

# Generating Fermion Masses in Emergent EWSB

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# What is the origin of mass?

## I. Higgs mechanism

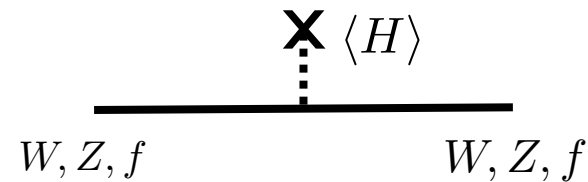
[Guralnik, Hagen, Kibble '64; Englert, Brout '64; Higgs '64]

Higgs boson:  $\langle H \rangle$  vacuum expectation value

- Elementary fermion and W, Z boson masses

W, Z-boson:  $m_{W,Z} \propto g \langle H \rangle$

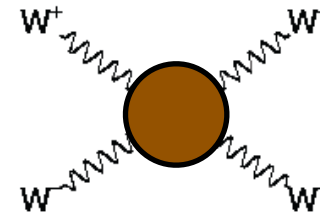
Fermion:  $m_f \propto \lambda \langle H \rangle$



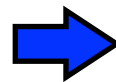
- WW scattering

Bad high-energy behaviour

$$\mathcal{A}(E) \stackrel{E \rightarrow \infty}{\sim} \frac{g^2 E^2}{32\pi m_W^2}$$



But, spin-0 Higgs boson



$$\mathcal{A}(E) \stackrel{E \rightarrow \infty}{\sim} \text{constant}$$

## 2. Strong dynamics

**e.g. QCD:** strong coupling at  $\Lambda_{QCD} = e^{-\frac{8\pi^2}{g^2 b_i}} M_P$

- Hadron mass spectrum

proton:  $m_P \propto \Lambda_{QCD}$

vector-mesons:

e.g. SU(2) isospin-triplet  $\rho^{0,\pm}$   $m_\rho \propto \Lambda_{QCD}$

isospin SU(2)  $\rightarrow$  global symmetry

- No unitarity violation



chiral Lagrangian  $\rightarrow$  QCD Lagrangian

Higgs boson not yet seen...maybe soon...  
...or are there surprises in store?

*Question:*

**Can one generate mass in the Standard Model without the Higgs mechanism?**

*Early work:*

Bjorken, 1977; Hung, Sakurai 1978

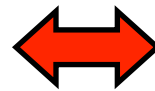
Abbot, Farhi 1981; Fritzsche, Schildknecht, Kogerler, 1982

Model building limited due to nonperturbative nature

## New approach:

Use AdS/CFT correspondence! [Maldacena, 97; Gubser, Klebanov, Polyakov, 98; Witten 98]

Effective 4D chiral  
Lagrangian of massive  
W, Z, fermions



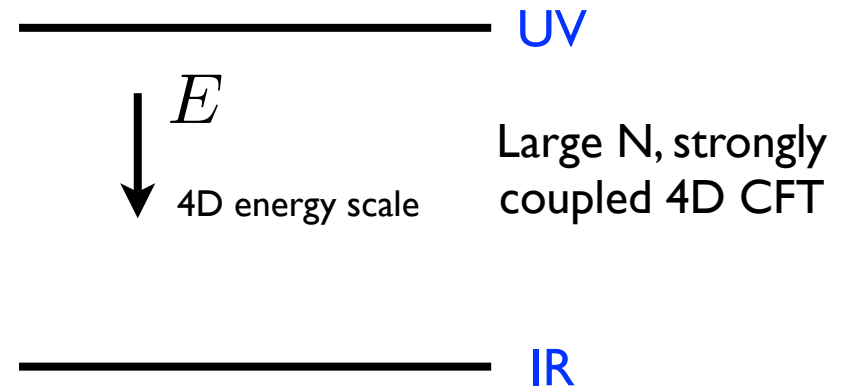
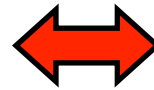
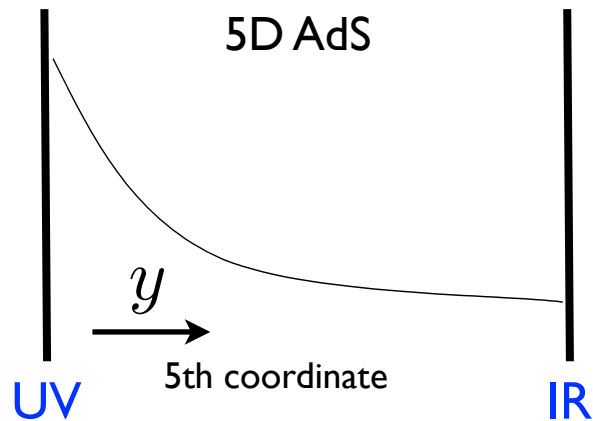
5D Lagrangian in  
warped dimension!  
[Randall, Sundrum 99]

## Challenges:

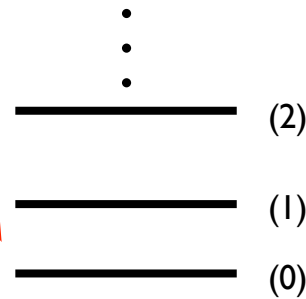
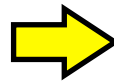
- Generate fermion and W, Z boson masses
- Universality of gauge couplings
- Consistent with EW precision tests
- Natural, no fine tuning.....

# AdS/CFT dictionary

[Arkani-Hamed, Randall, Porrati 00; Rattazzi, Zaffaroni 00; Perez-Victoria 01]



IR brane breaks conformal symmetry

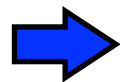
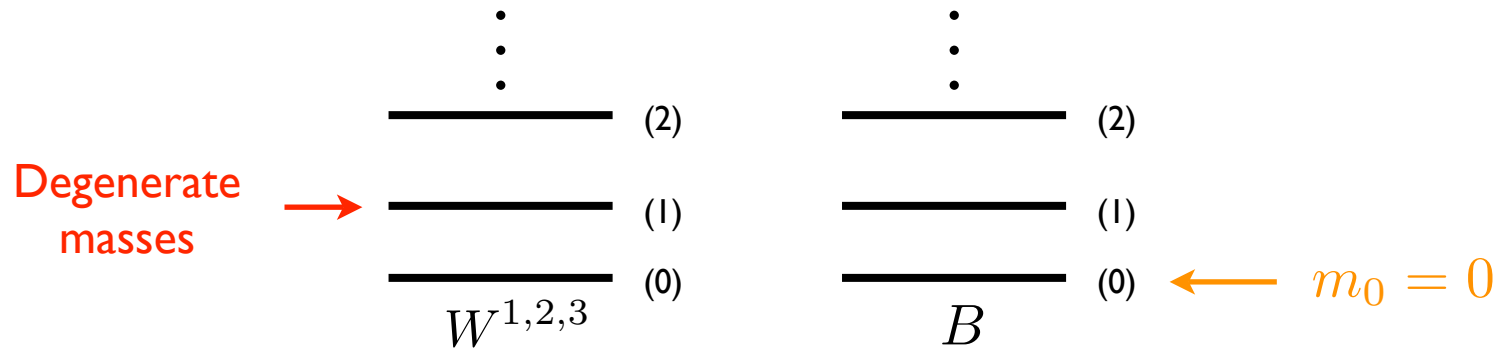


} Generates mass!

KK modes OR composite states of dual theory!

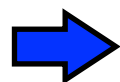
# But,

- Massless mode



Break EW symmetry at Planck scale  
to decouple massless modes!

- Heavy KK modes

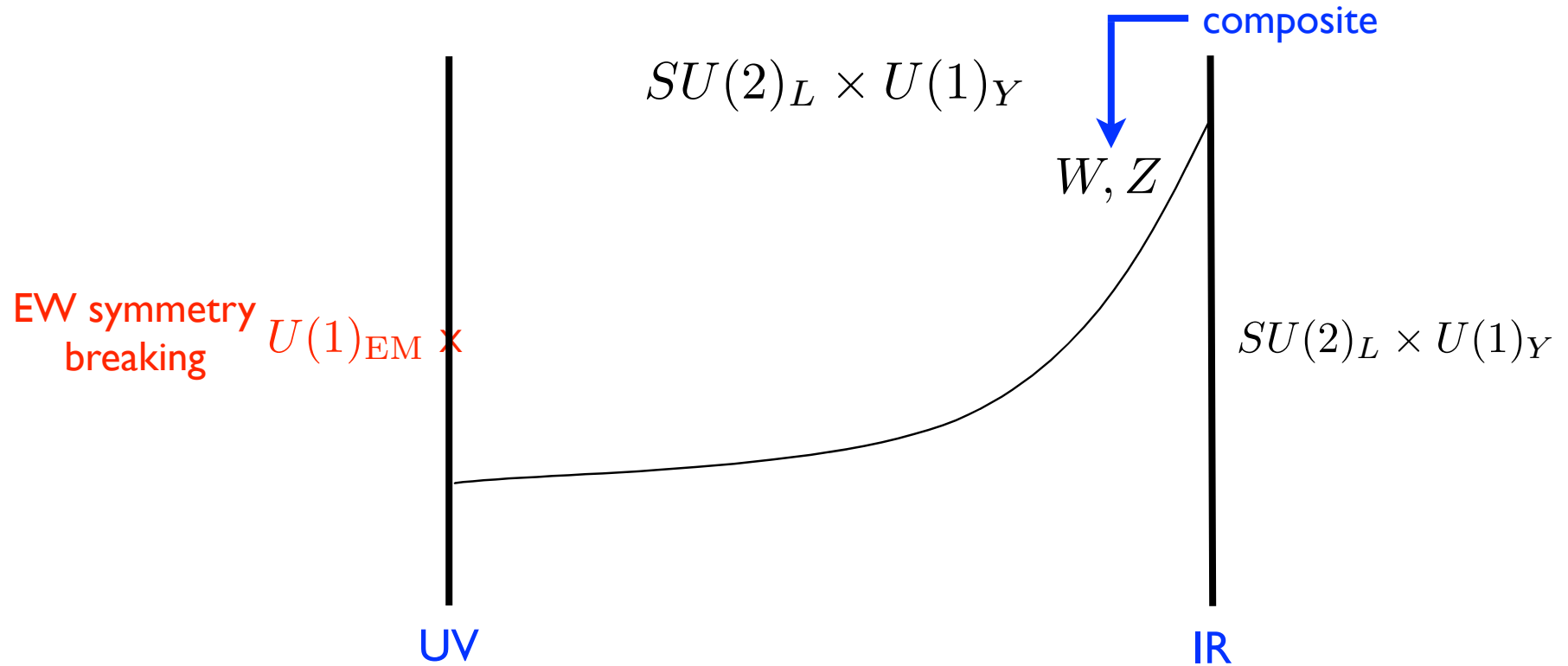


Separate lightest KK mode from rest of tower  
with brane kinetic terms!

[Carena, Ponton, Tait, Wagner 2002; Davoudiasl, Hewett, Rizzo 2002]

# 5D Model

[Cui, TG, Wells, arXiv:0907.0906]



5D action:

$$S = \int d^4x dz \sqrt{-g} \left[ -\frac{1}{4}(F_{MN}^{La})^2 - \frac{1}{4}(F_{MN}^Y)^2 - \frac{1}{2}(kz)\delta(z - z_{UV}) \frac{\zeta_Q}{g_{Y5}^2 + g_{L5}^2} (g_{Y5} F_{\mu\nu}^{L3} + g_{L5} F_{\mu\nu}^Y)^2 - \frac{1}{2}(kz)\delta(z - z_{IR}) (\zeta_L (F_{\mu\nu}^{La})^2 + \zeta_Y (F_{\mu\nu}^Y)^2) \right]$$

$\zeta_Q, \zeta_L, \zeta_Y$  = boundary kinetic term coefficients



# Mass spectrum:

Boundary  
conditions:

$$z = z_{UV} : \begin{cases} \partial_z (g_{Y5} A_\mu^{L3} + g_{L5} B_\mu) + \zeta_Q \square (g_{Y5} A_\mu^{L3} + g_{L5} B_\mu) = 0, \\ g_{L5} A_\mu^{L3} - g_{Y5} B_\mu = 0, \\ A_\mu^{L1,2} = 0, \end{cases}$$
$$z = z_{IR} : \begin{cases} \partial_z A_\mu^{La} - \zeta_L k z_{IR} \square A_\mu^{La} = 0, \\ \partial_z B_\mu - \zeta_Y k z_{IR} \square B_\mu = 0, \end{cases}$$

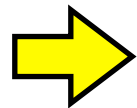
Obtain:

$$m_\gamma = 0$$

$$m_W \simeq \sqrt{\frac{2}{\zeta_L k}} m_{IR}$$

$$m_Z \simeq \sqrt{\frac{2}{\zeta_L k} + \frac{2}{\zeta_Q k (1 + g_{L5}^2 / g_{Y5}^2)}} m_{IR}$$

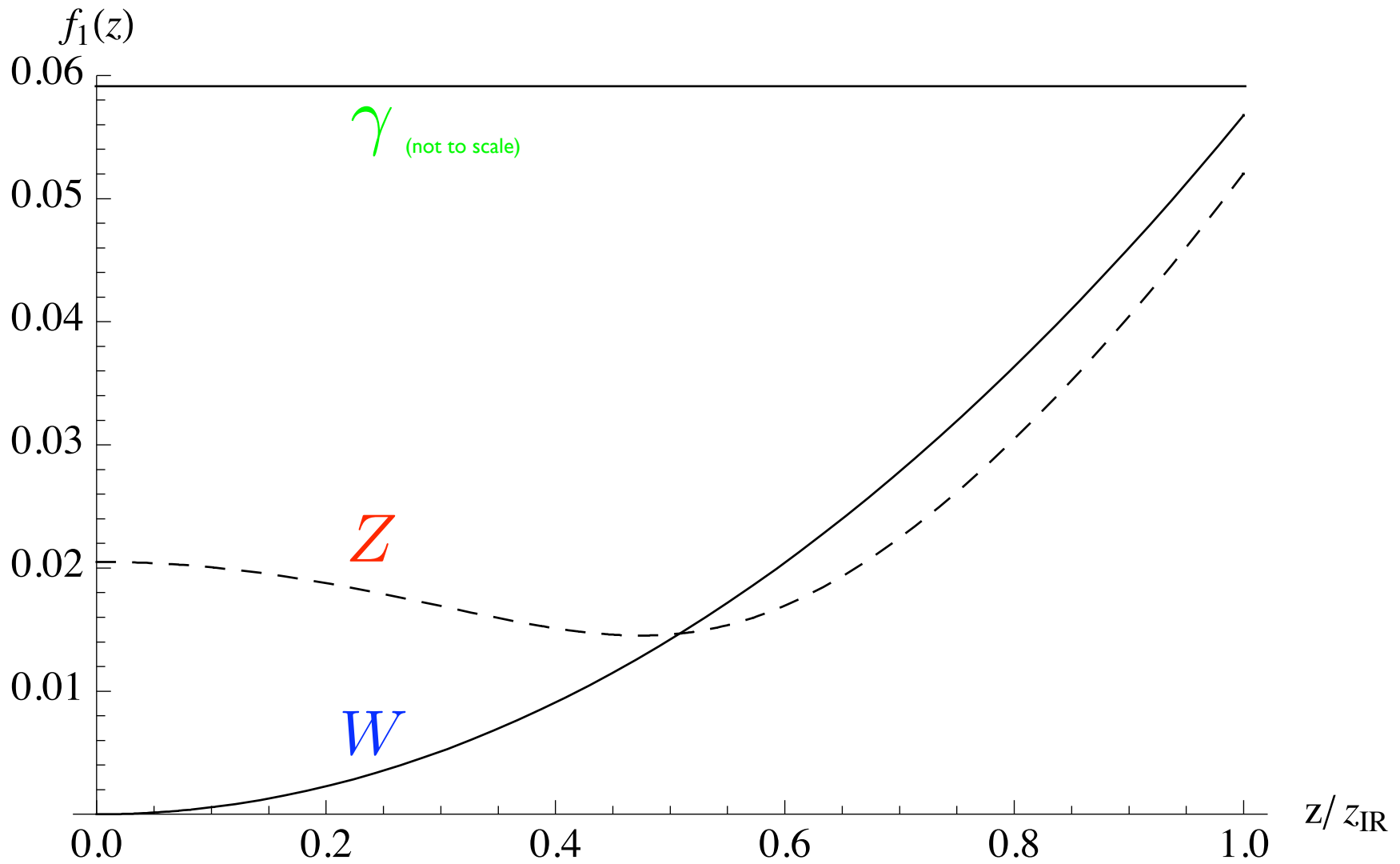
For:  $m_{IR} = \text{TeV}$      $\zeta_Q k \simeq 500$ ,  $\zeta_L k \simeq 310$ ,  $\zeta_Y k \simeq 0.1$



$$m_W \simeq 80.4 \text{ GeV}, \quad m_Z \simeq 91.2 \text{ GeV}$$

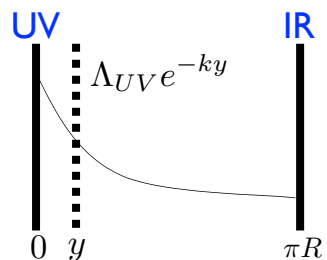
$$(m_{KK} \gtrsim 2 \text{ TeV})$$

# W, Z, photon profiles

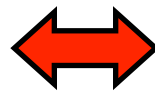


NB: Boundary kinetic terms introduce discontinuity at endpoints.

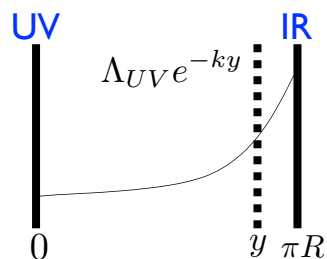
# Dual 4D interpretation



UV localized field



elementary “source” state

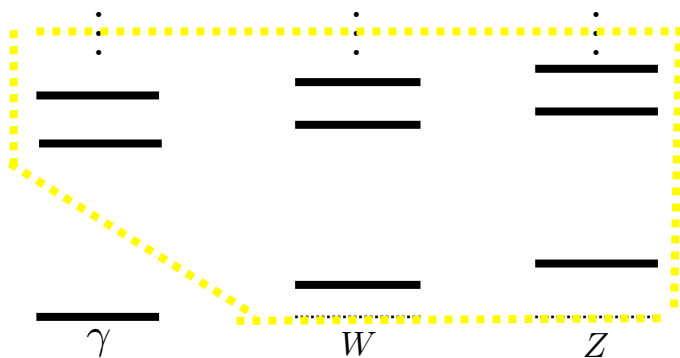


IR localized field

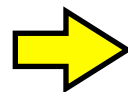


CFT bound state

$\therefore$  Composite W, Z but elementary photon!



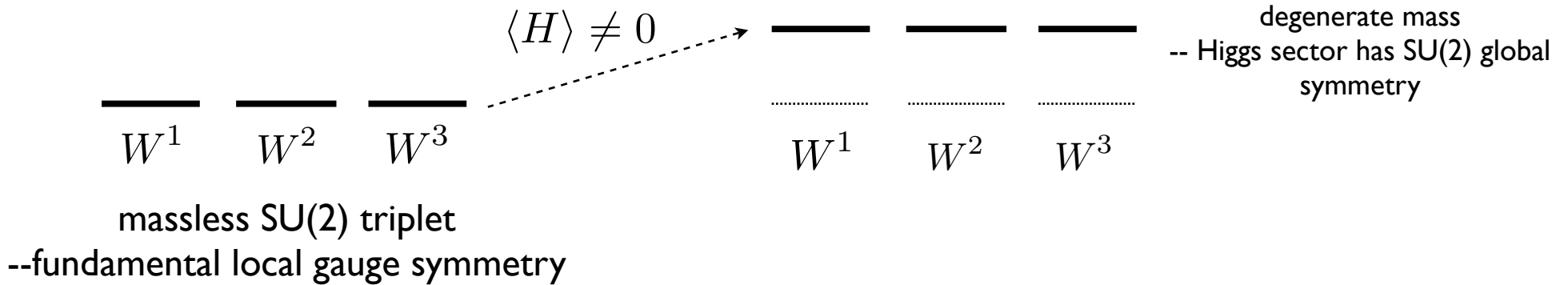
EWSB emerges at IR scale



“Emergent” EWSB

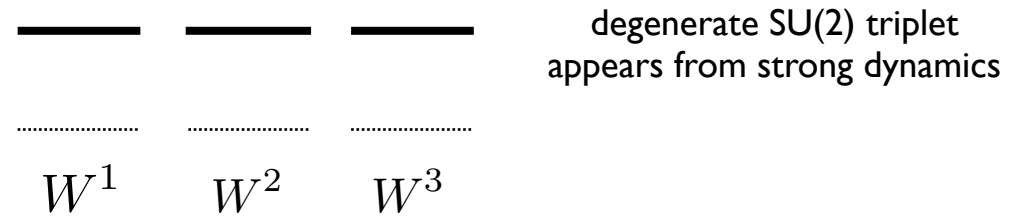
# Custodial Symmetry

- Higgs Mechanism in SM



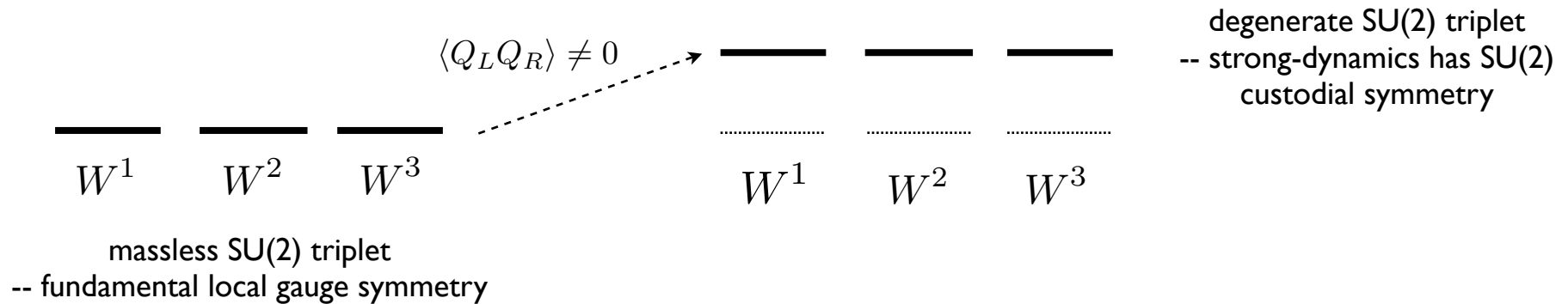
- Emergent EWSB

SU(2) symmetry is  
 NOT fundamental



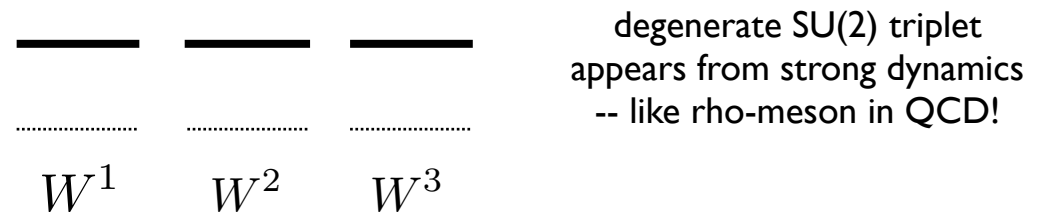
# Emergent EWSB is Higgsless... but no Higgs mechanism!

- Usual “Higgsless” (technicolor-like) [Csaki, Grojean, Pilo, Terning 04]



- Emergent EWSB

No Higgs mechanism



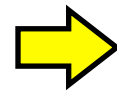
# Electroweak constraints

Assume fermions predominantly on IR brane

- **T parameter**      Custodial symmetry in limit     $\zeta_Y \rightarrow 0, \zeta_Q \rightarrow \infty$   
i.e. same boundary condition for  $A^{L1,2,3}$

- **S parameter**       $S \simeq \frac{8\pi}{g^2 + g'^2} \cos 2\theta_w \sin^2 \theta_w (1 + \beta^2) (m_Z z_{IR})^2$

$$\zeta_{Lk} \simeq 1000, \zeta_{Qk} \simeq 1700, \zeta_{Yk} \simeq 0.2 \\ m_{IR} \simeq 1.8 \text{ TeV}$$



$$S \simeq 0.1, \quad T \simeq 0.02$$

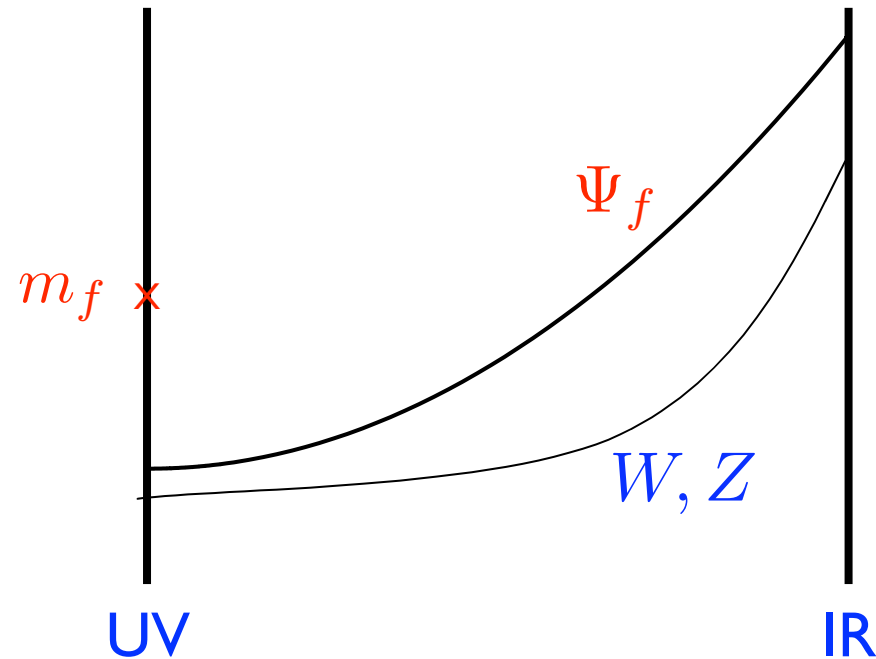
# What about fermion masses?

[Cui, TG, Stokes, to appear]

Assume universal bulk fermion profile

- Add UV boundary fermion masses

Fermion mass hierarchy via Froggatt-Nielsen mechanism



$$S_\psi = i \int d^5x \sqrt{-g} \left[ \frac{1}{2} (\bar{\Psi}_i^{(L)} \Gamma^M D_M \Psi_i^{(L)} - D_M \bar{\Psi}_i^{(L)} \Gamma^M \Psi_i^{(L)}) + \underbrace{m_L^{(i)} \bar{\Psi}_i^{(L)} \Psi_i^{(L)}}_{= ck} + (L \leftrightarrow R) \right]$$

$$S_m^{(UV)} = i \int d^5x \sqrt{-g} \lambda_5^{(i)} \left[ \bar{\Psi}_i^{(L)} \Psi_i^{(R)} + \bar{\Psi}_i^{(R)} \Psi_i^{(L)} \right] (kz) \delta(z - z_{UV})$$

$$S_{KE}^{(IR)} = i \int d^5x \sqrt{-g} \left[ \frac{1}{2} \eta_{iL} (\bar{\Psi}_i^{(L)} \Gamma^\mu D_\mu \Psi_i^{(L)} - D_\mu \bar{\Psi}_i^{(L)} \Gamma^\mu \Psi_i^{(L)}) + (L \leftrightarrow R) \right] (kz) \delta(z - z_{IR})$$

# Example: massless bulk fermions ( $c=0$ )

$$|f_{L-}^{(n)}(z)| = |f_{R+}^{(n)}(z)| = N_n^{(0)} (kz)^2 [\cos(\hat{m}_n - m_n z) - (\eta k) \hat{m}_n \sin(\hat{m}_n - m_n z)]$$

where

$$N_n^{(0)} \simeq \frac{1}{\sqrt{z_{\text{IR}}}} \sqrt{\frac{1}{1 + (\eta k)/2 + (\eta k)^2 \hat{m}_n^2}} \quad \hat{m} = \frac{m}{m_{\text{IR}}}$$

Obtain for ( $\eta k = 10$ )

$$m_e \leq m \leq m_t \quad \text{with} \quad 3.1 \times 10^{-6} \leq \lambda_5 \leq 1.15$$



# W,Z boson couplings

Determined by wavefunction overlap:

e.g. 
$$g_W \simeq \frac{g_{5L}}{\sqrt{\zeta_L}} \frac{2}{\eta k} \left[ \underbrace{\frac{1}{3}}_{\text{universal}} + \xi_{IR} k \underbrace{(1 - 2(\eta k) \hat{m}_i \hat{m}_j)}_{\text{flavor-dependent}} \right]$$

$$\hat{m} = \frac{m}{m_{IR}} \ll 1$$

$$\xi_{IR} = \sqrt{\frac{\zeta_L}{2}} \Lambda \eta$$

➔  $\left\{ \begin{array}{l} \text{Light fermions: nonuniversality at the per-mille level!} \\ \text{3rd generation: nonuniversality at 15\%-25\% level} \end{array} \right.$

$$\frac{g_{W-}(tb)}{g_{W-}(ud)} = 0.854 \quad \frac{g_{Z-}(\text{top})}{g_{Z-}^{(SM)}(\text{top})} = 0.746 \quad \frac{g_{Z+}(\text{top})}{g_{Z+}^{(SM)}(\text{top})} = 0.745$$

Wtb: 20% level @Tevatron arXiv:0903.0850 Single top production

Ztt: 40% level @LHC with 300 fb<sup>-1</sup>

**Gauge coupling universality due to light fermion masses!**

# Anomalous top couplings electroweak corrections

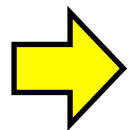
[Larios, Perez, Yuan '99]

Obtain:

$$\epsilon_1^{SM} + \delta\epsilon_1 \simeq 19 \times 10^{-3}; \quad \epsilon_b^{SM} + \delta\epsilon_b \simeq -13 \times 10^{-3}$$

This compares with:

$$\begin{aligned} 4.4 \times 10^{-3} &\leq \epsilon_1^{exp} \leq 6.4 \times 10^{-3}, & 68\% \text{ C.L.} \\ -6.2 \times 10^{-3} &\leq \epsilon_b^{exp} \leq -3.1 \times 10^{-3} & 68\% \text{ C.L.} \end{aligned}$$

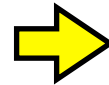


Requires special treatment of top quark

e.g. separate brane for top [Cacciapaglia, Csaki, Grojean, Reece, Terning '05]

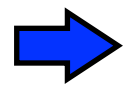
# WW scattering

Composite W,Z boson



Momentum dependent  
form factor

$$F_{WWZ}(q^2) = \frac{1}{N_Z(q^2)N_W^2} \left\{ \left[ \int_{z_{UV}}^{z_{IR}} \frac{dz}{kz} f^{L3}(q^2, z)(f_W(z))^2 \right] + \zeta_L f^{L3}(q^2, z_{IR})(f_W(z_{IR}))^2 \right\}$$



Possible deviation in W, Z-boson vertices at LHC  
(in progress)

Interestingly, in large N theory there  
are no partons inside hadrons!

[Polchinski-Strassler 02]

i.e. composite W, Z bosons are unlike vector-mesons in QCD!

# Summary

- Generate W, Z boson and fermion masses from strong dynamics, not Higgs mechanism
- Electroweak symmetry breaking “emerges” at IR scale
- Composite W, Z bosons lead to deviations in couplings at the LHC
- Requires further model-building to successfully incorporate top quark....