



# Future Perspective of Particle Physics (& Astrophysics)

**3<sup>rd</sup> KNO Workshop**

**(November 2, 2018, KNU)**

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This is only **my personal perspective**  
in year **2018 !!!**





Maybe ??



# Maybe ??

- Supersymmetry  .....  String

# Maybe ??

- Supersymmetry  .....
  - Extra Dimensions (ADD, UED, RS, ....) 
  - Extended Higgs
- String

# Maybe ??

- Supersymmetry  .....  String
- Extra Dimensions (ADD, UED, RS, ....)
- Extended Higgs
- Strong CP, Axion
- GUT, guts, extra U(1)'s, .....
- Naturalness, Hierarchy, Fine tuning, .....
- .....
- .....
- Unparticles
- Clockworks

Could be ?

# Could be ?

- Dark energy 
- Quark-gluon plasma

modified GR



# Could be ?

- Dark energy → modified GR
- Quark-gluon plasma
- Baryogenesis → Leptogenesis
- Inflation → Multiverse



Must be !

# Must be !

- Gravitational wave 

Graviton

# Must be !

- Gravitational wave
- Dark Matter



Graviton

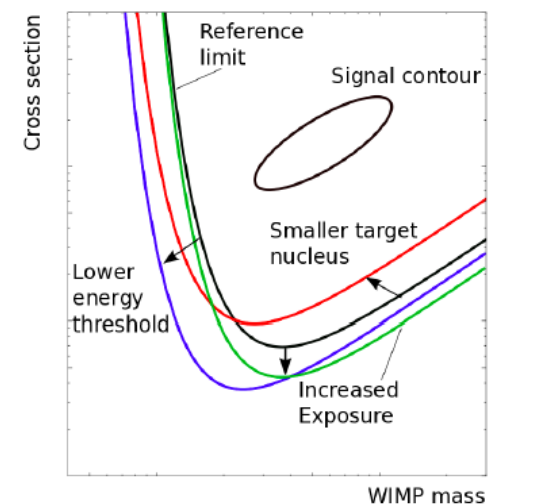
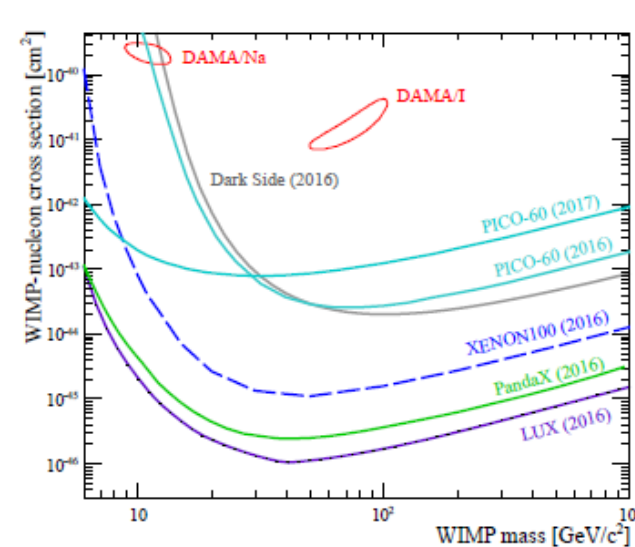
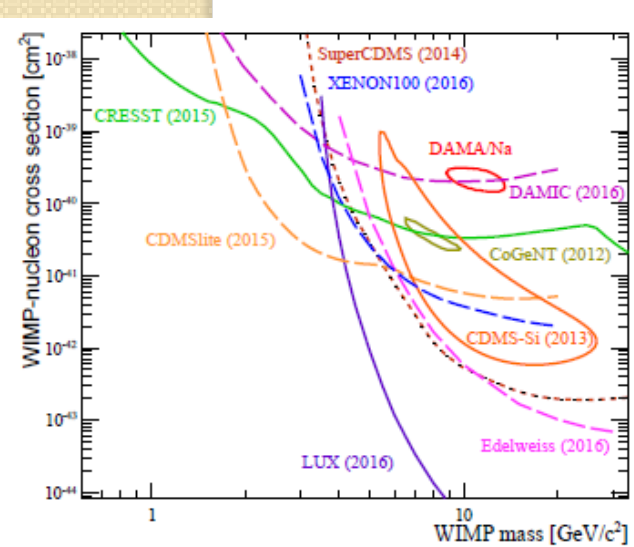
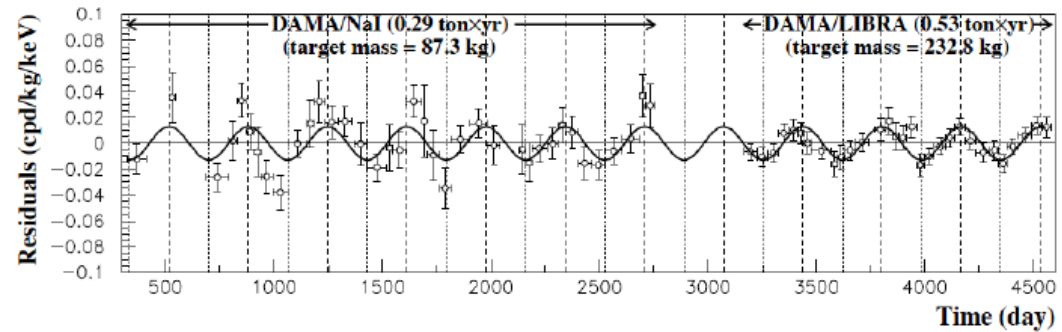
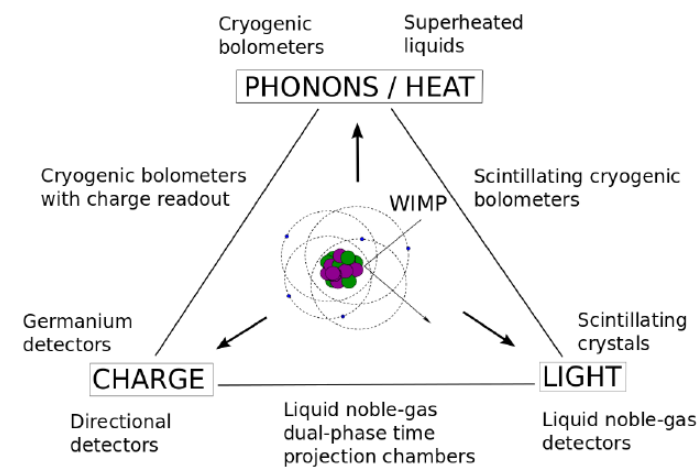
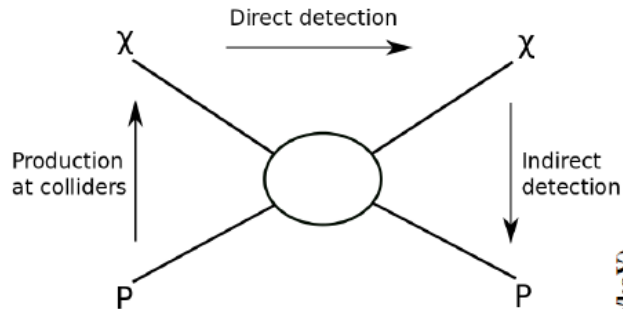
# Must be !

- Gravitational wave →
- Dark Matter
- Neutrino

Graviton

# Dark Matter

- [arXiv:1509.08762v2](https://arxiv.org/abs/1509.08762v2)



# Neutrinos (mass, PMNS, CP)

- ❖ In the SM, neutrinos are
  - ◆ massless ( $m_\nu = 0$ ) and
  - ◆ only left-handed ( $\nu_L$ ). No right-handed neutrinos ( $\nu_R$ ) observed yet.
- ❖ Giving neutrinos mass in the SM is possible iff we introduce  $\nu_R$ ,

$$\mathcal{L}_{\text{SM}} \supset -m_\nu (\bar{\nu}_R \nu_L + \bar{\nu}_L \nu_R), \quad \text{where} \quad m_\nu = \frac{Y_\nu v}{\sqrt{2}},$$

$Y_\nu$  = Higgs-neutrino Yukawa coupling constant,

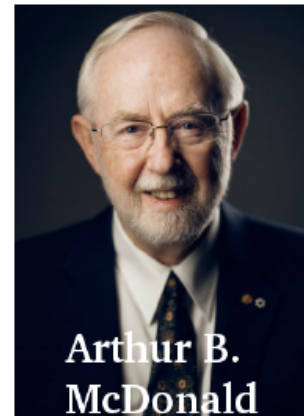
$v$  = Higgs VEV.

- ❖ neutrino oscillation  $\implies m_\nu \neq 0$ .
- ❖ **Nobel Prize in Physics 2015**

“for the discovery of neutrino oscillations, which shows that neutrinos have mass”.



Takaaki Kajita



Arthur B.  
McDonald

There are various suggestions as to how neutrinos can get mass.

❖ **Dirac mass:**

◆ *Assumption:*  $\nu_R$  exists.

◆ *Lagrangian:*

$$\mathcal{L}_{\text{mass}}^D = -m_\nu^D (\overline{\nu}_R \nu_L + \overline{\nu}_L \nu_R).$$

◆ *Disadvantage:* No reason for  $m_\nu^D$  to be small.

◆ *Challenge:* Finding  $\nu_R$ .

❖ **Majorana mass:**

◆ *Assumption:* neutrino  $\equiv$  anti-neutrino.

◆ *Lagrangian:*

$$\mathcal{L}_{\text{mass}}^M = \frac{1}{2} m_\nu^M (\overline{\nu}_L^C \nu_L + \overline{\nu}_L \nu_L^C).$$

◆ *Disadvantage:*  $\mathcal{L}_{\text{mass}}^M$  is not invariant under  $SU(2)_L \times U(1)_Y$  gauge group  
 $\therefore \mathcal{L}_{\text{mass}}^M$  is not allowed by SM.

◆ *Challenge:* To ascertain the Majorana nature of light neutrino.



❖ **See-saw mechanism:** A simpler version of Dirac-Majorana mass, with a nice twist.

◆ *Assumptions:*  $m_\nu^L = 0$  and  $m_\nu^D \ll m_\nu^R$ .

◆ *Lagrangian:*

$$\begin{aligned}\mathcal{L}_{\text{mass}}^{D+M} &= \frac{1}{2} m_\nu^R (\overline{\nu}_R^C \nu_R) - m_\nu^D (\overline{\nu}_R \nu_L) + \text{H.c.} \\ &= \frac{1}{2} (m_1 \overline{\nu}_1^C \nu_1 + m_2 \overline{\nu}_2^C \nu_2) + \text{H.c.},\end{aligned}$$

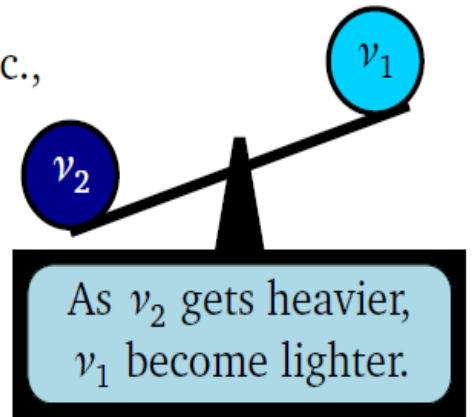
where  $m_1 \approx -\frac{(m_\nu^D)^2}{m_\nu^R}$  and  $m_2 \approx m_\nu^R$ .

◆ *Advantage:*  $m_1 \ll m_2 \implies \nu_1$  is a light neutrino

◆ *Challenges:*

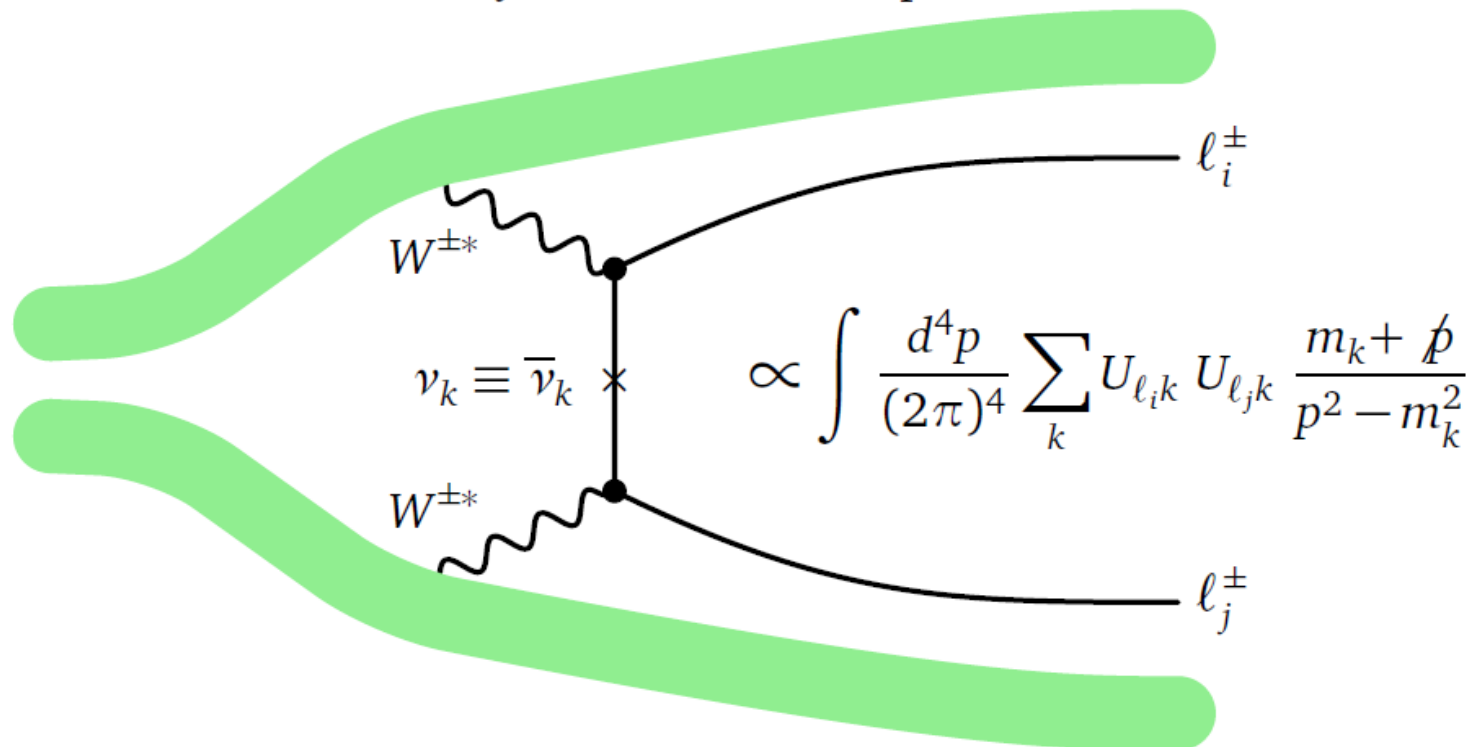
➔ To find the heavy  $\nu_2$  experimentally.

➔ To prove that both the light  $\nu_1$  and heavy  $\nu_2$  are Majorana neutrinos.



# Looking for Majorana neutrinos via $\Delta L = 2$ processes

- ❖ Neutrinos: the only known *elementary fermions* that can have Majorana nature ( $\nu \equiv \bar{\nu}$ ).
- ❖ Majorana neutrino: very unique phenomenology (lepton number non-conservation), they mediate  $\Delta L = 2$  processes.



- ❖  $\Delta L = 2$  processes play crucial role to probe Majorana nature of  $\nu$ 's.
  - ◆ neutrinoless double-beta ( $0\nu\beta\beta$ ) decay
  - ◆ Rare meson decays with  $\Delta L = 2$
  - ◆ Collider searches at LHC

- ❖ Decay rate of any  $\Delta L = 2$  process with final leptons  $\ell_1^+ \ell_2^+$ :

$$\Gamma_{\Delta L=2} \propto \left| \sum_k U_{\ell_1 k} U_{\ell_2 k} \frac{m_k}{p^2 - m_k^2 + im_k \Gamma_k} \right|^2,$$

where we have used the fact that  $(1 - \gamma^5) \not{p}(1 - \gamma^5) = 0$ .

- ◆ Light  $\nu$ :

$$\Gamma_{\Delta L=2} \propto \left| \sum_k U_{\ell_1 k} U_{\ell_2 k} m_k \right|^2 = |m_{\ell_1 \ell_2}|^2.$$

- ◆ Heavy  $\nu$ :

$$\Gamma_{\Delta L=2} \propto \left| \sum_k \frac{U_{\ell_1 k} U_{\ell_2 k}}{m_k} \right|^2.$$

- ◆ Resonant  $\nu$ :

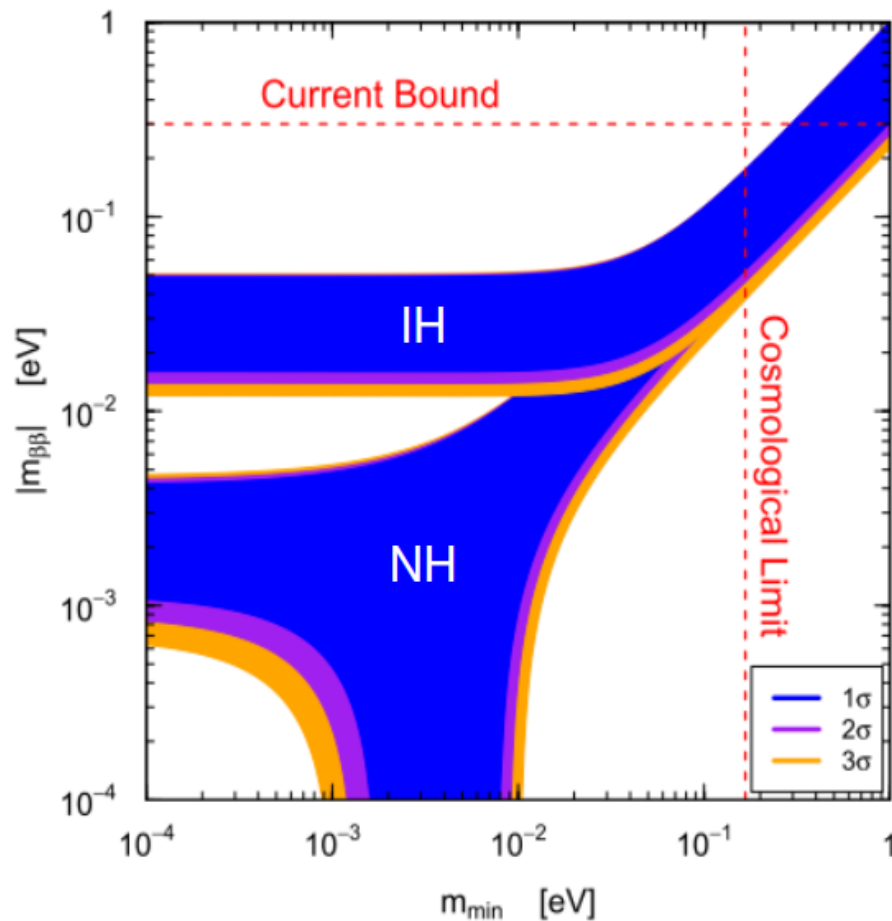
$$\Gamma_{\Delta L=2} \propto \frac{\Gamma(N \rightarrow i) \Gamma(N \rightarrow f)}{m_N \Gamma_N}.$$

- ❖ The half-life of a nucleus decaying via  $0\nu\beta\beta$  is,

$$\left[ T_{1/2}^{0\nu} \right]^{-1} = G_{0\nu} |M_{0\nu}| |m_{\beta\beta}|^2,$$

where

- ◆  $G_{0\nu}$  is phase space factor,
- ◆  $M_{0\nu}$  is the *nuclear matrix element*, (large theoretical uncertainty)
- ◆  $m_{\beta\beta}$  is *effective Majorana mass*.  $m_{\beta\beta} = \sum_{k=1}^3 U_{ek}^2 m_k$  is complex, in general, and can be zero due to possible cancellations arising from phases in  $U_{ek}$ .



NH: Normal hierarchy  
 IH: Inverted hierarchy

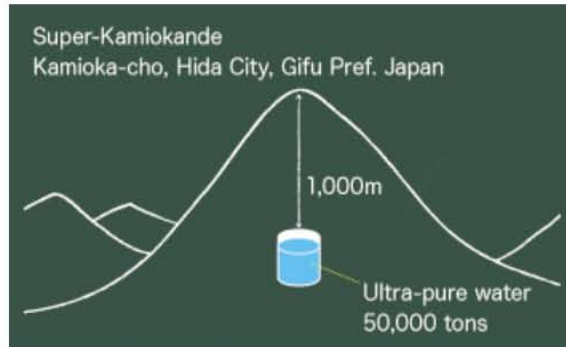
S. M. Bilenky and C. Giunti

Mod. Phys. Lett. A 27, 1230015 (2012),

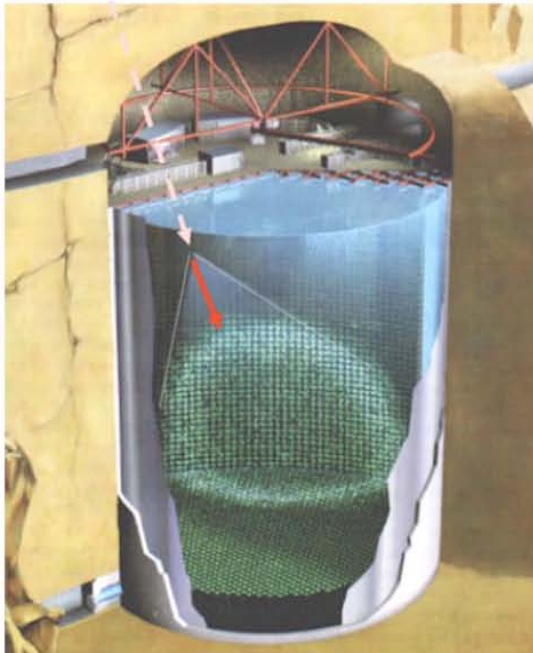
arXiv:1203.5250

- ❖ If  $m_{\beta\beta} < 10^{-2}$ , only NH is viable and the  $T_{1/2}^{0\nu}$  will be much larger than the current experimental lower bound.

# Neutrinos (mass, PMNS, CP)



Super-K



Super-K → Hyper-K

Currently running exp.

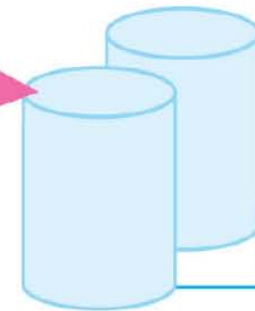
Future exp.

20 times in  
fiducial volume

50,000 tons



Super-Kamiokande



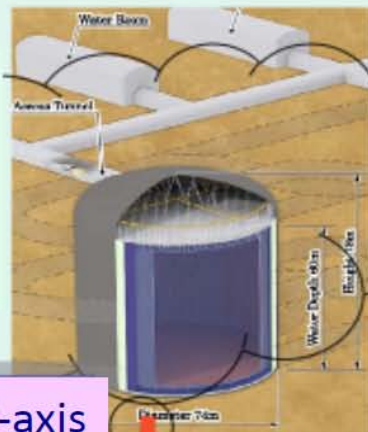
2 X 260 kton

520,000 tons

Hyper-Kamiokande

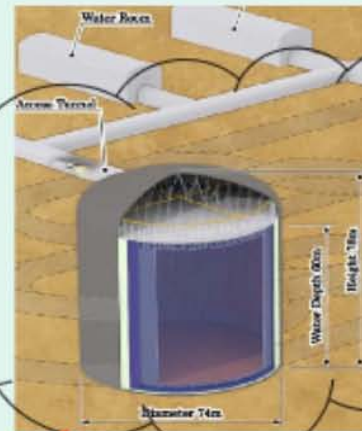
# 2<sup>nd</sup> Hyper-K Detector in Korea

**KNO**  
Korean  
Neutrino  
Observatory



1~3 deg. off-axis

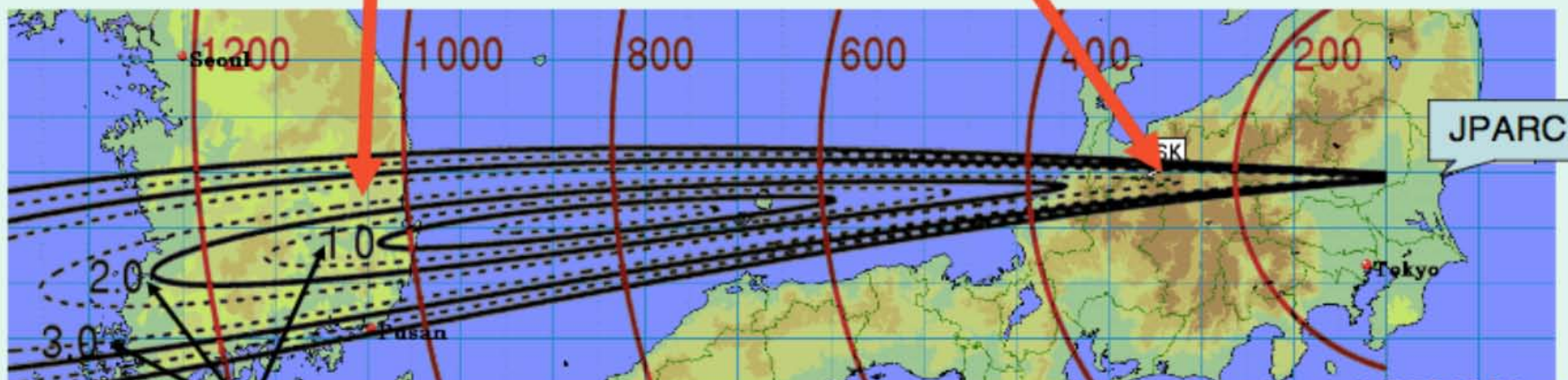
**T2HKK**



**Hyper-K**

2.5 deg. off axis

**The J-PARC  $\nu$  beam comes to Korea.**



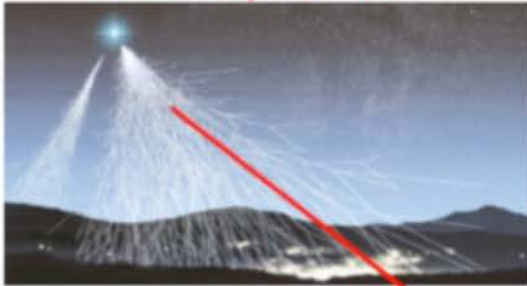
**Off-axis angle**

see hep-ph/0504061

By K. Hagiwara, N. Okamura, K. Senda

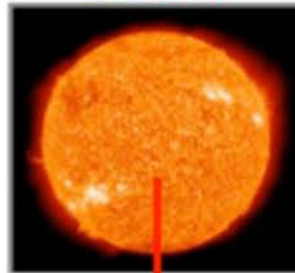
# Broad Physics Program with KNO

Atmospheric  $\nu$



Neutrino oscillation

Solar  $\nu$



Supernova  $\nu$

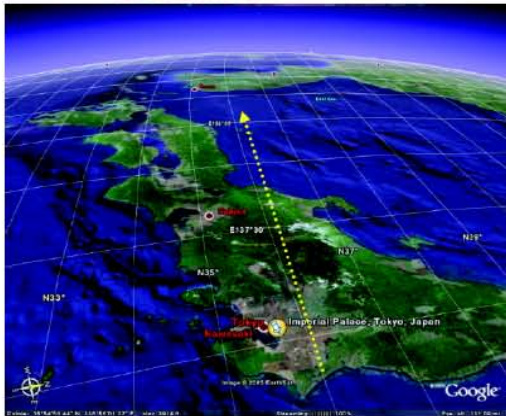


WIMP  $\chi\chi \rightarrow \nu\nu$

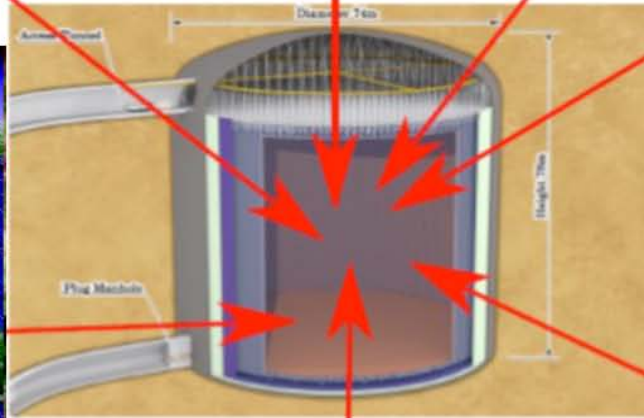


Neutrino telescope

Beam  $\nu$

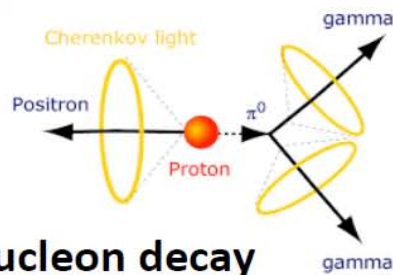
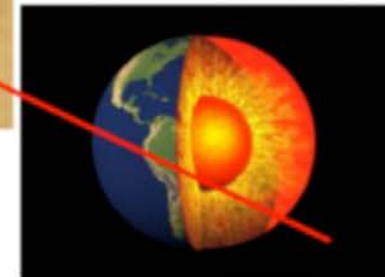


CPV & neutrino mass ordering (MO)



New step to geo-science

$\nu$  Tomography



Nucleon decay

Lifetime :  $10^{35}$  yr



# Proton Decay

Baryogenesis → Baryon number violation → Proton decay

Super-K ( $p \rightarrow e^+ \pi^0$  : 2015)  $T_p > 1.67 \times 10^{34}$  years

SU(5) GUT predicted  $< 10^{31}$  years !!

Theory class	Proton lifetime (years) <sup>[11]</sup>
Minimal SU(5) ( <u>Georgi–Glashow</u> )	$10^{30} \dots 10^{31}$
Minimal <u>SUSY</u> SU(5)	$10^{28} \dots 10^{32}$
<u>SUGRA</u> SU(5)	$10^{32} \dots 10^{34}$
SUSY SU(5)( <u>MSSM</u> )	$\sim 10^{34}$
Minimal (Basic) SO(10) – Non SUSY	$< \sim 10^{35}$ (maximum range)
SUSY SO(10)	$10^{32} \dots 10^{35}$
SUSY SO(10) MSSM G(224)	$2 \cdot 10^{34}$
<u>Flipped SU(5)</u> (MSSM)	$10^{35} \dots 10^{36}$
SUSY SU(5) – 5 dimensions	$10^{34} \dots 10^{35}$

T2HKK would possibly kill (almost) all, or confirm one of GUT

# miniBooNE and light sterile neutrino?

## Observation of a Significant Excess of Electron-Like Events in the MiniBooNE Short-Baseline Neutrino Experiment

A. A. Aguilar-Arevalo<sup>13</sup>, B. C. Brown<sup>6</sup>, L. Bugel<sup>12</sup>, G. Cheng<sup>5</sup>, J. M. Conrad<sup>12</sup>, R. L. Cooper<sup>10,15</sup>, R. Dharmapalan<sup>1,2</sup>, A. Diaz<sup>12</sup>, Z. Djurcic<sup>2</sup>, D. A. Finley<sup>6</sup>, R. Ford<sup>6</sup>, F. G. Garcia<sup>6</sup>, G. T. Garvey<sup>10</sup>, J. Grange<sup>7</sup>, E.-C. Huang<sup>10</sup>, W. Huelsnitz<sup>10</sup>, C. Ignarra<sup>12</sup>, R. A. Johnson<sup>3</sup>, G. Karagiorgi<sup>5</sup>, T. Katori<sup>12,16</sup>, T. Kobilarcik<sup>6</sup>, W. C. Louis<sup>10</sup>, C. Mariani<sup>19</sup>, W. Marsh<sup>6</sup>, G. B. Mills<sup>10,†</sup>, J. Mirabal<sup>10</sup>, J. Monroe<sup>18</sup>, C. D. Moore<sup>6</sup>, J. Mousseau<sup>14</sup>, P. Nienaber<sup>17</sup>, J. Nowak<sup>9</sup>, B. Osmanov<sup>7</sup>, Z. Pavlovic<sup>6</sup>, D. Perevalov<sup>6</sup>, H. Ray<sup>7</sup>, B. P. Roe<sup>14</sup>, A. D. Russell<sup>6</sup>, M. H. Shaevitz<sup>5</sup>, J. Spitz<sup>14</sup>, I. Stancu<sup>1</sup>, R. Tayloe<sup>8</sup>, R. T. Thornton<sup>10</sup>, M. Tzanov<sup>4,11</sup>, R. G. Van de Water<sup>10</sup>, D. H. White<sup>10</sup>, D. A. Wickremasinghe<sup>3</sup>, E. D. Zimmerman<sup>4</sup>

(The MiniBooNE Collaboration)

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<sup>19</sup>Center for Neutrino Physics; Virginia Tech; Blacksburg, VA 24061, USA

<sup>†</sup>Deceased

(Dated: May 31, 2018)

	No sterile neutrino	One sterile neutrino $\nu_s$
Decay mode	$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau$	$\tau^- \rightarrow \mu^- \bar{\nu}_\mu \nu_\tau, \mu^- \bar{\nu}_\mu \nu_s, \mu^- \bar{\nu}_s \nu_\tau, \mu^- \bar{\nu}_s \nu_s$
Decay rate	$\Gamma_\tau = \frac{(G_F^0)^2 m_\tau^5}{192\pi^3} \times f(m_\mu^2/m_\tau^2)$	$\Gamma_\tau = \frac{(G_F^0)^2 m_\tau^5}{192\pi^3} \times \rho_{\mu\tau} \times f(m_\mu^2/m_\tau^2)$

$$f(x) = 1 - 8x + 8x^3 - x^4 - 12x^2 \log x,$$

$$\rho_{\mu\tau} = 1 + |V_{\mu s}|^2 + |V_{\tau s}|^2 + |V_{\mu s}|^2 |V_{\tau s}|^2.$$

$$\frac{\Gamma_\tau}{\Gamma_\mu} = \begin{cases} \left(\frac{m_\tau}{m_\mu}\right)^5 \frac{f(m_\mu^2/m_\tau^2)}{f(m_e^2/m_\mu^2)} & \text{(No sterile neutrino)} \\ \left(\frac{m_\tau}{m_\mu}\right)^5 \frac{f(m_\mu^2/m_\tau^2)}{f(m_e^2/m_\mu^2)} \frac{\rho_{\mu\tau}}{\rho_{e\mu}} & \text{(One sterile neutrino } \nu_s) \end{cases}$$

$$\rho_{e\mu} = 1 + |V_{e s}|^2 + |V_{\mu s}|^2 + |V_{e s}|^2 |V_{\mu s}|^2$$

$$\frac{\Gamma_\tau}{\Gamma_\mu} = \begin{cases} \left(\frac{m_\tau}{m_\mu}\right)^5 \left(\frac{f(m_\mu^2/m_\tau^2)}{f(m_e^2/m_\mu^2)}\right) \frac{(1 + \frac{3}{5}(m_\tau^2/m_W^2)) (1 + (\frac{\alpha(m_\tau^2)}{2\pi}(\frac{25}{4} - \pi^2)))}{(1 + \frac{3}{5}(m_\mu^2/m_W^2)) (1 + (\frac{\alpha(m_\mu^2)}{2\pi}(\frac{25}{4} - \pi^2)))} & \text{(No sterile neutrino)} \\ \left(\frac{m_\tau}{m_\mu}\right)^5 \left(\frac{f(m_\mu^2/m_\tau^2)}{f(m_e^2/m_\mu^2)}\right) \frac{(1 + \frac{3}{5}(m_\tau^2/m_W^2)) (1 + (\frac{\alpha(m_\tau^2)}{2\pi}(\frac{25}{4} - \pi^2)))}{(1 + \frac{3}{5}(m_\mu^2/m_W^2)) (1 + (\frac{\alpha(m_\mu^2)}{2\pi}(\frac{25}{4} - \pi^2)))} \times \frac{\rho_{\mu\tau}}{\rho_{e\mu}} & \text{(One sterile neutrino } \nu_s) \end{cases}$$

$$\frac{1}{2} \leq \frac{\rho_{\mu\tau}}{\rho_{e\mu}} \leq 2.$$

	No sterile neutrino	One sterile neutrino $\nu_s$
Process	$\tau^- \rightarrow P^- \nu_\tau$	$\tau^- \rightarrow P^- \nu_\tau, P^- \nu_s$
Decay rate	$\Gamma_{\tau \rightarrow P\nu} = \frac{(G_F^0)^2  V_{UD}^0 ^2}{16\pi} f_P^2 m_\tau^3 \left(1 - \frac{m_P^2}{m_\tau^2}\right)^2$	$\Gamma_{\tau \rightarrow P\nu} = \frac{(G_F^0)^2  V_{UD}^0 ^2}{16\pi} f_P^2 m_\tau^3 \left(1 - \frac{m_P^2}{m_\tau^2}\right)^2 (1 +  V_{\tau s} ^2)$
Process	$P^- \rightarrow \mu^- \bar{\nu}_\mu$	$P^- \rightarrow \mu^- \bar{\nu}_\mu, \mu^- \bar{\nu}_s$
Decay rate	$\Gamma_{P \rightarrow \mu\nu} = \frac{(G_F^0)^2  V_{UD}^0 ^2}{8\pi} f_P^2 m_\mu^2 m_P \left(1 - \frac{m_\mu^2}{m_P^2}\right)^2$	$\Gamma_{P \rightarrow \mu\nu} = \frac{(G_F^0)^2  V_{UD}^0 ^2}{8\pi} f_P^2 m_\mu^2 m_P \left(1 - \frac{m_\mu^2}{m_P^2}\right)^2 (1 +  V_{\mu s} ^2)$

$$\frac{\Gamma_{\tau \rightarrow P\nu}}{\Gamma_{P \rightarrow \mu\nu}} = \begin{cases} \frac{1}{2} \frac{m_P^3}{m_\mu^2 m_\tau} \left( \frac{m_\tau^2 - m_P^2}{m_P^2 - m_\mu^2} \right)^2 & \text{(No sterile neutrino)} \\ \frac{1}{2} \frac{m_P^3}{m_\mu^2 m_\tau} \left( \frac{m_\tau^2 - m_P^2}{m_P^2 - m_\mu^2} \right)^2 \left( \frac{1 + |V_{\tau s}|^2}{1 + |V_{\mu s}|^2} \right) & \text{(One sterile neutrino } \nu_s) \end{cases}$$

$$\frac{\Gamma_{\tau \rightarrow P\nu}}{\Gamma_{P \rightarrow \mu\nu}} = \begin{cases} \frac{1}{2} \frac{m_P^3}{m_\mu^2 m_\tau} \left( \frac{m_\tau^2 - m_P^2}{m_P^2 - m_\mu^2} \right)^2 \frac{1 + (2\alpha/\pi) \ln(m_Z/m_\tau)}{1 + \frac{3}{2}(\alpha/\pi) \ln(m_Z/m_P) + \frac{1}{2}(\alpha/\pi) \ln(m_Z/m_{P^*})} & \text{(No sterile neutrino)} \\ \frac{1}{2} \frac{m_P^3}{m_\mu^2 m_\tau} \left( \frac{m_\tau^2 - m_P^2}{m_P^2 - m_\mu^2} \right)^2 \frac{1 + (2\alpha/\pi) \ln(m_Z/m_\tau)}{1 + \frac{3}{2}(\alpha/\pi) \ln(m_Z/m_P) + \frac{1}{2}(\alpha/\pi) \ln(m_Z/m_{P^*})} \left( \frac{1 + |V_{\tau s}|^2}{1 + |V_{\mu s}|^2} \right) & \text{(One sterile neutrino } \nu_s) \end{cases}$$

	No sterile neutrino	One sterile neutrino $\nu_s$
Decay mode	$Z \rightarrow \nu_\ell \bar{\nu}_\ell$	$Z \rightarrow \nu_\ell \bar{\nu}_\ell, \nu_s \bar{\nu}_\ell, \nu_\ell \bar{\nu}_s, \nu_s \bar{\nu}_s$
Decay rate	$\Gamma_{\text{inv}} = \frac{G_F^0 m_Z^3}{4\pi\sqrt{2}}$	$\Gamma_{\text{inv}} = \frac{G_F^0 m_Z^3}{4\pi\sqrt{2}} \left( 1 + \sum_{\ell=e,\mu,\tau} ( V_{\ell s} ^2 +  V_{\ell s} ^4) \right)$

$$\Gamma_{\text{inv}} = \begin{cases} m_Z^3 \sqrt{\frac{14\pi}{T_\mu m_\mu^5}} f(m_e^2/m_\mu^2) & \text{(No sterile neutrino)} \\ m_Z^3 \sqrt{\frac{14\pi}{T_\mu m_\mu^5}} f(m_e^2/m_\mu^2) \left( \frac{1 + \sum_{\ell=e,\mu,\tau} (|V_{\ell s}|^2 + |V_{\ell s}|^4)}{\sqrt{1 + |V_{es}|^2 + |V_{\mu s}|^2 + |V_{es}|^2 |V_{\mu s}|^2}} \right) & \text{(One sterile neutrino } \nu_s) \end{cases}$$

$$T_\mu = \frac{1}{\Gamma_\mu}$$

$$\frac{N_\nu}{3} = \frac{\Gamma_{\text{inv}}^{\text{exp}}}{\Gamma_{\text{inv}}^{\text{SM}}}, \quad N_\nu = 3 \left( \frac{1 + \sum_{\ell=e,\mu,\tau} (|V_{\ell s}|^2 + |V_{\ell s}|^4)}{\sqrt{1 + |V_{es}|^2 + |V_{\mu s}|^2 + |V_{es}|^2 |V_{\mu s}|^2}} \right)$$

According to PDG the number of light active neutrinos is  $N_\nu = 2.9840 \pm 0.0082$ , which gives us

$$\frac{1 + |V_{es}|^2 + |V_{\mu s}|^2 + |V_{\tau s}|^2}{\sqrt{1 + |V_{es}|^2 + |V_{\mu s}|^2}} \approx \frac{N_\nu}{3} = 0.9947 \pm 0.0027.$$

$$\frac{d\Gamma(\tau^- \rightarrow \mu^- + \text{"missing"})}{dE_\mu} = \begin{cases} \frac{(G_F^0)^2}{12\pi^3} (3E_\mu(m_\tau^2 + m_\mu^2) - 2m_\tau(m_\mu^2 + 2E_\mu^2)) \sqrt{E_\mu^2 - m_\mu^2} & \text{(No sterile neutrino)} \\ \frac{(G_F^0)^2 \rho_{\mu\tau}}{12\pi^3} (3E_\mu(m_\tau^2 + m_\mu^2) - 2m_\tau(m_\mu^2 + 2E_\mu^2)) \sqrt{E_\mu^2 - m_\mu^2} & \text{(One sterile neutrino } \nu_s) \end{cases}$$

$$T_\mu = (2.1969811 \pm 0.0000022) \times 10^{-6} \text{ s} = (2.1969811 \pm 0.0000022) \times 1.52 \times 10^{18} \text{ GeV}^{-1}$$

$$= (3.3394113 \pm 0.0000033) \times 10^{18} \text{ GeV}^{-1},$$

$$m_\mu = 105.6583715 \pm 0.0000035 \text{ MeV} = 0.1056583715 \pm 0.0000000035 \text{ GeV},$$

$$m_\tau = 1776.82 \pm 0.16 \text{ MeV} = 1.77682 \pm 0.00016 \text{ GeV}.$$

