

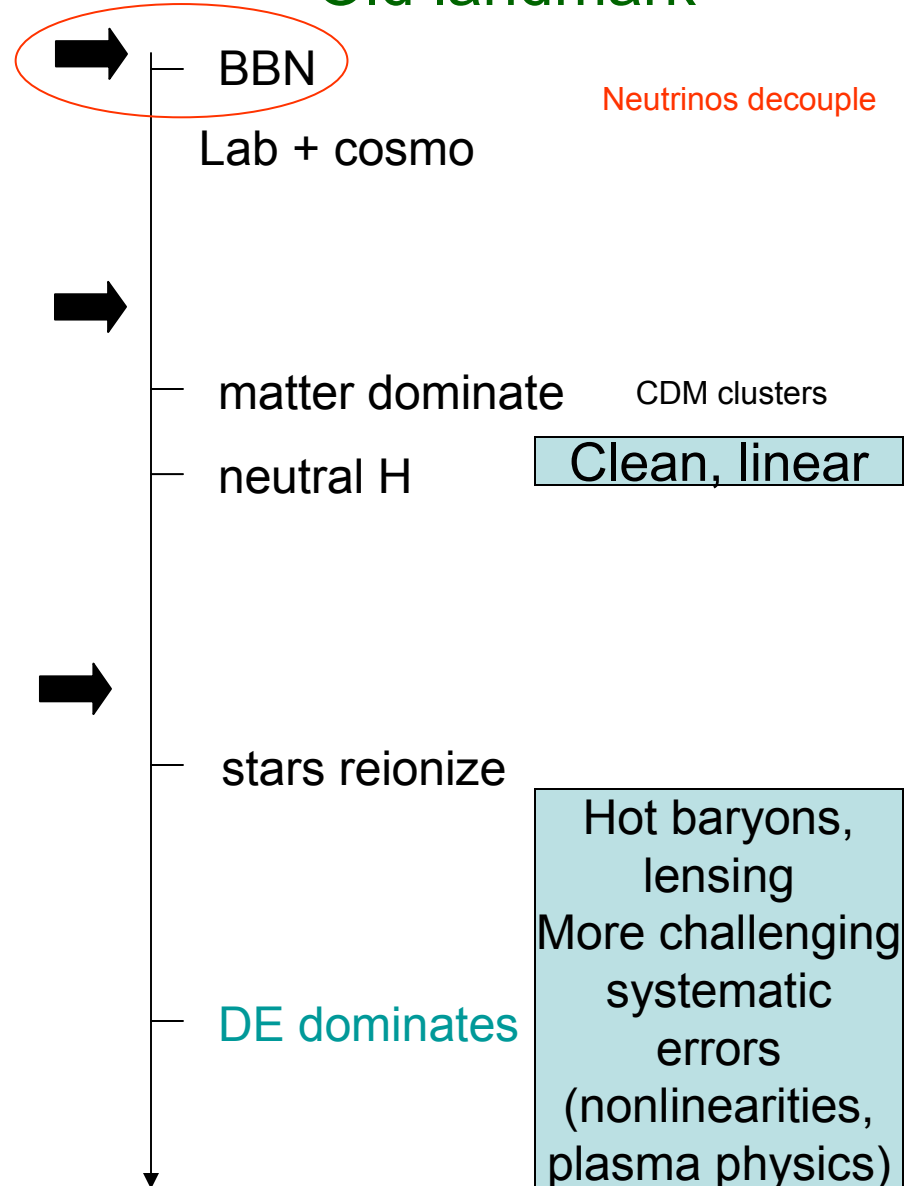
# Cosmological Implications of Electroweak Phase Transition



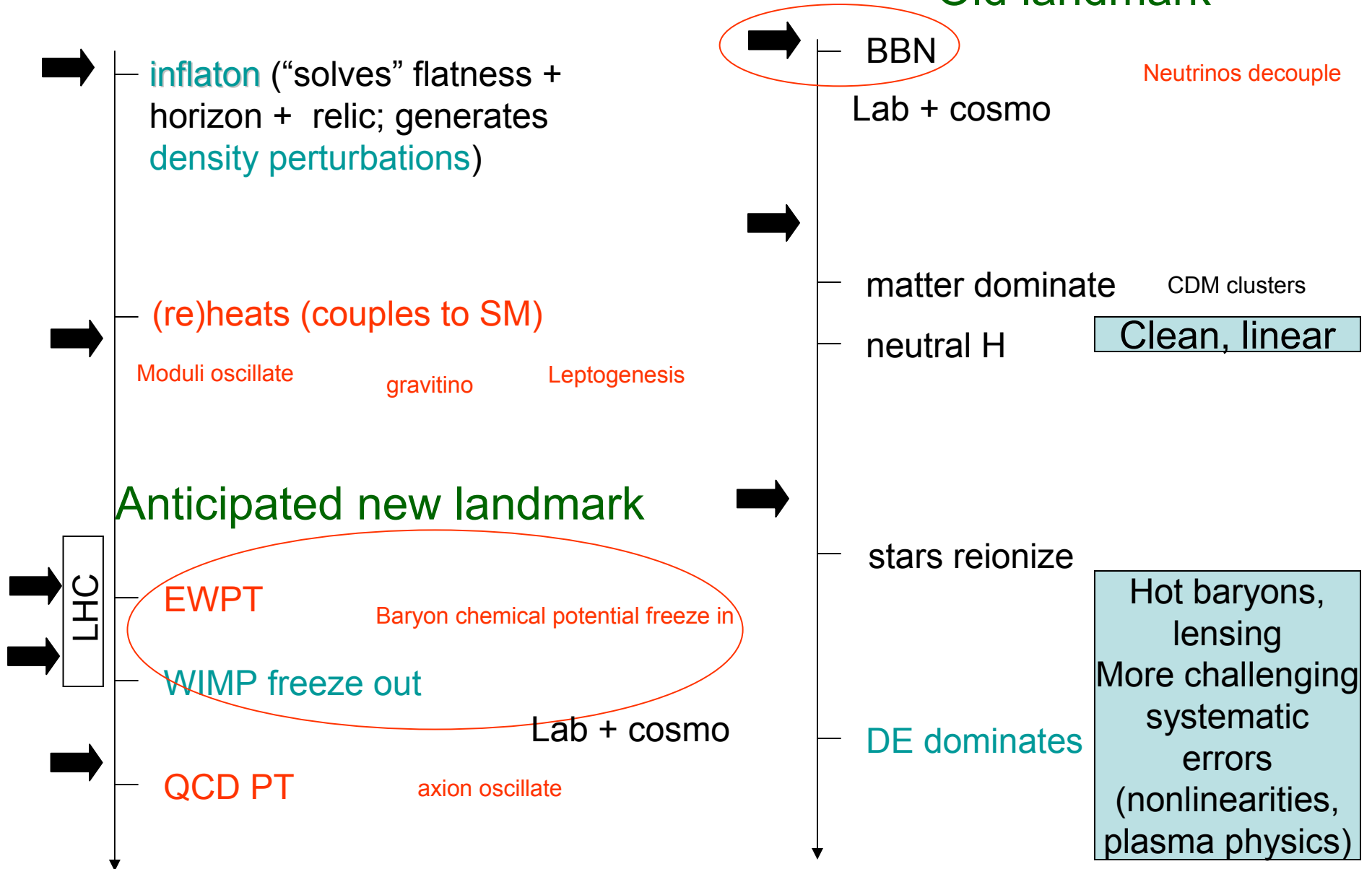
Daniel J. H. Chung

[focus: works with **Andrew Long** (1004.0942)  
& **Peng Zhou** (1003.2462)]

# (Lack of) Rigidity Old landmark



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# Perturbative Scalar EWSB as Universe Cools

UV sensitivity of scalar field + symmetry commuting with KMS

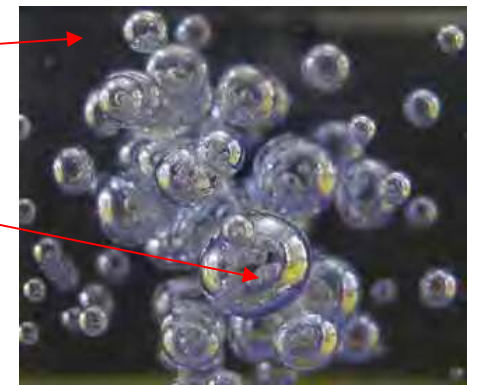
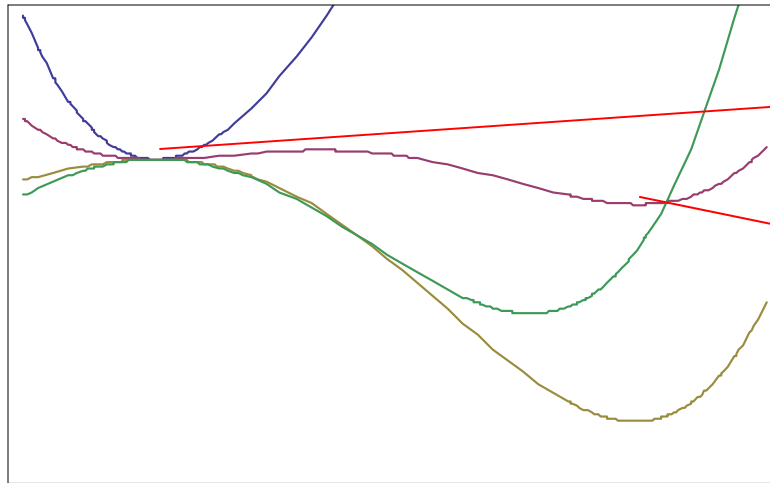
$$\longrightarrow c_{1i}\Lambda^2\phi_i + c_{2i}\Lambda^2\phi_i^2$$

$$\longrightarrow c'_{1i}T^2\phi_i + c'_{2i}T^2\phi_i^2$$

$SU(2)_L \otimes U(1)_Y$  if Higgs

EW symmetry restoration at high temperature. Broken at low temperature.

[Kirzhnits, Linde 72]



# Implications?

- **Electroweak Baryogenesis:** Bubble plasma dynamics
  - Good: Overconstraint possible
  - Bad: 1 number, mild tuning of parameters
- **Leptogenesis: B-L to B conversion**
  - Good: Connection to a lot of “natural” UV physics
  - Bad: Overconstraint unlikely
- **Gravity Waves:** Bubble stirs up fluid
  - Good: Overconstraint possible
  - Bad: Measurability is uncertain
- **DM: Freeze out physics can be affected**
  - Good: Overconstraint possible
  - Bad: narrow parametric window
- **CC: IR contribution**
  - Good: Overconstraint possible
  - Bad: narrow parametric window, and dependence on multiple discoveries

new analysis w/  
Long, Tulin, and Wang  
In progress
- **Clustering: too small scale and effects easily washed out**

# Electroweak Baryogenesis in $\mu\nu$ SSM

$\mu\nu$ SSM Use the N field of NMSSM as a right handed neutrino [Lopez-Fogliani, Munoz 05]

$$\mathbb{Z}_3 \longrightarrow Y_\nu^i \hat{L}_i \cdot \hat{H}_2 \hat{\nu}_i^c - \lambda \hat{H}_1 \cdot \hat{H}_2 \hat{\nu}_i^c + \frac{1}{3} \kappa (\hat{\nu}_i^c)^3 \quad \text{in } W$$

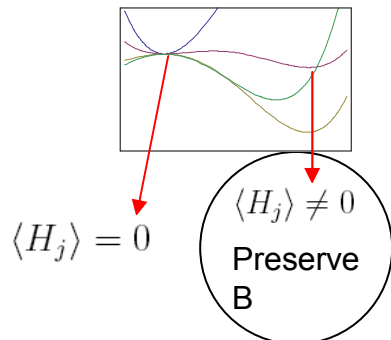
Multiple singlets

“mu” term  
electroweak scale

low scale see-saw

standard thermal leptogenesis scenario is not an option.

Question: Is electroweak baryogenesis possible? [Kuzmin, Rubakov, Shaposhnikov 85]



$$\sqrt{2} \frac{v(T_c)}{T_c} \gtrsim 1.3$$

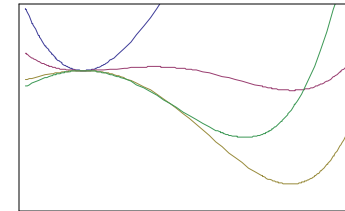
Partial answer: There are parameter regions giving strongly 1st order PT.

# Not too large, not too small

$$V_T(\phi) \approx \left(\frac{1}{2}M^2 + c_1 T^2\right)\phi^2 - E_{\text{eff}}\phi^3 + F_{\text{na}}(\phi, T) + \frac{\lambda_{\text{eff}}}{4}\phi^4$$

$$0 \leq \frac{E_{\text{eff}}}{\lambda_{\text{eff}}\phi(0)} \leq \frac{1}{2}$$

174 GeV



Like NMSSM

$$\sum_i^3 \left[ -a_\lambda H_1 H_2 \tilde{\nu}_i^c + \frac{1}{3} a_\kappa (\tilde{\nu}_i^c)^3 + \text{h.c.} \right]$$

$W$  + D-terms  $\rightarrow$  Higgs mass dependence

$$Y_\nu \approx 6 \times 10^{-7} \left( \frac{\sin[\beta]}{\sin[\arctan 2.6]} \right)^{-1} \text{ is unimportant for this.}$$

$\frac{1}{2}$  marks the point when  $\frac{v(T_c)}{T_c} \rightarrow \infty$

However, phase transition parametric search can be different than NMSSM because of rotation in singlet vector space during PT.

# Example of a Transition Different from NMSSM

At high T

$$H_i = 0 \quad + \quad \text{all nonsinglet scalars vanish.} \quad \text{e.g. } -a_\lambda H_1 \cdot H_2 \tilde{\nu}_i^c$$

Freeze these scalars and consider tree level:  $\mathbb{Z}_3 \longrightarrow \mathbb{Z}_3 \otimes \mathbb{Z}_3 \otimes \mathbb{Z}_3$

$$\tilde{\nu}_j^c \longrightarrow e^{in_j 2\pi/3} \tilde{\nu}_j^c$$

When T is lowered, degenerate minima forms

$$\longrightarrow \text{coset rep of } \mathbb{Z}_3 \otimes \mathbb{Z}_3 \otimes \mathbb{Z}_3$$

Since an artifact of freezing by hand and omitting field fluctuations, loop corrections break the degeneracy.

$\longrightarrow$  Intermediate T singlet minimum energy is sensitive to radiative corrections!

From one of these minima, EWPT occurs.

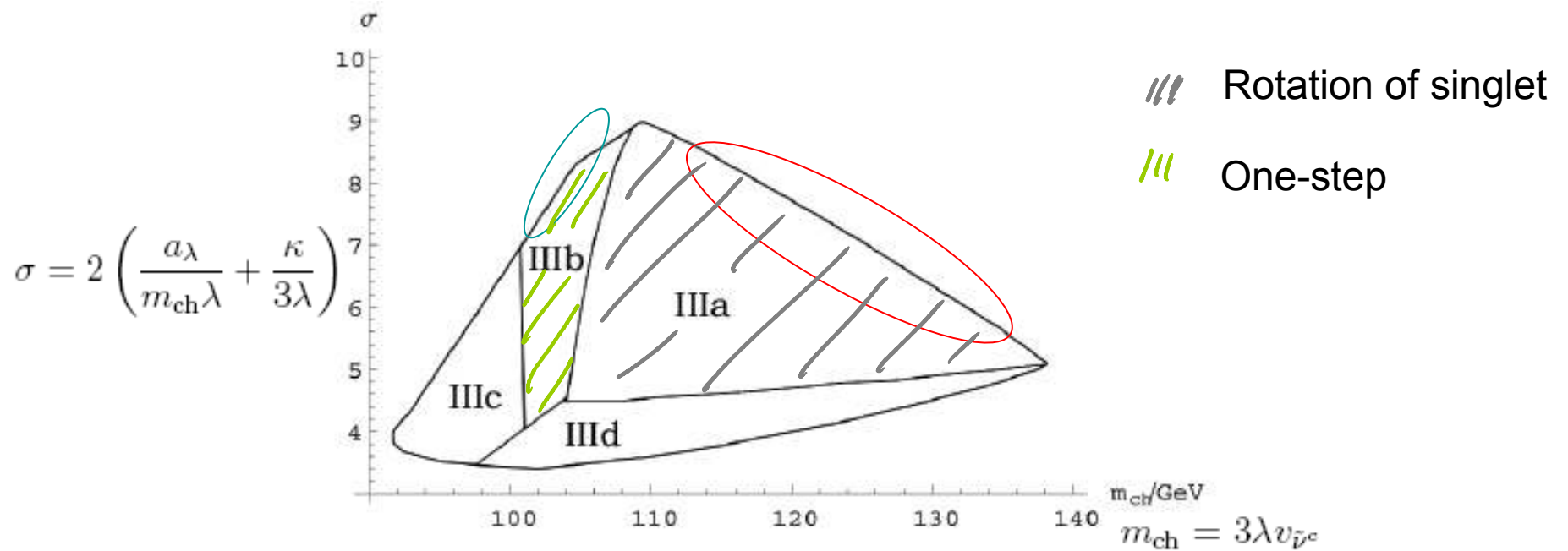
Tuning to achieve  $\frac{E_{\text{eff}}}{\lambda_{\text{eff}} \phi(0)} \approx \frac{1}{2} \longrightarrow$  Sensitive to radiative corrections.

$$a_\lambda H_1 \cdot H_2 \tilde{\nu}_i^c \quad \text{and} \quad -m_{\tilde{\nu}^c}^2 |\tilde{\nu}_i^c|^2 \quad \text{become important}$$



$$a_\lambda H_1 \cdot H_2 \tilde{\nu}_i^c \in \mathcal{L}_s$$

$$-\lambda H_1 \cdot H_2 \nu_i^c + \frac{1}{3} \kappa (\nu_i^c)^3 \in W$$



[1004.0942 w/ [Andrew Long](#)]

Interesting: tuning has a group theoretic origin.

# Gravity Wave at EWPT

[Steinhardt, Witten, Kosowsky, Turner, Watkins, Kamionkowski, Apreeda, Maggiore, Nicolis, Riotto, Caprini, Durrer, Servant, Grojean, Huber, Konstandin, Ashoorion,...]

Following arguments of 0711.2593 and astro-ph/9310044:

$$\rho_{GW} \sim \frac{1}{M_p^2} \left(\frac{a_{PT}}{a}\right)^4 \left\langle \frac{d}{dt} \left(\frac{1}{\square} T_{ij}\right) \frac{d}{dt} \left(\frac{1}{\square} T_{ij}\right) \right\rangle|_{PT}$$

$$\left\langle \tilde{T}_{ij}(t'_1, \vec{k}_1) \tilde{T}_{ij}^*(t'_2, \vec{k}_2) \right\rangle = (2\pi)^3 \delta^{(3)}(\vec{k}_1 - \vec{k}_2) P(k_1, t'_1, t'_2) \left[ \rho_f^{\text{rest}} \gamma_{v_f}^2 v_f^2 \right]^2 a_*^2$$

Observe:

assumption

bubble wall spatial distribution/deformations

$[M]^0$

$$F_{k\Delta t}((t'_1 - t_*)/\Delta t, (t'_2 - t_*)/\Delta t) \equiv k^3 P(k, t'_1, t'_2)$$

assumption of leading conformal symmetry breaking scale.

i.e.  $\Lambda/\Delta t$  related quantities are suppressed in the relevant k range

$$\frac{d\rho_{GW}}{d \ln k} \sim \frac{(\Delta t)^2}{M_p^2} \left(\frac{a_*}{a}\right)^4 \left[ \rho_f^{\text{rest}} \gamma_{v_f}^2 v_f^2 \right]^2 \int dq'_1 dq'_2 \cos [k\Delta t(q'_1 - q'_2)] F_{k\Delta t}(q'_1, q'_2)$$

propagation

Since  $\Delta t \propto H_*^{-1}$ ,  $H_*$  sensitivity can be read off.

$$H^2 = \frac{\rho_R + \rho_{\text{hidden}}}{3M_p^2}$$

$$\xi \equiv \frac{H(T_*)}{H^{(U)}(T_*)}$$

$$\frac{d\rho_{GW}(k)}{d \ln k} \rightarrow \frac{1}{\xi^2} \frac{d\rho_{GW}(k/\xi)}{d \ln k} \quad [1003.2462 \text{ w/ Peng Zhou}]$$

Because of the large  $k$  separation between peak  $k$  scales relevant for GW measurement

$$\Delta t \sim 10^{12} \text{ GeV}^{-1}$$

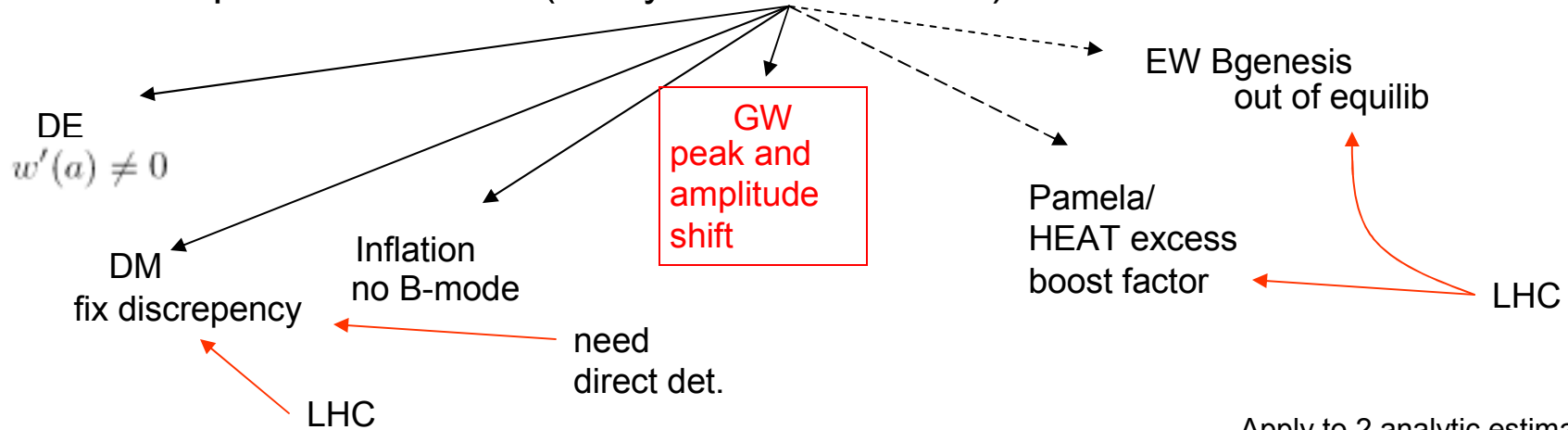
and short distance  $(gT_*)^{-1} \sim 0.1 \text{ GeV}^{-1}$  physics scales,  
**robust and insensitive to computational uncertainties.**

Can still suffer from non-standard cosmological dependence.  
e.g. late time entropy dilution.

# Application: Quintessence BC with kinetic energy dominance

[Barrow, Kamionkowski, Turner, Salati, Rosati, Profumo, Ullio, Pallis, Everett, Matchev, ...]

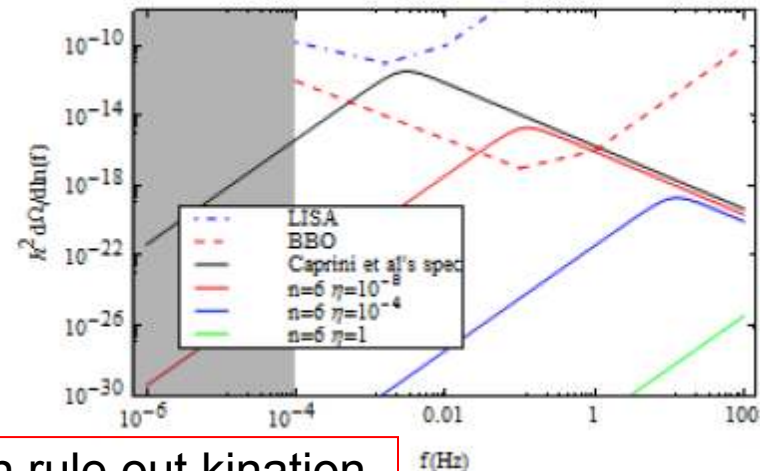
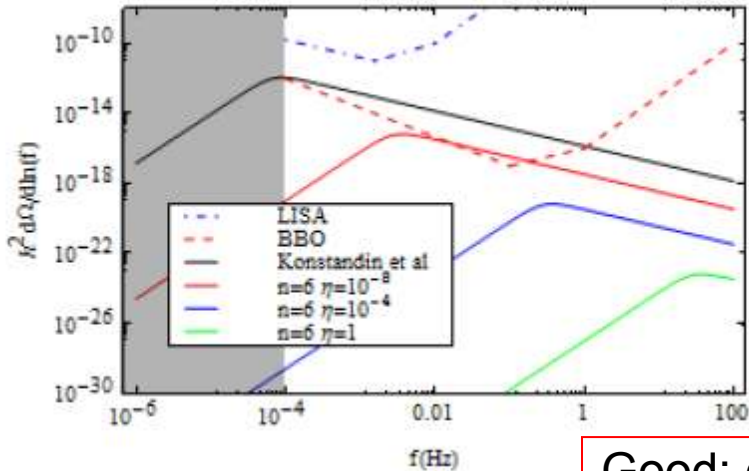
1-parameter class (many functional forms) can be overconstrained



Apply to 2 analytic estimates:  
Huber, Konstandin 08;  
Caprini, Durrer, Servant 07

Optimistic example,

$$\frac{V(\vec{\phi}_i) - V(\vec{\phi}_f)}{\rho_{\text{rad}}} = 0.2 \quad v_b = 0.82$$



[1003.2462 w/ Peng Zhou]

Good: can rule out kination  
Bad: may be negative signal

# Summary

- Measuring the scalar sector sufficiently accurately → BBN of the new century
- $\mu\nu$ SSM satisfies the 1<sup>st</sup> order PT requirement for electroweak baryogenesis.
  - Singlet vector rotation during PT is different from NMSSM.
  - T=0 radiative corrections are Important.
- Gravity waves from EW scale PT is a robust probe of the decoupled (from SM) energy contribution to that era.

$$\frac{d\rho_{GW}(k)}{d\ln k} \rightarrow \frac{1}{\xi^2} \frac{d\rho_{GW}(k/\xi)}{d\ln k}$$

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- Some overview references
  - [hep-ph/0609145](#)
  - [hep-ph/0312378](#)
  - [hep-ph/0303065](#)
  - [hep-ph/0208043](#)
  - [hep-ph/0006119](#)
  - [hep-ph/9901362](#)
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