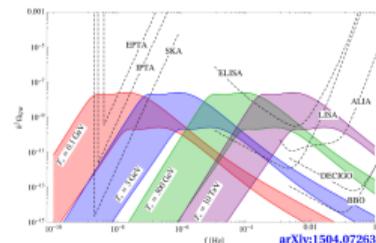
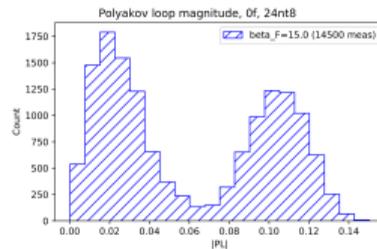
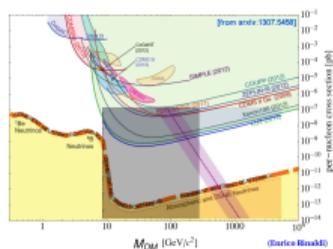
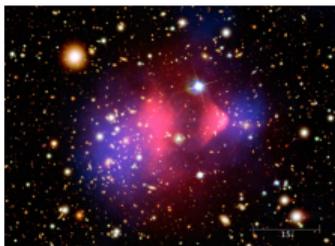


Stealth dark matter and gravitational waves



David Schaich (University of Liverpool)

Lattice 2019, 19 June

Work in progress with the [Lattice Strong Dynamics Collaboration](#)

Lattice Strong Dynamics Collaboration

Argonne Xiao-Yong Jin, James Osborn

Bern Andrew Gasbarro

Boston Rich Brower, Dean Howarth, Claudio Rebbi

Colorado **Ethan Neil**, Oliver Witzel

UC Davis Joseph Kiskis

Livermore Pavlos Vranas

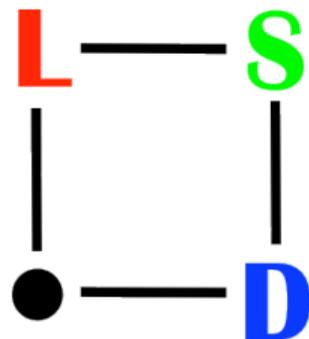
Liverpool **DS**

Nvidia Evan Weinberg

Oregon **Graham Kribs**

RIKEN **Enrico Rinaldi**

Yale Thomas Appelquist, Kimmy Cushman, George Fleming



Exploring the range of possible phenomena in strongly coupled field theories

Overview

Stealth dark matter

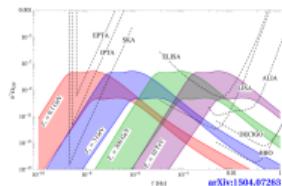
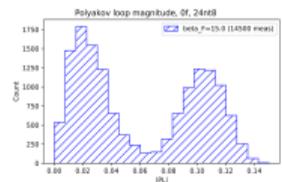
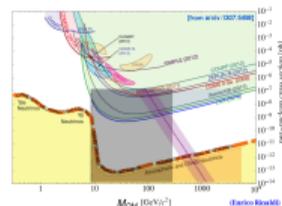
Attractive and viable composite dark matter model

Exploring gravitational waves from first-order transition

Stealth dark matter motivational review

4-flavor SU(4) lattice phase diagram

Gravitational wave prospects

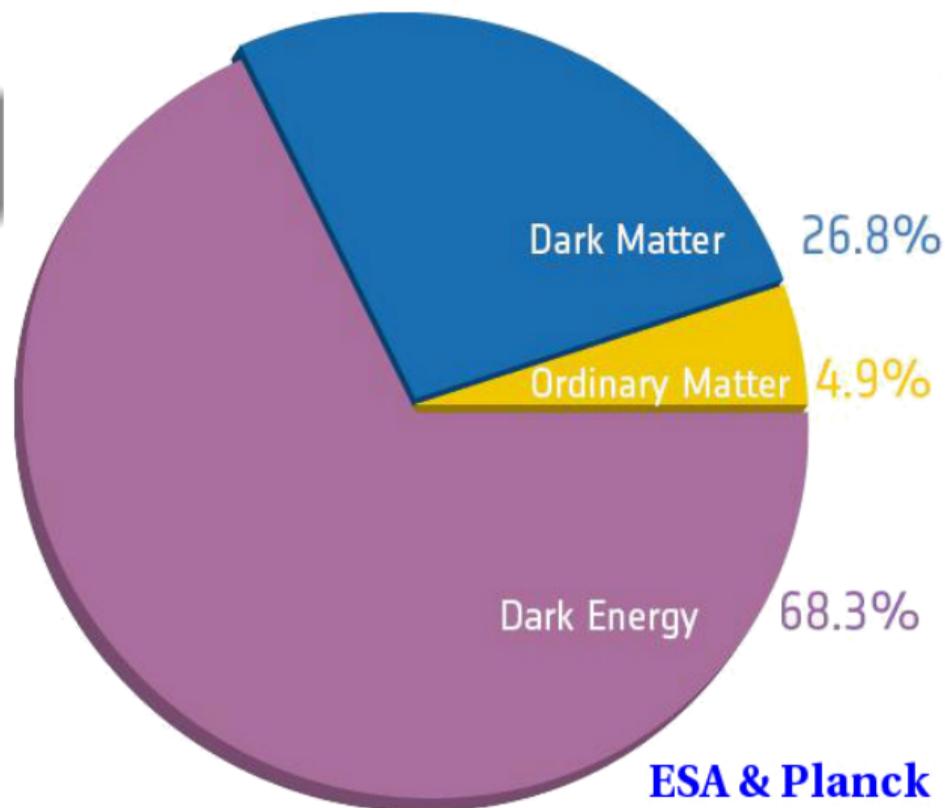


Dark matter

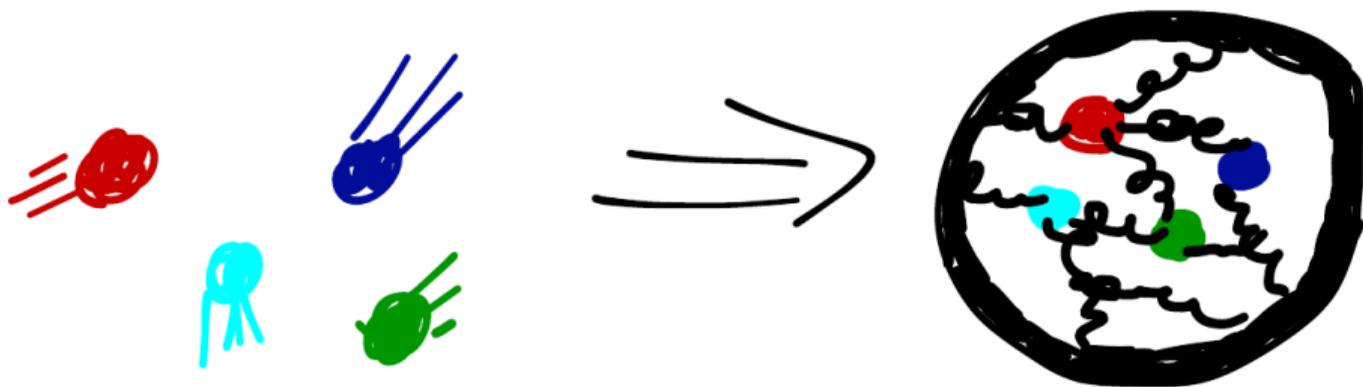
Consistent gravitational evidence
from kiloparsec to Gpc scales

$$\frac{\Omega_{\text{dark}}}{\Omega_{\text{ordinary}}} \approx 5 \quad \dots \text{not } 10^5 \text{ or } 10^{-5}$$

→ non-gravitational interactions
with standard model



Composite dark matter



Early universe

Deconfined charged fermions \rightarrow non-gravitational interactions

Present day

Confined neutral 'dark baryons' \rightarrow no experimental detections

Stealth dark matter

[PRL **115** 171803; PRD **92** 075030]

SU(4) dark sector with four moderately heavy fundamental fermions

Lightest scalar 'baryon' is stable dark matter candidate

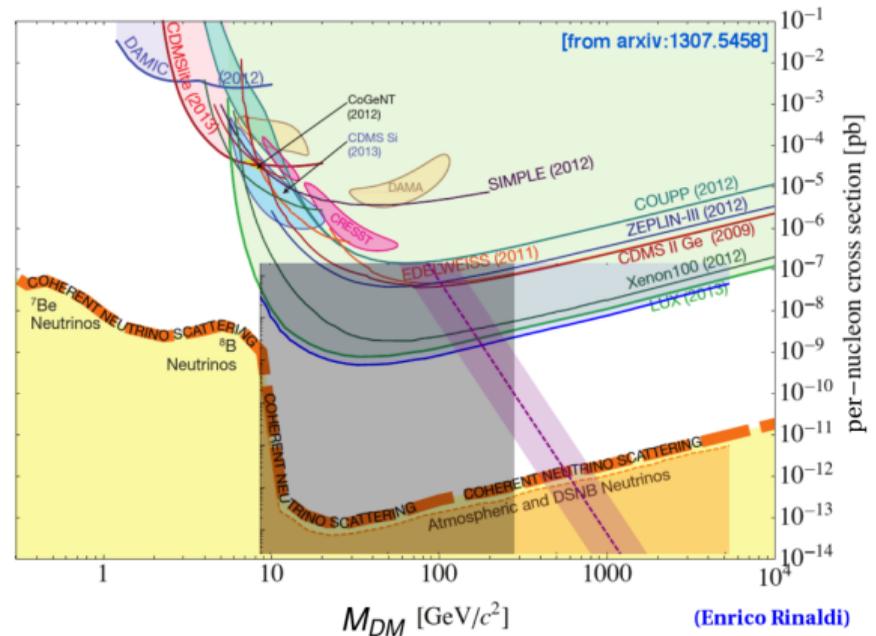
Direct detection

Symmetries

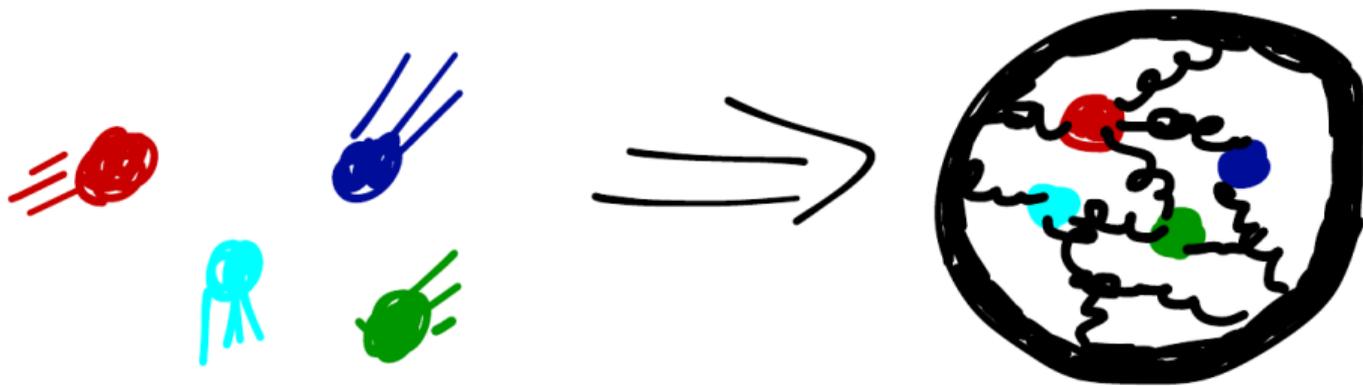
→ electric polarizability
is leading interaction

Collider searches

Charged 'meson' Drell–Yan
rules out shaded region



Gravitational waves



Gravitational waves

First-order confinement transition \rightarrow stochastic background

\Rightarrow Lattice studies of stealth dark matter phase transition

Phase diagram expectations

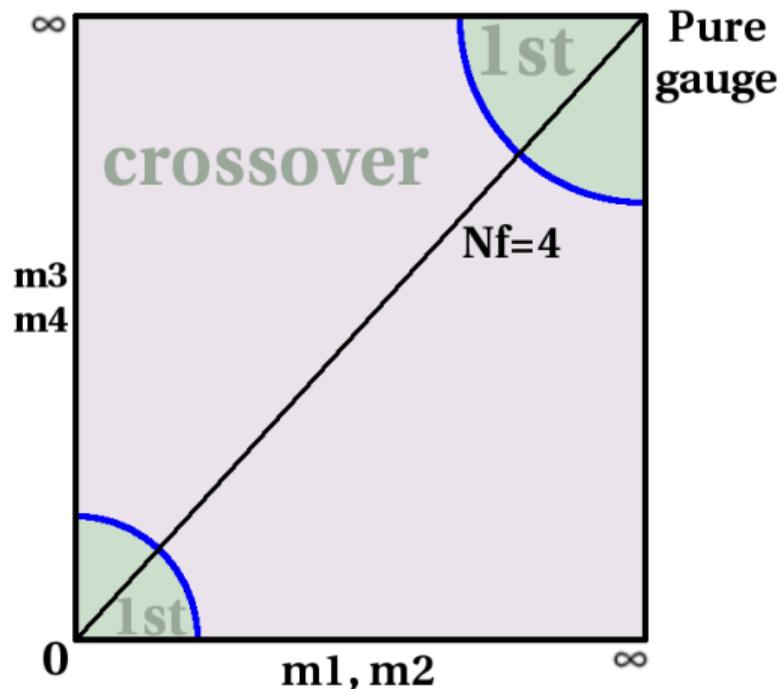
Pure-gauge transition is first order

Becomes stronger as N increases

First-order transition persists
for sufficiently heavy fermions

How heavy is sufficient for SU(4)?

Using $N_F = 4$ unrooted staggered fermions
gauge action with both fundamental & adjoint plaquette terms



The lattice phase diagram game

Fermion masses $m = 0.05, 0.067, 0.1, 0.2$ (and pure gauge)

×

Temporal extents $N_T = 4, 6, 8, 12$

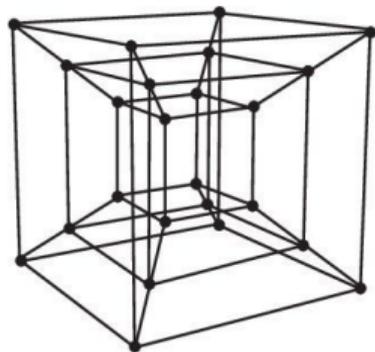
×

Aspect ratios $L/N_T = 2, 3, 4, 6, 8$

×

Scan coupling β_F to sweep temperatures high \longrightarrow low and low \longrightarrow high

= 985 ensembles and counting [5,000–50,000 MD time units per ensemble]



The lattice phase diagram game

Fermion masses $m = 0.05, 0.067, \mathbf{0.1}, 0.2$ (and pure gauge)

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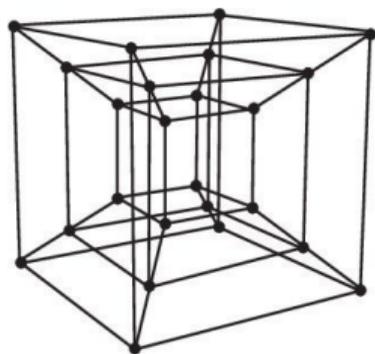
×

Aspect ratios $L/N_T = \mathbf{2}, \mathbf{3}, \mathbf{4}, 6, 8$

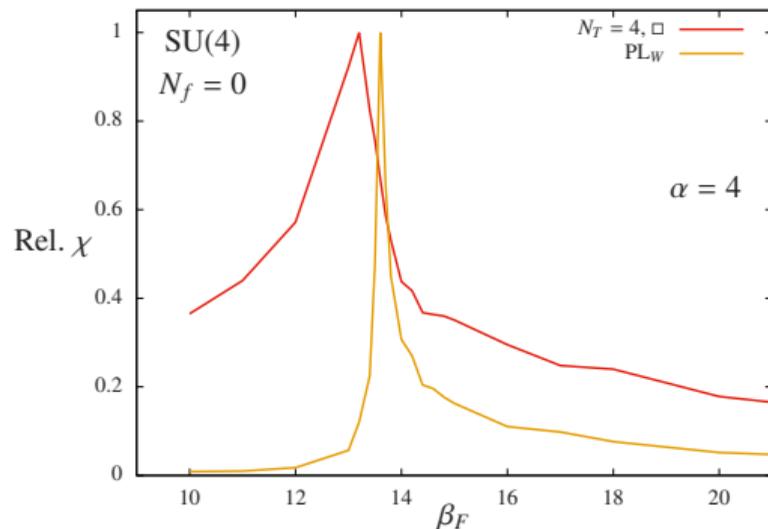
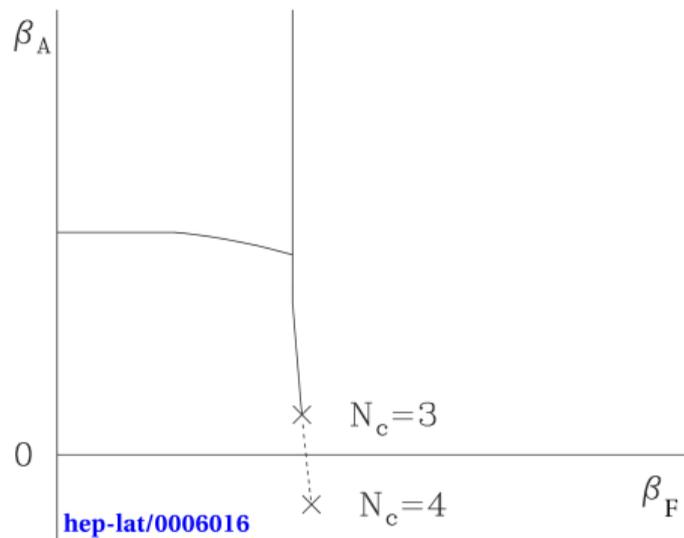
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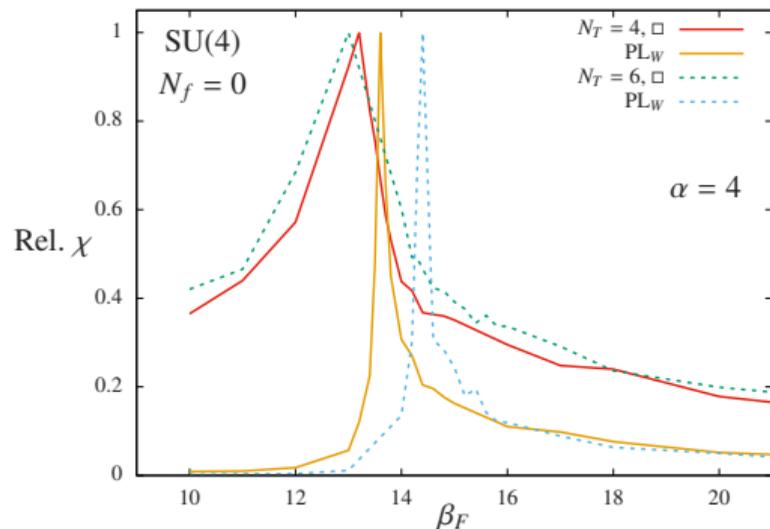
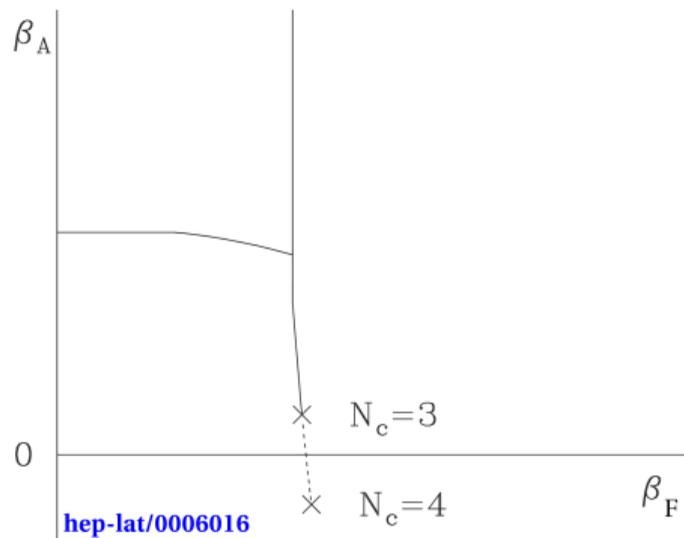
Pure gauge checks: Bulk and thermal transitions



Try to avoid bulk transition for small $N_T \rightarrow$ use $\beta_A = -\beta_F/4$

Still need $N_T > 4$ for clear separation between bulk & thermal transitions

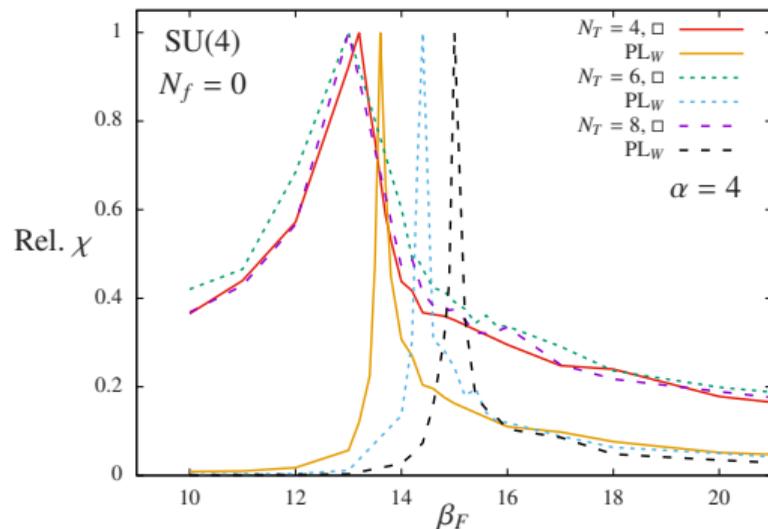
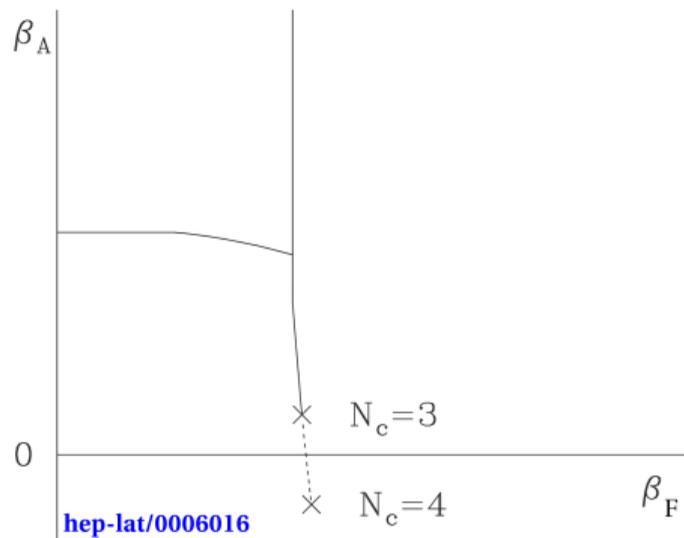
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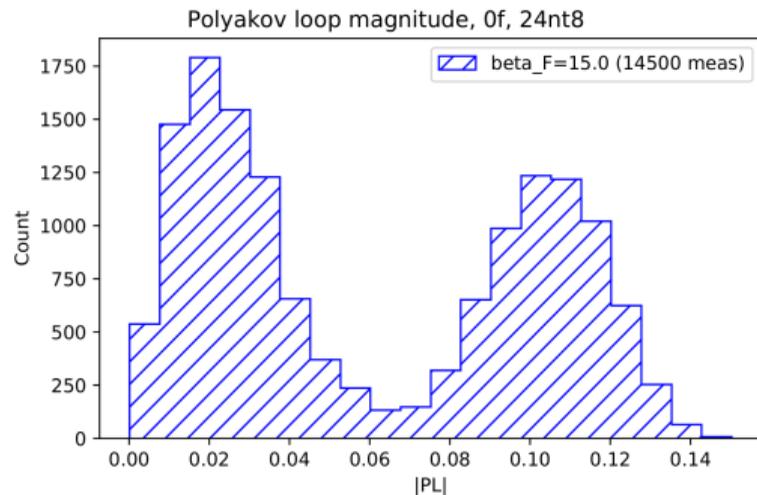
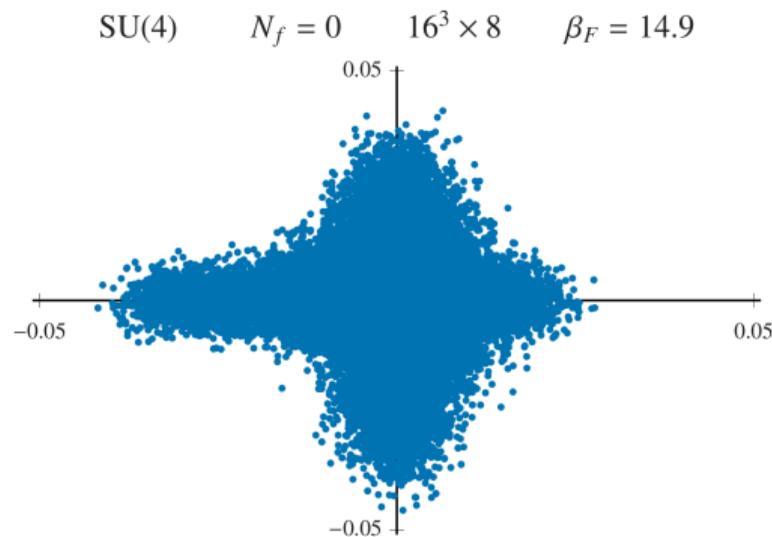
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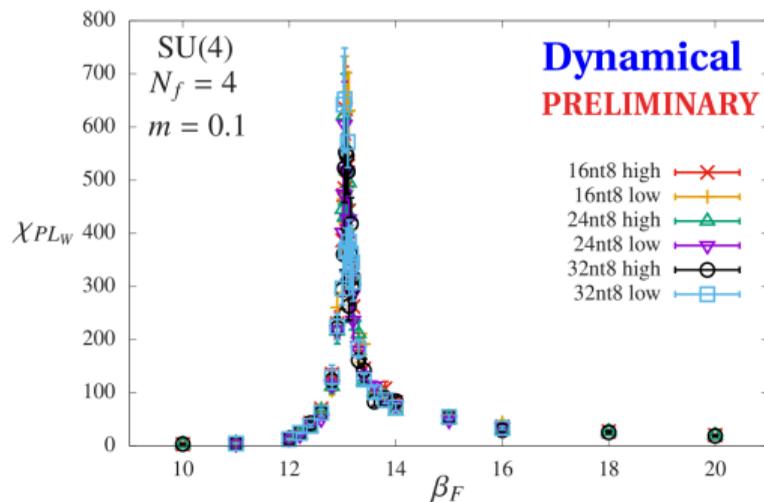
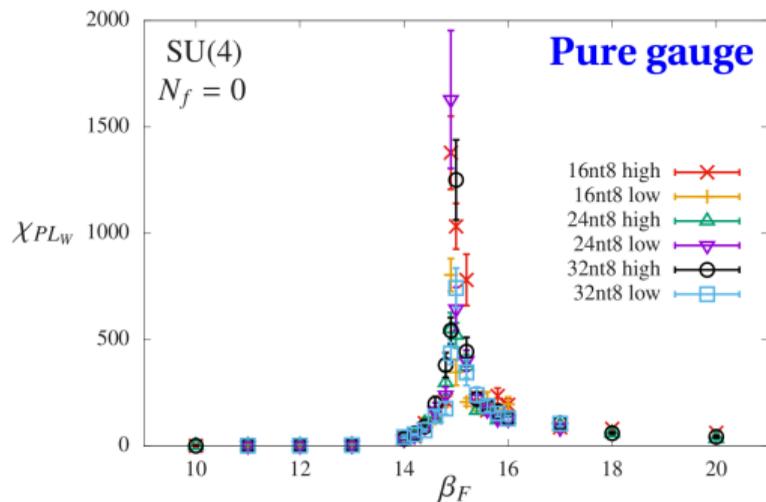
Pure gauge checks: Order of thermal transition



Two peaks in Polyakov loop magnitude histogram \longrightarrow first-order transition ✓

Hysteresis not clearly visible even in pure-gauge case

Dynamical results: Still looks first order



Pure-gauge & dynamical susceptibilities show same behavior

→ evidence for first-order transition with $m \geq 0.1$

Fundamental fermions explicitly break Z_N → don't see two peaks in histograms

What does $m \geq 0.1$ mean?

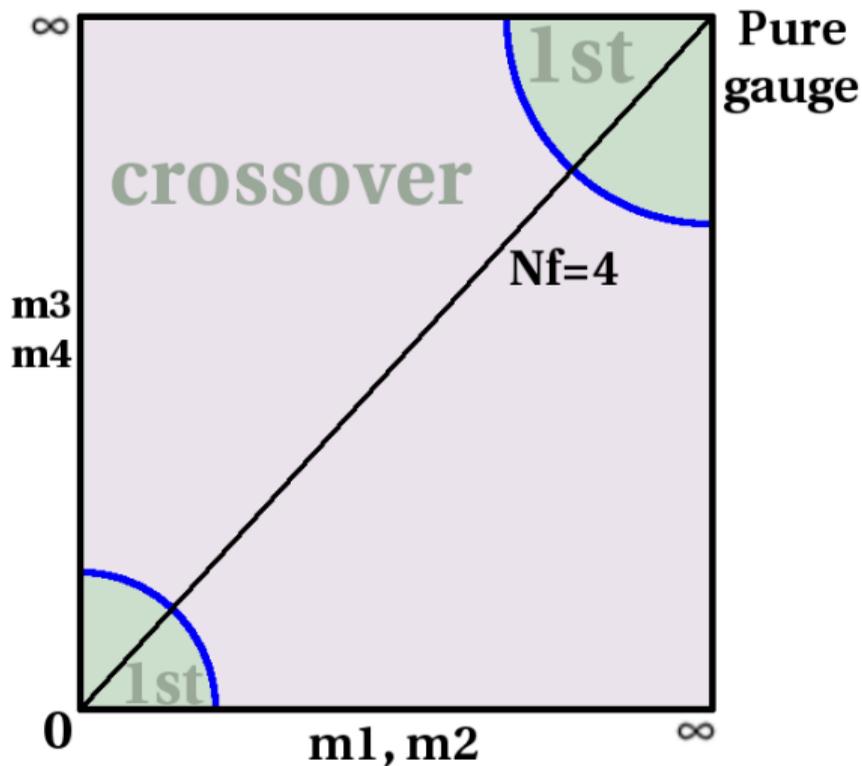
How heavy is sufficient for SU(4)?

Spectrum measurements

Zero-temp. $24^3 \times 48$ ensembles
around each transition

→ $M_P/M_V = 0.80(3)$ for $m = 0.1$

→ $M_P/M_V = 0.91(1)$ for $m = 0.2$



Previous work considered $0.55 \leq M_P/M_V \leq 0.77$ → now adding $m = 0.05$

From first-order transition to gravitational wave signal

First-order transition \rightarrow gravitational wave background will be produced

How do we predict its features?

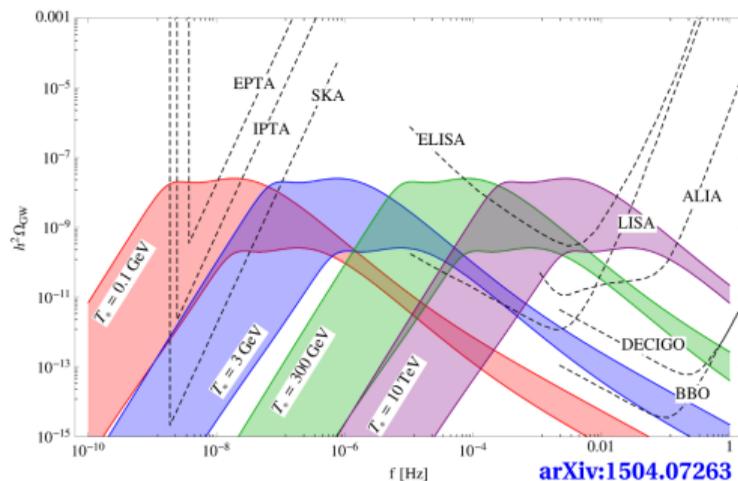
Four key parameters

Transition temperature $T_* \lesssim T_c$

Vacuum energy fraction from **latent heat**

Bubble nucleation rate (transition duration)

Bubble wall speed



Next step: Latent heat $\Delta\epsilon$

First-order transition \rightarrow gravitational wave background will be produced

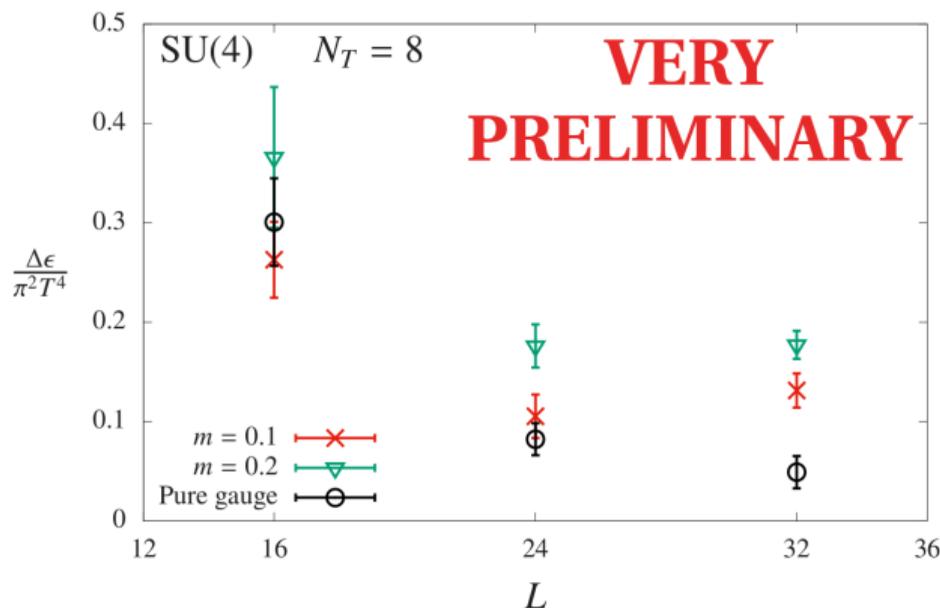
How do we predict its features?

Vacuum energy fraction

$$\alpha \approx \frac{30}{4N(N^2 - 1)} \frac{\Delta\epsilon}{\pi^2 T_*^4}$$

Latent heat $\Delta\epsilon$

is change in energy density
at transition



Recapitulation and outlook

Stealth dark matter

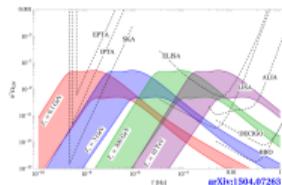
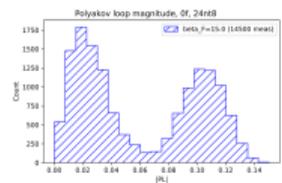
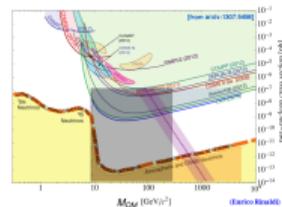
Attractive and viable composite dark matter model

Exploring gravitational waves from first-order transition

Gravitational wave observatories will add to constraints from collider searches and direct detection experiments

SU(4) confinement transition appears first order for $M_P/M_V \gtrsim 0.8$, smaller masses underway

Next steps are latent heat, etc., for signal prediction



Thank you!

Lattice Strong Dynamics Collaboration

Especially Graham Kribs, Ethan Neil, Enrico Rinaldi

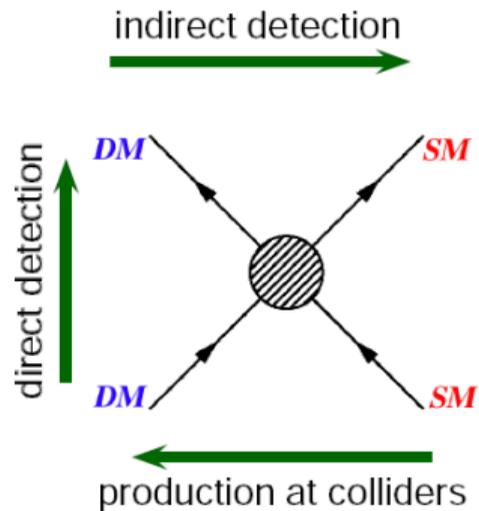
Funding and computing resources



UK Research
and Innovation



Backup: Thermal freeze-out for relic density

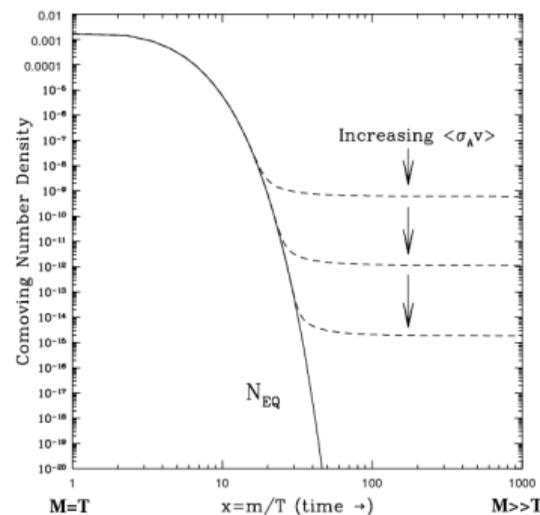


Requires non-gravitational
DM–SM interactions

DM \leftrightarrow SM for $T \gtrsim M_{DM}$

DM \rightarrow SM for $T \lesssim M_{DM}$
 \implies rapid depletion of Ω_{DM}

Hubble expansion
 \implies dilution \rightarrow freeze-out



$2 \rightarrow 2$ scattering relates coupling and mass, $200\alpha \sim \frac{M_{DM}}{100 \text{ GeV}}$

Strong $\alpha \sim 16 \rightarrow$ 'natural' $M_{DM} \sim 300 \text{ TeV}$ (smaller for $2 \rightarrow n$ scattering)

Backup: Two roads to natural asymmetric dark matter

Relate dark matter relic density to baryon asymmetry

$$\begin{aligned}\Omega_D &\approx 5\Omega_B \\ \implies M_D n_D &\approx 5M_B n_B\end{aligned}$$

$$n_D \sim n_B \implies M_D \sim 5M_B \approx 5 \text{ GeV}$$

High-dim. interactions relate baryon# and DM# violation

$$M_D \gg M_B \implies n_B \gg n_D \sim \exp[-M_D/T_s] \quad T_s \sim 200 \text{ GeV}$$

EW sphaleron processes above T_s distribute asymmetries

Both require non-gravitational interactions with known particles

Backup: Confirming thermal transition

Fix $m \cdot N_T \approx 0.8$ \longrightarrow transition moves to $\beta_F \rightarrow \infty$ as $N_T \rightarrow \infty$ \checkmark

