

# The inclusive Higgs width in the SMEFT

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in collaboration with M. Trott and T. Corbett  
to appear very soon!



The Niels Bohr  
International Academy



**SMEFT** = Effective Field Theory with **SM fields** + **symmetries**

a Taylor expansion in canonical dimensions ( $v, E/\Lambda$ ):

$$\mathcal{L}_{\text{SMEFT}} = \mathcal{L}_{\text{SM}} + \frac{1}{\Lambda} \mathcal{L}_5 + \frac{1}{\Lambda^2} \mathcal{L}_6 + \frac{1}{\Lambda^3} \mathcal{L}_7 + \frac{1}{\Lambda^4} \mathcal{L}_8 + \dots$$

$$\mathcal{L}_n = \sum_i C_i \mathcal{O}_i^{d=n}$$

$C_i$  free parameters ( Wilson coefficients )

$\mathcal{O}_i$  invariant operators that form  
a complete basis

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---

 describes impact of **any** UV ▶ nearly decoupled:  $\Lambda \gg v, E$

▶ converges to SM in the limit  $E \ll \Lambda$

 not just a parameterization but **a consistent QFT**  $\rightarrow$  loops, RGE etc.

# The SMEFT for LHC experiments

lack of direct discoveries so far → systematic **indirect searches** needed

SMEFT is the best tool for this!

see talk by J. de Blas

- ▶ reasonably **model-independent**
- ▶ **complete & well-defined.** → long-term, extensible analysis plan  
→ combination with other experiments

significant developments happened in the last 5 - 10 yrs.

- ▶ main focus  $\mathcal{L}_6$ : leading effects @LHC
- ▶ theory improvements
- ▶ tools for phenomenology

**bottom-up approach:** constraining (measuring!) as many parameters as possible, minimizing UV assumptions

- ▶ requires a **global** analysis: EW + Higgs + top + ...
- ▶ minimum bias setup, flavor symmetric → **20-30** params relevant @LHC

see talk by A. Biekötter

# The Higgs width

a crucial observable for the Higgs sector

SM: 
$$\Gamma_H \simeq 4 \text{ MeV} \quad \rightarrow \quad \frac{\Gamma_H}{m_H} \simeq 3 \cdot 10^{-5} \ll 1$$

⇒ Higgs measurements can be factored into

$$\sigma(i \rightarrow H) \times Br(H \rightarrow f)$$

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SMEFT: probe separately production and decay 👍

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$\Rightarrow$  Higgs measurements can be factored into

$$\sigma(i \rightarrow H) \times Br(H \rightarrow f)$$

SMEFT: probe separately production and decay 👍

$$Br_{\text{SMEFT}}(H \rightarrow f) = \left[ \frac{\Gamma(H \rightarrow f)}{\Gamma_H^{\text{tot}}} \right]_{\text{SM}} \left[ 1 + \frac{\delta\Gamma(H \rightarrow f)}{\Gamma_{\text{SM}}(H \rightarrow f)} - \frac{\delta\Gamma_H^{\text{tot}}}{\Gamma_{H,\text{SM}}^{\text{tot}}} \right]$$

- ▶ both  $\delta\Gamma(H \rightarrow f)$  and  $\delta\Gamma_H^{\text{tot}}$  need to be determined
- ▶  $\delta\Gamma_H^{\text{tot}}$  enters all processes  $\rightarrow$  **strong impact** on global SMEFT analyses!

# The Higgs width in the SMEFT - preliminaries

Focus on the leading contributions:

- ▶ LO in the EFT: up to SM -  $\mathcal{L}_6$  **interference**.

$$\Gamma_H = \Gamma_{H,SM} \left[ 1 + \frac{\delta\Gamma_H}{\Gamma_{H,SM}} \right] \quad \frac{\delta\Gamma_H}{\Gamma_{H,SM}} = \sum_i a_i \bar{C}_i = \sum_i a_i \left( C_i \frac{v^2}{\Lambda^2} \right)$$

- ▶ **tree level**.

SM couplings  $H\gamma\gamma$ ,  $HZ\gamma$ ,  $Hgg$  included as effective vertices for  $H \rightarrow f\bar{f}\gamma / \gamma\gamma / gg$ .  
Neglected in other channels.

- ▶ up to **4-body** decays.

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Conventions and assumptions:

- ▶ Warsaw basis Grzadkowski, Iskrzynski, Misiak, Rosiek 1008.4884
- ▶ **U(3)<sup>5</sup> flavor symmetry**  $\rightarrow g_{Hff} \sim y_f$  also in the SMEFT
- ▶ **inclusive** calculation, not differential  $\rightarrow$  CP odd terms do not contribute
- ▶ EW input scheme:  $\{m_Z, m_W, G_F\} \rightarrow \delta m_W, \delta m_Z = 0, \delta e \neq 0$  ↪ backup



# The Higgs width in the SMEFT

leading channels:

$$H \rightarrow \bar{f}f$$

$$H \rightarrow gg$$

$$H \rightarrow \gamma\gamma$$

$$H \rightarrow \bar{f}f\gamma$$

$$H \rightarrow 4f$$

- ▶  $\Gamma(H \rightarrow 4f), \Gamma(H \rightarrow \gamma\gamma), \Gamma(H \rightarrow \bar{b}b)$  most relevant ones individually
- ▶ all need to be calculated for  $\delta\Gamma_H^{\text{tot}} \rightarrow Br$

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$$\frac{\Gamma(H \rightarrow \bar{f}f)}{\Gamma_{SM}(H \rightarrow \bar{f}f)} \simeq 1 + 2\delta g_{Hff}$$

$$\delta g_{Hff} = \bar{C}_{H\Box} - \frac{\bar{C}_{HD}}{4} - \bar{C}_{HI}^{(3)} + \frac{\bar{C}'_{II}}{2} - \frac{5}{2}\bar{C}_{fH}$$

Alonso, Jenkins, Manohar, Trott 1312.2014

- ▶ renorm. of the H field
  - ▶ contrib. to  $\mu$  decay  $\rightarrow G_F \rightarrow v$
  - ▶ direct  $\mathcal{O}_{fH}$  contribution  $\left(-\frac{3}{2}\bar{C}_{fH}\right)$   
+  
contrib. to  $m_f \rightarrow y_f$   $\left(-\bar{C}_{fH}\right)$
- 
- ▶  $\Gamma(H \rightarrow 4f), \Gamma(H \rightarrow \gamma\gamma), \Gamma(H \rightarrow \bar{b}b)$  most relevant ones individually
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$$H \rightarrow \bar{f}f\gamma$$

$$H \rightarrow 4f$$

$$\frac{\Gamma(h \rightarrow gg)}{\Gamma^{SM}(h \rightarrow gg)} \simeq 1 + \frac{16\pi^2}{g_s^2 I^g} \bar{C}_{HG}, \quad I^g \simeq 0.375$$

Manohar,Wise 0601212

- ▶  $\Gamma(H \rightarrow 4f), \Gamma(H \rightarrow \gamma\gamma), \Gamma(H \rightarrow \bar{b}b)$  most relevant ones individually
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$$\mathcal{C}_{\gamma\gamma} = s_\theta^2 \bar{C}_{HW} + c_\theta^2 \bar{C}_{HB} - s_\theta c_\theta \bar{C}_{HWB}$$

Bergström, Hulth Nucl.Phys.B259(1985)137  
Manohar, Wise 0601212

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→  $H \rightarrow \gamma\gamma$

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**loop-factor enhancement**  
in the relative correction:

tree-level SMEFT vs loop SM

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# The Higgs width in the SMEFT

leading channels:

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$$H \rightarrow \bar{f}f\gamma$$

$$H \rightarrow 4f$$

available as  $H \rightarrow ZZ^*$ ,  $H \rightarrow WW^*$   $\times Br(Z, W)$   
relying on narrow width approx. for  $Z, W$ .

good in SM but **not sufficient** in the SMEFT!

main reason: tree  $\gamma\gamma, Z\gamma$  mediated diagrams

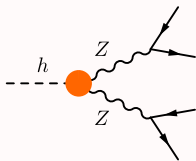
also missing:

- ▶ CC - NC interference
- ▶ crossed-current interference in  $ZZ$  diagrams
- ▶  $\delta\Gamma_V, \delta m_V^2$  corrections for off-shell boson

- ▶  $\Gamma(H \rightarrow 4f), \Gamma(H \rightarrow \gamma\gamma), \Gamma(H \rightarrow \bar{b}b)$  most relevant ones individually
- ▶ all need to be calculated for  $\delta\Gamma_H^{\text{tot}} \rightarrow Br$

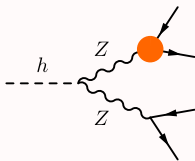
# H → 4f in the SMEFT

① corrections to SM diagrams

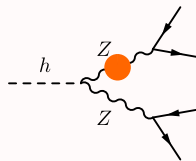


$$\propto g_{\mu\nu} \text{ (SM-like)}$$

$$\propto g_{\mu\nu} p \cdot q - p_\nu q_\mu$$



$$\delta g_L, \delta g_R$$



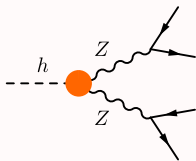
$$\frac{-im_Z \delta \Gamma_Z + (2m_Z - i\Gamma_Z) \delta m_Z}{p^2 - m_Z^2 + i\Gamma_Z m_Z}$$



hard to extract from  
MC simulation!  
full treatment requires  
analytic calculation

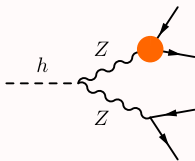
# H $\rightarrow$ 4f in the SMEFT

## ① corrections to SM diagrams

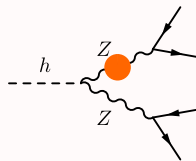


$$\propto g_{\mu\nu} \text{ (SM-like)}$$

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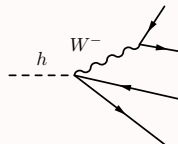
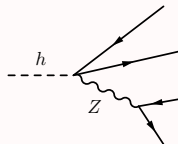
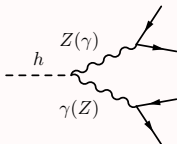
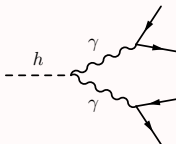


$$\delta g_L, \delta g_R$$



$$\frac{-im_Z \delta \Gamma_Z + (2m_Z - i\Gamma_Z) \delta m_Z}{p^2 - m_Z^2 + i\Gamma_Z m_Z}$$

## ② genuine SMEFT diagrams

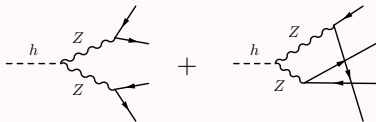




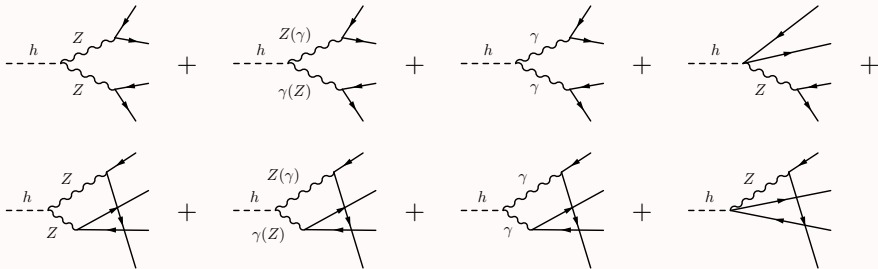
# H $\rightarrow$ 4f in the SMEFT - complexity

$$h \rightarrow e^+ e^- e^+ e^-$$

SM



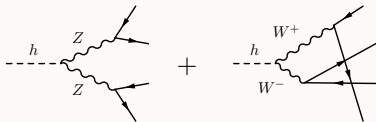
interfering with



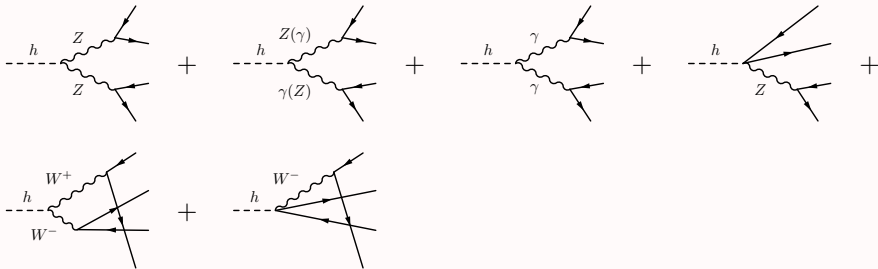
# H $\rightarrow$ 4f in the SMEFT - complexity

$$h \rightarrow \bar{u} u \bar{d} d$$

SM

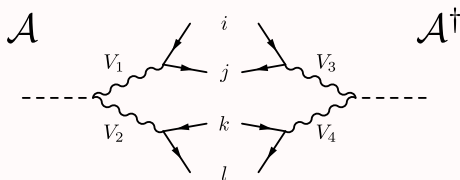


interfering with



# H $\rightarrow$ 4f - analytic calculation

fully analytical treatment. automated with general decomposition:



$$\mathcal{A}\mathcal{A}^\dagger \sim g_{HV_1V_2} g_{HV_3V_4} \sum_n \mathcal{T}^{(n)}$$

$$\mathcal{T}^{(n)} = \mathcal{K}^{(n)} \left( g_{L,R}^{ij,V_1}, g_{L,R}^{ij,V_3}, g_{L,R}^{kl,V_2}, g_{L,R}^{kl,V_4} \right) \mathcal{F}_{V_1V_2V_3V_4}^{(n)}(p_a, m_a), \quad a = \{i, j, k, l\}$$

- ▶ for  $m_i, m_j, m_k, m_l = 0$  there are only 8 independent  $\mathcal{F}_{V_1V_2V_3V_4}$
- ▶  $\mathcal{F}$  computed for every  $\{V\}$  set.  
numerical integration of phase space: **Vegas** in Mathematica.  
cross-check: 2 independent parameterizations of phase sp., RAMBO.

# H → 4f - results

Example:  $H \rightarrow e^+ e^- \mu^+ \mu^-$   $m_i, m_j, m_k, m_l = 0$

$$\frac{\delta\Gamma(H \rightarrow e^+ e^- \mu^+ \mu^-)}{\Gamma_{\text{SM}}(H \rightarrow e^+ e^- \mu^+ \mu^-)} = \sum_i a_i \bar{C}_i$$

	$\bar{C}_{HW}$	$\bar{C}_{HB}$	$\bar{C}_{HWB}$	$\bar{C}_{H\Box}$	$\bar{C}_{HD}$	$\bar{C}_{Hl}^{(1)}$	$\bar{C}_{Hl}^{(3)}$	$\bar{C}_{He}$	$\bar{C}_{Hq}^{(1)}$	$\bar{C}_{Hq}^{(3)}$	$\bar{C}_{Hu}$	$\bar{C}_{Hd}$	$\bar{C}'_{ll}$
Z	-0.78	-0.22	0.30	2	0.17	4.38	-1.62	-3.52					3.
A	1.04	-1.08	-0.68										
E						-2.23	-2.23	1.80					
G			-0.38		0.06	0.15	1.14	0.15	-0.39	-1.34	-0.20	0.15	-0.83
tot	0.26	-1.30	-0.76	2.	0.23	2.30	-2.71	-1.58	-0.39	-1.34	-0.20	0.15	2.17

Z	corrections to SM diagram
A	$\gamma$ diagrams
E	contact diagrams ( $HZee$ )
G	$\delta\Gamma_Z^{\text{tot}}/\Gamma_{Z,SM}$ on + off-shell Z

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# Impact of previously neglected contributions

## (1) photon-mediated diagrams

$\mathcal{O}(1 - 250)\%$  effect

	with $\gamma$			without $\gamma$		
	$\bar{C}_{HW}$	$\bar{C}_{HB}$	$\bar{C}_{HWB}$	$\bar{C}_{HW}$	$\bar{C}_{HB}$	$\bar{C}_{HWB}$
$h \rightarrow e^+ e^- \mu^+ \mu^-$	0.26	-1.30	-0.38	-0.77	-0.22	0.30
$h \rightarrow \bar{u} u \bar{c} c$	1.45	-2.63	-0.29	-0.77	-0.22	1.33
$h \rightarrow e^+ e^- \bar{d} d$	0.50	-1.55	-0.37	-0.77	-0.22	0.47
$h \rightarrow e^+ e^- e^+ e^-$	0.02	-2.28	0.27	-0.76	-0.21	0.44
$h \rightarrow \bar{u} u \bar{u} u$	1.39	-2.72	-0.14	-0.76	-0.21	1.19
$h \rightarrow e^+ e^- \bar{\nu}_e \nu_e$	-1.49	0.01	-0.06	-1.48	-0.007	-0.07

# Impact of previously neglected contributions

## (2) $Z - W$ interference terms

$\mathcal{O}(1 - 200)\%$  effect

$\delta\Gamma(H \rightarrow e^+ e^- \bar{\nu}_e \nu_e) / \Gamma_{\text{SM}}$  omitting  $\gamma$  and  $\delta\Gamma_Z, \delta\Gamma_W$  contrib.

	$\bar{C}_{HW}$	$\bar{C}_{HB}$	$\bar{C}_{HWB}$	$\bar{C}_{H\Box}$	$\bar{C}_{HD}$	$\bar{C}_{HI}^{(1)}$	$\bar{C}_{HI}^{(3)}$	$\bar{C}_{He}$	$\bar{C}_{Hq}^{(1)}$	$\bar{C}_{Hq}^{(3)}$	$\bar{C}_{Hu}$	$\bar{C}_{Hd}$	$\bar{C}'_{ll}$
full	-1.49	-0.007	-0.07	2.	-0.55	-0.008	-3.74	-0.04	0	0	0	0	3.
NW	-1.46	-0.01	-0.003	2.	-0.49	0.004	-3.77	-0.04	0.	0.	0.	0.	3.

full	$ \mathcal{A}_{ZZ} ^2 +  \mathcal{A}_{WW} ^2 + 2\text{Re}\mathcal{A}_{ZZ}\mathcal{A}_{WW}^\dagger$
NW	$ \mathcal{A}_{ZZ} ^2 +  \mathcal{A}_{WW} ^2$

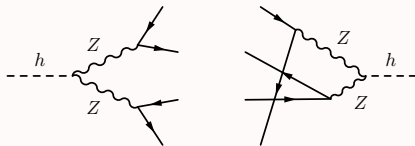
breakdown of the full case:

	$\bar{C}_{HW}$	$\bar{C}_{HB}$	$\bar{C}_{HWB}$	$\bar{C}_{H\Box}$	$\bar{C}_{HD}$	$\bar{C}_{HI}^{(1)}$	$\bar{C}_{HI}^{(3)}$	$\bar{C}_{He}$	$\bar{C}_{Hq}^{(1)}$	$\bar{C}_{Hq}^{(3)}$	$\bar{C}_{Hu}$	$\bar{C}_{Hd}$	$\bar{C}'_{ll}$
ZZ	-0.04	-0.01	-0.003	0.09	-0.008	0.004	-0.19	-0.04	0	0	0	0	0.14
WW	-1.49	0	0	2.0	-0.50	0	-3.77	0	0	0	0	0	3.00
WZ	0.04	0.004	-0.06	-0.10	-0.04	-0.01	0.21	0	0	0	0	0	-0.14
tot	-1.49	-0.007	-0.07	2.	-0.55	-0.008	-3.74	-0.04	0	0	0	0	3.

# Impact of previously neglected contributions

## (3) NC crossed - interference terms

$\mathcal{O}(\text{few} - 40)\%$  effect



$\delta\Gamma(H \rightarrow e^+e^-e^+e^-)/\Gamma_{\text{SM}}$  incl. only ZZ and HZee diagrams

	$\bar{C}_{HW}$	$\bar{C}_{HB}$	$\bar{C}_{HWB}$	$\bar{C}_{H0}$	$\bar{C}_{HD}$	$\bar{C}_{Hl}^{(1)}$	$\bar{C}_{Hl}^{(3)}$	$\bar{C}_{He}$	$\bar{C}_{Hq}^{(1)}$	$\bar{C}_{Hq}^{(3)}$	$\bar{C}_{Hu}$	$\bar{C}_{Hd}$	$\bar{C}'_{ll}$
full	-0.75	-0.22	0.43	2.	0.28	2.09	-3.91	-1.64	0	0	0	0	3.
NW	-0.78	-0.221	0.30	2.	0.17	2.15	-3.85	-1.73	0.	0.	0.	0.	3.

full:  $|\mathcal{A}_{ijkl}|^2 + |\mathcal{A}_{ilkj}|^2 + 2\text{Re}\mathcal{A}_{ijkl}\mathcal{A}_{ilkj}^\dagger$

NW:  $|\mathcal{A}_{ijkl}|^2 + |\mathcal{A}_{ilkj}|^2$



# Impact of previously neglected contributions

## (4) $\delta\Gamma_V$ , $\delta m_V$ from off-shell boson

$\mathcal{O}(\text{few})\%$  effect

narrow width approx.:

$$\frac{\delta\Gamma(H \rightarrow VV^* \rightarrow 4f)}{\Gamma_{SM}(H \rightarrow VV^* \rightarrow 4f)} = -\frac{\delta\Gamma_V}{\Gamma_{V,SM}} + \dots$$

full calculation:

$h \rightarrow e^+ e^- \mu^+ \mu^-$	$-0.820$	$\delta\Gamma_Z/\Gamma_{Z,SM}$	
$h \rightarrow e^+ e^- e^+ e^-$	$-0.748$	$\delta\Gamma_Z/\Gamma_{Z,SM}$	
$h \rightarrow e^+ \nu_e \bar{\nu}_\mu \mu^-$	$-0.915$	$\delta\Gamma_W/\Gamma_{W,SM}$	
$h \rightarrow e^+ \nu_e \bar{\nu}_e e^-$	$-0.914$	$\delta\Gamma_W/\Gamma_{W,SM}$	$- 0.038 \delta\Gamma_Z/\Gamma_{Z,SM}$

# H → 4f summary

- ▶ we did a **fully analytic** calculation, with numerical integration of phase space
- ▶ also generated all channels with MG5\_aMC@NLO using the **SMEFTsim** package → agreement to 1% or better ✓
- ▶ analytic treatment has a few advantages:
  - ▶ allows to separate contributions
  - ▶ easier to **linearize in  $\delta\Gamma_V, \delta m_V$**
  - ▶ more stable for the massless fermions case with  $\gamma$  diagrams
  - ▶ calculation can be **automated** in a dedicated package → much faster than MC generation
- ▶ some previously neglected contributions turn out to be relevant:  
 **$\gamma$  diagrams and  $Z - W$  interference**

Brivio, Jiang, Trott 1709.06492

# The total Higgs width in the SMEFT

putting together all the main contributions\* we obtain

$$\Gamma_H^{\text{tot}} = \Gamma_{H,SM}^{\text{tot}} \left[ 1 + \frac{\delta\Gamma_H^{\text{tot}}}{\Gamma_{H,SM}^{\text{tot}}} \right]$$

$$\Gamma_{H,SM}^{\text{tot}} = 5.98 \text{ MeV}$$

$$\begin{aligned} \frac{\delta\Gamma_H^{\text{tot}}}{\Gamma_{H,SM}^{\text{tot}}} = & -1.43\bar{C}_{dH} - 0.13\bar{C}_{uH} - 0.09\bar{C}_{eH} \\ & + 22.24\bar{C}_{HG} - 0.80\bar{C}_{HW} - 1.05\bar{C}_{HB} + 0.85\bar{C}_{HWB} + 1.92\bar{C}_{H\Box} - 0.47\bar{C}_{HD} \\ & - 0.004\bar{C}_{HI}^{(1)} - 2.18\bar{C}_{HI}^{(3)} + 0.001\bar{C}_{He} + 0.003\bar{C}_{Hq}^{(1)} + 0.019\bar{C}_{Hq}^{(3)} \\ & + 0.00004\bar{C}_{Hu} - 0.0005\bar{C}_{Hd} + 1.10\bar{C}'_{II} \end{aligned}$$

\*  $gg + \gamma\gamma + \bar{b}b + \bar{c}c + \tau^+\tau^- + 4f + \bar{f}f\gamma$

PRELIMINARY

- ▶ the inclusive Higgs width is a crucial observable for the Higgs sector
- ▶ improved calculation of  $H \rightarrow 4f, H \rightarrow \bar{f}f\gamma$  without relying on the narrow width approx. for  $Z, W$   
→ important for LHC measurements
- ▶ joined all the main channels into  $\delta\Gamma_H^{\text{tot}}$
- ▶ the complete analysis will appear very soon!  
with an **automated package** that gives  $\text{Br}_{H \rightarrow X}(C_i)$
- ▶  $\text{Br}$ 's and  $\Gamma_H^{\text{tot}}$  are computed **once and for all!**  
→ can be used directly without further MC generation
- ▶ possible refinements:  
 $\{\alpha_{em}, m_Z, G_F\}$  input scheme  
full massive fermions treatment  
phase space integration with cuts  
...

**Backup slides**

$X^3$		$\varphi^6$ and $\varphi^4 D^2$		$\psi^2 \varphi^3$	
$Q_G$	$f^{ABC} G_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{\varphi}$	$(\varphi^{\dagger} \varphi)^3$	$Q_{e\varphi}$	$(\varphi^{\dagger} \varphi)(\bar{l}_p e_r \varphi)$
$Q_{\tilde{G}}$	$f^{ABC} \tilde{G}_{\mu}^{A\nu} G_{\nu}^{B\rho} G_{\rho}^{C\mu}$	$Q_{\varphi \square}$	$(\varphi^{\dagger} \varphi) \square (\varphi^{\dagger} \varphi)$	$Q_{u\varphi}$	$(\varphi^{\dagger} \varphi)(\bar{q}_p u_r \tilde{\varphi})$
$Q_W$	$\varepsilon^{IJK} W_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$	$Q_{\varphi D}$	$(\varphi^{\dagger} D^{\mu} \varphi)^{\star} (\varphi^{\dagger} D_{\mu} \varphi)$	$Q_{d\varphi}$	$(\varphi^{\dagger} \varphi)(\bar{q}_p d_r \varphi)$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_{\mu}^{I\nu} W_{\nu}^{J\rho} W_{\rho}^{K\mu}$				
$X^2 \varphi^2$		$\psi^2 X \varphi$		$\psi^2 \varphi^2 D$	
$Q_{\varphi G}$	$\varphi^{\dagger} \varphi G_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eW}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi l}^{(1)}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{l}_p \gamma^{\mu} l_r)$
$Q_{\varphi \tilde{G}}$	$\varphi^{\dagger} \varphi \tilde{G}_{\mu\nu}^A G^{A\mu\nu}$	$Q_{eB}$	$(\bar{l}_p \sigma^{\mu\nu} e_r) \varphi B_{\mu\nu}$	$Q_{\varphi l}^{(3)}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu}^I \varphi)(\bar{l}_p \tau^I \gamma^{\mu} l_r)$
$Q_{\varphi W}$	$\varphi^{\dagger} \varphi W_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A u_r) \tilde{\varphi} G_{\mu\nu}^A$	$Q_{\varphi e}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{e}_p \gamma^{\mu} e_r)$
$Q_{\varphi \tilde{W}}$	$\varphi^{\dagger} \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$	$Q_{uW}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tau^I \tilde{\varphi} W_{\mu\nu}^I$	$Q_{\varphi q}^{(1)}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{q}_p \gamma^{\mu} q_r)$
$Q_{\varphi B}$	$\varphi^{\dagger} \varphi B_{\mu\nu} B^{\mu\nu}$	$Q_{uB}$	$(\bar{q}_p \sigma^{\mu\nu} u_r) \tilde{\varphi} B_{\mu\nu}$	$Q_{\varphi q}^{(3)}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu}^I \varphi)(\bar{q}_p \tau^I \gamma^{\mu} q_r)$
$Q_{\varphi \tilde{B}}$	$\varphi^{\dagger} \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$	$Q_{dG}$	$(\bar{q}_p \sigma^{\mu\nu} T^A d_r) \varphi G_{\mu\nu}^A$	$Q_{\varphi u}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{u}_p \gamma^{\mu} u_r)$
$Q_{\varphi WB}$	$\varphi^{\dagger} \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$	$Q_{dW}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \tau^I \varphi W_{\mu\nu}^I$	$Q_{\varphi d}$	$(\varphi^{\dagger} i \overleftrightarrow{D}_{\mu} \varphi)(\bar{d}_p \gamma^{\mu} d_r)$
$Q_{\varphi \tilde{W}B}$	$\varphi^{\dagger} \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$	$Q_{dB}$	$(\bar{q}_p \sigma^{\mu\nu} d_r) \varphi B_{\mu\nu}$	$Q_{\varphi ud}$	$i(\tilde{\varphi}^{\dagger} D_{\mu} \varphi)(\bar{u}_p \gamma^{\mu} d_r)$

$(\bar{L}L)(\bar{L}L)$		$(\bar{R}R)(\bar{R}R)$		$(\bar{L}L)(\bar{R}R)$	
$Q_{ll}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{l}_s \gamma^\mu l_t)$	$Q_{ee}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{e}_s \gamma^\mu e_t)$	$Q_{le}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{qq}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{uu}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{lu}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{u}_s \gamma^\mu u_t)$
$Q_{qq}^{(3)}$	$(\bar{q}_p \gamma_\mu \tau^I q_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{dd}$	$(\bar{d}_p \gamma_\mu d_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{ld}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{d}_s \gamma^\mu d_t)$
$Q_{lq}^{(1)}$	$(\bar{l}_p \gamma_\mu l_r)(\bar{q}_s \gamma^\mu q_t)$	$Q_{eu}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{u}_s \gamma^\mu u_t)$	$Q_{qe}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{e}_s \gamma^\mu e_t)$
$Q_{lq}^{(3)}$	$(\bar{l}_p \gamma_\mu \tau^I l_r)(\bar{q}_s \gamma^\mu \tau^I q_t)$	$Q_{ed}$	$(\bar{e}_p \gamma_\mu e_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{u}_s \gamma^\mu u_t)$
		$Q_{ud}^{(1)}$	$(\bar{u}_p \gamma_\mu u_r)(\bar{d}_s \gamma^\mu d_t)$	$Q_{qu}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{u}_s \gamma^\mu T^A u_t)$
		$Q_{ud}^{(8)}$	$(\bar{u}_p \gamma_\mu T^A u_r)(\bar{d}_s \gamma^\mu T^A d_t)$	$Q_{qd}^{(1)}$	$(\bar{q}_p \gamma_\mu q_r)(\bar{d}_s \gamma^\mu d_t)$
				$Q_{qd}^{(8)}$	$(\bar{q}_p \gamma_\mu T^A q_r)(\bar{d}_s \gamma^\mu T^A d_t)$
$(\bar{L}R)(\bar{R}L)$ and $(\bar{L}R)(\bar{L}R)$		$B$ -violating			
$Q_{ledq}$	$(\bar{l}_p^j e_r)(\bar{d}_s^j q_t^j)$	$Q_{duq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(d_p^\alpha)^T C u_r^\beta] [(q_s^\gamma)^T C l_t^k]$		
$Q_{quqd}^{(1)}$	$(\bar{q}_p^j u_r) \varepsilon_{jk} (\bar{q}_s^k d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jk} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(u_s^\gamma)^T C e_t]$		
$Q_{quqd}^{(8)}$	$(\bar{q}_p^j T^A u_r) \varepsilon_{jk} (\bar{q}_s^k T^A d_t)$	$Q_{qqq}$	$\varepsilon^{\alpha\beta\gamma} \varepsilon_{jkmn} [(q_p^{\alpha j})^T C q_r^{\beta k}] [(q_s^m)^T C l_t^n]$		
$Q_{lequ}^{(1)}$	$(\bar{l}_p^j e_r) \varepsilon_{jk} (\bar{q}_s^k u_t)$	$Q_{duu}$	$\varepsilon^{\alpha\beta\gamma} [(d_p^\alpha)^T C u_r^\beta] [(u_s^\gamma)^T C e_t]$		
$Q_{lequ}^{(3)}$	$(\bar{l}_p^j \sigma_{\mu\nu} e_r) \varepsilon_{jk} (\bar{q}_s^k \sigma^{\mu\nu} u_t)$				

# Shifts from input parameters

SM case.

Parameters in the canonically normalized Lagrangian :  $\bar{v}, \bar{g}_1, \bar{g}_2, s_{\bar{\theta}}$

The values can be inferred from the measurements e.g. of  $\{\alpha_{\text{em}}, m_Z, G_f\}$  :

$$\alpha_{\text{em}} = \frac{\bar{g}_1 \bar{g}_2}{\bar{g}_1^2 + \bar{g}_2^2}$$

$$m_Z = \frac{\bar{g}_2 \bar{v}}{2c_{\bar{\theta}}}$$

$$G_f = \frac{1}{\sqrt{2}\bar{v}^2}$$

→

$$\hat{v}^2 = \frac{1}{\sqrt{2}G_f}$$

$$\sin \hat{\theta}^2 = \frac{1}{2} \left( 1 - \sqrt{1 - \frac{4\pi\alpha_{\text{em}}}{\sqrt{2}G_f m_Z^2}} \right)$$

$$\hat{g}_1 = \frac{\sqrt{4\pi\alpha_{\text{em}}}}{\cos \hat{\theta}}$$

$$\hat{g}_2 = \frac{\sqrt{4\pi\alpha_{\text{em}}}}{\sin \hat{\theta}}$$

in the SM at tree-level  $\bar{\kappa} = \hat{\kappa}$



# Shifts from input parameters

SMEFT case.

Parameters in the canonically normalized Lagrangian :  $\bar{v}, \bar{g}_1, \bar{g}_2, s_{\bar{\theta}}$

The values can be inferred from the measurements e.g. of  $\{\alpha_{\text{em}}, m_Z, G_f\}$  :

$$\begin{aligned}\alpha_{\text{em}} &= \frac{\bar{g}_1 \bar{g}_2}{\bar{g}_1^2 + \bar{g}_2^2} \left[ 1 + \bar{v}^2 C_{HWB} \frac{\bar{g}_2^3 / \bar{g}_1}{\bar{g}_1^2 + \bar{g}_2^2} \right] & \hat{v}^2 &= \frac{1}{\sqrt{2} G_f} \\ m_Z &= \frac{\bar{g}_2 \bar{v}}{2 c_{\bar{\theta}}} + \delta m_Z(C_i) & \sin \hat{\theta}^2 &= \frac{1}{2} \left( 1 - \sqrt{1 - \frac{4\pi \alpha_{\text{em}}}{\sqrt{2} G_f m_Z^2}} \right) \\ G_f &= \frac{1}{\sqrt{2} \bar{v}^2} + \delta G_f(C_i) & \hat{g}_1 &= \frac{\sqrt{4\pi \alpha_{\text{em}}}}{\cos \hat{\theta}} \\ & & \hat{g}_2 &= \frac{\sqrt{4\pi \alpha_{\text{em}}}}{\sin \hat{\theta}}\end{aligned}$$

in the SM at tree-level  $\bar{\kappa} = \hat{\kappa}$

in the SMEFT  $\bar{\kappa} = \hat{\kappa} + \delta \kappa(C_i)$

# Shifts from input parameters

To have numerical predictions it is necessary to replace  $\bar{\kappa} \rightarrow \hat{\kappa} + \delta\kappa(C_i)$  for all the parameters in the Lagrangian.

---

$\{\alpha_{\text{em}}, m_Z, G_f\}$  scheme

$$\delta m_Z^2 = m_Z^2 \hat{v}^2 \left( \frac{c_{HD}}{2} + 2c_{\hat{\theta}} s_{\hat{\theta}} c_{HWB} \right)$$

$$\delta G_f = \frac{\hat{v}^2}{\sqrt{2}} \left( (c_{HI}^{(3)})_{11} + (c_{HI}^{(3)})_{22} - (c_{II})_{1221} \right)$$

$$\delta g_1 = \frac{s_{\hat{\theta}}^2}{2(1-2s_{\hat{\theta}}^2)} \left( \sqrt{2}\delta G_f + \delta m_Z^2/m_Z^2 + 2\frac{c_{\hat{\theta}}^3}{s_{\hat{\theta}}} c_{HWB} \hat{v}^2 \right)$$

$$\delta g_2 = -\frac{c_{\hat{\theta}}^2}{2(1-2s_{\hat{\theta}}^2)} \left( \sqrt{2}\delta G_f + \delta m_Z^2/m_Z^2 + 2\frac{s_{\hat{\theta}}^3}{c_{\hat{\theta}}} c_{HWB} \hat{v}^2 \right)$$

$$\delta s_{\hat{\theta}}^2 = 2c_{\hat{\theta}}^2 s_{\hat{\theta}}^2 (\delta g_1 - \delta g_2) + c_{\hat{\theta}} s_{\hat{\theta}} (1 - 2s_{\hat{\theta}}^2) c_{HWB} \hat{v}^2$$

$$\delta m_h^2 = m_h^2 \hat{v}^2 \left( 2c_{H\Box} - \frac{c_{HD}}{2} - \frac{3c_H}{2\lambda m} \right)$$

# Shifts from input parameters

To have numerical predictions it is necessary to replace  $\bar{\kappa} \rightarrow \hat{\kappa} + \delta\kappa(C_i)$   
for all the parameters in the Lagrangian.

---

$\{m_W, m_Z, G_f\}$  scheme

$$\delta m_Z^2 = m_Z^2 \hat{v}^2 \left( \frac{c_{HD}}{2} + 2c_{\hat{\theta}} s_{\hat{\theta}} c_{HWB} \right)$$

$$\delta G_f = \frac{\hat{v}^2}{\sqrt{2}} \left( (c_{HI}^{(3)})_{11} + (c_{HI}^{(3)})_{22} - (c_{II})_{1221} \right)$$

$$\delta g_1 = -\frac{1}{2} \left( \sqrt{2} \delta G_f + \frac{1}{s_{\hat{\theta}}^2} \frac{\delta m_Z^2}{m_Z^2} \right)$$

$$\delta g_2 = -\frac{1}{\sqrt{2}} \delta G_f$$

$$\delta s_{\hat{\theta}}^2 = 2c_{\hat{\theta}}^2 s_{\hat{\theta}}^2 (\delta g_1 - \delta g_2) + c_{\hat{\theta}} s_{\hat{\theta}} (1 - 2s_{\hat{\theta}}^2) c_{HWB} \hat{v}^2$$

$$\delta m_h^2 = m_h^2 \hat{v}^2 \left( 2c_{CH\Box} - \frac{c_{HD}}{2} - \frac{3c_{CH}}{2\lambda m} \right)$$

# The SMEFTsim package

an UFO & FeynRules model with\*:

Brivio, Jiang, Trott 1709.06492  
feynrules.irmp.ucl.ac.be/wiki/SMEFT

1. the complete B-conserving Warsaw basis for 3 generations , including all complex phases and ~~CP~~ terms
2. automatic field redefinitions to have **canonical kinetic terms**
3. automatic **parameter shifts** due to the choice of an input parameters set

 [backup](#)

Main scope:

estimate **tree-level**  $|\mathcal{A}_{\text{SM}}\mathcal{A}_{d=6}^*|$  **interference** terms  $\rightarrow$  theo. accuracy  $\gtrsim 1\%$

\* at the moment only LO, unitary gauge implementation

# The SMEFTsim package

6 different implementations available

Brivio, Jiang, Trott 1709.06492

$$\textcircled{3} \text{ flavor structures } \left\{ \begin{array}{l} \text{general} \\ U(3)^5 \text{ symmetric} \\ \text{linear MFV} \end{array} \right. \times \textcircled{2} \text{ input schemes } \left\{ \begin{array}{l} \hat{\alpha}_{em}, \hat{m}_Z, \hat{G}_f \\ \hat{m}_W, \hat{m}_Z, \hat{G}_f \end{array} \right.$$

[feynrules.irmp.ucl.ac.be/wiki/SMEFT](http://feynrules.irmp.ucl.ac.be/wiki/SMEFT)

[viki: SMEFT](#)  
**Standard Model Effective Field Theory – The SMEFTsim package**  
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 NBIA and Discovery Center, Niels Bohr Institute, University of Copenhagen

Pre-exported UFO files (include restriction cards)

	Set A		Set B	
	$\alpha$ scheme	$m_W$ scheme	$\alpha$ scheme	$m_W$ scheme
Flavor general SMEFT	<a href="#">SMEFTsim_A_general_alphaScheme_UFO.tar.gz</a> ↓	<a href="#">SMEFTsim_A_general_MwScheme_UFO.tar.gz</a> ↓	<a href="#">SMEFT_alpha_UFO.zip</a> ↓	<a href="#">SMEFT_mW_UFO.zip</a> ↓
MFV SMEFT	<a href="#">SMEFTsim_A_MFV_alphaScheme_UFO.tar.gz</a> ↓	<a href="#">SMEFTsim_A_MFV_MwScheme_UFO.tar.gz</a> ↓	<a href="#">SMEFT_alpha_MFV_UFO.zip</a> ↓	<a href="#">SMEFT_mW_MFV_UFO.zip</a> ↓
$U(3)^5$ SMEFT	<a href="#">SMEFTsim_A_U35_alphaScheme_UFO.tar.gz</a> ↓	<a href="#">SMEFTsim_A_U35_MwScheme_UFO.tar.gz</a> ↓	<a href="#">SMEFT_alpha_FLU_UFO.zip</a> ↓	<a href="#">SMEFT_mW_FLU_UFO.zip</a> ↓