

A Quench Protection Database-Tool and Analysis of Quench Heater tests in HL-LHC Nb₃Sn Magnets

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Susana Izquierdo-Bermudez (CERN)

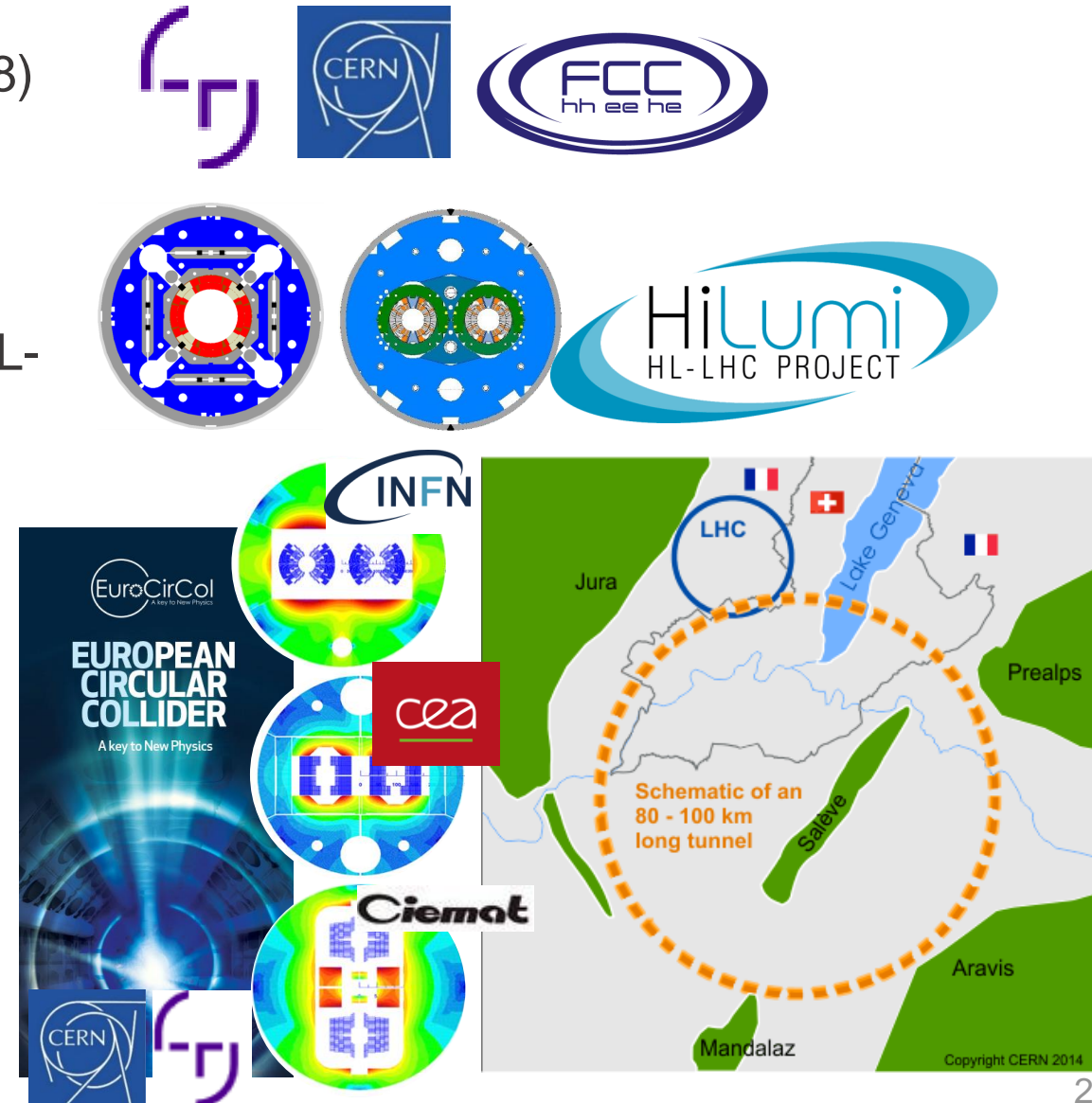
with support from the CERN SM-18 test facility team, in particular Hugo Bajas and Gerard Willering

Context

FCC addendum for a CERN-TAU Project (2016-2018)

Project goals:

- Systematic analysis of quench heater tests in HL-LHC magnets
- Systematic data storage in an Excel-based database tool
- Validation of the simulation models used for the heater design for the FCC 16 T Nb₃Sn dipoles

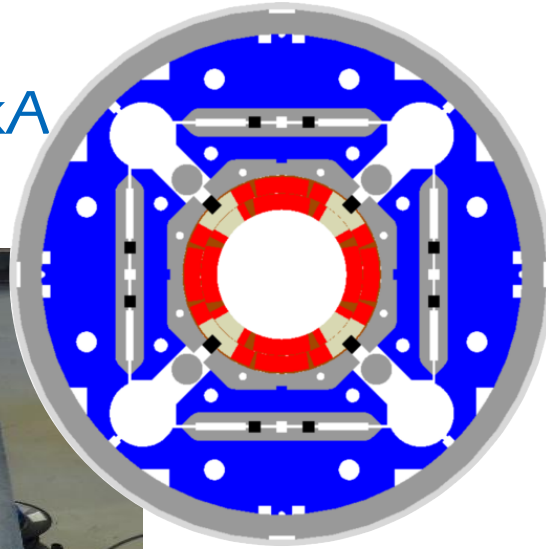


HL-LHC magnet models



MQXFS3, 5

1.2 m, 12 T, 16.5 kA
1.2 MJ/m

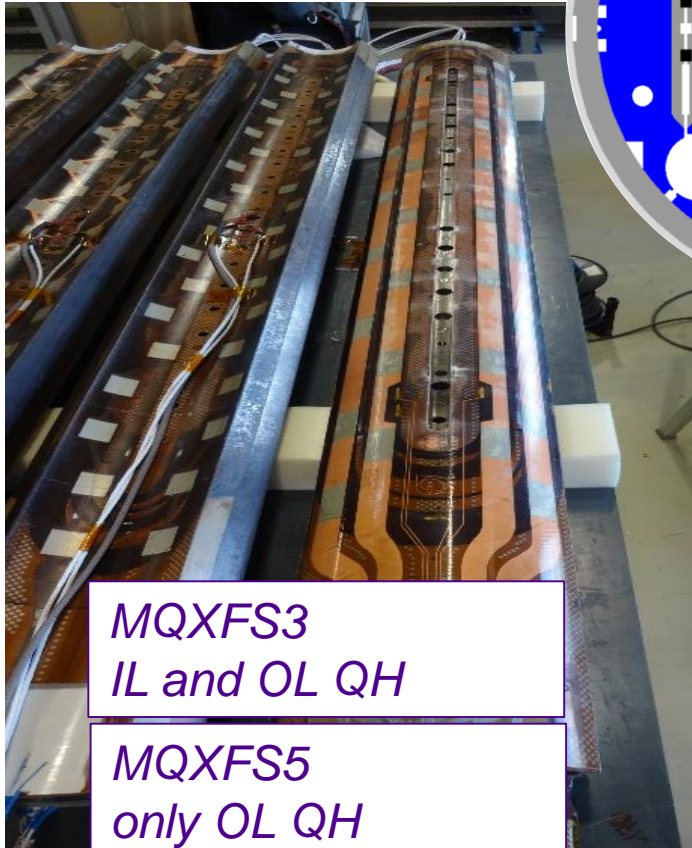
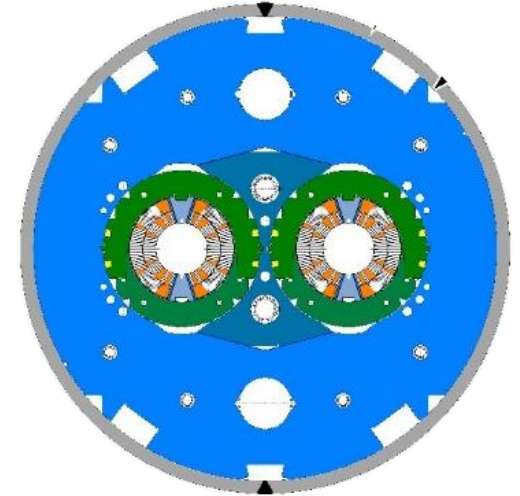


11 T:

SP101,3,5,6;

DP101

1.7 m, 11 T, 12 kA,
0.5 MJ/m/ ap.



MQXFS3
IL and OL QH

MQXFS5
only OL QH



Details of magnet designs can be found in [1-6],
the main parameters summarized also in the appendix

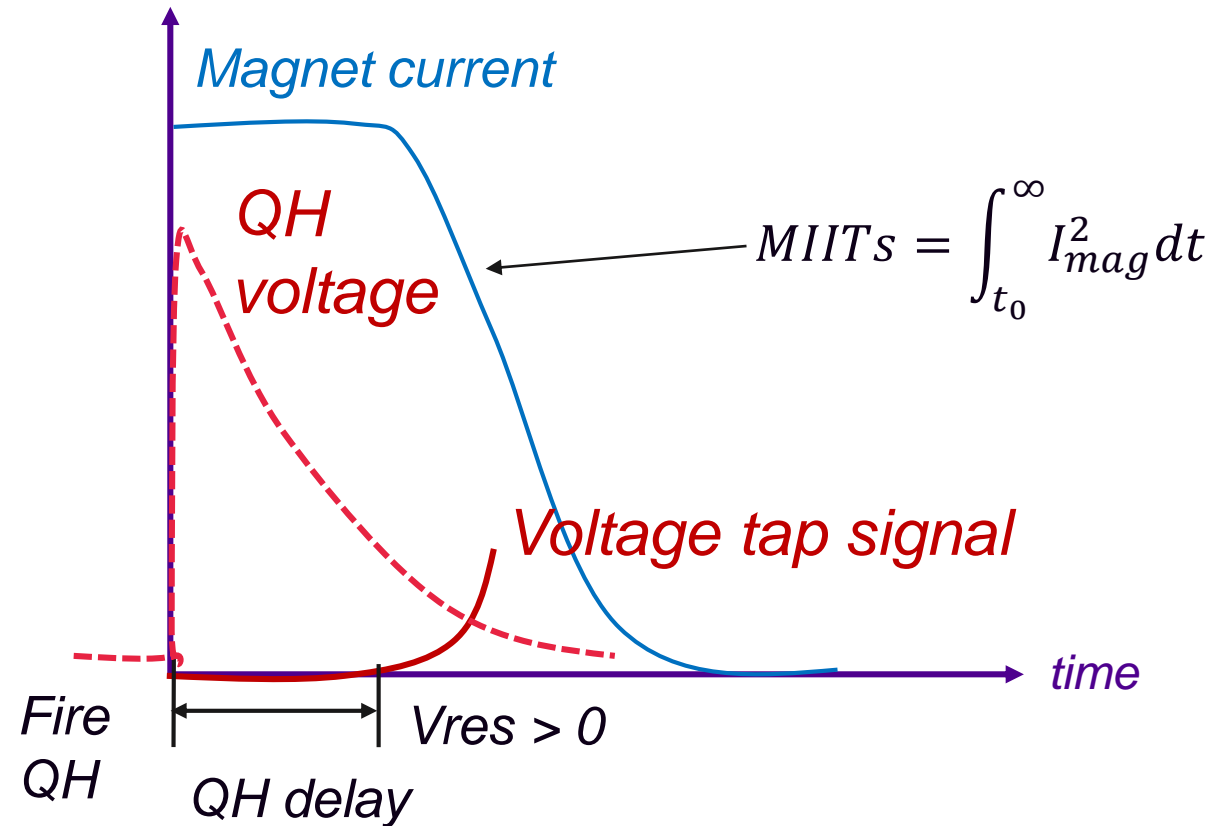
Quench heater (QH) tests

Measurement of heater delays

Time delay between firing a heater and a quench onset in coil

and
quench integrals (MIITs)

How fast the current decays after activating heater-based protection?

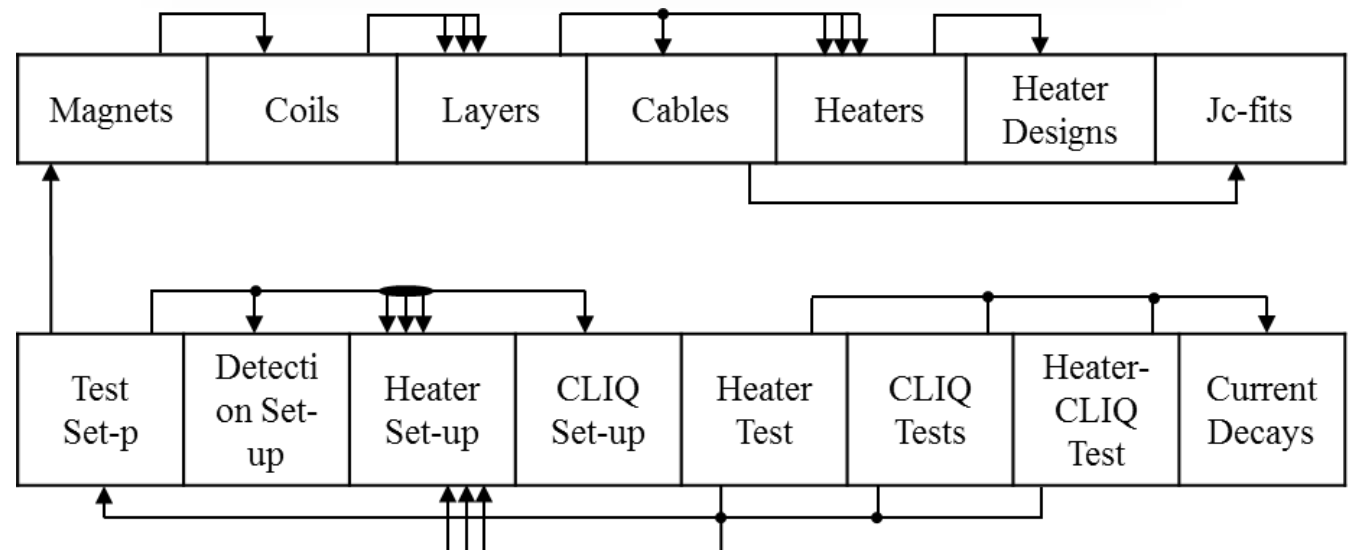
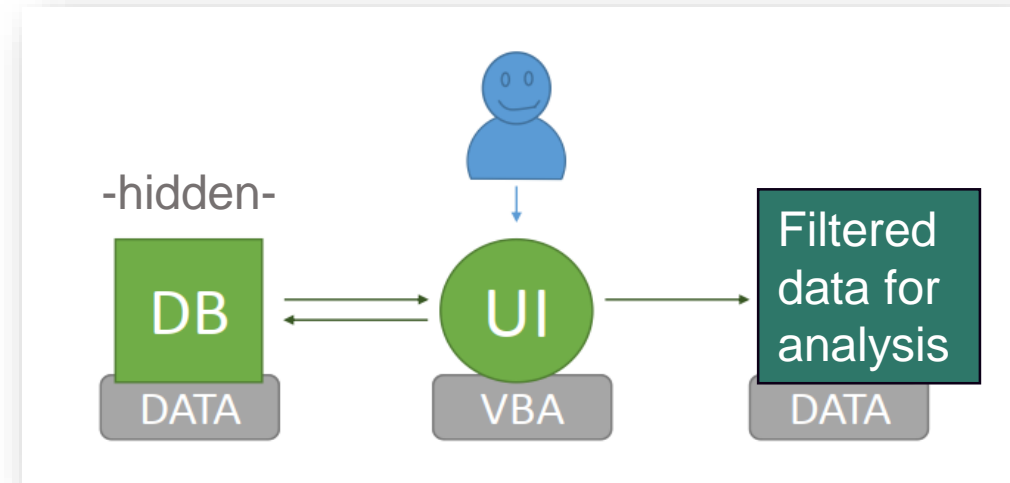


Heater test results previously analyzed, see for example [4-10].

We re-analyzed the raw data to ensure all stored data is consistently interpreted.

Quench Protection Database tool (QPDB)

- Consists of 2 Excel files:
 - **Datafile (DB)**
 - **User Interface (UI)**
- Relational
 - Items (coils, cables,..) are tables in their own tabs
- Aimed for logical structure, accounting all parameters relevant for heater tests
- Flexible for future modifications
 - E.g. adding other tests or simulations
- Reference for magnet design evolution



QPDB: Features

- Example of use and internally computed quantities

UI in view mode, "Magnets" sheet

	A	B	C	D	E	F	G	H	I	J	K
1											
2		Display database hierarchy									
3											
4											
5											
6	Magnet ID	Date of edit	Author of edit	l_{mag} (m)	Apert. (mm)	T_{op} (K)	I_{nom} (A)	I_{ult} (A)	B_{nom} (T)	$I_{SSL, nom}$ (A)	$T_{cs, n}$
7	MQXFS4	4/4/19	Tiina Salmi	1.192	150	1.9	16470	17790	11.41	22139	7.
8	MBHSP107	7/24/18	Carmelo Barbagallo	1.691	60	1.9	11850	12850	11.64	14686	6.
9	MBHSP106	3/13/18	Tiina Salmi	1.700	60	1.9	11850	12800	11.69	14911	6.
10	MQXFS1	3/13/18	Tiina Salmi	1.192	150	1.9	16470	17890	11.41		
11	MBHDP102	1/30/19	Tiina Salmi	1.690	60	1.9	11850	12800	11.77	14345	5.
12	MQXFS5a	3/13/18	Tiina Salmi	1.196	150	1.9	16470	17890	11.41	20188	6.
13	MBHSP105	3/13/18	Tiina Salmi	1.690	60	1.9	11850	12800	11.64	14884	6.
14	MBHSP104	3/13/18	Tiina Salmi	1.690	60	1.9	11850	12800	11.64	14651	5.
15	MBHDP101	1/30/19	Tiina Salmi	1.690	60	1.9	11850	12800	11.94	14018	5.
16	MBHSP103	3/13/18	Tiina Salmi	1.690	60	1.9	11850	12800	11.64	14379	5.
17	MQXFS3b	3/13/18	Tiina Salmi	1.196	150	1.9	16470	17890	11.41	21396	6.

	T	
1		
2		
3		
4		
5		
6	$L_d, fit a_4$	L
7	0.00E+00	0.
8	2.33E-15	-9
9	2.33E-15	-9
10	0.00E+00	0.
11	7.84E-15	-3
12	0.00E+00	0.
13	2.33E-15	-9
14	2.33E-15	-9
15	4.50E-15	-1
16	2.33E-15	-9
17	0.00E+00	0.

Navigation bar showing tabs: Main | **Magnets** | Coils | Layers | Cables

QPDB: Features

- Example of use and internally computed quantities

UI in view mode, "Magnets" sheet

Magnet ID	Date of edit	Author of edit	I_{mag} (m)	Apert. (mm)	T_{op} (K)	I_{nom} (A)	I_{ult} (A)	B_{nom} (T)	$I_{SSL, nom}$ (A)	$T_{cs, n}$
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MQXFS3b	3/13/18	Tiina Salmi	1.196	150	1.9	16470	17890	11.41	21396	6.

$L_d, fit a_4$	L
0.00E+00	0.
2.33E-15	-9
2.33E-15	-9
0.00E+00	0.
7.84E-15	-3
0.00E+00	0.
2.33E-15	-9
2.33E-15	-9
4.50E-15	-1
2.33E-15	-9
0.00E+00	0.

Quantities directly input

Internally computed

Internally computed e.g., cross-sections, resistances, I_{SSL} , T_{cs} , MIITs....

QPDB: Features

- Example of use and internally computed quantities

UI in view mode, "Magnets" sheet

The keys linking magnet to its coils

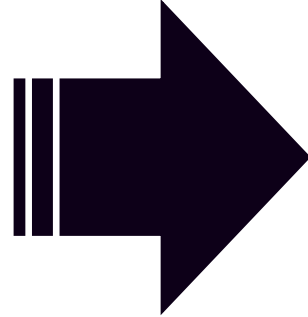
	A	T	U	V	W	X	Y	Z	AA	AB	AC
1											
2											
3											
4											
5											
6	Magnet ID	$L_a, fit a_4$	$L_a, fit a_5$	$L_a, fit a_6$	Comments	References	Coil IDs	Column1	Column2	Column3	
7	MQXFS4	0.00E+00	0.00E+00	0.00E+00			MQXF - C108	MQXF - C109	MQXF - C110	MQXF - C111	
8	MBHSP107	2.33E-15	-9.42E-20	1.41E-24	Loadline wo s [1] A. V. Zlobi		11T - C120	11T - C121			
9	MBHSP106	2.33E-15	-9.42E-20	1.41E-24			11T - C116	11T - C117			
10	MQXFS1	0.00E+00	0.00E+00	0.00E+00			MQXF - C103	MQXF - C104	MQXF - LP03	MQXF - LP05	
11	MBHDP102	7.84E-15	-3.63E-19	6.22E-24	Loadline for 3D Bp with sf		11T - C109	11T - C112	11T - C114	11T - C115	
12	MQXFS5a	0.00E+00	0.00E+00	0.00E+00			MQXF - C203	MQXF - C204	MQXF - C205	MQXF - C206	
13	MBHSP105	2.33E-15	-9.42E-20	1.41E-24	Loadline wo s [1] A.V. Zlobi		11T - C114	11T - C115			
14	MBHSP104	2.33E-15	-9.42E-20	1.41E-24	Loadline wo s [1] A.V. Zlobi		11T - C112	11T - C113			
15	MBHDP101	4.50E-15	-1.50E-19	1.30E-24	Loadline for 3 [1] A.V. Zlobi		11T - C109	11T - C111	11T - C106	11T - C108	
16	MBHSP103	2.33E-15	-9.42E-20	1.41E-24	Loadline wo s [1] A.V. Zlobi		11T - C109	11T - C111			
17	MQXFS3b	0.00E+00	0.00E+00	0.00E+00	The same as MQXFS03a		MQXF - LP07	MQXF - C105	MQXF - C106	MQXF - C107	

→ VBA macros follow the links

Data selection & extraction

	A	B	C	D	E	F
1						
2	Display database hierarchy					
3						
4						
5						
6	Heater test ID	Date of edit	Author of edit	Test set-up	Magnet ID	Test description
72	MQXFS3a_hh01	28/06/2017	Tiina Salmi	MQXFS3a_QI_1	MQXFS3a	
73	MQXFS3a_hh02	28/02/2018	Tiina Salmi	MQXFS3a_QI_1	MQXFS3a	
74	MQXFS3a_hh03	28/06/2017	Tiina Salmi	MQXFS3a_QI_1	MQXFS3a	
75	MQXFS3a_hh05	1/22/19	Tiina Salmi	MQXFS3a_QI_1	MQXFS3a	
76	MQXFS3a_hh07	1/22/19	Tiina Salmi	MQXFS3a_QI_1	MQXFS3a	
77	MQXFS3a_hh08	1/22/19	Tiina Salmi	MQXFS3a_QI_1	MQXFS3a	
78	MQXFS3a_hh09	1/2/19	Tiina Salmi	MQXFS3a_QI_1	MQXFS3a	
79	MQXFS3b_hh50	21/08/2017	Tiina Salmi	MQXFS3b_HH_1	MQXFS3b	
80	MQXFS3b_hh51	1/2/19	Tiina Salmi	MQXFS3b_HH_1	MQXFS3b	
81	MQXFS5a_hh001	12/01/2018	Timo Tarhasaari	MQXFS5_HH_1	MQXFS5a	
82	MQXFS5a_hh009	12/01/2018	Timo Tarhasaari	MQXFS5_HH_1	MQXFS5a	
83	MQXFS5a_hh010	1/25/19	Tiina Salmi	MQXFS5_HH_1	MQXFS5a	
84	MQXFS5a_hh011	1/25/19	Tiina Salmi	MQXFS5_HH_1	MQXFS5a	
85	MQXFS5a_hh012	1/22/19	Tiina Salmi	MQXFS5_HH_1	MQXFS5a	

This button creates a new workbook containing the selected data



Data can be selected in the pivot tables

Sort A to Z
Sort Z to A
Sort by Color
Clear Filter From "Test description"
Filter by Color
Text Filters

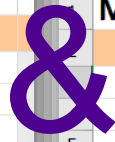
Search

- (Select All)
- Heater delay: 1 IL QH C106 (right)
- Heater delay: IL QH
- Heater delay: IL QH C107
- Heater delay: OL HF at C204 (left)
- Heater delay: OL HF QH
- Heater delay: OL HF QH at C206 & C207

OK Cancel

Extracted workbook

- Stand-alone workbook with all measurement and magnet parameters linked to the selection



	A	B	C	D
1	Heater Test			
2	Heater test ID	Date of edit	Author of edit	Test set-up ID
3	MQXFS3a_hh30	04/05/2018	Tiina Salmi	MQXFS3a_QI_1
4	MQXFS3a_hh31	04/05/2018	Tiina Salmi	MQXFS3a_QI_1
5	MQXFS3a_hh32	04/05/2018	Tiina Salmi	MQXFS3a_QI_1
6	MQXFS3a_hh33	04/05/2018	Tiina Salmi	MQXFS3a_QI_1
7	MQXFS3a_hh34	04/05/2018	Tiina Salmi	MQXFS3a_QI_1
8	MQXFS5a_hh049	12/01/2018	Timo Tarhasaari	MQXFS5_HH_1
9	MQXFS5a_hh050	12/01/2018	Timo Tarhasaari	MQXFS5_HH_1
10	MQXFS5a_hh051	12/01/2018	Timo Tarhasaari	MQXFS5_HH_1
11	MQXFS5a_hh054	1/22/19	Tiina Salmi	MQXFS5_HH_1
12	MQXFS5a_hh055	12/01/2018	Timo Tarhasaari	MQXFS5_HH_1
13	MQXFS5a_hh066	12/5/18	Tiina Salmi	MQXFS5a_HHC204
14	MQXFS5a_hh063	12/5/18	Tiina Salmi	MQXFS5a_HHC204
15	MQXFS5a_hh064	12/5/18	Tiina Salmi	MQXFS5a_HHC204
16	MQXFS5a_hh065	12/5/18	Tiina Salmi	MQXFS5a_HHC204
17				
18				
19	Test Set-up			
20	Test set-up ID	Date of edit	Author of edit	Magnet ID
21	MQXFS3a_QI_1	26/04/2017	Tiina Salmi	MQXFS3a
22	MQXFS5_HH_1	10/11/2017	Tiina Salmi	MQXFS5a
23	MQXFS5a_HHC204	08/12/2017	Tiina Salmi	MQXFS5a
24				

	A	B	C	D	E	F
	Magnets					
	Magnet ID	Date of edit	Author of edit	l_{mag} (m)	Apert. (mm)	T_{op} (K)
	MQXFS3a	3/13/18	Tiina Salmi	1.196	150	1.9
	MQXFS5a	3/13/18	Tiina Salmi	1.196	150	1.9
	Coils					
	Coil ID	Date of edit	Author of edit	N_{layers}	$R_{\text{meas.}}$ (Ohm)	$R_{\text{comp.}}$ (Ohm)
	MQXF - LP07	06/04/2017	Timo Tarhasaari	2		0.200
	MQXF - C105	06/04/2017	Timo Tarhasaari	2		0.199
	MQXF - C106	06/04/2017	Timo Tarhasaari	2		0.200
	MQXF - C107	06/04/2017	Timo Tarhasaari	2		0.199
	MQXF - C203	27/10/2017	Tiina Salmi	2	0.184	0.200
	MQXF - C204	27/10/2017	Tiina Salmi	2	0.182	0.198
	MQXF - C205	27/10/2017	Tiina Salmi	2	0.182	0.198
	MQXF - C206	27/10/2017	Tiina Salmi	2	0.182	0.198
	Layers					
	Layer ID	Date of edit	Author of edit	N_{turns}	Cable ID	l_{cable} (m)
	MQXF - LP07_L1	09/06/2017	Tiina Salmi	22	P43OL1062A	66
	MQXF - LP07_L2	09/06/2017	Tiina Salmi	28	P43OL1062A	84
	MQXF - C105_L1	09/06/2017	Tiina Salmi	22	H16OC0199A	66

Simulation models for FCC

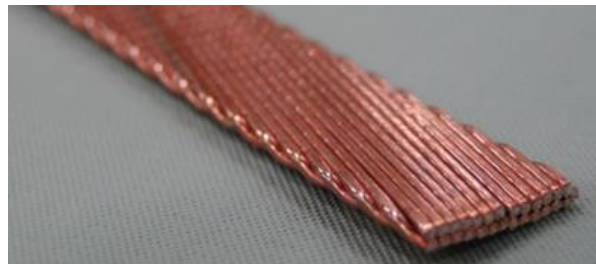
Heater delays with CoHDA
 2D heat diffusion from heater to coil
 → Quench when cable Tcs reached



Current decays with Coodi

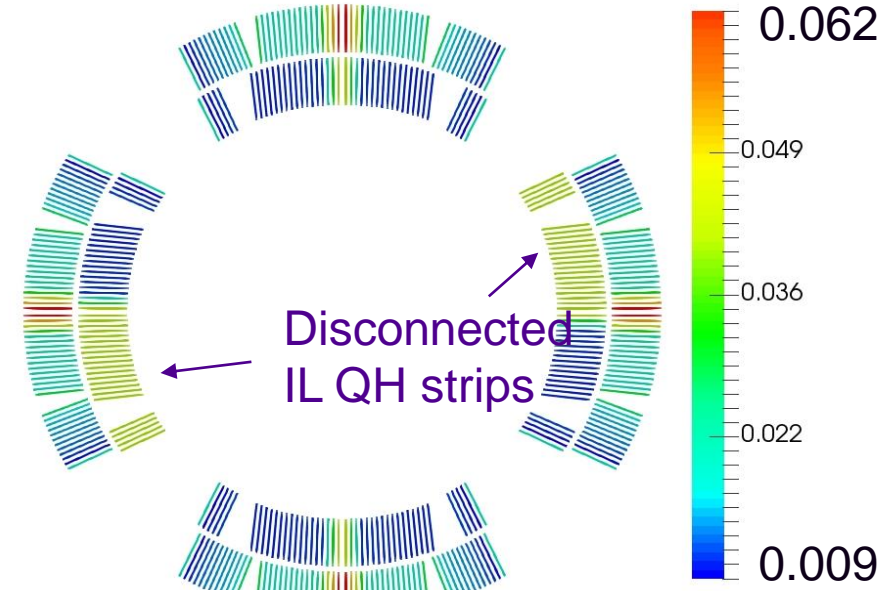
Coodi: Adiabatic model where QH delays & quench propagation input in each turn

Used the data to define how to simulate current flow in the cable



Cable photo from FNAL

Simulated quench delay in MQXS3 (s)



Case A



Case B

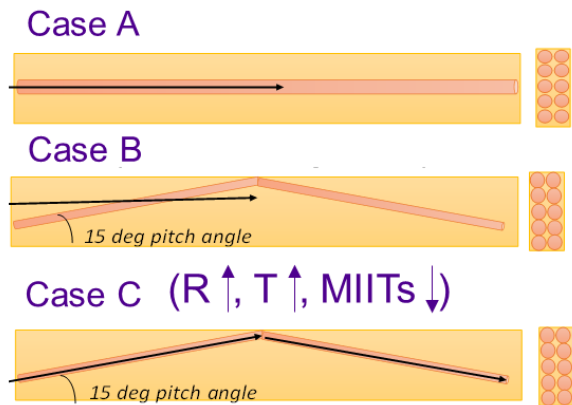


Case C (R ↑, T ↑, MIITs ↓)



Simulated vs. measured magnet resistance: MQXFS3b, QI with OL + IL QH

Options for current flow in cable:



Measured resistance from current decay

$$R(t) = - \frac{\ln \left(\frac{i(t + \Delta t)}{i(t)} \right) L(i)}{\Delta t}$$

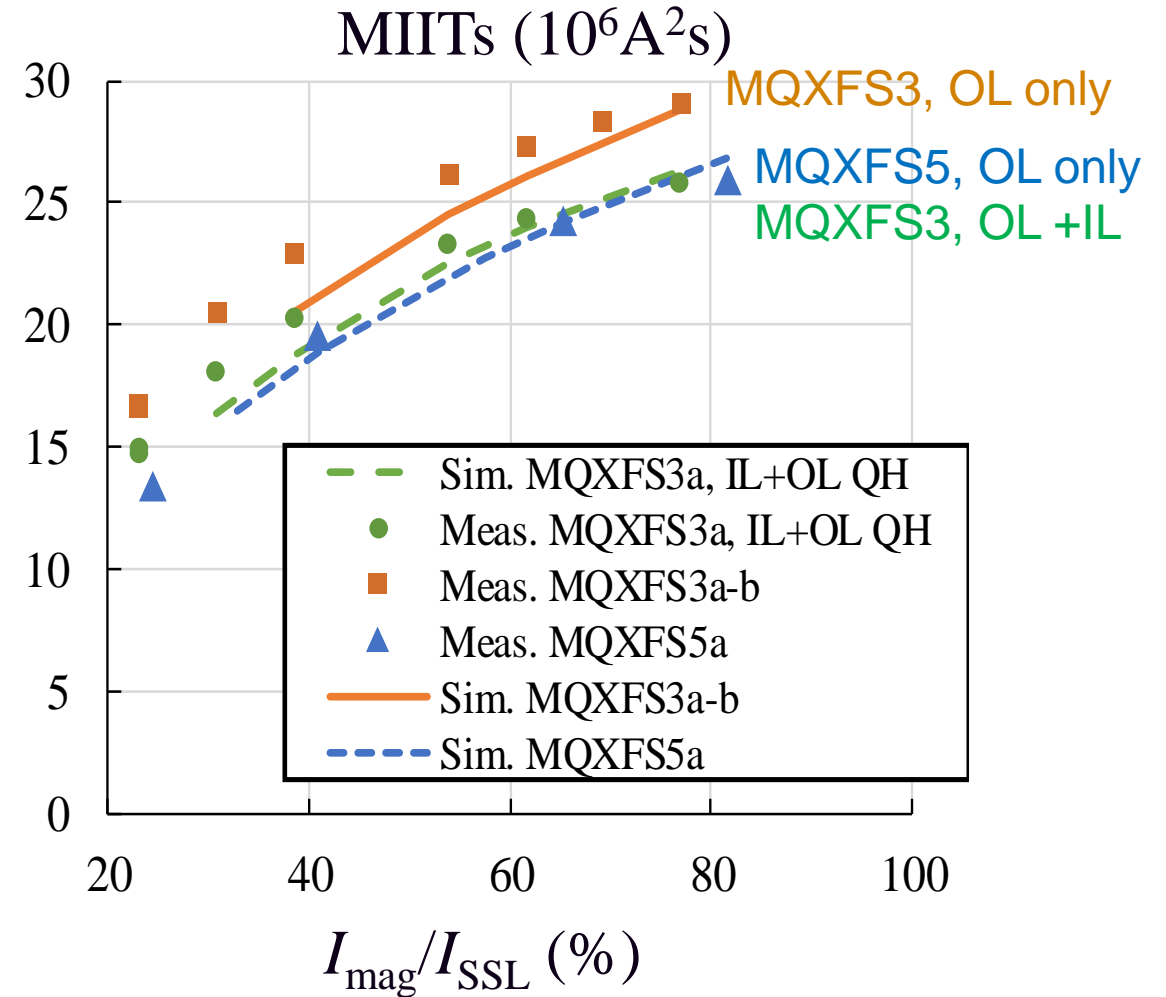
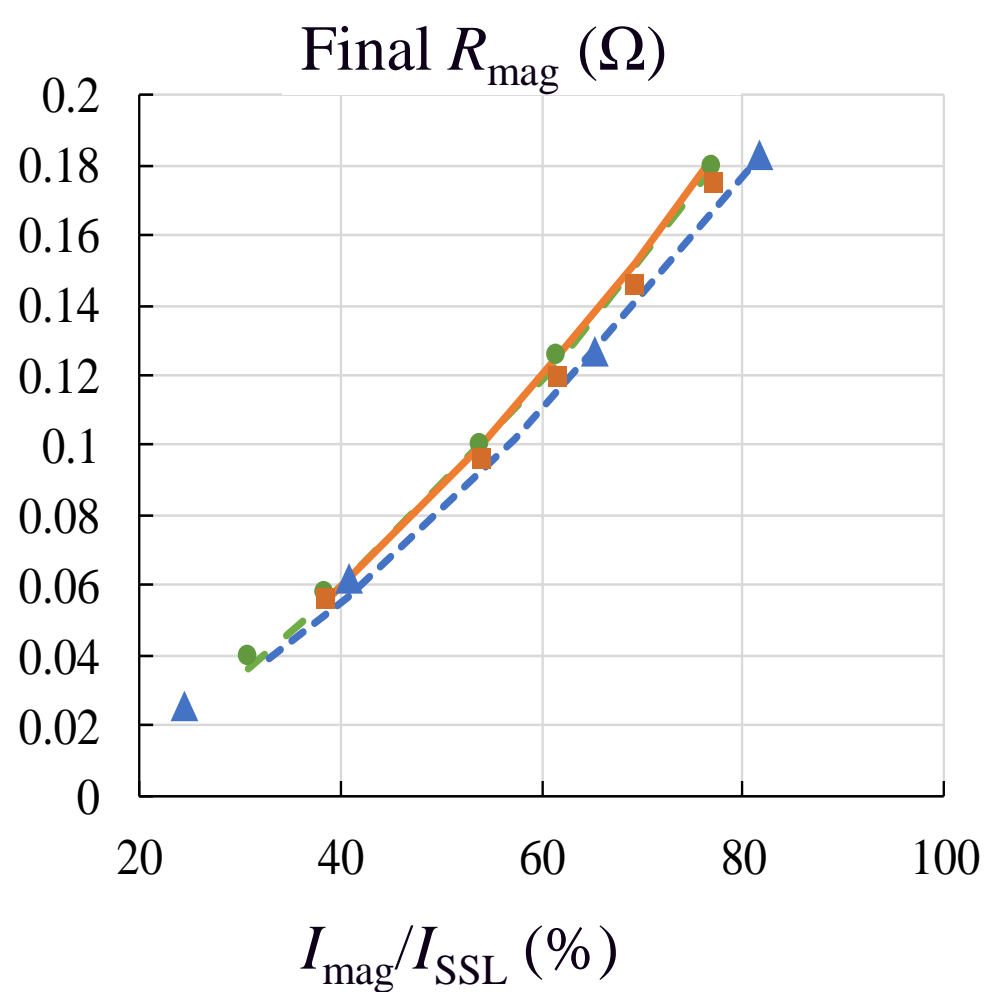
MIITs starting from the heater activation

	$R_{\text{mag,max}}$ (Ω)	MIITs ($10^6 \text{A}^2\text{s}$)	Δ MIITs (%)
Measurement	0.180	25.8	
Case A	0.175	27	5
Case B	0.163	28.5	11
Case C	0.179	26.3	2

Case C closest, MIITs within 2%

Also the coil RT resistance pointed towards Case C

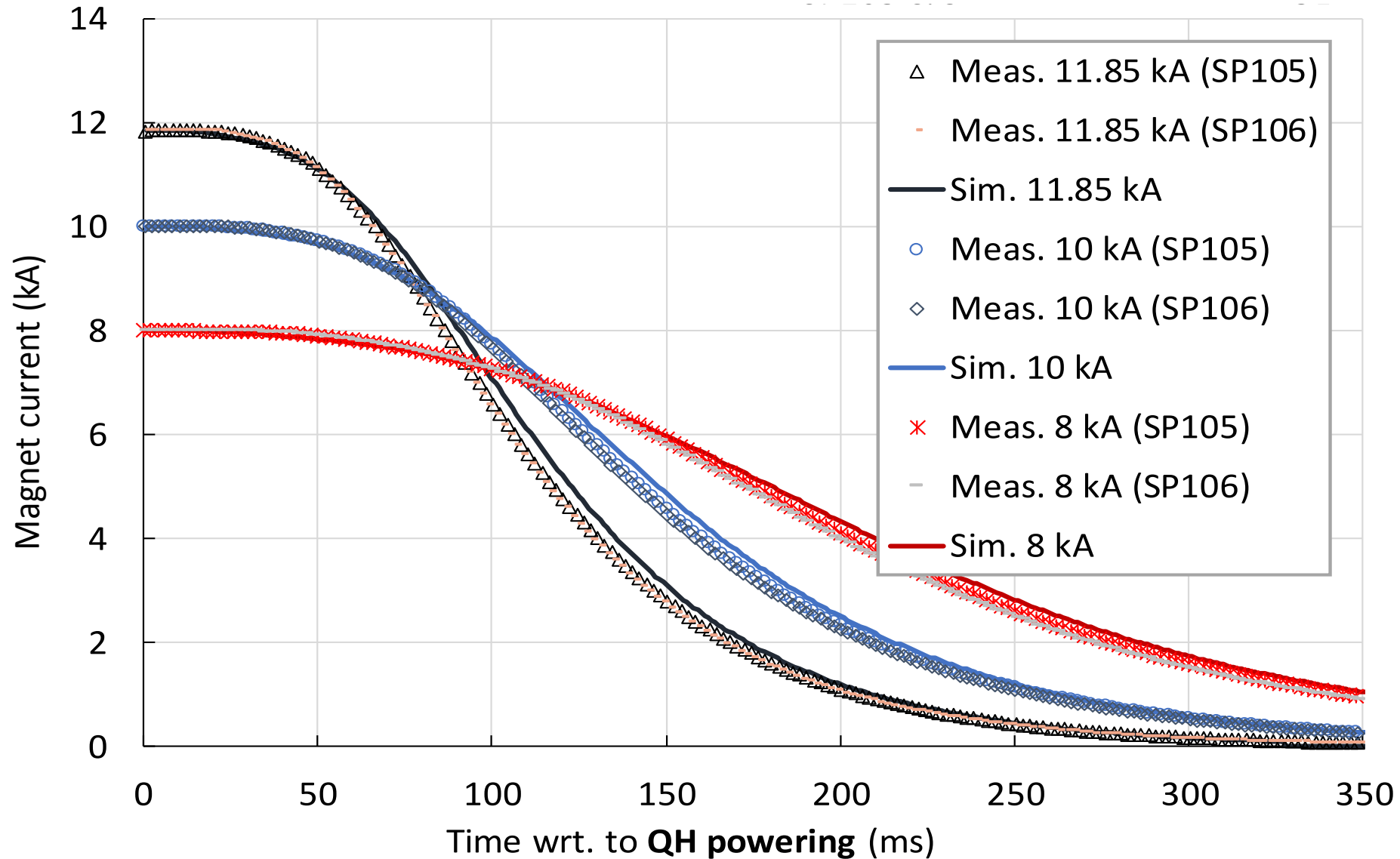
Simulation vs. measurement: MQXF



With Case C excellent agreement in MQXFS5,
tends to underestimate MIITs in MQXFS3 low current

Simulated vs. measured current decay: 11 T

SP105 & SP106,
 QI-study, OL QH



Simulated vs. measured current decay: 11 T 11 T SP105

I_{mag} (kA)	R_{mag} (Ω)		$T_{\text{avg.}}$ (K)		MIIts (MA ² s)		Δ MIIts (%)
	Meas.	Sim.	Meas.	Sim.	Meas.	Sim.	
11.85	0.23	0.23	106	112	12.34	12.64	3
10.00	0.176	0.176	91	96	11.63	11.78	2
8.00	0.125	0.123	79	81	10.41	10.7	3
6.00	0.80±0.2 0	0.73	66±8	65	8.85	9.3	6

Simulated and measured MIIts for current decay after heater activation within 3%, above 8 kA

Conclusions

- Proposed a DB for storing magnet parameters and test data
 - Useful in all phases of magnet development
- Stored data from heater tests in HL-LHC prototypes tested at CERN
- Used data for validation of simulation assumptions in the FCC 16 T dipole magnet design
 - Helped to define cable simulation method
- Future of the tool uncertain due to required maintenance and competing systems
- This may be a useful too for personal use thanks to its relative simplicity and accessibility.
 - Contact if interested: tiina.m.salmi@tuni.fi

Thank you!

References

[1]	P. Ferracin <i>et al.</i> , "Development of MQXF: The Nb ₃ Sn Low- β Quadrupole for the HiLumi LHC," <i>IEEE TAS</i> , 26(4), 2016
[2]	F. Savary <i>et al.</i> , "Design and Construction of the Full-Length Prototype of the 11-T Dipole Magnet for the High Luminosity LHC Project at CERN," <i>IEEE TAS</i> 28(3), 2018
[3]	E. Ravaioli <i>et al.</i> , "Quench Protection System Optimization for the High Luminosity LHC Nb ₃ Sn Quadrupoles", <i>IEEE TAS</i> 27(4), 2017
[4]	S. Izquierdo-Bermudez, <i>et al.</i> , "Quench Protection of the 11 T Nb ₃ Sn Dipole for the High Luminosity LHC", <i>IEEE TAS</i> 28(3), 2018
[5]	H. Bajas <i>et al.</i> , "Test Result of the Short Models MQXFS3 and MQXFS5 for the HL-LHC Upgrade," <i>IEEE TAS</i> 28(3), 2018
[6]	G. Willering <i>et al.</i> , "Comparison of Cold Powering Performance of 2-m-Long Nb ₃ Sn 11 T Model Magnets," <i>IEEE TAS</i> 28(3), 2018
[7]	S. Izquierdo Bermudez <i>et al.</i> , "Overview of the Quench Heater Performance for MQXF, the Nb ₃ Sn Low- β Quadrupole for the High Luminosity LHC," <i>IEEE TAS</i> 28(4), 2018
[8]	S. Izquierdo Bermudez <i>et al.</i> , "Quench Protection of the 11 T Nb ₃ Sn Dipole for the High Luminosity LHC," <i>IEEE TAS</i> 28(3), 2018
[9]	S. Izquierdo Bermudez <i>et al.</i> , "Quench Protection Studies of the 11-T Nb ₃ Sn Dipole for the LHC Upgrade," <i>IEEE TAS</i> 26(4), 2016.
[10]	S. I. Bermudez <i>et al.</i> , "Quench Protection Study of a 11 T Nb ₃ Sn Model Dipole for the High Luminosity LHC," <i>IEEE TAS</i> 29(5), 2019

Simulation tools and assumptions

Heater delays with CoHDA

- 2-D heat diffusion model for heater delays (accounts for the heater station length)
- Quench when cable maximum temperature reaches T_{cs} , computed based on maximum field in cable
- Thermal properties for based on cable average magnetic field
- T. Salmi et al., "A Novel Computer Code for Modeling Quench Protection Heaters in High-Field Nb₃Sn Accelerator Magnets", *IEEE TAS*, 24(4), 2014.
- T. Salmi et al., "Analysis of uncertainties in protection heater delay time measurements and simulations in Nb₃Sn high-field accelerator magnets" *IEEE TAS*, 25(4), 2015.

Current decay with Coodi

- Heater delay and quench propagation velocity are input for each turn
 - Quench propagation: 18 m/s btw heating stations, 11 ms btw turns, 22 ms btw layers at nominal current
- Adiabatic temperature calculation
- Coil cross-section discretized at turn level
- T. Salmi et al., "Quench protection analysis integrated in the design of dipoles for the Future Circular Collider", *Phys. Rev. Accel. Beams* 20, 032401
- T. Salmi et al., "The Impact of Protection Heater Delays Distribution on the Hotspot Temperature in a High-Field Accelerator Magnet", *IEEE TAS*, 26(4), 2016.

Material properties

- Nb₃Sn specific heat capacity is based on G. S. Knapp, et al., "Phonon properties of A-15 superconductors obtained from heat-capacity measurements", *Phys. Rev. B* 13, 3783–3789, 1976 above 20 K, and on L. Dresner, "Stability of superconductors", Plenum, 1995 below 20 K
- Other material properties are based on NIST data NIST - E.D. Marquardt et al., "Cryogenic material properties database", in Proc. 11th Int. Cryocooler Conf., Keystone, 2000, <http://cryogenics.nist.gov/MPropsMAY/material%20properties.htm>

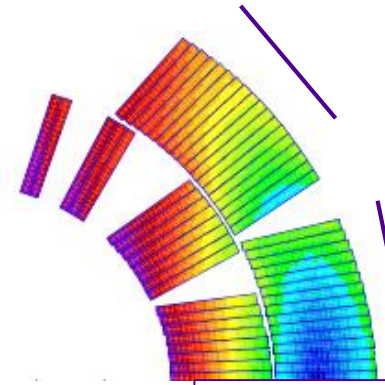
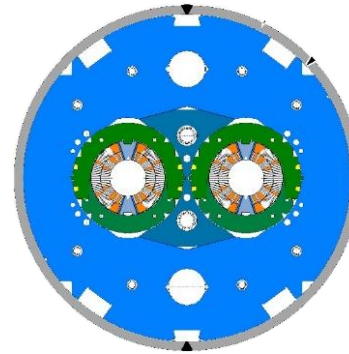
Appendix & extra material

MQXFS03a-b

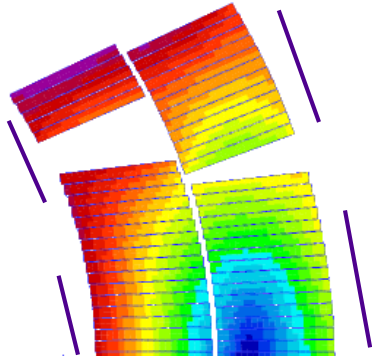
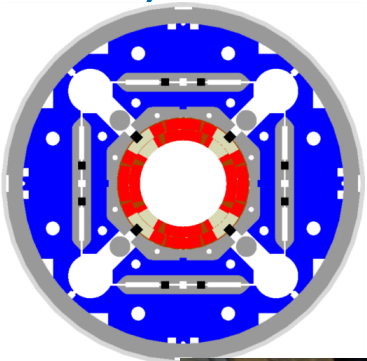
, 1.2 m

HL-LHC magnets

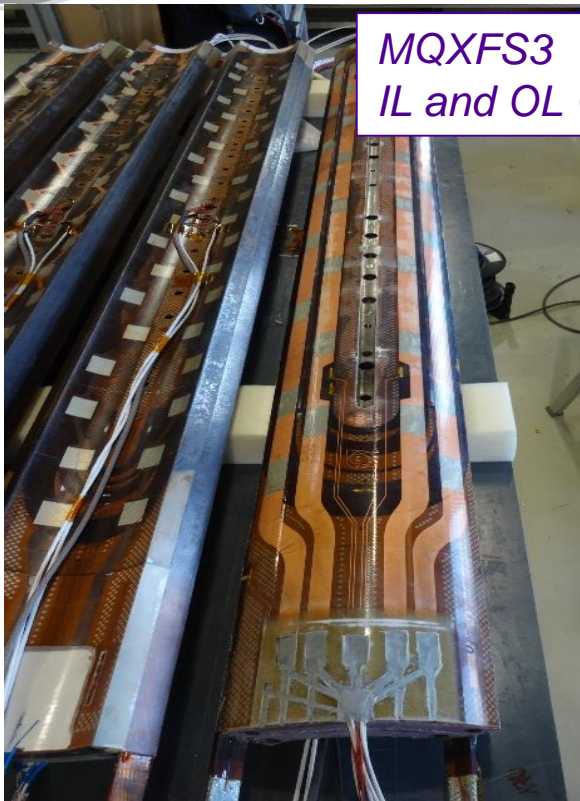
11 T, 1.7 m



11 T OL QH



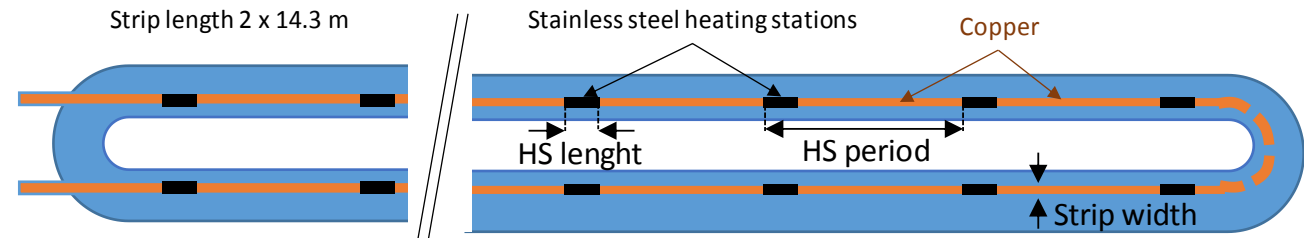
MQXFS3
IL and OL QH



	MQXFS quads	11 T dipole SP104/SP105	ECC Cosθ HF / LF
I_{nom} (A)	16470	11850	11240
B_{peak} (T)	11.4	11.6	16.4
L_d (mH/m)	8.2	5.8	18.4 (1-ap.)
J_{eng} (A/mm ²)	469	523	370 / 515
J_{Cu} (A/mm ²) (one strand)	1330	1374 / 1563	~ 1170/1165
E_{stored} (J/mm ³)	129	130	~ 122
$T_{max, 40 ms delay}$ (K)	260	280 / 310	310 (@ I_{nom})
$T_{max, 20 ms delay}$ (K)	190	200 / 210	240 (@ I_{nom})

QH – Quench heaters

- :
 - Cu-plated stainless steel strips:
 - SS thickn. 25 μm , Cu thickn. 10 μm
 - Insulation to coil: 50 μm polyimide
- Powering with capacitor bank discharge:
 - (LHC: 900 V and 7 mF)



F. Rodriguez-Mateos and F. Sonneman, "Quench heater studies for the LHC magnets", Proc. of PAC, 2001.
 H. Felice et al., "Instrumentation and Quench Protection for LARP Nb₃Sn Magnets", *IEEE TAS*, 19(3), 2009.³P. Ferracin et al, "Development of MQXF, the Nb₃Sn Low- β Quadrupole for the HiLumi LHC ", *IEEE TAS*, 26(4), 2016.

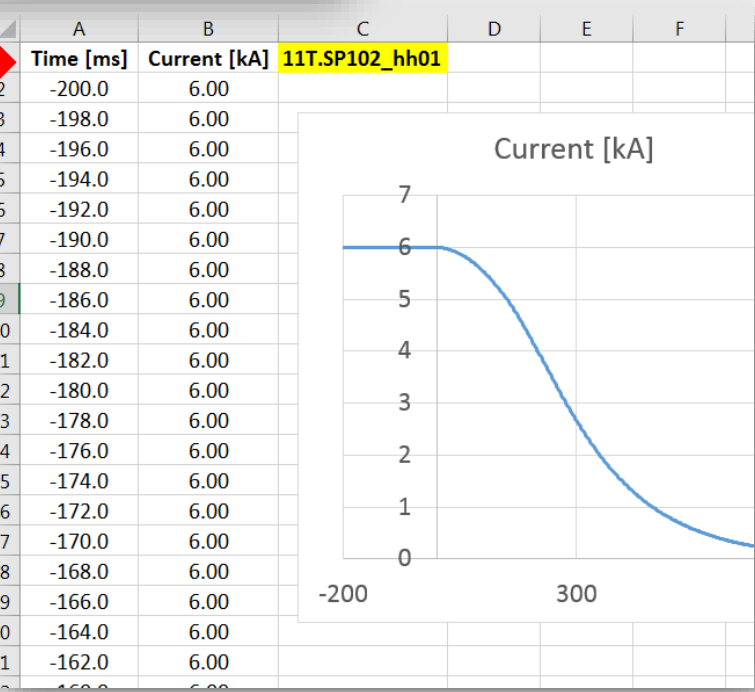
Storing of the current decay

- Piecewise polynomial fit

Display database hierarchy

Show (Time,Current)-profile

Show (Time,Current)-profile



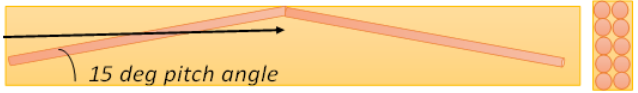
Simulated vs. measured magnet resistance: MQXFS3b, QI with OL + IL QH

Options for current flow in cable:

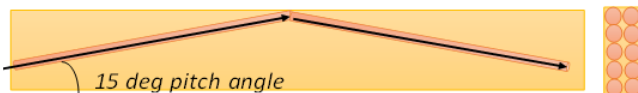
Case A



Case B



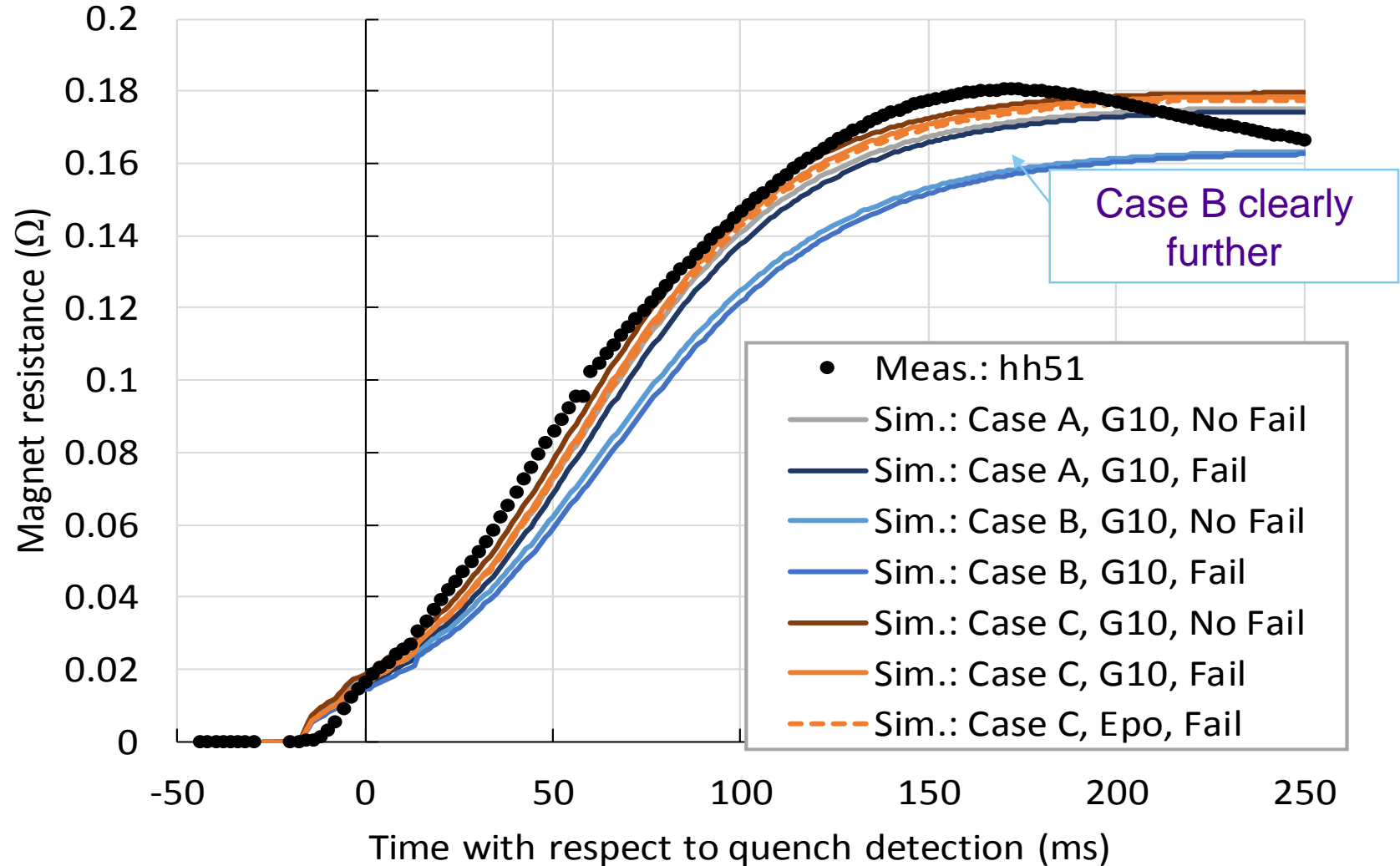
Case C (R ↑, T ↑, MIITs ↓)



Measured resistance from current decay

$$R(t) = - \frac{\ln\left(\frac{i(t + \Delta t)}{i(t)}\right) L(i)}{\Delta t}$$

MQXFS3b, QI-Study: IL+OL QH at 16.5

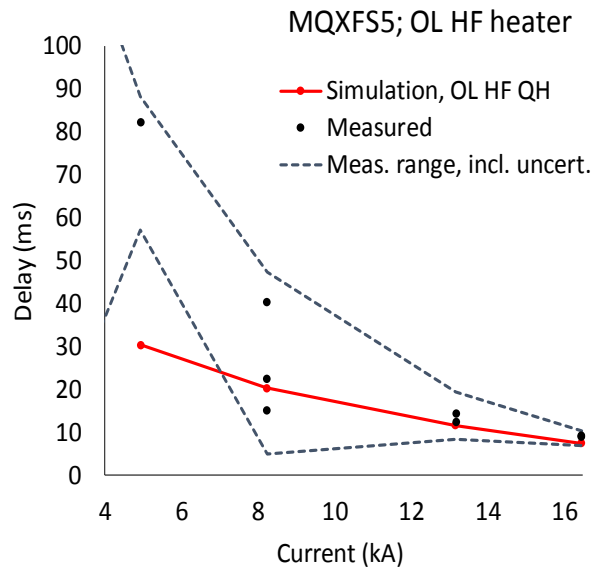
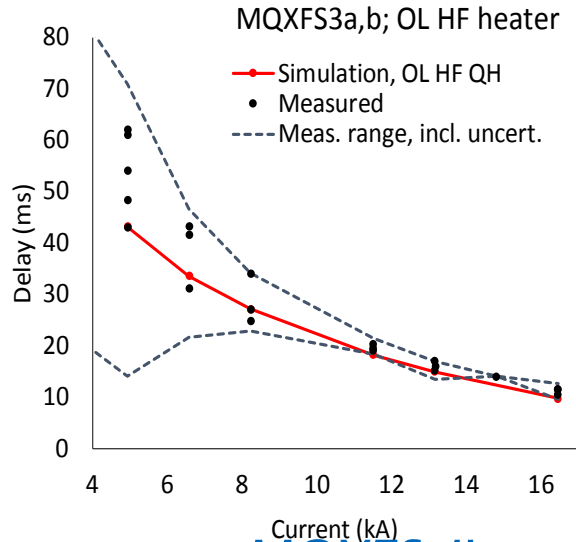


Analysis of quench heater delays

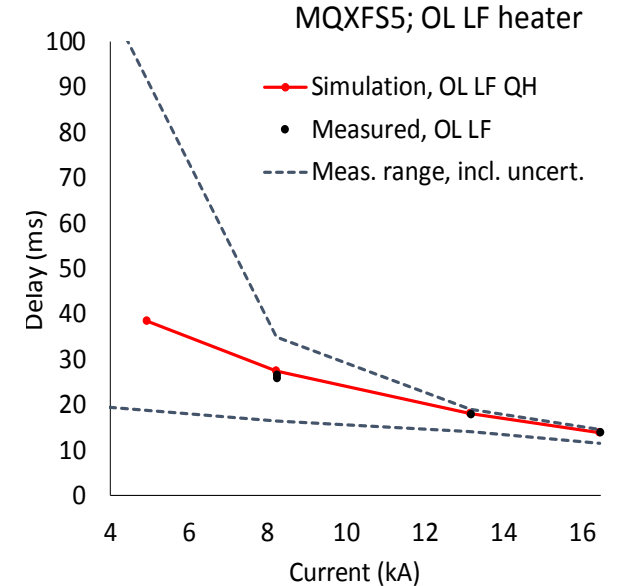
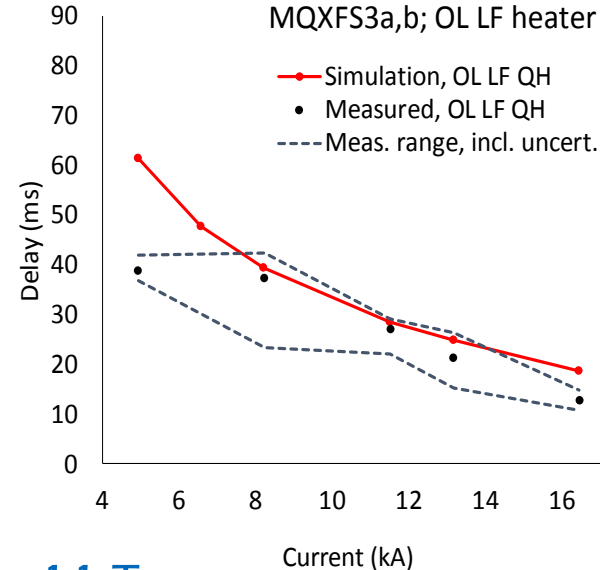
- Defining quench onset is not always clear
- We stored best estimate and error bars estimating the range of possible quench onset
- Typically uncertainty is larger at lower currents

Summary of QH delays: MQXF

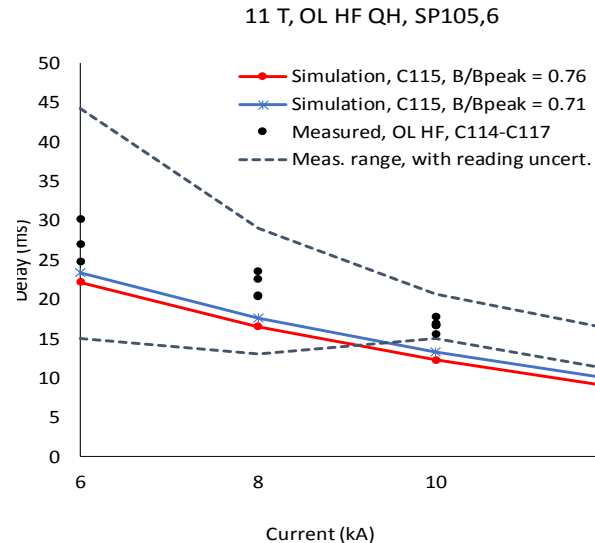
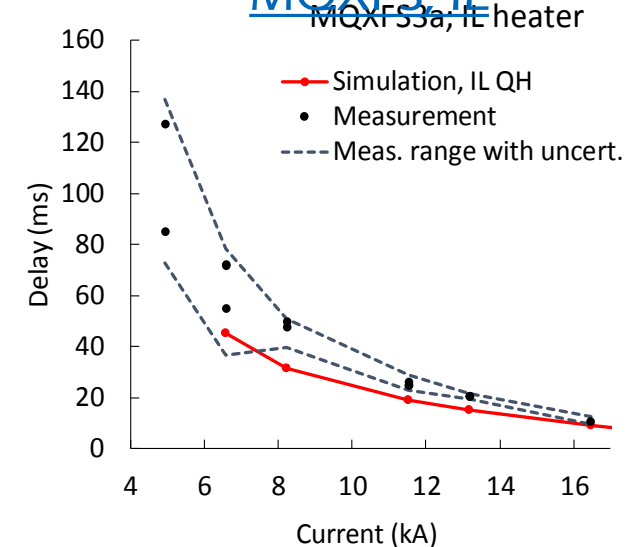
MOXFS, OL HF



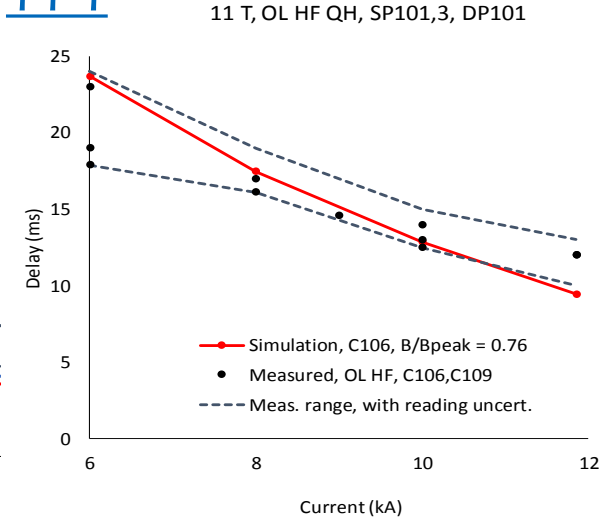
MOXFS, OL LF



MOXFS, IL



11 T

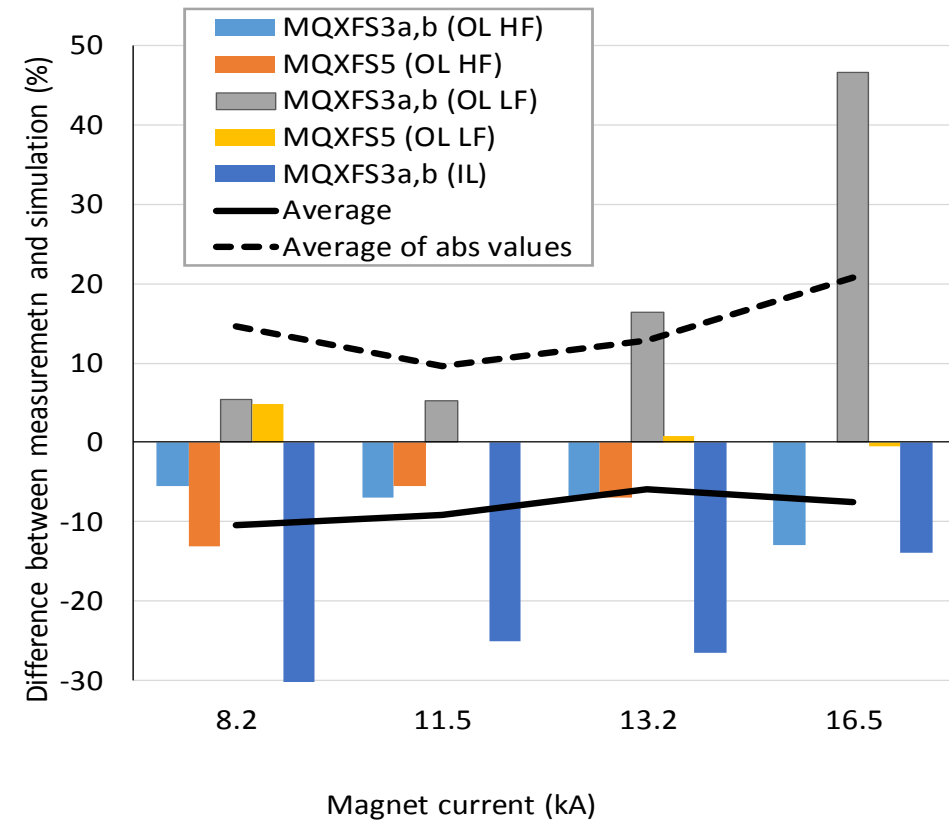
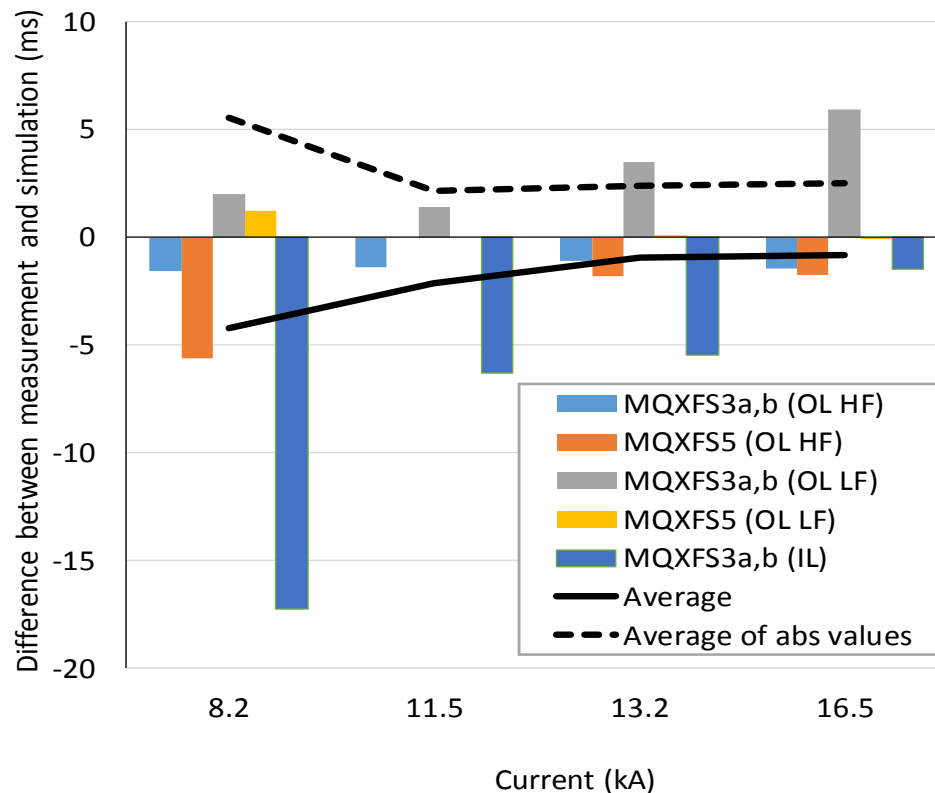


Difference of simulation and average measured is mostly within 20%

The exceptions are MQXFS3 OL LF at I_{nom} , and IL below I_{nom}

Difference between simulation and measurement (MQXF)

- Comparison to average of simulated values at each current, for each heater test type
- The difference is significant (>20%) for MQXFS3 LF heater at nominal current, and IL heaters at lower than nominal
 - IL expected, LF to be studied better after more measurements



Average uncertainty

- An attempt to include the signal reading uncertainty, and the measurement reproducibility

$$\varepsilon_{avg} = \frac{1}{n} \sum_{i=1}^n (t_{d,i} - t_{d,avg}) + \frac{1}{n} \sum_{i=1}^n (\Delta t_{d,max,i})$$

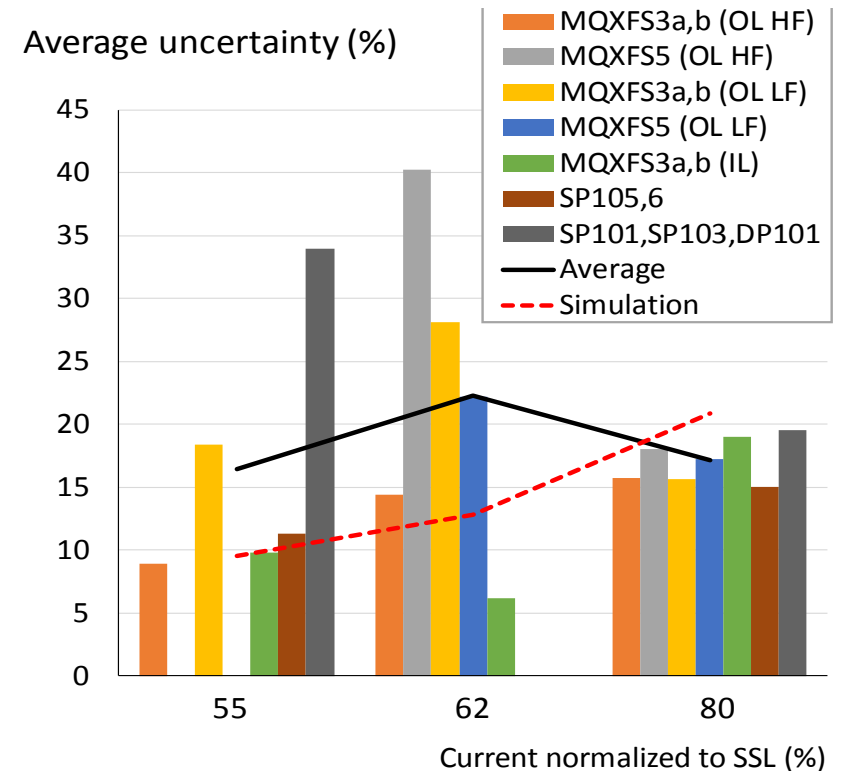
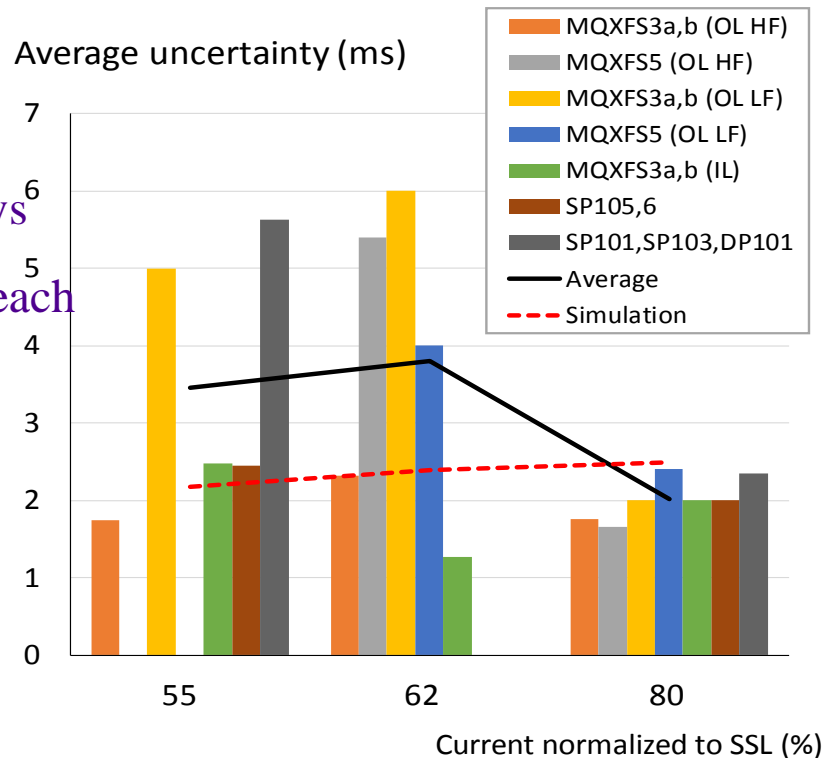
n : Number of measurements

$t_{d,i}$: Measured delay

$t_{d,avg}$: Average of measured delays

$\Delta t_{d,max,i}$: Larger error bar in each delay measurement

Needs more data to be useful parameter



Magnet resistance relation to final average temperature

MQXFS3b, IL + OL QH at nominal current

