

# Neutrinos at colliders and LNV

Martin Hirsch

Instituto de Física Corpuscular - CSIC  
Universidad Valencia, Spain



VNIVERSITAT  
ID VALÈNCIA



GENERALITAT  
VALENCIANA

**IFIC**  
INSTITUT DE FÍSICA  
CORPUSCULAR



EXCELENCIA  
SEVERO  
OCHOA



**CSIC**  
CONSEJO SUPERIOR DE INVESTIGACIONES CIENTÍFICAS

**ASTROPARTICLES**  
Astroparticles and High Energy Physics Group

<http://www.astroparticles.es/>



# *Experimental talks*

---

J.P. Chou

New detectors at the lifetime frontier of the LHC and beyond

L. Shchutska

LHC searches for heavy neutral leptons and displaced signatures



# Outline

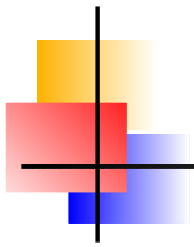
---

*I.* Introduction

*II.* Seesaw @ LHC

*III.* Beyond minimal seesaw(s)

*IV.* Leptogenesis and LHC



*I.*

# Introduction

or

Why is  $m_\nu$  so small?

# Global fit: Oscillation data

<https://globalfit.astroparticles.es/>

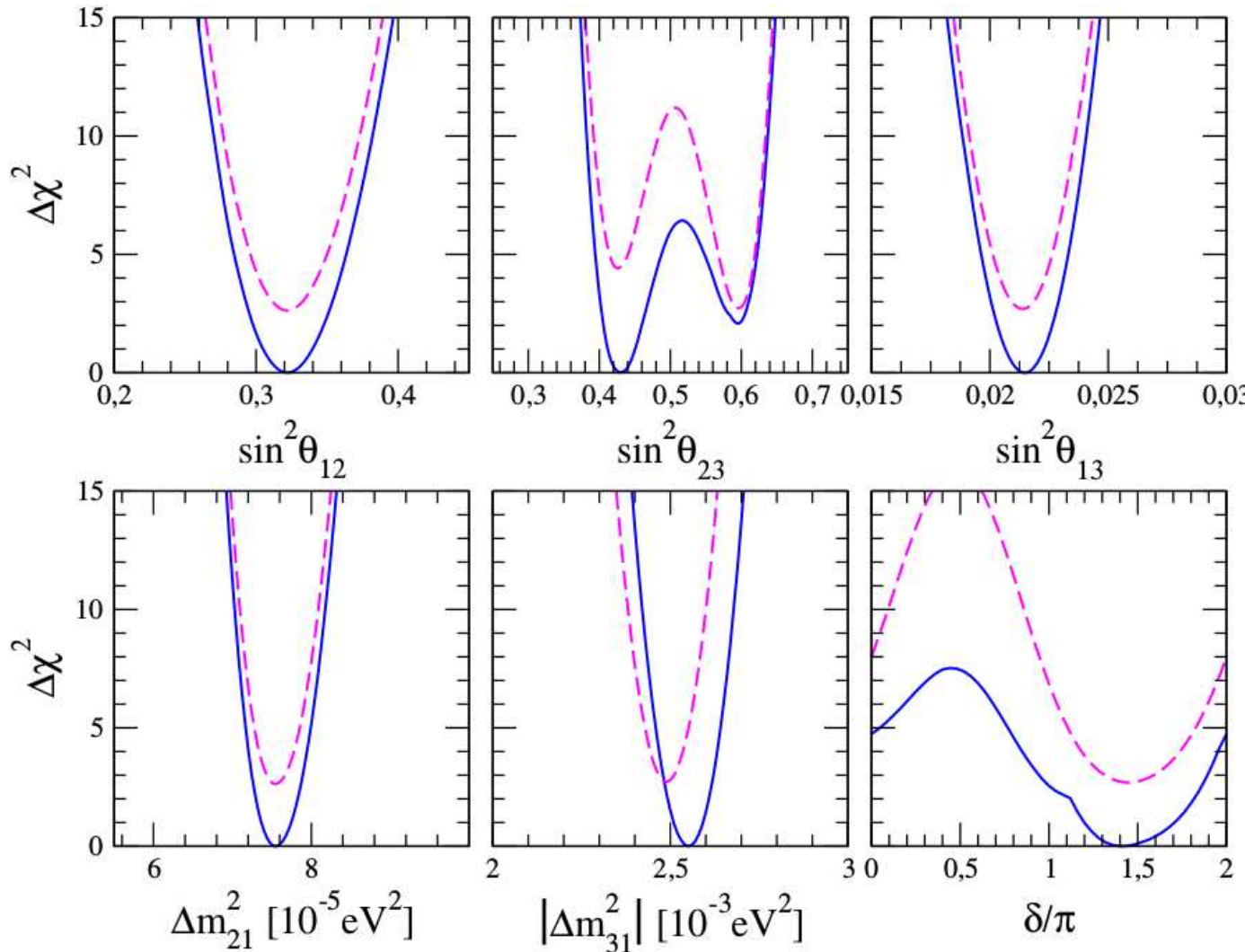
P. de Salas et al.,  
PLB782 (2018) 633

$\theta_{12} \equiv$  solar angle  
 $\theta_{23} \equiv$  atmospheric  
 $\theta_{13} \equiv$  reactor

full: NH

dashed: IH

$\Delta m_{12}^2 \equiv$  solar scale  
 $\Delta m_{23}^2 \equiv$  atm. scale  
 $\delta \equiv$  Dirac phase



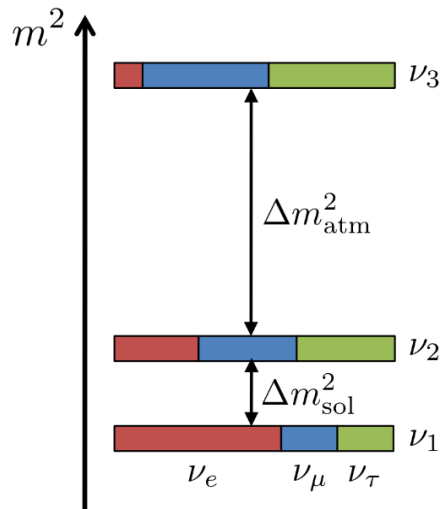
Experiments: Super-K (atm), Super-K (solar), SNO, Gallex, Borexino, KamLAND, MINOS, NO $\nu$ A, T2K, IceCube-DeepCore, RENO, Double-Chooz, DayaBay, ...

# Neutrino oscillations

## Normal ordering (NO)

$$m_1 < m_2 < m_3$$

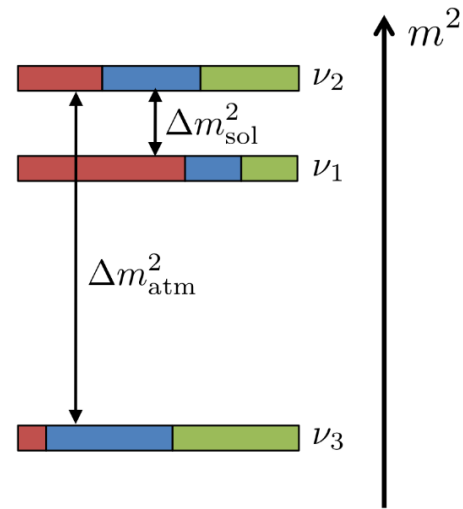
$$\sum m_k \gtrsim 0.06 \text{ eV}$$



## Inverted ordering (IO)

$$m_3 < m_1 < m_2$$

$$\sum m_k \gtrsim 0.1 \text{ eV}$$



20 years after  
Super-K, 1998

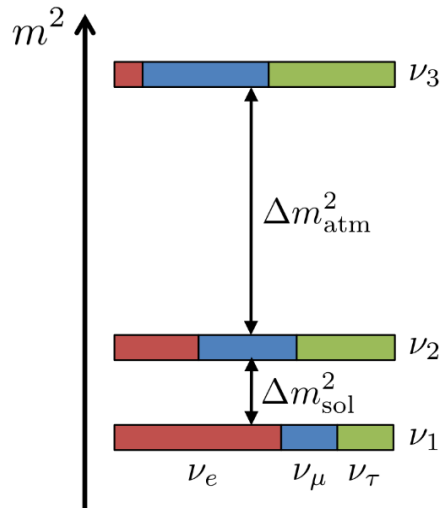
2  $\Delta m^2$  and  
all 3  $\theta_{ij}$   
measured with  
high precision,  
but ...

# Neutrino oscillations

## Normal ordering (NO)

$$m_1 < m_2 < m_3$$

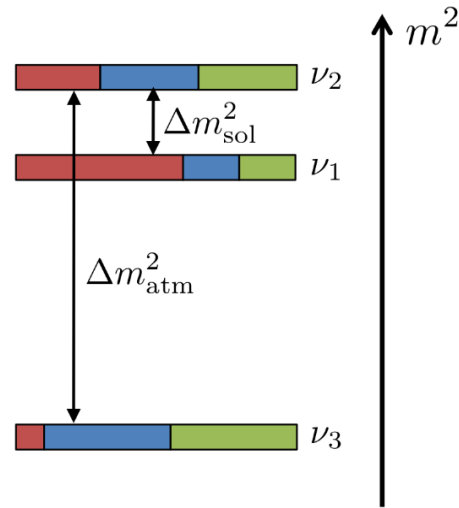
$$\sum m_k \gtrsim 0.06 \text{ eV}$$



## Inverted ordering (IO)

$$m_3 < m_1 < m_2$$

$$\sum m_k \gtrsim 0.1 \text{ eV}$$



20 years after  
Super-K, 1998

2  $\Delta m^2$  and  
all 3  $\theta_{ij}$   
measured with  
high precision,  
but ...

BUT, still unknown:

Absolute mass scale?

Which hierarchy?

CP phase?

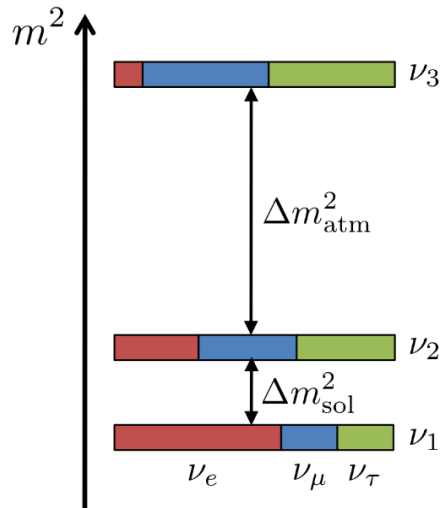
Majorana OR Dirac?

# Neutrino oscillations

## Normal ordering (NO)

$$m_1 < m_2 < m_3$$

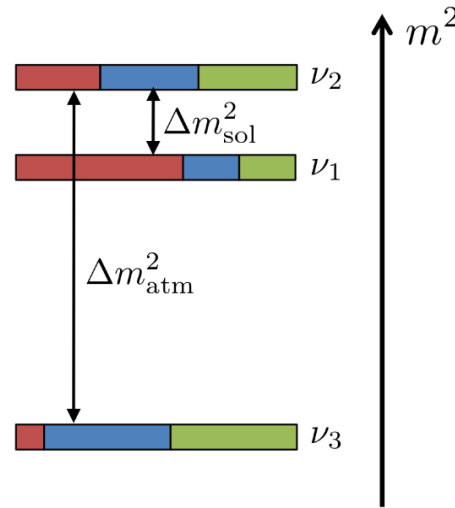
$$\sum m_k \gtrsim 0.06 \text{ eV}$$



## Inverted ordering (IO)

$$m_3 < m_1 < m_2$$

$$\sum m_k \gtrsim 0.1 \text{ eV}$$



20 years after  
Super-K, 1998

2  $\Delta m^2$  and  
all 3  $\theta_{ij}$   
measured with  
high precision,  
but ...

BUT, still unknown:

Absolute mass scale?

Which hierarchy?

CP phase?

Majorana OR Dirac?

Upper limit only,  $\sim 2 \text{ eV}$  ( $^3\text{H}$ ),  $\sim (0.1 - 0.2) \text{ eV}$  ( $0\nu\beta\beta$ )

$\sim 2 \sigma$  preference for NH

Indication for  $\delta \sim (3/2)\pi$

Unknown





# Theoretical expectation?

---

Majorana Neutrino mass

$$m_\nu \simeq \frac{(Yv)^2}{\Lambda}$$

Weinberg, 1979

Smallness of neutrino mass  
can be “explained” by:

⇒ High scale: **Large  $\Lambda$**   
“classical” seesaw

# Theoretical expectation?

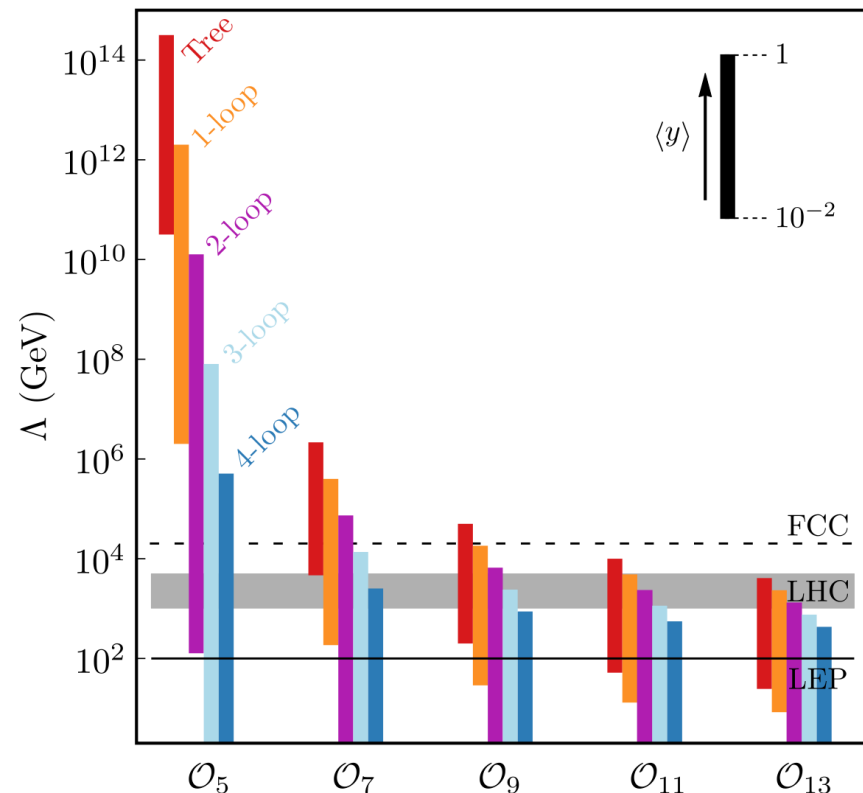
Majorana Neutrino mass generated from an  $n$ -loop dimension  $d$  diagram:

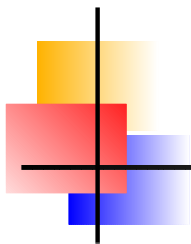
$$m_\nu \simeq \frac{(Yv)^2}{\Lambda} \cdot \epsilon \cdot \left(\frac{Y^2}{16\pi^2}\right)^n \cdot \left(\frac{Yv}{\Lambda}\right)^{d-5}$$

Smallness of neutrino mass can be “explained” by:

- ⇒ High scale: **Large  $\Lambda$**   
“classical” seesaw
- ⇒ Loop factor:  $n \geq 1$   
+ “smallish”  $Y \sim \mathcal{O}(10^{-3} - 10^{-1})$
- ⇒ Higher order:  $d = 7, 9, 11$
- ⇒ Nearly conserved  $L$ ,  
i.e. **small  $\epsilon$**  (“inverse seesaw”)

... or combination thereof

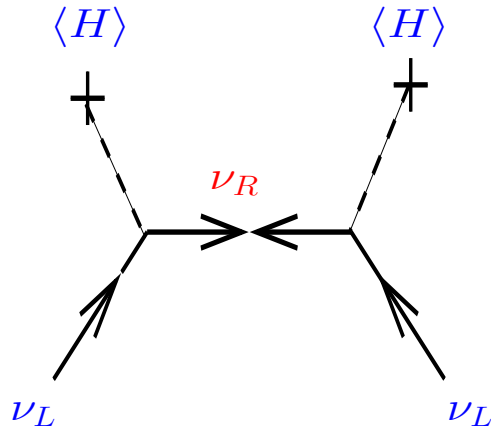




*II.*

# Seesaw @ LHC

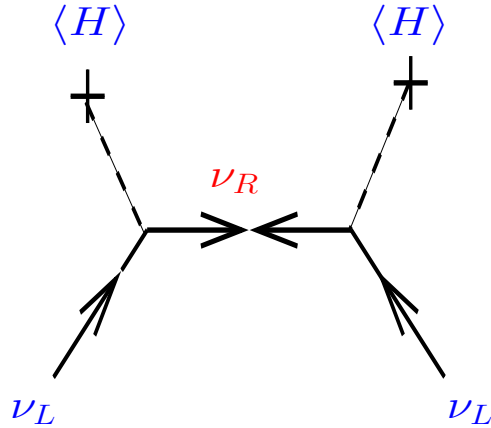
# HNL decay seesaw-I



$$m_\nu \simeq \frac{(m_D)^2}{M_M} = \frac{(Y_\nu v)^2}{M_M}$$

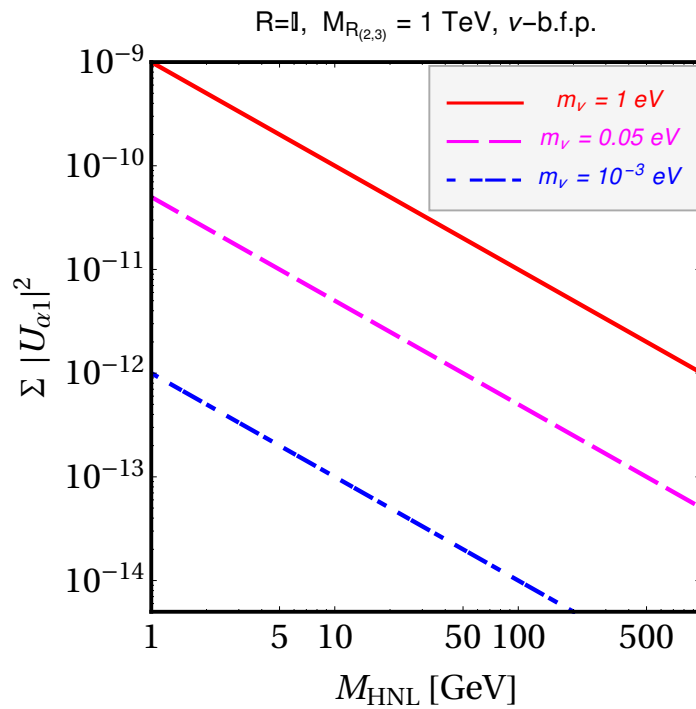
$$U_{\alpha i} \propto \frac{(Y_{\nu\alpha i} v)}{M_{M_i}} \propto \sqrt{\frac{m_{\nu\alpha}}{M_{M_i}}}$$

# HNL decay seesaw-I

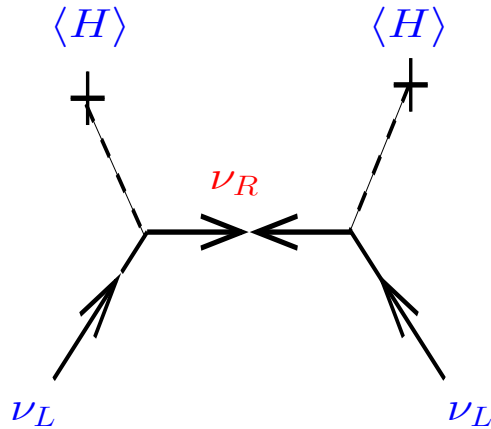


$$m_\nu \simeq \frac{(m_D)^2}{M_M} = \frac{(Y_\nu v)^2}{M_M}$$

$$U_{\alpha i} \propto \frac{(Y_{\nu \alpha i} v)}{M_{M_i}} \propto \sqrt{\frac{m_{\nu \alpha}}{M_{M_i}}}$$

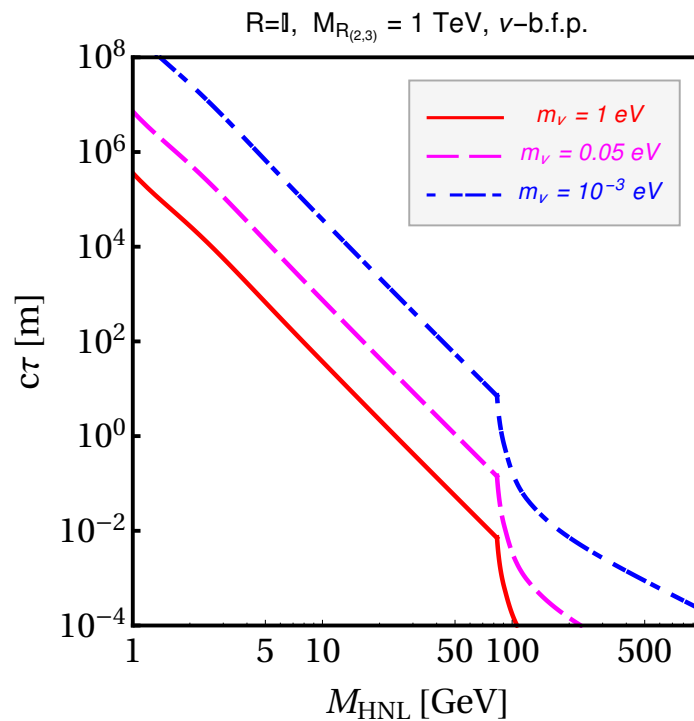


# Decay length seesaw-I



$$m_\nu \simeq \frac{(m_D)^2}{M_M} = \frac{(Y_\nu v)^2}{M_M}$$

$$U_{\alpha i} \propto \frac{(Y_{\nu\alpha i} v)}{M_{M_i}} \propto \sqrt{\frac{m_{\nu\alpha}}{M_{M_i}}}$$



Neutrino width from:  
 Atre et al.  
 JHEP 0905 (2009) 030  
 and  
 Bondarenko et al.  
 1805.08567



# Inverse seesaw

Inverse seesaw, basis  $(\nu_L, \nu_R^c, S_R^c)$ :

$$M_\nu = \begin{pmatrix} 0 & m_D^T & 0 \\ m_D & 0 & M_R \\ 0 & M_R^T & \mu \end{pmatrix}$$

Mohapatra &  
Valle, 1986

“Inverse” seesaw, because:

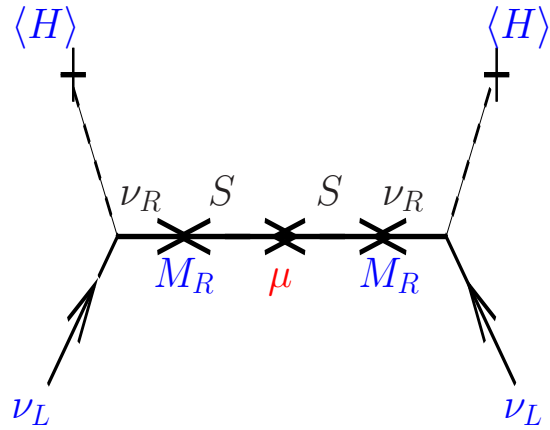
$$\begin{aligned} \hat{m}_\nu &= V_L m_\nu V_L^T = V_L m_D^T \cdot (M_R^T)^{-1} \cdot \mu \cdot (M_R)^{-1} \cdot m_D V_L^T \\ M_\pm &= \left( \hat{M}_R + \left\{ m_D \cdot m_D^T, \hat{M}_R^{-1} \right\} \right) \pm \frac{1}{2} \mu V \end{aligned}$$

⇒ - 3 light eigenvalues:  $\hat{m}_\nu$

⇒ - (3+3) heavy (nearly diagonal) eigenvalues :  $\hat{M}_\pm = \hat{M}_R \pm \frac{1}{2} \mu V$  **Quasi-Dirac!**

**Smallness** of  $m_\nu$  due to **nearly conserved L!**

# Decay length ISS

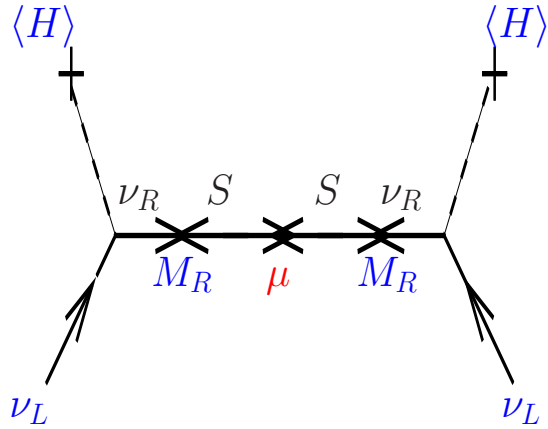


$$m_\nu \simeq \left( \frac{m_D}{M_R} \right)^2 \mu$$

$$U_{\alpha i} \propto \frac{m_D}{M_R} \propto \sqrt{\frac{m_\nu}{\mu}}$$

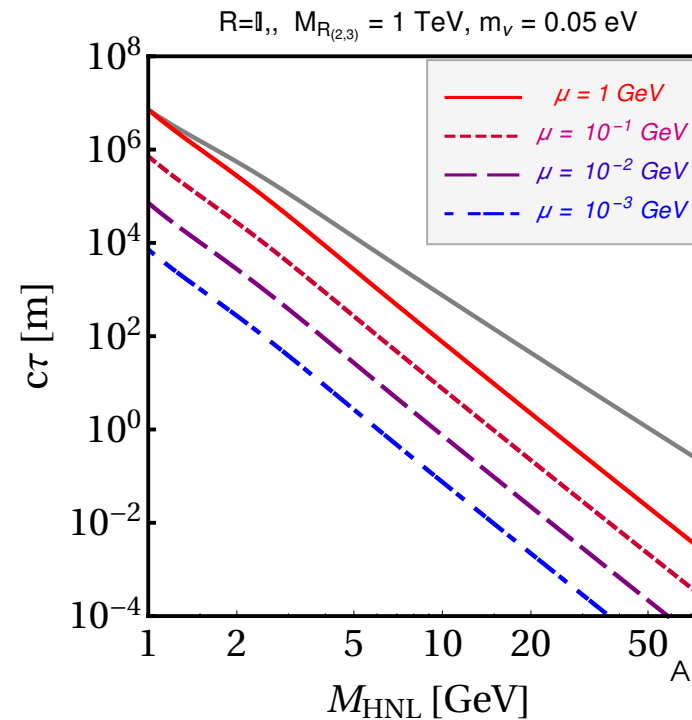
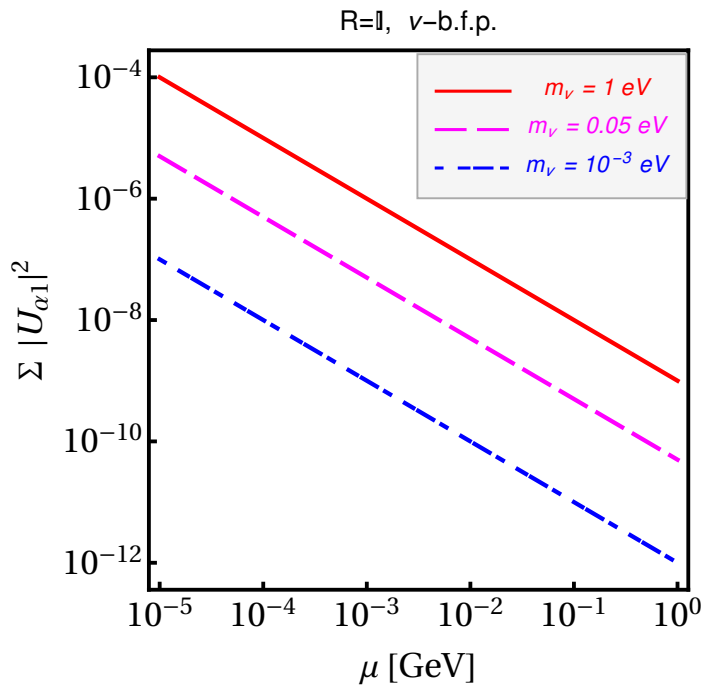


# Decay length ISS

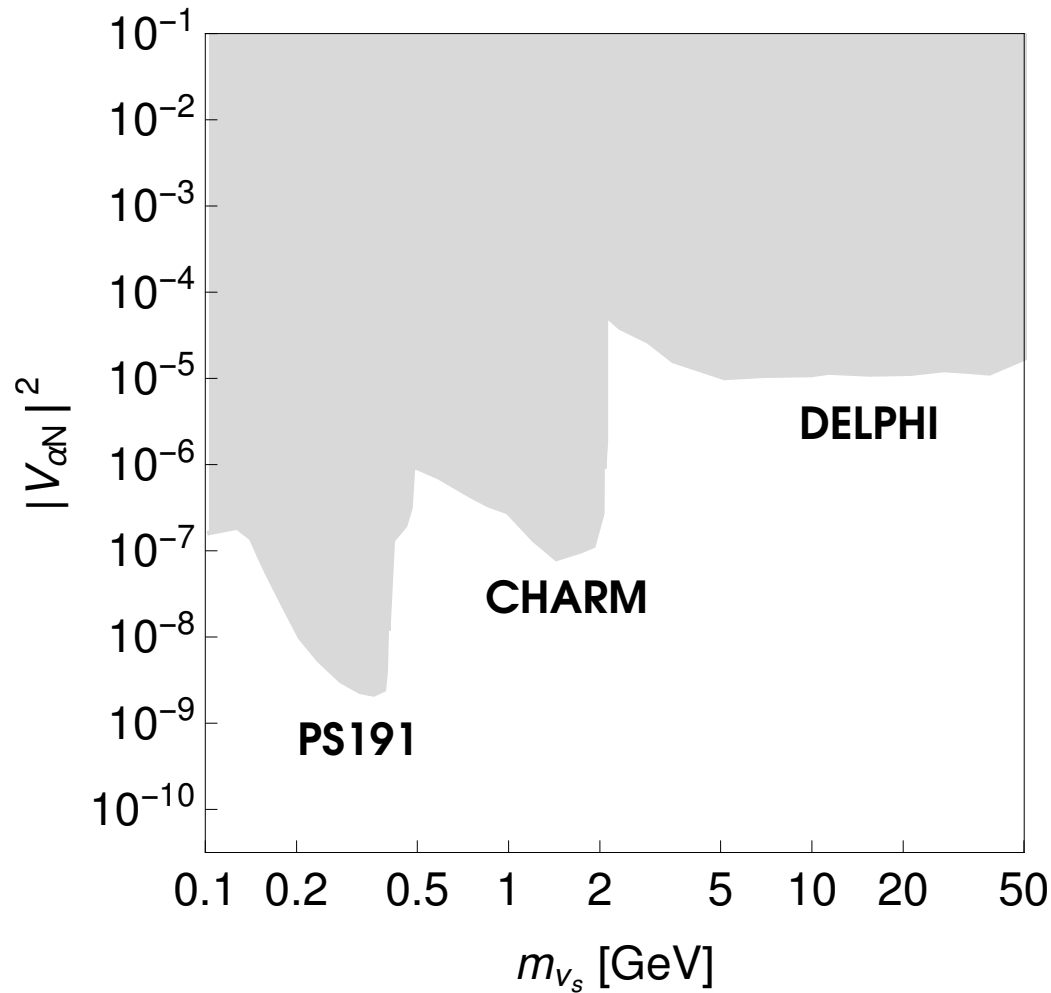


$$m_\nu \simeq \left( \frac{m_D}{M_R} \right)^2 \mu$$

$$U_{\alpha i} \propto \frac{m_D}{M_R} \propto \sqrt{\frac{m_\nu}{\mu}}$$



# Forecast searches



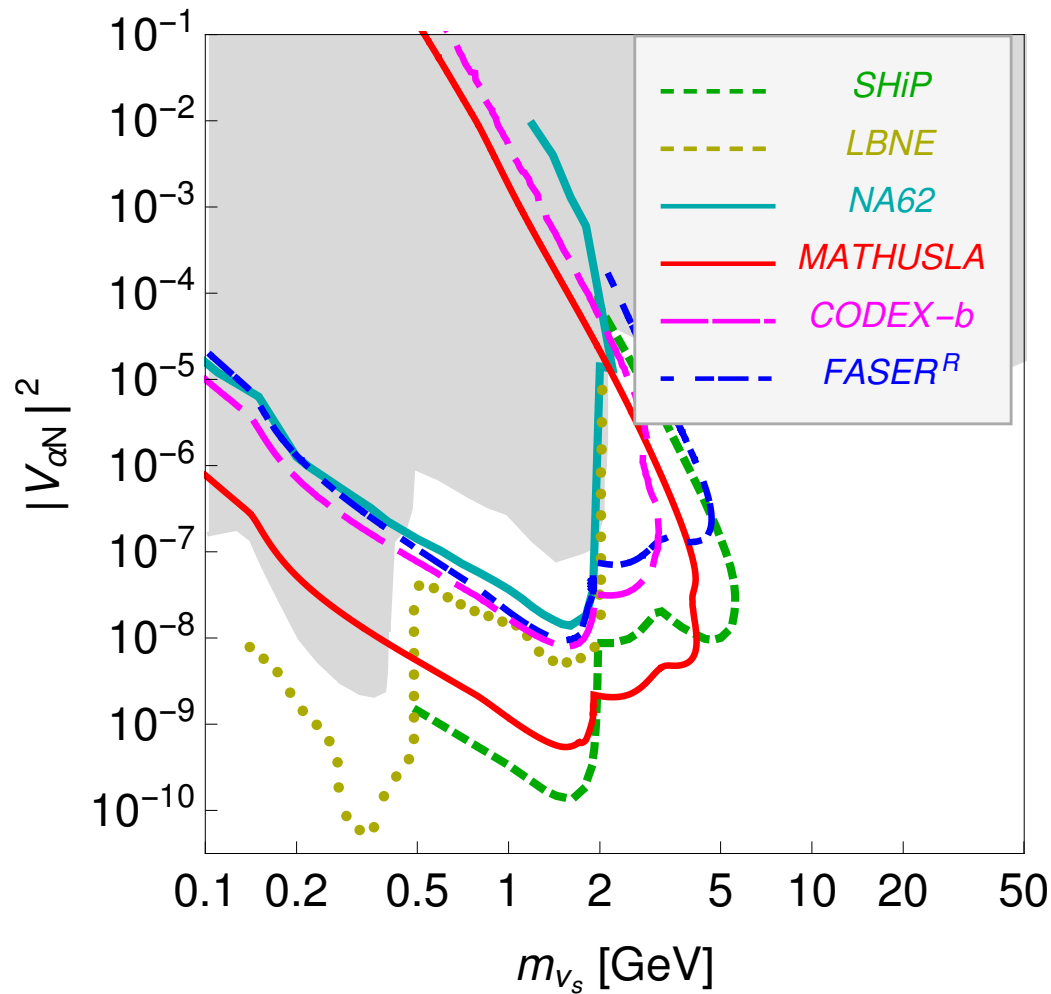
Existing limits as reviewed in:

[Atre et al,  
JHEP 0905 \(2009\) 030](#)

and

[D. Curtin et al.,  
1806.07396](#)

# Forecast searches



Plot from:  
Helo et al.; 1803.02212

SHiP; 1504.04855,  
1810.03636

LBNE; 1307.7335

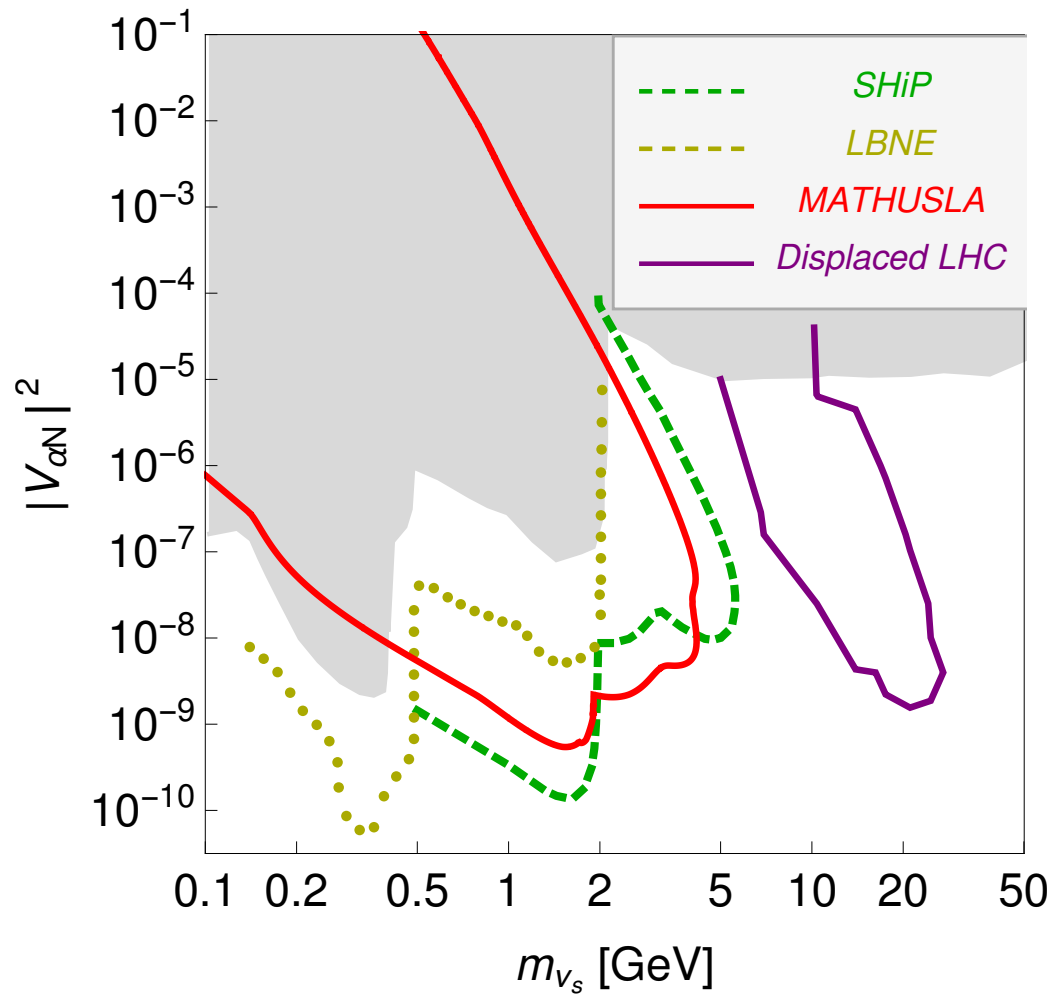
NA62; 1801.04207

MATHUSLA; 1806.07396

CODEXb; 1708.09395

FASER; 1708.09389

# Forecast searches

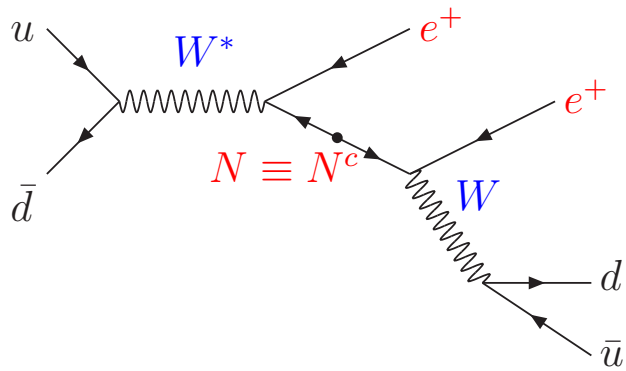


LHC displaced  
vertex search  
forecast for  
 $\mathcal{L} = 3/\text{ab}$ :

Cottin et al.;  
arXiv:1806.05191

# LN $\nu$ @ LHC

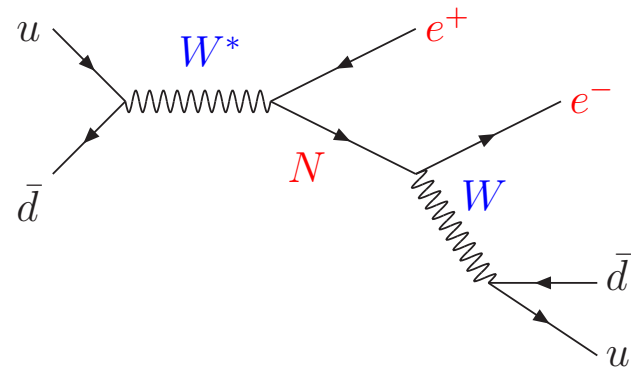
$$pp \rightarrow l^+l^+ + jj$$



Majorana neutrino

$$R_{ll} \equiv 1$$

$$pp \rightarrow l^+l^- + jj$$



Dirac neutrino

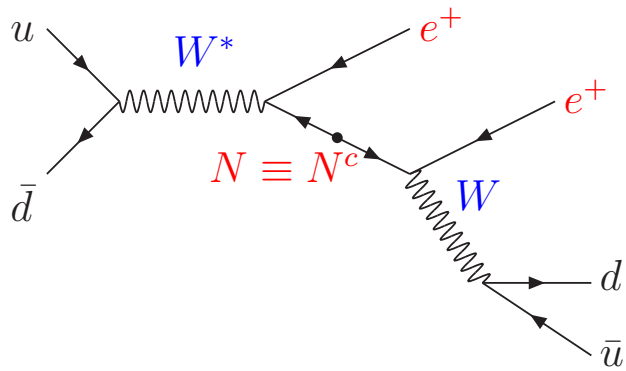
$$R_{ll} \equiv 0$$

where:

$$R_{ll} = \frac{\#(l^+l^+jj) + \#(l^-l^-jj)}{\#(l^+l^-jj)}$$

# LNv @ LHC

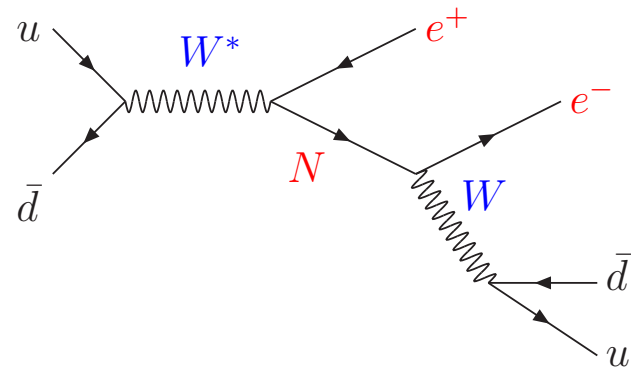
$$pp \rightarrow l^+l^+ + jj$$



Majorana neutrino

$$R_{ll} \equiv 1$$

$$pp \rightarrow l^+l^- + jj$$

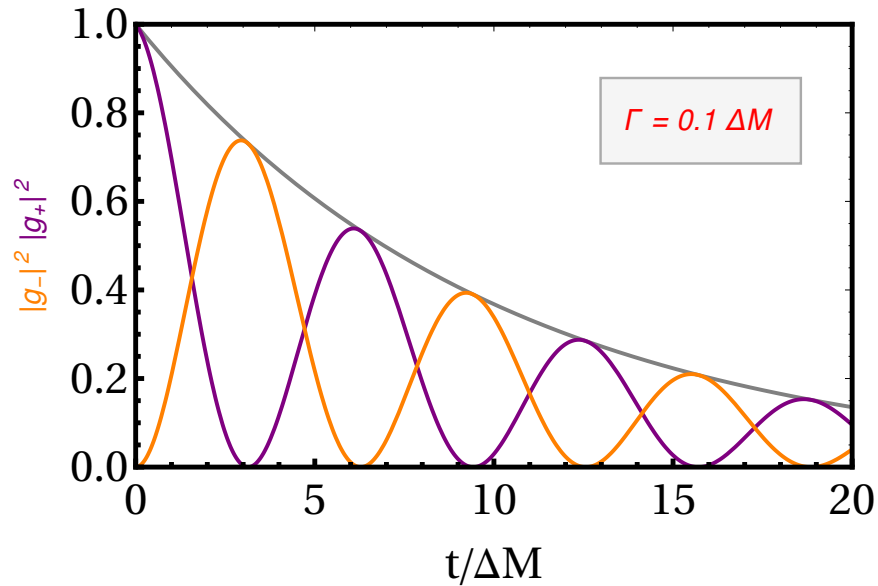


Dirac neutrino

$$R_{ll} \equiv 0$$

Can one have  $R_{ll} = 1/2, 1/4 \dots 1/13$ ?

# Quasi-Dirac $\nu$ oscillations



Quasi-Dirac neutrino as  
function of  $t$ :

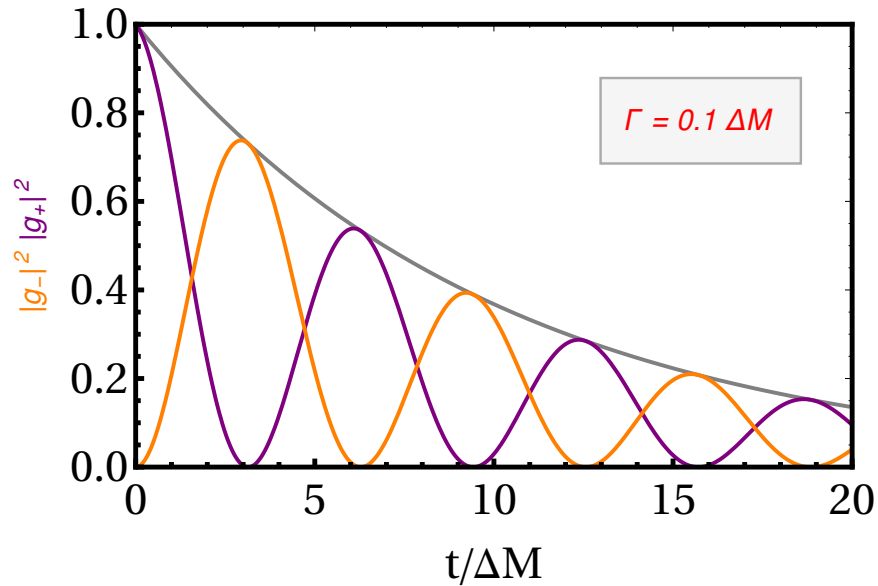
$$N_\ell(t) = g_+(t)N_\ell + g_-(t)N_{\bar{\ell}}$$

Physics interpretation:

if  $\Gamma \simeq \Delta M$

states can interfere!

# Quasi-Dirac $\nu$ oscillations



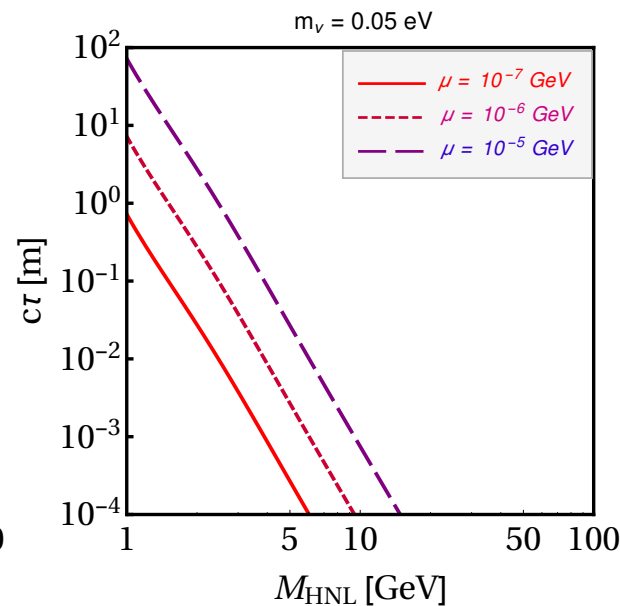
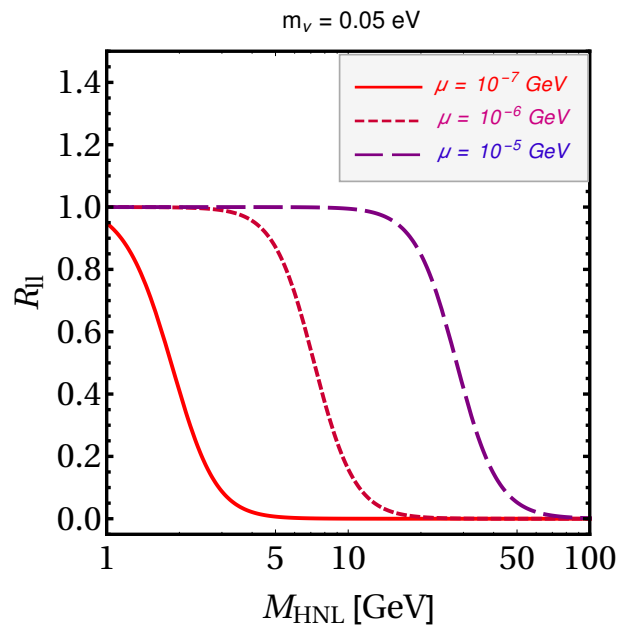
Quasi-Dirac neutrino as function of  $t$ :

$$N_\ell(t) = g_+(t)N_\ell + g_-(t)N_{\bar{\ell}}$$

Physics interpretation:

If  $\Gamma \simeq \Delta M$

states can interfere!

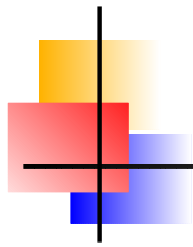


Anamiati et al.  
1607.05641

If decay length short,  
integrate over time:

$$R_{ll} = \frac{\Delta M^2}{2\Gamma^2 + \Delta M^2}$$





*III.*

Beyond minimal seesaw(s)

# Theoretical expectation?

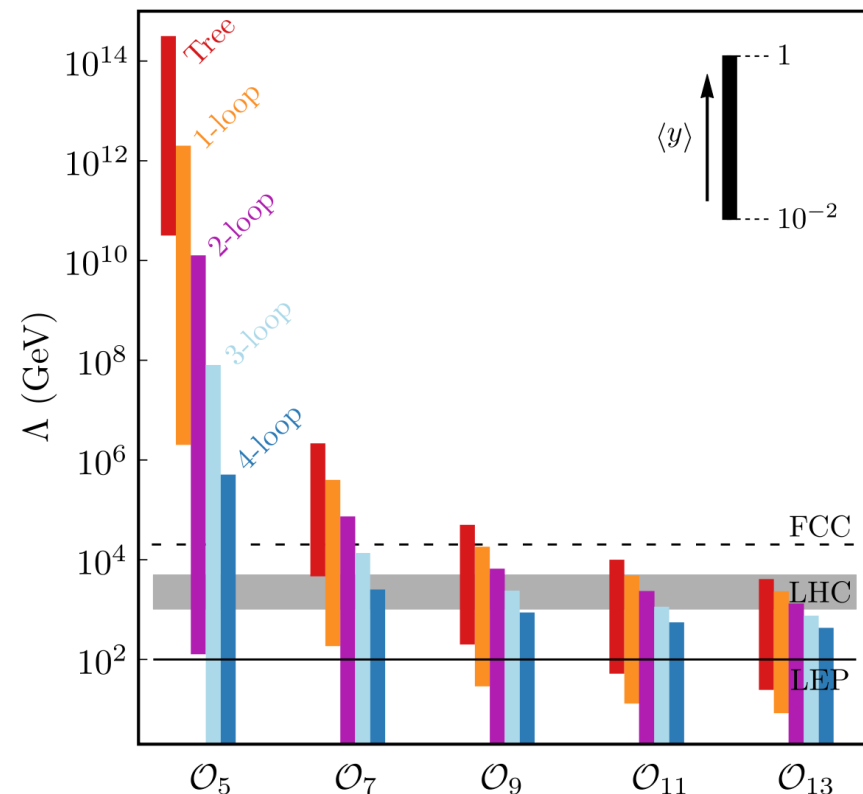
Majorana Neutrino mass generated from an  $n$ -loop dimension  $d$  diagram:

$$m_\nu \simeq \frac{(Yv)^2}{\Lambda} \cdot \epsilon \cdot \left(\frac{Y^2}{16\pi^2}\right)^n \cdot \left(\frac{Yv}{\Lambda}\right)^{d-5}$$

Smallness of neutrino mass can be “explained” by:

- ⇒ High scale: **Large  $\Lambda$**   
“classical” seesaw
- ⇒ Loop factor:  $n \geq 1$   
+ “smallish”  $Y \sim \mathcal{O}(10^{-3} - 10^{-1})$
- ⇒ Higher order:  $d = 7, 9, 11$
- ⇒ Nearly conserved  $L$ ,  
i.e. **small  $\epsilon$**  (“inverse seesaw”)

... or combination thereof





# $\Delta L = 2$ operators

---

$d = 5$ :

Weinberg, 1979

$$\mathcal{O}_W \propto \frac{c_{ij}}{\Lambda} (L_i H)(L_j H)$$



# $\Delta L = 2$ operators

---

$d = 5:$

Weinberg, 1979

$$\mathcal{O}_W \propto \frac{c_{ij}}{\Lambda} (L_i H)(L_j H)$$

One  $d=5$

$d = 7:$

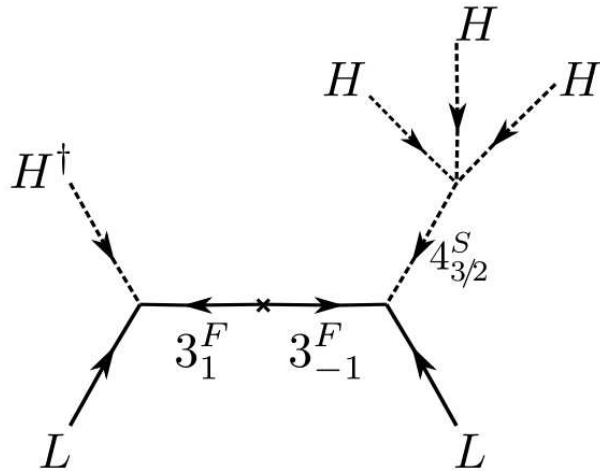
Babu & Leung, 2001

de Gouvea & Jenkins, 2007

$$\begin{aligned}\mathcal{O}_2 &\propto LLLe^c H \\ \mathcal{O}_3 &\propto LLQd^c H \\ \mathcal{O}_4 &\propto LL\bar{Q}\bar{u}^c H \\ \mathcal{O}_8 &\propto L\bar{e}^c\bar{u}^c d^c H\end{aligned}$$

$$\mathcal{O} \propto (LH)(LH)(H^\dagger H) \quad 4 (+1) d = 7$$

# High-d neutrino masses

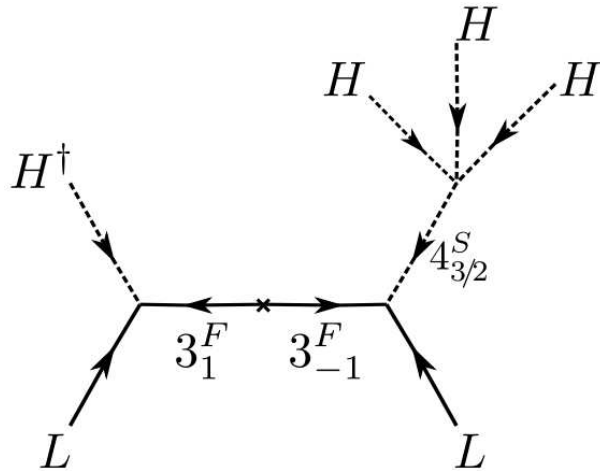


$d=7$ :

Babu, Nandi

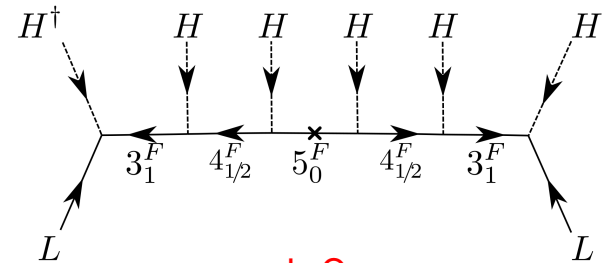
& Tavartkiladze, 2009 (BNT)

# High-d neutrino masses

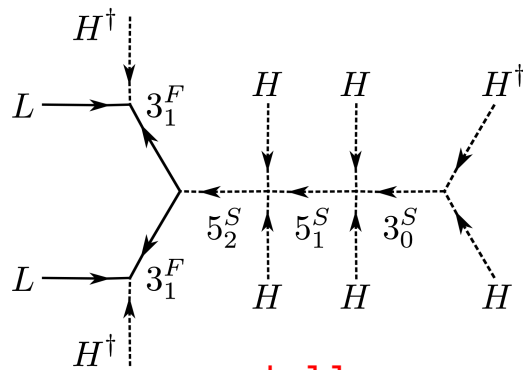


d=7:  
Babu, Nandi  
& Tavartkiladze, 2009 (BNT)

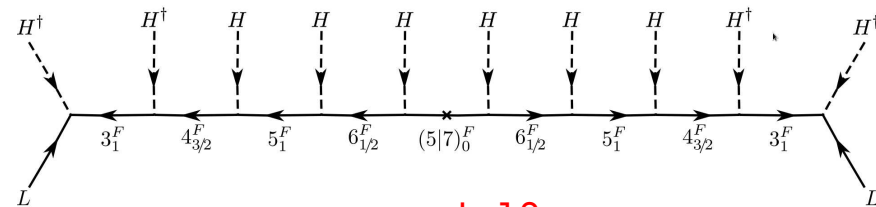
Anamiati et al. 2018



d=9



d=11



d=13

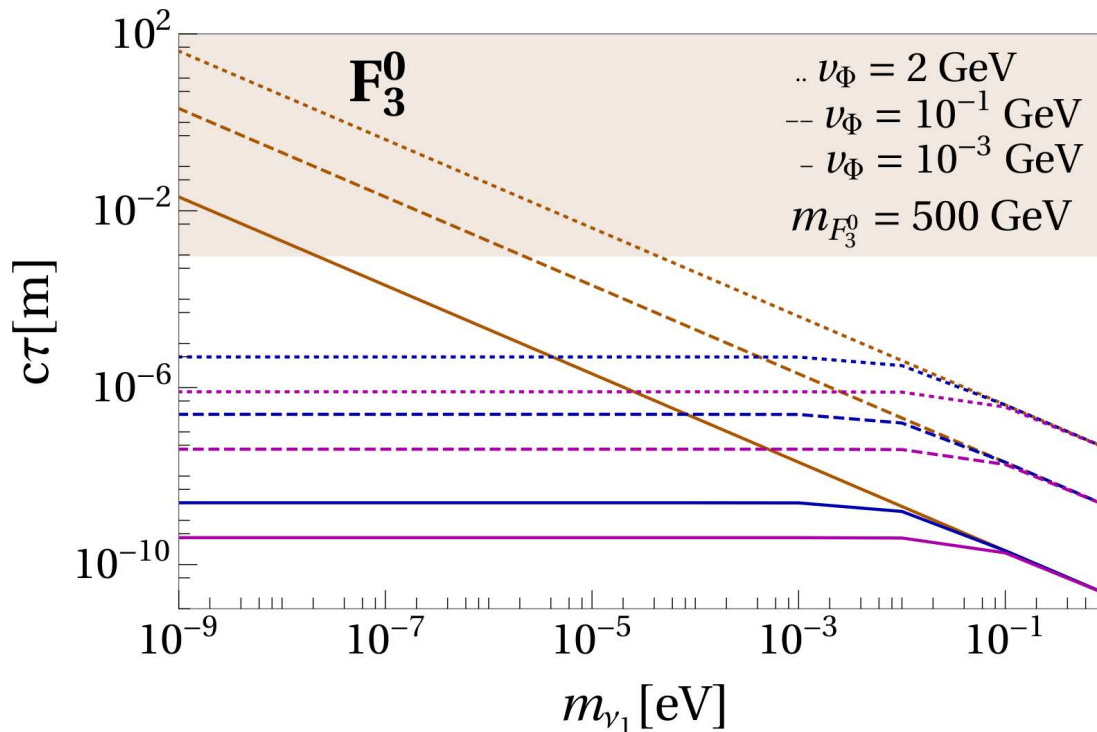
# BNT model

Neutrino mass matrix is as in “linear seesaw”:

$$m_\nu = (Y_3^T M_3^{-1} Y_3 + Y_3^T M_3^{-1} Y_3) v v_\Phi$$

Vev  $v_\Phi$  of quadruplet **seesaw suppressed**:

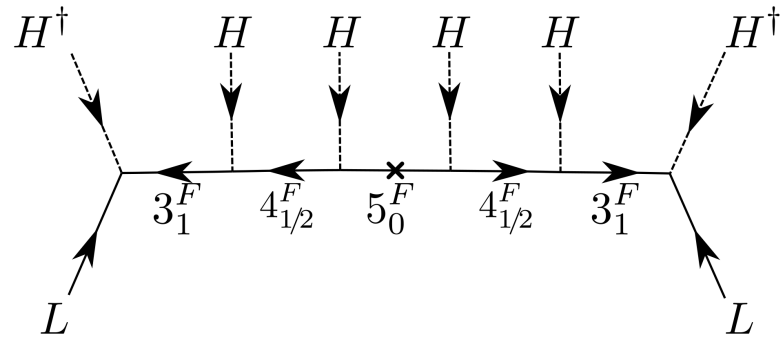
$$v_\Phi \sim \lambda_5 \frac{v^3}{m_{4S}^2}$$



Arbelaéz et al., 2019

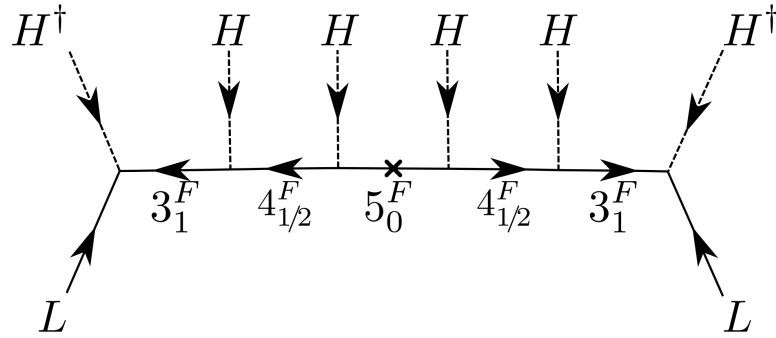
Decay length  
for different  $v_\Phi$   
as function of  $m_{\nu_1}$

# Decay length in $d=9$ model



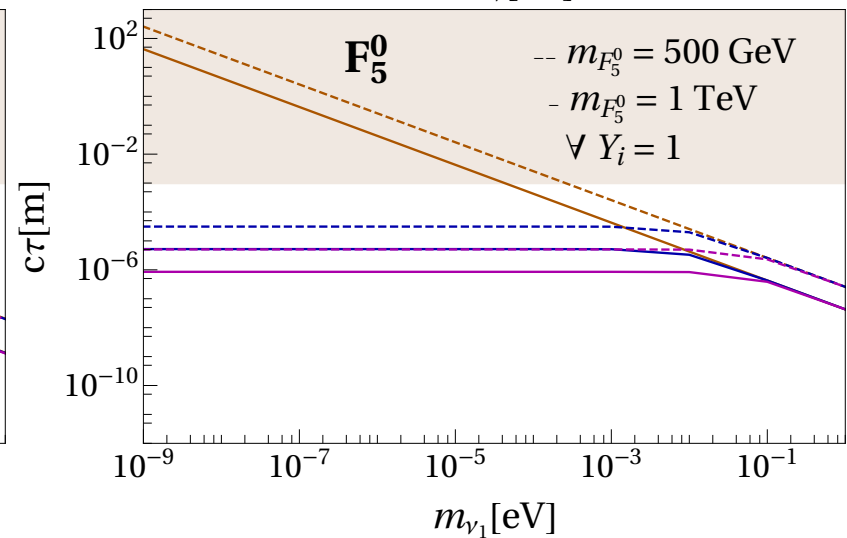
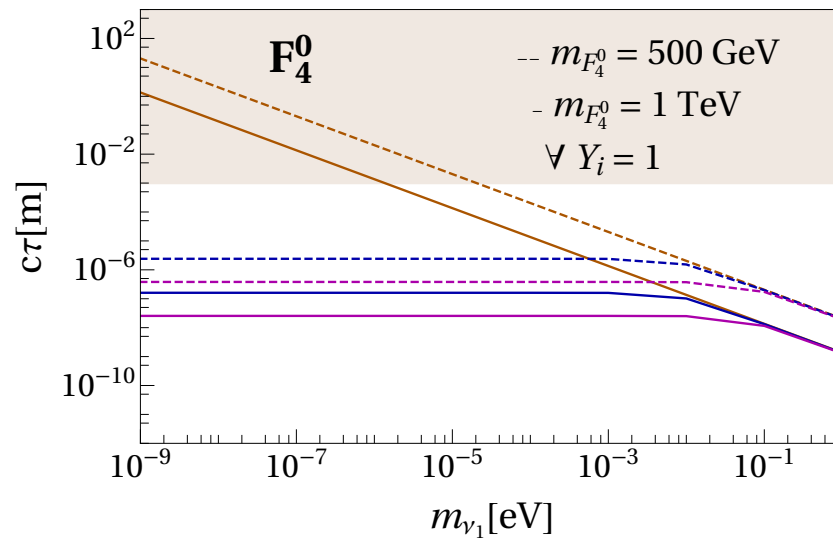
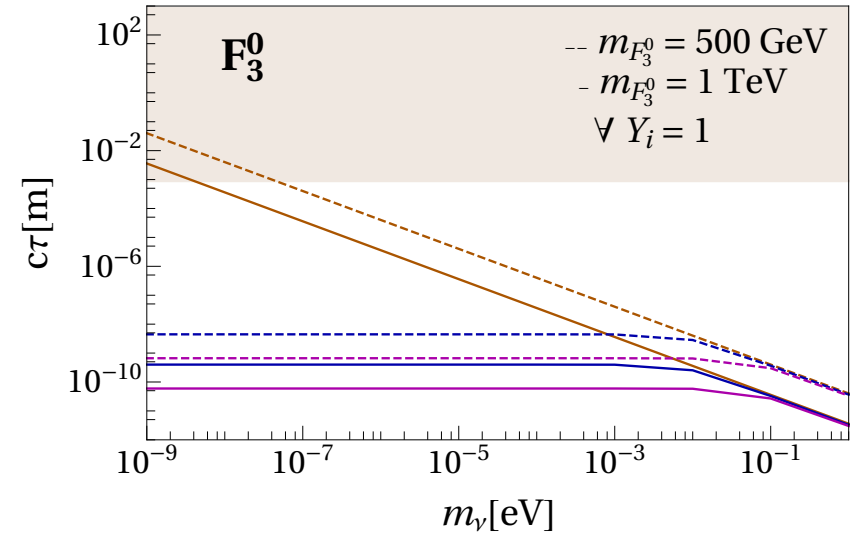


# Decay length in $d=9$ model



Arbelaéz et al., 2019

Decay length depends on which fermion is lightest





# $\Delta L = 2$ operators

---

$d = 5:$

Weinberg, 1979

$$\mathcal{O}_W \propto \frac{c_{ij}}{\Lambda} (L_i H)(L_j H)$$

One  $d=5$

$d = 7:$

Babu & Leung, 2001

de Gouvea & Jenkins, 2007

$$\mathcal{O}_2 \propto LLLe^c H$$

$$\mathcal{O}_3 \propto LLQd^c H$$

$$\mathcal{O}_4 \propto LL\bar{Q}\bar{u}^c H$$

$$\mathcal{O}_8 \propto L\bar{e}^c \bar{u}^c d^c H$$

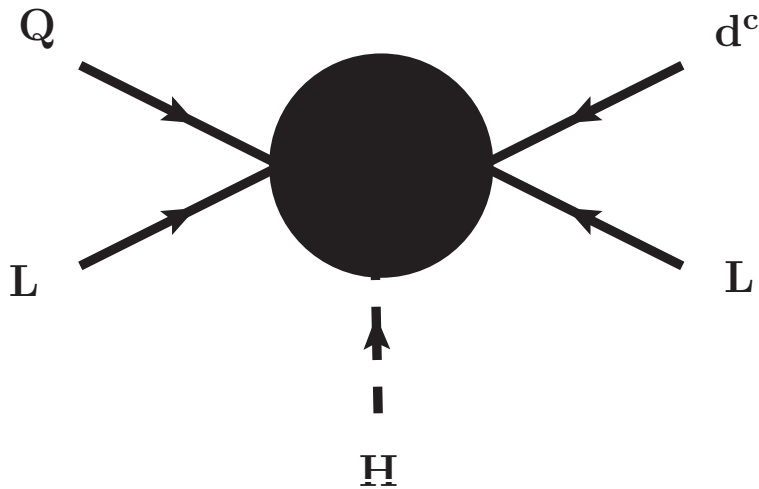
$$\mathcal{O} \propto (LH)(LH)(H^\dagger H)$$

4 (+1)  $d = 7$



# Example $d = 7$ : $LLQd^cH$

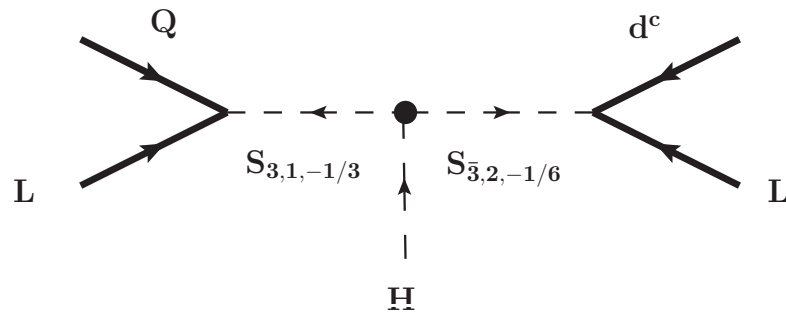
Graphically:



# Example $d = 7$ : $LLQd^cH$

More than one realization.

Example:



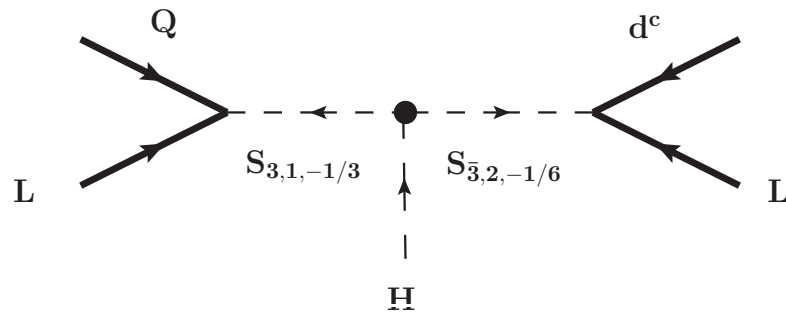
$S_{3,1,-1/3}$  - singlet leptoquark

$S_{3,2,1/6}$  - doublet leptoquark

$\Delta L = 2$ , so ...

# Example $d = 7$ : $LLQd^cH$

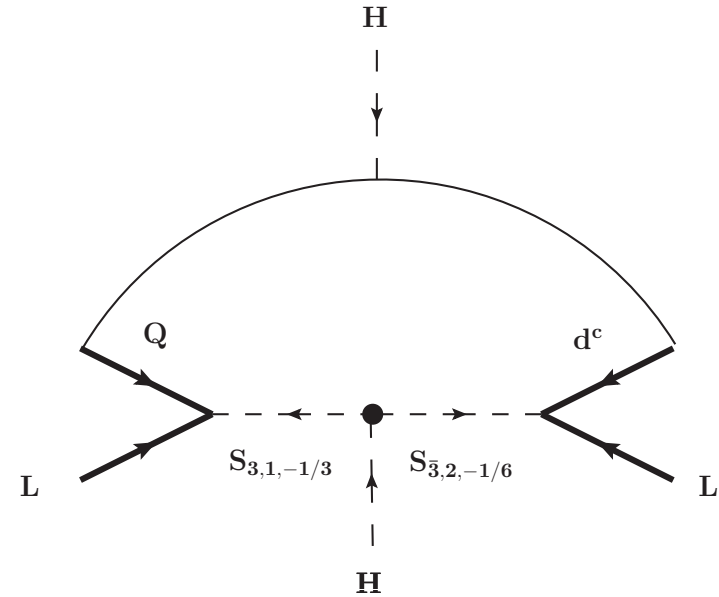
More than one realization.  
Example:



$S_{3,1,-1/3}$  - singlet leptoquark  
 $S_{\bar{3},2,-1/6}$  - doublet leptoquark

$\Delta L = 2$ , so ...

1-loop neutrino mass:





# $\Delta L = 2$ operators

$d = 5:$

Weinberg, 1979

$$\mathcal{O}_W \propto \frac{c_{ij}}{\Lambda} (L_i H)(L_j H)$$

One  $d=5$

$d = 7:$

Babu & Leung, 2001

de Gouvea & Jenkins, 2007

$$\mathcal{O}_2 \propto LLLe^c H$$

$$\mathcal{O}_3 \propto LLQd^c H$$

$$\mathcal{O}_4 \propto LL\bar{Q}\bar{u}^c H$$

$$\mathcal{O}_8 \propto L\bar{e}^c \bar{u}^c d^c H$$

$$\mathcal{O} \propto (LH)(LH)(H^\dagger H)$$

4 (+1)  $d = 7$

$d = 9:$

many  $d = 9$  and  $d = 11$  ops

$$\mathcal{O}_5 \propto LLQd^c HHH^\dagger$$

$$\mathcal{O}_6 \propto LL\bar{Q}\bar{u}^c HHH^\dagger H$$

$$\mathcal{O}_7 \propto LQ\bar{e}^c \bar{Q}HHH^\dagger$$

.....

$$\mathcal{O}_9 \propto LLLe^c Le^c$$

$$\mathcal{O}_{10} \propto LLLe^c Qd^c$$

$$\mathcal{O}_{11} \propto LLQd^c Qd^c$$

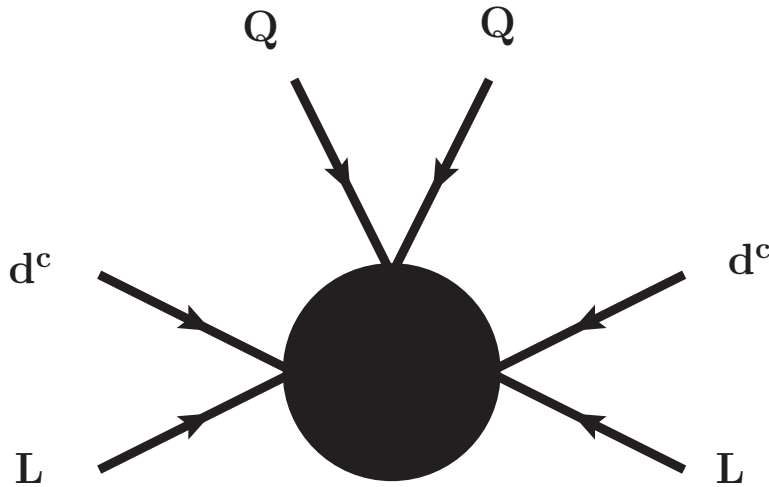
.....



# Example $d = 9$ : $LLQd^cQd^c$

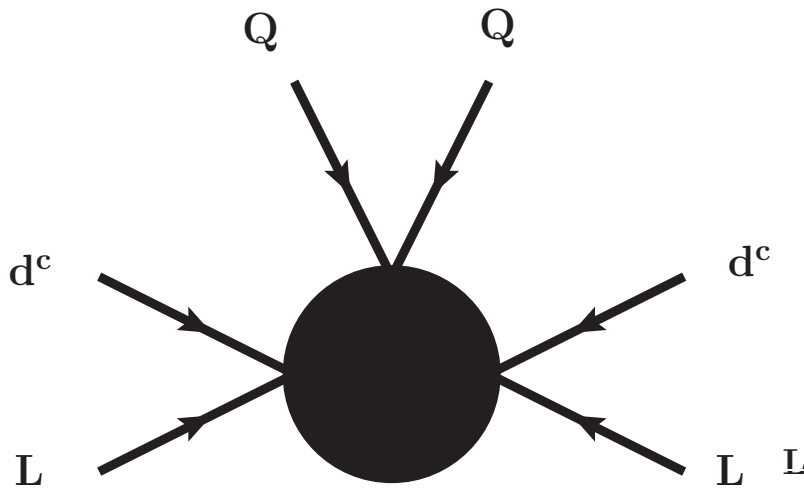
True  $d = 9$  operator:

Many, many realizations ...



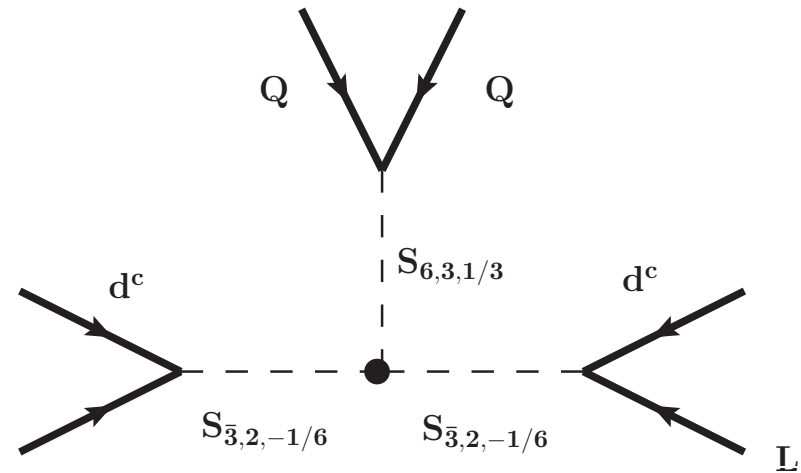
# Example $d = 9$ : $LLQd^cQd^c$

True  $d = 9$  operator:



Many, many realizations ...

One example:

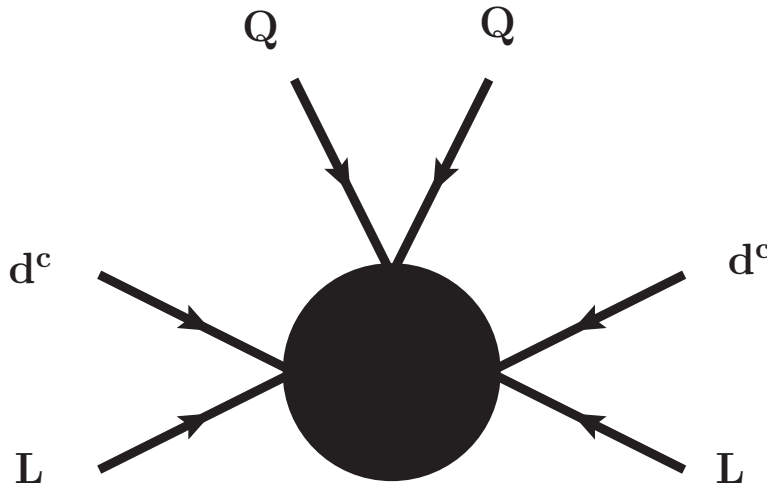


$S_{6,3,1/3}$  - triplet diquark  
 $S_{3,2,-1/6}$  - doublet leptoquark



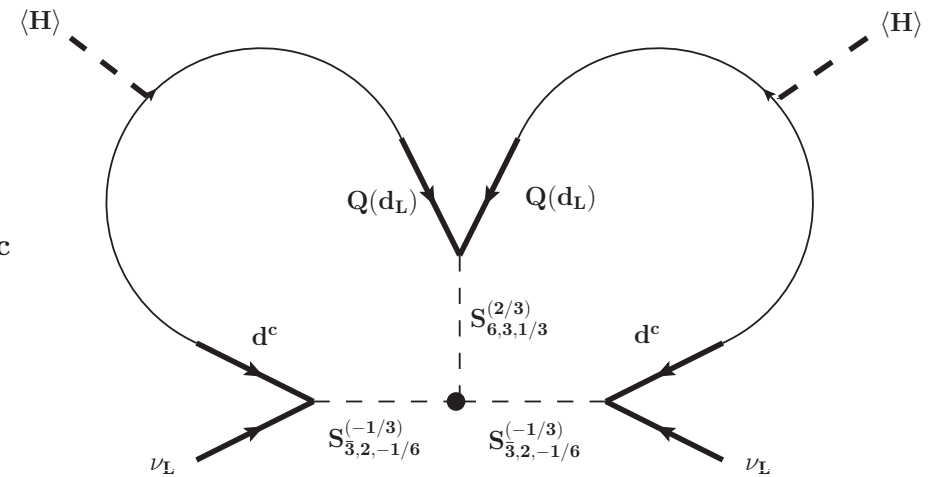
# Example $d = 9$ : $LLQd^cQd^c$

True  $d = 9$  operator:



Many, many realizations ...

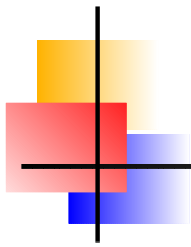
One example:



$S_{6,3,1/3}$  - triplet diquark

$S_{3,2,1/6}$  - doublet leptoquark

2-loop neutrino mass!



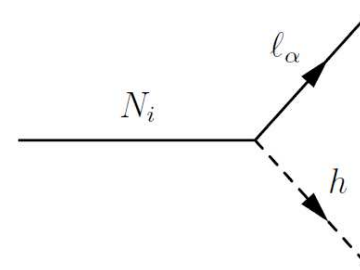
*IV.*

# Leptogenesis and LHC

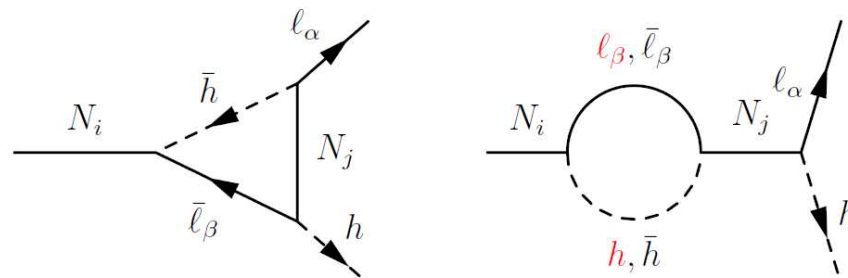
# Leptogenesis

Sakharov's conditions:

- (i) Baryon number violation
- (ii) C and CP violation
- (iii) **departure from thermal equilibrium**



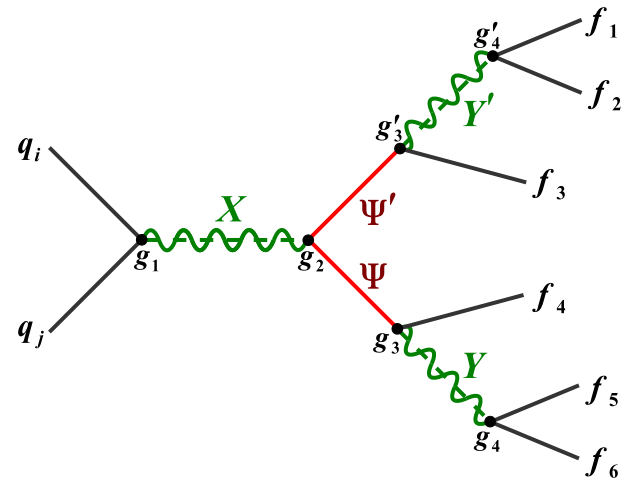
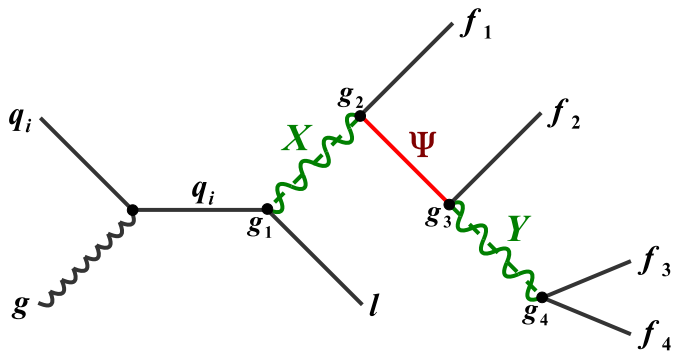
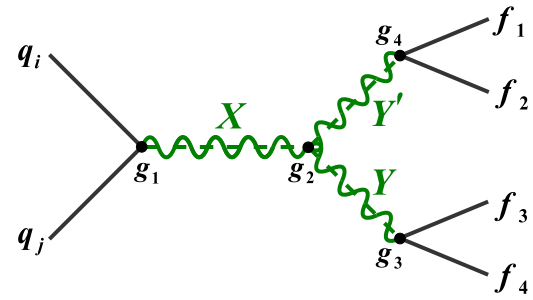
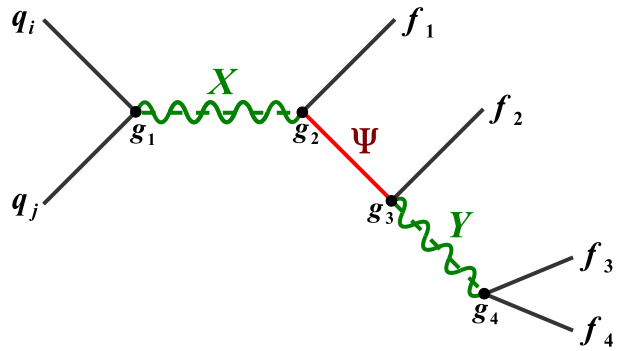
(e) Tree



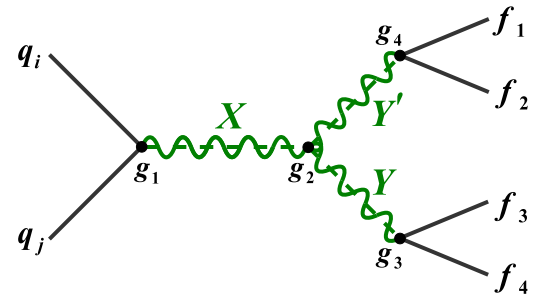
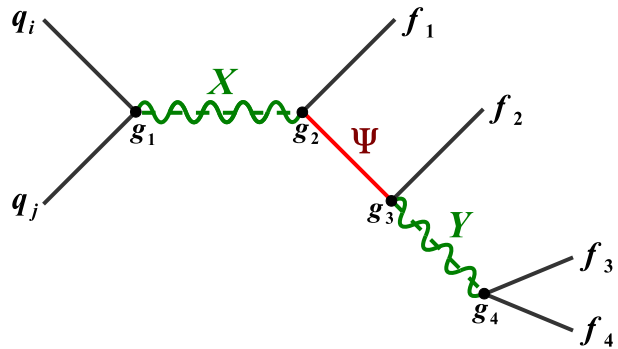
In **Leptogenesis**:

- (i) Convert L to B through SM sphalerons
- (ii) CP violation through interference tree  $\leftrightarrow$  1-loop
- (iii) **L out of equilibrium** via right-handed neutrino decay

# LNV @ LHC

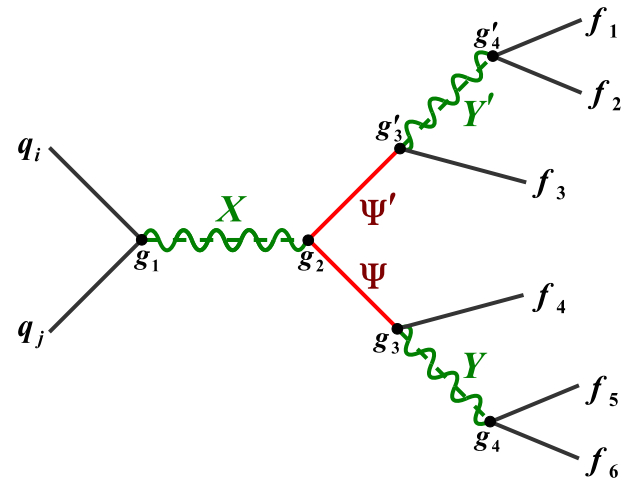
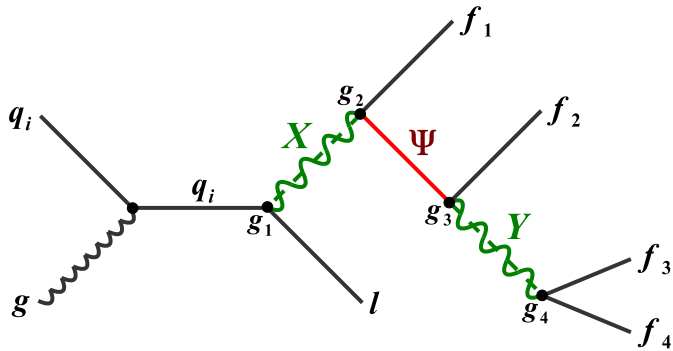


# LN $\nu$ @ LHC

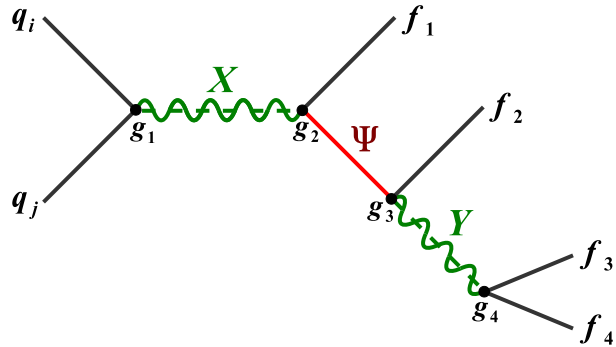


Example:

$$u\bar{d} \rightarrow W_R^+ \rightarrow l^+ N \rightarrow l^+ l^+ jj$$

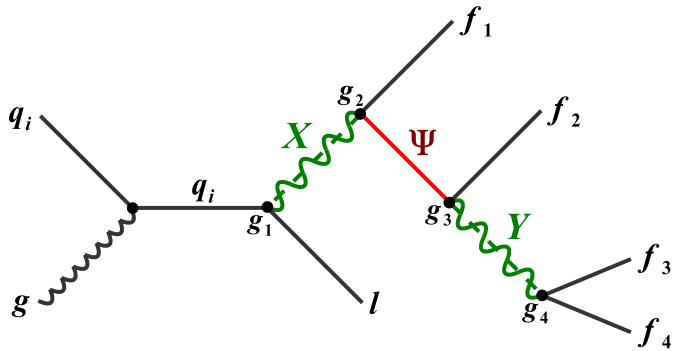


# LNV @ LHC

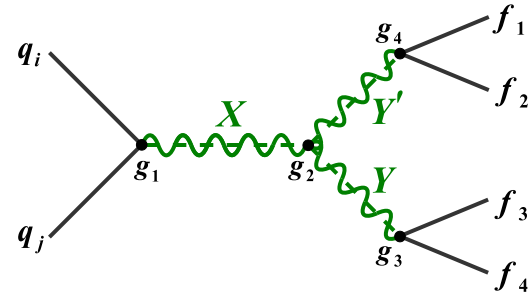


Example:

$$u\bar{d} \rightarrow W_R^+ \rightarrow l^+ N \rightarrow l^+ l^+ jj$$

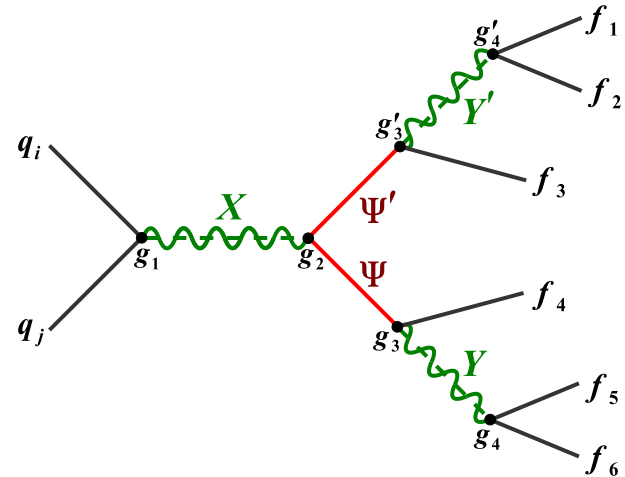


$$ug \rightarrow S_{3,1,1/3} + l^+ \rightarrow l^+ l^+ jjj$$



Example:

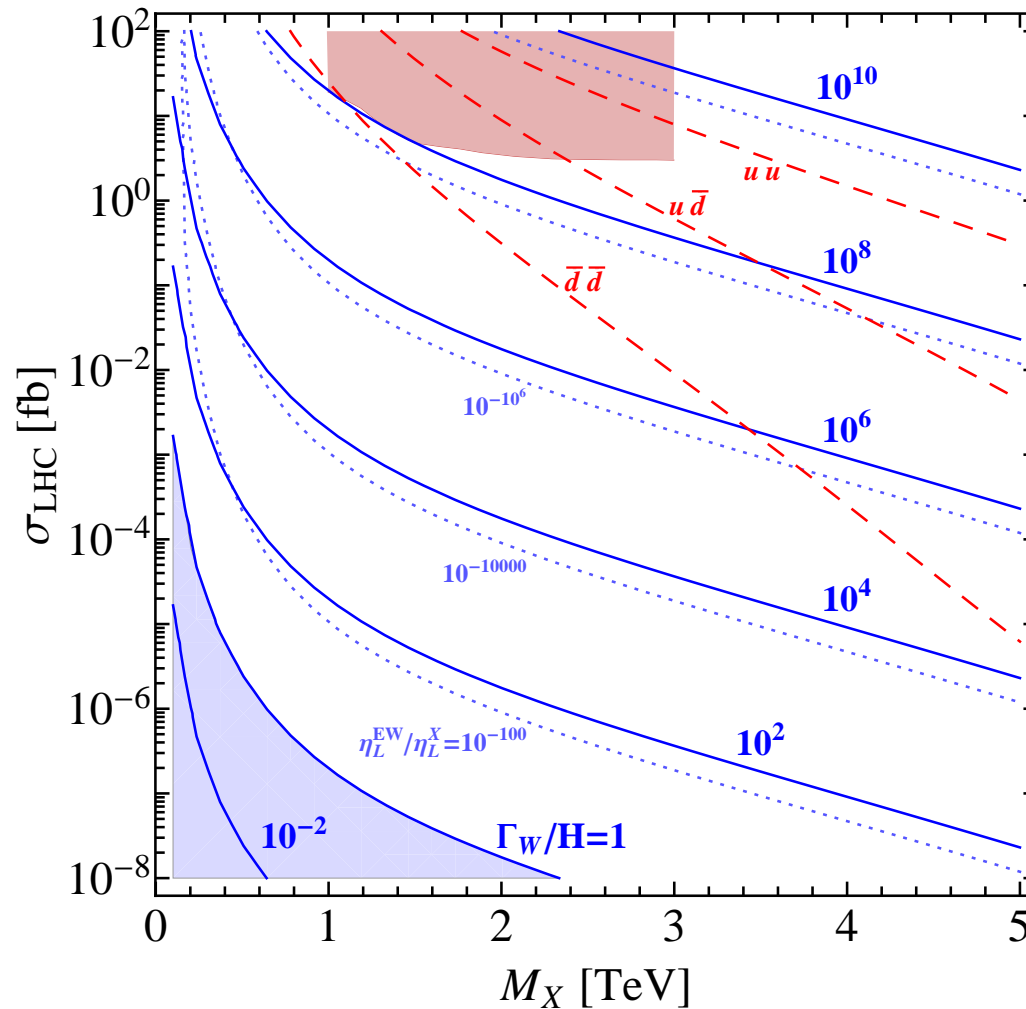
$$uu \rightarrow S_{6,3,1/3} \rightarrow 2S_{3,2,1/6} \rightarrow l^+ l^+ jj$$



$$q\bar{q} \rightarrow g \rightarrow \psi_{6,2,1/6} + \bar{\psi}_{6,2,1/6} \rightarrow l^+ l^+ jjjj$$

# Leptogenesis and LHC

Deppisch, Hartz  
& Hirsch (2014)



blue lines

washout factor  $\Gamma_W$

Suppression of  $L \propto 10^{-\Gamma_W}$

Observation of

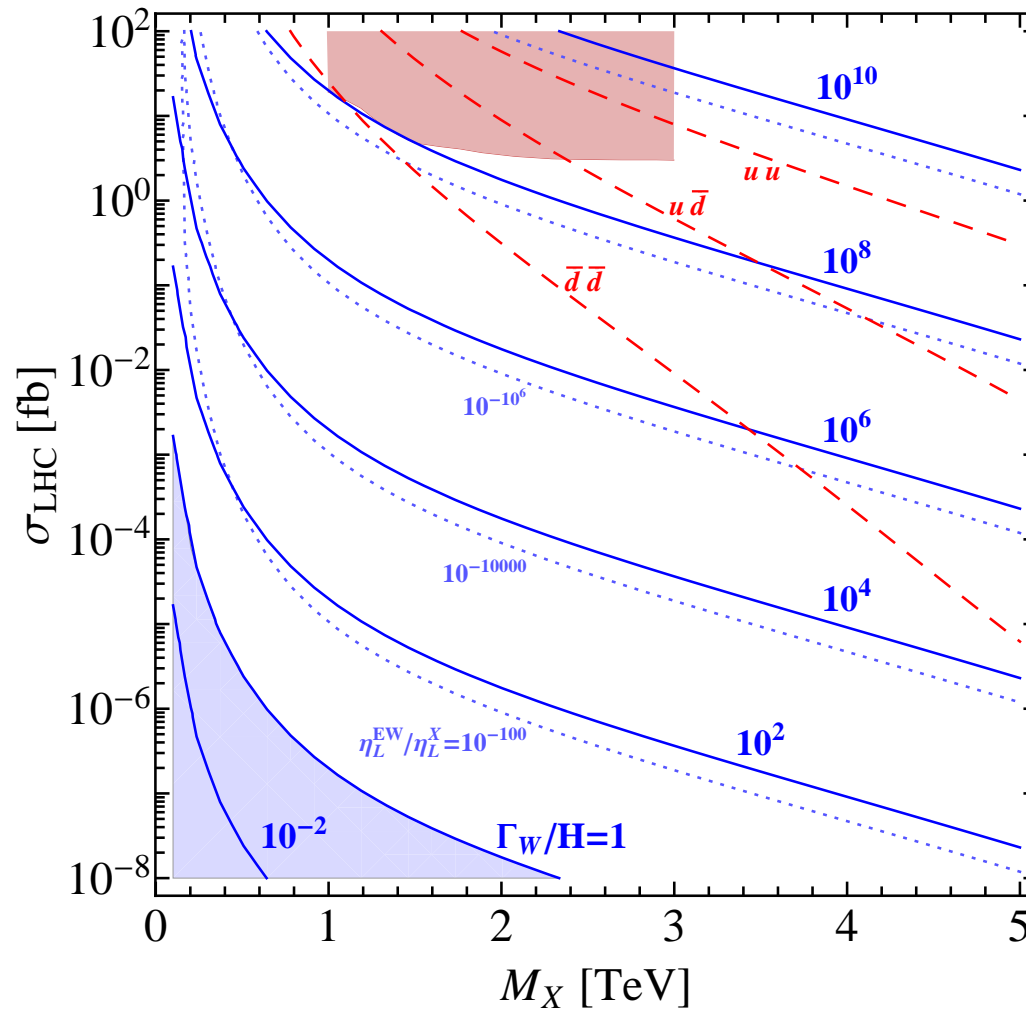
LNV @ LHC implies:

(High-scale) Leptogenesis  
is ruled out!

$$\sigma_{\text{LHC}} = \sigma_{pp \rightarrow l^\pm l^\pm + jj}$$

# Leptogenesis and LHC

Deppisch, Hartz  
& Hirsch (2014)



$$\sigma_{\text{LHC}} = \sigma_{pp \rightarrow l^\pm l^\pm + jj}$$

blue lines  
washout factor  $\Gamma_W$   
Suppression of  $L \propto 10^{-\Gamma_W}$

Observation of  
LNV @ LHC implies:  
(High-scale) Leptogenesis  
is ruled out!

Loopholes???

- (i) Resonant LG  
with  $m_N \ll m_X$ ?
- (ii) Hide LG in  $\tau$ 's?
- (iii) Frandsen et al.,  
1801.09314:

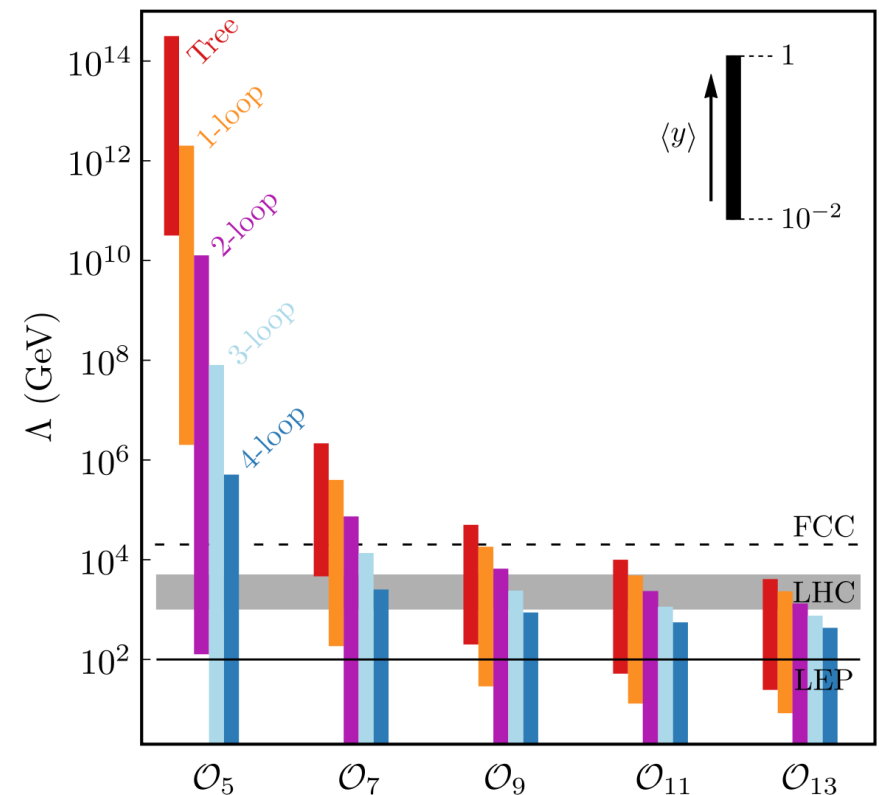
Additional global  $U(1)_X$   
"Asymmetric DM"

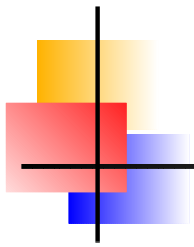


# Conclusions

## LVN & LHC:

- ⇒ Majorana neutrino mass and LVN always related
- ⇒ What is the **scale of LVN**?
- ⇒ Smallness of  $m_\nu$  implies small decay width of HNL
- ⇒ **Quasi-Dirac neutrinos** can have **LVN oscillations**
- ⇒ Observation of **LVN at LHC** implies high-scale leptogenesis ruled out



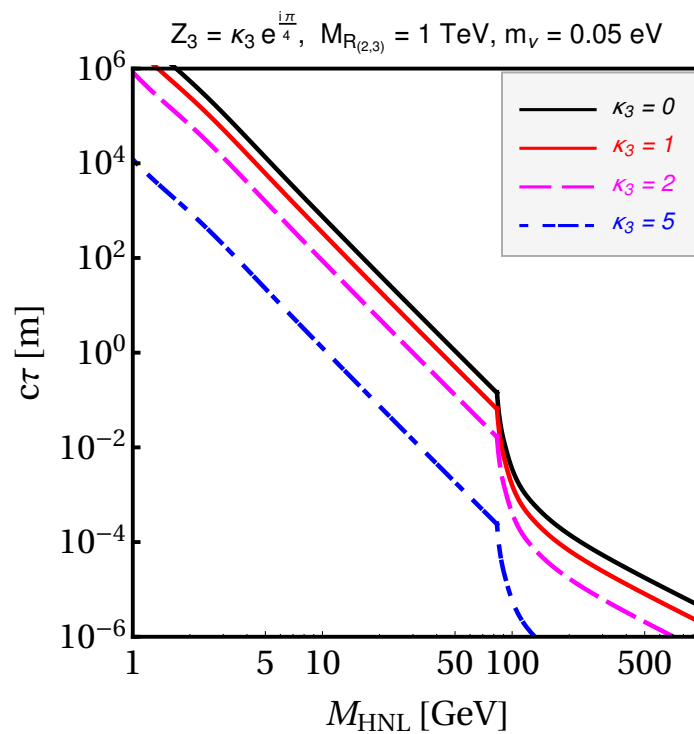


# Backup

# Decay length and $R$ -matrix

Casa & Ibarra, 2001:

$$m_D = i\sqrt{\hat{M}_R} \mathcal{R} \sqrt{m_{\nu_i}} U_\nu^\dagger$$



Parametrize  $\mathcal{R}$  as product of 3 complex rotations  $\sin(Z_i)$

Example:  $Z_3 = \kappa_3 e^{i\beta_3}$

Note:

For  $\kappa_i \gtrsim 1$

Loop contributions to  $m_\nu$   
larger than tree-level seesaw



# Quasi-Dirac $\nu$ oscillations

Write the state from  $W_{L/R}^+ \rightarrow \bar{\ell}N_\ell$  and its conjugate state from  $W_{L/R}^- \rightarrow \ell N_{\bar{\ell}}$  in terms of the mass eigenstates as:

$$N_\ell = \frac{1}{\sqrt{2}}(N_+ - iN_-),$$
$$N_{\bar{\ell}} = \frac{1}{\sqrt{2}}(N_+ + iN_-).$$

Let them evolve. After time  $t$ :

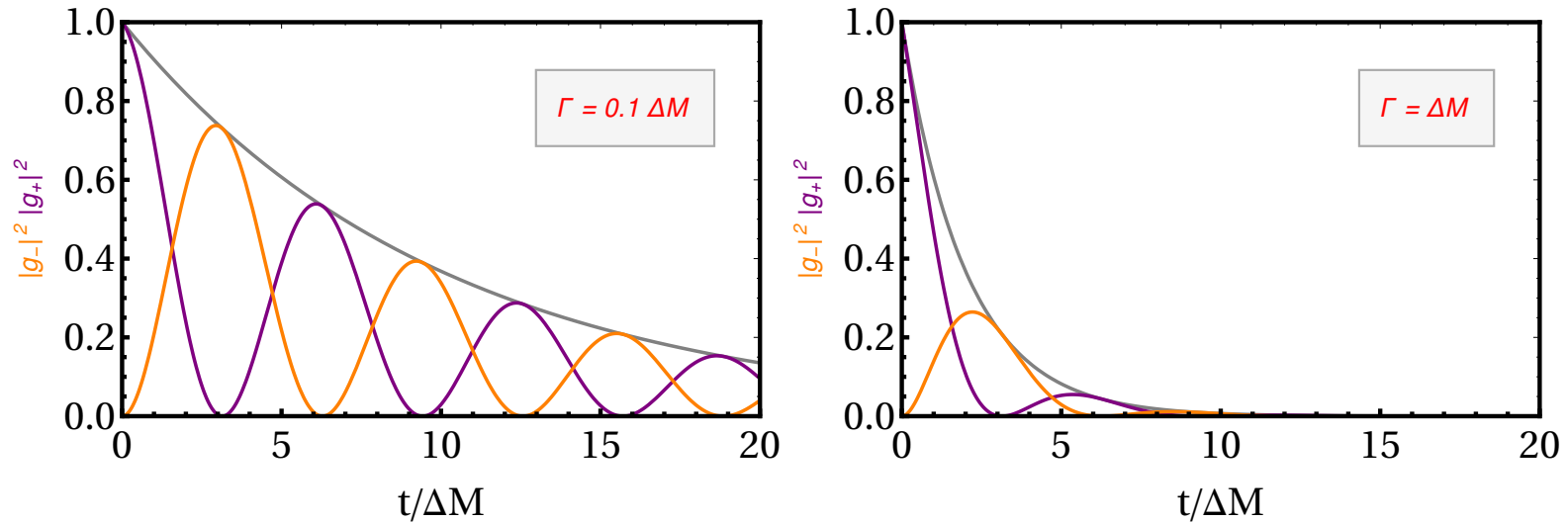
$$N_\ell(t) = g_+(t)N_\ell + g_-(t)N_{\bar{\ell}},$$
$$N_{\bar{\ell}}(t) = g_-(t)N_\ell + g_+(t)N_{\bar{\ell}},$$

where the oscillating amplitudes read :

$$g_+(t) = e^{-iMt} e^{-\frac{\Gamma}{2}t} \cos\left(\frac{\Delta M}{2}t\right),$$
$$g_-(t) = i e^{-iMt} e^{-\frac{\Gamma}{2}t} \sin\left(\frac{\Delta M}{2}t\right).$$

# Quasi-Dirac $\nu$ oscillations

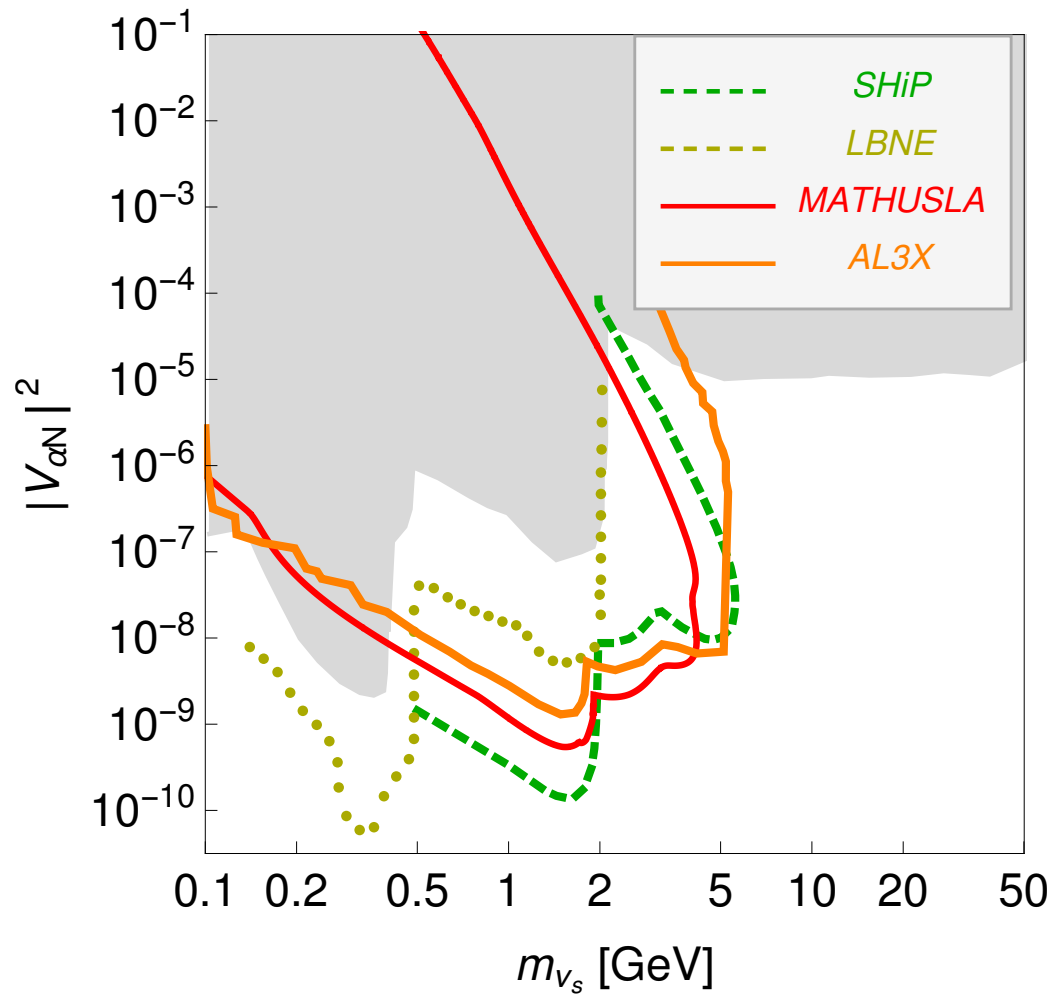
Oscillation and decay amplitudes as function of time:



If  $\Gamma \gtrsim 10^{-13}$  GeV (or so), decay length short. Integrate over time:

$$R_{ll} = \frac{\int_0^\infty |g_-|^2 dt}{\int_0^\infty |g_+|^2 dt} = \frac{\Delta M^2}{2\Gamma^2 + \Delta M^2}.$$

# Forecast searches



Plot from:  
Dercks et al.; 1811.01995

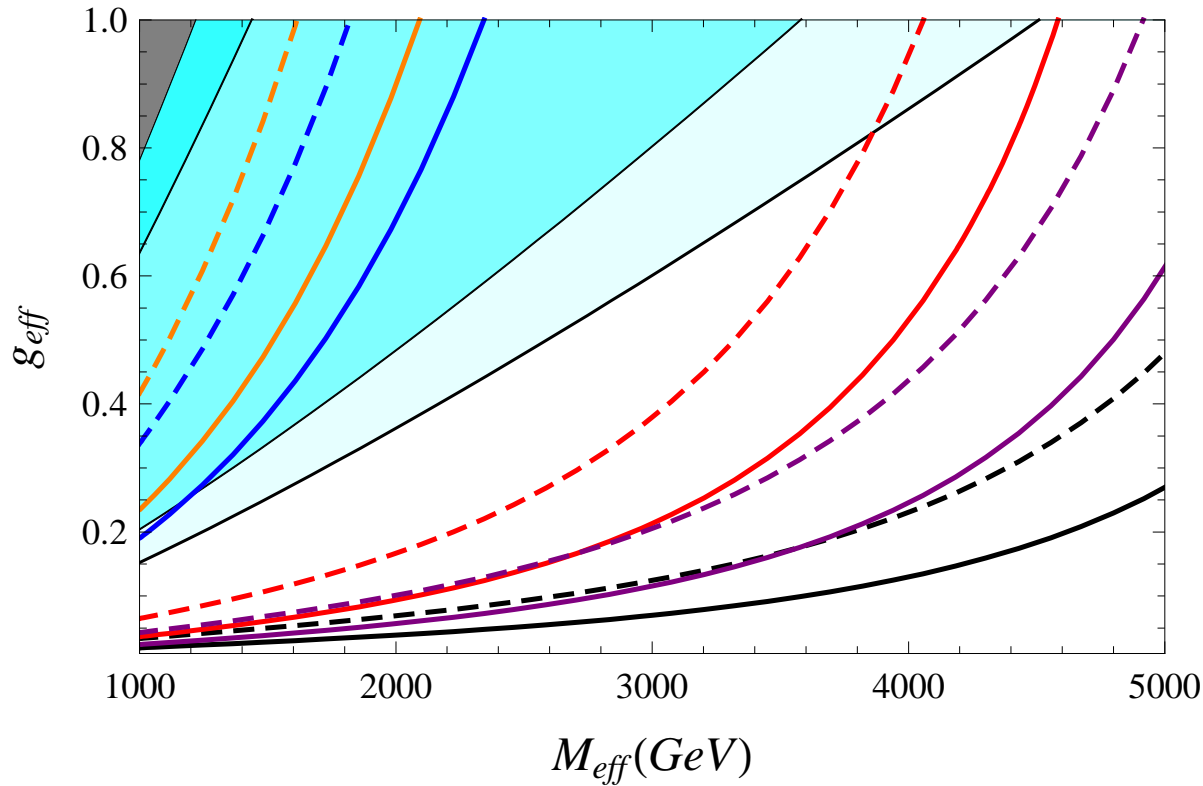
SHiP; 1504.04855,  
1810.03636

LBNE; 1307.7335

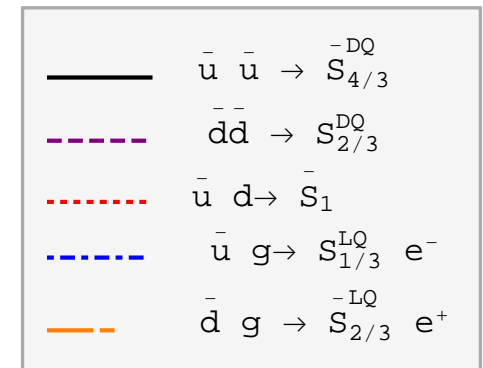
MATHUSLA; 1806.07396

AL3X; 1810.03636

# LNV models and LHC



J.C. Helo et al,  
PRD88 (2013)  
JHEP12 (2016) 130

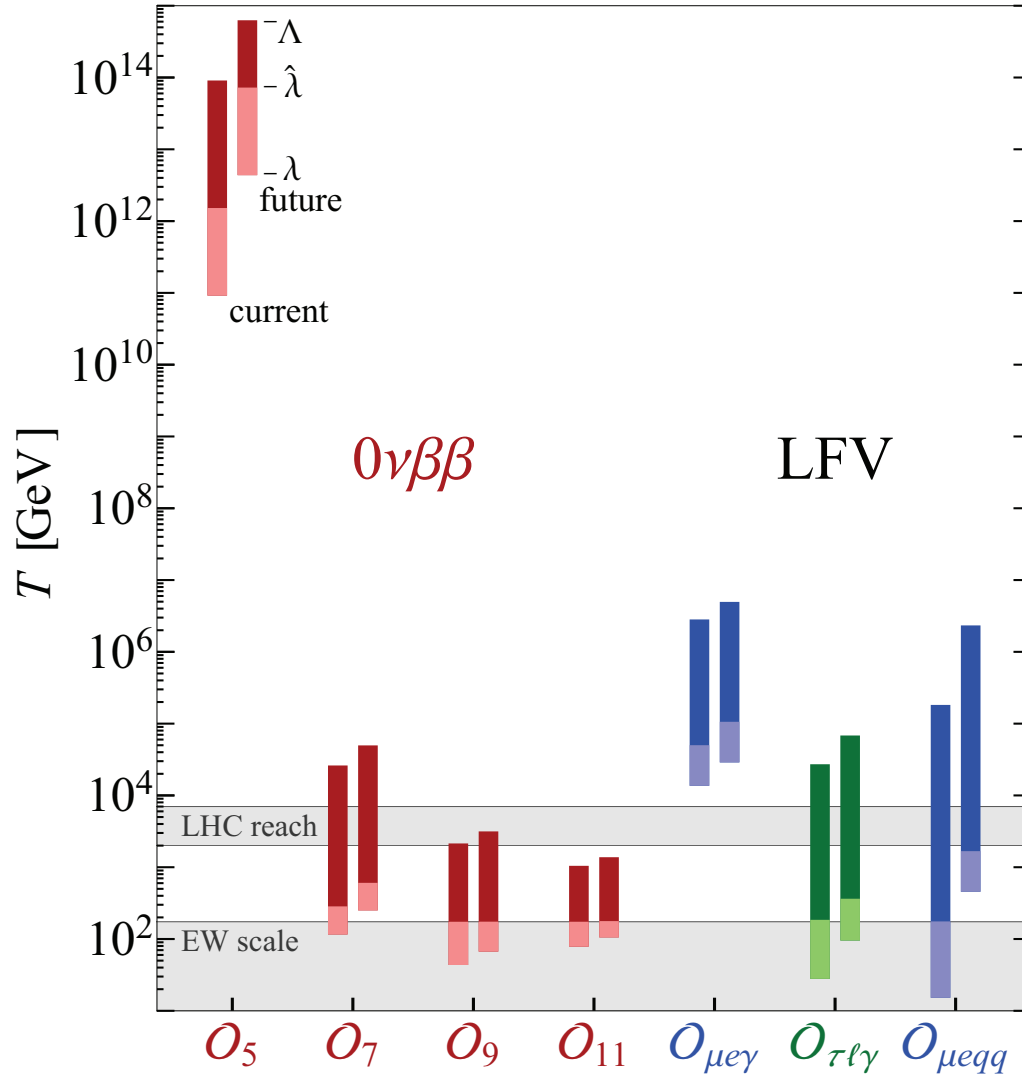


$g_{\text{eff}}$  - mean coupling

$M_{\text{eff}}$  - mean mass

Dashed (full) lines  $Br(S \rightarrow eejj) = 0.01$  (0.1)

# LG and $0\nu\beta\beta$ decay



Deppisch et al.,  
2015

If  $0\nu\beta\beta$  is found  
and demonstrated to be  
not due to  $\langle m_\nu \rangle$   
LG ruled out above  
scale  $\lambda$