

Symmetries of the Light Hadron Spectrum in High Temperature QCD

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Overview

High-temperature phase of QCD (previous talk by K. Suzuki):

- topological susceptibility consistent with zero (\exists critical quark mass?)
- $U(1)_A$ susceptibility strongly suppressed

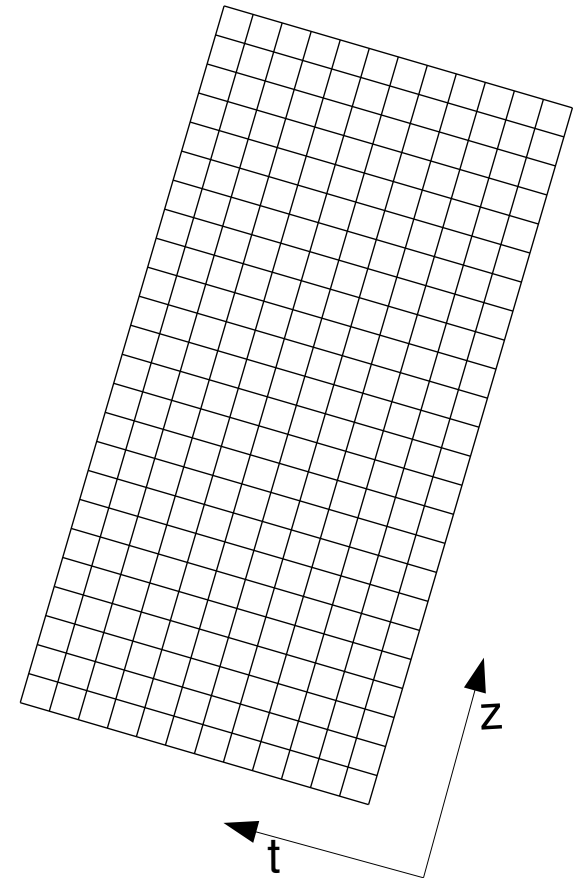
Outline:

- at $1.2 T_c$: $U(1)_A$ and $SU(2)_L \times SU(2)_R$ symmetries
 - for mesonic screening spectrum
 - for parity doubling in baryon spectrum
 - for baryonic screening spectrum
- at higher temperature:
 - $SU(2)_{CS}$ chiral spin and $SU(4)$ symmetries

Simulation Setup

- $n_f=2$ flavor QCD
- **2.6 GeV** cutoff ($1/a$)
- **domain wall fermions** with $m_{\text{res}} < 1$ MeV
- quark masses from $m_{\text{ud}} = \mathbf{2.6 MeV}$ to 26 MeV
- temperatures from $\mathbf{T = 220 MeV}$ to 1 GeV
 - pseudo-critical temperature: 175 MeV
 - point sources for quark propagators

$N_s^3 \times N_t$	β	T [MeV]	T/T _c
$24^3 \times 12$	4.30	220	1.2
$32^3 \times 12$	4.30	220	1.2
$40^3 \times 12$	4.30	220	1.2
$32^3 \times 8$	4.30	330	1.8
$32^3 \times 8$	4.37	220	2.2
$32^3 \times 6$	4.30	440	2.5
$32^3 \times 8$	4.50	480	2.7
$32^3 \times 4$	4.30	660	3.8
$32^3 \times 4$	4.50	960	5.5



Chiral Symmetries at $1.2 T_c$

Meson Operators

- local isovector operators: $O_\Gamma(x) = \bar{q}(x)(\vec{\tau} \otimes \Gamma)q(x)$

$$\langle O(t)\bar{O}(0) \rangle \sim e^{-mt} + e^{-m(N_t-t)}$$

- extract effective mass: $m_{eff}(t) = \ln \left| \frac{C(t)}{C(t+1)} \right|$ (or cosh to respect periodicity)

- for screening spectrum: $t \rightarrow z$, $C(n_z) = \sum_{n_x, n_y, n_t} \langle O(n_x, n_y, n_z, n_t)\bar{O}(\mathbf{0}) \rangle$

Chiral-Parity Group Rep.	Γ	Abbreviation	Symmetries
$(\frac{1}{2}, \frac{1}{2})_a$ $(\frac{1}{2}, \frac{1}{2})_b$	γ_5 $\mathbf{1}$	<i>PS</i> <i>S</i>	$] U(1)_A$
$[(0, 1) + (1, 0)]_a$ $[(0, 1) + (1, 0)]_a$ $(\frac{1}{2}, \frac{1}{2})_a$ $(\frac{1}{2}, \frac{1}{2})_b$	$\gamma_k \gamma_5$ γ_k $\gamma_k \gamma_3$ $\gamma_k \gamma_3 \gamma_5$	A V T X	$] SU(2)_A$ $] U(1)_A$

Chiral Symmetry of the Mesons Spectrum

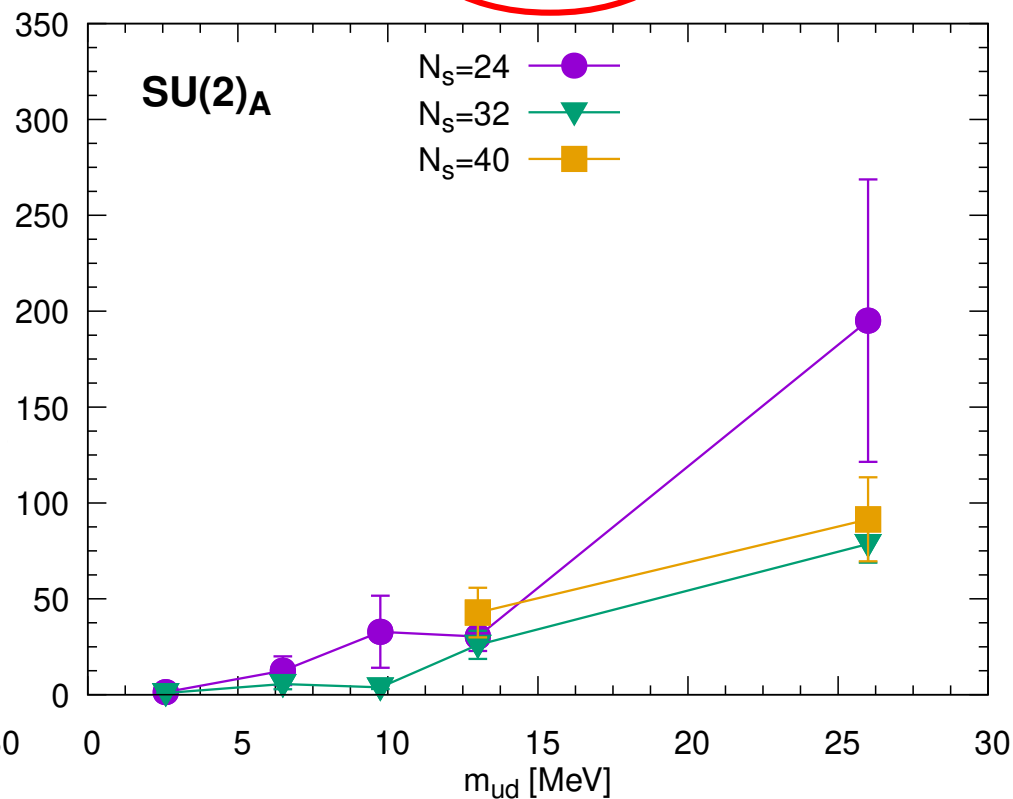
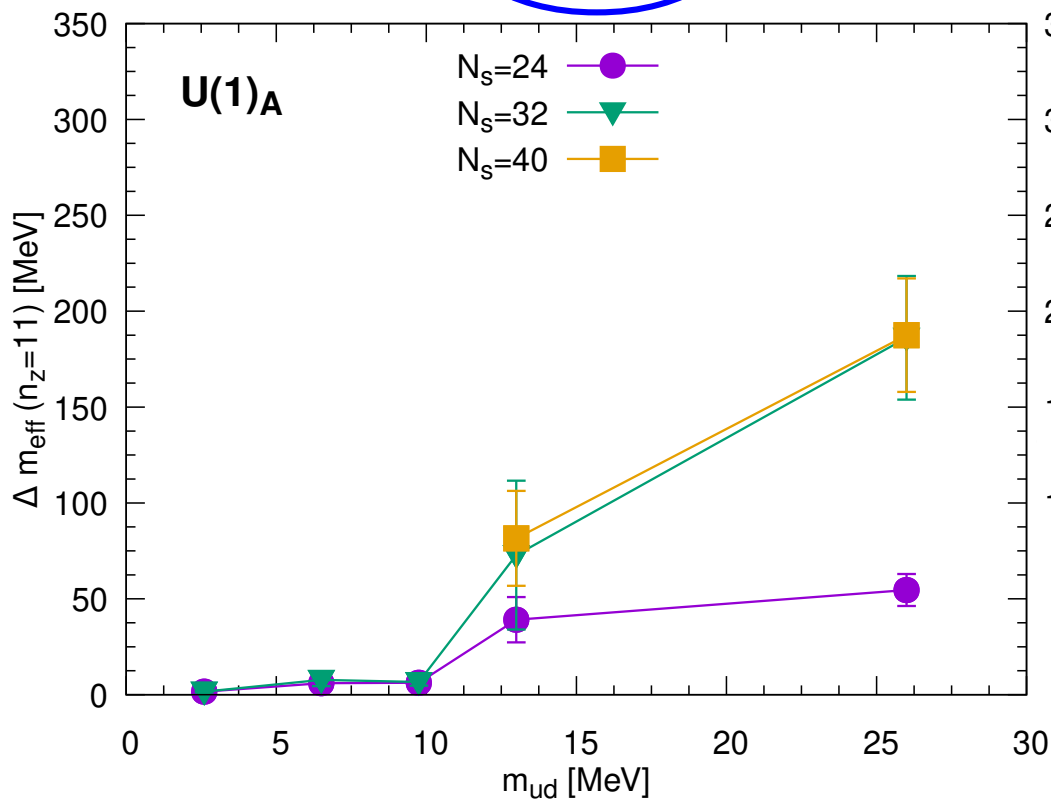
→ extract symmetry violation by comparing screening masses of related interpolating fields

@ 1.2 T_c

$$U(1)_A : \Delta m_{eff} = |m_{eff}^{PS} - m_{eff}^S|$$

$$PS \leftarrow e^{i(\gamma_5 \otimes \mathbf{1}) \vec{\theta}} \rightarrow S$$

$$V_x \leftarrow e^{i(\gamma_5 \otimes \vec{\tau}) \vec{\theta}} \rightarrow A_x$$



Baryon Operators

- local nucleon operators (isospin=1/2, spin=1/2)

- parity projection: $N_{\pm} = \frac{(1 \pm \gamma_4)}{2} N$

$$\langle N^{\pm}(t) \bar{N}^{\pm}(0) \rangle \sim e^{-m_{\pm} t} + e^{-m_{\mp}(N_t - t)}$$

positive parity
forward

negative parity
backward

- for screening spectrum: $t \rightarrow z$, $C(n_z) = \sum_{n_x, n_y, n_t} e^{in_t \omega_0} \langle N^{\pm}(n_x, n_y, n_z, n_t) \bar{N}^{\pm}(\mathbf{0}) \rangle$

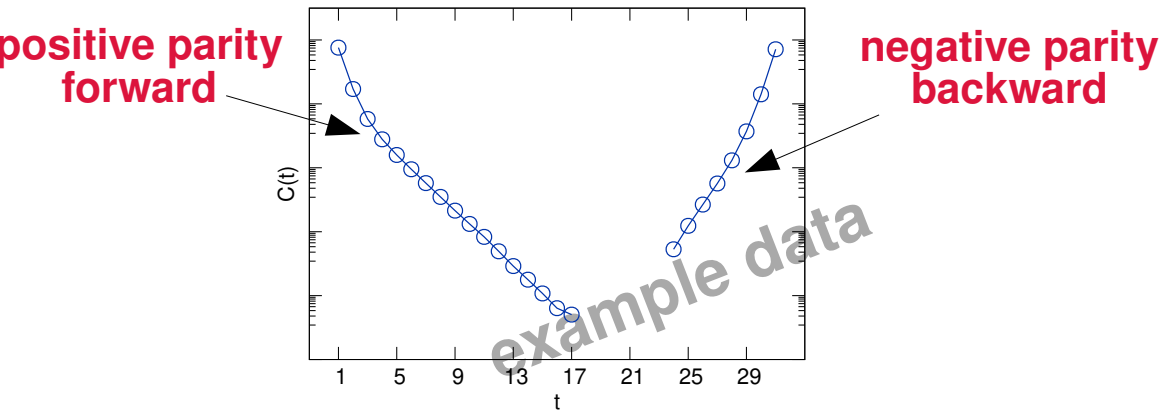
Chiral-Parity Group Rep.	Operator	Abbreviation	Symmetries
$[(0, \frac{1}{2}) + (\frac{1}{2}, 0)]_a$	$(\tilde{q}q)q$	N_1] $U(1)_A$
$[(0, \frac{1}{2}) + (\frac{1}{2}, 0)]_b$	$(\tilde{q}\gamma_5 q)\gamma_5 q$	N_2	
$(\frac{1}{2}, 1) + (1, \frac{1}{2})$	$(\tilde{q}\gamma_{\mu} q)\gamma^{\mu} q$	N_3] $SU(2)_A$
$(\frac{1}{2}, 1) + (1, \frac{1}{2})$	$(\tilde{q}\gamma_{\mu}\gamma_5\tau^i q)\gamma^{\mu}\gamma_5\tau^i q$	N_4	

$$\tilde{q} = q^T C \gamma_5 (i\tau_2)$$

Parity Doubling of Nucleons

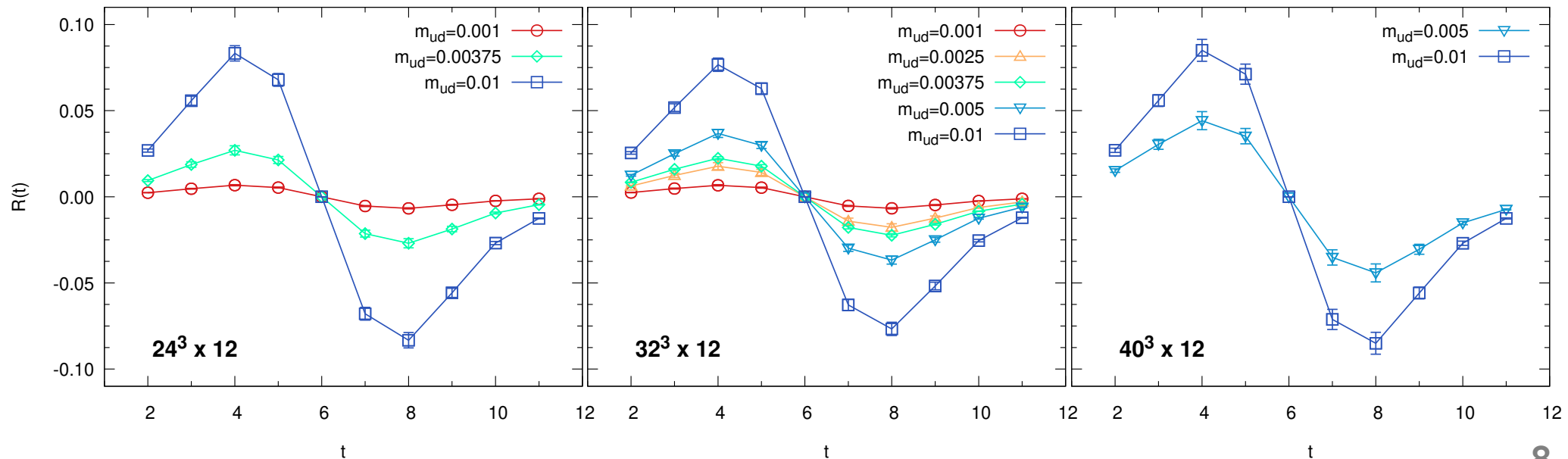
→ extract symmetry violation by comparing
positive and negative parity states of same interpolating field

@ 1.2 T_c



'R-parameter':

$$R(t) = \frac{N_1(t) - N_1(N_t - t)}{N_1(t) + N_1(N_t - t)}$$



Parity Doubling of Nucleons

→ extract symmetry violation by comparing
positive and negative parity states of same interpolating field

@ 1.2 T_c

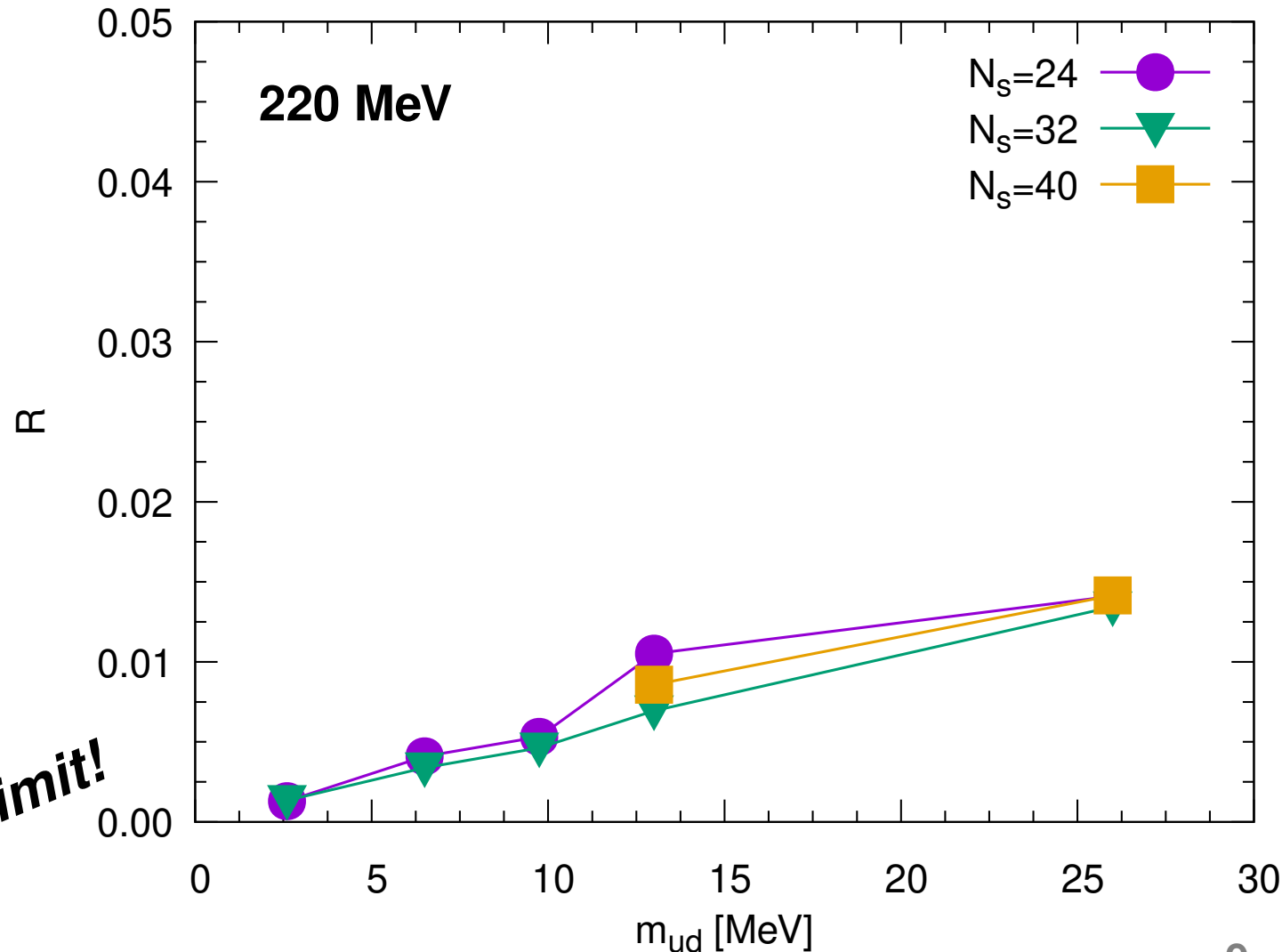
integrated 'R-parameter':

$$R = \frac{\sum_{t=1}^{N_t/2} R(t)/\sigma^2(t)}{\sum_{t=1}^{N_t/2} 1/\sigma^2(t)}$$

$R \neq 0$
no parity doubling

$R = 0$
parity doubling

in chiral limit!



Chiral Symmetry of the Baryon Spectrum

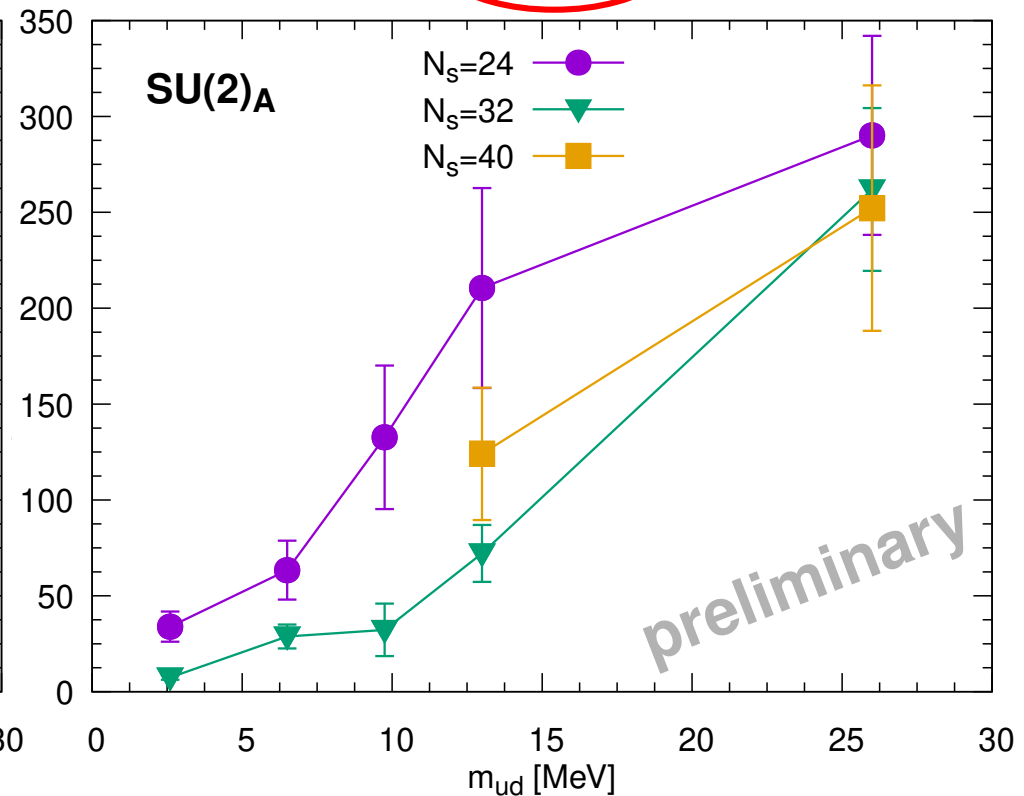
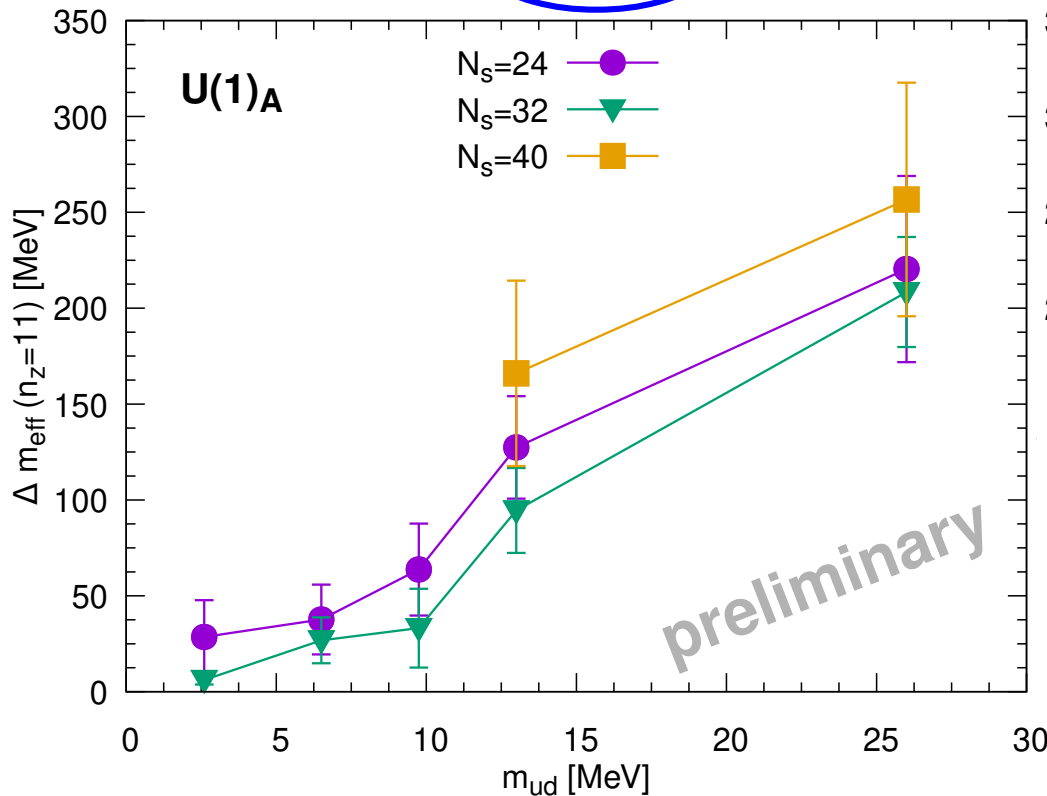
→ extract symmetry violation by comparing
screening masses of related interpolating fields

@ 1.2 T_c

$$U(1)_A : \Delta m_{eff} = |m_{eff}^{N_1^+} - m_{eff}^{N_2^+}|$$

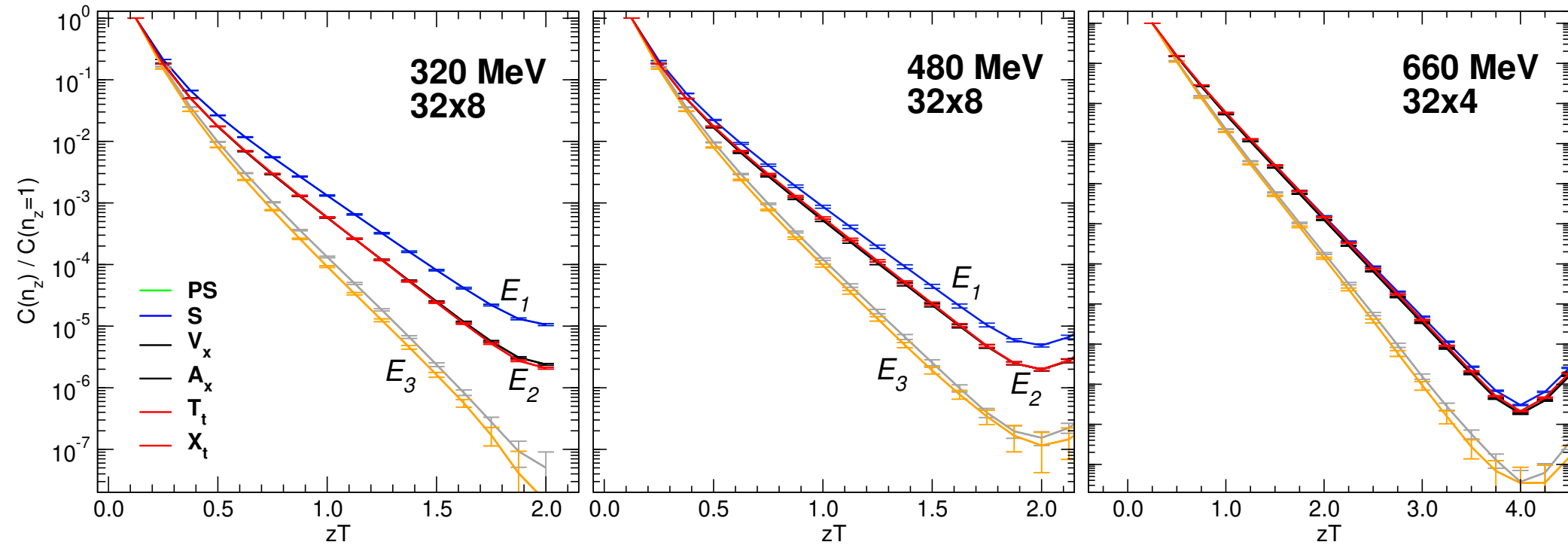
$$N_1^+ \leftarrow e^{i(\gamma_5 \otimes \mathbf{1})\vec{\theta}} \rightarrow N_2^+$$

$$N_3^+ \leftarrow e^{i(\gamma_5 \otimes \vec{\tau})\vec{\theta}} \rightarrow N_4^+$$



Symmetries at Higher Temperature

Temperature Evolution of Meson Spectrum



states of different chirality
connected by **chiral spin**:

$$SU(2)_{CS}$$

$$\{\gamma_2, -i\gamma_5\gamma_2, \gamma_5\} \Rightarrow A_x \leftrightarrow T_t \leftrightarrow X_t$$

minimal group containing
chiral spin and **chiral symmetry**:

$$SU(4)$$

$$V_x \leftrightarrow T_t \leftrightarrow X_t \leftrightarrow A_x \quad \leftarrow E_2$$

$$V_t \leftrightarrow T_x \leftrightarrow X_x \leftrightarrow A_t \quad \leftarrow E_3$$

Is High Temperature QCD 'more' symmetric?

E_1, E_2, E_3 groups show **multiplet structure**..

define '**kappa**' parameter

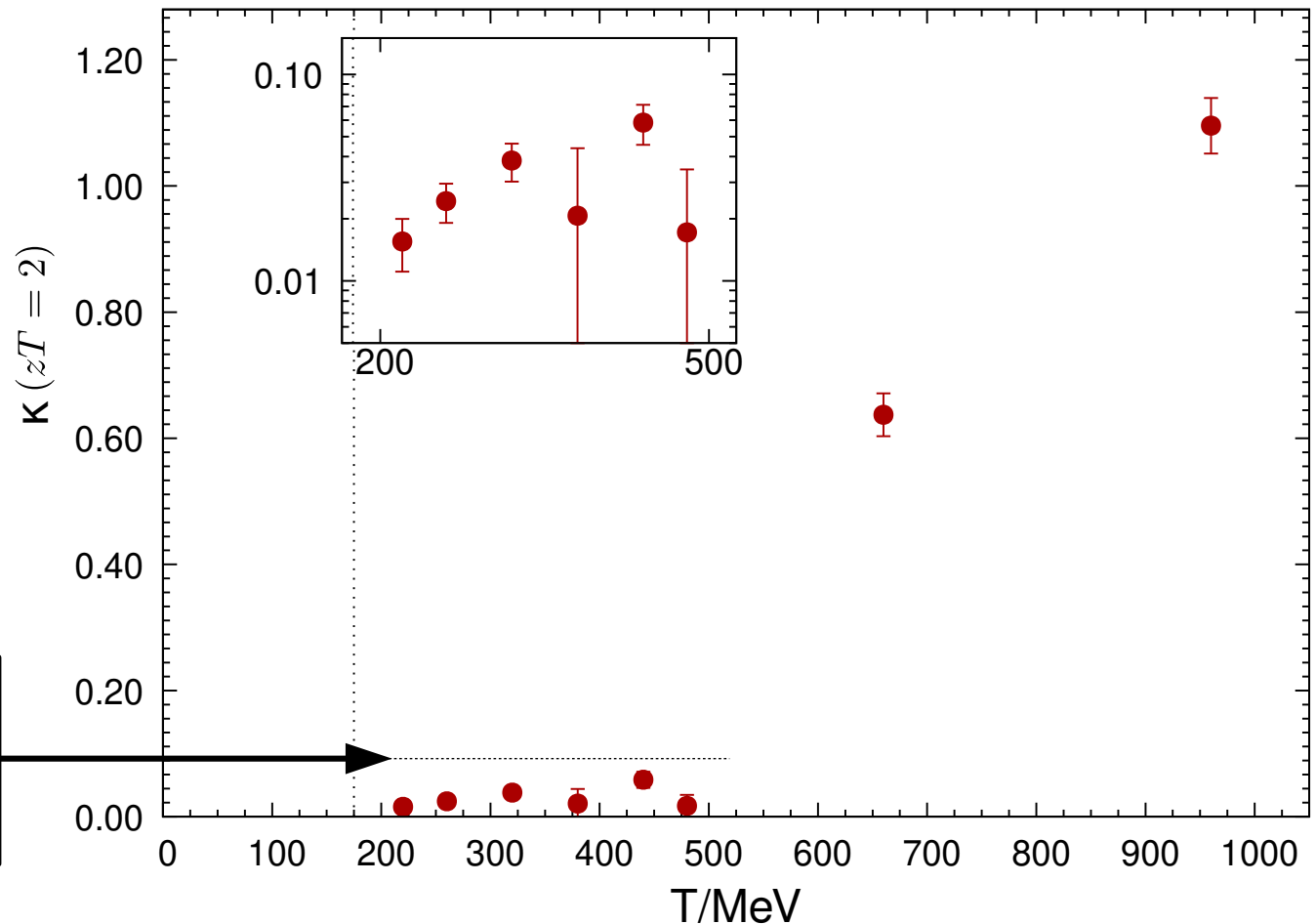
$$\kappa = \frac{|C_{A_x} - C_{T_t}|}{|C_{A_x} - C_S|}$$

as intuitive symmetry measure!

(distance **within** a multiplet relative to the distance **between** multiplets)

temperature range

$T \sim 220 - 500$ MeV



Chiral Spin and the Lagrangian

$$\Psi \xrightarrow{\text{SU}(2)_{CS}} e^{i\vec{\Sigma}\vec{\theta}/2}\Psi \quad \vec{\Sigma} = \{\gamma_k, -i\gamma_5\gamma_k, \gamma_5\}$$

free, massless fermions:

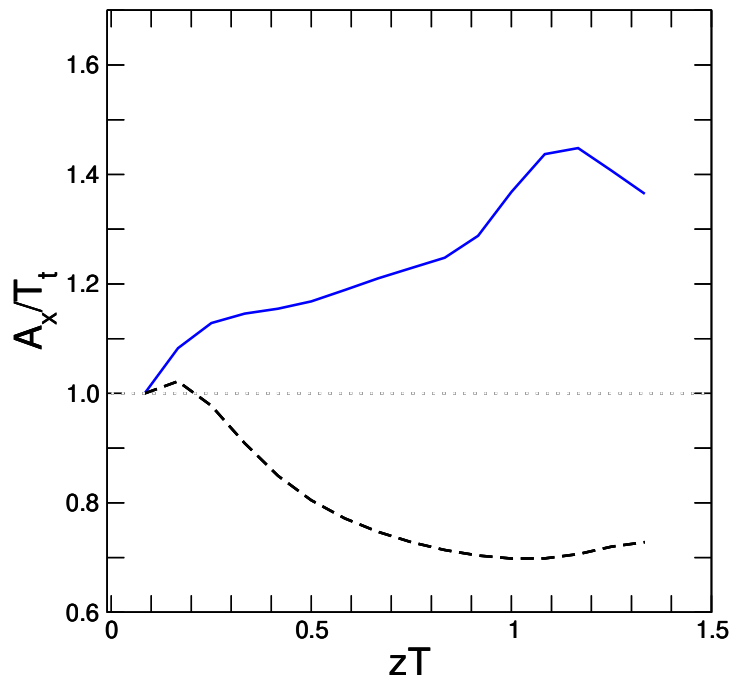
$$\mathcal{L} = \bar{\Psi} i \not{\partial} \Psi$$

covariant derivative:

$$D_\mu = \partial_\mu - igA_\mu$$

interacting, massless fermions:

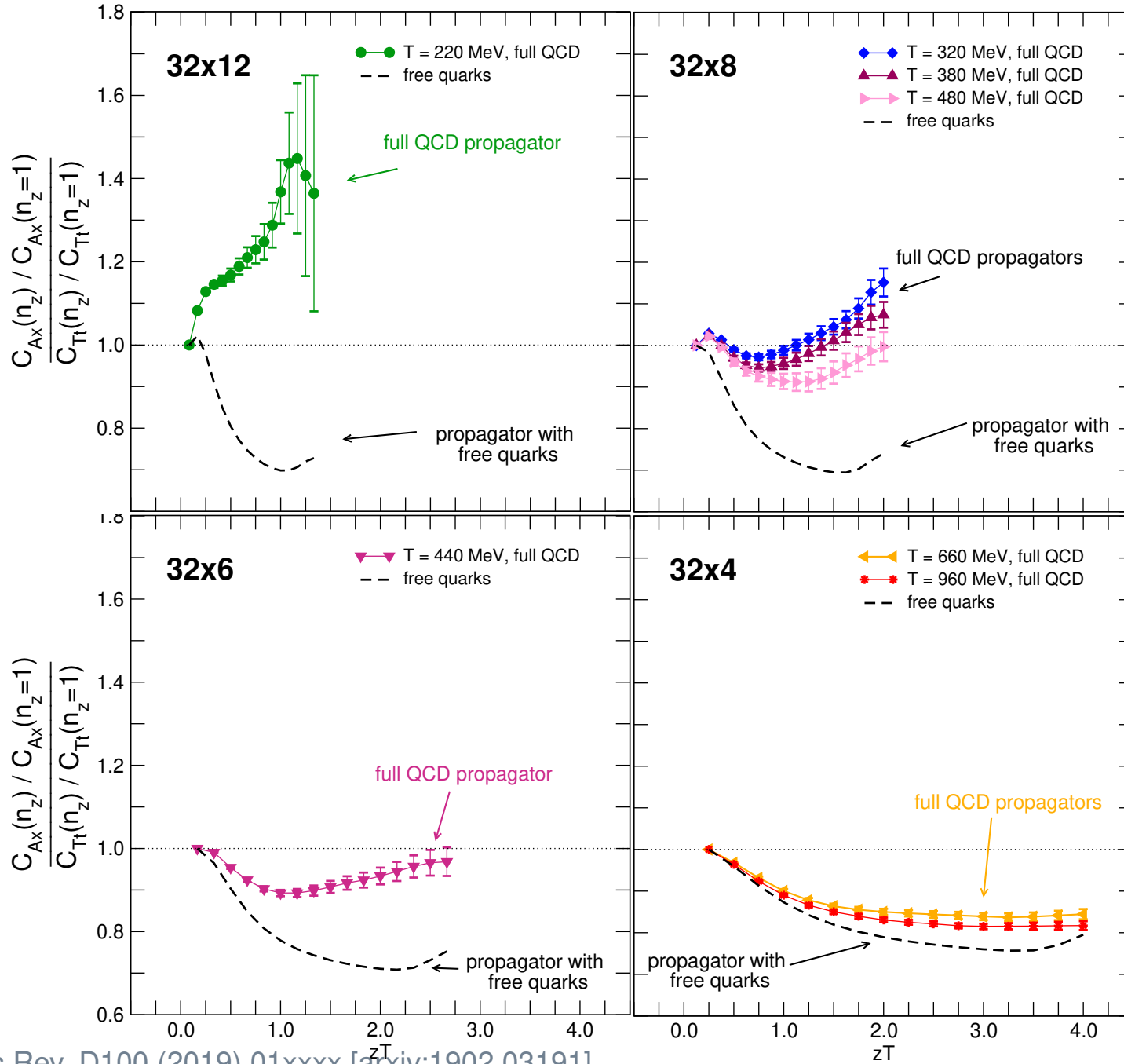
$$\mathcal{L} = \bar{\Psi} i \not{D} \Psi = \bar{\Psi} i \gamma^0 D_0 \Psi + \bar{\Psi} i \gamma^i D_i \Psi$$



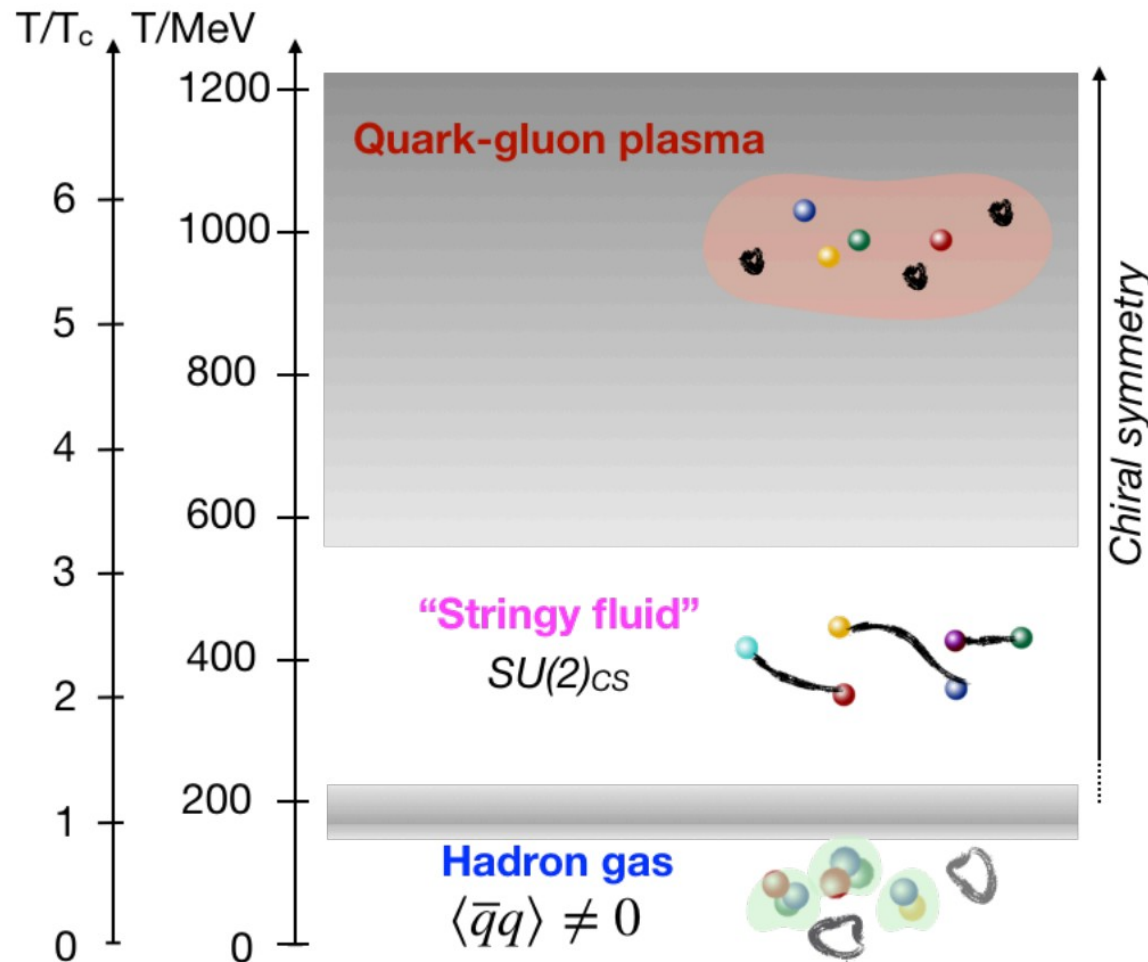
- **kinetic** term breaks chiral spin
- **electric** term is invariant
- **magnetic** term breaks chiral spin

*A and T mix under chiral spin transformations:
use ratio to measure breaking **within** multiplet!*

Interaction within SU(4) multiplets



Sketch of a 'new' Phase Diagram



strongly interacting matter

between
chiral transition
 and
 weakly interacting **QGP**

Chemical potential does not change picture:

$$S = \int_0^{1/T} \int d^3x \bar{\Psi} [\gamma_\mu D_\mu + \mu \gamma_4] \Psi$$

'stringy fluid' regime at experimental accessible temperatures!

Conclusions

Above chiral transition at 220 MeV:

- $SU(2)_L \times SU(2)_R$ restored
- $U(1)_A$ effectively restored
- **parity doubling** for baryons

At temperatures up to 500 MeV:

- QCD matter approximately **SU(4)** symmetric
- favors **color-electric** degrees of freedom
- chiral symmetry restoration \neq deconfinement