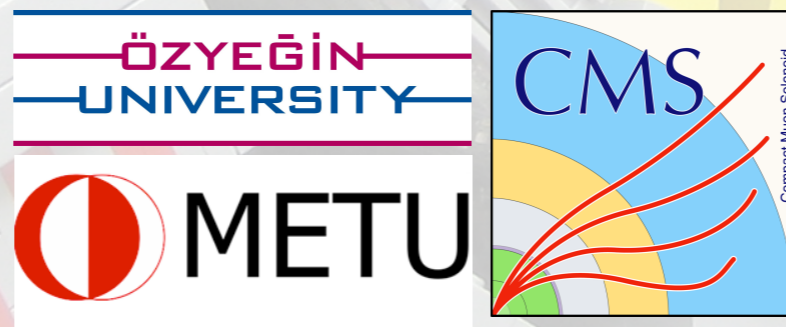


Spin correlations: Status of spin correlations in $pp \rightarrow t\bar{t}$

Bora Isildak
on behalf of the CMS Collaboration

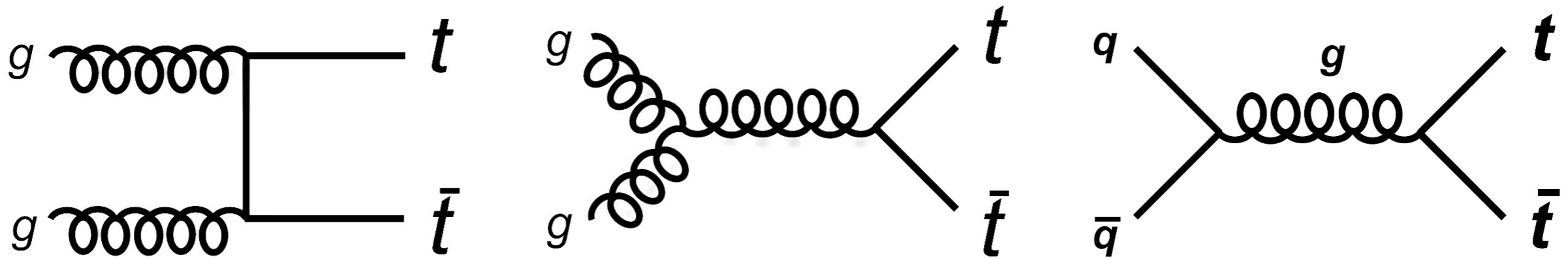


ALPS2019: Fourth Alpine LHC Physics Summit
22-27 Apr 2019, Obergurgl (Austria)

Introduction and Motivation

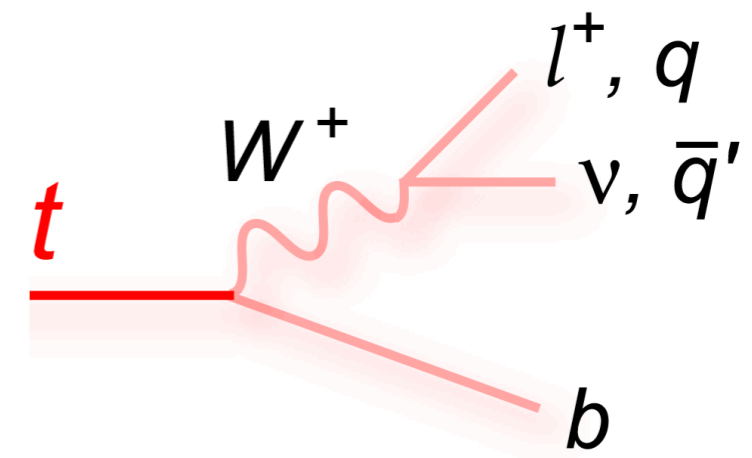


Introduction and Motivation



lifetime	<	QCD timescale	\ll	spin-flip timescale
10^{-25} s	<	10^{-24} s	\ll	10^{-21} s

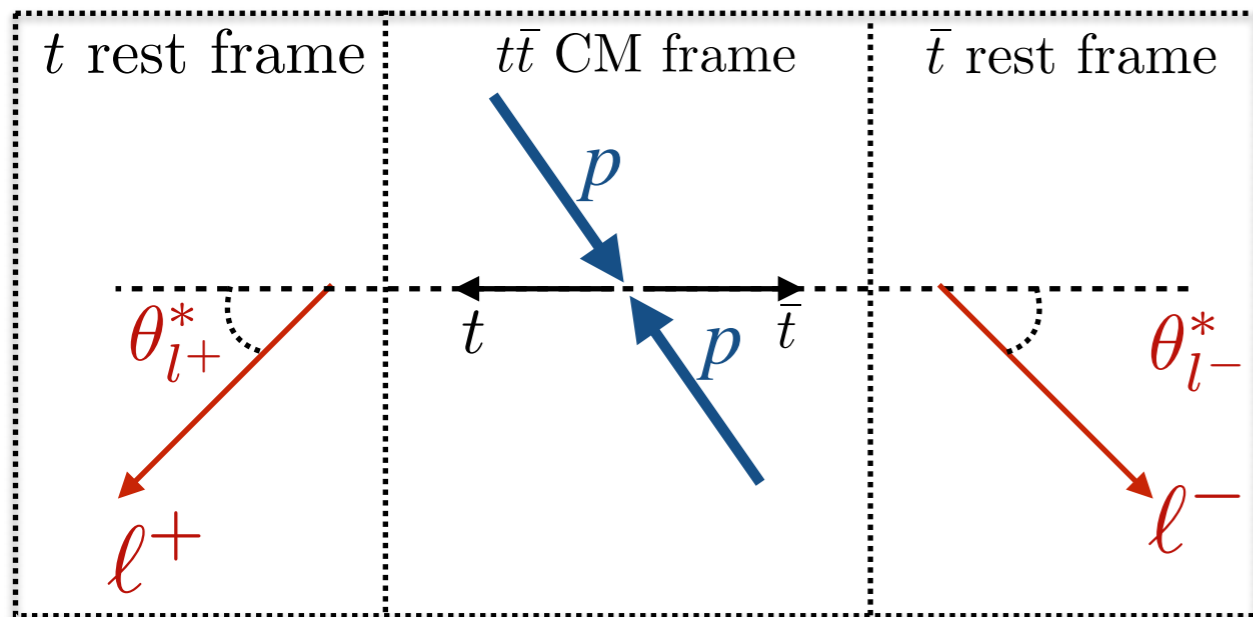
- Top quark decays before hadronization.
- Spins does not decorrelate in this short time
- and the decay particles carry the spin information



Introduction and Motivation

- Top quarks produced by strong interaction are unpolarized but QCD causes top-quark spins to be correlated at production.
- For low $t\bar{t}$ invariant masses, the production is dominated by the fusion of pairs of gluons with the same helicities
- There are BSM scenarios predicting polarized top quarks, hence affecting the spin correlation.
- Therefore, it is highly important to measure the spin correlations of top quark pairs
- Two methods to measure top spin correlations
 - Direct Measurement: Requires the reconstruction of the $t\bar{t}$ system
 - Indirect Measurement: Angle between two lepton $\Delta\phi(l^-l^+)$
experimentally preferred
because lepton angles
have excellent resolution

Observables



θ measured in helicity basis (lepton angle in parent top's rest frame, relative to parent top's direction in $t\bar{t}$ CM frame).

the variable $A_P^{\text{CPV}} = (A_{P+} - A_{P-})/2$ measures possible polarization introduced by a maximally CP -violating process.

Polarization

$$P^\pm = 2A_{P^\pm} \quad A_{P^\pm} = \frac{N(\cos \theta_{\ell^\pm}^* > 0) - N(\cos \theta_{\ell^\pm}^* < 0)}{N(\cos \theta_{\ell^\pm}^* > 0) + N(\cos \theta_{\ell^\pm}^* < 0)}$$

Correlation

$$A_{\Delta\phi} = \frac{N(|\Delta\phi_{\ell^+\ell^-}| > \pi/2) - N(|\Delta\phi_{\ell^+\ell^-}| < \pi/2)}{N(|\Delta\phi_{\ell^+\ell^-}| > \pi/2) + N(|\Delta\phi_{\ell^+\ell^-}| < \pi/2)}$$

indirect measurement of top spin correlation

Spin Correlation Coefficient

$$C_{\text{hel}} = -4A_{c_1 c_2} \quad A_{c_1 c_2} = \frac{N(c_1 c_2 > 0) - N(c_1 c_2 < 0)}{N(c_1 c_2 > 0) + N(c_1 c_2 < 0)}$$

$c_1 = \cos \theta_{\ell^+}^*$ and $c_2 = \cos \theta_{\ell^-}^*$

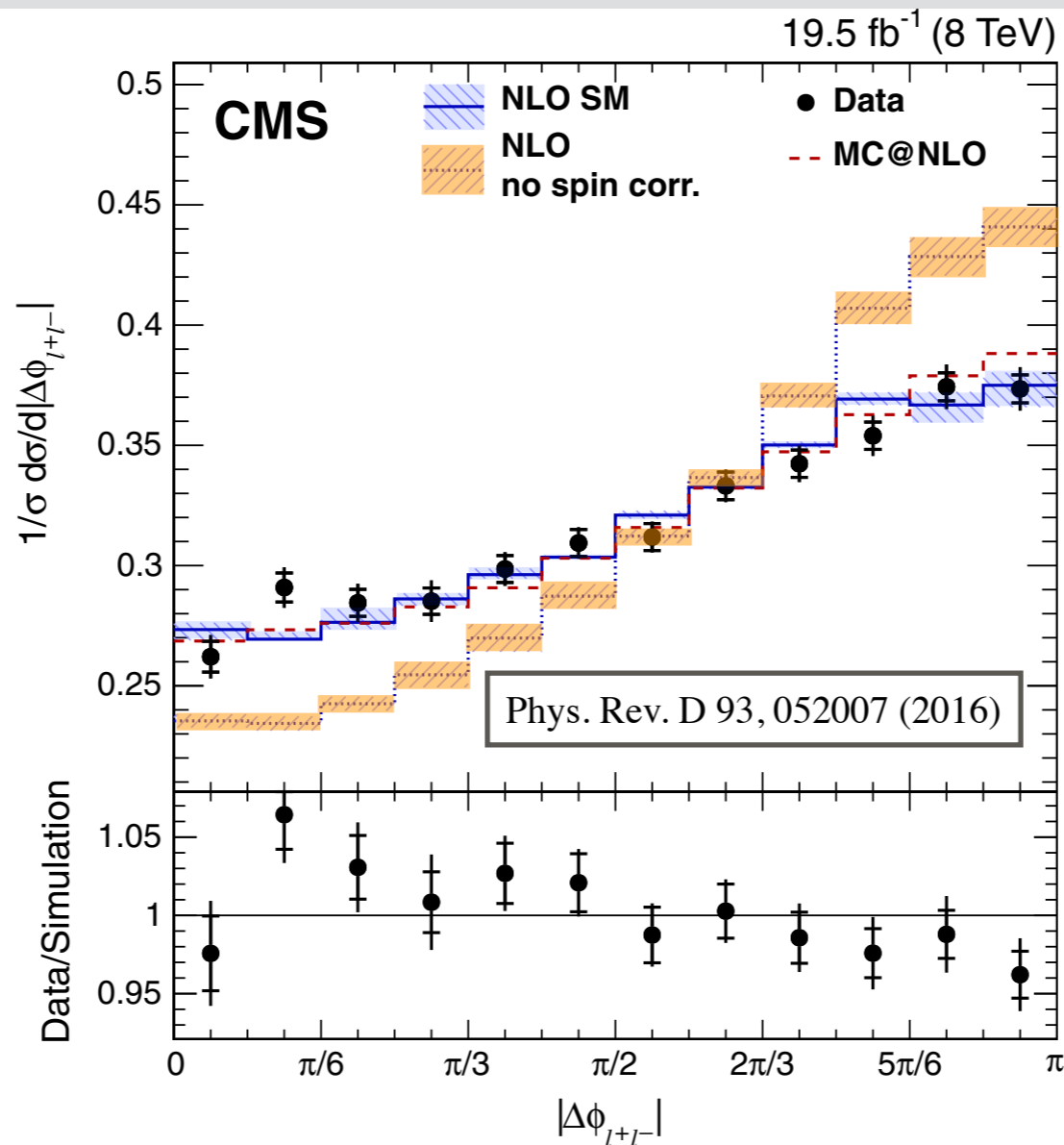
Spin Correlation Coefficient

$$D = -2A_{\cos \varphi} \quad A_{\cos \varphi} = \frac{N(\cos \varphi > 0) - N(\cos \varphi < 0)}{N(\cos \varphi > 0) + N(\cos \varphi < 0)}$$

$\varphi = \angle(\hat{\ell}_+, \hat{\ell}_-)$

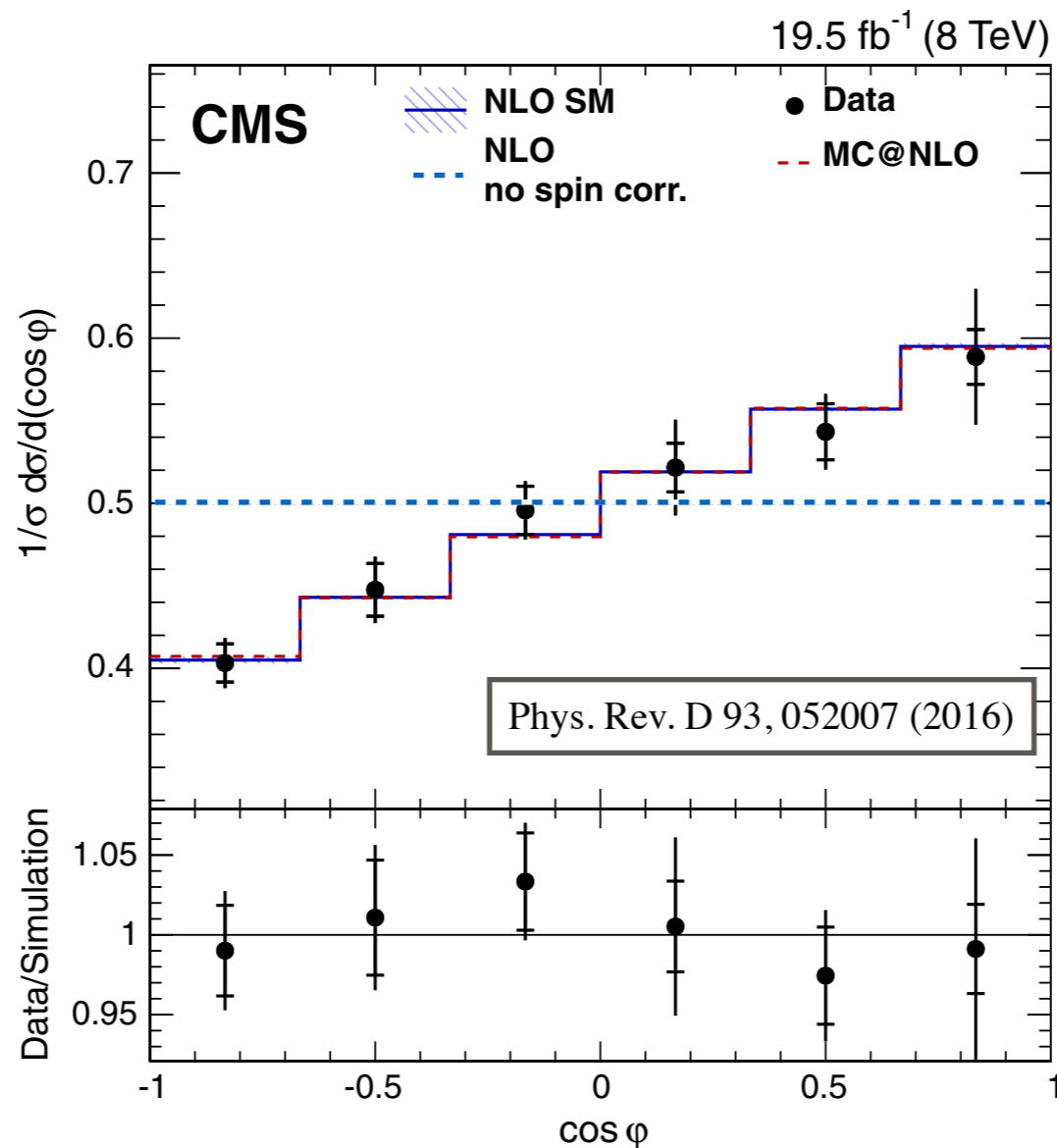
$\theta_{\ell^+}^*$ and $\theta_{\ell^-}^*$ are the helicity angles

CMS 8 TeV Results (unfolded to the parton level)



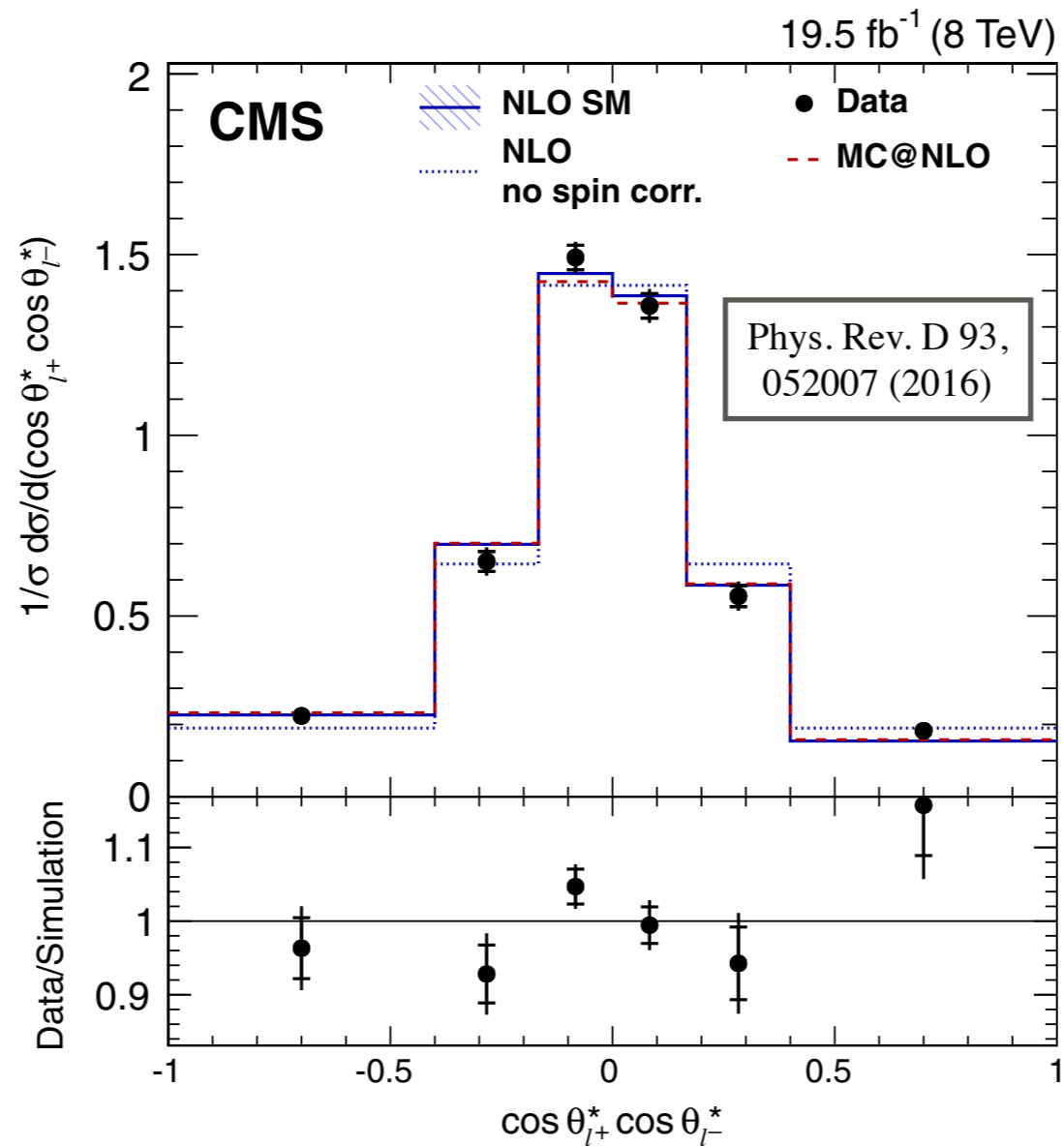
Asymmetry variable	Data (unfolded)	MC@NLO simulation	NLO, SM	NLO, no spin corr.
$A_{\Delta\phi}$	$0.094 \pm 0.005 \pm 0.012$	0.113 ± 0.001	$0.110^{+0.006}_{-0.009}$	$0.202^{+0.006}_{-0.009}$
$A_{\cos\varphi}$	$0.102 \pm 0.010 \pm 0.012$	0.114 ± 0.001	0.114 ± 0.006	0
$A_{c_1c_2}$	$-0.069 \pm 0.013 \pm 0.016$	-0.081 ± 0.001	-0.080 ± 0.004	0
A_P	$-0.011 \pm 0.007 \pm 0.028$	0	0.002 ± 0.001	...
A_P^{CPV}	$0.000 \pm 0.006 \pm 0.005$	0	0	...

CMS 8 TeV Results (unfolded to the parton level)



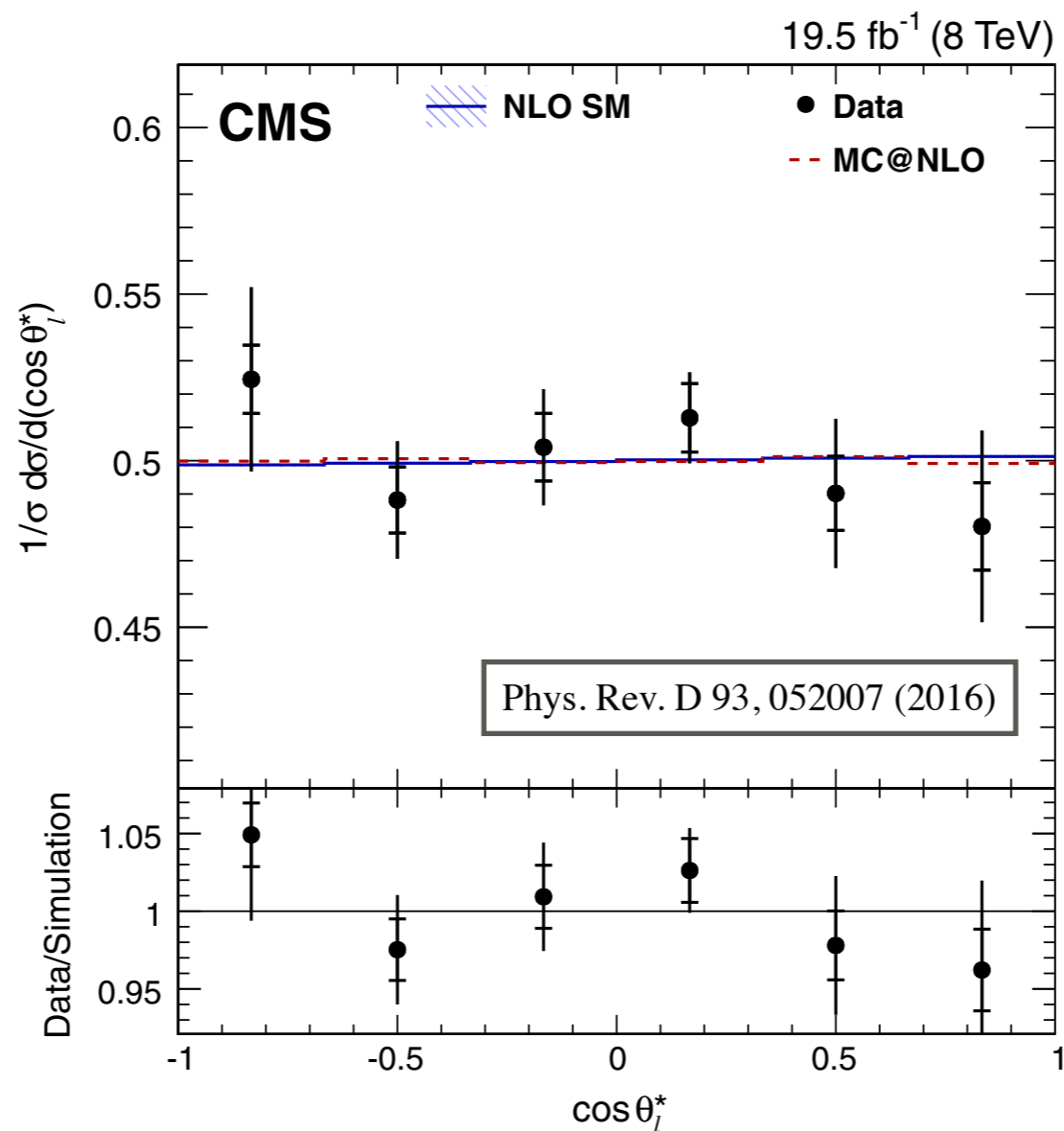
Asymmetry variable	Data (unfolded)	MC@NLO simulation	NLO, SM	NLO, no spin corr.
$A_{\Delta\phi}$	$0.094 \pm 0.005 \pm 0.012$	0.113 ± 0.001	$0.110^{+0.006}_{-0.009}$	$0.202^{+0.006}_{-0.009}$
$A_{\cos\phi}$	$0.102 \pm 0.010 \pm 0.012$	0.114 ± 0.001	0.114 ± 0.006	0
$A_{c_1c_2}$	$-0.069 \pm 0.013 \pm 0.016$	-0.081 ± 0.001	-0.080 ± 0.004	0
A_P	$-0.011 \pm 0.007 \pm 0.028$	0	0.002 ± 0.001	...
A_P^{CPV}	$0.000 \pm 0.006 \pm 0.005$	0	0	...

CMS 8 TeV Results (unfolded to the parton level)



Asymmetry variable	Data (unfolded)	MC@NLO simulation	NLO, SM	NLO, no spin corr.
$A_{\Delta\phi}$	$0.094 \pm 0.005 \pm 0.012$	0.113 ± 0.001	$0.110^{+0.006}_{-0.009}$	$0.202^{+0.006}_{-0.009}$
$A_{\cos\phi}$	$0.102 \pm 0.010 \pm 0.012$	0.114 ± 0.001	0.114 ± 0.006	0
$A_{c_1 c_2}$	$-0.069 \pm 0.013 \pm 0.016$	-0.081 ± 0.001	-0.080 ± 0.004	0
A_P	$-0.011 \pm 0.007 \pm 0.028$	0	0.002 ± 0.001	...
A_P^{CPV}	$0.000 \pm 0.006 \pm 0.005$	0	0	...

CMS 8 TeV Results (unfolded to the parton level)



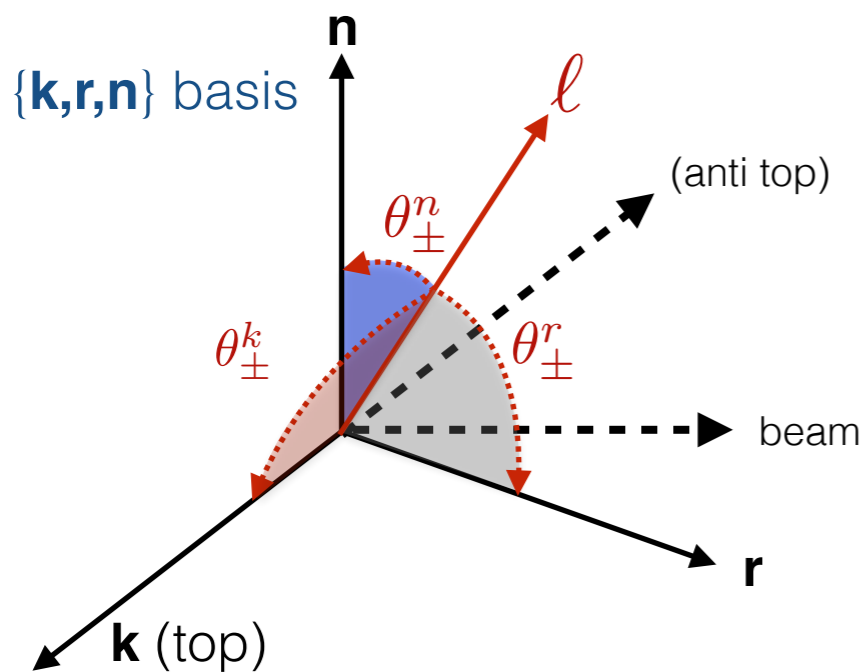
Asymmetry variable	Data (unfolded)	MC@NLO simulation	NLO, SM	NLO, no spin corr.
$A_{\Delta\phi}$	$0.094 \pm 0.005 \pm 0.012$	0.113 ± 0.001	$0.110^{+0.006}_{-0.009}$	$0.202^{+0.006}_{-0.009}$
$A_{\cos\varphi}$	$0.102 \pm 0.010 \pm 0.012$	0.114 ± 0.001	0.114 ± 0.006	0
$A_{c_1c_2}$	$-0.069 \pm 0.013 \pm 0.016$	-0.081 ± 0.001	-0.080 ± 0.004	0
A_P	$-0.011 \pm 0.007 \pm 0.028$	0	0.002 ± 0.001	...
A_P^{CPV}	$0.000 \pm 0.006 \pm 0.005$	0	0	...

Fit spin correlation strength as **fraction f_{SM} of the SM prediction**

$$f = \frac{N_{SM}^t}{N_{SM}^{t\bar{t}} + N_{uncor}^{t\bar{t}}} \quad f \in [0, 1]$$

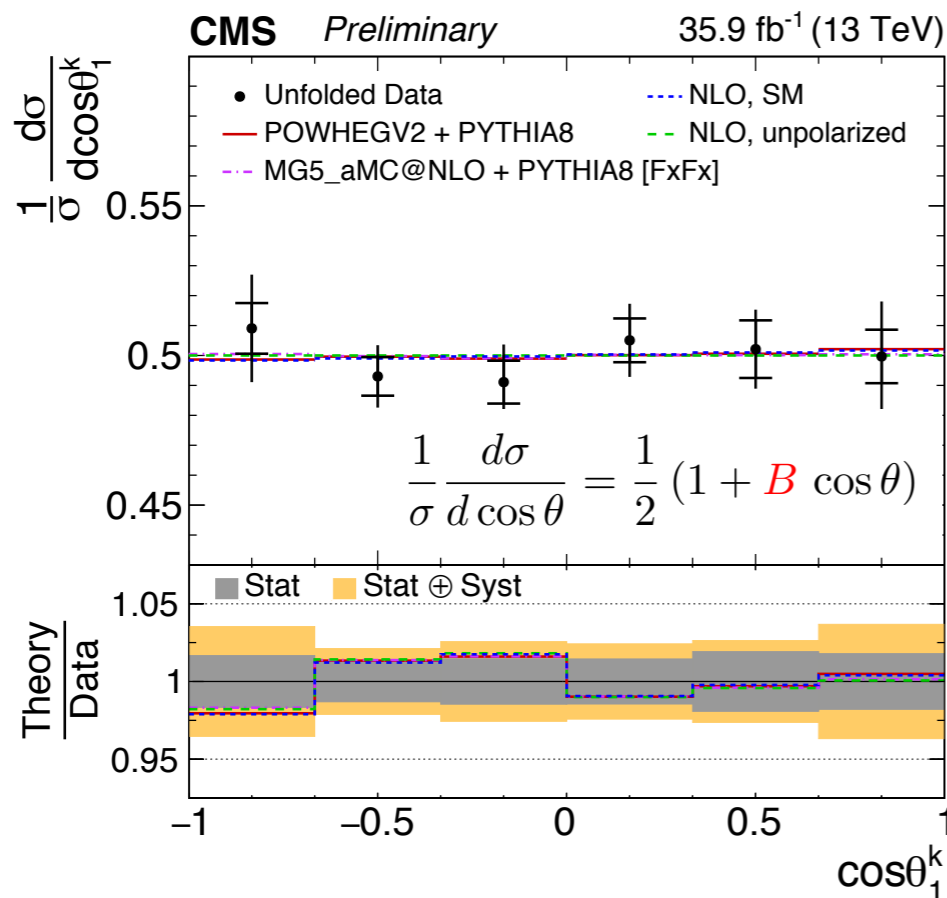
$$A^{\text{meas}} = f A^{SM} + (1 - f) A^{\text{uncor}}$$

Variable	$f_{SM} \pm (\text{stat}) \pm (\text{syst}) \pm (\text{theor})$	Total uncertainty
$A_{\Delta\phi}$	$1.14 \pm 0.06 \pm 0.13^{+0.08}_{-0.11}$	$+0.16$ -0.18
$A_{\cos\varphi}$	$0.90 \pm 0.09 \pm 0.10 \pm 0.05$	± 0.15
$A_{c_1 c_2}$	$0.87 \pm 0.17 \pm 0.21 \pm 0.04$	± 0.27
$A_{\Delta\phi} \text{ (vs } M_{t\bar{t}})$	$1.12 \pm 0.06 \pm 0.08^{+0.08}_{-0.11}$	$+0.12$ -0.15

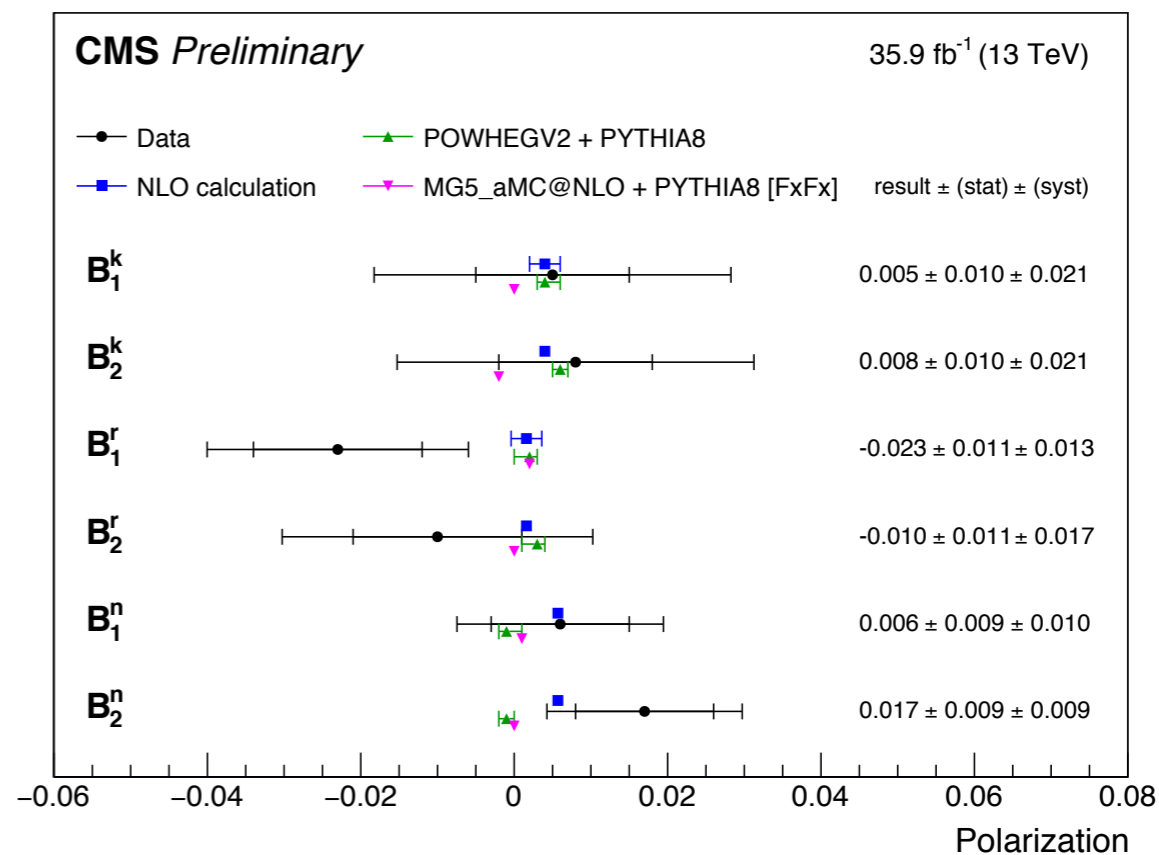


- Dilepton distribution **probes top spin in 3 dimensions**
- **Leptons follow parent top spin (average polarization given by 3-vectors $B^{+/-}$)**
- Relative lepton directions follow 3x3 matrix **C** of spin correlation coefficients

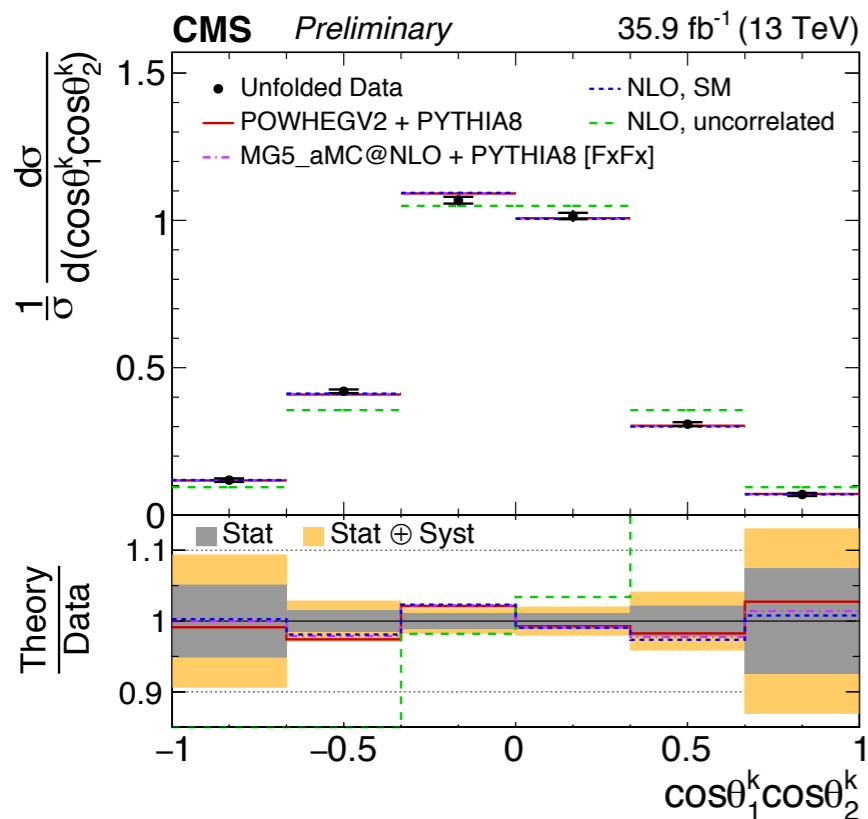
$$\frac{1}{\sigma} \frac{d\sigma}{dx} = \frac{1}{2} (1 + [\text{Coef.}]x) f(x)$$



[CMS-PAS-TOP-18-006](#)

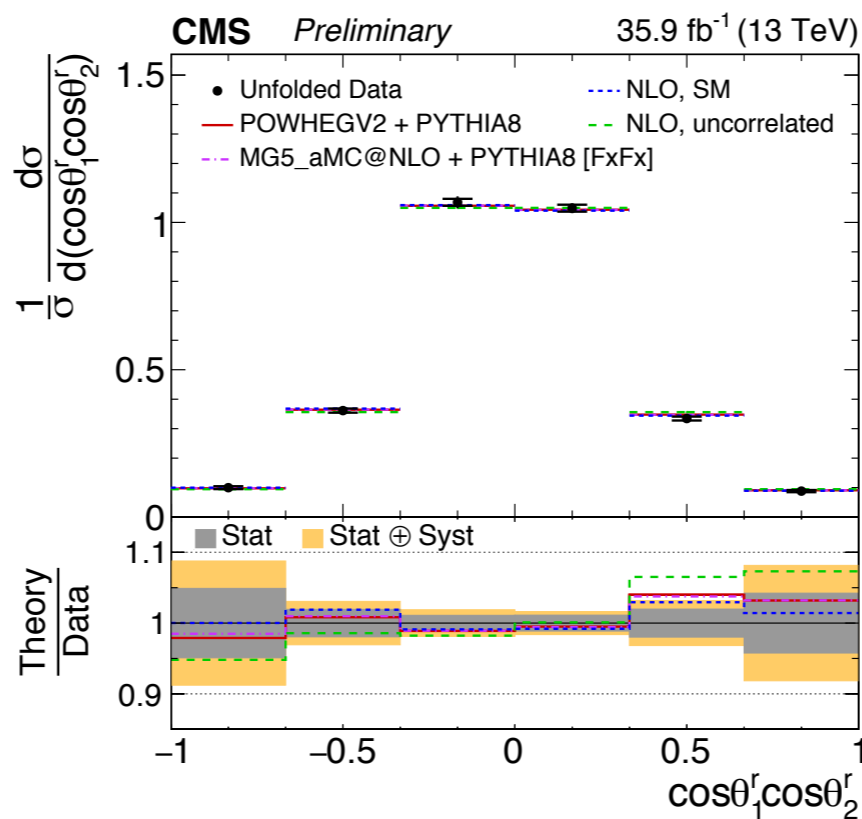


$$\frac{1}{\sigma} \frac{d\sigma}{d \cos \theta_1 \cos \theta_2} = \frac{1}{2} (1 - C \cos \theta_1 \cos \theta_2) \log \left(\frac{1}{|\cos \theta_1 \cos \theta_2|} \right)$$



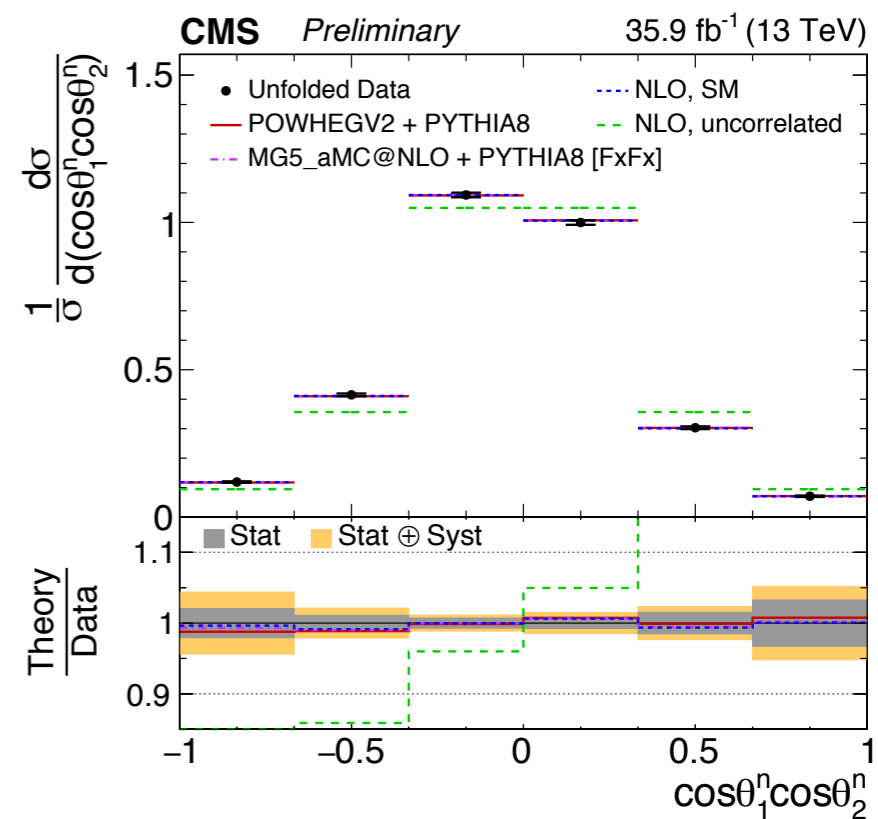
$$C_{kk} = 0.30 \pm 0.02 \pm 0.03$$

SM: 0.33



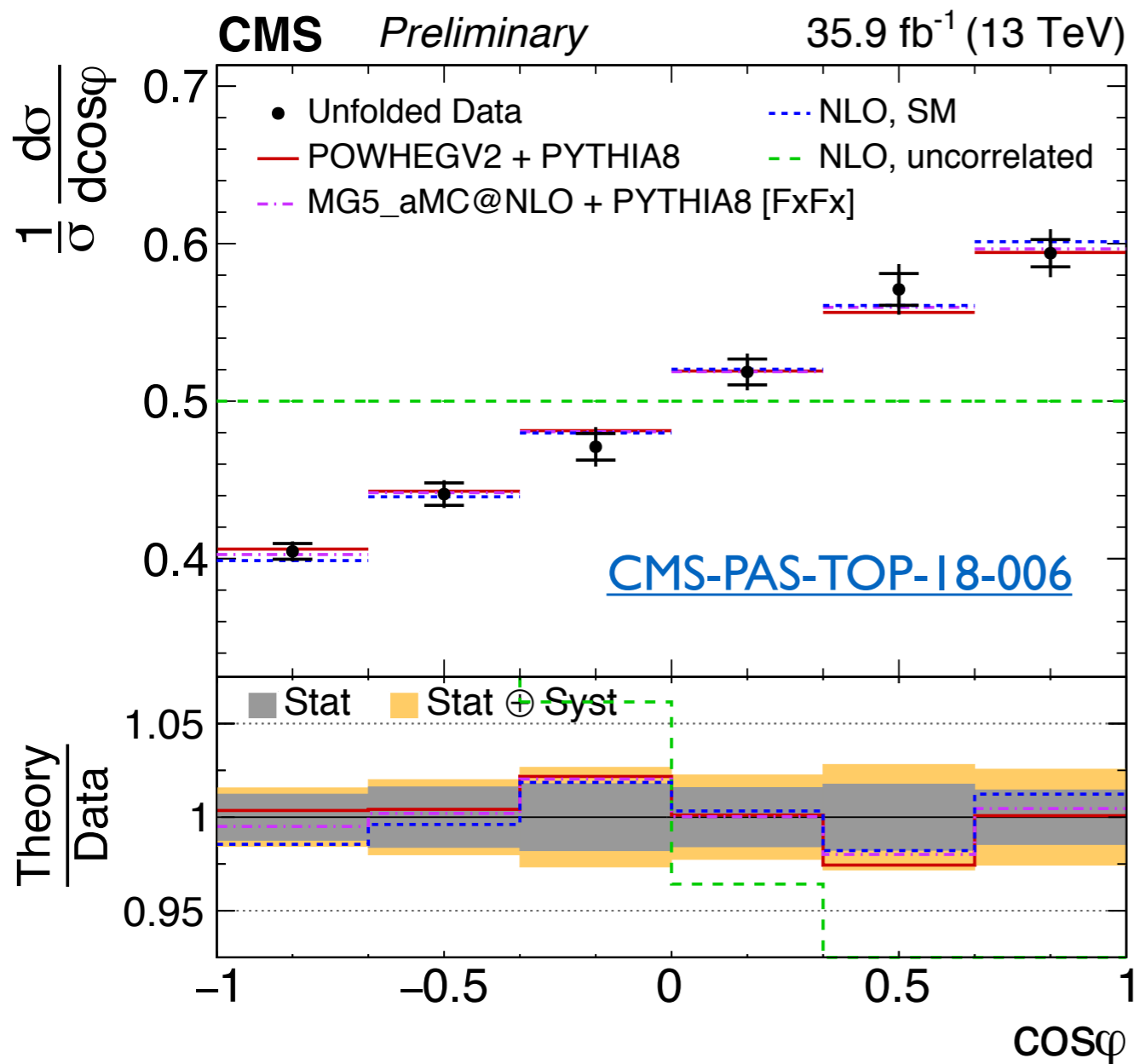
$$C_{rr} = 0.08 \pm 0.02 \pm 0.02$$

SM: 0.07



$$C_{nn} = 0.33 \pm 0.01 \pm 0.02$$

SM: 0.33



$$\frac{1}{\sigma} \frac{d\sigma}{d\cos\varphi} = \frac{1}{2} (1 - \boxed{D} \cos\varphi)$$

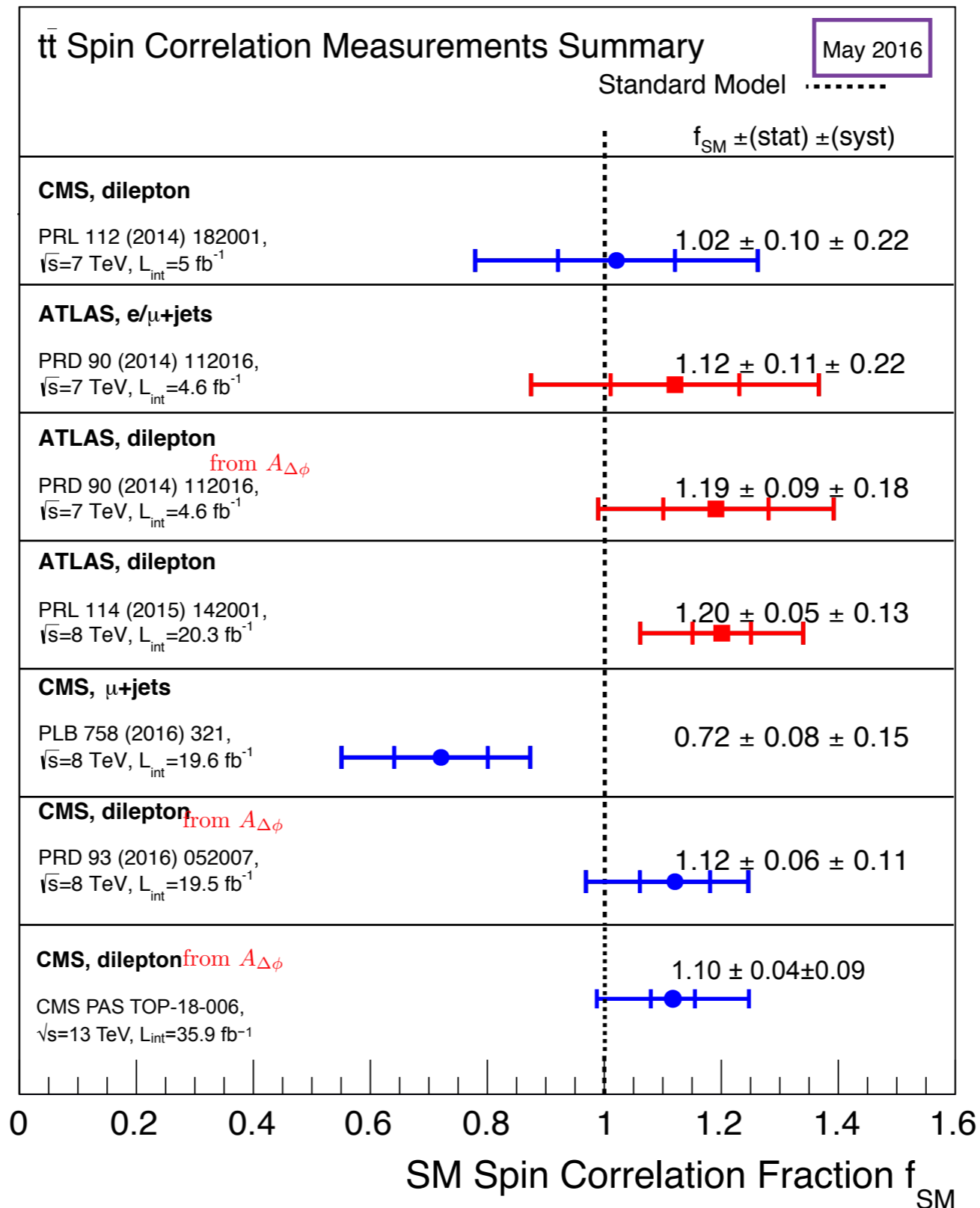
$$D = - (C_{kk} + C_{rr} + C_{nn}) / 3$$

$$D = -0.237 \pm 0.007 \pm 0.009$$

$$\text{SM} : -0.243$$

$$f_{\text{SM}} = 0.97 \pm 0.05$$

Summary of Spin Correlation Fractions



New Physics?

\mathcal{L}_{eff} is given in terms of chromo dipole couplings of the top quark to the gluon(s):

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} - \frac{\tilde{\mu}_t}{2} \bar{t} \sigma^{\mu\nu} T^a t G_{\mu\nu}^a - \frac{\tilde{d}_t}{2} \bar{t} i \sigma^{\mu\nu} \gamma_5 T^a t G_{\mu\nu}^a$$

dimensionless chromo-moments:

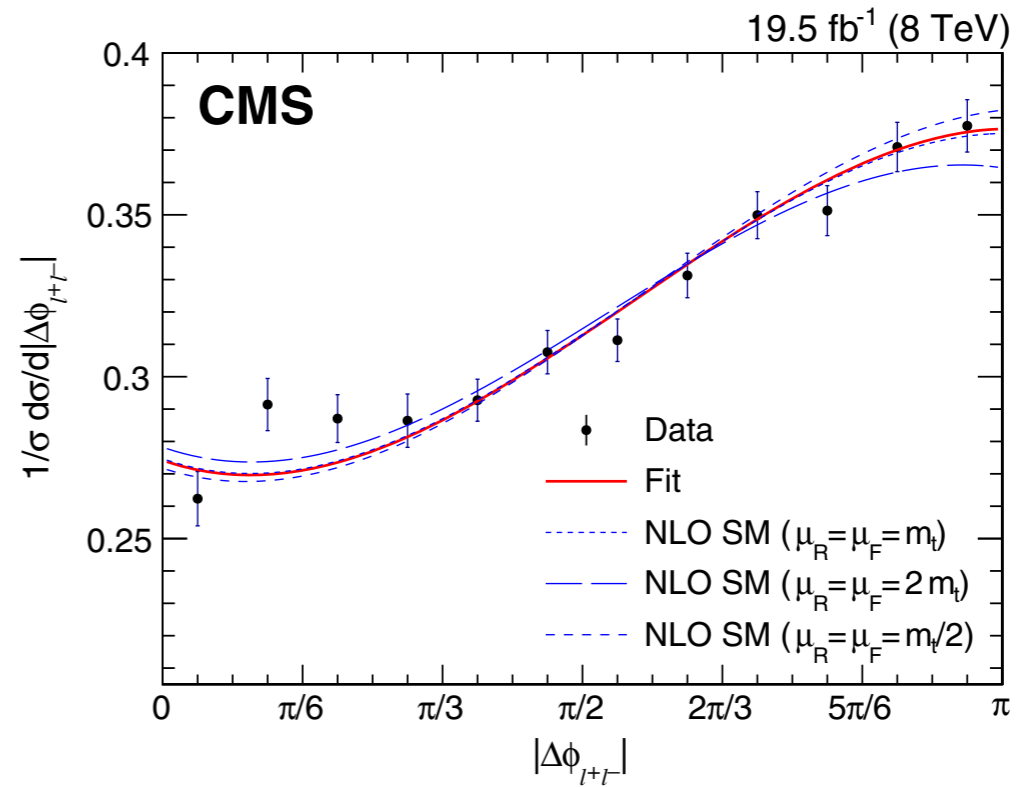
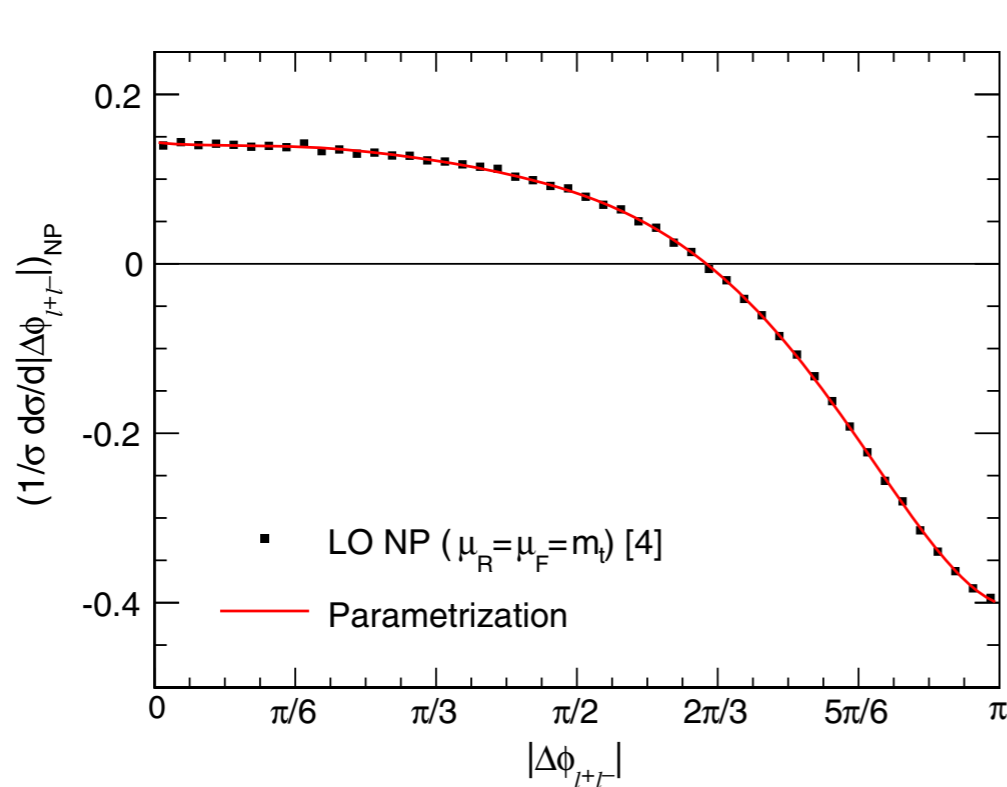
$$\hat{\mu}_t \equiv \frac{m_t}{g_s} \tilde{\mu}_t, \quad \hat{d}_t \equiv \frac{m_t}{g_s} \tilde{d}_t$$

In the presence of a small new physics (NP) contribution such that $\text{Re}(\hat{\mu}_t) \ll 1$, can be linearly expanded

$$\frac{1}{\sigma} \frac{d\sigma}{d|\Delta\phi_{\ell^+\ell^-}|} = \left(\frac{1}{\sigma} \frac{d\sigma}{d|\Delta\phi_{\ell^+\ell^-}|} \right)_{SM} + \text{Re}(\hat{\mu}_t) \left(\frac{1}{\sigma} \frac{d\sigma}{d|\Delta\phi_{\ell^+\ell^-}|} \right)_{NP}$$

New Physics?

$$\frac{1}{\sigma} \frac{d\sigma}{d|\Delta\phi_{\ell^+\ell^+}|} = \left(\frac{1}{\sigma} \frac{d\sigma}{d|\Delta\phi_{\ell^+\ell^-}|} \right)_{\text{SM}} + \text{Re}(\hat{\mu}_t) \left(\frac{1}{\sigma} \frac{d\sigma}{d|\Delta\phi_{\ell^+\ell^-}|} \right)_{\text{NP}}$$



$\text{Re}(\hat{\mu}_t) = -0.006 \pm 0.024$ corresponding 95% confidence level (C.L.) interval is $-0.053 < \text{Re}(\hat{\mu}_t) < 0.042$

Also, $D = D_{\text{SM}} + \text{Re}(\hat{\mu}_t) D_{\text{NP}}$

8 TeV	$M_{\tilde{t}\tilde{t}} \geq 2m_t$	$M_{\tilde{t}\tilde{t}} \leq 450 \text{ GeV}$	$M_{\tilde{t}\tilde{t}} > 450 \text{ GeV}$
D_{SM} (NLOW) expanded	-0.228(5)	-0.336(2)	-0.130(5)
D_{SM} (NLOW) unexpanded	-0.217(11)	-0.330(6)	-0.120(14)
D_{NP}	-1.712(19)	-1.696(14)	-1.653(20)

W. Bernreuther, Z.G. Si / Physics Letters B 725 (2013) 115–122

$\text{Re}(\hat{\mu}_t) = -0.014 \pm 0.020$

corresponding 95% confidence level (C.L.) interval is $-0.053 < \text{Re}(\hat{\mu}_t) < 0.027$

New Physics?

$$\text{Also, } D = D_{\text{SM}} + \text{Re}(\hat{\mu}_t) D_{\text{NP}}$$

8 TeV	$M_{t\bar{t}} \geq 2m_t$	$M_{t\bar{t}} \leq 450 \text{ GeV}$	$M_{t\bar{t}} > 450 \text{ GeV}$
D_{SM} (NLOW) expanded	-0.228(5)	-0.336(2)	-0.130(5)
D_{SM} (NLOW) unexpanded	-0.217(11)	-0.330(6)	-0.120(14)
D_{NP}	-1.712(19)	-1.696(14)	-1.653(20)

W. Bernreuther, Z.G. Si / Physics Letters B 725 (2013) 115–122

$$\text{Re}(\hat{\mu}_t) = -0.014 \pm 0.020$$

corresponding 95% confidence level (C.L.) interval
is $-0.053 < \text{Re}(\hat{\mu}_t) < 0.027$

$$\text{Similarly } P^{\text{CPV}} \text{ is related to } P^{\text{CPV}} = \text{Im}(\hat{d}_t) P_{\text{NP}}^{\text{CPV}}$$

from W. Bernreuther, Z.G. Si / Physics Letters B 725 (2013) 115-122

$$P_{\text{NP}}^{\text{CPV}} = 0.482 \pm 0.003$$

$$\text{Im}(\hat{d}_t) = -0.001 \pm 0.034$$

with the corresponding 95% C.L. interval $-0.068 < \text{Im}(\hat{d}_t) < 0.067$

for 13 TeV constraints, again see Afiq's Talk at YSF!

- Top quarks produced by strong interaction are unpolarized but QCD causes top-quark spins to be correlated at production.
- There are BSM scenarios predicting polarized top quarks, hence affecting the spin correlation.
- All measurements are in agreement with the SM expectations, and help constrain theories of physics beyond the SM.

