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Theory Predictions for Rare B decays

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SM@LHC 2019, Zurich, April 23rd 2019



Marie Skłodowska-Curie
Actions

Rare Decays (of hadrons)

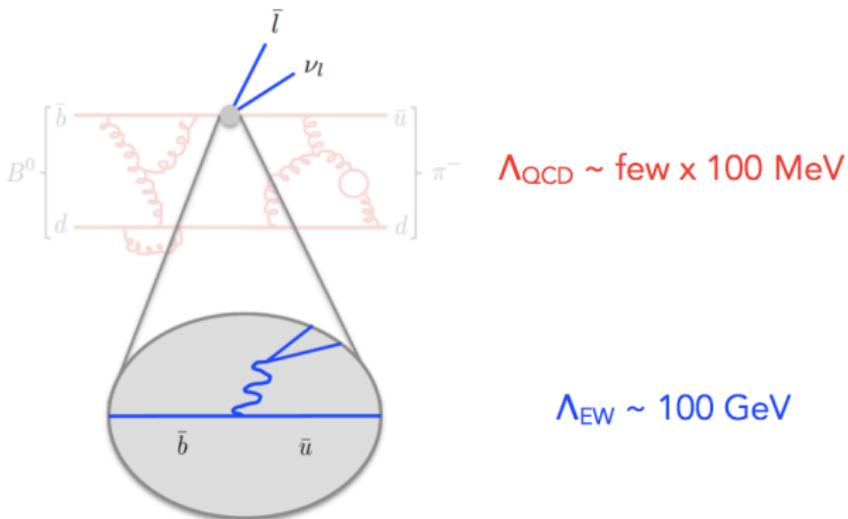
- ▶ Rare decays are those suppressed in the SM by e.g. loop, GIM, helicity, etc. They are very sensitive to BSM contributions.
- ▶ Rare decays have typically $\mathcal{B} < 10^{-6}$. Examples:

$$\begin{array}{lll} \mathcal{B}(K \rightarrow \pi \nu \bar{\nu}) \sim 10^{-11} & \mathcal{B}(K_S \rightarrow \mu^+ \mu^-) \sim 10^{-12} & \mathcal{B}(K \rightarrow \pi \ell \ell) \sim 10^{-7} \\ \mathcal{B}(D \rightarrow \rho \ell \ell) \sim 10^{-9} & \mathcal{B}(B \rightarrow K^* \ell \ell) \sim 10^{-6} & \mathcal{B}(B_s \rightarrow \mu^+ \mu^-) \sim 10^{-9} \end{array}$$

- ▶ Nevertheless, some rare decays are no longer ‘rare’ at the LHC!
E.g. $N(B \rightarrow K^* \mu \mu)_{\text{Run 1}} = 2398 \pm 57$
- ▶ Thus we require now theory predictions with $\sigma_{th} \lesssim 10\%$.

Effective Field Theory

- At scales $\mu \lesssim m_b$: $\mathcal{L}_{(B)\text{SM}} \longrightarrow \mathcal{L}_{\text{WET}} = \mathcal{L}_{\text{QED+QCD}}^{e,\mu,\tau,u,d,s,c,b} + C_i(\mu) \mathcal{O}_i(\mu)$



- EFT is convenient but also necessary.

EFT Predictions

Thus predictions for hadron decay observables require **three** ingredients:

1. Construct the EFT (operators, matching conditions, Anomalous dimensions)

Bobeth, Misiak, Urban '99; Misiak, Steinhauser '04, Gorbahn, Haisch '04; Gorbahn, Haisch, Misiak '05; Czakon, Haisch, Misiak '06
Aebischer, Crivellin, Fael, Greub '16, Aebischer, Fael, Greub, Virto '17, Jenkins, Manohar, Stoffer '17, ...

2. Calculate the decay amplitudes in the EFT, in terms of ‘canonical’ non-perturbative objects (matrix elements).
3. Deal with the non-perturbative matrix elements.

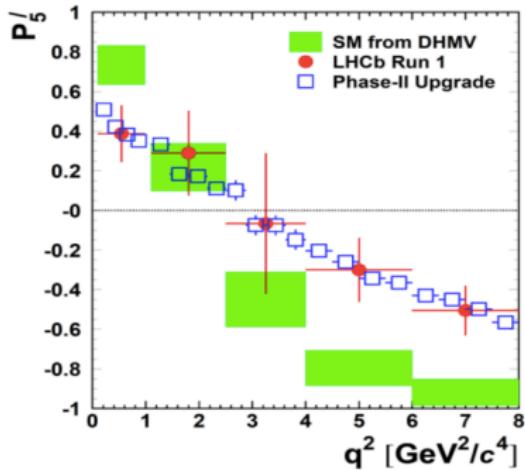
QCD anatomy of heavy-meson decays

Different non-perturbative objects and tools are needed :

1. Inclusive semileptonic:	$B_q \rightarrow X\ell\nu$	HQE
2. Exclusive leptonic:	$B_q \rightarrow \ell\ell$	f_B
3. Inclusive rad./dileptonic:	$B_q \rightarrow X\gamma, X\ell\ell$	HQE + factorization
4. Exclusive semileptonic:	$B_q \rightarrow M\ell\nu$	$F^{B \rightarrow M}$
5. Exclusive rad./dileptonic:	$B_q \rightarrow V\gamma, M\ell\ell$	$F^{B \rightarrow M}$ + factorization
6. Exclusive non-leptonic:	$B_q \rightarrow M_1 M_2$	factorization + $F^{B \rightarrow M}$ + Φ_M
NIOBE®	$B_q \rightarrow M_1 M_2 M_3$	factorization + ???

Plan for the talk

Guidelines from the conveners: Instead of covering everything, focus on selected subtopics of high interest and discuss them in more depth.



CERN-LHCC-2017-003, LHCb EoI (LHCb ~ 2035)

□ Bottleneck is SM uncertainties:
Assuming vanishing exp uncertainties

$$\text{Pull}(P_5^{[2.5, 4.0]}) = 3.5\sigma$$

$$\text{Pull}(P_5^{[4.0, 6.0]}) = 6.5\sigma$$

$$\text{Pull}(P_5^{[6.0, 8.0]}) = 5.4\sigma$$

This talk will focus on Exclusive $b \rightarrow s$ transitions. Proxy for many others.

Plan for the talk

1. Anatomy of $B \rightarrow K^{(*)}\ell\ell$ EFT Amplitudes

2. Local Form Factors

- Lattice vs LCSR
- Large-recoil relations
- Finite-width effects
- q^2 -dependence

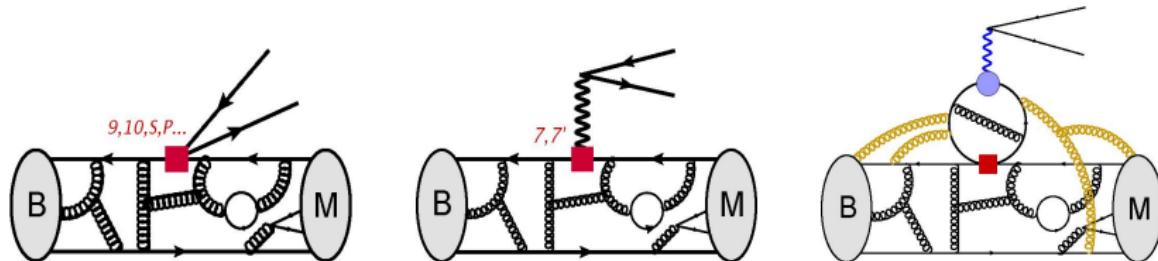
3. Non-Local Form Factors

- Factorization
- z -parametrization
- Tests ‘a posteriori’

4. LCDAs (not covered today)

5. EM corrections (not covered today)

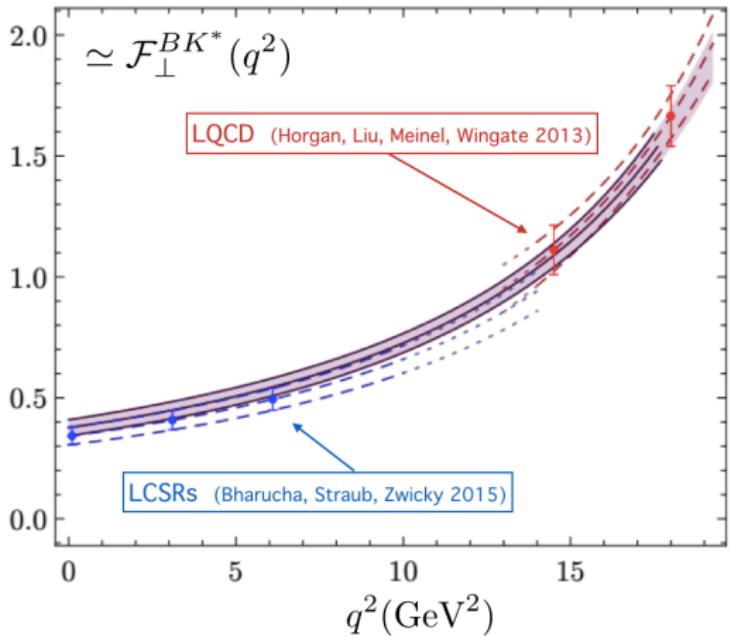
Anatomy of $B \rightarrow M_\lambda \ell^+ \ell^-$ EFT Amplitudes



$$\mathcal{A}_\lambda^{L,R} = \mathcal{N}_\lambda \left\{ (C_9 \mp C_{10}) \mathcal{F}_\lambda(q^2) + \frac{2m_b M_B}{q^2} \left[C_7 \mathcal{F}_\lambda^T(q^2) - 16\pi^2 \frac{M_B}{m_b} \mathcal{H}_\lambda(q^2) \right] \right\}$$

- Local (Form Factors) : $\mathcal{F}_\lambda^{(T)}(q^2) = \langle \bar{M}_\lambda(k) | \bar{s} \Gamma_\lambda^{(T)} b | \bar{B}(k+q) \rangle$
- Non-Local : $\mathcal{H}_\lambda(q^2) = i \mathcal{P}_\mu^\lambda \int d^4x e^{iq \cdot x} \langle \bar{M}_\lambda(k) | T\{\mathcal{J}_{\text{em}}^\mu(x), \mathcal{C}_i \mathcal{O}_i(0)\} | \bar{B}(q+k) \rangle$

'Local' Form Factors



q^2 -dependence :

$$\mathcal{F}(q^2) \propto \sum_k \alpha_k z(q^2)^k$$

"z-parametrization"

Bourrely, Caprini, Lellouch

"Optimized" observables :

$$P_1, P_2, \mathbf{P}'_5, \dots \text{ (a full basis)}$$

Mescia, Matias, Ramon, JV, 1202.4266

Descotes-Genon, Matias, Ramon, JV, 1207.2753

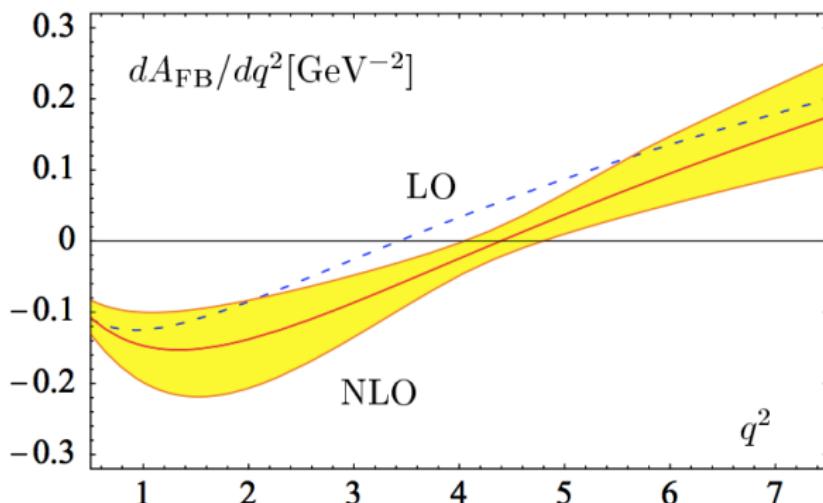
Descotes-Genon, Hurth, Matias, JV, 1303.5794

Finite width effects : $B \rightarrow K^*(\rightarrow K\pi)$
Accessible via LCSRs

Cheng, Khodjamirian, JV, 1701.01633
Cheng, Khodjamirian, JV, 1709.00173

$\mathcal{B}(B \rightarrow K^* \mu\mu)$ Forward-Backward Asymmetry Zero

Beneke, Feldmann, Seidel 2001



Partial cancellation of hadronic uncertainties in the zero-crossing

Hadronic Form Factors at Large Recoil

Beneke, Feldmann 2000; Descotes-Genon, Hofer, Matias, JV 2014

$$\begin{aligned} V(q^2) &= \frac{m_B + m_{K^*}}{m_B} \xi_{\perp}(q^2) + \Delta V^{\alpha_s}(q^2) + \Delta V^{\Lambda}(q^2), \\ A_1(q^2) &= \frac{2E}{m_B + m_{K^*}} \xi_{\perp}(q^2) + \Delta A_1^{\alpha_s}(q^2) + \Delta A_1^{\Lambda}(q^2), \\ A_2(q^2) &= \frac{m_B}{m_B - m_{K^*}} [\xi_{\perp}(q^2) - \xi_{\parallel}(q^2)] + \Delta A_2^{\alpha_s}(q^2) + \Delta A_2^{\Lambda}(q^2), \\ A_0(q^2) &= \frac{E}{m_{K^*}} \xi_{\parallel}(q^2) + \Delta A_0^{\alpha_s}(q^2) + \Delta A_0^{\Lambda}(q^2), \\ T_1(q^2) &= \xi_{\perp}(q^2) + \Delta T_1^{\alpha_s}(q^2) + \Delta T_1^{\Lambda}(q^2), \\ T_2(q^2) &= \frac{2E}{m_B} \xi_{\perp}(q^2) + \Delta T_2^{\alpha_s}(q^2) + \Delta T_2^{\Lambda}(q^2), \\ T_3(q^2) &= [\xi_{\perp}(q^2) - \xi_{\parallel}(q^2)] + \Delta T_3^{\alpha_s}(q^2) + \Delta T_3^{\Lambda}(q^2), \end{aligned}$$

$B \rightarrow K^* \ell \ell$ “Optimized” observables

- ▶ The K^* helicity provides an extra valuable degree of freedom
- ▶ In the Heavy-Quark limit some relations among form factors arise:

e.g.

$$\frac{\epsilon_-^{*\mu} q^\nu \langle K_-^* | \bar{s} \sigma_{\mu\nu} P_R b | B \rangle}{im_B \langle K_-^* | \bar{s} \not{q}^* P_L b | B \rangle} = 1 + \mathcal{O}(\alpha_s, \Lambda/m_b)$$

- ▶ One can build observables that depend only on these ratios, e.g.:

$$P'_5 = \sqrt{2} \frac{\text{Re}(\mathcal{A}_0^L \mathcal{A}_{\perp}^{L*} - \mathcal{A}_0^R \mathcal{A}_{\perp}^{R*})}{\sqrt{|\mathcal{A}_0|^2(|\mathcal{A}_{\perp}|^2 + |\mathcal{A}_{\parallel}|^2)}}$$

A full basis of “optimized” observables exists.

Mescia, Matias, Ramon, JV, 1202.4266

Descotes-Genon, Matias, Ramon, JV, 1207.2753

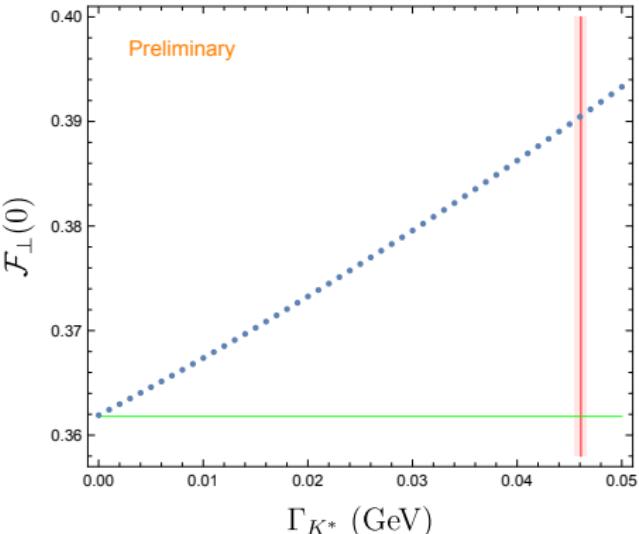
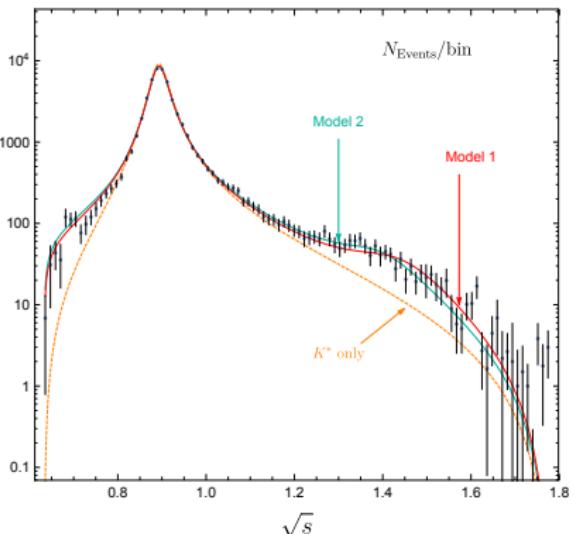
- ▶ These observables should be less sensitive to “miscalculations”.

Finite-width effects

(new)

Khodjamirian, Mannel, Offen 2006; Cheng, Khodjamirian, JV 2017, Descotes-Genon, Khodjamirian, JV, w.i.p.

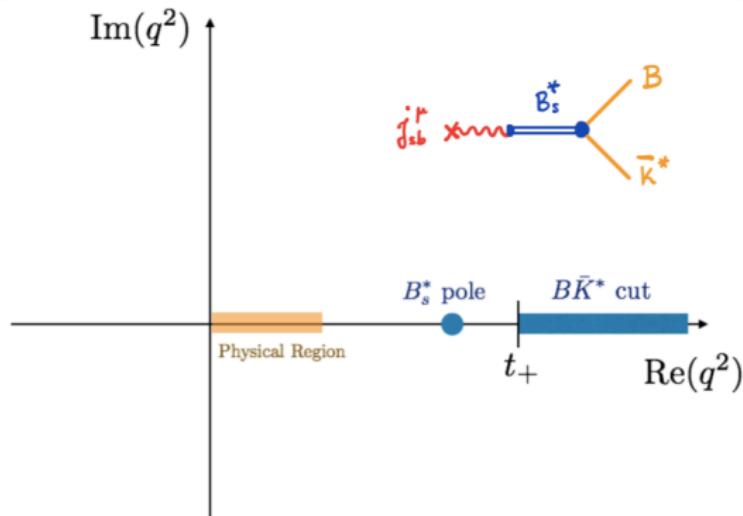
$$\text{Im} \langle 0 | T\{j_{K^*}, j_{sb}\} | B \rangle \sim \langle 0 | j_{K^*} \underbrace{|K^*\rangle\langle K^*|}_{|K\pi\rangle\langle K\pi|} j_{sb} | B \rangle$$



- ▶ Order 10% finite-width effects, similar to $B \rightarrow \rho$ form factors.

Form Factors : q^2 -dependence from analyticity

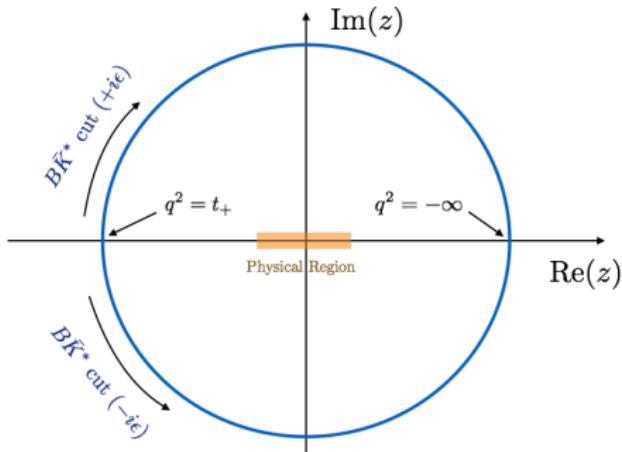
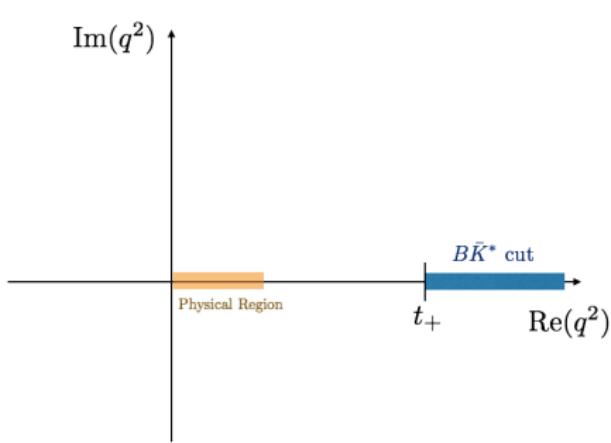
$\mathcal{F}_\lambda^{(T)}(q^2) = \langle \bar{M}_\lambda(k) | \bar{s} \Gamma_\lambda^{(T)} b | \bar{B}(k+q) \rangle$: Analytic structure in q^2 :



$$\widehat{\mathcal{F}}_\lambda^{(T)}(q^2) \equiv (q^2 - m_{B_s^*}^2) \mathcal{F}_\lambda^{(T)}(q^2) \quad \text{has no pole, only cut.}$$

Form Factors : q^2 -dependence from analyticity

► Conformal mapping :
$$z(q^2) = \frac{\sqrt{t_+ - q^2} - \sqrt{t_+ - t_0}}{\sqrt{t_+ - q^2} + \sqrt{t_+ - t_0}}$$



► "z-parametrization" : $\hat{\mathcal{F}}_\lambda^{(T)}(q^2(z))$ is analytic in $|z| < 1$

$$\mathcal{F}_\lambda^{(T)}(q^2) = \frac{1}{(q^2 - m_{B_s^*}^2)} \sum_k \alpha_k z(q^2)^k$$

Bourrely, Caprini, Lellouch

Form Factors : q^2 -dependence from analyticity

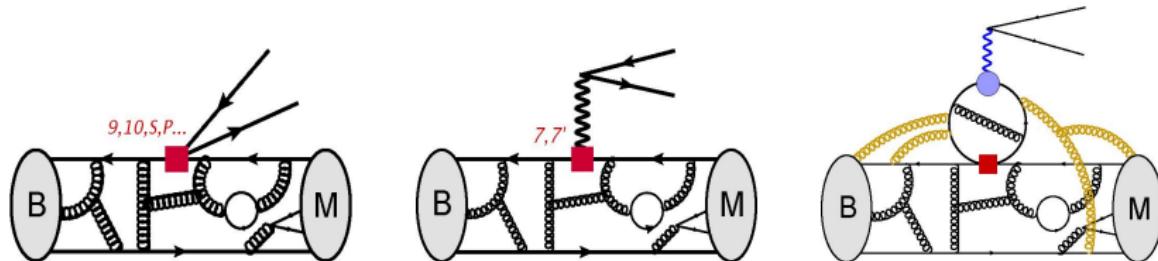
E.g. $B \rightarrow K$ form factors $f_{0,+,\pm T}$ from LQCD

($|z_{\text{phys}}| < 0.15$)

	b_0^+	b_1^+	b_2^+	b_0^0	b_1^0	b_2^0	b_0^T	b_1^T	b_2^T
Mean	0.466	-0.885	-0.213	0.292	0.281	0.150	0.460	-1.089	-1.114
error	0.014	0.128	0.548	0.010	0.125	0.441	0.019	0.236	0.971
b_0^+	1	0.450	0.190	0.857	0.598	0.531	0.752	0.229	0.117
b_1^+		1	0.677	0.708	0.958	0.927	0.227	0.443	0.287
b_2^+			1	0.595	0.770	0.819	-0.023	0.070	0.196
b_0^0				1	0.830	0.766	0.582	0.237	0.192
b_1^0					1	0.973	0.324	0.372	0.272
b_2^0						1	0.268	0.332	0.269
b_0^T							1	0.590	0.515
b_1^T								1	0.897
b_2^T									1

Fermilab-MILC 1509.06235

Anatomy of $B \rightarrow M_\lambda \ell^+ \ell^-$ EFT Amplitudes



$$\mathcal{A}_\lambda^{L,R} = \mathcal{N}_\lambda \left\{ (C_9 \mp C_{10}) \mathcal{F}_\lambda(q^2) + \frac{2m_b M_B}{q^2} \left[C_7 \mathcal{F}_\lambda^T(q^2) - 16\pi^2 \frac{M_B}{m_b} \mathcal{H}_\lambda(q^2) \right] \right\}$$

- ▶ Local (Form Factors) : $\mathcal{F}_\lambda^{(T)}(q^2) = \langle \bar{M}_\lambda(k) | \bar{s} \Gamma_\lambda^{(T)} b | \bar{B}(k+q) \rangle$
- ▶ Non-Local : $\mathcal{H}_\lambda(q^2) = i \mathcal{P}_\mu^\lambda \int d^4x e^{iq \cdot x} \langle \bar{M}_\lambda(k) | T\{\mathcal{J}_{\text{em}}^\mu(x), \mathcal{C}_i \mathcal{O}_i(0)\} | \bar{B}(q+k) \rangle$

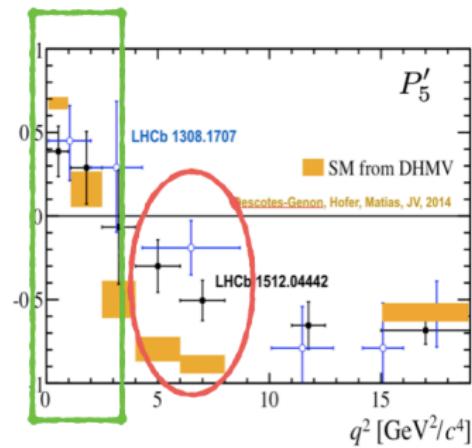
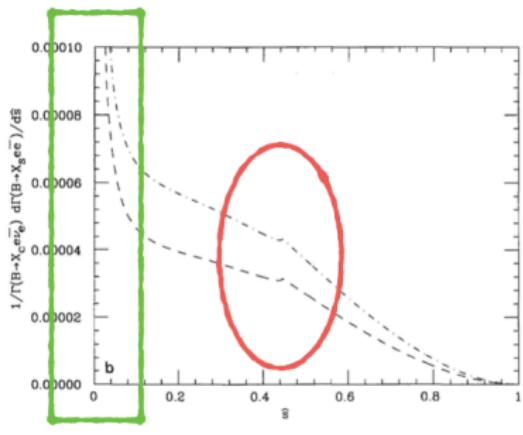
'Non-local' form factors

- QCD Factorization

Beneke, Feldmann, Seidel 2001

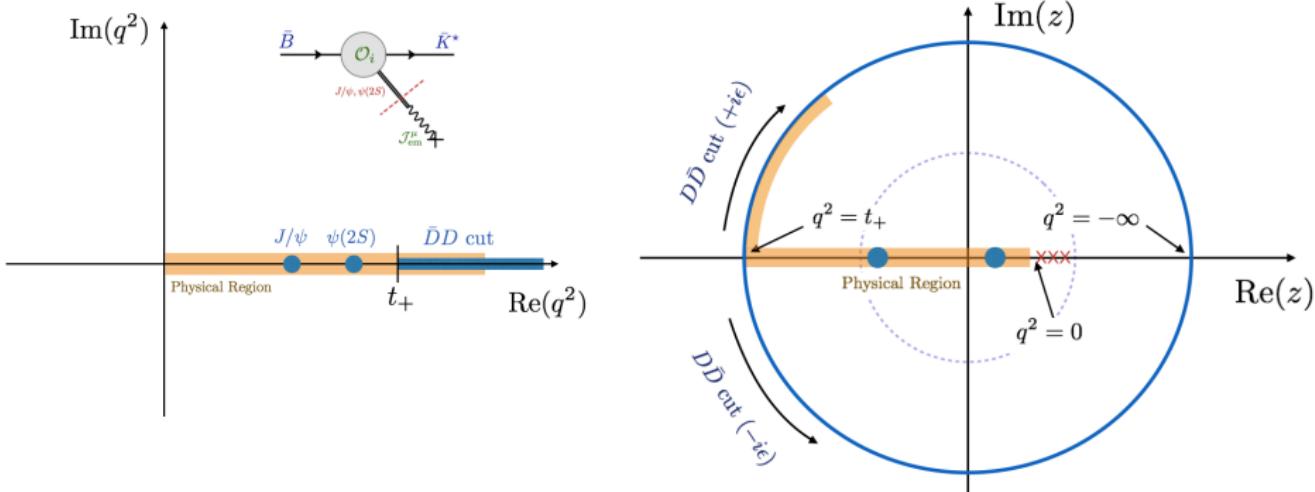
$$\mathcal{H}_\lambda(q^2) \sim \Delta C_9^\lambda(q^2) \mathcal{F}_\lambda(q^2) + \frac{1}{q^2} \Delta C_7^\lambda(q^2) \mathcal{F}_\lambda^T(q^2) + HSS + \mathcal{O}(\Lambda/m_B, \Lambda/E)$$

- It is assumed that the charm loop is dominated by short distances



- Kink at $q^2 = 4m_c^2$ symptom of breaking of perturbativity

Same strategy as form factors!



- $\hat{\mathcal{H}}_\lambda(q^2(z)) = (q^2 - M_{J/\psi}^2)(q^2 - M_{\psi(2S)}^2) \mathcal{H}_\lambda(q^2)$ is analytic in $|z| < 1$

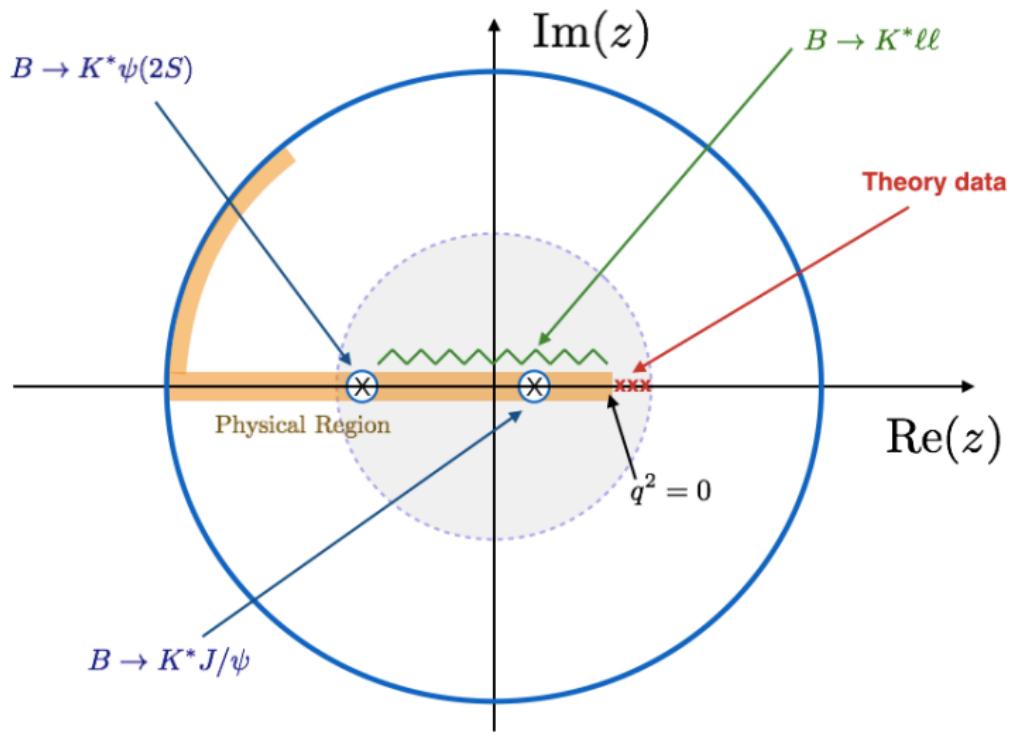
- Taylor expand $\hat{\mathcal{H}}_\lambda(z)$ around $z = 0$:

$$\hat{\mathcal{H}}_\lambda(z) = \left[\sum_{k=0}^K \alpha_k^{(\lambda)} z^k \right] \mathcal{F}_\lambda(z)$$

- Expansion needed for $|z| < 0.52$ ($-7 \text{ GeV}^2 \leq q^2 \leq 14 \text{ GeV}^2$)

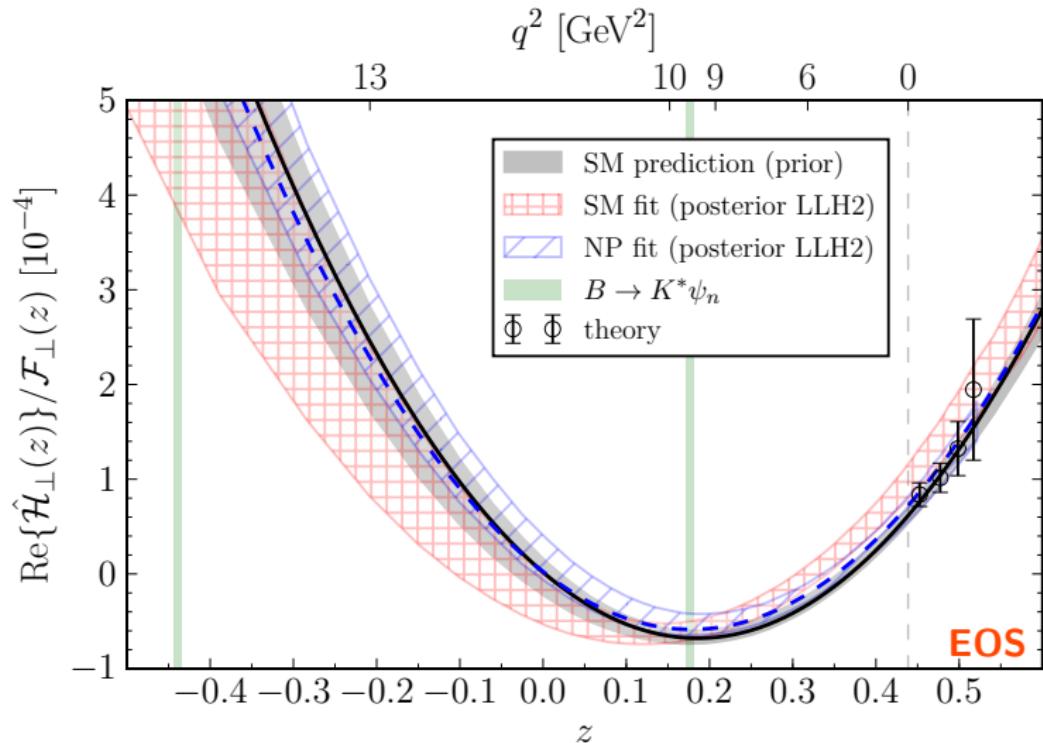
Fit to z -parametrisation

Bobeth, Chruszcz, van Dyk, JV, 1707.07305

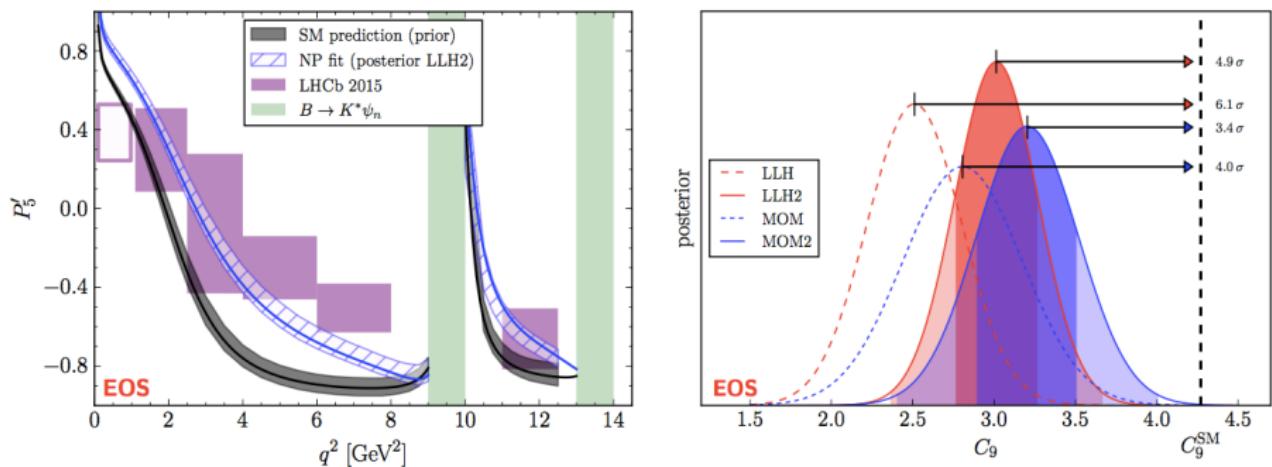


Fit to z -parametrisation

Bobeth, Chrzaszcz, van Dyk, JV, 1707.07305



SM predictions and Fit including $B \rightarrow K^* \mu^+ \mu^-$ data and $\mathcal{C}_9^{\text{NP}}$:

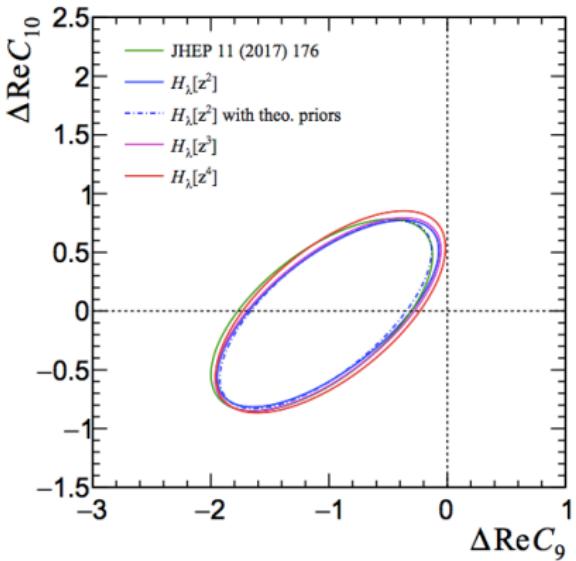
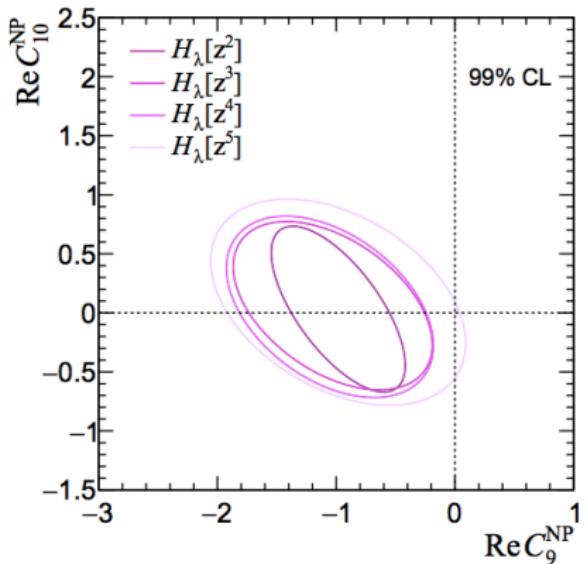


The NP hypothesis with $\mathcal{C}_9^{\text{NP}} \sim -1$ is favored strongly in the global fit

Prospects: LHC Run-2 unbinned fits to z-parametrization

Chrzaszcz, Mauri, Serra, Coutinho, van Dyk 1805.06378

Mauri, Serra, Coutinho 1805.06401

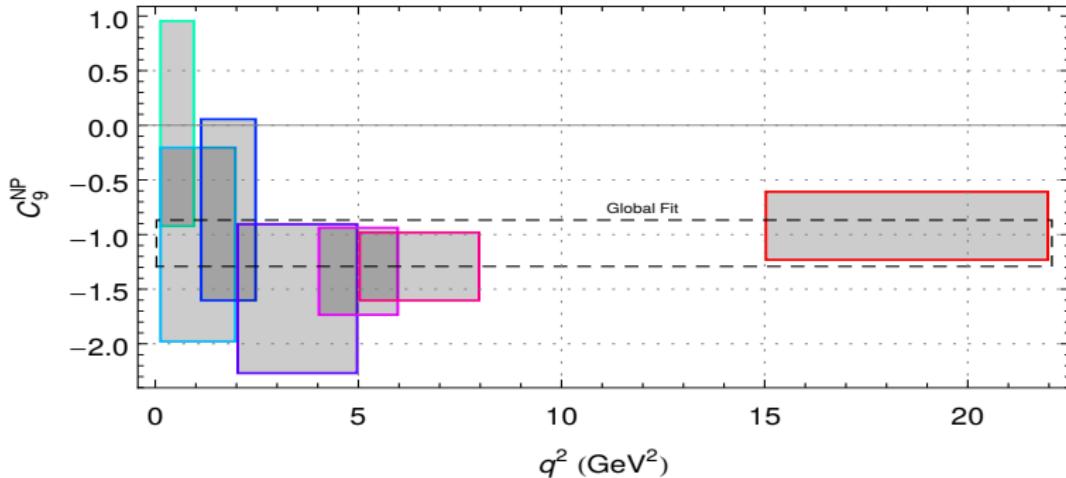


Unbinned fits to $B \rightarrow K^* \mu\mu$ (Left) and $B \rightarrow K^* \ell\ell$ (Right)

'A posteriori' test of non-local effect

- Testing the data : q^2 -dependence

Descotes-Genon, Hofer, Matias, JV 1510.04239



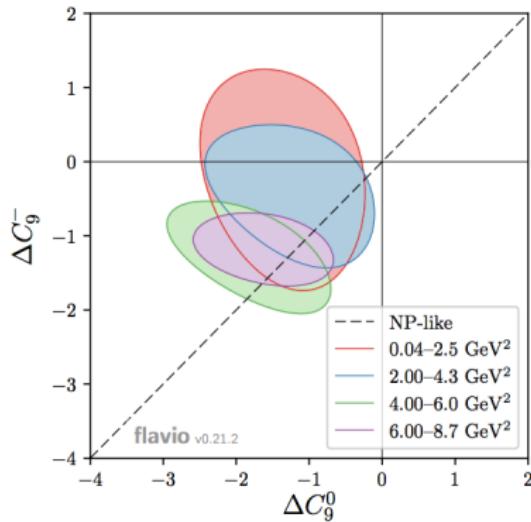
- Tiny uncertainites will allow to test hadronic contributions precisely

See also [Altmannshofer, Straub 1503.06199](#), [Ciuchini et al 1512.07157](#), [Chobanova et al 1702.02234](#)

'A posteriori' test of non-local effect

- Testing the data : K^* -helicity dependence

Altmannshofer, Niehoff, Stangl, Straub 1703.09189



- Tiny uncertainites will allow to test hadronic contributions precisely

Summary

- ▶ EFT Predictions for rare decays are limited by the determination of '**local**' and '**non-local**' form factors.
- ▶ For '**local**' form factors LQCD is promising, but:
 1. Need LCSR s for q^2 interpolation
 2. Finite width effects can be sizeable (currently beyond LQCD)
 3. Optimize observables exist, but **power corrections**
- ▶ The '**non-local**' form factors are the focus of most current efforts
 1. Need new ideas from LQCD
 2. Analyticity methods promising, but still rely on factorization @ $q^2 < 0$
 3. Unitarity bounds?
 4. 'A posteriori' tests / combined fits to NP and data promising @ Phase II.
- ▶ Many things left out (large q^2 , baryonic, inclusive, EM corrections, ...)

Thank you

Extra slides

Experimental constraints on z parametrisation $[B \rightarrow K^* \ell \ell]$

Bobeth, Chrzaszcz, van Dyk, Virto 2017

Experimental constraints :

- ▶ The residues of the poles are given by $B \rightarrow K^* \psi_n$:

$$\mathcal{H}_\lambda(q^2 \rightarrow M_{\psi_n}^2) \sim \frac{M_{\psi_n} f_{\psi_n}^* \mathcal{A}_\lambda^{\psi_n}}{M_B^2(q^2 - M_{\psi_n}^2)} + \dots$$

- ▶ Angular analyses **Belle**, **Babar**, **LHCb** determine :

$$|r_\perp^{\psi_n}|, |r_\parallel^{\psi_n}|, |r_0^{\psi_n}|, \arg\{r_\perp^{\psi_n} r_0^{\psi_n*}\}, \arg\{r_\parallel^{\psi_n} r_0^{\psi_n*}\},$$

$$\text{where } r_\lambda^{\psi_n} \equiv \underset{q^2 \rightarrow M_{\psi_n}^2}{\text{Res}} \frac{\mathcal{H}_\lambda(q^2)}{\mathcal{F}_\lambda(q^2)} \sim \frac{M_{\psi_n} f_{\psi_n}^* \mathcal{A}_\lambda^{\psi_n}}{M_B^2 \mathcal{F}_\lambda(M_{\psi_n}^2)}$$

- ▶ We produce correlated pseudo-observables from a fit (5+5).

Prior Fit to z parametrisation $[B \rightarrow K^* \ell \ell]$

Bobeth, Chrzaszcz, van Dyk, Virto 2017

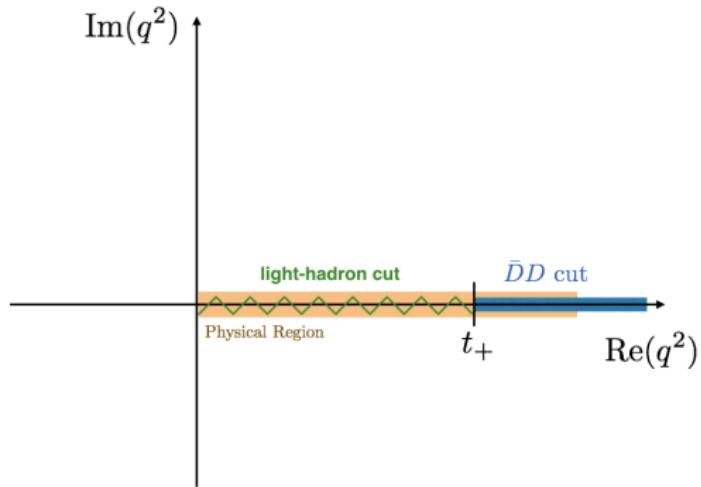
(Prior) Fit to Experimental and theoretical pseudo-observables :

k	0	1	2
$\text{Re}[\alpha_k^{(\perp)}]$	-0.06 ± 0.21	-6.77 ± 0.27	18.96 ± 0.59
$\text{Re}[\alpha_k^{(\parallel)}]$	-0.35 ± 0.62	-3.13 ± 0.41	12.20 ± 1.34
$\text{Re}[\alpha_k^{(0)}]$	0.05 ± 1.52	17.26 ± 1.64	-
$\text{Im}[\alpha_k^{(\perp)}]$	-0.21 ± 2.25	1.17 ± 3.58	-0.08 ± 2.24
$\text{Im}[\alpha_k^{(\parallel)}]$	-0.04 ± 3.67	-2.14 ± 2.46	6.03 ± 2.50
$\text{Im}[\alpha_k^{(0)}]$	-0.05 ± 4.99	4.29 ± 3.14	-

Table 1: Mean values and standard deviations (in units of 10^{-4}) of the prior PDF for the parameters $\alpha_k^{(\lambda)}$.

Light-hadron cut

The non-local ME of $O_{1,2}^c$ also contains a cut at low q^2 from intermediate “light-hadron” states:



$$\text{Disc}[\mathcal{H}_\lambda(\textcolor{blue}{q}^2 > t_+)] \sim \sum_X \langle 0 | j_{\text{em}} | X_{cc}^{1--} \rangle \langle X_{cc}^{1--} K^* | (\bar{s}c)(\bar{c}b) | \bar{B} \rangle$$

$$\text{Disc}[\mathcal{H}_\lambda(0 < q^2 < t_+)] \sim \sum_X \langle 0 | j_{\text{em}} | X^{1--} \rangle \langle X^{1--} K^* | (\bar{s}c)(\bar{c}b) | \bar{B} \rangle$$

Light-hadron cut

★ Support for $\langle X^{1--} K^* | (\bar{s}c)(\bar{c}b) | \bar{B} \rangle \ll \langle X_{cc}^{1--} K^* | (\bar{s}c)(\bar{c}b) | \bar{B} \rangle$:

► OZI rule.

► $\mathcal{B}(B \rightarrow K^{(*)}\omega) \approx 2 - 5 \cdot 10^{-6}$ (in agr. with QCDF from $[\bar{s}q][\bar{q}b]$)

$$\Rightarrow \langle K^*\omega | (\bar{s}c)(\bar{c}b) | \bar{B} \rangle \lesssim \underbrace{C_q/C_c}_{\text{few \%}} \langle K^*\omega | (\bar{s}q)(\bar{q}b) | \bar{B} \rangle$$

► Same argument for $\mathcal{B}(B \rightarrow K^{(*)}\phi)$

► In absence of OZI, the natural size of these BRs is 10^{-3} not 10^{-6} :

$$\mathcal{B}(B \rightarrow KJ/\psi) = 9 \times 10^{-4} \quad \mathcal{B}(B \rightarrow K^*J/\psi) = 1.3 \times 10^{-3}$$

$$\mathcal{B}(B \rightarrow K[D^*\bar{D}]) = 6 \times 10^{-3} \quad \mathcal{B}(B \rightarrow K[D^*\bar{D}^*]) = 8 \times 10^{-3}$$

$$\mathcal{B}(B \rightarrow K[D\bar{D}]) = 5 \times 10^{-4}$$

► Note also the **total** BR: $\mathcal{B}(B \rightarrow K^{(*)}[\bar{K}K]) \sim 10^{-5} \ll 10^{-3}$

► Test: $\mathcal{B}(B \rightarrow K^{(*)}X^{1--}(\text{high mass})) \ll 10^{-3}$

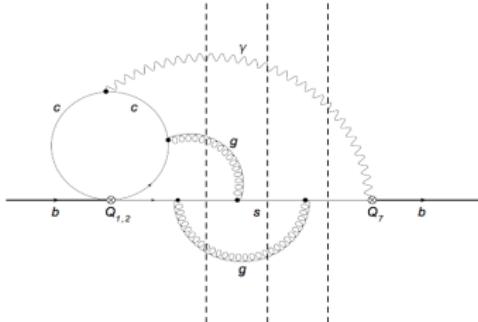
Light-hadron cut

Conclusion: OZI → Two order of magnitude suppression.

- ▶ But CKM- and penguin-suppressed light-quark loops are there.
- ▶ Not OZI suppressed.
- ▶ Must be constrained if precision is sought (but rough estimate might suffice).
- ▶ Can do dispersive analysis [Khodjamirian, Mannel, Wang 2012 ...](#)
- ▶ Could use $b \rightarrow d$ analogues + U-spin.

Inclusive Heavy Meson Decay:

- Optical Theorem
- Heavy-Quark Expansion
- Subleading Shape Functions



$$\Gamma(\bar{B} \rightarrow X_s \gamma)_{E_0} = \underbrace{\Gamma(b \rightarrow s\gamma) + \Gamma(b \rightarrow sg\gamma)}_{\text{Known @ NNLO}^{(1)}} + \underbrace{\Gamma(b \rightarrow sq\bar{q}\gamma)}_{\text{Known @ NLO}^{(2)}} + \dots + \underbrace{\mathcal{O}(1/m_b)}_{\sim 5\%^{(3)}}$$

⁽¹⁾ Misiak et al (many papers) and a tiny few w/o Misiak

⁽²⁾ Huber, Poradzinski, JV, 1411.7677

⁽³⁾ For $E_0 \sim 1.6$ GeV, Benzke, Lee, Neubert, Paz, 1003.5012

$$\mathcal{B}_{s\gamma}^{\text{th}} = (3.36 \pm 0.23) \cdot 10^{-4} \text{ (7\%)}^{(4)} \quad \text{vs.} \quad \mathcal{B}_{s\gamma}^{\text{exp}} = (3.43 \pm 0.22) \cdot 10^{-4} \text{ (6\%)}^{(5)}$$

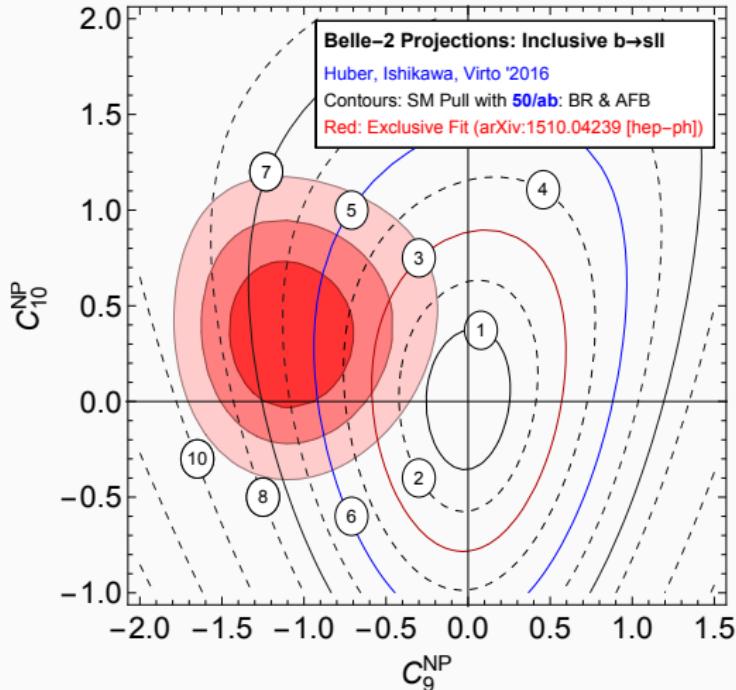
⁽⁴⁾ Misiak, JV, et al, 1503.01789

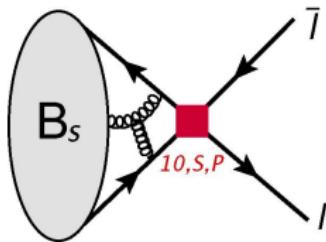
⁽⁵⁾ CLEO + BaBar + Belle

Note : $\Gamma_{LO} \sim |\mathcal{C}_7|^2 + |\mathcal{C}'_7|^2$

Complementarity with inclusive measurements at Belle-2

- Belle-II is directly sensitive to the $b \rightarrow s$ anomaly with $B \rightarrow X_s \mu^+ \mu^-$





$$\propto \langle 0 | \bar{s} \gamma^\mu \gamma_5 b | B_s \rangle \equiv f_{B_s} p_B^\mu \quad (\text{Decay Constant})$$

	LQCD ⁽¹⁾	QCDSRs ⁽²⁾
f_B	186(4)	207(17)
f_{B_s}	224(5)	242(17)

⁽¹⁾ FLAG 1607.00299 ; ⁽²⁾ Gelhausen, Khodjamirian, Pivovarov, Rosenthal 1305.5432

$$BR(B_s \rightarrow \ell \bar{\ell}) = \frac{\tau_{B_s} f_{B_s}^2 m_{B_s}^3}{2\pi} \sqrt{1 - \frac{4m_\ell^2}{m_{B_s}^2}} |\mathcal{C}_P^-|^2 + \left| \mathcal{C}_P^- + \frac{2m_\ell}{m_{B_s}} (\mathcal{C}_{10} - \mathcal{C}'_{10}) \right|^2$$

$$\bar{\mathcal{B}}_{s\mu}^{\text{th}} = (3.65 \pm 0.23) \cdot 10^{-9} \ (6.4\%)^{(3)} \quad \text{vs.} \quad \bar{\mathcal{B}}_{s\mu}^{\text{exp}} = (2.9 \pm 0.7) \cdot 10^{-9} \ (24\%)^{(4)}$$

(main th. uncertainties: f_B and CKM ; exp: statistic-dominated)

⁽³⁾ Bobeth, Gorbahn, Hermann, Misiak, Stamou, Steinhauser'2014 ; ⁽⁴⁾ CMS+LHCb 1411.4413

$B_s \rightarrow \mu^+ \mu^-$	$B \rightarrow X_s \mu^+ \mu^-$	$B \rightarrow K^* \gamma$	$B \rightarrow X_s \gamma$
$B \rightarrow K \mu \mu$	$B \rightarrow K^* \mu \mu$	$B_s \rightarrow \Phi \mu \mu$	$\Lambda_b \rightarrow \Lambda \mu \mu$
BRs	AOs	Low q^2	Large q^2
R_K	R_{K^*}	LFU	LFUV
LHCb	Belle/BaBar	ATLAS	CMS

“Anomalies”

- Observables with larger pulls:

Largest pulls	$\langle P'_5 \rangle_{[4,6]}$	$\langle P'_5 \rangle_{[6,8]}$	$R_K^{[1,6]}$	$R_{K^*}^{[0.045,1.1]}$	$R_{K^*}^{[1.1,6]}$	$\mathcal{B}_{B_s \rightarrow \phi \mu^+ \mu^-}^{[2,5]}$	$\mathcal{B}_{B_s \rightarrow \phi \mu^+ \mu^-}^{[5,8]}$
Experiment	-0.30 ± 0.16	-0.51 ± 0.12	$0.745^{+0.097}_{-0.082}$	$0.66^{+0.113}_{-0.074}$	$0.685^{+0.122}_{-0.083}$	0.77 ± 0.14	0.96 ± 0.15
SM prediction	-0.82 ± 0.08	-0.94 ± 0.08	1.00 ± 0.01	0.92 ± 0.02	1.00 ± 0.01	1.55 ± 0.33	1.88 ± 0.39
Pull (σ)	-2.9	-2.9	+2.6	+2.3	+2.6	+2.2	+2.2
Prediction for $\mathcal{C}_{9\mu}^{\text{NP}} = -1.1$	-0.50 ± 0.11	-0.73 ± 0.12	0.79 ± 0.01	0.90 ± 0.05	0.87 ± 0.08	1.30 ± 0.26	1.51 ± 0.30
Pull (σ)	-1.0	-1.3	+0.4	+1.9	+1.2	+1.8	+1.6

Effective Theory for $b \rightarrow s$ Transitions

For $\Lambda_{\text{EW}}, \Lambda_{\text{NP}} \gg M_B$: General model-indep. parametrization of NP :

$$\mathcal{L}_W = \mathcal{L}_{\text{QCD}} + \mathcal{L}_{\text{QED}} + \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* \sum_i \mathcal{C}_i(\mu) \mathcal{O}_i(\mu)$$

$$\mathcal{O}_1 = (\bar{c}\gamma_\mu P_L b)(\bar{s}\gamma^\mu P_L c) \quad \mathcal{O}_2 = (\bar{c}\gamma_\mu P_L T^a b)(\bar{s}\gamma^\mu P_L T^a c)$$

$$\mathcal{O}_7 = \frac{e}{16\pi^2} m_b (\bar{s}\sigma_{\mu\nu} P_R b) F^{\mu\nu} \quad \mathcal{O}_{7'} = \frac{e}{16\pi^2} m_b (\bar{s}\sigma_{\mu\nu} P_L b) F^{\mu\nu}$$

$$\mathcal{O}_{9e} = \frac{\alpha}{4\pi} (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \ell) \quad \mathcal{O}_{9'e} = \frac{\alpha}{4\pi} (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \ell)$$

$$\mathcal{O}_{10e} = \frac{\alpha}{4\pi} (\bar{s}\gamma_\mu P_L b)(\bar{\ell}\gamma^\mu \gamma_5 \ell) \quad \mathcal{O}_{10'e} = \frac{\alpha}{4\pi} (\bar{s}\gamma_\mu P_R b)(\bar{\ell}\gamma^\mu \gamma_5 \ell),$$

SM contributions to $\mathcal{C}_i(\mu_b)$ known to NNLL Bobeth, Misiak, Urban '99; Misiak, Steinhauser '04, Gorbahn, Haisch '04;

Gorbahn, Haisch, Misiak '05; Czakon, Haisch, Misiak '06

$$\mathcal{C}_{7\text{eff}}^{\text{SM}} = -0.3, \mathcal{C}_9^{\text{SM}} = 4.1, \mathcal{C}_{10}^{\text{SM}} = -4.3, \mathcal{C}_1^{\text{SM}} = 1.1, \mathcal{C}_2^{\text{SM}} = -0.4, \mathcal{C}_{\text{rest}}^{\text{SM}} \lesssim 10^{-2}$$

