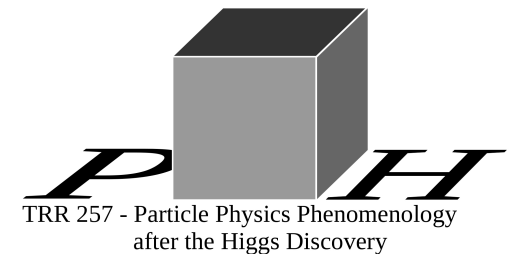


Theory status of top production and decay

M. Czakon

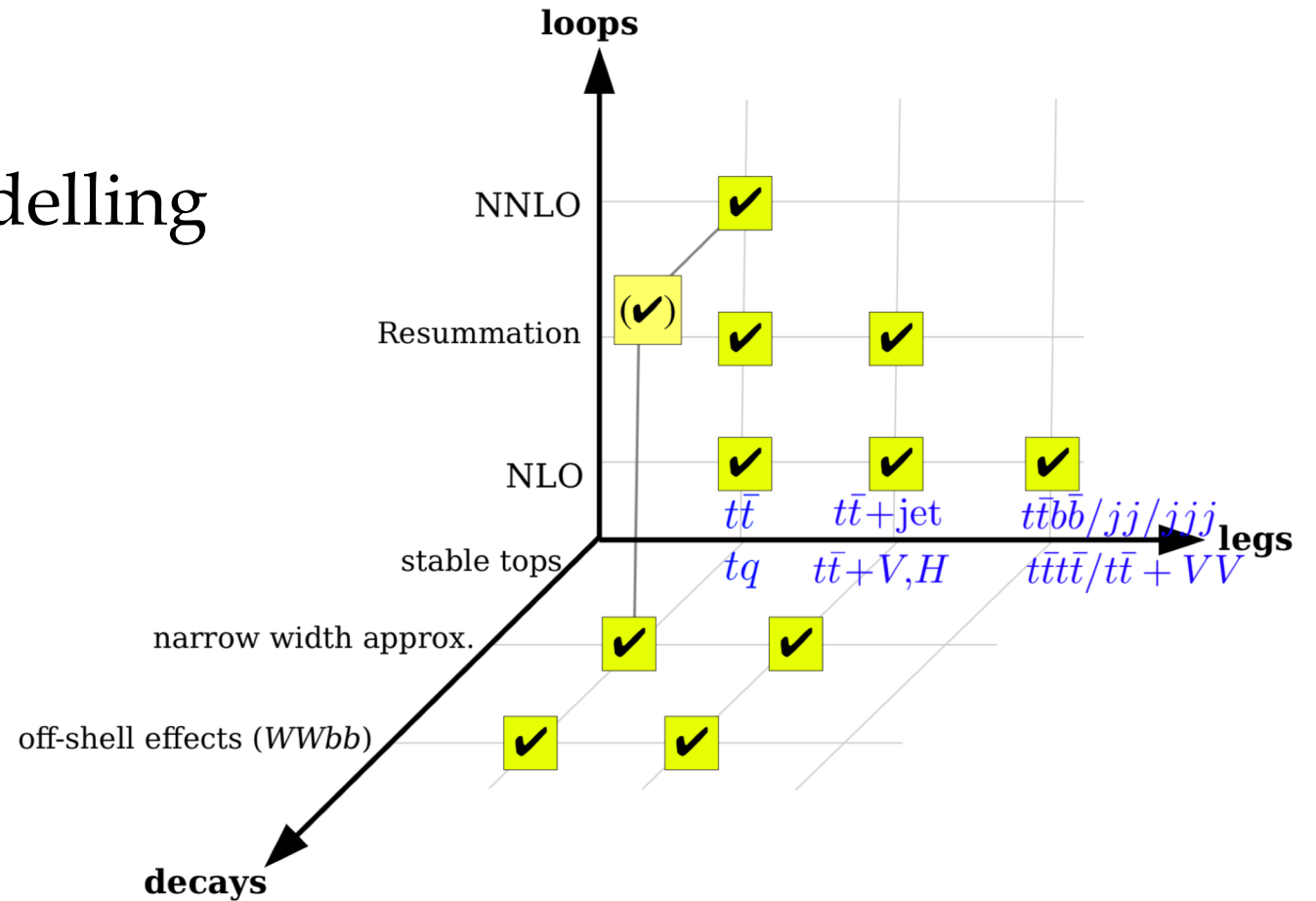
RWTH Aachen University



Plan

1. Precision at high orders
2. Sophisticated decay modelling

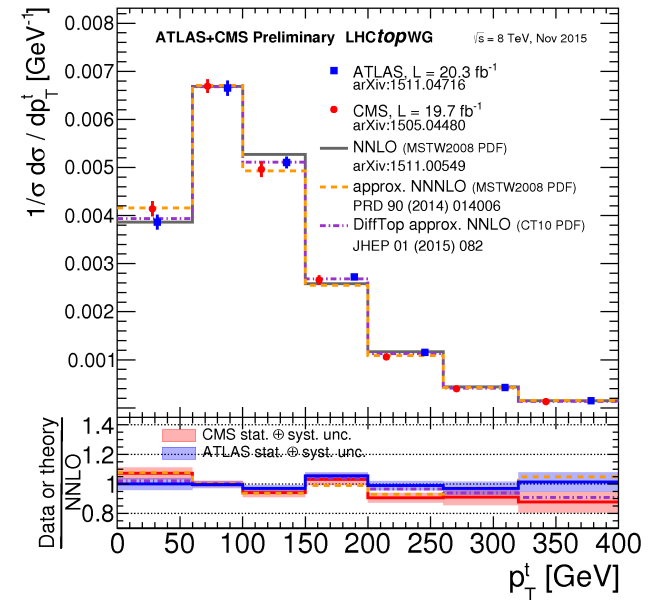
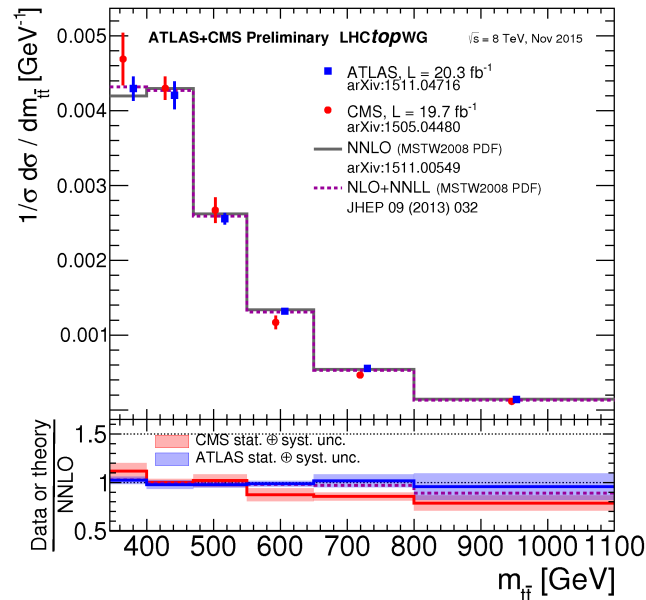
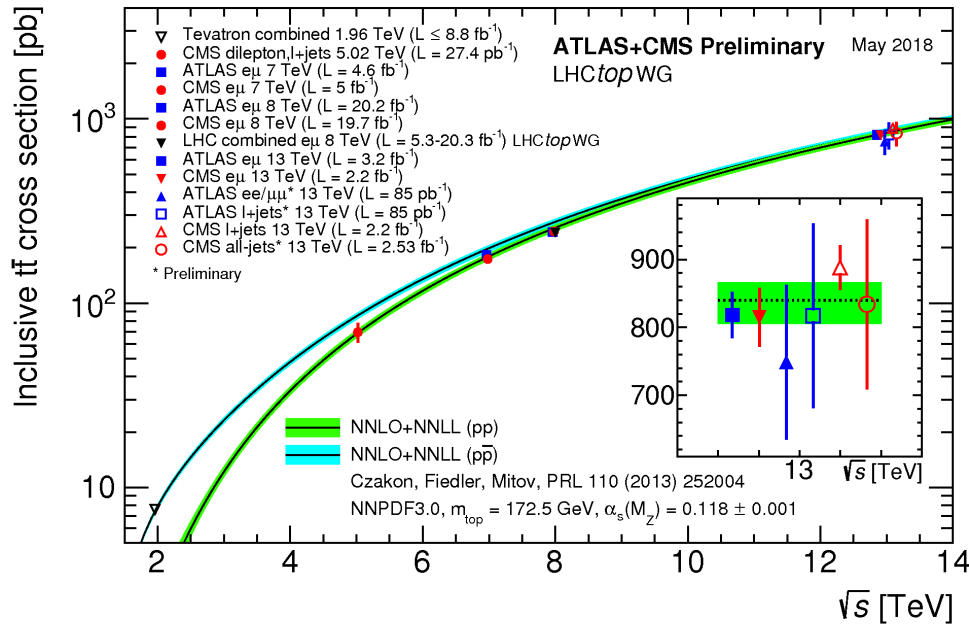
**ONLY TOP QUARK PAIRS
IN THIS TALK**



From M. Schulze, LHCP '18

Total and differential cross sections

- We are well in the hadron collider precision measurement territory !!!
- ... for a few years now



LHC Run 1

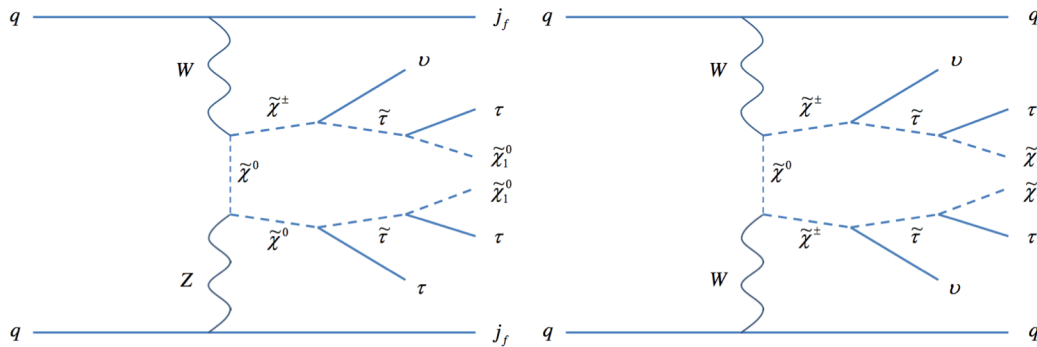
LHC Run 2

	LHC	$\sigma(t\bar{t})$ [pb]	L [fb $^{-1}$]	N_{event}
LHC Run 1	7 TeV	180	5	9×10^5
	8 TeV	256	20	5×10^6
LHC Run 2	13 TeV	835	36	3×10^7

Search for Supersymmetry...

- An example of the importance of top-quark cross sections as background
- Search for supersymmetry in the vector-boson fusion topology in proton-proton collisions

LHC @ 8 TeV

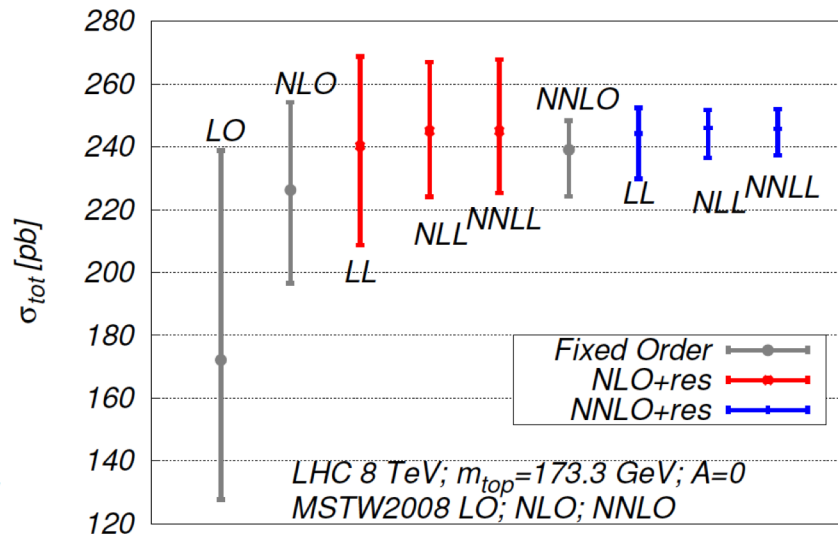
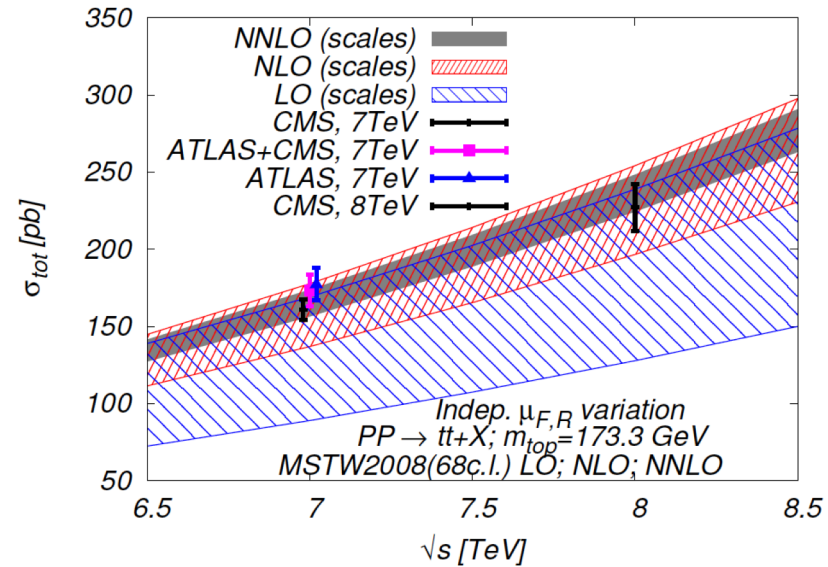
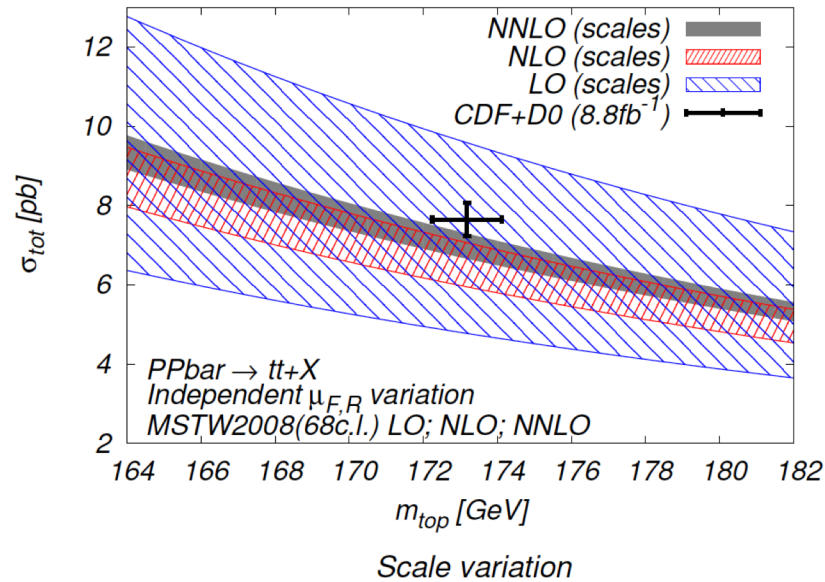


CERN-PH-EP/2015-213
2015/09/01

Process	$\mu^\pm \mu^\mp jj$	$e^\pm \mu^\mp jj$	$\mu^\pm \tau_h^\mp jj$	$\tau_h^\pm \tau_h^\mp jj$
Z+jets	4.3 ± 1.7	$3.7^{+2.1}_{-1.9}$	19.9 ± 2.9	12.3 ± 4.4
W+jets	<0.1	$4.2^{+3.3}_{-2.5}$	17.3 ± 3.0	2.0 ± 1.7
VV	2.8 ± 0.5	3.1 ± 0.7	2.9 ± 0.5	0.5 ± 0.2
t \bar{t}	24.0 ± 1.7	$19.0^{+2.3}_{-2.4}$	11.7 ± 2.8	—
QCD	—	—	—	6.3 ± 1.8
Higgs boson	1.0 ± 0.1	1.1 ± 0.5	—	1.1 ± 0.1
VBF Z	—	—	—	0.7 ± 0.2
Total	32.2 ± 2.4	$31.1^{+4.6}_{-4.1}$	51.8 ± 5.1	22.9 ± 5.1
Observed	31	22	41	31

Precision at high orders

Perturbation theory convergence

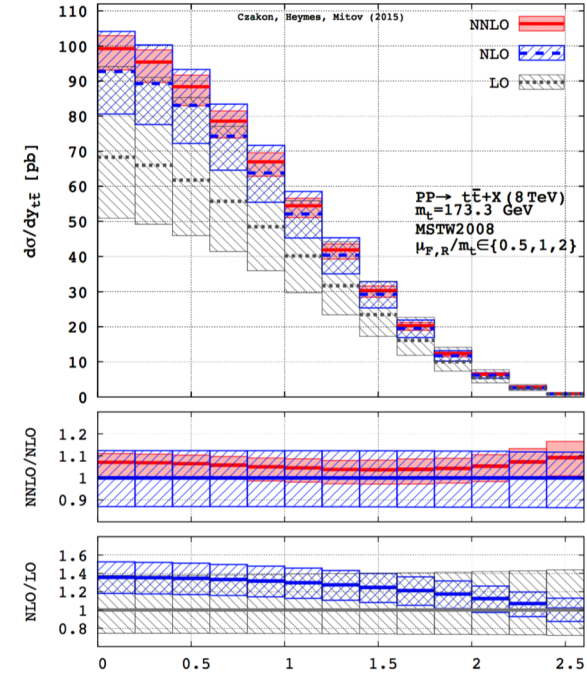
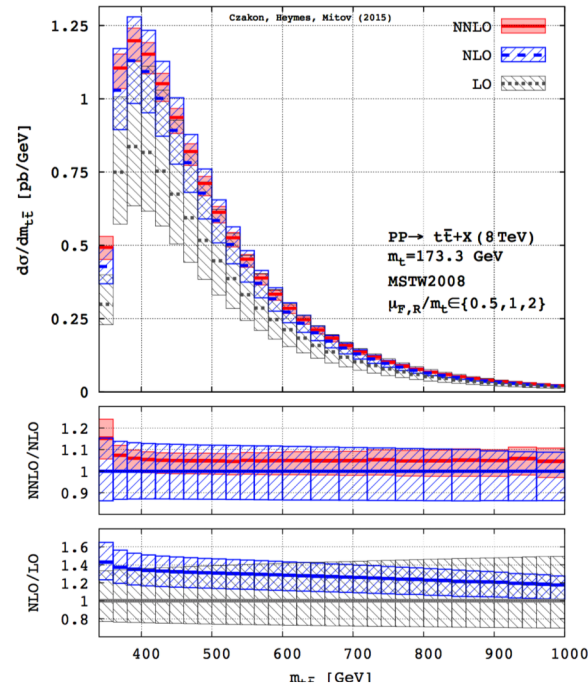
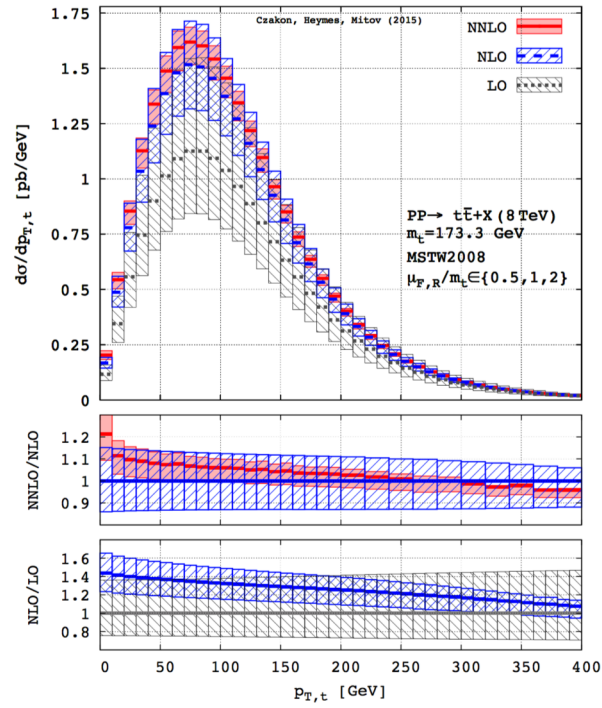


Concurrent uncertainties:

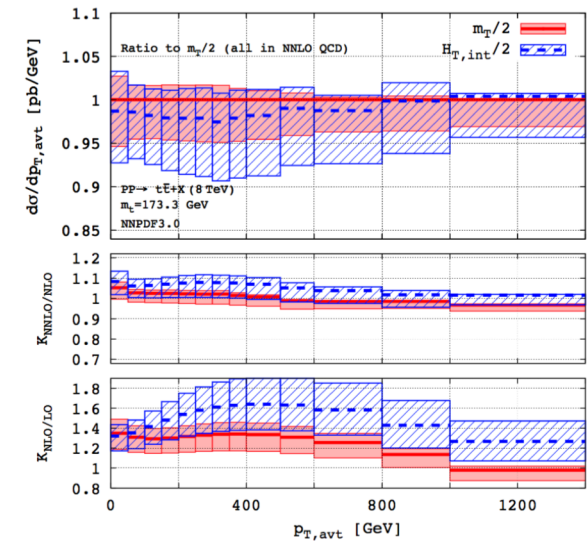
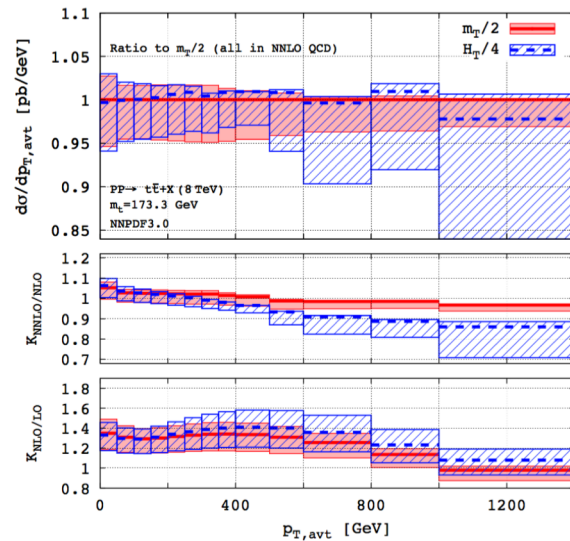
- Scales ~ 3%
- pdf (at 68%cl) ~ 2-3%
- α_S (parametric) ~ 1.5%
- m_{top} (parametric) ~ 3%

Soft gluon resummation makes a difference: **5% \rightarrow 3%**

... for differential distributions



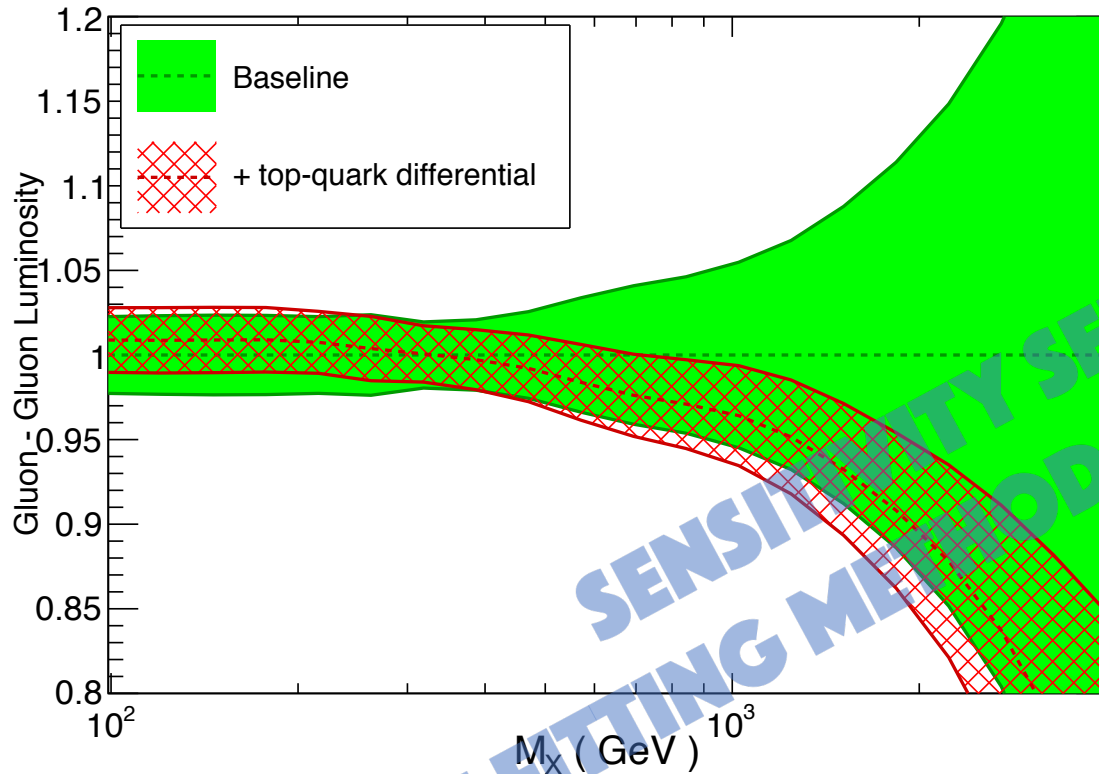
Convergence with fixed and dynamical scales



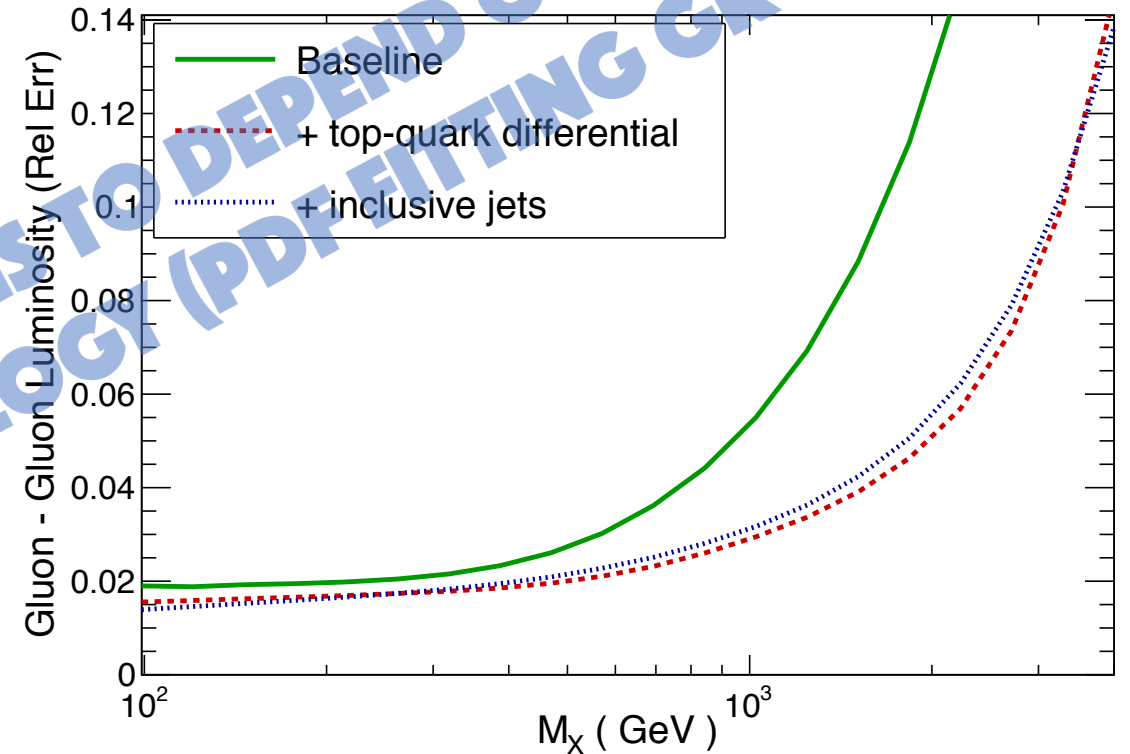
MC, Heymes, Mitov '15 '16

Application: PDF fits

NNLO, global fits, LHC 13 TeV



NNLO, global fits, LHC 13 TeV



MC, Hartland, Mitov, Nocera, Rojo '16

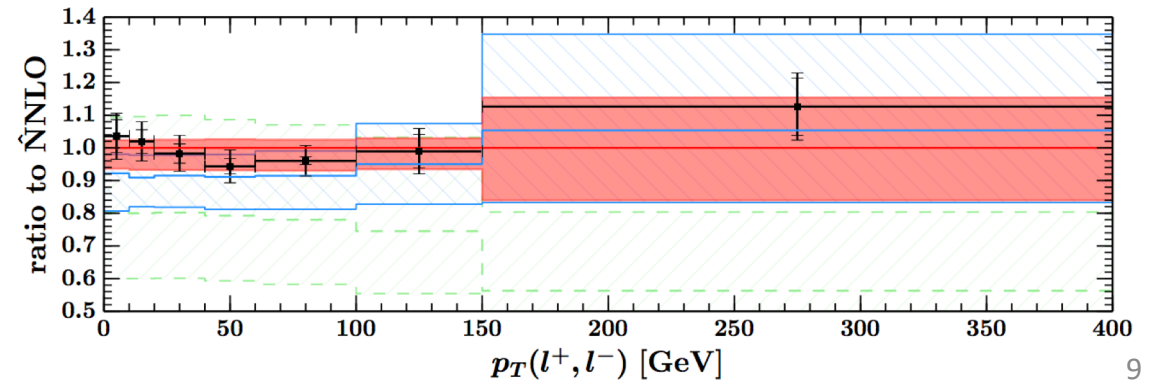
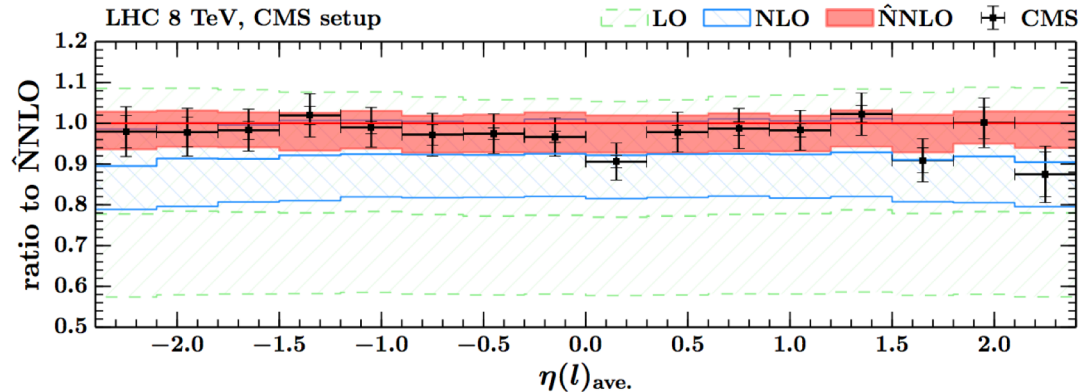
- the normalized y_t distribution from ATLAS at $\sqrt{s} = 8$ TeV (lepton+jets channel),
- the normalized $y_{t\bar{t}}$ distribution from CMS at $\sqrt{s} = 8$ TeV (lepton+jets channel),
- total inclusive cross-sections at $\sqrt{s} = 7, 8$ and 13 TeV (all available data).

First step towards NWA @ NNLO

- Exact matrix elements for everything but the production mechanism at NNLO QCD
Gao, Papanastasiou '17

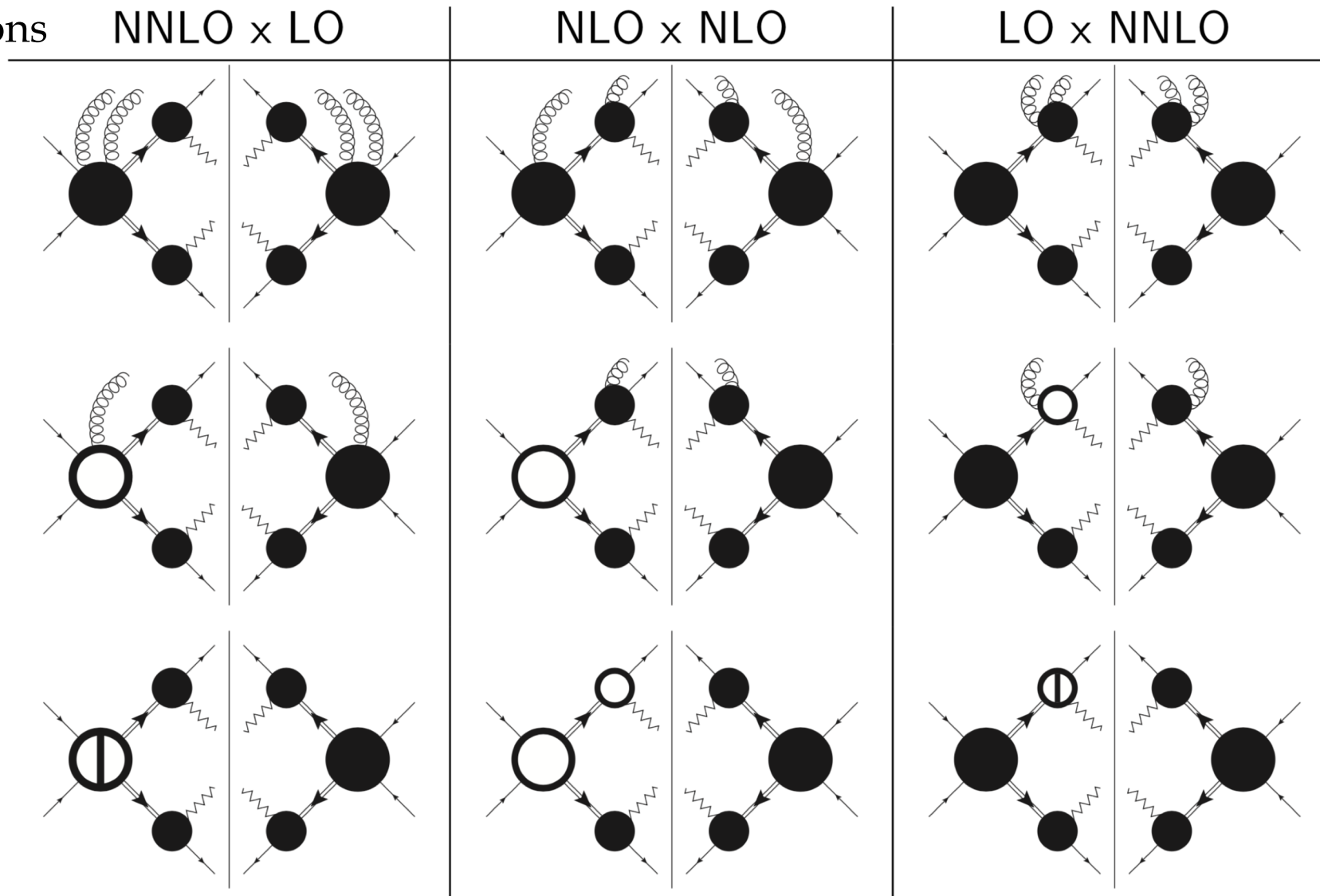
ATLAS setup, $e^\pm\mu^\mp$ channel [24]						
energy	fiducial volume	LO [pb]	NLO [pb]	\hat{N} NLO [pb]	$\delta_{\text{dec.}}$	ATLAS [pb]
7 TeV	$p_T(l^\pm) > 25$ GeV, $ \eta(l^\pm) < 2.5$	$1.592^{+39.2\%}_{-26.0\%}$	$2.007^{+11.9\%}_{-13.2\%}$	$2.210^{+2.2\%}_{-6.0\%}$	-0.3%	$2.305^{+3.8\%}_{-3.8\%}$
7 TeV	$p_T(l^\pm) > 30$ GeV, $ \eta(l^\pm) < 2.4$	$1.265^{+39.3\%}_{-26.1\%}$	$1.585^{+11.8\%}_{-13.1\%}$	$1.736^{+2.2\%}_{-6.0\%}$	-0.8%	$1.817^{+3.8\%}_{-3.8\%}$
8 TeV	$p_T(l^\pm) > 25$ GeV, $ \eta(l^\pm) < 2.5$	$2.249^{+37.9\%}_{-25.5\%}$	$2.855^{+11.9\%}_{-12.9\%}$	$3.130^{+2.3\%}_{-6.0\%}$	-0.3%	$3.036^{+4.1\%}_{-4.1\%}$
8 TeV	$p_T(l^\pm) > 30$ GeV, $ \eta(l^\pm) < 2.4$	$1.788^{+38.0\%}_{-25.5\%}$	$2.256^{+11.7\%}_{-12.9\%}$	$2.461^{+2.3\%}_{-6.1\%}$	-0.7%	$2.380^{+4.1\%}_{-4.1\%}$

CMS setup, $e^\pm\mu^\mp, e^+e^-, \mu^+\mu^-$ channel [25], 2 b -jets required (anti- k_t algorithm [66], $R = 0.5$)						
energy	fiducial volume	LO [pb]	NLO [pb]	\hat{N} NLO [pb]	$\delta_{\text{dec.}}$	CMS [pb]
8 TeV	$p_T(l^\pm) > 20$ GeV, $ \eta(l^\pm) < 2.4$, $p_T(J_b) > 30$ GeV, $ \eta(J_b) < 2.4$	$3.780^{+37.4\%}_{-25.3\%}$	$4.483^{+9.0\%}_{-11.5\%}$	$4.874^{+2.5\%}_{-6.8\%}$	-8.0%	$4.73^{+4.7\%}_{-4.7\%}$



Exact NWA results @ NNLO

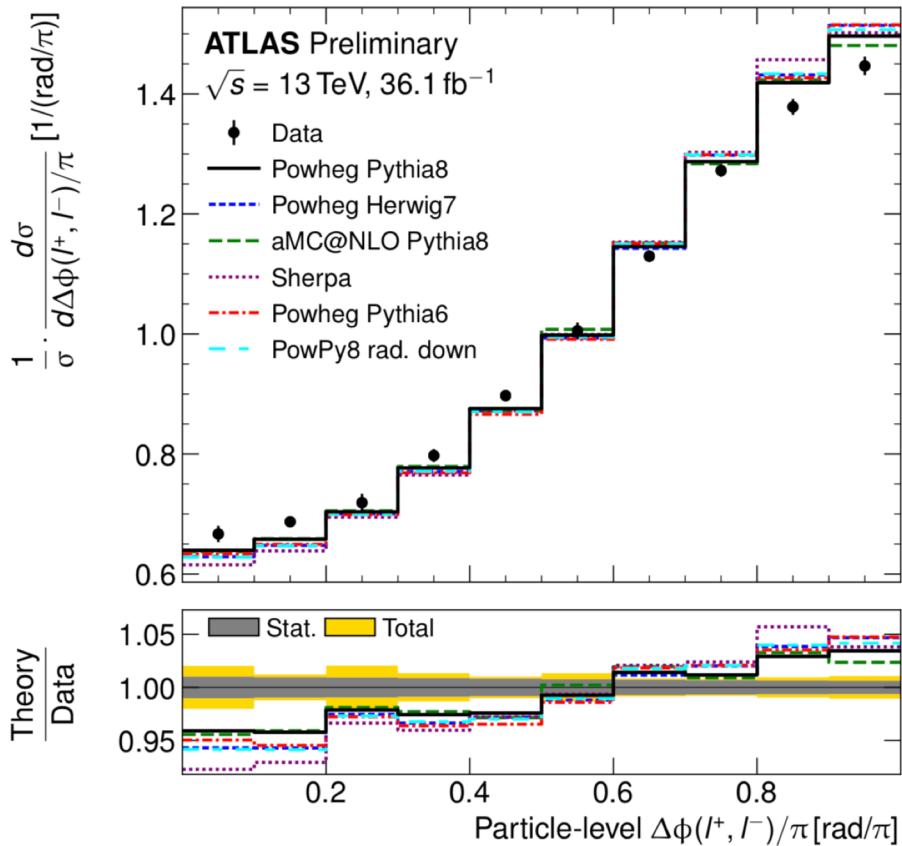
- Contributions



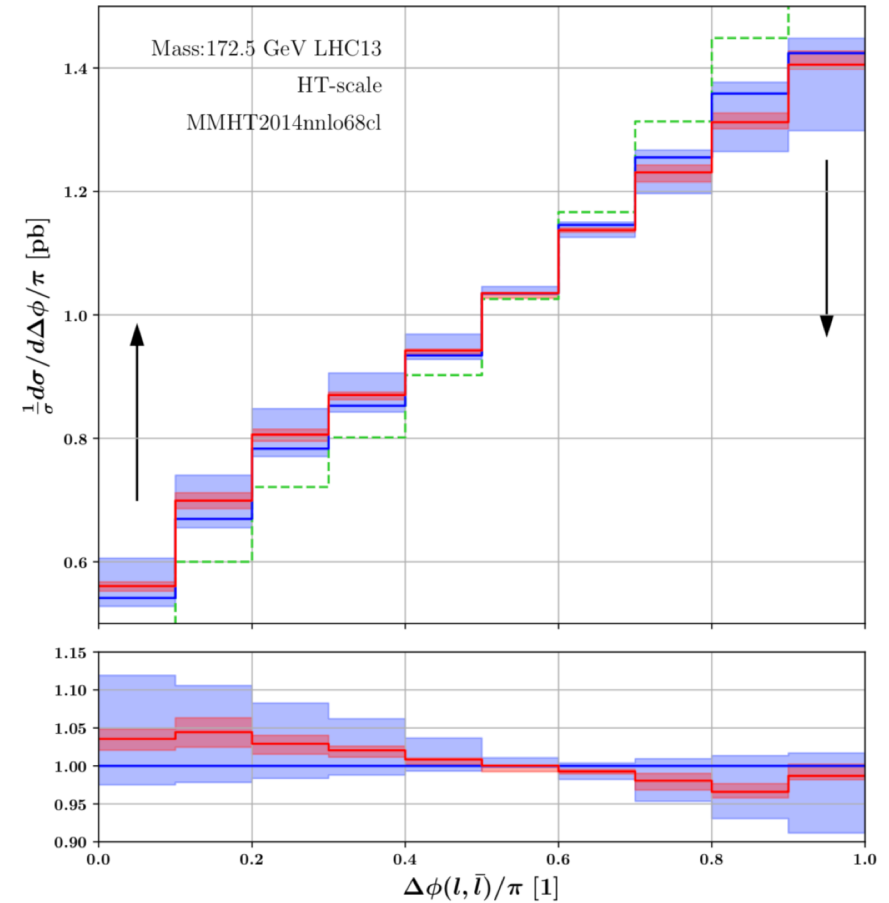
Exact NWA results @ NNLO

- Application in case of data/theory discrepancies

ATLAS-CONF-2018-027

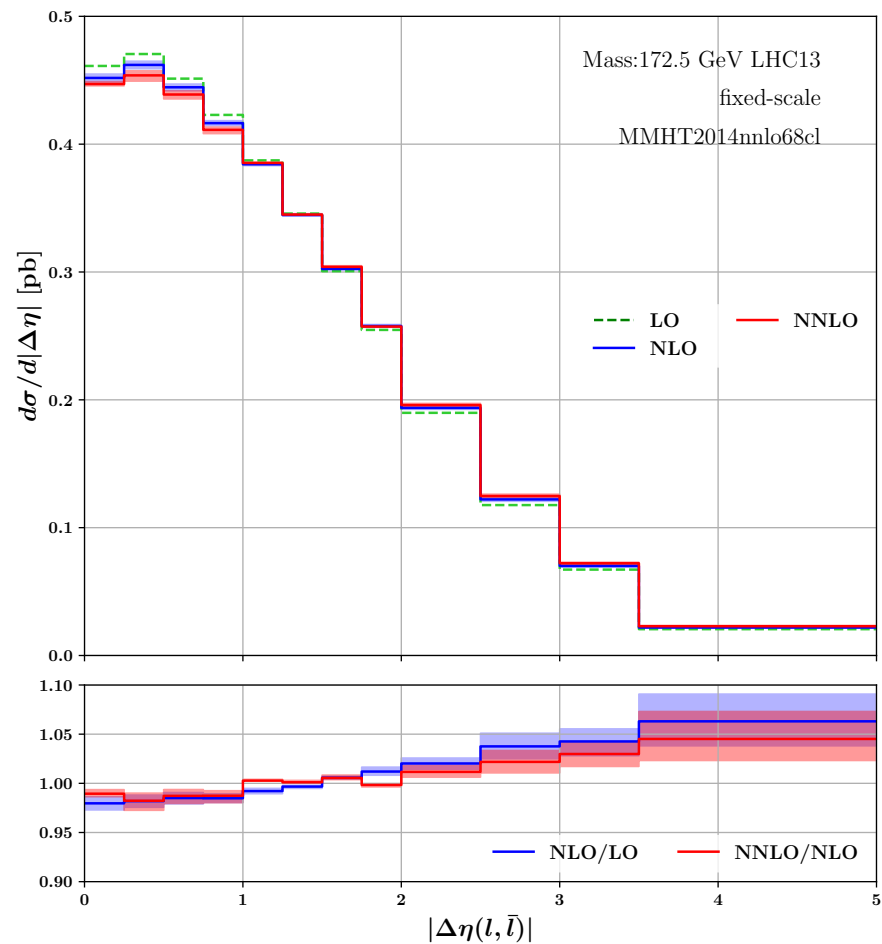


NWA @ NNLO predictions



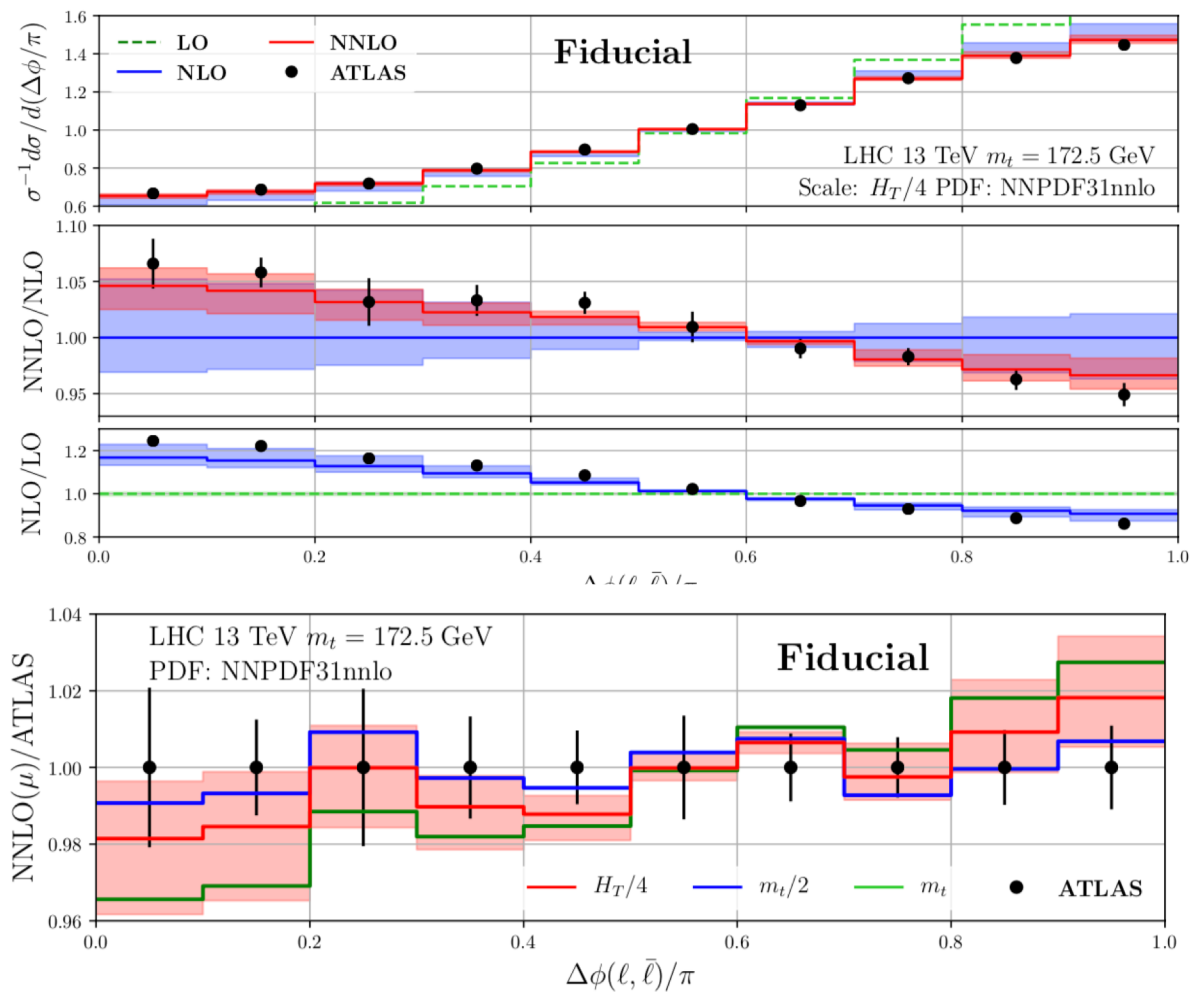
Exact NWA results @ NNLO

- Application in case of potentially noticeable effects in data



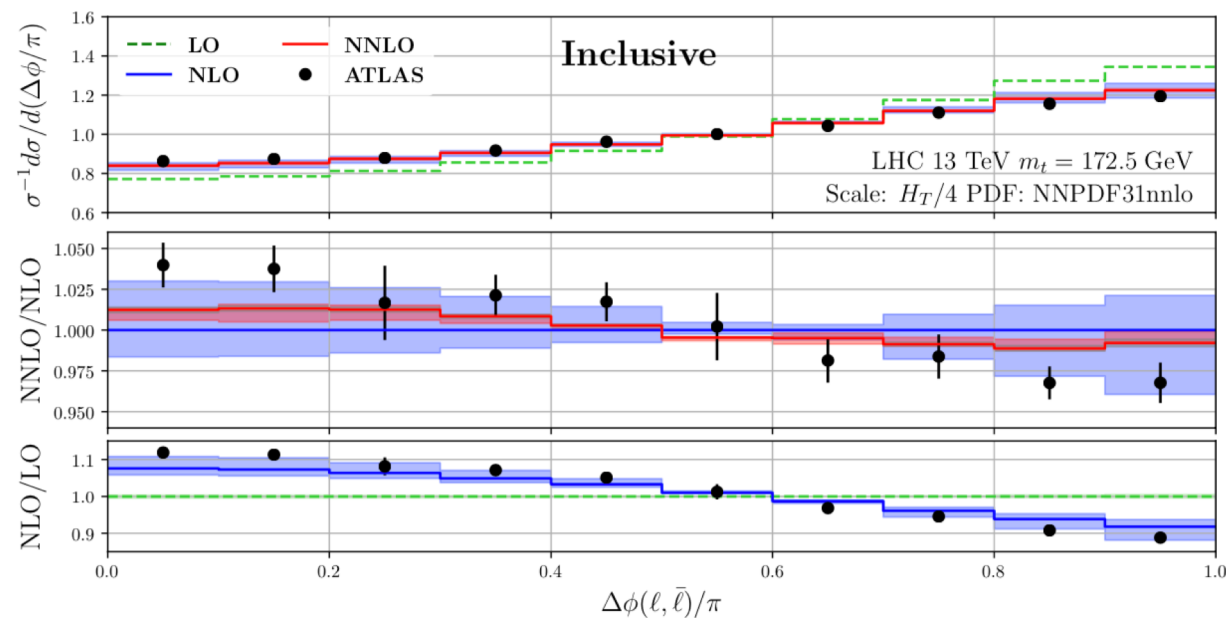
Exact NWA results @ NNLO

- Fine-tuned analysis reveals shortcomings in full phase space extrapolation



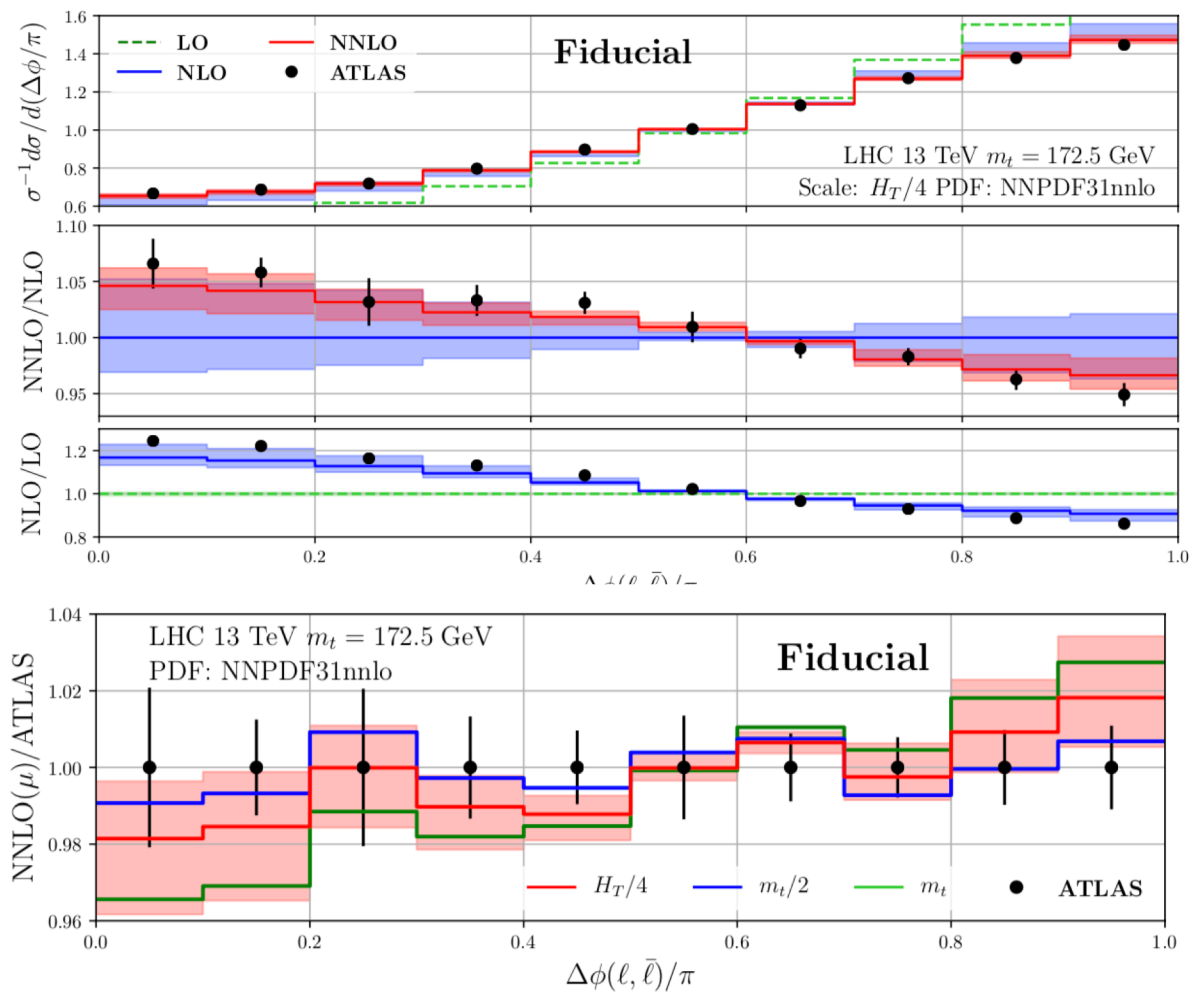
Negligible sensitivity to:

- Top quark mass
- Parton Distribution Functions
- Electroweak effects
- Radiation in the decay



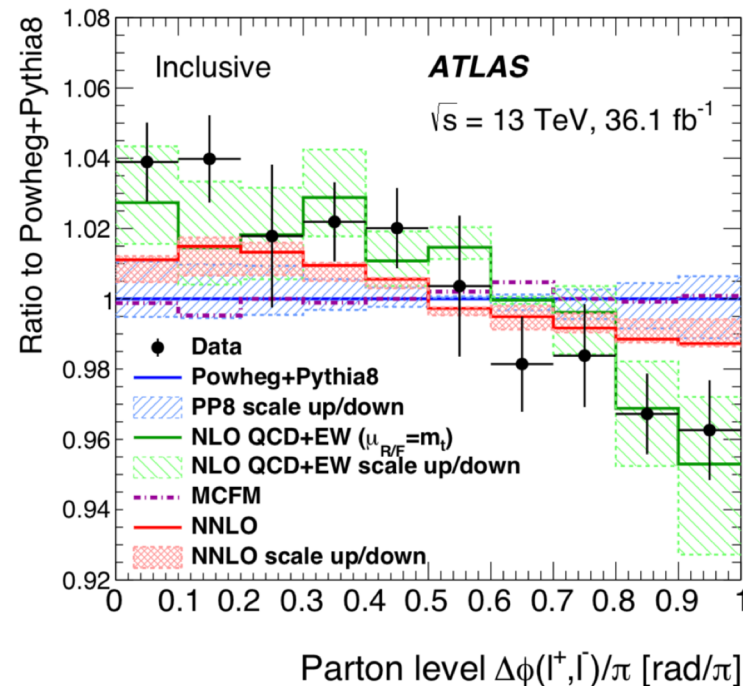
Exact NWA results @ NNLO

- Fine-tuned analysis reveals shortcomings in full phase space extrapolation



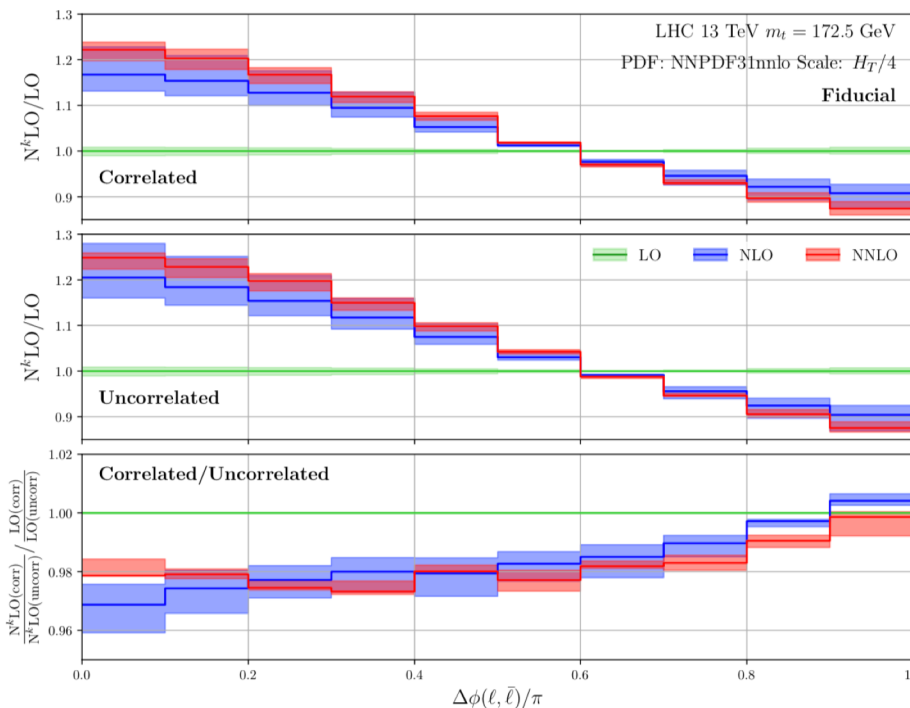
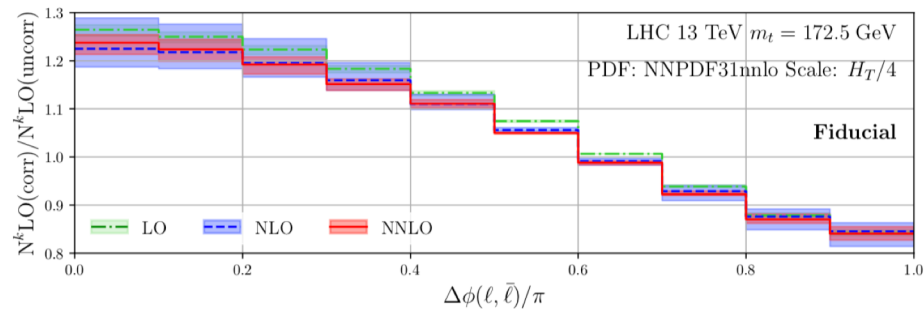
Negligible sensitivity to:

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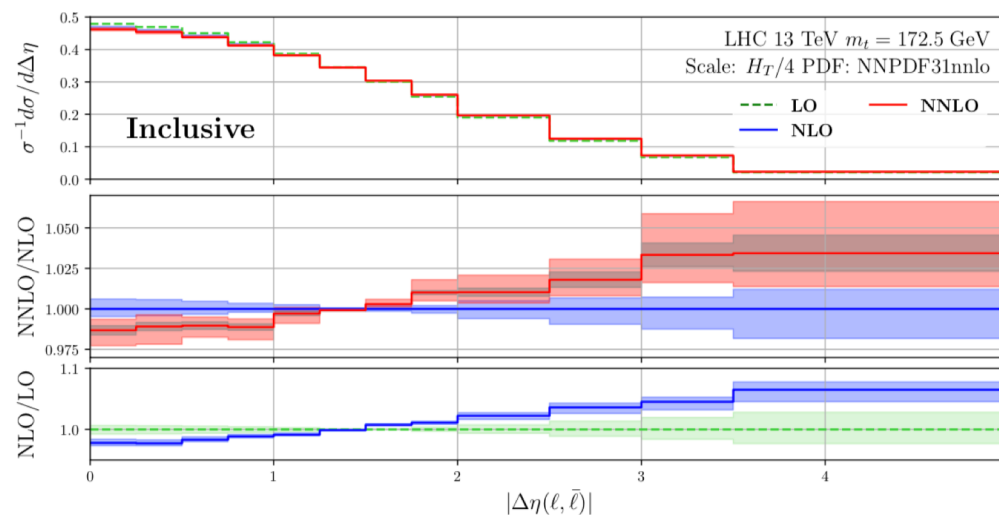
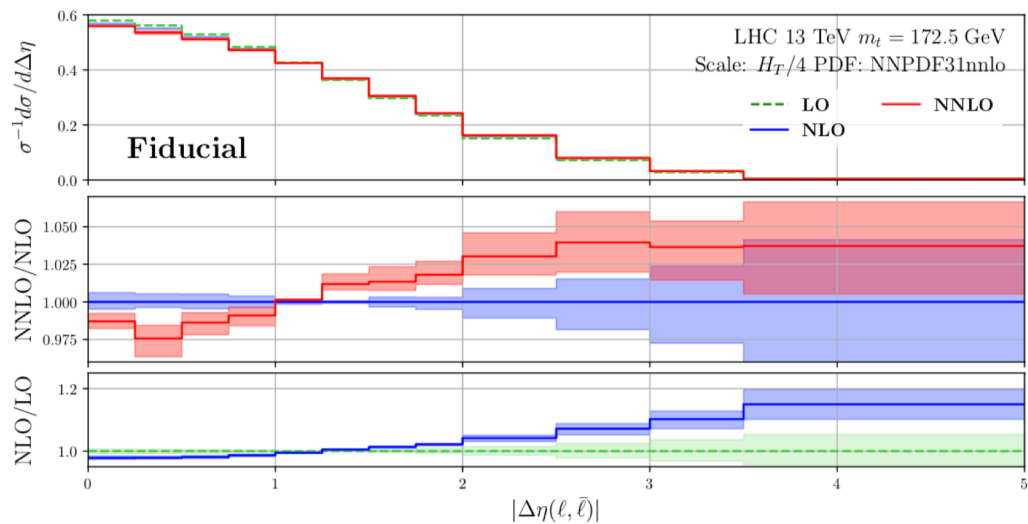


Exact NWA results @ NNLO

- Importance of spin correlations

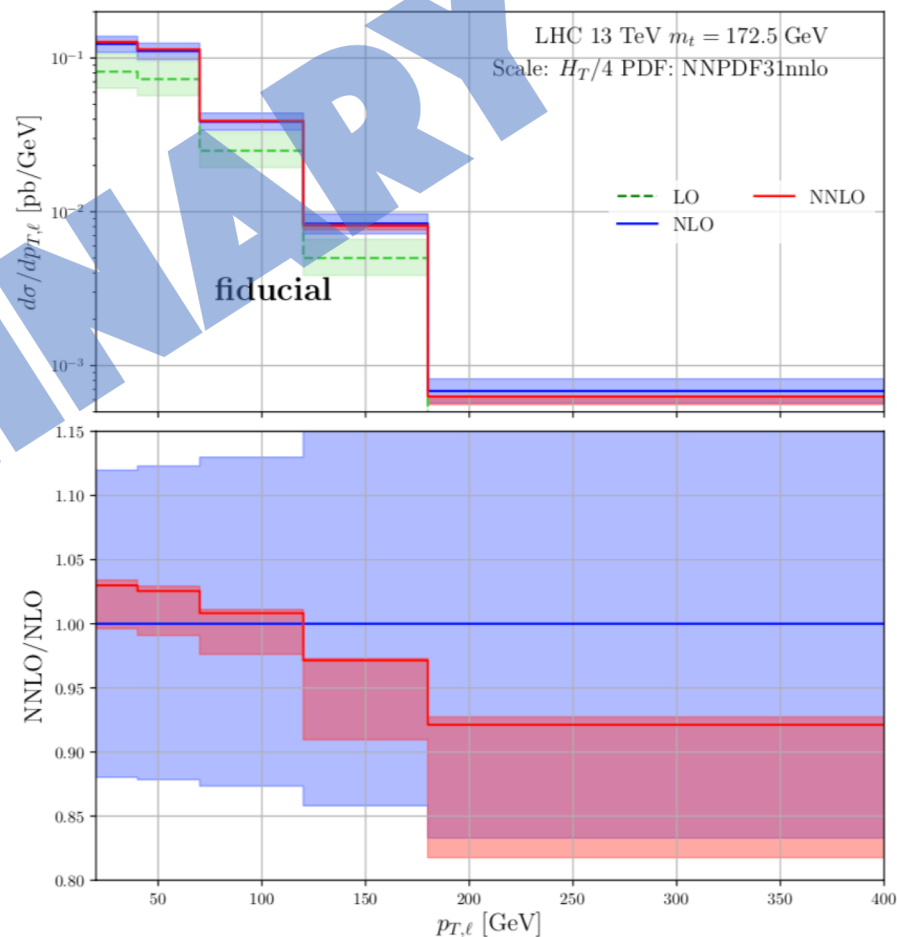
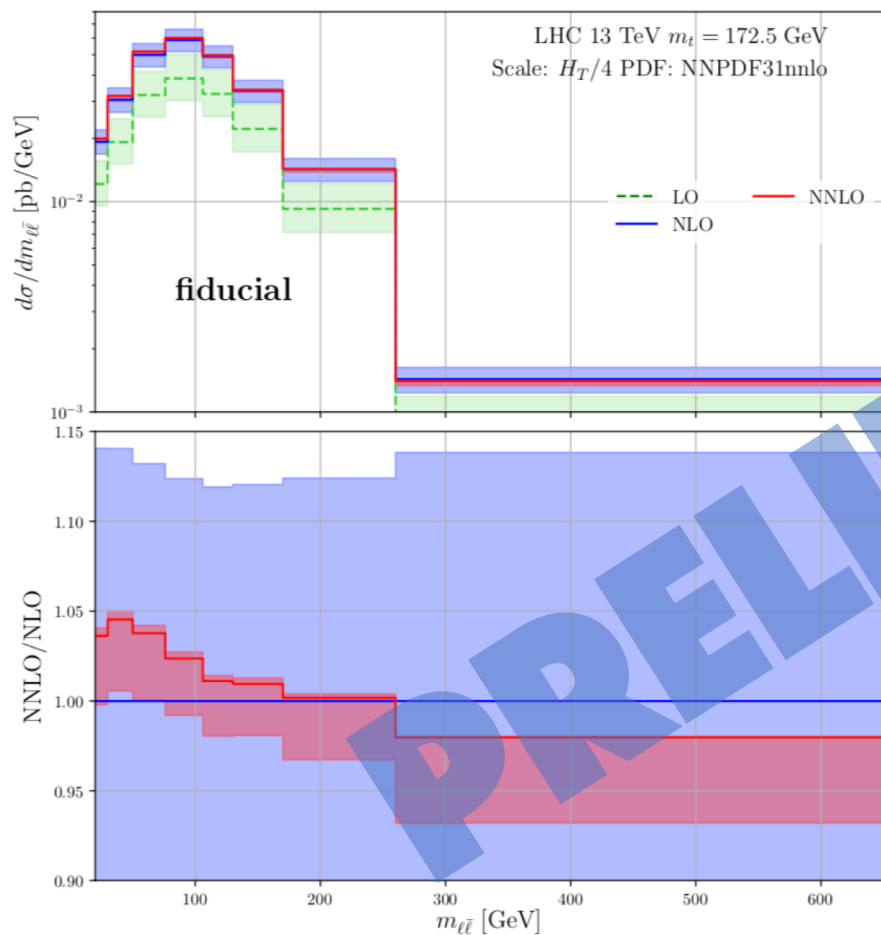


- Impact on other observables



Exact NWA results @ NNLO

- Further work



Electroweak effects for on-shell tops

- Long history

Beennakker, Denner, Hollik, Mertig, Sack, Wackeroth '94

Bernreuther, Fűcker, Si '05, '06

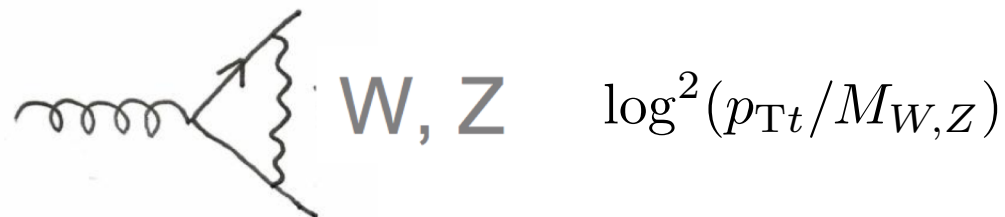
Moretti, Nolten, Ross '06

Kűhn, Scharf, Uwer '05, '06, '14

Pagani, Tsinikos, Zaro '16

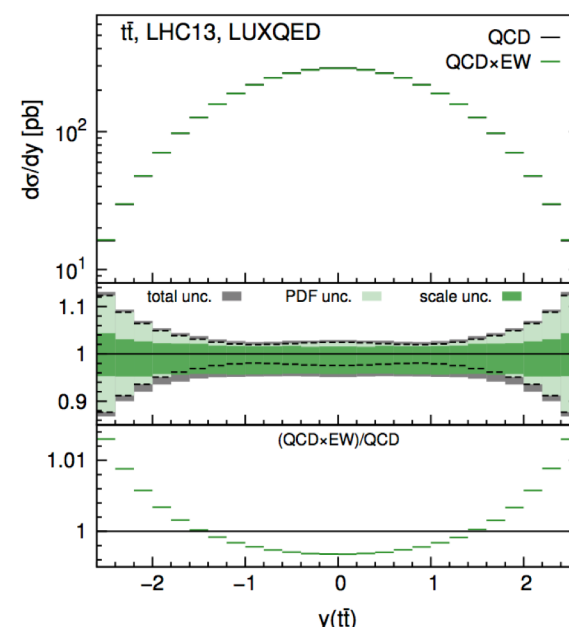
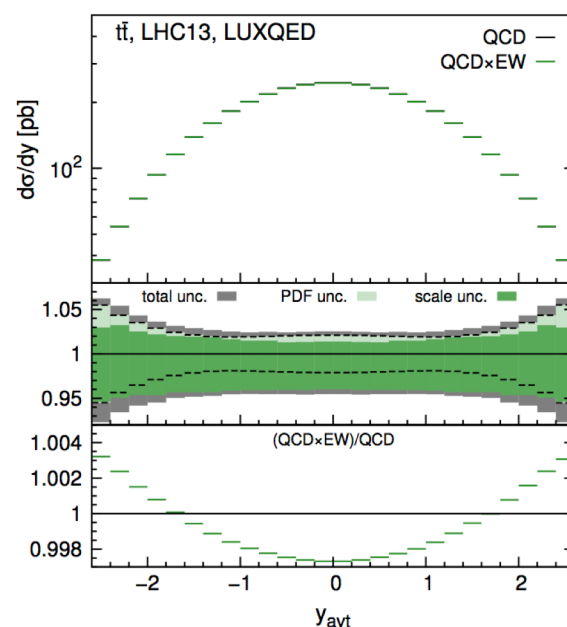
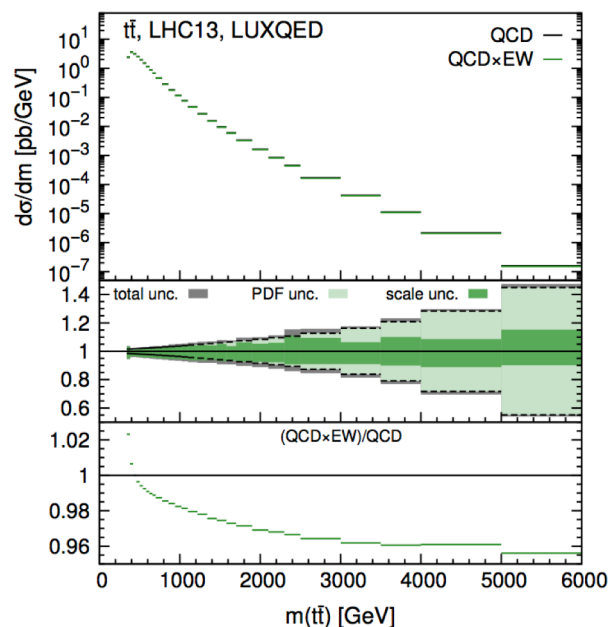
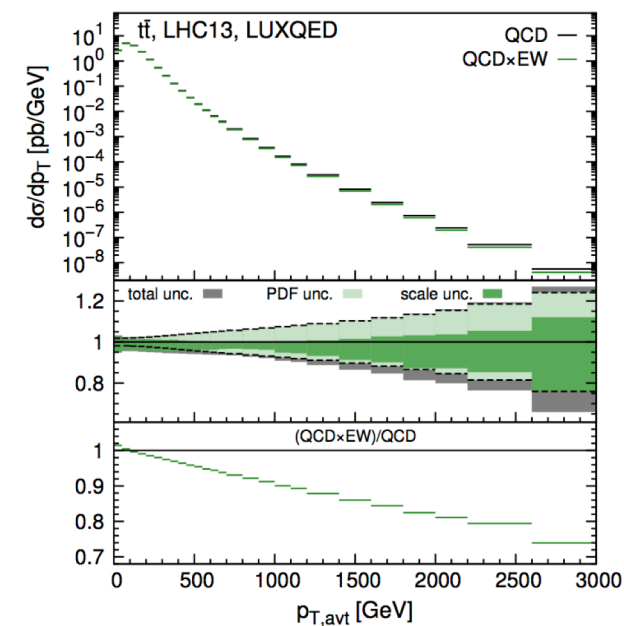
Denner, Pellen '16

- Large Sudakov logarithms



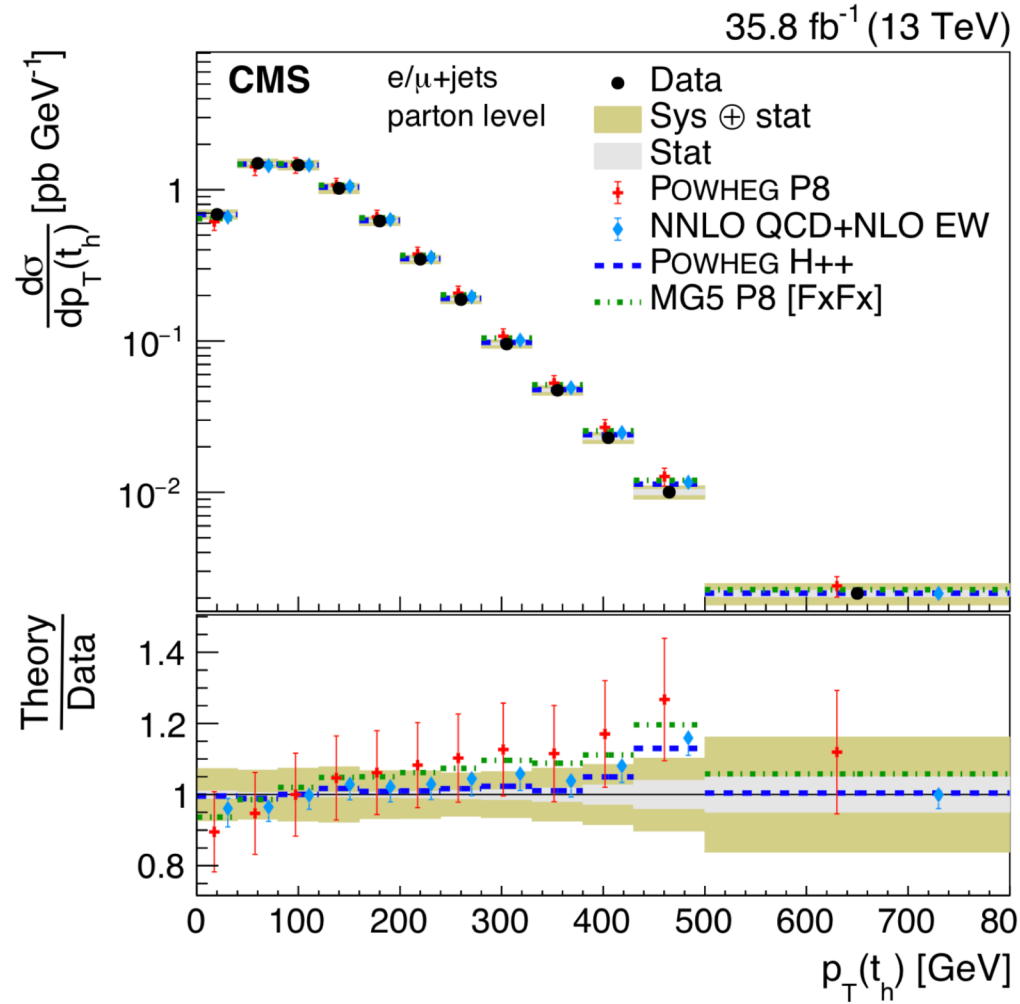
- Combination with NNLO QCD

MC, Heymes, Mitov, Pagani, Tsinikos, Zaro '17

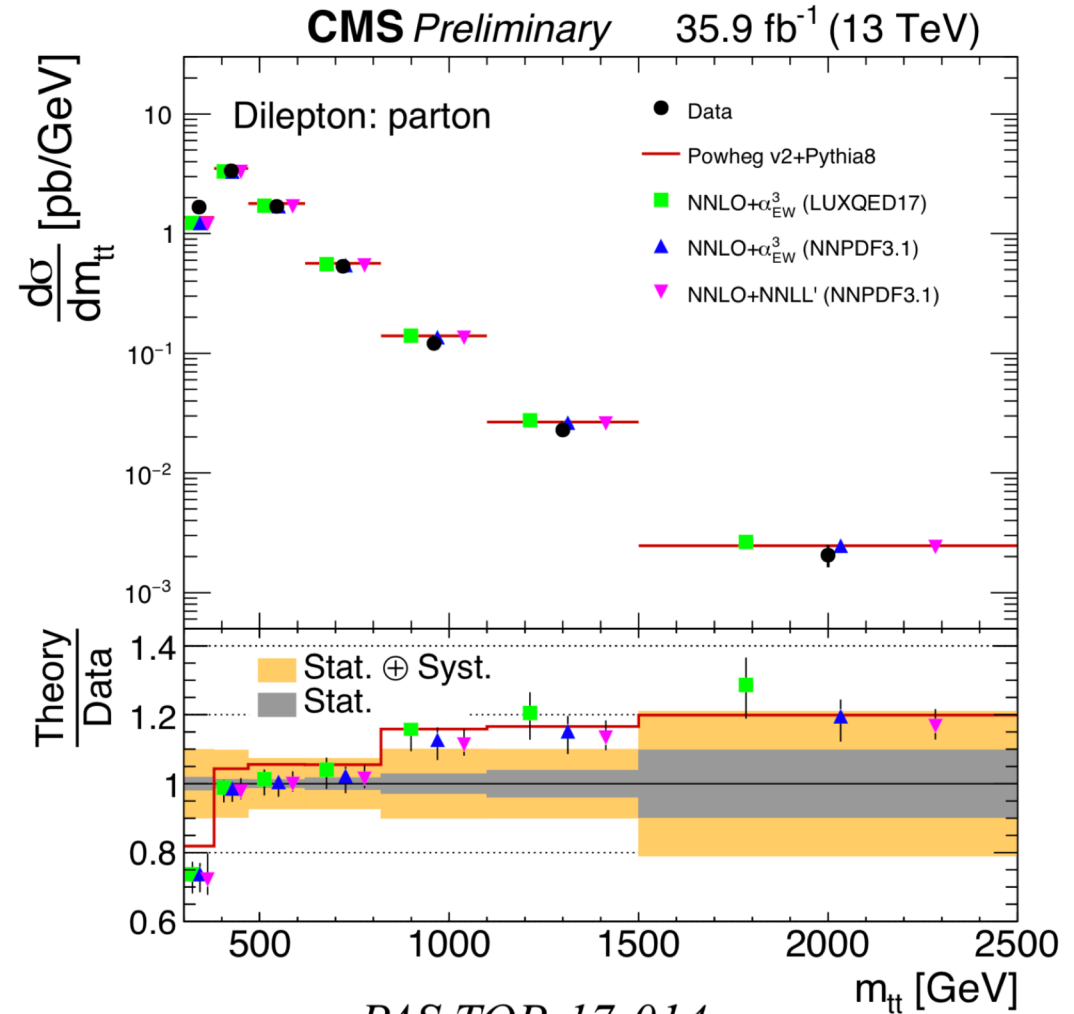


QCD x EW effects for on-shell tops

- Comparison with data after combination

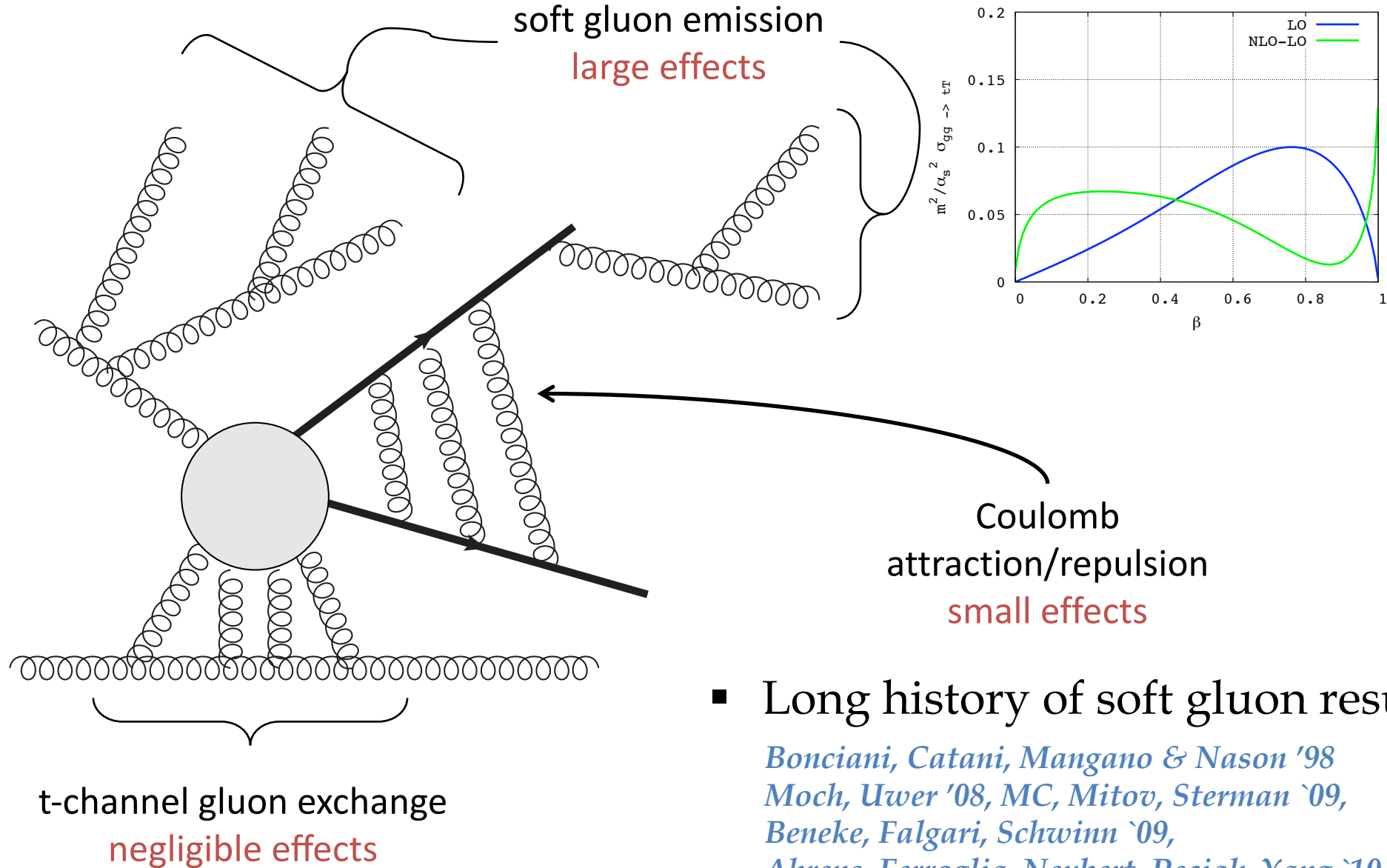


arXiv:1803.08856



PAS TOP-17-014

Dominant QCD effects and resummation



- Long history of soft gluon resummation

Bonciani, Catani, Mangano & Nason '98

Moch, Uwer '08, MC, Mitov, Sterman '09,

Beneke, Falgari, Schwinn '09,

Ahrens, Ferroglia, Neubert, Pecjak, Yang '10

Effects in the “Tails”

- Additionally to the potentially small gluon energies, m_t is small
- In this “boosted” regime there are two kinds of logs

$$\text{soft logs: } [\ln^n(1-z)/(1-z)]_+ \quad (z \equiv M_{t\bar{t}}^2/\hat{s})$$

$$\text{small-mass (collinear) logs: } \ln m_t/M_{t\bar{t}}$$

- Widely separated scales

$$\text{Soft Limit: } \hat{s}, t_1, m_t^2 \gg \hat{s}(1-z)^2$$

$$\text{Boosted Soft Limit: } \hat{s}, t_1 \gg m_t^2 \gg \hat{s}(1-z)^2 \gg m_t^2(1-z)^2$$

- Factorization possible

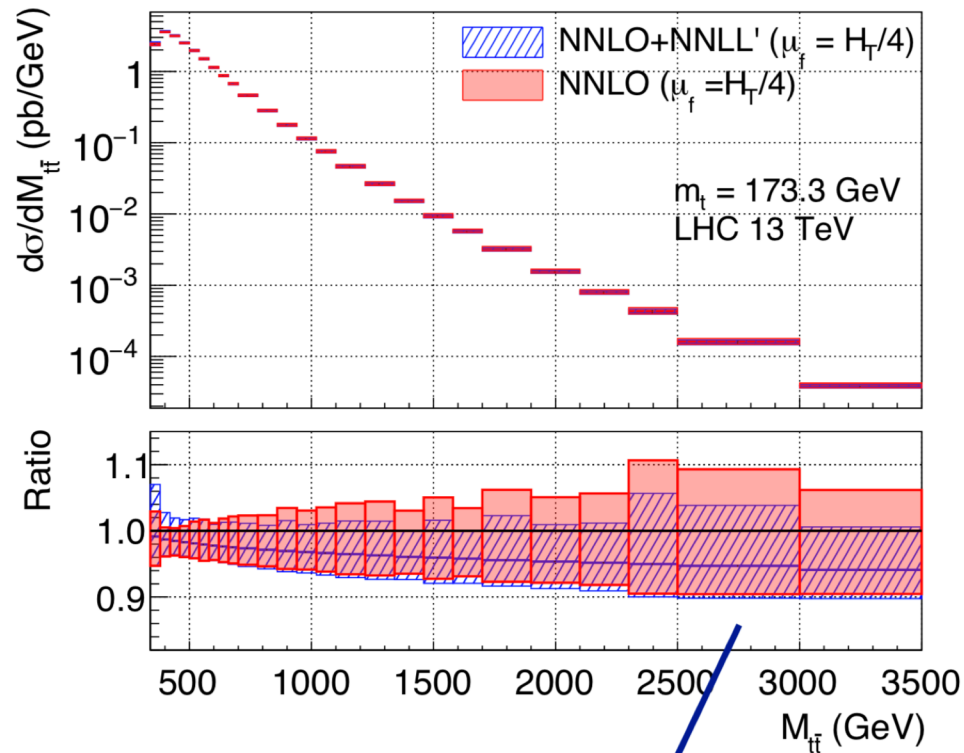
$$\begin{aligned} d\tilde{\sigma}_{ij}(\mu_f) = & \text{Tr} \left[\tilde{\mathbf{U}}_{ij}(\mu_f, \mu_h, \mu_s) \mathbf{H}_{ij}(M, \cos \theta, \mu_h) \tilde{\mathbf{U}}_{ij}^\dagger(\mu_f, \mu_h, \mu_s) \right. \\ & \left. \times \tilde{s}_{ij} \left(\ln \frac{M^2}{\bar{N}^2 \mu_s^2}, M, \cos \theta, \mu_s \right) \right] \times \tilde{U}_D^2(\mu_f, \mu_{dh}, \mu_{ds}) C_D^2(m_t, \mu_{dh}) \tilde{s}_D^2 \left(\ln \frac{m_t}{\bar{N} \mu_{ds}}, \mu_{ds} \right) \\ & + \mathcal{O} \left(\frac{1}{N} \right) + \mathcal{O} \left(\frac{m_t^2}{M^2} \right) \end{aligned}$$

Ferrogli, Pecjak, Scott, Yang '13
Pecjak, Scott, Wang, Yang '16

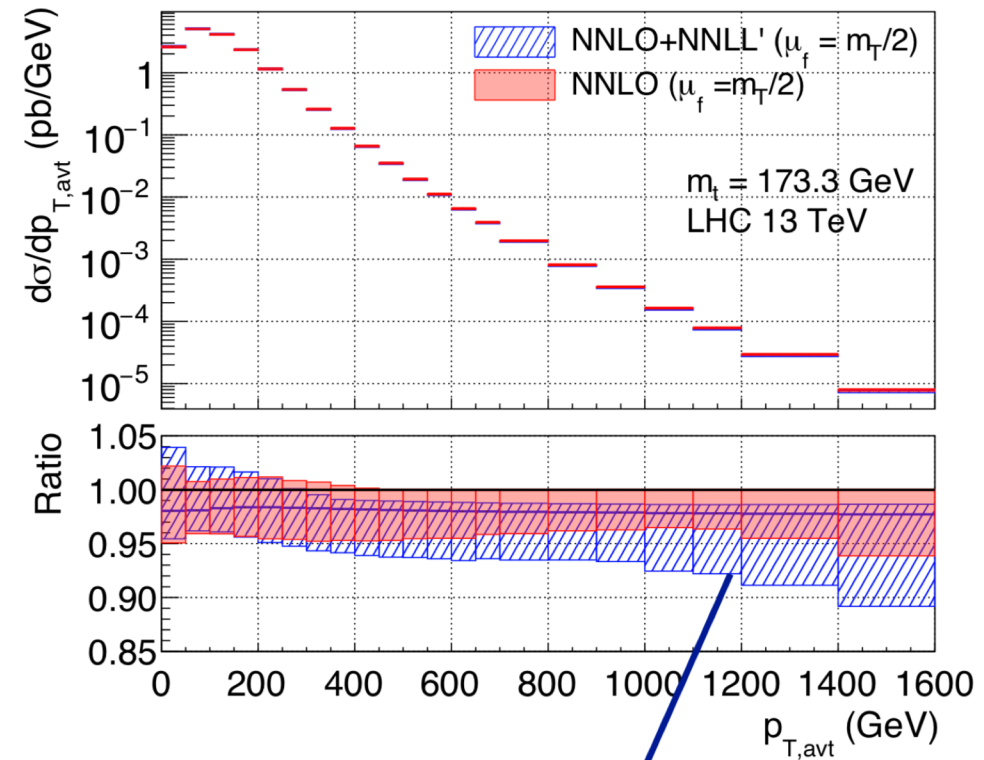
- Notice that there are 5 (!) scales now

Matched NNLO+NNLL` results

MC, Ferroglia, Heymes, Mitov, Pecjak, Scott, Wang, Yang `18



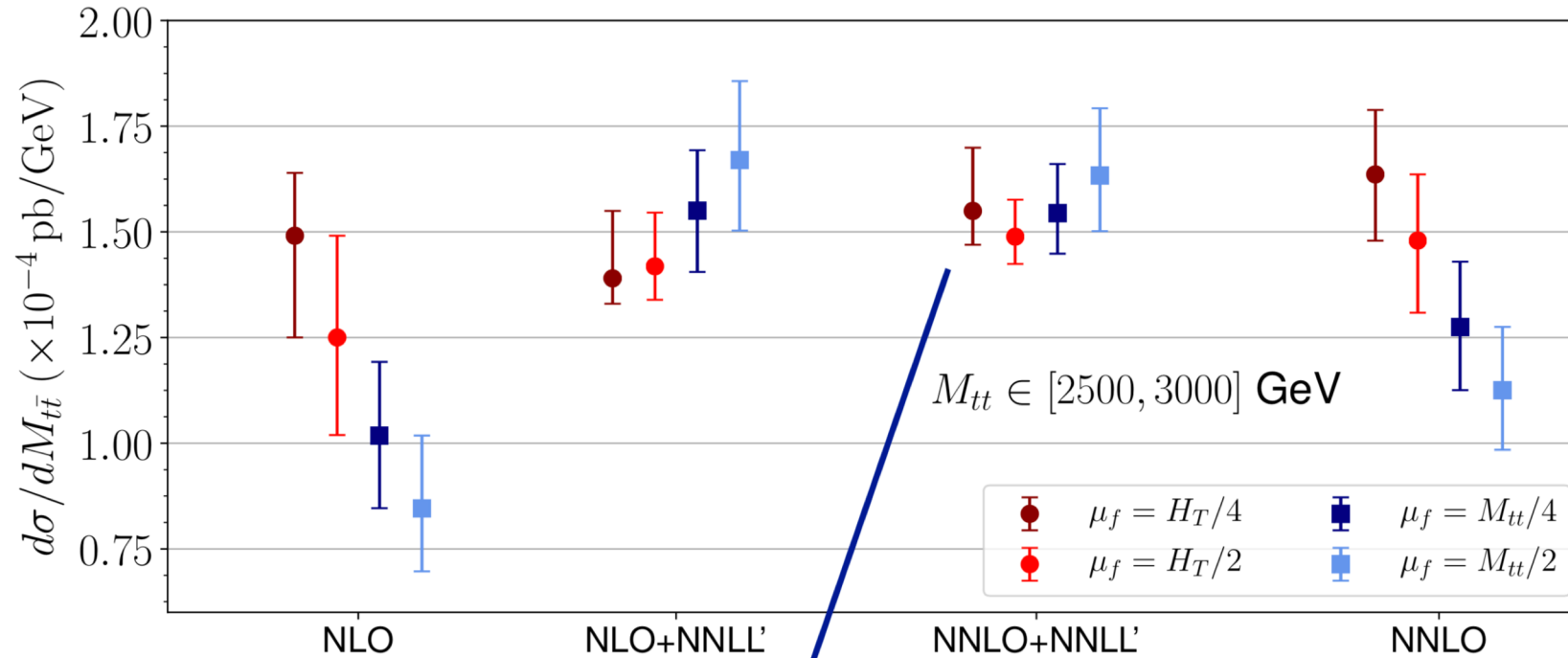
Resummation reduces
scale variation



Resummation
softens the spectrum

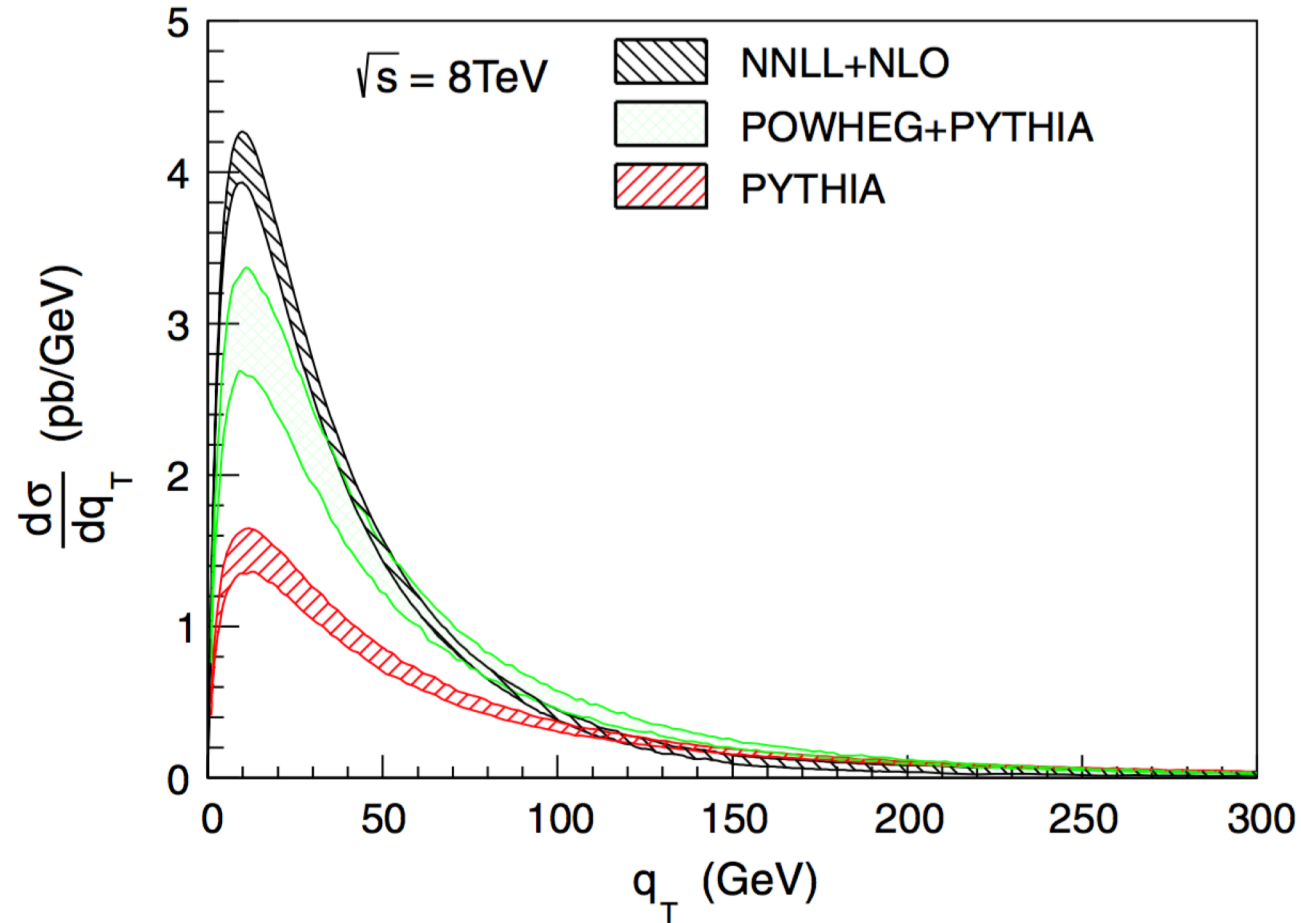
Matched NNLO+NNLL` results

MC, Ferroglia, Heymes, Mitov, Pecjak, Scott, Wang, Yang `18



Matched result insensitive to scale scheme choices

Another resummation: p_T of the pair



Plot taken from Li et al.

*Li, Li, Shao, Yang, Zhu '13
Catani, Grazzini, Torre '14*

Sophisticated decay modelling

Decay Modeling @ NLO

- Off-shell effects through direct simulation of the final state $l^+ \nu l^- \bar{\nu} b\bar{b}$

Denner, Dittmaier, Kallweit, Pozzorini '11 '12

Bevilacqua, MC, van Hameren, Papadopoulos, Worek '11

Heinrich, Maier, Nisius, Schlenk, Winter '13

- Off-shell effects with massive b-quarks (simultaneous top-pair and single-top)

Frederix '13

Cascioli, Kallweit, Maierhöfer, Pozzorini '13

- Off-shell effects in the semi-leptonic channel

Denner, Pellen '18

- Off-shell electroweak effects

Denner, Pellen '16

- More complicated processes

$$l^+ \nu l^- \bar{\nu} b\bar{b} + H$$

Denner, Feger '15,

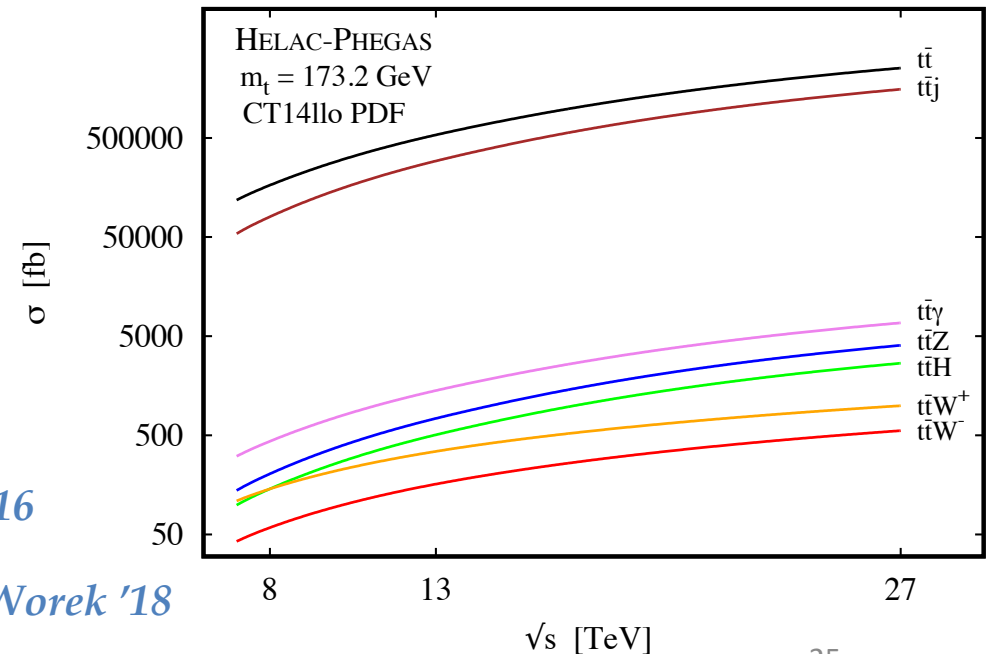
Denner, Lang, Pellen, Uccirati '17

$$l^+ \nu l^- \bar{\nu} b\bar{b} + jet$$

Bevilacqua, Hartanto, Kraus, Worek '16

$$l^+ \nu l^- \bar{\nu} b\bar{b} + \gamma$$

Bevilacqua, Hartanto, Kraus, Weber, Worek '18



Effects on Total Rates (Fiducial)

NWA Off-shell

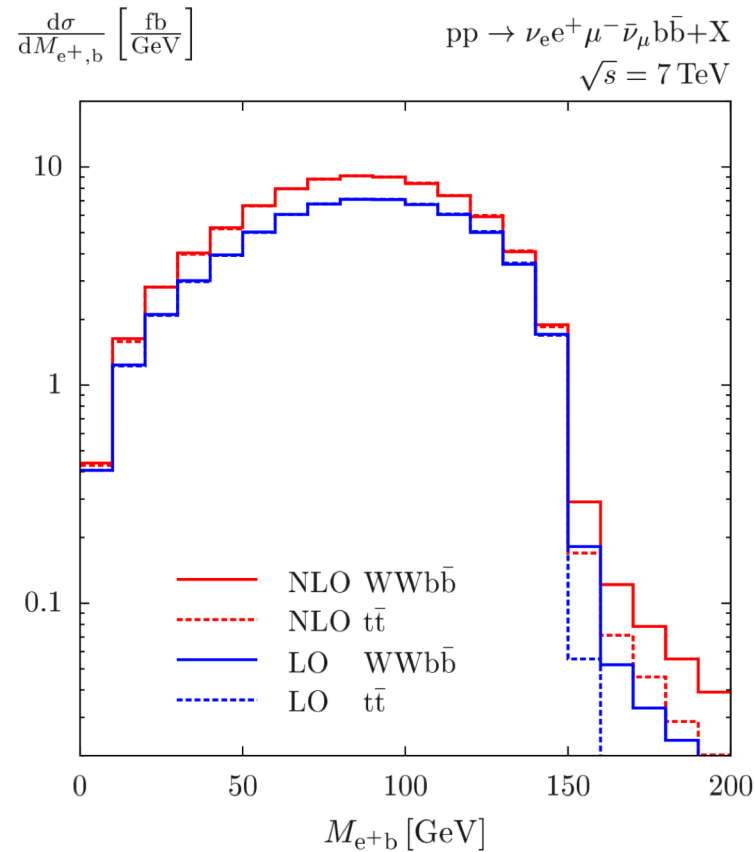
Collider	\sqrt{s} [TeV]	approx.	$\sigma_{t\bar{t}}$ [fb]	$\sigma_{WWb\bar{b}}$ [fb]	$\sigma_{t\bar{t}}/\sigma_{WWb\bar{b}} - 1$	Expected
Tevatron	1.96	LO	$44.691(8)^{+19.81}_{-12.58}$	$44.310(3)^{+19.68}_{-12.49}$	+ 0.861(19)%	+ 0.8%
		NLO	$42.16(3)^{+0.00}_{-2.91}$	$41.75(5)^{+0.00}_{-2.63}$	+ 0.98(14)%	+ 0.9%
LHC	7	LO	$659.5(1)^{+261.8}_{-173.1}$	$662.35(4)^{+263.4}_{-174.1}$	- 0.431(16)%	- 0.4%
		NLO	$837(2)^{+42}_{-87}$	$840(2)^{+41}_{-87}$	- 0.41(31)%	- 0.2%
LHC	14	LO	$3306.3(1)^{+1086.8}_{-763.6}$	$3334.6(2)^{+1098.5}_{-771.2}$	- 0.849(7)%	- - -
		NLO	$4253(3)^{+282}_{-404}$	$4286(7)^{+283}_{-407}$	- 0.77(19)%	- - -

Denner, Dittmaier, Kallweit, Pozzorini, Schulze '12

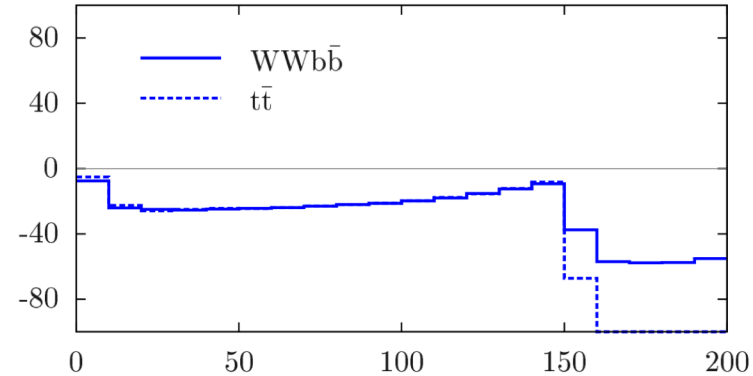
Tevatron (LHC) $R = 0.4 (0.5)$ $p_{T,b\text{-jet}} > 20 (30) \text{ GeV}, |\eta_{b\text{-jet}}| < 2.5$

$p_{T,\text{miss}} > 25 (20) \text{ GeV}$ $p_{T,l} > 20 \text{ GeV}$ and $|\eta_l| < 2.5$

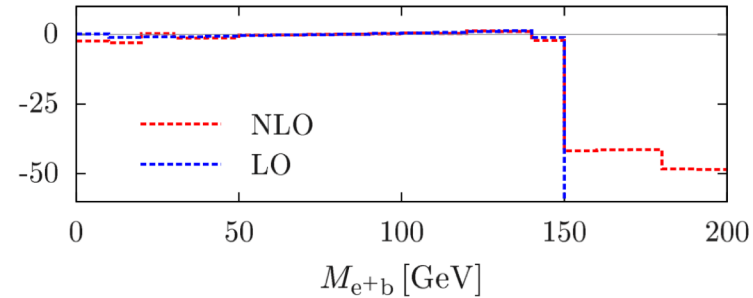
Finite Width Sensitive Observables



LO/NLO - 1 [%]



$t\bar{t}/WWb\bar{b} - 1$ [%]



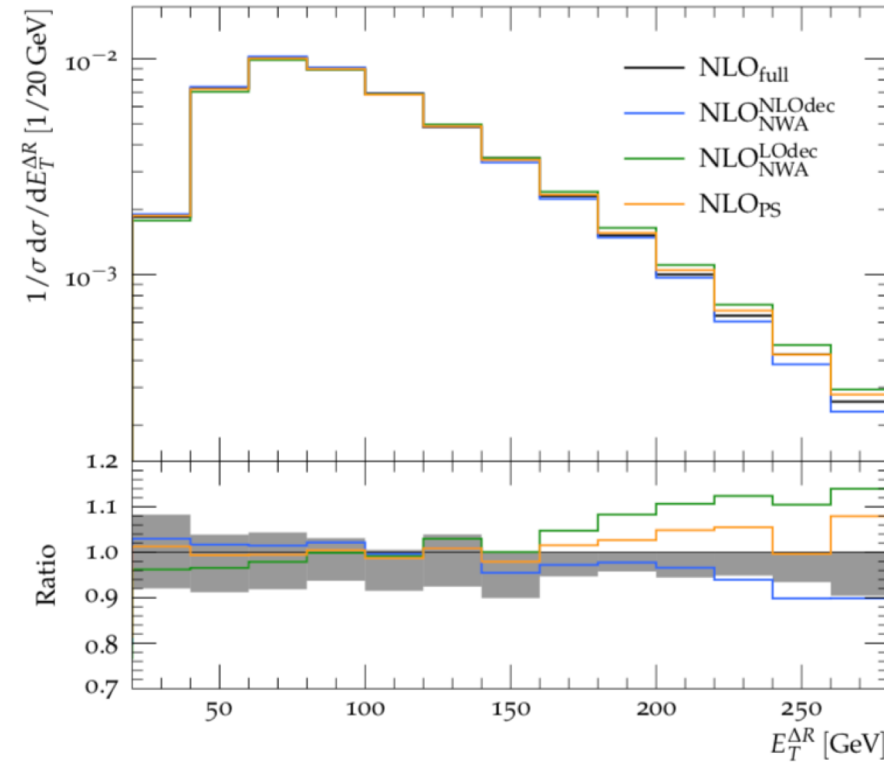
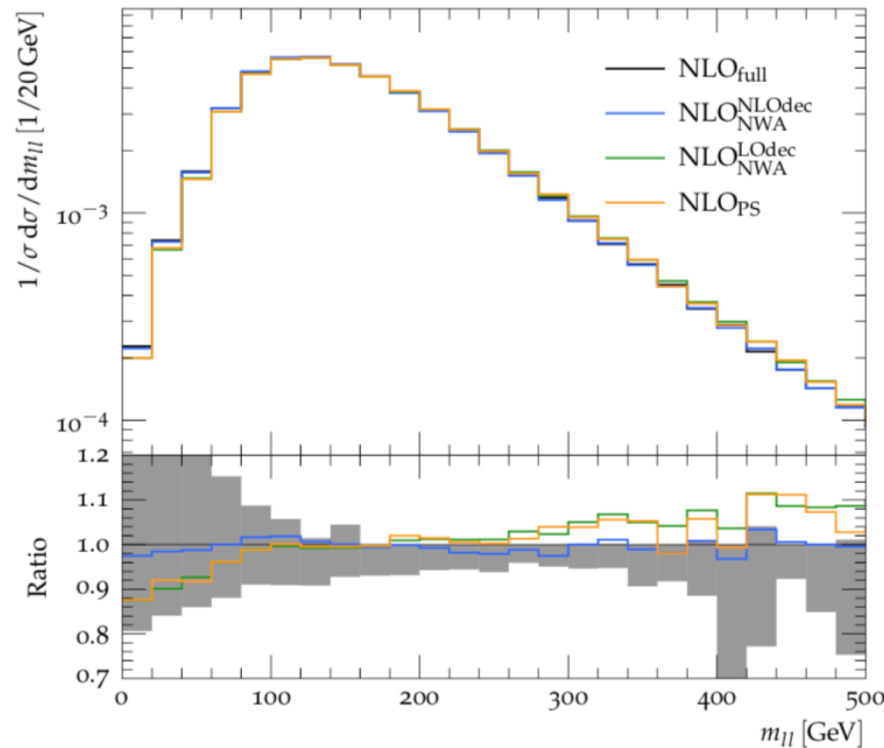
Denner, Dittmaier, Kallweit, Pozzorini, Schulze `12

- Large effects easily found by reaching past kinematic end-points

Finite Width Sensitive Observables

Off-shell, NWA, PS

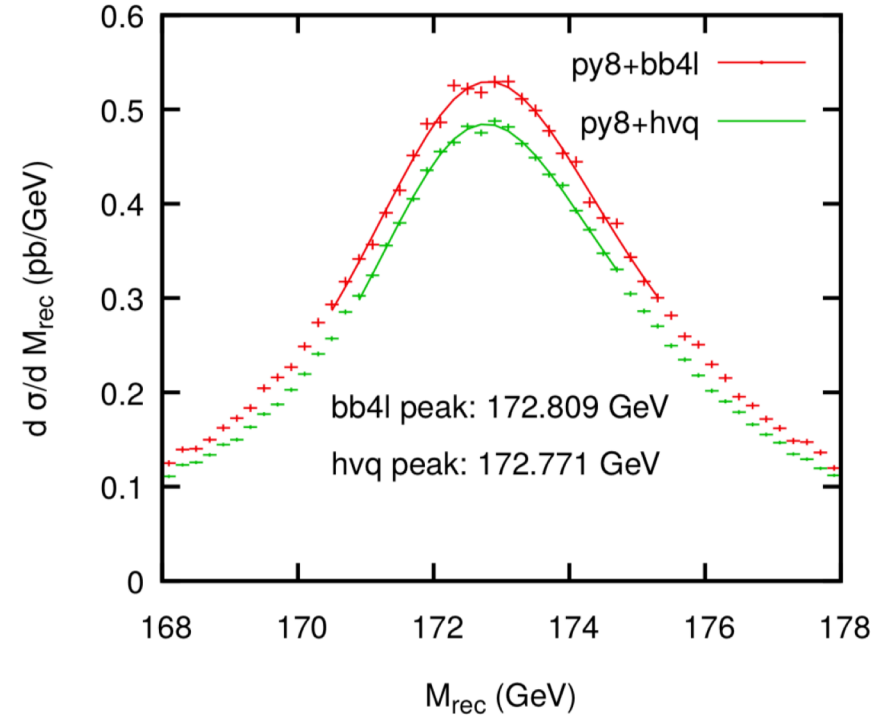
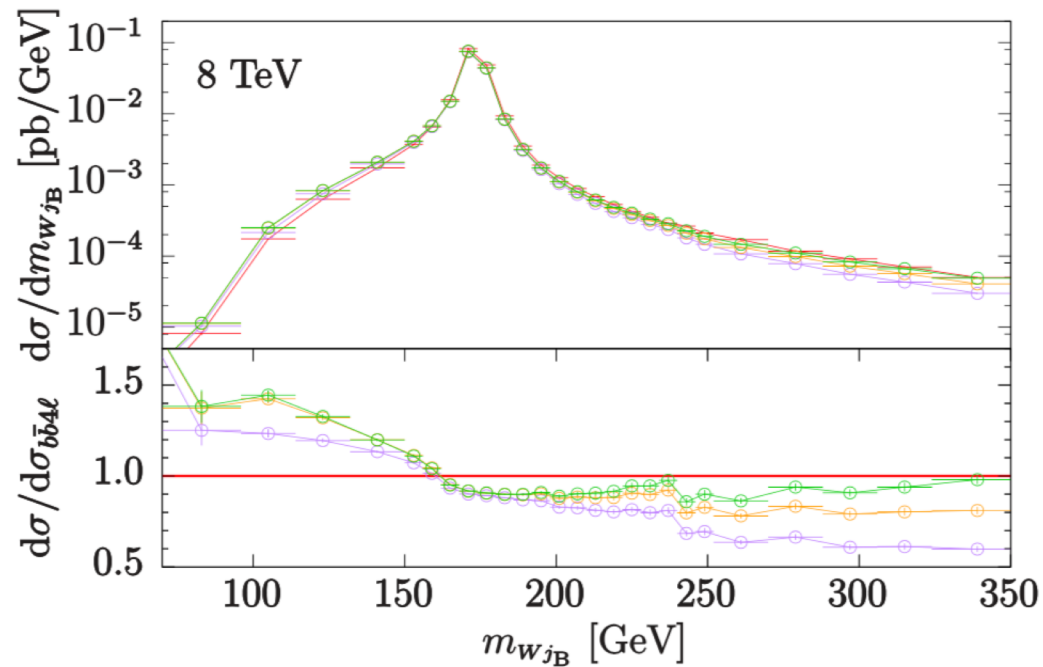
$pp \rightarrow t\bar{t} \rightarrow e^+ \nu_e \mu^- \bar{\nu}_\mu b\bar{b}$ @ 13 TeV LHC



Heinrich, Maier, Nisius, Schlenk, Schulze, Scyboz, Winter '18

Off-shell matching to parton showers

- ▶ —•— b_bbar_4l: $pp \rightarrow \ell^+ \nu_\ell \ell^- \bar{\nu}_\ell b \bar{b}$ @NLO, allrad scheme
- ▶ —○— hvq: $t\bar{t}$ @NLO, decay @LO, no Wt contribution
- ▶ —○— hvq + ST_wtch_DS: tt & Wt @NLO, t decay @LO
- ▶ —○— hvq + ST_wtch_DR: tt & Wt @NLO, t decay @LO



	$M_{\text{rec}} \text{ (GeV)}$					
	Full			Shower only		
	b \bar{b} 4l	hvq	Δ	b \bar{b} 4l	hvq	Δ
$\sigma = 0$	172.809	172.771	0.038	172.544	172.493	0.051
$\sigma = 15$	172.698	172.548	0.150	171.396	171.303	0.093

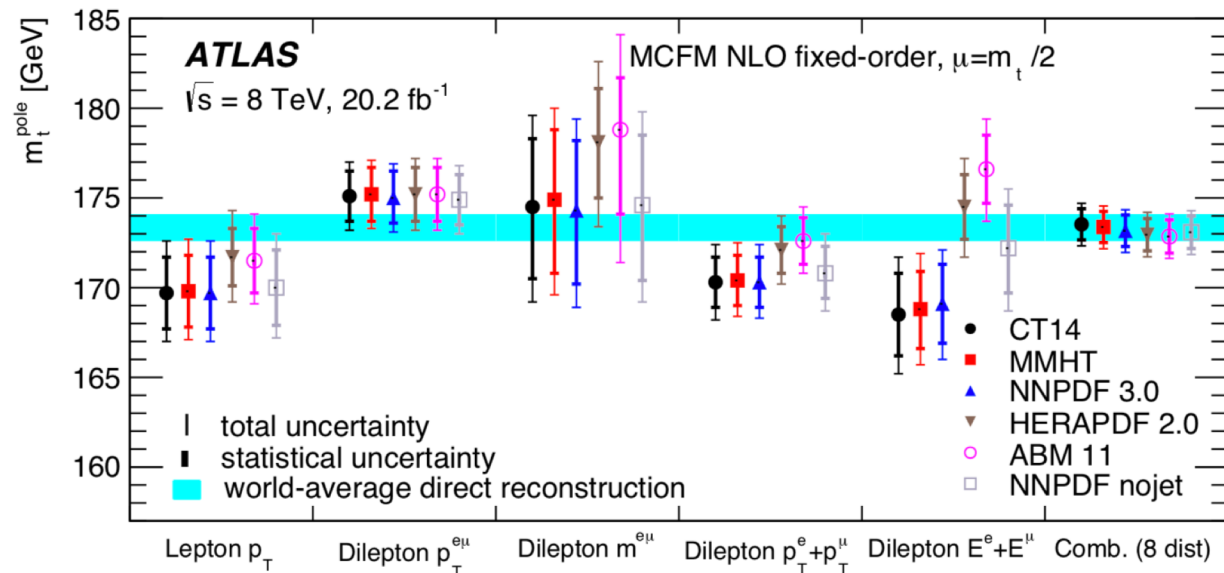
Conclusions

An example open problem

- ❖ Merging off-shell top quark effects @ NLO in QCD with NNLO QCD top quark predictions for $pp \rightarrow tt$ in *di-lepton* channel
- ❖ Determination of the top quark mass from leptonic observables \rightarrow Fiducial σ_{tt}

$$p_T^{\ell^+}, p_T^{\ell\ell}, M_{\ell\ell}, (E^{\ell^+} + E^{\ell^-}), (p_T^{\ell^+} + p_T^{\ell^-}), \eta^{\ell^+}, \eta^{\ell\ell}, \Delta\phi_{\ell\ell}$$

$$m_t = 172.2 \pm 0.9 \text{ (stat.)} \pm 0.8 \text{ (syst.)} \pm 1.2 \text{ (th.) GeV}$$



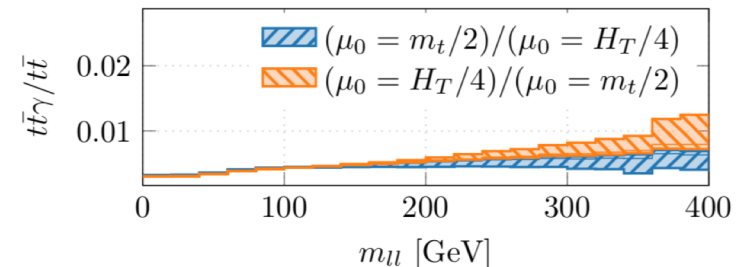
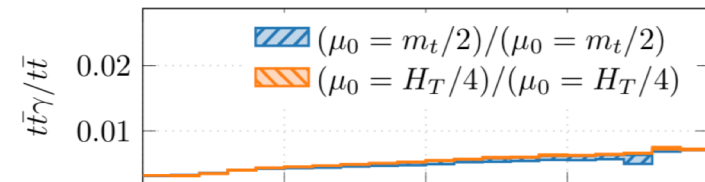
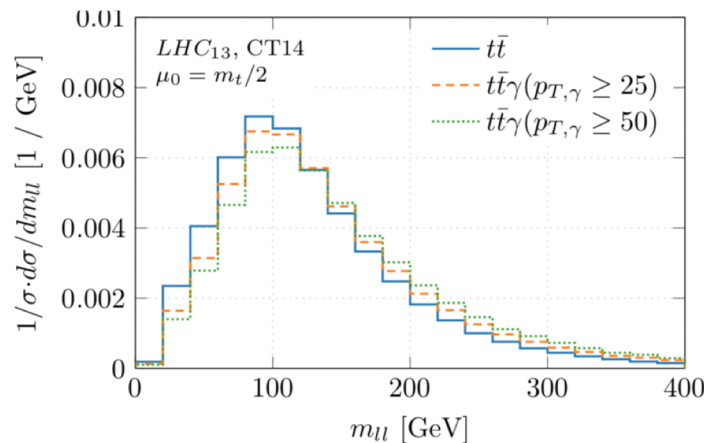
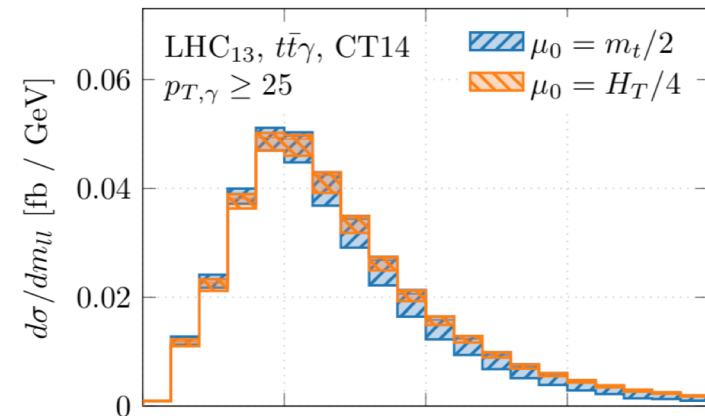
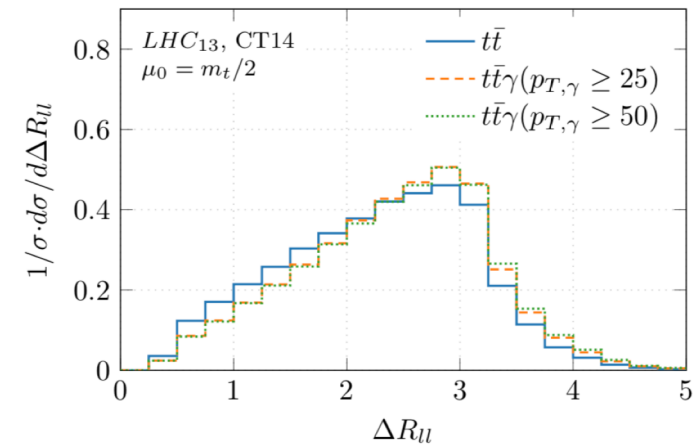
- ❖ Various tt NLO generators interfaced to PS used
- ❖ $d\sigma_{tt}/dX$ modeled poorly by NLO+PS
- ❖ The most precise result obtained from fixed-order NLO predictions
- ❖ *Measurements limited by theory uncertainties stemming from modeling of top quark decays !*

Precision improvement through ratios: $t\bar{t}\gamma/t\bar{t}$

- ❖ 1% – 3% precision for *Integrated Cross Section Ratios*
- ❖ *Differential Ratios* with 1% – 6% precision:
- ❖ Such high precision has only been reserved till now for NNLO !

Off-shell Tops

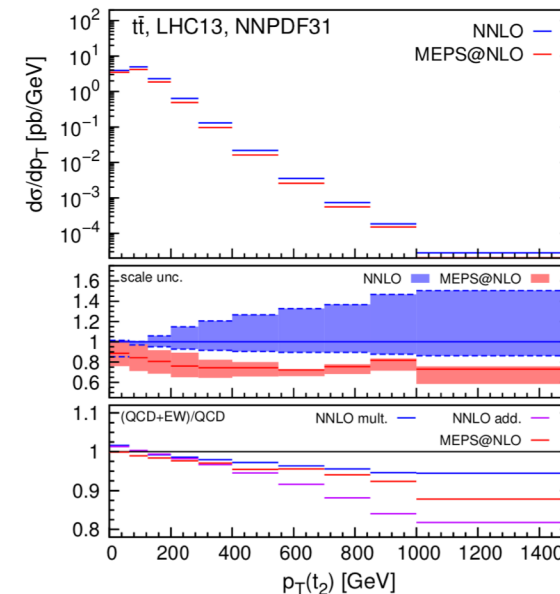
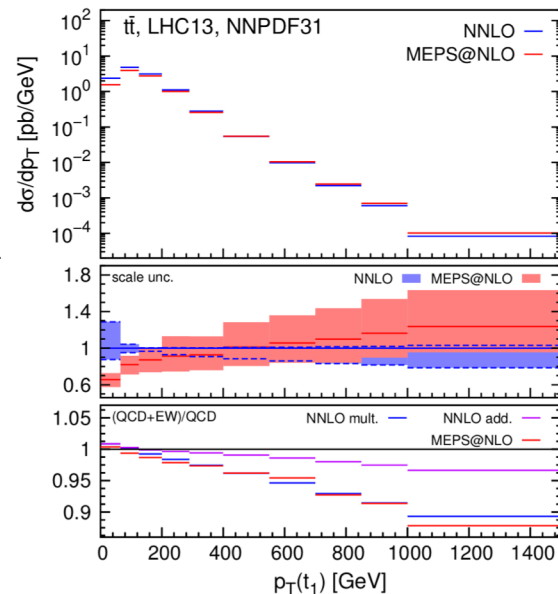
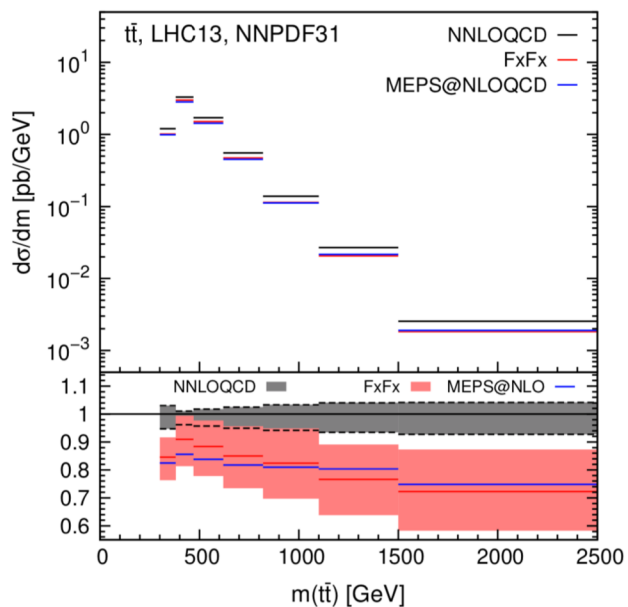
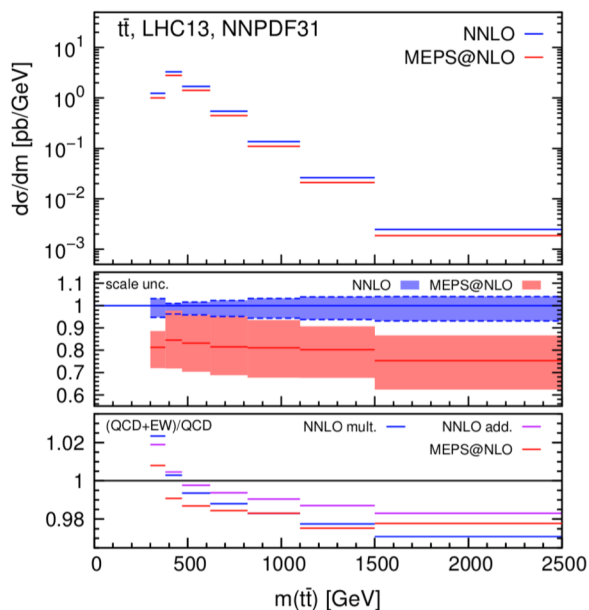
$M_{b\bar{b}}, M_{\ell\ell}, \Delta\phi_{\ell\ell}, p_{T,\ell_1}$



Merging vs Fixed Order

❖ *On-shell tops and EW corrections included*

Not described at Fixed Order



Large discrepancies to Merging

Top-quark physics

- Booming topic with lots of applications and interest outside the QCD community
- Fixed-order perturbation theory and resummation rather well understood
- Nevertheless, lots of work necessary for reliable predictions in the case of decay modelling
- How to include the knowledge in Monte Carlo event generators?