

Effective Field Theory after a New-Physics Discovery

Matthias König Physik-Institut Universität Zürich *"From the Planck scale to the EW scale"* Granada, Jun 3, 2019













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Integrate out high-scale physics \rightarrow Match onto EFT Lagrangian! *Example*: TeV-scale NP in low-energy observables



So what about the case of $q^2 \sim \Lambda^2$?



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 $\stackrel{?}{\Rightarrow}$ High-energy processes computable at **fixed order**.



 \Rightarrow Whether $q^2 \sim m_f^2$ or $q^2 \sim M^2$: there are logs to be summed.



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$$\mathcal{L}_{\text{eff}} = \frac{C_{\phi}}{\Lambda} S |D_{\mu}\phi|^2 + \frac{C_g}{\Lambda} S F^a_{\mu\nu} F^{a,\mu\nu} + \frac{C_u}{\Lambda} S \bar{Q}_L \tilde{\phi} u_R + \frac{C_d}{\Lambda} S \bar{Q}_L \phi d_R$$

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- **3** The **power-counting** implied by this EFT does **not** reproduce the actual scaling of the amplitudes:

$$\mathcal{A}(S \to hh) = \mathcal{O}(\lambda^0), \ \mathcal{A}(S \to VV) = \mathcal{O}(\lambda), \ \mathcal{A}(S \to \bar{f}f) = \mathcal{O}(\lambda)$$





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Lots of (interesting) field-theory implications: non-local operators, $C \cdot \langle \mathcal{O} \rangle \rightarrow \int d\omega C(\omega) \cdot \langle \mathcal{O} \rangle(\omega)$, Wilson lines, power-counting \neq field mass-dimension, multiple effective fields per particle, ...



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Somewhat more technical but also more powerful than local EFTs!



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Write out all possible operators:

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Based on:

Effective Field Theory after a New-Physics Discovery

Stefan Alte, MK, Matthias Neubert

JHEP 1808 (2018) 095, [arXiv:1806.01278]

Effective Theory for a Heavy Scalar Coupled to the SM via Vector-Like Quarks

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[arXiv:1902.04593]





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- If $m_{\Psi} \gg m_S$, then we integrate can out Ψ Wilson-style and obtain the "SMEFT+S". To properly separate the scales m_S and μ_{SM} , we **match** this EFT **onto the SCET**.
- If $m_{\Psi} \sim m_S$, then we integrate can out Ψ without taking the local limit, directly matching the UV theory onto the SCET.

$m_{\Psi} \gg m_S$	$\mathcal{L}_{ ext{SCET}_{ ext{BSM}}}$	$\mathcal{L}_{ ext{SMEFT}+S}$	$\mathcal{L}_{\mathrm{UV}}$
$m_{\Psi} \sim m_S \ \mu$	SM $\mathcal{L}_{ ext{SCET}_{ ext{BSM}}}$ n	$\mathcal{L}_{\mathrm{UV}}$ $\mathcal{L}_{\mathrm{UV}}$ m	$l_{\Psi} = \mu$



Operators responsible for he most relevant decays of the S: At $\mathcal{O}(\lambda^2)$: - See

$$O_{AA} = S g_{\mu\nu}^{\perp} \mathcal{A}_c^{\mu,a} \mathcal{A}_{\bar{c}}^{\nu,a} \qquad S \to \gamma\gamma$$
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$$O_{\phi\phi}(\mu) = S \left(\Phi_{n_1}^{\dagger} \Phi_{n_2} + \Phi_{n_2}^{\dagger} \Phi_{n_1} \right) \qquad \begin{array}{c} S \to \mathsf{hh} \\ S \to W_L W_L \\ S \to Z_L Z_L \end{array}$$



Details and full list of operators:



$$\sim \mathcal{M}_{\rm LO} \left\{ 1 + \frac{\alpha_s(\mu) C_F}{\pi} \ln^2 \frac{\mu^2}{m_q^2} \right\}$$



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Important effects when predicting **decay rates** or putting **constraints** on models!



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Resummation is important, rates always decreased!





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Thank you for your attention!

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Bonus slides

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A matching example



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[Alte, MK, Neubert (2019), [arXiv:1902.04593]]





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 $\begin{array}{l} \mbox{Compare with EFT amplitude} \rightarrow \ C_{Q_L \bar{d}_R \phi}(u,\mu) = \frac{V_Q^\dagger G}{u\,\xi-1}. \end{array}$ (all given in the paper)



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 $\label{eq:compare} \text{Compare with EFT amplitude} \ \rightarrow \ C_{Q_L \bar{d}_R \phi}(u,\mu) = \frac{V_Q^\dagger G}{u\,\xi-1}.$

Also, in the limit of $m_{\Psi} \gg m_S$: $C_{Q_L \bar{d}_R \phi}(u, \mu) = -V_Q^{\dagger} G$, which depends neither on m_S nor on $u \rightarrow$ local!









$$\cdots \checkmark A \longrightarrow C_{GG}(m_S) = \frac{T_F}{\pi^2} \left[\left(\frac{4m_{\Psi}^2}{m_S^2} - 1 \right) \arcsin^2 \left(\frac{m_S}{2m_{\Psi}} \right) - 1 \right]$$

Wilson coefficient depends again on the momentum transfer $(Q^2 = m_S^2)$.



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Take-away message:

Matching no work of magic! Just compute amplitudes, expand around $\lambda=m_{\rm SM}/m_S$ small, equate with the EFT amplitudes, use the RG to resum the large logs!



No. 28-"Three Log" Load of Sugar Pine at the Mill Pond.