



Theories of Flavour

From the Planck Scale to the Electroweak Scale

I will certainly be around for lunch, so I look forward to seeing you then.

Steve King

NExT Meeting, Southampton,

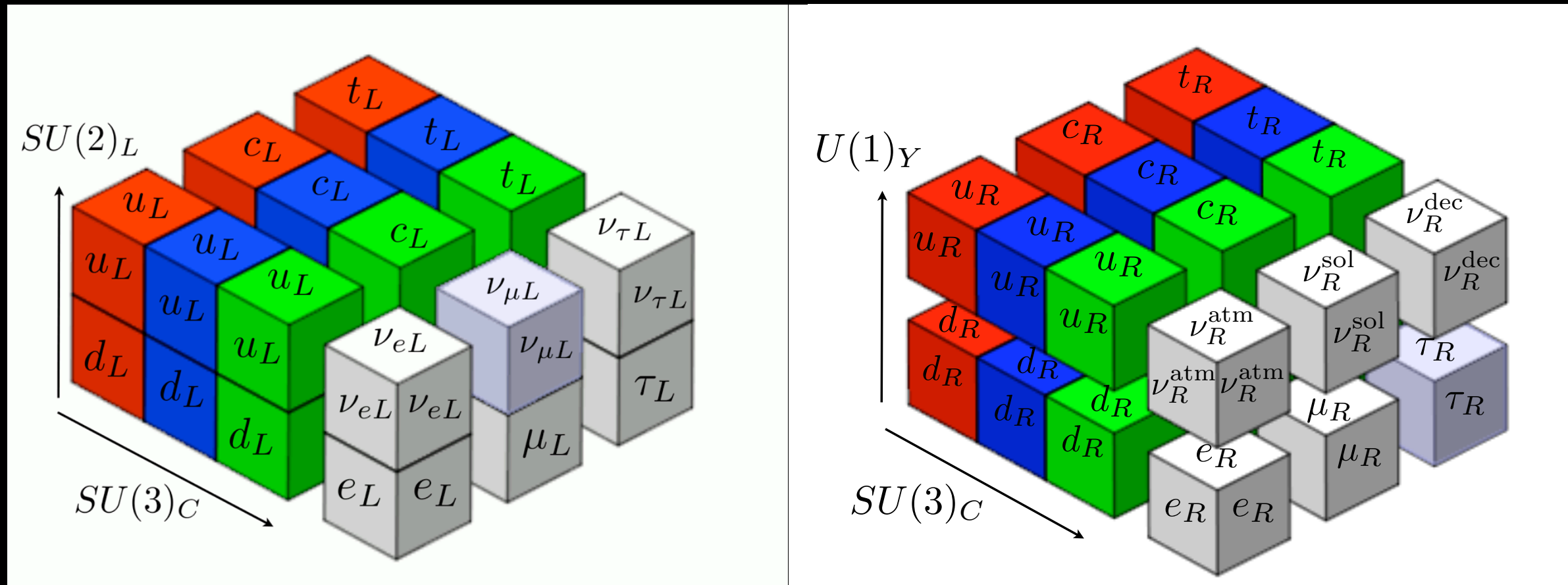
7th November, 2018

Prelude

The Flavour Problem

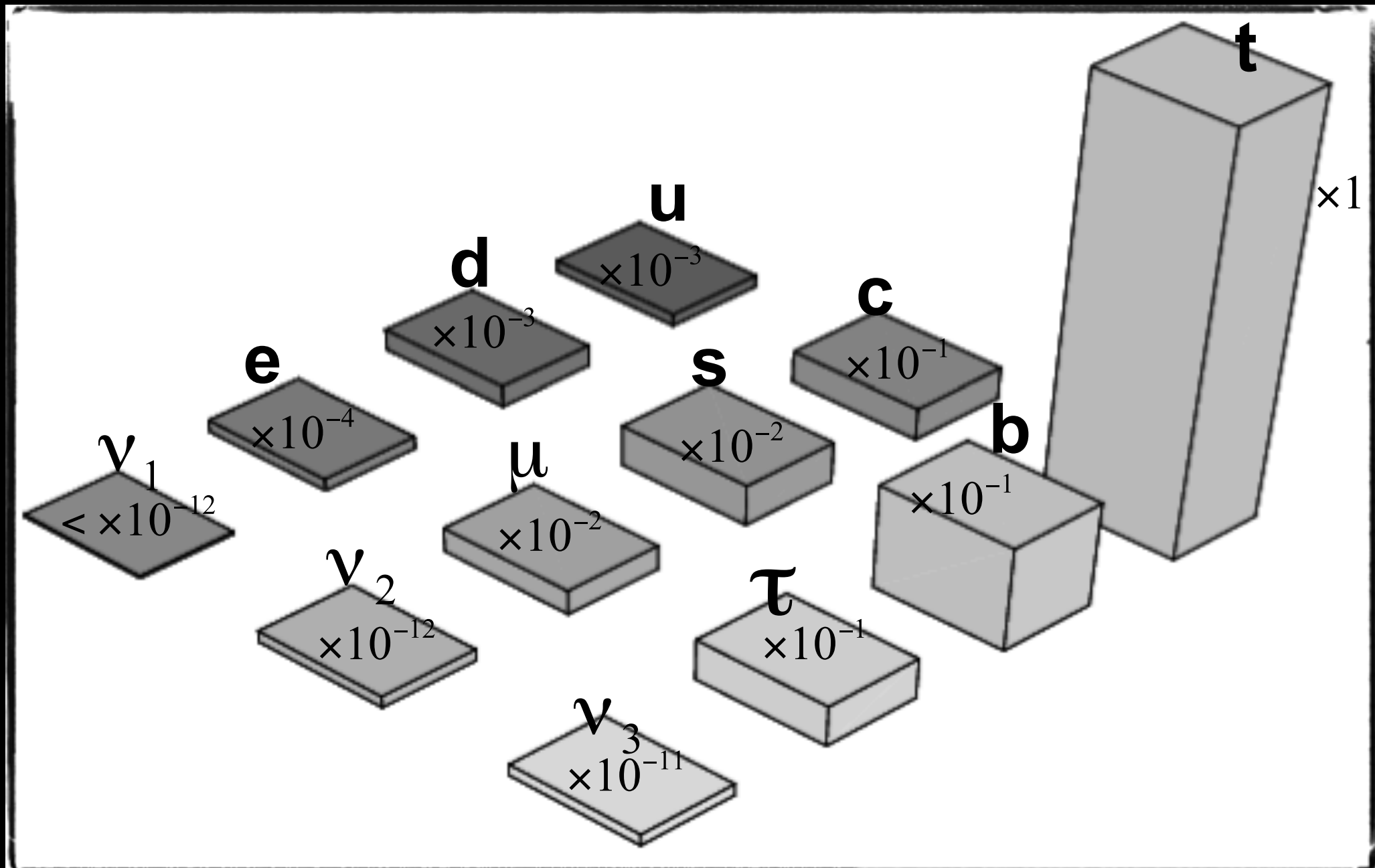
Theories of Flavour with effective Yukawa couplings

The Standard Model

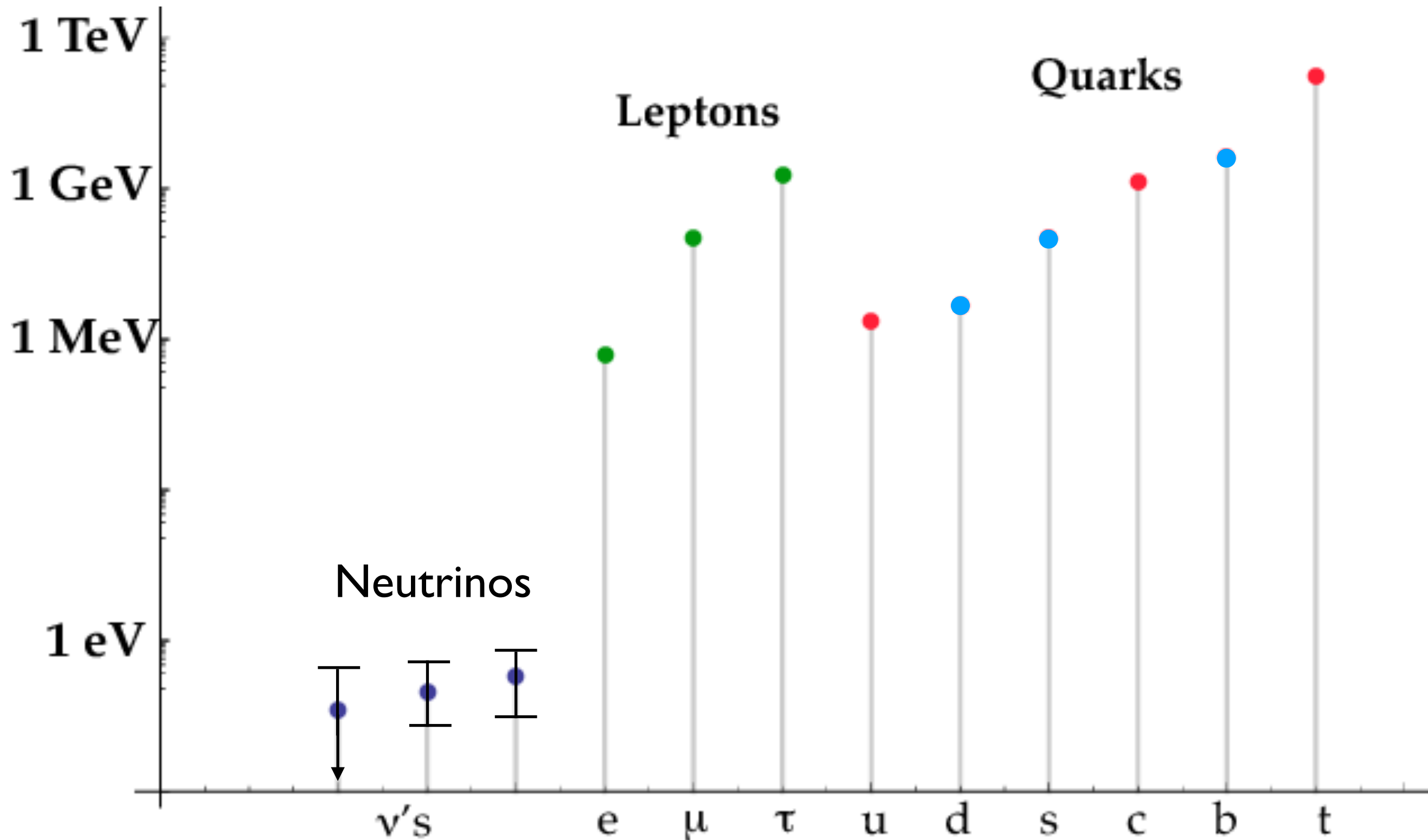


has flavour problem...

The Flavour Problem

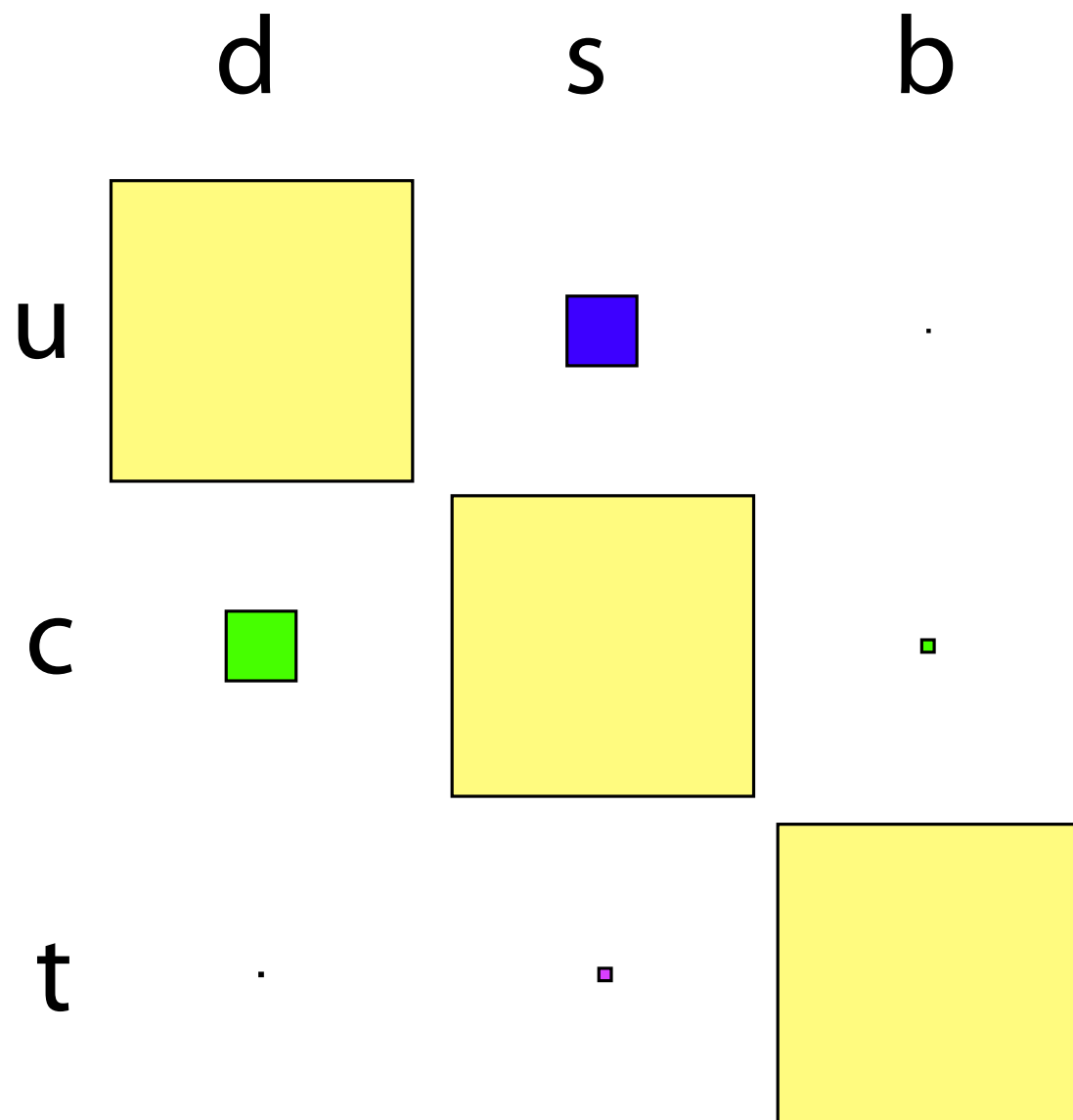


Masses

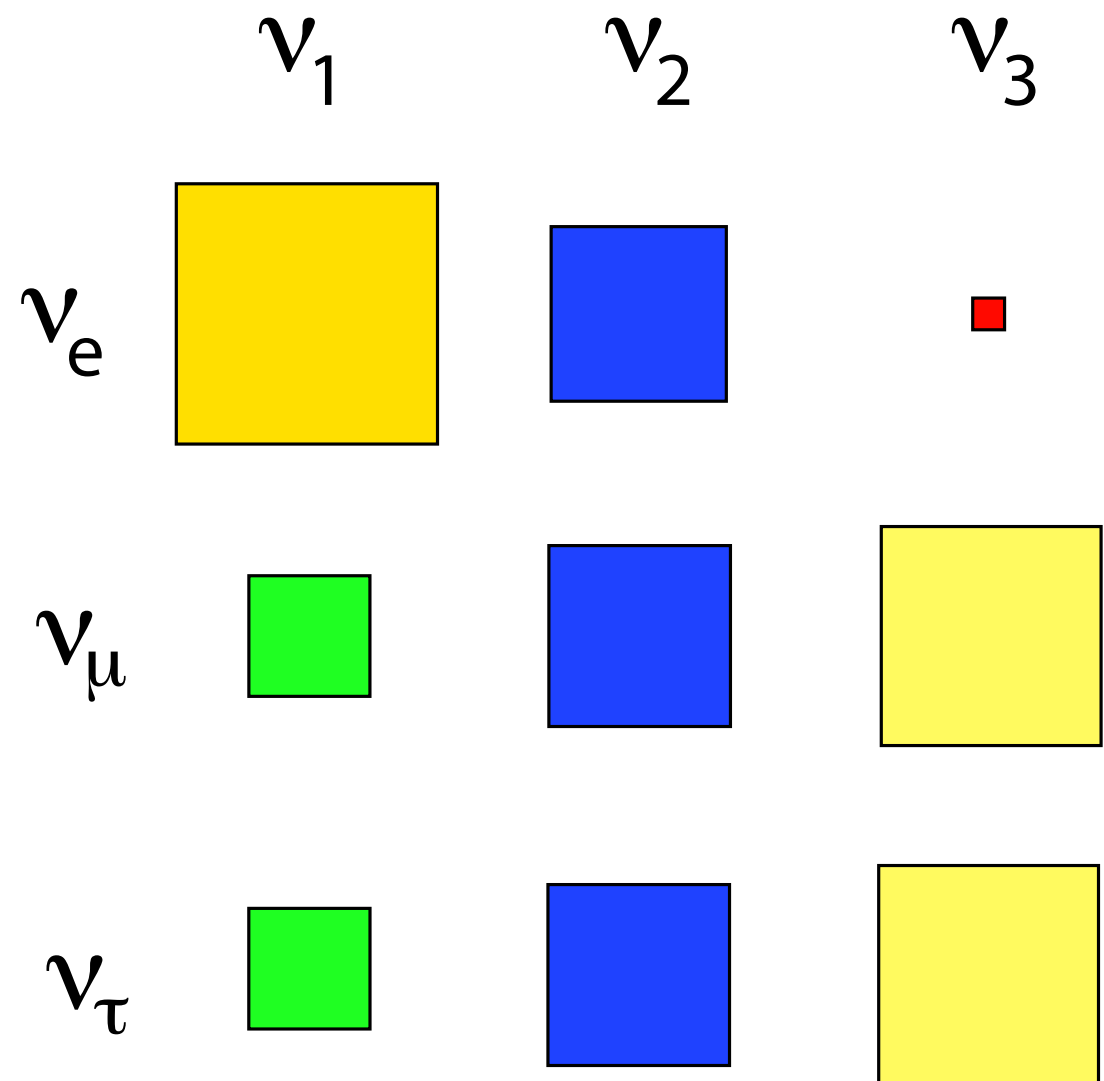


Mixing

CKM



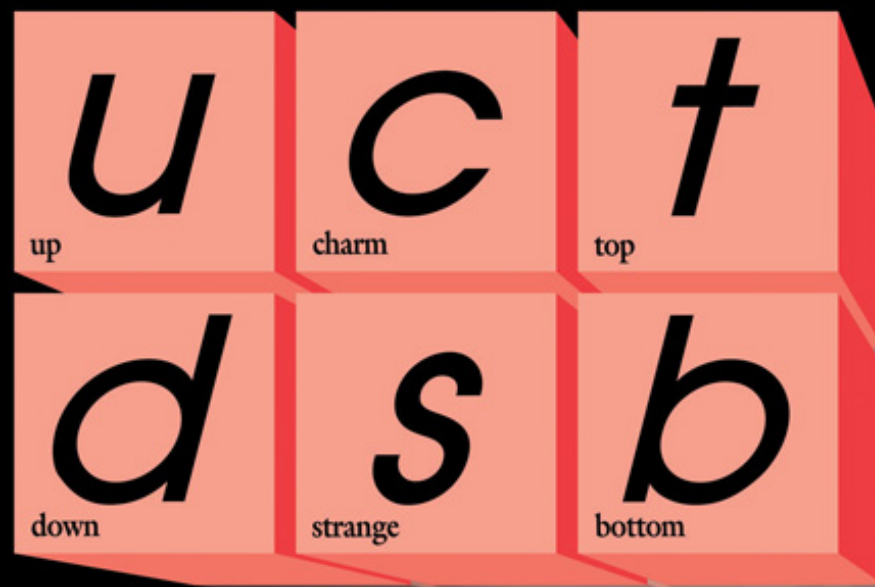
PMNS



Angles and CP

	θ_{12}	θ_{23}	θ_{13}	δ
Quarks	13° $\pm 0.1^\circ$	2.4° $\pm 0.1^\circ$	0.2° $\pm 0.05^\circ$	70° $\pm 5^\circ$
Leptons	34° $\pm 1^\circ$	45° $\pm 5^\circ$	8.5° $\pm 0.15^\circ$	-130° $\pm 40^\circ$

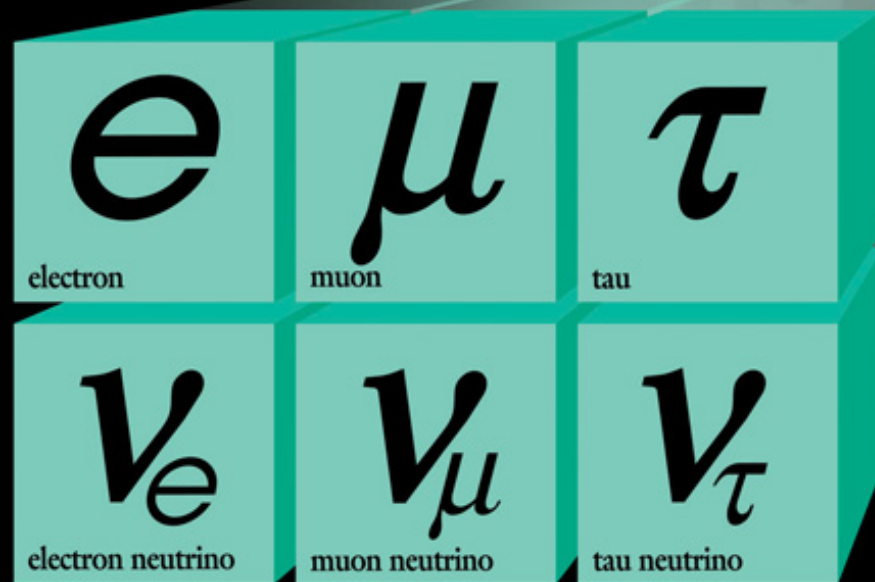
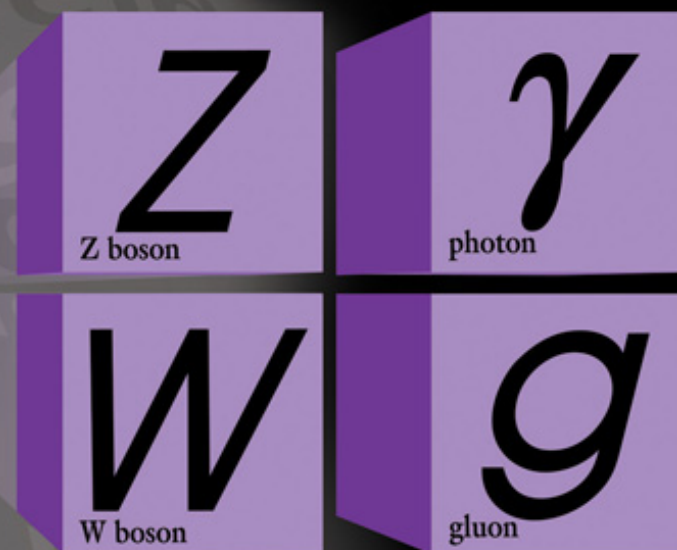
Quarks



Higgs



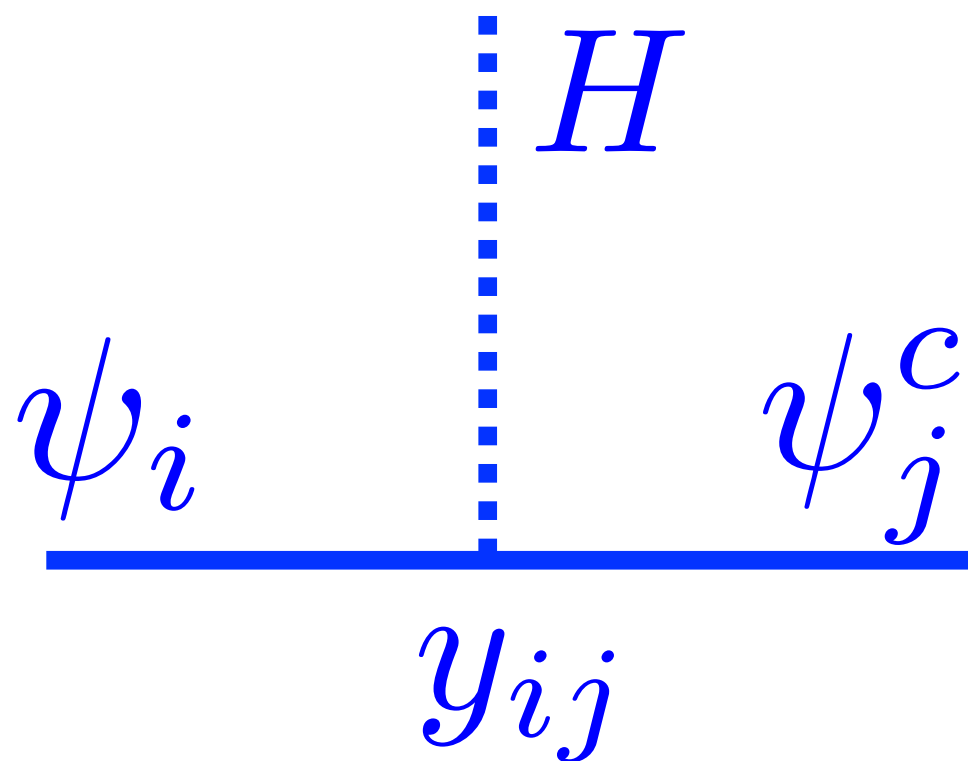
Forces



Leptons

Yukawa couplings

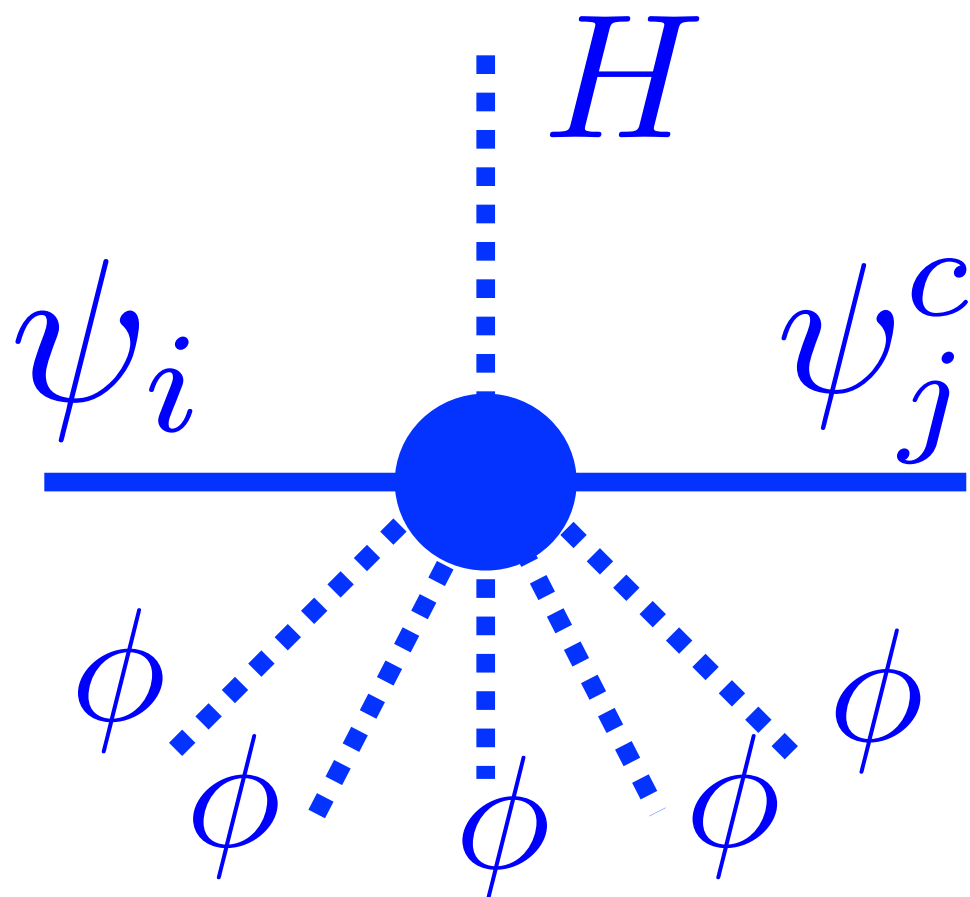
$$y_{ij} H \psi_i \psi_j^c$$



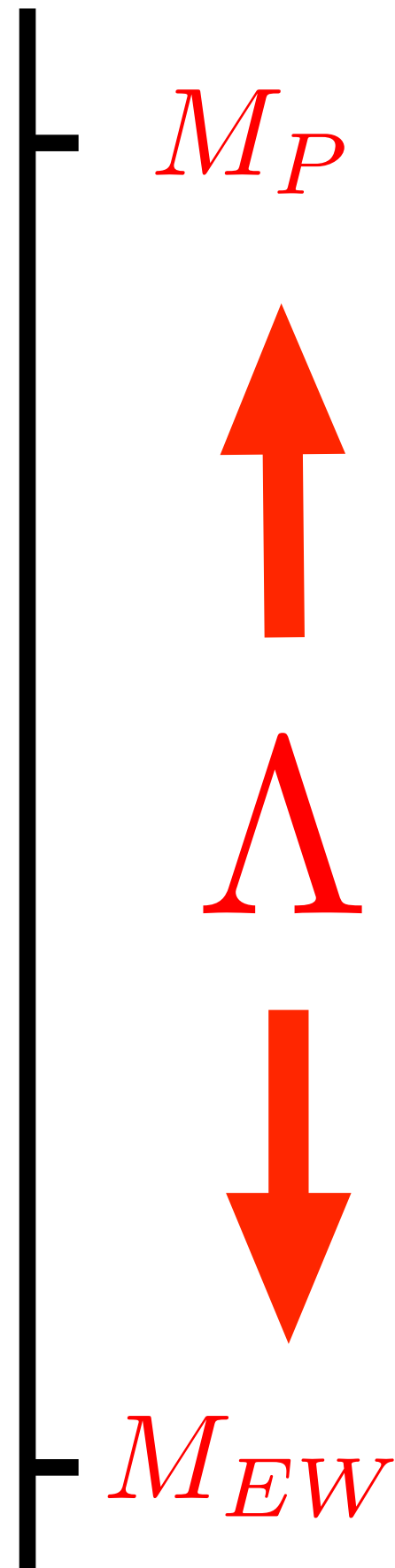
Why so small
(apart from
top quark)?

Effective Yukawa couplings

$$\left(\frac{\langle \phi_i \rangle}{\Lambda_{i,n}^\psi} \right)^n \left(\frac{\langle \phi_j \rangle}{\Lambda_{j,m}^{\psi^c}} \right)^m H \psi_i \psi_j^c$$



Yukawas small
due to
powers
of ratios $\frac{\langle \phi \rangle}{\Lambda}$

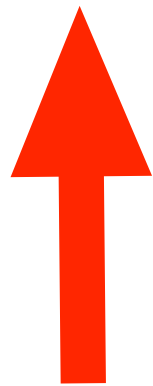


Flavour scales can be from the Planck scale to electroweak scale

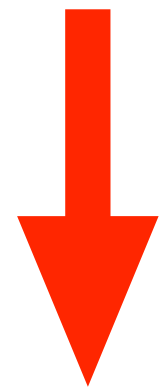
Keeping fixed ratios

$$\frac{\langle \phi \rangle}{\Lambda}$$

M_P



Λ



M_{EW}

SUSY GUTs

suggest high scale
theory of flavour

Phenomenological
hints from B physics

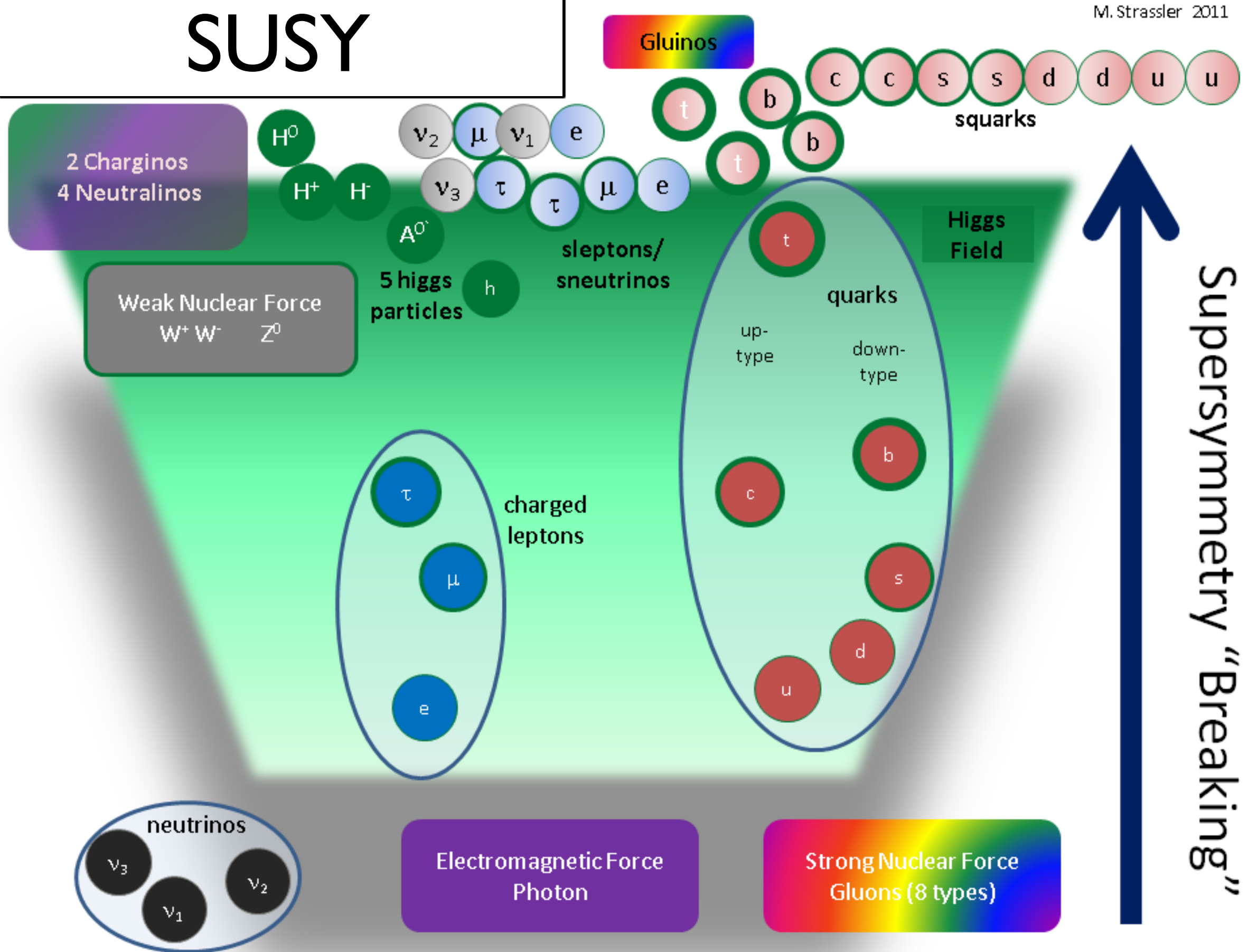
suggest low scale
theory of flavour

Part I

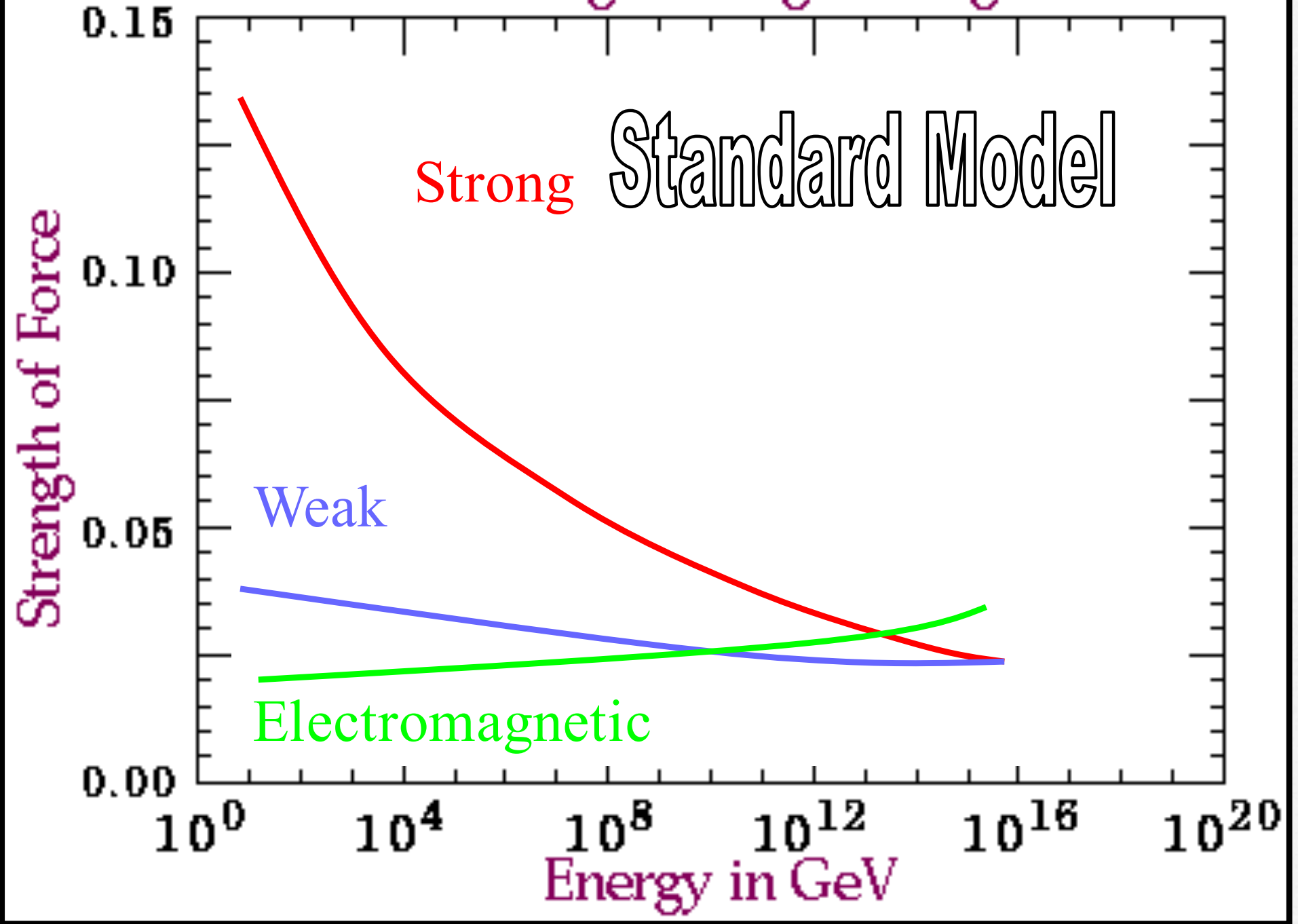
SUSY GUTs of Flavour

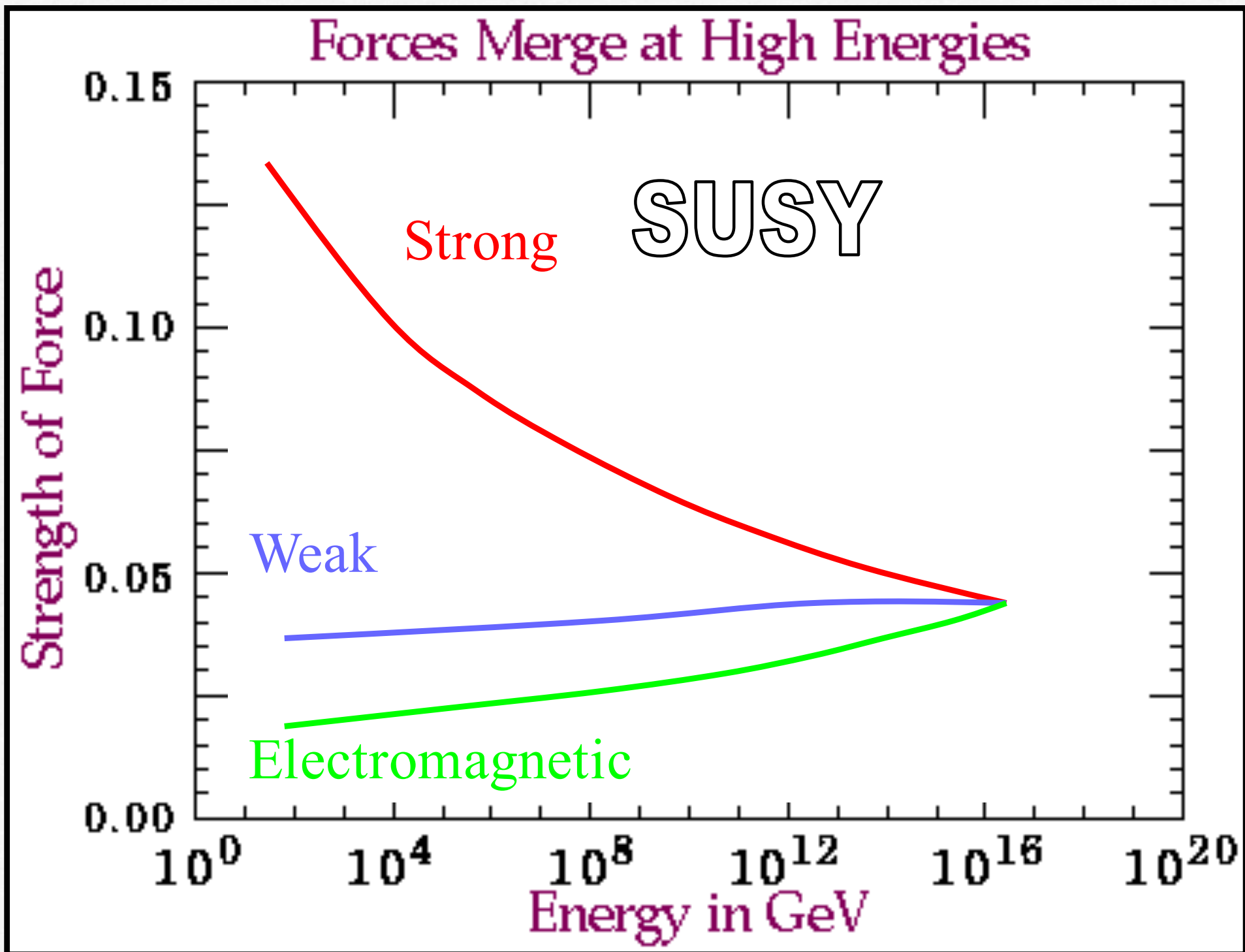
High scale theories of flavour

SUSY

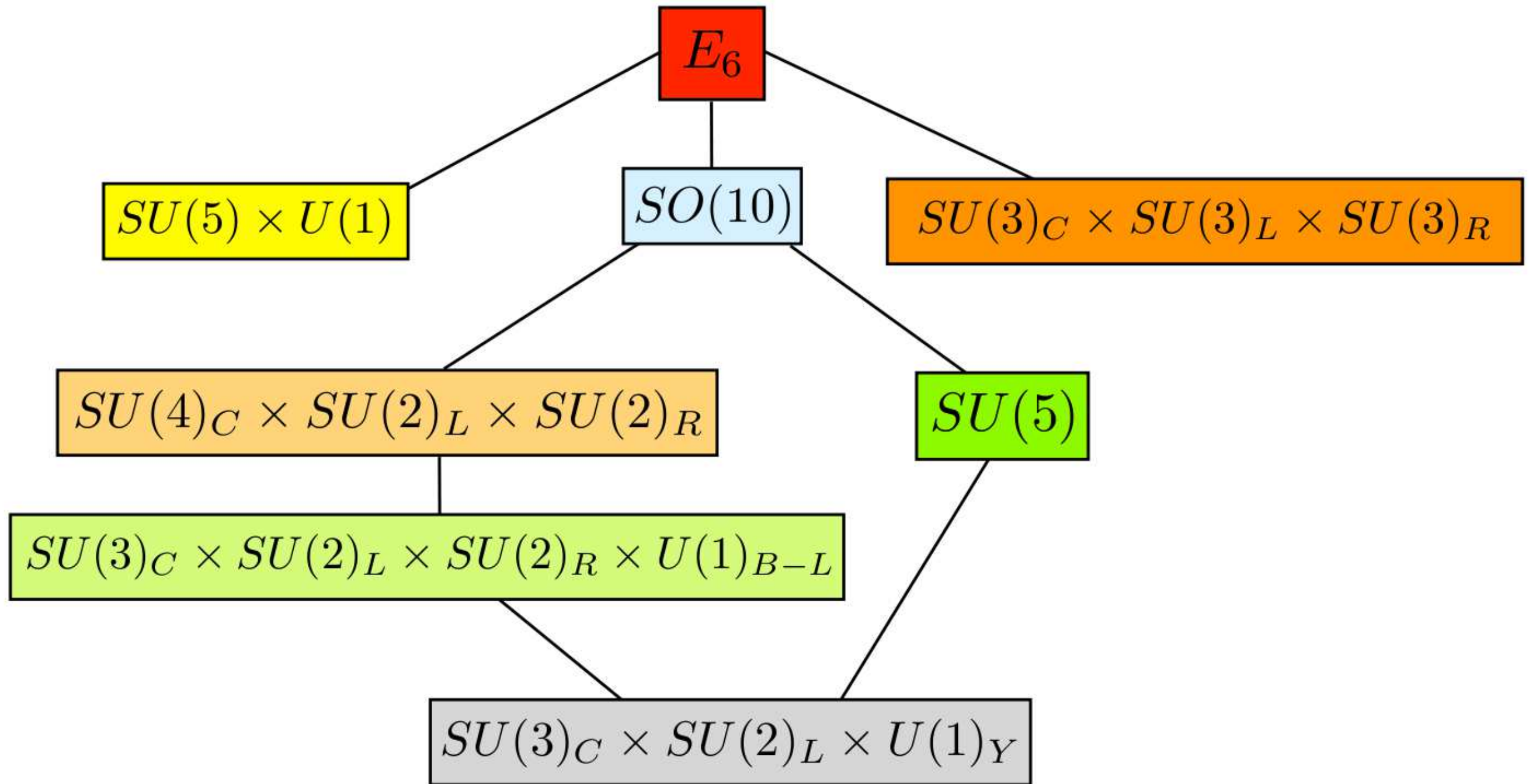


Forces Merge at High Energies





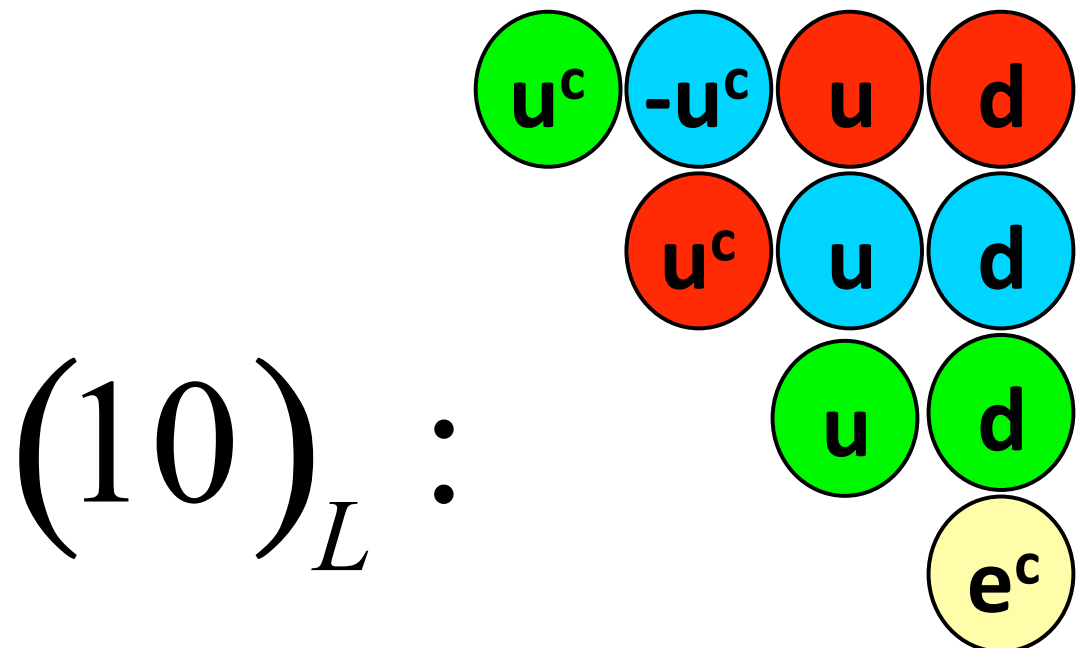
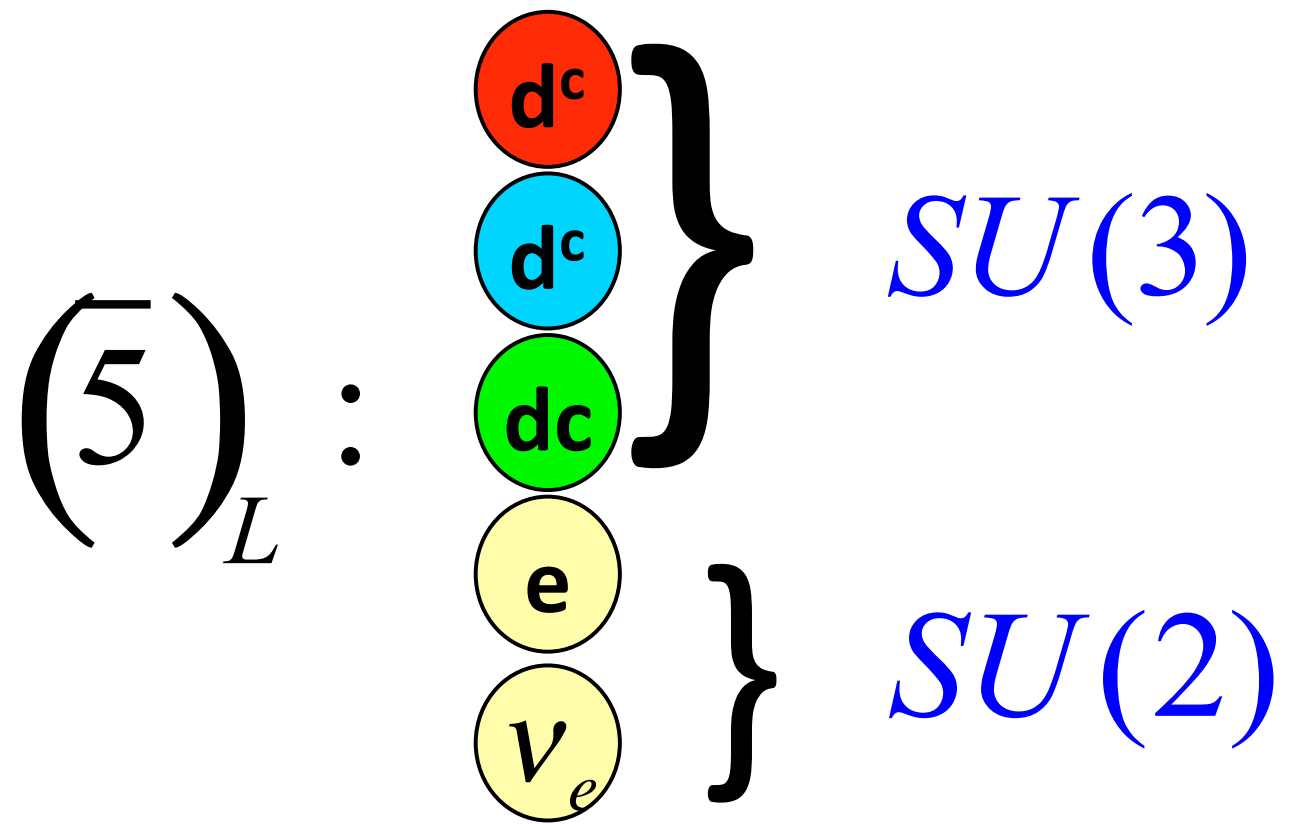
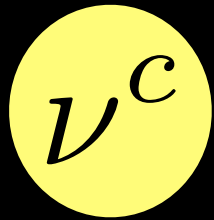
GUTs



SU(5) GUT

Georgi, Glashow 1974

Right-handed
neutrino is
optional singlet



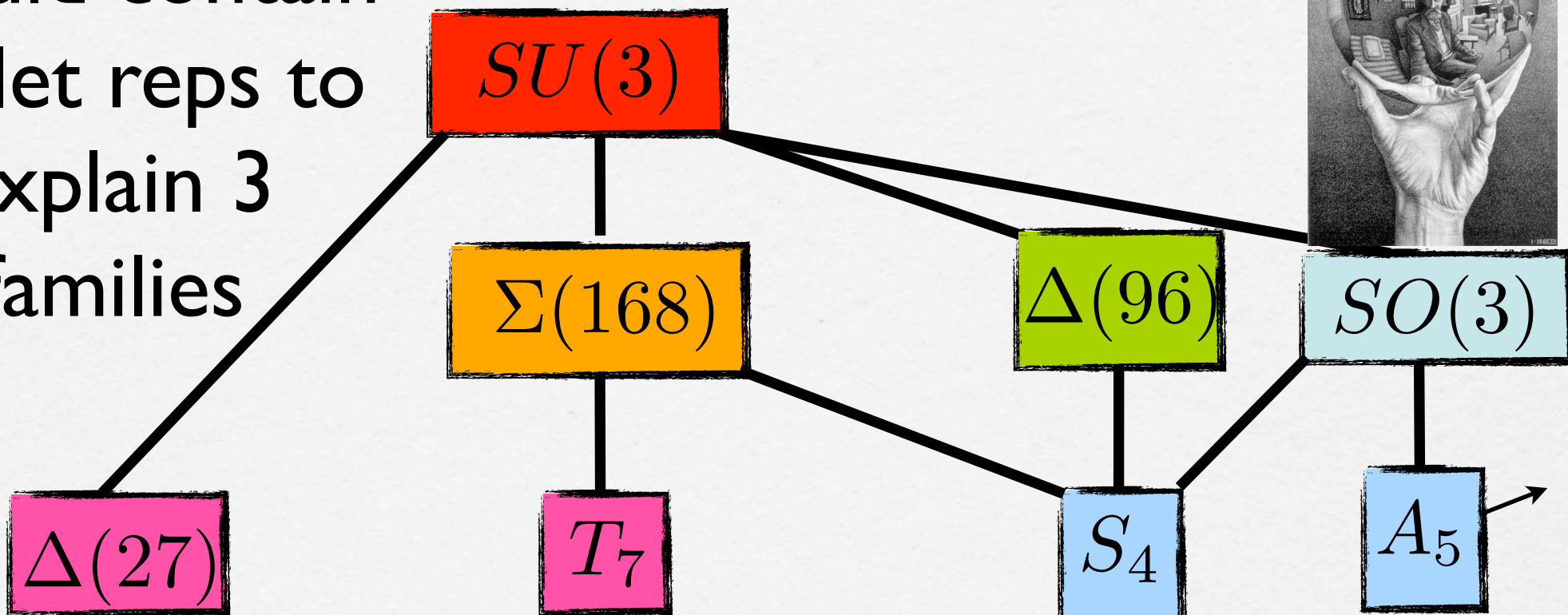
For references see review SFK 1701.04413

GUTs with flavour symmetry

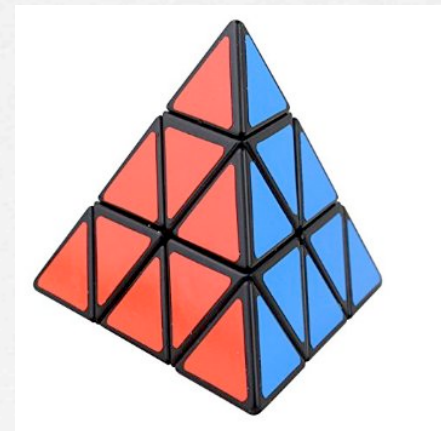
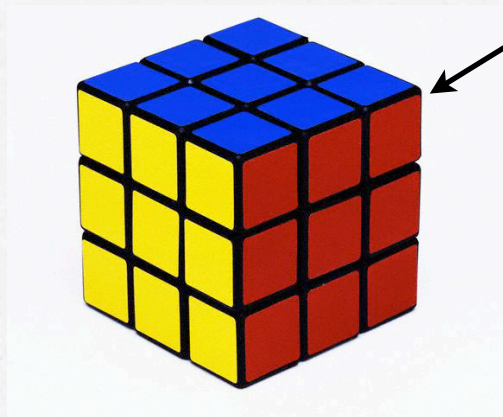
G_{FAM}	G_{GUT}	$SU(2)_L \times U(1)_Y$	$SU(5)$	PS	$SO(10)$
S_3		[29]			[142]
A_4		[30, 34, 51, 53, 64, 143–145]	[146–149]	[68, 150, 151]	
T'		[152]	[153]		
S_4		[31, 51, 53, 145, 155]	[156, 157]	[154]	[158]
A_5		[53, 159]	[160]		
T_7		[161, 162]			
$\Delta(27)$		[163]			[164]
$\Delta(96)$		[165, 166]	[167]		[168]
D_N		[169]			
Q_N		[170]			
other		[171]	[172]	[173]	

Flavour Symmetry

Should contain triplet reps to explain 3 families

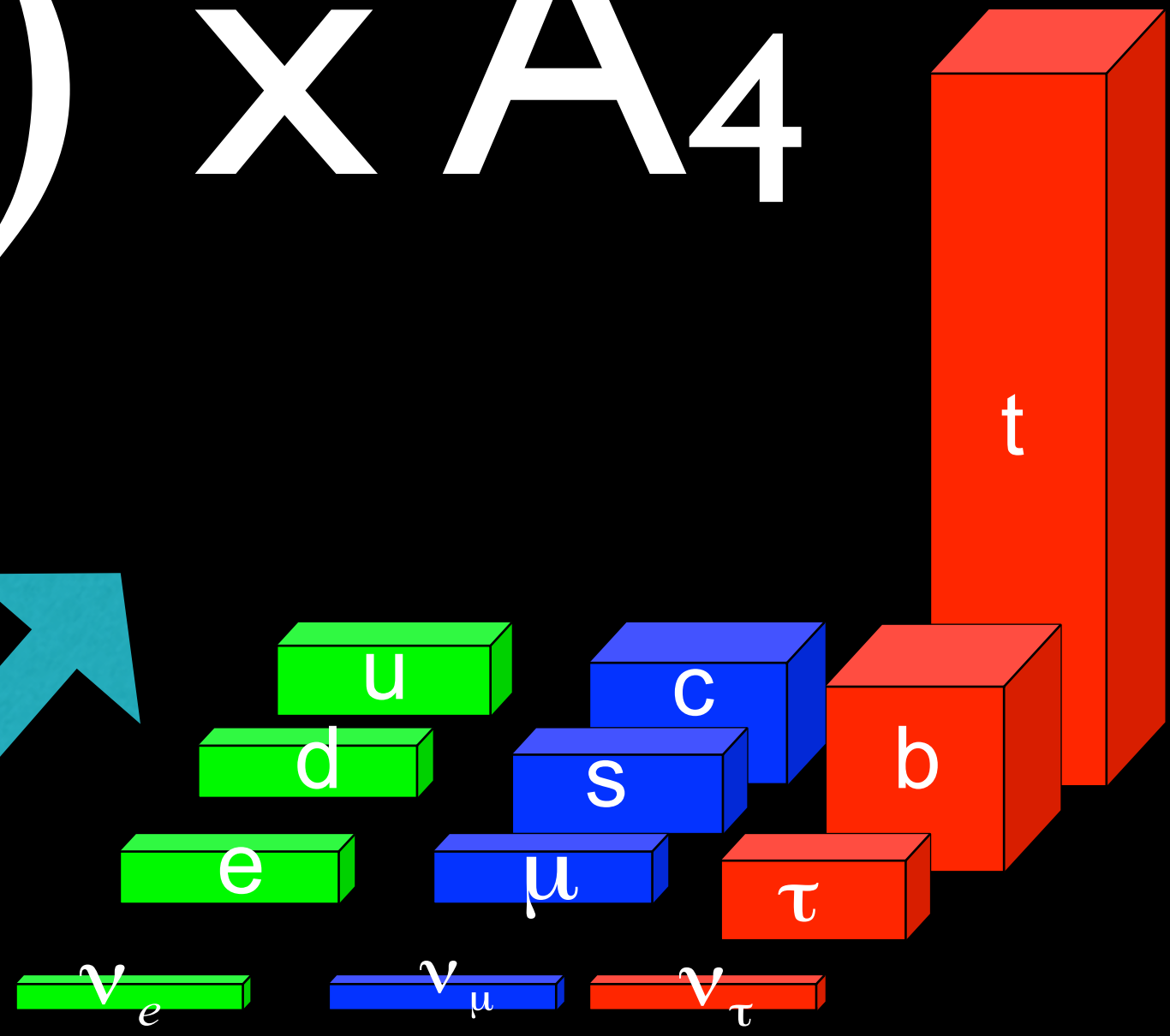


Can arise from extra dimensions



SU(5) × A₄

SU(5)



$F \sim (3, 5^*)$

$T_i \sim (1, 10)$

A₄

SU(5)xA₄ predicts Yukawa matrices

Solves the strong CP problem:

$$\arg \det (Y^u Y^d) = 0$$

$$Y^u = \begin{pmatrix} u_{11} |\tilde{\xi}^4| & u_{12} |\tilde{\xi}^3| & u_{13} |\tilde{\xi}^2| \\ u_{12} |\tilde{\xi}^3| & u_{22} |\tilde{\xi}^2| & u_{23} |\tilde{\xi}| \\ u_{13} |\tilde{\xi}^2| & u_{23} |\tilde{\xi}| & u_{33} \end{pmatrix}$$

$$Y^d = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{1}{4} d_{11} \frac{|v_\xi v_e|}{|v_{\Lambda_{24}}|^2} & d_{12} \frac{|v_\xi v_\mu|}{|v_{\Lambda_{24}} v_{H_{24}}|} e^{i\zeta} & 0 \\ 0 & 2d_{22} \frac{|v_{H_{24}} v_\mu|}{M^2} & 0 \\ 0 & 0 & d_{33} \frac{|v_\tau|}{M} \end{pmatrix}$$

Up matrix has small mixing and no phases

Down matrix gives Cabibbo mixing and CP phase

$$m_D = \begin{pmatrix} 0 & b \\ a & 3b \\ a & b \end{pmatrix} \quad M_R = \begin{pmatrix} M_{\text{atm}} & 0 \\ 0 & M_{\text{sol}} \end{pmatrix}$$

$$Y^e = \frac{1}{\sqrt{2}} \begin{pmatrix} \frac{1}{9} d_{11} \frac{|v_\xi v_e|}{|v_{\Lambda_{24}}|^2} & 0 & 0 \\ d_{12} \frac{|v_\xi v_\mu|}{|v_{\Lambda_{24}} v_{H_{24}}|} e^{i\zeta} & 9d_{22} \frac{|v_{H_{24}} v_\mu|}{M^2} & 0 \\ 0 & 0 & d_{33} \frac{|v_\tau|}{M} \end{pmatrix}$$

Littlest Seesaw with 4 parameters

No LH charged lepton mixing to leading order

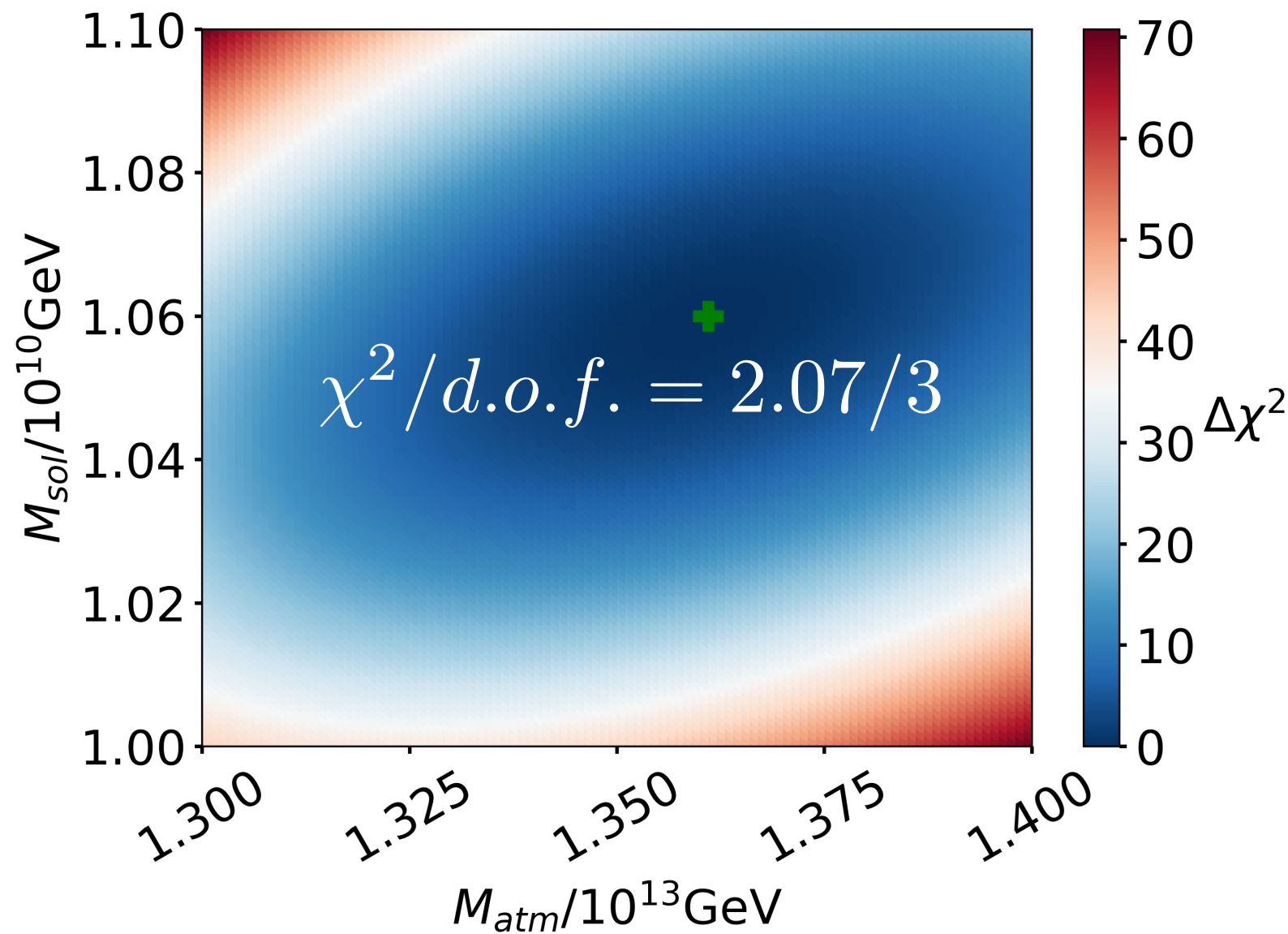
The Fitting high-energy Littlest Seesaw parameters using low-energy neutrino data and leptogenesis

4 real input parameters

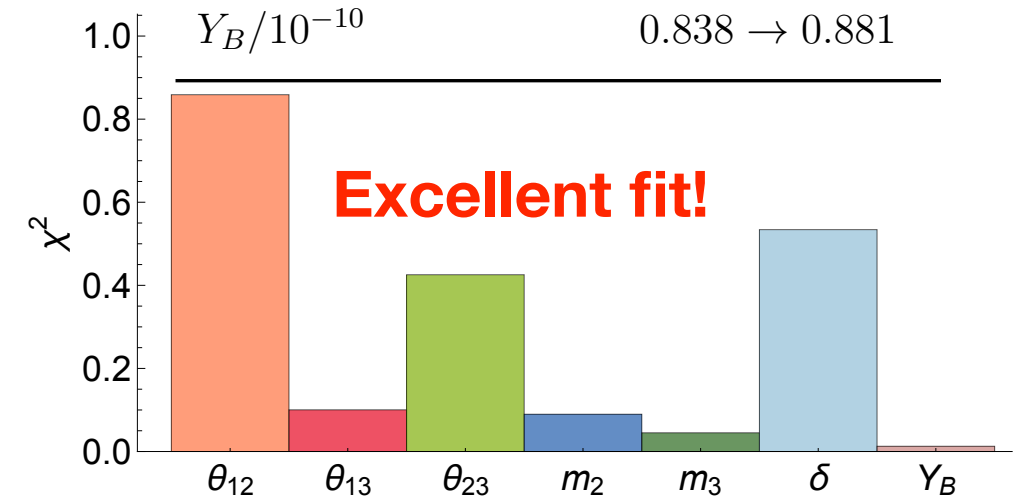
$$m_D = \begin{pmatrix} 0 & b \\ a & 3b \\ a & b \end{pmatrix} \quad M_R = \begin{pmatrix} M_{\text{atm}} & 0 \\ 0 & M_{\text{sol}} \end{pmatrix}$$

Predicts:

3 neutrino masses ($m_1=0$),
3 mixing angles,
1 Dirac CP phase,
2 Majorana phases (1 zero)
1 BAU parameter Y_B
= 10 observables
of which 7 are constrained



Predicted	1σ range
$\theta_{12}/^\circ$	34.291 \rightarrow 34.379
$\theta_{13}/^\circ$	8.384 \rightarrow 8.784
$\theta_{23}/^\circ$	44.044 \rightarrow 44.434
$\Delta m_{12}^2/10^{-5}\text{eV}^2$	7.058 \rightarrow 7.615
$\Delta m_{31}^2/10^{-3}\text{eV}^2$	2.435 \rightarrow 2.562
$\delta/^\circ$	-93.708 \rightarrow -92.180
$Y_B/10^{-10}$	0.838 \rightarrow 0.881



SUSY SU(5) \times A₄ @LHC

SUSY breaking masses at M_{GUT}

$$m_F = m_{\tilde{D}_i^c} = m_{\tilde{L}_i} = m_{H_u} = m_{H_d},$$

$$m_{T1} = m_{\tilde{Q}_1} = m_{\tilde{U}_1^c} = m_{\tilde{E}_1^c},$$

$$m_{T2} = m_{\tilde{Q}_2} = m_{\tilde{U}_2^c} = m_{\tilde{E}_2^c},$$

$$m_{T3} = m_{\tilde{Q}_3} = m_{\tilde{U}_3^c} = m_{\tilde{E}_3^c}.$$

Light charginos, neutralinos and RH smuons

	Parameter/Observable	Scenario 1	Scenario 2		Parameter/Observable	Scenario 1	Scenario 2
MFV Parameters at GUT scale	m_F	5000	5000	Physical masses	m_h	126.7	127.3
	m_{T1}	5000	5000		$m_{\tilde{g}}$	5570.5	5625.7
	m_{T2}	200	233.2		$m_{\tilde{\mu}_L}$	4996.7	4997.5
	m_{T3}	2995	2995		$m_{\tilde{\mu}_R}$	102.1	254.4
	a_{33}^{TT}	-940	-940		$m_{\tilde{\chi}_1^0}$	94.6	250.4
	a_{33}^{FT}	-1966	-1966		$m_{\tilde{\chi}_2^0}$	323.6	322.0
	M_1	250.0	600.0		$m_{\tilde{\chi}_3^0}$	2248.8	2331.1
	M_2	415.2	415.2		$m_{\tilde{\chi}_4^0}$	2248.8	2331.2
	M_3	2551.6	2551.6		$m_{\tilde{\chi}_1^\pm}$	323.8	322.2
	M_{H_u}	4242.6	4242.6		$m_{\tilde{\chi}_2^\pm}$	2249.8	2332.2
	M_{H_d}	4242.6	4242.6	$\Omega_{\tilde{\chi}_1^0} h^2$	0.116	0.120	
	$\tan \beta$	30	30	$\sigma_{SI}^{Proton} / 10^{-14} pb$	2.987	1.055	
	μ	-2163.1	-2246.8	$\sigma_{SI}^{Neutron} / 10^{-14} pb$	3.249	0.986	

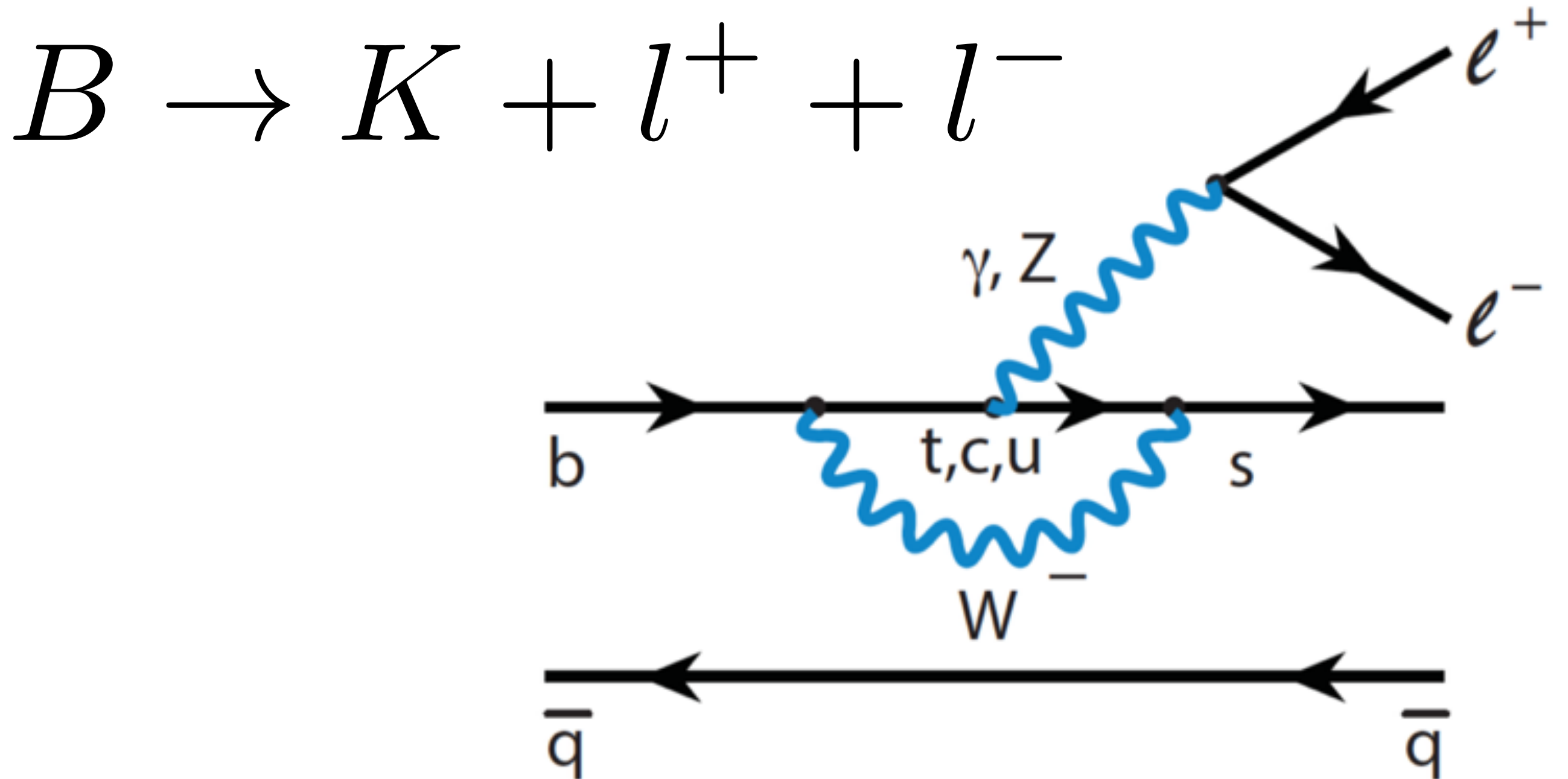
Flavour Violating Parameters at M_{GUT}

Parameters	Scenario 1	Scenario 2	Most constraining obs. 1	Most constraining obs. 2
$(\delta^T)_{12}$	$[-0.015, 0.015]$	$[-0.12, 0.12]^\dagger$	$\mu \rightarrow 3e, \mu \rightarrow e\gamma, \Omega_{\tilde{\chi}_1^0} h^2$	$\Omega_{\tilde{\chi}_1^0} h^2, \mu \rightarrow e\gamma$
$(\delta^T)_{13}$	$] -0.06, 0.06[$	$[-0.3, 0.3]^\dagger$	$\Omega_{\tilde{\chi}_1^0} h^2$	$\Omega_{\tilde{\chi}_1^0} h^2$
$(\delta^T)_{23}$	$[0, 0]^*$	$[-0.1, 0.1]^\dagger$	$\Omega_{\tilde{\chi}_1^0} h^2, \mu \rightarrow 3e, \mu \rightarrow e\gamma$	$\Omega_{\tilde{\chi}_1^0} h^2, \mu \rightarrow 3e, \mu \rightarrow e\gamma,$
$(\delta^F)_{12}$	$[-0.008, 0.008]$	$[-0.015, 0.015]^\dagger$	$\mu \rightarrow 3e, \mu \rightarrow e\gamma$	$\mu \rightarrow 3e, \mu \rightarrow e\gamma$
$(\delta^F)_{13}$	$] -0.01, 0.01[$	$[-0.15, 0.15]^\dagger$	$\mu \rightarrow e\gamma$	$\mu \rightarrow 3e, \mu \rightarrow e\gamma$
$(\delta^F)_{23}$	$] -0.015, 0.015[$	$[-0.15, 0.15]^\dagger$	$\mu \rightarrow e\gamma, \Omega_{\tilde{\chi}_1^0} h^2$	$\Omega_{\tilde{\chi}_1^0} h^2, \mu \rightarrow e\gamma, \mu \rightarrow 3e$
$(\delta^{TT})_{12}$	$[-3, 3.5] \times 10^{-5}$	$[-1, 1.5]^\dagger \times 10^{-3}$	prior	prior, $\Omega_{\tilde{\chi}_1^0} h^2$
$(\delta^{TT})_{13}$	$] -6, 7] \times 10^{-5}$	$[-4, 2.5]^\dagger \times 10^{-3}$	prior, $\Omega_{\tilde{\chi}_1^0} h^2$	prior, $\Omega_{\tilde{\chi}_1^0} h^2$
$(\delta^{TT})_{23}$	$] -0.5, 4[\times 10^{-5}$	$[-0.25, 0.2]^\dagger$	prior, $\Omega_{\tilde{\chi}_1^0} h^2$	prior, $\Omega_{\tilde{\chi}_1^0} h^2$
$(\delta^{FT})_{12}$	$[-0.0015, 0.0015]$	$[-1.2, 1.2]^\dagger \times 10^{-4}$	$\Omega_{\tilde{\chi}_1^0} h^2$	$\mu \rightarrow 3e, \Omega_{\tilde{\chi}_1^0} h^2, \mu \rightarrow e\gamma$
$(\delta^{FT})_{13}$	$] -0.002, 0.002[$	$[-5, 5] \times 10^{-4}$	$\Omega_{\tilde{\chi}_1^0} h^2$	$\Omega_{\tilde{\chi}_1^0} h^2, \mu \rightarrow 3e, \mu \rightarrow e\gamma$
$(\delta^{FT})_{21}$	$[0, 0]^*$	$[-1.2, 1.2]^\dagger \times 10^{-4}$	prior	$\Omega_{\tilde{\chi}_1^0} h^2, \text{prior}$
$(\delta^{FT})_{23}$	$] -0.0022, 0.0022[$	$[-6, 6]^\dagger \times 10^{-4}$	$\Omega_{\tilde{\chi}_1^0} h^2$	$\mu \rightarrow 3e, \Omega_{\tilde{\chi}_1^0} h^2, \mu \rightarrow e\gamma$
$(\delta^{FT})_{31}$	$] -0.0004, 0.0004[$	$[-2, 2]^\dagger \times 10^{-4}$	$\Omega_{\tilde{\chi}_1^0} h^2$	$\Omega_{\tilde{\chi}_1^0} h^2$
$(\delta^{FT})_{32}$	$[0, 0]^*$	$[-1.5, 1.5] \times 10^{-4}$	prior	$\Omega_{\tilde{\chi}_1^0} h^2$

Part II

Phenomenological hints from B physics

Low scale theories of flavour



- $b \rightarrow s l^+ l^-$ transitions are rare in the SM (no tree level contributions: GIM, CKM, in some cases helicity suppressed)
- ideally suited for indirect New Physics searches (indirectly sensitive to energy scales $O(100\text{TeV})$)

LFU tests with $B \rightarrow K(^*)\mu\mu$ and $B \rightarrow K(^*)ee$ decays: $R(K)$ and $R(K^*)$

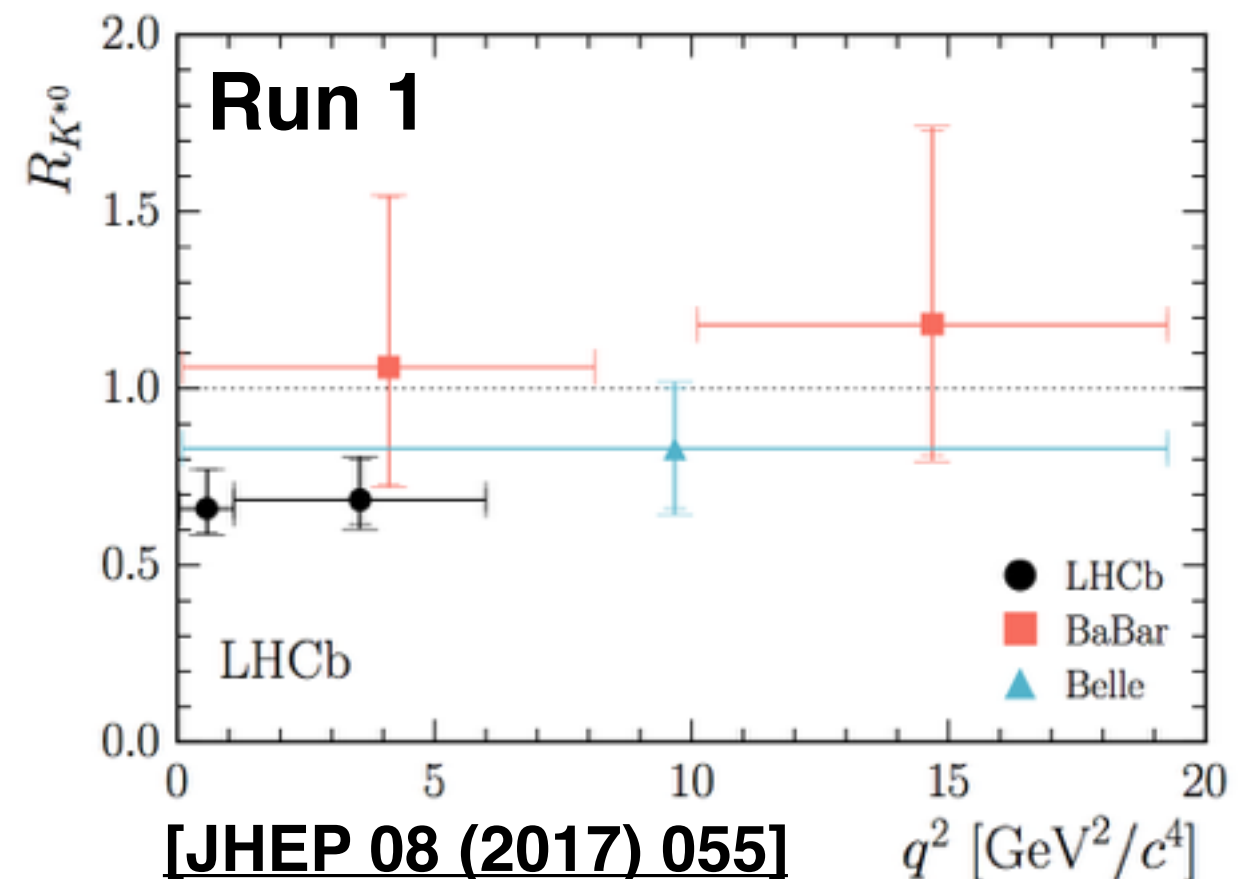
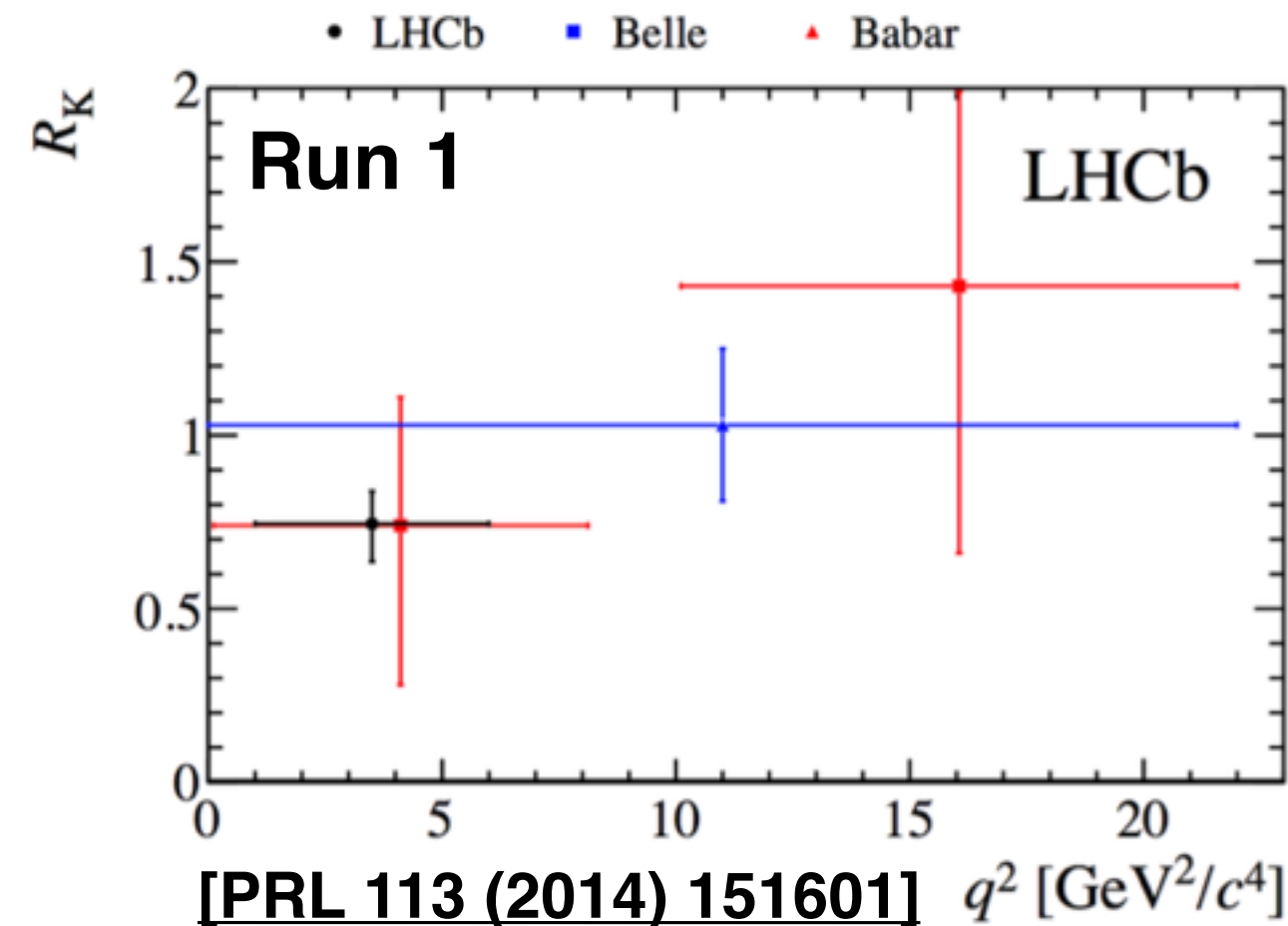
- Theoretical uncertainties on the exclusive $B \rightarrow K(^*)ll$ branching fractions are reduced to a per-mille level in ratios (*hadronic effects cancel*):

$$R(K) = \frac{B^+ \rightarrow K^+ \mu^+ \mu^-}{B^+ \rightarrow K^+ e^+ e^-} \quad R(K^*) = \frac{B^0 \rightarrow K^{*0} \mu^+ \mu^-}{B^0 \rightarrow K^{*0} e^+ e^-}$$

- SM, $R(K)$ and $R(K^*)$ expected to be close to unity.
- Sensitive to new neutral and heavy gauge bosons, lepto-quarks, Z' models.

R(K) and R(K*) results

LHCb focusses on the q^2 regions with reliable theoretical predictions and small contributions from the resonant modes. Precision limited by statistics.



$$R_K = 0.745^{+0.090}_{-0.074}(\text{stat}) \pm 0.036(\text{syst}).$$

2.6 σ Deviation from Standard Model

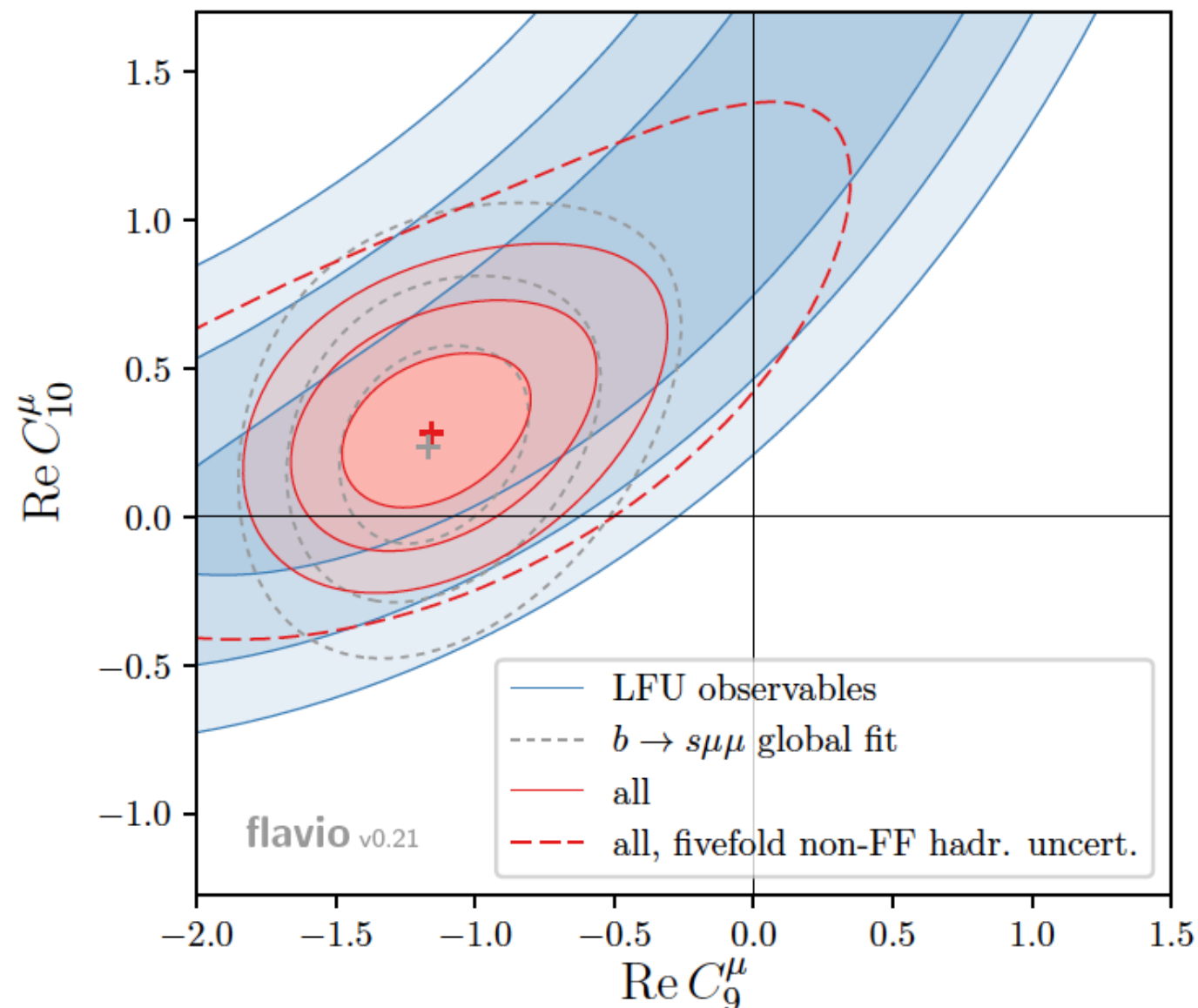
$$R_{K^{*0}} = \begin{cases} 0.66 \pm_{-0.07}^{+0.11}(\text{stat}) \pm 0.03(\text{syst}) & \text{for } 0.045 < q^2 < 1.1 \text{ GeV}^2/c^4, \\ 0.69 \pm_{-0.07}^{+0.11}(\text{stat}) \pm 0.05(\text{syst}) & \text{for } 1.1 < q^2 < 6.0 \text{ GeV}^2/c^4. \end{cases}$$

2.1 - 2.4 σ

Possible operators for R_K, R_{K^*}

$$\mathcal{L}_{b \rightarrow s \mu \mu}^{\text{NP}} \supset \frac{4G_F}{\sqrt{2}} V_{tb} V_{ts}^* (\delta C_9^\mu O_9^\mu + \delta C_{10}^\mu O_{10}^\mu) + \text{h.c.}$$

Altmannshofer, Stangl, Straub '17

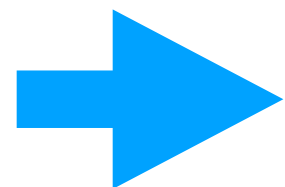


$$O_9^\mu = \frac{\alpha}{4\pi} (\bar{s}_L \gamma_\mu b_L) (\bar{\mu} \gamma^\mu \mu),$$

$$O_{10}^\mu = \frac{\alpha}{4\pi} (\bar{s}_L \gamma_\mu b_L) (\bar{\mu} \gamma^\mu \gamma_5 \mu).$$

Assuming LH currents
and LFU observables

$$(\bar{s}_L \gamma_\mu b_L) (\bar{\mu}_L \gamma^\mu \mu_L)$$



$$\text{Re}(\delta C_9^\mu) = -\text{Re}(\delta C_{10}^\mu) \in [-0.81, -0.48]$$

Z' interpretation of R_K, R_{K^*}

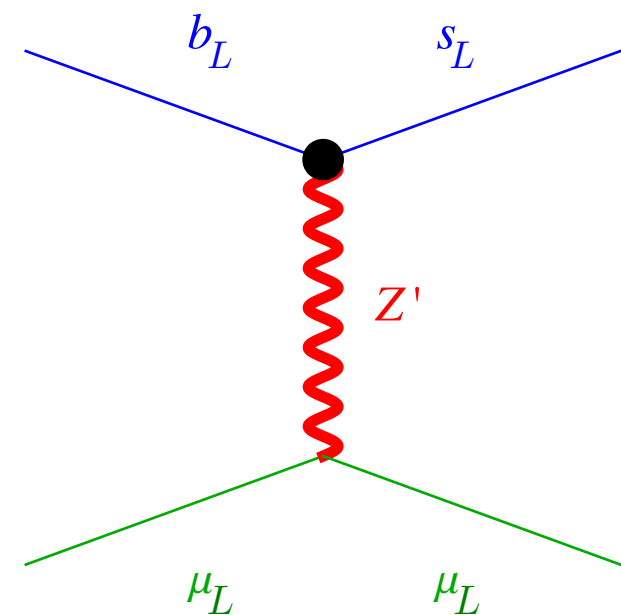
$$\Delta\mathcal{L}_{\text{eff}} \supset G_{bs\mu}(\bar{b}_L\gamma^\mu s_L)(\bar{\mu}_L\gamma_\mu\mu_L) + \text{h.c.}, \quad G_{bs\mu} \approx \frac{1}{(31.5 \text{ TeV})^2}.$$

$$G_{bs\mu} > 0 \text{ matches } C_9^\mu < 0 \text{ and } C_9^\mu = -C_{10}^\mu$$

Could originate from massive Z' model with couplings

$$\mathcal{L} \supset Z'_\mu \left(g_{bb}\bar{b}_L\gamma^\mu b_L + g_{\mu\mu}\bar{\mu}_L\gamma^\mu\mu_L \right)$$

$$V_{ts} \sim -0.04$$



$$G_{bs\mu} = -\frac{g_{bs}g_{\mu\mu}}{M_{Z'}^2} = -\frac{V_{ts}g_{bb}g_{\mu\mu}}{M_{Z'}^2} \approx \frac{1}{(31.5 \text{ TeV})^2}.$$

$$\frac{g_{bb}g_{\mu\mu}}{M_{Z'}^2} \approx \frac{1}{(6.4 \text{ TeV})^2} \quad R_K, R_{K^*}$$

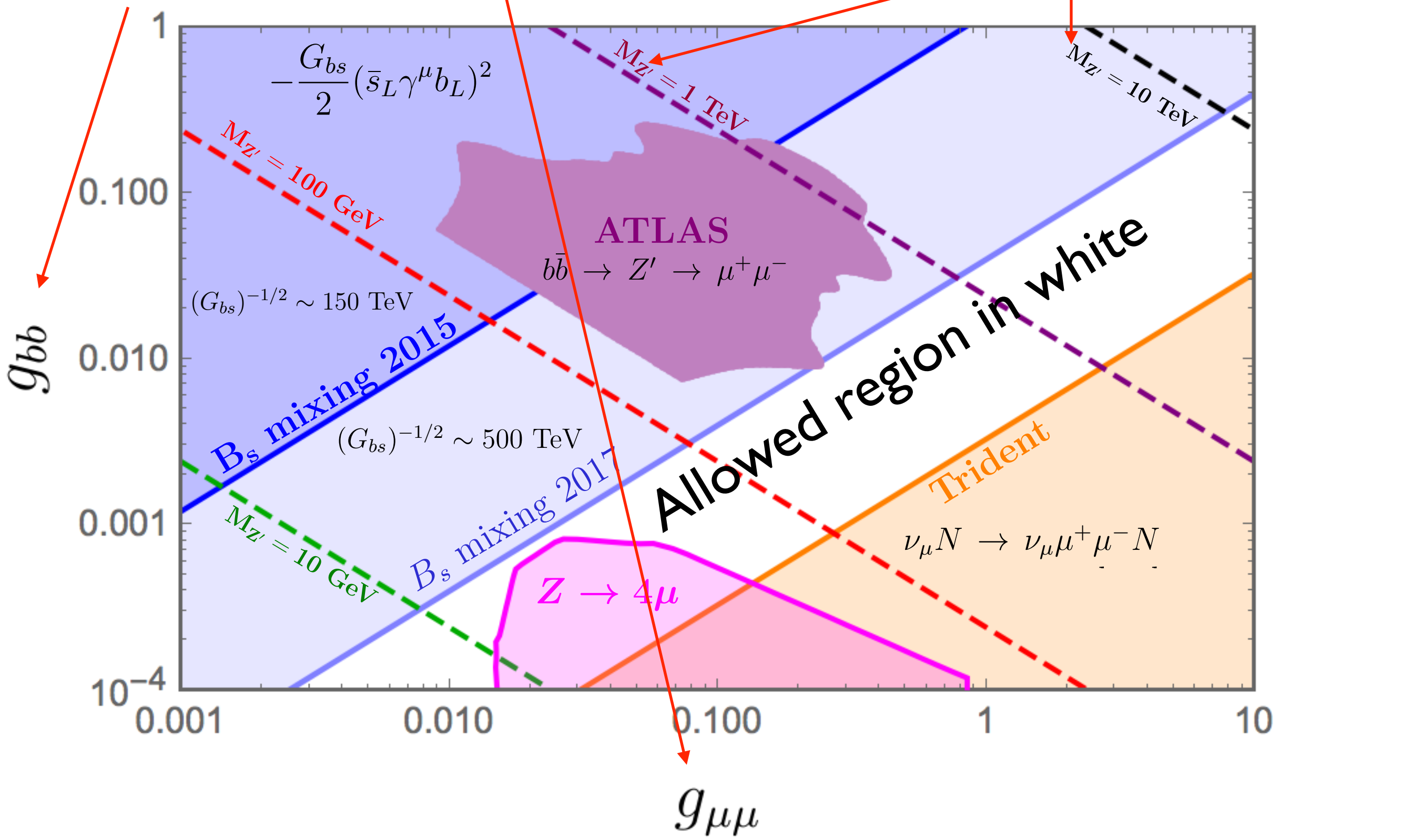
Comment on signs: $g_{bb}, g_{\mu\mu} > 0, \quad g_{bs} = g_{bb}V_{ts} < 0$

Constraints

Falkowski, SFK, Perdomo, Pierre
1803.04430

$$Z'_\mu \left(g_{bb} \bar{b}_L \gamma^\mu b_L + g_{\mu\mu} \bar{\mu}_L \gamma^\mu \mu_L \right)$$

R_K, R_{K^*} fixes $\frac{g_{bb} g_{\mu\mu}}{M_{Z'}^2} \approx \frac{1}{(6.4 \text{ TeV})^2}$

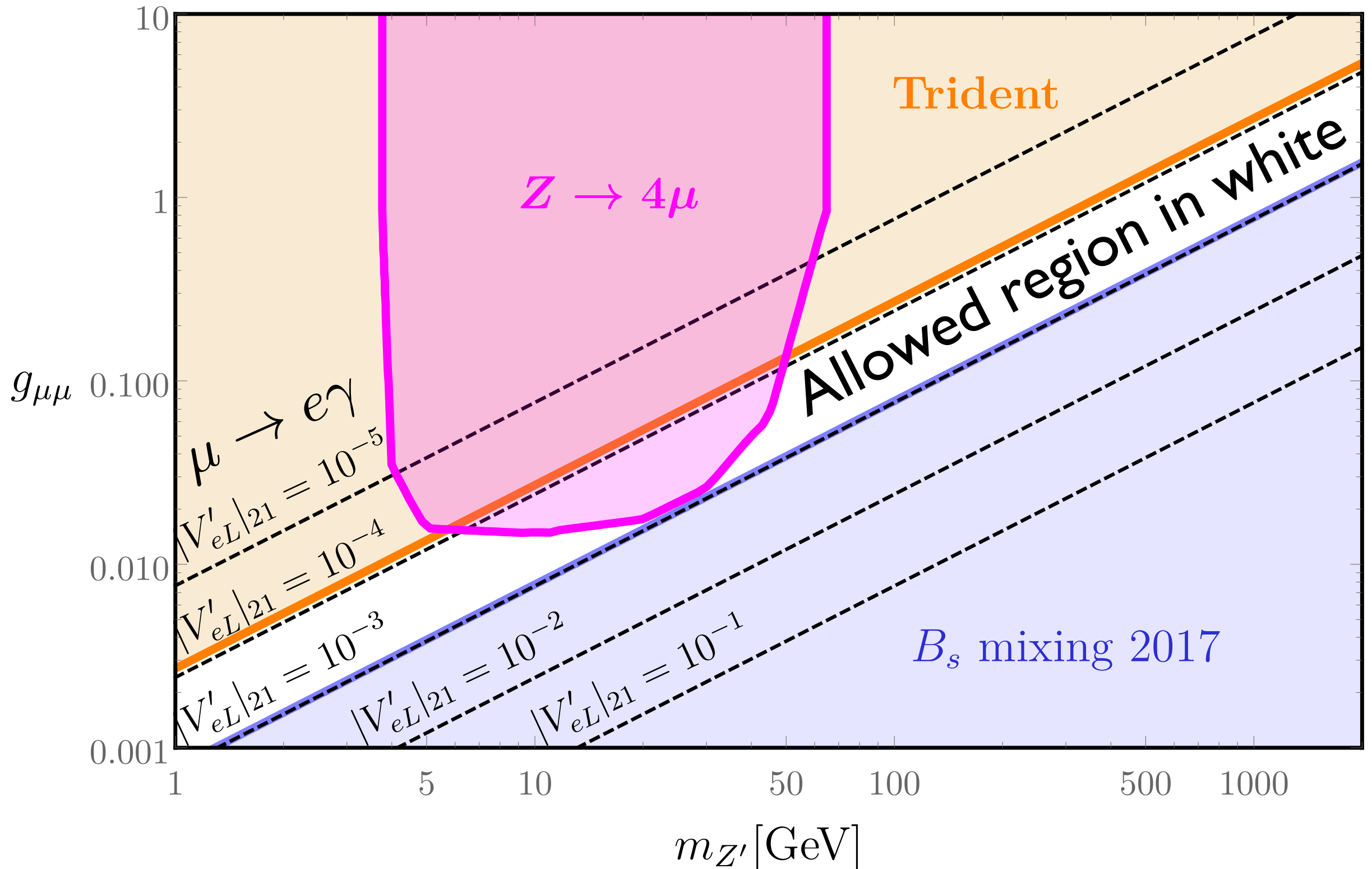


Constraints

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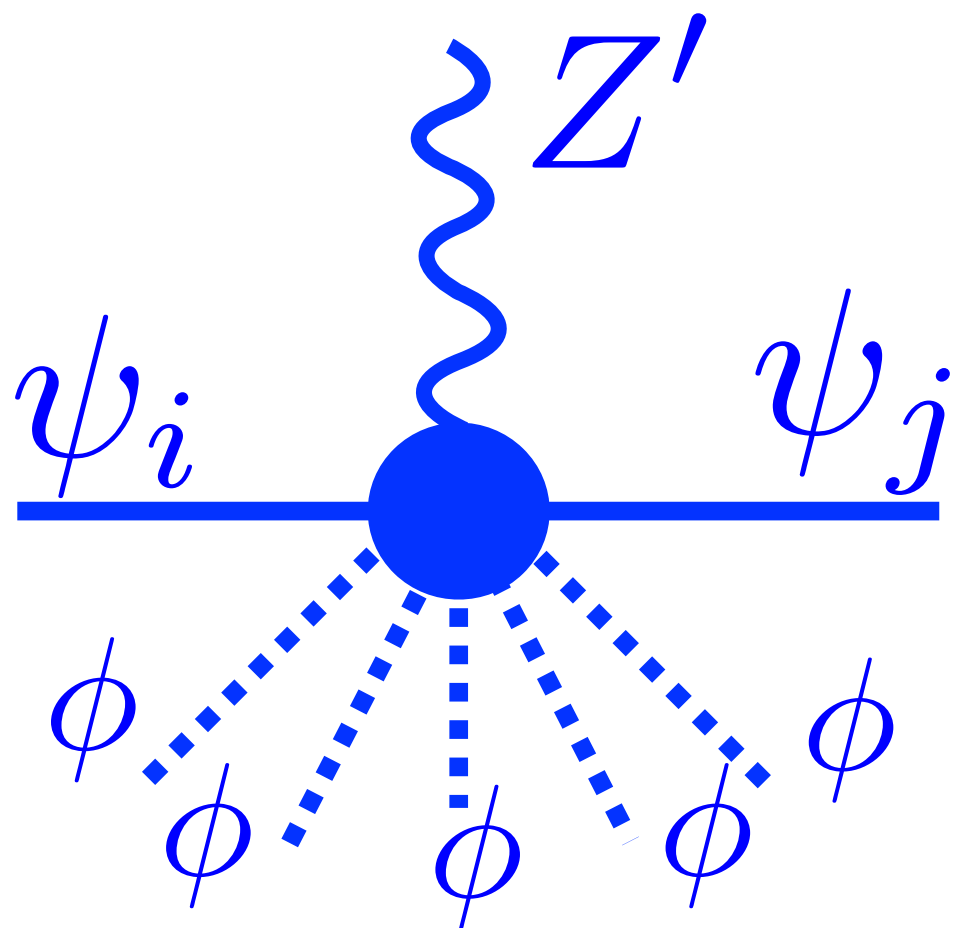
$$Z'_\mu (g_{bb}\bar{b}_L\gamma^\mu b_L + g_{\mu\mu}\bar{\mu}_L\gamma^\mu \mu_L)$$

$$\frac{g_{bb}g_{\mu\mu}}{M_{Z'}^2} \approx \frac{1}{(6.4 \text{ TeV})^2}$$



Effective Z' couplings

$$\left(\frac{\langle \phi_i^\dagger \rangle}{\Lambda_{i,n}^{1\psi}} \right)^n \left(\frac{\langle \phi_j \rangle}{\Lambda_{j,m}^{1\psi}} \right)^m g' Z'_\mu \psi_i^\dagger \gamma^\mu \psi_j$$



Z' couplings
small

due to
powers
of ratios $\frac{\langle \phi \rangle}{\Lambda}$

M_P

Now the scale is fixed

$$M_{Z'} \sim g' \langle \phi_i \rangle$$

$$\sim TeV$$

$\Lambda \sim TeV$

Phenomenological
hints from B physics

suggest low scale

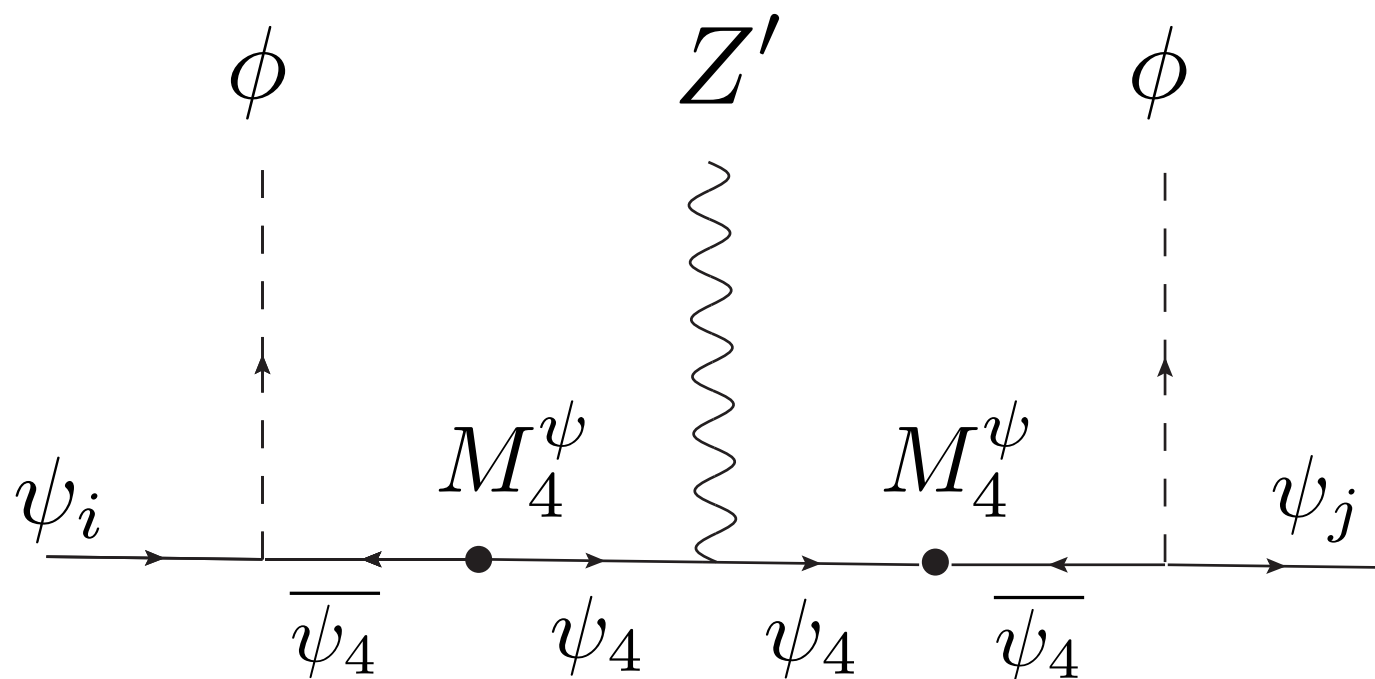
theory of flavour

M_{EW}

Example of Flavourful Z' model

Introduce a vector-like fourth family
which carries $U(1)'$ charge

Usual three families do not carry $U(1)'$ charge
but couple to Z' via fourth family mixing



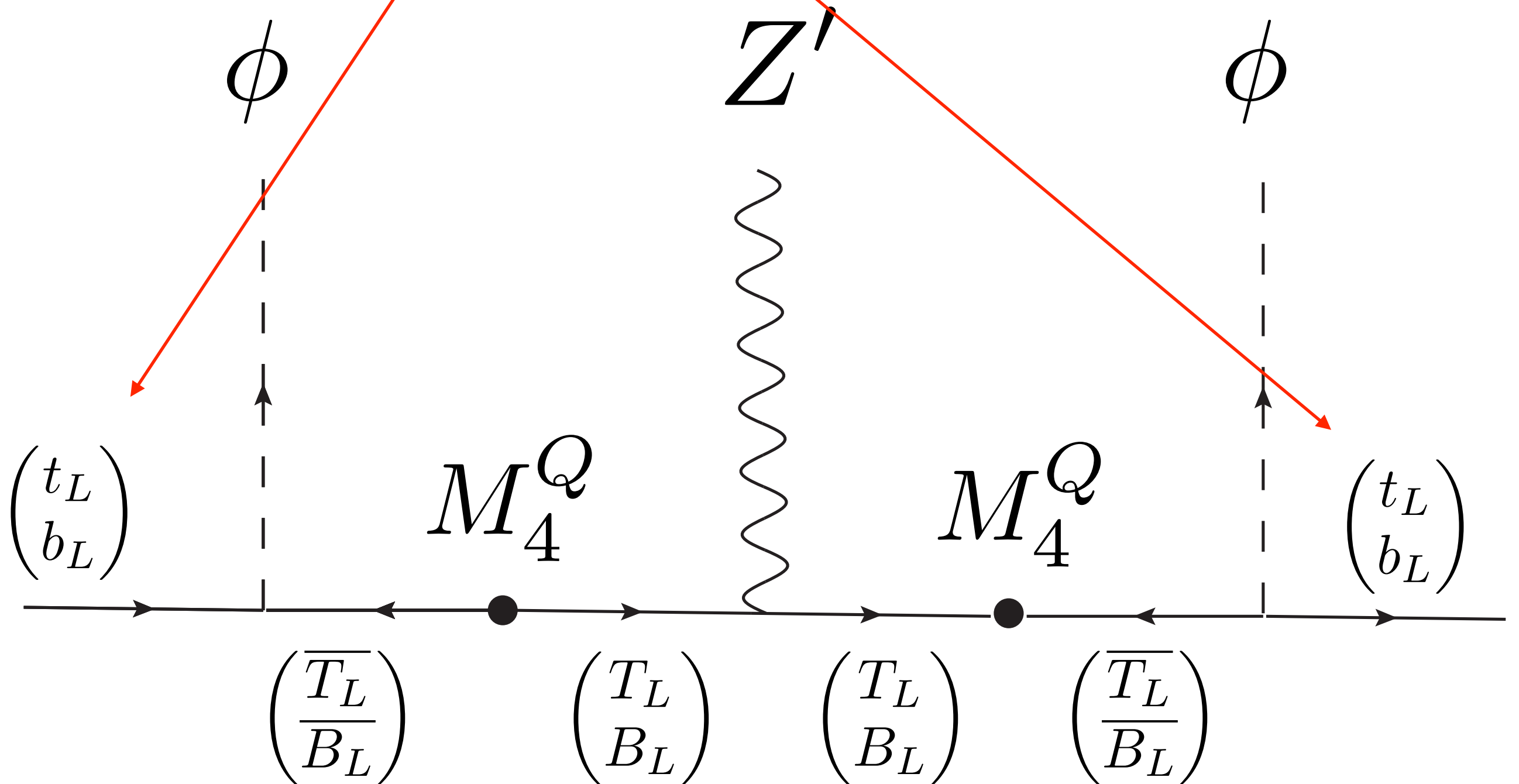
$$\frac{x_i^\psi \langle \phi \rangle}{M_4^\psi} \frac{x_j^\psi \langle \phi \rangle}{M_4^\psi} g' Z'_\mu \psi_i^\dagger \gamma^\mu \psi_j$$

“Fermiophobic model”
(afraid of Z')

“Fermiophobic model”

SFK 1706.06100

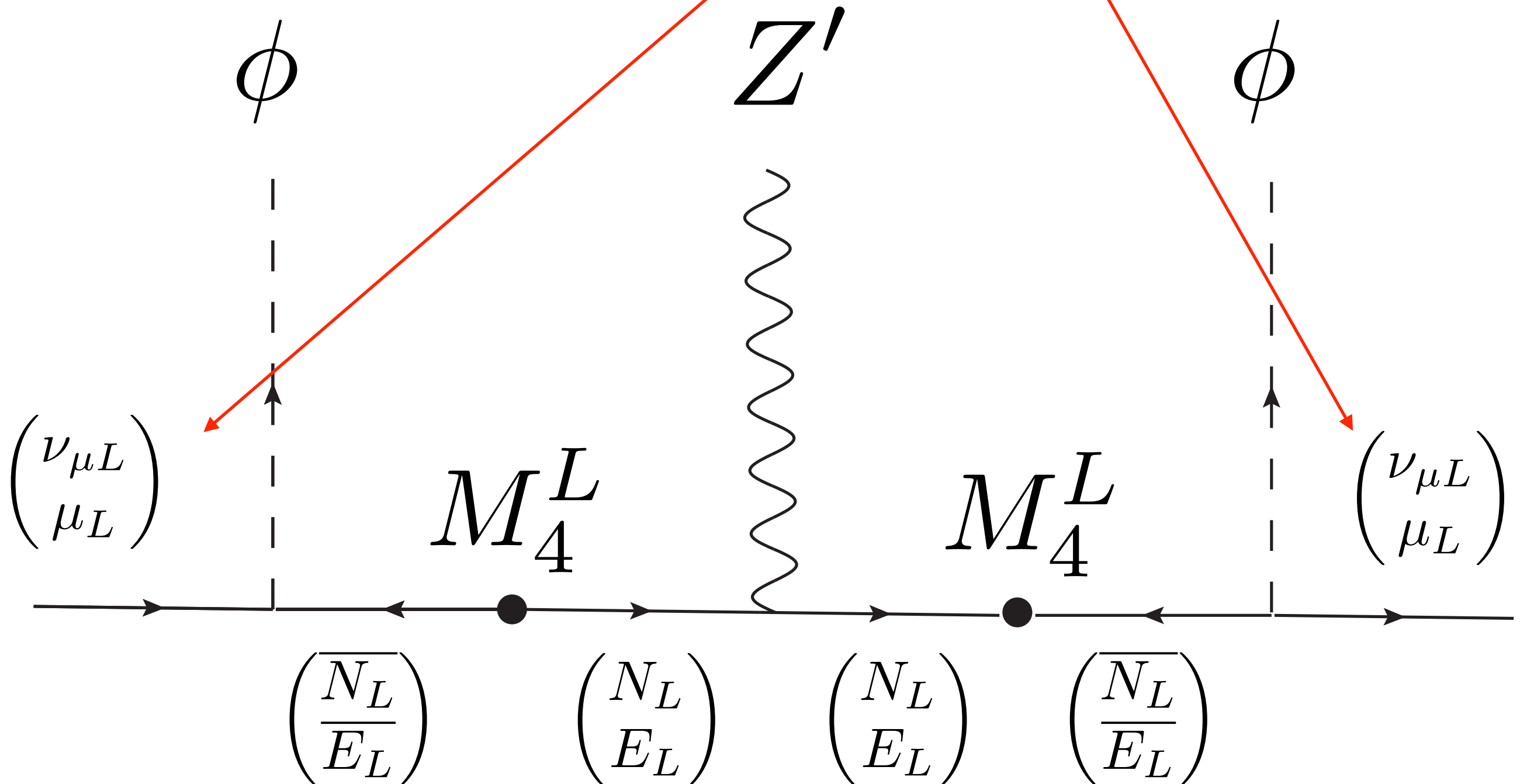
$$\mathcal{L} \supset Z'_\mu \left(g_{bb} \bar{b}_L \gamma^\mu b_L + g_{\mu\mu} \bar{\mu}_L \gamma^\mu \mu_L \right)$$



“Fermiophobic model”

SFK 1706.06100

$$\mathcal{L} \supset Z'_\mu \left(g_{bb} \bar{b}_L \gamma^\mu b_L + g_{\mu\mu} \bar{\mu}_L \gamma^\mu \mu_L \right)$$



$R_{\kappa(*)}$ and the origin of Yukawa couplings

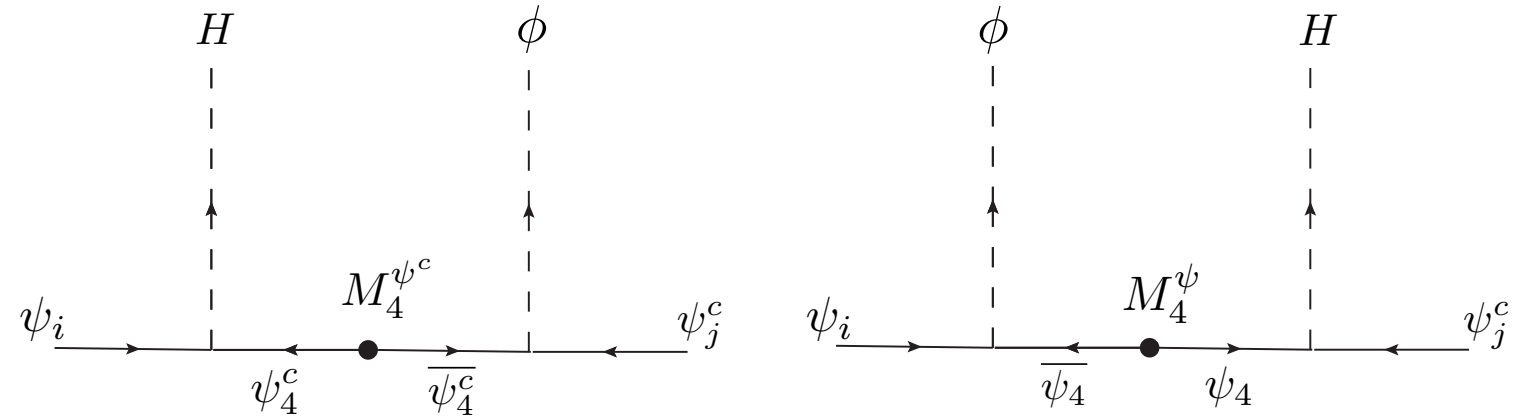
SFK 1806.06780

“Fermiophobic model”

Yukawas generated via mixing with fourth family

Ferretti, SFK, Romanino hep-ph/0609047

Field	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)'$
Q_i	3	2	1/6	0
u_i^c	$\bar{\mathbf{3}}$	1	-2/3	0
d_i^c	$\bar{\mathbf{3}}$	1	1/3	0
L_i	1	2	-1/2	0
e_i^c	1	1	1	0
ν_i^c	1	1	0	0
Q_4	3	2	1/6	1
u_4^c	$\bar{\mathbf{3}}$	1	-2/3	1
d_4^c	$\bar{\mathbf{3}}$	1	1/3	1
L_4	1	2	-1/2	1
e_4^c	1	1	1	1
ν_4^c	1	1	0	1
\overline{Q}_4	$\bar{\mathbf{3}}$	$\bar{\mathbf{2}}$	-1/6	-1
\overline{u}_4^c	3	1	2/3	-1
\overline{d}_4^c	3	1	-1/3	-1
\overline{L}_4	1	$\bar{\mathbf{2}}$	1/2	-1
\overline{e}_4^c	1	1	-1	-1
$\overline{\nu}_4^c$	1	1	0	-1
ϕ	1	1	0	1
H_u	1	2	1/2	-1
H_d	1	2	-1/2	-1



Yukawas

$$\frac{x_j^{\psi^c} \langle \phi \rangle}{M_4^{\psi^c}} y_{i4}^{\psi} H \psi_i \psi_j^c + \frac{x_i^{\psi} \langle \phi \rangle}{M_4^{\psi}} y_{4j}^{\psi} H \psi_i \psi_j^c$$

R κ (*) and the origin of Yukawa couplings

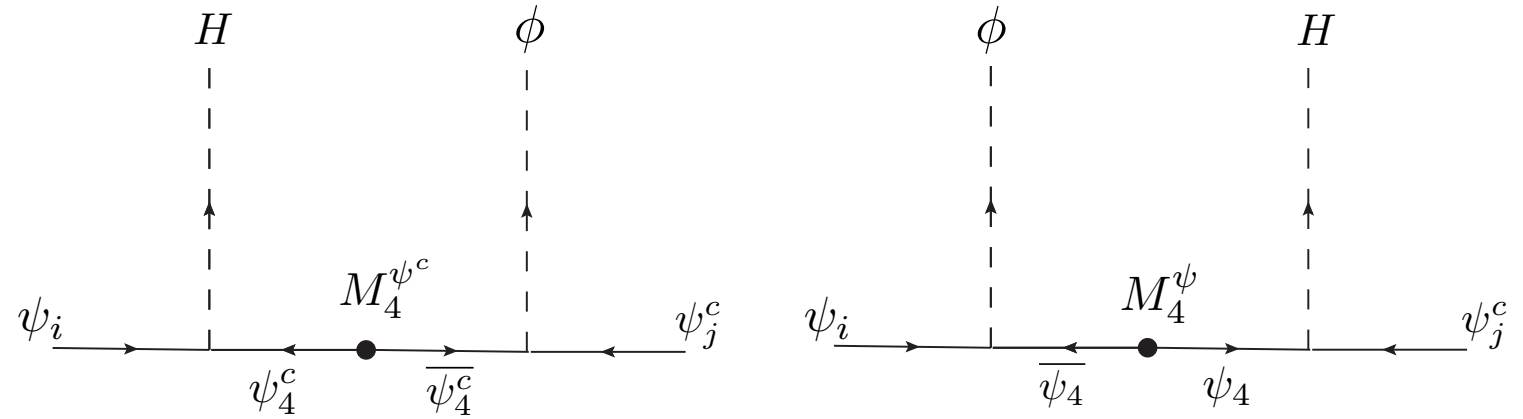
SFK 1806.06780

“Fermiophobic model”

Field	$SU(3)_c$	$SU(2)_L$	$U(1)_Y$	$U(1)'$
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L_i	1	2	-1/2	0
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d_4^c	$\bar{\mathbf{3}}$	1	1/3	1
L_4	1	2	-1/2	1
e_4^c	1	1	1	1
ν_4^c	1	1	0	1
\bar{Q}_4	$\bar{\mathbf{3}}$	$\bar{\mathbf{2}}$	-1/6	-1
\bar{u}_4^c	3	1	2/3	-1
\bar{d}_4^c	3	1	-1/3	-1
\bar{L}_4	1	$\bar{\mathbf{2}}$	1/2	-1
\bar{e}_4^c	1	1	-1	-1
$\bar{\nu}_4^c$	1	1	0	-1
ϕ	1	1	0	1
H_u	1	2	1/2	-1
H_d	1	2	-1/2	-1

Yukawas generated via mixing with fourth family

Ferretti, SFK, Romanino hep-ph/0609047

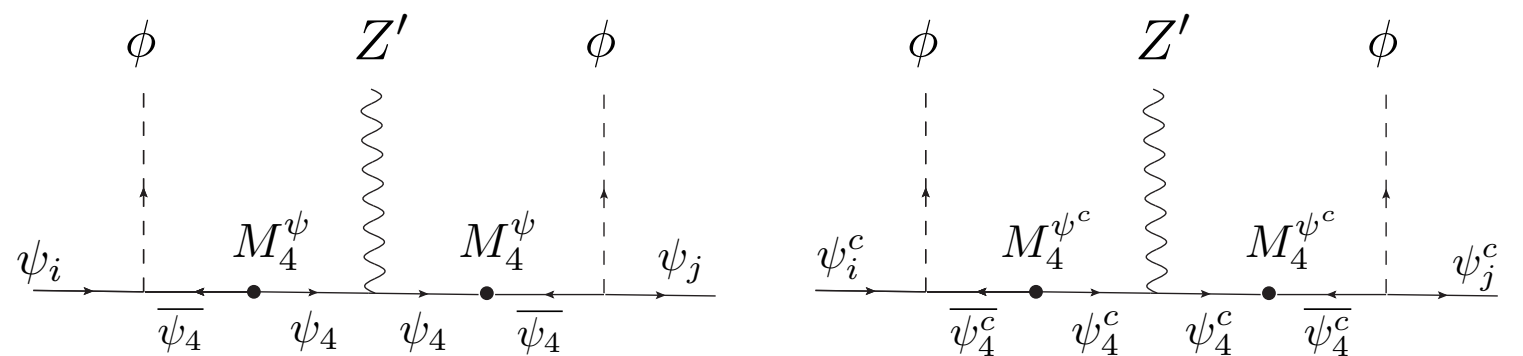


Yukawas

$$\frac{x_j^{\psi^c} \langle \phi \rangle}{M_4^{\psi^c}} y_{i4}^{\psi} H \psi_i \psi_j^c + \frac{x_i^{\psi} \langle \phi \rangle}{M_4^{\psi}} y_{4j}^{\psi} H \psi_i \psi_j^c$$

Z' couplings generated via mixing with fourth family

SFK 1706.06100



Z' couplings

$$\frac{x_i^{\psi} \langle \phi \rangle}{M_4^{\psi}} \frac{x_j^{\psi} \langle \phi \rangle}{M_4^{\psi}} g' Z'_\mu \psi_i^\dagger \gamma^\mu \psi_j + \frac{x_i^{\psi^c} \langle \phi \rangle}{M_4^{\psi^c}} \frac{x_j^{\psi^c} \langle \phi \rangle}{M_4^{\psi^c}} g' Z'_\mu \psi_i^{c\dagger} \gamma^\mu \psi_j^c$$

R_K(*) and the origin of Yukawa couplings

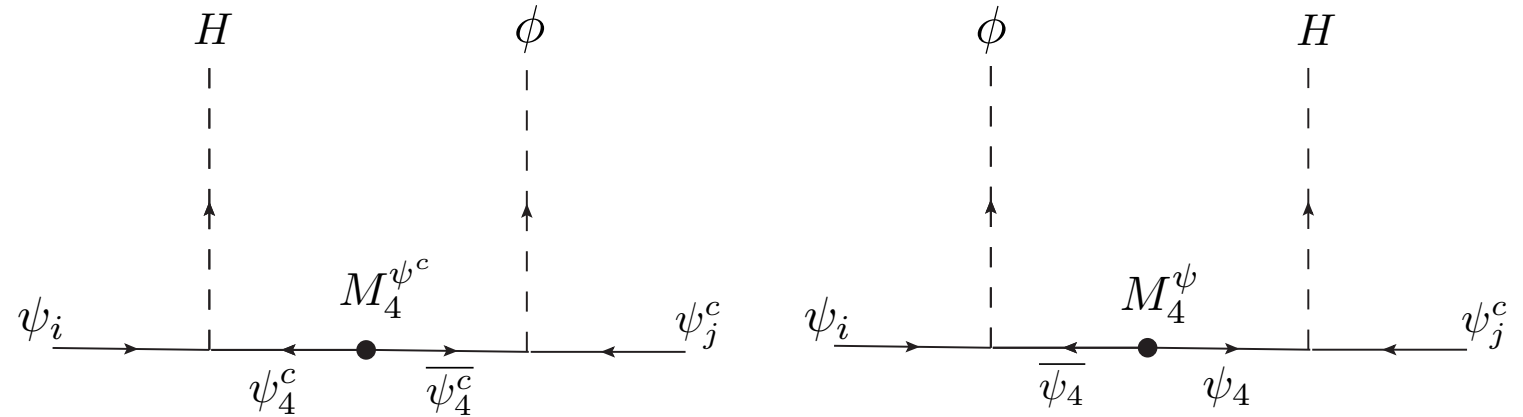
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“Fermiophobic model”

Yukawa and Z' couplings are related

SFK 1806.06780

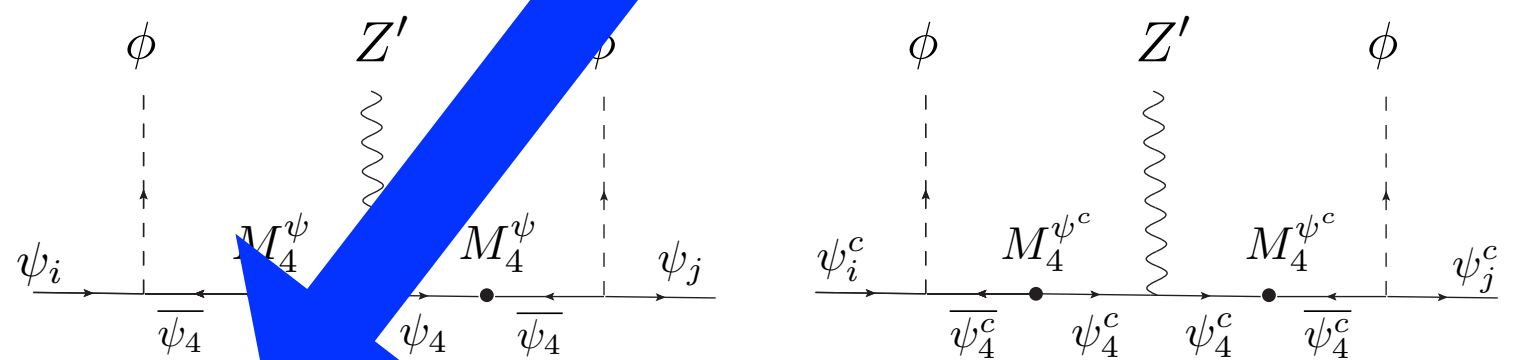
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d_i^c	$\bar{\mathbf{3}}$	1	1/3	0
L_i	1	2	-1/2	0
e_i^c	1	1	1	0
ν_i^c	1	1	0	0
Q_4	3	2	1/6	1
u_4^c	$\bar{\mathbf{3}}$	1	-2/3	1
d_4^c	$\bar{\mathbf{3}}$	1	1/3	1
L_4	1	2	-1/2	1
e_4^c	1	1	1	1
ν_4^c	1	1	0	1
\overline{Q}_4	$\bar{\mathbf{3}}$	$\bar{\mathbf{2}}$	-1/6	-1
\overline{u}_4^c	3	1	2/3	-1
\overline{d}_4^c	3	1	-1/3	-1
\overline{L}_4	1	$\bar{\mathbf{2}}$	1/2	-1
\overline{e}_4^c	1	1	-1	-1
$\overline{\nu}_4^c$	1	1	0	-1
ϕ	1	1	0	1
H_u	1	2	1/2	-1
H_d	1	2	-1/2	-1



Yukawas

$$\frac{x_j^{\psi^c} \langle \phi \rangle}{M_4^{\psi^c}} y_{i4}^{\psi} H \psi_i \psi_j^c + \frac{x_i^{\psi} \langle \phi \rangle}{M_4^{\psi}} y_{4j}^{\psi} H \psi_i \psi_j^c$$

Z' muon coupling
related to muon Yukawa
-- too small?



Z' couplings

$$\frac{x_i^{\psi} \langle \phi \rangle}{M_4^{\psi}} \frac{x_j^{\psi} \langle \phi \rangle}{M_4^{\psi}} g' Z'_\mu \psi_i^\dagger \gamma^\mu \psi_j + \frac{x_i^{\psi^c} \langle \phi \rangle}{M_4^{\psi^c}} \frac{x_j^{\psi^c} \langle \phi \rangle}{M_4^{\psi^c}} g' Z'_\mu \psi_i^{c\dagger} \gamma^\mu \psi_j^c$$

R_K(*) and the origin of Yukawa couplings

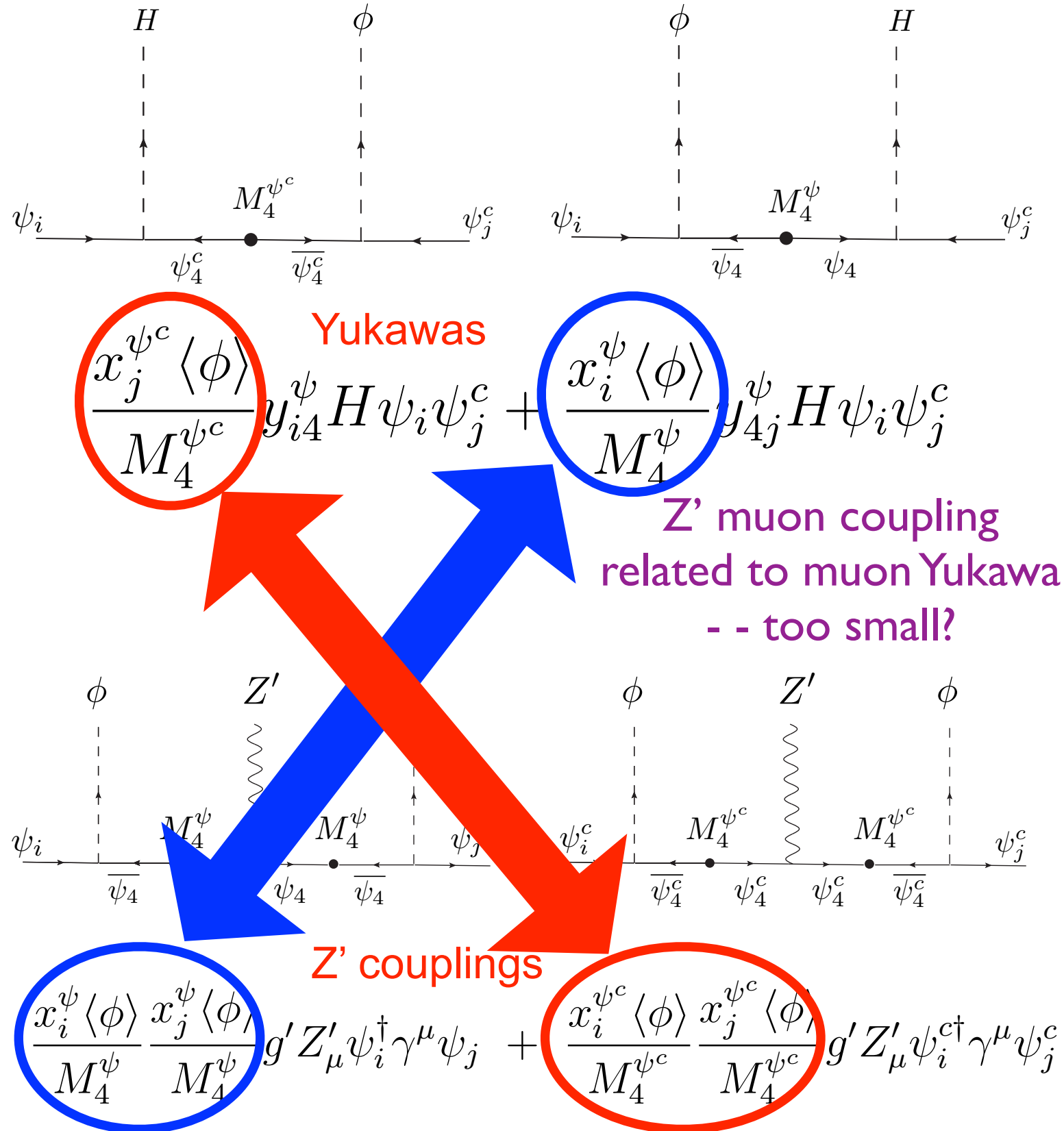
SFK 1806.06780

“Fermiophobic model”

Yukawa and Z' couplings are related

SFK 1806.06780

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d_i^c	$\bar{\mathbf{3}}$	1	1/3	0
L_i	1	2	-1/2	0
e_i^c	1	1	1	0
ν_i^c	1	1	0	0
Q_4	3	2	1/6	1
u_4^c	$\bar{\mathbf{3}}$	1	-2/3	1
d_4^c	$\bar{\mathbf{3}}$	1	1/3	1
L_4	1	2	-1/2	1
e_4^c	1	1	1	1
ν_4^c	1	1	0	1
\bar{Q}_4	$\bar{\mathbf{3}}$	$\bar{\mathbf{2}}$	-1/6	-1
\bar{u}_4^c	3	1	2/3	-1
\bar{d}_4^c	3	1	-1/3	-1
\bar{L}_4	1	$\bar{\mathbf{2}}$	1/2	-1
\bar{e}_4^c	1	1	-1	-1
$\bar{\nu}_4^c$	1	1	0	-1
ϕ	1	1	0	1
H_u	1	2	1/2	-1
H_d	1	2	-1/2	-1



Finale

The Flavour Problem

- Not going away - biggest problem of SM ?
- More interesting since neutrino mass & mixing

Theories of Flavour near Planck Scale

- Well motivated by SUSY GUTs
- Include discrete family symmetry from orbifolding
- Many possibilities - hard to test (but Littlest Seesaw)
- Need to discover SUSY!

Theories of Flavour near Electroweak scale

- Motivated by anomalies in B physics
- Many phenomenological constraints
- Models under construction