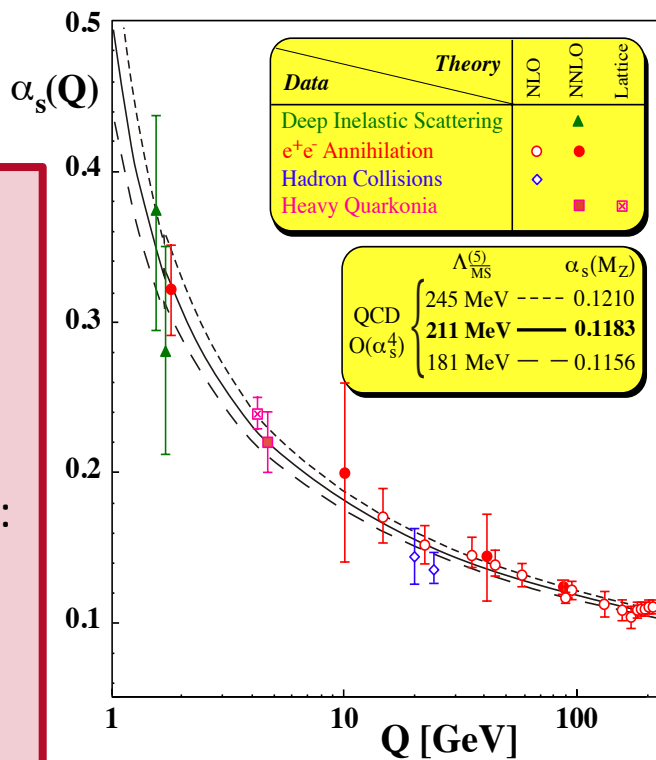
How does hadron structure **emerge** from basic constituents?

Dual behavior of strong interactions QCD



Differently from electromagnetic and weak interaction perturbation
QCD: theory only simple at high energies -> asymptotic freedom

**strong coupling:
 the world
 of hadrons**



Nobel prize 2004

Gross Politzer Wilczek



**weak coupling:
 asymptotic
 freedom**

- **Unraveling strong QCD**
 Origin of mass, spin, hadron imaging
- **Precision hadron physics**
 impact on new physics searches:
 $(g-2)_\mu$, dark photon search, proton radius puzzle, weak mixing angle
- **Theory tools**
 lattice QCD: ab initio
 EFT/phenomenology: interplay with precision hadron data

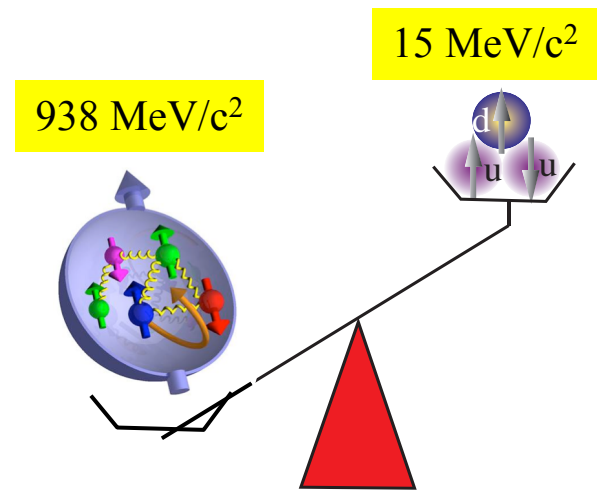
Challenges for the Standard Model

- Neutrino Sector
- Baryon-antibaryon asymmetry
- Dark Matter
- Dark Energy
-

THREE GENERATIONS OF MATTER

	I	II	III	CHARGE:	
MATTER CONSTITUENTS: FERMIONS	QUARKS				
	UP 2.75	CHARM 1300	TOP 178000	$-\frac{2}{3}$	Z^0 91188
	DOWN 6	STRANGE 110	BOTTOM 4500	$-\frac{1}{3}$	W^+ / W^- 80430
LEPTONS	ELECTRON 0.511	MUON 105.7	TAU 1777	-1	$< 10^{-23}$ PHOTON
	NEUTRINO $< 3 \cdot 10^{-6}$	NEUTRINO < 0.19	NEUTRINO < 18.2	0	theory: 0 GLUON

ALL MASSES IN MEV;
ANIMAL MASSES
SCALE WITH
PARTICLE MASSES



Search for New Physics

Generally believed to consist of particles beyond the Standard Model

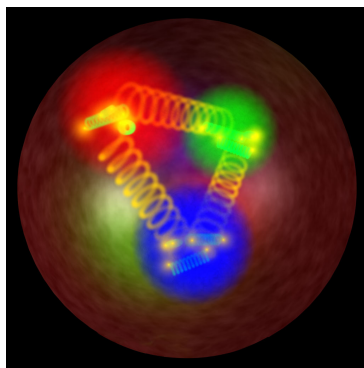
Understanding Low-Energy QCD

The world of Hadrons as bound systems of quarks/gluons

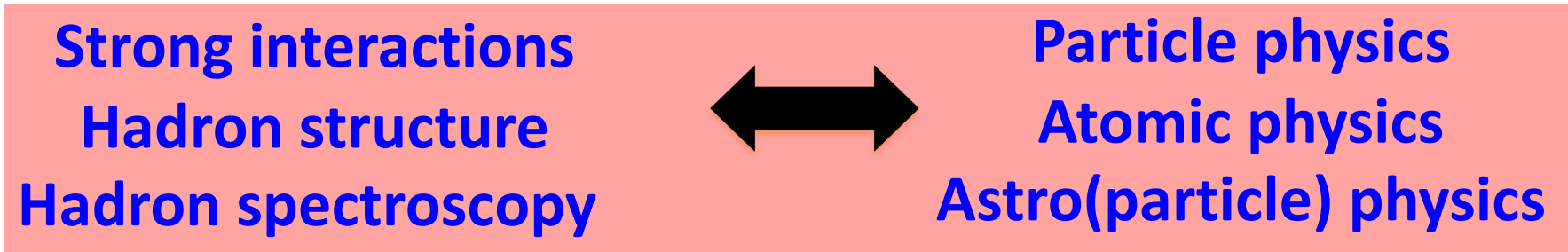
Low-energy frontier of the Standard Model

Hadron physics (= The Low-Energy Frontier of the Standard Model)

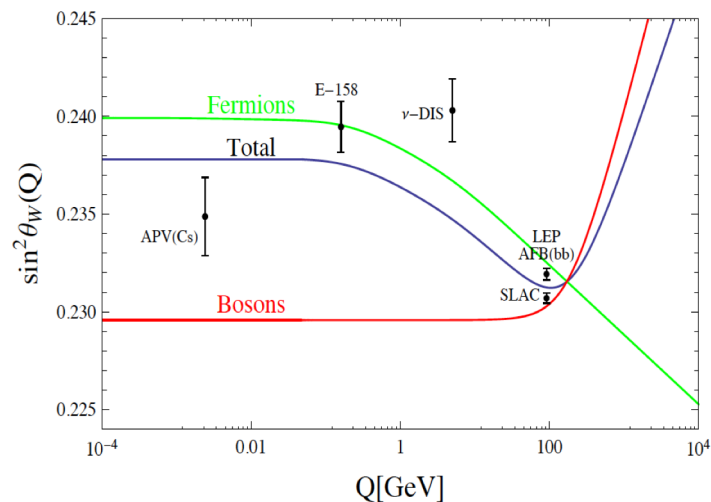
plays a central and connecting role in interpretation of measurements at the precision frontier of the Standard Model



- $\sin^2\theta_W$
- $(g-2)_\mu$
- R_E
Proton charge radius
- Dark Photon
- Nuclear EOS



Low-Energy Tests of the Weak Mixing Angle



Electroweak sector of Standard Model

➔ Right/left handed fermion fields

$$\xrightarrow{\text{red arrow}} \psi^R = \frac{1}{2}(1 + \gamma_5)\psi$$

$$\xleftarrow{\text{red arrow}} \psi^L = \frac{1}{2}(1 - \gamma_5)\psi$$

➔ SU(2): weak isospin gauge symmetry

	t	t_3
$\Psi^L = \begin{pmatrix} \nu_l^L \\ l^L \end{pmatrix}$	1/2	+1/2
	1/2	-1/2
$\psi^R = l^R$	0	0

$$\mathcal{L}^{SU(2)} = \bar{\Psi}^L i\gamma^\mu (\partial_\mu + igt_i W_{i\mu}) \Psi^L + \bar{\psi}^R i\gamma^\mu \partial_\mu \psi^R$$

t_i ($i = 1,2,3$): generators of SU(2)

$W_{1\mu}, W_{2\mu}, W_{3\mu}$: 3 gauge fields

➔ charged current (CC) interaction

Charged gauge fields: $W^\mu = (W_1^\mu - iW_2^\mu) / \sqrt{2}$
 $W^{\mu\dagger} = (W_1^\mu + iW_2^\mu) / \sqrt{2}$

$$\mathcal{L}_{int}^{SU(2)} = \mathcal{L}_{CC} - \frac{g}{4} \{ \bar{\psi}_{\nu_l} \gamma^\mu (1 - \gamma_5) \psi_{\nu_l} - \bar{\psi}_l \gamma^\mu (1 - \gamma_5) \psi_l \} W_{3\mu}$$

$$\mathcal{L}_{CC} = -\frac{g}{2\sqrt{2}} \{ \bar{\psi}_{\nu_l} \gamma^\mu (1 - \gamma_5) \psi_l W_\mu + \bar{\psi}_l \gamma^\mu (1 - \gamma_5) \psi_{\nu_l} W_\mu^\dagger \}$$

Electroweak sector of Standard Model

→ $U(1)_Y$: weak hypercharge gauge symmetry

2 neutral currents:

- 3rd component of weak isospin: $J_3^\mu = \frac{1}{2} \bar{\psi}_{\nu_l}^L \gamma^\mu \psi_{\nu_l}^L - \frac{1}{2} \bar{\psi}_l^L \gamma^\mu \psi_l^L$

- electromagnetic current: $J_{em}^\mu = - (\bar{\psi}_l^L \gamma^\mu \psi_l^L + \bar{\psi}_l^R \gamma^\mu \psi_l^R)$

Combine them by introducing weak hypercharge quantum number Y such that electric charge

$$Q = Y/2 + t_3$$

	t	t_3	Y	Q
$\Psi^L = \begin{pmatrix} \nu_l^L \\ l^L \end{pmatrix}$	1/2	+1/2	-1	0
	1/2	-1/2	-1	-1
$\psi^R = l^R$	0	0	-2	-1

$$\mathcal{L}_{int}^{U(1)_Y} = -\frac{g'}{2} \left\{ -\bar{\psi}_{\nu_l}^L \gamma^\mu \psi_{\nu_l}^L - \bar{\psi}_l^L \gamma^\mu \psi_l^L - 2\bar{\psi}_l^R \gamma^\mu \psi_l^R \right\} B_\mu$$

Electroweak sector of Standard Model

➔ Structure of electroweak neutral current (NC)

$$\begin{aligned}
 \mathcal{L}_{int}^{NC} &= -g\bar{\Psi}_l^L \gamma^\mu t_3 \Psi_l^L W_3^\mu + g'\bar{\psi}_{\nu_l}^L \gamma^\mu \frac{1}{2}\psi_{\nu_l}^L B_\mu + g'\bar{\psi}_l^L \gamma^\mu \frac{1}{2}\psi_l^L B_\mu + g'\bar{\psi}_l^R \gamma^\mu \psi_l^R B_\mu \\
 &= \underbrace{-\frac{1}{2}\bar{\psi}_{\nu_l}^L \gamma^\mu \psi_{\nu_l}^L (gW_3^\mu - g'B_\mu)}_{\text{should not contain photon field}} + \underbrace{\frac{1}{2}\bar{\psi}_l^L \gamma^\mu \psi_l^L (gW_3^\mu - g'B_\mu) + (\bar{\psi}_l^L \gamma^\mu \psi_l^L + \bar{\psi}_l^R \gamma^\mu \psi_l^R) g'B_\mu}_{\text{Electromagnetic current}}
 \end{aligned}$$

➔ Electroweak unification: weak mixing angle

Glashow-Salam-Weinberg model (1967, 1968)

$$\begin{pmatrix} W_3^\mu \\ B^\mu \end{pmatrix} = \begin{pmatrix} \cos \theta_W & \sin \theta_W \\ -\sin \theta_W & \cos \theta_W \end{pmatrix} \begin{pmatrix} Z^\mu \\ A^\mu \end{pmatrix}$$

A^μ : photon field

$$g \sin \theta_W = g' \cos \theta_W = e$$

→ Electroweak neutral current (NC) in Standard Model

$$\mathcal{L}_{int}^{NC} = -e J_{em}^\mu A_\mu - \frac{g}{\cos \theta_W} J_{NC}^\mu Z_\mu$$

$$J_{em}^\mu = -(\bar{\psi}_l^L \gamma^\mu \psi_l^L + \bar{\psi}_l^R \gamma^\mu \psi_l^R)$$

$$J_{NC}^\mu = J_3^\mu - \sin^2 \theta_W J_{em}^\mu = \frac{1}{4} \bar{\psi}_{\nu_l} \gamma^\mu (1 - \gamma_5) \psi_{\nu_l} - \frac{1}{4} \bar{\psi}_l \gamma^\mu ([1 - 4 \sin^2 \theta_W] - \gamma_5) \psi_l$$

Vector interaction
is suppressed

Determination from electroweak
precision observables:

$$\sin^2 \theta_W \approx 0.23 \rightarrow 1 - 4 \sin^2 \theta_W \approx 0.08$$

Accessing $\sin^2 \theta_W$: proton weak charge

➔ Electroweak Lagrangian → Parity-Violating electron-quark term:

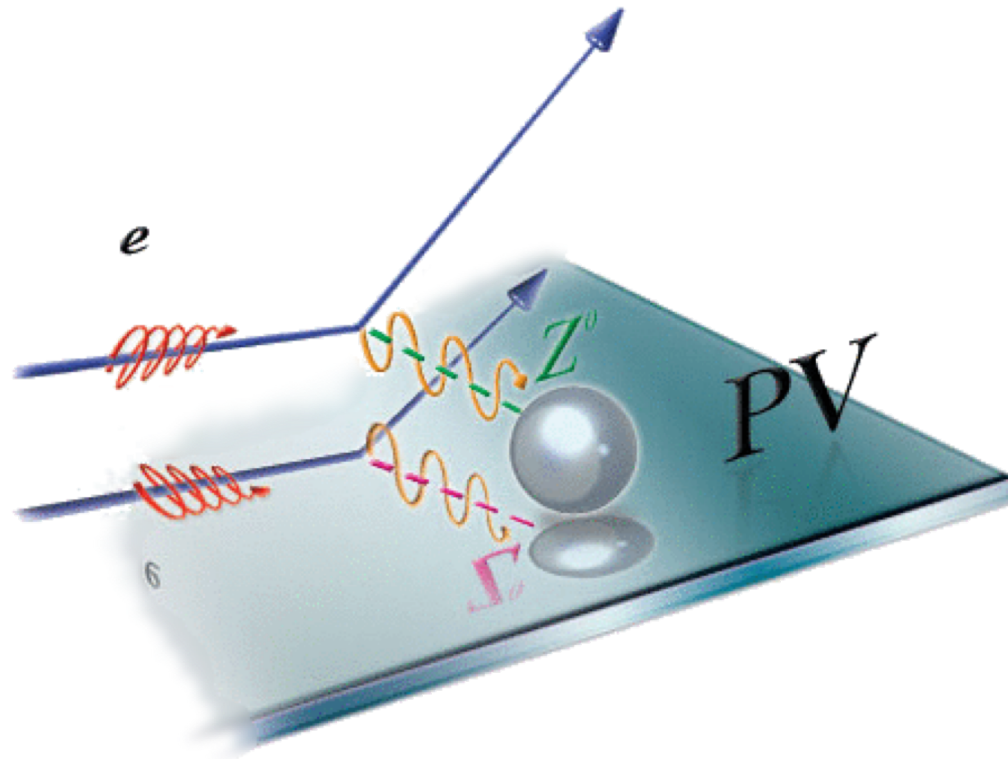
$$\mathcal{L}_{PV}^{EW} = \frac{G_F}{\sqrt{2}} \left[g_A^e (\bar{e} \gamma_\mu \gamma_5 e) \cdot \sum_q g_V^q (\bar{q} \gamma^\mu q) + g_V^e (\bar{e} \gamma_\mu e) \cdot \sum_q g_A^q (\bar{q} \gamma^\mu \gamma_5 q) \right]$$

$$\frac{g^2}{8M_W^2} = \frac{G_F}{\sqrt{2}} \quad C_{1q} = 2g_A^e g_V^q$$

-Electroweak Charges-

Particle	Electric Charge	Weak Vector Charge ($\sin^2 \theta_W \approx \frac{1}{4}$)
u	$+\frac{2}{3}$	$-2C_{1u} = +1 - \frac{8}{3} \sin^2 \theta_W \approx +\frac{1}{3}$
d	$-\frac{1}{3}$	$-2C_{1d} = -1 + \frac{4}{3} \sin^2 \theta_W \approx -\frac{2}{3}$
p(uud)	+1	$Q_W^p = 1 - 4 \sin^2 \theta_W \approx 0$ ← Proton's Weak Charge
n(udd)	0	$Q_W^n = -1$

Parity violating electron scattering



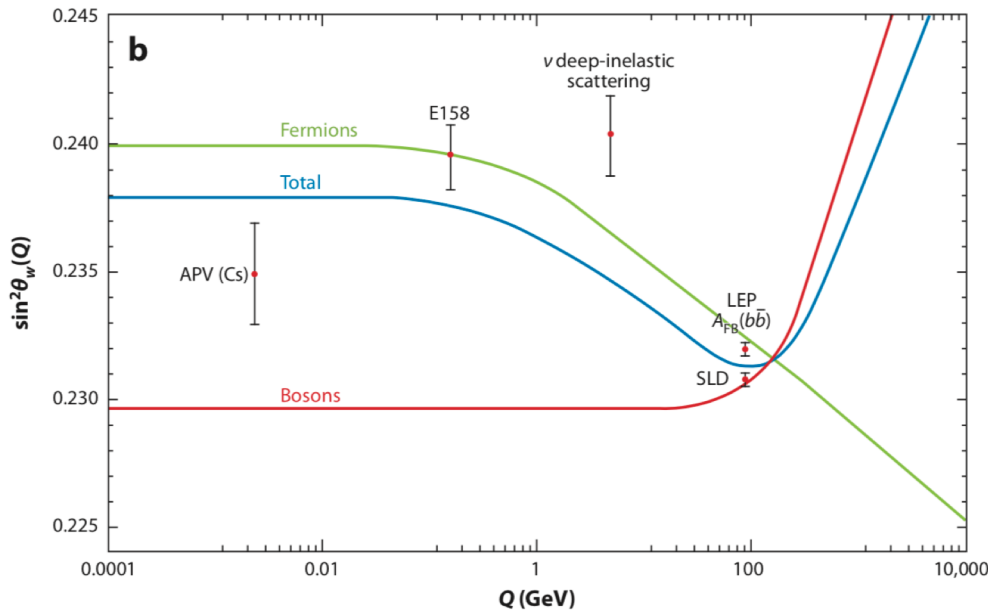
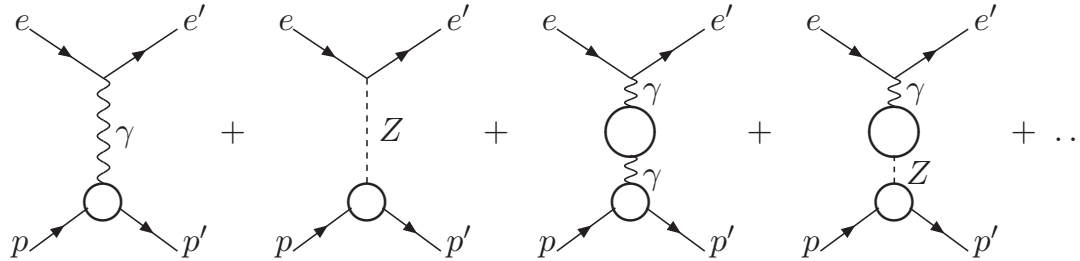
$$A_{PV} = \frac{\sigma_R - \sigma_L}{\sigma_R + \sigma_L} \sim \frac{2M_{EM}^* M_{Weak}}{|M_{EM}|^2}$$

For forward angle scattering
at low Q^2 :
 A_{PV} accesses Q_W^p :

Running of $\sin^2 \theta_W$: Standard Model test

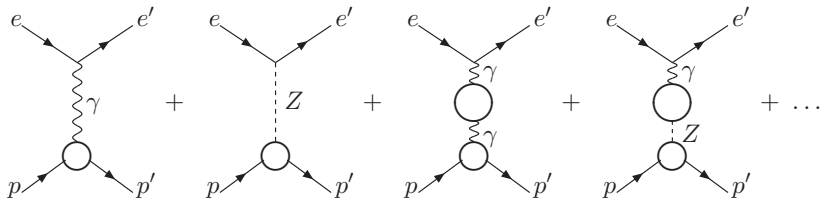
SM: universal quantum corrections leads to a scale dependent, „running“ $\sin^2 \theta_W(Q)$

$$\sin^2 \theta_W(Q) = e^2(Q)/g^2(Q)$$

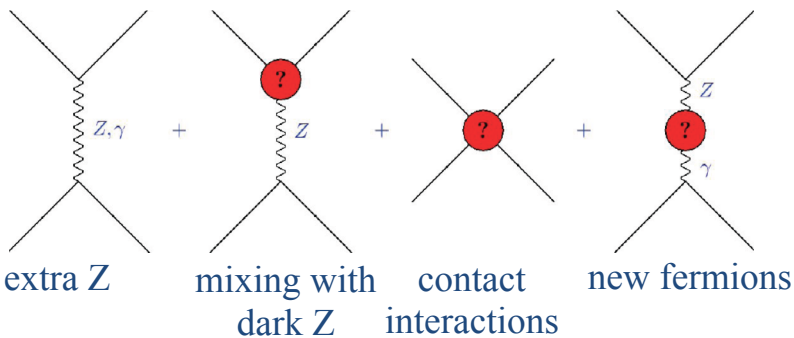


Running of $\sin^2 \theta_W$: New Physics Search

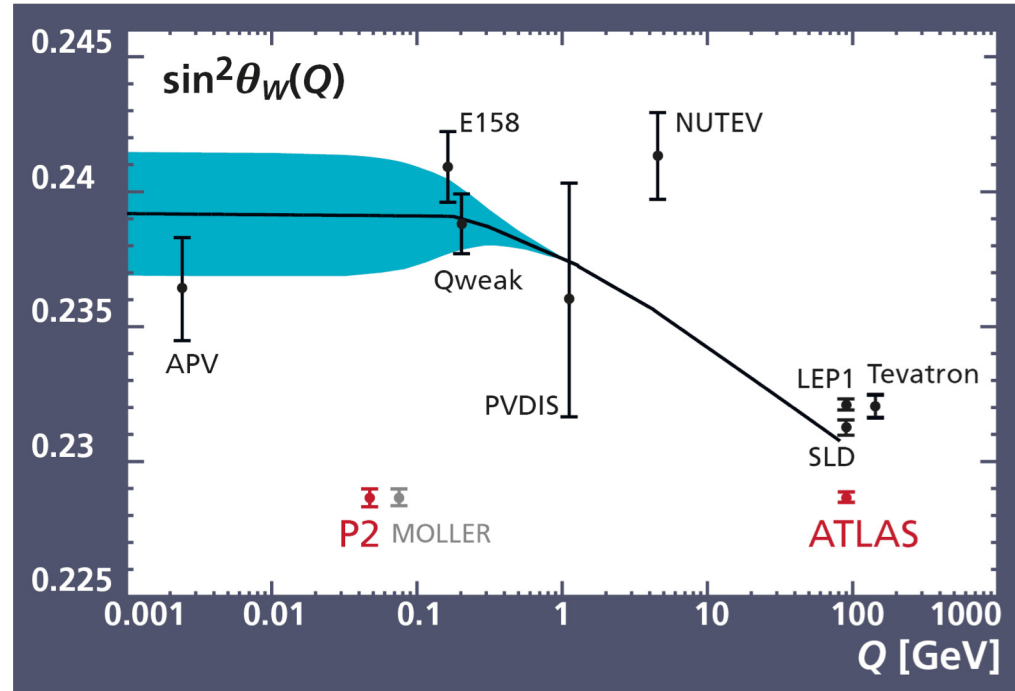
SM: universal quantum corrections leads to a scale dependent, „running“ $\sin^2 \theta_W(Q)$



Sensitivity to new beyond SM physics:



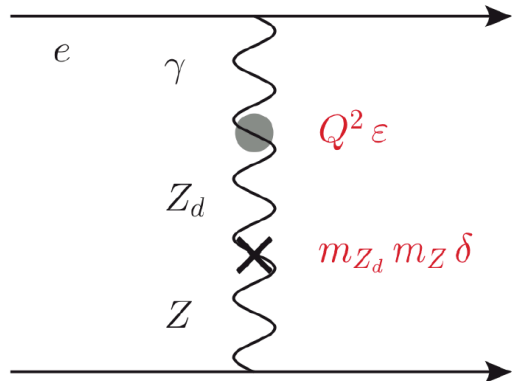
contact int: $\Lambda_{\text{new}} \approx 17 \text{ TeV}$ (E158@SLAC)



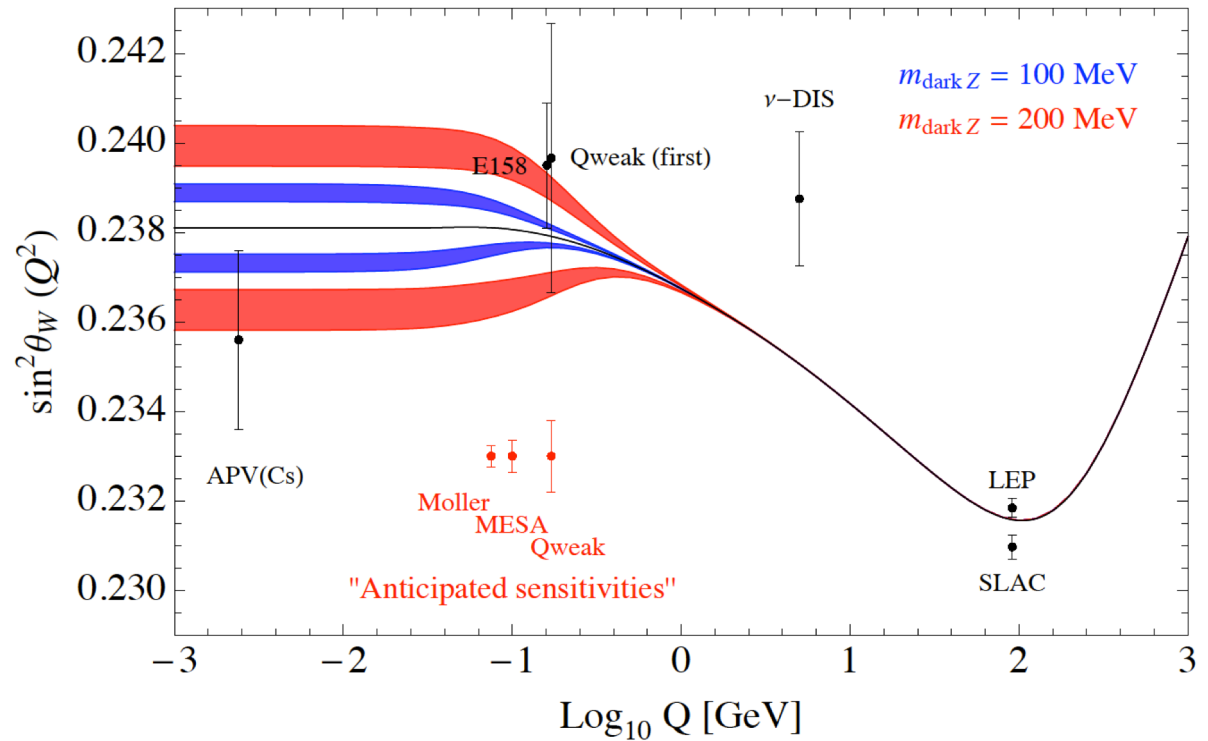
P2@MESA: 0.13 % measurement of $\sin^2 \theta_W$
 $\Lambda_{\text{new}} \approx 49 \text{ TeV}$

➔ exceeding scale in direct LHC searches
 complementarity with precision searches @ LHC

Running of $\sin^2 \theta_W$: New Physics Search



Marciano (2014)



Mainz Energy-Recovering Superconducting Accelerator

Extracted Beam Mode

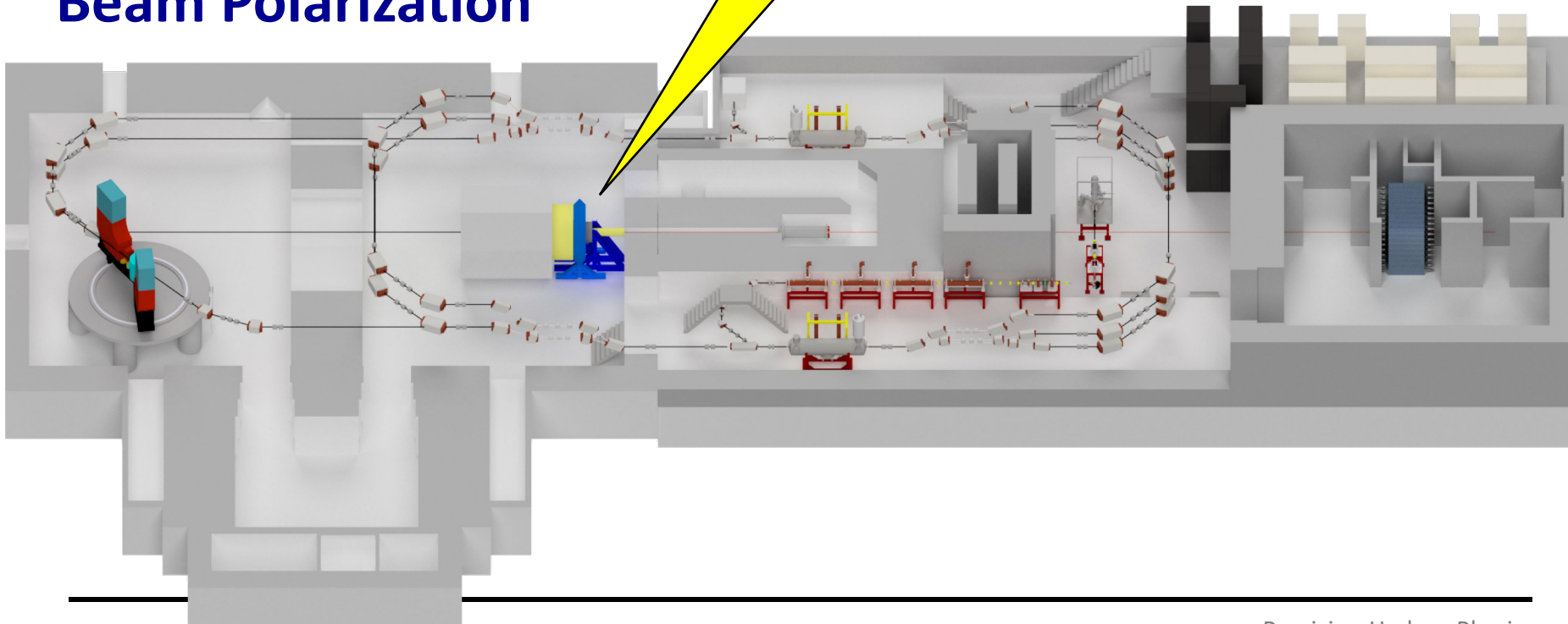
$$E_{\max} = 155 \text{ MeV}$$

$$I_{\max} = 150 \mu\text{A}$$

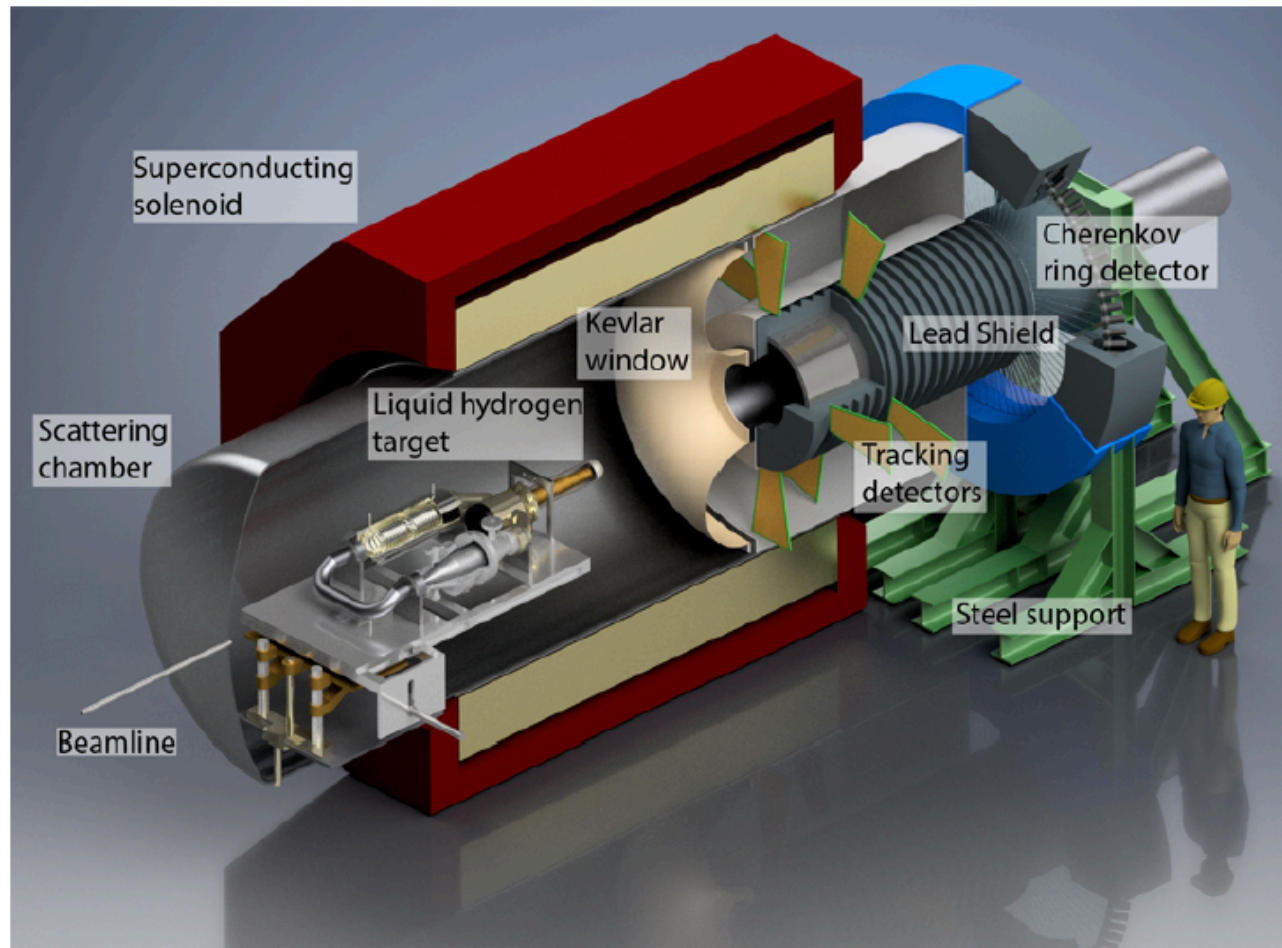
Beam Polarization

Mode 1:
Extracted Beam
P2 Experiment

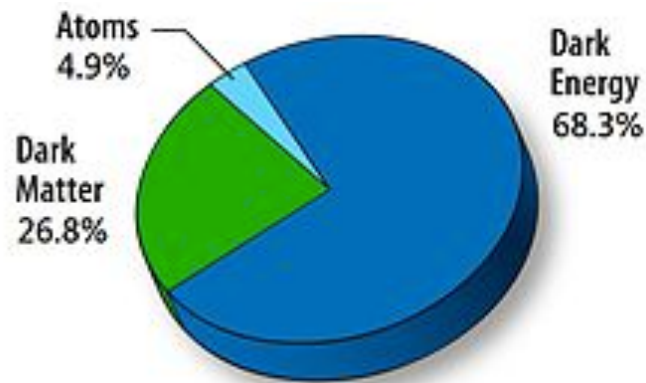
3 recirculations →
6 passes through SRF cavities



A Low- Q^2 Measurement of $\sin^2\theta_W$ at MESA

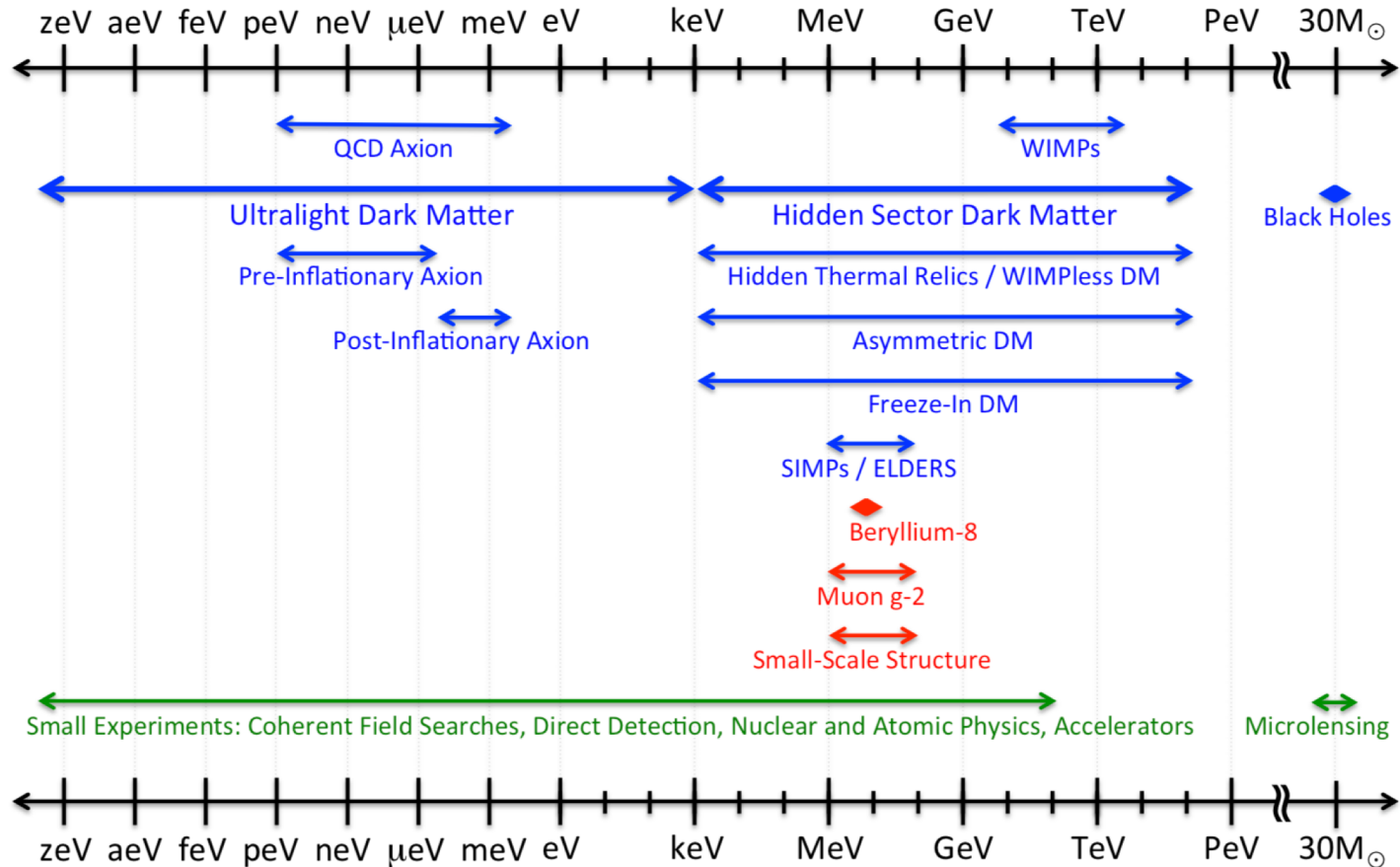


Search for a Dark Photon & Light dark matter



Dark Sector searches: worldwide effort

Dark Sector Candidates, Anomalies, and Search Techniques

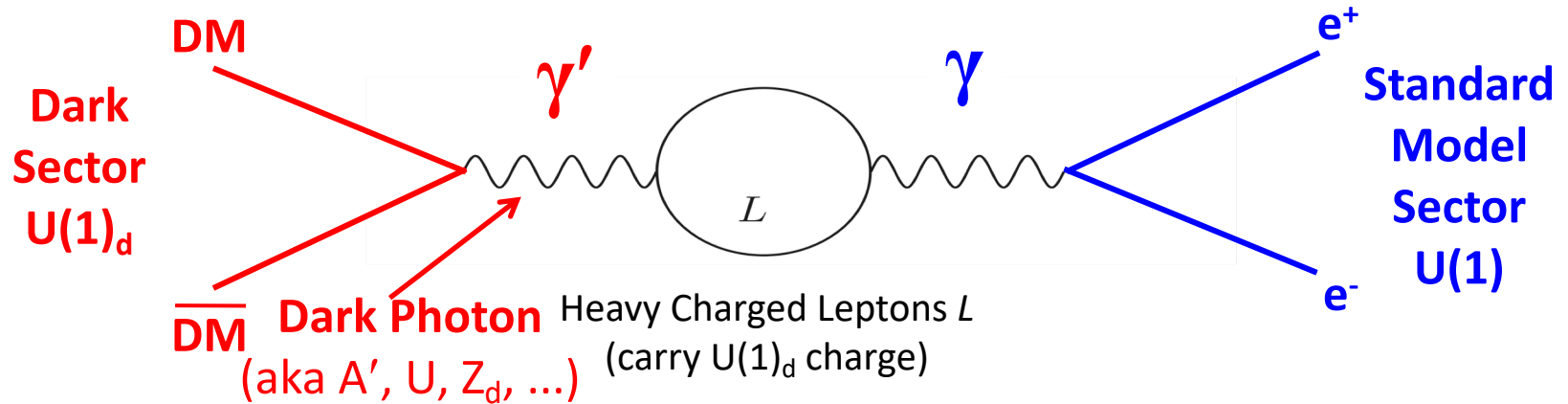


US cosmic visions Community Report: [arXiv1707:04591 \[hep-ph\]](https://arxiv.org/abs/1707.04591)

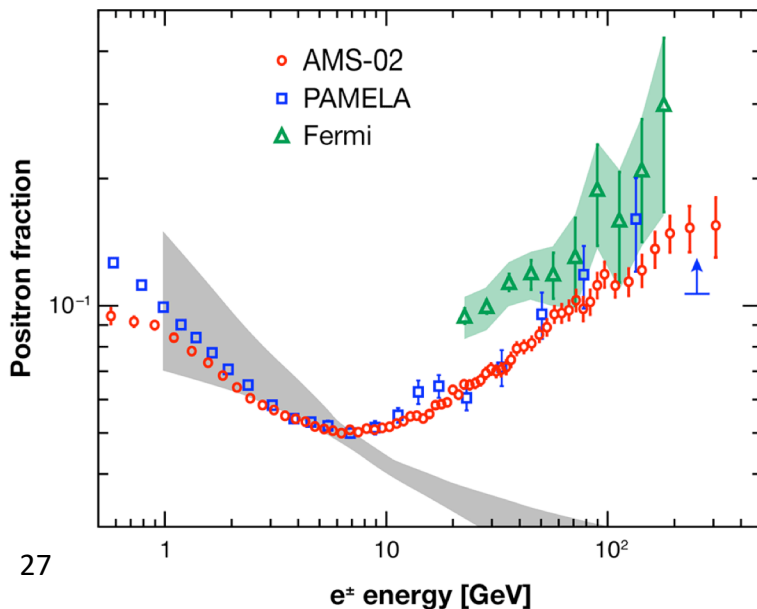
Kinetic Mixing: Dark photon/Dark Matter

A way to relate the dark sector to the SM (coupling $\sim \epsilon^2$)

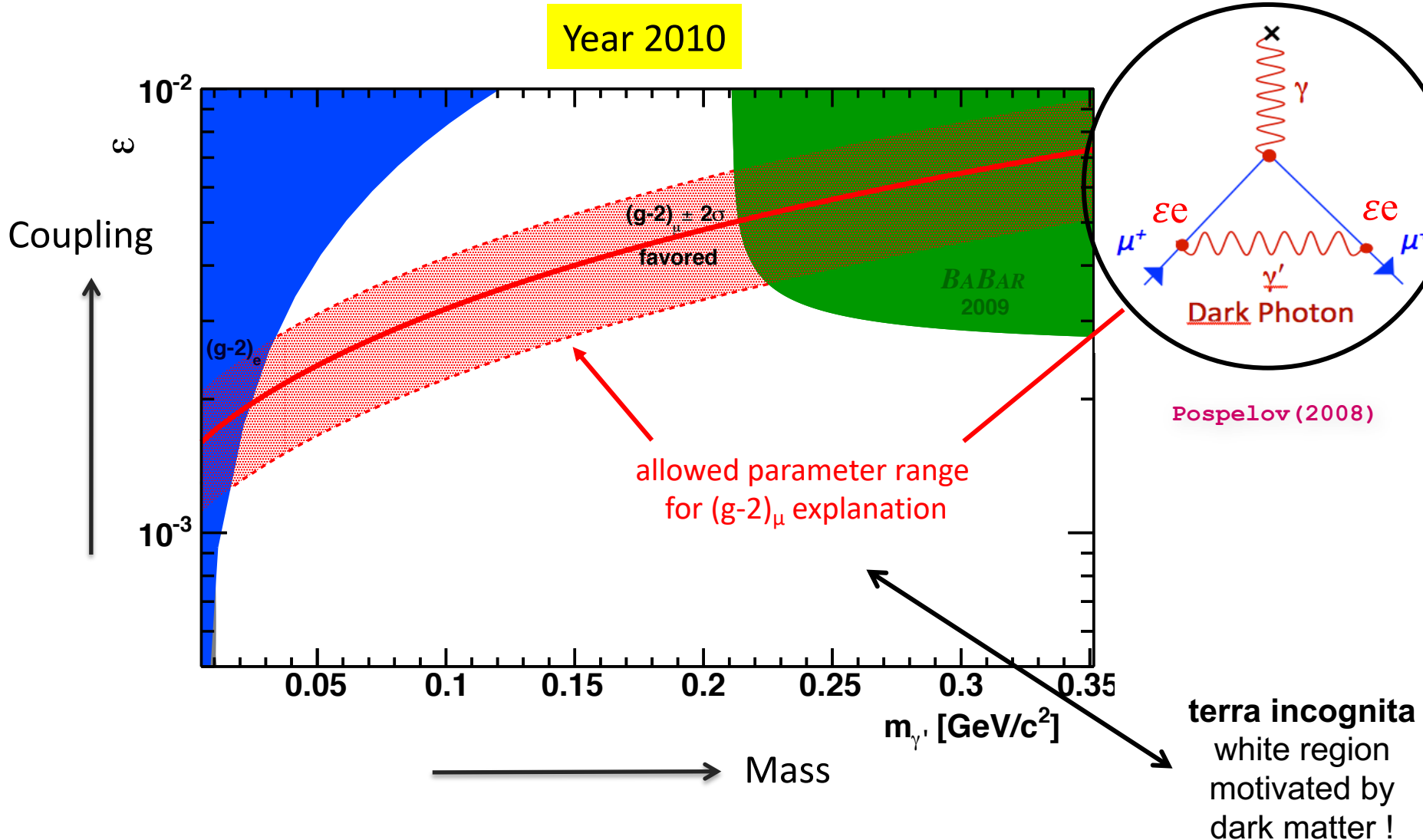
Holdom (1986)



Excess of positrons in cosmic ray spectrum due to Dark Matter annihilation?



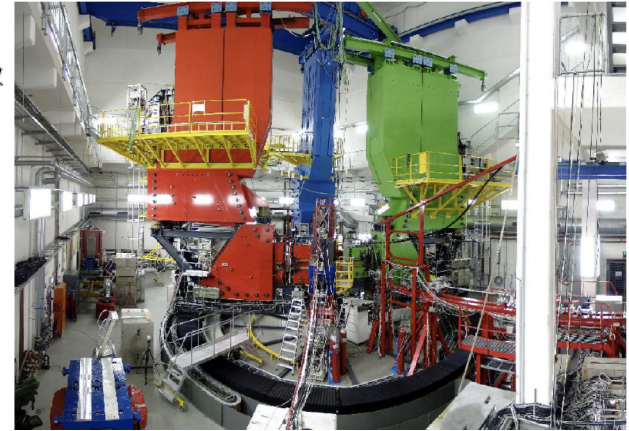
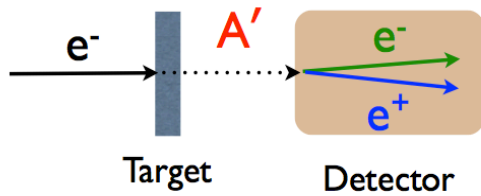
Dark Photon Status in 2010



Results from past years

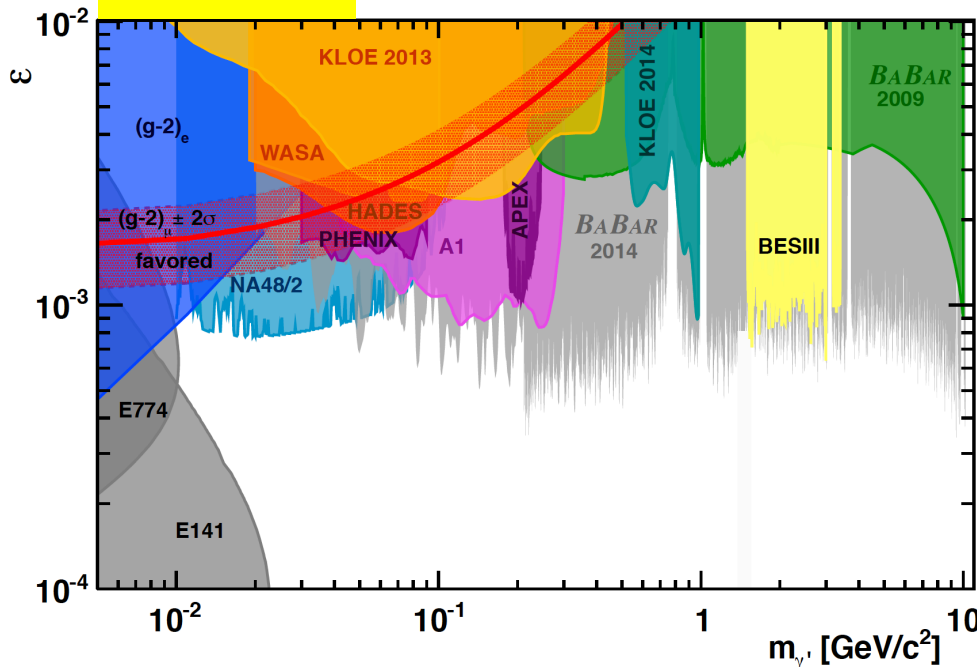
Low-Energy Electron Accelerators with high Intensity ideally suited for Dark Photon search

Bjorken et al. (2009)



Bethe-Heitler type process

Year 2015



Dark Photon as explanation for $(g-2)_\mu$ (almost) ruled out !
... at least in most straight-forward model

Low-mass range will be covered by MESA project

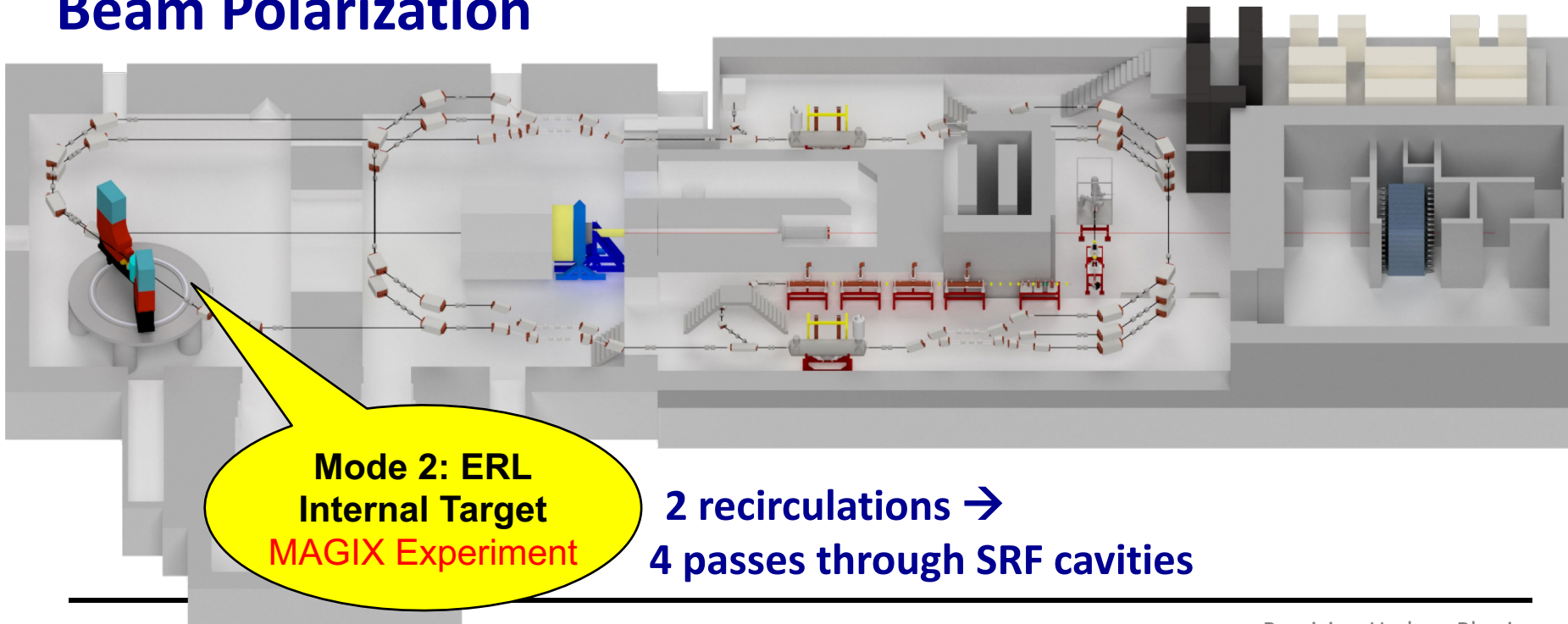
Mainz Energy-Recovering Superconducting Accelerator

Recirculating ERL Mode

$E_{\max} = 105 \text{ MeV}$

$I_{\max} > 1 \text{ mA}$

Beam Polarization

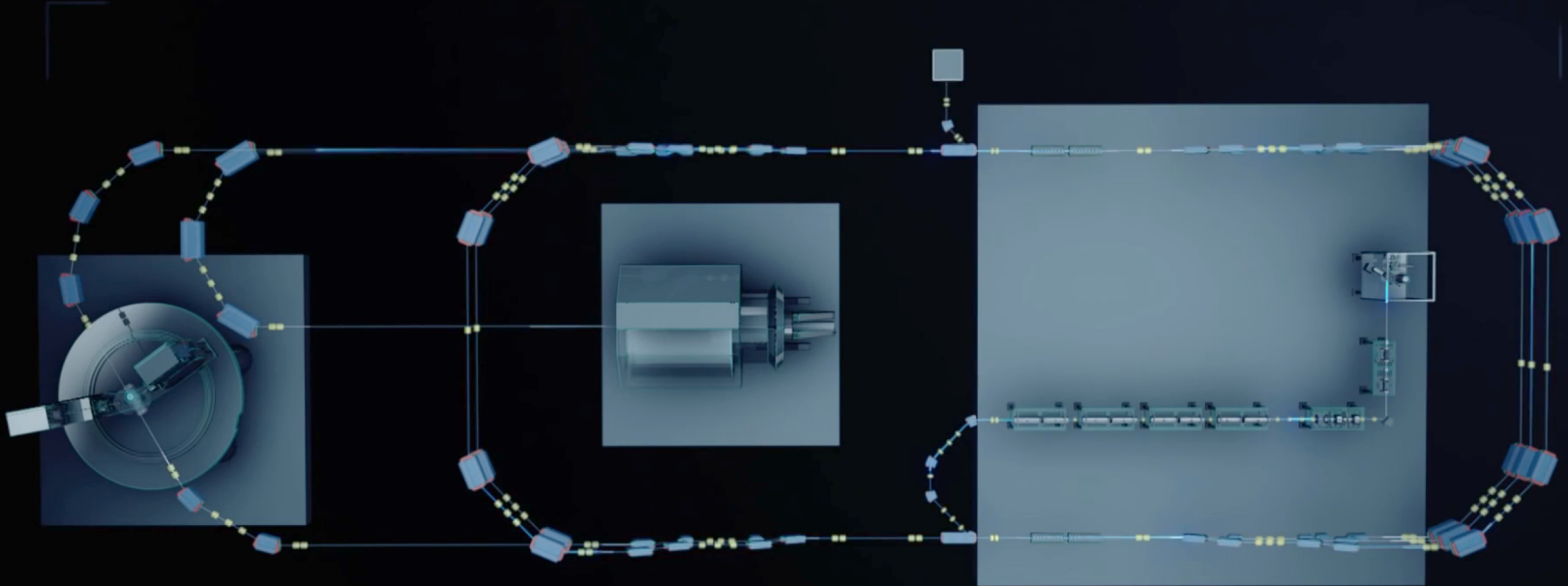


Internal Expt. MAGIX @ MESA ERL Mode

**Operation of a high-intensity (polarized) ERL beam
in conjunction with light internal target**

→ a novel technique in nuclear and particle physics

→ precise measurement of low momenta tracks at competitive luminosities



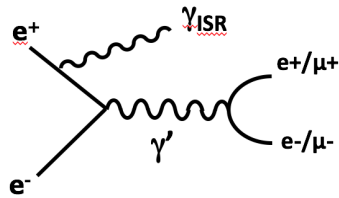
Dark Sector Searches at MAGIX



Visible Dark Photon Model

$$M_{\text{Dark Photon}} \ll M_{\text{Dark Matter}}$$

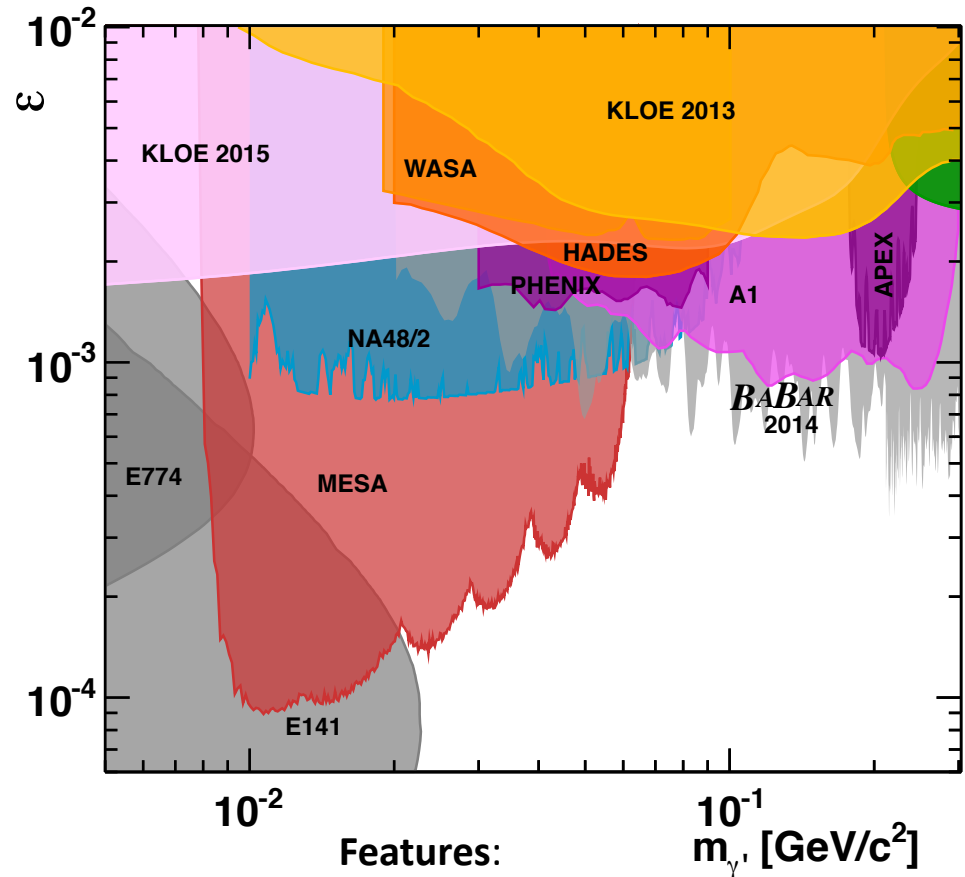
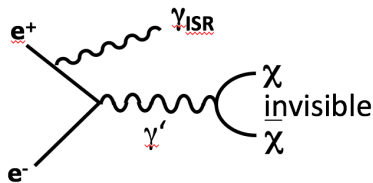
Dark Photon decaying into SM particles



Invisible Dark Photon Model

$$M_{\text{Dark Photon}} > M_{\text{Dark Matter}}$$

Dark Photon decaying into Dark matter particles

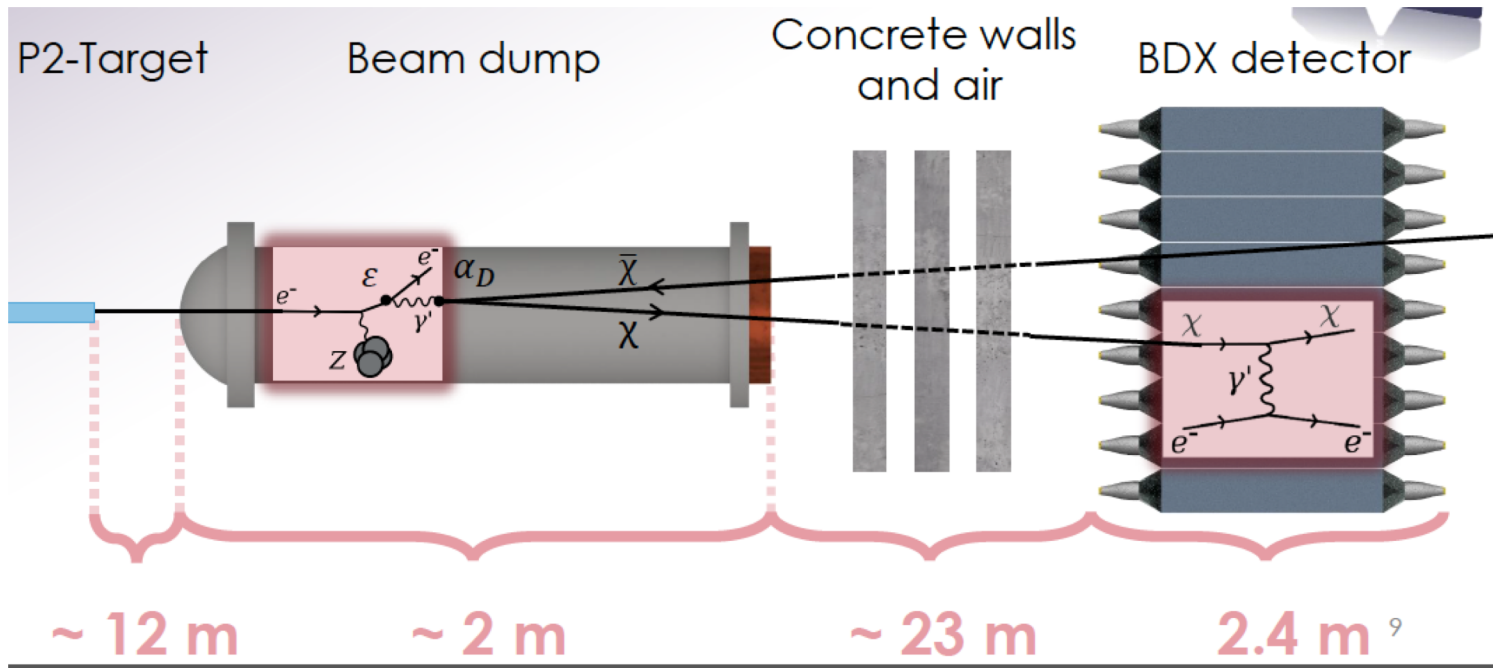


Features:

- Xe gas target
- Luminosity $10^{35} \text{ cm}^{-2}\text{s}^{-1}$
- 6 month of data taking

Beam Dump Experiment (BDX) @ MESA

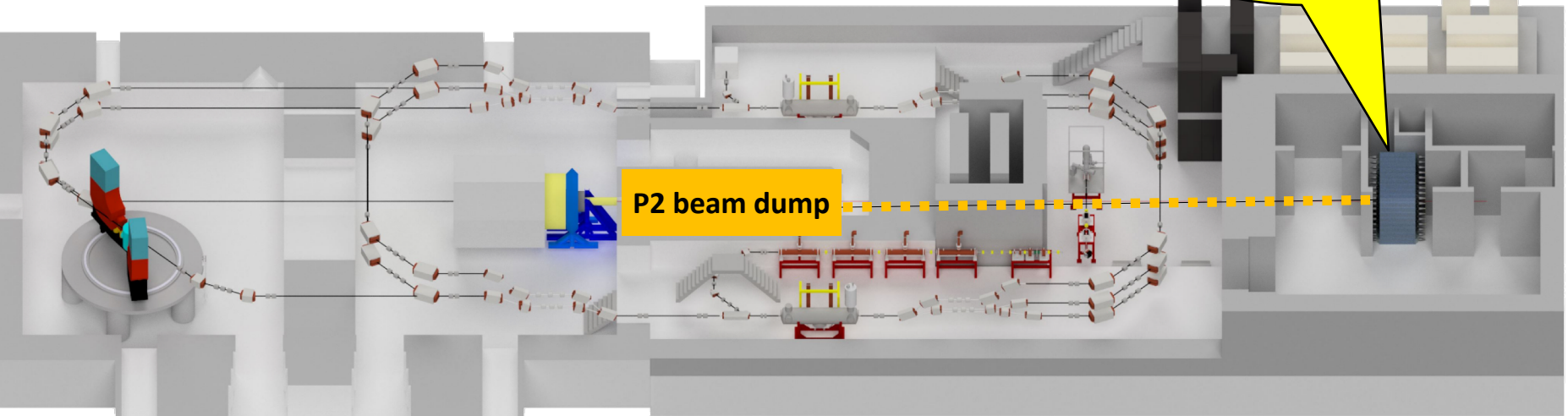
Electron Scattering (MESA) on Beam Dump
→ Collimated pair of Dark Matter particles !



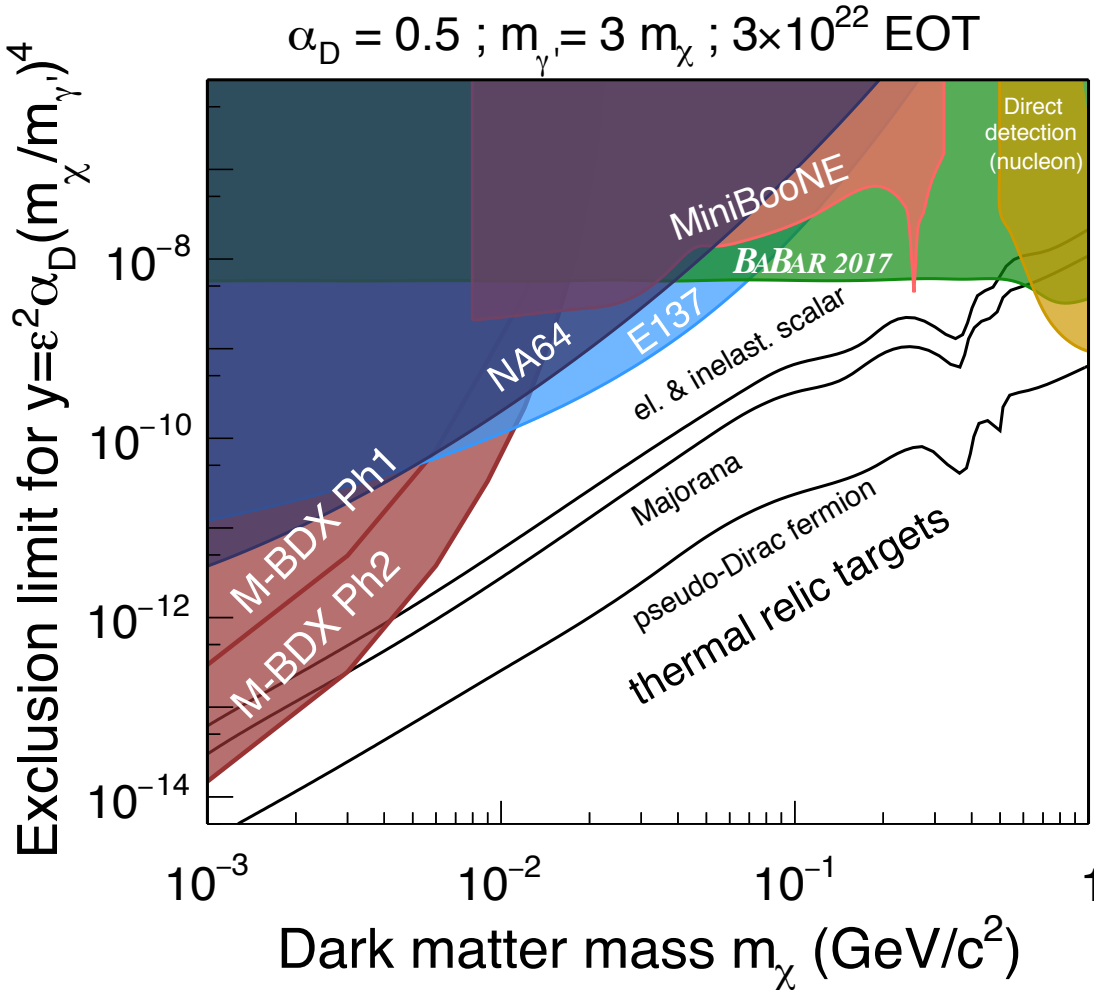
10,000 hours data taking @ 150 μA
→ $>10^{22}$ electrons on target (EOT)

**Electron Scattering (MESA) on Beam Dump
→ Collimated pair of Dark Matter particles !**

**Extracted beam
BDX Experiment**

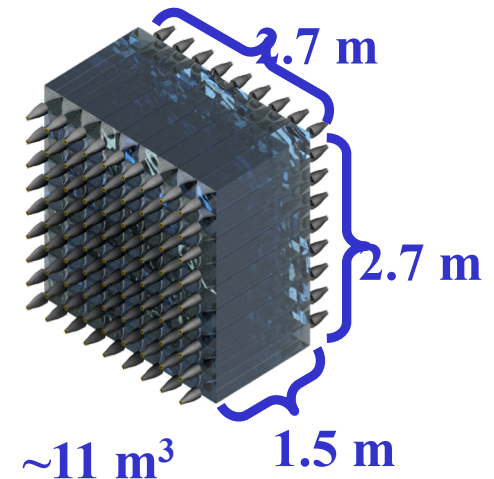


**10,000 hours data taking @ 150 μ A
→ $>10^{22}$ electrons on target (EOT)**

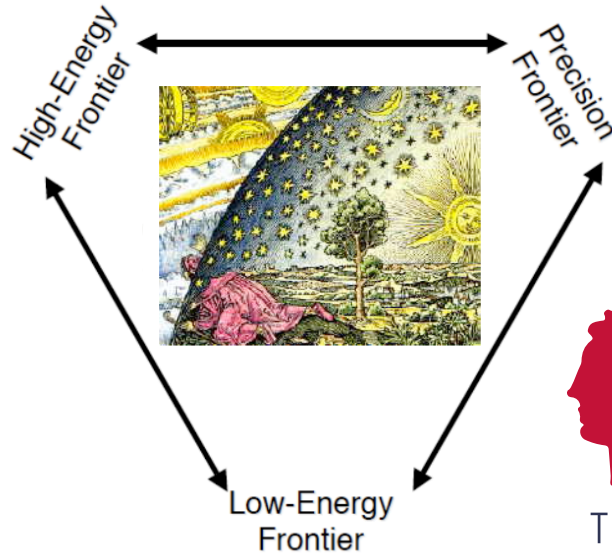
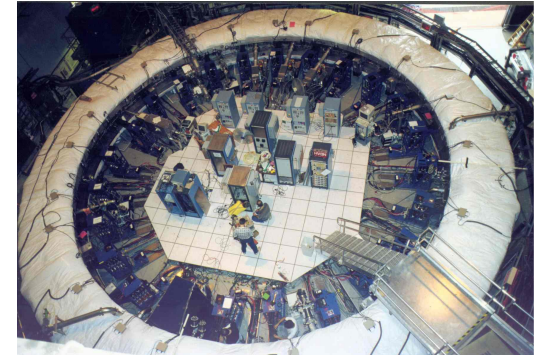
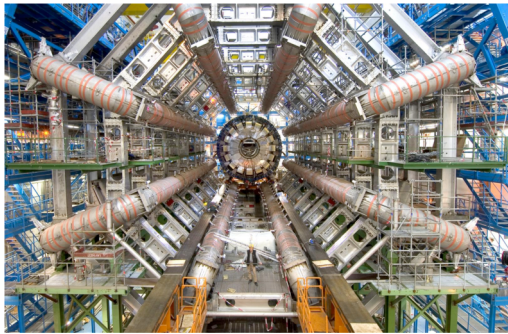


Detector layouts:

- Phase 1: existing PbF2 crystals of A4 experiment (0.13 m³ volume)
- Phase 2: 11m³ Leadglass calorimeter



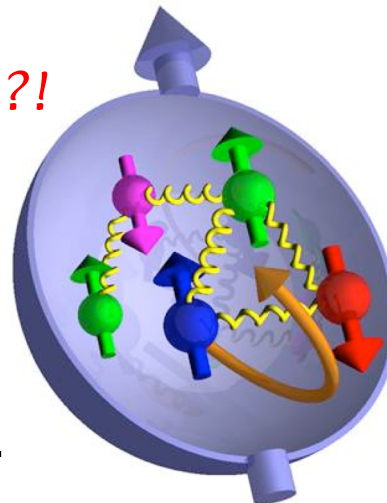
Conclusions



THE LOW-ENERGY FRONTIER
OF THE STANDARD MODEL

Puzzles at low Energies ?!

- Proton Radius
- $(g-2)_\mu$
- Dark Photon



Low Energy experiments
study the structure
of particles
and more than that !

→ New tools: MESA