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# $a_{\mu}$ , $a_e$ and Implications for a Muon EDM

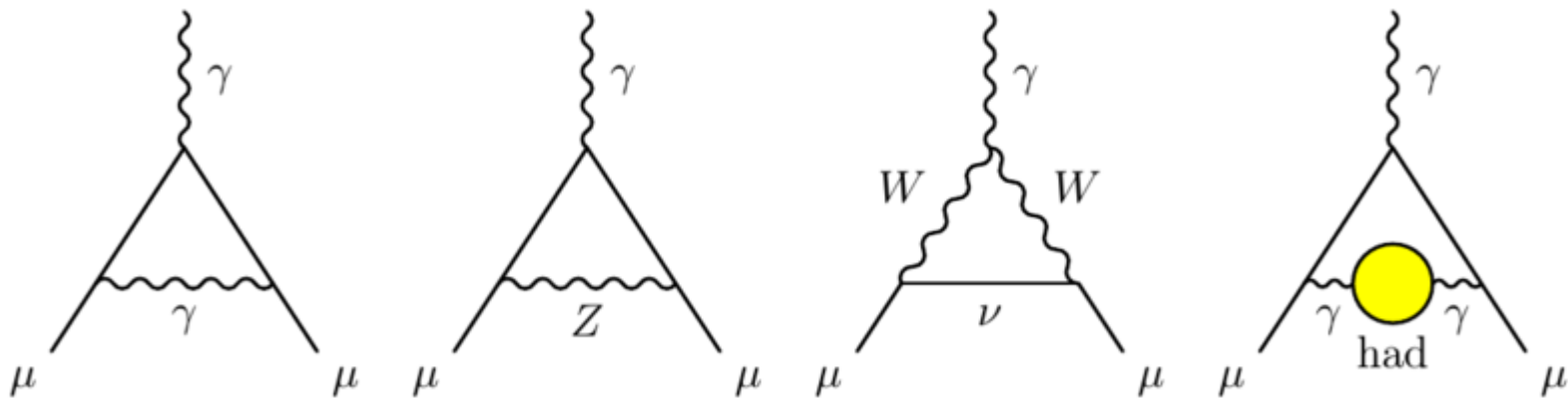
Based on: AC, and M. Hoferichter and P. Schmidt-Wellenburg; arXiv:1807.11484

- Introduction: Searching for NP with flavour observables
- Experimental situation: Lepton Flavour Universality Violation
- Anomalous magnetic moments
  - $a_\mu$
  - $a_e$
- Combined explanations
- A large muon EDM
- Conclusions

- Single measurement from BNL
- Theory prediction sound but challenging because of hadronic effects.

$$\Delta a_{\mu} = (236 \pm 87) \times 10^{-11}$$

- Soon new experimental results from Fermilab



3 $\sigma$  deviation (order of SM-EW contribution)

- AMM usually used to determine  $\alpha$
- With *now* best determination of  $\alpha$  from Cs atoms

$$a_e^{\text{SM}} \Big|_{\alpha_{\text{Cs}}} = 1,159,652,181.61(23) \times 10^{-12}$$

- Compared to the electron AMM measurement

$$\Delta a_e = a_e^{\text{exp}} - a_e^{\text{SM}} = -0.88(36) \times 10^{-12}$$

- Normalized to the lepton mass

$$-3 \leq \frac{\Delta a_\mu}{m_\mu} \Big/ \frac{\Delta a_e}{m_e} \leq -130 \quad \text{or} \quad -0.006 \leq \frac{\Delta a_\mu}{m_\mu^2} \Big/ \frac{\Delta a_e}{m_e^2} \leq -0.26$$

2.5  $\sigma$  deviation with opposite sign than  $a_\mu$

- Effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = c_R^{\ell_f \ell_i} \bar{\ell}_f \sigma_{\mu\nu} P_R \ell_i F^{\mu\nu} + \text{h.c.}$$

- Anomalous magnetic moment

$$a_{\ell_i} = -\frac{4m_{\ell_i}}{e} \text{Re} c_R^{\ell_i \ell_i}$$

- Electric Dipole moment

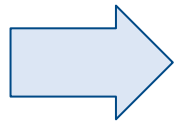
$$d_{\ell_i} = -2 \text{Im} c_R^{\ell_i \ell_i}$$

- Radiative Lepton decays

$$\text{Br}[\mu \rightarrow e\gamma] = \frac{m_\mu^3}{4\pi \Gamma_\mu} (|c_R^{e\mu}|^2 + |c_R^{\mu e}|^2)$$

Processes intrinsically connected

- Effect of the order of the EW-SM contribution needed



enhancement necessary

- Light particles
  - Neutral scalars
  - Neutral vector ( $Z'$  Dark Photon)
- Chiral enhancement: Chirality flip does not come from the muon mass but rather from an NP mass inside the loop

Light particles or chiral enhancement

- Light particles:  $m_W^2 / m^2$ 
  - Neutral scalars:  $\Phi$
  - Neutral vector (Z' Dark Photon):  $V$

$$c_R^{\mu\mu} = \frac{e}{16\pi^2} m_\mu \left( |\Gamma^{\mu L}|^2 + |\Gamma^{\mu R}|^2 \right) \frac{f_{\Phi,V} \left( \frac{M_\Psi^2}{m^2} \right) + Qg \left( \frac{M_\Psi^2}{m^2} \right)}{m^2}$$

$Q$  = charge of the fermion       $f, g$  = loop functions

- Same sign in muon and electron AMM
- Strong limits from direct searches for dark photons etc..

By construction real, i.e. no EDMs

- Enhancement by the mass of the fermion in the loop

$$c_R^{fi} = \frac{e}{16\pi^2} \Gamma_{\Psi}^{\mu L*} \Gamma_{\Psi}^{\mu R} M_{\Psi} \frac{f\left(\frac{M_{\Psi}^2}{M^2}\right) + Qg\left(\frac{M_{\Psi}^2}{M^2}\right)}{M^2}$$

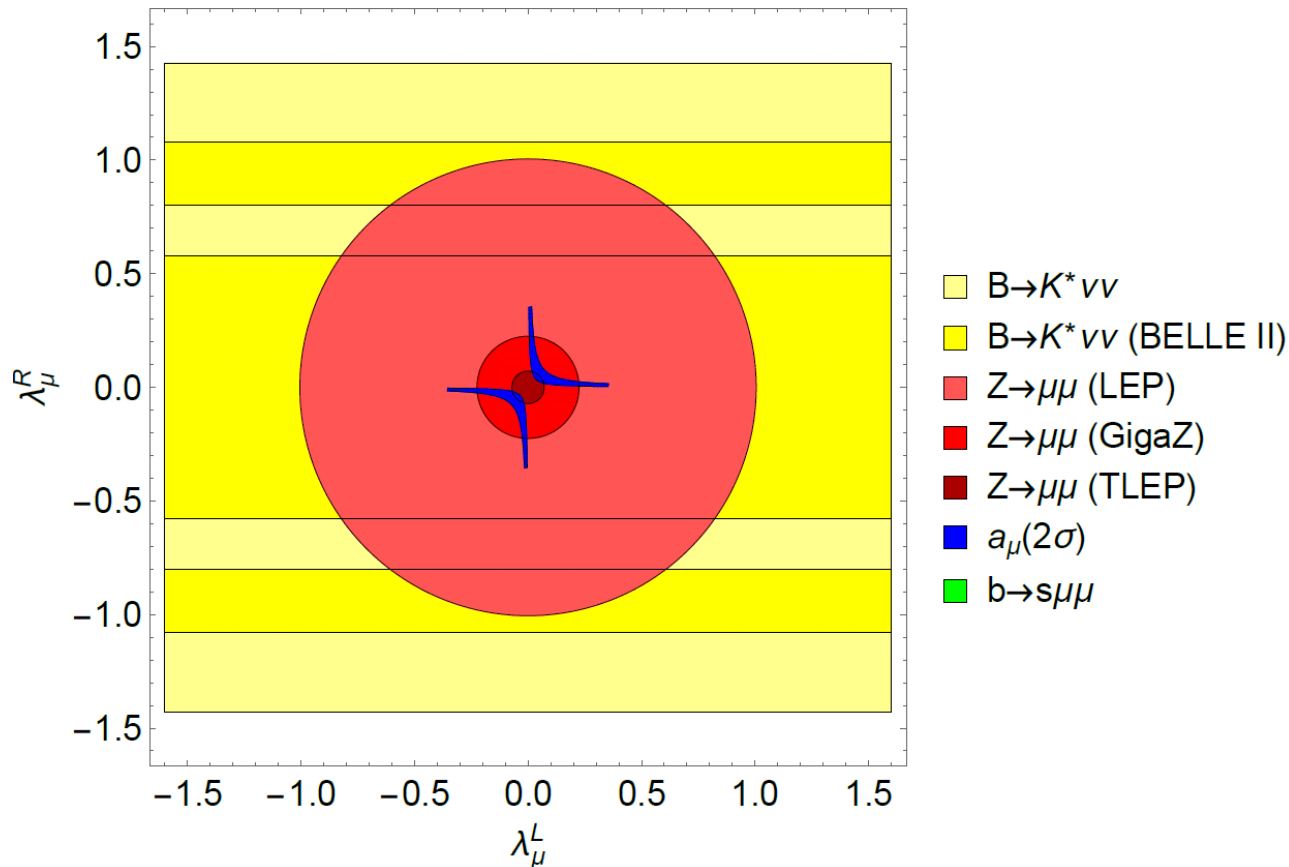
$Q, M_{\Psi}$  = charge, mass of the fermion      $f, g$  = loop functions

- MSSM:  $(\tan(\beta))$
- Leptoquarks:  $m_t/m_{\mu}$
- Model with vector like fermions:  $m_{\Psi}/m_{\mu}$

A priori arbitrary phase



## ■ Chirally enhanced effects via top-loops



$\lambda_\mu^{L,R}$

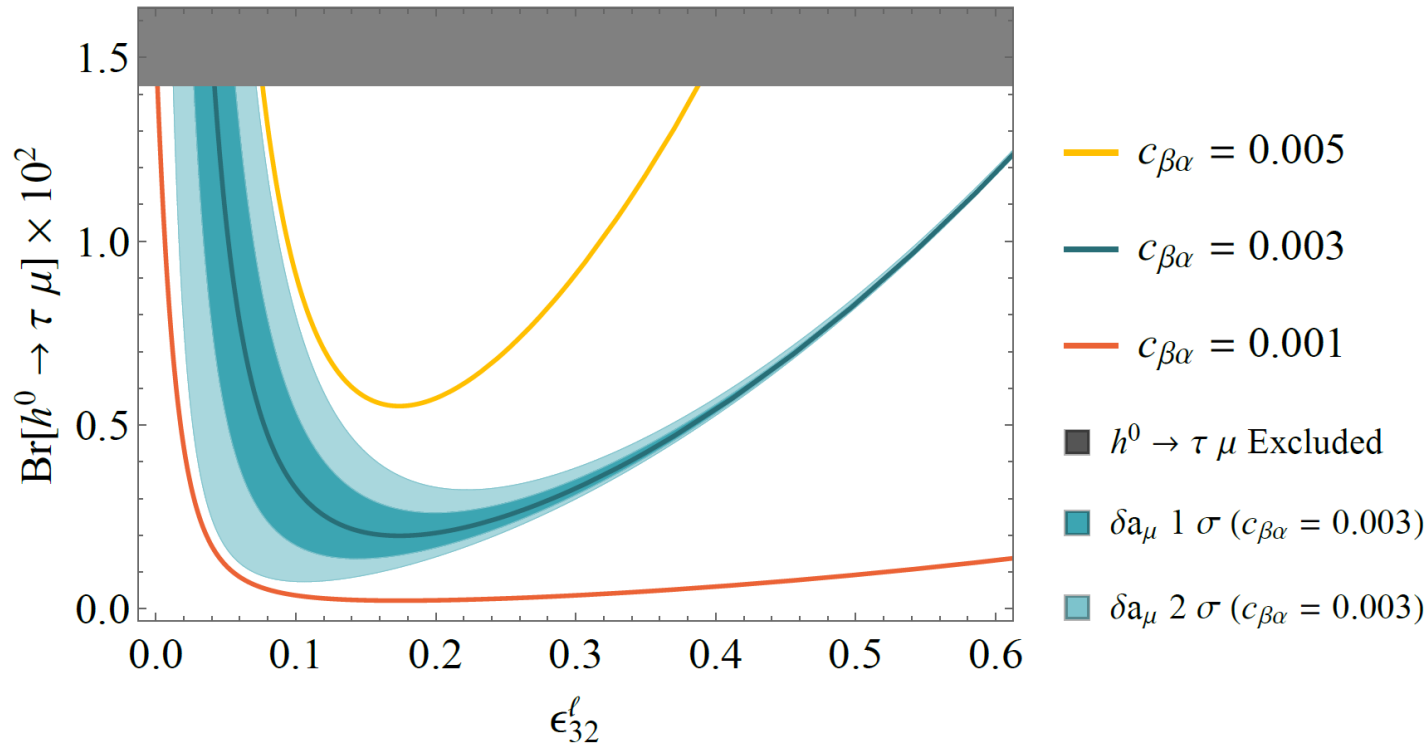
Left-, right-  
handed  
muons-top  
coupling

E. Leskow, A.C.,  
G. D'Ambrosio,  
D. Müller  
arXiv:1612.06858

$Z \rightarrow \mu \mu$  at future colliders

## ■ Chirally enhancement of $m_\mu/m_e$

AC, D. Müller, C. Wiegand  
arXiv:1903.10440



Unavoidable constraints from  $h \rightarrow \tau \mu$

- Opposite sign:  no single light mediator

- Minimal Flavour Violation:

$$\Delta a_\mu / \Delta a_e \neq m_\mu^2 / m_e^2$$

 generic flavour structure

- Single new particle:

$$\text{Br}[\mu \rightarrow e\gamma] = \frac{\alpha m_\mu^2}{16m_e \Gamma_\mu} |\Delta a_\mu \Delta a_e| \sim 8 \times 10^{-5}$$

8 orders of magnitude too large

 several new particles

**Muon and electron sector must be decoupled**

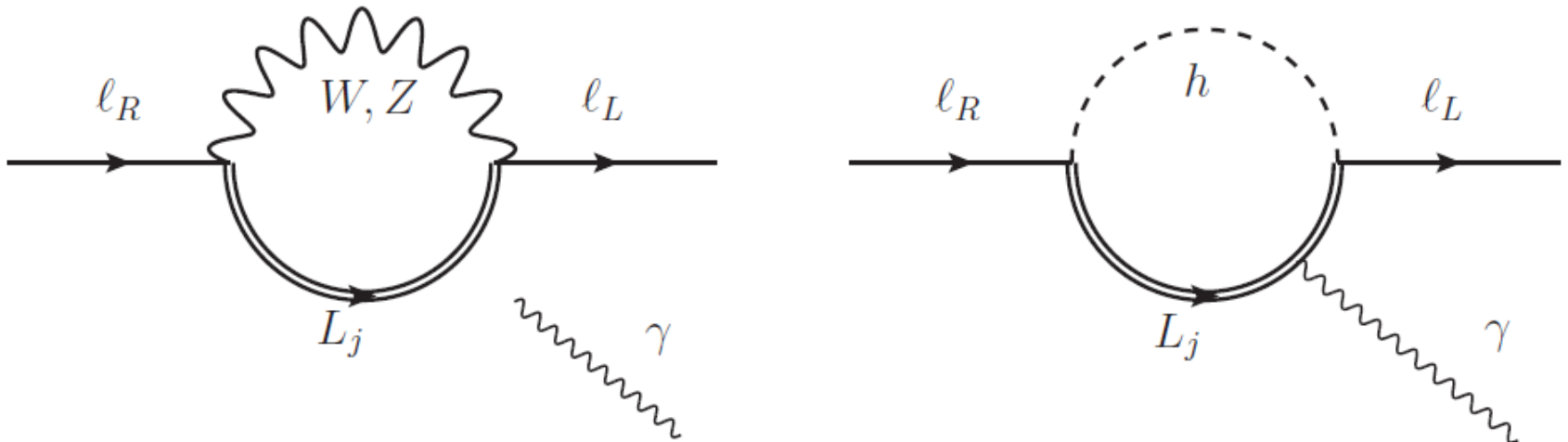
- MSSM
  - Constrained MFV does not work
  - With generic A-terms has problem with vacuum stability
  - With large  $\tan(\beta)$  and flavour violation
- 2HDMs & LQs: Problems with  $\mu \rightarrow e\gamma$
- Extra dimensions
  - Can only explain the muon or the electron AMM because of  $\mu \rightarrow e\gamma$

Most popular models do not work

# Model with new vector-like leptons

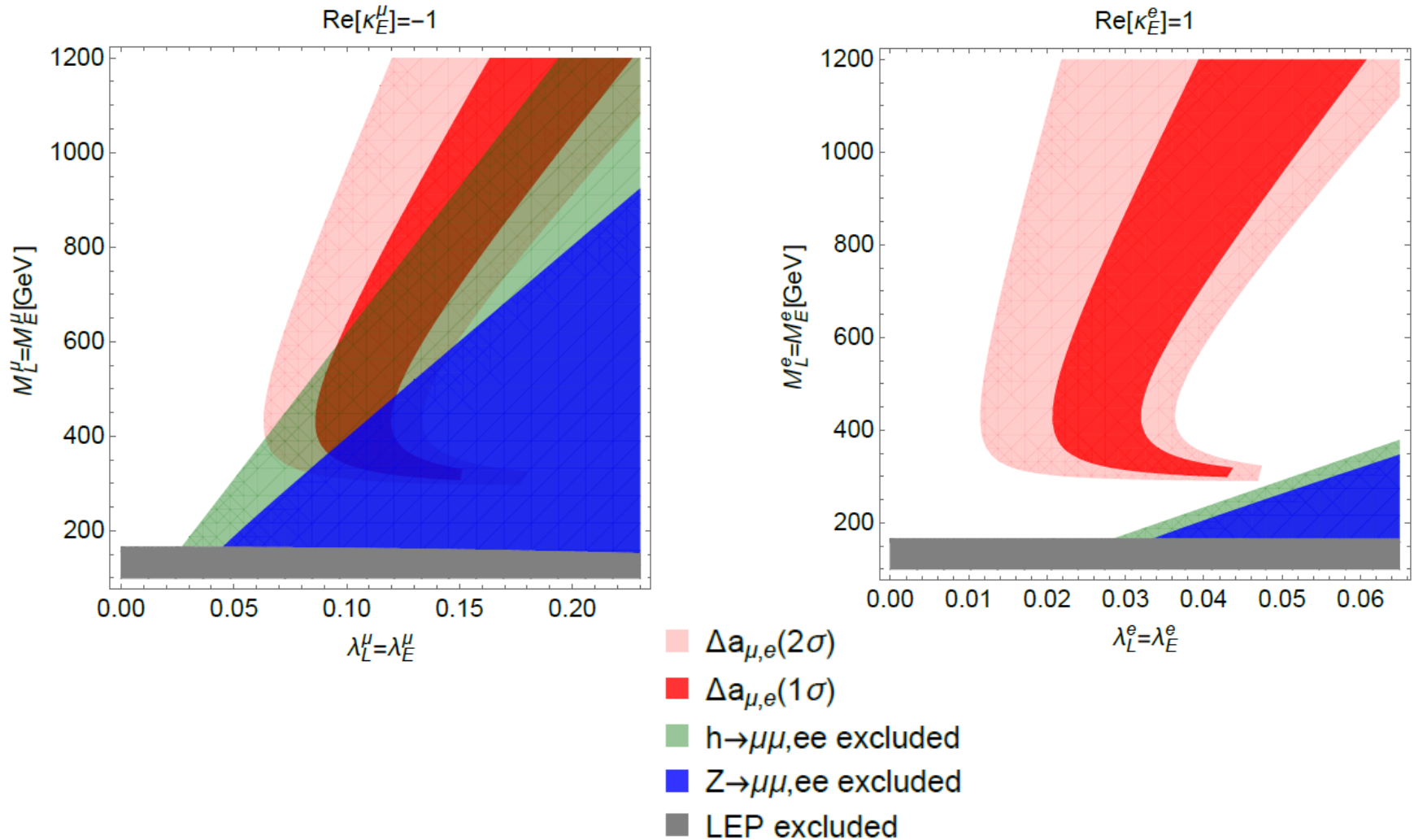
$$\mathcal{L}_M = -M_L \bar{L}_L L_R - M_E \bar{E}_L E_R + \text{h.c.},$$

$$\begin{aligned} \mathcal{L}_H = & -\kappa_L \bar{L}_L H E_R - \kappa_E \bar{L}_R H E_L \\ & - \lambda_L \bar{L}_L \ell_R H - \lambda_E \bar{E}_R \tilde{H} \ell_L + \text{h.c.} \end{aligned}$$



Chirally enhanced by  $v\kappa_{L,R}/m_\mu$

# Model with new vector-like leptons



Works for  $a_e$  but tension with  $a_\mu$

- Add neutral scalar
  - Effect in  $a_\mu$  possible without affecting  $h \rightarrow \mu\mu$
- Impose abelian flavour symmetry (e.g.  $L_\mu - L_\tau$ ) in order to avoid  $\mu \rightarrow e\gamma$
- More minimal model with one generation of vector-like fermions possible if  $a_e$  is explained by the SM Higgs and  $a_\mu$  via a new scalar
- New scalar could be  $L_\mu - L_\tau$  flavon

Many realizations possible

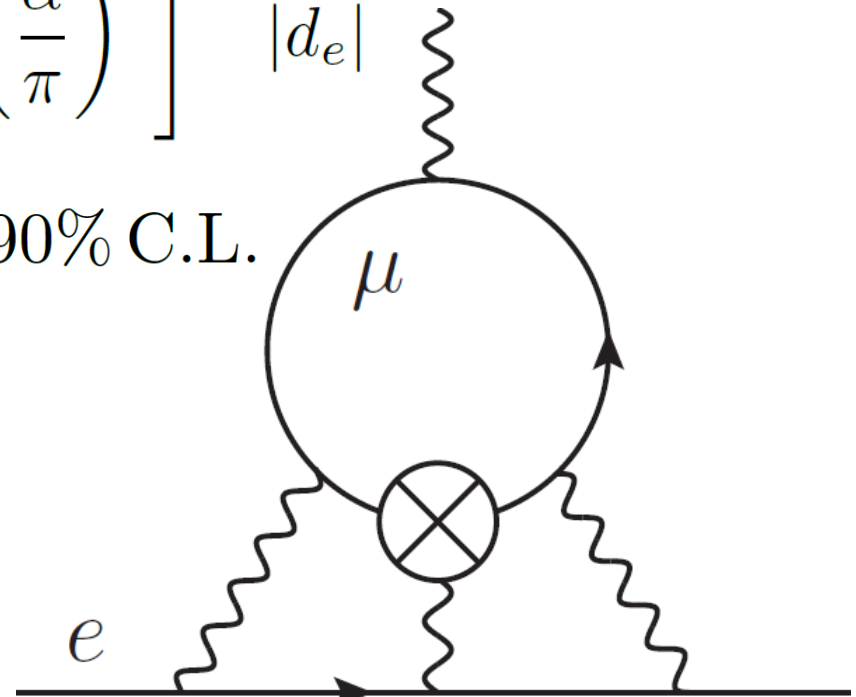
- MFV:
- Contribution only starts at the 3-loop level

$$|d_\mu| \leq \left[ \left( \frac{15}{4} \zeta(3) - \frac{31}{12} \right) \frac{m_e}{m_\mu} \left( \frac{\alpha}{\pi} \right)^3 \right]^{-1} |d_e|$$

$$|d_\mu| \leq 0.9 \times 10^{-19} e \text{ cm} \quad 90\% \text{ C.L.}$$

- Direct limit

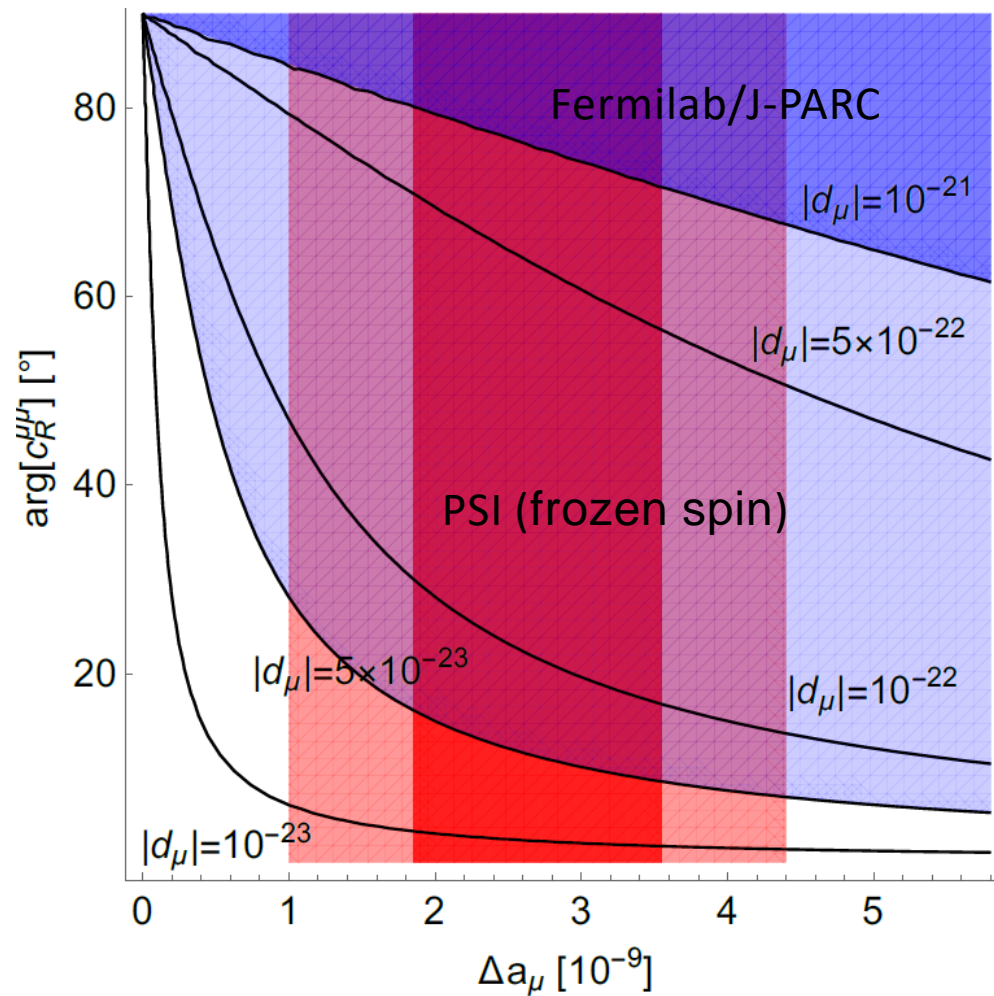
$$|d_\mu| < 1.5 \times 10^{-19} e \text{ cm}$$



Improvement of direct limit important



# Future experimental sensitivity



Dedicated experiment needed?

# Conclusions

